## Phased Array System Toolbox ${ }^{\text {TM }}$

 Reference®

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## Revision History

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Objects

# phased.ADPCACanceller 

Package: phased

Adaptive DPCA (ADPCA) pulse canceller

## Description

The ADPCACanceller object implements an adaptive displaced phase center array pulse canceller for a uniform linear array (ULA).

To compute the output signal of the space time pulse canceller:
1 Define and set up your ADPCA pulse canceller. See "Construction" on page 1-2.
2 Call step to execute the ADPCA algorithm according to the properties of phased.ADPCACanceller. The behavior of step is specific to each object in the toolbox.

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object ${ }^{\mathrm{TM}}$, you can call the object with arguments, as if it were a function. For example, y = step(obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.

## Construction

H = phased.ADPCACanceller creates an adaptive displaced phase center array (ADPCA) canceller System object, H. This object performs two-pulse ADPCA processing on the input data.
$H=$ phased.ADPCACanceller(Name,Value) creates an ADPCA object, $H$, with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN). See "Properties" on page 1-2 for the list of available property names.

## Properties

## SensorArray

Uniform linear array
Uniform linear array, specified as a phased. ULA System object.
Default: phased.ULA with default property values

## PropagationSpeed

Signal propagation speed
Specify the propagation speed of the signal, in meters per second, as a positive scalar. You can specify this property as single or double precision.

Default: Speed of light

## OperatingFrequency

System operating frequency
Specify the operating frequency of the system in hertz as a positive scalar. The default value corresponds to 300 MHz . You can specify this property as single or double precision.

Default: 3e8

## PRFSource

Source of pulse repetition frequency
Source of the PRF values for the STAP processor, specified as 'Property' or 'Input port '. When you set this property to 'Property ' ', the PRF is determined by the value of the PRF property. When you set this property to 'Input port', the PRF is determined by an input argument to the step method at execution time.

Default: 'Property'
PRF
Pulse repetition frequency
Pulse repetition frequency (PRF) of the received signal, specified as a positive scalar. Units are in Hertz. This property can be specified as single or double precision.

## Dependencies

To enable this property, set the PRFSource property to 'Property '.
Default: 1

## DirectionSource

Source of receiving main lobe direction
Specify whether the targeting direction for the STAP processor comes from the Direction property of this object or from an input argument in step. Values of this property are:

| 'Property' | The Direction property of this object specifies the targeting <br> direction. |
| :--- | :--- |
| ' Input port' | An input argument in each invocation of step specifies the <br> targeting direction. |

## Default: 'Property'

## Direction

Receiving mainlobe direction (degrees)
Specify the receiving mainlobe direction of the receiving sensor array as a column vector of length 2 . The direction is specified in the format of [AzimuthAngle; ElevationAngle] (in degrees). Azimuth angle should be between -180 and 180. Elevation angle should be between -90 and 90 . This property applies when you set the DirectionSource property to 'Property'. This property can be specified as single or double precision.

Default: [0; 0]

## NumPhaseShifterBits

Number of phase shifter quantization bits
The number of bits used to quantize the phase shift component of beamformer or steering vector weights. Specify the number of bits as a non-negative integer. A value of zero indicates that no quantization is performed. You can specify this property as single or double precision.

Default: 0

## DopplerSource

Source of targeting Doppler
Specify whether the targeting Doppler for the STAP processor comes from the Doppler property of this object or from an input argument in step. Values of this property are:

| 'Property' | The Doppler property of this object specifies the Doppler. |
| :--- | :--- |
| 'Input port' | An input argument in each invocation of step specifies the Doppler. |
| Default: 'Property' |  |
| Doppler |  |

Targeting Doppler frequency (Hz)
Specify the targeting Doppler of the STAP processor as a scalar. This property applies when you set the DopplerSource property to 'Property '. This property can be specified as single or double precision.

Default: 0

## WeightsOutputPort

Output processing weights
To obtain the weights used in the STAP processor, set this property to true and use the corresponding output argument when invoking step. If you do not want to obtain the weights, set this property to false.

Default: false

## PreDopplerOutput

Output pre-Doppler result
Set this property to true to output the processing result before applying the Doppler filtering. Set this property to false to output the processing result after the Doppler filtering.

## Default: false

## NumGuardCells

Number of guard cells

Specify the number of guard cells used in the training as an even integer. This property specifies the total number of cells on both sides of the cell under test. This property can be specified as single or double precision.

Default: 2, indicating that there is one guard cell at both the front and back of the cell under test

## NumTrainingCells

Number of training cells
Specify the number of training cells used in the training as an even integer. Whenever possible, the training cells are equally divided before and after the cell under test. This property can be specified as single or double precision.

Default: 2, indicating that there is one training cell at both the front and back of the cell under test

## Methods

step Perform ADPCA processing on input data

## Common to All System Objects

release $\quad$ Allow System object property value changes

## Examples

## Process Radar Data Cube Using ADPCA Processor

Process a radar data cube using an ADPCA processor. Weights are calculated for the 71st cell of the data cube. Set the look direction to $(0,0)$ degrees and the Doppler shift to 12.980 kHz .

## Load radar data file and compute weights

```
load STAPExampleData;
canceller = phased.ADPCACanceller('SensorArray',STAPEx_HArray,...
    'PRF',STAPEx_PRF,...
    'PropagationSpeed',STAPEx_PropagationSpeed,...
    'OperatingFrequency',STAPE\overline{x_OperatingFrequency,...}
    'NumTrainingCells',100,...
    'Weights0utputPort',true,...
    'DirectionSource','Input port',...
    'DopplerSource','Input port');
[y,w] = canceller(STAPEx_ReceivePulse,71,[0; 0],12.980e3);
```


## Create AnglerDoppler System object and plot response

```
sAngeDop = phased.AngleDopplerResponse(...
    'SensorArray',canceller.SensorArray,...
    'OperatingFrequency',canceller.OperatingFrequency,...
    'PRF',canceller.PRF,...
    'PropagationSpeed',canceller.PropagationSpeed);
plotResponse(sAngeDop,w)
```



## Algorithms

## Single Precision

This System object supports single and double precision for input data, properties, and arguments. If the input data X is single precision, the output data is single precision. If the input data X is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

## Version History

Introduced in R2011a

## References

[1] Guerci, J. R. Space-Time Adaptive Processing for Radar. Boston: Artech House, 2003.
[2] Ward, J. "Space-Time Adaptive Processing for Airborne Radar Data Systems," Technical Report 1015, MIT Lincoln Laboratory, December, 1994.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
See "System Objects in MATLAB Code Generation" (MATLAB Coder).
This System object supports single and double precision for input data, properties, and arguments. If the input data X is single precision, the output data is single precision. If the input data X is double
precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

## See Also

phased.AngleDopplerResponse | phased.DPCACanceller | phased. STAPSMIBeamformer | uv2azel | phitheta2azel

## step

System object: phased. ADPCACanceller
Package: phased
Perform ADPCA processing on input data

## Syntax

$Y=\operatorname{step}(H, X, C U T I D X)$
Y = step(H,X,CUTIDX,ANG)
Y = step(H,X,CUTIDX,DOP)
Y = step(H,X,CUTIDX, PRF)
[ $\mathrm{Y}, \mathrm{W}$ ] = step( $\qquad$ )

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.
$Y=$ step ( $H, X$, CUTIDX) applies the ADPCA pulse cancellation algorithm to the input data $X$. The algorithm calculates the processing weights according to the range cell specified by CUTIDX. This syntax is available when the DirectionSource property is 'Property' and the DopplerSource property is 'Property '. The receiving mainlobe direction is the Direction property value. The output $Y$ contains the result of pulse cancellation either before or after Doppler filtering, depending on the PreDopplerOutput property value.
$Y=$ step ( $\mathrm{H}, \mathrm{X}$, CUTIDX, ANG) uses ANG as the receiving main lobe direction. This syntax is available when the DirectionSource property is 'Input port' and the DopplerSource property is 'Property'.

Y = step (H,X,CUTIDX, DOP) uses DOP as the targeting Doppler frequency. This syntax is available when the DopplerSource property is 'Input port'.
$Y=\operatorname{step}(H, X, C U T I D X, P R F)$ uses PRF as the pulse repetition frequency. This syntax is available when the PRFSource property is 'Input port'.
$[\mathrm{Y}, \mathrm{W}]=\operatorname{step}(\ldots \quad$ ) also returns the processing weights, W . This syntax is available when the WeightsOutputPort property is true.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## H

Pulse canceller object.

## X

Input data. X must be a 3 -dimensional M -by-N-by-P numeric array whose dimensions are (range, channels, pulses). You can specify this argument as single or double precision.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

## CUTIDX

Range cell. You can specify this argument as single or double precision.

## PRF

Pulse repetition frequency specified as a positive scalar. To enable this argument, set the PRFSource property to 'Input port'. You can specify this argument as single or double precision. Units are in Hertz.

## ANG

Receiving main lobe direction. ANG must be a 2-by-1 vector in the form [AzimuthAngle; ElevationAngle], in degrees. The azimuth angle must be between -180 and 180. The elevation angle must be between -90 and 90 . You can specify this argument as single or double precision.

Default: Direction property of H

## DOP

Targeting Doppler frequency in hertz. DOP must be a scalar. You can specify this argument as single or double precision.

Default: Doppler property of H

## Output Arguments

## Y

Result of applying pulse cancelling to the input data. The meaning and dimensions of $Y$ depend on the PreDopplerOutput property of H :

- If PreDopplerOutput is true, Y contains the pre-Doppler data. Y is an M-by-(P-1) matrix. Each column in $Y$ represents the result obtained by cancelling the two successive pulses.
- If PreDopplerOutput is false, $Y$ contains the result of applying an FFT-based Doppler filter to the pre-Doppler data. The targeting Doppler is the Doppler property value. Y is a column vector of length M .


## W

Processing weights the pulse canceller used to obtain the pre-Doppler data. The dimensions of W depend on the PreDopplerOutput property of H :

- If PreDopplerOutput is true, W is a 2 N -by-(P-1) matrix. The columns in W correspond to successive pulses in $X$.
- If PreDopplerOutput is false, $W$ is a column vector of length ( $\mathrm{N}^{*} \mathrm{P}$ ).


## Examples

## Plot Response of ADPCA Processor with Quantized Weights

Process a radar data cube using an ADPCA processor. Weights are calculated for the 71st cell of the data cube. Load the data cube from STAPExampleData. mat. Quantize the weights to 4 bits. Set the look direction to $(0,0)$ degrees and the Doppler shift to 12.980 kHz .

```
load STAPExampleData;
sADPCA = phased.ADPCACanceller('SensorArray',STAPEx_HArray,...
    'PRF',STAPEx_PRF, ...
    'Propagation\overline{Speed',STAPEx_PropagationSpeed,...}
    'OperatingFrequency',STAPE\overline{Ex_OperatingFrequency,...}
    'NumTrainingCells',100,...
    'Weights0utputPort',true,...
    'DirectionSource','Input port',...
    'DopplerSource','Input port',...
    'NumPhaseShifterBits',4);
[y,w] = step(sADPCA,STAPEx_ReceivePulse,71,[0; 0],12.980e3);
sAngDop = phased.AngleDopplerResponse(...
    'SensorArray',sADPCA.SensorArray,...
    'OperatingFrequency',sADPCA.OperatingFrequency,...
    'PRF' , sADPCA. PRF, ...
    'PropagationSpeed',sADPCA.PropagationSpeed);
plotResponse(sAngDop,w);
```



## See Also

uv2azel| phitheta2azel

# phased.AngleDopplerResponse 

Package: phased

Angle-Doppler response

## Description

The AngleDopplerResponse object calculates the angle-Doppler response of input data.
To compute the angle-Doppler response:
1 Define and set up your angle-Doppler response calculator. See "Construction" on page 1-12.
2 Call step to compute the angle-Doppler response of the input signal according to the properties of phased.AngleDopplerResponse. The behavior of step is specific to each object in the toolbox.

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, x ) and $\mathrm{y}=\mathrm{obj}(\mathrm{x})$ perform equivalent operations.

## Construction

H = phased.AngleDopplerResponse creates an angle-Doppler response System object, H. This object calculates the angle-Doppler response of the input data.

H = phased.AngleDopplerResponse(Name,Value) creates angle-Doppler object, H, with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN).

## Properties

## SensorArray

Sensor array
Sensor array specified as an array System object belonging to the phased package. A sensor array can contain subarrays.

Default: phased.ULA with default property values

## PropagationSpeed

Signal propagation speed
Specify the propagation speed of the signal, in meters per second, as a positive scalar. You can specify this property as single or double precision.

Default: Speed of light

## OperatingFrequency

System operating frequency
Specify the operating frequency of the system in hertz as a positive scalar. The default value corresponds to 300 MHz . You can specify this property as single or double precision.

Default: 3e8
PRFSource
Source of PRF values
Source of the PRF values for the STAP processor, specified as 'Property' or 'Input port'. When you set this property to 'Property', the PRF is determined by the value of the PRF property. When you set this property to 'Input port', the PRF is determined by an input argument to the step method at execution time.

Default: 'Property'
PRF
Pulse repetition frequency
Specify the pulse repetition frequency (PRF) in hertz of the input signal as a positive scalar. This property applies when you set the PRFSource property to 'Property'. You can specify this property as single or double precision.

## Default: 1

## ElevationAngleSource

Source of elevation angle
Specify whether the elevation angle comes from the ElevationAngle property of this object or from an input argument in step. Values of this property are:

| 'Property' | The ElevationAngle property of this object specifies the <br> elevation angle. |
| :--- | :--- |
| 'Input port' | An input argument in each invocation of step specifies the <br> elevation angle. |

## Default: 'Property'

## ElevationAngle

Elevation angle
Specify the elevation angle in degrees used to calculate the angle-Doppler response as a scalar. The angle must be between -90 and 90. This property applies when you set the ElevationAngleSource property to 'Property'. You can specify this property as single or double precision.

## Default: 0

## NumAngleSamples

Number of samples in angular domain
Specify the number of samples in the angular domain used to calculate the angle-Doppler response as a positive integer. This value must be greater than 2 . You can specify this property as single or double precision.

Default: 256

## NumDopplerSamples

Number of samples in Doppler domain
Specify the number of samples in the Doppler domain used to calculate the angle-Doppler response as a positive integer. This value must be greater than 2 . You can specify this property as single or double precision.

Default: 256

## Methods

| plotResponse | Plot angle-Doppler response |
| :--- | :--- |
| step | Calculate angle-Doppler response |

Common to All System Objects
release $\quad$ Allow System object property value changes

## Examples

## Calculate Angle-Doppler Response

Calculate the angle-Doppler response of the 190th cell of a collected data cube.
Load data cube and construct a phased. AngleDopplerResponse System object ${ }^{\mathrm{TM}}$.
load STAPExampleData;
x = shiftdim(STAPEx_ReceivePulse(190,:,:));
response $=$ phased.An̄gleDopplerResponse(...
'SensorArray', STAPEx_HArray,...
'OperatingFrequency ',STAPEx_OperatingFrequency,...
'PropagationSpeed', STAPEx_PropagationSpeed, . . .
'PRF',STAPEx_PRF);
Plot angle-Doppler response.

```
[resp,ang_grid,dop grid] = response(x);
contour(ang_grid,dop_grid,abs(resp))
xlabel('Angle')
ylabel('Doppler')
```



## Algorithms

## Response Computation

phased. AngleDopplerResponse generates the response using a conventional beamformer and an FFT-based Doppler filter. For further details, see [1].

## Single Precision

This System object supports single and double precision for input data, properties, and arguments. If the input data $X$ is single precision, the output data is single precision. If the input data $X$ is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

## Version History

Introduced in R2011a

## References

[1] Guerci, J. R. Space-Time Adaptive Processing for Radar. Boston: Artech House, 2003.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
See "System Objects in MATLAB Code Generation" (MATLAB Coder).

```
See Also
phased.ADPCACanceller|phased.DPCACanceller|phased.STAPSMIBeamformer|uv2azel|
phitheta2azel
```


## plotResponse

System object: phased. AngleDopplerResponse
Package: phased
Plot angle-Doppler response

## Syntax

plotResponse (H, X)
plotResponse(H,X,ELANG)
plotResponse(H, X, PRF)
plotResponse (__, Name, Value)
hPlot = plotResponse( $\qquad$ )

## Description

plotResponse $(H, X)$ plots the angle-Doppler response of the data in $X$ in decibels. This syntax is available when the ElevationAngleSource property is 'Property'.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
plotResponse( $\mathrm{H}, \mathrm{X}, \mathrm{ELANG}$ ) plots the angle-Doppler response calculated using the specified elevation angle ELANG. This syntax is available when the ElevationAngleSource property is 'Input port'.
plotResponse( $\mathrm{H}, \mathrm{X}, \mathrm{PRF}$ ) plots the angle-Doppler response calculated using the specified pulse repetition frequency PRF. This syntax is available when the PRFSource property is 'Input port'.
plotResponse( $\qquad$ ,Name, Value) plots the angle-Doppler response with additional options specified by one or more Name, Value pair arguments.
hPlot $=$ plotResponse( $\qquad$ ) returns the handle of the image in the figure window, using any of the input arguments in the previous syntaxes.

## Input Arguments

## H

Angle-Doppler response object.

## X

Input data.

## ELANG

Elevation angle in degrees.
Default: Value of Elevation property of H

## PRF

Pulse repetition frequency specified as a positive scalar. To enable this argument, set the PRFSource property to 'Input port'. Units are in Hertz.

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## NormalizeDoppler

Set this value to true to normalize the Doppler frequency. Set this value to false to plot the angleDoppler response without normalizing the Doppler frequency.

Default: false
Unit
The unit of the plot. Valid values are 'db', 'mag', and 'pow'.
Default: 'db'

## Examples

## Plot Angle-Doppler Response

Plot the angle-Doppler response of the 190th cell of a collected data cube.

```
load STAPExampleData;
x = shiftdim(STAPEx_ReceivePulse(190,:,:));
hadresp = phased.AngleDopplerResponse(...
    'SensorArray',STAPEx_HArray,...
    'OperatingFrequency',STAPEx_OperatingFrequency,...
    'PropagationSpeed',STAPEx_PropagationSpeed,...
    'PRF',STAPEx PRF);
plotResponse(hadresp,x,'NormalizeDoppler',true);
```



## See Also

uv2azel|phitheta2azel

## step

System object: phased.AngleDopplerResponse
Package: phased
Calculate angle-Doppler response

## Syntax

[RESP,ANG_GRID,DOP_GRID] = step $(H, X)$
[RESP,ANG_GRID,DOP GRID] = step (H,X,ELANG)
RESP,ANG_GRID,DOP_GRID $=\operatorname{step}(H, X, P R F)$

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step $(o b j, x)$ and $y=o b j(x)$ perform equivalent operations.
[RESP,ANG_GRID,DOP_GRID] = step $(H, X)$ calculates the angle-Doppler response of the data X . RESP is the complex angle-Doppler response. ANG GRID and DOP GRID provide the angle samples and Doppler samples, respectively, at which the angle-Doppler response is evaluated. This syntax is available when the ElevationAngleSource property is 'Property'.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
[RESP,ANG_GRID,DOP_GRID] = step(H,X,ELANG) calculates the angle-Doppler response using the specified elevation angle ELANG. This syntax is available when the ElevationAngleSource property is 'Input port'.

RESP, ANG_GRID,DOP_GRID = step ( $\mathrm{H}, \mathrm{X}, \mathrm{PRF}$ ) uses PRF as the pulse repetition frequency. This syntax is available when the PRFSource property is 'Input port'.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## H

Angle-Doppler response object.

## X

Input data as a matrix or column vector.
If $X$ is a matrix, the number of rows in the matrix must equal the number of elements of the array specified in the SensorArray property of H .

If $X$ is a vector, the number of rows must be an integer multiple of the number of elements of the array specified in the SensorAr ray property of H . In addition, the multiple must be at least 2.

## ELANG

Elevation angle in degrees. You can specify this argument as single or double precision.
Default: Value of Elevation property of H
PRF
Pulse repetition frequency specified as a positive scalar. To enable this argument, set the PRFSource property to 'Input port'. Units are in Hertz. You can specify this argument as single or double precision.

## Output Arguments

## RESP

Complex angle-Doppler response of $X$. RESP is a P-by-Q matrix. P is determined by the NumDopplerSamples property of H and Q is determined by the NumAngleSamples property.

## ANG_GRID

Angle samples at which the angle-Doppler response is evaluated. ANG_GRID is a column vector of length Q.

## DOP_GRID

Doppler samples at which the angle-Doppler response is evaluated. DOP_GRID is a column vector of length $P$.

## Examples

## Calculate Angle-Doppler Response

Calculate the angle-Doppler response of the 190th cell of a collected data cube.
Load data cube and construct a phased. AngleDopplerResponse System object ${ }^{\mathrm{TM}}$.

```
load STAPExampleData;
x = shiftdim(STAPEx_ReceivePulse(190,:,:));
response = phased.An̄gleDopplerResponse(...
    'SensorArray', STAPEx_HArray,...
    'OperatingFrequency',STAPEx_OperatingFrequency,...
    'PropagationSpeed',STAPEx_PropagationSpeed,...
    'PRF',STAPEx_PRF);
```

Plot angle-Doppler response.
[resp,ang_grid,dop_grid] = response(x);
contour(ang_grid,dop_grid, abs(resp))
xlabel('Angle')
ylabel('Doppler')


## Algorithms

phased.AngleDopplerResponse generates the response using a conventional beamformer and an FFT-based Doppler filter. For further details, see [1].

## References

[1] Guerci, J. R. Space-Time Adaptive Processing for Radar. Boston: Artech House, 2003.

## See Also <br> uv2azel | phitheta2azel|azel2uv| azel2phitheta

## phased.ArrayGain

Package: phased
Sensor array gain

## Description

The ArrayGain object calculates the array gain for a sensor array. The array gain on page 1-24 is defined as the signal to noise ratio (SNR) improvement between the array output and the individual channel input, assuming the noise is spatially white. It is related to the array response but is not the same.

To compute the SNR gain of the antenna for specified directions:
1 Define and set up your array gain calculator. See "Construction" on page 1-23.
2 Call step to estimate the gain according to the properties of phased.ArrayGain. The behavior of step is specific to each object in the toolbox.

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.

## Construction

H = phased.ArrayGain creates an array gain System object, H. This object calculates the array gain of a 2-element uniform linear array for specified directions.

H = phased.ArrayGain(Name,Value) creates and array-gain object, H, with the specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN).

## Properties

## SensorArray

Sensor array
Sensor array specified as an array System object belonging to the phased package. A sensor array can contain subarrays.

Default: phased.ULA with default property values

## PropagationSpeed

Signal propagation speed
Specify the propagation speed of the signal, in meters per second, as a positive scalar.
Default: Speed of light

## WeightsInputPort

Add input to specify weights
To specify weights, set this property to true and use the corresponding input argument when you invoke step. If you do not want to specify weights, set this property to false.

## Default: false

## Methods

step Calculate array gain of sensor array

## Common to All System Objects

release $\quad$ Allow System object property value changes

## Examples

## Array Gain of 4-Element ULA

Calculate the array gain for a 4 -element uniform linear array (ULA) in the direction $30^{\circ}$ azimuth and $20^{\circ}$ elevation. The array operating frequency is 300 MHz .

```
fc = 300e6;
array = phased.ULA(4);
gain = phased.ArrayGain('SensorArray',array);
g = gain(fc,[30;20])
g = -17.1783
```


## More About

## Array Gain

The array gain is defined as the signal to noise ratio (SNR) improvement between the array output and the individual channel input, assuming the noise is spatially white. You can express the array gain as follows:

$$
\frac{S N R_{\text {out }}}{S N R_{\text {in }}}=\frac{\left(\frac{w^{H} v s v^{H} w}{w^{H} N w}\right)}{\left(\frac{s}{N}\right)}=\frac{w^{H} v v^{H} w}{w^{H} w}
$$

In this equation:

- $w$ is the vector of weights applied on the sensor array. When you use phased.ArrayGain, you can optionally specify weights by setting the WeightsInputPort property to true and specifying the $W$ argument in the step method syntax.
- $v$ is the steering vector representing the array response toward a given direction. When you call the step method, the ANG argument specifies the direction.
- $s$ is the input signal power.
- $N$ is the noise power.
- $H$ denotes the complex conjugate transpose.

For example, if a rectangular taper is used in the array, the array gain is the square of the array response normalized by the number of elements in the array.

## Version History

Introduced in R2011a

## References

[1] Guerci, J. R. Space-Time Adaptive Processing for Radar. Boston: Artech House, 2003.
[2] Van Trees, H. Optimum Array Processing. New York: Wiley-Interscience, 2002.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{Tm}}$.
Usage notes and limitations:

- Does not support arrays containing polarized antenna elements, that is, the phased.ShortDipoleAntennaElement or phased.CrossedDipoleAntennaElement antennas.
- See "System Objects in MATLAB Code Generation" (MATLAB Coder).


## See Also

phased.ArrayResponse|phased.ElementDelay|phased.SteeringVector

## step

System object: phased.ArrayGain
Package: phased
Calculate array gain of sensor array

## Syntax

G = step(H,FREQ,ANG)
G = step(H,FREQ,ANG,WEIGHTS)
G = step(H,FREQ,ANG,STEERANGLE)
G = step(H,FREQ,ANG,WEIGHTS,STEERANGLE)
G = step(H,FREQ,ANG,WS)

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.
$\mathrm{G}=\mathrm{step}(\mathrm{H}, \mathrm{FREQ}, \mathrm{ANG})$ returns the array gain on page 1-29 G of the array for the operating frequencies specified in FREQ and directions specified in ANG.

G = step(H, FREQ,ANG,WEIGHTS) applies weights WEIGHTS on the sensor array. This syntax is available when you set the WeightsInputPort property to true.

G = step(H,FREQ,ANG,STEERANGLE) uses STEERANGLE as the subarray steering angle. This syntax is available when you configure H so that H . Sensor is an array that contains subarrays, and H.Sensor.SubarraySteering is either 'Phase' or 'Time'.

G = step(H,FREQ,ANG,WEIGHTS,STEERANGLE) combines all input arguments. This syntax is available when you configure $H$ so that $H$. WeightsInputPort is true, H . Sensor is an array that contains subarrays, and H.Sensor.SubarraySteering is either 'Phase' or 'Time'.

G = step(H,FREQ,ANG,WS) uses WS as weights applied to each element within each subarray. To use this syntax, set the SensorArray property to an array that supports subarrays and set the SubarraySteering property of the array to 'Custom'.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## H

Array gain object.

## FREQ

Operating frequencies of array in hertz. FREQ is a row vector of length L. Typical values are within the range specified by a property of the sensor element. The element is H.SensorArray.Element, H.SensorArray.Array.Element, or H.SensorArray.Subarray. Element, depending on the type of array. The frequency range property is named FrequencyRange or FrequencyVector, depending on the type of element in the array. The element has zero response at frequencies outside that range.

## ANG

Directions in degrees. ANG can be either a 2-by-M matrix or a row vector of length M.
If ANG is a 2-by-M matrix, each column of the matrix specifies the direction in the form [azimuth; elevation]. The azimuth angle must be between -180 and 180 degrees, inclusive. The elevation angle must be between -90 and 90 degrees, inclusive.

If ANG is a row vector of length M , each element specifies a direction's azimuth angle. In this case, the corresponding elevation angle is assumed to be 0 .

## WEIGHTS

Weights on the sensor array. WEIGHTS can be either an N-by-L matrix or a column vector of length N . N is the number of subarrays if H . SensorArray contains subarrays, or the number of elements otherwise. $L$ is the number of frequencies specified in FREQ.

If WEIGHTS is a matrix, each column of the matrix represents the weights at the corresponding frequency in FREQ.

If WEIGHTS is a vector, the weights apply at all frequencies in FREQ.

## STEERANGLE

Subarray steering angle in degrees. STEERANGLE can be a length-2 column vector or a scalar.
If STEERANGLE is a length-2 vector, it has the form [azimuth; elevation]. The azimuth angle must be between -180 and 180 degrees, and the elevation angle must be between -90 and 90 degrees.

If STEERANGLE is a scalar, it represents the azimuth angle. In this case, the elevation angle is assumed to be 0 .

## WS

Subarray element weights
Subarray element weights, specified as complex-valued $N_{S E}$-by- $N$ matrix or 1-by- $N$ cell array where $N$ is the number of subarrays. These weights are applied to the individual elements within a subarray.

Subarray element weights

| Sensor Array | Subarray weights |
| :--- | :--- |
| phased. ReplicatedSubarray | All subarrays have the same dimensions and <br> sizes. Then, the subarray weights form an $N_{S E}$-by- <br> $N$ matrix. $N_{S E}$ is the number of elements in each <br> subarray and $N$ is the number of subarrays. Each <br> column of WS specifies the weights for the <br> corresponding subarray. |
| phased. PartitionedArray | Subarrays may not have the same dimensions and <br> sizes. In this case, you can specify subarray <br> weights as |
|  | an $N_{S E}$-by- $N$ matrix, where $N_{S E}$ is now the <br> number of elements in the largest subarray. <br> The first $Q$ entries in each column are the <br> element weights for the subarray where $Q$ is <br> the number of elements in the subarray. <br> a 1-by- $N$ cell array. Each cell contains a <br> column vector of weights for the <br> corresponding subarray. The column vectors <br> have lengths equal to the number of elements <br> in the corresponding subarray. |
|  |  |

## Dependencies

To enable this argument, set the SensorArray property to an array that contains subarrays and set the SubarraySteering property of the array to 'Custom'.

## Output Arguments

## G

Gain of sensor array, in decibels. G is an M-by-L matrix. G contains the gain at the M angles specified in ANG and the L frequencies specified in FREQ.

## Examples

## Array Gain of 6-Element ULA

Construct a uniform linear array (ULA) having six elements and operating at 1 GHz . The array elements are spaced at one-half the operating wavelength. Find the array gain in dB in the direction $45^{\circ}$ azimuth and $10^{\circ}$ elevation.

Create the phased.ArrayGain System object ${ }^{\mathrm{TM}}$.

```
fc = 1e9;
```

lambda = physconst('LightSpeed')/fc;
array $=$ phased.ULA('NumElements',6,'ElementSpacing', lambda/2);
gain = phased.ArrayGain('SensorArray',array);

Determine array gain at the specified operating frequency and angle.

```
arraygain = gain(fc,[45;10])
arraygain = -17.9275
```


## More About

## Array Gain

The array gain is defined as the signal to noise ratio (SNR) improvement between the array output and the individual channel input, assuming the noise is spatially white. You can express the array gain as follows:

$$
\frac{S N R_{\mathrm{out}}}{S N R_{\mathrm{in}}}=\frac{\left(\frac{w^{H}{ }_{v S v^{H}}{ }_{w}}{w^{H} N w}\right)}{\left(\frac{s}{N}\right)}=\frac{w^{H} v v^{H} w}{w^{H} w}
$$

In this equation:

- $\quad w$ is the vector of weights applied on the sensor array. When you use phased. ArrayGain, you can optionally specify weights by setting the WeightsInputPort property to true and specifying the $W$ argument in the step method syntax.
- $\quad v$ is the steering vector representing the array response toward a given direction. When you call the step method, the ANG argument specifies the direction.
- $s$ is the input signal power.
- $N$ is the noise power.
- $H$ denotes the complex conjugate transpose.

For example, if a rectangular taper is used in the array, the array gain is the square of the array response normalized by the number of elements in the array.

## See Also

uv2azel | phitheta2azel

## phased.ArrayResponse

Package: phased
Sensor array response

## Description

The ArrayResponse object calculates the complex-valued response of a sensor array.
To compute the response of the array for specified directions:
1 Define and set up your array response calculator. See "Construction" on page 1-30.
2 Call step to estimate the response according to the properties of phased.ArrayResponse. The behavior of step is specific to each object in the toolbox.

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step (obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.

## Construction

H = phased.ArrayResponse creates an array response System object, H. This object calculates the response of a sensor array for the specified directions. By default, a 2-element uniform linear array (ULA) is used.

H = phased.ArrayResponse(Name, Value) creates object, H, with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN).

## Properties

## SensorArray

Handle to sensor array used to calculate response
Specify the sensor array as a handle. The sensor array must be an array object in the phased package. The array can contain subarrays.

Default: phased.ULA with default property values

## PropagationSpeed

Signal propagation speed
Specify the propagation speed of the signal, in meters per second, as a positive scalar.
Default: Speed of light

## WeightsInputPort

Add input to specify weights
To specify weights, set this property to true and use the corresponding input argument when you invoke step. If you do not want to specify weights, set this property to false.

## Default: false

## EnablePolarization

Enable polarization simulation
Set this property to true to let the array response simulate polarization. Set this property to false to ignore polarization. This property applies only when the array specified in the SensorArray property is capable of simulating polarization.

Default: false

## Methods

step Calculate array response of sensor array

## Common to All System Objects

| release | Allow System object property value changes |
| :--- | :--- | :--- |

## Examples

## Plot Array Response

Calculate array response for a 4 -element uniform linear array (ULA) in the direction of 30 degrees azimuth and 20 degrees elevation. Assume the array's operating frequency is 300 MHz .

## Construct ULA and ArrayResponse System objects

```
fc = 300e6;
c = physconst('LightSpeed');
array = phased.ULA(4);
response = phased.ArrayResponse('SensorArray',array);
resp = response(fc,[30;20])
resp = 0.2768 + 0.0000i
```


## Plot the array response in dB

Plot the normalized power in db as an azimuth cut at 0 degrees elevation.

```
pattern(array,fc,[-180:180],0,'PropagationSpeed',c,'CoordinateSystem','rectangular','Type','powe
```



## Version History

Introduced in R2011a

## References

[1] Van Trees, H. Optimum Array Processing. New York: Wiley-Interscience, 2002.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:
See "System Objects in MATLAB Code Generation" (MATLAB Coder).

## See Also

phased.ArrayGain|phased.ElementDelay|phased.ConformalArray|phased.ULA| phased.URA|phased.SteeringVector

## step

System object: phased.ArrayResponse
Package: phased
Calculate array response of sensor array

## Syntax

RESP = step(H,FREQ,ANG)
RESP = step(H,FREQ,ANG,WEIGHTS)
RESP $=\operatorname{step}(H, F R E Q, A N G, S T E E R A N G L E)$
RESP $=$ step (H,FREQ,ANG,WEIGHTS,STEERANGLE)
RESP $=\operatorname{step}(H$, FREQ,ANG,WS)

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.

RESP = step ( $\mathrm{H}, \mathrm{FREQ}, \mathrm{ANG}$ ) returns the array response RESP at operating frequencies specified in FREQ and directions specified in ANG.

RESP $=\operatorname{step}(H$, FREQ, ANG, WEIGHTS) applies weights WEIGHTS on the sensor array. This syntax is available when you set the WeightsInputPort property to true.

RESP = step ( $\mathrm{H}, \mathrm{FREQ}$, ANG, STEERANGLE) uses STEERANGLE as the subarray steering angle. This syntax is available when you configure H so that H . Sensor is an array that contains subarrays, and H.Sensor.SubarraySteering is either 'Phase' or 'Time'.

RESP $=$ step ( H, FREQ, ANG,WEIGHTS,STEERANGLE) combines all input arguments. This syntax is available when you configure H so that H . WeightsInputPort is true, H . Sensor is an array that contains subarrays, and H.Sensor.SubarraySteering is either 'Phase' or 'Time'.

RESP $=$ step ( H, FREQ , ANG ,WS) uses WS as weights applied to each element within each subarray. To use this syntax, set the SensorArray property to an array that supports subarrays and set the SubarraySteering property of the array to 'Custom'.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## H

Array response object.

## FREQ

Operating frequencies of array in hertz. FREQ is a row vector of length L. Typical values are within the range specified by a property of the sensor element. The element is H. SensorArray.Element, H. SensorArray.Array.Element, or H.SensorArray. Subarray. Element, depending on the type of array. The frequency range property is named FrequencyRange or FrequencyVector, depending on the type of element in the array. The element has zero response at frequencies outside that range. The element has zero response at frequencies outside that range.

## ANG

Directions in degrees. ANG can be either a 2-by-M matrix or a row vector of length M.
If ANG is a 2-by-M matrix, each column of the matrix specifies the direction in the form [azimuth; elevation]. The azimuth angle must be between -180 and 180 degrees, inclusive. The elevation angle must be between -90 and 90 degrees, inclusive.

If ANG is a row vector of length $M$, each element specifies a direction's azimuth angle. In this case, the corresponding elevation angle is assumed to be 0 .

## WEIGHTS

Weights on the sensor array. WEIGHTS can be either an N-by-L matrix or a column vector of length N . N is the number of subarrays if H . SensorArray contains subarrays, or the number of elements otherwise. L is the number of frequencies specified in FREQ.

If WEIGHTS is a matrix, each column of the matrix represents the weights at the corresponding frequency in FREQ.

If WEIGHTS is a vector, the weights apply at all frequencies in FREQ.

## STEERANGLE

Subarray steering angle in degrees. STEERANGLE can be a length-2 column vector or a scalar.
If STEERANGLE is a length-2 vector, it has the form [azimuth; elevation]. The azimuth angle must be between -180 and 180 degrees, and the elevation angle must be between -90 and 90 degrees.

If STEERANGLE is a scalar, it represents the azimuth angle. In this case, the elevation angle is assumed to be 0 .

## WS

Subarray element weights
Subarray element weights, specified as complex-valued $N_{S E}$-by- $N$ matrix or 1-by- $N$ cell array where $N$ is the number of subarrays. These weights are applied to the individual elements within a subarray.

Subarray element weights

| Sensor Array | Subarray weights |
| :---: | :---: |
| phased. ReplicatedSubarray | All subarrays have the same dimensions and sizes. Then, the subarray weights form an $N_{S E}$-by$N$ matrix. $N_{S E}$ is the number of elements in each subarray and $N$ is the number of subarrays. Each column of WS specifies the weights for the corresponding subarray. |
| phased.PartitionedArray | Subarrays may not have the same dimensions and sizes. In this case, you can specify subarray weights as <br> - an $N_{S E}$-by- $N$ matrix, where $N_{S E}$ is now the number of elements in the largest subarray. The first $Q$ entries in each column are the element weights for the subarray where $Q$ is the number of elements in the subarray. <br> - a 1 -by- $N$ cell array. Each cell contains a column vector of weights for the corresponding subarray. The column vectors have lengths equal to the number of elements in the corresponding subarray. |

## Dependencies

To enable this argument, set the SensorArray property to an array that contains subarrays and set the SubarraySteering property of the array to 'Custom'.

## Output Arguments

## RESP

Voltage response of the sensor array. The response depends on whether the EnablePolarization property is set to true or false.

- If the EnablePolarization property is set to false, the voltage response, RESP, has the dimensions $M$-by-L. $M$ represents the number of angles specified in the input argument ANG while $L$ represents the number of frequencies specified in FREQ.
- If the EnablePolarization property is set to true, the voltage response, RESP, is a MATLAB ${ }^{\circledR}$ st ruct containing two fields, RESP.H and RESP.V. The RESP.H field represents the array's horizontal polarization response, while RESP.V represents the array's vertical polarization response. Each field has the dimensions $M$-by-L. $M$ represents the number of angles specified in the input argument, ANG, while $L$ represents the number of frequencies specified in FREQ.


## Examples

## Array Response of ULA

Find the response of a 6 -element uniform linear array operating at 1 GHz . The array elements are spaced one-half wavelength apart. The incident signal direction is $45^{\circ}$ azimuth and $10^{\circ}$ elevation. Obtain the response at this direction.

```
fc = 1e9;
```

lambda = physconst('LightSpeed')/fc;

Create the ULA array.

```
array = phased.ULA('NumElements',6,'ElementSpacing',lambda/2);
```

Create the array response System object ${ }^{\mathrm{TM}}$.
response = phased.ArrayResponse('SensorArray',array); resp = response(fc,[45;10]);

## See Also <br> uv2azel|phitheta2azel

## clone

Create identical object

## Syntax

object_clone = clone(original_object)

## Description

object_clone = clone(original_object) creates a copy, object_clone, of the input object, original_object, with identical property values.

## Input Arguments

original_object - Object to be cloned object

Object to be cloned.

## Output Arguments

object_clone - Object clone
object
Object clone, returned as an object of the same class as original_object.

## Version History

Introduced in R2019a

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\text {TM }}$.

## reset

Reset object state and property values

## Syntax

reset(obj)

## Description

reset (obj) resets the internal state and input properties of the object obj.

- If obj writes or reads a file, reset resets the object to the beginning of the file.
- If obj changes properties, reset resets the properties to their initial default values.
- If obj uses a random number generation seed, reset resets the seed property.


## Input Arguments

obj - Object to reset
object
Object whose state you want to reset.

## Version History

Introduced in R2019a

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

## release

Release resources and allow changes to object property values and input characteristics

## Syntax

release(obj)

## Description

release(obj) releases system resources such as memory, file handles, or hardware connections, and allows you to change properties and input characteristics of obj.

## Input Arguments

obj - Object to release
object
Object you want to release.

## Version History

Introduced in R2019a

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\text {TM }}$.

# phased.BackscatterRadarTarget 

Package: phased

Backscatter radar target

## Description

The phased. BackscatterRadarTarget System object models the backscatter of a signal from a target. Backscattering is a special case of radar target scattering when the incident and reflected angles are the same. This type of scattering applies to monostatic radar configurations. The radar cross-section determines the backscattering response of a target to an incident signal. This System object lets you specify an angle-dependent radar cross-section model that covers a range of incident angles.

The phased.BackscatterRadarTarget System object creates a backscattered signal for polarized and nonpolarized signals. While electromagnetic radar signals are polarized, you can often ignore polarization in your simulation and process the signals as scalar signals. To ignore polarization, specify the EnablePolarization property as false. To employ polarization, specify the EnablePolarization property as true.

For nonpolarized signals, you specify the radar cross section as an array of radar cross-section (RCS) values at discrete azimuth and elevation points. The System object interpolates values for incident angles between array points. For polarized signals, you specify the radar scattering matrix using three arrays defined at discrete azimuth and elevation points. These three arrays correspond to the $H H, H V$, and $V V$ polarization components. The $V H$ component is computed using the conjugate symmetry property of the $H V$ component.

For both nonpolarized and polarized signal cases, you can employ one of four Swerling models to generate random fluctuations in the RCS or radar scattering matrix. Choose the model using the Model property. Then, use the SeedSource and Seed properties to control the fluctuations.

| EnablePolarization | Use these properties |
| :--- | :--- |
| false | RCSPattern |
| true | ShhPattern, SvvPattern, and ShvPattern |

To perform radar backscattering:
1 Create the phased.BackscatterRadarTarget object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

target = phased.BackscatterRadarTarget

```
target = phased.BackscatterRadarTarget(Name,Value)
```


## Description

target $=$ phased.BackscatterRadarTarget creates a backscatter radar target System object, target.
target $=$ phased. BackscatterRadarTarget (Name, Value) creates a backscatter radar target System object, target, with each specified property Name set to the specified Value. You can specify additional name and value pair arguments in any order as (Name1, Value1,...,NameN, ValueN).

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## EnablePolarization - Enable polarized signals

false (default)| true
Option to enable processing of polarized signals, specified as false or true. Set this property to true to allow the target to simulate the reflection of polarized radiation. Set this property to false to ignore polarization.

Example: true
Data Types: logical

## AzimuthAngles - Azimuth angles

[-180:180] (default) | 1-by-P real-valued row vector | $P$-by-1 real-valued column vector
Azimuth angles used to define the angular coordinates of each column of the matrices specified by the RCSPattern, ShhPattern, ShvPattern, or SvvPattern properties. Specify the azimuth angles as a length $P$ vector. $P$ must be greater than two. Angle units are in degrees.
Example: [-45:0.1:45]
Data Types: double

## ElevationAngles - Elevation angles

[-90:90] (default) | 1-by-Q real-valued row vector | $Q$-by-1 real-valued column vector
Elevation angles used to define the angular coordinates of each row of the matrices specified by the RCSPattern, ShhPattern, ShvPattern, or SvvPattern properties. Specify the elevation angles as a length $Q$ vector. $Q$ must be greater than two. Angle units are in degrees.

Example: [-30:0.1:30]
Data Types: double
RCSPattern - Radar cross-section pattern
ones (181, 361) (default) | Q-by-P real-valued matrix \| Q-by-P-by-M real-valued array | 1-by-P realvalued vector $\mid M$-by- $P$ real-valued matrix

Radar cross-section (RCS) pattern, specified as a $Q$-by- $P$ real-valued matrix or a $Q$-by- $P$-by- $M$ realvalued array. $Q$ is the length of the vector in the ElevationAngles property. $P$ is the length of the vector in the AzimuthAngles property. $M$ is the number of RCS patterns. The number of patterns corresponds to the number of signals sig passed into the function. You can, however, use a single pattern to model multiple signals reflecting from a single target. Pattern units are square-meters.

You can also specify the pattern as a function only of azimuth for a single elevation. In this case, specify the pattern as either a 1 -by- $P$ vector or an $M$-by- $P$ matrix. Each row is a separate pattern.

This property applies when the EnablePolarization property is false.
Example: [1,.5;.5,1]
Data Types: double

## ShhPattern - Radar-scattering matrix HH polarization component

ones $(181,361)$ (default) | $Q$-by-P complex-valued matrix | $Q$-by- $P$-by-M complex-valued array | 1-by$P$ complex-valued vector | $M$-by- $P$ complex-valued matrix

Radar scattering matrix HH polarization component, specified as a $Q$-by- $P$ complex-valued matrix or a $Q$-by- $P$-by- $M$ complex-valued array. $Q$ is the length of the vector in the ElevationAngles property. $P$ is the length of the vector in the AzimuthAngles property. $M$ is the number of target patterns. The number of patterns corresponds to the number of signals sig passed into the function. You can, however, use a single pattern to model multiple signals reflecting from a single target. Scattering matrix units are meters.

You can also specify the pattern as a function only of azimuth for a single elevation. Then, specify the pattern as either a 1 -by- $P$ vector or an $M$-by- $P$ matrix. Each row is a separate pattern.

This property applies when the EnablePolarization property is true.
Example: [1,1;1i,1i]
Data Types: double
Complex Number Support: Yes

## SvvPattern - Radar scattering matrix VV polarization component

ones $(181,361)$ (default) | $Q$-by-P complex-valued matrix | $Q$-by-P-by-M complex-valued array | 1-by$P$ complex-valued vector | $M$-by- $P$ complex-valued matrix

Radar scattering matrix $V V$ polarization component, specified as a $Q$-by- $P$ complex-valued matrix or a $Q$-by- $P$-by- $M$ complex-valued array. $Q$ is the length of the vector in the ElevationAngles property. $P$ is the length of the vector in the AzimuthAngles property. $M$ is the number of target patterns. The number of patterns corresponds to the number of signals sig passed into the function. You can, however, use a single pattern to model multiple signals reflecting from a single target. Scattering matrix units are meters.

You can also specify the pattern as a function only of azimuth for a single elevation. In this case, specify the pattern as either a 1 -by- $P$ vector or an $M$-by- $P$ matrix. Each row is a separate pattern.

This property applies when the EnablePolarization property is true.
Example: [1,1;1i,1i]
Data Types: double
Complex Number Support: Yes

## ShvPattern - Radar scattering matrix HV polarization component

ones (181, 361) (default) | Q-by-P complex-valued matrix | $Q$-by- $P$-by- $M$ complex-valued array | 1-by$P$ complex-valued vector $\mid M$-by- $P$ complex-valued matrix

Radar scattering matrix $H V$ polarization component, specified as a $Q$-by- $P$ complex-valued matrix or a $Q$-by- $P$-by- $M$ complex-valued array. $Q$ is the length of the vector in the ElevationAngles property. $P$ is the length of the vector in the AzimuthAngles property. $M$ is the number of target patterns. The number of patterns corresponds to the number of signals aig passed into the function. You can, however, use a single pattern to model multiple signals reflecting from a single target. Scattering matrix units are meters.

You can also specify the pattern as a function only of azimuth for a single elevation. In this case, specify the pattern as either a 1 -by- $P$ vector or an $M$-by- $P$ matrix. Each row is a separate pattern.

This property applies when the EnablePolarization property is true.
Example: [1,1;1i,1i]
Data Types: double
Complex Number Support: Yes
Model - Target fluctuation model
'Nonfluctuating' (default)|'Swerling1' | 'Swerling2' |'Swerling3'|'Swerling4'
Target fluctuation model, specified as 'Nonfluctuating', 'Swerling1', 'Swerling2',
'Swerling3', or 'Swerling4'. If you set this property to a value other than 'Nonfluctuating', use the update input argument when calling the function.

Example: 'Swerling3'
Data Types: char

## PropagationSpeed - Signal propagation speed

physconst('LightSpeed') (default) | positive scalar
Signal propagation speed, specified as a positive scalar. Units are in meters per second. The default propagation speed is the value returned by physconst ('LightSpeed'). See physconst for more information.

Example: 3e8
Data Types: double
OperatingFrequency - Operating frequency
300e6 (default) | positive scalar
Operating frequency, specified as a positive scalar. Units are in Hz.
Example: 1e9
Data Types: double
SeedSource - Seed source of random number generator for RCS fluctuation model
'Auto' (default)| 'Property'
Seed source of random number generator for RCS fluctuation model, specified as 'Auto ' or 'Property '. When you set this property to 'Auto ', the System object generates random numbers using the default MATLAB random number generator. When you set this property to 'Property',
you specify the random number generator seed using the Seed property. This property applies when you set the Model property to 'Swerling1', 'Swerling2', 'Swerling3', or 'Swerling4'. When you use this object with Parallel Computing Toolbox ${ }^{\mathrm{TM}}$ software, you set this property to 'Auto '.

## Example: 'Property'

Data Types: char

## Seed - Random number generator seed

0 (default) | nonnegative integer less than $2^{32}$
Random number generator seed, specified as a nonnegative integer less than $2^{32}$. This property applies when the SeedSource property is set to 'Property '.

Example: 32301
Data Types: double

## Usage

## Syntax

```
refl_sig = target(sig,ang)
refl_sig = target(sig,ang,update)
refl_sig = target(sig,ang,laxes)
refl_sig = target(sig,ang,laxes,update)
```


## Description

refl_sig = target(sig,ang) returns the reflected signal, refl sig, of an incident nonpolarized signal, sig, arriving at the target from the angle, ang. This syntax applies when you set the EnablePolarization property to false and the Model property to 'Nonfluctuating '. In this case, the values specified in the RCSPattern property are used to compute the RCS values for the incident and reflected directions, ang.
refl_sig = target(sig, ang, update) uses update to control whether to update the RCS values. This syntax applies when you set the EnablePolarization property to false and the Model property to one of the fluctuating RCS models: 'Swerling1', 'Swerling2', 'Swerling3', or 'Swerling4'. If update is true, a new RCS value is generated. If update is false, the previous RCS value is used.
refl_sig = target(sig,ang,laxes) returns the reflected signal, refl_sig, of an incident polarized signal, sig. The matrix, laxes, specifies the local target coordinate system. This syntax applies when you set EnablePolarization to true and the Model property to 'Nonfluctuating'. The values specified in the ShhPattern, SvvPattern, and ShvPattern properties are used to compute the scattering matrices for the incident and reflected directions, ang.
refl_sig = target(sig,ang,laxes,update) uses the update argument to control whether to update the scattering matrix values. This syntax applies when you set the EnablePolarization property to true and the Model property to one of the fluctuating RCS models: 'Swerling1', 'Swerling2', 'Swerling3', or 'Swerling4'. If update is true, a new RCS value is generated. If update is false, the previous RCS value is used.

## Input Arguments

## sig - Narrowband signal

$N$-by-M complex-valued matrix | 1-by-M struct array containing complex-valued fields

- Narrowband nonpolarized signal, specified as an $N$-by- $M$ complex-valued matrix. The quantity $N$ is the number of signal samples and $M$ is the number of signals reflecting off the target. Each column corresponds to an independent signal incident at a different reflecting angle.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

- Narrowband polarized signal, specified as a 1-by-M struct array containing complex-valued fields. Each struct element contains three $N$-by- 1 column vectors of electromagnetic field components (sig. X , sig. Y, sig. Z) representing the polarized signal that reflects from the target.

For polarized fields, the struct element contains three $N$-by-1 complex-valued column vectors, sig. X, sig. Y, and sig. Z. These vectors represent the $x, y$, and $z$ Cartesian components of the polarized signal.

The size of the first dimension of the matrix fields within the struct can vary to simulate a changing signal length such as a pulse waveform with variable pulse repetition frequency.

The size of the first dimension of the matrix fields within the struct can vary to simulate a changing signal length such as a pulse waveform with variable pulse repetition frequency.

Example: [1, 1; j, 1;0.5,0]
Data Types: double
Complex Number Support: Yes

## ang - Incident signal direction

2-by-1 positive real-valued column vector | 2 -by-M positive real-valued column matrix
Incident signal direction, specified as a 2 -by-1 positive real-valued column vector or a 2 -by- $M$ positive real-valued column matrix. Each column of ang specifies the incident direction of the corresponding signal in the form of an [AzimuthAngle; ElevationAngle] pair. Units are degrees. The number of columns in ang must match the number of independent signals in sig.

## Example: [30;45]

Data Types: double

## update - Update RCS

false (default) | true
Allow the RCS values for fluctuation models to update, specified as false or true. When update is true, a new RCS value is generated with each call to the function. If update is false, the RCS remains unchanged with each call to function.

Example: true
Data Types: logical

## laxes - Local coordinate matrix

eye (3, 3) (default) | 3-by-3 real-valued orthonormal matrix | 3-by-3-by-M real-valued array

Local coordinate system matrix, specified as a 3-by-3 real-valued orthonormal matrix or a 3-by-3-by-M real-valued array. The matrix columns specify the local coordinate system orthonormal $x$-axis, $y$-axis, and $z$-axis, respectively. Each axis is a vector of the form ( $x ; y ; z$ ) with respect to the global coordinate system. When sig has only one signal, laxes is a 3-by-3 matrix. When sig has multiple signals, you can use a single 3-by-3 matrix for multiple signals in sig. In this case, all targets have the same local coordinate systems. When you specify laxes as a 3-by-3-by-M MATLAB array, each page (third index) defines a 3-by-3 local coordinate matrix for the corresponding target.

Example: [1, 0, 0;0,0.7071, -0.7071;0,0.7071,0.7071]
Data Types: double

## Output Arguments

## refl_sig - Narrowband reflected signal

$N$-by- $M$ complex-valued matrix | 1 -by- $M$ struct array containing complex-valued fields

- Narrowband nonpolarized signal, specified as an $N$-by- $M$ complex-valued matrix. Each column contains an independent signal reflected from the target.

The quantity $N$ is the number of signal samples and $M$ is the number of signals reflecting off the target. Each column corresponds to a reflecting angle.

- Narrowband polarized signal, specified as a 1-by-M struct array containing complex-valued fields. Each struct element contains three $N$-by-1 column vectors of electromagnetic field components (sig.X,sig.Y,sig.Z) representing the polarized signal that reflects from the target.

For polarized fields, the struct element contains three $N$-by- 1 complex-valued column vectors, sig.X, sig.Y, and sig.Z. These vectors represent the $x, y$, and $z$ Cartesian components of the polarized signal.

The output refl_sig contains signal samples arriving at the signal destination within the current input time frame. When the propagation time from source to destination exceeds the current time frame duration, the output does not contain all contributions from the input of the current time frame. The remaining output appears in the next call to function.

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:
release(obj)

## Common to All System Objects

step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object

## Examples

## Backscatter Nonpolarized Signal

Calculate the reflected radar signal from a nonfluctuating point target with a peak RCS of $10.0 \mathrm{~m}^{2}$. Use a simplified expression of an RCS pattern of a target for illustrative purposes. Real RCS patterns are more complicated. The RCS pattern covers a range of angles from $10^{\circ}-30^{\circ}$ in azimuth and $5^{\circ}-15^{\circ}$ in elevation. The RCS peaks at $20^{\circ}$ azimuth and $10^{\circ}$ elevation. Assume that the radar operating frequency is 1 GHz and that the signal is a sinusoid at 1 MHz .

Create and plot the RCS pattern.

```
azmax = 20.0;
elmax = 10.0;
azpatangs = 10.0:0.1:30.0;
elpatangs = 5.0:0.1:15.0;
rcspattern = 10.0*cosd(4*(elpatangs - elmax))'*cosd(4*(azpatangs - azmax));
imagesc(azpatangs,elpatangs,rcspattern)
axis image
axis tight
title('RCS')
xlabel('Azimuth (deg)')
ylabel('Elevation (deg)')
```



Generate and plot 50 samples of the radar signal.

```
foper = 1.0e9;
freq = 1.0e6;
fs = 10*freq;
```

nsamp = 50;
t = (0:(nsamp-1))'/fs;
$\operatorname{sig}=\sin \left(2 *\right.$ pi $\left.^{*} f r e q^{*} t\right)$;
plot(t*1e6,sig)
xlabel('Time (\mu seconds)')
ylabel('Signal Amplitude')
grid


Create the phased.BackscatterRadarTarget System object ${ }^{\text {TM }}$.
target $=$ phased. BackscatterRadarTarget('Model','Nonfluctuating',...
'AzimuthAngles', azpatangs,'ElevationAngles',elpatangs,...
'RCSPattern', rcspattern,'OperatingFrequency',foper);
For a sequence of incident angles at constant elevation angle, find and plot the scattered signal amplitude.

```
az0 = 13.0;
el = 10.0;
az = az0 + (0:2:20);
naz = length(az);
ss = zeros(1,naz);
for k = 1:naz
    y = target(sig,[az(k);el]);
    ss(k) = max(abs(y));
end
plot(az,ss,'.')
xlabel('Azimuth (deg)')
```

```
ylabel('Scattered Signal Amplitude')
```

grid


## Backscatter Polarized Signal

Calculate the polarized radar signal scattered from a Swerling1 fluctuating point target. Assume the target axis is rotated from the global coordinate system. Use simple expressions for the scattering patterns for illustration. Real scattering patterns are more complicated. For polarized signals, you need to specify the $H H, H V$, and $V V$ components of the scattering matrix for a range of incident angles. In this example, the patterns cover the range $10^{\circ}-30^{\circ}$ in azimuth and $5^{\circ}-15^{\circ}$ in elevation. Angles are with respect to the target local coordinate system. Assume that the radar operating frequency is 1 GHz and that the signal is a sinusoid with a frequency of 1 MHz . The incident angle is $13.0^{\circ}$ azimuth and $14.0^{\circ}$ elevation with respect to the target orientation.

Create and plot the scattering matrix patterns.

```
azmax = 20.0;
elmax = 10.0;
azpatangs = (10.0:0.1:35.0);
elpatangs = (5.0:0.1:15.0);
shhpat = cosd(4*(elpatangs - elmax))'*cosd(4*(azpatangs - azmax));
shvpat = li*cosd(4*(elpatangs - elmax))'*sind(4*(azpatangs - azmax));
svvpat = sind(4*(elpatangs - elmax))'*sind(4*(azpatangs - azmax));
subplot(1,3,1)
```

```
imagesc(azpatangs,elpatangs,abs(shhpat))
axis image
axis tight
title('HH')
xlabel('Azimuth (deg)')
ylabel('Elevation (deg)')
subplot(1,3,2)
imagesc(azpatangs,elpatangs,abs(shvpat))
axis image
axis tight
title('HV')
xlabel('Azimuth (deg)')
subplot(1,3,3)
imagesc(azpatangs,elpatangs,abs(svvpat))
axis image
axis tight
title('VV')
xlabel('Azimuth (deg)')
```



Create the phased.BackscatterRadarTarget System object ${ }^{\mathrm{TM}}$.
target $=$ phased.BackscatterRadarTarget('EnablePolarization',true, ...
'Model', 'Swerling1','AzimuthAngles',azpatangs,...
'ElevationAngles',elpatangs,'ShhPattern',shhpat,'ShvPattern', shvpat,... 'SvvPattern',svvpat);

Generate 50 samples of a polarized radar signal.

```
foper = 1.0e9;
freq = 1.0e6;
fs = 10*freq;
nsamp = 50;
t = (0:(nsamp-1))'/fs;
signal.X = exp(li*2*pi*freq*t);
signal.Y = exp(li*2*pi*freq*t + pi/3);
signal.Z = zeros(size(signal.X));
tgtaxes = azelaxes(60,10);
ang = [13.0;14.0];
```

Reflect the signal from the target and plot its components.

```
refl_signal = target(signal,ang,tgtaxes,true);
figure
plot(t*le6,real(refl_signal.X))
hold on
plot(t*le6,real(refl_signal.Y))
plot(t*le6,real(refl_signal.Z))
hold off
xlabel('Time \mu seconds')
ylabel('Amplitude')
grid
```



## More About

## Backscattered Radiation

For a narrowband nonpolarized signal, the reflected signal, $Y$, is

$$
Y=\sqrt{G} \cdot X,
$$

where:

- $X$ is the incoming signal.
- $G$ is the target gain factor, a dimensionless quantity given by

$$
G=\frac{4 \Pi \sigma}{\lambda^{2}} .
$$

- $\sigma$ is the mean radar cross-section (RCS) of the target.
- $\lambda$ is the wavelength of the incoming signal.

The incident signal on the target is scaled by the square root of the gain factor.
For narrowband polarized waves, the single scalar signal, $X$, is replaced by a vector signal, $\left(E_{H}, E_{V}\right)$, with horizontal and vertical components. The scattering matrix, $S$, replaces the scalar cross-section, $\sigma$. Through the scattering matrix, the incident horizontal and vertical polarized signals are converted into the reflected horizontal and vertical polarized signals.

$$
\left[\begin{array}{l}
E_{H}^{(s c a t)} \\
E_{V}^{(s c a t)}
\end{array}\right]=\sqrt{\frac{4 \pi}{\lambda^{2}}}\left[\begin{array}{ll}
S_{H H} & S_{V H} \\
S_{H V} & S_{V V}
\end{array}\right]\left[\begin{array}{l}
E_{H}^{(i n c)} \\
E_{V}^{(i n c)}
\end{array}\right]=\sqrt{\frac{4 \pi}{\lambda^{2}}}[S]\left[\begin{array}{l}
E_{H}^{(i n c)} \\
E_{V}^{(i n c)}
\end{array}\right]
$$

For further details, see [1] or [2].

## Version History

## Introduced in R2016a

## References

[1] Mott, H. Antennas for Radar and Communications. New York: John Wiley \& Sons, 1992.
[2] Richards, M. A. Fundamentals of Radar Signal Processing. New York: McGraw-Hill, 2005.
[3] Skolnik, M. Introduction to Radar Systems, 3rd Ed. New York: McGraw-Hill, 2001.

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
See "System Objects in MATLAB Code Generation" (MATLAB Coder).

## See Also

phased.RadarTarget | phased.WidebandBackscatterRadarTarget |
phased. BackscatterSonarTarget | backscatterPedestrian | backscatterBicyclist

## Topics

"Modeling Target Radar Cross Section" (Radar Toolbox)
"Simulating Test Signals for a Radar Receiver"
"Swerling Target Models"

## reset

System object: phased.BackscatterRadarTarget
Package: phased
Reset states of System object

## Syntax

reset(sBSTgt)

## Description

reset (sBSTgt) resets the internal state of the phased. BackscatterRadarTarget object, sBSTgt. This method resets the random number generator state if SeedSource is a property of this System object and has the value 'Property '.

## Input Arguments

sBSTgt - Backscatter radar target
System object
Backscatter radar target, specified as a System object.
Example: phased.BackscatterRadarTarget

## Version History

Introduced in R2016a

## step

System object: phased. BackscatterRadarTarget
Package: phased
Backscatter incoming signal

## Syntax

```
refl_sig = step(target,sig,ang)
refl_sig = step(target,sig,ang,update)
refl_sig = step(target,sig,ang,laxes)
refl_sig = step(target,sig,ang,laxes,update)
```


## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.
refl_sig = step(target,sig,ang) returns the reflected signal, refl_sig, of an incident nonpolarized signal, sig, arriving at the target from the angle, ang. This syntax applies when you set the EnablePolarization property to false and the Model property to 'Nonfluctuating'. In this case, the values specified in the RCSPattern property are used to compute the RCS values for the incident and reflected directions, ang.
refl_sig = step(target,sig,ang, update) uses update to control whether to update the RCS values. This syntax applies when you set the EnablePolarization property to false and the Model property to one of the fluctuating RCS models: 'Swerling1', 'Swerling2', 'Swerling3', or 'Swerling4'. If update is true, a new RCS value is generated. If update is false, the previous RCS value is used.
refl_sig = step(target,sig,ang,laxes) returns the reflected signal, refl_sig, of an incident polarized signal, sig. The matrix, laxes, specifies the local target coordinate system. This syntax applies when you set EnablePolarization to true and the Model property to
'Nonfluctuating '. The values specified in the ShhPattern, SvvPattern, and ShvPattern properties are used to compute the scattering matrices for the incident and reflected directions, ang.
refl_sig = step(target, sig,ang,laxes, update) uses the update argument to control whether to update the scattering matrix values. This syntax applies when you set the EnablePolarization property to true and the Model property to one of the fluctuating RCS models: 'Swerling1', 'Swerling2', 'Swerling3', or 'Swerling4'. If update is true, a new RCS value is generated. If update is false, the previous RCS value is used.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object
issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## target - Backscatter target

System object
Backscatter target, specified as a System object.
Example: phased.BackscatterRadarTarget

## sig - Narrowband signal

$N$-by-M complex-valued matrix | 1 -by- $M$ struct array containing complex-valued fields

- Narrowband nonpolarized signal, specified as an $N$-by- $M$ complex-valued matrix. The quantity $N$ is the number of signal samples and $M$ is the number of signals reflecting off the target. Each column corresponds to an independent signal incident at a different reflecting angle.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

- Narrowband polarized signal, specified as a 1-by-M struct array containing complex-valued fields. Each struct element contains three $N$-by-1 column vectors of electromagnetic field components (sig.X,sig.Y, sig.Z) representing the polarized signal that reflects from the target.

For polarized fields, the struct element contains three $N$-by- 1 complex-valued column vectors, sig. X , sig. Y , and sig.Z. These vectors represent the $x, y$, and $z$ Cartesian components of the polarized signal.

The size of the first dimension of the matrix fields within the struct can vary to simulate a changing signal length such as a pulse waveform with variable pulse repetition frequency.

Example: [1, 1; j, 1;0.5,0]
Data Types: double
Complex Number Support: Yes

## ang - Incident signal direction

2-by-1 positive real-valued column vector | 2 -by- $M$ positive real-valued column matrix
Incident signal direction, specified as a 2 -by- 1 positive real-valued column vector or a 2 -by- $M$ positive real-valued column matrix. Each column of ang specifies the incident direction of the corresponding signal in the form of an [AzimuthAngle; ElevationAngle] pair. Units are degrees. The number of columns in ang must match the number of independent signals in sig.

## Example: [30;45]

Data Types: double

## update - Update RCS

false (default) | true

Allow the RCS values for fluctuation models to update, specified as false or true. When update is true, a new RCS value is generated with each call to the step method. If update is false, the RCS remains unchanged with each call to step.
Example: true
Data Types: logical

## laxes - Local coordinate matrix

eye ( 3,3 ) (default) | 3-by-3 real-valued orthonormal matrix | 3-by-3-by-M real-valued array
Local coordinate system matrix, specified as a 3-by-3 real-valued orthonormal matrix or a 3-by-3-by-M real-valued array. The matrix columns specify the local coordinate system orthonormal $x$-axis, $y$-axis, and $z$-axis, respectively. Each axis is a vector of the form ( $x ; y ; z$ ) with respect to the global coordinate system. When sig has only one signal, laxes is a 3 -by-3 matrix. When sig has multiple signals, you can use a single 3-by-3 matrix for multiple signals in sig. In this case, all targets have the same local coordinate systems. When you specify laxes as a 3-by-3-by-M MATLAB array, each page (third index) defines a 3-by-3 local coordinate matrix for the corresponding target.
Example: [1,0,0;0,0.7071,-0.7071;0,0.7071,0.7071]
Data Types: double

## Output Arguments

## refl_sig - Narrowband reflected signal

$N$-by- $M$ complex-valued matrix | 1 -by- $M$ struct array containing complex-valued fields

- Narrowband nonpolarized signal, specified as an $N$-by- $M$ complex-valued matrix. Each column contains an independent signal reflected from the target.

The quantity $N$ is the number of signal samples and $M$ is the number of signals reflecting off the target. Each column corresponds to a reflecting angle.

- Narrowband polarized signal, specified as a 1-by-M struct array containing complex-valued fields. Each struct element contains three $N$-by-1 column vectors of electromagnetic field components (sig.X,sig.Y,sig.Z) representing the polarized signal that reflects from the target.

For polarized fields, the struct element contains three $N$-by-1 complex-valued column vectors, sig.X, sig.Y, and sig.Z. These vectors represent the $x, y$, and $z$ Cartesian components of the polarized signal.

The output refl_sig contains signal samples arriving at the signal destination within the current input time frame. When the propagation time from source to destination exceeds the current time frame duration, the output does not contain all contributions from the input of the current time frame. The remaining output appears in the next call to step.

## Examples

## Backscatter Nonpolarized Signal

Calculate the reflected radar signal from a nonfluctuating point target with a peak RCS of $10.0 \mathrm{~m}^{2}$. Use a simplified expression of an RCS pattern of a target for illustrative purposes. Real RCS patterns
are more complicated. The RCS pattern covers a range of angles from $10^{\circ}-30^{\circ}$ in azimuth and $5^{\circ}-15^{\circ}$ in elevation. The RCS peaks at $20^{\circ}$ azimuth and $10^{\circ}$ elevation. Assume that the radar operating frequency is 1 GHz and that the signal is a sinusoid at 1 MHz .

Create and plot the RCS pattern.

```
azmax = 20.0;
elmax = 10.0;
azpatangs = 10.0:0.1:30.0;
elpatangs = 5.0:0.1:15.0;
rcspattern = 10.0*cosd(4*(elpatangs - elmax))'*cosd(4*(azpatangs - azmax));
imagesc(azpatangs,elpatangs,rcspattern)
axis image
axis tight
title('RCS')
xlabel('Azimuth (deg)')
ylabel('Elevation (deg)')
```



Generate and plot 50 samples of the radar signal.

```
foper = 1.0e9;
freq = 1.0e6;
fs = 10*freq;
nsamp = 50;
t = (0:(nsamp-1))'/fs;
sig = sin(2*pi*freq*t);
plot(t*le6,sig)
xlabel('Time (\mu seconds)')
```

ylabel('Signal Amplitude')
grid


Create the phased.BackscatterRadarTarget System object ${ }^{\mathrm{TM}}$.
target $=$ phased.BackscatterRadarTarget('Model','Nonfluctuating',...
'AzimuthAngles', azpatangs, 'ElevationAngles',elpatangs,...
'RCSPattern', rcspattern,'OperatingFrequency' , foper);
For a sequence of incident angles at constant elevation angle, find and plot the scattered signal amplitude.

```
az0 = 13.0;
el = 10.0;
az = az0 + (0:2:20);
naz = length(az);
ss = zeros(1,naz);
for k = l:naz
    y = target(sig,[az(k);el]);
    ss(k) = max(abs(y));
end
plot(az,ss,'.')
xlabel('Azimuth (deg)')
ylabel('Scattered Signal Amplitude')
grid
```



## Backscatter Polarized Signal

Calculate the polarized radar signal scattered from a Swerling1 fluctuating point target. Assume the target axis is rotated from the global coordinate system. Use simple expressions for the scattering patterns for illustration. Real scattering patterns are more complicated. For polarized signals, you need to specify the $H H, H V$, and $V V$ components of the scattering matrix for a range of incident angles. In this example, the patterns cover the range $10^{\circ}-30^{\circ}$ in azimuth and $5^{\circ}-15^{\circ}$ in elevation. Angles are with respect to the target local coordinate system. Assume that the radar operating frequency is 1 GHz and that the signal is a sinusoid with a frequency of 1 MHz . The incident angle is $13.0^{\circ}$ azimuth and $14.0^{\circ}$ elevation with respect to the target orientation.

Create and plot the scattering matrix patterns.

```
azmax = 20.0;
elmax = 10.0;
azpatangs = (10.0:0.1:35.0);
elpatangs = (5.0:0.1:15.0);
shhpat = cosd(4*(elpatangs - elmax))'*cosd(4*(azpatangs - azmax));
shvpat = li*cosd(4*(elpatangs - elmax))'*sind(4*(azpatangs - azmax));
svvpat = sind(4*(elpatangs - elmax))'*sind(4*(azpatangs - azmax));
subplot(1,3,1)
imagesc(azpatangs,elpatangs,abs(shhpat))
axis image
axis tight
```

```
title('HH')
xlabel('Azimuth (deg)')
ylabel('Elevation (deg)')
subplot(1,3,2)
imagesc(azpatangs,elpatangs,abs(shvpat))
axis image
axis tight
title('HV')
xlabel('Azimuth (deg)')
subplot(1,3,3)
imagesc(azpatangs,elpatangs,abs(svvpat))
axis image
axis tight
title('VV')
xlabel('Azimuth (deg)')
```



Create the phased.BackscatterRadarTarget System object ${ }^{\text {TM }}$.
target = phased.BackscatterRadarTarget('EnablePolarization',true,...
'Model', 'Swerling1', 'AzimuthAngles',azpatangs,...
'ElevationAngles',elpatangs, 'ShhPattern', shhpat, 'ShvPattern', shvpat,... 'SvvPattern',svvpat);

Generate 50 samples of a polarized radar signal.
foper = 1.0e9;
freq = 1.0e6;
$\mathrm{fs}=10 * \mathrm{freq}$;

```
nsamp = 50;
t = (0:(nsamp-1))'/fs;
signal.X = exp(li*2*pi*freq*t);
signal.Y = exp(li*2*pi*freq*t + pi/3);
signal.Z = zeros(size(signal.X));
tgtaxes = azelaxes(60,10);
ang = [13.0;14.0];
```

Reflect the signal from the target and plot its components.

```
refl_signal = target(signal,ang,tgtaxes,true);
```

figure
plot(t*le6,real(refl_signal.X))
hold on
plot(t*1e6,real(refl_signal.Y))
plot(t*le6,real(refl_signal.Z))
hold off
xlabel('Time \mu seconds')
ylabel('Amplitude')
grid


## Version History

Introduced in R2016a

## See Also

phased.RadarTarget | phased.WidebandBackscatterRadarTarget

# phased.BackscatterSonarTarget 

Package: phased

Sonar target backscatter

## Description

The phased.BackscatterSonarTarget System object models the backscattering of a signal from an underwater or surface target. Backscattering is a special case of sonar target scattering when the incident and reflected angles are the same. This type of scattering applies to monostatic sonar configurations. The sonar target strength (TS) determines the backscattering response of a target to an incoming signal. This object lets you specify an angle-dependent sonar target strength model that covers a range of incident angles.

The object lets you specify the target strength as an array of values at discrete azimuth and elevation points. The object interpolates values for incident angles between array points.

You can employ one of four Swerling models to generate random fluctuations in the target strength. Choose the fluctuation model using the Model property. Then, use the SeedSource and Seed properties to control the fluctuations.

To model a backscattered reflected sonar signal:
1 Define and set up your sonar target. You can set phased. BackscatterSonarTarget System object properties at construction time or leave them to their default values. See "Construction" on page 1-64. Some properties that you set at construction time can be changed later. These properties are tunable.
2 To compute the reflected signal, call the step method of phased. BackscatterSonarTarget. The output of the method depends on the properties of the phased. BackscatterSonarTarget System object. You can change tunable properties at any time.

Note Instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, $y=s t e p(o b j, x)$ and $y=$ obj $(x)$ perform equivalent operations.

## Construction

target $=$ phased.BackscatterSonarTarget creates a backscatter sonar target System object, target.
target $=$ phased.BackscatterSonarTarget (Name, Value) creates a backscatter sonar target System object, target, with each specified property Name set to the specified Value. You can specify additional name and value pair arguments in any order as (Name1, Valuel,...,NameN, ValueN).

## Properties

## AzimuthAngles - Target strength azimuth angles

[-180:180] (default) | real-valued 1-by-P row vector | real-valued P-by-1 column vector

Target strength azimuth angles, specified as a real-valued 1-by- $P$ row vector or $P$-by-1 column vector. These angles define the azimuth coordinates of each column of the matrix specified by the TSPattern property. $P$ must be greater than two. Angle units are in degrees.
Example: [-45:0.1:45]
Data Types: double
ElevationAngles - Elevation angles
[-90:90] (default) | real-valued 1-by- $Q$ row vector $\mid$ real-valued $Q$-by-1 column vector
Target strength elevation angles, specified as a real-valued 1-by- $Q$ row vector or $Q$-by-1 column vector. These angles define the elevation coordinates of each row of the matrix specified by the TSPattern property. $Q$ must be greater than two. Angle units are in degrees.
Example: [-30:0.1:30]
Data Types: double

## TSPattern - Sonar target strength pattern

zeros $(181,361)$ (default) | $Q$-by-P real-valued matrix | $Q$-by- $P$-by-M real-valued array | 1-by-P realvalued vector | $M$-by- $P$ real-valued matrix

Sonar target strength (TS) pattern, specified as a real-valued $Q$-by- $P$ matrix or $Q$-by- $P$-by- $M$ array. $Q$ is the length of the vector in the ElevationAngles property. $P$ is the length of the vector in the AzimuthAngles property. $M$ is the number of target patterns. The number of patterns corresponds to the number of signals passed into the step method. You can, however, use a single pattern to model multiple signals reflecting from a single target. Pattern units are dB .

You can also specify the pattern as a function only of azimuth for a single elevation. In this case, specify the pattern as either a 1 -by- $P$ vector or an $M$-by- $P$ matrix. Each row is a separate pattern.
Example: [1,2;3,4]
Data Types: double

## Model - Target fluctuation model

'Nonfluctuating' (default)|'Swerling1'|'Swerling2' | 'Swerling3' |'Swerling4'
Target fluctuation model, specified as 'Nonfluctuating', 'Swerling1', 'Swerling2', 'Swerling3', or 'Swerling4'. If you set this property to a value other than 'Nonfluctuating', use the update input argument when calling the step method.
Example: 'Swerling3'
Data Types: char

## SeedSource - Seed source of random number generator for TS fluctuation model 'Auto ' (default)|'Property'

Seed source of random number generator for TS fluctuation model, specified as 'Auto ' or 'Property'. When you set this property to 'Auto', the System object generates random numbers using the default MATLAB random number generator. When you set this property to 'Property ', you specify the random number generator seed using the Seed property. This property applies when you set the Model property to 'Swerling1', 'Swerling2', 'Swerling3', or 'Swerling4'. When you use this object with Parallel Computing Toolbox software, you set this property to 'Auto'.
Example: 'Property'

## Data Types: char

## Seed - Random number generator seed

0 (default) | nonnegative integer less than $2^{32}$
Random number generator seed, specified as a nonnegative integer less than $2^{32}$.
Example: 32301

## Dependencies

To enable this property, set the SeedSource property to 'Property ' .
Data Types: double

## Methods

| reset | Reset states of System object |
| :--- | :--- |
| step | Backscatter incoming sonar signal |

## Common to All System Objects

release Allow System object property value changes

## Examples

## Backscatter Sonar Signal from Nonfluctuating Target

Calculate the reflected sonar signal from a nonfluctuating point target with a peak target strength (TS) of 10.0 db . For illustrative purposes, use a simplified expression for the TS pattern of a target. Real TS patterns are more complicated. The TS pattern covers a range of angles from $10^{\circ}$ to $30^{\circ}$ in azimuth and from $5^{\circ}$ to $15^{\circ}$ in elevation. The TS peaks at $20^{\circ}$ azimuth and $10^{\circ}$ elevation. Assume that the sonar operating frequency is 10 kHz and that the signal is a sinusoid at 9500 kHz .

Create and plot the TS pattern.

```
azmax = 20.0;
elmax = 10.0;
azpatangs = [10.0:0.1:35.0];
elpatangs = [5.0:0.1:15.0];
tspattern = 10.0*cosd(4*(elpatangs - elmax))'*cosd(4*(azpatangs - azmax));
tspatterndb = 10*log10(tspattern);
imagesc(azpatangs,elpatangs,tspatterndb)
colorbar
axis image
axis tight
title('TS')
xlabel('Azimuth (deg)')
ylabel('Elevation (deg)')
```



Generate and plot 50 samples of the sonar signal.

```
freq = 9.5e3;
fs = 100*freq;
nsamp = 500;
t = [0:(nsamp-1)]'/fs;
sig = sin(2*pi*freq*t);
plot(t*le6,sig)
xlabel('Time (\mu seconds)')
ylabel('Signal Amplitude')
grid
```



Create the phased.BackscatterSonarTarget System object ${ }^{\mathrm{TM}}$.

```
target = phased.BackscatterSonarTarget('Model','Nonfluctuating', ...
    'AzimuthAngles',azpatangs,'ElevationAngles',elpatangs, ...
    'TSPattern',tspattern);
```

For a sequence of different azimuth incident angles (at constant elevation angle), plot the maximum scattered signal amplitude.

```
az0 = 13.0;
el = 10.0;
naz = 20;
az = az0 + [0:1:20];
naz = length(az);
ss = zeros(1,naz);
for k = 1:naz
    y = target(sig,[az(k);el]);
    ss(k) = max(abs(y));
end
plot(az,ss,'o')
xlabel('Azimuth (deg)')
ylabel('Backscattered Signal Amplitude')
grid
```



## Backscatter Sonar Signal from Fluctuating Target

Calculate the reflected sonar signal from a Swerling2 fluctuating point target with a peak target strength (TS) of 10.0 db . For illustrative purposes, use a simplified expression for the TS pattern of a target. Real TS patterns are more complicated. The TS pattern covers a range of angles from $10^{\circ}$ to $30^{\circ}$ in azimuth and from $5^{\circ}$ ro $15^{\circ}$ in elevation. The TS peaks at $20^{\circ}$ azimuth and $10^{\circ}$ elevation. Assume that the sonar operating frequency is 10 kHz and that the signal is a sinusoid at 9500 kHz .

Create and plot the TS pattern.

```
azmax = 20.0;
elmax = 10.0;
azpatangs = [10.0:0.1:35.0];
elpatangs = [5.0:0.1:15.0];
tspattern = 10.0*cosd(4*(elpatangs - elmax))'*cosd(4*(azpatangs - azmax));
tspatterndb = 10*log10(tspattern);
imagesc(azpatangs,elpatangs,tspatterndb)
colorbar
axis image
axis tight
title('TS')
xlabel('Azimuth (deg)')
ylabel('Elevation (deg)')
```



Generate the sonar signal.

```
freq = 9.5e3;
fs = 10*freq;
nsamp = 50;
t = [0:(nsamp-1)]'/fs;
sig = sin(2*pi*freq*t);
```

Create the phased.BackscatterSonarTarget System object ${ }^{\mathrm{TM}}$.

```
target = phased.BackscatterSonarTarget('Model','Nonfluctuating',...
    'AzimuthAngles',azpatangs,'ElevationAngles',elpatangs,...
    'TSPattern',tspattern,'Model','Swerling2');
```

Compute and plot the fluctuating signal amplitude for 20 time steps.

```
az = 20.0;
el = 10.0;
nsteps = 20;
ss = zeros(1,nsteps);
for k = 1:nsteps
    y = target(sig,[az;el],true);
    ss(k) = max(abs(y));
end
plot([0:(nsteps-1)]*1000/fs,ss,'o')
xlabel('Time (msec)')
ylabel('Backscattered Signal Amplitude')
grid
```



## More About

## Backscattered Sound Radiation

For narrowband acoustic signals, the reflected signal, $Y$, is given by

$$
Y=\sqrt{G} \cdot X,
$$

where

- $X$ is the incoming signal.
- $G$ is the target gain factor given by $10^{T S / 10}$ where $T S$ is the target strength in dB. Specify target strength using the TSPattern property.

For a more detailed explanation of target strength, see "[1] [2]" on page 1-71.

## Version History

Introduced in R2017a

## References

[1] Urick, R.J. Principles of Underwater Sound, 3rd Edition. New York: Peninsula Publishing, 1996.
[2] Sherman, C.S., and J. Butler Transducers and Arrays for Underwater Sound. New York: Springer, 2007.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{rm}}$.
Usage notes and limitations:
See "System Objects in MATLAB Code Generation" (MATLAB Coder).

## See Also

## Objects

phased.BackscatterRadarTarget | phased.IsoSpeedUnderwaterPaths |
phased.WidebandBackscatterRadarTarget| phased.RadarTarget |
backscatterPedestrian|backscatterBicyclist

## Topics

"Underwater Target Detection with an Active Sonar System"
"Locating an Acoustic Beacon with a Passive Sonar System"
"Swerling Target Models"

## reset

System object: phased.BackscatterSonarTarget
Package: phased
Reset states of System object

## Syntax

reset(target)

## Description

reset (target) resets the internal state of the phased. BackscatterSonarTarget object, target. This method resets the random number generator state if SeedSource is a property of this System object and has the value 'Property '.

## Input Arguments

target - Backscatter sonar target
phased.BackscatterSonarTarget System object
Backscatter sonar target, specified as a phased.BackscatterSonarTarget System object.
Example: phased.BackscatterSonarTarget

## Version History

Introduced in R2017a

## step

System object: phased. BackscatterSonarTarget
Package: phased
Backscatter incoming sonar signal

## Syntax

refl_sig = step(target,sig,ang)
refl_sig = step(target,sig,ang,update)

## Description

Note Instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, $y=\operatorname{step}(o b j, x)$ and $y=$ obj ( $x$ ) perform equivalent operations.
refl_sig = step(target,sig,ang) returns the reflected signal, refl_sig, of an incident sonar signal, sig, arriving at the target from the angle, ang.
refl_sig = step(target,sig,ang, update) uses update to control whether to update the target strength (TS) values. This syntax applies when you set the Model property to one of the fluctuating TS models: 'Swerling1', 'Swerling2', 'Swerling3', or 'Swerling4'. If update is true, a new TS value is generated. If update is false, the previous TS value is used.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## target - Backscatter sonar target

phased. BackscatterSonarTarget System object
Backscatter sonar target, specified as a phased. BackscatterSonarTarget System object.

## sig - Sonar signal

$N$-by-M complex-valued matrix
Sonar signal, specified as an $N$-by- $M$ complex-valued matrix. The quantity $N$ is the number of signal samples and $M$ is the number of signals reflecting off the target. Each column corresponds to an independent signal incident at a different reflecting angle.

When you specify the TSPattern property as a $Q$-by- $P$-by- $M$, a separate pattern is used for each signal. When you specify TSPattern as a $Q$-by-Pmatrix, the same pattern is used for every signal.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
Example: [1,1;j,1;0.5,0]
Data Types: double
Complex Number Support: Yes

## ang - Incident signal direction

2-by-1 positive real-valued column vector | 2 -by- $M$ positive real-valued column matrix
Incident signal direction, specified as a 2 -by- 1 positive real-valued column vector or a 2 -by- $M$ positive real-valued column matrix. Each column of ang specifies the incident direction of the corresponding signal in the form of an [AzimuthAngle; ElevationAngle] pair. Units are degrees. The number of columns in ang must match the number of independent signals in sig.

Example: [30;45]
Data Types: double

## update - Update target strength

false (default) | true
Allow the TS values for fluctuation models to update, specified as false or true. When update is true, a new TS value is generated with each call to the step method. If update is false, TS remains unchanged with each call to step.
Example: true
Data Types: logical

## Output Arguments

## refl_sig - Narrowband reflected sonar signal

$N$-by- $\bar{M}$ complex-valued matrix
Narrowband reflected sonar signal, specified as an $N$-by- $M$ complex-valued matrix. Each column contains an independent signal reflected from the target.

The quantity $N$ is the number of signal samples and $M$ is the number of signals reflecting off the target. Each column corresponds to a reflecting angle.

The output refl_sig contains signal samples arriving at the signal destination within the current input time frame. When the propagation time from source to destination exceeds the current time frame duration, the output will not contain all contributions from the input of the current time frame. The remaining output appears in the next call to step.

## Examples

## Backscatter Sonar Signal from Nonfluctuating Target

Calculate the reflected sonar signal from a nonfluctuating point target with a peak target strength (TS) of 10.0 db . For illustrative purposes, use a simplified expression for the TS pattern of a target. Real TS patterns are more complicated. The TS pattern covers a range of angles from $10^{\circ}$ to $30^{\circ}$ in
azimuth and from $5^{\circ}$ to $15^{\circ}$ in elevation. The TS peaks at $20^{\circ}$ azimuth and $10^{\circ}$ elevation. Assume that the sonar operating frequency is 10 kHz and that the signal is a sinusoid at 9500 kHz .

Create and plot the TS pattern.

```
azmax = 20.0;
elmax = 10.0;
azpatangs = [10.0:0.1:35.0];
elpatangs = [5.0:0.1:15.0];
tspattern = 10.0*cosd(4*(elpatangs - elmax))'*cosd(4*(azpatangs - azmax));
tspatterndb = 10*log10(tspattern);
imagesc(azpatangs,elpatangs,tspatterndb)
colorbar
axis image
axis tight
title('TS')
xlabel('Azimuth (deg)')
ylabel('Elevation (deg)')
```



Generate and plot 50 samples of the sonar signal.

```
freq = 9.5e3;
fs = 100*freq;
nsamp = 500;
t = [0:(nsamp-1)]'/fs;
sig = sin(2*pi*freq*t);
plot(t*le6,sig)
xlabel('Time (\mu seconds)')
```

ylabel('Signal Amplitude')
grid


Create the phased.BackscatterSonarTarget System object ${ }^{\mathrm{TM}}$.
target $=$ phased. BackscatterSonarTarget('Model','Nonfluctuating',..
'AzimuthAngles',azpatangs,'ElevationAngles',elpatangs, ...
'TSPattern',tspattern) ;
For a sequence of different azimuth incident angles (at constant elevation angle), plot the maximum scattered signal amplitude.

```
az0 = 13.0;
el = 10.0;
naz = 20;
az = az0 + [0:1:20];
naz = length(az);
ss = zeros(1,naz);
for k = 1:naz
    y = target(sig,[az(k);el]);
    ss(k) = max(abs(y));
end
plot(az,ss,'o')
xlabel('Azimuth (deg)')
ylabel('Backscattered Signal Amplitude')
grid
```



## Backscatter Sonar Signal from Fluctuating Target

Calculate the reflected sonar signal from a Swerling2 fluctuating point target with a peak target strength (TS) of 10.0 db . For illustrative purposes, use a simplified expression for the TS pattern of a target. Real TS patterns are more complicated. The TS pattern covers a range of angles from $10^{\circ}$ to $30^{\circ}$ in azimuth and from $5^{\circ}$ ro $15^{\circ}$ in elevation. The TS peaks at $20^{\circ}$ azimuth and $10^{\circ}$ elevation. Assume that the sonar operating frequency is 10 kHz and that the signal is a sinusoid at 9500 kHz .

Create and plot the TS pattern.

```
azmax = 20.0;
elmax = 10.0;
azpatangs = [10.0:0.1:35.0];
elpatangs = [5.0:0.1:15.0];
tspattern = 10.0*cosd(4*(elpatangs - elmax))'*cosd(4*(azpatangs - azmax));
tspatterndb = 10*log10(tspattern);
imagesc(azpatangs,elpatangs,tspatterndb)
colorbar
axis image
axis tight
title('TS')
xlabel('Azimuth (deg)')
ylabel('Elevation (deg)')
```

TS


Generate the sonar signal.

```
freq = 9.5e3;
fs = 10*freq;
nsamp = 50;
t = [0:(nsamp-1)]'/fs;
sig = sin(2*pi*freq*t);
```

Create the phased.BackscatterSonarTarget System object ${ }^{\mathrm{TM}}$.

```
target = phased.BackscatterSonarTarget('Model','Nonfluctuating',...
    'AzimuthAngles',azpatangs,'ElevationAngles',elpatangs,...
    'TSPattern',tspattern,'Model','Swerling2');
```

Compute and plot the fluctuating signal amplitude for 20 time steps.

```
az = 20.0;
el = 10.0;
nsteps = 20;
ss = zeros(1,nsteps);
for k = 1:nsteps
    y = target(sig,[az;el],true);
    ss(k) = max(abs(y));
end
plot([0:(nsteps-1)]*1000/fs,ss,'o')
xlabel('Time (msec)')
ylabel('Backscattered Signal Amplitude')
grid
```



Version History
Introduced in R2017a

## phased.BeamscanEstimator

Package: phased
Beamscan spatial spectrum estimator for ULA

## Description

The phased. BeamscanEstimator System object calculates a beamscan spatial spectrum estimate for a uniform linear array (ULA). The object estimates the incoming signal spatial spectrum using a narrowband conventional beamformer.

To estimate the spatial spectrum:
1 Create the phased. BeamscanEstimator object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

estimator $=$ phased. BeamscanEstimator estimator $=$ phased. BeamscanEstimator(Name,Value)

## Description

estimator $=$ phased. BeamscanEstimator creates a beamscan spatial spectrum estimator System object.
estimator $=$ phased. BeamscanEstimator(Name,Value) creates an object, estimator, with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Namel,Valuel,...,NameN,ValueN).

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## SensorArray - ULA sensor array

phased.ULA System object (default)
ULA sensor array, specified as a phased.ULA System object. If you do not specify any name-value pair properties for the ULA sensor array, the default properties of the array are used.

PropagationSpeed - Signal propagation speed
physconst('LightSpeed') (default) | real-valued positive scalar
Signal propagation speed, specified as a real-valued positive scalar. Units are in meters per second. The default propagation speed is the value returned by physconst('LightSpeed').
Example: 3e8
Data Types: single | double

## OperatingFrequency - Operating frequency <br> 300e6 (default) | positive scalar

Operating frequency, specified as a positive scalar. Units are in Hz .
Example: 1e9
Data Types: single | double

## NumPhaseShifterBits - Number of phase shifter quantization bits

0 (default) | non-negative scalar
The number of bits used to quantize the phase shift component of beamformer or steering vector weights, specified as a non-negative integer. A value of zero indicates that no quantization is performed.

Example: 5
Data Types: single | double
ForwardBackwardAveraging - Enable forward-backward averaging false (default) |true

Enable forward-backward averaging, specified as false or true. Set this property to true to use forward-backward averaging to estimate the covariance matrix for sensor arrays with a conjugate symmetric array manifold.
Data Types: logical

## SpatialSmoothing - Enable spatial smoothing <br> 0 (default) | nonnegative integer

Option to enable spatial smoothing, specified as a nonnegative integer. Use spatial smoothing to compute the arrival directions of coherent signals. A value of zero specifies no spatial smoothing. A positive value represents the number of subarrays used to compute the smoothed (averaged) source covariance matrix. Each increment in this value lets you handle one additional coherent source, but reduces the effective number of array elements by one. The length of the smoothing aperture, $L$, depends on the array length, $M$, and the averaging number, $K$, by $L=M-K+1$. The maximum value of $K$ is $M-2$.

## Example: 5

Data Types: double

## ScanAngles - Broadside scan angles

[-90:90] (default) | real-valued K-length vector

Broadside scan angles, specified as a real-valued vector. Units are in degrees. Broadside angles are between the search direction and the ULA array axis. The angles lie between $-90^{\circ}$ and $90^{\circ}$, inclusive. Specify the angles in increasing value.

Example: [-20:20]
Data Types: single|double

## DOAOutputPort - Enable directions of arrival output <br> false (default)| true

Option to enable directions-of-arrival (DOA) output, specified as false or true. To obtain the DOA of signals, set this property to true. The DOAs are returned in the second output argument when the object is executed.
Data Types: logical

## NumSignals - Number of arriving signals

1 (default) | positive integer
Number of arriving signals for DOA estimation, specified as a positive integer.

## Example: 3

## Dependencies

To enable this property, set the DOAOutputPort property to true.
Data Types: single | double

## Usage

## Syntax

Y = estimator (X)
[Y,ANG] = estimator(X)

## Description

$\mathrm{Y}=$ estimator $(\mathrm{X})$ estimates the spatial spectrum from data X .
The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
[ $\mathrm{Y}, \mathrm{ANG}$ ] = estimator $(\mathrm{X})$ returns the directions of arrival, ANG, of the signals. To enable this syntax, set the DOAOutputPort property to true. ANG is a row vector of the estimated broadside angles (in degrees). You can specify ANG as single or double precision. If the object cannot identify a signal direction, it will return NaN .

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

X - Channel data
complex-valued matrix
Channel data, specified as a complex-valued matrix. Columns of the data matrix correspond to channels.

Data Types: single | double
Complex Number Support: Yes

## Output Arguments

## Y - Magnitude of estimated spatial spectrum

real-valued 1-by-L column vector
Magnitude of the estimated spatial spectrum, returned as a real-valued 1-by- $L$ column vector. $L$ is the number of scan angles specified by the ScanAngles property.

Data Types: single | double

## ANG - Estimated broadside angles

real-valued 1-by-K row vector | NaN
Estimated broadside angles of signal arrivals, returned as a real-valued 1-by-K row vector. Units are in degrees. The NaN value in any vector element indicates that an estimate could not be found.

```
Data Types: single | double
```


## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:
release(obj)

## Specific to spectral estimation

plotSpectrum Plot spatial spectrum

## Common to All System Objects

step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object

## Examples

## Estimate Directions of Arrival of Two Signals

Estimate the DOA's of two signals received by a 10 -element ULA with element spacing of 1 meter. The antenna operating frequency is 150 MHz . The actual direction of the first signal is $10^{\circ}$ in azimuth and $20^{\circ}$ in elevation. The direction of the second signal is $60^{\circ}$ in azimuth and $-5^{\circ}$ in elevation.

Create the signals and array.
fs = 8000;
t = (0:1/fs:1).';
$\mathrm{xl}=\cos (2 * \mathrm{pi} * \mathrm{t} * 300)$;
$x 2=\cos \left(2 *\right.$ pi $\left.^{*} t * 400\right)$;
antenna = phased.IsotropicAntennaElement('FrequencyRange',[100e6 300e6]);
array = phased.ULA('Element', antenna,'NumElements',10,'ElementSpacing',1);
fc = 150e6;
$\mathrm{x}=$ collectPlaneWave(array,[x1 x2],[10 20;60 -5]',fc);
noise $=0.1^{*}($ randn(size(x)) $+1 i * r a n d n(s i z e(x))) ;$
Solve for the DOAs.

```
estimator = phased.BeamscanEstimator('SensorArray',array, ...
    'OperatingFrequency',fc,'DOAOutputPort',true,'NumSignals',2);
[~,doas] = estimator(x + noise);
doas = broadside2az(sort(doas),[20 -5]);
disp(doas)
    9.5829 60.3813
```

Because the default values for the ScanAngles property has a granularity of $1^{\circ}$, the DOA estimates are not accurate. Improve the accuracy by choosing a finer grid.

```
estimator2 = phased.BeamscanEstimator('SensorArray',array, ...
    'OperatingFrequency',fc,'ScanAngles',-60:0.1:60, ...
    'DOAOutputPort',true,'NumSignals',2);
[~,doas] = estimator2(x + noise);
doas = broadside2az(sort(doas),[20 -5]);
disp(doas)
    10.0093 59.9751
```


## Plot the beamscan spectrum

plotSpectrum(estimator)


## Algorithms

## Data Precision

This System object supports single and double precision for input data, properties, and arguments. If the input data X is single precision, the output data is single precision. If the input data X is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

## Version History

## Introduced in R2011a

## References

[1] Van Trees, H. Optimum Array Processing. New York: Wiley-Interscience, 2002, pp. 1142-1143.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:

See "System Objects in MATLAB Code Generation" (MATLAB Coder).
This System object supports single and double precision for input data, properties, and arguments. If the input data $X$ is single precision, the output data is single precision. If the input data $X$ is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

## See Also

broadside2az | phased. BeamscanEstimator2D

## phased.BeamscanEstimator2D

Package: phased
2-D beamscan spatial spectrum estimator

## Description

The phased.BeamscanEstimator2D System object calculates a beamscan 2-D spatial spectrum estimate for any Phased Array System Toolbox array. The object estimates the incoming signal spatial spectrum using a narrowband conventional beamformer.

To estimate the spatial spectrum:
1 Create the phased. BeamscanEstimator2D object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

```
estimator = phased.BeamscanEstimator2D
estimator = phased.BeamscanEstimator2D(Name,Value)
```


## Description

estimator $=$ phased.BeamscanEstimator2D creates a beamscan 2-D spatial spectrum estimator System object.
estimator = phased.BeamscanEstimator2D(Name,Value) creates an object, estimator, with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN).

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## SensorArray - Sensor array

phased.ULA array with default array properties (default) | Phased Array System Toolbox array System object

Sensor array, specified as a Phased Array System Toolbox array System object.

Example: phased.URA
PropagationSpeed - Signal propagation speed
physconst('LightSpeed') (default) | real-valued positive scalar
Signal propagation speed, specified as a real-valued positive scalar. Units are in meters per second. The default propagation speed is the value returned by physconst('LightSpeed').
Example: 3e8
Data Types: single|double
OperatingFrequency - Operating frequency
300e6 (default) | positive scalar
Operating frequency, specified as a positive scalar. Units are in Hz.
Example: 1e9
Data Types: single | double

## NumPhaseShifterBits - Number of phase shifter quantization bits

0 (default) | non-negative scalar
The number of bits used to quantize the phase shift component of beamformer or steering vector weights, specified as a non-negative integer. A value of zero indicates that no quantization is performed.

Example: 5
Data Types: single | double

## ForwardBackwardAveraging - Enable forward-backward averaging false (default) | true

Enable forward-backward averaging, specified as false or true. Set this property to true to use forward-backward averaging to estimate the covariance matrix for sensor arrays with a conjugate symmetric array manifold.
Data Types: logical

## AzimuthScanAngles - Azimuth scan angles

[-90:90] (default) | real-valued row vector
Azimuth scan angles, specified as a or real-valued row vector. Angle units are in degrees. The angle values must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive, and be in ascending order.
Example: [-30:20]
Data Types: single | double

## ElevationScanAngles - Elevation scan angles

0 (default) | real-valued row vector
Elevation scan angles, specified as a real-valued row vector. Angle units are in degrees. The angle values must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive, and be in ascending order.
Example: [-70:75]
Data Types: single | double

## DOAOutputPort - Enable directions of arrival output <br> false (default) | true

Option to enable directions-of-arrival (DOA) output, specified as false or true. To obtain the DOA of signals, set this property to true. The DOAs are returned in the second output argument when the object is executed.

## Data Types: logical

## NumSignals - Number of arriving signals

1 (default) | positive integer
Number of arriving signals for DOA estimation, specified as a positive integer.
Example: 3

## Dependencies

To enable this property, set the DOAOutputPort property to true.

## Data Types: single | double

## Usage

## Syntax

Y = estimator(X)
[Y,ANG] = estimator(X)

## Description

$Y=$ estimator $(X)$ estimates the spatial spectrum from data $X$.
The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
[ $\mathrm{Y}, \mathrm{ANG}$ ] = estimator $(\mathrm{X})$ returns the directions of arrival, ANG, of the signals. To enable this syntax, set the DOAOutputPort property to true. ANG is a 2 -by- $N$ matrix of the estimated azimuths and elevations of the signal direction. $N$ is specified by the NumSignals property. If the object cannot identify a signal direction, it will return NaN .

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## X - Array data

complex-valued matrix
Array data, specified as a complex-valued matrix. Columns of the data matrix correspond to channels.

Data Types: single|double
Complex Number Support: Yes

## Output Arguments

Y - Magnitude of estimated spatial spectrum
positive, real-valued, $K$-by- $L$ matrix
Magnitude of the estimated spatial spectrum, returned as a positive, real-valued, $K$-by- $L$ matrix.
Data Types: single|double

## ANG - Estimated direction angles of signal arrivals

## real-valued 2-by-K matrix | NaN

Estimated direction angles of signal arrivals, returned as a real-valued 2-by-K matrix. Each column has the form [azimuth; elevation]. The NaN value in any matrix element indicates that an estimate could not be found. Units are in degrees.
Data Types: single | double

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```


## Specific to spectral estimation

plotSpectrum Plot spatial spectrum

## Common to All System Objects

step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object

## Examples

## Estimate Directions of Arrival of Two Signals

Estimate the DOAs of two signals received by a 50 -element URA with a rectangular lattice. The antenna operating frequency is 150 MHz . The actual direction of the first signal is $-37^{\circ}$ in azimuth and $0^{\circ}$ in elevation. The direction of the second signal is $17^{\circ}$ in azimuth and $20^{\circ}$ in elevation.

```
antenna = phased.IsotropicAntennaElement('FrequencyRange',[100e6 300e6]);
array = phased.URA('Element',antenna,'Size',[5 10],'ElementSpacing',[1 0.6]);
fc = 150e6;
lambda = physconst('LightSpeed')/fc;
angl = [-37.5; 10.2];
ang2 = [17.4; 20.6];
x = sensorsig(getElementPosition(array)/lambda,8000,[ang1 ang2],0.2);
```

```
estimator = phased.BeamscanEstimator2D('SensorArray',array,'OperatingFrequency',fc, ...
    'DOAOutputPort',true,'NumSignals',2,'AzimuthScanAngles',-50:50,'ElevationScanAngles',-30:30)
[~,doas] = estimator(x);
disp(doas)
    17 -37
    20 10
```

Because the values for the AzimuthScanAngles and ElevationScanAngles properties have a granularity of $1^{\circ}$, the DOA estimates are not accurate. Improve the accuracy by choosing a finer grid

```
estimator2 = phased.BeamscanEstimator2D('SensorArray',array,'OperatingFrequency',fc, ...
    'DOAOutputPort',true,'NumSignals',2,'AzimuthScanAngles',-50:0.05:50,'ElevationScanAngles',-3
[~,doas] = estimator2(x);
disp(doas)
```

    17.3000-37.4000
    \(20.5000 \quad 10.3000\)
    Plot the beamscan spatial spectrum
plotSpectrum(estimator)

## 2-D Beamscan Spatial Spectrum



## Algorithms

## Data Precision

This System object supports single and double precision for input data, properties, and arguments. If the input data X is single precision, the output data is single precision. If the input data X is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

## Version History

Introduced in R2011a

## References

[1] Van Trees, H. Optimum Array Processing. New York: Wiley-Interscience, 2002.

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:

See "System Objects in MATLAB Code Generation" (MATLAB Coder).
This System object supports single and double precision for input data, properties, and arguments. If the input data $X$ is single precision, the output data is single precision. If the input data $X$ is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

## See Also

phased.BeamscanEstimator|uv2azel | phitheta2azel

## plotSpectrum

System object: phased. BeamscanEstimator2D
Package: phased
Plot spatial spectrum

## Syntax

plotSpectrum(estimator)
plotSpectrum(estimator,Name, Value)
hl = plotSpectrum( $\qquad$ )

## Description

plotSpectrum(estimator) plots the spatial spectrum resulting from the most recent execution of the object.
plotSpectrum(estimator, Name, Value) plots the spatial spectrum with additional options specified by one or more Name, Value pair arguments.
hl = plotSpectrum( $\qquad$ ) returns the line handle in the figure.

## Input Arguments

H

Spatial spectrum estimator object.

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## NormalizeResponse

Set this value to true to plot the normalized spectrum. Setting this value to false plots the spectrum without normalization.

Default: false
Title
Character vector to use as figure title.

## Default: ' '

## Unit

Plot units, specified as 'db', 'mag', or 'pow'.
Default: 'db'

## Examples

## Estimate Directions of Arrival of Two Signals

Estimate the DOAs of two signals received by a 50 -element URA with a rectangular lattice. The antenna operating frequency is 150 MHz . The actual direction of the first signal is $-37^{\circ}$ in azimuth and $0^{\circ}$ in elevation. The direction of the second signal is $17^{\circ}$ in azimuth and $20^{\circ}$ in elevation.

```
antenna = phased.IsotropicAntennaElement('FrequencyRange',[100e6 300e6]);
array = phased.URA('Element',antenna,'Size',[5 10],'ElementSpacing',[1 0.6]);
fc = 150e6;
lambda = physconst('LightSpeed')/fc;
angl = [-37.5; 10.2];
ang2 = [17.4; 20.6];
x = sensorsig(getElementPosition(array)/lambda,8000,[ang1 ang2],0.2);
estimator = phased.BeamscanEstimator2D('SensorArray',array,'OperatingFrequency',fc, ...
    'DOAOutputPort',true,'NumSignals',2,'AzimuthScanAngles',-50:50,'ElevationScanAngles',-30:30)
[~,doas] = estimator(x);
disp(doas)
    17-37
    20 10
```

Because the values for the AzimuthScanAngles and ElevationScanAngles properties have a granularity of $1^{\circ}$, the DOA estimates are not accurate. Improve the accuracy by choosing a finer grid

```
estimator2 = phased.BeamscanEstimator2D('SensorArray',array,'OperatingFrequency',fc, ...
    'DOAOutputPort',true,'NumSignals',2,'AzimuthScanAngles',-50:0.05:50,'ElevationScanAngles', -3( 
[~,doas] = estimator2(x);
disp(doas)
    17.3000 -37.4000
    20.5000 10.3000
```

Plot the beamscan spatial spectrum

```
plotSpectrum(estimator)
```


## 2-D Beamscan Spatial Spectrum



## reset

System object: phased.BeamscanEstimator2D
Package: phased
Reset states of 2-D beamscan spatial spectrum estimator object

## Syntax

reset (H)

## Description

reset $(\mathrm{H})$ resets the states of the BeamscanEstimator2D object, H .

## step

System object: phased. BeamscanEstimator2D
Package: phased
Perform 2-D spatial spectrum estimation

## Syntax

```
Y = step(H,X)
[Y,ANG] = step(H,X)
```


## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step (obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.
$\mathrm{Y}=\operatorname{step}(\mathrm{H}, \mathrm{X})$ estimates the spatial spectrum from X using the estimator $\mathrm{H} . \mathrm{X}$ is a matrix whose columns correspond to channels. Y is a matrix representing the magnitude of the estimated 2-D spatial spectrum. $Y$ has a row dimension equal to the number of elevation angles specified in ElevationScanAngles and a column dimension equal to the number of azimuth angles specified in AzimuthScanAngles. You can specify X as single or double precision.
[ $\mathrm{Y}, \mathrm{ANG}$ ] $=\operatorname{step}(\mathrm{H}, \mathrm{X})$ returns additional output ANG as the signal's direction of arrival (DOA) when the DOAOutputPort property is true. ANG is a two row matrix where the first row represents the estimated azimuth and the second row represents the estimated elevation (in degrees).

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Examples

## Estimate DOAs of Two Sinusoidal Signals

Estimate the DOAs of two sinusoidal signals received by a 50 -element URA with a rectangular lattice. The antenna operating frequency is 150 MHz . The actual direction of the first signal is $-37^{\circ}$ in azimuth and $0^{\circ}$ in elevation. The direction of the second signal is $17^{\circ}$ in azimuth and $20^{\circ}$ in elevation.

Create the signals and solve for the DOA's.

```
fs = 8000;
t = (0:1/fs:1).';
x1 = cos(2*pi*t*300);
x2 = cos(2*pi*t*400);
array = phased.URA('Size',[5 10],'ElementSpacing',[1 0.6]);
array.Element.FrequencyRange = [100e6 300e6];
fc = 150e6;
x = collectPlaneWave(array,[x1 x2],[-37 0; 17 20]',fc);
noise = 0.1*(randn(size(x)) + li*randn(size(x)));
estimator = phased.BeamscanEstimator2D('SensorArray',array, ...
    'OperatingFrequency',fc, ...
    'DOAOutputPort',true,'NumSignals',2, ...
    'AzimuthScanAngles',-50:50, ...
    'ElevationScanAngles',-30:30);
[~,doas] = estimator(x + noise)
doas = 2×2
    -37 17
        0 20
```

Plot the spatial spectrum.
plotSpectrum(estimator)

## 2-D Beamscan Spatial Spectrum



## See Also

azel2uv|azel2phitheta

# phased.BeamspaceESPRITEstimator 

Package: phased
Beamspace ESPRIT direction of arrival (DOA) estimator for ULA

## Description

The BeamspaceESPRITEstimator object computes a DOA estimate for a uniform linear array. The computation uses the estimation of signal parameters via rotational invariance techniques (ESPRIT) algorithm in beamspace.

To estimate the direction of arrival (DOA):
1 Define and set up your DOA estimator. See "Construction" on page 1-102.
2 Call step to estimate the DOA according to the properties of phased.BeamspaceESPRITEstimator. The behavior of step is specific to each object in the toolbox.

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.

## Construction

H = phased.BeamspaceESPRRITEstimator creates a beamspace ESPRIT DOA estimator System object, H. The object estimates the signal's direction of arrival using the beamspace ESPRIT algorithm with a uniform linear array (ULA).

H = phased.BeamspaceESPRITEstimator(Name, Value) creates object, H, with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN).

## Properties

## SensorArray

Handle to sensor array
Specify the sensor array as a handle. The sensor array must be a phased. ULA object.
Default: phased.ULA with default property values

## PropagationSpeed

Signal propagation speed
Specify the propagation speed of the signal, in meters per second, as a positive scalar. You can specify this property as single or double precision.

Default: Speed of light
OperatingFrequency
System operating frequency
Specify the operating frequency of the system in hertz as a positive scalar. The default value corresponds to 300 MHz . You can specify this property as single or double precision.

Default: 3e8

## SpatialSmoothing

Spatial smoothing
Specify the number of averaging used by spatial smoothing to estimate the covariance matrix as a nonnegative integer. Each additional smoothing handles one extra coherent source, but reduces the effective number of element by 1. The maximum value of this property is $\mathrm{M}-2$, where M is the number of sensors. You can specify this property as single or double precision.

Default: 0, indicating no spatial smoothing

## NumSignalsSource

## Source of number of signals

Specify the source of the number of signals as one of 'Auto' or 'Property'. If you set this property to 'Auto', the number of signals is estimated by the method specified by the NumSignalsMethod property. You can specify this property as single or double precision.

Default: 'Auto'

## NumSignalsMethod

Method to estimate number of signals
Specify the method to estimate the number of signals as one of 'AIC' or 'MDL'. 'AIC' uses the Akaike Information Criterion and 'MDL' uses Minimum Description Length Criterion. This property applies when you set the NumSignalsSource property to 'Auto'.

Default: 'AIC'

## NumSignals

Number of signals
Specify the number of signals as a positive integer scalar. This property applies when you set the NumSignalsSource property to 'Property'. You can specify this property as single or double precision.

## Default: 1

Method
Type of least square method

Specify the least squares method used for ESPRIT as one of 'TLS' or 'LS'. 'TLS' refers to total least squares and 'LS' refers to least squares.

Default: 'TLS'

## BeamFanCenter

Beam fan center direction (in degrees)
Specify the direction of the center of the beam fan (in degrees) as a real scalar value between - 90 and 90 . You can specify this property as single or double precision. This property is tunable.

Default: 0

## NumBeamsSource

Source of number of beams
Specify the source of the number of beams as one of 'Auto' or 'Property'. If you set this property to 'Auto', the number of beams equals $\mathrm{N}-\mathrm{L}$, where N is the number of array elements and L is the value of the SpatialSmoothing property.

Default: 'Auto'
NumBeams
Number of beams
Specify the number of beams as a positive scalar integer. The lower the number of beams, the greater the reduction in computational cost. This property applies when you set the NumBeamsSource to ' Property '. You can specify this property as single or double precision.

## Default: 2

## Methods

step Perform DOA estimation

## Common to All System Objects

release $\quad$ Allow System object property value changes

## Examples

## Estimate DOA of Two Signals Using Beamspace ESPRIT

Estimate the directions of arrival (DOA) of two signals received by a standard 10-element ULA with element spacing 1 meter. The antenna operating frequency is 150 MHz . The actual direction of the first signal is $10^{\circ}$ in azimuth and $20^{\circ}$ in elevation. The direction of the second signal is $45^{\circ}$ in azimuth and $60^{\circ}$ in elevation.

Create the two signals arriving at the array.

```
fs = 8000;
t = (0:1/fs:1).';
x1 = cos(2*pi*t*300);
x2 = cos(2*pi*t*400);
array = phased.ULA('NumElements',10,'ElementSpacing',1);
array.Element.FrequencyRange = [100e6 300e6];
fc = 150e6;
x = collectPlaneWave(array,[x1 x2],[10 20;45 60]',fc);
noise = 0.1/sqrt(2)*(randn(size(x)) + li*randn(size(x)));
```

Set up the beamspace ESPRIT estimator and solve for the DOAs.

```
estimator = phased.BeamspaceESPRITEstimator('SensorArray',array, ...
    'OperatingFrequency',fc,'NumSignalsSource','Property','NumSignals',2);
doas = estimator(x + noise);
az = broadside2az(sort(doas),[20 60])
az = 1×2
    9.9972 45.0061
```


## Algorithms

## Data Precision

This System object supports single and double precision for input data, properties, and arguments. If the input data X is single precision, the output data is single precision. If the input data X is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

## Version History

## Introduced in R2011a

## References

[1] Van Trees, H. Optimum Array Processing. New York: Wiley-Interscience, 2002.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
See "System Objects in MATLAB Code Generation" (MATLAB Coder).
This System object supports single and double precision for input data, properties, and arguments. If the input data $X$ is single precision, the output data is single precision. If the input data $X$ is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

## See Also

broadside2az|phased.ESPRITEstimator

## step

System object: phased. BeamspaceESPRITEstimator
Package: phased
Perform DOA estimation

## Syntax

ANG $=$ step $(H, X)$

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = $\underline{\text { step }(o b j, x) \text { and } y=o b j(x) \text { perform equivalent operations. }}$

ANG $=\operatorname{step}(\mathrm{H}, \mathrm{X})$ estimates the DOAs from X using the DOA estimator $\mathrm{H} . \mathrm{X}$ is a matrix whose columns correspond to channels. ANG is a row vector of the estimated broadside angles (in degrees). You can specify the input data $X$ as single or double precision.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Examples

## Estimate DOA of Two Signals Using Beamspace ESPRIT

Estimate the directions of arrival (DOA) of two signals received by a standard 10-element ULA with element spacing 1 meter. The antenna operating frequency is 150 MHz . The actual direction of the first signal is $10^{\circ}$ in azimuth and $20^{\circ}$ in elevation. The direction of the second signal is $45^{\circ}$ in azimuth and $60^{\circ}$ in elevation.

Create the two signals arriving at the array.

```
fs = 8000;
t = (0:1/fs:1).';
x1 = cos(2*pi*t*300);
x2 = cos(2*pi*t*400);
array = phased.ULA('NumElements',10,'ElementSpacing',1);
```

```
array.Element.FrequencyRange = [100e6 300e6];
fc = 150e6;
x = collectPlaneWave(array,[x1 x2],[10 20;45 60]',fc);
noise = 0.1/sqrt(2)*(randn(size(x)) + li*randn(size(x)));
```

Set up the beamspace ESPRIT estimator and solve for the DOAs.
estimator = phased.BeamspaceESPRITEstimator('SensorArray',array, ...
'OperatingFrequency',fc,'NumSignalsSource','Property','NumSignals',2);
doas = estimator(x + noise);
az = broadside2az(sort(doas),[20 60])
$a z=1 \times 2$
9.997245 .0061

## phased.CFARDetector

Package: phased
Constant false alarm rate (CFAR) detector

## Description

The CFARDetector object implements a one-dimensional constant false-alarm rate (CFAR) detector. Detection processing is performed on selected elements (called cells) of the input data. A detection is declared when a cell value in the input data exceeds a threshold. To maintain a constant false alarmrate, the threshold is set to a multiple of the local noise power of the input data. The detector estimates local noise power for a cell-under-test (CUT) from surrounding cells using one of three cell averaging methods, or an order statistics method. The cell-averaging methods are cell averaging (CA), greatest-of cell averaging (GOCA), or smallest-of cell averaging (SOCA).

For more information about CFAR detectors, see [1].
For each test cell, the detector:
1 estimates the noise statistic from the cell values in the training band surrounding the CUT cell.
2 computes the threshold by multiplying the noise estimate by the threshold factor.
3 compares the CUT cell value to the threshold to determine whether a target is present or absent. If the value is greater than the threshold, a target is present.

To run the detector
1 Define and set up your CFAR detector. See "Construction" on page 1-109.
2 Call step to perform CFAR detection according to the properties of phased. CFARDetector. The behavior of step is specific to each object in the toolbox.

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.

## Construction

H = phased.CFARDetector creates a CFAR detector System object, H. The object performs CFAR detection on input data.

H = phased.CFARDetector(Name, Value) creates the object, H , with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN).

## Properties

## Method

CFAR algorithm

Specify the CFAR detector algorithm as one of

| 'CA' | Cell-averaging CFAR |
| :--- | :--- |
| ' GOCA ' | Greatest-of cell-averaging CFAR |
| 'OS ' | Order statistic CFAR |
| 'SOCA ' | Smallest-of cell-averaging CFAR |

## Default: ' CA '

## Rank

## Rank of order statistic

Specify the rank of the order statistic as a positive integer scalar. The value must be less than or equal to the value of the NumTrainingCells property. This property applies only when you set the Method property to ' $0 S^{\prime}$. This property supports single and double precision,

## Default: 1

## NumGuardCells

Number of guard cells
Specify the number of guard cells used in training as an even integer. This property specifies the total number of cells on both sides of the cell under test. This property supports single and double precision,

Default: 2, indicating that there is one guard cell at both the front and back of the cell under test

## NumTrainingCells

Number of training cells
Specify the number of training cells used in training as an even integer. Whenever possible, the training cells are equally divided before and after the cell under test. This property supports single and double precision.

Default: 2, indicating that there is one training cell at both the front and back of the cell under test

## ThresholdFactor

Methods of obtaining threshold factor
Specify whether the threshold factor comes from an automatic calculation, the CustomThresholdFactor property of this object, or an input argument in step. Values of this property are:

| 'Auto ' | The application calculates the threshold factor automatically <br> based on the desired probability of false alarm specified in <br> the ProbabilityFalseAlarm property. The calculation <br> assumes each independent signal in the input is a single pulse <br> coming out of a square law detector with no pulse integration. <br> The calculation also assumes the noise is white Gaussian. |
| :--- | :--- |


| 'Custom' | The CustomThresholdFactor property of this object <br> specifies the threshold factor. |
| :--- | :--- |
| 'Input port' | An input argument in each invocation of step specifies the <br> threshold factor. |

## Default: 'Auto'

## ProbabilityFalseAlarm

Desired probability of false alarm
Specify the desired probability of false alarm as a scalar between 0 and 1 (not inclusive). This property applies only when you set the ThresholdFactor property to 'Auto'.

Default: 0.1

## CustomThresholdFactor

Custom threshold factor
Specify the custom threshold factor as a positive scalar. This property applies only when you set the ThresholdFactor property to 'Custom'. This property is tunable. This property supports single and double precision,

## Default: 1

## OutputFormat

## Format of detection results

Format of detection results returned by the step method, specified as 'CUT result ' or 'Detection index'.

- When set to 'CUT result', the results are logical detection values (1 or 0 ) for each tested cell. 1 indicates that the value of the tested cell exceeds a detection threshold.
- When set to 'Detection index', the results form a vector or matrix containing the indices of tested cells which exceed a detection threshold. You can use this format as input to the phased.RangeEstimator and phased. DopplerEstimator System objects.

Default: 'CUT result'

## ThresholdOutputPort

## Output detection threshold

To obtain the detection threshold, set this property to true and use the corresponding output argument when invoking step. If you do not want to obtain the detection threshold, set this property to false.

Default: false
NoisePowerOutputPort
Output estimated noise

To obtain the estimated noise, set this property to true and use the corresponding output argument when invoking step. If you do not want to obtain the estimated noise, set this property to false.

Default: false
NumDetectionsSource
Source of the number of detections
Source of the number of detections, specified as 'Auto ' or 'Property'. When you set this property to 'Auto', the number of detection indices reported is the total number of cells under test that have detections. If you set this property to 'Property', the number of reported detections is determined by the value of the NumDetections property.

## Dependencies

To enable this property, set the OutputFormat property to 'Detection index'.
Default: 'Auto'
NumDetections
Maximum number of detections to report
Maximum number of detection indices to report, specified as a positive integer.

## Dependencies

To enable this property, set the OutputFormat property to 'Detection index' and the NumDetectionsSource property to 'Property'.

Default: 1

## Methods

step Perform CFAR detection

## Common to All System Objects

release Allow System object property value changes

## Examples

## Compute PFA Using CFAR Detector on Noise

Perform cell-averaging CFAR detection on a given Gaussian noise vector with a desired probability of false alarm (pfa) of 0.1. Assume that the data comes from a square law detector and no pulse integration is performed. Use 50 cells to estimate the noise level and 1 cell to separate the test cell and training cells. Perform the detection on all cells of the input.

```
detector = phased.CFARDetector('NumTrainingCells',50,...
    'NumGuardCells',2,'ProbabilityFalseAlarm',0.1);
N = 1000;
x = 1/sqrt(2)*(randn(N,1) + li*randn(N,1));
```

```
dets = detector(abs(x).^2,1:N);
pfa = sum(dets)/N
pfa = 0.1140
```


## Compute CFAR Detection Indices

Perform cell-averaging CFAR detection on a given Gaussian noise vector with a desired probability of false alarm (pfa) of 0.005 . Assume that the data comes from a square law detector and no pulse integration is performed. Perform the detection on all cells of the input. Use 50 cells to estimate the noise level and 1 cell to separate the test cell and training cells. Display the detection indices.

```
rng default;
detector = phased.CFARDetector('NumTrainingCells',50,'NumGuardCells',2, ...
    'ProbabilityFalseAlarm',0.005,'OutputFormat','Detection index');
N = 1000;
x1 = 1/sqrt(2)*(randn(N,1) + li*randn(N,1));
x2 = 1/sqrt(2)*(randn(N,1) + li*randn(N,1));
x = [x1,x2];
cutidx = 1:N;
dets = detector(abs(x).^2,cutidx)
dets = 2×11
\begin{tabular}{rrrrrrrrrrr}
339 & 537 & 538 & 734 & 786 & 827 & 979 & 136 & 418 & 539 & 874 \\
1 & 1 & 1 & 1 & 1 & 1 & 1 & 2 & 2 & 2 & 2
\end{tabular}
```


## Algorithms

CFAR Detection
phased. CFARDetector uses cell averaging in three steps:
1 Identify the training cells from the input, and form the noise estimate. The next table indicates how the detector forms the noise estimate, depending on the Method property value.

| Method | Noise Estimate |
| :--- | :--- |
| 'CA' | Use the average of the values in all the training cells. |
| 'GOCA' | Select the greater of the averages in the front training cells and <br> rear training cells. |
| 'OS' | Sort the values in the training cells in ascending order. Select the <br> $N$ Nth item, where $N$ is the value of the Rank property. |
| 'SOCA' | Select the smaller of the averages in the front training cells and <br> rear training cells. |

2 Multiply the noise estimate by the threshold factor to form the threshold.
3 Compare the value in the test cell against the threshold to determine whether the target is present or absent. If the value is greater than the threshold, the target is present.

## Data Precision

This System object supports single and double precision for input data, properties, and arguments. If the input data X is single precision, the output data is single precision. If the input data X is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

## Version History

## Introduced in R2011a

## References

[1] Richards, M. A. Fundamentals of Radar Signal Processing. New York: McGraw-Hill, 2005.

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
See "System Objects in MATLAB Code Generation" (MATLAB Coder).
This System object supports single and double precision for input data, properties, and arguments. If the input data $X$ is single precision, the output data is single precision. If the input data $X$ is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

See Also<br>npwgnthresh | phased.MatchedFilter | phased.TimeVaryingGain

## step

System object: phased. CFARDetector
Package: phased
Perform CFAR detection

## Syntax

```
Y = step(H,X,cutidx)
[Y,th] = step(
```

$\qquad$

```
[Y, noise] \(=\operatorname{step}(\quad\) )
\(Y=\operatorname{step}(H, X\), cutidx,thfac)
[ \(\mathrm{Y}, \mathrm{TH}, \mathrm{N}]=\operatorname{step}(\mathrm{H}, \mathrm{X}\), cutidx,thfac)
```


## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step $(o b j, x)$ and $y=o b j(x)$ perform equivalent operations.
$\mathrm{Y}=\operatorname{step}(\mathrm{H}, \mathrm{X}$, cutidx) performs CFAR detection on specified elements of the input data, $\mathrm{X} . \mathrm{X}$ can either be a real-valued $M$-by- 1 column vector or a real-valued $M$-by- $N$ matrix. cutidx is a length- $D$ vector of indices specifying the input elements or cells under test (CUT) on which to perform detection processing. When $X$ is a vector, cutidx specifies the element. When $X$ is a matrix, cutidx specifies the row of the element. The same index applies to all columns of the matrix. Detection is performed independently along each column of $X$ for the indices specified in cutidx. You can specify the input arguments as single or double precision.

The output argument $Y$ contains detection results. The format of $Y$ depends on the OutputFormat property.

- When OutputFormat is 'Cut result', Y is a $D$-by- 1 vector or a $D$-by- $N$ matrix containing logical detection results. $D$ is the length of cutidx and $N$ is the number of columns of $X$. The rows of $Y$ correspond to the rows in cutidx. For each row, $Y$ contains 1 in a column if there is a detection in the corresponding column of $X$. Otherwise, $Y$ contains a 0.
- When OutputFormat is 'Detection index', Y is a 1 -by- $L$ vector or a 2-by-L matrix containing detections indices. $L$ is the number of detections found in the input data. When $X$ is a column vector, Y contains the index for each detection in X . When X is a matrix, Y contains the row and column indices of each detection in $X$. Each column of $Y$ has the form [detrow; detcol]. When the NumDetectionsSource property is set to 'Property', L equals the value of the NumDetections property. If the number of actual detections is less than this value, columns without detections are set to NaN .

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
$[\mathrm{Y}, \mathrm{th}]=\operatorname{step}(\ldots \quad$ ) also returns the detection threshold, th, applied to detected cells under test.

- When OutputFormat is 'CUT result', th also returns the detection threshold th.
- When OutputFormat is 'Detection index', th returns a detection threshold for each corresponding detection in Y. When the NumDetectionsSource property is set to 'Property', $L$ equals the value of the NumDetections property. If the number of actual detections is less than this value, columns without detections are set to NaN.

To enable this syntax, set the ThresholdOutputPort property to true.
[ Y , noise] $=\operatorname{step}(\ldots \quad$ ) also returns the estimated noise power, noise, for each detected cell under test in X .

- When OutputFormat is 'CUT result', noise returns a noise power estimate.
- When OutputFormat is 'Detection index', noise returns a noise power estimate for each corresponding detection in Y. When the NumDetectionsSource property is set to 'Property', $L$ equals the value of the NumDetections property. If the number of actual detections is less than this value, columns without detections are set to NaN .

To enable this syntax, set the NoisePowerOutputPort property to true.
$Y=\operatorname{step}(H, X$, cutidx, thfac), in addition, specifies thfac as the threshold factor used to calculate the detection threshold. thfac must be a positive scalar. To enable this syntax, set the ThresholdFactor property to 'Input port'.

You can combine optional input and output arguments when their enabling properties are set. Optional inputs and outputs must be listed in the same order as the order of the enabling properties. For example, $[\mathrm{Y}, \mathrm{TH}, \mathrm{N}]=\operatorname{step}(\mathrm{H}, \mathrm{X}$, cutidx,thfac).

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Examples

## Compute PFA Using CFAR Detector on Noise

Perform cell-averaging CFAR detection on a given Gaussian noise vector with a desired probability of false alarm (pfa) of 0.1. Assume that the data comes from a square law detector and no pulse integration is performed. Use 50 cells to estimate the noise level and 1 cell to separate the test cell and training cells. Perform the detection on all cells of the input.

```
detector = phased.CFARDetector('NumTrainingCells',50,...
    'NumGuardCells',2,'ProbabilityFalseAlarm',0.1);
N = 1000;
x = 1/sqrt(2)*(randn(N,1) + li*randn(N,1));
dets = detector(abs(x).^2,1:N);
pfa = sum(dets)/N
pfa = 0.1140
```


## Compute CFAR Detection Indices

Perform cell-averaging CFAR detection on a given Gaussian noise vector with a desired probability of false alarm (pfa) of 0.005 . Assume that the data comes from a square law detector and no pulse integration is performed. Perform the detection on all cells of the input. Use 50 cells to estimate the noise level and 1 cell to separate the test cell and training cells. Display the detection indices.

```
rng default;
detector = phased.CFARDetector('NumTrainingCells',50,'NumGuardCells',2, ...
    'ProbabilityFalseAlarm',0.005,'OutputFormat','Detection index');
N = 1000;
x1 = 1/sqrt(2)*(randn(N,1) + li*randn(N,1));
x2 = 1/sqrt(2)*(randn(N,1) + 1i*randn(N,1));
x = [x1,x2];
cutidx = 1:N;
dets = detector(abs(x).^2,cutidx)
dets = 2×11
\begin{tabular}{rrrrrrrrrrr}
339 & 537 & 538 & 734 & 786 & 827 & 979 & 136 & 418 & 539 & 874 \\
1 & 1 & 1 & 1 & 1 & 1 & 1 & 2 & 2 & 2 & 2
\end{tabular}
```


## Algorithms

phased.CFARDetector uses cell averaging in three steps:
1 Identify the training cells from the input, and form the noise estimate. The next table indicates how the detector forms the noise estimate, depending on the Method property value.

| Method | Noise Estimate |
| :--- | :--- |
| 'CA' | Use the average of the values in all the training cells. |
| ' GOCA' | Select the greater of the averages in the front training cells and <br> rear training cells. |
| ' OS' | Sort the values in the training cells in ascending order. Select the <br> Nth item, where $N$ is the value of the Rank property. |
| ' SOCA' | Select the smaller of the averages in the front training cells and <br> rear training cells. |

2 Multiply the noise estimate by the threshold factor to form the threshold.
3 Compare the value in the test cell against the threshold to determine whether the target is present or absent. If the value is greater than the threshold, the target is present.

For details, see [1].

## References

[1] Richards, M. A. Fundamentals of Radar Signal Processing. New York: McGraw-Hill, 2005.

# phased.CFARDetector2D 

Package: phased

Two-dimensional CFAR detector

## Description

phased.CFARDetector2D System object implements a constant false-alarm rate detector (CFAR) for selected elements (called cells) of two-dimensional image data. A detection is declared when an image cell value exceeds a threshold. To maintain a constant false alarm-rate, the threshold is set to a multiple of the image noise power. The detector estimates noise power for a cell-under-test (CUT) from surrounding cells using one of three cell averaging methods, or an order statistics method. The cell-averaging methods are cell averaging (CA), greatest-of cell averaging (GOCA), or smallest-of cell averaging (SOCA).

For each test cell, the detector:
1 estimates the noise statistic from the cell values in the training band surrounding the CUT cell.
2 computes the threshold by multiplying the noise estimate by the threshold factor.
3 compares the CUT cell value to the threshold to determine whether a target is present or absent. If the value is greater than the threshold, a target is present.

To run the detector
1 Define and set up your 2-D CFAR detector. You can set the phased. CFARDetector2D System object properties when you create the object, or leave them set to their default values. See "Construction" on page 1-118. Some properties that you set at construction time can be changed later. These properties are tunable.
2 Find the detections by calling the step method. The output of this method depends on the properties of the phased. CFARDetector2D System object.

Note Alternatively, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.

## Construction

detector $=$ phased.CFARDetector2D creates a 2-D CFAR detector System object, detector.
detector $=$ phased.CFARDetector2D(Name,Value) creates a 2-D CFAR System object, detector, with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN).

## Properties

## Method - Two-dimensional CFAR averaging method

'CA' (default)|'GOCA'|'SOCA'|'OS'

Two-dimensional CFAR averaging method, specified as 'CA', 'GOCA', 'SOCA', or 'OS'. For 'CA', 'GOCA', 'SOCA' , the noise power is the sample mean derived from the training band. For ' 0 ' ' , the noise power is the $k$ th cell value obtained from numerically ordering all training cell values. Set $k$ using the Rank property.

| Averaging Method | Description |
| :--- | :--- |
| CA - Cell-averaging algorithm | Computes the sample mean of all training cells <br> surrounding the CUT cell. |
| GOCA - Greatest-of cell-averaging algorithm | Splits the 2-D training window surrounding the <br> CUT cell into left and right halves. Then, the <br> algorithm computes the sample mean for each <br> half and selects the largest mean. |
| SOCA - Smallest-of cell-averaging algorithm | Splits the 2-D training window surrounding the <br> CUT cell into left and right halves. Then, the <br> algorithm computes the sample mean for each <br> half and selects the smallest mean. |
| OS - Order statistic algorithm | Sorts training cells in ascending order of numeric <br> values. Then the algorithm selects the $k$ th value <br> from the list. $k$ is the rank specified by the Rank <br> parameter. |

## Example: 'OS'

Data Types: char

## GuardBandSize - Widths of guard band

[1 1] (default) | nonnegative integer | 2-element vector of nonnegative integers
The number of rows and columns of the guard band cells on each side of the CUT cell, specified as nonnegative integers. The first element specifies the guard band size along the row dimension. The second element specifies the guard band size along the column dimension. Specifying this property as a single integer is equivalent to specifying a guard band with the same value for both dimensions. For example, a value of [1 1], indicates that there is a one guard-cell-wide region surrounding each CUT cell. A value of zero indicates there are no guard cells.

## Example: [2 3]

Data Types: single | double

## TrainingBandSize - Widths of training band

## [1 1] (default) | positive integer | 2 -element vector of positive integers

The number of rows and columns of the training band cells on each side of the CUT cell, specified as a positive integer or a 1-by-2 matrix of positive integers. The first element specifies the training band size along the row dimension. The second element specifies the training band size along the column dimension. Specifying this property as a scalar is equivalent to specifying a training band with the same value for both dimensions. For example, a value of [11] indicates a 1 training-cell-wide region surrounding the CUT cell.
Example: [-30:0.1:30]
Data Types: single | double

## Rank - Rank of order statistic

1 (default) | positive integer

Rank of the order statistic used in the 2-D CFAR algorithm, specified as a positive integer. The value of this property must lie between 1 and $N_{\text {train }}$, where $N_{\text {train }}$ is the number of training cells. A value of 1 selects the smallest value in the training region.

## Example: 5

## Dependencies

To enable this property, set the Method property to ' 0 ' '.

## Data Types: single | double

## ThresholdFactor - Threshold factor method <br> 'Auto' (default)|'Input port'|'Custom'

Threshold factor method, specified as 'Auto','Input port', or 'Custom'.
When you set the ThresholdFactor property to 'Auto', the threshold factor is calculated from the desired probability of false alarm set in the ProbabilityFalseAlarm property. The calculation assumes that each independent signal in the input is a single pulse coming out of a square law detector with no pulse integration. In addition, the noise is assumed to be white Gaussian.

When you set the ThresholdFactor property to 'Input port', the threshold factor is obtained from an input argument of the step method.

When you set the ThresholdFactor property to 'Custom', the threshold factor is obtained from the value of the CustomThresholdFactor property.
Example: 'Custom'
Data Types: char

## ProbabilityFalseAlarm - Required probability of false alarm

0.1 (default) | positive scalar between 0 and 1

Required probability of false alarm, specified as a real positive scalar between 0 and 1 . The algorithm calculates the threshold factor from the required probability of false alarm.

Example: 0.001

## Dependencies

To enable this property, set the ThresholdFactor property to 'Auto '.
Data Types: single | double

## CustomThresholdFactor - Custom threshold factor

1 (default) | positive scalar
Custom threshold factor, specified as a real positive scalar. This property is tunable.

## Dependencies

To enable this property, set the ThresholdFactor property to 'Custom'.

## Data Types: single | double

OutputFormat - Format of detection results
'CUT result' (default)|'Detection index'

Format of detection results returned by the step method, specified as 'CUT result ' or 'Detection index'.

- When set to 'CUT result', the results are logical detection values (1 or 0 ) for each tested cell.
- When set to 'Detection index', the results form a vector or matrix containing the indices of tested cells that exceed a detection threshold. You can use this format as input to the phased.RangeEstimator and phased.DopplerEstimator System objects.

Data Types: char

## ThresholdOutputPort - Enable detection threshold output

false (default) | true
Option to enable detection threshold output, specified as false or true. Setting this property to true returns the detection threshold via an output argument, th, of the step method.

## Data Types: logical

## NoisePowerOutputPort - Enable noise power output <br> false (default)|true

Option to enable output of noise power, specified as false or true. Setting this property to true returns the noise power via the output argument, noise, of the step method.
Data Types: logical

## NumDetectionsSource - Source of the number of detections

'Auto' (default)|'Property'
Source of the number of detections, specified as 'Auto' or 'Property'. When you set this property to 'Auto ', the number of detection indices reported is the total number of cells under test that have detections. If you set this property to 'Property ', the number of reported detections is determined by the value of the NumDetections property.

## Dependencies

To enable this property, set the OutputFormat property to 'Detection index'.
Data Types: char
NumDetections - Maximum number of detection indices to report
1 (default) | positive integer
Maximum number of detection indices to report, specified as a positive integer.

## Dependencies

To enable this property, set the OutputFormat property to 'Detection index' and the NumDetectionsSource property to 'Property'.
Data Types: double

## Methods

| reset | Reset states of System object |
| :--- | :--- |
| step | Two-dimensional CFAR detection |

## Common to All System Objects

release Allow System object property value changes

## Examples

## Set 2-D CFAR Threshold for Noise-Only Data

This example shows how to set a 2-D CFAR threshold based upon a required probability of false alarm (pfa).

Perform cell-averaging CFAR detection on a 41-by-41 matrix of cells containing Gaussian noise. Estimate the empirical pfa and compare it to the required pfa. To get a good estimate, perform this simulation on 1000 similar matrices. First, set a threshold using the required pfa. In this case, there are no targets and the pfa can be estimated from the number of cells that exceed the threshold. Assume that the data is processed through a square-law detector and that no pulse integration is performed. Use a training-cell band of 3 cells in width and 4 cells in height. Use a guard band of 3 cells in width and 2 cells in height to separate the cells under test (CUT) from the training cells. Specify a required pfa of $5.0 \mathrm{e}-4$.

```
p = 5e-4;
rs = RandStream.create('mt19937ar','Seed',5);
N = 41;
ntrials = 1000;
detector = phased.CFARDetector2D('TrainingBandSize',[4,3], ...
    'ThresholdFactor','Auto','GuardBandSize',[2,3], ...
    'ProbabilityFalseAlarm',p,'Method','SOCA','ThresholdOutputPort',true);
```

Create a 41-by-41 image containing random complex data. Then, square the data to simulate a square-law detector.

```
x = 2/sqrt(2)*(randn(rs,N,N,ntrials) + li*randn(rs,N,N,ntrials));
x2 = abs(x).^2;
```

Process all the cells in each image. To do this, find the row and column of each CUT cell whose training region falls entirely within each image.

```
Ngc = detector.GuardBandSize(2);
Ngr = detector.GuardBandSize(1);
Ntc = detector.TrainingBandSize(2);
Ntr = detector.TrainingBandSize(1);
cutidx = [];
colstart = Ntc + Ngc + 1;
colend = N - ( Ntc + Ngc);
rowstart = Ntr + Ngr + 1;
rowend = N - ( Ntr + Ngr);
for m = colstart:colend
    for n = rowstart:rowend
        cutidx = [cutidx,[n;m]];
```

```
    end
end
ncutcells = size(cutidx,2);
```

Display the CUT cells.

```
cutimage = zeros(N,N);
```

for k = 1:ncutcells
cutimage(cutidx(1,k), cutidx $(2, k))=1$;
end
imagesc(cutimage)
axis equal


Perform the detection on all CUT cells. Return the detection classification and the threshold used to classify the cell.
[dets,th] = detector(x2,cutidx);
Find and display an image with a false alarm for illustration.

```
di = [];
for k = 1:ntrials
    d = dets(:,k);
    if (any(d) > 0)
        di = [di,k];
    end
end
idx = di(1);
```

```
detimg = zeros(N,N);
for k = 1:ncutcells
    detimg(cutidx(1,k),cutidx(2,k)) = dets(k,idx);
end
imagesc(detimg)
axis equal
```



Compute the empirical pfa.
pfa $=$ sum(dets(:))/ntrials/ncutcells
$p f a=4.5898 e-04$
The empirical and specified pfa agree.
Display the average empirical threshold value over all images.
mean(th(:))
ans $=31.7139$
Compute the theoretical threshold factor for the required pfa.

```
threshfactor = npwgnthresh(p,1,'noncoherent');
```

threshfactor = 10^(threshfactor/10);
disp(threshfactor)
7.6009

The theoretical threshold factor multiplied by the noise variance should agree with the measured threshold.

```
noisevar = mean(x2(:));
disp(threshfactor*noisevar);
```

30.4118

The theoretical threshold and empirical threshold agree to within an acceptable difference.

## Detect Targets in Background Noise

Perform cell-averaging CFAR detection on a 41-by-41 matrix of cells containing five closely-spaced targets in Gaussian noise. Perform this detection on a simulation of 1000 images. Use two detectors with different guard band regions. Set the thresholds manually using the Custom threshold factor. Assume that the data is processed through a square law-detector and that no pulse integration is performed. Use a training cell band of 2 cells in width and 2 cells in height. For the first detector, use a guard band of 1 cell all around to separate the CUT cells from the training cells. For the second detector, use a guard band of 8 cells all around.

```
p = 5e-4;
rs = RandStream.create('mt19937ar','Seed',5);
N = 41;
ntrials = 1000;
```

Create 1000 41-by-41 images of complex random noise with standard deviation of 1 .
$\mathrm{s}=1$;
$\mathrm{X}=\mathrm{s} / \mathrm{sqrt}(2)^{*}\left(\operatorname{randn}(\mathrm{rs}, \mathrm{N}, \mathrm{N}, \mathrm{ntrials})+\mathrm{li}^{*} \operatorname{randn}(\mathrm{rs}, \mathrm{N}, \mathrm{N}, \mathrm{ntrials})\right)$;
Set the target cells values to 1.5. Then, square the cell values.

```
A = 1.5;
x(23,20,:) = A;
x(23,18,:) = A;
x(23,23,:) = A;
x(20,22,:) = A;
x(21,18,:) = A;
x2 = abs(x).^2;
```

Display the target cells.

```
xtgt = zeros(N,N);
xtgt(23,20,:) = A;
xtgt(23,18,:) = A;
xtgt(23,23,:) = A;
xtgt(20,22,:) = A;
xtgt(21,18,:) = A;
imagesc(xtgt)
axis equal
axis tight
```



Set the CUT cells to be the target cells.

```
cutidx(1,1) = 23;
cutidx(2,1) = 20;
cutidx(1,2) = 23;
cutidx(2,2) = 18;
cutidx(1,3) = 23;
cutidx(2,3) = 23;
cutidx(1,4) = 20;
cutidx(2,4) = 22;
cutidx(1,5) = 21;
cutidx(2,5) = 18;
```

Perform the detection on all CUT cells using two CFAR 2-D detectors. The first detector has a small guard band region. The training region can include neighboring targets which can affect the computation of the noise power. The second detector has a larger guard band region, which precludes target cells from being used in the noise computation.

Create the two CFAR detectors.

```
detector1 = phased.CFARDetector2D('TrainingBandSize',[2,2], ...
    'GuardBandSize',[1,1],'ThresholdFactor','Custom','Method','CA', ...
    'CustomThresholdFactor',2,'ThresholdOutputPort',true);
detector2 = phased.CFARDetector2D('TrainingBandSize',[2,2], ..
    'GuardBandSize',[8,8],'ThresholdFactor','Custom','Method','CA', ...
    'CustomThresholdFactor',2,'ThresholdOutputPort',true);
```

Return the detection classifications and the thresholds used to classify the cells. Then, compute the probabilities of detection.

```
[dets1,th1] = detector1(x2,cutidx);
ndets = numel(detsl(:));
pd1 = sum(dets1(:))/ndets
pd1 = 0.6416
[dets2,th2] = detector2(x2,cutidx);
pd2 = sum(dets2(:))/ndets
pd2 = 0.9396
```

The detector with the larger guard-band region has a higher pfa because the noise is more accurately estimated.

## More About

## Training Cells

CFAR 2-D requires an estimate of the noise power. Noise power is computed from cells that are assumed not to contain any target signal. These cells are the training cells. Training cells form a band around the cell-under-test (CUT) cell but may be separated from the CUT cell by a guard band. The detection threshold is computed by multiplying the noise power by the threshold factor.


For GOCA and SOCA averaging, the noise power is derived from the mean value of one of the left or right halves of the training cell region.

Because the number of columns in the training region is odd, the cells in the middle column are assigned equally to either the left or right half.

When using the order-statistic method, the rank cannot be larger than the number of cells in the training cell region, $N_{\text {train. }}$. You can compute $N_{\text {train }}$.

- $N_{T C}$ is the number of training band columns.
- $N_{T R}$ is the number of training band rows.
- $N_{G C}$ is the number of guard band columns.
- $N_{G R}$ is the number of guard band rows.

The total number of cells in the combined training region, guard region, and CUT cell is $N_{\text {total }}=\left(2 N_{T C}\right.$ $\left.+2 N_{G C}+1\right)\left(2 N_{T R}+2 N_{G R}+1\right)$.

The total number of cells in the combined guard region and CUT cell is $N_{\text {guard }}=\left(2 N_{G C}+1\right)\left(2 N_{G R}+1\right)$.
The number of training cells is $N_{\text {train }}=N_{\text {total }}-N_{\text {guard }}$.
By construction, the number of training cells is always even. Therefore, to implement a median filter, you can choose a rank of $N_{\text {train }} / 2$ or $N_{\text {train }} / 2+1$.

## Algorithms

## Data Precision

This System object supports single and double precision for input data, properties, and arguments. If the input data $X$ is single precision, the output data is single precision. If the input data $X$ is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

## Version History

Introduced in R2016b

## References

[1] Mott, H. Antennas for Radar and Communications. New York: John Wiley \& Sons, 1992.
[2] Richards, M. A. Fundamentals of Radar Signal Processing. New York: McGraw-Hill, 2005.
[3] Skolnik, M. Introduction to Radar Systems, 3rd Ed. New York: McGraw-Hill, 2001.

## Extended Capabilities

## $\mathbf{C} / \mathbf{C}++$ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® $\mathrm{Coder}^{\mathrm{TM}}$.
Usage notes and limitations:
See "System Objects in MATLAB Code Generation" (MATLAB Coder).
This System object supports single and double precision for input data, properties, and arguments. If the input data $X$ is single precision, the output data is single precision. If the input data $X$ is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

## See Also

## Functions

npwgnthresh | rocpfa
Objects
phased.CFARDetector
Blocks
2-D CFAR Detector | CFAR Detector

## Topics

"Modeling Target Radar Cross Section" (Radar Toolbox)
"Simulating Test Signals for a Radar Receiver"

## reset

System object: phased. CFARDetector2D
Package: phased
Reset states of System object

## Syntax

reset(detector)

## Description

reset (detector) resets the internal state of the phased.CFARDetector2Dobject, detector.

## Input Arguments

detector - Two-dimensional CFAR detector
phased.CFARDetector2D System object
Two-dimensional CFAR detector, specified as a phased. CFARDetector2D System object.

## Version History

Introduced in R2016b

## step

## System object: phased. CFARDetector2D

Package: phased
Two-dimensional CFAR detection

## Syntax

```
Y = step(detector,X,cutidx)
Y = step(detector, X,cutidx,K)
[Y,th] = step(__)
[Y,noise] = step(___)
```


## Description

Note Alternatively, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step $(\mathrm{obj}, \mathrm{x})$ and $\mathrm{y}=\mathrm{obj}(\mathrm{x})$ perform equivalent operations.
$Y=$ step (detector, $X$, cutidx) performs 2-D CFAR detection on input image data, $X$, for the image cells under test (CUT) specified by cutidx. $Y$ contains the detection results for the CUT cells.
$\mathrm{Y}=$ step (detector, X, cutidx, K ) also specifies a threshold factor, K , for setting the detection threshold. This syntax applies when the ThresholdFactor property of the detector is set to 'Input port'.
[ $\mathrm{Y}, \mathrm{th}]=\operatorname{step}(\ldots \quad$ ) also returns the detection threshold, th, applied to detected cells under test. To enable this syntax, set the ThresholdOutputPort property to true.
[Y,noise] = step( $\qquad$ ) also returns the estimated noise power, noise, applied to detected cells under test. To enable this syntax, set the NoisePowerOutputPort property to true.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## detector - Two-dimensional CFAR detector

phased. CFARDetector2D System object
Two-dimensional CFAR detector, specified as a phased. CFARDetector2D System object.

## X - Input image

real $M$-by- $N$ matrix | real $M$-by- $N$-by- $P$ array

Input image, specified as a real $M$-by- $N$ matrix or a real $M$-by- $N$-by- $P$ array. $M$ and $N$ represent the rows and columns of a matrix. Each page is an independent 2-D signal.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
Example: $[1,1 ; 2.5,1 ; 0.5,0.1]$
Data Types: single|double

## cutidx - Test cells

2-by-D matrix of positive integers
Test cells, specified as a 2-by- $D$ matrix of positive integers, where $D$ is the number of test cells. Each column of cutidx specifies the row and column indices of a CUT cell. The same indices apply to all pages in the input array. You must restrict the locations of CUT cells so that their training regions lie completely within the input images.

Example: $[10,15 ; 11,15 ; 12,15]$
Data Types: single|double

## K - Detection threshold factor <br> positive scalar

Threshold factor used to calculate the detection threshold, specified as a positive scalar.

## Dependencies

To enable this input argument, set the ThresholdFactor property of the detector object to 'Input port'

Data Types: single|double

## Output Arguments

## Y - Detection results

$L$-by- $P$ logical matrix
Detection results, whose format depends on the OutputFormat property

- When OutputFormat is 'Cut result', Y is a $D$-by- $P$ matrix containing logical detection results for cells under test. $D$ is the length of cutidx and $P$ is the number of pages of $X$. The rows of $Y$ correspond to the rows of cutidx. For each row, $Y$ contains 1 in a column if there is a detection in the corresponding cell in $X$. Otherwise, $Y$ contains a 0.
- When OutputFormat is 'Detection report', Y is a $K$-by- $L$ matrix containing detections indices. $K$ is the number of dimensions of $X . L$ is the number of detections found in the input data. When $X$ is a matrix, $Y$ contains the row and column indices of each detection in $X$ in the form [detrow; detcol]. When $X$ is an array, $Y$ contains the row, column, and page indices of each detection in $X$ in the form [detrow; detcol; detpage]. When the NumDetectionsSource property is set to 'Property', $L$ equals the value of the NumDetections property. If the number of actual detections is less than this value, columns without detections are set to NaN .

Data Types: single | double

## th - Computed detection threshold

real-valued matrix
Computed detection threshold for each detected cell, returned as a real-valued matrix. Th has the same dimensions as Y .

- When OutputFormat is 'CUT result', Th returns the detection threshold whenever an element of $Y$ is 1 and NaN whenever an element of Y is 0 .
- When OutputFormat is 'Detection index', th returns a detection threshold for each corresponding detection in Y. When the NumDetectionsSource property is set to 'Property', $L$ equals the value of the NumDetections property. If the number of actual detections is less than this value, columns without detections are set to NaN .

Dependencies
To enable this output argument, set the ThresholdOutputPort to true.

## Data Types: single | double

## noise - Estimated noise power

real-valued matrix
Estimated noise power for each detected cell, returned as a real-valued matrix. noise has the same dimensions as Y .

- When OutputFormat is 'CUT result', noise returns the noise power whenever an element of Y is 1 and NaN whenever an element of Y is 0 .
- When OutputFormat is 'Detection index', noise returns a noise power for each corresponding detection in Y. When the NumDetectionsSource property is set to 'Property ', $L$ equals the value of the NumDetections property. If the number of actual detections is less than this value, columns without detections are set to NaN .


## Dependencies

To enable this output argument, set the NoisePowerOutputPort to true.
Data Types: single | double

## Examples

## Set 2-D CFAR Threshold for Noise-Only Data

This example shows how to set a 2-D CFAR threshold based upon a required probability of false alarm (pfa).

Perform cell-averaging CFAR detection on a 41-by-41 matrix of cells containing Gaussian noise. Estimate the empirical pfa and compare it to the required pfa. To get a good estimate, perform this simulation on 1000 similar matrices. First, set a threshold using the required pfa. In this case, there are no targets and the pfa can be estimated from the number of cells that exceed the threshold. Assume that the data is processed through a square-law detector and that no pulse integration is performed. Use a training-cell band of 3 cells in width and 4 cells in height. Use a guard band of 3 cells in width and 2 cells in height to separate the cells under test (CUT) from the training cells. Specify a required pfa of $5.0 \mathrm{e}-4$.

```
p = 5e-4;
rs = RandStream.create('mt19937ar','Seed',5);
N = 41;
ntrials = 1000;
detector = phased.CFARDetector2D('TrainingBandSize',[4,3], ...
    'ThresholdFactor','Auto','GuardBandSize',[2,3], ...
    'ProbabilityFalseAlarm',p,'Method','SOCA','Threshold0utputPort',true);
```

Create a 41-by-41 image containing random complex data. Then, square the data to simulate a square-law detector.
$x=2 / s q r t(2) *(r a n d n(r s, N, N, n t r i a l s)+1 i * r a n d n(r s, N, N, n t r i a l s)) ;$
$x 2=\operatorname{abs}(x) . \wedge 2$;
Process all the cells in each image. To do this, find the row and column of each CUT cell whose training region falls entirely within each image.

```
Ngc = detector.GuardBandSize(2);
Ngr = detector.GuardBandSize(1);
Ntc = detector.TrainingBandSize(2);
Ntr = detector.TrainingBandSize(1);
cutidx = [];
colstart = Ntc + Ngc + 1;
colend = N - ( Ntc + Ngc);
rowstart = Ntr + Ngr + 1;
rowend = N - ( Ntr + Ngr);
for m = colstart:colend
    for n = rowstart:rowend
        cutidx = [cutidx,[n;m]];
    end
end
ncutcells = size(cutidx,2);
```

Display the CUT cells.

```
cutimage = zeros(N,N);
for k = 1:ncutcells
    cutimage(cutidx(1,k),cutidx(2,k)) = 1;
end
imagesc(cutimage)
axis equal
```



Perform the detection on all CUT cells. Return the detection classification and the threshold used to classify the cell.

```
[dets,th] = detector(x2,cutidx);
```

Find and display an image with a false alarm for illustration.

```
di = [];
for k = 1:ntrials
    d = dets(:,k);
    if (any(d) > 0)
        di = [di,k];
    end
end
idx = di(1);
detimg = zeros(N,N);
for k = 1:ncutcells
    detimg(cutidx(1,k),cutidx(2,k)) = dets(k,idx);
end
imagesc(detimg)
axis equal
```



Compute the empirical pfa.
pfa $=$ sum(dets(:))/ntrials/ncutcells
$\mathrm{pfa}=4.5898 \mathrm{e}-04$
The empirical and specified pfa agree.
Display the average empirical threshold value over all images.
mean(th(:))
ans $=31.7139$
Compute the theoretical threshold factor for the required pfa.
threshfactor = npwgnthresh(p,1,'noncoherent');
threshfactor = 10^(threshfactor/10);
disp(threshfactor)
7.6009

The theoretical threshold factor multiplied by the noise variance should agree with the measured threshold.

```
noisevar = mean(x2(:));
disp(threshfactor*noisevar);
```

30.4118

The theoretical threshold and empirical threshold agree to within an acceptable difference.

## Detect Targets in Background Noise

Perform cell-averaging CFAR detection on a 41-by-41 matrix of cells containing five closely-spaced targets in Gaussian noise. Perform this detection on a simulation of 1000 images. Use two detectors with different guard band regions. Set the thresholds manually using the Custom threshold factor. Assume that the data is processed through a square law-detector and that no pulse integration is performed. Use a training cell band of 2 cells in width and 2 cells in height. For the first detector, use a guard band of 1 cell all around to separate the CUT cells from the training cells. For the second detector, use a guard band of 8 cells all around.

```
p = 5e-4;
rs = RandStream.create('mt19937ar','Seed',5);
N = 41;
ntrials = 1000;
```

Create 1000 41-by-41 images of complex random noise with standard deviation of 1 .

```
s = 1;
x = s/sqrt(2)*(randn(rs,N,N,ntrials) + li*randn(rs,N,N,ntrials));
```

Set the target cells values to 1.5. Then, square the cell values.

```
A = 1.5;
x(23,20,:) = A;
x(23,18,:) = A;
x(23,23,:) = A;
x(20,22,:) = A;
x(21,18,:) = A;
x2 = abs(x).^2;
```

Display the target cells.

```
xtgt = zeros(N,N);
xtgt(23,20,:) = A;
xtgt(23,18,:) = A;
xtgt(23,23,:) = A;
xtgt(20,22,:) = A;
xtgt(21,18,:) = A;
imagesc(xtgt)
axis equal
axis tight
```



Set the CUT cells to be the target cells.

```
cutidx(1,1) = 23;
cutidx(2,1) = 20;
cutidx(1,2) = 23;
cutidx(2,2) = 18;
cutidx(1,3) = 23;
cutidx(2,3) = 23;
cutidx(1,4) = 20;
cutidx(2,4) = 22;
cutidx(1,5) = 21;
cutidx(2,5) = 18;
```

Perform the detection on all CUT cells using two CFAR 2-D detectors. The first detector has a small guard band region. The training region can include neighboring targets which can affect the computation of the noise power. The second detector has a larger guard band region, which precludes target cells from being used in the noise computation.

Create the two CFAR detectors.

```
detector1 = phased.CFARDetector2D('TrainingBandSize',[2,2], ...
    'GuardBandSize',[1,1],'ThresholdFactor','Custom','Method','CA', ...
    'CustomThresholdFactor',2,'Threshold0utputPort',true);
detector2 = phased.CFARDetector2D('TrainingBandSize',[2,2],
    'GuardBandSize',[8,8],'ThresholdFactor','Custom','Method','CA', ...
    'CustomThresholdFactor',2,'Threshold0utputPort',true);
```

Return the detection classifications and the thresholds used to classify the cells. Then, compute the probabilities of detection.

```
[dets1,th1] = detector1(x2,cutidx);
ndets = numel(dets1(:));
pd1 = sum(detsl(:))/ndets
pd1 = 0.6416
[dets2,th2] = detector2(x2,cutidx);
pd2 = sum(dets2(:))/ndets
pd2 = 0.9396
```

The detector with the larger guard-band region has a higher pfa because the noise is more accurately estimated.

## Version History

Introduced in R2016b

## See Also

phased.CFARDetector

# phased.Collector 

Package: phased
Narrowband signal collector

## Description

The phased.Collector System object implements a narrowband signal collector. A collector converts incident narrowband wave fields arriving from specified directions into signals to be further processed. Wave fields are incident on antenna and microphone elements, sensor arrays, or subarrays. The object collects signals in one of two ways controlled by the Wavefront property.

- If the Wavefront property is set to 'Plane', the collected signals at each element or subarray are formed from the coherent sum of all incident plane wave fields sampled at each array element or subarray.
- If the Wavefront property is set to 'Unspecified ', the collected signals are formed from an independent field incident on each individual sensor element.

You can use this object to

- model arriving signals as polarized or nonpolarized fields depending upon whether the element or array supports polarization and the value of the Polarization property. Using polarization, you can receive a signal as a polarized electromagnetic field, or receive two independent signals using dual (i.e. orthogonal) polarization directions.
- model incoming acoustic fields by using nonpolarized microphone and sonar transducer array elements and by setting the "Polarization" on page 1-0 to 'None'. You must also set the PropagationSpeed to a value appropriate for the medium.
- collect fields at subarrays created by the phased. ReplicatedSubarray and phased.PartitionedArray objects. You can steer all subarrays in the same direction using the steering angle argument, STEERANG, or steer each subarray in a different direction using the subarray element weights argument, WS. You cannot set the Wavefront property to 'Unspecified ' for subarrays.

To collect arriving signals at the elements or arrays:
1 Create the phased. Collector object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

```
collector = phased.Collector
collector = phased.Collector(Name,Value)
```


## Description

collector $=$ phased. Collector creates a narrowband signal collector object, collector, with default property values.
collector $=$ phased.Collector(Name,Value) creates a narrowband signal collector with each property Name set to a specified Value. You can specify additional name-value pair arguments in any order as (Namel,Value1,...,NameN,ValueN). Enclose each property name in single quotes.
Example: collector $=$
phased.collector('Sensor', phased.URA, 'OperatingFrequency', 300e6) sets the sensor array to a uniform rectangular array (URA) with default URA property values. The beamformer has an operating frequency of 300 MHz .

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## Sensor - Sensor element or sensor array

phased.ULA array with default property values (default) | Phased Array System Toolbox sensor or array

Sensor element or sensor array, specified as a System object belonging to Phased Array System Toolbox. A sensor array can contain subarrays.
Example: phased.URA

## PropagationSpeed - Signal propagation speed

physconst('LightSpeed') (default)| positive scalar
Signal propagation speed, specified as a positive scalar. Units are in meters per second. The default propagation speed is the value returned by physconst('LightSpeed'). See physconst for more information.

## Example: 3e8

Data Types: double

## OperatingFrequency - Operating frequency

300e6 (default) | positive scalar
Operating frequency, specified as a positive scalar. Units are in Hz .
Example: 1e9
Data Types: double

## Wavefront - Type of incoming wavefront <br> 'Plane' (default)|'Unspecified'

The type of incoming wavefront, specified as 'Plane' or 'Unspecified':

- 'Plane' - input signals are multiple plane waves impinging on the entire array. Each plane wave is received by all collecting elements.
- 'Unspecified ' - collected signals are independent fields incident on individual sensor elements. If the Sensor property is an array that contains subarrays, you cannot set the Wavefront property to 'Unspecified'.

Data Types: char

## SensorGainMeasure - Specify sensor gain

'dB' (default)|'dBi'
Sensor gain measure, specified as 'dB' or ' dBi '.

- When you set this property to ' dB ', the input signal power is scaled by the sensor power pattern (in dB ) at the corresponding direction and then combined.
- When you set this property to ' $\mathrm{dBi}^{\prime}$ ', the input signal power is scaled by the directivity pattern (in dBi ) at the corresponding direction and then combined. This option is useful when you want to compare results with the values predicted by the radar equation that uses dBi to specify the antenna gain. The computation using the ' $\mathrm{dBi}^{\prime}$ option is expensive as it requires an integration over all directions to compute the total radiated power of the sensor.


## Dependencies

To enable this property, set the Wavefront property to 'Plane'.
Data Types: char

## Polarization - Polarization configuration

'None' (default) | 'Combined ' | 'Dual'
Polarization configuration, specified as 'None', 'Combined', or 'Dual'. When you set this property to 'None', the incident fields are considered scalar fields. When you set this property to 'Combined ' , the incident fields are polarized and represent a single arriving signal whose polarization reflects the sensor's inherent polarization. When you set this property to 'Dual', the $H$ and $V$ polarization components of the fields are independent signals.

Example: 'Dual'
Data Types: char

## WeightsInputPort - Enable weights input

false (default)|true
Enable weights input, specified as false or true. When true, use the object input argument $W$ to specify weights. Weights are applied to individual array elements (or at the subarray level when subarrays are supported).
Data Types: logical

## Usage

## Syntax

```
Y = collector(X,ANG)
Y = collector(X,ANG,LAXES)
```

```
[YH,YV] = collector(X,ANG,LAXES)
[___] = collector(___,W
[___] = collector(___,STEERANG)
[____] = collector(___, WS)
```


## Description

$\mathrm{Y}=$ collector(X,ANG) collects the signals, X , arriving from the directions specified by ANG. Y contains the collected signals.
$\mathrm{Y}=$ collector (X,ANG,LAXES) also specifies LAXES as the local coordinate system axes directions. To use this syntax, set the Polarization property to 'Combined '.
[YH,YV] = collector (X, ANG, LAXES) returns an H-polarization component of the field, YH , and a V-polarization component, YV. To use this syntax, set the Polarization property to 'Dual'.
[___ ] = collector (__ W ) also specifies W as array element or subarray weights. To use this syntax, set the WeightsInputPort property to true.
[___] = collector (__ , STEERANG) also specifies STEERANG as the subarray steering angle. To use this syntax, set the Sensor property to an array that supports subarrays and set the SubarraySteering property of that array to either 'Phase' or 'Time'.
$\qquad$ ] = collector( $\qquad$ ,WS) also specifies WS as the weights applied to each element within each subarray. To use this syntax, set the Sensor property to an array that supports subarrays and set the SubarraySteering of that array to 'Custom'.

## Input Arguments

## X - Arriving signals

complex-valued $M$-by-L matrix | complex-valued 1-by-L cell array of structures
Arriving signals, specified as a complex-valued $M$-by- $L$ matrix or complex-valued 1-by- $L$ cell array of structures. $M$ is the number of signal samples and $L$ is the number of arrival angles. This argument represents the arriving fields.

- If the Polarization property value is set to 'None', X is an $M$-by- $L$ matrix.
- If the Polarization property value is set to 'Combined' or 'Dual', X is a 1 -by- L cell array of structures. Each cell corresponds to a separate arriving signal. Each struct contains three column vectors containing the $X, Y$, and $Z$ components of the polarized fields defined with respect to the global coordinate system.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

## Dependencies

To enable this argument, set the Polarization property to 'None' or 'Combined '.

```
Data Types: double
Complex Number Support: Yes
```


## ANG - Arrival directions of signals

real-valued 2-by-L matrix

Arrival directions of signals, specified as a real-valued 2-by-L matrix. Each column specifies an arrival direction in the form [AzimuthAngle;ElevationAngle]. The azimuth angle must lie between $180^{\circ}$ and $180^{\circ}$, inclusive. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive. When the Wavefront property is false, the number of angles must equal the number of array elements, $N$. Units are in degrees.
Example: [30,20;45,0]
Data Types: double

## LAXES - Local coordinate system

real-valued 3-by-3 orthogonal matrix
Local coordinate system, specified as a real-valued 3-by-3 orthogonal matrix. The matrix columns specify the local coordinate system's orthonormal $x, y$, and $z$ axes with respect to the global coordinate system.

## Example: rotx (30)

## Dependencies

To enable this argument, set the Polarization property to 'Combined ' or 'Dual'.
Data Types: double

## W - Element or subarray weights

$N$-by-1 column vector
Element or subarray weights, specified as a complex-valued $N$-by- 1 column vector where $N$ is the number of array elements (or subarrays when the array supports subarrays).

## Dependencies

To enable this argument, set the WeightsInputPort property to true.
Data Types: double
Complex Number Support: Yes

## WS - Subarray element weights

complex-valued $N_{\text {SE }}$-by- $N$ matrix | 1 -by- $N$ cell array
Subarray element weights, specified as complex-valued $N_{\text {SE }}$-by- $N$ matrix or 1-by- $N$ cell array where $N$ is the number of subarrays. These weights are applied to the individual elements within a subarray.

Subarray element weights

| Sensor Array | Subarray weights |
| :---: | :---: |
| phased. ReplicatedSubarray | All subarrays have the same dimensions and sizes. Then, the subarray weights form an $N_{\mathrm{SE}^{-}}$-by$N$ matrix. $N_{\text {SE }}$ is the number of elements in each subarray and $N$ is the number of subarrays. Each column of WS specifies the weights for the corresponding subarray. |
| phased.PartitionedArray | Subarrays may not have the same dimensions and sizes. In this case, you can specify subarray weights as <br> - an $N_{\mathrm{SE}}-$ by- $N$ matrix, where $N_{\mathrm{SE}}$ is now the number of elements in the largest subarray. The first $Q$ entries in each column are the element weights for the subarray where $Q$ is the number of elements in the subarray. <br> - a 1-by- $N$ cell array. Each cell contains a column vector of weights for the corresponding subarray. The column vectors have lengths equal to the number of elements in the corresponding subarray. |

## Dependencies

To enable this argument, set the Sensor property to an array that contains subarrays and set the SubarraySteering property of the array to 'Custom'.

Data Types: double
Complex Number Support: Yes

## STEERANG - Subarray steering angle

real-valued 2-by-1 vector
Subarray steering angle, specified as a length- 2 column vector. The vector has the form [azimuthAngle;elevationAngle]. The azimuth angle must be between $-180^{\circ}$ and $180^{\circ}$, inclusive. The elevation angle must be between $-90^{\circ}$ and $90^{\circ}$, inclusive. Units are in degrees.

## Example: [20;15]

## Dependencies

To enable this argument, set the Sensor property to an array that supports subarrays and set the SubarraySteering property of that array to either 'Phase' or 'Time'

## Data Types: double

## Output Arguments

## Y - Collected signal

complex-valued $M$-by- $N$ matrix
Collected signal, returned as a complex-valued $M$-by- $N$ matrix. $M$ is the length of the input signal. $N$ is the number of array elements (or subarrays when subarrays are supported). Each column
corresponds to the signal collected by the corresponding array element (or corresponding subarrays when subarrays are supported).

## Dependencies

To enable this argument, set the Polarization property to 'None' or 'Combined '.
Data Types: double

## YH - Collected horizontal polarization signal <br> complex-valued $M$-by- $N$ matrix

Collected horizontal polarization signal, returned as a complex-valued $M$-by- $N$ matrix. $M$ is the length of the input signal. $N$ is the number of array elements (or subarrays when subarrays are supported). Each column corresponds to the signal collected by the corresponding array element (or corresponding subarrays when subarrays are supported).

## Dependencies

To enable this argument, set the Polarization property to 'Dual '.

## Data Types: double

## YV - Collected vertical polarization signal

complex-valued $M$-by- $N$ matrix
Collected horizontal polarization signal, returned as a complex-valued $M$-by- $N$ matrix. $M$ is the length of the input signal. $N$ is the number of array elements (or subarrays when subarrays are supported). Each column corresponds to the signal collected by the corresponding array element (or corresponding subarrays when subarrays are supported).

## Dependencies

To enable this argument, set the Polarization property to 'Dual '.
Data Types: double

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:
release(obj)

## Common to All System Objects

step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object

## Examples

## Collect Wideband Signal at Single Antenna

Use the phased. Collector System object ${ }^{\text {TM }}$ to construct a signal arriving at a single isotropic antenna from $10^{\circ}$ azimuth and $30^{\circ}$ elevation.

```
antenna = phased.IsotropicAntennaElement;
collector = phased.Collector('Sensor',antenna);
x = [1;0;-1];
incidentAngle = [10;30];
y = collector(x,incidentAngle)
y = 3x1
    1
    0
    -1
```


## Collect Signal at Uniform Linear Array

Collect a far-field signal arriving at a 3-element uniform linear array (ULA) of isotropic antenna elements.

```
antenna = phased.ULA('NumElements',3);
collector = phased.Collector('Sensor',antenna,'OperatingFrequency',1e9);
x = [1;0;-1];
incidentAngle = [10 30]';
y = collector(x,incidentAngle)
y = 3x3 complex
    -0.0051 - 1.0000i 1.0000 + 0.0000i -0.0051 + 1.0000i
    0.0000 + 0.0000i 0.0000 + 0.0000i 0.0000 + 0.0000i
    0.0051 + 1.0000i -1.0000 + 0.0000i 0.0051 - 1.0000i
```


## Collect Different Signals at Array Elements

Collect different signals at a three-element array. Each input signal comes from a different direction.

```
array = phased.ULA('NumElements',3);
collector = phased.Collector('Sensor',array,'OperatingFrequency',1e9,...
    'Wavefront','Unspecified');
```

Each column is a signal for one element.

```
x = rand(10,3)
x = 10\times3
\begin{tabular}{lll}
0.8147 & 0.1576 & 0.6557 \\
0.9058 & 0.9706 & 0.0357 \\
0.1270 & 0.9572 & 0.8491
\end{tabular}
```

| 0.9134 | 0.4854 | 0.9340 |
| :--- | :--- | :--- |
| 0.6324 | 0.8003 | 0.6787 |
| 0.0975 | 0.1419 | 0.7577 |
| 0.2785 | 0.4218 | 0.7431 |
| 0.5469 | 0.9157 | 0.3922 |
| 0.9575 | 0.7922 | 0.6555 |
| 0.9649 | 0.9595 | 0.1712 |

Specify three incident angles.
incidentAngles = [10 0; 20 5; 45 2]';
$y=$ collector(x,incidentAngles)
$y=10 \times 3$

| 0.8147 | 0.1576 | 0.6557 |
| :--- | :--- | :--- |
| 0.9058 | 0.9706 | 0.0357 |
| 0.1270 | 0.9572 | 0.8491 |
| 0.9134 | 0.4854 | 0.9340 |
| 0.6324 | 0.8003 | 0.6787 |
| 0.0975 | 0.1419 | 0.7577 |
| 0.2785 | 0.4218 | 0.7431 |
| 0.5469 | 0.9157 | 0.3922 |
| 0.9575 | 0.7922 | 0.6555 |
| 0.9649 | 0.9595 | 0.1712 |

## Collect Plane Wave at ULA

Construct a 4 -element uniform linear array (ULA). The array operating frequency is 1 GHz . The array element spacing is one half the corresponding wavelength. Model the collection of a 200 Hz sinusoid from the far field incident on the array at $45^{\circ}$ azimuth and $10^{\circ}$ elevation.

Create the array.

```
fc = 1e9;
lambda = physconst('LightSpeed')/fc;
array = phased.ULA('NumElements',4,'ElementSpacing',lambda/2);
```

Create the sinusoid signal.

```
t = linspace(0,1,1e3);
x = cos(2*pi*200*t)';
```

Construct the collector object and obtain the received signal.

```
collector = phased.Collector('Sensor',array, ...
    'PropagationSpeed',physconst('LightSpeed'),'Wavefront','Plane', ...
    'OperatingFrequency',fc);
incidentangle = [45;10];
receivedsig = collector(x,incidentangle);
```


## Measure Target Scattering Matrix Using Dual Polarization

Use a dual-polarization system to obtain target scattering information. Simulate a transmitter and receiver where the vertical and horizontal components are transmitted successively using the input ports of the transmitter. The signals from the two polarization output ports of the receiver are then used to determine the target scattering matrix.

```
scmat = [0 1i; 1i 2];
radiator = phased.Radiator('Sensor', ...
    phased.CustomAntennaElement('SpecifyPolarizationPattern',true), ...
        'Polarization','Dual');
target = phased.RadarTarget('EnablePolarization',true,'ScatteringMatrix', ...
    scmat);
collector = phased.Collector('Sensor', ...
    phased.CustomAntennaElement('SpecifyPolarizationPattern',true), ...
    'Polarization','Dual');
xh = 1;
xv = 1;
```

Transmit a horizontal component and display the reflected Shh and Svh polarization components.

```
x = radiator(xh,0,[0;0],eye(3));
xrefl = target(x,[0;0],eye(3));
[Shh,Svh] = collector(xrefl,[0;0],eye(3))
Shh = 0
Svh = 0.0000 + 3.5474i
```

Transmit a vertical component and display the reflected Shv and Svv polarization components.

```
x = radiator(0,xv,[0;0],eye(3));
xrefl = target(x,[0;0],eye(3));
[Shv,Svv] = collector(xrefl,[0;0],eye(3))
Shv = 0.0000 + 3.5474i
Svv = 7.0947
```


## Algorithms

If the Wavefront property value is ' Pl ane' , phased. Collector collects each plane wave signal using the phase approximation of the time delays across collecting elements in the far field.

If the Wavefront property value is 'Unspecified', phased. Collector collects each channel independently.

For further details, see [1].

## Version History

Introduced in R2011a

## References

[1] Van Trees, H. Optimum Array Processing. New York: Wiley-Interscience, 2002.

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
See "System Objects in MATLAB Code Generation" (MATLAB Coder).

## See Also

phased.WidebandCollector|phased.Radiator|phased.WidebandRadiator

## step

System object: phased.Collector
Package: phased
Collect signals

## Syntax

Y = step( $\mathrm{H}, \mathrm{X}, \mathrm{ANG}$ )
Y = step(H,X,ANG,LAXES)
Y = step(H,X,ANG,WEIGHTS)
Y = step(H,X,ANG, STEERANGLE)
Y $=$ step ( $\mathrm{H}, \mathrm{X}$, ANG, LAXES, WEIGHTS, STEERANGLE)

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.
$Y=$ step ( $\mathrm{H}, \mathrm{X}, \mathrm{ANG}$ ) collects signals X arriving from directions ANG. The collection process depends on the Wavefront property of H , as follows:

- If Wavefront has the value 'Plane', each collecting element collects all the far field signals in X . Each column of $Y$ contains the output of the corresponding element in response to all the signals in $X$.
- If Wavefront has the value 'Unspecified ', each collecting element collects only one impinging signal from $X$. Each column of $Y$ contains the output of the corresponding element in response to the corresponding column of $X$. The 'Unspecified ' option is available when the Sensor property of H does not contain subarrays.

Y = step ( $\mathrm{H}, \mathrm{X}, \mathrm{ANG}, \mathrm{LAXES}$ ) uses LAXES as the local coordinate system axes directions. This syntax is available when you set the EnablePolarization property to true.

Y = step ( $\mathrm{H}, \mathrm{X}$, ANG, WEIGHTS) uses WEIGHTS as the weight vector. This syntax is available when you set the WeightsInputPort property to true.
$\mathrm{Y}=\operatorname{step}(\mathrm{H}, \mathrm{X}$, ANG, STEERANGLE) uses STEERANGLE as the subarray steering angle. This syntax is available when you configure H so that H . Sensor is an array that contains subarrays and H.Sensor.SubarraySteering is either 'Phase' or 'Time'.
$Y=\operatorname{step}(H, X, A N G, L A X E S, W E I G H T S, S T E E R A N G L E)$ combines all input arguments. This syntax is available when you configure H so that H . WeightsInputPort is true, H . Sensor is an array that contains subarrays, and H.Sensor. SubarraySteering is either 'Phase' or 'Time'.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of
the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## H

Collector object.

## X

Arriving signals. Each column of $X$ represents a separate signal. The specific interpretation of $X$ depends on the Wavefront property of H .

| Wavefront Property <br> Value | Description |
| :--- | :--- |
| 'Plane ' | Each column of $X$ is a far field signal. |
| 'Unspecified ' | Each column of $X$ is the signal impinging on the corresponding element. <br> In this case, the number of columns in $X$ must equal the number of <br> collecting elements in the Sensor property. |

- If the EnablePolarization property value is set to false, X is a matrix. The number of columns of the matrix equals the number of separate signals.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

- If the EnablePolarization property value is set to true, X is a row vector of MATLAB struct type. The dimension of the struct array equals the number of separate signals. Each struct member contains three column-vector fields, $\mathrm{X}, \mathrm{Y}$, and Z , representing the $x, y$, and $z$ components of the polarized wave vector signals in the global coordinate system.

The size of the first dimension of the matrix fields within the struct can vary to simulate a changing signal length such as a pulse waveform with variable pulse repetition frequency.

## ANG

Incident directions of signals, specified as a two-row matrix. Each column specifies the incident direction of the corresponding column of X. Each column of ANG has the form [azimuth; elevation], in degrees. The azimuth angle must be between -180 and 180 degrees, inclusive. The elevation angle must be between -90 and 90 degrees, inclusive.

## LAXES

Local coordinate system. LAXES is a 3-by-3 matrix whose columns specify the local coordinate system's orthonormal $x, y$, and $z$ axes, respectively. Each axis is specified in terms of $[x ; y ; z$ ] with respect to the global coordinate system. This argument is only used when the EnablePolarization property is set to true.

## WEIGHTS

Vector of weights. WEIGHTS is a column vector of length M , where M is the number of collecting elements.

Default: ones (M, 1)

## STEERANGLE

Subarray steering angle, specified as a length- 2 column vector. The vector has the form [azimuth; elevation], in degrees. The azimuth angle must be between -180 and 180 degrees, inclusive. The elevation angle must be between -90 and 90 degrees, inclusive.

## Output Arguments

## Y

Collected signals. Each column of Y contains the output of the corresponding element. The output is the response to all the signals in X , or one signal in X , depending on the Wavefront property of H .

## Examples

## Collect Plane Wave at ULA

Construct a 4 -element uniform linear array (ULA). The array operating frequency is 1 GHz . The array element spacing is one half the corresponding wavelength. Model the collection of a 200 Hz sinusoid from the far field incident on the array at $45^{\circ}$ azimuth and $10^{\circ}$ elevation.

Create the array.

```
fc = 1e9;
lambda = physconst('LightSpeed')/fc;
array = phased.ULA('NumElements',4,'ElementSpacing',lambda/2);
```

Create the sinusoid signal.

```
t = linspace(0,1,1e3);
x = cos(2*pi*200*t)';
```

Construct the collector object and obtain the received signal.

```
collector = phased.Collector('Sensor',array, ...
    'PropagationSpeed',physconst('LightSpeed'),'Wavefront','Plane', ...
    'OperatingFrequency',fc);
incidentangle = [45;10];
receivedsig = collector(x,incidentangle);
```


## Algorithms

If the Wavefront property value is ' Pl ane', phased. Collector collects each plane wave signal using the phase approximation of the time delays across collecting elements in the far field.

If the Wavefront property value is 'Unspecified', phased. Collector collects each channel independently.

For further details, see [1].

## References

[1] Van Trees, H. Optimum Array Processing. New York: Wiley-Interscience, 2002.

## See Also

uv2azel| phitheta2azel

# phased.ConformalArray 

Package: phased
Conformal array

## Description

The ConformalArray object constructs a conformal array. A conformal array can have elements in any position pointing in any direction.

To compute the response for each element in the array for specified directions:
1 Define and set up your conformal array. See "Construction" on page 1-156.
2 Call step to compute the response according to the properties of phased. ConformalArray. The behavior of step is specific to each object in the toolbox.

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.

## Construction

H = phased. ConformalArray creates a conformal array System object, H . The object models a conformal array formed with identical sensor elements.

H = phased.ConformalArray(Name, Value) creates object, H, with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN).

H = phased.ConformalArray(POS,NV,Name,Value) creates a conformal array object, H, with the ElementPosition property set to POS, the ElementNormal property set to NV, and other specified property Names set to the specified Values. POS and NV are value-only arguments. When specifying a value-only argument, specify all preceding value-only arguments. You can specify namevalue arguments in any order.

## Properties

## Element

Element of array
Sensor element array, specified as a Phased Array System Toolbox antenna, microphone, or transducer element or an Antenna Toolbox ${ }^{\mathrm{TM}}$ antenna System object

Default: isotropic antenna element System object with default properties

## ElementPosition

Element positions

ElementPosition specifies the positions of the elements in the conformal array. ElementPosition must be a 3 -by-N matrix, where N indicates the number of elements in the conformal array. Each column of ElementPosition represents the position, in the form [x; y; z] (in meters), of a single element in the local coordinate system of the array. The local coordinate system has its origin at an arbitrary point. The default value of this property represents a single element at the origin of the local coordinate system.

Default: [0; 0; 0]

## ElementNormal

Element normal directions
ElementNormal specifies the normal directions of the elements in the conformal array. Angle units are degrees. The value assigned to ElementNormal must be either a 2 -by- $N$ matrix or a 2 -by- 1 column vector. The variable $N$ indicates the number of elements in the array. If the value of ElementNormal is a matrix, each column specifies the normal direction of the corresponding element in the form [azimuth; elevation] with respect to the local coordinate system. The local coordinate system aligns the positive $x$-axis with the direction normal to the conformal array. If the value of ElementNormal is a 2-by-1 column vector, it specifies the same pointing direction for all elements in the array.

You can use the ElementPosition and ElementNormal properties to represent any arrangement in which pairs of elements differ by certain transformations. The transformations can combine translation, azimuth rotation, and elevation rotation. However, you cannot use transformations that require rotation about the normal.

Default: [0; 0]

## Taper

Element taper or weighting
Element tapering or weighting, specified as a complex-valued scalar, 1-by- $N$ row vector, or $N$-by-1 column vector. Weights are applied to each element in the sensor array. $N$ is the number of elements along in the array as determined by the size of the ElementPosition property. If the Taper parameter is a scalar, the same taper value is applied to all elements. If the value of Taper is a vector, each taper values is applied to the corresponding element.

## Default: 1

## Methods

| Specific to phased. ConformalArray Object |  |
| :--- | :--- |
| beamwidth | Compute and display beamwidth of an array |
| collectPla <br> neWave | Simulate received plane waves |
| directivit <br> y | Directivity of conformal array |
| getElement <br> Normal | Normal vector to array elements |


| Specific to phased. ConformalArray Object |  |
| :--- | :--- |
| getElement <br> Position | Positions of array elements |
| getNumElem <br> ents | Number of elements in array |
| getTaper | Array element tapers |
| isPolariza <br> tionCapabl <br> e | Polarization capability |
| pattern | Plot conformal array pattern |
| patternAzi <br> muth | Plot conformal array directivity or pattern versus azimuth |
| patternEle <br> vation | Plot conformal array directivity or pattern versus elevation |
| perturbati <br> ons | Perturbations defined on phased array |
| perturbedA <br> rray | Apply perturbations to phased array |
| perturbedP <br> attern | Compute and plot azimuth pattern of perturbed array |
| step | Output responses of array elements |
| viewArray | View array geometry |

## Common to All System Objects

| release | Allow System object property value changes |
| :--- | :--- | :--- |

## Examples

## Plot Power Pattern of 8-Element Uniform Circular Array

Using the ConformalArray System object ${ }^{\text {tw }}$, construct an 8 -element uniform circular array (UCA) of isotropic antenna elements. Plot a normalized azimuth power pattern at 0 degrees elevation. Assume the operating frequency is 1 GHz and the wave propagation speed is the speed of light.
$\mathrm{N}=8$;
azang $=(0: \mathrm{N}-1) * 360 / \mathrm{N}-180$;
sCA = phased.ConformalArray(...
'ElementPosition',[cosd(azang);sind(azang); zeros(1,N)],...
'ElementNormal',[azang;zeros(1,N)]);
$\mathrm{fc}=1 \mathrm{e}$;
c = physconst('LightSpeed');
pattern(sCA, fc, [-180:180],0,...
'PropagationSpeed ', c, 'Type' , 'powerdb ' , ...
'CoordinateSystem','polar')


Normalized Power (dB), Broadside at $0.00^{\circ}$

## Plot Pattern of 31-Element Uniform Circular Sonar Array

Construct a 31 -element acoustic uniform circular sonar array (UCA) using the ConformalArray System object ${ }^{\mathrm{TM}}$. Assume the array is one meter in diameter. Using the ElevationAngles parameter, restrict the display to $+/-40$ degrees in 0.1 degree increments. Assume the operating frequency is 4 kHz . A typical value for the speed of sound in seawater is $1500.0 \mathrm{~m} / \mathrm{s}$.

## Construct the array

$\mathrm{N}=31$;
theta $=(0: N-1) * 360 / \mathrm{N}-180$;
Radius = 0.5;
sMic = phased.OmnidirectionalMicrophoneElement(...
'FrequencyRange', [0, 10000], 'BackBaffled' , true) ;
sArray $=$ phased.ConformalArray('Element',sMic,...
'ElementPosition', Radius*[zeros(1,N); cosd(theta); sind(theta)],...
'ElementNormal', [ones(1,N);zeros(1,N)]);
Plot the magnitude pattern

```
fc = 4000;
c = 1500.0;
pattern(sArray,fc,0,[-40:0.1:40],...
    'PropagationSpeed',c,...
```

```
'CoordinateSystem','polar',...
'Type','efield')
```



Normalized Magnitude, Broadside at $0.00^{\circ}$
Plot the directivity pattern
pattern(sArray,fc,0,[-40:0.1:40],...
'PropagationSpeed', c,...
'CoordinateSystem','polar',...
'Type','directivity')


Directivity (dBi), Broadside at $0.00^{\circ}$

## Version History <br> Introduced in R2011a

## References

[1] Josefsson, L. and P. Persson. Conformal Array Antenna Theory and Design. Piscataway, NJ: IEEE Press, 2006.
[2] Van Trees, H. Optimum Array Processing. New York: Wiley-Interscience, 2002.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:

- pattern, patternAzimuth, patternElevation, plotResponse, and viewArray methods are not supported.
- See "System Objects in MATLAB Code Generation" (MATLAB Coder).


## See Also

phased.ReplicatedSubarray|phased.PartitionedArray
phased.CosineAntennaElement | phased.CustomAntennaElement |
phased.IsotropicAntennaElement | phased.ULA|phased.URA|uv2azel|phased.UCA|
phitheta2azel
Topics
Phased Array Gallery

## directivity

System object: phased. ConformalArray
Package: phased
Directivity of conformal array

## Syntax

D = directivity (H,FREQ,ANGLE)
D = directivity (H, FREQ, ANGLE, Name, Value)

## Description

D = directivity (H, FREQ, ANGLE) computes the "Directivity" on page 1-166 of a conformal array of antenna or microphone elements, $H$, at frequencies specified by the FREQ and in angles of direction specified by the ANGLE.

The integration used when computing array directivity has a minimum sampling grid of 0.1 degrees. If an array pattern has a beamwidth smaller than this, the directivity value will be inaccurate.

D = directivity (H, FREQ, ANGLE, Name, Value) computes the directivity with additional options specified by one or more Name, Value pair arguments.

## Input Arguments

## H - Conformal array

System object
Conformal array specified as a phased. ConformalArray System object.
Example: H = phased.ConformalArray;

## FREQ - Frequency for computing directivity and patterns

positive scalar | 1-by-L real-valued row vector
Frequencies for computing directivity and patterns, specified as a positive scalar or 1-by-L realvalued row vector. Frequency units are in hertz.

- For an antenna, microphone, or sonar hydrophone or projector element, FREQ must lie within the range of values specified by the FrequencyRange or FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased.CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: [1e8 2e6]
Data Types: double

## ANGLE - Angles for computing directivity

1-by- $M$ real-valued row vector | 2 -by- $M$ real-valued matrix
Angles for computing directivity, specified as a 1-by- $M$ real-valued row vector or a 2 -by- $M$ real-valued matrix, where $M$ is the number of angular directions. Angle units are in degrees. If ANGLE is a 2-by- $M$ matrix, then each column specifies a direction in azimuth and elevation, [az;el]. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

If ANGLE is a $1-b y-M$ vector, then each entry represents an azimuth angle, with the elevation angle assumed to be zero.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the xy plane. This angle is positive when measured from the $x$-axis toward the $y$-axis. The elevation angle is the angle between the direction vector and $x y$ plane. This angle is positive when measured towards the $z$-axis. See "Azimuth and Elevation Angles".
Example: [45 60; 0 10]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Namel=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## PropagationSpeed - Signal propagation speed

speed of light (default) | positive scalar
Signal propagation speed, specified as the comma-separated pair consisting of
' PropagationSpeed ' and a positive scalar in meters per second.
Example: 'PropagationSpeed', physconst('LightSpeed')
Data Types: double
Weights - Array weights
1 (default) | $N$-by-1 complex-valued column vector $\mid N$-by- $L$ complex-valued matrix
Array weights, specified as the comma-separated pair consisting of 'Weights' and an $N$-by-1 complex-valued column vector or $N$-by- $L$ complex-valued matrix. Array weights are applied to the elements of the array to produce array steering, tapering, or both. The dimension $N$ is the number of elements in the array. The dimension $L$ is the number of frequencies specified by FREQ.

| Weights Dimension | FREQ Dimension | Purpose |
| :--- | :--- | :--- |
| $N$-by-1 complex-valued column <br> vector | Scalar or 1-by- $L$ row vector | Applies a set of weights for the <br> single frequency or for all $L$ <br> frequencies. |
| $N$-by- $L$ complex-valued matrix | 1-by-L row vector | Applies each of the $L$ columns of <br> 'Weights' for the <br> Corresponding frequency in <br> FREQ. |

Note Use complex weights to steer the array response toward different directions. You can create weights using the phased. SteeringVector System object or you can compute your own weights. In general, you apply Hermitian conjugation before using weights in any Phased Array System Toolbox function or System object such as phased. Radiator or phased. Collector. However, for the directivity, pattern, patternAzimuth, and patternElevation methods of any array System object use the steering vector without conjugation.

## Example: 'Weights',ones(N,M)

Data Types: double
Complex Number Support: Yes

## Output Arguments

## D - Directivity

M-by-L matrix
Directivity, returned as an $M$-by- $L$ matrix. Each row corresponds to one of the $M$ angles specified by ANGLE. Each column corresponds to one of the $L$ frequency values specified in FREQ. Directivity units are in dBi where dBi is defined as the gain of an element relative to an isotropic radiator.

## Examples

## Directivity of Conformal Array

Compute the directivity of a circular array constructed using a conformal array System object ${ }^{\mathrm{TM}}$.
Construct a 21 -element uniform circular sonar array (UCA) of backbaffled omnidirectional microphones. The array is one meter in diameter. Set the operating frequency to 4 kHz . A typical value for the speed of sound in seawater is $1500.0 \mathrm{~m} / \mathrm{s}$.

```
N = 21;
theta = (0:N-1)*360/N-180;
Radius = 0.5;
myMic = phased.OmnidirectionalMicrophoneElement;
myMicFrequencyRange = [0,5000];
myMic.BackBaffled = true;
myArray = phased.ConformalArray;
myArray.Element = myMic;
myArray.ElementPosition = Radius*[zeros(1,N);cosd(theta);sind(theta)];
myArray.ElementNormal = [ones(1,N);zeros(1,N)];
c = 1500.0;
fc = 4000;
```

Steer the array to 30 degrees in azimuth and compute the directivity in the steering direction.

```
lambda = c/fc;
ang = [30;0];
w = steervec(getElementPosition(myArray)/lambda,ang);
d = directivity(myArray,fc,ang,...
    'PropagationSpeed',c,...
    'Weights',w)
d = 15.1633
```


## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \Pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## See Also

pattern | patternAzimuth | patternElevation

## collectPlaneWave

System object: phased. ConformalArray
Package: phased
Simulate received plane waves

## Syntax

```
Y = collectPlaneWave(H,X,ANG)
Y = collectPlaneWave(H,X,ANG,FREQ)
Y = collectPlaneWave(H,X,ANG,FREQ,C)
```


## Description

$Y=\operatorname{collectPlaneWave}(H, X, A N G)$ returns the received signals at the sensor array, $H$, when the input signals indicated by $X$ arrive at the array from the directions specified in ANG.
$Y=$ collectPlaneWave ( $H, X$, ANG, $F R E Q$ ), in addition, specifies the incoming signal carrier frequency in FREQ.
$Y=\operatorname{collectPlaneWave}(H, X, A N G, F R E Q, C)$, in addition, specifies the signal propagation speed in C.

## Input Arguments

## H

Array object.
X
Incoming signals, specified as an M-column matrix. Each column of $X$ represents an individual incoming signal.

## ANG

Directions from which incoming signals arrive, in degrees. ANG can be either a 2-by-M matrix or a row vector of length M .

If ANG is a 2-by-M matrix, each column specifies the direction of arrival of the corresponding signal in X. Each column of ANG is in the form [azimuth; elevation]. The azimuth angle must be between $-180^{\circ}$ and $180^{\circ}$, inclusive. The elevation angle must be between $-90^{\circ}$ and $90^{\circ}$, inclusive.

If ANG is a row vector of length M , each entry in ANG specifies the azimuth angle. In this case, the corresponding elevation angle is assumed to be $0^{\circ}$.

FREQ
Carrier frequency of signal in hertz. FREQ must be a scalar.
Default: 3e8

## C

Propagation speed of signal in meters per second.
Default: Speed of light

## Output Arguments

## Y

Received signals. Y is an N-column matrix, where N is the number of elements in the array H. Each column of $Y$ is the received signal at the corresponding array element, with all incoming signals combined.

## Examples

## Simulate Received Signals at Conformal Array

Simulate two received signals at an 8 -element uniform circular array. The signals arrive from $10^{\circ}$ and $30^{\circ}$ azimuth, respectively. Both signals have an elevation angle of $0^{\circ}$. Assume the propagation speed is the speed of light and the carrier frequency of the signal is 100 MHz .

N = 8;
azang = (0:N-1)*360/N-180;
array $=$ phased.ConformalArray('ElementPosition', ...
[cosd(azang); sind(azang);zeros(1,N)],'ElementNormal',[azang;zeros(1,N)]);
y = collectPlaneWave(array, randn (4,2),[10 30],100e6);

## Algorithms

collectPlaneWave modulates the input signal with a phase corresponding to the delay caused by the direction of arrival. The method does not account for the response of individual elements in the array.

For further details, see [1].

## References

[1] Van Trees, H. Optimum Array Processing. New York: Wiley-Interscience, 2002.

## See Also

uv2azel|phitheta2azel

## getElementNormal

System object: phased. ConformalArray<br>Package: phased<br>Normal vector to array elements

## Syntax

normvec $=$ getElementNormal(sConfArray)
normvec $=$ getElementNormal(sConfArray,elemidx)

## Description

normvec $=$ getElementNormal(sConfArray) returns the normal vectors of the array elements of the phased.sConfArray System object, sConfArray. The output argument normvec is a 2-by- $N$ matrix, where $N$ is the number of elements in array, sConfArray. Each column of normvec defines the normal direction of an element in the local coordinate system in the form[az;el]. Units are degrees. The origin of the local coordinate system is defined by the phase center of the array.
normvec = getElementNormal(sConfArray, elemidx) returns only the normal vectors of the elements specified in the element index vector, elemidx. This syntax can use any of the input arguments in the previous syntax.

## Input Arguments

sConfArray - Conformal array
phased. ConformalArray System object
Conformal array, specified as a phased. ConformalArray System object.
Example: phased. ConformalArray
elemidx - Element indices
all array elements (default) | integer-valued 1-by-M row vector | integer-valued $M$-by-1 column vector
Element indices, specified as a 1 -by- $M$ or $M$-by-1 vector. Index values lie in the range 1 to $N$ where $N$ is the number of elements of the array. When elemidx is specified, getElementNormal returns the normal vectors of the elements contained in elemidx.

Example: [1,5,4]

## Output Arguments

## normvec - Element normal vectors

2 -by- $P$ real-valued vector
Element normal vectors, specified as a 2 -by- $P$ real-valued vector. Each column of normvec takes the form [az,el]. When elemidx is not specified, $P$ equals the array dimension. When elemidx is specified, $P$ equals the length of elemidx, $M$.

## Examples

## Conformal Array Element Normals

Construct a 5 -element acoustic cross array (UCA) using the ConformalArray System object ${ }^{\mathrm{Tm}}$. Assume the operating frequency is 4 kHz . A typical value for the speed of sound in seawater is $1500.0 \mathrm{~m} / \mathrm{s}$. Display the array normal vectors.

```
N = 5;
fc = 4000;
c = 1500.0;
lam = c/fc;
x = zeros(1,N);
y = [-1,0,1,0,0]*lam/2;
z = [0,0,0,-1,1]*lam/2;
sMic = phased.OmnidirectionalMicrophoneElement(...
    'FrequencyRange',[0,10000],'BackBaffled',true);
sConformArray = phased.ConformalArray('Element',sMic,...
    'ElementPosition',[x;y;z],...
    'ElementNormal',[45*ones(1,N);zeros(1,N)]);
pos = getElementPosition(sConformArray)
pos = 3\times5
```

| 0 | 0 | 0 | 0 | 0 |
| ---: | ---: | ---: | ---: | ---: |
| -0.1875 | 0 | 0.1875 | 0 | 0 |
| 0 | 0 | 0 | -0.1875 | 0.1875 |

normvec $=$ getElementNormal(sConformArray)
normvec $=2 \times 5$

| 45 | 45 | 45 | 45 | 45 |
| ---: | ---: | ---: | ---: | ---: |
| 0 | 0 | 0 | 0 | 0 |

## Version History

Introduced in R2016a

## getElementPosition

System object: phased. ConformalArray
Package: phased
Positions of array elements

## Syntax

POS = getElementPosition(H)
POS = getElementPosition(H,ELEIDX)

## Description

POS = getElementPosition(H) returns the element positions of the conformal array H. POS is an $3 x N$ matrix where $N$ is the number of elements in H . Each column of POS defines the position of an element in the local coordinate system, in meters, using the form $[\mathrm{x} ; \mathrm{y} ; \mathrm{z}]$.

For details regarding the local coordinate system of the conformal array, enter phased.ConformalArray.coordinateSystemInfo.

POS = getElementPosition(H,ELEIDX) returns the positions of the elements that are specified in the element index vector ELEIDX.

## Examples

## Element Positions of Conformal Array

Construct a three-element conformal array and obtain the element positions.

```
array = phased.ConformalArray('ElementPosition',[-1,0,1;0,0,0;0,0,0]);
pos = getElementPosition(array)
pos = 3\times3
\begin{tabular}{rrr}
-1 & 0 & 1 \\
0 & 0 & 0 \\
0 & 0 & 0
\end{tabular}
```


## getNumElements

System object: phased. ConformalArray
Package: phased
Number of elements in array

## Syntax

N = getNumElements(H)

## Description

$N=$ getNumElements( $H$ ) returns the number of elements, $N$, in the conformal array object H .

## Examples

## Number of Elements of Conformal Array

Construct a three-element conformal array and obtain the number of elements.
array = phased.ConformalArray('ElementPosition', [-1, 0,$1 ; 0,0,0 ; 0,0,0])$;
$\mathrm{N}=$ getNumElements(array)
$N=3$

## getTaper

System object: phased. ConformalArray
Package: phased
Array element tapers

## Syntax

wts = getTaper(h)

## Description

wts = getTaper(h) returns the tapers applied to each element of a conformal array, h. Tapers are often referred to as weights.

## Input Arguments

h - Conformal array
phased. ConformalArray System object
Conformal array specified as a phased. ConformalArray System object.

## Output Arguments

## wts - Array element tapers

$N$-by-1 complex-valued vector
Array element tapers returned as an $N$-by-1, complex-valued vector, where $N$ is the number of elements in the array.

## Examples

## Create and View a Tapered Array

## Create a two-ring tapered disk array

Create a two-ring disk array and set the taper values on the outer ring to be smaller than those on the inner ring.

```
elemAngles = ([0:5]*360/6);
elemPosInner = 0.5*[zeros(size(elemAngles));...
    cosd(elemAngles);...
    sind(elemAngles)];
elemPosOuter = [zeros(size(elemAngles));...
    cosd(elemAngles);...
    sind(elemAngles)];
elemNorms = repmat([0;0],1,12);
taper = [ones(size(elemAngles)),0.3*ones(size(elemAngles))];
```

```
ha = phased.ConformalArray(...
    [elemPosInner,elemPosOuter],elemNorms,'Taper',taper);
```

Display the taper values
w = getTaper(ha)
$w=12 \times 1$
1.0000
1.0000

1. 0000
1.0000
1.0000
1.0000
0.3000
0.3000
0.3000
0.3000

## View the array

viewArray(ha,'ShowTaper',true,'ShowIndex','all');

## Array Geometry



Array Span:
X axis $=0.000 \mathrm{~m}$
$Y$ axis $=2.000 \mathrm{~m}$
$Z$ axis $=1.732 \mathrm{~m}$

## isPolarizationCapable

System object: phased. ConformalArray
Package: phased
Polarization capability

## Syntax

flag = isPolarizationCapable(h)

## Description

flag = isPolarizationCapable(h) returns a Boolean value, flag, indicating whether the array supports polarization. An array supports polarization if all of its constituent sensor elements support polarization.

## Input Arguments

h - Conformal array
Conformal array specified as a phased. ConformalArray System object.

## Output Arguments

## flag - Polarization-capability flag

Polarization-capability returned as a Boolean value true if the array supports polarization or false if it does not.

## Examples

## Conformal Array of Short-Dipole Antennas Supports Polarization

Show that a circular conformal array of phased.ShortDipoleAntennaElement antenna elements supports polarization.

```
N = 8;
azang = (0:N-1)*360/N-180;
antenna = phased.ShortDipoleAntennaElement;
array = phased.ConformalArray(...
    'Element',antenna,'ElementPosition',[cosd(azang);sind(azang);zeros(1,N)],...
    'ElementNormal',[azang;zeros(1,N)]);
isPolarizationCapable(array)
ans = logical
    1
```

The returned value 1 shows that this array supports polarization.

## pattern

System object: phased. ConformalArray
Package: phased
Plot conformal array pattern

## Syntax

```
pattern(sArray,FREQ)
pattern(sArray,FREQ,AZ)
pattern(sArray,FREQ,AZ,EL)
pattern(__,Name,Value)
[PAT,AZ_ANG,EL_ANG] = pattern(
```

$\qquad$

``` )
```


## Description

pattern(sArray, FREQ) plots the 3-D array directivity pattern (in dBi) for the array specified in sArray. The operating frequency is specified in FREQ.

The integration used when computing array directivity has a minimum sampling grid of 0.1 degrees. If an array pattern has a beamwidth smaller than this, the directivity value will be inaccurate.
pattern(sArray, FREQ,AZ) plots the array directivity pattern at the specified azimuth angle.
pattern(sArray, FREQ, AZ, EL) plots the array directivity pattern at specified azimuth and elevation angles.
pattern( $\qquad$ ,Name, Value) plots the array pattern with additional options specified by one or more Name, Value pair arguments.
[PAT,AZ_ANG,EL_ANG] = pattern( __ ) returns the array pattern in PAT. The AZ_ANG output contains the coordinate values corresponding to the rows of PAT. The EL_ANG output contains the coordinate values corresponding to the columns of PAT. If the 'CoordinateSystem' parameter is set to ' uv' , then AZ_ANG contains the $U$ coordinates of the pattern and EL_ANG contains the $V$ coordinates of the pattern. Otherwise, they are in angular units in degrees. $U V$ units are dimensionless.

Note This method replaces the plotResponse method. See "Convert plotResponse to pattern" on page 1-184 for guidelines on how to use pattern in place of plotResponse.

## Input Arguments

## sArray - Conformal array

System object
Conformal array, specified as a phased. ConformalArray System object.
Example: sArray= phased.ConformalArray;

## FREQ - Frequency for computing directivity and patterns

positive scalar | 1-by-L real-valued row vector
Frequencies for computing directivity and patterns, specified as a positive scalar or 1-by-L realvalued row vector. Frequency units are in hertz.

- For an antenna, microphone, or sonar hydrophone or projector element, FREQ must lie within the range of values specified by the FrequencyRange or FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased. CustomAntennaElement and phased.CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: [1e8 2e6]
Data Types: double

## AZ - Azimuth angles

[-180:180] (default) | 1-by- $N$ real-valued row vector
Azimuth angles for computing directivity and pattern, specified as a 1-by- $N$ real-valued row vector where $N$ is the number of azimuth angles. Angle units are in degrees. Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the $x y$ plane. When measured from the $x$-axis toward the $y$-axis, this angle is positive.

## Example: [-45:2:45]

Data Types: double

## EL - Elevation angles

[-90:90] (default) | 1-by-M real-valued row vector
Elevation angles for computing directivity and pattern, specified as a 1-by-M real-valued row vector where $M$ is the number of desired elevation directions. Angle units are in degrees. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

The elevation angle is the angle between the direction vector and $x y$-plane. The elevation angle is positive when measured towards the $z$-axis.
Example: [-75:1:70]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

```
CoordinateSystem - Plotting coordinate system
'polar' (default)|'rectangular'|'uv'
```

Plotting coordinate system of the pattern, specified as the comma-separated pair consisting of 'CoordinateSystem' and one of 'polar', 'rectangular', or 'uv'. When
'CoordinateSystem' is set to 'polar' or 'rectangular', the AZ and EL arguments specify the pattern azimuth and elevation, respectively. AZ values must lie between $-180^{\circ}$ and $180^{\circ}$. EL values must lie between $-90^{\circ}$ and $90^{\circ}$. If 'CoordinateSystem' is set to 'uv', AZ and EL then specify $U$ and $V$ coordinates, respectively. AZ and EL must lie between -1 and 1.
Example: 'uv'
Data Types: char

## Type - Displayed pattern type

'directivity' (default) |'efield'|'power'|'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type ' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb' - power pattern converted to dB.

Example: 'powerdb'
Data Types: char

## Orientation - Array orientation

[0;0;0]. (default)|3-by-1 real-valued column vector
Array orientation, specified as a 3-by-1 real-valued column vector containing the rotation angles with respect to the $x-y$-, and $z$-axes of the local coordinate system, respectively.

## Normalize - Display normalize pattern

true (default) | false
Display normalized pattern, specified as the comma-separated pair consisting of 'Normalize' and a Boolean. Set this parameter to true to display a normalized pattern. This parameter does not apply when you set 'Type' to 'directivity'. Directivity patterns are already normalized.
Data Types: logical

## ShowArray - View array geometry

false (default)| true
View the array geometry along with the 3D radiation pattern, specified as false or true.
Data Types: logical
ShowLocalCoordinates - Show local coordinate axes
true (default) | false
Show the local coordinate axes, specified as true or false.
Data Types: logical

## ShowColorbar - Show colorbar

true (default) | false

Show the colorbar, specified as true or false.
Data Types: logical

## Parent - Handle to axis

scalar
Handle to the axes along which the array geometry is displayed specified as a scalar.

## PlotStyle - Plotting style

'overlay' (default)|'waterfall'
Plotting style, specified as the comma-separated pair consisting of 'Plotstyle' and either 'overlay' or 'waterfall'. This parameter applies when you specify multiple frequencies in FREQ in 2-D plots. You can draw 2-D plots by setting one of the arguments AZ or EL to a scalar.

## Data Types: char

## Polarization - Polarized field component

'combined' (default) | 'H' | 'V'
Polarized field component to display, specified as the comma-separated pair consisting of 'Polarization' and 'combined ', 'H', or 'V'. This parameter applies only when the sensors are polarization-capable and when the 'Type' parameter is not set to 'directivity'. This table shows the meaning of the display options.

| 'Polarization' | Display |
| :--- | :--- |
| ' combined ' | Combined $H$ and $V$ polarization components |
| 'H' | $H$ polarization component |
| ' $\mathrm{V}^{\prime}$ | $V$ polarization component |

Example: 'V '

## Data Types: char

## PropagationSpeed - Signal propagation speed

speed of light (default) | positive scalar
Signal propagation speed, specified as the comma-separated pair consisting of
' PropagationSpeed ' and a positive scalar in meters per second.
Example: 'PropagationSpeed', physconst('LightSpeed')
Data Types: double

## Weights - Array weights

1 (default) | $N$-by-1 complex-valued column vector | $N$-by-L complex-valued matrix
Array weights, specified as the comma-separated pair consisting of 'Weights' and an N -by-1 complex-valued column vector or $N$-by- $L$ complex-valued matrix. Array weights are applied to the elements of the array to produce array steering, tapering, or both. The dimension $N$ is the number of elements in the array. The dimension $L$ is the number of frequencies specified by FREQ.

| Weights Dimension | FREQ Dimension | Purpose |
| :--- | :--- | :--- |
| $N$-by-1 complex-valued column <br> vector | Scalar or 1-by- $L$ row vector | Applies a set of weights for the <br> single frequency or for all $L$ <br> frequencies. |
| $N$-by- $L$ complex-valued matrix | 1-by- $L$ row vector | Applies each of the $L$ columns of <br> 'Weights' for the <br> corresponding frequency in <br> FREQ. |

Note Use complex weights to steer the array response toward different directions. You can create weights using the phased. SteeringVector System object or you can compute your own weights. In general, you apply Hermitian conjugation before using weights in any Phased Array System Toolbox function or System object such as phased. Radiator or phased. Collector. However, for the directivity, pattern, patternAzimuth, and patternElevation methods of any array System object use the steering vector without conjugation.

Example: 'Weights',ones(N,M)
Data Types: double
Complex Number Support: Yes

## Output Arguments

## PAT - Array pattern

$M$-by- $N$ real-valued matrix
Array pattern, returned as an $M$-by- $N$ real-valued matrix. The dimensions of PAT correspond to the dimensions of the output arguments AZ_ANG and EL_ANG.

## AZ_ANG - Azimuth angles

scalar | 1-by- $N$ real-valued row vector
Azimuth angles for displaying directivity or response pattern, returned as a scalar or 1-by- $N$ realvalued row vector corresponding to the dimension set in AZ. The columns of PAT correspond to the values in AZ_ANG. Units are in degrees.

## EL_ANG - Elevation angles

scalar | 1-by-M real-valued row vector
Elevation angles for displaying directivity or response, returned as a scalar or 1-by-M real-valued row vector corresponding to the dimension set in EL. The rows of PAT correspond to the values in EL_ANG. Units are in degrees.

## Examples

## Plot Power Pattern of 8-Element Uniform Circular Array

Using the ConformalArray System object ${ }^{\mathrm{TM}}$, construct an 8 -element uniform circular array (UCA) of isotropic antenna elements. Plot a normalized azimuth power pattern at 0 degrees elevation. Assume the operating frequency is 1 GHz and the wave propagation speed is the speed of light.

N = 8;
azang $=(0: \mathrm{N}-1) * 360 / \mathrm{N}-180$;
$\mathrm{sCA}=$ phased.ConformalArray(...
'ElementPosition',[cosd(azang);sind(azang);zeros(1,N)],...
'ElementNormal', [azang;zeros(1,N)]);
$\mathrm{fc}=1 \mathrm{e}$;
c = physconst('LightSpeed');
pattern(sCA,fc,[-180:180],0,...
'PropagationSpeed', c, 'Type', 'powerdb',...
'CoordinateSystem','polar')


Normalized Power (dB), Broadside at $0.00^{\circ}$

## Plot Pattern of 31-Element Uniform Circular Sonar Array

Construct a 31 -element acoustic uniform circular sonar array (UCA) using the ConformalArray System object ${ }^{\mathrm{TM}}$. Assume the array is one meter in diameter. Using the ElevationAngles parameter, restrict the display to $+/-40$ degrees in 0.1 degree increments. Assume the operating frequency is 4 kHz . A typical value for the speed of sound in seawater is $1500.0 \mathrm{~m} / \mathrm{s}$.

## Construct the array

$\mathrm{N}=31$;
theta $=(0: \mathrm{N}-1) * 360 / \mathrm{N}-180$;
Radius = 0.5;
sMic = phased.OmnidirectionalMicrophoneElement(...
'FrequencyRange', [0, 10000], 'BackBaffled' , true) ;
sArray = phased.ConformalArray('Element',sMic,...
'ElementPosition', Radius*[zeros(1,N); cosd(theta); sind(theta)],...
'ElementNormal', [ones(1,N); zeros(1,N)]);
Plot the magnitude pattern

```
fc = 4000;
c = 1500.0;
pattern(sArray,fc,0,[-40:0.1:40],...
    'PropagationSpeed',c,...
    'CoordinateSystem','polar',...
    'Type','efield')
```



Normalized Magnitude, Broadside at $0.00^{\circ}$
Plot the directivity pattern

```
pattern(sArray,fc,0,[-40:0.1:40],...
    'PropagationSpeed',c,...
    'CoordinateSystem','polar',...
    'Type','directivity')
```



Directivity (dBi), Broadside at $0.00^{\circ}$

## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \Pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Convert plotResponse to pattern

For antenna, microphone, and array System objects, the pattern method replaces the plotResponse method. In addition, two new simplified methods exist just to draw 2-D azimuth and elevation pattern plots. These methods are azimuthPattern and elevationPattern.

The following table is a guide for converting your code from using plotResponse to pattern. Notice that some of the inputs have changed from input arguments to Name-Value pairs and conversely. The general pattern method syntax is
pattern(H,FREQ,AZ,EL, 'Name1','Value1',...,'NameN', 'ValueN')

| plotResponse Inputs | plotResponse Description | pattern Inputs |
| :--- | :--- | :--- |
| H argument | Antenna, microphone, or array <br> System object. | H argument (no change) |
| FREQ argument | Operating frequency. | FREQ argument (no change) |
| V argument | Propagation speed. This argument <br> is used only for arrays. | 'PropagationSpeed ' name-value <br> pair. This parameter is only used for <br> arrays. |


| plotResponse Inputs | plotResponse Description |  | pattern Inputs |  |
| :---: | :---: | :---: | :---: | :---: |
| 'Format' and 'RespCut' namevalue pairs | These options work together to let you create a plot in angle space (line or polar style) or $U V$ space. They also determine whether the plot is 2-D or 3-D. This table shows you how to create different types of plots using plotResponse. |  | 'CoordinateSystem' name-value pair used together with the AZ and EL input arguments. <br> 'CoordinateSystem' has the same options as the plotResponse method 'Format ' name-value pair, except that 'line' is now named 'rectangular'. The table shows how to create different types of plots using pattern. |  |
|  | Display space |  |  |  |
|  | Angle space (2D) |  |  |  |
|  |  | Set 'RespCut'to 'Az' or'El'. Set'Format' to'line' or'polar'.Set the displayaxis using eitherthe'AzimuthAngleS' or'ElevationAngles' name-value pairs. | Display space |  |
|  |  |  | Angle space (2D) <br> Angle space (3D) | Set <br> 'Coordinate <br> System' to rectangular' or 'polar'. <br> Specify either AZ or EL as a scalar. |
|  |  |  |  | Set <br> 'Coordinate <br> System' to 'rectangular' |
|  | Angle space (3D) | Set 'RespCut' to '3D'. Set 'Format' to ' line' or 'polar'. <br> Set the display axis using both the 'AzimuthAngle ${ }^{\prime}$ and 'Elevation Angles ' namevalue pairs. |  | or 'polar'. <br> Specify both AZ and EL as vectors. |
|  |  |  | UV space (2D) | Set <br> 'Coordinate <br> System' to 'uv'. Use AZ to specify a $U$ space vector. Use EL to specify a $V$-space scalar. |
|  |  |  | UV space (3D) | Set |
|  | UV space (2D) | Set 'RespCut' to'U'. Set 'Format' to 'UV '. Set the display range using the 'UGrid' namevalue pair. |  | System' to 'uv'. Use AZ to specify a $U$ space vector. <br> Use EL to specify a $V$-space vector. |
|  |  |  | If you set CoordinateSystem to 'uv', enter the UV grid values using AZ and EL . |  |
|  | UV space (3D) | $\begin{aligned} & \text { Set 'RespCut' } \\ & \text { to'3D'. Set } \\ & \text { 'Format' to } \end{aligned}$ |  |  |


| plotResponse Inputs | plotResponse Description |  | pattern Inputs |
| :---: | :---: | :---: | :---: |
|  | Display space |  |  |
|  |  | 'UV'. Set the display range using both the 'UGrid' and 'VGrid' namevalue pairs. |  |
| 'CutAngle' name-value pair | Constant angle at to take an azimuth or elevation cut. When producing a 2-D plot and when 'RespCut' is set to 'Az' or 'El', use 'CutAngle' to set the slice across which to view the plot. |  | No equivalent name-value pair. To create a cut, specify either AZ or EL as a scalar, not a vector. |
| 'NormalizeResponse' namevalue pair | Normalizes the plot. When 'Unit' is set to 'dbi', you cannot specify 'NormalizeResponse'. |  | Use the 'Normalize' name-value pair. When 'Type' is set to 'directivity' you cannot specify 'Normalize'. |
| 'OverlayFreq' name-value pair | Plot multiple frequencies on the same 2-D plot. Available only when 'Format' is set to 'line' or 'uv' and 'RespCut' is not set to '3D'. The value true produces an overlay plot and the value false produces a waterfall plot. |  | 'PlotStyle' name-value pair plots multiple frequencies on the same 2-D plot. <br> The values 'overlay' and 'waterfall' correspond to 'OverlayFreq' values of true and false. The option 'waterfall' is allowed only when 'CoordinateSystem' is set to 'rectangular' or 'uv'. |
| 'Polarization' name-value pair | Determines how to plot polarized fields. Options are 'None', 'Combined', 'H', or 'V'. |  | 'Polarization' name-value pair determines how to plot polarized fields. The 'None ' option is removed. The options 'Combined ', 'H', or 'V' are unchanged. |
| 'Unit ' name-value pair | Determines the plot units. Choose 'db', 'mag', 'pow', or 'dbi', where the default is ' db '. |  | 'Type ' name-value pair, uses equivalent options with different names |
|  |  |  | plotResponse pattern |
|  |  |  | 'db' 'powerdb' <br> 'mag' 'efield' <br> 'pow' 'power' <br> 'dbi' 'directivity' |
| 'Weights ' name-value pair | Array element tapers (or weights). |  | 'Weights ' name-value pair (no change). |
| 'AzimuthAngles ' name-value pair | Azimuth angles used to display the antenna or array response. |  | AZ argument |


| plotResponse Inputs | plotResponse Description | pattern Inputs |
| :--- | :--- | :--- |
| 'ElevationAngles ' name-value <br> pair | Elevation angles used to display the <br> antenna or array response. | EL argument |
| 'UGrid' name-value pair | Contains $U$ coordinates in $U V$ - <br> space. | AZ argument when <br> 'CoordinateSystem ' name-value <br> pair is set to ' uv ' |
| 'VGrid' name-value pair | Contains V-coordinates in $U V$-space. | EL argument when <br> 'CoordinateSystem ' name-value <br> pair is set to 'uv ' |

## Version History <br> Introduced in R2015a

## See Also <br> patternAzimuth |patternElevation

## patternAzimuth

System object: phased. ConformalArray
Package: phased
Plot conformal array directivity or pattern versus azimuth

## Syntax

```
patternAzimuth(sArray,FREQ)
patternAzimuth(sArray,FREQ,EL)
patternAzimuth(sArray,FREQ,EL,Name,Value)
PAT = patternAzimuth(
```

$\qquad$

``` )
```


## Description

patternAzimuth (sArray, FREQ) plots the 2-D array directivity pattern versus azimuth (in dBi) for the array sArray at zero degrees elevation angle. The argument FREQ specifies the operating frequency.

The integration used when computing array directivity has a minimum sampling grid of 0.1 degrees. If an array pattern has a beamwidth smaller than this, the directivity value will be inaccurate.
patternAzimuth(sArray, FREQ,EL), in addition, plots the 2-D array directivity pattern versus azimuth (in dBi ) for the array sArray at the elevation angle specified by $E L$. When $E L$ is a vector, multiple overlaid plots are created.
patternAzimuth(sArray, FREQ,EL,Name, Value) plots the array pattern with additional options specified by one or more Name, Value pair arguments.

PAT = patternAzimuth ( _ _ ) returns the array pattern. PAT is a matrix whose entries represent the pattern at corresponding sampling points specified by the 'Azimuth ' parameter and the EL input argument.

## Input Arguments

## sArray - Conformal array

System object
Conformal array, specified as a phased.ConformalArray System object.
Example: sArray= phased.ConformalArray;

## FREQ - Frequency for computing directivity and pattern

positive scalar
Frequency for computing directivity and pattern, specified as a positive scalar. Frequency units are in hertz.

- For an antenna or microphone element, FREQ must lie within the range of values specified by the FrequencyRange or the FrequencyVector property of the element. Otherwise, the element
produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased.CustomMic rophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: 1e8
Data Types: double

## EL - Elevation angles

1 -by- $N$ real-valued row vector
Elevation angles for computing sensor or array directivities and patterns, specified as a 1-by- $N$ realvalued row vector. The quantity $N$ is the number of requested elevation directions. Angle units are in degrees. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

The elevation angle is the angle between the direction vector and the $x y$ plane. When measured toward the $z$-axis, this angle is positive.
Example: [0, 10, 20]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Type - Displayed pattern type

'directivity' (default)|'efield'|'power'|'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb' - power pattern converted to dB.

Example: 'powerdb'
Data Types: char

## PropagationSpeed - Signal propagation speed

speed of light (default) | positive scalar
Signal propagation speed, specified as the comma-separated pair consisting of ' PropagationSpeed ' and a positive scalar in meters per second.
Example: 'PropagationSpeed', physconst('LightSpeed')
Data Types: double

## Weights - Array weights

M-by-1 complex-valued column vector
Array weights, specified as the comma-separated pair consisting of 'Weights' and an $M$-by- 1 complex-valued column vector. Array weights are applied to the elements of the array to produce array steering, tapering, or both. The dimension $M$ is the number of elements in the array.

Note Use complex weights to steer the array response toward different directions. You can create weights using the phased. SteeringVector System object or you can compute your own weights. In general, you apply Hermitian conjugation before using weights in any Phased Array System Toolbox function or System object such as phased. Radiator or phased. Collector. However, for the directivity, pattern, patternAzimuth, and patternElevation methods of any array System object use the steering vector without conjugation.

## Example: 'Weights' , ones (10,1)

Data Types: double
Complex Number Support: Yes

## Azimuth - Azimuth angles

[-180:180] (default) | 1-by-P real-valued row vector
Azimuth angles, specified as the comma-separated pair consisting of 'Azimuth' and a 1-by-P realvalued row vector. Azimuth angles define where the array pattern is calculated.
Example: 'Azimuth', [-90:2:90]
Data Types: double

## Parent - Handle to axis

scalar
Handle to the axes along which the array geometry is displayed specified as a scalar.

## Output Arguments

## PAT - Array directivity or pattern

L-by-N real-valued matrix

Array directivity or pattern, returned as an $L$-by- $N$ real-valued matrix. The dimension $L$ is the number of azimuth values determined by the 'Azimuth' name-value pair argument. The dimension $N$ is the number of elevation angles, as determined by the EL input argument.

## Examples

## Plot Azimuth Pattern of 5-Element Cross Sonar Array

Construct a 5 -element acoustic cross array (UCA) using the ConformalArray System object ${ }^{\mathrm{TM}}$. Assume the operating frequency is 4 kHz . A typical value for the speed of sound in seawater is $1500.0 \mathrm{~m} / \mathrm{s}$. Plot the array patterns at two different elevation angles.

```
Construct and view array
N = 5;
fc = 4000;
c = 1500.0;
lam = c/fc;
x = zeros(1,N);
y = [-1,0,1,0,0]*lam/2;
z = [0,0,0,-1,1]*lam/2;
sMic = phased.OmnidirectionalMicrophoneElement(...
    'FrequencyRange',[0,10000],'BackBaffled',true);
sArray = phased.ConformalArray('Element',sMic,...
    'ElementPosition',[x;y;z],...
    'ElementNormal',[zeros(1,N);zeros(1,N)]);
viewArray(sArray)
```


## Array Geometry



Plot azimuth pattern for magnitude
fc = 4000;
c = 1500.0;
patternAzimuth(sArray,fc,[0,20],...
'PropagationSpeed ', c, ...
'Type', 'efield')


Plot azimuth pattern for directivity
patternAzimuth(sArray,fc,[0,20],...
'PropagationSpeed ', c, ...
'Type','directivity')


Directivity (dBi), Broadside at $0.00^{\circ}$

## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Version History

Introduced in R2015a

## See Also

pattern | patternElevation

## patternElevation

System object: phased. ConformalArray
Package: phased
Plot conformal array directivity or pattern versus elevation

## Syntax

```
patternElevation(sArray,FREQ)
patternElevation(sArray,FREQ,AZ)
patternElevation(sArray,FREQ,AZ,Name,Value)
PAT = patternElevation(
```

$\qquad$

``` )
```


## Description

patternElevation(sArray, FREQ) plots the 2-D array directivity pattern versus elevation (in dBi ) for the array sArray at zero degrees azimuth angle. When AZ is a vector, multiple overlaid plots are created. The argument FREQ specifies the operating frequency.

The integration used when computing array directivity has a minimum sampling grid of 0.1 degrees. If an array pattern has a beamwidth smaller than this, the directivity value will be inaccurate.
patternElevation(sArray, FREQ, AZ), in addition, plots the 2-D element directivity pattern versus elevation (in dBi ) at the azimuth angle specified by $A Z$. When $A Z$ is a vector, multiple overlaid plots are created.
patternElevation(sArray,FREQ,AZ,Name, Value) plots the array pattern with additional options specified by one or more Name, Value pair arguments.

PAT = patternElevation ( _ ) returns the array pattern. PAT is a matrix whose entries represent the pattern at corresponding sampling points specified by the 'Elevation' parameter and the AZ input argument.

## Input Arguments

## sArray - Conformal array

System object
Conformal array, specified as a phased. ConformalArray System object.
Example: sArray= phased.ConformalArray;
FREQ - Frequency for computing directivity and pattern
positive scalar
Frequency for computing directivity and pattern, specified as a positive scalar. Frequency units are in hertz.

- For an antenna or microphone element, FREQ must lie within the range of values specified by the FrequencyRange or the FrequencyVector property of the element. Otherwise, the element
produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased.CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: 1e8
Data Types: double

## AZ - Azimuth angles for computing directivity and pattern

1-by- $N$ real-valued row vector
Azimuth angles for computing sensor or array directivities and patterns, specified as a 1 -by- $N$ realvalued row vector where $N$ is the number of desired azimuth directions. Angle units are in degrees. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the $x y$ plane. This angle is positive when measured from the $x$-axis toward the $y$-axis.
Example: [0,10,20]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Type - Displayed pattern type

'directivity' (default)|'efield'|'power'|'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb' - power pattern converted to dB.

Example: 'powerdb'
Data Types: char

## PropagationSpeed - Signal propagation speed

speed of light (default) | positive scalar
Signal propagation speed, specified as the comma-separated pair consisting of ' PropagationSpeed ' and a positive scalar in meters per second.
Example: 'PropagationSpeed', physconst('LightSpeed')
Data Types: double

## Weights - Array weights

M-by-1 complex-valued column vector
Array weights, specified as the comma-separated pair consisting of 'Weights' and an $M$-by-1 complex-valued column vector. Array weights are applied to the elements of the array to produce array steering, tapering, or both. The dimension $M$ is the number of elements in the array.

Note Use complex weights to steer the array response toward different directions. You can create weights using the phased. SteeringVector System object or you can compute your own weights. In general, you apply Hermitian conjugation before using weights in any Phased Array System Toolbox function or System object such as phased.Radiator or phased. Collector. However, for the directivity, pattern, patternAzimuth, and patternElevation methods of any array System object use the steering vector without conjugation.

## Example: 'Weights', ones (10,1)

Data Types: double
Complex Number Support: Yes

## Elevation - Elevation angles

[-90:90] (default) | 1-by-P real-valued row vector
Elevation angles, specified as the comma-separated pair consisting of 'Elevation' and a 1-by-P real-valued row vector. Elevation angles define where the array pattern is calculated.
Example: 'Elevation', [-90:2:90]
Data Types: double

## Parent - Handle to axis

scalar
Handle to the axes along which the array geometry is displayed specified as a scalar.

## Output Arguments

## PAT - Array directivity or pattern

L-by- $N$ real-valued matrix

Array directivity or pattern, returned as an $L$-by- $N$ real-valued matrix. The dimension $L$ is the number of elevation angles determined by the 'Elevation' name-value pair argument. The dimension $N$ is the number of azimuth angles determined by the AZ argument.

## Examples

## Plot Elevation Pattern of 5-Element Cross Sonar Array

Construct a 5 -element acoustic cross array (UCA) using the ConformalArray System object ${ }^{\mathrm{TM}}$. Assume the operating frequency is 4 kHz . A typical value for the speed of sound in seawater is $1500.0 \mathrm{~m} / \mathrm{s}$. Plot the array patterns at two different azimuth angles.

```
Construct and view array
N = 5;
fc = 4000;
c = 1500.0;
lam = c/fc;
x = zeros(1,N);
y = [-1,0,1,0,0]*lam/2;
z = [0,0,0,-1,1]*lam/2;
sMic = phased.OmnidirectionalMicrophoneElement(...
    'FrequencyRange',[0,10000],'BackBaffled',true);
sArray = phased.ConformalArray('Element',sMic,...
    'ElementPosition',[x;y;z],...
    'ElementNormal',[zeros(1,N);zeros(1,N)]);
viewArray(sArray)
```


## Array Geometry



Plot magnitude elevation pattern

```
fc = 4000;
c = 1500.0;
patternElevation(sArray,fc,[0,90],...
    'PropagationSpeed',c,...
    'Type','efield')
```



## Plot directivity elevation pattern

Plot the pattern for elevation angles between -60 and 6 - degrees at 0.1 degree resolution.

```
patternElevation(sArray,fc,[0,90],...
```

'PropagationSpeed ', c, ...
'Type','directivity',...
'Elevation', [-60:0.1:60])


Directivity (dBi), Broadside at $0.00^{\circ}$

## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\mathrm{total}}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Version History

## Introduced in R2015a

## See Also

pattern| patternAzimuth

## plotResponse

System object: phased. ConformalArray
Package: phased
Plot response pattern of array

## Syntax

plotResponse(H, FREQ, V)
plotResponse(H, FREQ, V, Name, Value)
hPlot = plotResponse( $\qquad$ )

## Description

plotResponse ( $\mathrm{H}, \mathrm{FREQ}, \mathrm{V}$ ) plots the array response pattern along the azimuth cut, where the elevation angle is 0 . The operating frequency is specified in FREQ. The propagation speed is specified in $V$.
plotResponse( $\mathrm{H}, \mathrm{FREQ}, \mathrm{V}$, Name, Value) plots the array response with additional options specified by one or more Name, Value pair arguments.
hPlot = plotResponse( $\qquad$ ) returns handles of the lines or surface in the figure window, using any of the input arguments in the previous syntaxes.

## Input Arguments

## H

Array object

## FREQ

Operating frequency in Hertz specified as a scalar or 1-by- $K$ row vector. Values must lie within the range specified by a property of H . That property is named FrequencyRange or FrequencyVector, depending on the type of element in the array. The element has no response at frequencies outside that range. If you set the 'RespCut ' property of H to ' 3 D ' , FREQ must be a scalar. When FREQ is a row vector, plot Response draws multiple frequency responses on the same axes.

## V

Propagation speed in meters per second.

## Name-Value Pair Arguments

Specify optional pairs of arguments as Namel=Value1, . . , NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## CutAngle

Cut angle as a scalar. This argument is applicable only when RespCut is ' Az ' or ' El '. If RespCut is 'Az' , CutAngle must be between -90 and 90. If RespCut is 'El', CutAngle must be between -180 and 180.

Default: 0

## Format

Format of the plot, using one of 'Line', 'Polar', or 'UV '. If you set Format to 'UV ', FREQ must be a scalar.

Default: 'Line'

## NormalizeResponse

Set this value to true to normalize the response pattern. Set this value to false to plot the response pattern without normalizing it. This parameter is not applicable when you set the Unit parameter value to 'dbi'.

## Default: true

## OverlayFreq

Set this value to true to overlay pattern cuts in a 2-D line plot. Set this value to false to plot pattern cuts against frequency in a 3-D waterfall plot. If this value is false, FREQ must be a vector with at least two entries.

This parameter applies only when Format is not 'Polar' and RespCut is not '3D '.

## Default: true

## Polarization

Specify the polarization options for plotting the array response pattern. The allowable values are |'None' | 'Combined' | 'H' | 'V' | where

- 'None' specifies plotting a nonpolarized response pattern
- 'Combined ' specifies plotting a combined polarization response pattern
- 'H' specifies plotting the horizontal polarization response pattern
- 'V ' specifies plotting the vertical polarization response pattern

For arrays that do not support polarization, the only allowed value is 'None '. This parameter is not applicable when you set the Unit parameter value to ' dbi ' .

Default: 'None'

## RespCut

Cut of the response. Valid values depend on Format, as follows:

- If Format is 'Line' or 'Polar', the valid values of RespCut are 'Az', 'El', and '3D'. The default is ' Az '.
- If Format is 'UV', the valid values of RespCut are 'U' and '3D'. The default is 'U'.

If you set RespCut to ' 3D' , FREQ must be a scalar.

## Unit

The unit of the plot. Valid values are 'db', 'mag', 'pow', or 'dbi'. This parameter determines the type of plot that is produced.

| Unit value | Plot type |
| :--- | :--- |
| db | power pattern in dB scale |
| mag | field pattern |
| pow | power pattern |
| dbi | directivity |

Default: 'db'

## Weights

Weight values applied to the array, specified as a length- $N$ column vector or $N$-by- $M$ matrix. The dimension $N$ is the number of elements in the array. The interpretation of $M$ depends upon whether the input argument FREQ is a scalar or row vector.

| Weights Dimensions | FREQ Dimension | Purpose |
| :--- | :--- | :--- |
| $N$-by-1 column vector | Scalar or 1-by- $M$ row vector | Apply one set of weights for the <br> same single frequency or all $M$ <br> frequencies. |
| $N$-by- $M$ matrix | Scalar | Apply all of the $M$ different <br> columns in Weights for the <br> same single frequency. |
|  |  | Apply each of the $M$ different <br> columns in Weights for the <br> corresponding frequency in <br> FREQ. |
|  |  |  |

## AzimuthAngles

Azimuth angles for plotting array response, specified as a row vector. The AzimuthAngles parameter sets the display range and resolution of azimuth angles for visualizing the radiation pattern. This parameter is allowed only when the RespCut parameter is set to 'Az' or '3D' and the Format parameter is set to 'Line' or 'Polar'. The values of azimuth angles should lie between $180^{\circ}$ and $180^{\circ}$ and must be in nondecreasing order. When you set the RespCut parameter to ' 3 D ', you can set the AzimuthAngles and ElevationAngles parameters simultaneously.

Default: [-180:180]

## ElevationAngles

Elevation angles for plotting array response, specified as a row vector. The ElevationAngles parameter sets the display range and resolution of elevation angles for visualizing the radiation pattern. This parameter is allowed only when the RespCut parameter is set to ' El ' or ' 3 D ' and the

Format parameter is set to 'Line' or 'Polar'. The values of elevation angles should lie between $90^{\circ}$ and $90^{\circ}$ and must be in nondecreasing order. When yous set the RespCut parameter to ' 3 D ', you can set the ElevationAngles and AzimuthAngles parameters simultaneously.

Default: [-90:90]
UGrid
$U$ coordinate values for plotting array response, specified as a row vector. The UGrid parameter sets the display range and resolution of the $U$ coordinates for visualizing the radiation pattern in $U / V$ space. This parameter is allowed only when the Format parameter is set to 'UV' and the RespCut parameter is set to ' $U$ ' or ' $3 D$ '. The values of UGrid should be between -1 and 1 and should be specified in nondecreasing order. You can set the UGrid and VGrid parameters simultaneously.

Default: [-1:0.01:1]

## VGrid

$V$ coordinate values for plotting array response, specified as a row vector. The VGrid parameter sets the display range and resolution of the $V$ coordinates for visualizing the radiation pattern in $U / V$ space. This parameter is allowed only when the Format parameter is set to 'UV' and the RespCut parameter is set to ' $3 D^{\prime}$ '. The values of VGrid should be between -1 and 1 and should be specified in nondecreasing order. You can set VGrid and UGrid parameters simultaneously.

Default: [-1:0.01:1]

## Examples

## Plot Power Pattern of 8-Element Uniform Circular Array

Using the ConformalArray System object ${ }^{\mathrm{TM}}$, construct an 8 -element uniform circular array (UCA) of isotropic antenna elements. Plot a normalized azimuth power pattern at 0 degrees elevation. Assume the operating frequency is 1 GHz and the wave propagation speed is the speed of light.

```
N = 8;
azang = (0:N-1)*360/N-180;
sCA = phased.ConformalArray(...
    'ElementPosition',[cosd(azang);sind(azang);zeros(1,N)],...
    'ElementNormal',[azang;zeros(1,N)]);
fc = le9;
c = physconst('LightSpeed');
pattern(sCA,fc,[-180:180],0,...
    'PropagationSpeed',c,'Type','powerdb ',...
    'CoordinateSystem','polar')
```



Normalized Power (dB), Broadside at $0.00^{\circ}$

## Plot Pattern of 31-Element Uniform Circular Sonar Array

Construct a 31-element acoustic uniform circular sonar array (UCA) using the ConformalArray System object ${ }^{\mathrm{TM}}$. Assume the array is one meter in diameter. Using the ElevationAngles parameter, restrict the display to $+/-40$ degrees in 0.1 degree increments. Assume the operating frequency is 4 kHz . A typical value for the speed of sound in seawater is $1500.0 \mathrm{~m} / \mathrm{s}$.

## Construct the array

$N=31 ;$
theta $=(0: \mathrm{N}-1) * 360 / \mathrm{N}-180$;
Radius = 0.5;
sMic = phased.OmnidirectionalMicrophoneElement(...
'FrequencyRange', [0, 10000], 'BackBaffled' , true) ;
sArray $=$ phased.ConformalArray('Element',sMic,...
'ElementPosition', Radius*[zeros(1,N); cosd(theta); sind(theta)],...
'ElementNormal', [ones(1,N);zeros(1,N)]);
Plot the magnitude pattern

```
fc = 4000;
c = 1500.0;
pattern(sArray,fc,0,[-40:0.1:40],...
    'PropagationSpeed',c,...
```

```
'CoordinateSystem','polar',...
'Type','efield')
```



Normalized Magnitude, Broadside at $0.00^{\circ}$
Plot the directivity pattern
pattern(sArray,fc,0,[-40:0.1:40],...
'PropagationSpeed', c,...
'CoordinateSystem','polar',...
'Type','directivity')


Directivity (dBi), Broadside at $0.00^{\circ}$

## See Also

uv2azel|azel2uv

## step

System object: phased. ConformalArray
Package: phased
Output responses of array elements

## Syntax

RESP = step(H,FREQ,ANG)

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step (obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.

RESP $=$ step ( $H$, FREQ, ANG) returns the response of the array elements, RESP, at operating frequencies specified in FREQ and directions specified in ANG.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## H

Array object

## FREQ

Operating frequencies of array in hertz. FREQ is a row vector of length $L$. Typical values are within the range specified by a property of H . Element. That property is named FrequencyRange or FrequencyVector, depending on the type of element in the array. The element has zero response at frequencies outside that range.

## ANG

Directions in degrees. ANG is either a 2 -by- $M$ matrix or a row vector of length $M$.
If ANG is a 2 -by- $M$ matrix, each column of the matrix specifies the direction in the form [azimuth; elevation]. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive.

If ANG is a row vector of length $M$, each element specifies the azimuth angle of the direction. In this case, the corresponding elevation angle is assumed to be $0^{\circ}$.

## Output Arguments

## RESP

Voltage responses of the phased array. The output depends on whether the array supports polarization or not.

- If the array is not capable of supporting polarization, the voltage response, RESP, has the dimensions $N$-by- $M$-by- $L$. $N$ is the number of elements in the array. The dimension $M$ is the number of angles specified in ANG. $L$ is the number of frequencies specified in FREQ. For any element, the columns of RESP contain the responses of the array elements for the corresponding direction specified in ANG. Each of the $L$ pages of RESP contains the responses of the array elements for the corresponding frequency specified in FREQ.
- If the array is capable of supporting polarization, the voltage response, RESP, is a MATLAB struct containing two fields, RESP.H and RESP.V. The field, RESP.H, represents the array's horizontal polarization response, while RESP. V represents the array's vertical polarization response. Each field has the dimensions $N$-by- $M$-by-L. $N$ is the number of elements in the array, and $M$ is the number of angles specified in ANG. $L$ is the number of frequencies specified in FREQ. Each column of RESP contains the responses of the array elements for the corresponding direction specified in ANG. Each of the $L$ pages of RESP contains the responses of the array elements for the corresponding frequency specified in FREQ.


## Examples

## Response of 8-Element Uniform Circular Array

Using the ConformalArray System object ${ }^{\mathrm{Tm}}$, construct an 8 -element uniform circular array (UCA) of isotropic antenna elements. The radius of the array is one meter. Assume the operating frequency is 1 GHz and the wave propagation speed is the speed of light.

```
N = 8;
azang = (0:N-1)*360/N-180;
sCA = phased.ConformalArray(...
    'ElementPosition',[cosd(azang);sind(azang);zeros(1,N)],...
    'ElementNormal',[azang;zeros(1,N)]);
```

Get the element response at 35 degrees azimuth and 5 degrees elevation.

```
fc = 1e9;
ang = [30;5];
resp = step(sCA,fc,ang)
resp = 8\times1
    1
    1
    1
    1
    1
    1
```


## See Also

uv2azel | phitheta2azel

## viewArray

System object: phased. ConformalArray
Package: phased
View array geometry

## Syntax

```
viewArray(H)
viewArray(H,Name,Value)
hPlot = viewArray(
```

$\qquad$

``` )
```


## Description

viewArray (H) plots the geometry of the array specified in H .
viewArray ( $\mathrm{H}, \mathrm{Name}$, Value) plots the geometry of the array, with additional options specified by one or more Name, Value pair arguments.
hPlot = viewArray( $\qquad$ ) returns the handle of the array elements in the figure window. All input arguments described for the previous syntaxes also apply here.

## Input Arguments

## H

Array object.

## Name-Value Pair Arguments

Specify optional pairs of arguments as Namel=Value1, . . . ,NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Parent

Handle to the axes along which the array geometry is displayed.

## ShowNormals

Set this value to true to show the normal directions of all elements of the array. Set this value to false to plot the elements without showing normal directions.

Default: false

## ShowLocalCoordinates

Logical flag specifying whether to show the local coordinate axes.

Default: true

## ShowAnnotation

Logical flag specifying whether to show the annotations in the UI panel of the figure. Annotation shows aperture size and element spacing based on array axis of array.

Default: true

## Orientation

Orientation of the array, specified as a 3-by-1 column vector containing the rotation angles with respect to the $\mathrm{x}-\mathrm{y}$-, and z -axes of the local coordinate system, respectively. The default value is [0;0;0].

Default: [0;0;0]

## ShowTaper

Set this value to true to specify whether to change the element color brightness in proportion to the element taper magnitude. When this value is set to false, all elements are drawn with the same color.

Default: false

## ShowIndex

Vector specifying the element indices to show in the figure. Each number in the vector must be an integer between 1 and the number of elements. You can also specify the value 'All' to show the indices of all elements of the array or 'None' to suppress indices.

Default: 'None'

## Title

Character vector specifying the title of the plot.
Default: 'Array Geometry'

## Output Arguments

hPlot
Handle of array elements in figure window.

## Examples

## View Uniform Circular Array

Display the element positions and normal directions of all elements of an 8 -element uniform circular array.

```
Create the uniform circular array
N = 8;
azang = (0:N-1)*360/N - 180;
ha = phased.ConformalArray(...
    'ElementPosition',[cosd(azang);sind(azang);zeros(1,N)],...
    'ElementNormal',[azang;zeros(1,N)]);
```

Display the positions and normal directions of the elements

```
viewArray(ha,'ShowNormals',true);
```


## Array Geometry



[^0]
## See Also

phased.ArrayResponse
Topics
Phased Array Gallery

## phased.CardioidAntennaElement

Package: phased
Cardioid antenna element

## Description

The CardioidAntennaElement System object models an antenna with a "Cardioid Response" on page 1-221. Cardioid antennas are often used in direction finding. The cardioid response can be implemented by placing two isotropic radiators in an array, a quarter-wavelength apart and $90^{\circ}$ out of phase. The default rotation of the cardioid pattern has a null at $180^{\circ}$ azimuth and $0^{\circ}$ elevation. The $0^{\circ}$ azimuth and $0^{\circ}$ elevation is considered to be the main response axis of the antenna. When placed in a linear or a rectangular array, the main response axis is aligned with the array normal.

To compute the response of the antenna element for specified directions:
1 Create the phased.CardioidAntennaElement object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

antenna = phased.CardioidAntennaElement
antenna = phased.CardioidAntennaElement(Name=Value)

## Description

antenna = phased.CardioidAntennaElement creates a cardioid antenna System object, antenna. This object models an antenna element whose response is a cardioid with a null at $180^{\circ}$ azimuth and $0^{\circ}$ elevation.
antenna = phased.CardioidAntennaElement (Name=Value) creates a cardioid antenna object, antenna, with each specified property set to the specified value. You can specify multiple name-value arguments in any order. For example, FrequencyRange=[lle6 1e9] specifies that the antenna operates in a frequency range from 1 MHz to 1 GHz .

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## FrequencyRange - Operating frequency range

## [0 1e20] (default) | nonnegative, real-valued 1-by-2 row vector

Operating frequency range of the antenna, specified as a nonnegative, real-valued, 1-by-2 row vector in the form [LowerBound HigherBound]. The antenna element has no response outside the specified frequency range. Units are in Hz .

Data Types: double
NullAxisDirection - Null axis direction
" -x" (default) | "+x" | " - y" | "+y" | " - z" | "+z"
Null axis direction, specified as one of these:



For more information, see "Cardioid Response" on page 1-221.
Data Types: double

## Usage

## Syntax

RESP = antenna(FREQ,ANG)

## Description

RESP = antenna(FREQ, ANG) returns the antenna voltage response RESP at operating frequencies specified in FREQ and directions specified in ANG.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## FREQ - Operating frequency of antenna element

nonnegative scalar | nonnegative, real-valued 1-by- $L$ row vector
Operating frequency of the antenna element, specified as a nonnegative scalar or nonnegative, realvalued 1 -by- L row vector. Frequency units are in Hz .

FREQ must lie within the range of values specified by the FrequencyRange or the
FrequencyVector property of the element. Otherwise, the element produces no response and the response is returned as -Inf. Element objects use the FrequencyRange property, except for phased. CustomAntennaElement, which uses the FrequencyVector property.

Example: [1e8 2e6]
Data Types: double

## ANG - Azimuth and elevation angles of response directions

real-valued 1-by-M row vector | real-valued 2-by-M matrix
Azimuth and elevation angles of the response directions, specified as a real-valued 1-by- $M$ row vector or a real-valued 2-by-M matrix, where $M$ is the number of angular directions. Angle units are in degrees. The azimuth angle must lie in the range $-180^{\circ}$ to $180^{\circ}$, inclusive. The elevation angle must lie in the range $-90^{\circ}$ to $90^{\circ}$, inclusive.

- If ANG is a 1 -by-M vector, each element specifies the azimuth angle of the direction. In this case, the corresponding elevation angle is assumed to be zero.
- If ANG is a 2 -by- $M$ matrix, each column of the matrix specifies the direction in the form [azimuth;elevation].

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the $x y$-plane. This angle is positive when measured from the $x$-axis toward the $y$-axis. The elevation angle is the angle between the direction vector and $x y$-plane. This angle is positive when measured toward the $z$-axis. See the definition of "Azimuth and Elevation Angles".
Example: [110 125; 15 10]
Data Types: double

## Output Arguments

## RESP - Voltage response of antenna

M-by-L matrix
Voltage response of the antenna element, returned as a matrix of size $M$-by-L. In this matrix, $M$ represents the number of angles specified in ANG and $L$ represents the number of frequencies specified in FREQ.
Data Types: double

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```


## Specific to Antenna and Transducer Element System Objects

patternElevation
patternAzimuth
pattern
beamwidth
directivity
isPolarizationCapable

Plot antenna or transducer element directivity and pattern versus elevation Plot antenna or transducer element directivity and pattern versus azimuth Plot antenna or transducer element directivity and patterns Compute and display beamwidth of sensor element pattern Directivity of antenna or transducer element
Antenna element polarization capability

## Common to All System Objects

step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object

## Examples

## Cardioid Antenna Response

Create a cardioid antenna and plot its azimuth response. The antenna can work between 800 MHz and 1.2 GHz and has an operating frequency of 1 GHz .

```
element = phased.CardioidAntennaElement( ...
    FrequencyRange=[800e6 1.2e9]);
fc = 1e9;
pattern(element,fc,-180:180,0,CoordinateSystem="polar")
```



Directivity (dBi), Broadside at $0.00^{\circ}$

Find the response of the antenna at the boresight.

```
ang = [0 0]';
resp = element(fc,ang)
resp = 1
```


## More About

## Cardioid Response

The phased.CardioidAntennaElement object returns the field response (also called field pattern) of the cardioid antenna element.

If $a z$ is the azimuth angle in degrees and el is the elevation angle in degrees, the field response has a different expression depending on the value specified for NullAxisDirection.

| $"-\mathbf{x "}$ | $"-\mathbf{y} "$ | $"-z^{\prime \prime}$ |
| :--- | :--- | :--- |
| $f(a z, e l)$ | $f(a z, e l)$ | $f(a z, e l)$ |
| $=\frac{\sin \left(\frac{\pi}{2} \sin \left(a z-90^{\circ}\right) \cos (e l)+\frac{\pi}{2}\right)}{2 \sin \left(\frac{1}{2}\left(\frac{\pi}{2} \sin \left(a z-90^{\circ}\right) \cos (\phi l)+\frac{\pi}{2}\right)\right) 2 \sin \left(\frac{1}{2}\left(\frac{\pi}{2} \sin \left(a z-180^{\circ}\right) \cos (e l)+\frac{\pi}{2}\right)\right.} \sin \sin \left(\frac{1}{2}\left(\frac{\pi}{2} \sin (-e l)+\frac{\pi}{2}\right)\right)$ |  |  |


| $"+\mathbf{x "}$ | $"+\mathbf{y} "$ | $"+\mathbf{z "}$ |
| :--- | :--- | :--- |
| $f(a z, e l)$ | $f(a z, e l)$ | $f(a z, e l)$ |
| $\left.=\frac{\sin \left(\frac{\pi}{2} \sin \left(a z+90^{\circ}\right) \cos (e l)+\frac{\pi}{2}\right)}{2 \sin \left(\frac{1}{2}\left(\frac{\pi}{2} \sin \left(a z+90^{\circ}\right) \cos (\phi l)+\frac{\bar{\pi}}{2}\right)\right.}\right) 2 \sin \left(\frac{\pi}{2}\left(\frac{\pi}{2} \sin (a z) \cos (e l)+\frac{\pi}{2}\right)\right.$ | $=\frac{\sin \left(\frac{\pi}{2} \sin (e l)+\frac{\pi}{2}\right)}{2 \sin \left(\frac{1}{2}\left(\frac{\pi}{2} \sin (e l)+\frac{\pi}{2}\right)\right)}$ |  |

## Version History

Introduced in R2021b

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder ${ }^{\mathrm{TM}}$.
Usage notes and limitations:

- The pattern, patternAzimuth, and patternElevation object functions are not supported.
- See "System Objects in MATLAB Code Generation" (MATLAB Coder).


## See Also

phased.ConformalArray | phased.CustomAntennaElement |
phased.CosineAntennaElement | phased.GaussianAntennaElement |
phased.IsotropicAntennaElement|phased.SincAntennaElement|phased.ULA|
phased.URA

## phased.GaussianAntennaElement

Package: phased
Gaussian antenna element

## Description

The GaussianAntennaElement System object models an antenna with a "Gaussian Response" on page 1-226. Despite being an idealized antenna pattern, the Gaussian is often used to approximate other antennas in simulations because its response closely follows the pattern of many antennas out to about the -10 dB level. The Gaussian beam has no sidelobes. The $0^{\circ}$ azimuth and $0^{\circ}$ elevation is considered to be the main response axis of the antenna. When placed in a linear or a rectangular array, the main response axis is aligned with the array normal.

To compute the response of the antenna element for specified directions:
1 Create the phased.GaussianAntennaElement object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

antenna = phased.GaussianAntennaElement
antenna = phased.GaussianAntennaElement(Name=Value)

## Description

antenna = phased.GaussianAntennaElement creates a Gaussian antenna System object, antenna. This object models a Gaussian beam, which closely follows the pattern of many antennas out to about the -10 dB level. The Gaussian beam has no sidelobes.
antenna = phased.GaussianAntennaElement(Name=Value) creates a Gaussian antenna object, antenna, with each specified property set to the specified value. You can specify multiple name-value arguments in any order. For example, FrequencyRange=[le6 le9] specifies that the antenna operates in a frequency range from 1 MHz to 1 GHz .

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## FrequencyRange - Operating frequency range

[0 1e20] (default) | nonnegative, real-valued 1-by-2 row vector
Operating frequency range of the antenna, specified as a nonnegative, real-valued, 1-by-2 row vector in the form [LowerBound HigherBound]. The antenna element has no response outside the specified frequency range. Units are in Hz .

Data Types: double

## Beamwidth - Beamwidth of antenna pattern

## [10 10] (default) | scalar | 1-by-2 real-valued vector

Beamwidth of the antenna pattern, specified as either a scalar or a 1-by-2 real-valued vector. When the specified value is a 1 -by-2 vector, it has the form of [AzimuthBeamwidth
ElevationBeamwidth]. If the specified value is a scalar, the azimuth and elevation beamwidths are equal. Units are in degrees.
Example: 15
Data Types: double

## Usage

## Syntax

RESP = antenna(FREQ,ANG)

## Description

RESP = antenna(FREQ,ANG) returns the antenna voltage response RESP at operating frequencies specified in FREQ and directions specified in ANG.

## Input Arguments

## FREQ - Operating frequency of antenna element

nonnegative scalar | nonnegative, real-valued 1 -by- $L$ row vector
Operating frequency of the antenna element, specified as a nonnegative scalar or nonnegative, realvalued 1 -by- L row vector. Frequency units are in Hz .

FREQ must lie within the range of values specified by the FrequencyRange or the FrequencyVector property of the element. Otherwise, the element produces no response and the response is returned as -Inf. Element objects use the FrequencyRange property, except for phased.CustomAntennaElement, which uses the FrequencyVector property.
Example: [1e8 2e6]
Data Types: double
ANG - Azimuth and elevation angles of response directions
real-valued 1-by-M row vector | real-valued 2-by-M matrix
Azimuth and elevation angles of the response directions, specified as a real-valued 1-by- $M$ row vector or a real-valued 2 -by- $M$ matrix, where $M$ is the number of angular directions. Angle units are in degrees. The azimuth angle must lie in the range $-180^{\circ}$ to $180^{\circ}$, inclusive. The elevation angle must lie in the range $-90^{\circ}$ to $90^{\circ}$, inclusive.

- If ANG is a 1-by- $M$ vector, each element specifies the azimuth angle of the direction. In this case, the corresponding elevation angle is assumed to be zero.
- If ANG is a 2-by-M matrix, each column of the matrix specifies the direction in the form [azimuth;elevation].

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the $x y$-plane. This angle is positive when measured from the $x$-axis toward the $y$-axis. The elevation angle is the angle between the direction vector and $x y$-plane. This angle is positive when measured toward the $z$-axis. See the definition of "Azimuth and Elevation Angles".

Example: [110 125; 15 10]
Data Types: double

## Output Arguments

RESP - Voltage response of antenna
M-by-L matrix
Voltage response of the antenna element, returned as a matrix of size $M$-by- $L$. In this matrix, $M$ represents the number of angles specified in ANG and $L$ represents the number of frequencies specified in FREQ.
Data Types: double

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```


## Specific to Antenna and Transducer Element System Objects

| directivity | Directivity of antenna or transducer element |
| :--- | :--- |
| beamwidth | Compute and display beamwidth of sensor element pattern |
| pattern | Plot antenna or transducer element directivity and patterns |
| patternAzimuth | Plot antenna or transducer element directivity and pattern versus azimuth |
| patternElevation | Plot antenna or transducer element directivity and pattern versus elevation |
| isPolarizationCapable | Antenna element polarization capability |

## Common to All System Objects

| step | Run System object algorithm <br> release |
| :--- | :--- |
| Release resources and allow changes to System object property values and input <br> characteristics |  |
| reset | Reset internal states of System object |

## Examples

## Gaussian Antenna Response

Create a Gaussian antenna and plot its azimuth response. The antenna can work between 800 MHz and 1.2 GHz and has an operating frequency of 1 GHz .

```
element = phased.GaussianAntennaElement( ...
    FrequencyRange=[800e6 1.2e9]);
fc = le9;
pattern(element,fc,-180:180,0,CoordinateSystem="polar")
```



Directivity (dBi), Broadside at $0.00^{\circ}$

Find the response of the antenna at the boresight.

```
ang = [0 0]';
resp = element(fc,ang)
resp = 1
```


## More About

## Gaussian Response

The phased.GaussianAntennaElement object returns the field response (also called field pattern) of the Gaussian antenna element.

If $a z$ is the azimuth angle in degrees and $e l$ is the elevation angle in degrees, the field response is

$$
f(a z, e l)=\exp \left(-2 \log 2\left(\frac{a z}{\mathrm{HPBW}_{a z}}\right)^{2}\right) \exp \left(-2 \log 2\left(\frac{e l}{\mathrm{HPBW}_{e l}}\right)^{2}\right),
$$

where the azimuth half-power beamwidth $\mathrm{HPBW}_{a z}$ is specified as the first element of Beamwidth and the elevation half-power beamwidth $\mathrm{HPBW}_{e l}$ is specified as the second element of Beamwidth.

## Version History

## Introduced in R2021b

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:

- The pattern, patternAzimuth, and patternElevation object functions are not supported.
- See "System Objects in MATLAB Code Generation" (MATLAB Coder).


## See Also

phased.CardioidAntennaElement | phased.ConformalArray| phased.CustomAntennaElement | phased.CosineAntennaElement |
phased.IsotropicAntennaElement|phased.SincAntennaElement|phased.ULA|
phased.URA
Topics
"Gaussian Antenna as Approximation for Spiral Antenna"

## phased.SincAntennaElement

Package: phased
Sinc antenna element

## Description

The SincAntennaElement System object models an antenna with a "Sinc Response" on page 1-231. A sinc antenna is representative of a uniformly illuminated rectangular antenna. Sinc antenna patterns are often used as an approximation for sector or array antennas. The sidelobes are -13.6 dB relative to the main beam gain. The $0^{\circ}$ azimuth and $0^{\circ}$ elevation is considered to be the main response axis of the antenna. When placed in a linear or a rectangular array, the main response axis is aligned with the array normal.

To compute the response of the antenna element for specified directions:
1 Create the phased.SincAntennaElement object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

antenna = phased.SincAntennaElement
antenna $=$ phased.SincAntennaElement (Name=Value)

## Description

antenna $=$ phased. SincAntennaElement creates a sinc antenna System object, antenna. This object models an antenna element whose response is a sinc antenna, which is representative of a uniformly illuminated rectangular antenna. The sidelobes are -13.6 dB relative to the main beam gain.
antenna = phased.SincAntennaElement(Name=Value) creates a sinc antenna object, antenna, with each specified property set to the specified value. You can specify multiple name-value arguments in any order. For example, FrequencyRange=[lle6 1e9] specifies that the antenna operates in a frequency range from 1 MHz to 1 GHz .

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## FrequencyRange - Operating frequency range

[0 le20] (default)| nonnegative, real-valued 1-by-2 row vector
Operating frequency range of the antenna, specified as a nonnegative, real-valued, 1-by-2 row vector in the form [LowerBound HigherBound]. The antenna element has no response outside the specified frequency range. Units are in Hz .

Data Types: double

## Beamwidth - Beamwidth of antenna pattern

## [10 10] (default) | scalar | 1-by-2 real-valued vector

Beamwidth of the antenna pattern, specified as either a scalar or a 1-by-2 real-valued vector. When the specified value is a 1-by-2 vector, it has the form of [AzimuthBeamwidth
ElevationBeamwidth]. If the specified value is a scalar, the azimuth and elevation beamwidths are equal. Units are in degrees.
Example: 15
Data Types: double

## Usage

## Syntax

RESP $=$ antenna(FREQ, ANG)

## Description

RESP = antenna (FREQ, ANG) returns the antenna voltage response RESP at operating frequencies specified in FREQ and directions specified in ANG.

## Input Arguments

## FREQ - Operating frequency of antenna element

nonnegative scalar | nonnegative, real-valued 1-by- $L$ row vector
Operating frequency of the antenna element, specified as a nonnegative scalar or nonnegative, realvalued 1-by- $L$ row vector. Frequency units are in Hz.

FREQ must lie within the range of values specified by the FrequencyRange or the FrequencyVector property of the element. Otherwise, the element produces no response and the response is returned as -Inf. Element objects use the FrequencyRange property, except for phased. CustomAntennaElement, which uses the FrequencyVector property.

Example: [1e8 2e6]
Data Types: double
ANG - Azimuth and elevation angles of response directions
real-valued 1-by- $M$ row vector | real-valued 2-by- $M$ matrix
Azimuth and elevation angles of the response directions, specified as a real-valued 1-by- $M$ row vector or a real-valued 2-by- $M$ matrix, where $M$ is the number of angular directions. Angle units are in degrees. The azimuth angle must lie in the range $-180^{\circ}$ to $180^{\circ}$, inclusive. The elevation angle must lie in the range $-90^{\circ}$ to $90^{\circ}$, inclusive.

- If ANG is a 1-by- $M$ vector, each element specifies the azimuth angle of the direction. In this case, the corresponding elevation angle is assumed to be zero.
- If ANG is a 2-by-M matrix, each column of the matrix specifies the direction in the form [azimuth;elevation].

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the $x y$-plane. This angle is positive when measured from the $x$-axis toward the $y$-axis. The elevation angle is the angle between the direction vector and $x y$-plane. This angle is positive when measured toward the $z$-axis. See the definition of "Azimuth and Elevation Angles".

Example: [110 125; 15 10]
Data Types: double

## Output Arguments

RESP - Voltage response of antenna
M-by-L matrix
Voltage response of the antenna element, returned as a matrix of size $M$-by- $L$. In this matrix, $M$ represents the number of angles specified in ANG and $L$ represents the number of frequencies specified in FREQ.

Data Types: double

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```


## Specific to Antenna and Transducer Element System Objects

| directivity | Directivity of antenna or transducer element |
| :--- | :--- |
| beamwidth | Compute and display beamwidth of sensor element pattern |
| pattern | Plot antenna or transducer element directivity and patterns |
| patternAzimuth | Plot antenna or transducer element directivity and pattern versus azimuth |
| patternElevation | Plot antenna or transducer element directivity and pattern versus elevation |
| isPolarizationCapable | Antenna element polarization capability |

## Common to All System Objects

| step | Run System object algorithm <br> release |
| :--- | :--- |
| Release resources and allow changes to System object property values and input <br> characteristics |  |
| reset | Reset internal states of System object |

## Examples

## Sinc Antenna Response

Create a sinc antenna and plot its azimuth response. The antenna can work between 800 MHz and 1.2 GHz and has an operating frequency of 1 GHz .

```
element = phased.SincAntennaElement( ...
    FrequencyRange=[800e6 1.2e9]);
fc = 1e9;
pattern(element,fc,-180:180,0,CoordinateSystem="polar")
```



Directivity (dBi), Broadside at $0.00^{\circ}$

Find the response of the antenna at the boresight.

```
ang = [0 0]';
resp = element(fc,ang)
resp = 1
```


## More About

## Sinc Response

The phased. SincAntennaElement object returns the field response (also called field pattern) of the sinc antenna element.

If $a z$ is the azimuth angle in degrees and el is the elevation angle in degrees, the field response is

$$
f(a z, e l)=\frac{\sin \left(u_{a z}\right)}{u_{a z}} \frac{\sin \left(u_{e l}\right)}{u_{e l}}
$$

where:

- The azimuth factor $u_{a z}$ depends on $a z$ and the azimuth half-power beamwidth $H_{P B W}^{a z}$ :

$$
u_{a z}=\frac{x_{0} \sin (a z)}{\sin \left(\frac{1}{2} \times \mathrm{HPBW}_{a z}\right)}
$$

Specify $\mathrm{HPBW}_{a z}$ as the first element of Beamwidth.

- The elevation factor $u_{e l}$ depends on $e l$ and the elevation half-power beamwidth $H P B W_{e l}$ :

$$
u_{e l}=\frac{x_{0} \sin (e l)}{\sin \left(\frac{1}{2} \times \mathrm{HPBW}_{e l}\right)}
$$

Specify $\mathrm{HPBW}_{e l}$ as the second element of Beamwidth.

- The normalization factor $x_{0}$ ensures the power is $1 / 2$ at the half-power beamwidth angle. The factor is a solution of

$$
\sin x=\frac{x}{\sqrt{2}} .
$$

## Version History

Introduced in R2021b

## References

[1] Blake, Lamont V. Machine Plotting of Radar Vertical-Plane Coverage Diagrams. Naval Research Laboratory Report 7098, 1970.

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\text {TM }}$.
Usage notes and limitations:

- The pattern, patternAzimuth, and patternElevation object functions are not supported.
- See "System Objects in MATLAB Code Generation" (MATLAB Coder).

```
See Also
phased.CardioidAntennaElement | phased.ConformalArray|
phased.CustomAntennaElement | phased.CosineAntennaElement |
phased.GaussianAntennaElement | phased.IsotropicAntennaElement | phased.ULA |
phased.URA
```


## Topics

```
"Sinc Antenna as Approximation for Array Response Pattern"
```


## phased.CosineAntennaElement

Package: phased
Cosine antenna element

## Description

The CosineAntennaElement object models an antenna with a cosine response on page 1-245 in both azimuth and elevation. The main response axis (MRA) points to $0^{\circ}$ azimuth and $0^{\circ}$ elevation in the antenna coordinate system. When placed in a linear array, the MRA is normal to the array axis (see, for example, phased.ULA). When placed in a planar array, the MRA points along the array normal (see, for example, phased.URA).

To compute the response of the antenna element for specified directions:
1 Create the phased.CosineAntennaElement object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?
This antenna element does not support polarization.

## Creation

## Syntax

antenna = phased.CosineAntennaElement
antenna $=$ phased.CosineAntennaElement(Name, Value)

## Description

antenna = phased.CosineAntennaElement creates a cosine antenna System object, antenna. This object models an antenna element whose response is a cosine function raised to nonnegative powers in the azimuth and elevation directions.
antenna = phased.CosineAntennaElement(Name, Value) creates a cosine antenna object, antenna, with each specified property set to the specified value. You can specify additional namevalue pair arguments in any order as (Name1,Value1,...,NameN,ValueN).

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## FrequencyRange - Operating frequency range

[0 le20] (default)| nonnegative, real-valued 1-by-2 row vector
Operating frequency range of the antenna, specified as a nonnegative, real-valued, 1-by-2 row vector in the form [LowerBound HigherBound]. The antenna element has no response outside the specified frequency range. Units are in Hz .

Data Types: double

## CosinePower - Exponent of cosine pattern

[1.5 1.5] (default) | non-negative scalar | non-negative, real-valued, 1-by-2 vector
Exponents of the cosine pattern, specified as a non-negative scalar or a non-negative, real-valued, 1-by-2 vector. Exponent values must be real numbers greater than or equal to zero. When you set CosinePower to a scalar, both the azimuth direction cosine pattern and the elevation direction cosine pattern are raised to the same power. When you set CosinePower to a 1-by-2 vector, the first element is the exponent for the azimuth direction cosine pattern. The second element is the exponent for the elevation direction cosine pattern.
Example: [1.5 1.3]
Data Types: double

## Usage

## Syntax

RESP = antenna(FREQ,ANG)

## Description

RESP = antenna(FREQ,ANG) returns the antenna voltage response RESP at operating frequencies specified in FREQ and directions specified in ANG.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## FREQ - Operating frequency of antenna element

nonnegative scalar | nonnegative, real-valued 1-by-L row vector
Operating frequency of the antenna element, specified as a nonnegative scalar or nonnegative, realvalued 1 -by- L row vector. Frequency units are in Hz .

FREQ must lie within the range of values specified by the FrequencyRange or the FrequencyVector property of the element. Otherwise, the element produces no response and the response is returned as -Inf. Element objects use the FrequencyRange property, except for phased. CustomAntennaElement, which uses the FrequencyVector property.

Example: [1e8 2e6]
Data Types: double

## ANG - Azimuth and elevation angles of response directions

real-valued 1-by-M row vector | real-valued 2-by-M matrix
Azimuth and elevation angles of the response directions, specified as a real-valued 1-by-M row vector or a real-valued 2-by-M matrix, where $M$ is the number of angular directions. Angle units are in degrees. The azimuth angle must lie in the range $-180^{\circ}$ to $180^{\circ}$, inclusive. The elevation angle must lie in the range $-90^{\circ}$ to $90^{\circ}$, inclusive.

- If ANG is a 1 -by-M vector, each element specifies the azimuth angle of the direction. In this case, the corresponding elevation angle is assumed to be zero.
- If ANG is a 2 -by- $M$ matrix, each column of the matrix specifies the direction in the form [azimuth;elevation].

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the $x y$-plane. This angle is positive when measured from the $x$-axis toward the $y$-axis. The elevation angle is the angle between the direction vector and $x y$-plane. This angle is positive when measured toward the $z$-axis. See the definition of "Azimuth and Elevation Angles".

Example: [110 125; 15 10]
Data Types: double

## Output Arguments

RESP - Voltage response of antenna
complex-valued $M$-by- $L$ matrix
Voltage response of antenna element, returned as a complex-valued $M$-by- $L$ matrix. In this matrix, $M$ represents the number of angles specified in ANG and $L$ represents the number of frequencies specified in FREQ.

Data Types: double

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```


## Specific to Antenna and Transducer Element System Objects

beamwidth
directivity
isPolarizationCapable
pattern
patternAzimuth
patternElevation

Compute and display beamwidth of sensor element pattern Directivity of antenna or transducer element Antenna element polarization capability Plot antenna or transducer element directivity and patterns Plot antenna or transducer element directivity and pattern versus azimuth Plot antenna or transducer element directivity and pattern versus elevation

## Common to All System Objects

step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object

## Examples

## Cosine Antenna Response

Construct a cosine antenna element and find its response in one direction. The cosine response is raised to a power of 1.5 in both azimuth and elevation. The antenna frequency range lies in the X band (from 8 to 12 GHz ) at 10 GHz . Obtain the antenna's response for an incident angle of $30^{\circ}$ azimuth and $5^{\circ}$ elevation.

```
antenna = phased.CosineAntennaElement('FrequencyRange',[8e9 12e9], ...
    'CosinePower',1.5);
fc = 10.0e9;
ang = [30;5];
resp = antenna(fc,ang)
resp = 0.8013
```


## Plot Power Response of Cosine Antenna

Construct a cosine pattern antenna and calculate its response at boresight ( 0 degrees azimuth and 0 degrees elevation). Then, plot the antenna pattern. Assume the antenna works between 800 MHz and 1.2 GHz and its operating frequency is 1 GHz . Set the azimuth exponent to 1.5 and elevation exponent to 2.5.

```
antenna = phased.CosineAntennaElement('FrequencyRange',[800e6 1.2e9],...
    'CosinePower',[1.5 2.5]);
fc = 1e9;
resp = antenna(fc,[0;0]);
pattern(antenna,fc,0,-90:90,'Type','powerdb','CoordinateSystem','polar')
```



Normalized Power (dB), Broadside at $0.00^{\circ}$
pattern(antenna,fc,-180:180,0,'Type','powerdb','CoordinateSystem','polar')


Normalized Power (dB), Broadside at $0.00^{\circ}$

## Plot 3-D Polar Pattern of Cosine Antenna

Construct a cosine antenna element using default parameters. Assume the antenna operating frequency is 1 GHz . Then, plot the antenna response in 3-D polar format.

```
antenna = phased.CosineAntennaElement;
fc = 1e9;
pattern(antenna,fc,[-180:180],[-90:90],'Type','powerdb', ...
    'CoordinateSystem','polar')
```



## Directivity of Cosine Antenna

Compute the directivity of a cosine antenna element at seven azimuth directions centered around boresight (zero degrees azimuth and zero degrees elevation). All elevation angles are set to zero degrees.

Create a cosine antenna element system object with the CosinePower exponents set to 1.8.
antenna = phased.CosineAntennaElement('CosinePower',[1.8,1.8]);
Set the directivity angles so that the elevation angles are zero. Set the frequency to 1 GHz .
ang $=[-30,-20,-10,0,10,20,30 ; 0,0,0,0,0,0,0] ;$
freq = 1e9;
Compute the directivity.
d = directivity(antenna,freq,ang)
d $=7 \times 1$
7.3890
8.6654
9.3985
9.6379

```
9.3985
8.6654
7.3890
```

The maximum directivity is at boresight.

## Plot Azimuth-Cut of Cosine Antenna Response Pattern

Construct a cosine antenna element using default parameters. Then, plot the pattern of the field magnitude. Assume the antenna operating frequency is 1 GHz . Restrict the response to the range of azimuth angles from -30 to 30 degrees in 0.1 degree increments. The default elevation angle is 0 degrees.

```
antenna = phased.CosineAntennaElement;
fc = 1e9;
pattern(antenna,fc,[-30:0.1:30],0,'Type','efield', ...
    'CoordinateSystem','polar')
```



Normalized Magnitude, Broadside at $0.00^{\circ}$

## Plot Directivity of Cosine Antenna

Construct a cosine-pattern antenna. Assume the antenna works between 1 and 2 GHz and its operating frequency is 1.5 GHz . Set the azimuth angle cosine power to 2.5 and the elevation angle cosine power to 3.5. Then, plot an elevation cut of its directivity.

```
antenna = phased.CosineAntennaElement('FrequencyRange', ...
    [1e9 2e9],'CosinePower',[2.5,3.5]);
fc = 1.5e9;
pattern(antenna,fc,0,-90:90,'Type','directivity', ...
    'CoordinateSystem','rectangular')
```



The directivity is maximum at 0 degrees elevation and attains a value of approximately 12 dB .

## Limited-Angle Azimuth Pattern of Cosine Antenna

Plot constant-elevation azimuth directivity patterns of a cosine antenna element at 0 degrees and 30 degrees elevation. Assume the operating frequency is 500 MHz .

```
fc = 500e6;
antenna = phased.CosineAntennaElement('FrequencyRange',[100,900]*1e6, ...
    CosinePower',[3,2]);
patternAzimuth(antenna,fc,[0 30])
```



Directivity (dBi), Broadside at $0.00^{\circ}$
Plot a limited range of azimuth angles by specifying the Azimuth parameter. Note the change in scale.
patternAzimuth(antenna,fc,[0 30],'Azimuth',-20:20)


Directivity (dBi), Broadside at $0.00^{\circ}$

## Limited-Angle Elevation Pattern of Cosine Antenna

Plot constant-azimuth elevation directivity patterns of a cosine antenna element at 45 and 55 degrees azimuth. Assume the operating frequency is 500 MHz .
$\mathrm{fc}=500 \mathrm{e} 6$;
antenna = phased.CosineAntennaElement('FrequencyRange',[100,900]*1e6, ...
'CosinePower',[3,2]);
patternElevation(antenna,fc,[45 55])


Directivity (dBi), Broadside at $0.00^{\circ}$
Plot a limited range of elevation angles using the Elevation parameter. Note the change in scale. patternElevation(antenna,fc,[45 55],'Elevation',-20:20)


Directivity (dBi), Broadside at $0.00^{\circ}$

## Cosine Antenna Does Not Support Polarization

Create a cosine antenna element using the phased.CosineAntennaElement System object ${ }^{\mathrm{TM}}$ and show that it does not support polarization.

```
antenna = phased.CosineAntennaElement('FrequencyRange',[1.0,10]*1e9);
isPolarizationCapable(antenna)
ans = logical
    0
```

The returned value 0 shows that the antenna element does not support polarization.

## More About

## Cosine Response

The object returns the field response (also called field pattern)

$$
f(a z, e l)=\cos ^{m}(a z) \cos ^{n}(e l)
$$

of the cosine antenna element.

In this expression

- $a z$ is the azimuth angle.
- el is the elevation angle.
- The exponents $m$ and $n$ are real numbers greater than or equal to zero.

The response is defined for azimuth and elevation angles between $-90^{\circ}$ and $90^{\circ}$, inclusive, and is always positive. There is no response at the backside of a cosine antenna. The cosine response pattern achieves a maximum value of 1 at $0^{\circ}$ azimuth and $0^{\circ}$ elevation. Larger exponent values narrow the response pattern of the element and increase the directivity.

The power response (or power pattern) is the squared value of the field response.

$$
P(a z, e l)=\cos ^{2 m}(a z) \cos ^{2 n}(e l)
$$

## Version History

Introduced in R2011a

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:

- The pattern, patternAzimuth, and patternElevation object functions are not supported.
- See "System Objects in MATLAB Code Generation" (MATLAB Coder).


## See Also

phased.CrossedDipoleAntennaElement | phased.CustomAntennaElement | phased.IsotropicAntennaElement | phased.ShortDipoleAntennaElement | phased.ULA | phased.URA|phased.UCA| phased.ConformalArray|phased.CardioidAntennaElement | phased.SincAntennaElement |phased.GaussianAntennaElement|uv2azel| phitheta2azel

# phased.CrossedDipoleAntennaElement 

Package: phased

Crossed-dipole antenna element

## Description

The phased.CrossedDipoleAntennaElement System object models a crossed-dipole antenna element which is used to generate circularly polarized fields. A crossed-dipole antenna is formed from two orthogonal short-dipole antennas. By default, one dipole lies along $y$-axis and the other along the $z$-axis in the antenna local coordinate system. You can rotate the antenna in the $y z$-plane using the RotationAngle property. This antenna object generates right hand or left hand circularly polarized fields, or linearly polarized fields controlled using the Polarization property. These fields are pure along the $x$-axis (defined by $0^{\circ}$ azimuth and $0^{\circ}$ elevation angles).

To compute the response of the antenna element:
1 Create the phased.CrossedDipoleAntennaElement object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

```
antenna = phased.CrossedDipoleAntennaElement
antenna = phased.CrossedDipoleAntennaElement(Name,Value)
```


## Description

antenna = phased.CrossedDipoleAntennaElement creates a crossed-dipole antenna with default property values.
antenna $=$ phased.CrossedDipoleAntennaElement(Name,Value) creates a crossed-dipole antenna with each specified property set to the specified value. You can specify additional namevalue pair arguments in any order as (Name1,Value1,...,NameN,ValueN).

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## FrequencyRange - Operating frequency range

[0 le20] (default) | nonnegative, real-valued 1-by-2 row vector
Operating frequency range of the antenna, specified as a nonnegative, real-valued, 1-by-2 row vector in the form [LowerBound HigherBound]. The antenna element has no response outside the specified frequency range. Units are in Hz .
Data Types: double

## RotationAngle - Crossed-dipole rotation angle

0 (default) | scalar between $-45^{\circ}$ and $+45^{\circ}$
Crossed-dipole rotation angle, specified as a scalar between $-45^{\circ}$ and $+45^{\circ}$. The rotation angle specifies the angle of rotation of the two dipoles around the $x$-axis. The rotation angle is measured counter-clockwise around the $x$-axis looking towards to origin. A default value of $0^{\circ}$ corresponds to the case where one dipole is along the $z$-axis and the other dipole is along the $y$-axis. Units are in degrees.

## Data Types: double

## Polarization - Crossed-dipole field polarization

'RHCP' (default) | 'LHCP' | 'Linear'
Polarization of the field generated by the antenna, specified as 'RHCP', 'LHCP', or 'Linear'.

- 'RHCP ' - right hand circularly polarize field. The horizontal field has a $90^{\circ}$ phase advance compared to the vertical field.
- ' LHCP ' - left hand circularly polarize field. The horizontal field has a $90^{\circ}$ delay compared to the vertical field.
- 'Linear' - linearly polarized field. The horizontal and vertical fields are in phase.

Example: 'Linear'
Data Types: char | string

## Usage

## Syntax

RESP = antenna(FREQ,ANG)

## Description

RESP = antenna(FREQ,ANG) returns the antenna voltage response, RESP, at the operating frequencies specified in FREQ and in the directions specified in ANG.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## FREQ - Operating frequency of antenna element

nonnegative scalar | nonnegative, real-valued 1-by-L row vector
Operating frequency of the antenna element, specified as a nonnegative scalar or nonnegative, realvalued 1 -by- L row vector. Frequency units are in Hz .

FREQ must lie within the range of values specified by the FrequencyRange or the FrequencyVector property of the element. Otherwise, the element produces no response and the response is returned as -Inf. Element objects use the FrequencyRange property, except for phased. CustomAntennaElement, which uses the FrequencyVector property.

Example: [1e8 2e6]
Data Types: double

## ANG - Azimuth and elevation angles of response directions

real-valued 1-by-M row vector | real-valued 2-by-M matrix
Azimuth and elevation angles of the response directions, specified as a real-valued 1-by- $M$ row vector or a real-valued 2-by-M matrix, where $M$ is the number of angular directions. Angle units are in degrees. The azimuth angle must lie in the range $-180^{\circ}$ to $180^{\circ}$, inclusive. The elevation angle must lie in the range $-90^{\circ}$ to $90^{\circ}$, inclusive.

- If ANG is a 1 -by-M vector, each element specifies the azimuth angle of the direction. In this case, the corresponding elevation angle is assumed to be zero.
- If ANG is a 2-by-M matrix, each column of the matrix specifies the direction in the form [azimuth;elevation].

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the $x y$-plane. This angle is positive when measured from the $x$-axis toward the $y$-axis. The elevation angle is the angle between the direction vector and $x y$-plane. This angle is positive when measured toward the $z$-axis. See the definition of "Azimuth and Elevation Angles".

Example: [110 125; 15 10]
Data Types: double

## Output Arguments

## RESP - Antenna voltage response

structure
Voltage response of the antenna, returned as a MATLAB structure with fields H and V . H and V contain responses for the horizontal and vertical polarization components of the radiation fields, respectively. Both H and V are complex-valued, $M$-by- $L$ matrices. $M$ represents the number of angles specified in ANG, and $L$ represents the number of frequencies specified in FREQ.
Data Types: double

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```


## Specific to Antenna and Transducer Element System Objects

beamwidth directivity isPolarizationCapable pattern patternAzimuth patternElevation

Compute and display beamwidth of sensor element pattern Directivity of antenna or transducer element Antenna element polarization capability
Plot antenna or transducer element directivity and patterns
Plot antenna or transducer element directivity and pattern versus azimuth Plot antenna or transducer element directivity and pattern versus elevation

## Common to All System Objects

step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object

## Examples

## Compute Crossed-Dipole Antenna Response

Find the response of a crossed-dipole antenna at boresight, $0^{\circ}$ azimuth and $0^{\circ}$ elevation, and offboresight at $30^{\circ}$ azimuth and $0^{\circ}$ elevation. The antenna operates at 250 MHz .

```
antenna = phased.CrossedDipoleAntennaElement('FrequencyRange',[100 900]*1e6);
ang = [0 30;0 0];
fc = 250e6;
resp = antenna(fc,ang);
disp(resp.H)
    0.0000 - 1.2247i
    0.0000 - 1.0607i
disp(resp.V)
    -1.2247
    -1.2247
```


## Plot Response of a Crossed-Dipole Antenna

Plot the response patterns of a crossed-dipole antenna used in an L-band radar with a frequency range between 1-2 GHz. First, set up the radar parameters, and obtain the vertical and horizontal polarization responses in five different directions specified by elevation angles of $-30,-15,0,15$ and 30 degrees, all at 0 degrees azimuth angle. The responses are computed at an operating frequency of 1.5 GHz .

```
antenna = phased.CrossedDipoleAntennaElement('FrequencyRange',[1,2]*1e9);
fc = 1.5e9;
resp = antenna(fc,[0,0,0,0,0;-30,-15,0,15,30]);
[resp.V, resp.H]
ans = 5×2 complex
```

| $-1.0607+0.0000 i$ | $0.0000-1.2247 i$ |
| :--- | :--- |
| $-1.1830+0.0000 i$ | $0.0000-1.2247 i$ |
| $-1.2247+0.0000 i$ | $0.0000-1.2247 i$ |
| $-1.1830+0.0000 i$ | $0.0000-1.2247 i$ |
| $-1.0607+0.0000 i$ | $0.0000-1.2247 i$ |

Next, draw a 3-D plot of the combined polarization response.
pattern(antenna,fc,-180:180,-90:90,'CoordinateSystem','polar', ...
'Type','powerdb', 'Polarization', 'combined')


## Directivity of Crossed-Dipole Antenna Element

Compute the directivity of a crossed-dipole antenna element in several different directions.
Create a crossed-dipole antenna element System object ${ }^{\mathrm{TM}}$.
antenna $=$ phased.CrossedDipoleAntennaElement;
Set the angles of interest to be at zero-degrees constant elevation angle. The seven azimuth angles are centered around boresight (zero degrees azimuth and zero degrees elevation). Set the desired frequency to 1 GHz .
ang $=[-30,-20,-10,0,10,20,30 ; 0,0,0,0,0,0,0] ;$
freq = 1e9;
Compute the directivity along the constant elevation cut.
d = directivity(antenna,freq,ang)
$d=7 \times 1$
1.1811
1.4992
1.6950
1.7610
1.6950
1.4992
1.1811

## Plot 3-D Polar Patterns of Crossed-Dipole Antenna

Construct a crossed-dipole antenna element that operates in the frequency range from 100 MHz to 1.5 GHz . Then, plot the 3-D polar power pattern for the horizontal polarization component. Assume the antenna operates at 1 GHz .

```
antenna = phased.CrossedDipoleAntennaElement('FrequencyRange',[100 1500]*1e6);
```

fc = 1e9;
pattern(antenna,fc,-180:180,-90:90,'Type','powerdb', ...
'CoordinateSystem','polar','Polarization','H')


Next, plot the vertical polarization component.

```
pattern(antenna,fc,-180:180,-90:90,'Type','powerdb', ...
```

    'CoordinateSystem','polar','Polarization', 'V')
    

## Plot Crossed-Dipole Antenna Pattern at Constant Elevation

Construct a crossed-dipole antenna element. Then, plot the pattern of the horizontal component of the field magnitude at an elevation angle of 0 degrees. Assume the antenna operating frequency is 1 GHz . Restrict the response to the range of azimuth angles from -70 to 70 degrees in 0.1 degree increments.

```
antenna = phased.CrossedDipoleAntennaElement('FrequencyRange',[0.5 1.5]*1e9);
fc = 1e9;
pattern(antenna,fc,-70:0.1:70,0,'Type','efield', ...
    'CoordinateSystem','polar','Polarization','combined')
```



Normalized Magnitude, Broadside at $0.00^{\circ}$

## Plot Directivity of Crossed-Dipole Antenna

Create a crossed-dipole antenna. Assume the antenna works between 1 and 2 GHz and its operating frequency is 1.5 GHz . Then, plot the directivity at a constant azimuth of $0^{\circ}$.

```
antenna = phased.CrossedDipoleAntennaElement('FrequencyRange',[1e9 2e9]);
fc = 1.5e9;
pattern(antenna,fc,0,-90:90,'Type','directivity', ...
    'CoordinateSystem','rectangular')
```



The directivity is maximum at $0^{\circ}$ elevation and attains a value of approximately 1.75 dB .

## Plot Azimuth Pattern of Crossed-Dipole Antenna Element

Plot the azimuth directivity pattern of a crossed-dipole antenna at two different elevations: $0^{\circ}$ and $30^{\circ}$. Assume the operating frequency is 500 MHz .
fc = 500e6;
antenna = phased.CrossedDipoleAntennaElement('FrequencyRange',[100,900]*1e6); patternAzimuth(antenna,fc,[0 30])


Directivity (dBi), Broadside at $0.00^{\circ}$
Plot a limited range of azimuth angles using the Azimuth parameter. Notice the change in scale. patternAzimuth(antenna,fc,[0 30],'Azimuth',[-20:20])


Directivity (dBi), Broadside at $0.00^{\circ}$

## Plot Elevation Pattern of Crossed-Dipole Antenna Element

Plot the elevation directivity pattern of a crossed-dipole antenna at two different azimuths: $45^{\circ}$ and $55^{\circ}$. Assume the operating frequency is 500 MHz .
$\mathrm{fc}=500 \mathrm{e} 6$;
sCD = phased.CrossedDipoleAntennaElement('FrequencyRange',[100,900]*1e6); patternElevation(sCD,fc,[45 55])


Directivity (dBi), Broadside at $0.00^{\circ}$
Plot a reduced range of elevation angles using the Elevation parameter. Notice the change in scale. patternElevation(sCD,fc,[45 55],'Elevation',-20:20)


Directivity (dBi), Broadside at $0.00^{\circ}$

## Vertical and Horizontal Responses of Crossed-Dipole Antenna

This example shows how to create a crossed-dipole antenna operating between 100 and 900 MHz and then how to plot its vertical and horizontal polarization response at 250 MHz in the form of a 3-D polar plot.

```
antenna = phased.CrossedDipoleAntennaElement(...
    'FrequencyRange',[100 900]*1e6);
pattern(antenna,250e6,-180:180,-90:90,'CoordinateSystem','polar','Polarization','V', ...
    'Type','powerdb')
```



The antenna pattern of the vertical-polarization component is almost isotropic and has a maximum at $0^{\circ}$ elevation and $0^{\circ}$ azimuth, as shown in the figure above.

Plot the antenna's horizontal polarization response. The pattern of the horizontal polarization response also has a maximum at $0^{\circ}$ elevation and $0^{\circ}$ azimuth but no response at $\pm 90^{\circ}$ azimuth.

```
pattern(antenna,250e6,-180:180,-90:90,'CoordinateSystem','polar','Polarization','H', ...
    'Type','powerdb')
```



## Crossed-Dipole Antenna Supports Polarization

Show that the phased.CrossedDipoleAntennaElement antenna element supports polarization.

```
antenna = phased.CrossedDipoleAntennaElement;
isPolarizationCapable(antenna)
ans = logical
    1
```

The returned value of 1 shows that the crossed-dipole antenna element supports polarization.

## Plot 3-D Polar Patterns of Rotated Crossed-Dipole Antenna

Construct a crossed-dipole antenna element designed to operate in the frequency range from 100 MHz to 1.5 GHz . Assume the polarization is linear. Rotate the antenna by -45 degrees. Plot the 3-D polar power pattern for the horizontal and vertical polarization components at 1 GHz .

```
antenna = phased.CrossedDipoleAntennaElement('FrequencyRange',[100 1500]*1e6, ...
    'RotationAngle',-45.0,'Polarization','Linear');
fc = 1e9;
```

pattern(antenna,fc,-180:180,-90:90,'Type',' powerdb','Normalize',false, ...
'CoordinateSystem', 'polar','Polarization','H')

3D Response Pattern


Next, plot the vertical polarization component.
pattern(antenna,fc,-180:180,-90:90,'Type','powerdb','Normalize',false, ...
'CoordinateSystem', 'polar','Polarization', 'V')


## Algorithms

The total response of a crossed-dipole antenna element is a combination of its frequency response and spatial response. phased.CrossedDipoleAntennaElement calculates both responses using nearest neighbor interpolation, and then multiplies the responses to form the total response.

## Version History

Introduced in R2013a

## References

[1] Mott, H., Antennas for Radar and Communications, John Wiley \& Sons, 1992.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.
Usage notes and limitations:

- The pattern, patternAzimuth, and patternElevation object functions are not supported.
- See "System Objects in MATLAB Code Generation" (MATLAB Coder).


## See Also

phased.CosineAntennaElement | phased.CustomAntennaElement |
phased.IsotropicAntennaElement | phased.ShortDipoleAntennaElement | phased.ULA | phased.URA|phased.UCA|phased.ConformalArray|uv2azelpat | phitheta2azelpat | uv2azel| phitheta2azel

## phased.CustomAntennaElement

Package: phased
Custom antenna element

## Description

The phased.CustomAntennaElement System object models an antenna element with a custom spatial response pattern. The response pattern can be defined for polarized or non-polarized fields.

To create a custom antenna element:
1 Create the phased.CustomAntennaElement object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

antenna = phased.CustomAntennaElement
antenna = phased.CustomAntennaElement(Name,Value)

## Description

antenna = phased.CustomAntennaElement creates a System object, antenna, with default property values. The default response pattern is spatially isotropic.
antenna = phased.CustomAntennaElement(Name, Value) creates a custom antenna object, antenna, with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN). For example, the output response of the object depends on whether polarization is set or not.

- To create a nonpolarized response pattern, set the SpecifyPolarizationPattern property to false (default). Then, use the MagnitudePattern and PhasePattern properties to define the response pattern.
- To create a polarized response pattern, set the SpecifyPolarizationPattern property to true. Then, use any or all of the HorizontalMagnitudePattern, HorizontalPhasePattern, VerticalMagnitudePattern, and VerticalPhasePattern properties to define the response pattern.


## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.

For more information on changing property values, see System Design in MATLAB Using System Objects.

## FrequencyVector - Response and pattern frequency vector

[0 1e20] (default) | 1-by-L row vector
Frequencies at which the frequency response and antenna patterns are to be returned, specified as a 1-by- $L$ row vector. The elements of the vector must be in increasing order. The antenna element has no response outside the frequency range specified by the minimum and maximum elements of the frequency vector. Units are in Hz.

Example: [200:50:300]*1e6
Data Types: double

## FrequencyResponse - Frequency responses of antenna element

[0 0] (default) | real-valued 1-by-L vector
Frequency responses at the frequencies defined in FrequencyVector property, specified as a 1-by-L row vector. $L$ equals the length of the vector specified in the FrequencyVector property. Units are in dB .

Example: [ 0600$]$
Data Types: double
PatternCoordinateSystem - Coordinate system of custom antenna pattern
'az-el' (default)| 'phi-theta'
Coordinate system of custom antenna pattern, specified 'az-el' or 'phi-theta'. When you specify 'az-el', use the AzimuthAngles and ElevationAngles properties to specify the pattern coordinates system. When you specify 'phi-theta', use the PhiAngles and ThetaAngles properties to specify the pattern coordinates system.

## Data Types: char

## AzimuthAngles - Azimuth angles

[-180:180] (default) | real-valued length-P vector
Specify the azimuth angles as a length- $P$ vector. These angles are the azimuth angles where the custom radiation pattern is specified. $P$ must be greater than 2 . The azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$ and be in strictly increasing order. Units are in degrees.
Example: [30 40 50]

## Dependencies

To enable this property, set the PatternCoordinateSystem property to 'az-el'.

## Data Types: double

## ElevationAngles - Elevation angles

[-90:90] (default) | real-valued length- $Q$ vector
Specify the elevation angles as a length- $Q$ vector. These angles are the elevation angles where the custom radiation pattern is specified. $Q$ must be greater than 2 . The elevation angles must lie between $-90^{\circ}$ and $90^{\circ}$ and be in strictly increasing order. Units are in degrees.

Example: [-30 0 +30]

## Dependencies

To enable this property, set the PatternCoordinateSystem property to 'az-el'.
Data Types: double
PhiAngles - Phi angles in phi-theta coordinates system
0:360 (default) | real-valued $P$-length vector
Phi angles used to represent the element response pattern in phi-theta coordinates, specified as a real-valued $P$-length vector. Phi angles lie between $0^{\circ}$ and $360^{\circ}$. $P$ must be greater than 2 . Look here for definitions of "Phi and Theta Angles".

## Example: [90:180]

## Dependencies

To enable this property, set the PatternCoordinateSystem property to 'phi-theta'.

## Data Types: double

## ThetaAngles - Theta angles in phi-theta coordinate system

## 0:180 (default) | real-valued $Q$-length vector

Theta angles used to represent the element response pattern in phi-theta coordinates, specified as a real-valued $Q$-length vector. The theta angle lies between $0^{\circ}$ and $180^{\circ}$. Look here for definitions of "Phi and Theta Angles". $Q$ must be greater than 2.
Example: [40:80]

## Dependencies

To enable this property, set the PatternCoordinateSystem property to 'phi-theta'.

## Data Types: double

## SpecifyPolarizationPattern - Polarized array response <br> false (default) | true

Polarized array response, specified as false or true.

- When the SpecifyPolarizationPattern property is set to false, the antenna element transmits or receives non-polarized radiation. In this case, use the MagnitudePattern property to set the antenna response pattern.
- When the SpecifyPolarizationPattern property is set to true, the antenna element transmits or receives polarized radiation. In this case, use the HorizontalMagnitudePattern and HorizontalPhasePattern properties to set the horizontal polarization response pattern and the VerticalMagnitudePattern and VerticalPhasePattern properties to set the vertical polarization response pattern.

Data Types: logical

## MagnitudePattern - Magnitude of combined antenna radiation pattern

zeros $(181,361)$ (default) | real-valued $Q$-by- $P$ matrix | real-valued $Q$-by- $P$-by-L array
The magnitude of the combined polarization antenna radiation, pattern specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by-L array. This property is used only when the SpecifyPolarizationPattern property is set to false. Magnitude units are in dB.

- If the value of this property is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the FrequencyVector property.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the FrequencyVector property.

If the pattern contains a NaN at any azimuth and elevation direction, it is converted to - Inf, indicating zero response in that direction. The custom antenna object uses interpolation to estimate the response of the antenna at a given direction. To avoid interpolation errors, the custom response pattern must contain azimuth angles in the range [-180, 180] degrees. Set the range of elevation angles to [-90,90] degrees.

## Data Types: double

## PhasePattern - Phase of combined antenna radiation pattern

zeros $(181,361)$ (default) | real-valued $Q$-by-P matrix | real-valued $Q$-by- $P$-by- $L$ array
The phase of the combined polarization antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- L array. This property is used only when the SpecifyPolarizationPattern property is set to false. Units are in degrees.

- If the value of this property is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the FrequencyVector property.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the FrequencyVector property.

The custom antenna object uses interpolation to estimate the response of the antenna at a given direction. To avoid interpolation errors, the custom response pattern must contain azimuth angles in the range $\left[-180^{\circ}, 180^{\circ}\right]$. Set the range of elevation angles to $\left[-90^{\circ}, 90^{\circ}\right]$.
Data Types: double

## HorizontalMagnitudePattern - Magnitude of horizontal polarization component of antenna radiation pattern

zeros $(181,361)$ (default) | real-valued $Q$-by- $P$ matrix | real-valued $Q$-by- $P$-by-L array
The magnitude of the horizontal polarization component of the antenna radiation pattern, specified as a real-valued $Q$-by- $P$ matrix or real-valued a $Q$-by- $P$-by- $L$ array. Magnitude units are in dB .

- If the value of this property is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the FrequencyVector property.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the FrequencyVector property.

If the magnitude pattern contains a NaN at any azimuth and elevation direction, it is converted to Inf, indicating zero response in that direction. The custom antenna object uses interpolation to estimate the response of the antenna at a given direction. To avoid interpolation errors, the custom response pattern must contain azimuth angles in the range [ $-180,180]^{\circ}$ and elevation angles in the range $[-90,90]^{\circ}$.

## Dependencies

To enable this property, set the SpecifyPolarizationPattern property to true.
Data Types: double

## HorizontalPhasePattern - Phase of horizontal polarization component of antenna radiation pattern <br> zeros $(181,361)$ (default) | real-valued $Q$-by-P matrix | real-valued $Q$-by- $P$-by-L array

The phase of the horizontal polarization component of the antenna radiation pattern, specified as a real-valued $Q$-by- $P$ matrix or a real-valued $Q$-by- $P$-by- $L$ array. This property is used only when the SpecifyPolarizationPattern property is set to true. Phase units are in degrees.

- If the value of this property is a $Q$-by-P matrix, the same pattern is applied to all frequencies specified in the FrequencyVector property.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the FrequencyVector property.

The custom antenna object uses interpolation to estimate the response of the antenna at a given direction. To avoid interpolation errors, the custom response pattern must contain azimuth angles in the range $[-180,180]^{\circ}$ and elevation angles in the range $[-90,90]^{\circ}$.

## Dependencies

To enable this property, set the SpecifyPolarizationPattern property to true.

```
Data Types: double
```


## VerticalMagnitudePattern - Magnitude of vertical polarization component of antenna radiation pattern <br> zeros $(181,361)$ (default) | real-valued $Q$-by-P matrix | real-valued $Q$-by- $P$-by-L array

The magnitude of the vertical polarization component of the antenna radiation pattern specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array. This property is used only when the SpecifyPolarizationPattern property is set to true. Magnitude units are in dB.

- If the value of this property is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the FrequencyVector property.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the FrequencyVector property.

If the pattern contains a NaN at any azimuth and elevation direction, it is converted to - Inf, indicating zero response in that direction. The custom antenna object uses interpolation to estimate the response of the antenna at a given direction. To avoid interpolation errors, the custom response pattern must contain azimuth angles in the range $[-180,180]^{\circ}$ and elevation angles in the range [ 90, 90] ${ }^{\circ}$.

## Dependencies

To enable this property, set the SpecifyPolarizationPattern property to true.
Data Types: double

## VerticalPhasePattern - Phase of vertical polarization component of antenna radiation pattern <br> zeros $(181,361)$ (default) | real-valued $Q$-by-P matrix | real-valued $Q$-by- $P$-by-L array

The phase of the vertical polarization component of the antenna radiation pattern, specified as a $Q$ -by- $P$ matrix or a $Q$-by- $P$-by- $L$ array. This property is used only when the SpecifyPolarizationPattern property is set to true. Phase units are in degrees.

- If the value of this property is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the FrequencyVector property.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the FrequencyVector property.

The custom antenna object uses interpolation to estimate the response of the antenna at a given direction. To avoid interpolation errors, the custom response pattern must contain azimuth angles in the range $[-180,180]^{\circ}$ and elevation angles in the range $[-90,90]^{\circ}$.

## Dependencies

To enable this property, set the SpecifyPolarizationPattern property to true.
Data Types: double

## MatchArrayNormal - Match element normal to array normal

true (default) | false
Set this property to true to align the antenna element to an array normal. The antenna pattern is rotated so that the $x$-axis of the element coordinate system points along the array normal. This property is used only when the antenna element belongs to an array. Use the property in conjunction with the ArrayNormal property of the phased. URA and phased. UCA System objects. Set this property to false to use the element pattern without rotation. The default value is .

Data Types: logical

## Usage

## Syntax

RESP = antenna(FREQ,ANG)

## Description

RESP = antenna (FREQ, ANG) returns the antenna's voltage response RESP at operating frequencies specified in FREQ and directions specified in ANG. The form of RESP depends upon whether the antenna element supports polarization as determined by the SpecifyPolarizationPattern property. If SpecifyPolarizationPattern is set to false, RESP is an $M$-by- $L$ matrix containing the antenna response at the $M$ angles specified in ANG and at the $L$ frequencies specified in FREQ. If SpecifyPolarizationPattern is set to true, RESP is a MATLAB struct containing two fields, RESP.H and RESP.V, representing the antenna's response in horizontal and vertical polarization, respectively. Each field is an $M$-by- $L$ matrix containing the antenna response at the $M$ angles specified in ANG and at the $L$ frequencies specified in FREQ.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## FREQ - Operating frequency of antenna element

nonnegative scalar | nonnegative, real-valued 1-by-L row vector
Operating frequency of the antenna element, specified as a nonnegative scalar or nonnegative, realvalued 1 -by- L row vector. Frequency units are in Hz .

FREQ must lie within the range of values specified by the FrequencyRange or the FrequencyVector property of the element. Otherwise, the element produces no response and the response is returned as -Inf. Element objects use the FrequencyRange property, except for phased. CustomAntennaElement, which uses the FrequencyVector property.

Example: [1e8 2e6]
Data Types: double

## ANG - Azimuth and elevation angles of response directions

real-valued 1-by-M row vector | real-valued 2-by-M matrix
Azimuth and elevation angles of the response directions, specified as a real-valued 1-by-M row vector or a real-valued 2-by-M matrix, where $M$ is the number of angular directions. Angle units are in degrees. The azimuth angle must lie in the range $-180^{\circ}$ to $180^{\circ}$, inclusive. The elevation angle must lie in the range $-90^{\circ}$ to $90^{\circ}$, inclusive.

- If ANG is a 1 -by-M vector, each element specifies the azimuth angle of the direction. In this case, the corresponding elevation angle is assumed to be zero.
- If ANG is a 2 -by- $M$ matrix, each column of the matrix specifies the direction in the form [azimuth;elevation].

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the $x y$-plane. This angle is positive when measured from the $x$-axis toward the $y$-axis. The elevation angle is the angle between the direction vector and $x y$-plane. This angle is positive when measured toward the $z$-axis. See the definition of "Azimuth and Elevation Angles".
Example: [110 125; 15 10]
Data Types: double

## Output Arguments

## RESP - Voltage response of antenna

complex-valued $M$-by- $L$ matrix
Voltage response of antenna element, returned as a complex-valued $M$-by- $L$ matrix. In this matrix, $M$ represents the number of angles specified in ANG and $L$ represents the number of frequencies specified in FREQ.
Data Types: double

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```


## Specific to Antenna and Transducer Element System Objects

beamwidth directivity
isPolarizationCapable pattern patternAzimuth patternElevation

Compute and display beamwidth of sensor element pattern Directivity of antenna or transducer element Antenna element polarization capability
Plot antenna or transducer element directivity and patterns
Plot antenna or transducer element directivity and pattern versus azimuth Plot antenna or transducer element directivity and pattern versus elevation

## Common to All System Objects

step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object

## Examples

## Response and Directivity of Custom Antenna

Create a user-defined antenna with a cosine pattern. Then, plot an elevation cut of the antenna's power response.

The user-defined pattern is omnidirectional in the azimuth direction and has a cosine pattern in the elevation direction. Assume the antenna operates at 1 GHz . Obtain the response at $20^{\circ}$ azimuth and $30^{\circ}$ elevation.

```
fc = 1e9;
azang = -180:180;
elang = -90:90;
magpattern = mag2db(repmat(cosd(elang)',1,numel(azang)));
phasepattern = zeros(size(magpattern));
antenna = phased.CustomAntennaElement('AzimuthAngles',azang, ...
    'ElevationAngles',elang,'MagnitudePattern',magpattern, ...
    'PhasePattern',phasepattern);
resp = antenna(fc,[20;30])
resp = 0.8660
```

Plot an elevation cut of the power response.

```
pattern(antenna,fc,20,-90:90,'CoordinateSystem','polar','Type','powerdb')
```



Normalized Power (dB), Broadside at $0.00^{\circ}$
Plot an elevation cut of the directivity.
pattern(antenna,fc,20,-90:90,'CoordinateSystem','polar','Type','directivity')


Directivity (dBi), Broadside at $0.00^{\circ}$

## Antenna Radiation Pattern in U-V Coordinates

Define a custom antenna in $u-v$ space. Then, calculate and plot the response.
Define the radiation pattern (in dB ) of an antenna in terms of $u$ and $v$ coordinates within the unit circle.

```
u = -1:0.01:1;
v = -1:0.01:1;
[u_grid,v_grid] = meshgrid(u,v);
pat_uv = sqrt(1 - u_grid.^2 - v_grid.^2);
pat_uv(hypot(u_grid,v_grid) >= \overline{1})=0;
```

Create an antenna with this radiation pattern. Convert $u$-v coordinates to azimuth and elevation coordinates.

```
[pat_azel,az,el] = uv2azelpat(pat_uv,u,v);
```

array = phased.CustomAntennaElemeñt('AzimuthAngles',az,'ElevationAngles',el, ...
'MagnitudePattern', mag2db(pat_azel), 'PhasePattern', 45*ones(size(pat_azel)));

Calculate the response in the direction $u=0.5, v=0$. Assume the antenna operates at 1 GHz . The output of the step method is in linear units.

```
dir_uv = [0.5;0];
dir_azel = uv2azel(dir_uv);
```

```
fc = 1e9;
resp = array(fc,dir_azel)
resp = 0.6124 + 0.6124i
```

Plot the 3D response in $u-v$ coordinates.

```
pattern(array,fc,[-1:.01:1],[-1:.01:1],'CoordinateSystem','uv','Type','powerdb')
```



Display the antenna response as a line plot in $u-v$ coordinates.
pattern(array,fc,[-1:.01:1],0,'CoordinateSystem','uv','Type',' powerdb')


## Polarized Antenna Radiation Patterns

Model a short dipole antenna oriented along the $x$-axis of the local antenna coordinate system. For this type of antenna, the horizontal and vertical components of the electric field are given by $E_{H}=\frac{j \omega \mu I L}{4 \pi r} \sin (\mathrm{az})$ and $E_{V}=-\frac{j \omega \mu I L}{4 \pi r} \sin (\mathrm{el}) \cos (\mathrm{az})$.

Specify a normalized radiation pattern of a short dipole antenna terms of azimuth, $a z$, and elevation, el, coordinates. The vertical and horizontal radiation patterns are normalized to a maximum of unity.

```
az = [-180:180];
el = [-90:90];
[az_grid,el_grid] = meshgrid(az,el);
horz_pat_azel = ...
    mag2\overline{db}(abs(sind(az_grid)));
vert_pat_azel = ...
    mag2db(abs(sind(el_grid).*cosd(az_grid)));
```

Set up the antenna. Specify the SpecifyPolarizationPattern property to produce polarized radiation. In addition, use the HorizontalMagnitudePattern and VerticalMagnitudePattern properties to specify the pattern magnitude values. The HorizontalPhasePattern and VerticalPhasePattern properties take default values of zero.
antenna $=$ phased.CustomAntennaElement(...
'AzimuthAngles',az,'ElevationAngles',el,...
'SpecifyPolarizationPattern',true,...
'HorizontalMagnitudePattern',horz_pat_azel,...
'VerticalMagnitudePattern', vert_pat_azel);
Assume the antenna operates at 1 GHz .
fc = 1e9;
Display the vertical response pattern.
pattern(antenna,fc,[-180:180],[-90:90],...
'CoordinateSystem','polar',...
'Type', 'powerdb', ..
'Polarization','V')


Display the horizontal response pattern.
pattern(antenna,fc,[-180:180], [-90:90],...
'CoordinateSystem','polar',...
'Type', 'powerdb',..
'Polarization','H')


The combined polarization response, shown below, illustrates the $x$-axis null of the dipole.

```
pattern(antenna,fc,[-180:180],[-90:90],...
```

'CoordinateSystem', 'polar',...
'Type', 'powerdb',...
'Polarization', 'combined')


## Match Custom Antenna Normal to Array Normal

Define a custom antenna in $u-v$ space. Show how the array response pattern is affected by the choice of the MatchArrayNormal property of the phased.CustomAntennaElement.

Define the response pattern (in dB ) of an antenna as a function of $u$ and $v$ coordinates within the unit circle. The antenna operates at 1 GHz .

```
fc = 1e9;
c = physconst('LightSpeed');
u = -1:0.01:1;
v = -1:0.01:1;
[u_grid,v_grid] = meshgrid(u,v);
pat_uv = sqrt(1 - u_grid.^2 - v_grid.^2);
pat_uv(hypot(u_grid,v_grid) >= 1) = 0;
```

Create a custom antenna with this pattern. Convert $u-v$ coordinates to azimuth and elevation coordinates. Set MatchArrayNormal to false.

```
[pat_azel,az,el] = uv2azelpat(pat_uv,u,v);
antenna = phased.CustomAntennaElement('AzimuthAngles',az,'ElevationAngles',el, ...
    'MagnitudePattern',mag2db(pat_azel),'PhasePattern',45*ones(size(pat_azel)), ...
    "MatchArrayNormal",false);
```

Construct a 3-by-3 URA with this element and display the antenna pattern in 3-D polar coordinates. The element spacing is one-half wavelength. The array normal points along the $y$-axis.

```
lam = c/fc;
array = phased.URA('Element',antenna,'Size',[3 3],'ElementSpacing', ...
    [lam/2 lam/2],'ArrayNormal','y');
pattern(array,fc,-180:180,-90:90,'PropagationSpeed',c, ...
    'CoordinateSystem','polar','Type','powerdb','Normalize',true)
```



The pattern shows the interplay between the element pattern pointing along the $x$-axis and the array pattern pointing along the $y$-axis.

Create another custom antenna with the same radiation pattern. Set MatchArrayNormal to true. Then create another array with this element.

```
antenna2 = phased.CustomAntennaElement('AzimuthAngles',az,'ElevationAngles',el, ...
    'MagnitudePattern',mag2db(pat_azel),'PhasePattern',45*ones(size(pat_azel)), ...
    "MatchArrayNormal",true);
array2 = phased.URA('Element',antenna2,'Size',[3 3],'ElementSpacing', ...
    [lam/2 lam/2],'ArrayNormal','y');
pattern(array2,fc,-180:180,-90:90,'PropagationSpeed',c, ...
    'CoordinateSystem','polar','Type','powerdb','Normalize',true)
```



This pattern shows the aligned element and array patterns pointing along the $y$-axis.

## Custom Antenna Element Response at $30^{\circ}$ Elevation

Construct a user-defined antenna with an omnidirectional response in azimuth and a cosine pattern in elevation. The antenna operates at 1 GHz . Plot the response pattern. Then, find the antenna response at $30^{\circ}$.

```
antenna = phased.CustomAntennaElement;
antenna.AzimuthAngles = -180:180;
antenna.ElevationAngles = -90:90;
antenna.MagnitudePattern = mag2db(repmat(cosd(antenna.ElevationAngles)',...
    1, numel(antenna.AzimuthAngles)));
```

Find the response at $30^{\circ}$ elevation for an operating frequency of 1 GHz .

```
fc = 1.0e9;
resp = antenna(fc,[0;30])
resp = 0.8660
```


## Antenna with Custom Radiation Pattern

Create a custom antenna element object. The radiation pattern has a cosine dependence on elevation angle but is independent of azimuth angle.

```
az = -180:90:180;
el = -90:45:90;
elresp = cosd(el);
magpattern = mag2db(repmat(elresp',1,numel(az)));
phasepattern = zeros(size(magpattern));
antenna = phased.CustomAntennaElement('AzimuthAngles',az,...
    'ElevationAngles',el,'MagnitudePattern',magpattern, ...
    'PhasePattern',phasepattern);
```

Display the radiation pattern.

| disp(antenna.MagnitudePattern) |  |  |  |  |
| ---: | ---: | ---: | ---: | ---: |
| -Inf | - Inf | - Inf | - Inf | - Inf |
| -3.0103 | -3.0103 | -3.0103 | -3.0103 | -3.0103 |
| 0 | 0 | 0 | 0 | 0 |
| -3.0103 | -3.0103 | -3.0103 | -3.0103 | -3.0103 |
| - Inf | - Inf | - Inf | -Inf | - Inf |

Calculate the antenna response at the azimuth-elevation pairs $(-30,0)$ and $(-45,0)$ at 500 MHz .

```
ang = [-30 0; -45 0];
resp = antenna(500.0e6,ang);
disp(resp)
    0.7071
    1.0000
```

The following code illustrates how nearest-neighbor interpolation is used to find the antenna voltage response in the two directions. The total response is the product of the angular response and the frequency response.

```
g = interp2(deg2rad(antenna.AzimuthAngles),...
    deg2rad(antenna.ElevationAngles),...
    db2mag(antenna.MagnitudePattern),...
    deg2rad(ang(1,:))', deg2rad(ang(2,:))','nearest',0);
h = interp1(antenna.FrequencyVector,...
    db2mag(antenna.FrequencyResponse),500e6,'nearest',0);
antresp = h.*g;
```

Compare the value of antresp to the response of the antenna.
disp(mag2db(antresp))
$-3.0103$
0

## Directivity of Custom Antenna

Compute the directivity of a custom antenna element.

Define an antenna pattern for a custom antenna element in azimuth-elevation space. The pattern is omnidirectional in the azimuth direction and has a cosine pattern in the elevation direction. Assume the antenna operates at 1 GHz . Get the response at zero degrees azimuth and from -30 to 30 degrees elevation.

```
fc = 1e9;
azang = [-180:180];
elang = [-90:90];
magpattern = mag2db(repmat(cosd(elang)',1,numel(azang)));
phasepattern = zeros(size(magpattern));
antenna = phased.CustomAntennaElement('AzimuthAngles',azang, ...
    'ElevationAngles',elang,'MagnitudePattern',magpattern, ...
    'PhasePattern',phasepattern);
```

Calculate the directivities as a function of elevation for $0^{\circ}$ azimuth angle.

```
angs = [0,0,0,0,0,0,0;-30,-20,-10,0,10,20,30];
freq = le9;
d = directivity(antenna,freq,angs)
d = 7x1
    0.5115
    1.2206
    1.6279
    1.7609
    1.6279
    1.2206
    0.5115
```

The directivity is maximum at $0^{\circ}$ elevation.

## Custom Antenna Element Supports Polarization

Show that the CustomAntennaElement antenna element supports polarization when the SpecifyPolarizationPattern property is set to true.

```
antenna = phased.CustomAntennaElement('SpecifyPolarizationPattern',true);
isPolarizationCapable(antenna)
ans = logical
    1
```

The returned value 1 shows that this antenna element supports polarization.

## Power and Directivity Patterns of Custom Antenna

Create a custom antenna with a cosine pattern. Show the response at boresight. Then, plot the antenna's field and directivity patterns.

Create the antenna and calculate the response. The user-defined pattern is omnidirectional in the azimuth direction and has a cosine pattern in the elevation direction. Assume the antenna works at 1 GHz.

```
fc = 1e9;
antenna = phased.CustomAntennaElement;
antenna.AzimuthAngles = -180:180;
antenna.ElevationAngles = -90:90;
antenna.MagnitudePattern = mag2db(repmat(cosd(antenna.ElevationAngles)', ...
    1, numel(antenna.AzimuthAngles)));
resp = antenna(fc,[0;0])
resp = 1
```

Plot an elevation cut of the magnitude response as a line plot.
pattern(antenna,fc,0,[-90:90],'CoordinateSystem','rectangular', ...
'Type', 'efield')


Plot an elevation cut of the directivity as a line plot, showing that the maximum directivity is approximately 2 dB .

```
pattern(antenna,fc,0,[-90:90],'CoordinateSystem','rectangular', ...
    'Type','directivity')
```



## Pattern of Custom Antenna over Selected Range of Angles

Create a custom antenna System object ${ }^{\mathrm{TM}}$. The user-defined pattern is omnidirectional in the azimuth direction and has a cosine pattern in the elevation direction. Assume the antenna operates at a frequency of 1 GHz . First show the response at boresight. Display the 3-D pattern for a 60 degree range of azimuth and elevation angles centered at 0 degrees azimuth and 0 degrees elevation in 0.1 degree increments.

```
fc = 1e9;
azang = -180:180;
elang = -90:90;
magpattern = mag2db(repmat(cosd(elang)',1,numel(azang)));
antenna = phased.CustomAntennaElement('AzimuthAngles',azang, ...
    'ElevationAngles',elang,'MagnitudePattern',magpattern);
resp = antenna(fc,[0;0])
resp = 1
```

Plot the power pattern for a range of angles.
pattern(antenna,fc,[-30:0.1:30],[-30:0.1:30],'CoordinateSystem','polar', ...
'Type','power')


## Reduced Azimuth Pattern of Custom Antenna Element

Create an antenna with a custom response. The user-defined pattern has a sine pattern in the azimuth direction and a cosine pattern in the elevation direction. Assume the antenna operates at a frequency of 500 MHz . Plot an azimuth cut of the power pattern of the custom antenna element at 0 and 30 degrees elevation. Assume the operating frequency is 500 MHz .

Create the antenna element.

```
fc = 500e6;
```

antenna $=$ phased.CustomAntennaElement;
antenna.AzimuthAngles $=-180: 180$;
antenna.ElevationAngles = -90:90;
antenna.MagnitudePattern = mag2db(abs(cosd(antenna.ElevationAngles)'*sind(antenna.AzimuthAngles)
patternAzimuth(antenna,fc,[0 30],'Type','powerdb')


Power (dB), Broadside at $0.00^{\circ}$

Plot a reduced range of azimuth angles using the Azimuth parameter.
patternAzimuth(antenna,fc,[0 30],'Azimuth',[-45:45],'Type','powerdb')


Power (dB), Broadside at $0.00^{\circ}$

## Reduced Elevation Pattern of Custom Antenna Element

Create an antenna with a custom response. The user-defined pattern has a sine pattern in the azimuth direction and a cosine pattern in the elevation direction. Assume the antenna operates at a frequency of 500 MHz . Plot an elevation cut of the power of the custom antenna element at 0 and 30 degrees elevation. Assume the operating frequency is 500 MHz .

Create the antenna element.
fc = 500e6;
antenna $=$ phased.CustomAntennaElement;
antenna.AzimuthAngles $=-180: 180$;
antenna.ElevationAngles = -90:90;
antenna.MagnitudePattern = mag2db(abs(cosd(antenna.ElevationAngles)'*sind(antenna.AzimuthAngles) patternElevation(antenna,fc,[0 30],'Type','powerdb')


Power (dB), Broadside at $0.00^{\circ}$

Plot a reduced range of elevation angles using the Azimuth parameter.
patternElevation(antenna,fc,[0 30],'Elevation',[-45:45],'Type','powerdb')


Power (dB), Broadside at $0.00^{\circ}$

## Algorithms

The total response of a custom antenna element is a combination of its frequency response and spatial response. phased. CustomAntennaElement calculates both responses using nearest neighbor interpolation, and then multiplies the responses to form the total response.

## Version History

Introduced in R2011a

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder ${ }^{\mathrm{TM}}$.
Usage notes and limitations:

- pattern, patternAzimuth, patternElevation, and plotResponse methods are not supported.
- See "System Objects in MATLAB Code Generation" (MATLAB Coder).


## See Also

phased. ConformalArray | phased.CrossedDipoleAntennaElement | phased.CosineAntennaElement | phased.IsotropicAntennaElement | phased. ShortDipoleAntennaElement | phased.ULA | phased.URA | uv2azelpat | phitheta2azelpat|uv2azel| phitheta2azel

## directivity

System object: phased. CustomAntennaElement
Package: phased
Directivity of custom antenna element

## Syntax

D = directivity (H,FREQ,ANGLE)

## Description

D = directivity (H, FREQ,ANGLE) returns the "Directivity" on page 1-295 of a custom antenna element, $H$, at frequencies specified by FREQ and in direction angles specified by ANGLE.

## Input Arguments

## H - Custom antenna element

System object
Custom antenna element specified as a phased.CustomAntennaElement System object.
Example: H = phased.CustomAntennaElement;

## FREQ - Frequency for computing directivity and patterns

positive scalar | 1-by-L real-valued row vector
Frequencies for computing directivity and patterns, specified as a positive scalar or 1-by-L realvalued row vector. Frequency units are in hertz.

- For an antenna, microphone, or sonar hydrophone or projector element, FREQ must lie within the range of values specified by the FrequencyRange or FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased. CustomAntennaElement and phased.CustomMic rophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.


## Example: [1e8 2e6]

Data Types: double

## ANGLE - Angles for computing directivity

1-by-M real-valued row vector | 2 -by- $M$ real-valued matrix
Angles for computing directivity, specified as a 1-by- $M$ real-valued row vector or a 2 -by- $M$ real-valued matrix, where $M$ is the number of angular directions. Angle units are in degrees. If ANGLE is a 2 -by- $M$ matrix, then each column specifies a direction in azimuth and elevation, [az;el]. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

If ANGLE is a 1 -by- $M$ vector, then each entry represents an azimuth angle, with the elevation angle assumed to be zero.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the xy plane. This angle is positive when measured from the $x$-axis toward the $y$-axis. The elevation angle is the angle between the direction vector and $x y$ plane. This angle is positive when measured towards the $z$-axis. See "Azimuth and Elevation Angles".

Example: [45 60; 0 10]
Data Types: double

## Output Arguments

## D - Directivity

M-by-L matrix
Directivity, returned as an $M$-by- $L$ matrix. Each row corresponds to one of the $M$ angles specified by ANGLE. Each column corresponds to one of the $L$ frequency values specified in FREQ. Directivity units are in dBi where dBi is defined as the gain of an element relative to an isotropic radiator.

## Examples

## Directivity of Custom Antenna

Compute the directivity of a custom antenna element.
Define an antenna pattern for a custom antenna element in azimuth-elevation space. The pattern is omnidirectional in the azimuth direction and has a cosine pattern in the elevation direction. Assume the antenna operates at 1 GHz . Get the response at zero degrees azimuth and from -30 to 30 degrees elevation.

```
fc = 1e9;
azang = [-180:180];
elang = [-90:90];
magpattern = mag2db(repmat(cosd(elang)',1,numel(azang)));
phasepattern = zeros(size(magpattern));
antenna = phased.CustomAntennaElement('AzimuthAngles',azang, ...
    'ElevationAngles',elang,'MagnitudePattern',magpattern, ...
    'PhasePattern',phasepattern);
```

Calculate the directivities as a function of elevation for $0^{\circ}$ azimuth angle.

```
angs = [0,0,0,0,0,0,0;-30,-20,-10,0,10,20,30];
freq = le9;
d = directivity(antenna,freq,angs)
d = 7\times1
    0.5115
    1.2206
    1.6279
    1.7609
    1.6279
    1.2206
```

0.5115

The directivity is maximum at $0^{\circ}$ elevation.

## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\mathrm{total}}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

See Also<br>pattern | patternElevation | patternAzimuth

## isPolarizationCapable

System object: phased. CustomAntennaElement
Package: phased
Polarization capability

## Syntax

flag = isPolarizationCapable(antenna)

## Description

flag = isPolarizationCapable(antenna) returns a Boolean value, flag, indicating whether the phased. CustomAntennaElement System object supports polarization. An antenna element supports polarization if it can create or respond to polarized fields. This antenna object supports both polarized and nonpolarized fields.

## Input Arguments

## antenna - Custom antenna element

phased.CustomAntennaElement System object
Custom antenna element, specified as a phased.CustomAntennaElement System object.

## Output Arguments

## flag - Polarization-capability flag

Polarization-capability returned as a Boolean value true if the antenna element supports polarization or false if it does not. The returned value depends upon the value of the SpecifyPolarizationPattern property. If SpecifyPolarizationPattern is true, then flag is true. Otherwise it is false.

## Examples

## Custom Antenna Element Supports Polarization

Show that the CustomAntennaElement antenna element supports polarization when the SpecifyPolarizationPattern property is set to true.

```
antenna = phased.CustomAntennaElement('SpecifyPolarizationPattern',true);
isPolarizationCapable(antenna)
ans = logical
    1
```

The returned value 1 shows that this antenna element supports polarization.

## pattern

System object: phased. CustomAntennaElement
Package: phased
Plot custom antenna element directivity and patterns

## Syntax

```
pattern(sElem,FREQ)
pattern(sElem,FREQ,AZ)
pattern(sElem,FREQ,AZ,EL)
pattern(
    ,Name,Value)
[PAT,AZ_ANG,EL_ANG] = pattern(
```

$\qquad$

``` )
```


## Description

pattern (sElem, FREQ) plots the 3-D array directivity pattern (in dBi) for the element specified in $s E l e m$. The operating frequency is specified in FREQ.
pattern(sElem, FREQ, AZ) plots the element directivity pattern at the specified azimuth angle.
pattern(sElem, FREQ,AZ,EL) plots the element directivity pattern at specified azimuth and elevation angles.
pattern(__,Name,Value) plots the element pattern with additional options specified by one or more Name, Value pair arguments.
[PAT,AZ_ANG,EL_ANG] = pattern( $\qquad$ ) returns the element pattern in PAT. The AZ_ANG output contains the coordinate values corresponding to the rows of PAT. The EL_ANG output contains the coordinate values corresponding to the columns of PAT. If the 'CoordinateSystem' parameter is set to ' $u v$ ' , then AZ_ANG contains the $U$ coordinates of the pattern and EL_ANG contains the $V$ coordinates of the pattern. Otherwise, they are in angular units in degrees. $U V$ units are dimensionless.

Note This method replaces the plotResponse method. See "Convert plotResponse to pattern" on page 1-305 for guidelines on how to use pattern in place of plotResponse.

## Input Arguments

## sElem - Custom antenna element

System object
Custom antenna element, specified as a phased.CustomAntennaElement System object.
Example: sElem = phased.CustomAntennaElement;
FREQ - Frequency for computing directivity and patterns
positive scalar | 1-by-L real-valued row vector

Frequencies for computing directivity and patterns, specified as a positive scalar or 1-by-L realvalued row vector. Frequency units are in hertz.

- For an antenna, microphone, or sonar hydrophone or projector element, FREQ must lie within the range of values specified by the FrequencyRange or FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased. CustomAntennaElement and phased. CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: [1e8 2e6]
Data Types: double

## AZ - Azimuth angles

[-180:180] (default) | 1-by- $N$ real-valued row vector
Azimuth angles for computing directivity and pattern, specified as a $1-b y-N$ real-valued row vector where $N$ is the number of azimuth angles. Angle units are in degrees. Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the xy plane. When measured from the $x$-axis toward the $y$-axis, this angle is positive.

## Example: [-45:2:45]

Data Types: double

## EL - Elevation angles

[-90:90] (default) | 1-by-M real-valued row vector
Elevation angles for computing directivity and pattern, specified as a 1-by- $M$ real-valued row vector where $M$ is the number of desired elevation directions. Angle units are in degrees. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

The elevation angle is the angle between the direction vector and $x y$-plane. The elevation angle is positive when measured towards the $z$-axis.
Example: [-75:1:70]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## CoordinateSystem - Plotting coordinate system

'polar' (default)|'rectangular'|'uv'
Plotting coordinate system of the pattern, specified as the comma-separated pair consisting of
'CoordinateSystem' and one of 'polar', 'rectangular', or 'uv'. When
'CoordinateSystem' is set to 'polar' or 'rectangular', the AZ and EL arguments specify the
pattern azimuth and elevation, respectively. AZ values must lie between $-180^{\circ}$ and $180^{\circ}$. EL values must lie between $-90^{\circ}$ and $90^{\circ}$. If 'CoordinateSystem' is set to 'uv', AZ and EL then specify $U$ and $V$ coordinates, respectively. AZ and EL must lie between -1 and 1.
Example: 'uv'
Data Types: char

## Type - Displayed pattern type

'directivity' (default) |'efield'|'power'|'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type ' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb ' - power pattern converted to dB.

Example: 'powerdb'
Data Types: char

## Normalize - Display normalize pattern

true (default) | false
Display normalized pattern, specified as the comma-separated pair consisting of 'Normalize' and a Boolean. Set this parameter to true to display a normalized pattern. This parameter does not apply when you set 'Type' to 'directivity'. Directivity patterns are already normalized.
Data Types: logical

## PlotStyle - Plotting style

'overlay' (default)|'waterfall'
Plotting style, specified as the comma-separated pair consisting of 'Plotstyle' and either ' overlay' or 'waterfall'. This parameter applies when you specify multiple frequencies in FREQ in 2-D plots. You can draw 2-D plots by setting one of the arguments AZ or EL to a scalar.

## Data Types: char

## Polarization - Polarized field component

'combined' (default)| 'H' | 'V'
Polarized field component to display, specified as the comma-separated pair consisting of 'Polarization' and 'combined ', 'H' , or 'V'. This parameter applies only when the sensors are polarization-capable and when the 'Type' parameter is not set to 'directivity'. This table shows the meaning of the display options.

| ' Polarization ' | Display |
| :--- | :--- |
| ' combined ' | Combined $H$ and $V$ polarization components |
| ' $\mathrm{H}^{\prime}$ | $H$ polarization component |
| ' $\mathrm{V}^{\prime}$ | $V$ polarization component |

Example: 'V'

## Output Arguments

PAT - Element pattern<br>$N$-by-M real-valued matrix

Element pattern, returned as an $N$-by- $M$ real-valued matrix. The pattern is a function of azimuth and elevation. The rows of PAT correspond to the azimuth angles in the vector specified by EL_ANG. The columns correspond to the elevation angles in the vector specified by AZ_ANG.

## AZ_ANG - Azimuth angles

scalar | 1-by-N real-valued row vector
Azimuth angles for displaying directivity or response pattern, returned as a scalar or 1-by-N realvalued row vector corresponding to the dimension set in AZ. The columns of PAT correspond to the values in AZ_ANG. Units are in degrees.

## EL_ANG - Elevation angles

scalar | 1-by-M real-valued row vector
Elevation angles for displaying directivity or response, returned as a scalar or 1-by-M real-valued row vector corresponding to the dimension set in EL. The rows of PAT correspond to the values in EL_ANG. Units are in degrees.

## Examples

## Power and Directivity Patterns of Custom Antenna

Create a custom antenna with a cosine pattern. Show the response at boresight. Then, plot the antenna's field and directivity patterns.

Create the antenna and calculate the response. The user-defined pattern is omnidirectional in the azimuth direction and has a cosine pattern in the elevation direction. Assume the antenna works at 1 GHz.

```
fc = 1e9;
antenna = phased.CustomAntennaElement;
antenna.AzimuthAngles = -180:180;
antenna.ElevationAngles = -90:90;
antenna.MagnitudePattern = mag2db(repmat(cosd(antenna.ElevationAngles)', ...
    1,numel(antenna.AzimuthAngles)));
resp = antenna(fc,[0;0])
resp = 1
```

Plot an elevation cut of the magnitude response as a line plot.

```
pattern(antenna,fc,0,[-90:90],'CoordinateSystem','rectangular', ...
    'Type','efield')
```



Plot an elevation cut of the directivity as a line plot, showing that the maximum directivity is approximately 2 dB .
pattern(antenna,fc,0,[-90:90],'CoordinateSystem','rectangular', ...
'Type','directivity')


## Pattern of Custom Antenna over Selected Range of Angles

Create a custom antenna System object ${ }^{\mathrm{TM}}$. The user-defined pattern is omnidirectional in the azimuth direction and has a cosine pattern in the elevation direction. Assume the antenna operates at a frequency of 1 GHz . First show the response at boresight. Display the 3-D pattern for a 60 degree range of azimuth and elevation angles centered at 0 degrees azimuth and 0 degrees elevation in 0.1 degree increments.

```
fc = 1e9;
azang = -180:180;
elang = -90:90;
magpattern = mag2db(repmat(cosd(elang)',1,numel(azang)));
antenna = phased.CustomAntennaElement('AzimuthAngles',azang, ...
    'ElevationAngles',elang,'MagnitudePattern',magpattern);
resp = antenna(fc,[0;0])
resp = 1
```

Plot the power pattern for a range of angles.

```
pattern(antenna,fc,[-30:0.1:30],[-30:0.1:30],'CoordinateSystem','polar', ...
    'Type','power')
```



## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \Pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\mathrm{total}}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Convert plotResponse to pattern

For antenna, microphone, and array System objects, the pattern method replaces the plotResponse method. In addition, two new simplified methods exist just to draw 2-D azimuth and elevation pattern plots. These methods are azimuthPattern and elevationPattern.

The following table is a guide for converting your code from using plotResponse to pattern. Notice that some of the inputs have changed from input arguments to Name-Value pairs and conversely. The general pattern method syntax is
pattern(H,FREQ,AZ,EL, 'Name1', 'Value1',...,' NameN', 'ValueN')

| plotResponse Inputs | plotResponse Description | pattern Inputs |
| :--- | :--- | :--- |
| H argument | Antenna, microphone, or array <br> System object. | H argument (no change) |
| FREQ argument | Operating frequency. | FREQ argument (no change) |
| V argument | Propagation speed. This argument <br> is used only for arrays. | 'PropagationSpeed ' name-value <br> pair. This parameter is only used for <br> arrays. |


| plotResponse Inputs | plotResponse Description |  | pattern Inputs |  |
| :---: | :---: | :---: | :---: | :---: |
| 'Format' and 'RespCut' namevalue pairs | These options work together to let you create a plot in angle space (line or polar style) or $U V$ space. They also determine whether the plot is 2-D or 3-D. This table shows you how to create different types of plots using plotResponse. |  | 'CoordinateSystem' name-value pair used together with the AZ and EL input arguments. <br> 'CoordinateSystem' has the same options as the plotResponse method 'Format ' name-value pair, except that 'line' is now named 'rectangular'. The table shows how to create different types of plots using pattern. |  |
|  | Display space |  |  |  |
|  | Angle space (2D) |  |  |  |
|  |  | Set 'RespCut'to 'Az' or'El'. Set'Format' to'line' or'polar'.Set the displayaxis using eitherthe'AzimuthAngleS' or'ElevationAngles' name-value pairs. | Display space |  |
|  |  |  | Angle space (2D) <br> Angle space (3D) | Set <br> 'Coordinate <br> System' to rectangular' or 'polar'. <br> Specify either AZ or EL as a scalar. |
|  |  |  |  | Set <br> 'Coordinate <br> System' to 'rectangular' |
|  | Angle space (3D) | Set 'RespCut' to '3D'. Set 'Format' to ' line' or 'polar'. <br> Set the display axis using both the 'AzimuthAngle ${ }^{\prime}$ and 'Elevation Angles ' namevalue pairs. |  | or 'polar'. <br> Specify both AZ and EL as vectors. |
|  |  |  | UV space (2D) | Set <br> 'Coordinate <br> System' to 'uv'. Use AZ to specify a $U$ space vector. Use EL to specify a $V$-space scalar. |
|  |  |  | UV space (3D) | Set |
|  | UV space (2D) | Set 'RespCut' to'U'. Set 'Format' to 'UV '. Set the display range using the 'UGrid' namevalue pair. |  | System' to 'uv'. Use AZ to specify a $U$ space vector. <br> Use EL to specify a $V$-space vector. |
|  |  |  | If you set CoordinateSystem to 'uv', enter the UV grid values using AZ and EL . |  |
|  | UV space (3D) | $\begin{aligned} & \text { Set 'RespCut' } \\ & \text { to'3D'. Set } \\ & \text { 'Format' to } \end{aligned}$ |  |  |



| plotResponse Inputs | plotResponse Description | pattern Inputs |
| :--- | :--- | :--- |
| 'ElevationAngles ' name-value <br> pair | Elevation angles used to display the <br> antenna or array response. | EL argument |
| 'UGrid' name-value pair | Contains $U$ coordinates in $U V$ - <br> space. | AZ argument when <br> 'CoordinateSystem ' name-value <br> pair is set to ' uv ' |
| 'VGrid' name-value pair | Contains V-coordinates in $U V$-space. | EL argument when <br> 'CoordinateSystem ' name-value <br> pair is set to 'uv ' |

## Version History <br> Introduced in R2015a

See Also<br>patternElevation|patternAzimuth

## patternAzimuth

System object: phased. CustomAntennaElement
Package: phased
Plot custom antenna element directivity or pattern versus azimuth

## Syntax

```
patternAzimuth(sElem,FREQ)
patternAzimuth(sElem,FREQ,EL)
patternAzimuth(sElem,FREQ,EL,Name,Value)
PAT = patternAzimuth(
```

$\qquad$

## Description

patternAzimuth (sElem, FREQ) plots the 2-D element directivity pattern versus azimuth (in dBi) for the element sElem at zero degrees elevation angle. The argument FREQ specifies the operating frequency.
patternAzimuth(sElem, FREQ,EL), in addition, plots the 2-D element directivity pattern versus azimuth (in dBi ) at the elevation angle specified by EL . When EL is a vector, multiple overlaid plots are created.
patternAzimuth(sElem, FREQ,EL,Name, Value) plots the element pattern with additional options specified by one or more Name, Value pair arguments.

PAT = patternAzimuth( $\qquad$ ) returns the element pattern. PAT is a matrix whose entries represent the pattern at corresponding sampling points specified by the 'Azimuth' parameter and the EL input argument.

## Input Arguments

## sElem - Custom antenna element

System object
Custom antenna element, specified as a phased.CustomAntennaElement System object.
Example: sElem $=$ phased.CustomAntennaElement;

## FREQ - Frequency for computing directivity and pattern

positive scalar
Frequency for computing directivity and pattern, specified as a positive scalar. Frequency units are in hertz.

- For an antenna or microphone element, FREQ must lie within the range of values specified by the FrequencyRange or the FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased. CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: 1e8
Data Types: double

## EL - Elevation angles

## 1-by- $N$ real-valued row vector

Elevation angles for computing sensor or array directivities and patterns, specified as a 1-by- $N$ realvalued row vector. The quantity $N$ is the number of requested elevation directions. Angle units are in degrees. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

The elevation angle is the angle between the direction vector and the xy plane. When measured toward the $z$-axis, this angle is positive.
Example: [0, 10, 20]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Type - Displayed pattern type

'directivity' (default) | 'efield' | 'power' | 'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power ' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb ' - power pattern converted to dB.

Example: 'powerdb'
Data Types: char

## Azimuth - Azimuth angles

[-180:180] (default) | 1-by-P real-valued row vector
Azimuth angles, specified as the comma-separated pair consisting of 'Azimuth' and a 1-by-P realvalued row vector. Azimuth angles define where the array pattern is calculated.
Example: 'Azimuth', [-90:2:90]
Data Types: double

## Output Arguments

## PAT - Element directivity or pattern

$P$-by- $N$ real-valued matrix
Element directivity or pattern, returned as an $P$-by- $N$ real-valued matrix. The dimension $P$ is the number of azimuth values determined by the 'Azimuth' name-value pair argument. The dimension $N$ is the number of elevation angles, as determined by the EL input argument.

## Examples

## Reduced Azimuth Pattern of Custom Antenna Element

Create an antenna with a custom response. The user-defined pattern has a sine pattern in the azimuth direction and a cosine pattern in the elevation direction. Assume the antenna operates at a frequency of 500 MHz . Plot an azimuth cut of the power pattern of the custom antenna element at 0 and 30 degrees elevation. Assume the operating frequency is 500 MHz .

Create the antenna element.

```
fc = 500e6;
antenna = phased.CustomAntennaElement;
antenna.AzimuthAngles = -180:180;
antenna.ElevationAngles = -90:90;
antenna.MagnitudePattern = mag2db(abs(cosd(antenna.ElevationAngles)'*sind(antenna.AzimuthAngles)
patternAzimuth(antenna,fc,[0 30],'Type','powerdb')
```



Power (dB), Broadside at $0.00^{\circ}$

Plot a reduced range of azimuth angles using the Azimuth parameter.
patternAzimuth(antenna,fc,[0 30],'Azimuth',[-45:45],'Type','powerdb')


Power (dB), Broadside at $0.00^{\circ}$

## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Version History Introduced in R2015a

See Also<br>pattern| patternElevation

## patternElevation

System object: phased. CustomAntennaElement
Package: phased
Plot custom antenna element directivity or pattern versus elevation

## Syntax

```
patternElevation(sElem,FREQ)
patternElevation(sElem,FREQ,AZ)
patternElevation(sElem,FREQ,AZ,Name,Value)
PAT = patternElevation(
```

$\qquad$

``` )
```


## Description

patternElevation(sElem, FREQ) plots the 2-D element directivity pattern versus elevation (in dBi) for the element sElem at zero degrees azimuth angle. The argument FREQ specifies the operating frequency.
patternElevation(sElem,FREQ,AZ), in addition, plots the 2-D element directivity pattern versus elevation (in dBi ) at the azimuth angle specified by $A Z$. When $A Z$ is a vector, multiple overlaid plots are created.
patternElevation(sElem,FREQ,AZ,Name, Value) plots the element pattern with additional options specified by one or more Name, Value pair arguments.

PAT = patternElevation( $\qquad$ ) returns the element pattern. PAT is a matrix whose entries represent the pattern at corresponding sampling points specified by the 'Elevation' parameter and the AZ input argument.

## Input Arguments

## sElem - Custom antenna element

System object
Custom antenna element, specified as a phased.CustomAntennaElement System object.
Example: sElem = phased.CustomAntennaElement;

## FREQ - Frequency for computing directivity and pattern

positive scalar
Frequency for computing directivity and pattern, specified as a positive scalar. Frequency units are in hertz.

- For an antenna or microphone element, FREQ must lie within the range of values specified by the FrequencyRange or the FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased. CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: 1e8
Data Types: double

## AZ - Azimuth angles for computing directivity and pattern

1-by- $N$ real-valued row vector
Azimuth angles for computing sensor or array directivities and patterns, specified as a 1-by- N realvalued row vector where $N$ is the number of desired azimuth directions. Angle units are in degrees. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the xy plane. This angle is positive when measured from the $x$-axis toward the $y$-axis.
Example: [0, 10, 20]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Type - Displayed pattern type

'directivity' (default) | 'efield' | 'power' | 'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power ' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb ' - power pattern converted to dB.

Example: 'powerdb'
Data Types: char

## Elevation - Elevation angles

[-90:90] (default)| 1-by-P real-valued row vector
Elevation angles, specified as the comma-separated pair consisting of 'Elevation' and a 1-by-P real-valued row vector. Elevation angles define where the array pattern is calculated.
Example: 'Elevation', [-90:2:90]
Data Types: double

## Output Arguments

## PAT - Element directivity or pattern

$P$-by- $N$ real-valued matrix
Element directivity or pattern, returned as an $P$-by- $N$ real-valued matrix. The dimension $P$ is the number of elevation angles determined by the 'Elevation' name-value pair argument. The dimension $N$ is the number of azimuth angles determined by the AZ argument.

## Examples

## Reduced Elevation Pattern of Custom Antenna Element

Create an antenna with a custom response. The user-defined pattern has a sine pattern in the azimuth direction and a cosine pattern in the elevation direction. Assume the antenna operates at a frequency of 500 MHz . Plot an elevation cut of the power of the custom antenna element at 0 and 30 degrees elevation. Assume the operating frequency is 500 MHz .

Create the antenna element.

```
fc = 500e6;
antenna = phased.CustomAntennaElement;
antenna.AzimuthAngles = -180:180;
antenna.ElevationAngles = -90:90;
antenna.MagnitudePattern = mag2db(abs(cosd(antenna.ElevationAngles)'*sind(antenna.AzimuthAngles)
patternElevation(antenna,fc,[0 30],'Type','powerdb')
```



Power (dB), Broadside at $0.00^{\circ}$

Plot a reduced range of elevation angles using the Azimuth parameter.
patternElevation(antenna,fc,[0 30],'Elevation',[-45:45],'Type','powerdb')


Power (dB), Broadside at $0.00^{\circ}$

## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\mathrm{total}}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Version History Introduced in R2015a

## See Also

pattern| patternAzimuth

## plotResponse

System object: phased. CustomAntennaElement
Package: phased
Plot response pattern of antenna

## Syntax

plotResponse(H,FREQ)
plotResponse(H,FREQ,Name, Value)
hPlot = plotResponse( $\qquad$ )

## Description

plotResponse( $\mathrm{H}, \mathrm{FREQ}$ ) plots the element response pattern along the azimuth cut, where the elevation angle is 0 . The operating frequency is specified in FREQ.
plotResponse(H, FREQ,Name, Value) plots the element response with additional options specified by one or more Name, Value pair arguments.
hPlot $=$ plotResponse ( __ $)$ returns handles of the lines or surface in the figure window, using any of the input arguments in the previous syntaxes.

## Input Arguments

## H

Element System object

## FREQ

Operating frequency in Hertz specified as a scalar or 1-by-K row vector. FREQ must lie within the range specified by the FrequencyVector property of H . If you set the 'RespCut ' property of H to ' 3 D ' , FREQ must be a scalar. When FREQ is a row vector, plotResponse draws multiple frequency responses on the same axes.

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## CutAngle

Cut angle specified as a scalar. This argument is applicable only when RespCut is ' Az ' or ' El '. If RespCut is 'Az', CutAngle must be between -90 and 90. If RespCut is 'El', CutAngle must be between -180 and 180 .

## Default: 0

## Format

Format of the plot, using one of 'Line', 'Polar', or 'UV'. If you set Format to 'UV', FREQ must be a scalar.

Default: 'Line'

## NormalizeResponse

Set this value to true to normalize the response pattern. Set this value to false to plot the response pattern without normalizing it. This parameter is not applicable when you set the Unit parameter value to 'dbi'.

Default: true

## OverlayFreq

Set this value to true to overlay pattern cuts in a 2-D line plot. Set this value to false to plot pattern cuts against frequency in a 3-D waterfall plot. If this value is false, FREQ must be a vector with at least two entries.

This parameter applies only when Format is not 'Polar' and RespCut is not '3D'.

## Default: true

## Polarization

Specify the polarization options for plotting the antenna response pattern. The allowable values are |'None' | 'Combined' | 'H' | 'V' | where

- 'None' specifies plotting a nonpolarized response pattern
- 'Combined ' specifies plotting a combined polarization response pattern
- 'H' specifies plotting the horizontal polarization response pattern
- 'V ' specifies plotting the vertical polarization response pattern

For antennas that do not support polarization, the only allowed value is 'None'. This parameter is not applicable when you set the Unit parameter value to 'dbi ' .

Default: 'None'

## RespCut

Cut of the response. Valid values depend on Format, as follows:

- If Format is 'Line' or 'Polar', the valid values of RespCut are 'Az', 'El', and '3D'. The default is ' Az '.
- If Format is 'UV', the valid values of RespCut are 'U' and '3D'. The default is 'U'.

If you set RespCut to ' 3 D ' , FREQ must be a scalar.

## Unit

The unit of the plot. Valid values are 'db', 'mag', 'pow', or 'dbi'. This parameter determines the type of plot that is produced.

| Unit value | Plot type |
| :--- | :--- |
| db | power pattern in dB scale |
| mag | field pattern |
| pow | power pattern |
| dbi | directivity |

Default: 'db'

## AzimuthAngles

Azimuth angles for plotting element response, specified as a row vector. The AzimuthAngles parameter sets the display range and resolution of azimuth angles for visualizing the radiation pattern. This parameter is allowed only when the RespCut parameter is set to ' Az ' or ' $3 D^{\prime}$ and the Format parameter is set to 'Line' or 'Polar'. The values of azimuth angles should lie between $180^{\circ}$ and $180^{\circ}$ and must be in nondecreasing order. When you set the RespCut parameter to '3D ', you can set the AzimuthAngles and ElevationAngles parameters simultaneously.

Default: [-180:180]

## ElevationAngles

Elevation angles for plotting element response, specified as a row vector. The ElevationAngles parameter sets the display range and resolution of elevation angles for visualizing the radiation pattern. This parameter is allowed only when the RespCut parameter is set to ' $E l$ ' or ' $3 D^{\prime}$ ' and the Format parameter is set to 'Line' or 'Polar'. The values of elevation angles should lie between $90^{\circ}$ and $90^{\circ}$ and must be in nondecreasing order. When you set the RespCut parameter to ' 3D ', you can set the ElevationAngles and AzimuthAngles parameters simultaneously.

Default: [-90:90]

## UGrid

$U$ coordinate values for plotting element response, specified as a row vector. The UGrid parameter sets the display range and resolution of the $U$ coordinates for visualizing the radiation pattern in $U / V$ space. This parameter is allowed only when the Format parameter is set to 'UV' and the RespCut parameter is set to ' $U$ ' or ' $3 D$ '. The values of $U G r i d$ should be between -1 and 1 and should be specified in nondecreasing order. You can set the UGrid and VGrid parameters simultaneously.

Default: [-1:0.01:1]

## VGrid

$V$ coordinate values for plotting element response, specified as a row vector. The VGrid parameter sets the display range and resolution of the $V$ coordinates for visualizing the radiation pattern in $U / V$ space. This parameter is allowed only when the Format parameter is set to 'UV' and the RespCut parameter is set to ' 3 D '. The values of VGrid should be between -1 and 1 and should be specified in nondecreasing order. You can set the VGrid and UGrid parameters simultaneously.

Default: [-1:0.01:1]

## Examples

## Plot Response and Directivity of Custom Antenna

Create a custom antenna with a cosine pattern. Then, plot the antenna's response.
Create the antenna and calculate the response. The user-defined pattern is omnidirectional in the azimuth direction and has a cosine pattern in the elevation direction. Assume the antenna works at 1 GHz.

```
fc = 1e9;
azang = [-180:180];
elang = [-90:90];
magpattern = mag2db(repmat(cosd(elang)',1,numel(azang)));
phasepattern = zeros(size(magpattern));
antenna = phased.CustomAntennaElement('AzimuthAngles',azang, ...
    'ElevationAngles',elang,'MagnitudePattern',magpattern, ...
    'PhasePattern',phasepattern);
```

Plot an elevation cut of the magnitude response as a line plot.
plotResponse(antenna,fc,'RespCut','El','ElevationAngles', [-90:0.1:90],...
'Format','Line','Unit','mag')


Plot an elevation cut of the directivity as a line plot, showing that the maximum directivity is approximately 2 dB .
plotResponse(antenna,fc,'RespCut','El','ElevationAngles',[-90:0.1:90],...
'Format','Line', 'Unit','dbi')


## Plot Response of Custom Antenna Over Selected Range of Angles

Create an antenna with a custom response. The user-defined pattern is omnidirectional in the azimuth direction and has a cosine pattern in the elevation direction. Assume the antenna operates at a frequency of 1 GHz . Display the 3-D response for a 60 degree range of azimuth and elevation angles centered at 0 degrees azimuth and 0 degrees elevation in 0.1 degree increments.

```
fc = 1e9;
azang = [-180:180];
elang = [-90:90];
magpattern = mag2db(repmat(cosd(elang)',1,numel(azang)));
phasepattern = zeros(size(magpattern));
antenna = phased.CustomAntennaElement('AzimuthAngles',azang, ...
    'ElevationAngles',elang,'MagnitudePattern',magpattern, ...
    'PhasePattern',phasepattern);
resp = antenna(fc,[0;0]);
plotResponse(antenna,fc,'RespCut','3D','AzimuthAngles',[-30:0.1:30],...
    'ElevationAngles',[-30:0.1:30],'Format','Polar','Unit','pow')
```



See Also
uv2azel|azel2uv

## step

System object: phased. CustomAntennaElement
Package: phased
Output response of antenna element

## Syntax

RESP = step(H,FREQ,ANG)

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, $\mathrm{y}=$ step (obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.

RESP $=$ step ( $\mathrm{H}, \mathrm{FREQ}, \mathrm{ANG}$ ) returns the antenna's voltage response RESP at operating frequencies specified in FREQ and directions specified in ANG. The form of RESP depends upon whether the antenna element supports polarization as determined by the SpecifyPolarizationPattern property. If SpecifyPolarizationPattern is set to false, RESP is an M-by-L matrix containing the antenna response at the $M$ angles specified in ANG and at the $L$ frequencies specified in FREQ. If SpecifyPolarizationPattern is set to true, RESP is a MATLAB struct containing two fields, RESP.H and RESP.V, representing the antenna's response in horizontal and vertical polarization, respectively. Each field is an $M$-by- $L$ matrix containing the antenna response at the $M$ angles specified in ANG and at the $L$ frequencies specified in FREQ.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## H

Antenna element object.

## FREQ

Operating frequencies of antenna in hertz. FREQ is a row vector of length $L$.

## ANG

Directions in degrees. ANG can be either a 2-by-M matrix or a row vector of length M.

If ANG is a 2-by-M matrix, each column of the matrix specifies the direction in the form [azimuth; elevation]. The azimuth angle must be between -180 and 180 degrees, inclusive. The elevation angle must be between -90 and 90 degrees, inclusive.

If ANG is a row vector of length $M$, each element specifies a direction's azimuth angle. In this case, the corresponding elevation angle is assumed to be 0 .

## Output Arguments

## RESP

Voltage response of antenna element. The output depends on whether the antenna element supports polarization or not.

- If the antenna element does not support polarization, RESP is an $M$-by- $L$ matrix. In this matrix, $M$ represents the number of angles specified in ANG while $L$ represents the number of frequencies specified in FREQ.
- If the antenna element supports polarization, RESP is a MATLAB struct with fields RESP.H and RESP.V containing responses for the horizontal and vertical polarization components of the antenna radiation pattern. RESP. H and RESP.V are $M$-by- $L$ matrices. In these matrices, $M$ represents the number of angles specified in ANG while $L$ represents the number of frequencies specified in FREQ.


## Examples

## Custom Antenna Element Response at $30^{\circ}$ Elevation

Construct a user-defined antenna with an omnidirectional response in azimuth and a cosine pattern in elevation. The antenna operates at 1 GHz . Plot the response pattern. Then, find the antenna response at $30^{\circ}$.

```
antenna = phased.CustomAntennaElement;
antenna.AzimuthAngles = -180:180;
antenna.ElevationAngles = -90:90;
antenna.MagnitudePattern = mag2db(repmat(cosd(antenna.ElevationAngles)',...
    1, numel(antenna.AzimuthAngles)));
```

Find the response at $30^{\circ}$ elevation for an operating frequency of 1 GHz .

```
fc = 1.0e9;
resp = antenna(fc,[0;30])
resp = 0.8660
```


## Antenna with Custom Radiation Pattern

Create a custom antenna element object. The radiation pattern has a cosine dependence on elevation angle but is independent of azimuth angle.

```
az = -180:90:180;
el = -90:45:90;
```

```
elresp = cosd(el);
magpattern = mag2db(repmat(elresp',1,numel(az)));
phasepattern = zeros(size(magpattern));
antenna = phased.CustomAntennaElement('AzimuthAngles',az,...
    'ElevationAngles',el,'MagnitudePattern',magpattern, ...
    'PhasePattern',phasepattern);
```

Display the radiation pattern.

| disp (antenna.MagnitudePattern) |  |  |  |  |
| ---: | ---: | ---: | ---: | ---: |
| -Inf | - Inf | - Inf | - Inf | -Inf |
| -3.0103 | -3.0103 | -3.0103 | -3.0103 | -3.0103 |
| 0 | 0 | 0 | 0 | 0 |
| -3.0103 | -3.0103 | -3.0103 | -3.0103 | -3.0103 |
| - Inf | - Inf | - Inf | - Inf | - Inf |

Calculate the antenna response at the azimuth-elevation pairs $(-30,0)$ and $(-45,0)$ at 500 MHz .

```
ang = [-30 0; -45 0];
resp = antenna(500.0e6,ang);
disp(resp)
    0.7071
    1.0000
```

The following code illustrates how nearest-neighbor interpolation is used to find the antenna voltage response in the two directions. The total response is the product of the angular response and the frequency response.

```
g = interp2(deg2rad(antenna.AzimuthAngles),...
    deg2rad(antenna.ElevationAngles),...
    db2mag(antenna.MagnitudePattern),...
    deg2rad(ang(1,:))', deg2rad(ang(2,:))','nearest',0);
h = interp1(antenna.FrequencyVector,...
    db2mag(antenna.FrequencyResponse),500e6,'nearest',0);
antresp = h.*g;
```

Compare the value of antresp to the response of the antenna.

```
disp(mag2db(antresp))
```

    -3. 0103
            0
    
## Algorithms

The total response of a custom antenna element is a combination of its frequency response and spatial response. phased. CustomAntennaElement calculates both responses using nearest neighbor interpolation, and then multiplies the responses to form the total response.

## See Also <br> uv2azel | phitheta2azel

# phased.CustomMicrophoneElement 

Package: phased

Custom microphone element

## Description

The CustomMicrophoneElement System object models a microphone element with a custom spatial response pattern.

To compute the response of the microphone element for specified directions:
1 Create the phased. CustomMicrophoneElement object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

microphone $=$ phased.CustomMicrophoneElement
microphone $=$ phased.CustomMicrophoneElement(Name=Value)

## Description

microphone = phased.CustomMicrophoneElement creates a custom microphone System object, microphone, with default object properties.
microphone $=$ phased.CustomMicrophoneElement(Name=Value) creates a custom microphone object, microphone, with each specified property set to the specified value. You can specify additional name-value pair arguments in any order as (Namel=Value1,...,NameN=ValueN).
Example: microphone $=$ phased.CustomMicrophoneElement (FrequencyVector=[0 1000], FrequencyResponse=[0-10], PolarPatternFrequencies=[100 1000]) creates a custom microphone element with its frequency response specified at 0 and 1000 Hz . The frequency response at these frequencies is 0 and -10 dB . The pattern frequencies are 100 and 1000 Hz .

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## FrequencyVector - Operating frequencies

## [0 le20] (default)| 1-by-L real-valued vector of positive values

The frequencies where the element responses are measured, specified as 1-by- $L$ real-valued vector of positive values. The elements of the vector must be in increasing magnitude. The microphone element has no response outside the specified frequency range. Units are Hz.

Data Types: double

## FrequencyResponse - Frequency responses

## [0 0] (default)| 1-by-L real-valued vector

Frequency responses measured at the frequencies defined in the FrequencyVector property, specified as a1-by- $L$ real-valued vector. The length of the vector must equal the length of the frequency vector specified in the FrequencyVector property. Units are dB.

Data Types: double
PolarPatternFrequencies - Polar pattern measuring frequencies
1e3 (default) | 1-by-M real-valued vector of positive values
Measuring frequencies of the polar patterns, specified as a1-by-M real-valued vector of positive values. The measuring frequencies must be within the frequency range specified in the FrequencyVector property. Units are Hz.

Data Types: double
PolarPatternAngles - Polar pattern measuring angles
[-180:180] (default) | 1-by-N real-valued vector
Measuring angles in degrees of the polar patterns, specified as a 1-by- $N$ real-valued vector. The angles are measured from the central pickup axis of the microphone, and must be between $-180^{\circ}$ and $180^{\circ}$, inclusive.

Data Types: double

## PolarPattern - Polar pattern

Omnidirectional pattern with 0 dB response (default) | $M$-by- $N$ real-valued matrix
Polar patterns of the microphone element, specified as an $M$-by- $N$ real-valued matrix. $M$ is the number of measuring frequencies specified in the PolarPatternFrequencies property. $N$ is the number of measuring angles specified in the PolarPatternAngles property. Each row of the matrix represents the magnitude of the polar pattern measured at the corresponding frequency specified in the PolarPatternFrequencies property and corresponding angles specified in the PolarPatternAngles property.

The pattern is assumed to be measured in the azimuth plane where the elevation angle is 0 and where the central pickup axis is assumed to be zero degrees azimuth and zero degrees elevation. The polar pattern is assumed to be symmetric around the central axis and therefore the microphone's response pattern in 3-D space can be constructed from the polar pattern. Units are dB.

Data Types: double

## Usage

## Syntax

RESP = microphone(FREQ,ANG)

## Description

RESP = microphone (FREQ, ANG) returns the microphone's magnitude response, RESP, at frequencies specified in FREQ and directions specified in ANG.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## FREQ - Signal frequencies

1-by-P row vector of positive values
Signal frequencies, specified as a 1-by- $P$ row vector of positive values. Units are Hz .

## ANG - Response directions

1-by- $Q$ vector of real-values | 2-by- $Q$ matrix of real-values
Response directions, specified as a 1-by- $Q$ vector of real-values or a 2-by- $Q$ matrix of real-values.

- If ANG is a 1-by- $Q$ vector, each element specifies a direction's azimuth angle. The azimuth angle must be between $-180^{\circ}$ and $180^{\circ}$, inclusive. In this case, the corresponding elevation angle is assumed to be zero.
- If ANG is a 2-by-Q matrix, each column of the matrix specifies the direction in the form [azimuth; elevation]. The azimuth angle must be between $-180^{\circ}$ and $180^{\circ}$, inclusive. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive.

Units are in degrees.

## Output Arguments

## RESP - Microphone response

$Q$-by-P real-valued matrix
Microphone magnitude response, returned as an $Q$-by- $P$ real-valued matrix. The matrix contains the responses of the microphone element at the $Q$ angles specified in ANG and the $P$ frequencies specified in FREQ.

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```


## Specific to Antenna and Transducer Element System Objects

beamwidth
directivity
isPolarizationCapable
pattern
patternAzimuth
patternElevation

Compute and display beamwidth of sensor element pattern Directivity of antenna or transducer element
Antenna element polarization capability
Plot antenna or transducer element directivity and patterns
Plot antenna or transducer element directivity and pattern versus azimuth
Plot antenna or transducer element directivity and pattern versus elevation

## Common to All System Objects

step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object

## Examples

## Custom Microphone Response

Construct a custom cardioid microphone with an operating frequency of 700 Hz . Find the microphone response in the directions: $(0,0)$ degrees azimuth and elevation and $(40,50)$ degrees azimuth and elevation.

```
microphone = phased.CustomMicrophoneElement;
microphone.PolarPatternFrequencies = [500 1000];
microphone.PolarPattern = mag2db([ ...
    0.5+0.5*cosd(microphone.PolarPatternAngles); ...
    0.6+0.4*cosd(microphone.PolarPatternAngles)]);
fc = 700;
ang = [0 0; 40 50]';
resp = microphone(fc,ang)
resp = 2×1
    1.0000
    0.7424
```


## Custom Cardioid Microphone Response

Create a custom cardioid microphone, and calculate the microphone response at 500, 1500, and 2000 Hz in two directions: $(0,0)$ azimuth and elevation, and $(40,50)$ azimuth and elevation. Then display the microphone pattern.

```
microphone = phased.CustomMicrophoneElement( ...
    PolarPatternFrequencies=[500 1000]);
microphone.PolarPattern = mag2db([...
    0.5+0.5*cosd(microphone.PolarPatternAngles); ...
    0.6+0.4*cosd(microphone.PolarPatternAngles)]);
```

Obtain the microphone response in two directions.

```
resp = microphone([500 1500 2000],[0 0; 40 50]')
resp = 2\times3
\begin{tabular}{lll}
1.0000 & 1.0000 & 1.0000 \\
0.7424 & 0.7939 & 0.7939
\end{tabular}
```

Display the microphone power pattern.

```
pattern(microphone,500,-180:180,0,'Type','powerdb')
```



Normalized Power (dB), Broadside at $0.00^{\circ}$

## Directivity of Custom Microphone Element

Compute the directivity of a custom microphone element. Create a custom cardioid microphone, and plot the microphone's response at 700 Hz for elevations between -90 and +90 degrees.

Define the pattern for the custom microphone element. The System object's PolarPatternAngles property has default value of [-180:180] degrees.
myAnt = phased.CustomMicrophoneElement; myAnt.PolarPatternFrequencies = [500 1000]; myAnt. PolarPattern $=$ mag2db([...

```
0.5+0.5*cosd(myAnt.PolarPatternAngles);...
0.6+0.4*cosd(myAnt.PolarPatternAngles)]);
```

Calculate the directivity as a function of elevation at zero degrees azimuth.

```
elev = [-90:5:90];
azm = zeros(size(elev));
ang = [azm;elev];
freq = 700;
d = directivity(myAnt,freq,ang);
plot(elev,d)
xlabel('Elevation (deg)')
ylabel('Directivity (dBi)')
```



The directivity is maximum at $0^{\circ}$ elevation.

## Custom Microphone Does Not Support Polarization

Show that the phased.CustomMicrophoneElement microphone element does not support polarization.

```
microphone = phased.CustomMicrophoneElement;
isPolarizationCapable(microphone)
```

```
ans = logical
    0
```

The returned value 0 shows that the custom microphone element does not support polarization.

## Azimuth Power Pattern and Directivity of Cardioid Microphone

Design a cardioid microphone to operate in the frequency range between 500 and 1000 Hz .

```
sCustMike = phased.CustomMicrophoneElement;
sCustMike.PolarPatternFrequencies = [500 1000];
sCustMike.PolarPattern = mag2db([...
    0.5+0.5*cosd(sCustMike.PolarPatternAngles);...
    0.6+0.4*cosd(sCustMike.PolarPatternAngles)]);
```

Display a polar plot of an azimuth cut of the response at 500 Hz and 1000 Hz .

```
fc = 500;
pattern(sCustMike,[fc 2*fc],[-180:180],0,...
    'CoordinateSystem','polar',...
    'Type','powerdb');
```



Normalized Power (dB), Broadside at $0.00^{\circ}$

Plot the directivity as a line plot for the same two frequencies.
pattern(sCustMike,[fc 2*fc],[-180:180],0,...
'CoordinateSystem', rectangular',...
'Type', 'directivity');


## Power Pattern of Cardioid Microphone in U/V Space

Plot a $u$-cut of the power pattern of a custom cardioid microphone designed to operate in the frequency range $500-1000 \mathrm{~Hz}$.

Create a cardioid microphone.

```
sCustMike = phased.CustomMicrophoneElement;
sCustMike.PolarPatternFrequencies = [500 1000];
sCustMike.PolarPattern = mag2db([...
    0.5+0.5*}\operatorname{cosd(sCustMike.PolarPatternAngles); .. .
    0.6+0.4*cosd(sCustMike.PolarPatternAngles)]);
```

Plot the power pattern.
$\mathrm{fc}=500$;
pattern(sCustMike,fc, [-1:.01:1],0,...
'CoordinateSystem', 'uv',...
'Type', 'powerdb');


## 3-D Pattern of Cardioid Microphone over Restricted Range of Angles

Plot the 3-D magnitude pattern of a custom cardioid microphone with both the azimuth and elevation angles restricted to the range - 40 to 40 degrees in 0.1 degree increments.

Create a custom microphone element with a cardioid pattern.

```
sCustMike = phased.CustomMicrophoneElement;
sCustMike.PolarPatternFrequencies = [500 1000];
sCustMike.PolarPattern = mag2db([...
    0.5+0.5*cosd(sCustMike.PolarPatternAngles); ...
    0.6+0.4*cosd(sCustMike.PolarPatternAngles)]);
```

Plot the 3-D magnitude pattern.

```
fc = 500;
pattern(sCustMike,fc,[-40:0.1:40],[-40:0.1:40],...
    'CoordinateSystem','polar',...
    'Type','efield');
```



## Azimuth Pattern of Cardioid Microphone over Reduced Angular Range

Plot the azimuth directivity pattern of a custom cardioid microphone at both 0 and 30 degrees elevation.

Create a custom microphone element with a cardioid pattern.

```
sCustMike = phased.CustomMicrophoneElement;
sCustMike.PolarPatternFrequencies = [500 1000];
sCustMike.PolarPattern = mag2db([...
    0.5+0.5*cosd(sCustMike.PolarPatternAngles);...
    0.6+0.4*cosd(sCustMike.PolarPatternAngles)]);
```

Plot the directivity at 500 Hz .
$\mathrm{fc}=500$;
patternAzimuth(sCustMike,fc,[0 30])


Directivity (dBi), Broadside at $0.00^{\circ}$

Plot the directivity for a reduced range of azimuth angles using the Azimuth parameter. Notice the change in scale.
fc = 500;
patternAzimuth(sCustMike,fc,[0 30],...
'Azimuth', [-40:.1:40])


Directivity (dBi), Broadside at $0.00^{\circ}$

## Elevation Pattern of Cardioid Microphone over Reduced Angular Range

Plot the elevation directivity pattern of a custom cardioid microphone at both 0 and 45 degrees azimuth.

Create a custom microphone element with a cardioid pattern.

```
sCustMike = phased.CustomMicrophoneElement;
sCustMike.PolarPatternFrequencies = [500 1000];
sCustMike.PolarPattern = mag2db([...
    0.5+0.5*cosd(sCustMike.PolarPatternAngles); ...
    0.6+0.4*cosd(sCustMike.PolarPatternAngles)]);
```

Plot the directivity at 500 Hz .
$\mathrm{fc}=500$;
patternElevation(sCustMike,fc,[0 30])


Directivity (dBi), Broadside at $0.00^{\circ}$

Plot the directivity for a reduced range of azimuth angles using the Azimuth parameter. Notice the change in scale.
fc = 500;
patternElevation(sCustMike,fc,[0 45],...
'Elevation', [-40:.1:40])


Directivity (dBi), Broadside at $0.00^{\circ}$

## Algorithms

The total response of a custom microphone element is a combination of its frequency response and spatial response. phased. CustomMicrophoneElement calculates both responses using nearest neighbor interpolation and then multiplies them to form the total response. When the PolarPatternFrequencies property value is nonscalar, the object specifies multiple polar patterns. In this case, the interpolation uses the polar pattern that is measured closest to the specified frequency.

## Version History

Introduced in R2011a

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:

- pattern, patternAzimuth, patternElevation, and plotResponse methods are not supported.
- See "System Objects in MATLAB Code Generation" (MATLAB Coder).


## See Also

phased.IsotropicProjector|phased.IsotropicHydrophone|
phased.OmnidirectionalMicrophoneElement|phased.ULA|phased.URA|
phased.ConformalArray|uv2azel|phitheta2azel

## directivity

System object: phased.CustomMicrophoneElement
Package: phased
Directivity of custom microphone element

## Syntax

D = directivity (H,FREQ,ANGLE)

## Description

D = directivity ( $\mathrm{H}, \mathrm{FREQ}, \mathrm{ANGLE}$ ) returns the "Directivity ( dBi )" on page 1-347 of a custom microphone element, $H$, at frequencies specified by FREQ and in direction angles specified by ANGLE.

## Input Arguments

## H - Custom microphone element

System object
Custom microphone element specified as a phased.CustomMicrophoneElement System object.
Example: H = phased.CustomMicrophoneElement;

## FREQ - Frequency for computing directivity and patterns

positive scalar | 1-by-L real-valued row vector
Frequencies for computing directivity and patterns, specified as a positive scalar or 1-by-L realvalued row vector. Frequency units are in hertz.

- For an antenna, microphone, or sonar hydrophone or projector element, FREQ must lie within the range of values specified by the FrequencyRange or FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased. CustomAntennaElement and phased.CustomMic rophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.


## Example: [1e8 2e6]

Data Types: double

## ANGLE - Angles for computing directivity

1-by-M real-valued row vector | 2 -by- $M$ real-valued matrix
Angles for computing directivity, specified as a 1-by- $M$ real-valued row vector or a 2 -by- $M$ real-valued matrix, where $M$ is the number of angular directions. Angle units are in degrees. If ANGLE is a 2 -by- $M$ matrix, then each column specifies a direction in azimuth and elevation, [az;el]. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

If ANGLE is a 1 -by- $M$ vector, then each entry represents an azimuth angle, with the elevation angle assumed to be zero.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the xy plane. This angle is positive when measured from the $x$-axis toward the $y$-axis. The elevation angle is the angle between the direction vector and $x y$ plane. This angle is positive when measured towards the $z$-axis. See "Azimuth and Elevation Angles".

Example: [45 60; 0 10]
Data Types: double

## Output Arguments

## D - Directivity

$M$-by-L matrix
Directivity, returned as an $M$-by- $L$ matrix. Each row corresponds to one of the $M$ angles specified by ANGLE. Each column corresponds to one of the $L$ frequency values specified in FREQ. Directivity units are in dBi where dBi is defined as the gain of an element relative to an isotropic radiator.

## Examples

## Directivity of Custom Microphone Element

Compute the directivity of a custom microphone element. Create a custom cardioid microphone, and plot the microphone's response at 700 Hz for elevations between -90 and +90 degrees.

Define the pattern for the custom microphone element. The System object's PolarPatternAngles property has default value of [-180:180] degrees.

```
myAnt = phased.CustomMicrophoneElement;
myAnt.PolarPatternFrequencies = [500 1000];
myAnt.PolarPattern = mag2db([...
    0.5+0.5*cosd(myAnt.PolarPatternAngles); ...
    0.6+0.4*cosd(myAnt.PolarPatternAngles)]);
```

Calculate the directivity as a function of elevation at zero degrees azimuth.

```
elev = [-90:5:90];
azm = zeros(size(elev));
ang = [azm;elev];
freq = 700;
d = directivity(myAnt,freq,ang);
plot(elev,d)
xlabel('Elevation (deg)')
ylabel('Directivity (dBi)')
```



The directivity is maximum at $0^{\circ}$ elevation.

## More About

## Directivity (dBi)

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## See Also

pattern | patternElevation | patternAzimuth

## isPolarizationCapable

System object: phased.CustomMicrophoneElement
Package: phased
Polarization capability

## Syntax

flag = isPolarizationCapable(h)

## Description

flag = isPolarizationCapable(h) returns a Boolean value, flag, indicating whether the phased.CustomMicrophoneElement supports polarization. An element supports polarization if it can create or respond to polarized fields. This microphone element, as with all microphone elements, does not support polarization.

## Input Arguments

## h - Custom microphone element

Custom microphone element specified as a phased.CustomMicrophoneElement System object.

## Output Arguments

## flag - Polarization-capability flag

Polarization-capability returned as a Boolean value true if the microphone element supports polarization or false if it does not. Because the phased. CustomMicrophoneElement object does not support polarization, flag is always returned as false.

## Examples

## Custom Microphone Does Not Support Polarization

Show that the phased.CustomMicrophoneElement microphone element does not support polarization.

```
microphone = phased.CustomMicrophoneElement;
isPolarizationCapable(microphone)
ans = logical
    0
```

The returned value 0 shows that the custom microphone element does not support polarization.

## pattern

System object: phased.CustomMicrophoneElement
Package: phased
Plot custom microphone element directivity and patterns

## Syntax

```
pattern(sElem,FREQ)
pattern(sElem,FREQ,AZ)
pattern(sElem,FREQ,AZ,EL)
pattern(
    ,Name,Value)
[PAT,AZ_ANG,EL_ANG] = pattern(
```

$\qquad$

``` )
```


## Description

pattern (sElem, FREQ) plots the 3-D array directivity pattern (in dBi) for the element specified in sElem. The operating frequency is specified in FREQ.
pattern(sElem, FREQ, AZ) plots the element directivity pattern at the specified azimuth angle.
pattern(sElem, FREQ,AZ,EL) plots the element directivity pattern at specified azimuth and elevation angles.
pattern(__,Name,Value) plots the element pattern with additional options specified by one or more Name, Value pair arguments.
[PAT,AZ_ANG,EL_ANG] = pattern (___ ) returns the element pattern in PAT. The AZ_ANG output contains the coordinate values corresponding to the rows of PAT. The EL_ANG output contains the coordinate values corresponding to the columns of PAT. If the 'CoordinateSystem' parameter is set to ' uv', then AZ_ANG contains the $U$ coordinates of the pattern and EL_ANG contains the $V$ coordinates of the pattern. Otherwise, they are in angular units in degrees. $U V$ units are dimensionless.

Note This method replaces the plotResponse method. See "Convert plotResponse to pattern" on page 1-357 for guidelines on how to use pattern in place of plotResponse.

## Input Arguments

## sElem - Custom microphone element

System object
Custom microphone element, specified as a phased.CustomMicrophoneElement System object.
Example: sElem = phased.CustomMicrophoneElement;
FREQ - Frequency for computing directivity and patterns
positive scalar | 1-by-L real-valued row vector

Frequencies for computing directivity and patterns, specified as a positive scalar or 1-by-L realvalued row vector. Frequency units are in hertz.

- For an antenna, microphone, or sonar hydrophone or projector element, FREQ must lie within the range of values specified by the FrequencyRange or FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased. CustomAntennaElement and phased. CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: [1e8 2e6]
Data Types: double

## AZ - Azimuth angles

[-180:180] (default) | 1-by- $N$ real-valued row vector
Azimuth angles for computing directivity and pattern, specified as a $1-b y-N$ real-valued row vector where $N$ is the number of azimuth angles. Angle units are in degrees. Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the xy plane. When measured from the $x$-axis toward the $y$-axis, this angle is positive.

## Example: [-45:2:45]

Data Types: double

## EL - Elevation angles

[-90:90] (default) | 1-by-M real-valued row vector
Elevation angles for computing directivity and pattern, specified as a 1-by- $M$ real-valued row vector where $M$ is the number of desired elevation directions. Angle units are in degrees. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

The elevation angle is the angle between the direction vector and $x y$-plane. The elevation angle is positive when measured towards the $z$-axis.
Example: [-75:1:70]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## CoordinateSystem - Plotting coordinate system

'polar' (default)|'rectangular'|'uv'
Plotting coordinate system of the pattern, specified as the comma-separated pair consisting of
'CoordinateSystem' and one of 'polar', 'rectangular', or 'uv'. When
'CoordinateSystem' is set to 'polar' or 'rectangular', the AZ and EL arguments specify the
pattern azimuth and elevation, respectively. AZ values must lie between $-180^{\circ}$ and $180^{\circ}$. EL values must lie between $-90^{\circ}$ and $90^{\circ}$. If 'CoordinateSystem' is set to 'uv', AZ and EL then specify $U$ and $V$ coordinates, respectively. AZ and EL must lie between -1 and 1.
Example: 'uv'
Data Types: char

## Type - Displayed pattern type

'directivity' (default) | 'efield'|'power'|'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type ' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb ' - power pattern converted to dB.

Example: ' powerdb'
Data Types: char

## Normalize - Display normalize pattern

true (default) | false
Display normalized pattern, specified as the comma-separated pair consisting of 'Normalize' and a Boolean. Set this parameter to true to display a normalized pattern. This parameter does not apply when you set 'Type' to 'directivity'. Directivity patterns are already normalized.

Data Types: logical

## PlotStyle - Plotting style

'overlay' (default)| 'waterfall'
Plotting style, specified as the comma-separated pair consisting of 'Plotstyle' and either 'overlay' or 'waterfall'. This parameter applies when you specify multiple frequencies in FREQ in 2-D plots. You can draw 2-D plots by setting one of the arguments AZ or EL to a scalar.

## Data Types: char

## Output Arguments

## PAT - Element pattern

$N$-by-M real-valued matrix
Element pattern, returned as an $N$-by- $M$ real-valued matrix. The pattern is a function of azimuth and elevation. The rows of PAT correspond to the azimuth angles in the vector specified by EL_ANG. The columns correspond to the elevation angles in the vector specified by AZ_ANG.

## AZ_ANG - Azimuth angles

```
scalar | 1-by-N real-valued row vector
```

Azimuth angles for displaying directivity or response pattern, returned as a scalar or 1-by-N realvalued row vector corresponding to the dimension set in AZ. The columns of PAT correspond to the values in AZ_ANG. Units are in degrees.

## EL_ANG - Elevation angles

scalar | 1-by-M real-valued row vector
Elevation angles for displaying directivity or response, returned as a scalar or 1-by-M real-valued row vector corresponding to the dimension set in EL. The rows of PAT correspond to the values in EL_ANG. Units are in degrees.

## Examples

## Azimuth Power Pattern and Directivity of Cardioid Microphone

Design a cardioid microphone to operate in the frequency range between 500 and 1000 Hz .

```
sCustMike = phased.CustomMicrophoneElement;
sCustMike.PolarPatternFrequencies = [500 1000];
sCustMike.PolarPattern = mag2db([...
    0.5+0.5*cosd(sCustMike.PolarPatternAngles); ...
    0.6+0.4*cosd(sCustMike.PolarPatternAngles)]);
```

Display a polar plot of an azimuth cut of the response at 500 Hz and 1000 Hz .

```
fc = 500;
pattern(sCustMike,[fc 2*fc],[-180:180],0,...
    'CoordinateSystem','polar',...
    'Type','powerdb');
```



Normalized Power (dB), Broadside at $0.00^{\circ}$

Plot the directivity as a line plot for the same two frequencies.
pattern(sCustMike,[fc 2*fc],[-180:180],0,...
'CoordinateSystem', 'rectangular',...
'Type','directivity');


## Power Pattern of Cardioid Microphone in U/V Space

Plot a $u$-cut of the power pattern of a custom cardioid microphone designed to operate in the frequency range $500-1000 \mathrm{~Hz}$.

Create a cardioid microphone.

```
sCustMike = phased.CustomMicrophoneElement;
sCustMike.PolarPatternFrequencies = [500 1000];
sCustMike.PolarPattern = mag2db([...
    0.5+0.5*cosd(sCustMike.PolarPatternAngles);...
    0.6+0.4*cosd(sCustMike.PolarPatternAngles)]);
```

Plot the power pattern.

```
fc = 500;
pattern(sCustMike,fc,[-1:.01:1],0,...
    'CoordinateSystem','uv',...
    'Type','powerdb');
```



## 3-D Pattern of Cardioid Microphone over Restricted Range of Angles

Plot the 3-D magnitude pattern of a custom cardioid microphone with both the azimuth and elevation angles restricted to the range -40 to 40 degrees in 0.1 degree increments.

Create a custom microphone element with a cardioid pattern.

```
sCustMike = phased.CustomMicrophoneElement;
sCustMike.PolarPatternFrequencies = [500 1000];
sCustMike.PolarPattern = mag2db([...
    0.5+0.5*cosd(sCustMike.PolarPatternAngles);...
    0.6+0.4*cosd(sCustMike.PolarPatternAngles)]);
```

Plot the 3-D magnitude pattern.

```
fc = 500;
pattern(sCustMike,fc,[-40:0.1:40],[-40:0.1:40],...
    'CoordinateSystem','polar',...
    'Type','efield');
```



## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \Pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Convert plotResponse to pattern

For antenna, microphone, and array System objects, the pattern method replaces the plotResponse method. In addition, two new simplified methods exist just to draw 2-D azimuth and elevation pattern plots. These methods are azimuthPattern and elevationPattern.

The following table is a guide for converting your code from using plotResponse to pattern. Notice that some of the inputs have changed from input arguments to Name-Value pairs and conversely. The general pattern method syntax is
pattern(H,FREQ,AZ,EL, 'Name1', 'Value1',...,' NameN', 'ValueN')

| plotResponse Inputs | plotResponse Description | pattern Inputs |
| :--- | :--- | :--- |
| H argument | Antenna, microphone, or array <br> System object. | H argument (no change) |
| FREQ argument | Operating frequency. | FREQ argument (no change) |
| V argument | Propagation speed. This argument <br> is used only for arrays. | 'PropagationSpeed ' name-value <br> pair. This parameter is only used for <br> arrays. |


| plotResponse Inputs | plotResponse Description |  | pattern Inputs |  |
| :---: | :---: | :---: | :---: | :---: |
| 'Format' and 'RespCut' namevalue pairs | These options work together to let you create a plot in angle space (line or polar style) or $U V$ space. They also determine whether the plot is 2-D or 3-D. This table shows you how to create different types of plots using plotResponse. |  | 'CoordinateSystem' name-value pair used together with the AZ and EL input arguments. <br> 'CoordinateSystem' has the same options as the plotResponse method 'Format ' name-value pair, except that 'line' is now named 'rectangular'. The table shows how to create different types of plots using pattern. |  |
|  | Display space |  |  |  |
|  | Angle space (2D) |  |  |  |
|  |  | Set 'RespCut'to 'Az' or'El'. Set'Format' to'line' or'polar'.Set the displayaxis using eitherthe'AzimuthAngleS' or'ElevationAngles' name-value pairs. | Display space |  |
|  |  |  | Angle space (2D) <br> Angle space (3D) | Set <br> 'Coordinate <br> System' to rectangular' or 'polar'. <br> Specify either AZ or EL as a scalar. |
|  |  |  |  | Set <br> 'Coordinate <br> System' to 'rectangular' |
|  | Angle space (3D) | Set 'RespCut' to '3D'. Set 'Format' to ' line' or 'polar'. <br> Set the display axis using both the 'AzimuthAngle ${ }^{\prime}$ and 'Elevation Angles ' namevalue pairs. |  | or 'polar'. <br> Specify both AZ and EL as vectors. |
|  |  |  | UV space (2D) | Set <br> 'Coordinate <br> System' to 'uv'. Use AZ to specify a $U$ space vector. Use EL to specify a $V$-space scalar. |
|  |  |  | UV space (3D) | Set |
|  | UV space (2D) | Set 'RespCut' to'U'. Set 'Format' to 'UV '. Set the display range using the 'UGrid' namevalue pair. |  | System' to 'uv'. Use AZ to specify a $U$ space vector. <br> Use EL to specify a $V$-space vector. |
|  |  |  | If you set CoordinateSystem to 'uv', enter the UV grid values using AZ and EL . |  |
|  | UV space (3D) | $\begin{aligned} & \text { Set 'RespCut' } \\ & \text { to'3D'. Set } \\ & \text { 'Format' to } \end{aligned}$ |  |  |


| plotResponse Inputs | plotResponse Description |  | pattern Inputs |
| :---: | :---: | :---: | :---: |
|  | Display space |  |  |
|  |  | 'UV '. Set the display range using both the 'UGrid' and 'VGrid' namevalue pairs. |  |
| 'CutAngle' name-value pair | Constant angle at to take an azimuth or elevation cut. When producing a 2-D plot and when 'RespCut' is set to 'Az' or 'El', use 'CutAngle' to set the slice across which to view the plot. |  | No equivalent name-value pair. To create a cut, specify either AZ or EL as a scalar, not a vector. |
| 'NormalizeResponse' namevalue pair | Normalizes the plot. When 'Unit' is set to 'dbi', you cannot specify 'NormalizeResponse'. |  | Use the 'Normalize' name-value pair. When 'Type' is set to 'directivity' you cannot specify 'Normalize'. |
| 'OverlayFreq' name-value pair | Plot multiple frequencies on the same 2-D plot. Available only when 'Format' is set to 'line' or 'uv' and 'RespCut' is not set to '3D'. The value true produces an overlay plot and the value false produces a waterfall plot. |  | 'PlotStyle' name-value pair plots multiple frequencies on the same 2-D plot. <br> The values 'overlay' and 'waterfall' correspond to 'OverlayFreq' values of true and false. The option 'waterfall' is allowed only when 'CoordinateSystem' is set to 'rectangular' or 'uv'. |
| 'Polarization' name-value pair | Determines how to plot polarized fields. Options are 'None', 'Combined', 'H', or 'V'. |  | 'Polarization ' name-value pair determines how to plot polarized fields. The 'None ' option is removed. The options 'Combined ', 'H', or 'V' are unchanged. |
| 'Unit' name-value pair | Determines the plot units. Choose db', 'mag', 'pow', or 'dbi', where the default is ' db ' |  | 'Type ' name-value pair, uses equivalent options with different names |
|  |  |  | plotResponse pattern |
|  |  |  | 'db' 'powerdb' <br> 'mag' 'efield' <br> 'pow' 'power' <br> 'dbi' 'directivity' |
| 'Weights ' name-value pair | Array element tapers (or weights). |  | 'Weights ' name-value pair (no change). |
| 'AzimuthAngles ' name-value pair | Azimuth angles used to display the antenna or array response. |  | AZ argument |


| plotResponse Inputs | plotResponse Description | pattern Inputs |
| :--- | :--- | :--- |
| 'ElevationAngles ' name-value <br> pair | Elevation angles used to display the <br> antenna or array response. | EL argument |
| 'UGrid' name-value pair | Contains $U$ coordinates in $U V$ - <br> space. | AZ argument when <br> 'CoordinateSystem ' name-value <br> pair is set to ' uv ' |
| 'VGrid' name-value pair | Contains V-coordinates in $U V$-space. | EL argument when <br> 'CoordinateSystem ' name-value <br> pair is set to 'uv ' |

## Version History <br> Introduced in R2015a

See Also<br>patternAzimuth | patternElevation

## patternAzimuth

System object: phased.CustomMicrophoneElement
Package: phased
Plot custom microphone element directivity or pattern versus azimuth

## Syntax

```
patternAzimuth(sElem,FREQ)
patternAzimuth(sElem,FREQ,EL)
patternAzimuth(sElem,FREQ,EL,Name,Value)
PAT = patternAzimuth(
```

$\qquad$

## Description

patternAzimuth (sElem, FREQ) plots the 2-D element directivity pattern versus azimuth (in dBi) for the element sElem at zero degrees elevation angle. The argument FREQ specifies the operating frequency.
patternAzimuth(sElem, FREQ,EL), in addition, plots the 2-D element directivity pattern versus azimuth (in dBi ) at the elevation angle specified by EL. When EL is a vector, multiple overlaid plots are created.
patternAzimuth(sElem, FREQ,EL,Name, Value) plots the element pattern with additional options specified by one or more Name, Value pair arguments.

PAT = patternAzimuth( $\qquad$ ) returns the element pattern. PAT is a matrix whose entries represent the pattern at corresponding sampling points specified by the 'Azimuth' parameter and the EL input argument.

## Input Arguments

## sElem - Custom microphone element

System object
Custom microphone element, specified as a phased.CustomMicrophoneElement System object.
Example: sElem = phased.CustomMicrophoneElement;

## FREQ - Frequency for computing directivity and pattern

positive scalar
Frequency for computing directivity and pattern, specified as a positive scalar. Frequency units are in hertz.

- For an antenna or microphone element, FREQ must lie within the range of values specified by the FrequencyRange or the FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased. CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: 1e8
Data Types: double

## EL - Elevation angles

## 1-by- $N$ real-valued row vector

Elevation angles for computing sensor or array directivities and patterns, specified as a 1-by- $N$ realvalued row vector. The quantity $N$ is the number of requested elevation directions. Angle units are in degrees. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

The elevation angle is the angle between the direction vector and the xy plane. When measured toward the $z$-axis, this angle is positive.
Example: [0,10,20]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Type - Displayed pattern type

'directivity' (default) | 'efield' | 'power' | 'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power ' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb ' - power pattern converted to dB.

Example: 'powerdb'
Data Types: char

## Azimuth - Azimuth angles

[-180:180] (default) | 1-by-P real-valued row vector
Azimuth angles, specified as the comma-separated pair consisting of 'Azimuth' and a 1-by-P realvalued row vector. Azimuth angles define where the array pattern is calculated.
Example: 'Azimuth', [-90:2:90]
Data Types: double

## Output Arguments

## PAT - Element directivity or pattern

$P$-by- $N$ real-valued matrix
Element directivity or pattern, returned as an $P$-by- $N$ real-valued matrix. The dimension $P$ is the number of azimuth values determined by the 'Azimuth' name-value pair argument. The dimension $N$ is the number of elevation angles, as determined by the EL input argument.

## Examples

## Azimuth Pattern of Cardioid Microphone over Reduced Angular Range

Plot the azimuth directivity pattern of a custom cardioid microphone at both 0 and 30 degrees elevation.

Create a custom microphone element with a cardioid pattern.

```
sCustMike = phased.CustomMicrophoneElement;
sCustMike.PolarPatternFrequencies = [500 1000];
sCustMike.PolarPattern = mag2db([...
    0.5+0.5*cosd(sCustMike.PolarPatternAngles);...
    0.6+0.4*cosd(sCustMike.PolarPatternAngles)]);
```

Plot the directivity at 500 Hz .

```
fc = 500;
```

patternAzimuth(sCustMike,fc,[0 30])


Directivity (dBi), Broadside at $0.00^{\circ}$

Plot the directivity for a reduced range of azimuth angles using the Azimuth parameter. Notice the change in scale.
fc = 500;
patternAzimuth(sCustMike,fc,[0 30],...
'Azimuth', [-40:.1:40])


Directivity (dBi), Broadside at $0.00^{\circ}$

## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Version History Introduced in R2015a

## See Also

pattern| patternElevation

## patternElevation

System object: phased.CustomMicrophoneElement
Package: phased
Plot custom microphone element directivity or pattern versus elevation

## Syntax

```
patternElevation(sElem,FREQ)
patternElevation(sElem,FREQ,AZ)
patternElevation(sElem,FREQ,AZ,Name,Value)
PAT = patternElevation(
```

$\qquad$

``` )
```


## Description

patternElevation(sElem, FREQ) plots the 2-D element directivity pattern versus elevation (in dBi) for the element sElem at zero degrees azimuth angle. The argument FREQ specifies the operating frequency.
patternElevation(sElem,FREQ,AZ), in addition, plots the 2-D element directivity pattern versus elevation (in dBi ) at the azimuth angle specified by $A Z$. When $A Z$ is a vector, multiple overlaid plots are created.
patternElevation(sElem,FREQ,AZ,Name, Value) plots the element pattern with additional options specified by one or more Name, Value pair arguments.

PAT = patternElevation( $\qquad$ ) returns the element pattern. PAT is a matrix whose entries represent the pattern at corresponding sampling points specified by the 'Elevation' parameter and the AZ input argument.

## Input Arguments

## sElem - Custom microphone element

System object
Custom microphone element, specified as a phased.CustomMicrophoneElement System object.
Example: sElem = phased.CustomMicrophoneElement;

## FREQ - Frequency for computing directivity and pattern

positive scalar
Frequency for computing directivity and pattern, specified as a positive scalar. Frequency units are in hertz.

- For an antenna or microphone element, FREQ must lie within the range of values specified by the FrequencyRange or the FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased. CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: 1e8
Data Types: double

## AZ - Azimuth angles for computing directivity and pattern

1-by- $N$ real-valued row vector
Azimuth angles for computing sensor or array directivities and patterns, specified as a 1-by- N realvalued row vector where $N$ is the number of desired azimuth directions. Angle units are in degrees. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the xy plane. This angle is positive when measured from the $x$-axis toward the $y$-axis.
Example: [0,10,20]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Type - Displayed pattern type

'directivity' (default) | 'efield' | 'power' | 'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb ' - power pattern converted to dB.

Example: 'powerdb'
Data Types: char

## Elevation - Elevation angles

[-90:90] (default)| 1-by-P real-valued row vector
Elevation angles, specified as the comma-separated pair consisting of 'Elevation' and a 1-by-P real-valued row vector. Elevation angles define where the array pattern is calculated.
Example: 'Elevation', [-90:2:90]
Data Types: double

## Output Arguments

## PAT - Element directivity or pattern

$P$-by- $N$ real-valued matrix
Element directivity or pattern, returned as an $P$-by- $N$ real-valued matrix. The dimension $P$ is the number of elevation angles determined by the 'Elevation' name-value pair argument. The dimension $N$ is the number of azimuth angles determined by the AZ argument.

## Examples

## Elevation Pattern of Cardioid Microphone over Reduced Angular Range

Plot the elevation directivity pattern of a custom cardioid microphone at both 0 and 45 degrees azimuth.

Create a custom microphone element with a cardioid pattern.

```
sCustMike = phased.CustomMicrophoneElement;
sCustMike.PolarPatternFrequencies = [500 1000];
sCustMike.PolarPattern = mag2db([...
    0.5+0.5*cosd(sCustMike.PolarPatternAngles);...
    0.6+0.4*cosd(sCustMike.PolarPatternAngles)]);
```

Plot the directivity at 500 Hz .

```
fc = 500;
```

patternElevation(sCustMike,fc,[0 30])


Directivity (dBi), Broadside at $0.00^{\circ}$

Plot the directivity for a reduced range of azimuth angles using the Azimuth parameter. Notice the change in scale.
fc = 500;
patternElevation(sCustMike,fc,[0 45],...
'Elevation', [-40:.1:40])


Directivity (dBi), Broadside at $0.00^{\circ}$

## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\mathrm{total}}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Version History Introduced in R2015a

See Also
pattern|patternAzimuth

## plotResponse

System object: phased. CustomMicrophoneElement
Package: phased
Plot response pattern of microphone

## Syntax

plotResponse(H,FREQ)
plotResponse(H,FREQ, Name, Value)
hPlot = plotResponse( $\qquad$ )

## Description

plotResponse( $\mathrm{H}, \mathrm{FREQ}$ ) plots the element response pattern along the azimuth cut, where the elevation angle is 0 . The operating frequency is specified in FREQ.
plotResponse(H, FREQ,Name, Value) plots the element response with additional options specified by one or more Name, Value pair arguments.
hPlot $=$ plotResponse ( __ $)$ returns handles of the lines or surface in the figure window, using any of the input arguments in the previous syntaxes.

## Input Arguments

## H

Element System object

## FREQ

Operating frequency in Hertz specified as a scalar or 1-by-K row vector. FREQ must lie within the range specified by the FrequencyVector property of H . If you set the 'RespCut ' property of H to ' 3 D ' , FREQ must be a scalar. When FREQ is a row vector, plotResponse draws multiple frequency responses on the same axes.

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## CutAngle

Cut angle specified as a scalar. This argument is applicable only when RespCut is ' Az ' or ' El '. If RespCut is 'Az', CutAngle must be between -90 and 90. If RespCut is 'El', CutAngle must be between -180 and 180 .

## Default: 0

## Format

Format of the plot, using one of 'Line', 'Polar', or 'UV'. If you set Format to 'UV', FREQ must be a scalar.

Default: 'Line'

## NormalizeResponse

Set this value to true to normalize the response pattern. Set this value to false to plot the response pattern without normalizing it. This parameter is not applicable when you set the Unit parameter value to 'dbi'.

Default: true

## OverlayFreq

Set this value to true to overlay pattern cuts in a 2-D line plot. Set this value to false to plot pattern cuts against frequency in a 3-D waterfall plot. If this value is false, FREQ must be a vector with at least two entries.

This parameter applies only when Format is not 'Polar' and RespCut is not '3D'.

## Default: true

## Polarization

Specify the polarization options for plotting the antenna response pattern. The allowable values are |'None' | 'Combined' | 'H' | 'V' | where

- 'None' specifies plotting a nonpolarized response pattern
- 'Combined ' specifies plotting a combined polarization response pattern
- 'H' specifies plotting the horizontal polarization response pattern
- 'V ' specifies plotting the vertical polarization response pattern

For antennas that do not support polarization, the only allowed value is 'None'. This parameter is not applicable when you set the Unit parameter value to 'dbi ' .

Default: 'None'

## RespCut

Cut of the response. Valid values depend on Format, as follows:

- If Format is 'Line' or 'Polar', the valid values of RespCut are 'Az', 'El', and '3D'. The default is ' Az '.
- If Format is 'UV', the valid values of RespCut are 'U' and '3D'. The default is 'U'.

If you set RespCut to ' 3D' , FREQ must be a scalar.

## Unit

The unit of the plot. Valid values are 'db', 'mag', 'pow', or 'dbi'. This parameter determines the type of plot that is produced.

| Unit value | Plot type |
| :--- | :--- |
| db | power pattern in dB scale |
| mag | field pattern |
| pow | power pattern |
| dbi | directivity |

Default: 'db'

## AzimuthAngles

Azimuth angles for plotting element response, specified as a row vector. The AzimuthAngles parameter sets the display range and resolution of azimuth angles for visualizing the radiation pattern. This parameter is allowed only when the RespCut parameter is set to ' Az ' or ' $3 D^{\prime}$ and the Format parameter is set to 'Line' or 'Polar'. The values of azimuth angles should lie between $180^{\circ}$ and $180^{\circ}$ and must be in nondecreasing order. When you set the RespCut parameter to '3D ', you can set the AzimuthAngles and ElevationAngles parameters simultaneously.

Default: [-180:180]

## ElevationAngles

Elevation angles for plotting element response, specified as a row vector. The ElevationAngles parameter sets the display range and resolution of elevation angles for visualizing the radiation pattern. This parameter is allowed only when the RespCut parameter is set to ' $E l$ ' or ' $3 D^{\prime}$ ' and the Format parameter is set to 'Line' or 'Polar'. The values of elevation angles should lie between $90^{\circ}$ and $90^{\circ}$ and must be in nondecreasing order. When you set the RespCut parameter to ' 3D ', you can set the ElevationAngles and AzimuthAngles parameters simultaneously.

Default: [-90:90]

## UGrid

$U$ coordinate values for plotting element response, specified as a row vector. The UGrid parameter sets the display range and resolution of the $U$ coordinates for visualizing the radiation pattern in $U / V$ space. This parameter is allowed only when the Format parameter is set to 'UV' and the RespCut parameter is set to ' $U$ ' or ' $3 D$ '. The values of $U G r i d$ should be between -1 and 1 and should be specified in nondecreasing order. You can set the UGrid and VGrid parameters simultaneously.

Default: [-1:0.01:1]

## VGrid

$V$ coordinate values for plotting element response, specified as a row vector. The VGrid parameter sets the display range and resolution of the $V$ coordinates for visualizing the radiation pattern in $U / V$ space. This parameter is allowed only when the Format parameter is set to 'UV' and the RespCut parameter is set to ' 3 D '. The values of VGrid should be between -1 and 1 and should be specified in nondecreasing order. You can set the VGrid and UGrid parameters simultaneously.

Default: [-1:0.01:1]

## Examples

## Azimuth Response and Directivity of Cardioid Microphone

Design a cardioid microphone to operate in the frequency range between 500 and 1000 Hz .
h = phased.CustomMicrophoneElement;
h.PolarPatternFrequencies = [500 1000];
h.PolarPattern $=$ mag2db([...
$0.5+0.5^{*} \operatorname{cosd}$ (h.PolarPatternAngles); ...
$0.6+0.4^{*} \operatorname{cosd}(\mathrm{~h}$. PolarPatternAngles)]);
Display a polar plot of an azimuth cut of the response at 500 Hz and 1000 Hz .
fc = 500;
plotResponse(h,[fc 2*fc],'RespCut','Az','Format','Polar');


Normalized Power (dB), Broadside at $0.00^{\circ}$

Plot the directivity as a line plot for the same two frequencies.
plotResponse(h,[fc 2*fc],'RespCut','Az','Format','Line','Unit','dbi');


## Response of Cardioid Microphone in U/V Space

Plot a $u$-cut of the response of a custom cardioid microphone that is designed to operate in the frequency range $500-1000 \mathrm{~Hz}$.

Create a cardioid microphone.
h = phased.CustomMicrophoneElement;
h.PolarPatternFrequencies = [500 1000];
h.PolarPattern $=$ mag2db([...
$0.5+0.5 * \operatorname{cosd}(h . P o l a r P a t t e r n A n g l e s) ;$...
$0.6+0.4^{*} \operatorname{cosd}(\mathrm{~h}$. PolarPatternAngles)]);
Plot the response.
$\mathrm{fc}=500$;
plotResponse(h,fc,'Format','UV');


## 3-D Response of Cardioid Microphone over Restricted Range of Angles

Plot the 3-D response of a custom cardioid microphone in space but with both the azimuth and elevation angles restricted to the range -40 to 40 degrees in 0.1 degree increments.

Create a custom microphone element with a cardioid pattern.
$\mathrm{h}=$ phased.CustomMicrophoneElement;
h.PolarPatternFrequencies = [500 1000];
h.PolarPattern $=$ mag2db([...
$0.5+0.5^{*} \operatorname{cosd}(h . P o l a r P a t t e r n A n g l e s) ; .$.
0.6+0.4*cosd(h.PolarPatternAngles)]);

Plot the 3-D response.

```
fc = 500;
plotResponse(h,fc,'Format','polar','RespCut','3D',...
    'Unit','mag','AzimuthAngles',[-40:0.1:40],...
    'ElevationAngles',[-40:0.1:40]);
```



See Also

uv2azel|azel2uv

## step

System object: phased. CustomMicrophoneElement
Package: phased
Output response of microphone

## Syntax

RESP = step(H,FREQ,ANG)

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = $\operatorname{step}(\mathrm{obj}, \mathrm{x})$ and $\mathrm{y}=\mathrm{obj}(\mathrm{x})$ perform equivalent operations.

RESP $=$ step ( $\mathrm{H}, \mathrm{FREQ}, \mathrm{ANG}$ ) returns the microphone's magnitude response, RESP, at frequencies specified in FREQ and directions specified in ANG.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## H

Microphone object.

## FREQ

Frequencies in hertz. FREQ is a row vector of length $L$.

## ANG

Directions in degrees. ANG can be either a 2-by-M matrix or a row vector of length M.
If ANG is a 2-by-M matrix, each column of the matrix specifies the direction in the form [azimuth; elevation]. The azimuth angle must be between -180 and 180 degrees, inclusive. The elevation angle must be between -90 and 90 degrees, inclusive.

If ANG is a row vector of length $M$, each element specifies a direction's azimuth angle. In this case, the corresponding elevation angle is assumed to be 0 .

## Output Arguments

## RESP

Response of microphone. RESP is an M-by-L matrix that contains the responses of the microphone element at the $M$ angles specified in ANG and the $L$ frequencies specified in FREQ.

## Examples

## Custom Microphone Response

Construct a custom cardioid microphone with an operating frequency of 700 Hz . Find the microphone response in the directions: $(0,0)$ degrees azimuth and elevation and $(40,50)$ degrees azimuth and elevation.

```
microphone = phased.CustomMicrophoneElement;
microphone.PolarPatternFrequencies = [500 1000];
microphone.PolarPattern = mag2db([ ...
    0.5+0.5*cosd(microphone.PolarPatternAngles); ...
    0.6+0.4*cosd(microphone.PolarPatternAngles)]);
fc = 700;
ang = [0 0; 40 50]';
resp = microphone(fc,ang)
resp = 2x1
    1.0000
    0.7424
```


## Algorithms

The total response of a custom microphone element is a combination of its frequency response and spatial response. phased. CustomMicrophoneElement calculates both responses using nearest neighbor interpolation and then multiplies them to form the total response. When the PolarPatternFrequencies property value is nonscalar, the object specifies multiple polar patterns. In this case, the interpolation uses the polar pattern that is measured closest to the specified frequency.

## See Also

uv2azel | phitheta2azel

# phased.DopplerEstimator 

Package: phased
Doppler estimation

## Description

The phased.DopplerEstimator System object estimates Doppler frequencies of targets. Input to the estimator consists of detection locations output from a detector, and a range-Doppler response data cube. When detections are clustered, the Doppler frequencies are computed using cluster information. Clustering associates multiple detections into one extended detection.

To compute Doppler values for detections:
1 Define and set up your Doppler estimator using the "Construction" on page 1-382 procedure that follows.
2 Call the step method to compute the Doppler of detections, using the properties you specify for the phased.DopplerEstimator System object.

Note Instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, $\mathrm{y}=\mathrm{step}(\mathrm{obj}, \mathrm{x})$ and $\mathrm{y}=$ obj $(x)$ perform equivalent operations.

## Construction

estimator = phased.DopplerEstimator creates a Doppler estimator System object, estimator.
estimator = phased.DopplerEstimator(Name, Value) creates a System object, estimator, with each specified property Name set to the specified Value. You can specify additional name and value pair arguments in any order as (Name1, Value1,...,NameN, ValueN).

## Properties

## NumEstimatesSource - Source of requested number of Doppler estimates <br> 'Auto ' (default)|'Property'

Source of the number of requested Doppler estimates, specified as 'Auto' or 'Property'.
If you set this property to 'Auto ', the number of estimates equals the number of columns in the detidx input argument of the step method. If cluster IDs are provided, the number of estimates equals the number of unique cluster IDs.

If you set this property to 'Property', the number of reported estimates is obtained from the value of the NumEstimates property.
Data Types: char

## NumEstimates - Maximum number of estimates

## 1 (default) | positive integer

The maximum number of estimates to report, specified as a positive integer. When the number of requested estimates is greater than the number of columns in the detidx argument of the step method, the remainder is filled with NaN .

## Dependencies

To enable this property, set the NumEstimatesSource property to 'Property'.
Data Types: c|double

## ClusterInputPort - Accept clusterids as input

false (default)| true
Option to accept clusterids as an input argument to the step method, specified as false or true. Setting this property to true enables the clusterid input argument of the step method.
Data Types: logical
VarianceOutputPort - Enable output of Doppler variance estimates false (default)| true

Option to enable output of Doppler variance estimate, specified as false or true. Doppler variances estimates are returned in the dopvar output argument of the step method.
Data Types: logical
NumPulses - Number of pulses in Doppler-processed waveform
2 (default) | positive integer
The number of pulses in the Doppler processed data cube, specified as a positive integer.

## Dependencies

To enable this property, set the VarianceOutputPort property to true.
Data Types: single | double

## NoisePowerSource - Source of noise power values

'Property' (default)|'Input port'
Source of noise power values, specified as 'Property ' or 'Input port'. Noise power is used to compute Doppler estimation variance and SNR. If you set this property to 'Property', the value of the NoisePower property represents the noise power at the detection locations. If you set this property to 'Input port', you can specify noise power using the noisepower input argument of the step method.

Data Types: char

## NoisePower - Noise power

1.0 (default) | positive scalar

Constant noise power value over the range-Doppler data cube, specified as a positive scalar. Noise power units are linear. The same noise power value is applied to all detections.

## Dependencies

To enable this property, set the VarianceOutputPort property to true and set NoisePowerSource to 'Property'.

Data Types: single | double

## Methods

step
Estimate target Doppler

## Common to All System Objects

release $\quad$ Allow System object property value changes

## Examples

## Estimate Range and Speed of Three Targets

To estimate the range and speed of three targets, create a range-Doppler map using the phased. RangeDopplerResponse System object ${ }^{\mathrm{TM}}$. Then use the phased. RangeEstimator and phased. DopplerEstimator System objects to estimate range and speed. The transmitter and receiver are collocated isotropic antenna elements forming a monostatic radar system.

The transmitted signal is a linear FM waveform with a pulse repetition interval (PRI) of $7.0 \mu \mathrm{~s}$ and a duty cycle of $2 \%$. The operating frequency is 77 GHz and the sample rate is 150 MHz .

```
fs = 150e6;
c = physconst('LightSpeed');
fc = 77.0e9;
pri = 7e-6;
prf = 1/pri;
```

Set up the scenario parameters. The transmitter and receiver are stationary and located at the origin. The targets are 500, 530, and 750 meters from the radar along the $x$-axis. The targets move along the $x$-axis at speeds of $-60,20$, and $40 \mathrm{~m} / \mathrm{s}$. All three targets have a nonfluctuating radar cross-section (RCS) of 10 dB . Create the target and radar platforms.

```
Numtgts = 3;
tgtpos = zeros(Numtgts);
tgtpos(1,:) = [500 530 750];
tgtvel = zeros(3,Numtgts);
tgtvel(1,:) = [-60 20 40];
tgtrcs = db2pow(10)*[1 1 1];
tgtmotion = phased.Platform(tgtpos,tgtvel);
target = phased.RadarTarget('PropagationSpeed',c,'OperatingFrequency',fc, ...
    'MeanRCS',tgtrcs);
radarpos = [0;0;0];
radarvel = [0;0;0];
radarmotion = phased.Platform(radarpos,radarvel);
Create the transmitter and receiver antennas.
```

```
txantenna = phased.IsotropicAntennaElement;
```

txantenna = phased.IsotropicAntennaElement;
rxantenna = clone(txantenna);

```
rxantenna = clone(txantenna);
```

Set up the transmitter-end signal processing. Create an upsweep linear FM signal with a bandwidth of one half the sample rate. Find the length of the PRI in samples and then estimate the rms bandwidth and range resolution.

```
bw = fs/2;
waveform = phased.LinearFMWaveform('SampleRate',fs, ...
    'PRF',prf,'OutputFormat','Pulses','NumPulses',1,'SweepBandwidth',fs/2, ...
    'DurationSpecification','Duty cycle','DutyCycle',0.02);
sig = waveform();
Nr = length(sig);
bwrms = bandwidth(waveform)/sqrt(12);
rngrms = c/bwrms;
```

Set up the transmitter and radiator System object properties. The peak output power is 10 W and the transmitter gain is 36 dB .

```
peakpower = 10;
txgain = 36.0;
transmitter = phased.Transmitter( ...
    'PeakPower',peakpower, ...
    'Gain',txgain, ...
    'InUse0utputPort',true);
radiator = phased.Radiator( ...
    'Sensor',txantenna,...
    'PropagationSpeed ',c,...
    'OperatingFrequency',fc);
```

Set up the free-space channel in two-way propagation mode.

```
channel = phased.FreeSpace( ...
    'SampleRate',fs, ...
    'PropagationSpeed',c, ...
    'OperatingFrequency',fc, ...
    'TwoWayPropagation',true);
```

Set up the receiver-end processing. Set the receiver gain and noise figure.

```
collector = phased.Collector( ...
    'Sensor',rxantenna, ...
    'PropagationSpeed',c, ...
    'OperatingFrequency',fc);
rxgain = 42.0;
noisefig = 1;
receiver = phased.ReceiverPreamp( ...
    'SampleRate',fs, ...
    'Gain',rxgain, ...
    'NoiseFigure',noisefig);
```

Loop over the pulses to create a data cube of 128 pulses. For each step of the loop, move the target and propagate the signal. Then put the received signal into the data cube. The data cube contains the received signal per pulse. Ordinarily, a data cube has three dimensions where the last dimension corresponds to antennas or beams. Because only one sensor is used, the cube has only two dimensions.

The processing steps are:
1 Move the radar and targets.

2 Transmit a waveform.
3 Propagate the waveform signal to the target.
4 Reflect the signal from the target.
5 Propagate the waveform back to the radar. Two-way propagation enables you to combine the return propagation with the outbound propagation.
6 Receive the signal at the radar.
7 Load the signal into the data cube.

```
Np = 128;
dt = pri;
cube = zeros(Nr,Np);
for n = 1:Np
    [sensorpos,sensorvel] = radarmotion(dt);
    [tgtpos,tgtvel] = tgtmotion(dt);
    [tgtrng,tgtang] = rangeangle(tgtpos,sensorpos);
    sig = waveform();
    [txsig,txstatus] = transmitter(sig);
    txsig = radiator(txsig,tgtang);
    txsig = channel(txsig,sensorpos,tgtpos,sensorvel,tgtvel);
    tgtsig = target(txsig);
    rxcol = collector(tgtsig,tgtang);
    rxsig = receiver(rxcol);
    cube(:,n) = rxsig;
end
```

Display the data cube containing signals per pulse.

```
imagesc([0:(Np-1)]*pri*1e6,[0:(Nr-1)]/fs*1e6,abs(cube))
xlabel('Slow Time {\mu}s')
ylabel('Fast Time {\mu}s')
axis xy
```



Create and display the range-Doppler image for 128 Doppler bins. The image shows range vertically and speed horizontally. Use the linear FM waveform for match filtering. The image is here is the range-Doppler map.

```
ndop = 128;
rangedopresp = phased.RangeDopplerResponse('SampleRate',fs, ...
    'PropagationSpeed',c,'DopplerFFTLengthSource','Property', ...
    'DopplerFFTLength',ndop,'DopplerOutput','Speed', ...
    'OperatingFrequency',fc);
matchingcoeff = getMatchedFilter(waveform);
[rngdopresp,rnggrid,dopgrid] = rangedopresp(cube,matchingcoeff);
imagesc(dopgrid,rnggrid,10*log10(abs(rngdopresp)))
xlabel('Closing Speed (m/s)')
ylabel('Range (m)')
axis xy
```



Because the targets lie along the positive $x$-axis, positive velocity in the global coordinate system corresponds to negative closing speed. Negative velocity in the global coordinate system corresponds to positive closing speed.

Estimate the noise power after matched filtering. Create a constant noise background image for simulation purposes.

```
mfgain = matchingcoeff'*matchingcoeff;
dopgain = Np;
noisebw = fs;
noisepower = noisepow(noisebw,receiver.NoiseFigure,receiver.ReferenceTemperature);
noisepowerprc = mfgain*dopgain*noisepower;
noise = noisepowerprc*ones(size(rngdopresp));
Create the range and Doppler estimator objects.
```

```
rangeestimator = phased.RangeEstimator('NumEstimatesSource','Auto', ...
```

rangeestimator = phased.RangeEstimator('NumEstimatesSource','Auto', ...
'VarianceOutputPort',true,'NoisePowerSource','Input port', ...
'VarianceOutputPort',true,'NoisePowerSource','Input port', ...
'RMSResolution',rngrms);
'RMSResolution',rngrms);
dopestimator = phased.DopplerEstimator('VarianceOutputPort',true, ...
dopestimator = phased.DopplerEstimator('VarianceOutputPort',true, ...
'NoisePowerSource','Input port','NumPulses',Np);

```
    'NoisePowerSource','Input port','NumPulses',Np);
```

Locate the target indices in the range-Doppler image. Instead of using a CFAR detector, for simplicity, use the known locations and speeds of the targets to obtain the corresponding index in the rangeDoppler image.

```
detidx = NaN(2,Numtgts);
tgtrng = rangeangle(tgtpos,radarpos);
```

```
tgtspd = radialspeed(tgtpos,tgtvel,radarpos,radarvel);
tgtdop = 2*speed2dop(tgtspd,c/fc);
for m = 1:numel(tgtrng)
    [~,iMin] = min(abs(rnggrid-tgtrng(m)));
    detidx(1,m) = iMin;
    [~,iMin] = min(abs(dopgrid-tgtspd(m)));
    detidx(2,m) = iMin;
end
```

Find the noise power at the detection locations.

```
ind = sub2ind(size(noise),detidx(1,:),detidx(2,:));
```

Estimate the range and range variance at the detection locations. The estimated ranges agree with the postulated ranges.

```
[rngest,rngvar] = rangeestimator(rngdopresp,rnggrid,detidx,noise(ind))
rngest = 3x1
    499.7911
    529.8380
    750.0983
rngvar = 3x1
10-4 x
    0.0273
    0.0276
    0.2094
```

Estimate the speed and speed variance at the detection locations. The estimated speeds agree with the predicted speeds.

```
[spdest,spdvar] = dopestimator(rngdopresp,dopgrid,detidx,noise(ind))
spdest = 3\times1
    60.5241
    -19.6167
    -39.5838
spdvar = 3x1
10-5 x
    0.0806
    0.0816
    0.6188
```


## Algorithms

## Estimation Algorithm

The phased. DopplerEstimator System object estimates the Doppler frequency of a detection by following these steps of the Doppler estimator are

1 Input a Doppler-processed response data cube obtained from the
phased. RangeDopplerResponse System object. The first dimension of the cube represents the fast-time or equivalent range of the returned signal samples. The second dimension represents the spatial information, such as sensors or beams. The last dimension represents the response as a function of Doppler frequency. Only this dimension is used to estimate detection Doppler frequency. All others are ignored. See "Radar Data Cube".
2 Input the matrix of detection indices that specify the location of detections in the data cube. Each column denotes a separate detection. The row entries designate indices into the data cube. To return these detection indices as an output of the phased. CFARDetector or phased. CFARDetector2D detectors. To return these indices, set the detector OutputFormat property of either CFAR detector to 'Detection index'.
3 Optionally input a row vector of cluster IDs. This vector is equal in length to the number of detections. Each element of this vector assigns an ID to a corresponding detection. To form clusters of detections, the same ID can be assigned to more than one detection. To enable this option, set the ClusterInputPort property to true.
4 When ClusterInputPort is false, the object computes Doppler frequencies for each detection. The algorithm finds the response values at the detection index and at two adjacent indices in the cube along the Doppler dimension. Then, the algorithm fits a quadratic curve to the magnitudes of the Doppler response at these three indices. The peak of the curve indicates the detection location. When detections occur at the first or last sample in the Doppler dimension, the object estimates the detection location from a two-point centroid. The centroid is formed using the location of the detection index and the sample next to the detection index.

When the object computes Doppler frequencies for each cluster. The algorithm finds the indices of the largest response value in the cluster. Then, the algorithm fits a quadratic curve to that detection in the same way as for individual detections.
5 The object converts the fractional index values to Doppler frequency or speed by using appropriate units from the dopgrid input argument of the step method. You can obtain values for dopgrid using the phased. RangeDopplerResponse System object.

## Data Precision

This System object supports single and double precision for input data, properties, and arguments. If the input data $X$ is single precision, the output data is single precision. If the input data $X$ is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

## Version History <br> Introduced in R2017a

## References

[1] Richards, M. Fundamentals of Radar Signal Processing. 2nd ed. McGraw-Hill Professional Engineering, 2014.
[2] Richards, M., J. Scheer, and W. Holm, Principles of Modern Radar: Basic Principles. SciTech Publishing, 2010.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\text {TM }}$.
Usage notes and limitations:

- See "System Objects in MATLAB Code Generation" (MATLAB Coder).

This System object supports single and double precision for input data, properties, and arguments. If the input data X is single precision, the output data is single precision. If the input data X is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

## See Also

## Functions

rangeangle | dop2speed | speed2dop | range2bw | bw2 range
Objects
phased.RangeEstimator|phased.RangeDopplerResponse|phased.CFARDetector| phased.CFARDetector2D

## Topics

"Radar Data Cube"

## step

System object: phased. DopplerEstimator
Package: phased
Estimate target Doppler

## Syntax

```
dopest = step(estimator,resp,dopgrid,detidx)
[dopest,dopvar] = step(estimator,resp,dopgrid,detidx,noisepower)
[dopest,dopvar] = step(estimator,resp,dopgrid,detidx,clusterids)
[dopest,dopvar] = step(estimator,resp,dopgrid,detidx,noisepower,clusterids)
```


## Description

Note Instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj,x) and y = obj $(x)$ perform equivalent operations.
dopest = step(estimator, resp,dopgrid,detidx) estimates Doppler frequencies of detections derived from the range-Doppler response data, resp. Doppler estimates are computed for each detection position reported in detidx. The dopgrid argument sets the units for the Doppler dimension of the response data cube.
[dopest,dopvar] = step(estimator,resp,dopgrid,detidx, noisepower) also specifies the noise power. This syntax applies when you set the VarianceOutputPort property to true and the NoisePowerSource property to 'Input port'.
[dopest,dopvar] = step(estimator, resp,dopgrid,detidx,clusterids) also specifies the clusterids for the detections. This syntax applies when you set the ClusterInputPort property to true.

You can combine optional input and output arguments when their enabling properties are set. Optional inputs and outputs must be listed in the same order as the order of the enabling properties. For example, [dopest,dopvar] = step(estimator, resp,dopgrid,detidx, noisepower, clusterids).

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

estimator - Doppler estimator
phased.DopplerEstimator System object

Doppler estimator, specified as a phased.DopplerEstimator System object.

## Example: phased.DopplerEstimator

## resp - Doppler-processed response data cube

complex-valued $P$-by-1 column vector | complex-valued $M$-by- $P$ matrix | complex-valued $M$-by- $N$-by- $P$ array

Doppler-processed response data cube, specified as a complex-valued $P$-by- 1 column vector, a complex-valued $M$-by- $P$ matrix, or a complex-valued $M$-by- $N$-by- $P$ array. $M$ represents the number of fast-time or range samples. $N$ is the number of spatial elements, such as sensor elements or beams. $P$ is the number of Doppler bins.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
Data Types: single | double

## dopgrid - Doppler grid values along Doppler dimension <br> real-valued $P$-by-1 column vector

Doppler grid values along the Doppler dimension of the resp argument, specified as a real-valued $P$ -by-1 column vector. dopgrid defines the Doppler values corresponding to the Doppler dimension of the resp argument. Doppler values must be monotonically increasing and equally spaced. You can specify the grid values to be velocity or frequency. Units are in hertz or meters/sec.
Example: [-0.3,-0.2,-0.1,0,0.1,0.2,0.3]
Data Types: single | double

## detidx - Detection indices

real-valued $N_{d}$-by- $Q$ matrix
Detection indices, specified as a real-valued $N_{d}$-by- $Q$ matrix. $Q$ is the number of detections and $N_{d}$ is the number of dimensions of the response data cube, resp. Each column of detidx contains the $N_{d}$ indices of the detection in the response data cube.

To generate detection indices, you can use the phased. CFARDetector or phased.CFARDetector2D objects.
Data Types: single | double

## noisepower - Noise power at detection locations

positive scalar | real-valued 1-by-Q row vector of positive values
Noise power at detection locations, specified as a positive scalar or real-valued 1-by-Q row vector of positive values. $Q$ is the number of detections specified in detidx.

## Dependencies

To enable this input argument, set the NoisePowerSource property to Input port.
Data Types: single | double
clusterids - Cluster IDs
real-valued 1-by-Q row vector of positive values

Cluster IDs, specified as a real-valued 1-by- $Q$ row vector where $Q$ is the number of detections specified in detidx. Each element of clusterids corresponds to a column in detidx. Detections with the same cluster ID belong to the same cluster.

## Dependencies

To enable this input argument, set the ClusterInputPort property to true.
Data Types: single|double

## Output Arguments

## dopest - Doppler estimates

real-valued $K$-by-1 column vector
Doppler estimates, returned as a real-valued $K$-by- 1 column vector.

- When ClusterInputPort is false, Doppler estimates are computed for each detection location in the detidx argument. Then $K$ equals the column dimension, $Q$, of detidx.
- When ClusterInputPort is true, Doppler estimates are computed for each cluster ID in the clusterids argument. Then $K$ equals the number of unique cluster IDs, $Q$.

Data Types: single | double

## dopvar - Doppler estimation variance

positive, real-valued $K$-by- 1 column vector
Doppler estimation variance, returned as a positive, real-valued $K$-by- 1 column vector, where $K$ is the dimension of dopest. Each element of dopvar corresponds to an element of dopest. The estimator variance is computed using the Ziv-Zakai bound.
Data Types: single | double

## Examples

## Estimate Range and Speed of Three Targets

To estimate the range and speed of three targets, create a range-Doppler map using the phased.RangeDopplerResponse System object ${ }^{\text {TM }}$. Then use the phased.RangeEstimator and phased.DopplerEstimator System objects to estimate range and speed. The transmitter and receiver are collocated isotropic antenna elements forming a monostatic radar system.

The transmitted signal is a linear FM waveform with a pulse repetition interval (PRI) of 7.0 s and a duty cycle of $2 \%$. The operating frequency is 77 GHz and the sample rate is 150 MHz .

```
fs = 150e6;
c = physconst('LightSpeed');
fc = 77.0e9;
pri = 7e-6;
prf = 1/pri;
```

Set up the scenario parameters. The transmitter and receiver are stationary and located at the origin. The targets are 500, 530, and 750 meters from the radar along the $x$-axis. The targets move along the
$x$-axis at speeds of $-60,20$, and $40 \mathrm{~m} / \mathrm{s}$. All three targets have a nonfluctuating radar cross-section (RCS) of 10 dB . Create the target and radar platforms.

```
Numtgts = 3;
tgtpos = zeros(Numtgts);
tgtpos(1,:) = [500 530 750];
tgtvel = zeros(3,Numtgts);
tgtvel(1,:) = [-60 20 40];
tgtrcs = db2pow(10)*[ll 1 1];
tgtmotion = phased.Platform(tgtpos,tgtvel);
target = phased.RadarTarget('PropagationSpeed',c,'OperatingFrequency',fc, ...
    'MeanRCS',tgtrcs);
radarpos = [0;0;0];
radarvel = [0;0;0];
radarmotion = phased.Platform(radarpos,radarvel);
```

Create the transmitter and receiver antennas.

```
txantenna = phased.IsotropicAntennaElement;
rxantenna = clone(txantenna);
```

Set up the transmitter-end signal processing. Create an upsweep linear FM signal with a bandwidth of one half the sample rate. Find the length of the PRI in samples and then estimate the rms bandwidth and range resolution.

```
bw = fs/2;
waveform = phased.LinearFMWaveform('SampleRate',fs, ...
    'PRF',prf,'OutputFormat','Pulses','NumPulses',1,'SweepBandwidth',fs/2, ...
    'DurationSpecification','Duty cycle','DutyCycle',0.02);
sig = waveform();
Nr = length(sig);
bwrms = bandwidth(waveform)/sqrt(12);
rngrms = c/bwrms;
```

Set up the transmitter and radiator System object properties. The peak output power is 10 W and the transmitter gain is 36 dB .

```
peakpower = 10;
txgain = 36.0;
transmitter = phased.Transmitter( ...
    'PeakPower',peakpower, ...
    'Gain',txgain, ...
    'InUseOutputPort',true);
radiator = phased.Radiator( ...
    'Sensor',txantenna,...
    'PropagationSpeed',c,...
    'OperatingFrequency',fc);
```

Set up the free-space channel in two-way propagation mode.

```
channel = phased.FreeSpace( ...
    'SampleRate',fs, ...
    'PropagationSpeed',c, ...
    'OperatingFrequency',fc, ...
    'TwoWayPropagation',true);
```

Set up the receiver-end processing. Set the receiver gain and noise figure.

```
collector = phased.Collector( ...
    'Sensor',rxantenna, ...
    'PropagationSpeed',c, ...
    'OperatingFrequency',fc);
rxgain = 42.0;
noisefig = 1;
receiver = phased.ReceiverPreamp( ...
    'SampleRate',fs, ...
    'Gain',rxgain, ...
    'NoiseFigure',noisefig);
```

Loop over the pulses to create a data cube of 128 pulses. For each step of the loop, move the target and propagate the signal. Then put the received signal into the data cube. The data cube contains the received signal per pulse. Ordinarily, a data cube has three dimensions where the last dimension corresponds to antennas or beams. Because only one sensor is used, the cube has only two dimensions.

The processing steps are:
1 Move the radar and targets.
2 Transmit a waveform.
3 Propagate the waveform signal to the target.
4 Reflect the signal from the target.
5 Propagate the waveform back to the radar. Two-way propagation enables you to combine the return propagation with the outbound propagation.
6 Receive the signal at the radar.
7 Load the signal into the data cube.

```
Np = 128;
dt = pri;
cube = zeros(Nr,Np);
for n = 1:Np
    [sensorpos,sensorvel] = radarmotion(dt);
    [tgtpos,tgtvel] = tgtmotion(dt);
    [tgtrng,tgtang] = rangeangle(tgtpos,sensorpos);
    sig = waveform();
    [txsig,txstatus] = transmitter(sig);
    txsig = radiator(txsig,tgtang);
    txsig = channel(txsig,sensorpos,tgtpos,sensorvel,tgtvel);
    tgtsig = target(txsig);
    rxcol = collector(tgtsig,tgtang);
    rxsig = receiver(rxcol);
    cube(:,n) = rxsig;
end
```

Display the data cube containing signals per pulse.

```
imagesc([0:(Np-1)]*pri*1e6,[0:(Nr-1)]/fs*1e6,abs(cube))
xlabel('Slow Time {\mu}s')
ylabel('Fast Time {\mu}s')
axis xy
```



Create and display the range-Doppler image for 128 Doppler bins. The image shows range vertically and speed horizontally. Use the linear FM waveform for match filtering. The image is here is the range-Doppler map.

```
ndop = 128;
rangedopresp = phased.RangeDopplerResponse('SampleRate',fs, ...
    'PropagationSpeed',c,'DopplerFFTLengthSource','Property', ...
    'DopplerFFTLength',ndop,'DopplerOutput','Speed', ...
    'OperatingFrequency',fc);
matchingcoeff = getMatchedFilter(waveform);
[rngdopresp,rnggrid,dopgrid] = rangedopresp(cube,matchingcoeff);
imagesc(dopgrid,rnggrid,10*log10(abs(rngdopresp)))
xlabel('Closing Speed (m/s)')
ylabel('Range (m)')
axis xy
```



Because the targets lie along the positive $x$-axis, positive velocity in the global coordinate system corresponds to negative closing speed. Negative velocity in the global coordinate system corresponds to positive closing speed.

Estimate the noise power after matched filtering. Create a constant noise background image for simulation purposes.

```
mfgain = matchingcoeff'*matchingcoeff;
dopgain = Np;
noisebw = fs;
noisepower = noisepow(noisebw,receiver.NoiseFigure,receiver.ReferenceTemperature);
noisepowerprc = mfgain*dopgain*noisepower;
noise = noisepowerprc*ones(size(rngdopresp));
Create the range and Doppler estimator objects.
```

```
rangeestimator = phased.RangeEstimator('NumEstimatesSource','Auto', ...
```

rangeestimator = phased.RangeEstimator('NumEstimatesSource','Auto', ...
'VarianceOutputPort',true,'NoisePowerSource','Input port', ...
'VarianceOutputPort',true,'NoisePowerSource','Input port', ...
'RMSResolution',rngrms);
'RMSResolution',rngrms);
dopestimator = phased.DopplerEstimator('VarianceOutputPort',true, ...
dopestimator = phased.DopplerEstimator('VarianceOutputPort',true, ...
'NoisePowerSource','Input port','NumPulses',Np);

```
    'NoisePowerSource','Input port','NumPulses',Np);
```

Locate the target indices in the range-Doppler image. Instead of using a CFAR detector, for simplicity, use the known locations and speeds of the targets to obtain the corresponding index in the rangeDoppler image.

```
detidx = NaN(2,Numtgts);
tgtrng = rangeangle(tgtpos,radarpos);
```

```
tgtspd = radialspeed(tgtpos,tgtvel,radarpos,radarvel);
tgtdop = 2*speed2dop(tgtspd,c/fc);
for m = 1:numel(tgtrng)
    [~,iMin] = min(abs(rnggrid-tgtrng(m)));
    detidx(1,m) = iMin;
    [~,iMin] = min(abs(dopgrid-tgtspd(m)));
    detidx(2,m) = iMin;
end
```

Find the noise power at the detection locations.

```
ind = sub2ind(size(noise),detidx(1,:),detidx(2,:));
```

Estimate the range and range variance at the detection locations. The estimated ranges agree with the postulated ranges.

```
[rngest,rngvar] = rangeestimator(rngdopresp,rnggrid,detidx,noise(ind))
rngest = 3\times1
```

    499.7911
    529.8380
    750.0983
    rngvar $=3 \times 1$
$10^{-4} \times$
0.0273
0.0276
0.2094

Estimate the speed and speed variance at the detection locations. The estimated speeds agree with the predicted speeds.

```
[spdest,spdvar] = dopestimator(rngdopresp,dopgrid,detidx,noise(ind))
spdest = 3\times1
    60.5241
    -19.6167
    -39.5838
spdvar = 3\times1
10-5 x
    0.0806
    0.0816
    0.6188
```


## Version History

Introduced in R2017a

# phased.DPCACanceller 

Package: phased

Displaced phase center array (DPCA) pulse canceller

## Description

The DPCACanceller object implements a displaced phase center array pulse canceller for a uniform linear array (ULA).

To compute the output signal of the space time pulse canceller:
1 Define and set up your DPCA pulse canceller. See "Construction" on page 1-400.
2 Call step to execute the DPCA algorithm according to the properties of phased.DPCACanceller. The behavior of step is specific to each object in the toolbox.

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step $(o b j, x)$ and $y=o b j(x)$ perform equivalent operations.

## Construction

H = phased.DPCACanceller creates a displaced phase center array (DPCA) canceller System object, H. The object performs two-pulse DPCA processing on the input data.

H = phased.DPCACanceller(Name,Value) creates a DPCA object, H, with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN).

## Properties

## SensorArray

Uniform linear array
Uniform linear array, specified as a phased.ULA System object.
Default: phased.ULA with default property values

## PropagationSpeed

Signal propagation speed
Specify the propagation speed of the signal, in meters per second, as a positive scalar. You can specify this property as single or double precision.

Default: Speed of light

## OperatingFrequency

System operating frequency
Specify the operating frequency of the system in hertz as a positive scalar. The default value corresponds to 300 MHz . You can specify this property as single or double precision.

Default: 3e8

## PRFSource

Source of pulse repetition frequency
Source of the PRF values for the STAP processor, specified as 'Property ' or 'Input port '. When you set this property to 'Property' , the PRF is determined by the value of the PRF property. When you set this property to 'Input port', the PRF is determined by an input argument to the step method at execution time.

Default: 'Property'
PRF
Pulse repetition frequency
Pulse repetition frequency (PRF) of the received signal, specified as a positive scalar. Units are in Hertz. This property can be specified as single or double precision.

## Dependencies

To enable this property, set the PRFSource property to 'Property '.
Default: 1

## DirectionSource

Source of receiving mainlobe direction
Specify whether the targeting direction for the STAP processor comes from the Direction property of this object or from an input argument in step. Values of this property are:

| 'Property' | The Direction property of this object specifies the targeting <br> direction. |
| :--- | :--- |
| 'Input port' | An input argument in each invocation of step specifies the <br> targeting direction. |

## Default: 'Property'

## Direction

Receiving mainlobe direction
Specify the receiving mainlobe direction of the receiving sensor array as a column vector of length 2 . The direction is specified in the format of [AzimuthAngle; ElevationAngle] (in degrees). The azimuth angle should be between $-180^{\circ}$ and $180^{\circ}$. The elevation angle should be between $-90^{\circ}$ and $90^{\circ}$. This property applies when you set the DirectionSource property to 'Property '. You can specify this argument as single or double precision.

Default: [0; 0]

## NumPhaseShifterBits

Number of phase shifter quantization bits
The number of bits used to quantize the phase shift component of beamformer or steering vector weights. Specify the number of bits as a non-negative integer. A value of zero indicates that no quantization is performed. You can specify this property as single or double precision.

## Default: 0

## DopplerSource

Source of targeting Doppler
Specify whether the targeting Doppler for the STAP processor comes from the Doppler property of this object or from an input argument in step. Values of this property are:

| 'Property' | The Doppler property of this object specifies the Doppler. |
| :--- | :--- |
| 'Input port' | An input argument in each invocation of step specifies the Doppler. |
| Default: 'Property' |  |
| Doppler |  |

Targeting Doppler frequency (hertz)
Specify the targeting Doppler of the STAP processor as a scalar. This property applies when you set the DopplerSource property to 'Property'. You can specify this property as single or double precision.

## Default: 0

## WeightsOutputPort

Output processing weights
To obtain the weights used in the STAP processor, set this property to true and use the corresponding output argument when invoking step. If you do not want to obtain the weights, set this property to false.

Default: false

## PreDopplerOutput

Output pre-Doppler result
Set this property to true to output the processing result before applying the Doppler filtering. Set this property to false to output the processing result after the Doppler filtering.

Default: false

## Methods

step $\quad$ Perform DPCA processing on input data

## Common to All System Objects

release Allow System object property value changes

## Examples

## Process Data Cube Using DPCA

Process a data cube using a DPCA processor. The weights are calculated for the 71st cell of the collected data cube. The look direction is $(0,0)$ degrees and the Doppler shift is 12.980 kHz .

```
load STAPExampleData;
Hs = phased.DPCACanceller('SensorArray',STAPEx_HArray,...
    'PRF',STAPEx PRF,...
    'PropagationSpeed',STAPEx_PropagationSpeed,...
    'OperatingFrequency',STAPEx_OperatingFrequency,...
    'Weights0utputPort',true,...
    'DirectionSource','Input port',...
    'DopplerSource','Input port');
[y,w] = step(Hs,STAPEx_ReceivePulse,71,[0;0],12.980e3);
sAngDop = phased.AngleDopplerResponse(...
    'SensorArray',Hs.SensorArray,...
    'OperatingFrequency',Hs.OperatingFrequency,...
    'PRF',Hs.PRF,...
    'PropagationSpeed',Hs.PropagationSpeed);
plotResponse(sAngDop,w)
```



## Algorithms

## Single Precision

This System object supports single and double precision for input data, properties, and arguments. If the input data $X$ is single precision, the output data is single precision. If the input data $X$ is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

## Version History

Introduced in R2011a

## References

[1] Guerci, J. R. Space-Time Adaptive Processing for Radar. Boston: Artech House, 2003.
[2] Ward, J. "Space-Time Adaptive Processing for Airborne Radar Data Systems," Technical Report 1015, MIT Lincoln Laboratory, December, 1994.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.
Usage notes and limitations:

## See Also

phased.ADPCACanceller|phased.AngleDopplerResponse | phased.STAPSMIBeamformer| uv2azel | phitheta2azel

## step

System object: phased. DPCACanceller
Package: phased
Perform DPCA processing on input data

## Syntax

$Y=\operatorname{step}(H, X, C U T I D X)$
Y = step(H,X,CUTIDX,ANG)
Y = step(H,X,CUTIDX,DOP)
Y = step(H,X,CUTIDX, PRF)
[ $\mathrm{Y}, \mathrm{W}$ ] = step( $\qquad$ )

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.
$Y=$ step (H,X, CUTIDX) applies the DPCA pulse cancellation algorithm to the input data $X$. The algorithm calculates the processing weights according to the range cell specified by CUTIDX. This syntax is available when the DirectionSource property is 'Property' and the DopplerSource property is 'Property '. The receiving mainlobe direction is the Direction property value. The output $Y$ contains the result of pulse cancellation either before or after Doppler filtering, depending on the PreDopplerOutput property value.
$Y=$ step ( $\mathrm{H}, \mathrm{X}$, CUTIDX, ANG) uses ANG as the receiving main lobe direction. This syntax is available when the DirectionSource property is 'Input port' and the DopplerSource property is 'Property'.

Y = step (H,X,CUTIDX, DOP) uses DOP as the targeting Doppler frequency. This syntax is available when the DopplerSource property is 'Input port'.
$\mathrm{Y}=\operatorname{step}(\mathrm{H}, \mathrm{X}, \mathrm{CUTIDX}, \mathrm{PRF})$ uses PRF as the pulse repetition frequency. This syntax is available when the PRFSource property is 'Input port'.
$[\mathrm{Y}, \mathrm{W}]=\operatorname{step}(\ldots \quad$ ) also returns the processing weights, W . This syntax is available when the WeightsOutputPort property is true.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## H

Pulse canceller object.

## X

Input data. X must be a 3 -dimensional M -by-N-by-P numeric array whose dimensions are (range, channels, pulses). You can specify this argument as single or double precision.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

## CUTIDX

Range cell. You can specify this argument as single or double precision.

## PRF

Pulse repetition frequency specified as a positive scalar. To enable this argument, set the PRFSource property to 'Input port'. You can specify this argument as single or double precision. Units are in Hertz.

## ANG

Receiving main lobe direction. ANG must be a 2-by-1 vector in the form [AzimuthAngle; ElevationAngle], in degrees. The azimuth angle must be between -180 and 180. The elevation angle must be between -90 and 90 . You can specify this argument as single or double precision.

Default: Direction property of H

## DOP

Targeting Doppler frequency in hertz. DOP must be a scalar. You can specify this argument as single or double precision.

Default: Doppler property of H

## Output Arguments

## Y

Result of applying pulse cancelling to the input data. The meaning and dimensions of $Y$ depend on the PreDopplerOutput property of H :

- If PreDopplerOutput is true, Y contains the pre-Doppler data. Y is an M -by-(P-1) matrix. Each column in $Y$ represents the result obtained by cancelling the two successive pulses.
- If PreDopplerOutput is false, $Y$ contains the result of applying an FFT-based Doppler filter to the pre-Doppler data. The targeting Doppler is the Doppler property value. Y is a column vector of length M .


## W

Processing weights the pulse canceller used to obtain the pre-Doppler data. The dimensions of W depend on the PreDopplerOutput property of H :

- If PreDopplerOutput is true, W is a 2 N -by-(P-1) matrix. The columns in W correspond to successive pulses in $X$.
- If PreDopplerOutput is false, $W$ is a column vector of length ( $\mathrm{N}^{*} \mathrm{P}$ ).


## Examples

## Process Data Cube Using DPCA

Process a data cube using a DPCA processor. The weights are calculated for the 71st cell of the collected data cube. The look direction is $(0,0)$ degrees and the Doppler shift is 12.980 kHz .

```
load STAPExampleData;
Hs = phased.DPCACanceller('SensorArray',STAPEx_HArray,...
    'PRF',STAPEx_PRF,...
    'PropagationSpeed',STAPEx_PropagationSpeed,...
    'OperatingFrequency', STAPE\overline{Ex_OperatingFrequency,...}
    'WeightsOutputPort',true,...
    'DirectionSource','Input port',...
    'DopplerSource','Input port');
[y,w] = step(Hs,STAPEx_ReceivePulse,71,[0;0],12.980e3);
sAngDop = phased.AngleDopplerResponse(...
    'SensorArray',Hs.SensorArray,...
    'OperatingFrequency',Hs.OperatingFrequency,...
    'PRF',Hs.PRF,...
    'PropagationSpeed',Hs.PropagationSpeed);
plotResponse(sAngDop,w)
```



## See Also

uv2azel| phitheta2azel

## phased.ElementDelay

Package: phased
Sensor array element delay estimator

## Description

The ElementDelay object calculates the signal delay for elements in an array.
To compute the signal delay across the array elements:
1 Define and set up your element delay estimator. See "Construction" on page 1-410.
2 Call step to estimate the delay according to the properties of phased.ElementDelay. The behavior of step is specific to each object in the toolbox.

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.

## Construction

H = phased.ElementDelay creates an element delay estimator System object, H. The object calculates the signal delay for elements in an array when the signal arrives the array from specified directions. By default, a 2-element uniform linear array (ULA) is used.

H = phased.ElementDelay(Name, Value) creates object, H, with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN).

## Properties

## SensorArray

Handle to sensor array used to calculate the delay
Specify the sensor array as a handle. The sensor array must be an array object in the phased package. The array cannot contain subarrays.

Default: phased.ULA with default property values

## PropagationSpeed

Signal propagation speed
Specify the propagation speed of the signal, in meters per second, as a positive scalar. You can specify this property as single or double precision.

Default: Speed of light

## Methods

step Calculate delay for elements

## Common to All System Objects

release $\quad$ Allow System object property value changes

## Examples

## Element Delay for Uniform Linear Array

Calculate the element delay for a uniform linear array when the input is impinging on the array from $30^{\circ}$ azimuth and $20^{\circ}$ elevation.

```
array = phased.ULA('NumElements',4);
delay = phased.ElementDelay('SensorArray',array);
tau = delay([30;20])
tau = 4×1
10-8}
    0.1175
    0.0392
    -0.0392
    -0.1175
```


## Algorithms

## Data Precision

This System object supports single and double precision for input data, properties, and arguments.

## Version History

Introduced in R2011a

## References

[1] Van Trees, H. Optimum Array Processing. New York: Wiley-Interscience, 2002.

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® $\mathrm{Coder}^{\mathrm{TM}}$.
Usage notes and limitations:

- See "System Objects in MATLAB Code Generation" (MATLAB Coder).
- This System object supports single and double precision for input data, properties, and arguments.


## See Also

phased.ArrayGain|phased.ArrayResponse|phased.SteeringVector

## step

System object: phased.ElementDelay
Package: phased
Calculate delay for elements

## Syntax

TAU = step(H,ANG)

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.

TAU $=\operatorname{step}(\mathrm{H}, \mathrm{ANG})$ returns the delay TAU of each element relative to the array's phase center for the signal incident directions specified by ANG.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## H

Element delay object.

## ANG

Signal incident directions in degrees. ANG can be either a 2-by-M matrix or a row vector of length M. This argument can be single or double precision.

If ANG is a 2 -by-M matrix, each column of the matrix specifies the direction in the form [azimuth; elevation]. The azimuth angle must be between -180 and 180 degrees, inclusive. The elevation angle must be between -90 and 90 degrees, inclusive.

If ANG is a row vector of length M , each element specifies a direction's azimuth angle. In this case, the corresponding elevation angle is assumed to be 0 .

## Output Arguments

## TAU

Delay in seconds.TAU is an N-by-M matrix, where N is the number of elements in the array. Each column of TAU contains the delays of the array elements for the corresponding direction specified in ANG. This argument can be single or double precision.

## Examples

## Element Delay for Uniform Linear Array

Calculate the element delay for a uniform linear array when the input is impinging on the array from $30^{\circ}$ azimuth and $20^{\circ}$ elevation.

```
array = phased.ULA('NumElements',4);
delay = phased.ElementDelay('SensorArray',array);
tau = delay([30;20])
tau = 4×1
10-8}
    0.1175
    0.0392
    -0.0392
    -0.1175
```


## See Also

uv2azel | phitheta2azel

## phased.ESPRITEstimator

Package: phased
ESPRIT direction of arrival (DOA) estimator for ULA

## Description

The phased.ESPRITEstimator System object estimate the direction of arrival of signals parameters via rotational invariance (ESPRIT) direction of arrival estimate.

To estimate the direction of arrival (DOA):
1 Define and set up your DOA estimator. See "Construction" on page 1-415.
2 Call step to estimate the DOA according to the properties of phased.ESPRITEstimator. The behavior of step is specific to each object in the toolbox.

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, x ) and $\mathrm{y}=\mathrm{obj}(\mathrm{x})$ perform equivalent operations.

## Construction

H = phased.ESPRITEstimator creates an ESPRIT DOA estimator System object, H. The object estimates the signal's direction-of-arrival (DOA) using the ESPRIT algorithm with a uniform linear array (ULA).

H = phased.ESPRITEstimator(Name,Value) creates object, H, with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN).

## Properties

## SensorArray

Handle to sensor array
Specify the sensor array as a handle. The sensor array must be a phased. ULA object.
Default: phased.ULA with default property values

## PropagationSpeed

Signal propagation speed
Specify the propagation speed of the signal, in meters per second, as a positive scalar. You can specify this property as single or double precision.

Default: Speed of light

## OperatingFrequency

System operating frequency
Specify the operating frequency of the system in hertz as a positive scalar. The default value corresponds to 300 MHz . You can specify this property as single or double precision.

## Default: 3e8

## ForwardBackwardAveraging

Perform forward-backward averaging
Set this property to true to use forward-backward averaging to estimate the covariance matrix for sensor arrays with conjugate symmetric array manifold.

Default: false
SpatialSmoothing
Spatial smoothing
Specify the number of averaging used by spatial smoothing to estimate the covariance matrix as a nonnegative integer. Each additional smoothing handles one extra coherent source, but reduces the effective number of element by 1. The maximum value of this property is $\mathrm{M}-2$, where M is the number of sensors. You can specify this property as single or double precision.

Default: 0, indicating no spatial smoothing

## NumSignalsSource

Source of number of signals
Specify the source of the number of signals as one of 'Auto' or 'Property '. If you set this property to 'Auto', the number of signals is estimated by the method specified by the NumSignalsMethod property.

## Default: 'Auto'

## NumSignalsMethod

Method to estimate number of signals
Specify the method to estimate the number of signals as one of 'AIC' or 'MDL'. The 'AIC' uses the Akaike Information Criterion and the 'MDL' uses Minimum Description Length criterion. This property applies when you set the NumSignalsSource property to 'Auto'.

Default: 'AIC'

## NumSignals

Number of signals
Specify the number of signals as a positive integer scalar. This property applies when you set the NumSignalsSource property to 'Property'. The number of signals, $N_{\text {sig }}$, must be smaller than the number of elements, $N_{\text {sub }}$, in the subarray derived from the array specified in the SensorArray
property. See "ESPRIT Subarrays" on page 1-418. You can specify this property as single or double precision.

## Default: 1

## Method

Type of least squares method
Specify the least squares method used for ESPRIT as one of 'TLS' or 'LS'. 'TLS' refers to total least squares and 'LS' refers to least squares.

Default: 'TLS'
RowWeighting
Row weighting factor
Specify the row weighting factor for signal subspace eigenvectors as a positive integer scalar. This property controls the weights applied to the selection matrices. In most cases the higher value the better. However, it can never be greater than (Nsub-1)/2 where Nsub is the number of elements in the subarray derived from the array specified in the SensorArray property. See "ESPRIT Subarrays" on page 1-418. You can specify this property as single or double precision.

## Default: 1

## Methods

step Perform DOA estimation

## Common to All System Objects

release Allow System object property value changes

## Examples

## Estimate DOAs of Two Signals

Estimate the directions-of-arrival (DOA) of two signals received by a standard 10 -element ULA with element spacing 1 m . The antenna operating frequency is 150 MHz . The actual direction of the first signal is $10^{\circ}$ in azimuth and $20^{\circ}$ in elevation. The direction of the second signal is $45^{\circ}$ in azimuth and $60^{\circ}$ in elevation.

Create the signals.

```
fs = 8.0e3;
t = (0:1/fs:1).';
x1 = cos(2*pi*t*300);
x2 = cos(2*pi*t*400);
array = phased.ULA('NumElements',10,'ElementSpacing',1);
array.Element.FrequencyRange = [100e6 300e6];
fc = 150e6;
```

Create the plane waves and add noise.

```
x = collectPlaneWave(array,[x1 x2],[10 20;45 60]',fc);
noise = 0.1/sqrt(2)*(randn(size(x)) + li*randn(size(x)));
```

Estimate the arrival angles.

```
estimator = phased.ESPRITEstimator('SensorArray',array,...
    'OperatingFrequency',fc);
doas = estimator(x + noise);
az = broadside2az(sort(doas),[20 60])
az = 1\times2
    10.0000 45.0126
```


## Algorithms

## ESPRIT Subarrays

The ESPRIT algorithm, as implemented in the phased.ESPRITEstimator System object, reorganizes the ULA elements into two overlapping subarrays. For an original N-element array, the first subarray consist of elements $1, \ldots, N-1$ of the original array. The second subarray consist of elements $2, \ldots, N$ of the original array. There are $N_{\text {sub }}=N-1$ elements in each subarray.

## Data Precision

This System object supports single and double precision for input data, properties, and arguments. If the input data X is single precision, the output data is single precision. If the input data X is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

## Version History

## Introduced in R2011a

## References

[1] Van Trees, H. Optimum Array Processing. New York: Wiley-Interscience, 2002.

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:
See "System Objects in MATLAB Code Generation" (MATLAB Coder).
This System object supports single and double precision for input data, properties, and arguments. If the input data X is single precision, the output data is single precision. If the input data X is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

## See Also

broadside2az

## step

System object: phased.ESPRITEstimator
Package: phased
Perform DOA estimation

## Syntax

ANG $=$ step $(H, X)$

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.

ANG $=\operatorname{step}(H, X)$ estimates the DOAs from $X$ using the DOA estimator, $\mathrm{H} . \mathrm{X}$ is a matrix whose columns correspond to channels. ANG is a row vector of the estimated broadside angles (in degrees). You can specify this argument as single or double precision.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Examples

## Estimate DOAs of Two Signals

Estimate the directions-of-arrival (DOA) of two signals received by a standard 10 -element ULA with element spacing 1 m . The antenna operating frequency is 150 MHz . The actual direction of the first signal is $10^{\circ}$ in azimuth and $20^{\circ}$ in elevation. The direction of the second signal is $45^{\circ}$ in azimuth and $60^{\circ}$ in elevation.

Create the signals.

```
fs = 8.0e3;
t = (0:1/fs:1).';
x1 = cos(2*pi*t*300);
x2 = cos(2*pi*t*400);
array = phased.ULA('NumElements',10,'ElementSpacing',1);
```

```
array.Element.FrequencyRange = [100e6 300e6];
fc = 150e6;
```

Create the plane waves and add noise.

```
x = collectPlaneWave(array,[x1 x2],[10 20;45 60]',fc);
```

noise $=0.1 / s q r t(2) *(\operatorname{randn}(\operatorname{size}(x))+1 i * r a n d n(s i z e(x))) ;$

Estimate the arrival angles.

```
estimator = phased.ESPRITEstimator('SensorArray',array,...
    'OperatingFrequency',fc);
doas = estimator(x + noise);
az = broadside2az(sort(doas),[20 60])
az = 1\times2
    10.0000 45.0126
```


## phased.FMCWWaveform

Package: phased
FMCW waveform

## Description

The FMCWWaveform object creates an FMCW (frequency modulated continuous wave) waveform.
To obtain waveform samples:
1 Define and set up your FMCW waveform. See "Construction" on page 1-422.
2 Call step to generate the FMCW waveform samples according to the properties of phased. FMCWWaveform. The behavior of step is specific to each object in the toolbox.

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, $y=$ $\operatorname{step}(o b j, x)$ and $y=o b j(x)$ perform equivalent operations. When the only argument to the step method is the System object itself, replace $y=s t e p(o b j)$ by $y=o b j()$.

## Construction

H = phased. FMCWWaveform creates an FMCW waveform System object, H. The object generates samples of an FMCW waveform.

H = phased. FMCWWaveform(Name, Value) creates an FMCW waveform object, H, with additional options specified by one or more Name, Value pair arguments. Name is a property name on page 1422, and Value is the corresponding value. Name must appear inside single quotes (' ' ). You can specify several name-value pair arguments in any order as Name1, Value1, ..., NameN, ValueN.

## Properties

## SampleRate

Sample rate
Specify the same rate, in hertz, as a positive scalar. The default value of this property corresponds to 1 MHz.

The quantity (SampleRate .* SweepTime) is a scalar or vector that must contain only integers.
Default: 1e6

## SweepTime

Duration of each linear FM sweep
Specify the duration of the upsweep or downsweep, in seconds, as a row vector of positive, real numbers. The default value corresponds to $100 \mu \mathrm{~s}$.

If SweepDirection is 'Triangle', the sweep time is half the sweep period because each period consists of an upsweep and a downsweep. If SweepDirection is 'Up' or 'Down', the sweep time equals the sweep period.

The quantity (SampleRate .* SweepTime) is a scalar or vector that must contain only integers.
To implement a varying sweep time, specify SweepTime as a nonscalar row vector. The waveform uses successive entries of the vector as the sweep time for successive periods of the waveform. If the last element of the vector is reached, the process continues cyclically with the first entry of the vector.

If SweepTime and SweepBandwidth are both nonscalar, they must have the same length.
Default: 1e-4

## SweepBandwidth

FM sweep bandwidth
Specify the bandwidth of the linear FM sweeping, in hertz, as a row vector of positive, real numbers. The default value corresponds to 100 kHz .

To implement a varying bandwidth, specify SweepBandwidth as a nonscalar row vector. The waveform uses successive entries of the vector as the sweep bandwidth for successive periods of the waveform. If the last element of the SweepBandwidth vector is reached, the process continues cyclically with the first entry of the vector.

If SweepTime and SweepBandwidth are both nonscalar, they must have the same length.

## Default: 1e5

## SweepDirection

FM sweep direction
Specify the direction of the linear FM sweep as one of 'Up'|'Down '|'Triangle'.
Default: 'Up'

## SweepInterval

Location of FM sweep interval
If you set this property value to 'Positive', the waveform sweeps in the interval between 0 and $B$, where $B$ is the SweepBandwidth property value. If you set this property value to 'Symmetric', the waveform sweeps in the interval between $-B / 2$ and $B / 2$.

Default: 'Positive'

## OutputFormat

Output signal format
Specify the format of the output signal as one of 'Sweeps ' or 'Samples'. When you set the OutputFormat property to 'Sweeps', the output of the step method is in the form of multiple
sweeps. In this case, the number of sweeps is the value of the NumSweeps property. If the SweepDirection property is 'Triangle', each sweep is half a period.

When you set the OutputFormat property to 'Samples', the output of the step method is in the form of multiple samples. In this case, the number of samples is the value of the NumSamples property.

## Default: 'Sweeps'

## NumSamples

Number of samples in output
Specify the number of samples in the output of the step method as a positive integer. This property applies only when you set the OutputFormat property to 'Samples'.

Default: 100

## NumSweeps

Number of sweeps in output
Specify the number of sweeps in the output of the step method as a positive integer. This property applies only when you set the OutputFormat property to 'Sweeps '.

## Default: 1

## Methods

| plot | Plot FMCW waveform |
| :--- | :--- |
| reset | Reset states of FMCW waveform object |
| step | Samples of FMCW waveform |

## Common to All System Objects

| release | Allow System object property value changes |
| :--- | :--- |

## Examples

## Plot FMCW Waveform

Create and plot an upsweep FMCW waveform.

```
waveform = phased.FMCWWaveform('SweepBandwidth',100.0e3,...
    'OutputFormat','Sweeps','NumSweeps',2);
plot(waveform)
```



## Spectrogram of Triangle Sweep FMCW Waveform

Generate samples of a triangle sweep FMCW Waveform. Then, plot the spectrogram of the sweep. The sweep has a 10 MHz bandwidth.

```
sFMCW = phased.FMCWWaveform('SweepBandwidth',10.0e6,...
    'SampleRate',20.0e6,'SweepDirection','Triangle',...
    'NumSweeps',2);
sig = step(sFMCW);
windowlength = 32;
noverlap = 16;
nfft = 32;
spectrogram(sig,windowlength,noverlap,nfft,sFMCW.SampleRate,'yaxis')
```



## More About

## Triangle Sweep

In each period of a triangle sweep, the waveform sweeps up with a slope of $B / T$ and then down with a slope of $-B / T$. $B$ is the sweep bandwidth, and $T$ is the sweep time. The sweep period is $2 T$.


## Upsweep

In each period of an upsweep, the waveform sweeps with a slope of $B / T . B$ is the sweep bandwidth, and $T$ is the sweep time.


## Downsweep

In each period of a downsweep, the waveform sweeps with a slope of $-B / T . B$ is the sweep bandwidth, and $T$ is the sweep time.


## Version History

Introduced in R2012b

## References

[1] Issakov, Vadim. Microwave Circuits for 24 GHz Automotive Radar in Silicon-based Technologies. Berlin: Springer, 2010.
[2] Skolnik, M.I. Introduction to Radar Systems. New York: McGraw-Hill, 1980.

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® $\mathrm{Coder}^{\mathrm{TM}}$.
Usage notes and limitations:

- plot method is not supported.
- See "System Objects in MATLAB Code Generation" (MATLAB Coder).


## See Also

range2time | time2range | range2bw | phased. LinearFMWaveform

## Topics

"Automotive Adaptive Cruise Control Using FMCW Technology" (Radar Toolbox)

## plot

System object: phased. FMCWWaveform
Package: phased
Plot FMCW waveform

## Syntax

```
plot(Hwav)
plot(Hwav,Name,Value)
plot(Hwav,Name,Value,LineSpec)
h = plot(
```

$\qquad$

``` )
```


## Description

plot (Hwav) plots the real part of the waveform specified by Hwav.
plot (Hwav, Name, Value) plots the waveform with additional options specified by one or more Name, Value pair arguments.
plot (Hwav, Name, Value, LineSpec) specifies the same line color, line style, or marker options as are available in the MATLAB plot function.
h = plot( $\qquad$ ) returns the line handle in the figure.

## Input Arguments

## Hwav

Waveform object. This variable must be a scalar that represents a single waveform object.

## LineSpec

Character vector to specifies the same line color, style, or marker options as are available in the MATLAB plot function. If you specify a PlotType value of ' complex', then LineSpec applies to both the real and imaginary subplots.

Default: 'b'

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## PlotType

Specifies whether the function plots the real part, imaginary part, or both parts of the waveform. Valid values are 'real','imag', and 'complex'.

Default: 'real'

## SweepIdx

Index of the sweep to plot. This value must be a positive integer scalar.

## Default: 1

## Output Arguments

h
Handle to the line or lines in the figure. For a PlotType value of 'complex', h is a column vector. The first and second elements of this vector are the handles to the lines in the real and imaginary subplots, respectively.

## Examples

## Plot FMCW Waveform

Create and plot an upsweep FMCW waveform.
waveform $=$ phased. $\mathrm{FMCWWaveform('SweepBandwidth',100.0e3}, \mathrm{\ldots}$
'OutputFormat','Sweeps', 'NumSweeps', 2) ;
plot(waveform)

FMCW waveform: real part, sweep 1


## reset

System object: phased. FMCWWaveform
Package: phased
Reset states of FMCW waveform object

## Syntax

reset (H)

## Description

reset (H) resets the states of the FMCWWaveform object, H. Afterward, the next call to step restarts the sweep of the waveform.

## step

System object: phased. FMCWWaveform
Package: phased
Samples of FMCW waveform

## Syntax

Y = step(H)

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step $(o b j, x)$ and $y=o b j(x)$ perform equivalent operations. When the only argument to the step method is the System object itself, replace $\mathrm{y}=\operatorname{step}(\mathrm{obj})$ by $\mathrm{y}=\mathrm{obj}(\mathrm{)}$.
$\mathrm{Y}=\operatorname{step}(\mathrm{H})$ returns samples of the FMCW waveform in a column vector, Y .

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## H

FMCW waveform object.

## Output Arguments

Y
Column vector containing the waveform samples.
If H . OutputFormat is 'Samples', Y consists of H . NumSamples samples.
If H . OutputFormat is 'Sweeps', Y consists of H . NumSweeps sweeps. Also, if H. SweepDirection is 'Triangle', each sweep is half a period.

## Examples

## Spectrogram of Triangle Sweep FMCW Waveform

Generate samples of a triangle sweep FMCW Waveform. Then, plot the spectrogram of the sweep. The sweep has a 10 MHz bandwidth.

```
sFMCW = phased.FMCWWaveform('SweepBandwidth',10.0e6,...
    'SampleRate',20.0e6,'SweepDirection','Triangle',...
    'NumSweeps',2);
sig = step(sFMCW);
windowlength = 32;
noverlap = 16;
nfft = 32;
spectrogram(sig,windowlength,noverlap,nfft,sFMCW.SampleRate,'yaxis')
```



# phased.FreeSpace 

Package: phased<br>Free space environment

## Description

The phased. FreeSpace System object models narrowband signal propagation from one point to another in a free-space environment. The object applies range-dependent time delay, gain and phase shift to the input signal. The object accounts for Doppler shift when either the source or destination is moving. A free-space environment is a boundaryless medium with a speed of signal propagation independent of position and direction. The signal propagates along a straight line from source to destination. For example, you can use this object to model the propagation of a signal from a radar to a target and back to the radar.

For non-polarized signals, the FreeSpace System object lets you propagate signals from a single point to multiple points or from multiple points to a single point. Multiple-point to multiple-point propagation is not supported.

To compute the propagated signal in free space:
1 Define and set up your free space environment. See "Construction" on page 1-434.
2 Call step to propagate the signal through a free space environment according to the properties of phased. FreeSpace. The behavior of step is specific to each object in the toolbox.

When propagating a round trip signal in free-space, you can either use one FreeSpace System object to compute the two-way propagation delay or two separate FreeSpace System objects to compute one-way propagation delays in each direction. Due to filter distortion, the total round trip delay when you employ two-way propagation can differ from the delay when you use two one-way phased. FreeSpace System objects. It is more accurate to use a single two-way phased. FreeSpace System object. This option is set by the TwoWayPropagation property.

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, $y=$ $\operatorname{step}(o b j, x)$ and $y=o b j(x)$ perform equivalent operations.

## Construction

$H=$ phased. FreeSpace creates a free space environment System object, $H$.
H = phased.FreeSpace(Name, Value) creates a free space environment object, H, with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN).

## Properties

## PropagationSpeed

Signal propagation speed

Specify signal wave propagation speed in free space as a real positive scalar. Units are meters per second.

Default: Speed of light

## OperatingFrequency

Signal carrier frequency
A scalar containing the carrier frequency of the narrowband signal. Units are hertz.
Default: 3e8
TwoWayPropagation
Perform two-way propagation
Set this property to true to perform round-trip propagation between the origin and destination that you specify in the step command. Set this property to false to perform one-way propagation from the origin to the destination.

Default: false

## SampleRate

Sample rate
A scalar containing the sample rate. Units of sample rate are hertz. The algorithm uses this value to determine the propagation delay in number of samples.

## Default: 1e6

## MaximumDistanceSource

Source of maximum distance value
Source of maximum distance value, specified as 'Auto' or 'Property'. This choice selects how the maximum one-way propagation distance is determined. The maximum one-way propagation distance is used to allocate sufficient memory for delay computation. When you set this property to 'Auto, the System object automatically allocates memory. When you set this property to 'Property' , you specify the maximum one-way propagation distance using the value of the MaximumDistance property.

## Default: 'Auto'

## MaximumDistance

Maximum one-way propagation distance
Maximum one-way propagation distance, specified as a real-valued positive scalar. Units are meters. This property applies when you set the MaximumDistanceSource property to 'Property '. Any signal that propagates more than the maximum one-way distance is ignored. The maximum distance should be greater than or equal to the largest position-to-position distance.

Default: 10000

## MaximumNumInputSamplesSource

Source of maximum number of samples.
The source of the maximum number of samples in the input signal, specified as 'Auto' or 'Property'. When you set this property to 'Auto', the propagation model automatically allocates enough memory to buffer the first input signal. When you set this property to 'Property', specify the maximum number of samples in the input signal using the MaximumNumInputSamples property. Any input signal longer than that value is truncated.

This property applies when you set the MaximumDistanceSource property to 'Property'.
To use this object with variable-size input signals in a MATLAB Function Block in Simulink ${ }^{\circledR}$, set the MaximumNumInputSamplesSource property to 'Property' and set a value for the MaximumNumInputSamples property.

Default: 'Auto'

## MaximumNumInputSamples

Maximum number of input signal samples.
Maximum number of samples in the input signal, specified as a positive integer. This property limits the size of the input signal. Any input signal longer than this value is truncated. The input signal is the first argument to the step method. The number of samples is the number of rows in the input.

This property applies when you set the MaximumNumInputSamplesSource property to
'Property'.
Default: 100

## Methods

| reset | Reset internal states of propagation channel |
| :--- | :--- |
| step | Propagate signal from one location to another |

## Common to All System Objects

release $\quad$ Allow System object property value changes

## Examples

## Signal Propagation from Stationary Radar to Stationary Target

Calculate the amplitude of a signal propagating in free-space from a radar at (40000,0,0) to a target at $(300,200,50)$. Assume both the radar and the target are stationary. The sample rate is 8000 Hz while the operating frequency of the radar is 300 MHz . Transmit five samples of a unit amplitude signal. The signal propagation speed takes the default value of the speed of light. Examine the amplitude of the signal at the target.

```
fs = 8e3;
fop = 3e8;
```

```
freesp = phased.FreeSpace(SampleRate=fs, ...
    OperatingFrequency=fop);
pos1 = [40000;0;0];
pos2 = [300;200;50];
vel1 = [0;0;0];
vel2 = [0;0;0];
```

Create the transmitted signal.
$x=$ ones $(5,1)$;
Find the received signal at the target.

```
y = freesp(x,pos1,pos2,vel1,vel2);
disp(y)
    1.0e-05 *
    0.0000 + 0.0000i
    0.1870 - 0.0229i
    0.1988 - 0.0243i
    0.1988 - 0.0243i
    0.1988 - 0.0243i
```

The first sample is zero because the signal has not yet reached the target.
Manually compute the loss using the formula

```
    \(L=(4 \pi R / \lambda)^{2}\)
R = sqrt((pos1-pos2)'*(pos1-pos2));
lambda = physconst('Lightspeed')/fop;
\(\mathrm{L}=\left(4^{*} \mathrm{pi} * \mathrm{R} / \text { lambda }\right)^{\wedge} 2\)
\(\mathrm{L}=2.4924 \mathrm{e}+11\)
```

Because the transmitted amplitude is unity, the magnitude-squared value of the signal at the target for the third sample equals the inverse of the loss.

```
disp(1/abs(y(3))^2)
    2.4924e+11
```


## Signal Propagation from Moving Radar to Moving Target

Calculate the result of propagating a signal in free space from a radar at $(1000,0,0)$ to a target at $(300,200,50)$. Assume the radar moves at $10 \mathrm{~m} / \mathrm{s}$ along the $x$-axis, while the target moves at $15 \mathrm{~m} / \mathrm{s}$ along the $y$-axis. The sample rate is 8000 Hz while the operating frequency of the radar is 300 MHz . The signal propagation speed takes the default value of the speed of light. Transmit five samples of a unit amplitude signal and examine the amplitude of the signal at the target.

```
fs = 8000;
fop = 3e8;
freesp = phased.FreeSpace(SampleRate=fs, ...
    OperatingFrequency=fop);
```

```
pos1 = [1000;0;0];
pos2 = [300;200;50];
vel1 = [10;0;0];
vel2 = [0;15;0];
y = freesp(ones(5,1),pos1,pos2,vel1,vel2);
disp(y)
    1.0e-03 *
    0.0126 - 0.1061i
    0.0117 - 0.1083i
    0.0105 - 0.1085i
    0.0094 - 0.1086i
    0.0082 - 0.1087i
```

Because the transmitted amplitude is unity, the square of the signal at the target equals the inverse of the loss.

```
disp(1/abs(y(2))^2)
```

    \(8.4206 e+07\)
    
## More About

## Freespace Time Delay and Path Loss

When the origin and destination are stationary relative to each other, you can write the output signal of a free-space channel as $Y(t)=\chi(t-\tau) / L_{f s p}$. The quantity $\tau$ is the signal delay and $L_{f s p}$ is the free-space path loss. The delay $\tau$ is given by $R / c$, where $R$ is the propagation distance and $c$ is the propagation speed. The free-space path loss is given by

$$
L_{f s p}=\frac{(4 \Pi R)^{2}}{\lambda^{2}}
$$

where $\lambda$ is the signal wavelength.
This formula assumes that the target is in the far field of the transmitting element or array. In the near field, the free-space path loss formula is not valid and can result in a loss smaller than one, equivalent to a signal gain. Therefore, the loss is set to unity for range values, $R \leq \lambda / 4 \Pi$.

When the origin and destination have relative motion, the processing also introduces a Doppler frequency shift. The frequency shift is $v / \lambda$ for one-way propagation and $2 v / \lambda$ for two-way propagation. The quantity $v$ is the relative speed of the destination with respect to the origin.

For more details on free space channel propagation, see [2].

## Version History

## Introduced in R2011a

## References

[1] Proakis, J. Digital Communications. New York: McGraw-Hill, 2001.
[2] Skolnik, M. Introduction to Radar Systems, 3rd Ed. New York: McGraw-Hill, 2001.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:

- Requires dynamic memory allocation. See "Limitations for System Objects that Require Dynamic Memory Allocation".
- See "System Objects in MATLAB Code Generation" (MATLAB Coder).


## See Also

fspl|phased.RadarTarget

## reset

System object: phased.FreeSpace
Package: phased
Reset internal states of propagation channel

## Syntax

reset (H)

## Description

reset $(\mathrm{H})$ resets the states of the FreeSpace object, H .

## step

System object: phased. FreeSpace
Package: phased
Propagate signal from one location to another

## Syntax

Y = step(SFS,F,origin_pos,dest_pos,origin_vel,dest_vel)

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.

Y = step(SFS,F,origin_pos,dest_pos,origin_vel,dest_vel) returns the resulting signal $Y$ when the narrowband signal $F$ propagates in free space from the position or positions specified in origin_pos to the position or positions specified in dest_pos. For non-polarized signals, either the origin_pos or dest_pos arguments can specify more than one point. Using both arguments to specify multiple points is not allowed. The velocity of the signal origin is specified in origin_vel and the velocity of the signal destination is specified in dest_vel. The dimensions of origin_vel and dest_vel must agree with the dimensions of origin_pos and dest_pos, respectively.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## SFS - Free-space propagator

System object
Free-space propagator, specified as a System object.

## F - Narrowband signal <br> $M$-element complex-valued column vector, $M$-by- $N$ complex-valued matrix or structure containing complex-valued fields.

Narrowband signal, specified as an $M$-element complex-valued column vector, $M$-by- $N$ complex-valued matrix or structure containing complex-valued fields.

| Polarization | Signal structure |
| :--- | :--- |
| Not enabled | The signal $X$ can be a complex-valued 1-by- $M$ <br> column vector or complex-valued $M$-by- $N$ matrix. <br> The quantity $M$ is the number of sample values of <br> the signal and $N$ is the number of signals to <br> propagate. When you specify $N$ signals, you need <br> to specify $N$ signal origins or $N$ signal <br> destinations. <br> The size of the first dimension of the input matrix <br> can vary to simulate a changing signal length. A <br> size change can occur, for example, in the case of <br> a pulse waveform with variable pulse repetition <br> frequency. |
| Enabled | The signal $X$ is a MATLAB struct containing <br> three matrix fields:X.X, X.Y, and $X . Z$ <br> representing the $x, y$, and $z$ components of the <br> polarized signals. |
| The size of the first dimension of the matrix fields <br> within the struct can vary to simulate a <br> changing signal length such as a pulse waveform <br> with variable pulse repetition frequency. |  |

## origin_pos - Signal origin

vector | matrix
Origin of the signal or signals, specified as a 3-by-1 real-valued column vector or 3-by- N real-valued matrix. Position units are meters. The quantity $N$ is the number of signals arriving from $N$ signal origins and matches the dimension specified in the signal X. If origin_pos is a column vector, it takes the form [x; $y ; z$ ]. If origin_pos is a matrix, each column specifies a different signal origin and has the form [x; y; z]. origin_pos and dest_pos cannot both be specified as matrices - at least one must be a 3 -by- 1 column vector.

## dest_pos - Signal destination

vector | matrix
Destination of the signal or signals, specified as a 3-by-1 column vector or 3-by- $N$ matrix. Position units are meters. The quantity $N$ is the number of signals arriving at $N$ signal destinations and matches the dimension specified in the signal $X$. If dest_pos is a column vector, it takes the form [ $x ; y ; z$ ]. If dest_pos is a matrix, each column specifies a different destination and has the form [ x ; y; z]. dest_pos and origin_pos cannot both be specified as matrices - at least one must be a 3-by-1 column vector.

## origin_vel - Velocity of signal origin

vector | matrix
Velocity of signal origin, specified as a 3-by-1 column vector or 3 -by- $N$ matrix. Velocity units are meters/second. The dimensions of origin_vel must match the dimensions of origin_pos. If origin_vel is a column vector, it takes the form [ Vx ; Vy; Vz]. If origin_vel is a 3 -by- $N$ matrix, each column specifies a different origin velocity and has the form [ $\mathrm{Vx} ; \mathrm{Vy} ; \overline{\mathrm{V} z}]$.

## dest_vel - Velocity of signal destinations

## vector | matrix

Velocity of signal destinations, specified as a 3-by-1 column vector or 3-by- $N$ matrix. Velocity units are meters/second. The dimensions of dest_vel must match the dimensions of dest pos. If dest vel is a column vector, it takes the form [ Vx ; Vy ; Vz ]. If dest_vel is a 3-by- $N$ matrix, each column specifies a different destination velocity and has the form [Vx; Vy; Vz].

## Output Arguments

## Y

Propagated signal, returned as a $M$-element complex-valued column vector, $M$-by- $N$ complex-valued matrix or MATLAB structure containing complex-valued fields.

If $X$ is a column vector or matrix, $Y$ is also a column vector or matrix with the same dimensions.
If $X$ is a struct, $Y$ is also a struct with the same fields. Each field in $Y$ contains the resulting signal of the corresponding field in $X$.

The output $Y$ contains signal samples arriving at the signal destination within the current time frame. The current time frame is defined as the time spanned by the current input. Whenever it takes longer than the current time frame for the signal to propagate from the origin to the destination, the output contains no contribution from the input of the current time frame.

## Examples

## Signal Propagation from Stationary Radar to Stationary Target

Calculate the amplitude of a signal propagating in free-space from a radar at (40000,0,0) to a target at $(300,200,50)$. Assume both the radar and the target are stationary. The sample rate is 8000 Hz while the operating frequency of the radar is 300 MHz . Transmit five samples of a unit amplitude signal. The signal propagation speed takes the default value of the speed of light. Examine the amplitude of the signal at the target.

```
fs = 8e3;
fop = 3e8;
freesp = phased.FreeSpace(SampleRate=fs, ...
    OperatingFrequency=fop);
pos1 = [40000;0;0];
pos2 = [300;200;50];
vel1 = [0;0;0];
vel2 = [0;0;0];
Create the transmitted signal.
```

```
x = ones(5,1);
```

```
x = ones(5,1);
```

Find the received signal at the target.

```
y = freesp(x,pos1,pos2,vel1,vel2);
disp(y)
    1.0e-05 *
```

```
0.0000 + 0.0000i
0.1870 - 0.0229i
0.1988 - 0.0243i
0.1988 - 0.0243i
0.1988 - 0.0243i
```

The first sample is zero because the signal has not yet reached the target.
Manually compute the loss using the formula

```
    L=(4\piR/\lambda)}\mp@subsup{)}{}{2
R = sqrt((pos1-pos2)'*(pos1-pos2));
lambda = physconst('Lightspeed')/fop;
L = (4*pi*R/lambda)^2
L = 2.4924e+11
```

Because the transmitted amplitude is unity, the magnitude-squared value of the signal at the target for the third sample equals the inverse of the loss.

```
disp(1/abs(y(3))^2)
    2.4924e+11
```


## Signal Propagation from Moving Radar to Moving Target

Calculate the result of propagating a signal in free space from a radar at $(1000,0,0)$ to a target at $(300,200,50)$. Assume the radar moves at $10 \mathrm{~m} / \mathrm{s}$ along the $x$-axis, while the target moves at $15 \mathrm{~m} / \mathrm{s}$ along the $y$-axis. The sample rate is 8000 Hz while the operating frequency of the radar is 300 MHz . The signal propagation speed takes the default value of the speed of light. Transmit five samples of a unit amplitude signal and examine the amplitude of the signal at the target.

```
fs = 8000;
fop = 3e8;
freesp = phased.FreeSpace(SampleRate=fs, ...
    OperatingFrequency=fop);
pos1 = [1000;0;0];
pos2 = [300;200;50];
vel1 = [10;0;0];
vel2 = [0;15;0];
y = freesp(ones(5,1),pos1,pos2,vel1,vel2);
disp(y)
    1.0e-03 *
    0.0126 - 0.1061i
    0.0117 - 0.1083i
    0.0105 - 0.1085i
    0.0094 - 0.1086i
    0.0082 - 0.1087i
```

Because the transmitted amplitude is unity, the square of the signal at the target equals the inverse of the loss.
$\operatorname{disp}\left(1 / a b s(y(2))^{\wedge} 2\right)$

## Propagation of Polarized Field from Source to Target

Create a uniform linear array (ULA) consisting of four short-dipole antenna elements that support polarization. Set the orientation of each dipole to the z-direction. Set the operating frequency to 300 MHz and the element spacing of the array to 0.4 meters. While the antenna element supports polarization, you must explicitly enable polarization in the Radiator System object ${ }^{\mathrm{TM}}$.

Create the short-dipole antenna element, ULA array, and radiator System objects. Set the CombineRadiatedSignals property to true to coherently combine the radiated signals from all antennas and the Polarization property to 'Combined ' to process polarized waves.

```
freq = 300e6;
nsensors = 4;
c = physconst('LightSpeed');
antenna = phased.ShortDipoleAntennaElement('FrequencyRange',[100e6 900e6],...
    'AxisDirection','Z');
array = phased.ULA('Element',antenna,...
    'NumElements',nsensors,...
    'ElementSpacing',0.4);
radiator = phased.Radiator('Sensor',array,...
    'PropagationSpeed',c,...
    'OperatingFrequency',freq,...
    'CombineRadiatedSignals',true,...
    'Polarization','Combined',...
    'WeightsInputPort',true);
```

Create a signal to be radiated. In this case, the signal consists of one cycle of a 4 kHz sinusoid. Set the signal amplitude to unity. Set the sampling frequency to 8 kHz . Choose radiating angles of 0 degrees azimuth and 20 degrees elevation. For polarization, you must set a local axes - in this case chosen to coincide with the global axes. Set uniform weights on the elements of the array.

```
fsig = 4000;
fs = 8000;
A = 1;
t = [0:0.01:2]/fs;
signal = A*sin(2*pi*fsig*t');
radiatingAngles = [0;20];
laxes = ones(3,3);
y = radiator(signal,radiatingAngles,laxes,[1,1,1,1].');
disp(y)
    X: [201x1 double]
    Y: [201x1 double]
    Z: [201x1 double]
```

The radiated signal is a struct containing the polarized field.
Use a FreeSpace System object to propagate the field from the origin to the destination.

```
propagator = phased.FreeSpace('PropagationSpeed',c,...
    'OperatingFrequency',freq,...
    'TwoWayPropagation',false,...
    'SampleRate',fs);
```

Set the signal origin, signal origin velocity, signal destination, and signal destination velocity.

```
origin_pos = [0; 0; 0]
dest_pos = [500; 200; 50];
origin_vel = [10; 0; 0];
dest_vel = [0; 15; 0];
```

Call the FreeSpace object to propagate the signals.
yprop = propagator(y,origin_pos,dest_pos,...
origin_vel,dest_vel);
Plot the x -component of the propagated signals.
figure
plot(1000*t, real(yprop.X))
xlabel('Time (millisec)')


## Propagate Signal to Multiple Destinations

Create a FreeSpace System object ${ }^{\text {TM }}$ to propagate a signal from one point to multiple points in space. Start by defining a signal origin and three destination points, all at different ranges.

Compute the propagation direction angles from the source to the destination locations. The source and destination are stationary.

```
pos1 = [0,0,0]';
vell = [0,0,0]';
pos2 = [[700;700;100],[1400;1400;200],2*[2100;2100;400]];
vel2 = zeros(size(pos2));
[rngs,radiatingAngles] = rangeangle(pos2,pos1);
```

Create the cosine antenna element, ULA array, and Radiator System objects.

```
fs = 8000;
freq = 300e6;
nsensors = 4;
sAnt = phased.CosineAntennaElement;
sArray = phased.ULA('Element',sAnt,'NumElements',nsensors);
sRad = phased.Radiator('Sensor',sArray,...
    'OperatingFrequency',freq,...
    'CombineRadiatedSignals',true,'WeightsInputPort',true);
```

Create a signal to be one cycle of a sinusoid of amplitude one and having a frequency of 4 kHz .
fsig $=4000$;
t = [0:0.01:2]'/fs;
signal $=$ sin(2*pi*fsig*t);
Radiate the signals in the destination directions. Apply a uniform weighting to the array.

```
y = step(sRad,signal,radiatingAngles,[1,1,1,1].');
```

Propagate the signals to the destination points.

```
sFSp = phased.FreeSpace('OperatingFrequency',freq,'SampleRate',fs);
yprop = step(sFSp,y,pos1,pos2,vel1,vel2);
```

Plot the propagated signal magnitudes for each range.

```
figure
plot(1000*t,abs(yprop(:,1)),1000*t,abs(yprop(:,2)),1000*t,abs(yprop(:,3)))
ylabel('Signal Magnitude')
xlabel('Time (millisec)')
```



## Algorithms

When the origin and destination are stationary relative to each other, you can write the output signal of a free-space channel as $Y(t)=x(t-\tau) / L_{f s p}$. The quantity $\tau$ is the signal delay and $L_{f s p}$ is the free-space path loss. The delay $\tau$ is given by $R / c$, where $R$ is the propagation distance and $c$ is the propagation speed. The free-space path loss is given by

$$
L_{f s p}=\frac{(4 \pi R)^{2}}{\lambda^{2}}
$$

where $\lambda$ is the signal wavelength.
This formula assumes that the target is in the far field of the transmitting element or array. In the near field, the free-space path loss formula is not valid and can result in a loss smaller than one, equivalent to a signal gain. Therefore, the loss is set to unity for range values, $R \leq \lambda / 4 \Pi$.

When the origin and destination have relative motion, the processing also introduces a Doppler frequency shift. The frequency shift is $v / \lambda$ for one-way propagation and $2 v / \lambda$ for two-way propagation. The quantity $v$ is the relative speed of the destination with respect to the origin.

For further details, see [2].

## References

[1] Proakis, J. Digital Communications. New York: McGraw-Hill, 2001.
[2] Skolnik, M. Introduction to Radar Systems, 3rd Ed. New York: McGraw-Hill, 2001.

## See Also

twoRayChannel | phased.WidebandFreeSpace

# phased.FrostBeamformer 

Package: phased
Frost beamformer

## Description

The phased. FrostBeamformer object implements a Frost beamformer. A Frost beamformer consists of a time-domain MVDR beamformer combined with a bank of FIR filters. The beamformer steers the beam towards a given direction while the FIR filters preserve the input signal power.

To compute the beamformed signal:
1 Create the phased. FrostBeamformer object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

beamformer = phased.FrostBeamformer beamformer = phased.FrostBeamformer(Name,Value)

## Description

beamformer $=$ phased. FrostBeamformer creates a Frost beamformer System object, beamformer, with default property values.
beamformer = phased.FrostBeamformer(Name, Value) creates a Frost beamformer object, beamformer, with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN). Enclose each property name in single quotes.
Example: beamformer =
phased.FrostBeamformer('SensorArray', phased.ULA('NumElements', 20), 'SampleRate $1,300 \mathrm{e} 3)$ sets the sensor array to a uniform linear array (ULA) with default ULA property values except for the number of elements. The beamformer has a sample rate of 300 kHz .

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## SensorArray - Sensor array

phased.ULA array with default array properties (default) | Phased Array System Toolbox array System object

Sensor array, specified as a Phased Array System Toolbox array System object. The array cannot contain subarrays.

Example: phased.URA

## PropagationSpeed - Signal propagation speed

physconst('LightSpeed') (default) | real-valued positive scalar
Signal propagation speed, specified as a real-valued positive scalar. Units are in meters per second. The default propagation speed is the value returned by physconst ('LightSpeed ').
Example: 3e8
Data Types: single | double

## SampleRate - Sample rate of signal

le6 (default) | positive scalar
Sample rate of signal, specified as a positive scalar. Units are in Hz. The System object uses this quantity to calculate the propagation delay in units of samples.
Example: le6
Data Types: single | double

## FilterLength - FIR filter length

2 (default) | positive integer
Length of FIR filter for each sensor element, specified as a positive integer.

## Example: 7

Data Types: single|double

## DiagonalLoadingFactor - Diagonal loading factor <br> 0 (default) | nonnegative scalar

Diagonal loading factor, specified as a nonnegative scalar. Diagonal loading is a technique used to achieve robust beamforming performance, especially when the sample size is small. A small sample size can lead to an inaccurate estimate of the covariance matrix. Diagonal loading also provides robustness due to steering vector errors. The diagonal loading technique adds a positive scalar multiple of the identity matrix to the sample covariance matrix.

Tunable: Yes
Data Types: single | double

## TrainingInputPort - Enable training data input <br> false (default) | true

Enable training data input, specified as false or true. When you set this property to true, use the training data input argument, XT , when running the object. Set this property to false to use the input data, X , as the training data.
Data Types: logical

## DirectionSource - Source of beamforming direction

'Property' (default)|'Input port'
Source of beamforming direction, specified as 'Property' or 'Input port'. Specify whether the beamforming direction comes from the Direction property of this object or from the input argument, ANG. Values of this property are:

| 'Property' | Specify the beamforming direction using the Direction <br> property. |
| :--- | :--- |
| 'Input port' | Specify the beamforming direction using the input argument, <br> ANG. |

## Data Types: char

## Direction - Beamforming directions

[0;0] (default) | real-valued 2-by-1 vector | real-valued 2-by-L matrix
Beamforming directions, specified as a real-valued 2-by-1 vector or a real-valued 2-by- $L$ matrix. For a matrix, each column specifies a different beamforming direction. Each column has the form [AzimuthAngle; ElevationAngle]. Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$ and elevation angles must lie between $-90^{\circ}$ and $90^{\circ}$. All angles are defined with respect to the local coordinate system of the array. Units are in degrees.
Example: [40;30]

## Dependencies

To enable this property, set the DirectionSource property to 'Property'.
Data Types: single | double

## WeightsOutputPort - Enable beamforming weights output

false (default) | true
Enable the output of beamforming weights, specified as false or true. To obtain the beamforming weights, set this property to true and use the corresponding output argument, W. If you do not want to obtain the weights, set this property to false.

## Data Types: logical

## Usage

## Syntax

$\mathrm{Y}=$ beamformer(X)
Y = beamformer (X,XT)
$Y=$ beamformer(X,ANG)
$\mathrm{Y}=$ beamformer(X,XT,ANG)
$[\mathrm{Y}, \mathrm{W}]=$ beamformer( $\qquad$ )

## Description

$Y=$ beamformer (X) performs Frost beamforming on the input, $X$, and returns the beamformed output, Y . This syntax uses the input data, X , as training samples to calculate the beamforming weights.
$\mathrm{Y}=$ beamformer $(\mathrm{X}, \mathrm{XT})$ uses XT as training data to calculate the beamforming weights. To use this syntax, set the TrainingInputPort property to true.
$Y=$ beamformer (X,ANG) uses ANG as the beamforming direction. To use this syntax, set the DirectionSource property to 'Input port'.
$Y=$ beamformer (X,XT,ANG) combines all input arguments. To use this syntax, set the TrainingInputPort property to true and set the DirectionSource property to 'Input port '.
$[\mathrm{Y}, \mathrm{W}]=$ beamformer (__ ) returns the beamforming weights, W . To use this syntax, set the WeightsOutputPort property to true.

## Input Arguments

## X - Input signal

complex-valued $M$-by- $N$ matrix
Input signal, specified as a complex-valued $M$-by- $N$ matrix. $M$ is the signal length and $N$ is the number of array elements specified in the SensorArray property. $M$ must be larger than the length of the filter specified by the FilterLength property.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
Data Types: single | double
Complex Number Support: Yes

## XT - Training data

complex-valued $M$-by- $N$ matrix
Training data, specified as a complex-valued $M$-by- $N$ matrix. $M$ and $N$ are equal to the values for X .
The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
Example: [1 0.5 2.6; 2-0.2 0; 3-2 -1]

## Dependencies

To enable this argument, set the TrainingInputPort property to true.
Data Types: single| double
Complex Number Support: Yes

## ANG - Beamforming directions

[0;0] (default) | real-valued 2-by-1 column vector | real-valued 2-by-L matrix
Beamforming directions, specified as a real-valued 2-by-1 column vector The vector has the form [AzimuthAngle; ElevationAngle]. Units are in degrees. The azimuth angle must lie between $180^{\circ}$ and $180^{\circ}$, and the elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

Example: [40;10]

## Dependencies

To enable this argument, set the DirectionSource property to 'Input port'.

Data Types: double

## Output Arguments

## Y - Beamformed output

complex-valued 1-by- $M$ vector
Beamformed output, returned as a complex-valued 1-by-Mvector, where $M$ is the number of rows of the input X .
Data Types: single | double
Complex Number Support: Yes
W - Beamforming weights
complex-valued $L$-by-1 vector.
Beamforming weights, returned as a complex-valued $L$-by- 1 vector where $L$ is the number of degrees of freedom of the beamformer. The number of degrees of freedom is given by the product of the number of elements specified by the SensorArray property and the FIR filter length specified by FilterLength property.

## Dependencies

To enable this output, set the WeightsOutputPort property to true.
Data Types: single | double
Complex Number Support: Yes

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:
release(obj)

## Common to All System Objects

step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object

## Examples

## Apply Frost Beamforming to ULA

Apply Frost beamforming to an 11-element acoustic ULA array. The incident angle of the incoming signal is -50 degrees in azimuth and 30 degrees in elevation. The speed of sound in air is assumed to be $340 \mathrm{~m} / \mathrm{sec}$. The signal has added Gaussian white noise.

Simulate the signal.
array = phased.ULA('NumElements',11,'ElementSpacing',0.04);
array.Element.FrequencyRange = [20 20000];

```
fs = 8e3;
t = 0:1/fs:0.3;
x = chirp(t,0,1,500);
c = 340;
collector = phased.WidebandCollector('Sensor',array,...
    'PropagationSpeed ',c,'SampleRate',fs,...
    'ModulatedInput',false,'NumSubbands',8192) ;
incidentAngle = [-50;30];
x = collector(x.',incidentAngle);
noise = 0.2*randn(size(x));
rx = x + noise;
```

Beamform the signal.

```
beamformer = phased.FrostBeamformer('SensorArray',array,...
    'PropagationSpeed',c,'SampleRate',fs,...
    'Direction',incidentAngle,'FilterLength',5);
y = beamformer(rx);
```

Plot the beamformed output.

```
plot(t,rx(:,6),'r:',t,y)
xlabel('Time')
ylabel('Amplitude')
legend('Original','Beamformed')
```



## Find Frost Beamforming Weights

Find the beamformer weights of a Frost beamforming applied to signals received at a 7 -element acoustic ULA array. The incident angle of the incoming signal is $-20^{\circ}$ in azimuth and $30^{\circ}$ in elevation. The signal has added Gaussian white noise. The speed of sound in air is assumed to be $340 \mathrm{~m} / \mathrm{s}$. Use a filter length of 15.

First, create the signal.

```
numelements = 7;
element = phased.OmnidirectionalMicrophoneElement('FrequencyRange',[50,10000]);
array = phased.ULA('Element',element,'NumElements',numelements,'ElementSpacing',0.04);
fs = 8e3;
t = 0:1/fs:0.3;
x = chirp(t,0,1,500);
c = 340.0;
collector = phased.WidebandCollector('Sensor',array,...
    'PropagationSpeed ',c,'SampleRate',fs,...
    'ModulatedInput',false,'NumSubbands',8192);
incidentAngle = [-20;30];
x = collector(x.',incidentAngle);
noise = 0.2*randn(size(x));
rx = x + noise;
```

Create a beamformer with a filter length of 15 . Then, beamform the arriving signal and obtain the beamformer weights.

```
filterlength = 15;
beamformer = phased.FrostBeamformer('SensorArray',array, ...
    'PropagationSpeed',c,'SampleRate',fs,'Weights0utputPort',true, ...
    'Direction',incidentAngle,'FilterLength',filterlength);
[y,wt] = beamformer(rx);
size(wt)
ans = 1\times2
    105 1
```

There are $7 * 15=105$ weights computed as expected.
Compare the beamformed output with the signal arriving at the middle element of the array.

```
plot(1000*t,rx(:,4),'r:',1000*t,y)
xlabel('time (msec)')
ylabel('Amplitude')
legend('Middle Element','Beamformed')
```



## Algorithms

phased. FrostBeamformer uses a beamforming algorithm proposed by Frost. It can be considered the time-domain counterpart of the minimum variance distortionless response (MVDR) beamformer. The algorithm does the following:

1 Steers the array to the beamforming direction.
2 Applies an FIR filter to the output of each sensor to achieve the distortionless response constraint. The filter is specific to each sensor.
3 This System object supports single and double precision for input data, properties, and arguments. If the input data $X$ is single precision, the output data is single precision. If the input data $X$ is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

For more information about Frost beamforming, see [1].

## Version History <br> Introduced in R2011a

## References

[1] Frost, O. "An Algorithm For Linearly Constrained Adaptive Array Processing", Proceedings of the IEEE. Vol. 60, Number 8, August, 1972, pp. 926-935.
[2] Van Trees, H. Optimum Array Processing. New York: Wiley-Interscience, 2002.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:

- Requires dynamic memory allocation. See "Limitations for System Objects that Require Dynamic Memory Allocation".
- See "System Objects in MATLAB Code Generation" (MATLAB Coder).
- This System object supports single and double precision for input data, properties, and arguments. If the input data $X$ is single precision, the output data is single precision. If the input data $X$ is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.


## See Also

phased.PhaseShiftBeamformer| phased.SubbandPhaseShiftBeamformer| phased.TimeDelayBeamformer|phased.TimeDelayLCMVBeamformer

## step

System object: phased.FrostBeamformer
Package: phased
Perform Frost beamforming

## Syntax

$Y=\operatorname{step}(H, X)$
$Y=\operatorname{step}(H, X, X T)$
$Y=\operatorname{step}(H, X, A N G)$
$Y=\operatorname{step}(H, X, X T, A N G)$
$[\mathrm{Y}, \mathrm{W}]=\operatorname{step}($ $\qquad$ )

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.
$Y=\operatorname{step}(H, X)$ performs Frost beamforming on the input, $X$, and returns the beamformed output in Y.
$\mathrm{Y}=$ step $(\mathrm{H}, \mathrm{X}, \mathrm{XT})$ uses XT as the training samples to calculate the beamforming weights. This syntax is available when you set the TrainingInputPort property to true.
$\mathrm{Y}=\operatorname{step}(\mathrm{H}, \mathrm{X}, \mathrm{ANG})$ uses ANG as the beamforming direction. This syntax is available when you set the DirectionSource property to 'Input port'.

Y = step( $\mathrm{H}, \mathrm{X}, \mathrm{XT}, \mathrm{ANG}$ ) combines all input arguments. This syntax is available when you set the TrainingInputPort property to true and set the DirectionSource property to 'Input port'.
$[\mathrm{Y}, \mathrm{W}]=\operatorname{step}(\ldots \quad$ ) returns the beamforming weights, W . This syntax is available when you set the WeightsOutputPort property to true.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

H
Beamformer object.

## X

Input signal, specified as an $M$-by- $N$ matrix. $M$ must be larger than the FIR filter length specified in the FilterLength property. $N$ is the number of elements in the sensor array.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

## XT

Training samples, specified as an $M$-by- $N$ matrix. $M$ and $N$ have the same dimensions as X .
The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

## ANG

Beamforming directions, specified as a length-2 column vector. The vector has the form [AzimuthAngle; ElevationAngle], in degrees. The azimuth angle must be between -180 and 180 degrees, and the elevation angle must be between -90 and 90 degrees.

## Output Arguments

## Y

Beamformed output. Y is a column vector of length $M$, where $M$ is the number of rows in X .

## W

Beamforming weights. $W$ is a column vector of length $L$, where $L$ is the degrees of freedom of the beamformer. For a Frost beamformer, $\mathrm{H}, L$ is given by the product of the number of elements in the array and the FIR filter length.

## Examples

## Apply Frost Beamforming to ULA

Apply Frost beamforming to an 11-element acoustic ULA array. The incident angle of the incoming signal is -50 degrees in azimuth and 30 degrees in elevation. The speed of sound in air is assumed to be $340 \mathrm{~m} / \mathrm{sec}$. The signal has added Gaussian white noise.

Simulate the signal.

```
array = phased.ULA('NumElements',11,'ElementSpacing',0.04);
array.Element.FrequencyRange = [20 20000];
fs = 8e3;
t = 0:1/fs:0.3;
x = chirp(t,0,1,500);
c = 340;
collector = phased.WidebandCollector('Sensor',array,...
    'PropagationSpeed',c,'SampleRate',fs,...
```

'ModulatedInput',false,' NumSubbands', 8192) ;
incidentAngle = [-50;30];
$x=$ collector(x.',incidentAngle);
noise $=0.2 *$ randn(size(x));
rx = x + noise;
Beamform the signal.

```
beamformer = phased.FrostBeamformer('SensorArray',array,...
    'PropagationSpeed',c,'SampleRate',fs,...
    'Direction',incidentAngle,'FilterLength',5);
y = beamformer(rx);
```

Plot the beamformed output.

```
plot(t,rx(:,6),'r:',t,y)
xlabel('Time')
ylabel('Amplitude')
legend('Original','Beamformed')
```



## Algorithms

phased. FrostBeamformer uses a beamforming algorithm proposed by Frost. It can be considered the time-domain counterpart of the minimum variance distortionless response (MVDR) beamformer. The algorithm does the following:

1 Steers the array to the beamforming direction.
2 Applies an FIR filter to the output of each sensor to achieve the distortionless response constraint. The filter is specific to each sensor.

For further details, see [1].

## References

[1] Frost, O. "An Algorithm For Linearly Constrained Adaptive Array Processing", Proceedings of the IEEE. Vol. 60, Number 8, August, 1972, pp. 926-935.
[2] Van Trees, H. Optimum Array Processing. New York: Wiley-Interscience, 2002.

## See Also <br> uv2azel | phitheta2azel

## phased.FocusedSteeringVector

Package: phased
Focused sensor array steering vector

## Description

The phased.FocusedSteeringVector System object creates steering vectors for focusing a sensor array at a specified point at multiple ranges, directions, and frequencies.

To compute a focused steering vector for an array
1 Create the phased. FocusedSteeringVector object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

fsteervec = phased.FocusedSteeringVector
fsteervec $=$ phased.FocusedSteeringVector(Name,Value)

## Description

fsteervec $=$ phased. FocusedSteeringVector creates a focused steering vector System object fsteervec with default property values.
fsteervec = phased.FocusedSteeringVector(Name,Value) creates a focused steering vector System object with each property Name set to a specified Value. You can specify additional namevalue pair arguments in any order as (Name1,Value1,...,NameN,ValueN). Enclose each property name in single quotes.
Example: focusedsv = phased.FocusedSteeringVector('SensorArray', phased.URA([10, 20], 'ElementSpacing ', [0.25, 0.25]),'PropagationSpeed', physconst('LightSpeed')) creates a focused steering vector object for a 10 -by-20 uniform rectangular array (URA) with element spacing set to 0.25 meters The propagation speed is set to the speed of light.

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## SensorArray - Sensor array

phased.ULA array with default property values (default) | Phased Array System Toolbox array
Sensor array, specified as an array System object belonging to Phased Array System Toolbox. The sensor array can contain subarrays.
Example: phased.URA

## PropagationSpeed - Signal propagation speed

physconst('LightSpeed') (default) | positive scalar
Signal propagation speed, specified as a positive scalar. Units are in meters per second. The default propagation speed is the value returned by physconst('LightSpeed'). See physconst for more information.

Example: 3e8
Data Types: double

## IncludeElementResponse - Include individual element responses in the steering vector false (default) | true

Option to include individual element responses in the steering vector, specified as false or true. If this property is set to true, the steering vector includes individual array element responses. If this property is set to false, the steering vector is computed assuming that the elements are isotropic, regardless of how the elements are specified. Set this property to true when using polarized signals.

When the array specified in the SensorArray property contains subarrays, the steering vector applies to subarrays. If SensorArray does not contain subarrays, the steering vector applies to the array elements.
Data Types: logical

## NumPhaseShifterBits - Number of phase shifter quantization bits <br> 0 (default) | nonnegative integer

Number of phase shifter quantization bits, specified as a nonnegative integer. This number of bits is used to quantize the phase shift component of the beamformer or steering vector weights. A value of zero indicates that no quantization is performed.
Data Types: double

## EnablePolarization - Enable polarized fields

false (default) |true
Option to enable polarized fields, specified as false or true. Set this property to true to enable polarization. Set this property to false to ignore polarization. Enabling polarization requires that the sensor array specified in the SensorArray property can simulate polarization.

If you set this property to false for an array that actually supports polarization, then all polarization information is discarded. A combined pattern from the $H$ and $V$ polarization components is used at each element to compute the steering vector.

Data Types: logical

## Usage

## Syntax

FSV = fsteervec(FREQ,ANG,FOC)
[FSV,RANGE] = fsteervec(FREQ,ANG,FOC)

## Description

FSV = fsteervec (FREQ,ANG,FOC) returns the focused steering vector, FSV, pointing in the directions specified by ANG, for range FOC, and for the operating frequencies specified in FREQ. The meaning of FSV depends on the IncludeElementResponse property, as follows:

- When IncludeElementResponse is true, the components of FSV include individual element responses.
- When IncludeElementResponse is false, the computation assumes that the elements are isotropic and FSV does not include the individual element responses. If the array contains subarrays, FSV is the array factor among the subarrays. The phase center of each subarray is at its geometric center. If SensorArray does not contain subarrays, FSV is the array factor among the elements.
[FSV,RANGE] = fsteervec(FREQ,ANG,FOC) also returns the range RANGE from the focus point to each antenna element.

Input Arguments

## FREQ - Frequency for computing directivity and patterns

positive scalar | 1-by-L real-valued row vector
Frequencies for computing directivity and patterns, specified as a positive scalar or 1-by-L realvalued row vector. Frequency units are in hertz.

- For an antenna, microphone, or sonar hydrophone or projector element, FREQ must lie within the range of values specified by the FrequencyRange or FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased.CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: [1e8 2e6]
Data Types: double

## ANG - Angle focal point direction

1-by-M real-valued row vector | 2 -by- $M$ real-valued matrix
Angle focal point direction, specified as a 1-by- $M$ real-valued row vector or a 2 -by- $M$ real-valued matrix, where $M$ is the number of angular directions. Angle units are in degrees. If ANGLE is a 2-by- $M$ matrix, then each column specifies a direction in azimuth and elevation, [az;el]. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

If ANGLE is a 1 -by- $M$ vector, then each entry represents an azimuth angle, with the elevation angle assumed to be zero.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the xy plane. This angle is positive when measured from the $x$-axis toward the $y$-axis. The elevation angle is the angle between the direction vector and xy plane. This angle is positive when measured towards the $z$-axis. See "Azimuth and Elevation Angles".

```
Example: [45 60; 0 10]
```

Data Types: double

## FOC - Focal range

positive scalar | $M$-element row vector of positive values
Focal range, specified as a scalar or an $M$-element row vector of positive values. If ANG has more than one column, FOC must be a scalar or have the same number of columns as ANG. Units are in meters.
Data Types: double

## Output Arguments

## FSV - Focused steering vector

complex-valued $N$-by-M-by-L array | structures
Focused steering vector, returned as a complex-valued $N$-by- $M$-by- $L$ array or a structure containing arrays.

The form of the steering vector depends upon whether the EnablePolarization property is set to true or false.

- If EnablePolarization is set to false, the steering vector, FSV, is an $N$-by-M-by- $L$ array. The length of the first dimension, $N$, is the number of elements of the phased array. If SensorArray contains subarrays, $N$ is the number of subarrays. The length of the second dimension, $M$, corresponding to the number of steering directions specified in the ANG argument. The length of the third dimension, $L$, is the number of frequencies specified in the FREQ argument.
- If EnablePolarization is set to true, SV is a MATLAB struct containing two fields, SV.H and SV.V. These two fields represent the horizontal $(H)$ and vertical $(V)$ polarization components of the steering vector. Each field is an $N$-by- $M$-by- $L$ array. The length of the first dimension, $N$, is the number of elements of the phased array. If SensorArray contains subarrays, $N$ is the number of subarrays. The length of the second dimension, $M$, corresponds to the number of steering directions specified in the ANG argument. The length of the third dimension, $L$, is the number of frequencies specified in the FREQ argument.

Simulating polarization also requires that the sensor array specified in the SensorArray property can simulate polarization, and that the IncludeElementResponse property is set to true.

## Data Types: double

## RANGE - Range from array elements to array focus

N -by-M real-valued array of positive values
Range from array elements to array focus, returned as an $N$-by- $M$ real-valued array of positive values. Units are in meters.

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```


## Common to All System Objects

step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object

## Examples

## Focus ULA at Specified Point

Compute the focused steering vector of an 11-element uniform linear array. Focus the array in the direction of $45^{\circ}$ azimuth and $30^{\circ}$ elevation and at a range of 1 km . Assume the array operating frequency is 300 MHz and the elements are spaced 0.4 wavelengths apart.

```
fc = 300.0e6;
c = physconst('lightspeed');
az = 45.0;
el = 30.0;
foc = 1000.0;
lambda = c/fc;
elementspacing = 0.4*lambda;
nelem = 11;
array = phased.ULA(nelem,elementspacing);
fsteervec = phased.FocusedSteeringVector('SensorArray',array);
fsvec = fsteervec(fc,[az;el],foc);
```


## Compute Range of Element to Focus of URA

Compute the range from the focal point of a focused 3-by-4 URA to the array elements. The array focuses at a point 1000 m away in the direction of $45^{\circ}$ elevation and $30^{\circ}$ azimuth. The array operating frequency is 300 Mhz and the array elements are spaced $1 / 2$ wavelength apart.

```
fc = 300.0e6;
c = physconst('lightspeed');
az = 45.0;
el = 30.0;
foc = 1000.0;
lambda = c/fc;
elementspacing = 0.5*lambda;
```

Find the steering vector and element ranges.
array $=$ phased.URA([3,4],elementspacing);
fsteervec = phased.FocusedSteeringVector('SensorArray',array);

```
[fsvec,elemrng] = fsteervec(fc,[az;el],foc);
```

disp(elemrng)
1.0e+03 *

1. 0002
1.0005
2. 0007
0.9999
1.0002
1.0004
0.9996
0.9998
3. 0001
0.9993
0.9995
0.9998

## Version History

Introduced in R2021b

## References

[1] Van Trees, H. Optimum Array Processing. New York: Wiley-Interscience, 2002.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.
Usage notes and limitations:

- See "System Objects in MATLAB Code Generation" (MATLAB Coder).


## See Also

phased.ArrayGain | phased.ArrayResponse | phased.ElementDelay| phased.SteeringVector|phased.SphericalWavefrontArrayResponse

## Topics

"Examine the Response of a Focused Phased Array"

## phased.GCCEstimator

Package: phased
Wideband direction of arrival estimation

## Description

The phased.GCCEstimator System object creates a direction of arrival estimator for wideband signals. This System object estimates the direction of arrival or time of arrival among sensor array elements using the generalized cross-correlation with phase transform algorithm (GCC-PHAT). The algorithm assumes that all signals propagate from a single source lying in the array far field so the direction of arrival is the same for all sensors. The System object first estimates the correlations between all specified sensor pairs using GCC-PHAT and then finds the largest peak in each correlation. The peak identifies the delay between the signals arriving at each sensor pair. Finally, a least-squares estimate is used to derive the direction of arrival from all estimated delays.

To compute the direction of arrival for pairs of element in the array:
1 Define and set up a GCC-PHAT estimator System object, phased. GCCEstimator, using the "Construction" on page 1-469 procedure.
2 Call step to compute the direction of arrival of a signal using the properties of the phased.GCCEstimator System object.

The behavior of step is specific to each object in the toolbox.

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step $(o b j, x)$ and $y=o b j(x)$ perform equivalent operations.

## Construction

sGCC = phased.GCCEstimator creates a GCC direction of arrival estimator System object, sGCC. This object estimates the direction of arrival or time of arrival between sensor array elements using the GCC-PHAT algorithm.
sGCC = phased.GCCEstimator(Name,Value) returns a GCC direction of arrival estimator object, sGCC, with the specified property Name set to the specified Value. Name must appear inside single quotes (' ' ). You can specify several name-value pair arguments in any order as
Name1, Value1, . . . , NameN, ValueN.

## Properties

## SensorArray - Sensor array

phased. ULA System object (default) | Phased Array System Toolbox sensor array
Sensor array, specified as a Phased Array System Toolbox System object. The array can also consist of subarrays. If you do not specify this property, the default sensor array is a phased.ULA System object with default array property values.

Example: phased.URA
PropagationSpeed - Signal propagation speed
physconst('LightSpeed') (default) | real-valued positive scalar
Signal propagation speed, specified as a real-valued positive scalar. Units are in meters per second. The default propagation speed is the value returned by physconst('LightSpeed').
Example: 3e8
Data Types: single|double

## SampleRate - Signal sample rate

le6 (default) | positive real-valued scalar
Signal sample rate, specified as a positive real-valued scalar. Units are in hertz.
Example: 1e6
Data Types: single | double

## SensorPairSource - Source of sensor pairs

'Auto' (default)|'Property'
Source of sensor pairs, specified as either 'Auto' or 'Property'.

- 'Auto ' - choose this property value to compute correlations between the first sensor and all other sensors. The first sensor of the array is the reference channel.
- 'Property ' - choose this property value when you want to explicitly specify the sensor pairs to be used for computing correlations. Set the sensor pair indices using the SensorPair property. You can view the array indices using the viewArray method of any array System object.

Example: 'Auto'
Data Types: char

## SensorPair - Sensor pairs

[2;1] (default) | 2-by-N positive integer valued matrix
Sensor pairs used to compute correlations, specified as a 2 -by- $N$ positive integer-valued matrix. Each column of the matrix specifies a pair of sensors between which the correlation is computed. The second row specifies the reference sensors. Each entry in the matrix must be less than the number of array sensors or subarrays. To use the SensorPair property, you must also set the SensorPairSource value to 'Property'.
Example: [1, 3,5;2,4,6]
Data Types: double

## DelayOutputPort - Option to enable delay output

false (default) | true
Option to enable output of time delay values, specified as a Boolean. Set this property to true to output the delay values as an output argument of the step method. The delays correspond to the arrival angles of a signal between sensor pairs. Set this property to false to disable the output of delays.
Example: false

## Data Types: logical

## CorrelationOutputPort - Option to enable correlation output <br> false (default) | true

Option to enable output of correlation values, specified as a Boolean. Set this property to true to output the correlations and lags between sensor pairs as output arguments of the step method. Set this property to false to disable output of correlations.
Example: false
Data Types: logical

## Methods

reset Reset states of phased.GCCEstimator System object
step Estimate direction of arrival using generalized cross-correlation

## Common to All System Objects

| release | Allow System object property value changes |
| :--- | :--- | :--- |

## Examples

## GCC Estimate of Direction of Arrival at Microphone Array

Estimate the direction of arrival of a signal using the GCC-PHAT algorithm. The receiving array is a 5-by-5-element URA microphone array with elements spaced 0.25 meters apart. The arriving signal is a sequence of wideband chirps. The signal arrives from $17^{\circ}$ azimuth and $0^{\circ}$ elevation. Assume the speed of sound in air is $340 \mathrm{~m} / \mathrm{s}$.

Load the chirp signal.

```
load chirp;
c = 340.0;
```

Create the 5-by-5 microphone URA.

```
d = 0.25;
N = 5;
mic = phased.OmnidirectionalMicrophoneElement;
array = phased.URA([N,N],[d,d],'Element',mic);
```

Simulate the incoming signal using the WidebandCollector System object ${ }^{\mathrm{TM}}$.

```
arrivalAng = [17;0];
collector = phased.WidebandCollector('Sensor',array,'PropagationSpeed',c,...
    'SampleRate',Fs,'ModulatedInput',false);
signal = collector(y,arrivalAng);
```

Estimate the direction of arrival.

```
estimator = phased.GCCEstimator('SensorArray',array,...
    'PropagationSpeed',c,'SampleRate',Fs);
ang = estimator(signal)
```

```
ang = 2×1
```

16.4538
-0.7145

## Algorithms

## GCC-PHAT Cross-Correlation Algorithm

You can use generalized cross-correlation to estimate the time difference of arrival of a signal at two different sensors.

A model of a signal emitted by a source and received at two sensors is given by:

$$
\begin{aligned}
& r_{1}(t)=s(t)+n_{1}(t) \\
& r_{2}(t)=s(t-D)+n_{2}(t)
\end{aligned}
$$

where $D$ is the time difference of arrival (TDOA), or time lag, of the signal at one sensor with respect to the arrival time at a second sensor. You can estimate the time delay by finding the time lag that maximizes the cross-correlation between the two signals.

From the TDOA, you can estimate the broadside arrival angle of the plane wave with respect to the line connecting the two sensors. For two sensors separated by distance $L$, the broadside arrival angle, "Broadside Angles", is related to the time lag by

$$
\sin \beta=\frac{c \tau}{L}
$$

where $c$ is the propagation speed in the medium.
A common method of estimating time delay is to compute the cross-correlation between signals received at two sensors. To identify the time delay, locate the peak in the cross-correlation. When the signal-to-noise ratio (SNR) is large, the correlation peak, $\tau$, corresponds to the actual time delay $D$.

$$
\begin{aligned}
& R(\tau)=E\left\{r_{1}(t) r_{2}(t+\tau)\right\} \\
& \widehat{D}=\underset{\tau}{\operatorname{argmax}} R(\tau)
\end{aligned}
$$

When the correlation function is more sharply peaked, performance improves. You can sharpen a cross correlation peak using a weighting function that whitens the input signals. This technique is called generalized cross-correlation (GCC). One particular weighting function normalizes the signal spectral density by the spectrum magnitude, leading to the generalized cross-correlation phase transform method (GCC-PHAT).

$$
\begin{aligned}
& S(f)=\int_{-\infty}^{\infty} R(\tau) e^{-i 2 n f \tau} d \tau \\
& \tilde{R}(\tau)=\int_{-\infty}^{\infty} \frac{S(f)}{|S(f)|} e^{+i 2 \pi f \tau} d f \\
& \tilde{D}=\underset{\tau}{\operatorname{argmax}} \tilde{R}(\tau)
\end{aligned}
$$

If you use just one sensor pair, you can only estimate the broadside angle of arrival. However, if you use multiple pairs of non-collinear sensors, for example, in a URA, you can estimate the arrival
azimuth and elevation angles of the plane wave using least-square estimation. For $N$ sensors, you can write the delay time $\tau_{k j}$ of a signal arriving at the $k^{\text {th }}$ sensor with respect to the $j^{\text {th }}$ sensor by

$$
\begin{aligned}
& C \tau_{k j}=-\left(\vec{x}_{k}-\vec{x}_{j}\right) \cdot \vec{u} \\
& \vec{u}=\cos \alpha \sin \theta \widehat{i}+\sin \alpha \sin \theta \widehat{j}+\cos \theta \widehat{k}
\end{aligned}
$$

where $u$ is the unit propagation vector of the plane wave. The angles $\alpha$ and $\theta$ are the azimuth and elevation angles of the propagation vector. All angles and vectors are defined with respect to the local axes. You can solve the first equation using least-squares to yield the three components of the unit propagation vector. Then, you can solve the second equation for the azimuth and elevation angles.

## Data Precision

This System object supports single and double precision for input data, properties, and arguments. If the input data $X$ is single precision, the output data is single precision. If the input data $X$ is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

## Version History

## Introduced in R2015b

## References

[1] Knapp, C. H. and G.C. Carter, "The Generalized Correlation Method for Estimation of Time Delay." IEEE Transactions on Acoustics, Speech and Signal Processing. Vol. ASSP-24, No. 4, Aug 1976.
[2] G. C. Carter, "Coherence and Time Delay Estimation." Proceedings of the IEEE. Vol. 75, No. 2, Feb 1987.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
See "System Objects in MATLAB Code Generation" (MATLAB Coder).
This System object supports single and double precision for input data, properties, and arguments. If the input data X is single precision, the output data is single precision. If the input data X is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

## See Also

phased.BeamscanEstimator|phased.RootMUSICEstimator|gccphat

## reset

System object: phased.GCCEstimator
Package: phased
Reset states of phased.GCCEstimator System object

## Syntax

reset(S)

## Description

reset (S) resets the internal state of the phased.GCCEstimator object, S . This method resets the random number generator state if the SeedSource property is applicable and has the value 'Property'.

## Input Arguments

S - GCC-PHAT estimator
phased.GCCEstimator System object
GCC-PHAT estimator, specified as a phased. GCCEstimator System object.
Example: phased.GCCEstimator()

## Version History <br> Introduced in R2015b

## step

System object: phased. GCCEstimator
Package: phased
Estimate direction of arrival using generalized cross-correlation

## Syntax

ang = step(sGCC,X)
[ang,tau] = step(sGCC,X)
[ang,R,lag] = step(sGCC,X)
[ang,tau, R, lag] $=\operatorname{step}(s G C C, X)$

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.
ang $=\operatorname{step}(s G C C, X)$ returns the direction of arrival, ang, of an input signal $X$. The argument $X$ is a matrix specifying the received signals at the elements of the array specified in the SensorArray property. Signals propagate from a single source. Each column in X corresponds to the elements in the array (if an array is used) or the number of subarrays (if a subarray is used). Each row of $X$ represents a single time snapshot.
[ang,tau] = step(sGCC,X) returns the time delays, tau, estimated from the correlations between pairs of sensors. To use this syntax, set the DelayOutputPort property to true. The argument tau is a $P$-element row vector, where $P$ is the number of sensor pairs, and where $P=$ $N(N-1)$.
[ang, R,lag] = step(sGCC,X) returns the estimated correlations, R , between pairs of sensors, when you set the CorrelationOutputPort property to true. R is a matrix with $P$ columns where $P$ is the number of sensor pairs. Each column in R contains the correlation for the corresponding pair of sensors. lag is a column vector containing the time lags corresponding to the rows of the correlation matrix. The time lags are the same for all sensor pairs.

You can combine optional input arguments when their enabling properties are set. Optional inputs must be listed in the same order as their enabling properties. For example,[ang, tau, R, lag] = step (sGCC, X) is valid when you set both Delay0utputPort and CorrelationOutputPort to true.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## sGCC - GCC-PHAT estimator

phased.GCCEstimator System object
GCC-PHAT estimator, specified as a phased. GCCEstimator System object.
Example: phased.GCCEstimator

## X - Received signal

$M$-by- $N$ complex-valued matrix
Received signal, specified as an $M$-by- $N$ complex-valued matrix. The quantity $M$ is the number of sample values (snapshots) of the signal and $N$ is the number of sensor elements in the array. For subarrays, $N$ is the number of subarrays.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

Example: [[0;1;2;3;4;3;2;1;0],[1;2;3;4;3;2;1;0;0]]
Data Types: single |double
Complex Number Support: Yes

## Output Arguments

## ang - Direction of arrival

2-by-1 real-valued column vector | scalar
Direction of arrival of a signal, returned as a 2-by-1 real-valued column vector in the form [azimuth; elevation]. If the array is a uniform linear array, ang is a scalar representing the broadside angle. Angle units are in degrees, defined with respect to the local coordinate system of the array.

## tau - Time delays of arrival

1 -by- $P$ real-valued row vector
Time delays of arrival, returned as 1 -by- $P$ real-valued row vector. $P$ is the number of sensor pairs selected from the array.

- When SensorPairSource is set to 'Auto', $P=N-1 . N$ is the number of elements in the array.
- When SensorPairSource is set to 'Property', $P$ is the number of sensor pairs specified by the SensorPair property.

Time units are seconds. This output is enabled when you set the Delay0utputPort property to true.

## R - Estimated cross-correlation

( $2 M+1$ )-by-P complex-valued matrix
Estimated cross-correlation between pairs of sensors, returned as a ( $2 M+1$ )-by- $P$ complex-valued matrix, where $P$ is the number of sensor pairs selected from the array.

- When SensorPairSource is set to 'Auto',$P=N-1 . N$ is the number of elements in the array. The columns in R contain the correlations between the first sensor and all other sensors.
- When SensorPairSource is set to 'Property', $P$ is the number of sensor pairs specified by the SensorPair property. Each column in R contains the correlation for the corresponding pair of sensors.
$M$ is the number of time samples in the input signal. This output is enabled when you set the CorrelationOutputPort property to true.


## lag - Time lags

$M$-by-1 real-valued column vector
Time lags, returned as an ( $2 M+1$ )-by-1 real-valued column vector. $M$ is the number of time samples in the input signal. Each time lag applies to the corresponding row in the cross-correlation matrix.

## Examples

## Plot Correlations from GCC Estimator

Estimate the direction of arrival of a signal using GCC-PHAT. The receiving array is a 5 -by-5-element URA microphone array with elements spaced 25 centimeters apart. Choose 10 element pairs to compute the arrival angle. Assume the speed of sound in air is 340 meters/second. The arriving signal is a sequence of wideband sounds. Assume the signal arrives from 54 degrees azimuth and five degrees elevation. Estimate the arrival angle, and then plot the correlation function versus lag for a pair of elements.

Load the signal and extract a small portion for computation.

```
load gong;
y1 = y(1:100);
```

Set up the receiving array.

```
N = 5;
d = 0.25;
sMic = phased.OmnidirectionalMicrophoneElement;
sURA = phased.URA([N,N],[d,d],'Element',sMic);
```

Simulate the arriving plane wave using the WidebandCollector System object ${ }^{\mathrm{TM}}$.

```
c = 340.0;
arrivalAng = [54;5];
sWBC = phased.WidebandCollector('Sensor',sURA,...
    'PropagationSpeed',c,...
    'SampleRate',Fs,...
    'ModulatedInput',false);
signal = step(sWBC,y1,arrivalAng);
```

Estimate direction of arrival. Choose 10 sensors to correlate with the first element of the URA.

```
sensorpairs = [[2,4,6,8,10,12,14,16,18,20];ones(1,10)];
sGCC = phased.GCCEstimator('SensorArray',sURA,...
    'PropagationSpeed ', c, 'SampleRate',Fs,...
    'SensorPairSource','Property',...
    'SensorPair',sensorpairs,...
    'DelayOutputPort',true','CorrelationOutputPort',true);
[estimatedAng,taus,R,lags] = step(sGCC,signal);
```

The estimated angle is:
disp(estimatedAng)

$$
\begin{array}{r}
11.6720 \\
4.2189
\end{array}
$$

Plot the correlation between sensor 8 and sensor 1 . This pair corresponds to the fourth column of the correlation matrix. The estimated value of tau (in milliseconds) for this pair is:
disp(1000*taus(4))
0.0238
plot(1000*lags, real(R(:,4)))
xlabel('Time lags (msec)')
ylabel('Correlation')


## Algorithms

## Data Precision

This System object supports single and double precision for input data, properties, and arguments. If the input data X is single precision, the output data is single precision. If the input data X is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

## Version History

Introduced in R2015b

## References

[1] Charles H. Knapp and Carter, G.C., The Generalized Correlation Method for Estimation of Time Delay, IEEE Transactions on Acoustics, Speech and Signal Processing, Vol, ASSP-24, No. 4. August 1976.
[2] G. Clifford Carter Coherence and Time Delay Estimation, Proceedings of the IEEE, vol 75, No 2, Feb 1987.

## See Also

phased.BeamscanEstimator|phased.RootMUSICEstimator

# phased.GSCBeamformer 

Package: phased
Generalized sidelobe canceler beamformer

## Description

The phased.GSCBeamformer System object implements a generalized sidelobe cancellation (GSC) beamformer. A GSC beamformer splits the incoming signals into two channels. One channel goes through a conventional beamformer path and the second goes into a sidelobe canceling path. The algorithm first pre-steers the array to the beamforming direction and then adaptively chooses filter weights to minimize power at the output of the sidelobe canceling path. The algorithm uses least mean squares (LMS) to compute the adaptive weights. The final beamformed signal is the difference between the outputs of the two paths.

To compute the beamformed signal:
1 Create the phased.GSCBeamformer object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

beamformer = phased.GSCBeamformer
beamformer = phased.GSCBeamformer(Name,Value)

## Description

beamformer = phased.GSCBeamformer creates a GSC beamformer System object, beamformer, with default property values.
beamformer $=$ phased.GSCBeamformer(Name, Value) creates a GSC beamformer object, beamformer, with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN). Enclose each property name in single quotes.

Example: beamformer =
phased.GSCBeamformer('SensorArray',phased.ULA('NumElements',20),'SampleRate', 300 e 3 ) sets the sensor array to a uniform linear array (ULA) with default ULA property values except for the number of elements. The beamformer has a sample rate of 300 kHz .

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## SensorArray - Sensor array

phased.ULA array with default array properties (default) | Phased Array System Toolbox array System object

Sensor array, specified as a Phased Array System Toolbox array System object. The array cannot contain subarrays.

Example: phased.URA
PropagationSpeed - Signal propagation speed
physconst('LightSpeed') (default) | real-valued positive scalar
Signal propagation speed, specified as a real-valued positive scalar. Units are in meters per second. The default propagation speed is the value returned by physconst('LightSpeed').
Example: 3e8
Data Types: single | double

## SampleRate - Sample rate of signal

le6 (default) | positive scalar
Sample rate of signal, specified as a positive scalar. Units are in Hz. The System object uses this quantity to calculate the propagation delay in units of samples.
Example: 1e6
Data Types: single | double

## FilterLength - FIR filter length

1 (default) | positive integer
Length of the signal path FIR filters, specified as a positive integer. This property determines the adaptive filter size for the sidelobe canceling path. The FIR filter for the conventional beamforming path is a delta function of the same length.

Example: 4
Data Types: double | single

## LMSStepSize - Adaptive filter step size factor

0.1 (default) | positive real-valued scalar

The adaptive filter step size factor, specified as a positive real-valued scalar. This quantity, when divided by the total power in the sidelobe canceling path, sets the actual adaptive filter step size that is used in the LMS algorithm.
Data Types: double | single

## DirectionSource - Source of beamforming direction

'Property' (default)|'Input port'

Source of beamforming direction, specified as 'Property' or 'Input port'. Specify whether the beamforming direction comes from the Direction property of this object or from the input argument, ANG. Values of this property are:

| 'Property' | Specify the beamforming direction using the Direction <br> property. |
| :--- | :--- |
| 'Input port' | Specify the beamforming direction using the input argument, <br> ANG. |

## Data Types: char

## Direction - Beamforming directions

[0;0] (default) | real-valued 2-by-1 vector | real-valued 2-by-L matrix
Beamforming directions, specified as a real-valued 2-by-1 vector or a real-valued 2-by-L matrix. For a matrix, each column specifies a different beamforming direction. Each column has the form [AzimuthAngle; ElevationAngle]. Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$ and elevation angles must lie between $-90^{\circ}$ and $90^{\circ}$. All angles are defined with respect to the local coordinate system of the array. Units are in degrees.

Example: [40;30]

## Dependencies

To enable this property, set the DirectionSource property to 'Property'.
Data Types: single | double

## Usage

## Syntax

$\mathrm{Y}=$ beamformer(X)
Y = beamformer(X,ANG)

## Description

$\mathrm{Y}=$ beamformer( X ) performs GSC beamforming on the input, X , and returns the beamformed output, Y.
$Y=$ beamformer (X,ANG) uses ANG as the beamforming direction. To use this syntax, set the DirectionSource property to 'Input port'.

## Input Arguments

## X - Input signal

complex-valued $M$-by- $N$ matrix
Input signal, specified as a complex-valued $M$-by- $N$ matrix. $M$ is the signal length and $N$ is the number of array elements specified in the SensorArray property. $M$ must be larger than the length of the filter specified by the FilterLength property.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

## Data Types: double | single

Complex Number Support: Yes

## ANG - Beamforming directions

[0;0] (default) | real-valued 2-by-1 column vector | real-valued 2-by-L matrix
Beamforming directions, specified as a real-valued 2-by-1 column vector The vector has the form [AzimuthAngle; ElevationAngle]. Units are in degrees. The azimuth angle must lie between $180^{\circ}$ and $180^{\circ}$, and the elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

Example: [40;10]

## Dependencies

To enable this argument, set the DirectionSource property to 'Input port '.
Data Types: double

## Output Arguments

## Y - Beamformed output

complex-valued 1-by-M vector
Beamformed output, returned as a complex-valued 1-by-Mvector, where $M$ is the number of rows of the input $X$.

Data Types: double | single
Complex Number Support: Yes

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```


## Common to All System Objects

step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object

## Examples

## Generalized Sidelobe Cancellation on Uniform Linear Array

Create a GSC beamformer for a 11-element acoustic array in air. A chirp signal is incident on the array at $-50^{\circ}$ in azimuth and $0^{\circ}$ in elevation. Compare the GSC beamformed signal to a Frost beamformed signal. The signal propagation speed is $340 \mathrm{~m} / \mathrm{s}$ and the sample rate is 8 kHz .

Create the microphone and array System objects. The array element spacing is one-half wavelength. Set the signal frequency to the one-half the Nyquist frequency.

```
c = 340.0;
fs = 8.0e3;
fc = fs/2;
lam = c/fc;
transducer = phased.OmnidirectionalMicrophoneElement('FrequencyRange',[20 20000]);
array = phased.ULA('Element',transducer,'NumElements',11,'ElementSpacing',lam/2);
```

Simulate a chirp signal with a 500 Hz bandwidth.
t = 0:1/fs:.5;
signal $=$ chirp(t,0,0.5,500);
Create an incident wave arriving at the array. Add gaussian noise to the wave.

```
collector = phased.WidebandCollector('Sensor',array,'PropagationSpeed',c, ...
    'SampleRate',fs,'ModulatedInput',false,'NumSubbands',512);
incidentAngle = [-50;0];
signal = collector(signal.',incidentAngle);
noise = 0.5*randn(size(signal));
recsignal = signal + noise;
```

Perform Frost beamforming at the actual incident angle.

```
frostbeamformer = phased.FrostBeamformer('SensorArray',array,'PropagationSpeed', ...
    c,'SampleRate',fs,'Direction',incidentAngle,'FilterLength',15);
yfrost = frostbeamformer(recsignal);
```

Perform GSC beamforming and plot the beamformer output against the Frost beamformer output. Also plot the nonbeamformed signal arriving at the middle element of the array.

```
gscbeamformer = phased.GSCBeamformer('SensorArray',array, ...
    'PropagationSpeed',c,'SampleRate',fs,'Direction',incidentAngle, ...
    'FilterLength',15);
ygsc = gscbeamformer(recsignal);
plot(t*1000,recsignal(:,6),t*1000,yfrost,t,ygsc)
xlabel('Time (ms)')
ylabel('Amplitude')
```



Zoom in on a small portion of the output.
idx = 1000:1300;
plot(t(idx)*1000, recsignal(idx, 6), t(idx)*1000, yfrost(idx), t(idx)*1000,ygsc(idx)) xlabel('Time (ms)')
legend('Received signal','Frost beamformed signal','GSC beamformed signal')


## Generalized Sidelobe Cancellation in Two Directions

Create a GSC beamformer for an 11-element acoustic array in air. A chirp signal is incident on the array at $-50^{\circ}$ in azimuth and $0^{\circ}$ in elevation. Compute the beamformed signal in the direction of the incident wave and in another direction. Compare the two beamformed outputs. The signal propagation speed is $340 \mathrm{~m} / \mathrm{s}$ and the sample rate is 8 kHz . Create the microphone and array System objects. The array element spacing is one-half wavelength. Set the signal frequency to the one-half the Nyquist frequency.

$$
c=340.0 ;
$$

$$
\text { fs }=8.0 \mathrm{e} 3 \text {; }
$$

$$
\mathrm{fc}=\mathrm{fs} / 2 \text {; }
$$

lam = c/fc;
transducer = phased.OmnidirectionalMicrophoneElement('FrequencyRange',[20 20000]); array = phased.ULA('Element',transducer,'NumElements',11,'ElementSpacing',lam/2);

Simulate a chirp signal with a 500 Hz bandwidth.
$\mathrm{t}=0: 1 / \mathrm{fs}: 0.5$;
signal $=$ chirp(t, 0, 0.5,500);
Create an incident wavefield hitting the array.
collector = phased.WidebandCollector('Sensor', array,'PropagationSpeed', c, ...
'SampleRate',fs,'ModulatedInput',false, 'NumSubbands',512);

```
incidentAngle = [-50;0];
signal = collector(signal.',incidentAngle);
noise = 0.1*randn(size(signal));
recsignal = signal + noise;
```

Perform GSC beamforming and plot the beamformer outputs. Also plot the nonbeamformed signal arriving at the middle element of the array.
gscbeamformer = phased.GSCBeamformer('SensorArray', array, ...
'PropagationSpeed', c,'SampleRate',fs,'DirectionSource','Input port', ...
'FilterLength',5);
ygsci = gscbeamformer(recsignal,incidentAngle);
ygsco = gscbeamformer(recsignal,[20;30]);
plot( t *1000, recsignal(:, 6 ) , $\mathrm{t} * 1000, \mathrm{ygsci}, \mathrm{t} * 1000, \mathrm{ygsco})$
xlabel('Time (ms)')
ylabel('Amplitude')
legend('Received signal at element','GSC beamformed signal (incident direction)', ... 'GSC beamformed signal (other direction)','Location','southeast')


Zoom in on a small portion of the output.

```
idx = 1000:1300;
plot(t(idx)*1000,recsignal(idx,6),t(idx)*1000,ygsci(idx),t(idx)*1000,ygsco(idx))
xlabel('Time (ms)')
legend('Received signal at element','GSC beamformed signal (incident direction)', ...
    'GSC beamformed signal (other direction)','Location','southeast')
```



## Algorithms

## Generalized Sidelobe Cancellation

The generalized sidelobe canceler (GSC) is an efficient implementation of a linear constraint minimum variance (LCMV) beamformer. LCMV beamforming minimizes the output power of an array while preserving the power in one or more specified directions. This type of beamformer is called a constrained beamformer. You can compute exact weights for the constrained beamformer but the computation is costly when the number of elements is large. The computation requires the inversion of a large spatial covariance matrix. The GSC formulation converts the adaptive constrained optimization LCMV problem into an adaptive unconstrained problem, which simplifies the implementation.

In the GSC algorithm, incoming sensor data is split into two signal paths as shown in the block diagram. The upper path is a conventional beamformer. The lower path is an adaptive unconstrained beamformer whose purpose is to minimize the GSC output power. The GSC algorithm consists of these steps:

1 Presteer the element sensor data by time-shifting the incoming signals. Presteering time-aligns all sensor element signals. The time shifts depend on the arrival angle of the signal.
2 Pass the presteered signals through the upper path into a conventional beamformer with fixed weights, $\mathbf{w}_{\text {conv }}$.
3 Also pass the presteered signals through the lower path into the blocking matrix, B. The blocking matrix is orthogonal to the signal and removes the signal from the lower path.

4 Filter the lower path signals through a bank of FIR filters. The FilterLength property sets the length of the filters. The filter coefficients are the adaptive filter weights, $\mathbf{w}_{a d}$.
5 Compute the difference between the upper and lower signal paths. This difference is the beamformed GSC output.

6 Feed the beamformed output back into the filter. The filter adapts its weights using a least meansquare (LMS) algorithm. The actual adaptive LMS step size is equal to the value of the LMSStepSize property divided by the total signal power.


For more information, see [1].

## Data Precision

This System object supports single and double precision for input data, properties, and arguments. If the input data X is single precision, the output data is single precision. If the input data X is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

## Version History

Introduced in R2016b

## References

[1] Griffiths, L. J., and Charles W. Jim. "An alternative approach to linearly constrained adaptive beamforming." IEEE Transactions on Antennas and Propagation, 30.1 (1982): 27-34.
[2] Van Trees, H. Optimum Array Processing. New York: Wiley-Interscience, 2002.
[3] Johnson, D.H., and Dan E. Dudgeon, Array Signal Processing, Englewood Cliffs: Prentice-Hall, 1993.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.
Usage notes and limitations:

- Requires dynamic memory allocation. See "Limitations for System Objects that Require Dynamic Memory Allocation".
- See "System Objects in MATLAB Code Generation" (MATLAB Coder).
- This System object supports single and double precision for input data, properties, and arguments. If the input data $X$ is single precision, the output data is single precision. If the input data $X$ is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.


## See Also

phased.FrostBeamformer | phased.MVDRBeamformer | phased.PhaseShiftBeamformer | phased.SubbandPhaseShiftBeamformer|phased.TimeDelayBeamformer| phased.TimeDelayLCMVBeamformer

## phased.HeterogeneousConformalArray

Package: phased
Heterogeneous conformal array

## Description

The HeterogeneousConformalArray object constructs a conformal array from a heterogeneous set of antenna elements. A heterogeneous array is an array which consists of different kinds of antenna elements or an array of different kinds of microphone elements. A conformal array can have elements in any position pointing in any direction.

To compute the response for each element in the array for specified directions:
1 Define and set up your conformal array. See "Construction" on page 1-491.
2 Call step to compute the response according to the properties of phased.HeterogeneousConformalArray. The behavior of step is specific to each object in the toolbox.

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step $(o b j, x)$ and $y=o b j(x)$ perform equivalent operations.

## Construction

H = phased. HeterogeneousConformalArray creates a heterogeneous conformal array System object, H. This object models a heterogeneous conformal array formed with different kinds of sensor elements.

H = phased.HeterogeneousConformalArray(Name, Value) creates object, H, with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN).

## Properties

## ElementSet

Set of elements used in the array
Set of elements used in the sensor array, specified as a row MATLAB cell array. Elements specified in the ElementSet property must be either Phased Array System Toolbox antennas, microphones, or transducers System objects or Antenna Toolbox System object. In addition, all specified antenna elements must have the same polarization capability.

Default: One cell containing one isotropic antenna element

## ElementIndices

Elements location assignment

This property specifies the mapping of elements in the array. The property assigns elements to their locations in the array using the indices into the ElementSet property. The value of ElementIndices must be an length- $N$ row vector. In this vector, $N$ represents the number of elements in the array. The values in the vector specified by ElementIndices must be less than or equal to the number of entries in the ElementSet property.

Default:[11 22 1]
ElementPosition
Element positions
ElementPosition specifies the positions of the elements in the conformal array. The value of the ElementPosition property must be a 3 -by- $N$ matrix, where $N$ indicates the number of elements in the conformal array. Each column of ElementPosition represents the position, in the form [x; y; z] (in meters), of a single element in the local coordinate system of the array. The local coordinate system has its origin at an arbitrary point.

Default: [0; 0; 0]
ElementNormal
Element normal directions
ElementNormal specifies the normal directions of the elements in the conformal array. Angle units are degrees. The value assigned to ElementNormal must be either a 2 -by- $N$ matrix or a 2 -by- 1 column vector. The variable $N$ indicates the number of elements in the array. If the value of ElementNormal is a matrix, each column specifies the normal direction of the corresponding element in the form [azimuth; elevation] with respect to the local coordinate system. The local coordinate system aligns the positive $x$-axis with the direction normal to the conformal array. If the value of ElementNormal is a 2-by-1 column vector, it specifies the pointing direction of all elements in the array.

You can use the ElementPosition and ElementNormal properties to represent any arrangement in which pairs of elements differ by certain transformations. The transformations can combine translation, azimuth rotation, and elevation rotation. However, you cannot use transformations that require rotation about the normal.

Default: [0; 0]

## Taper

Element taper or weighting
Element tapering or weighting, specified as a complex-valued scalar, 1-by- $N$ row vector, or $N$-by-1 column vector. The quantity $N$ is the number of elements in the array as determined by the size of the ElementIndices property. Tapers, also known as weights, are applied to each sensor element in the sensor array and modify both the amplitude and phase of the received data. If 'Taper' is a scalar, the same taper value is applied to all elements. If 'Taper' is a vector, each taper value is applied to the corresponding sensor element.

## Default: 1

## Methods

| Specific to phased. HeterogeneousConformalArray Object |  |
| :--- | :--- |
| beamwidth | Compute and display beamwidth of an array |
| collectPla <br> neWave | Simulate received plane waves |
| directivit <br> y | Directivity of heterogeneous conformal array |
| getElement <br> Normal | Normal vector to array elements |
| getElement <br> Position | Positions of array elements |
| getNumElem <br> ents | Number of elements in array |
| getTaper | Array element tapers |
| isPolariza <br> tionCapabl <br> e | Polarization capability |
| pattern | Plot heterogeneous conformal array pattern |
| patternAzi <br> muth | Plot heterogeneous conformal array directivity or pattern versus azimuth |
| patternEle <br> vation | Plot heterogeneous conformal array directivity or pattern versus elevation |
| perturbati <br> ons | Perturbations defined on phased array |
| perturbedA <br> rray | Apply perturbations to phased array |
| perturbedP <br> attern | Compute and plot azimuth pattern of perturbed array |
| step | Output responses of array elements |
| viewArray | View array geometry |

## Common to All System Objects

| release | Allow System object property value changes |
| :--- | :--- |

## Examples

## Heterogeneous Uniform Circular Array

Construct an 8 -element heterogeneous uniform circular array (UCA) using the ConformalArray System object ${ }^{\text {TM }}$. Four of the elements have a cosine pattern with a power of 1.6 while the remaining elements have a cosine pattern with a power of 2.0. Plot the 3-D power response. Assume a 1 GHz operating frequency. The wave propagation speed is the speed of light.

```
Construct the array
sElement1 = phased.CosineAntennaElement('CosinePower',1.6);
sElement2 = phased.CosineAntennaElement('CosinePower',2.0);
N = 8;
azang = (0:N-1)*360/N-180;
sArray = phased.HeterogeneousConformalArray(...
    'ElementSet',{sElement1,sElement2},...
    'ElementIndices',[1 1 1 1 2 2 2 2],...
    'ElementPosition',[cosd(azang);sind(azang);zeros(1,N)],...
    'ElementNormal',[azang;zeros(1,N)]);
c = physconst('LightSpeed');
fc = 1e9;
```


## Create the 3-D power pattern

pattern(sArray,fc,[-180:180], [-90:90],...
'CoordinateSystem','polar',...
'Type','power')


Version History
Introduced in R2013a

## References

[1] Josefsson, L. and P. Persson. Conformal Array Antenna Theory and Design. Piscataway, NJ: IEEE Press, 2006.
[2] Van Trees, H. Optimum Array Processing. New York: Wiley-Interscience, 2002.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:

- pattern, patternAzimuth, patternElevation, plotResponse, and viewArray methods are not supported.
- See "System Objects in MATLAB Code Generation" (MATLAB Coder).


## See Also

phased.ReplicatedSubarray|phased.PartitionedArray|
phased.CosineAntennaElement | phased.CustomAntennaElement |
phased.IsotropicAntennaElement | phased.ULA| phased.UCA|phased.URA| phased.HeterogeneousULA | phased.HeterogeneousURA | phased.ConformalArray | uv2azel | phitheta2azel

## Topics

"Phased Array Gallery"

## directivity

System object: phased. HeterogeneousConformalArray
Package: phased
Directivity of heterogeneous conformal array

## Syntax

D = directivity (H,FREQ,ANGLE)
D = directivity (H,FREQ,ANGLE,Name,Value)

## Description

D = directivity ( $\mathrm{H}, \mathrm{FREQ}$, ANGLE) computes the "Directivity" on page 1-499 of a heterogeneous conformal array of antenna or microphone elements, H , at frequencies specified by the FREQ and in angles of direction specified by the ANGLE.

The integration used when computing array directivity has a minimum sampling grid of 0.1 degrees. If an array pattern has a beamwidth smaller than this, the directivity value will be inaccurate.

D = directivity (H, FREQ, ANGLE, Name, Value) computes the directivity with additional options specified by one or more Name, Value pair arguments.

## Input Arguments

## H - Heterogeneous conformal array

System object
Heterogeneous conformal array specified as a phased.HeterogeneousConformalArray System object.
Example: $\mathrm{H}=$ phased. HeterogeneousConformalArray;

## FREQ - Frequency for computing directivity and patterns

positive scalar | 1-by-L real-valued row vector
Frequencies for computing directivity and patterns, specified as a positive scalar or 1-by-L realvalued row vector. Frequency units are in hertz.

- For an antenna, microphone, or sonar hydrophone or projector element, FREQ must lie within the range of values specified by the FrequencyRange or FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased.CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: [1e8 2e6]
Data Types: double

## ANGLE - Angles for computing directivity

## 1-by- $M$ real-valued row vector | 2-by- $M$ real-valued matrix

Angles for computing directivity, specified as a 1-by- $M$ real-valued row vector or a 2 -by- $M$ real-valued matrix, where $M$ is the number of angular directions. Angle units are in degrees. If ANGLE is a 2 -by- $M$ matrix, then each column specifies a direction in azimuth and elevation, [az;el]. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

If ANGLE is a 1 -by- $M$ vector, then each entry represents an azimuth angle, with the elevation angle assumed to be zero.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the $x y$ plane. This angle is positive when measured from the $x$-axis toward the $y$-axis. The elevation angle is the angle between the direction vector and $x y$ plane. This angle is positive when measured towards the $z$-axis. See "Azimuth and Elevation Angles".
Example: [45 60; 0 10]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Namel=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## PropagationSpeed - Signal propagation speed

speed of light (default) | positive scalar
Signal propagation speed, specified as the comma-separated pair consisting of ' PropagationSpeed ' and a positive scalar in meters per second.
Example: 'PropagationSpeed', physconst('LightSpeed')
Data Types: double
Weights - Array weights
1 (default) $\mid N$-by-1 complex-valued column vector $\mid N$-by- $L$ complex-valued matrix
Array weights, specified as the comma-separated pair consisting of 'Weights' and an $N$-by- 1 complex-valued column vector or $N$-by- $L$ complex-valued matrix. Array weights are applied to the elements of the array to produce array steering, tapering, or both. The dimension $N$ is the number of elements in the array. The dimension $L$ is the number of frequencies specified by FREQ.

| Weights Dimension | FREQ Dimension | Purpose |
| :--- | :--- | :--- |
| $N$-by-1 complex-valued column <br> vector | Scalar or 1-by- $L$ row vector | Applies a set of weights for the <br> single frequency or for all $L$ <br> frequencies. |
| $N$-by- $L$ complex-valued matrix | 1-by-L row vector | Applies each of the $L$ columns of <br> 'Weights' for the <br> corresponding frequency in <br> FREQ. |

Note Use complex weights to steer the array response toward different directions. You can create weights using the phased.SteeringVector System object or you can compute your own weights. In general, you apply Hermitian conjugation before using weights in any Phased Array System Toolbox function or System object such as phased. Radiator or phased. Collector. However, for the directivity, pattern, patternAzimuth, and patternElevation methods of any array System object use the steering vector without conjugation.

Example: 'Weights',ones(N,M)
Data Types: double
Complex Number Support: Yes

## Output Arguments

## D - Directivity

M-by-L matrix
Directivity, returned as an $M$-by- $L$ matrix. Each row corresponds to one of the $M$ angles specified by ANGLE. Each column corresponds to one of the $L$ frequency values specified in FREQ. Directivity units are in dBi where dBi is defined as the gain of an element relative to an isotropic radiator.

## Examples

## Directivity of Heterogeneous Conformal Array

Compute the directivity of a steered heterogeneous conformal array. Construct a 24 -element heterogeneous disk array using elements having different antenna patterns and then show how to compute the array's directivity.

Set the signal speed to the speed of light and the signal frequency to 2 GHz .

```
c = physconst('LightSpeed');
freq = 2e9;
```

Choose two different types of elements - both are cosine antenna elements with different powers.

```
myElement1 = phased.CosineAntennaElement('CosinePower',1.5);
myElement2 = phased.CosineAntennaElement('CosinePower',1.8);
```

Set up a three-ring disk array with 8 elements per ring. The inner ring has different elements from the outer rings.

```
N = 8;
azang = (0:N-1)*360/N-180;
p0 = [zeros(1,N);cosd(azang);sind(azang)];
posn = [0.6*p0, 0.4*p0, 0.2*p0];
myArray = phased.HeterogeneousConformalArray;
myArray.ElementPosition = posn;
myArray.ElementNormal = zeros(2,3*N);
myArray.ElementSet = {myElement1,myElement2};
myArray.ElementIndices = [1 1 1 1 1 1 1 1,...
    11111111,...
    22222 2 2 2];
```

Set up the steering vector to point at 30 degrees azimuth and compute the directivity in that direction.

```
lambda = c/freq;
ang = [30;0];
w = steervec(getElementPosition(myArray)/lambda,ang);
d = directivity(myArray,freq,ang,'PropagationSpeed',c,...
    'Weights',w)
d = 20.9519
```


## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \Pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## See Also <br> pattern | patternAzimuth | patternElevation

## collectPlaneWave

System object: phased. HeterogeneousConformalArray
Package: phased
Simulate received plane waves

## Syntax

```
Y = collectPlaneWave(H,X,ANG)
Y = collectPlaneWave(H,X,ANG,FREQ)
Y = collectPlaneWave(H,X,ANG,FREQ,C)
```


## Description

$Y=\operatorname{collectPlaneWave}(H, X, A N G)$ returns the received signals at the sensor array, $H$, when the input signals indicated by $X$ arrive at the array from the directions specified in ANG.
$Y=\operatorname{collectPlaneWave}(H, X, A N G, F R E Q)$, in addition, specifies the incoming signal carrier frequency in FREQ.
$Y=\operatorname{collectPlaneWave}(H, X, A N G, F R E Q, C)$, in addition, specifies the signal propagation speed in C.

## Input Arguments

## H

Array object.
X
Incoming signals, specified as an M-column matrix. Each column of $X$ represents an individual incoming signal.

## ANG

Directions from which incoming signals arrive, in degrees. ANG can be either a 2-by-M matrix or a row vector of length $M$.

If ANG is a 2-by-M matrix, each column specifies the direction of arrival of the corresponding signal in X. Each column of ANG is in the form [azimuth; elevation]. The azimuth angle must be between $-180^{\circ}$ and $180^{\circ}$, inclusive. The elevation angle must be between $-90^{\circ}$ and $90^{\circ}$, inclusive.

If ANG is a row vector of length M , each entry in ANG specifies the azimuth angle. In this case, the corresponding elevation angle is assumed to be $0^{\circ}$.

FREQ
Carrier frequency of signal in hertz. FREQ must be a scalar.
Default: 3e8

## C

Propagation speed of signal in meters per second.
Default: Speed of light

## Output Arguments

## Y

Received signals. Y is an N-column matrix, where N is the number of elements in the array H. Each column of $Y$ is the received signal at the corresponding array element, with all incoming signals combined.

## Examples

## Simulate Received Signal at Heterogeneous Conformal Array

Simulate the received signal at an 8 -element heterogeneous uniform circular array created using the phased. HeterogeneousConformalArray System object ${ }^{\mathrm{TM}}$. The signals arrive from $10^{\circ}$ and $30^{\circ}$ azimuth. Both signals have an elevation angle of $0^{\circ}$. Assume the propagation speed is the speed of light.

```
antenna1 = phased.CosineAntennaElement('CosinePower',1.5);
antenna2 = phased.CosineAntennaElement('CosinePower',1.8);
N = 8;
azang = (0:N-1)*360/N-180;
array = phased.HeterogeneousConformalArray('ElementPosition', ...
    [cosd(azang);sind(azang);zeros(1,N)],'ElementNormal',[azang;zeros(1,N)], ...
    'ElementSet',{antenna1,antenna2},'ElementIndices',[11 1 1 1 2 2 2 2]);
c = physconst('LightSpeed');
y = collectPlaneWave(array,randn(4,2),[10 30],c);
disp(y(:,1:2))
0.7476 + 0.2890i 0.5378 + 0.5554i
0.9544 - 0.8005i -0.5059 + 1.3857i
-2.5374 - 0.5387i -1.3746 - 2.1411i
    1.0865 + 0.3377i 0.6977 + 0.8549i
```


## Algorithms

collectPlaneWave modulates the input signal with a phase corresponding to the delay caused by the direction of arrival. The method does not account for the response of individual elements in the array.

For further details, see Van Trees [1].

## References

[1] Van Trees, H. Optimum Array Processing. New York: Wiley-Interscience, 2002.

## getElementNormal

## System object: phased. HeterogeneousConformalArray

Package: phased
Normal vector to array elements

## Syntax

normvec = getElementNormal(sConfArray)
normvec = getElementNormal(sConfArray,elemidx)

## Description

normvec $=$ getElementNormal (sConfArray) returns the normal vectors of the array elements of the phased.sConfArray System object, sConfArray. The output argument normvec is a 2-by- $N$ matrix, where $N$ is the number of elements in array, sConfArray. Each column of normvec defines the normal direction of an element in the local coordinate system in the form [az;el]. Units are degrees. The origin of the local coordinate system is defined by the phase center of the array.
normvec $=$ getElementNormal(sConfArray, elemidx) returns only the normal vectors of the elements specified in the element index vector, elemidx. This syntax can use any of the input arguments in the previous syntax.

## Input Arguments

## sConfArray - Heterogeneous conformal array

phased.HeterogeneousConformalArray System object
Heterogeneous conformal array, specified as a phased. HeterogeneousConformalArray System object.

## Example: phased.HeterogeneousConformalArray

elemidx - Element indices
all array elements (default) | integer-valued 1-by-M row vector | integer-valued $M$-by-1 column vector
Element indices, specified as a 1 -by- $M$ or $M$-by-1 vector. Index values lie in the range 1 to $N$ where $N$ is the number of elements of the array. When elemidx is specified, getElementNormal returns the normal vectors of the elements contained in elemidx.
Example: [1,5,4]

## Output Arguments

## normvec - Element normal vectors

2 -by- $P$ real-valued vector
Element normal vectors, specified as a 2 -by- $P$ real-valued vector. Each column of normvec takes the form [az,el]. When elemidx is not specified, $P$ equals the array dimension. When elemidx is specified, $P$ equals the length of elemidx, $M$.

## Examples

## Display Heterogeneous Conformal Array Element Normals

Construct a 5 -element acoustic cross array (UCA) composed of two different types of cosine antenna elements. Use the Phased. HeterogeneousConformalArray System object ${ }^{\mathrm{TM}}$. Assume the operating frequency is 4 kHz . A typical value for the speed of sound in seawater is $1500.0 \mathrm{~m} / \mathrm{s}$. Display the array normal vectors.

```
N = 5;
fc = 4000;
c = 1500.0;
lam = c/fc;
x = zeros(1,N);
y = [-1,0,1,0,0]*lam/2;
z = [0,0,0,-1,1]*lam/2;
sCos1 = phased.CosineAntennaElement('CosinePower',1.5);
sCos2 = phased.CosineAntennaElement('CosinePower',1.8);
sHCA = phased.HeterogeneousConformalArray('ElementSet',{sCos1,sCos2},...
    'ElementIndices',[1,2,2,2,1],...
    'ElementPosition',[x;y;z],...
    'ElementNormal', [[-20,-10,0,10,20];zeros(1,N)]);
pos = getElementPosition(sHCA)
pos = 3\times5
```

| 0 | 0 | 0 | 0 | 0 |
| ---: | ---: | ---: | ---: | ---: |
| -0.1875 | 0 | 0.1875 | 0 | 0 |
| 0 | 0 | 0 | -0.1875 | 0.1875 |

```
normvec = getElementNormal(sHCA)
```

normvec $=2 \times 5$
$\begin{array}{lllll}-20 & -10 & 0 & 10 & 20\end{array}$
$\begin{array}{rrrrr}0 & 0 & 0 & 0 & 0\end{array}$

## Version History

Introduced in R2016a

## getElementPosition

System object: phased. HeterogeneousConformalArray
Package: phased
Positions of array elements

## Syntax

```
pos = getElementPosition(sHCA)
pos = getElementPosition(sHCA,elemidx)
```


## Description

pos $=$ getElementPosition(sHCA) returns the element positions of the
HeterogeneousConformalArray System object, sHCA. POS is an 3 -by- $N$ matrix where $N$ is the number of elements in H . Each column of pos defines the position of an element in the local coordinate system, in meters, in the form $[x ; y ; z]$.

For details regarding the local coordinate system of the conformal or heterogeneous conformal array, enter phased.ConformalArray.coordinateSystemInfo.
pos $=$ getElementPosition (sHCA, elemidx) returns the positions of the elements that are specified in the element index vector elemidx.

## Examples

## Element Positions of Heterogeneous Conformal Array

Construct an 8 -element heterogeneous conformal array with oriented short-dipole antenna elements. Then, obtain the positions of the first four elements.

```
sElement1 = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[100e6 le9],...
    'AxisDirection','Z');
sElement2 = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[100e6 le9],...
    'AxisDirection','Y');
N = 8; azang = (0:N-1)*360/N-180;
sArray = phased.HeterogeneousConformalArray(...
    'ElementPosition',...
    [cosd(azang);sind(azang);zeros(1,N)],...
    'ElementNormal',[azang;zeros(1,N)],...
    'ElementSet',{sElement1,sElement2},...
    'ElementIndices',[1 1 1 1 2 2 2 2]);
pos = getElementPosition(sArray);
disp(pos(:,1:4));
\begin{tabular}{rrrr}
-1.0000 & -0.7071 & 0 & 0.7071 \\
0 & -0.7071 & -1.0000 & -0.7071 \\
0 & 0 & 0 & 0
\end{tabular}
```

1 Objects

## getNumElements

System object: phased. HeterogeneousConformalArray
Package: phased
Number of elements in array

## Syntax

N = getNumElements(H)

## Description

$N=$ getNumElements $(H)$ returns the number of elements, $N$, in the conformal array object $H$.

## Examples

## Number of Elements in Heterogeneous Conformal Array

Construct a heterogeneous 8 -element circular array and use the getNumElements method to return the number of elements.

```
antenna1 = phased.ShortDipoleAntennaElement('FrequencyRange',[100e6 1e9], ...
    'AxisDirection','Z');
antenna2 = phased.ShortDipoleAntennaElement('FrequencyRange',[100e6 1e9], ...
    'AxisDirection','Y');
N = 8;
azang = (0:N-1)*360/N-180;
array = phased.HeterogeneousConformalArray('ElementPosition', ...
    [cosd(azang);sind(azang);zeros(1,N)], ...
    'ElementNormal',[azang;zeros(1,N)], ...
    'ElementSet',{antenna1,antenna2}, ...
    'ElementIndices',[1 1 1 1 2 2 2 2]);
N = getNumElements(array)
N = 8
```


## getTaper

System object: phased. HeterogeneousConformalArray
Package: phased
Array element tapers

## Syntax

wts = getTaper(h)

## Description

wts = getTaper(h) returns the tapers applied to each element of a conformal array, h. Tapers are often referred to as weights.

## Input Arguments

h - Conformal array
phased. HeterogeneousConformalArray System object
Conformal array specified as a phased. HeterogeneousConformalArray System object.

## Output Arguments

## wts - Array element tapers

$N$-by-1 complex-valued vector
Array element tapers returned as an $N$-by-1, complex-valued vector, where $N$ is the number of elements in the array.

## Examples

## Create Tapered Heterogeneous Conformal Disk Array

Create a 12 -element, 2 -ring tapered disk array where the outer ring is more heavily tapered than the inner ring.

```
antennal = phased.ShortDipoleAntennaElement('FrequencyRange',[100e6 le9], ...
    'AxisDirection','Z');
antenna2 = phased.ShortDipoleAntennaElement('FrequencyRange',[100e6 1e9], ...
    'AxisDirection','Y');
elemAngles = ([0:5]*360/6);
elemPosInner = 0.5*[zeros(size(elemAngles));cosd(elemAngles); ...
    sind(elemAngles)];
elemPosOuter = [zeros(size(elemAngles));cosd(elemAngles); ...
    sind(elemAngles)];
elemNorms = repmat([0;0],1,12);
taper = [ones(size(elemAngles)),0.3*ones(size(elemAngles))];
```

```
array \(=\) phased. HeterogeneousConformalArray('ElementSet',\{antennal, antenna2\}, ...
        'ElementIndices',[1 1 1 1 1 1 2 22222\(],\)
        'ElementPosition', [elemPosInner, elemPosOuter], 'ElementNormal',elemNorms, ...
        'Taper',taper);
w = getTaper(array)
\(w=12 \times 1\)
```

    1.0000
    1.0000
    1.0000
    1.0000
    1.0000
    1.0000
    0.3000
    0.3000
    0.3000
    0.3000
    Draw the array showing taper colors.

```
viewArray(array,'ShowTaper',true,'ShowIndex','all')
```


## Array Geometry



[^1]
## isPolarizationCapable

System object: phased. HeterogeneousConformalArray
Package: phased
Polarization capability

## Syntax

flag = isPolarizationCapable(h)

## Description

flag = isPolarizationCapable(h) returns a Boolean value, flag, indicating whether the array supports polarization. An array supports polarization if all of its constituent sensor elements support polarization.

## Input Arguments

h - Conformal array
Conformal array specified as a phased. HeterogeneousConformalArray System object.

## Output Arguments

## flag - Polarization-capability flag

Polarization-capability returned as a Boolean value true if the array supports polarization or false if it does not.

## Examples

## Conformal Heterogeneous Array Supports Polarization

Show that a disk heterogeneous conformal array of short-dipole antennas supports polarization.

```
antennal = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[100e6 le9],...
    'AxisDirection','Z');
antenna2 = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[100e6 le9],...
    'AxisDirection','Y');
elemAngles = ([0:5]*360/6);
elemPosInner = 0.5*[zeros(size(elemAngles));...
    cosd(elemAngles); sind(elemAngles)];
elemPosOuter = [zeros(size(elemAngles));...
    cosd(elemAngles); sind(elemAngles)];
elemNorms = repmat([0;0],1,12);
array = phased.HeterogeneousConformalArray(...
    'ElementSet',{antenna1,antenna2},...
```


## Array Geometry



The returned value of 1 shows that this array supports polarization when used with a polarized antenna.

## pattern

System object: phased. HeterogeneousConformalArray
Package: phased
Plot heterogeneous conformal array pattern

## Syntax

pattern(sArray,FREQ)
pattern(sArray,FREQ,AZ)
pattern(sArray,FREQ,AZ,EL)
pattern( _, Name, Value)
[PAT,AZ_ANG,EL_ANG] = pattern( $\qquad$ )

## Description

pattern(sArray, FREQ) plots the 3-D array directivity pattern (in dBi) for the array specified in sArray. The operating frequency is specified in FREQ.

The integration used when computing array directivity has a minimum sampling grid of 0.1 degrees. If an array pattern has a beamwidth smaller than this, the directivity value will be inaccurate.
pattern(sArray, FREQ,AZ) plots the array directivity pattern at the specified azimuth angle.
pattern(sArray, $\mathrm{FREQ}, \mathrm{AZ}, \mathrm{EL}$ ) plots the array directivity pattern at specified azimuth and elevation angles.
pattern( __, Name, Value) plots the array pattern with additional options specified by one or more Name, Value pair arguments.
[PAT,AZ ANG,EL ANG] = pattern( $\qquad$ ) returns the array pattern in PAT. The AZ_ANG output contains the coordinate values corresponding to the rows of PAT. The EL_ANG output contains the coordinate values corresponding to the columns of PAT. If the 'CoordinateSystem' parameter is set to 'uv', then AZ_ANG contains the $U$ coordinates of the pattern and EL_ANG contains the $V$ coordinates of the pattern. Otherwise, they are in angular units in degrees. $U V$ units are dimensionless.

Note This method replaces the plotResponse method. See "Convert plotResponse to pattern" on page 1-521 for guidelines on how to use pattern in place of plotResponse.

## Input Arguments

## sArray - Heterogeneous conformal array

System object
Heterogeneous conformal array, specified as a phased.HeterogeneousConformalArray System object.
Example: sArray= phased.HeterogeneousConformalArray;

## FREQ - Frequency for computing directivity and patterns

positive scalar | 1-by-L real-valued row vector
Frequencies for computing directivity and patterns, specified as a positive scalar or 1-by-L realvalued row vector. Frequency units are in hertz.

- For an antenna, microphone, or sonar hydrophone or projector element, FREQ must lie within the range of values specified by the FrequencyRange or FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased. CustomAntennaElement and phased.CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

```
Example: [1e8 2e6]
```

Data Types: double

## AZ - Azimuth angles

[-180:180] (default) | 1-by- $N$ real-valued row vector
Azimuth angles for computing directivity and pattern, specified as a 1-by- $N$ real-valued row vector where $N$ is the number of azimuth angles. Angle units are in degrees. Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the $x y$ plane. When measured from the $x$-axis toward the $y$-axis, this angle is positive.

## Example: [-45:2:45]

Data Types: double

## EL - Elevation angles

[-90:90] (default) | 1-by-M real-valued row vector
Elevation angles for computing directivity and pattern, specified as a 1-by-M real-valued row vector where $M$ is the number of desired elevation directions. Angle units are in degrees. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

The elevation angle is the angle between the direction vector and $x y$-plane. The elevation angle is positive when measured towards the $z$-axis.

Example: [-75:1:70]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

```
CoordinateSystem - Plotting coordinate system
'polar' (default)|'rectangular'|'uv'
```

Plotting coordinate system of the pattern, specified as the comma-separated pair consisting of 'CoordinateSystem' and one of 'polar', 'rectangular', or 'uv'. When
'CoordinateSystem' is set to 'polar' or 'rectangular', the AZ and EL arguments specify the pattern azimuth and elevation, respectively. AZ values must lie between $-180^{\circ}$ and $180^{\circ}$. EL values must lie between $-90^{\circ}$ and $90^{\circ}$. If 'CoordinateSystem' is set to ' uv ', AZ and EL then specify $U$ and $V$ coordinates, respectively. AZ and EL must lie between -1 and 1 .
Example: 'uv'
Data Types: char

## Type - Displayed pattern type

'directivity' (default)|'efield'|'power'|'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb' - power pattern converted to dB.

Example: 'powerdb'
Data Types: char

## Orientation - Array orientation

[0;0;0]. (default) | 3-by-1 real-valued column vector
Array orientation, specified as a 3-by-1 real-valued column vector containing the rotation angles with respect to the $x$-, $y$-, and $z$-axes of the local coordinate system, respectively.

## Normalize - Display normalize pattern

true (default) | false
Display normalized pattern, specified as the comma-separated pair consisting of 'Normalize' and a Boolean. Set this parameter to true to display a normalized pattern. This parameter does not apply when you set 'Type' to 'directivity'. Directivity patterns are already normalized.
Data Types: logical

## ShowArray - View array geometry

false (default) | true
View the array geometry along with the 3D radiation pattern, specified as false or true.
Data Types: logical
ShowLocalCoordinates - Show local coordinate axes
true (default) | false
Show the local coordinate axes, specified as true or false.
Data Types: logical

## ShowColorbar - Show colorbar

true (default) | false

Show the colorbar, specified as true or false.

## Data Types: logical

## Parent - Handle to axis

scalar
Handle to the axes along which the array geometry is displayed specified as a scalar.

## PlotStyle - Plotting style

'overlay' (default)|'waterfall'
Plotting style, specified as the comma-separated pair consisting of 'Plotstyle' and either 'overlay' or 'waterfall'. This parameter applies when you specify multiple frequencies in FREQ in 2-D plots. You can draw 2-D plots by setting one of the arguments AZ or EL to a scalar.

## Data Types: char

## Polarization - Polarized field component

```
'combined' (default)| 'H' | 'V'
```

Polarized field component to display, specified as the comma-separated pair consisting of 'Polarization' and 'combined', 'H', or 'V'. This parameter applies only when the sensors are polarization-capable and when the 'Type' parameter is not set to 'directivity'. This table shows the meaning of the display options.

| 'Polarization ' | Display |
| :--- | :--- |
| 'combined ' | Combined $H$ and $V$ polarization components |
| ' $\mathrm{H}^{\prime}$ | $H$ polarization component |
| ' $\mathrm{V}^{\prime}$ | $V$ polarization component |

Example: 'V '

## Data Types: char

## PropagationSpeed - Signal propagation speed

speed of light (default) | positive scalar
Signal propagation speed, specified as the comma-separated pair consisting of
' PropagationSpeed ' and a positive scalar in meters per second.
Example: 'PropagationSpeed', physconst('LightSpeed')
Data Types: double

## Weights - Array weights

1 (default) | $N$-by-1 complex-valued column vector | $N$-by-L complex-valued matrix
Array weights, specified as the comma-separated pair consisting of 'Weights' and an N -by-1 complex-valued column vector or $N$-by- $L$ complex-valued matrix. Array weights are applied to the elements of the array to produce array steering, tapering, or both. The dimension $N$ is the number of elements in the array. The dimension $L$ is the number of frequencies specified by FREQ.

| Weights Dimension | FREQ Dimension | Purpose |
| :--- | :--- | :--- |
| $N$-by-1 complex-valued column <br> vector | Scalar or 1-by- $L$ row vector | Applies a set of weights for the <br> single frequency or for all $L$ <br> frequencies. |
| $N$-by- $L$ complex-valued matrix | 1-by- $L$ row vector | Applies each of the $L$ columns of <br> 'Weights ' for the <br> corresponding frequency in <br> FREQ. |

Note Use complex weights to steer the array response toward different directions. You can create weights using the phased. SteeringVector System object or you can compute your own weights. In general, you apply Hermitian conjugation before using weights in any Phased Array System Toolbox function or System object such as phased. Radiator or phased. Collector. However, for the directivity, pattern, patternAzimuth, and patternElevation methods of any array System object use the steering vector without conjugation.

Example: 'Weights', ones ( $\mathrm{N}, \mathrm{M}$ )
Data Types: double
Complex Number Support: Yes

## Output Arguments

## PAT - Array pattern

$M$-by- $N$ real-valued matrix
Array pattern, returned as an $M$-by- $N$ real-valued matrix. The dimensions of PAT correspond to the dimensions of the output arguments AZ_ANG and EL_ANG.

## AZ_ANG - Azimuth angles

scalar | 1-by- $N$ real-valued row vector
Azimuth angles for displaying directivity or response pattern, returned as a scalar or 1-by- $N$ realvalued row vector corresponding to the dimension set in AZ. The columns of PAT correspond to the values in AZ_ANG. Units are in degrees.

## EL_ANG - Elevation angles

scalar | 1-by-M real-valued row vector
Elevation angles for displaying directivity or response, returned as a scalar or 1-by-M real-valued row vector corresponding to the dimension set in EL. The rows of PAT correspond to the values in EL_ANG. Units are in degrees.

## Examples

## Plot Power Patterns of 8-Element Heterogeneous Uniform Circular Array

Create an 8-element uniform circular array using the HeterogeneousConformalArray System object $^{\mathrm{TM}}$ with two different types of short-dipole elements. Then, plot the 3-D and 2-D power patterns.

## Create the array

```
sElement1 = phased.ShortDipoleAntennaElement('FrequencyRange',[1e9 5e9],...
    'AxisDirection','Z');
sElement2 = phased.ShortDipoleAntennaElement('FrequencyRange',[1e9 5e9],...
        'AxisDirection','Y');
N = 8;
azang = (0:N-1)*360/N-180;
sArray = phased.HeterogeneousConformalArray(...
    'ElementPosition',...
    0.4*[zeros(1,N);cosd(azang);sind(azang)],...
    'ElementNormal', zeros(2,N),...
    'ElementSet',{sElement1,sElement2},...
    'ElementIndices',[1 1 1 1 2 2 2 2]);
```

Plot 3-D power pattern
Assume the operating frequency is 1.5 GHz and the wave propagation speed is the speed of light.

```
c = physconst('LightSpeed');
fc = 1.5e9;
pattern(sArray,fc,[-180:180],[-90:90],...
    'PropagationSpeed',c',...
    'CoordinateSystem','polar',...
    'Type','powerdb',...
    'Polarization','combined')
```



## Plot 2-D power pattern

Take a cut of the 3-D power pattern at zero degrees elevation.

```
pattern(sArray,fc,[-180:180],0,...
    'PropagationSpeed ', c',...
    'CoordinateSystem','polar',...
    'Type','powerdb',...
    'Polarization','combined')
```



Normalized Power (dB), Broadside at $0.00^{\circ}$

## Plot Pattern of Disk Array

Construct a 24 -element disk array using elements with two different types of cosine antennas. Then, plot the array pattern.

## Create the array

The array consists of cosine antenna elements with different power exponents.

```
sElement1 = phased.CosineAntennaElement('CosinePower',1.5);
sElement2 = phased.CosineAntennaElement('CosinePower',1.8);
N = 8;
azang = (0:N-1)*360/N-180;
p0 = [zeros(1,N);cosd(azang);sind(azang)];
posn = [0.6*p0, 0.4*p0, 0.2*p0];
sArray1 = phased.HeterogeneousConformalArray(...
```

```
'ElementPosition',posn,...
'ElementNormal', zeros(2,3*N),...
'ElementSet',{sElement1,sElement2},...
'ElementIndices',[1 1 1 1 1 1 1 1,...
1 1 1 1 1 1 1 1,...
2 2 2 2 2 2 2 2]);
```


## View the disk array

viewArray(sArray1)


## Plot the power pattern

Plot the elevation power pattern of this array two different sets of element weights. The first set is uniform weights on the elements. The second set is a tapered set of weights set by the Weights parameter. Restrict the plot of the response from -60 to 60 degrees in 0.1 degree increments. Assume the operating frequency is 1 GHz and the wave propagation speed is the speed of light.

```
c = physconst('LightSpeed');
fc = 1e9;
wts1 = ones(3*N,1);
wts1 = wts1/sum(abs(wts1));
wts2 = [0.5*ones(N,1); 0.7*ones(N,1); 1*ones(N,1)];
wts2 = wts2/sum(abs(wts2));
pattern(sArray1,fc,0,[-60:0.1:60],'PropagationSpeed ',c,...
    'CoordinateSystem','polar',...
    'Type','powerdb','Weights',[wts1,wts2])
```



As expected, the tapered weights broaden the mainlobe and reduce the sidelobes.

## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \Pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as dBi. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Convert plotResponse to pattern

For antenna, microphone, and array System objects, the pattern method replaces the plotResponse method. In addition, two new simplified methods exist just to draw 2-D azimuth and elevation pattern plots. These methods are azimuthPattern and elevationPattern.

The following table is a guide for converting your code from using plotResponse to pattern. Notice that some of the inputs have changed from input arguments to Name-Value pairs and conversely. The general pattern method syntax is
pattern(H,FREQ,AZ,EL, 'Name1', 'Value1',...,' NameN', 'ValueN')

| plotResponse Inputs | plotResponse Description | pattern Inputs |
| :--- | :--- | :--- |
| H argument | Antenna, microphone, or array <br> System object. | H argument (no change) |
| FREQ argument | Operating frequency. | FREQ argument (no change) |
| V argument | Propagation speed. This argument <br> is used only for arrays. | 'PropagationSpeed ' name-value <br> pair. This parameter is only used for <br> arrays. |


| plotResponse Inputs | plotResponse Description |  | pattern Inputs |  |
| :---: | :---: | :---: | :---: | :---: |
| 'Format' and 'RespCut' namevalue pairs | These options work together to let you create a plot in angle space (line or polar style) or $U V$ space. They also determine whether the plot is 2-D or 3-D. This table shows you how to create different types of plots using plotResponse. |  | 'CoordinateSystem' name-value pair used together with the AZ and EL input arguments. <br> 'CoordinateSystem' has the same options as the plotResponse method 'Format ' name-value pair, except that 'line' is now named 'rectangular'. The table shows how to create different types of plots using pattern. |  |
|  | Display space |  |  |  |
|  | Angle space (2D) |  |  |  |
|  |  | Set 'RespCut'to 'Az' or'El'. Set'Format' to'line' or'polar'.Set the displayaxis using eitherthe'AzimuthAngleS' or'ElevationAngles' name-value pairs. | Display space |  |
|  |  |  | Angle space (2D) <br> Angle space (3D) | Set <br> 'Coordinate <br> System' to rectangular' or 'polar'. <br> Specify either AZ or EL as a scalar. |
|  |  |  |  | Set <br> 'Coordinate <br> System' to 'rectangular' |
|  | Angle space (3D) | Set 'RespCut' to '3D'. Set 'Format' to ' line' or 'polar'. <br> Set the display axis using both the 'AzimuthAngle ${ }^{\prime}$ and 'Elevation Angles ' namevalue pairs. |  | or 'polar'. <br> Specify both AZ and EL as vectors. |
|  |  |  | UV space (2D) | Set <br> 'Coordinate <br> System' to 'uv'. Use AZ to specify a $U$ space vector. Use EL to specify a $V$-space scalar. |
|  |  |  | UV space (3D) | Set |
|  | UV space (2D) | Set 'RespCut' to'U'. Set 'Format' to 'UV '. Set the display range using the 'UGrid' namevalue pair. |  | System' to 'uv'. Use AZ to specify a $U$ space vector. <br> Use EL to specify a $V$-space vector. |
|  |  |  | If you set CoordinateSystem to 'uv', enter the UV grid values using AZ and EL . |  |
|  | UV space (3D) | $\begin{aligned} & \text { Set 'RespCut' } \\ & \text { to'3D'. Set } \\ & \text { 'Format' to } \end{aligned}$ |  |  |



| plotResponse Inputs | plotResponse Description | pattern Inputs |
| :--- | :--- | :--- |
| 'ElevationAngles ' name-value <br> pair | Elevation angles used to display the <br> antenna or array response. | EL argument |
| 'UGrid' name-value pair | Contains $U$ coordinates in $U V$ - <br> space. | AZ argument when <br> 'CoordinateSystem ' name-value <br> pair is set to ' uv ' |
| 'VGrid' name-value pair | Contains V-coordinates in $U V$-space. | EL argument when <br> 'CoordinateSystem ' name-value <br> pair is set to 'uv ' |

## Version History <br> Introduced in R2015a

See Also<br>patternAzimuth | patternElevation

## patternAzimuth

System object: phased. HeterogeneousConformalArray
Package: phased
Plot heterogeneous conformal array directivity or pattern versus azimuth

## Syntax

```
patternAzimuth(sArray,FREQ)
patternAzimuth(sArray,FREQ,EL)
patternAzimuth(sArray,FREQ,EL,Name,Value)
PAT = patternAzimuth(
```

$\qquad$

## Description

patternAzimuth (sArray, FREQ) plots the 2-D array directivity pattern versus azimuth (in dBi) for the array sArray at zero degrees elevation angle. The argument FREQ specifies the operating frequency.

The integration used when computing array directivity has a minimum sampling grid of 0.1 degrees. If an array pattern has a beamwidth smaller than this, the directivity value will be inaccurate.
patternAzimuth(sArray, FREQ,EL), in addition, plots the 2-D array directivity pattern versus azimuth (in dBi) for the array sArray at the elevation angle specified by EL. When EL is a vector, multiple overlaid plots are created.
patternAzimuth(sArray, FREQ,EL,Name, Value) plots the array pattern with additional options specified by one or more Name, Value pair arguments.

PAT = patternAzimuth( $\qquad$ ) returns the array pattern. PAT is a matrix whose entries represent the pattern at corresponding sampling points specified by the 'Azimuth ' parameter and the EL input argument.

## Input Arguments

## sArray - Heterogeneous conformal array

System object
Heterogeneous conformal array, specified as a phased.HeterogeneousConformalArray System object.
Example: sArray= phased. HeterogeneousConformalArray;

## FREQ - Frequency for computing directivity and pattern

positive scalar
Frequency for computing directivity and pattern, specified as a positive scalar. Frequency units are in hertz.

- For an antenna or microphone element, FREQ must lie within the range of values specified by the FrequencyRange or the FrequencyVector property of the element. Otherwise, the element
produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased.CustomMic rophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: 1e8
Data Types: double

## EL - Elevation angles

1 -by- $N$ real-valued row vector
Elevation angles for computing sensor or array directivities and patterns, specified as a 1-by- $N$ realvalued row vector. The quantity $N$ is the number of requested elevation directions. Angle units are in degrees. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

The elevation angle is the angle between the direction vector and the $x y$ plane. When measured toward the $z$-axis, this angle is positive.
Example: [0, 10, 20]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Type - Displayed pattern type

'directivity' (default)|'efield'|'power'|'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb' - power pattern converted to dB.

Example: 'powerdb'
Data Types: char

## PropagationSpeed - Signal propagation speed

## speed of light (default) | positive scalar

Signal propagation speed, specified as the comma-separated pair consisting of ' PropagationSpeed ' and a positive scalar in meters per second.
Example: 'PropagationSpeed', physconst('LightSpeed')
Data Types: double

## Weights - Array weights

M-by-1 complex-valued column vector
Array weights, specified as the comma-separated pair consisting of 'Weights' and an $M$-by- 1 complex-valued column vector. Array weights are applied to the elements of the array to produce array steering, tapering, or both. The dimension $M$ is the number of elements in the array.

Note Use complex weights to steer the array response toward different directions. You can create weights using the phased. SteeringVector System object or you can compute your own weights. In general, you apply Hermitian conjugation before using weights in any Phased Array System Toolbox function or System object such as phased. Radiator or phased. Collector. However, for the directivity, pattern, patternAzimuth, and patternElevation methods of any array System object use the steering vector without conjugation.

Example: 'Weights', ones (10,1)
Data Types: double
Complex Number Support: Yes

## Azimuth - Azimuth angles

[-180:180] (default) | 1-by-P real-valued row vector
Azimuth angles, specified as the comma-separated pair consisting of 'Azimuth' and a 1-by-P realvalued row vector. Azimuth angles define where the array pattern is calculated.
Example: 'Azimuth', [-90:2:90]
Data Types: double

## Parent - Handle to axis

scalar
Handle to the axes along which the array geometry is displayed specified as a scalar.

## Output Arguments

## PAT - Array directivity or pattern

L-by- $N$ real-valued matrix
Array directivity or pattern, returned as an $L$-by- $N$ real-valued matrix. The dimension $L$ is the number of azimuth values determined by the 'Azimuth' name-value pair argument. The dimension $N$ is the number of elevation angles, as determined by the EL input argument.

## Examples

## Plot Azimuthal Directivity Pattern of Disk Array

Construct a 24-element disk array using elements with two different types of cosine antennas. Then, plot the array azimuthal directivity pattern.

## Create the array

The array consists of cosine antenna elements with different power exponents.

```
sElement1 = phased.CosineAntennaElement('CosinePower',1.5);
sElement2 = phased.CosineAntennaElement('CosinePower',1.8);
N = 8;
azang = (0:N-1)*360/N-180;
p0 = [zeros(1,N);cosd(azang);sind(azang)];
posn = [0.6*p0, 0.4*p0, 0.2*p0];
sArray = phased.HeterogeneousConformalArray(...
    'ElementPosition',posn,...
    'ElementNormal', zeros(2,3*N),...
    'ElementSet',{sElement1,sElement2},...
    'ElementIndices',[1 1 1 1 1 1 1 1,...
    1 1 1 1 1 1 1 1,...
    2 2 2 2 2 2 2 2]);
```


## View the disk array

```
viewArray(sArray)
```


## Array Geometry



[^2]
## Plot the power pattern

Plot the azimuthal power pattern of this array for three different elevation angles: 0,10 and 25 degrees. Apply radial tapering to the array. Assume the operating frequency is 1 GHz and the wave propagation speed is the speed of light.

```
c = physconst('LightSpeed');
fc = 1e9;
wts = [0.5*ones(N,1); 0.7*ones(N,1); 1.0*ones(N,1)];
wts = wts/sum(abs(wts));
```

patternAzimuth(sArray,fc,[0,10,25],'PropagationSpeed', c,...
'Type', 'directivity', 'Weights', wts)


## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \Pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Version History

Introduced in R2015a

See Also<br>patternElevation|pattern

## patternElevation

System object: phased. HeterogeneousConformalArray
Package: phased
Plot heterogeneous conformal array directivity or pattern versus elevation

## Syntax

patternElevation(sArray,FREQ)
patternElevation(sArray,FREQ,AZ)
patternElevation(sArray, FREQ, AZ, Name, Value)
PAT = patternElevation( $\qquad$

## Description

patternElevation(sArray, FREQ) plots the 2-D array directivity pattern versus elevation (in dBi) for the array sArray at zero degrees azimuth angle. When AZ is a vector, multiple overlaid plots are created. The argument FREQ specifies the operating frequency.

The integration used when computing array directivity has a minimum sampling grid of 0.1 degrees. If an array pattern has a beamwidth smaller than this, the directivity value will be inaccurate.
patternElevation(sArray, FREQ, AZ), in addition, plots the 2-D element directivity pattern versus elevation (in dBi ) at the azimuth angle specified by $A Z$. When $A Z$ is a vector, multiple overlaid plots are created.
patternElevation(sArray, FREQ,AZ,Name, Value) plots the array pattern with additional options specified by one or more Name, Value pair arguments.

PAT = patternElevation ( _ _ ) returns the array pattern. PAT is a matrix whose entries represent the pattern at corresponding sampling points specified by the 'Elevation' parameter and the AZ input argument.

## Input Arguments

## sArray - Heterogeneous conformal array

System object
Heterogeneous conformal array, specified as a phased.HeterogeneousConformalArray System object.
Example: sArray= phased.HeterogeneousConformalArray;

## FREQ - Frequency for computing directivity and pattern

positive scalar
Frequency for computing directivity and pattern, specified as a positive scalar. Frequency units are in hertz.

- For an antenna or microphone element, FREQ must lie within the range of values specified by the FrequencyRange or the FrequencyVector property of the element. Otherwise, the element
produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased.CustomMic rophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: 1e8
Data Types: double

## AZ - Azimuth angles for computing directivity and pattern

1 -by- $N$ real-valued row vector
Azimuth angles for computing sensor or array directivities and patterns, specified as a 1 -by- $N$ realvalued row vector where $N$ is the number of desired azimuth directions. Angle units are in degrees. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the $x y$ plane. This angle is positive when measured from the $x$-axis toward the $y$-axis.
Example: [0,10,20]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Type - Displayed pattern type

'directivity' (default)|'efield'|'power'|'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb' - power pattern converted to dB.

Example: 'powerdb'
Data Types: char

## PropagationSpeed - Signal propagation speed

speed of light (default) | positive scalar
Signal propagation speed, specified as the comma-separated pair consisting of ' PropagationSpeed ' and a positive scalar in meters per second.
Example: 'PropagationSpeed', physconst('LightSpeed')
Data Types: double

## Weights - Array weights

M-by-1 complex-valued column vector
Array weights, specified as the comma-separated pair consisting of 'Weights' and an $M$-by- 1 complex-valued column vector. Array weights are applied to the elements of the array to produce array steering, tapering, or both. The dimension $M$ is the number of elements in the array.

Note Use complex weights to steer the array response toward different directions. You can create weights using the phased. SteeringVector System object or you can compute your own weights. In general, you apply Hermitian conjugation before using weights in any Phased Array System Toolbox function or System object such as phased. Radiator or phased. Collector. However, for the directivity, pattern, patternAzimuth, and patternElevation methods of any array System object use the steering vector without conjugation.

```
Example: 'Weights', ones (10,1)
```

Data Types: double
Complex Number Support: Yes

## Elevation - Elevation angles

[-90:90] (default) | 1-by-P real-valued row vector
Elevation angles, specified as the comma-separated pair consisting of 'Elevation' and a 1-by-P real-valued row vector. Elevation angles define where the array pattern is calculated.
Example: 'Elevation', [-90:2:90]
Data Types: double

## Parent - Handle to axis

scalar
Handle to the axes along which the array geometry is displayed specified as a scalar.

## Output Arguments

## PAT - Array directivity or pattern

## L-by-N real-valued matrix

Array directivity or pattern, returned as an $L$-by- $N$ real-valued matrix. The dimension $L$ is the number of elevation angles determined by the 'Elevation' name-value pair argument. The dimension $N$ is the number of azimuth angles determined by the AZ argument.

## Examples

## Plot Elevation Directivity Pattern of Disk Array

Construct a 24 -element disk array using elements with two different types of cosine antennas. Then, plot the array elevation directivity pattern.

## Create the array

The array consists of cosine antenna elements with different power exponents.

```
sElement1 = phased.CosineAntennaElement('CosinePower',1.5);
sElement2 = phased.CosineAntennaElement('CosinePower',1.8);
N = 8;
azang = (0:N-1)*360/N-180;
p0 = [zeros(1,N);cosd(azang);sind(azang)];
posn = [0.6*p0, 0.4*p0, 0.2*p0];
sArray = phased.HeterogeneousConformalArray(...
    'ElementPosition',posn,...
    'ElementNormal', zeros(2,3*N),...
    'ElementSet',{sElement1,sElement2},...
    'ElementIndices',[1 1 1 1 1 1 1 1,...
    1 1 1 1 1 1 1 1,...
    2 2 2 2 2 2 2 2]);
```


## View the disk array

```
viewArray(sArray)
```


## Array Geometry



[^3]
## Plot the power pattern

Plot the elevation power pattern of this array for three different azimuth angles: $0,-20$ and 25 degrees. Apply radial tapering to the array. Assume the operating frequency is 1 GHz and the wave propagation speed is the speed of light.

```
c = physconst('LightSpeed');
fc = 1e9;
wts = [0.5*ones(N,1); 0.7*ones(N,1); 1*ones(N,1)];
wts = wts/sum(abs(wts));
```

```
patternElevation(sArray,fc,[-20,0,25],'PropagationSpeed',c,...
```

'Type', 'directivity', 'Weights', wts)


## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \Pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Version History

Introduced in R2015a

See Also<br>pattern| patternAzimuth

## plotResponse

System object: phased. HeterogeneousConformalArray<br>Package: phased

Plot response pattern of array

## Syntax

plotResponse(H, FREQ, V)
plotResponse(H, FREQ, V, Name, Value)
hPlot = plotResponse( $\qquad$ )

## Description

plotResponse( $\mathrm{H}, \mathrm{FREQ}, \mathrm{V}$ ) plots the array response pattern along the azimuth cut, where the elevation angle is 0 . The operating frequency is specified in FREQ. The propagation speed is specified in V.
plotResponse(H, FREQ, V,Name, Value) plots the array response with additional options specified by one or more Name, Value pair arguments.
hPlot = plotResponse( $\qquad$ ) returns handles of the lines or surface in the figure window, using any of the input arguments in the previous syntaxes.

## Input Arguments

## H

Array object

## FREQ

Operating frequency in Hertz specified as a scalar or 1-by-K row vector. Values must lie within the range specified by a property of H . That property is named FrequencyRange or FrequencyVector, depending on the type of element in the array. The element has no response at frequencies outside that range. If you set the 'RespCut ' property of $H$ to ' 3 D ' , FREQ must be a scalar. When FREQ is a row vector, plotResponse draws multiple frequency responses on the same axes.

## V

Propagation speed in meters per second.

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## CutAngle

Cut angle as a scalar. This argument is applicable only when RespCut is ' Az ' or ' El '. If RespCut is 'Az' , CutAngle must be between -90 and 90. If RespCut is 'El', CutAngle must be between -180 and 180.

Default: 0

## Format

Format of the plot, using one of 'Line', 'Polar', or 'UV '. If you set Format to 'UV ', FREQ must be a scalar.

Default: 'Line'

## NormalizeResponse

Set this value to true to normalize the response pattern. Set this value to false to plot the response pattern without normalizing it. This parameter is not applicable when you set the Unit parameter value to 'dbi'.

## Default: true

## OverlayFreq

Set this value to true to overlay pattern cuts in a 2-D line plot. Set this value to false to plot pattern cuts against frequency in a 3-D waterfall plot. If this value is false, FREQ must be a vector with at least two entries.

This parameter applies only when Format is not 'Polar' and RespCut is not '3D '.

## Default: true

## Polarization

Specify the polarization options for plotting the array response pattern. The allowable values are |'None' | 'Combined' | 'H' | 'V' | where

- 'None' specifies plotting a nonpolarized response pattern
- 'Combined ' specifies plotting a combined polarization response pattern
- 'H' specifies plotting the horizontal polarization response pattern
- 'V ' specifies plotting the vertical polarization response pattern

For arrays that do not support polarization, the only allowed value is 'None '. This parameter is not applicable when you set the Unit parameter value to ' dbi ' .

Default: 'None'

## RespCut

Cut of the response. Valid values depend on Format, as follows:

- If Format is 'Line' or 'Polar', the valid values of RespCut are 'Az', 'El', and '3D'. The default is ' Az '.
- If Format is 'UV', the valid values of RespCut are 'U' and '3D'. The default is 'U'.

If you set RespCut to ' 3D' , FREQ must be a scalar.

## Unit

The unit of the plot. Valid values are 'db', 'mag', 'pow', or 'dbi'. This parameter determines the type of plot that is produced.

| Unit value | Plot type |
| :--- | :--- |
| db | power pattern in dB scale |
| mag | field pattern |
| pow | power pattern |
| dbi | directivity |

Default: 'db'

## Weights

Weight values applied to the array, specified as a length- $N$ column vector or $N$-by- $M$ matrix. The dimension $N$ is the number of elements in the array. The interpretation of $M$ depends upon whether the input argument FREQ is a scalar or row vector.

| Weights Dimensions | FREQ Dimension | Purpose |
| :--- | :--- | :--- |
| $N$-by-1 column vector | Scalar or 1-by- $M$ row vector | Apply one set of weights for the <br> same single frequency or all $M$ <br> frequencies. |
| $N$-by- $M$ matrix | Scalar | Apply all of the $M$ different <br> columns in Weights for the <br> same single frequency. |
|  |  | Apply each of the $M$ different <br> columns in Weights for the <br> corresponding frequency in <br> FREQ. |
|  |  |  |

## AzimuthAngles

Azimuth angles for plotting array response, specified as a row vector. The AzimuthAngles parameter sets the display range and resolution of azimuth angles for visualizing the radiation pattern. This parameter is allowed only when the RespCut parameter is set to 'Az' or '3D' and the Format parameter is set to 'Line' or 'Polar'. The values of azimuth angles should lie between $180^{\circ}$ and $180^{\circ}$ and must be in nondecreasing order. When you set the RespCut parameter to ' 3 D ', you can set the AzimuthAngles and ElevationAngles parameters simultaneously.

Default: [-180:180]

## ElevationAngles

Elevation angles for plotting array response, specified as a row vector. The ElevationAngles parameter sets the display range and resolution of elevation angles for visualizing the radiation pattern. This parameter is allowed only when the RespCut parameter is set to ' El ' or ' 3 D ' and the

Format parameter is set to 'Line' or 'Polar'. The values of elevation angles should lie between $90^{\circ}$ and $90^{\circ}$ and must be in nondecreasing order. When yous set the RespCut parameter to ' $3 \mathrm{D}^{\prime}$, you can set the ElevationAngles and AzimuthAngles parameters simultaneously.

Default: [-90:90]
UGrid
$U$ coordinate values for plotting array response, specified as a row vector. The UGrid parameter sets the display range and resolution of the $U$ coordinates for visualizing the radiation pattern in $U / V$ space. This parameter is allowed only when the Format parameter is set to 'UV' and the RespCut parameter is set to ' $U$ ' or ' $3 D^{\prime}$ '. The values of UGrid should be between -1 and 1 and should be specified in nondecreasing order. You can set the UGrid and VGrid parameters simultaneously.

Default: [-1:0.01:1]

## VGrid

$V$ coordinate values for plotting array response, specified as a row vector. The VGrid parameter sets the display range and resolution of the $V$ coordinates for visualizing the radiation pattern in $U / V$ space. This parameter is allowed only when the Format parameter is set to 'UV' and the RespCut parameter is set to ' $3 D^{\prime}$ '. The values of VGrid should be between -1 and 1 and should be specified in nondecreasing order. You can set VGrid and UGrid parameters simultaneously.

Default: [-1:0.01:1]

## Examples

## Plot Response and Directivity of 8-Element Uniform Circular Array

This example shows how to construct an 8-element uniform circular array (UCA) with two different antenna patterns.

```
element1 = phased.CosineAntennaElement('CosinePower',1.5);
element2 = phased.CosineAntennaElement('CosinePower',1.8);
N = 8;
azang = (0:N-1)*360/N-180;
array = phased.HeterogeneousConformalArray( ...
    'ElementPosition',0.4*[zeros(1,N); cosd(azang); sind(azang)], ...
    'ElementNormal',zeros(2,N),'ElementSet',{element1,element2}, ...
    'ElementIndices',[1 1 1 1 2 2 2 2]);
```

Plot the array elevation response when the operating frequency is 1 GHz and the wave propagation speed is the speed of light.

```
c = physconst('LightSpeed');
fc = le9;
pattern(array,fc,0.0,-90:90,'PropagationSpeed',c,'CoordinateSystem','polar', ...
    'Type','powerdb')
```



Normalized Power (dB), Broadside at $0.00^{\circ}$

Plot the directivity.
pattern(array,fc,0.0,-90:90,'PropagationSpeed', c,'CoordinateSystem','polar', ...
'Type','directivity')


Directivity (dBi), Broadside at $0.00^{\circ}$

## Plot Response of Disk Array

This example shows how to construct a 24 -element disk array using elements with two different antenna patterns and plot its response.

```
sElement1 = phased.CosineAntennaElement('CosinePower',1.5);
sElement2 = phased.CosineAntennaElement('CosinePower',1.8);
N = 8; azang = (0:N-1)*360/N-180;
p0 = [zeros(1,N);cosd(azang);sind(azang)];
posn = [0.6*p0, 0.4*p0, 0.2*p0];
sArray1 = phased.HeterogeneousConformalArray(...
    'ElementPosition',posn,...
    'ElementNormal', zeros(2,3*N),...
    'ElementSet',{sElement1,sElement2},...
    'ElementIndices',[1 1 1 l 1 1 1 1,...
    1111111 1,...
    2 2 2 2 2 2 2 2]);
```

Show the array.

```
viewArray(sArray1);
```



Plot the elevation response of this array using uniform weights on the elements and also a tapered set of weights set by the Weights parameter. Using the ElevationAngles parameter, restrict the plot of the response from -60 to 60 degrees in 0.1 degree increments. Assume the operating frequency is 1 GHz and the wave propagation speed is the speed of light.

```
c = physconst('LightSpeed');
fc = 1e9;
wts1 = ones(3*N,1);
wts1 = wts1/sum(abs(wts1));
wts2 = [0.5*ones(N,1); 0.7*ones(N,1); 1*ones(N,1)];
wts2 = wts2/sum(abs(wts2));
plotResponse(sArray1,fc,c,'RespCut','El',...
    'Format','Polar',...
    'ElevationAngles',[-60:0.1:60],...
    'Weights',...
    [wts1,wts2],...
    'Unit','db');
```



As expected, the tapered weights broaden the mainlobe and reduce the sidelobes.

See Also<br>uv2azel|azel2uv

## step

## System object: phased. HeterogeneousConformalArray <br> Package: phased

Output responses of array elements

## Syntax

RESP = step(H,FREQ,ANG)

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step (obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.

RESP = step ( $\mathrm{H}, \mathrm{FREQ}, \mathrm{ANG}$ ) returns the array elements' responses RESP at operating frequencies specified in FREQ and directions specified in ANG.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## H

Array object

## FREQ

Operating frequencies of array in hertz. FREQ is a row vector of length $L$. Typical values are within the range specified by a property of H . Element. That property is named FrequencyRange or FrequencyVector, depending on the type of element in the array. The element has zero response at frequencies outside that range.

## ANG

Directions in degrees. ANG is either a 2 -by- $M$ matrix or a row vector of length $M$.
If ANG is a 2-by-M matrix, each column of the matrix specifies the direction in the form [azimuth; elevation]. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive.

If ANG is a row vector of length $M$, each element specifies the azimuth angle of the direction. In this case, the corresponding elevation angle is assumed to be $0^{\circ}$.

## Output Arguments

## RESP

Voltage responses of the phased array. The output depends on whether the array supports polarization or not.

- If the array is not capable of supporting polarization, the voltage response, RESP, has the dimensions $N$-by- $M$-by- $L$. $N$ is the number of elements in the array. The dimension $M$ is the number of angles specified in ANG. $L$ is the number of frequencies specified in FREQ. For any element, the columns of RESP contain the responses of the array elements for the corresponding direction specified in ANG. Each of the $L$ pages of RESP contains the responses of the array elements for the corresponding frequency specified in FREQ.
- If the array is capable of supporting polarization, the voltage response, RESP, is a MATLAB struct containing two fields, RESP.H and RESP.V. The field, RESP.H, represents the array's horizontal polarization response, while RESP.V represents the array's vertical polarization response. Each field has the dimensions $N$-by-M-by-L. $N$ is the number of elements in the array, and $M$ is the number of angles specified in ANG. $L$ is the number of frequencies specified in FREQ. Each column of RESP contains the responses of the array elements for the corresponding direction specified in ANG. Each of the $L$ pages of RESP contains the responses of the array elements for the corresponding frequency specified in FREQ.


## Examples

## Compute Response of Circular Conformal Array

Construct an 8 -element uniform circular array using the phased. HeterogeneousConformalArray System object ${ }^{\mathrm{TM}}$. Assume the operating frequency is 1 GHz . Find the response of each element in this array in the direction of $30^{\circ}$ azimuth and $5^{\circ}$.

```
antenna1 = phased.CosineAntennaElement('CosinePower',1.5);
antenna2 = phased.CosineAntennaElement('CosinePower',1.8);
N = 8;
azang = (0:N-1)*360/N-180;
array = phased.HeterogeneousConformalArray(...
    'ElementPosition',...
    [cosd(azang);sind(azang);zeros(1,N)],...
    'ElementNormal', zeros(2,N),...
    'ElementSet',{antenna1,antenna2},...
    'ElementIndices',[1 1 1 1 2 2 2 2]);
fc = 1e9;
ang = [30;5];
resp = array(fc,ang)
resp = 8\times1
    0.8013
    0.8013
    0.8013
    0.8013
```

0.7666
0.7666
0.7666
0.7666

## See Also

uv2azel|phitheta2azel

## viewArray

System object: phased. HeterogeneousConformalArray
Package: phased
View array geometry

## Syntax

```
viewArray(H)
viewArray(H,Name,Value)
hPlot = viewArray(
```

$\qquad$

``` )
```


## Description

viewArray (H) plots the geometry of the array specified in H .
viewArray ( $\mathrm{H}, \mathrm{Name}$, Value) plots the geometry of the array, with additional options specified by one or more Name, Value pair arguments.
hPlot = viewArray( $\qquad$ ) returns the handle of the array elements in the figure window. All input arguments described for the previous syntaxes also apply here.

## Input Arguments

## H

Array object

## Name-Value Pair Arguments

Specify optional pairs of arguments as Namel=Value1, . . . ,NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Parent

Handle to the axes along which the array geometry is displayed.

## ShowNormals

Set this value to true to show the normal directions of all elements of the array. Set this value to false to plot the elements without showing normal directions.

Default: false

## ShowLocalCoordinates

Logical flag specifying whether to show the local coordinate axes.

Default: true

## ShowAnnotation

Logical flag specifying whether to show the annotations in the UI panel of the figure. Annotation shows aperture size and element spacing based on array axis of array.

Default: true

## Orientation

Orientation of the array, specified as a 3-by-1 column vector containing the rotation angles with respect to the $x-, y$-, and $z$-axes of the local coordinate system, respectively. The default value is [0;0;0].

Default: [0;0;0]

## ShowTaper

Set this value to true to specify whether to change the element color brightness in proportion to the element taper magnitude. When this value is set to false, all elements are drawn with the same color.

Default: false

## ShowIndex

Vector specifying the element indices to show in the figure. Each number in the vector must be an integer between 1 and the number of elements. You can also specify the value 'All' to show the indices of all elements of the array or 'None' to suppress indices.

Default: 'None'

## Title

Character vector specifying the title of the plot.
Default: 'Array Geometry'

## Output Arguments

## hPlot

Handle of array elements in figure window.

## Examples

## Element Positions and Normal Directions for Uniform Circular Array

Display the element positions and normal directions for all elements of an 8-element heterogeneous uniform circular array.

Create the elements and the array.

```
antennal = phased.CosineAntennaElement('CosinePower',1.5);
antenna2 = phased.CosineAntennaElement('CosinePower',1.8);
N = 8;
azang = (0:N-1)*360/N-180;
array = phased.HeterogeneousConformalArray(...
    'ElementPosition',...
    [cosd(azang);sind(azang);zeros(1,N)],...
    'ElementNormal', zeros(2,N),...
    'ElementSet',{antenna1,antenna2},...
    'ElementIndices',[1 1 1 1 2 2 2 2]);
viewArray(array,'ShowIndex','all','ShowNormal',true);
```


## Array Geometry



## See Also

phased.ArrayResponse

## Topics

Phased Array Gallery

Array Span:<br>$X$ axis $=2 \mathrm{~m}$<br>$Y$ axis $=2 \mathrm{~m}$<br>$Z$ axis $=0 \mathrm{~m}$

## phased.HeterogeneousULA

Package: phased
Heterogeneous uniform linear array

## Description

The phased. HeterogeneousULA object creates a uniform linear array from a heterogeneous set of antenna elements. A heterogeneous array is an array in which the antenna or microphone elements may be of different kinds or have different properties. An example would be an array of elements each having different antenna patterns.

To compute the response for each element in the array for specified directions:
1 Define and set up your uniform linear array. See "Construction" on page 1-551.
2 Call step to compute the response according to the properties of phased. HeterogeneousULA. The behavior of step is specific to each object in the toolbox.

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.

## Construction

H = phased. HeterogeneousULA creates a heterogeneous uniform linear array (ULA) System object, H. The object models a heterogeneous ULA formed with generally different sensor elements. The origin of the local coordinate system is the phase center of the array. The positive $x$-axis is the direction normal to the array, and the elements of the array are located along the $y$-axis.

H = phased. HeterogeneousULA(Name, Value) creates object, H, with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN).

## Properties

## ElementSet

Set of elements used in the array
Set of elements used in the sensor array, specified as a row MATLAB cell array. Elements specified in the ElementSet property must be either Phased Array System Toolbox antennas, microphones, or transducers System objects or Antenna Toolbox System object. In addition, all specified antenna elements must have the same polarization capability.

Default: One cell containing one isotropic antenna element

## ElementIndices

Elements location assignment

This property specifies the mapping of elements in the array. The property assigns elements to their locations in the array using indices into the ElementSet property. ElementIndices must be a 1-by$N$ row vector where $N$ is greater than $1 . N$ is the number of elements in the sensor array. The values in ElementIndices should be less than or equal to the number of entries in the ElementSet property.

Default: [1 1]

## ElementSpacing

Element spacing
A scalar containing the spacing (in meters) between two adjacent elements in the array.
Default: 0.5

## ArrayAxis

Array axis
Array axis, specified as one of ' $x$ ', ' $y$ ', or ' $z$ '. ULA array elements are located along the selected coordinate system axis.

Element normal vectors are determined by the selected array axis

| ArrayAxis Property Value | Element Normal Direction |
| :--- | :--- |
| $' x^{\prime}$ | azimuth $=90^{\circ}$, elevation $=0^{\circ}(y$-axis $)$ |
| $' y '$ | azimuth $=0^{\circ}$, elevation $=0^{\circ}(x$-axis $)$ |
| $' z{ }^{\prime}$ | azimuth $=0^{\circ}$, elevation $=0^{\circ}(x$-axis $)$ |

Default: ' y '
Taper
Element tapering
Element tapering or weighting, specified as a complex-valued scalar, 1-by- $N$ row vector, or $N$-by-1 column vector. The quantity $N$ is the number of elements in the array as determined by the size of the ElementIndices property. Tapers, also known as weights, are applied to each sensor element in the sensor array and modify both the amplitude and phase of the received data. If 'Taper' is a scalar, the same taper value is applied to all elements. If 'Taper' is a vector, each taper value is applied to the corresponding sensor element.

Default: 1

## Methods

| Specific to phased. HeterogeneousULA Object |  |
| :--- | :--- |
| beamwidth | Compute and display beamwidth of an array |
| collectPla <br> neWave | Simulate received plane waves |


| Specific to phased. HeterogeneousULA Object |  |
| :--- | :--- |
| directivit <br> y | Directivity of heterogeneous uniform linear array |
| getElement <br> Normal | Normal vector for array elements |
| getElement <br> Position | Positions of array elements |
| getNumElem <br> ents | Number of elements in array |
| getTaper | Array element tapers |
| isPolariza <br> tionCapabl <br> e | Polarization capability |
| pattern | Plot heterogeneous ULA pattern |
| patternAzi <br> muth | Plot heterogeneous ULA directivity or pattern versus azimuth |
| patternEle <br> vation | Plot heterogeneous ULA array directivity or pattern versus elevation |
| perturbati <br> ons | Perturbations defined on phased array |
| perturbedA <br> rray | Apply perturbations to phased array |
| perturbedP <br> attern | Compute and plot azimuth pattern of perturbed array |
| step | Output responses of array elements |
| viewArray | View array geometry |

## Common to All System Objects

| release | Allow System object property value changes |
| :--- | :--- | :--- |

## Examples

## Power Pattern of 10-Element Heterogeneous ULA Array

Create a 10 -element heterogeneous ULA consisting of cosine antenna elements with different power exponents. Two elements at each end have power values of 1.5 while the inside elements have power exponents of 1.8 . Find the power pattern in dB of each element at boresight.

Construct the heterogeneous array and show the element responses at 1 GHz .

```
sElement1 = phased.CosineAntennaElement('CosinePower',1.5);
sElement2 = phased.CosineAntennaElement('CosinePower',1.8);
sArray = phased.HeterogeneousULA(...
    'ElementSet',{sElement1,sElement2},...
    'ElementIndices',[1 1 2 2 2 2 2 2 1 1 ]);
fc = 1e9;
```

```
ang = [0;0];
resp = step(sArray,fc,ang)
resp =
    1
    1
    1
    1
    1
    1
    1
    1
    1
    1
```

Plot an azimuth cut of the array response at 1 GHz .
c = physconst('LightSpeed');
plotResponse(sArray,fc,c,'RespCut','Az','Format','Polar'); pattern(sArray,fc,[-180:180],0,...
'PropagationSpeed', c, ...
'CoordinateSystem','polar',...
'Type', 'powerdb');


Normalized Power (dB), Broadside at $0.00^{\circ}$

## Pattern of Array of Polarized Short-Dipole Antennas

Construct a heterogeneous uniform line array of 10 short-dipole sensor elements. Because short dipoles support polarization, the array should also. Verify that the array supports polarization by looking at the output of isPolarizationCapable. Then, draw the array, showing the tapering.

## Construct the array

Construct the array. Then, verify that it supports polarization by looking at the returned value of the isPolarizationCapable method.

```
sElement1 = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[100e6 1e9],...
    'AxisDirection','Z');
sElement2 = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[100e6 le9],...
    'AxisDirection','Y');
sArray = phased.HeterogeneousULA(...
    'ElementSet',{sElement1,sElement2},...
    'ElementIndices',[1 1 2 2 2 2 2 2 1 1 ],...
    'Taper',taylorwin(10)');
isPolarizationCapable(sArray)
ans = logical
    1
```


## View the array

```
viewArray(sArray,'ShowTaper',true,'ShowIndex',...
    'All','ShowTaper',true)
```


## Array Geometry



> Aperture Size:
> Y axis $=5 \mathrm{~m}$
> Element Spacing:
> $\Delta y=500 \mathrm{~mm}$
> Array Axis: Y axis

## Show the response

Show the element horizontal polarization responses at 10 degrees azimuth angle.

```
fc = 150e6;
ang = [10];
resp = step(sArray,fc,ang)
resp = struct with fields:
    H: [10xl double]
    V: [10x1 double]
resp.H
ans = 10\times1
            0
            0
        -1.2442
        -1.6279
        -1.8498
        -1.8498
        -1.6279
        -1.2442
            0
            0
```

Plot the combined polarization response
c = physconst('LightSpeed');
pattern(sArray,fc,[-180:180],0,...
'PropagationSpeed', c, ...
'CoordinateSystem','polar',...
'Type', 'powerdb ' , . . .
'Polarization',' combined');


Normalized Power (dB), Broadside at $0.00^{\circ}$

## Version History

Introduced in R2013a

## References

[1] Brookner, E., ed. Radar Technology. Lexington, MA: LexBook, 1996.
[2] Van Trees, H. Optimum Array Processing. New York: Wiley-Interscience, 2002.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:

- pattern, patternAzimuth, patternElevation, plotResponse, and viewArray methods are not supported.
- See "System Objects in MATLAB Code Generation" (MATLAB Coder).


## See Also

phased.ULA|phased.UCA|phased.URA|phased.ReplicatedSubarray| phased.PartitionedArray | phased.HeterogeneousURA|phased.HeterogeneousURA | phased.CosineAntennaElement | phased.CrossedDipoleAntennaElement |
phased.CustomAntennaElement | phased.IsotropicAntennaElement |
phased.ShortDipoleAntennaElement

## Topics

"Phased Array Gallery"

## directivity

System object: phased. HeterogeneousULA
Package: phased
Directivity of heterogeneous uniform linear array

## Syntax

D = directivity (H, FREQ,ANGLE)
D = directivity (H, FREQ, ANGLE,Name, Value)

## Description

$\mathrm{D}=$ directivity ( $\mathrm{H}, \mathrm{FREQ}, \mathrm{ANGLE}$ ) computes the "Directivity ( dBi )" on page 1-562 of a heterogeneous uniform linear array of antenna or microphone elements, H , at frequencies specified by the FREQ and in angles of direction specified by the ANGLE.

The integration used when computing array directivity has a minimum sampling grid of 0.1 degrees. If an array pattern has a beamwidth smaller than this, the directivity value will be inaccurate.

D = directivity (H, FREQ, ANGLE, Name, Value) computes the directivity with additional options specified by one or more Name, Value pair arguments.

## Input Arguments

## H - Heterogeneous uniform linear array

System object
Heterogeneous uniform linear array, specified as a phased. HeterogeneousULA System object.
Example: H = phased.HeterogeneousULA;

## FREQ - Frequency for computing directivity and patterns

positive scalar | 1-by-L real-valued row vector
Frequencies for computing directivity and patterns, specified as a positive scalar or 1-by-L realvalued row vector. Frequency units are in hertz.

- For an antenna, microphone, or sonar hydrophone or projector element, FREQ must lie within the range of values specified by the FrequencyRange or FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased. CustomAntennaElement and phased.CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: [1e8 2e6]
Data Types: double

## ANGLE - Angles for computing directivity

1-by- $M$ real-valued row vector | 2 -by- $M$ real-valued matrix
Angles for computing directivity, specified as a 1-by- $M$ real-valued row vector or a 2 -by- $M$ real-valued matrix, where $M$ is the number of angular directions. Angle units are in degrees. If ANGLE is a 2-by- $M$ matrix, then each column specifies a direction in azimuth and elevation, [az;el]. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

If ANGLE is a $1-b y-M$ vector, then each entry represents an azimuth angle, with the elevation angle assumed to be zero.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the xy plane. This angle is positive when measured from the $x$-axis toward the $y$-axis. The elevation angle is the angle between the direction vector and $x y$ plane. This angle is positive when measured towards the $z$-axis. See "Azimuth and Elevation Angles".
Example: [45 60; 0 10]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Namel=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## PropagationSpeed - Signal propagation speed

speed of light (default) | positive scalar
Signal propagation speed, specified as the comma-separated pair consisting of
' PropagationSpeed ' and a positive scalar in meters per second.
Example: 'PropagationSpeed', physconst('LightSpeed')
Data Types: double
Weights - Array weights
1 (default) | $N$-by-1 complex-valued column vector $\mid N$-by- $L$ complex-valued matrix
Array weights, specified as the comma-separated pair consisting of 'Weights' and an $N$-by-1 complex-valued column vector or $N$-by- $L$ complex-valued matrix. Array weights are applied to the elements of the array to produce array steering, tapering, or both. The dimension $N$ is the number of elements in the array. The dimension $L$ is the number of frequencies specified by FREQ.

| Weights Dimension | FREQ Dimension | Purpose |
| :--- | :--- | :--- |
| $N$-by-1 complex-valued column <br> vector | Scalar or 1-by- $L$ row vector | Applies a set of weights for the <br> single frequency or for all $L$ <br> frequencies. |
| $N$-by- $L$ complex-valued matrix | 1-by-L row vector | Applies each of the $L$ columns of <br> 'Weights' for the <br> Corresponding frequency in <br> FREQ. |

Note Use complex weights to steer the array response toward different directions. You can create weights using the phased.SteeringVector System object or you can compute your own weights. In general, you apply Hermitian conjugation before using weights in any Phased Array System Toolbox function or System object such as phased. Radiator or phased. Collector. However, for the directivity, pattern, patternAzimuth, and patternElevation methods of any array System object use the steering vector without conjugation.

Example: 'Weights', ones ( $\mathrm{N}, \mathrm{M}$ )
Data Types: double
Complex Number Support: Yes

## Output Arguments

## D - Directivity

M-by-L matrix
Directivity, returned as an $M$-by- $L$ matrix. Each row corresponds to one of the $M$ angles specified by ANGLE. Each column corresponds to one of the $L$ frequency values specified in FREQ. Directivity units are in dBi where dBi is defined as the gain of an element relative to an isotropic radiator.

## Examples

## Directivity of Heterogeneous Uniform Linear Array

Compute the directivity of a 10 -element heterogeneous ULA consisting of cosine antenna elements with different power factors. The two elements at each end have power values of 1.5 while the inner elements have power values of 1.8.

Construct the heterogeneous array. Set the signal frequency to 1 GHz .

```
c = physconst('LightSpeed');
freq = 1e9;
ang = [30;0];
lambda = c/freq;
```

Create the cosine antenna elements.

```
myElement1 = phased.CosineAntennaElement;
myElement1.CosinePower = 1.5;
myElement2 = phased.CosineAntennaElement;
myElement2.CosinePower = 1.8;
```

Create the Heterogeneous ULA.
myArray = phased. HeterogeneousULA;
myArray.ElementSet = \{myElement1, myElement2\};
myArray.ElementIndices $=\left[\begin{array}{llllllllll}1 & 1 & 2 & 2 & 2 & 2 & 1\end{array}\right] ;$
myArray.ElementSpacing $=0.5^{*}$ lambda;

Create the steering vector and compute the directivity in the same direction as the steering vector.

```
w = steervec(getElementPosition(myArray)/lambda,ang);
d = directivity(myArray,freq,ang,'PropagationSpeed',c,...
    'Weights',w)
d = 17.0102
```


## More About

## Directivity (dBi)

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \Pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## See Also

pattern | patternAzimuth | patternElevation

## collectPlaneWave

System object: phased. HeterogeneousULA
Package: phased
Simulate received plane waves

## Syntax

```
Y = collectPlaneWave(H,X,ANG)
Y = collectPlaneWave(H,X,ANG,FREQ)
Y = collectPlaneWave(H,X,ANG,FREQ,C)
```


## Description

$Y=\operatorname{collectPlaneWave}(H, X, A N G)$ returns the received signals at the sensor array, $H$, when the input signals indicated by $X$ arrive at the array from the directions specified in ANG.
$Y=$ collectPlaneWave ( $H, X$, ANG, $F R E Q$ ), in addition, specifies the incoming signal carrier frequency in FREQ.
$Y=\operatorname{collectPlaneWave}(H, X, A N G, F R E Q, C)$, in addition, specifies the signal propagation speed in C.

## Input Arguments

## H

Array object.
X
Incoming signals, specified as an M-column matrix. Each column of $X$ represents an individual incoming signal.

## ANG

Directions from which incoming signals arrive, in degrees. ANG can be either a 2-by-M matrix or a row vector of length M .

If ANG is a 2-by-M matrix, each column specifies the direction of arrival of the corresponding signal in X. Each column of ANG is in the form [azimuth; elevation]. The azimuth angle must be between $-180^{\circ}$ and $180^{\circ}$, inclusive. The elevation angle must be between $-90^{\circ}$ and $90^{\circ}$, inclusive.

If ANG is a row vector of length M , each entry in ANG specifies the azimuth angle. In this case, the corresponding elevation angle is assumed to be $0^{\circ}$.

FREQ
Carrier frequency of signal in hertz. FREQ must be a scalar.
Default: 3e8

## C

Propagation speed of signal in meters per second.
Default: Speed of light

## Output Arguments

## Y

Received signals. Y is an N-column matrix, where N is the number of elements in the array H. Each column of $Y$ is the received signal at the corresponding array element, with all incoming signals combined.

## Examples

## Simulate Received Signals at Heterogeneous ULA

Simulate two received signal at a heterogeneous 4 -element ULA. The signals arrive from $10^{\circ}$ and $30^{\circ}$ degrees azimuth. Both signals have an elevation angle of $0^{\circ}$. Assume the propagation speed is the speed of light and the carrier frequency of the signal is 100 MHz .

```
antennal = phased.ShortDipoleAntennaElement('FrequencyRange',[100e6 1e9], ...
    'AxisDirection','Z');
antenna2 = phased.ShortDipoleAntennaElement('FrequencyRange',[100e6 1e9], ...
    'AxisDirection','Y');
array = phased.HeterogeneousULA('ElementSet',{antennal,antenna2}, ...
    'ElementIndices',[1 2 2 1]);
Create a random plane wave signal.
```

```
y = collectPlaneWave(array,randn(4,2),[10 30],1e8,physconst('LightSpeed'));
```

```
y = collectPlaneWave(array,randn(4,2),[10 30],1e8,physconst('LightSpeed'));
```

Display the signal at the first element.

```
y(:,1)
ans = 4\times1 complex
    0.7430 - 0.3705i
    0.8418 + 0.4308i
    2.4817 + 0.9157i
    1.0724 - 0.4748i
```


## Algorithms

collectPlaneWave modulates the input signal with a phase corresponding to the delay caused by the direction of arrival. The method does not account for the response of individual elements in the array.

For further details, see [1].

## References

[1] Van Trees, H. Optimum Array Processing. New York: Wiley-Interscience, 2002.

## See Also

uv2azel|phitheta2azel

## getElementNormal

System object: phased. HeterogeneousULA
Package: phased
Normal vector to array elements

## Syntax

normvec = getElementNormal(sULA)
normvec $=$ getElementNormal(sULA, elemidx)

## Description

normvec $=$ getElementNormal(sULA) returns the normal vectors of the array elements of the phased. HeterogeneousULA System object, sULA. The output argument normvec is a 2-by- $N$ matrix, where $N$ is the number of elements in array, sULA. Each column of normvec defines the normal direction of an element in the local coordinate system in the form [az;el]. Units are degrees. The origin of the local coordinate system is defined by the phase center of the array.
normvec $=$ getElementNormal(sULA, elemidx) returns only the normal vectors of the elements specified in the element index vector, elemidx. This syntax can use any of the input arguments in the previous syntax.

## Input Arguments

## sULA - Uniform line array

phased.HeterogeneousULA System object
Uniform line array, specified as a phased. HeterogeneousULA System object.
Example: sULA $=$ phased. HeterogeneousULA
elemidx - Element indices
all array elements (default) | integer-valued 1-by-M row vector | integer-valued $M$-by-1 column vector
Element indices, specified as a 1 -by- $M$ or $M$-by-1 vector. Index values lie in the range 1 to $N$ where $N$ is the number of elements of the array. When elemidx is specified, getElementNormal returns the normal vectors of the elements contained in elemidx.

Example: [1,5,4]

## Output Arguments

## normvec - Element normal vectors

2 -by- $P$ real-valued vector
Element normal vectors, specified as a 2-by-P real-valued vector. Each column of normvec takes the form [az,el]. When elemidx is not specified, $P$ equals the array dimension. When elemidx is specified, $P$ equals the length of elemidx, $M$.

## Examples

## Heterogeneous ULA Element Normals

Construct three 5 -element heterogeneous ULA's with elements along the $x$-, $y$-, and $z$-axes. Obtain the element normals.

Create two types of cosine antennas.

```
sCosAnt1 = phased.CosineAntennaElement('CosinePower',[1.5,1.5]);
sCosAnt2 = phased.CosineAntennaElement('CosinePower',[1.8,1.8]);
```

First, choose the array axis to lie along the $x$-axis.

```
sULA1 = phased.HeterogeneousULA('ElementSet',{sCosAnt1,sCosAnt2},...
    'ElementIndices',[1 2 2 2 1],'ArrayAxis','x');
norm = getElementNormal(sULA1)
norm = 2×5
\begin{tabular}{rrrrr}
90 & 90 & 90 & 90 & 90 \\
0 & 0 & 0 & 0 & 0
\end{tabular}
```

The element normal vectors point along the $y$-axis.
Next, choose the array axis along the $y$-axis.

```
sULA2 = phased.HeterogeneousULA('ElementSet',{sCosAnt1,sCosAnt2},...
    'ElementIndices',[1 2 2 2 1],'ArrayAxis','y');
norm = getElementNormal(sULA2)
norm = 2×5
    0}00000000
    0}0
```

The element normal vectors point along the $x$-axis.
Finally, set the array axis along the $z$-axis. Obtain the normal vectors of the odd-numbered elements.

```
sULA3 = phased.HeterogeneousULA('ElementSet',{sCosAnt1,sCosAnt2},...
    'ElementIndices',[1 2 2 2 1],'ArrayAxis','z');
norm = getElementNormal(sULA3,[1,3,5])
norm = 2×3
    0 0 0
    0 0 0
```

The element normal vectors also point along the $x$-axis.

# Version History <br> Introduced in R2016a 

## getElementPosition

System object: phased. HeterogeneousULA
Package: phased
Positions of array elements

## Syntax

```
pos = getElementPosition(sHULA)
```

pos $=$ getElementPosition(sHULA, elemidx)

## Description

pos $=$ getElementPosition (sHULA) returns the element positions of the phased. HeterogeneousULA System object, sHULA. pos is a 3 -by- $N$ matrix, where $N$ is the number of elements in sHULA. Each column of pos defines the position of an element in the local coordinate system, in meters, using the form [ $x ; y ; z$ ]. The origin of the local coordinate system is the phase center of the array. The positions of the array elements depend upon the value of the ArrayAxis property.
pos = getElementPosition(sHULA, elemidx) returns only the positions of the elements that are specified in the element index vector elemidx. This syntax can use any of the input arguments in the previous syntax.

## Examples

## Position of Heterogeneous ULA Elements

Construct a 4-element heterogeneous ULA of different types of short-dipole antenna elements. Then, obtain the element positions.

```
sElement1 = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[100e6 1e9],...
    'AxisDirection','Z');
sElement2 = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[100e6 1e9],...
    'AxisDirection','Y');
sArray = phased.HeterogeneousULA(...
    'ElementSet',{sElement1,sElement2},...
    'ElementIndices',[1 2 2 1]);
pos = getElementPosition(sArray)
pos = 3\times4
\begin{tabular}{rrrr}
0 & 0 & 0 & 0 \\
-0.7500 & -0.2500 & 0.2500 & 0.7500 \\
0 & 0 & 0 & 0
\end{tabular}
```


## getNumElements

System object: phased. HeterogeneousULA
Package: phased
Number of elements in array

## Syntax

N = getNumElements(array)

## Description

$\mathrm{N}=$ getNumElements(array) returns the number of elements, $N$, in the heterogeneous ULA object array.

## Examples

## Number of Elements of Heterogeneous ULA

Construct a 4 -element heterogeneous ULA. Then verify the number of elements in the array.

```
antenna1 = phased.ShortDipoleAntennaElement('FrequencyRange',[100e6 1e9], ...
    'AxisDirection','Z');
antenna2 = phased.ShortDipoleAntennaElement('FrequencyRange',[100e6 1e9], ...
    'AxisDirection','Y');
array = phased.HeterogeneousULA('ElementSet',{antennal,antenna2}, ...
    'ElementIndices',[1 2 2 1]);
N = getNumElements(array)
N = 4
```


## getTaper

System object: phased. HeterogeneousULA
Package: phased
Array element tapers

## Syntax

wts = getTaper(array)

## Description

wts = getTaper(array) returns the tapers, wts, applied to each element of the phased heterogeneous uniform line array (ULA), h. Tapers are often referred to as weights.

## Input Arguments

## array - Heterogeneous uniform line array

phased. HeterogeneousULA System object
Heterogeneous uniform line array, specified as a phased. HeterogeneousULA System object.

## Output Arguments

## wts - Array element tapers

$N$-by-1 complex-valued vector
Array element tapers returned as an $N$-by- 1 complex-valued vector, where $N$ is the number of elements in the array.

## Examples

## Heterogeneous ULA with Taylor Window Taper

Construct a 5 -element heterogeneous ULA with a Taylor window taper. The array consists of shortdipole antenna elements with different orientations.Then, obtain the element taper values.

```
antennal = phased.ShortDipoleAntennaElement('FrequencyRange',[100e6 1e9], ...
    'AxisDirection','Z');
antenna2 = phased.ShortDipoleAntennaElement('FrequencyRange',[100e6 1e9], ...
    'AxisDirection','Y');
array = phased.HeterogeneousULA('ElementSet',{antennal,antenna2}, ...
    'ElementIndices',[1 2 2 2 1],'Taper',taylorwin(5)');
w = getTaper(array)
w = 5 < 1
    0.5181
    1.2029
```

1.5581
1.2029
0.5181

## isPolarizationCapable

System object: phased. HeterogeneousULA
Package: phased
Polarization capability

## Syntax

flag = isPolarizationCapable(array)

## Description

flag = isPolarizationCapable(array) returns a Boolean value, flag, indicating whether the array supports polarization. An array supports polarization if all of its constituent sensor elements support polarization.

## Input Arguments

array - Heterogeneous uniform line array
phased. HeterogeneousULA System object
Heterogeneous uniform line array, specified as a phased. HeterogeneousULA System object.

## Output Arguments

## flag - Polarization-capability flag

Polarization-capability flag, returned as a Boolean value 1 if the array supports polarization or 0 if it does not.

## Examples

## Heterogeneous ULA of Short-Dipole Antenna Elements Supports Polarization

Show that a heterogeneous array of short-dipole antenna elements supports polarization.

```
antennal = phased.ShortDipoleAntennaElement('FrequencyRange',[100e6 1e9], ...
    'AxisDirection','Z');
antenna2 = phased.ShortDipoleAntennaElement('FrequencyRange',[100e6 1e9], ...
    'AxisDirection','Y');
array = phased.HeterogeneousULA('ElementSet',{antennal,antenna2}, ...
    'ElementIndices',[1 2 2 2 1]);
isPolarizationCapable(array)
ans = logical
    1
```


## pattern

System object: phased. HeterogeneousULA
Package: phased
Plot heterogeneous ULA pattern

## Syntax

```
pattern(sArray,FREQ)
pattern(sArray,FREQ,AZ)
pattern(sArray,FREQ,AZ,EL)
pattern( __ ,Name,Value)
[PAT,AZ_ANG,EL_ANG] = pattern(
```

$\qquad$

``` )
```


## Description

pattern (sArray, FREQ) plots the 3-D array directivity pattern (in dBi) for the array specified in sArray. The operating frequency is specified in FREQ.

The integration used when computing array directivity has a minimum sampling grid of 0.1 degrees. If an array pattern has a beamwidth smaller than this, the directivity value will be inaccurate.
pattern(sArray, FREQ, AZ) plots the array directivity pattern at the specified azimuth angle.
pattern(sArray, FREQ, AZ, EL) plots the array directivity pattern at specified azimuth and elevation angles.
pattern( $\qquad$ ,Name, Value) plots the array pattern with additional options specified by one or more Name, Value pair arguments.
[PAT,AZ_ANG,EL_ANG] = pattern( __ ) returns the array pattern in PAT. The AZ_ANG output contains the coordinate values corresponding to the rows of PAT. The EL_ANG output contains the coordinate values corresponding to the columns of PAT. If the 'CoordinateSystem' parameter is set to ' $u v$ ' , then AZ_ANG contains the $U$ coordinates of the pattern and EL_ANG contains the $V$ coordinates of the pattern. Otherwise, they are in angular units in degrees. $U V$ units are dimensionless.

Note This method replaces the plotResponse method. See "Convert plotResponse to pattern" on page 1-581 for guidelines on how to use pattern in place of plotResponse.

## Input Arguments

## sArray - Heterogeneous ULA

System object
Heterogeneous conformal array, specified as a phased. HeterogeneousULA System object.
Example: sArray= phased. HeterogeneousULA;

## FREQ - Frequency for computing directivity and patterns

positive scalar | 1-by-L real-valued row vector
Frequencies for computing directivity and patterns, specified as a positive scalar or 1-by-L realvalued row vector. Frequency units are in hertz.

- For an antenna, microphone, or sonar hydrophone or projector element, FREQ must lie within the range of values specified by the FrequencyRange or FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased. CustomAntennaElement and phased.CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

```
Example: [1e8 2e6]
```

Data Types: double

## AZ - Azimuth angles

[-180:180] (default) | 1-by- $N$ real-valued row vector
Azimuth angles for computing directivity and pattern, specified as a 1-by- $N$ real-valued row vector where $N$ is the number of azimuth angles. Angle units are in degrees. Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the $x y$ plane. When measured from the $x$-axis toward the $y$-axis, this angle is positive.

## Example: [-45:2:45]

Data Types: double

## EL - Elevation angles

[-90:90] (default) | 1-by-M real-valued row vector
Elevation angles for computing directivity and pattern, specified as a 1-by-M real-valued row vector where $M$ is the number of desired elevation directions. Angle units are in degrees. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

The elevation angle is the angle between the direction vector and $x y$-plane. The elevation angle is positive when measured towards the $z$-axis.

Example: [-75:1:70]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

```
CoordinateSystem - Plotting coordinate system
'polar' (default)|'rectangular'|'uv'
```

Plotting coordinate system of the pattern, specified as the comma-separated pair consisting of 'CoordinateSystem' and one of 'polar', 'rectangular', or 'uv'. When
'CoordinateSystem' is set to 'polar' or 'rectangular', the AZ and EL arguments specify the pattern azimuth and elevation, respectively. AZ values must lie between $-180^{\circ}$ and $180^{\circ}$. EL values must lie between $-90^{\circ}$ and $90^{\circ}$. If 'CoordinateSystem' is set to ' uv ', AZ and EL then specify $U$ and $V$ coordinates, respectively. AZ and EL must lie between -1 and 1 .
Example: 'uv'
Data Types: char

## Type - Displayed pattern type

'directivity' (default)|'efield'|'power'|'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb' - power pattern converted to dB.

Example: 'powerdb'
Data Types: char

## Orientation - Array orientation

[0;0;0]. (default) | 3-by-1 real-valued column vector
Array orientation, specified as a 3-by-1 real-valued column vector containing the rotation angles with respect to the $x$-, $y$-, and $z$-axes of the local coordinate system, respectively.

## Normalize - Display normalize pattern

true (default) | false
Display normalized pattern, specified as the comma-separated pair consisting of 'Normalize' and a Boolean. Set this parameter to true to display a normalized pattern. This parameter does not apply when you set 'Type' to 'directivity'. Directivity patterns are already normalized.
Data Types: logical

## ShowArray - View array geometry

false (default) | true
View the array geometry along with the 3D radiation pattern, specified as false or true.
Data Types: logical
ShowLocalCoordinates - Show local coordinate axes
true (default) | false
Show the local coordinate axes, specified as true or false.
Data Types: logical

## ShowColorbar - Show colorbar

true (default) | false

Show the colorbar, specified as true or false.

## Data Types: logical

## Parent - Handle to axis

scalar
Handle to the axes along which the array geometry is displayed specified as a scalar.

## PlotStyle - Plotting style

'overlay' (default)|'waterfall'
Plotting style, specified as the comma-separated pair consisting of 'Plotstyle' and either 'overlay' or 'waterfall'. This parameter applies when you specify multiple frequencies in FREQ in 2-D plots. You can draw 2-D plots by setting one of the arguments AZ or EL to a scalar.

## Data Types: char

## Polarization - Polarized field component

'combined' (default) | 'H' | 'V'
Polarized field component to display, specified as the comma-separated pair consisting of 'Polarization' and 'combined', 'H', or 'V'. This parameter applies only when the sensors are polarization-capable and when the 'Type' parameter is not set to 'directivity'. This table shows the meaning of the display options.

| 'Polarization ' | Display |
| :--- | :--- |
| ' combined ' | Combined $H$ and $V$ polarization components |
| 'H' | $H$ polarization component |
| 'V' | $V$ polarization component |

Example: 'V '

## Data Types: char

## PropagationSpeed - Signal propagation speed

speed of light (default) | positive scalar
Signal propagation speed, specified as the comma-separated pair consisting of
' PropagationSpeed ' and a positive scalar in meters per second.
Example: 'PropagationSpeed', physconst('LightSpeed')
Data Types: double

## Weights - Array weights

1 (default) | $N$-by-1 complex-valued column vector | $N$-by-L complex-valued matrix
Array weights, specified as the comma-separated pair consisting of 'Weights' and an N -by-1 complex-valued column vector or $N$-by- $L$ complex-valued matrix. Array weights are applied to the elements of the array to produce array steering, tapering, or both. The dimension $N$ is the number of elements in the array. The dimension $L$ is the number of frequencies specified by FREQ.

| Weights Dimension | FREQ Dimension | Purpose |
| :--- | :--- | :--- |
| $N$-by-1 complex-valued column <br> vector | Scalar or 1-by- $L$ row vector | Applies a set of weights for the <br> single frequency or for all $L$ <br> frequencies. |
| $N$-by- $L$ complex-valued matrix | 1-by- $L$ row vector | Applies each of the $L$ columns of <br> 'Weights ' for the <br> corresponding frequency in <br> FREQ. |

Note Use complex weights to steer the array response toward different directions. You can create weights using the phased. SteeringVector System object or you can compute your own weights. In general, you apply Hermitian conjugation before using weights in any Phased Array System Toolbox function or System object such as phased. Radiator or phased. Collector. However, for the directivity, pattern, patternAzimuth, and patternElevation methods of any array System object use the steering vector without conjugation.

Example: 'Weights', ones ( $\mathrm{N}, \mathrm{M}$ )
Data Types: double
Complex Number Support: Yes

## Output Arguments

## PAT - Array pattern

$M$-by- $N$ real-valued matrix
Array pattern, returned as an $M$-by- $N$ real-valued matrix. The dimensions of PAT correspond to the dimensions of the output arguments AZ_ANG and EL_ANG.

## AZ_ANG - Azimuth angles

scalar | 1-by- $N$ real-valued row vector
Azimuth angles for displaying directivity or response pattern, returned as a scalar or 1-by- $N$ realvalued row vector corresponding to the dimension set in AZ. The columns of PAT correspond to the values in AZ_ANG. Units are in degrees.

## EL_ANG - Elevation angles

scalar | 1-by-M real-valued row vector
Elevation angles for displaying directivity or response, returned as a scalar or 1-by-M real-valued row vector corresponding to the dimension set in EL. The rows of PAT correspond to the values in EL_ANG. Units are in degrees.

## Examples

## Azimuth Power Pattern For Two Frequencies

Create a 5-element heterogeneous ULA from short-dipole antenna elements with different axis directions. Draw the azimuth power pattern for the horizontal polarization component at 0 degrees elevation for two frequencies, 300 MHz and 400 MHz .

## Construct Heterogeneous ULA

Construct the array from z-directed and y-directed short dipole antenna elements.

```
sElement1 = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[2e8 5e8],...
    'AxisDirection','Z');
sElement2 = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[2e8 5e8],...
    'AxisDirection','Y');
sArray = phased.HeterogeneousULA(...
    'ElementSet',{sElement1,sElement2},...
    'ElementIndices',[1 2 2 2 1]);
```


## Plot the patterns

```
fc = [300e6 400e6];
c = physconst('LightSpeed');
pattern(sArray,fc,[-180:180],0,...
    'PropagationSpeed',c,...
    'CoordinateSystem','polar',...
    'Type','powerdb',...
    'PlotStyle','overlay',...
    'Polarization','H')
```



Normalized Power (dB), Broadside at $0.00^{\circ}$

## Directivity Pattern in UV Space

Create an 11 -element heterogeneous ULA from short-dipole antenna elements with different axis directions. Draw the 3-D power pattern for the horizontal polarization component at 300 MHz .

## Construct Heterogeneous ULA

Construct the array from z -directed and y -directed short dipole antenna elements.

```
sElement1 = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[2e8 5e8],...
    'AxisDirection','Z');
sElement2 = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[2e8 5e8],...
    'AxisDirection','Y');
sArray = phased.HeterogeneousULA(...
    'ElementSet',{sElement1,sElement2},...
    'ElementIndices',[1 1 1 2 2 2 2 2 1 1 1]);
```

Plot the patterns

```
fc = 300e6;
c = physconst('LightSpeed');
pattern(sArray,fc,-1:.01:1,-1:.01:1,...
    'PropagationSpeed',c,...
    'CoordinateSystem','uv',...
    'Type','powerdb',...
    'Polarization','H')
```



## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \Pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Convert plotResponse to pattern

For antenna, microphone, and array System objects, the pattern method replaces the plotResponse method. In addition, two new simplified methods exist just to draw 2-D azimuth and elevation pattern plots. These methods are azimuthPattern and elevationPattern.

The following table is a guide for converting your code from using plotResponse to pattern. Notice that some of the inputs have changed from input arguments to Name-Value pairs and conversely. The general pattern method syntax is
pattern(H,FREQ,AZ,EL,'Name1','Value1',...,'NameN','ValueN')

| plotResponse Inputs | plotResponse Description | pattern Inputs |
| :--- | :--- | :--- |
| H argument | Antenna, microphone, or array <br> System object. | H argument (no change) |
| FREQ argument | Operating frequency. | FREQ argument (no change) |
| V argument | Propagation speed. This argument <br> is used only for arrays. | 'PropagationSpeed ' name-value <br> pair. This parameter is only used for <br> arrays. |


| plotResponse Inputs | plotResponse Description |  | pattern Inputs |  |
| :---: | :---: | :---: | :---: | :---: |
| 'Format' and 'RespCut' namevalue pairs | These options work together to let you create a plot in angle space (line or polar style) or $U V$ space. They also determine whether the plot is 2-D or 3-D. This table shows you how to create different types of plots using plotResponse. |  | 'CoordinateSystem' name-value pair used together with the AZ and EL input arguments. <br> 'CoordinateSystem' has the same options as the plotResponse method 'Format ' name-value pair, except that ' line' is now named 'rectangular'. The table shows how to create different types of plots using pattern. |  |
|  | Display space <br> Angle space (2D) |  |  |  |
|  | Angle space (2D) | Set 'RespCut' <br> to 'Az' or |  |  |
|  |  | 'El'. Set <br> 'Format ' to <br> 'line' or 'polar'. | Display space |  |
|  |  | ' line' or 'polar'. <br> Set the display axis using either the 'AzimuthAngle | Angle space (2D) | Set <br> Coordinate <br> System' to <br> rectangular' <br> or 'polar' <br> Specify either AZ <br> or EL as a scalar. |
|  |  | s' or 'ElevationAng les' namevalue pairs. | Angle space (3D) | Set <br> 'Coordinate <br> System' to 'rectangular' |
|  | Angle space (3D) | Set 'RespCut' to '3D'. Set |  | or 'polar'. <br> Specify both AZ <br> and EL as <br> vectors. |
|  |  | 'polar'. <br> Set the display axis using both the 'AzimuthAngle s' and 'Elevation | $U V$ space (2D) | Set <br> Coordinate System' to uv'. Use AZ to specify a $U$ space vector. Use EL to specify a $V$-space scalar. |
|  |  | Angles' namevalue pairs. | UV space (3D) |  |
|  | UV space (2D) | Set 'RespCut' to'U'. Set 'Format ' to 'UV'. Set the display range using the 'UGrid' namevalue pair. |  | 'Coordinate <br> System' to <br> 'uv'. Use AZ to <br> specify a $U$ - <br> space vector. <br> Use EL to specify <br> a $V$-space vector. |
|  |  |  | If you set CoordinateSystem to 'uv ' , enter the UV grid values using $A Z$ and $E L$. |  |
|  | UV space (3D) | $\begin{aligned} & \text { Set 'RespCut' } \\ & \text { to'3D'. Set } \\ & \text { 'Format' to } \end{aligned}$ |  |  |


| plotResponse Inputs | plotResponse Description |  | pattern Inputs |
| :---: | :---: | :---: | :---: |
|  | Display space | 'UV '. Set the display range using both the 'UGrid' and 'VGrid ' namevalue pairs. |  |
| 'CutAngle' name-value pair | Constant angle at to take an azimuth or elevation cut. When producing a 2-D plot and when 'RespCut' is set to 'Az' or 'El', use 'CutAngle' to set the slice across which to view the plot. |  | No equivalent name-value pair. To create a cut, specify either AZ or EL as a scalar, not a vector. |
| 'NormalizeResponse' namevalue pair | Normalizes the plot. When 'Unit' is set to 'dbi' , you cannot specify 'NormalizeResponse'. |  | Use the 'Normalize' name-value pair. When 'Type' is set to 'directivity' you cannot specify 'Normalize'. |
| 'OverlayFreq' name-value pair | Plot multiple frequencies on the same 2-D plot. Available only when 'Format' is set to 'line' or 'uv and 'RespCut' is not set to '3D'. The value true produces an overlay plot and the value false produces a waterfall plot. |  | 'PlotStyle' name-value pair plots multiple frequencies on the same 2-D plot. <br> The values 'overlay' and 'waterfall' correspond to 'OverlayFreq' values of true and false. The option 'waterfall' is allowed only when 'CoordinateSystem' is set to 'rectangular' or 'uv'. |
| 'Polarization' name-value pair | Determines how to plot polarized fields. Options are 'None', 'Combined', 'H', or 'V'. |  | 'Polarization ' name-value pair determines how to plot polarized fields. The 'None ' option is removed. The options 'Combined ' , ' H ', or 'V' are unchanged. |
| ' Unit ' name-value pair | Determines the plot units. Choose 'db','mag', 'pow', or 'dbi', where the default is ' db ' |  | 'Type ' name-value pair, uses equivalent options with different names |
|  |  |  | plotResponse pattern |
|  |  |  | 'db' 'powerdb' <br> 'mag' 'efield' <br> 'pow' 'power' <br> 'dbi' 'directivity' |
| 'Weights ' name-value pair | Array element tapers (or weights). |  | 'Weights ' name-value pair (no change). |
| 'AzimuthAngles ' name-value pair | Azimuth angles used to display the antenna or array response. |  | AZ argument |


| plotResponse Inputs | plotResponse Description | pattern Inputs |
| :--- | :--- | :--- |
| 'ElevationAngles ' name-value <br> pair | Elevation angles used to display the <br> antenna or array response. | EL argument |
| ' UGrid' name-value pair | Contains $U$ coordinates in $U V$ - <br> space. | AZ argument when <br> 'CoordinateSystem ' name-value <br> pair is set to 'uv' |
| 'VGrid' name-value pair | Contains V-coordinates in $U V$-space. | EL argument when <br> 'CoordinateSystem ' name-value <br> pair is set to 'uv' |

## Version History <br> Introduced in R2015a

See Also<br>patternAzimuth|patternElevation

## patternAzimuth

System object: phased. HeterogeneousULA
Package: phased
Plot heterogeneous ULA directivity or pattern versus azimuth

## Syntax

```
patternAzimuth(sArray,FREQ)
patternAzimuth(sArray,FREQ,EL)
patternAzimuth(sArray,FREQ,EL,Name,Value)
PAT = patternAzimuth(
```

$\qquad$

``` )
```


## Description

patternAzimuth (sArray, FREQ) plots the 2-D array directivity pattern versus azimuth (in dBi) for the array sArray at zero degrees elevation angle. The argument FREQ specifies the operating frequency.

The integration used when computing array directivity has a minimum sampling grid of 0.1 degrees. If an array pattern has a beamwidth smaller than this, the directivity value will be inaccurate.
patternAzimuth(sArray, FREQ,EL), in addition, plots the 2-D array directivity pattern versus azimuth (in dBi) for the array sArray at the elevation angle specified by EL. When EL is a vector, multiple overlaid plots are created.
patternAzimuth(sArray, FREQ,EL,Name, Value) plots the array pattern with additional options specified by one or more Name, Value pair arguments.

PAT = patternAzimuth ( _ _ ) returns the array pattern. PAT is a matrix whose entries represent the pattern at corresponding sampling points specified by the 'Azimuth ' parameter and the EL input argument.

## Input Arguments

## sArray - Heterogeneous ULA

System object
Heterogeneous ULA, specified as a phased. HeterogeneousULA System object.
Example: sArray= phased.HeterogeneousULA;

## FREQ - Frequency for computing directivity and pattern

positive scalar
Frequency for computing directivity and pattern, specified as a positive scalar. Frequency units are in hertz.

- For an antenna or microphone element, FREQ must lie within the range of values specified by the FrequencyRange or the FrequencyVector property of the element. Otherwise, the element
produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased.CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: 1e8
Data Types: double

## EL - Elevation angles

## 1-by- $N$ real-valued row vector

Elevation angles for computing sensor or array directivities and patterns, specified as a 1-by- $N$ realvalued row vector. The quantity $N$ is the number of requested elevation directions. Angle units are in degrees. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

The elevation angle is the angle between the direction vector and the xy plane. When measured toward the $z$-axis, this angle is positive.
Example: [0, 10, 20]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Type - Displayed pattern type

'directivity' (default)|'efield'|'power'|'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb' - power pattern converted to dB.

Example: 'powerdb'
Data Types: char

## PropagationSpeed - Signal propagation speed

## speed of light (default) | positive scalar

Signal propagation speed, specified as the comma-separated pair consisting of ' PropagationSpeed ' and a positive scalar in meters per second.
Example: 'PropagationSpeed', physconst('LightSpeed')
Data Types: double

## Weights - Array weights

M-by-1 complex-valued column vector
Array weights, specified as the comma-separated pair consisting of 'Weights' and an M-by-1 complex-valued column vector. Array weights are applied to the elements of the array to produce array steering, tapering, or both. The dimension $M$ is the number of elements in the array.

Note Use complex weights to steer the array response toward different directions. You can create weights using the phased. SteeringVector System object or you can compute your own weights. In general, you apply Hermitian conjugation before using weights in any Phased Array System Toolbox function or System object such as phased. Radiator or phased. Collector. However, for the directivity, pattern, patternAzimuth, and patternElevation methods of any array System object use the steering vector without conjugation.

Example: 'Weights', ones (10, 1)
Data Types: double
Complex Number Support: Yes

## Azimuth - Azimuth angles

[-180:180] (default) | 1-by-P real-valued row vector
Azimuth angles, specified as the comma-separated pair consisting of 'Azimuth' and a 1-by-P realvalued row vector. Azimuth angles define where the array pattern is calculated.

Example: 'Azimuth', [-90:2:90]
Data Types: double

## Parent - Handle to axis

scalar
Handle to the axes along which the array geometry is displayed specified as a scalar.

## Output Arguments

## PAT - Array directivity or pattern

L-by- $N$ real-valued matrix
Array directivity or pattern, returned as an $L$-by- $N$ real-valued matrix. The dimension $L$ is the number of azimuth values determined by the 'Azimuth' name-value pair argument. The dimension $N$ is the number of elevation angles, as determined by the EL input argument.

## Examples

## Azimuth Directivity Pattern For Steered Array

Create an 11-element heterogeneous ULA from short-dipole antenna elements with different axis directions. The element spacing is 0.4 meters. Draw the azimuthal directivity pattern for 0 degrees elevation at an operating frequency of 300 MHz . Then, steer the array and draw the azimuthal directivity pattern.

## Construct Heterogeneous ULA

Construct the array from z-directed and y-directed short dipole antenna elements.

```
sElement1 = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[200e6 500e6],...
    'AxisDirection','Z');
sElement2 = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[200e6 500e6],...
    'AxisDirection','Y');
sArray = phased.HeterogeneousULA(...
    'ElementSpacing',0.4,...
    'ElementSet',{sElement1,sElement2},...
    'ElementIndices',[1 1 1 2 2 2 2 2 1 1 1]);
```


## Plot Directivity Pattern

$\mathrm{fc}=300 \mathrm{e} 6$;
c = physconst('LightSpeed');
lam = c/fc;
patternAzimuth(sArray,fc,0,...
'PropagationSpeed', c, ...
'Type','directivity')


Directivity (dBi), Broadside at $0.00^{\circ}$

## Steer Array and Plot Directivity Pattern

Steer the array to 30 degrees in azimuth by applying weights to achieve a linear phase shift.

```
theta = 30;
d = [0:10]*0.4;
ph = 2*pi*d'/lam*sind(theta);
wts = exp(1i*ph);
patternAzimuth(sArray,fc,0,...
    'PropagationSpeed',c,...
    'Type','directivity',....
    'Weights',wts)
```



Directivity (dBi), Broadside at $0.00^{\circ}$

## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\text {rad }}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that
the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as dBi . For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Version History

Introduced in R2015a

## See Also

pattern| patternElevation

## patternElevation

System object: phased. HeterogeneousULA
Package: phased
Plot heterogeneous ULA directivity or pattern versus elevation

## Syntax

```
patternElevation(sArray,FREQ)
patternElevation(sArray,FREQ,AZ)
patternElevation(sArray,FREQ,AZ,Name,Value)
PAT = patternElevation(
```

$\qquad$

``` )
```


## Description

patternElevation(sArray, FREQ) plots the 2-D array directivity pattern versus elevation (in dBi ) for the array sArray at zero degrees azimuth angle. When AZ is a vector, multiple overlaid plots are created. The argument FREQ specifies the operating frequency.

The integration used when computing array directivity has a minimum sampling grid of 0.1 degrees. If an array pattern has a beamwidth smaller than this, the directivity value will be inaccurate.
patternElevation(sArray, FREQ, AZ), in addition, plots the 2-D element directivity pattern versus elevation (in dBi ) at the azimuth angle specified by $A Z$. When $A Z$ is a vector, multiple overlaid plots are created.
patternElevation(sArray,FREQ,AZ,Name, Value) plots the array pattern with additional options specified by one or more Name, Value pair arguments.

PAT = patternElevation ( _ ) returns the array pattern. PAT is a matrix whose entries represent the pattern at corresponding sampling points specified by the 'Elevation' parameter and the AZ input argument.

## Input Arguments

## sArray - Heterogeneous ULA

System object
Heterogeneous ULA array, specified as a phased. HeterogeneousULA System object.
Example: sArray= phased.HeterogeneousULA;
FREQ - Frequency for computing directivity and pattern
positive scalar
Frequency for computing directivity and pattern, specified as a positive scalar. Frequency units are in hertz.

- For an antenna or microphone element, FREQ must lie within the range of values specified by the FrequencyRange or the FrequencyVector property of the element. Otherwise, the element
produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased.CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: 1e8
Data Types: double

## AZ - Azimuth angles for computing directivity and pattern

1-by- $N$ real-valued row vector
Azimuth angles for computing sensor or array directivities and patterns, specified as a 1 -by- $N$ realvalued row vector where $N$ is the number of desired azimuth directions. Angle units are in degrees. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the $x y$ plane. This angle is positive when measured from the $x$-axis toward the $y$-axis.
Example: [0,10,20]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Type - Displayed pattern type

'directivity' (default)|'efield'|'power'|'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb' - power pattern converted to dB.

Example: 'powerdb'
Data Types: char

## PropagationSpeed - Signal propagation speed

speed of light (default) | positive scalar
Signal propagation speed, specified as the comma-separated pair consisting of ' PropagationSpeed ' and a positive scalar in meters per second.
Example: 'PropagationSpeed', physconst('LightSpeed')
Data Types: double

## Weights - Array weights

M-by-1 complex-valued column vector
Array weights, specified as the comma-separated pair consisting of 'Weights' and an $M$-by-1 complex-valued column vector. Array weights are applied to the elements of the array to produce array steering, tapering, or both. The dimension $M$ is the number of elements in the array.

Note Use complex weights to steer the array response toward different directions. You can create weights using the phased. SteeringVector System object or you can compute your own weights. In general, you apply Hermitian conjugation before using weights in any Phased Array System Toolbox function or System object such as phased.Radiator or phased. Collector. However, for the directivity, pattern, patternAzimuth, and patternElevation methods of any array System object use the steering vector without conjugation.

## Example: 'Weights', ones (10,1)

Data Types: double
Complex Number Support: Yes

## Elevation - Elevation angles

[-90:90] (default) | 1-by-P real-valued row vector
Elevation angles, specified as the comma-separated pair consisting of 'Elevation' and a 1-by-P real-valued row vector. Elevation angles define where the array pattern is calculated.
Example: 'Elevation', [-90:2:90]
Data Types: double

## Parent - Handle to axis

scalar
Handle to the axes along which the array geometry is displayed specified as a scalar.

## Output Arguments

## PAT - Array directivity or pattern

L-by- $N$ real-valued matrix

Array directivity or pattern, returned as an $L$-by- $N$ real-valued matrix. The dimension $L$ is the number of elevation angles determined by the 'Elevation' name-value pair argument. The dimension $N$ is the number of azimuth angles determined by the $A Z$ argument.

## Examples

## Elevation Power Pattern for Two Azimuth Directions

Create an 11 -element heterogeneous ULA from short-dipole antenna elements with different axis directions. The element spacing is 0.4 meters. Draw the elevation power pattern for 0 and 30 degrees azimuth for 300 MHz .

## Construct Heterogeneous ULA

Construct the array from z-directed and y-directed short dipole antenna elements.

```
sElement1 = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[200e6 500e6],...
    'AxisDirection','Z');
sElement2 = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[200e6 500e6],...
    'AxisDirection','Y');
sArray = phased.HeterogeneousULA(...
    'ElementSpacing',0.4,...
    'ElementSet',{sElement1,sElement2},...
    'ElementIndices',[1 1 1 2 2 2 2 2 1 1 1]);
```


## Plot Directivity Pattern

```
fc = 300e6;
c = physconst('LightSpeed');
patternElevation(sArray,fc,[0,30],...
    'PropagationSpeed',c,...
    'Type','directivity')
```



Directivity (dBi), Broadside at $0.00^{\circ}$

## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Version History

 Introduced in R2015a
## See Also

pattern|patternAzimuth

## plotResponse

System object: phased. HeterogeneousULA
Package: phased
Plot response pattern of array

## Syntax

plotResponse(H, FREQ, V)
plotResponse(H, FREQ, V, Name, Value)
hPlot = plotResponse( $\qquad$ )

## Description

plotResponse ( $\mathrm{H}, \mathrm{FREQ}, \mathrm{V}$ ) plots the array response pattern along the azimuth cut, where the elevation angle is 0 . The operating frequency is specified in FREQ. The propagation speed is specified in $V$.
plotResponse(H, FREQ, V,Name, Value) plots the array response with additional options specified by one or more Name, Value pair arguments.
hPlot = plotResponse( $\qquad$ ) returns handles of the lines or surface in the figure window, using any of the input arguments in the previous syntaxes.

## Input Arguments

## H

Array object

## FREQ

Operating frequency in Hertz specified as a scalar or 1-by-K row vector. Values must lie within the range specified by a property of H . That property is named FrequencyRange or FrequencyVector, depending on the type of element in the array. The element has no response at frequencies outside that range. If you set the 'RespCut ' property of $H$ to ' $3 D^{\prime}$ ' FREQ must be a scalar. When FREQ is a row vector, plot Response draws multiple frequency responses on the same axes.

## V

Propagation speed in meters per second.

## Name-Value Pair Arguments

Specify optional pairs of arguments as Namel=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## CutAngle

Cut angle as a scalar. This argument is applicable only when RespCut is ' Az ' or ' El '. If RespCut is 'Az', CutAngle must be between -90 and 90. If RespCut is ' El ' , CutAngle must be between -180 and 180.

Default: 0

## Format

Format of the plot, using one of 'Line', 'Polar', or 'UV '. If you set Format to 'UV ', FREQ must be a scalar.

## Default: 'Line'

## NormalizeResponse

Set this value to true to normalize the response pattern. Set this value to false to plot the response pattern without normalizing it. This parameter is not applicable when you set the Unit parameter value to 'dbi'.

## Default: true

## OverlayFreq

Set this value to true to overlay pattern cuts in a 2-D line plot. Set this value to false to plot pattern cuts against frequency in a 3-D waterfall plot. If this value is false, FREQ must be a vector with at least two entries.

This parameter applies only when Format is not 'Polar' and RespCut is not '3D '.

## Default: true

## Polarization

Specify the polarization options for plotting the array response pattern. The allowable values are |'None' | 'Combined' | 'H' | 'V' | where

- 'None' specifies plotting a nonpolarized response pattern
- 'Combined ' specifies plotting a combined polarization response pattern
- 'H' specifies plotting the horizontal polarization response pattern
- 'V ' specifies plotting the vertical polarization response pattern

For arrays that do not support polarization, the only allowed value is 'None'. This parameter is not applicable when you set the Unit parameter value to ' dbi ' .

Default: 'None'

## RespCut

Cut of the response. Valid values depend on Format, as follows:

- If Format is 'Line' or 'Polar', the valid values of RespCut are 'Az', 'El', and '3D'. The default is ' Az '.
- If Format is 'UV', the valid values of RespCut are 'U' and '3D'. The default is 'U'.

If you set RespCut to '3D' , FREQ must be a scalar.

## Unit

The unit of the plot. Valid values are 'db', 'mag', 'pow', or 'dbi'. This parameter determines the type of plot that is produced.

| Unit value | Plot type |
| :--- | :--- |
| db | power pattern in dB scale |
| mag | field pattern |
| pow | power pattern |
| dbi | directivity |

Default: 'db'

## Weights

Weight values applied to the array, specified as a length- $N$ column vector or $N$-by- $M$ matrix. The dimension $N$ is the number of elements in the array. The interpretation of $M$ depends upon whether the input argument FREQ is a scalar or row vector.

| Weights Dimensions | FREQ Dimension | Purpose |
| :--- | :--- | :--- |
| $N$-by-1 column vector | Scalar or 1-by-M row vector | Apply one set of weights for the <br> same single frequency or all $M$ <br> frequencies. |
| $N$-by- $M$ matrix | Scalar | Apply all of the $M$ different <br> columns in Weights for the <br> same single frequency. |
|  | 1-by- $M$ row vector | Apply each of the $M$ different <br> columns in Weights for the <br> corresponding frequency in <br> FREQ. |

## AzimuthAngles

Azimuth angles for plotting array response, specified as a row vector. The AzimuthAngles parameter sets the display range and resolution of azimuth angles for visualizing the radiation pattern. This parameter is allowed only when the RespCut parameter is set to 'Az' or '3D' and the Format parameter is set to 'Line' or 'Polar'. The values of azimuth angles should lie between $180^{\circ}$ and $180^{\circ}$ and must be in nondecreasing order. When you set the RespCut parameter to ' 3D ', you can set the AzimuthAngles and ElevationAngles parameters simultaneously.

Default: [-180:180]

## ElevationAngles

Elevation angles for plotting array response, specified as a row vector. The ElevationAngles parameter sets the display range and resolution of elevation angles for visualizing the radiation pattern. This parameter is allowed only when the RespCut parameter is set to ' El ' or ' 3 D ' and the

Format parameter is set to 'Line' or 'Polar'. The values of elevation angles should lie between $90^{\circ}$ and $90^{\circ}$ and must be in nondecreasing order. When yous set the RespCut parameter to ' $3 \mathrm{D}^{\prime}$, you can set the ElevationAngles and AzimuthAngles parameters simultaneously.

Default: [-90:90]

## UGrid

$U$ coordinate values for plotting array response, specified as a row vector. The UGrid parameter sets the display range and resolution of the $U$ coordinates for visualizing the radiation pattern in $U / V$ space. This parameter is allowed only when the Format parameter is set to 'UV' and the RespCut parameter is set to ' $U$ ' or ' $3 D^{\prime}$ '. The values of UGrid should be between -1 and 1 and should be specified in nondecreasing order. You can set the UGrid and VGrid parameters simultaneously.

Default: [-1:0.01:1]

## VGrid

$V$ coordinate values for plotting array response, specified as a row vector. The VGrid parameter sets the display range and resolution of the $V$ coordinates for visualizing the radiation pattern in $U / V$ space. This parameter is allowed only when the Format parameter is set to 'UV' and the RespCut parameter is set to ' $3 D^{\prime}$ '. The values of VGrid should be between -1 and 1 and should be specified in nondecreasing order. You can set VGrid and UGrid parameters simultaneously.

Default: [-1:0.01:1]

## Examples

## Line Plot Showing Multiple Frequencies

Using a line plot, show the azimuth cut response of a 5-element heterogeneous uniform linear array along 0 degrees elevation. The plot shows the responses at operating frequencies of 200 MHz and 400 MHz .

Construct the array from z-directed and y-directed short dipole antenna elements.

```
sElement1 = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[2e8 5e8],...
    'AxisDirection','Z');
sElement2 = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[2e8 5e8],...
    'AxisDirection','Y');
sArray = phased.HeterogeneousULA(...
    'ElementSet',{sElement1,sElement2},...
    'ElementIndices',[1 2 2 2 1]);
```

Plot the response.

```
fc = [3e8 4e8];
c = physconst('LightSpeed');
plotResponse(sArray,fc,c);
```



## Plot Response and Directivity for 5-Element Array

Construct a 5 -element heterogeneous ULA of short-dipole antenna elements. Using the plotResponse method, plot the array's azimuth response in polar format. Assume each element's operating frequency spans $200-500 \mathrm{MHz}$ and the wave propagation speed is the speed of light.

```
sElement1 = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[2e8 5e8],...
    'AxisDirection','Z');
sElement2 = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[2e8 5e8],...
    'AxisDirection','Y');
sArray = phased.HeterogeneousULA(...
    'ElementSet',{sElement1,sElement2},...
    'ElementIndices',[1 2 2 2 1]);
```

Plot the response at 300 MHz .
fc = 3e8;
c = physconst('LightSpeed');
plotResponse(sArray,fc, c, 'RespCut','Az','Format','Polar');


Normalized Power (dB), Broadside at $0.00^{\circ}$
Plot the directivity of the array at 300 MHz .
plotResponse(sArray,fc,c,'RespCut','Az','Format','Polar',...
'Unit','dbi');


Directivity (dBi), Broadside at $0.00^{\circ}$

## Plot Response for 9-Element Array with Two Weight Sets

Construct a 9-element heterogeneous ULA of short-dipole antenna elements having different orientations. Assume each element response is in the frequency range $200-500 \mathrm{MHz}$. Using the plotResponse method, plot the array's azimuth response in polar format. Use the Weights parameter to set two different sets of tapering weights: a uniform tapering and a Taylor tapering. Use the AzimuthAngles parameter to restrict the display range from -45 to 45 degrees in 0.1 degree increments.

Construct the array.

```
sElement1 = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[2e8 5e8],...
    'AxisDirection','Z');
sElement2 = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[2e8 5e8],...
    'AxisDirection','Y');
sArray = phased.HeterogeneousULA(...
    'ElementSet',{sElement1,sElement2},...
    'ElementIndices',[1 1 2 2 2 2 2 1 1]);
```

Plot the response at 300 MHz .
$\mathrm{fc}=3 \mathrm{e} 8$;
wts1 = ones (9,1);
wts2 = taylorwin(9);
$\mathrm{c}=$ physconst('LightSpeed');
plotResponse(sArray,fc, c, 'RespCut', 'Az', ...
'AzimuthAngles', [-45:0.1:45],...
'Weights',[wts1,wts2]);


As expected, the tapered weighting broadens the mainlobe and reduces the sidelobes.

## See Also

uv2azel|azel2uv

## step

System object: phased. HeterogeneousULA
Package: phased
Output responses of array elements

## Syntax

RESP = step(H,FREQ,ANG)

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step $(\mathrm{obj}, \mathrm{x})$ and $\mathrm{y}=\mathrm{obj}(\mathrm{x})$ perform equivalent operations.

RESP = step ( $\mathrm{H}, \mathrm{FREQ}, \mathrm{ANG}$ ) returns the array elements' responses RESP at operating frequencies specified in FREQ and directions specified in ANG.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## H

Array object

## FREQ

Operating frequencies of array in hertz. FREQ is a row vector of length $L$. Typical values are within the range specified by a property of H . Element. That property is named FrequencyRange or FrequencyVector, depending on the type of element in the array. The element has zero response at frequencies outside that range.

## ANG

Directions in degrees. ANG is either a 2-by- $M$ matrix or a row vector of length $M$.
If ANG is a 2 -by- $M$ matrix, each column of the matrix specifies the direction in the form [azimuth; elevation]. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive.

If ANG is a row vector of length $M$, each element specifies the azimuth angle of the direction. In this case, the corresponding elevation angle is assumed to be $0^{\circ}$.

## Output Arguments

## RESP

Voltage responses of the phased array. The output depends on whether the array supports polarization or not.

- If the array is not capable of supporting polarization, the voltage response, RESP, has the dimensions $N$-by- $M$-by- $L$. $N$ is the number of elements in the array. The dimension $M$ is the number of angles specified in ANG. $L$ is the number of frequencies specified in FREQ. For any element, the columns of RESP contain the responses of the array elements for the corresponding direction specified in ANG. Each of the $L$ pages of RESP contains the responses of the array elements for the corresponding frequency specified in FREQ.
- If the array is capable of supporting polarization, the voltage response, RESP, is a MATLAB struct containing two fields, RESP.H and RESP.V. The field, RESP.H, represents the array's horizontal polarization response, while RESP.V represents the array's vertical polarization response. Each field has the dimensions $N$-by- $M$-by-L. $N$ is the number of elements in the array, and $M$ is the number of angles specified in ANG. $L$ is the number of frequencies specified in FREQ. Each column of RESP contains the responses of the array elements for the corresponding direction specified in ANG. Each of the $L$ pages of RESP contains the responses of the array elements for the corresponding frequency specified in FREQ.


## Examples

## Heterogeneous ULA of Cosine Antenna Elements

Create a 5-element heterogeneous ULA of cosine antenna elements with difference responses, and find the response of each element at $30^{\circ}$ azimuth.

```
antenna1 = phased.CosineAntennaElement('CosinePower',1.5);
antenna2 = phased.CosineAntennaElement('CosinePower',1.8);
array = phased.HeterogeneousULA(...
    'ElementSet',{antenna1,antenna2},...
    'ElementIndices',[1 2 2 2 1]);
fc = 1e9;
c = physconst('LightSpeed');
ang = [30;0];
resp = array(fc,ang)
resp = 5 x 1
    0.8059
    0.7719
    0.7719
    0.7719
    0.8059
```


## Response of Heterogeneous Microphone ULA Array

Find the response of a heterogeneous ULA array of 7 custom microphone elements with different responses.

Create two microphones with different response patterns.

```
mic1 = phased.CustomMicrophoneElement(...
```

    'FrequencyResponse',[20 20e3]);
    mic1.PolarPatternFrequencies $=$ [500 1000];
mic1. PolarPattern = mag2db([...
$0.5+0.5^{*}$ cosd(mic1.PolarPatternAngles) ; ...
0.6+0.4*cosd(mic1.PolarPatternAngles)]);
mic2 = phased.CustomMicrophoneElement(...
'FrequencyResponse',[20 20e3]);
mic2.PolarPatternFrequencies $=$ [500 1000];
mic2. PolarPattern = mag2db([...
ones(size(mic2. PolarPatternAngles)); ...
ones(size(mic2.PolarPatternAngles))]);

Create the heterogeneous ULA.

```
array = phased.HeterogeneousULA(...
    'ElementSet',{mic1,mic2},...
    'ElementIndices',[1 1 2 2 2 1 1]);
```

Find the array response at $40^{\circ}$ and $50^{\circ}$ azimuth.

```
fc = [1500, 2000];
ang = [40 50; 0 0];
resp = array(fc,ang)
resp =
resp(:,:,1) =
    9.0642 8.5712
    9.0642 8.5712
    10.0000 10.0000
    10.0000 10.0000
    10.0000 10.0000
        9.0642 8.5712
        9.0642 8.5712
resp(:,:,2) =
    9.0642 8.5712
    9.0642 8.5712
    10.0000 10.0000
    10.0000 10.0000
    10.0000 10.0000
        9.0642 8.5712
    9.0642 8.5712
```


## See Also

uv2azel|phitheta2azel

## viewArray

System object: phased. HeterogeneousULA
Package: phased
View array geometry

## Syntax

```
viewArray(H)
viewArray(H,Name,Value)
hPlot = viewArray(
```

$\qquad$

``` )
```


## Description

viewArray (H) plots the geometry of the array specified in H .
viewArray ( $\mathrm{H}, \mathrm{Name}$, Value) plots the geometry of the array, with additional options specified by one or more Name, Value pair arguments.
hPlot = viewArray( $\qquad$ ) returns the handle of the array elements in the figure window. All input arguments described for the previous syntaxes also apply here.

## Input Arguments

## H

Array object.

## Name-Value Pair Arguments

Specify optional pairs of arguments as Namel=Value1, . . . ,NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Parent

Handle to the axes along which the array geometry is displayed.

## ShowNormals

Set this value to true to show the normal directions of all elements of the array. Set this value to false to plot the elements without showing normal directions.

Default: false

## ShowLocalCoordinates

Logical flag specifying whether to show the local coordinate axes.

Default: true

## ShowAnnotation

Logical flag specifying whether to show the annotations in the UI panel of the figure. Annotation shows aperture size and element spacing based on array axis of array.

Default: true

## Orientation

Orientation of the array, specified as a 3-by-1 column vector containing the rotation angles with respect to the $x-, y$-, and $z$-axes of the local coordinate system, respectively. The default value is [0;0;0].

Default: [0;0;0]

## ShowTaper

Set this value to true to specify whether to change the element color brightness in proportion to the element taper magnitude. When this value is set to false, all elements are drawn with the same color.

Default: false

## ShowIndex

Vector specifying the element indices to show in the figure. Each number in the vector must be an integer between 1 and the number of elements. You can also specify the value 'All ' to show the indices of all elements of the array or 'None' to suppress indices.

Default: 'None'

## Title

Character vector specifying the title of the plot.
Default: 'Array Geometry'

## Output Arguments

## hPlot

Handle of array elements in figure window.

## Examples

## Geometry and Indices of Heterogeneous ULA Elements

Display the geometry of a 5-element heterogeneous ULA of cosine antenna elements, showing the indices for the first three elements.

```
sElement1 = phased.CosineAntennaElement('CosinePower',1.5);
sElement2 = phased.CosineAntennaElement('CosinePower',1.8);
```

sArray = phased.HeterogeneousULA(...
'ElementSet',\{sElement1,sElement2\},... 'ElementIndices',[1 2221$]) ;$
viewArray(sArray,'ShowIndex',[1:3])

## Array Geometry



[^4]
## See Also

phased.ArrayResponse

## Topics

Phased Array Gallery

## phased.HeterogeneousURA

Package: phased
Heterogeneous uniform rectangular array

## Description

The HeterogeneousURA object constructs a heterogeneous uniform rectangular array (URA).
To compute the response for each element in the array for specified directions:
1 Define and set up your uniform rectangular array. See "Construction" on page 1-613.
2 Call step to compute the response according to the properties of phased. HeterogeneousURA.
The behavior of step is specific to each object in the toolbox.

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step (obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.

## Construction

H = phased. HeterogeneousURA creates a heterogeneous uniform rectangular array (URA) System object, H. This object models a heterogeneous URA formed with sensor elements whose pattern may vary from element to element. Array elements are distributed in the $y z$-plane in a rectangular lattice. An $M$-by- $N$ heterogeneous URA has $M$ rows and $N$ columns. The array boresight direction is along the positive $x$-axis. The default array is a 2-by-2 URA of isotropic antenna elements.

H = phased. HeterogeneousURA (Name, Value) creates the object, H , with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN).

## Properties

## ElementSet

Set of elements used in the array
Set of elements used in the sensor array, specified as a row MATLAB cell array. Elements specified in the ElementSet property must be either Phased Array System Toolbox antennas, microphones, or transducers System objects or Antenna Toolbox System object. In addition, all specified antenna elements must have the same polarization capability.

Default: One cell containing one isotropic antenna element

## ElementIndices

Elements location assignment
This property specifies the mapping of elements in the array. The property assigns elements to their locations in the array using the indices into the ElementSet property. The value of

ElementIndices must be an $M$-by- $N$ matrix. In this matrix, $M$ represents the number of rows and $N$ represents the number of columns. Rows are along $y$-axis and columns are along $z$-axis of the local coordinate system. The values in the matrix specified by ElementIndices should be less than or equal to the number of entries in the ElementSet property.

Default: [1 1;1 1]

## ElementSpacing

Element spacing
A 1-by-2 vector or a scalar containing the element spacing (in meters) of the array. If ElementSpacing is a 1-by-2 vector, it is in the form of
[SpacingBetweenRows,SpacingBetweenColumns]. See "Spacing Between Columns" on page 1618 and "Spacing Between Rows" on page 1-618. If ElementSpacing is a scalar, both spacings are the same.

Default: [0.5 0.5]

## Lattice

Element lattice
Specify the element lattice as one of 'Rectangular' | 'Triangular'. When you set the Lattice property to 'Rectangular', all elements in the heterogeneous URA are aligned in both row and column directions. When you set the Lattice property to 'Triangular', the elements in even rows are shifted toward the positive row axis direction by a distance of half the element spacing along the row.

## Default: 'Rectangular'

## ArrayNormal

Array normal direction
Array normal direction, specified as one of ' $x$ ', ' $y$ ', or ' $z$ '.
URA elements lie in a plane orthogonal to the selected array normal direction. Element boresight directions point along the array normal direction

| ArrayNormal Property Value | Element Positions and Boresight Directions |
| :--- | :--- |
| ' $x$ ' | Array elements lie on the $y z$-plane. All element <br> boresight vectors point along the $x$-axis. |
| ' $y$ ' | Array elements lie on the $z x$-plane. All element <br> boresight vectors point along the $y$-axis. |
| $'^{\prime} z$ ' | Array elements lie on the $x y$-plane. All element <br> boresight vectors point along the $z$-axis. |

Default: ' x '

## Taper

Element tapers

Element tapers, specified as a complex-valued scalar, or a complex-valued 1-by-MN row vector, $M N$ -by-1 column vector, or $M$-by- $N$ matrix. Tapers are applied to each element in the sensor array. Tapers are often referred to as element weights. $M$ is the number of elements along the $z$-axis, and $N$ is the number of elements along $y$-axis. $M$ and $N$ correspond to the values of [NumberofRows, NumberOfColumns ] in the Size property. If Taper is a scalar, the same taper value is applied to all elements. If the value of Taper is a vector or matrix, taper values are applied to the corresponding elements. Tapers are used to modify both the amplitude and phase of the received data.

## Default: 1

## Methods

| Specific to phased. HeterogeneousURA Object |  |
| :--- | :--- |
| beamwidth | Compute and display beamwidth of an array |
| collectPla <br> neWave | Simulate received plane waves |
| directivit <br> y | Directivity of heterogeneous uniform rectangular array |
| getElement <br> Normal | Normal vector to array elements |
| getElement <br> Position | Positions of array elements |
| getNumElem <br> ents | Number of elements in array |
| getTaper | Array element tapers |
| isPolariza <br> tionCapabl <br> e | Polarization capability |
| pattern | Plot heterogeneous URA directivity and power pattern |
| patternAzi <br> muth | Plot heterogeneous URA directivity or pattern versus azimuth |
| patternEle <br> vation | Plot heterogeneous URA array directivity or pattern versus elevation |
| perturbati <br> ons | Perturbations defined on phased array |
| perturbedA <br> rray | Apply perturbations to phased array |
| perturbedP <br> attern | Compute and plot azimuth pattern of perturbed array |
| step | Output responses of array elements |
| viewArray | View array geometry |

## Common to All System Objects

| release | Allow System object property value changes |
| :--- | :--- |

## Examples

## Azimuth Pattern of 3-by-2 Heterogeneous URA

Construct a 3-by-2 heterogeneous URA with a rectangular lattice, and find the response of each element at 30 degrees azimuth and 0 degrees elevation. Assume the operating frequency is 1 GHz .

```
antenna1 = phased.CosineAntennaElement('CosinePower',1.5);
antenna2 = phased.CosineAntennaElement('CosinePower',1.8);
array = phased.HeterogeneousURA('ElementSet',{antenna1,antenna2}, ...
    ElementIndices',[1 1; 2 2; 1 1]);
fc = 1e9;
ang = [30;0];
resp = array(fc,ang)
resp = 6\times1
    0.8059
    0.7719
    0.8059
    0.8059
    0.7719
    0.8059
```

Plot the azimuth pattern of the array.

```
c = physconst('LightSpeed');
pattern(array,fc,[-180:180],0,'PropagationSpeed',c, ...
    'CoordinateSystem','polar','Type','powerdb','Normalize',true)
```



Normalized Power (dB), Broadside at $0.00^{\circ}$

## Draw Heterogeneous Triangular Lattice Array

Construct a 3-by-3 heterogeneous URA with a triangular lattice. The element spacing is 0.5 meter. Display the array shape.

```
sElement1 = phased.CosineAntennaElement('CosinePower',1.5);
sElement2 = phased.CosineAntennaElement('CosinePower',1.8);
sArray = phased.HeterogeneousURA(...
    'ElementSet',{sElement1,sElement2},...
    'ElementIndices',[1 1 1; 2 2 2; 1 1 1],...
    'Lattice','Triangular');
viewArray(sArray);
```


## Array Geometry



## More About

## Spacing Between Columns

The spacing between columns is the distance between adjacent elements in the same row.

## Spacing Between Rows

The spacing between rows is the distance along the column axis direction between adjacent rows.


## Version History

Introduced in R2013a

## References

[1] Brookner, E., ed. Radar Technology. Lexington, MA: LexBook, 1996.
[2] Brookner, E., ed. Practical Phased Array Antenna Systems. Boston: Artech House, 1991.
[3] Mailloux, R. J. "Phased Array Theory and Technology," Proceedings of the IEEE, Vol., 70, Number 3, 1982, pp. 246-291.
[4] Mott, H. Antennas for Radar and Communications, A Polarimetric Approach. New York: John Wiley \& Sons, 1992.
[5] Van Trees, H. Optimum Array Processing. New York: Wiley-Interscience, 2002.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\text {TM }}$.
Usage notes and limitations:

- pattern, patternAzimuth, patternElevation, plotResponse, and viewArray methods are not supported.
- See "System Objects in MATLAB Code Generation" (MATLAB Coder).


## See Also

phased.ReplicatedSubarray | phased.PartitionedArray| phased.ConformalArray | phased.CosineAntennaElement | phased.CustomAntennaElement |
phased.IsotropicAntennaElement|phased.ULA| phased.URA|phased.HeterogeneousULA | phased.UCA| phased.HeterogeneousConformalArray

## Topics

Phased Array Gallery

## directivity

System object: phased. HeterogeneousURA
Package: phased
Directivity of heterogeneous uniform rectangular array

## Syntax

D = directivity (H, FREQ,ANGLE)
D = directivity (H, FREQ, ANGLE, Name, Value)

## Description

D = directivity (H, FREQ, ANGLE) computes the "Directivity (dBi)" on page 1-624 of a heterogeneous uniform rectangular array of antenna or microphone elements, H , at frequencies specified by the FREQ and in angles of direction specified by the ANGLE.

The integration used when computing array directivity has a minimum sampling grid of 0.1 degrees. If an array pattern has a beamwidth smaller than this, the directivity value will be inaccurate.

D = directivity (H, FREQ, ANGLE, Name, Value) computes the directivity with additional options specified by one or more Name, Value pair arguments.

## Input Arguments

## H - Heterogeneous uniform rectangular array

System object
Uniform rectangular array specified as a phased. HeterogeneousURA System object.
Example: H = phased.HeterogeneousURA

## FREQ - Frequency for computing directivity and patterns

positive scalar | 1-by-L real-valued row vector
Frequencies for computing directivity and patterns, specified as a positive scalar or 1-by-L realvalued row vector. Frequency units are in hertz.

- For an antenna, microphone, or sonar hydrophone or projector element, FREQ must lie within the range of values specified by the FrequencyRange or FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased. CustomAntennaElement and phased.CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: [1e8 2e6]
Data Types: double

## ANGLE - Angles for computing directivity

1-by- $M$ real-valued row vector | 2 -by- $M$ real-valued matrix
Angles for computing directivity, specified as a 1-by- $M$ real-valued row vector or a 2 -by- $M$ real-valued matrix, where $M$ is the number of angular directions. Angle units are in degrees. If ANGLE is a 2-by- $M$ matrix, then each column specifies a direction in azimuth and elevation, [az;el]. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

If ANGLE is a $1-b y-M$ vector, then each entry represents an azimuth angle, with the elevation angle assumed to be zero.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the xy plane. This angle is positive when measured from the $x$-axis toward the $y$-axis. The elevation angle is the angle between the direction vector and $x y$ plane. This angle is positive when measured towards the $z$-axis. See "Azimuth and Elevation Angles".
Example: [45 60; 0 10]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## PropagationSpeed - Signal propagation speed

speed of light (default) | positive scalar
Signal propagation speed, specified as the comma-separated pair consisting of
'PropagationSpeed ' and a positive scalar in meters per second.
Example: 'PropagationSpeed', physconst('LightSpeed')
Data Types: double
Weights - Array weights
1 (default) | $N$-by-1 complex-valued column vector | $N$-by-L complex-valued matrix
Array weights, specified as the comma-separated pair consisting of 'Weights' and an $N$-by-1 complex-valued column vector or $N$-by- $L$ complex-valued matrix. Array weights are applied to the elements of the array to produce array steering, tapering, or both. The dimension $N$ is the number of elements in the array. The dimension $L$ is the number of frequencies specified by FREQ.

| Weights Dimension | FREQ Dimension | Purpose |
| :--- | :--- | :--- |
| $N$-by-1 complex-valued column <br> vector | Scalar or 1-by- $L$ row vector | Applies a set of weights for the <br> single frequency or for all $L$ <br> frequencies. |
| $N$-by- $L$ complex-valued matrix | 1-by-L row vector | Applies each of the $L$ columns of <br> 'Weights' for the <br> corresponding frequency in <br> FREQ. |

Note Use complex weights to steer the array response toward different directions. You can create weights using the phased.SteeringVector System object or you can compute your own weights. In general, you apply Hermitian conjugation before using weights in any Phased Array System Toolbox function or System object such as phased. Radiator or phased. Collector. However, for the directivity, pattern, patternAzimuth, and patternElevation methods of any array System object use the steering vector without conjugation.

## Example: 'Weights',ones(N,M)

Data Types: double
Complex Number Support: Yes

## Output Arguments

## D - Directivity

M-by-L matrix
Directivity, returned as an $M$-by- $L$ matrix. Each row corresponds to one of the $M$ angles specified by ANGLE. Each column corresponds to one of the $L$ frequency values specified in FREQ. Directivity units are in dBi where dBi is defined as the gain of an element relative to an isotropic radiator.

## Examples

## Directivity of Heterogeneous Uniform Rectangular Array

Compute the directivity of a 9-element 3-by-3 heterogeneous URA consisting of short-dipole antenna elements. The three elements on the middle row are Y -directed while all the remaining elements are Z-directed.

Set the signal frequency to 1 GHz .

```
c = physconst('LightSpeed');
freq = 1e9;
lambda = c/freq;
```

Create the array of short-dipole antenna elements. The elements have frequency ranges from 0 to 10 GHz.

```
myElement1 = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[0 10e9],...
    'AxisDirection','Z');
myElement2 = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[0 10e9],...
    'AxisDirection','Y');
myArray = phased.HeterogeneousURA(...
    'ElementSet',{myElement1,myElement2},...
    'ElementIndices',[1 1 1; 2 2 2; 1 1 1]);
```

Create the steering vector to point to 30 degrees azimuth and compute the directivity in the same direction as the steering vector.

```
ang = [30;0];
w = steervec(getElementPosition(myArray)/lambda,ang);
```

```
d = directivity(myArray,freq,ang,'PropagationSpeed', c,...
    'Weights', w)
\(\mathrm{d}=11.1405\)
```


## More About

## Directivity (dBi)

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

See Also<br>pattern | patternAzimuth | patternElevation

## collectPlaneWave

System object: phased. HeterogeneousURA
Package: phased
Simulate received plane waves

## Syntax

```
Y = collectPlaneWave(H,X,ANG)
Y = collectPlaneWave(H,X,ANG,FREQ)
Y = collectPlaneWave(H,X,ANG,FREQ,C)
```


## Description

$Y=\operatorname{collectPlaneWave}(H, X, A N G)$ returns the received signals at the sensor array, $H$, when the input signals indicated by $X$ arrive at the array from the directions specified in ANG.
$Y=$ collectPlaneWave ( $H, X$, ANG, $F R E Q$ ), in addition, specifies the incoming signal carrier frequency in FREQ.
$Y=\operatorname{collectPlaneWave}(H, X, A N G, F R E Q, C)$, in addition, specifies the signal propagation speed in C.

## Input Arguments

## H

Array object.
X
Incoming signals, specified as an M-column matrix. Each column of $X$ represents an individual incoming signal.

## ANG

Directions from which incoming signals arrive, in degrees. ANG can be either a 2-by-M matrix or a row vector of length M .

If ANG is a 2-by-M matrix, each column specifies the direction of arrival of the corresponding signal in X. Each column of ANG is in the form [azimuth; elevation]. The azimuth angle must be between $-180^{\circ}$ and $180^{\circ}$, inclusive. The elevation angle must be between $-90^{\circ}$ and $90^{\circ}$, inclusive.

If ANG is a row vector of length M , each entry in ANG specifies the azimuth angle. In this case, the corresponding elevation angle is assumed to be $0^{\circ}$.

FREQ
Carrier frequency of signal in hertz. FREQ must be a scalar.
Default: 3e8

## C

Propagation speed of signal in meters per second.
Default: Speed of light

## Output Arguments

## Y

Received signals. Y is an N -column matrix, where N is the number of elements in the array H. Each column of $Y$ is the received signal at the corresponding array element, with all incoming signals combined.

## Examples

## Create Received Signal at Heterogeneous URA

Simulate two received signals at a 2-by-2 element heterogeneous URA with two different cosine antenna patterns. The signals arrive from $10^{\circ}$ and $30^{\circ}$ azimuth. Both signals have an elevation angle of $0^{\circ}$.

```
antenna1 = phased.CosineAntennaElement('CosinePower',1.5);
antenna2 = phased.CosineAntennaElement('CosinePower',1.8);
array = phased.HeterogeneousURA(...
            'ElementSet',{antenna1,antenna2},...
            'ElementIndices',[1 2; 1 2]);
y = collectPlaneWave(array,randn(4,2),[10 30],1e8,physconst('LightSpeed'))
y = 4x4 complex
    0.8433 - 0.1314i 0.8433 - 0.1314i 0.8433 + 0.1314i 0.8433 + 0.1314i
    0.5632 + 0.1721i 0.5632 + 0.1721i 0.5632 - 0.1721i 0.5632 - 0.1721i
    -2.6683 + 0.3175i -2.6683 + 0.3175i -2.6683-0.3175i -2.6683 - 0.3175i
    1.1895 - 0.1671i 1.1895 - 0.1671i 1.1895 + 0.1671i 1.1895 + 0.1671i
```


## Algorithms

collectPlaneWave modulates the input signal with a phase corresponding to the delay caused by the direction of arrival. This method does not account for the response of individual elements in the array.

For further details, see [1].

## References

[1] Van Trees, H. Optimum Array Processing. New York: Wiley-Interscience, 2002.
uv2azel | phitheta2azel

## getElementNormal

System object: phased. HeterogeneousURA

Package: phased
Normal vector to array elements

## Syntax

normvec = getElementNormal(sURA)
normvec = getElementNormal(sURA,elemidx)

## Description

normvec $=$ getElementNormal(sURA) returns the normal vectors of the array elements of the phased.URA System object, sURA. The output argument normvec is a 2 -by- $N$ matrix, where $N$ is the number of elements in array, sURA. Each column of normvec defines the normal direction of an element in the local coordinate system in the form [az;el]. Units are degrees. The origin of the local coordinate system is defined by the phase center of the array.
normvec $=$ getElementNormal(sURA,elemidx) returns only the normal vectors of the elements specified in the element index vector, elemidx. This syntax can use any of the input arguments in the previous syntax.

## Input Arguments

sURA - Heterogeneous uniform rectangular array
phased. HeterogeneousURA System object
Uniform line array, specified as a phased. HeterogeneousURA System object.
Example: sULA = phased.HeterogeneousURA
elemidx - Element indices
all array elements (default) | integer-valued 1-by-M row vector | integer-valued $M$-by-1 column vector
Element indices, specified as a 1 -by- $M$ or $M$-by-1 vector. Index values lie in the range 1 to $N$ where $N$ is the number of elements of the array. When elemidx is specified, getElementNormal returns the normal vectors of the elements contained in elemidx.

Example: [1,5,4]

## Output Arguments

## normvec - Element normal vectors

2 -by- $P$ real-valued vector
Element normal vectors, specified as a 2-by-P real-valued vector. Each column of normvec takes the form [az,el]. When elemidx is not specified, $P$ equals the array dimension. When elemidx is specified, $P$ equals the length of elemidx, $M$. You can determine element indices using the viewArray method.

## Examples

## URA Element Normals

Construct three 2-by-2 URA's with element normals along the $x$-, $y$-, and $z$-axes. Obtain the element positions and normal directions.

First, choose the array normal along the $x$-axis.

```
sURA1 = phased.URA('Size',[2,2],'ArrayNormal','x');
pos = getElementPosition(sURA1)
pos = 3\times4
\begin{tabular}{rrrr}
0 & 0 & 0 & 0 \\
-0.2500 & -0.2500 & 0.2500 & 0.2500 \\
0.2500 & -0.2500 & 0.2500 & -0.2500
\end{tabular}
```

```
normvec = getElementNormal(sURA1)
```

normvec = getElementNormal(sURA1)
normvec = 2×4
normvec = 2×4
0 0 0 0
0}0

```

All elements lie in the \(y z\)-plane and the element normal vectors point along the \(x\)-axis \(\left(0^{\circ}, 0^{\circ}\right)\). Next, choose the array normal along the \(y\)-axis.
```

sURA2 = phased.URA('Size',[2,2],'ArrayNormal','y');
pos = getElementPosition(sURA2)
pos = 3\times4

| 0.2500 | 0.2500 | -0.2500 | -0.2500 |
| ---: | ---: | ---: | ---: |
| 0 | 0 | 0 | 0 |
| 0.2500 | -0.2500 | 0.2500 | -0.2500 |

normvec = getElementNormal(sURA2)
normvec = 2×4
90 90 90 90
0 0 0 0

```

All elements lie in the \(z x\)-plane and the element normal vectors point along the \(y\)-axis \(\left(90^{\circ}, 0^{\circ}\right)\).
Finally, set the array normal along the \(z\)-axis. Obtain the normal vectors of the odd-numbered elements.
```

sURA3 = phased.URA('Size',[2,2],'ArrayNormal','z');
pos = getElementPosition(sURA3)
pos = 3\times4

```
```

    0.2500 -0.2500 0.2500 0.2500
    0.2500 -0.2500 0.2500 -0.2500
    normvec = getElementNormal(sURA3,[1,3])
normvec = 2×2
0 0
90 90

```

All elements lie in the \(x y\)-plane and the element normal vectors point along the \(z\)-axis \(\left(0^{\circ}, 90^{\circ}\right)\).

\section*{Version History \\ Introduced in R2016a}

\section*{getElementPosition}

System object: phased. HeterogeneousURA
Package: phased
Positions of array elements

\section*{Syntax}
```

POS = getElementPosition(H)
POS = getElementPosition(H,ELEIDX)

```

\section*{Description}

POS = getElementPosition(H) returns the element positions of the HeterogeneousURA System object, H. POS is a 3-by-N matrix where N is the number of elements in H. Each column of POS defines the position of an element in the local coordinate system, in meters, using the form [x; y; \(z]\).

For details regarding the local coordinate system of the URA or heterogeneous URA, enter phased.URA. coordinateSystemInfo on the command line.

POS = getElementPosition(H,ELEIDX) returns the positions of the elements that are specified in the element index vector, ELEIDX. The element indices of a URA run down each column, then to the top of the next column to the right. For example, in a URA with 4 elements in each row and 3 elements in each column, the element in the third row and second column has an index value of 6 . This syntax can use any of the input arguments in the previous syntax.

\section*{Examples}

\section*{Element Positions of Heterogeneous URA}

Construct a heterogeneous URA with a rectangular lattice, and obtain the element positions.
```

antenna1 = phased.ShortDipoleAntennaElement('FrequencyRange',[100e6 1e9], ...
'AxisDirection','Z');
antenna2 = phased.ShortDipoleAntennaElement('FrequencyRange',[100e6 1e9], ...
'AxisDirection','Y');
array = phased.HeterogeneousURA('ElementSet',{antenna1,antenna2}, ...
'ElementIndices',[1 2; 2 1]);
pos = getElementPosition(array)
pos = 3\times4

| 0 | 0 | 0 | 0 |
| ---: | ---: | ---: | ---: |
| -0.2500 | -0.2500 | 0.2500 | 0.2500 |
| 0.2500 | -0.2500 | 0.2500 | -0.2500 |

```

\section*{getNumElements}

System object: phased. HeterogeneousURA
Package: phased
Number of elements in array

\section*{Syntax}

N = getNumElements(H)

\section*{Description}
\(N=\) getNumElements(H) returns the number of elements, \(N\), in the HeterogeneousURA System object H .

\section*{Examples}

Find Number of Elements of Heterogeneous URA
Construct a Heterogeneous URA, and obtain the number of elements.
```

antenna1 = phased.ShortDipoleAntennaElement('FrequencyRange',[100e6 1e9], ...
'AxisDirection','Z');
antenna2 = phased.ShortDipoleAntennaElement('FrequencyRange',[100e6 1e9], ...
'AxisDirection','Y');
array = phased.HeterogeneousURA('ElementSet',{antenna1,antenna2}, ...
'ElementIndices',[1 2; 2 1]);
N = getNumElements(array)
N = 4

```

\section*{getTaper}

System object: phased. HeterogeneousURA
Package: phased
Array element tapers

\section*{Syntax}
wts = getTaper(h)

\section*{Description}
wts = getTaper(h) returns the tapers, wts, applied to each element of the phased heterogeneous uniform rectangular array (URA), h. Tapers are often referred to as weights.

\section*{Input Arguments}
h - Uniform rectangular array
phased. HeterogeneousURA System object
Uniform rectangular array specified as a phased. HeterogeneousURA System object.

\section*{Output Arguments}

\section*{wts - Array element tapers}
\(N\)-by-1 complex-valued vector
Array element tapers returned as an \(N\)-by-1, complex-valued vector. The dimension \(N\) is the number of elements in the array. The array tapers are returned in the same order as the element indices. The element indices of a URA run down each column, then to the top of the next column to the right.

\section*{Examples}

\section*{Heterogeneous URA Array Element Tapering}

Construct a 2-by-5 element heterogeneous URA with a Taylor window taper along each row. Then, show the array with the element taper shading.
```

antenna1 = phased.ShortDipoleAntennaElement('FrequencyRange',[100e6 1e9], ...
'AxisDirection','Z');
antenna2 = phased.ShortDipoleAntennaElement('FrequencyRange',[100e6 1e9], ...
'AxisDirection','Y');
array = phased.HeterogeneousURA('ElementSet',{antenna1,antenna2},...
'ElementIndices',[1 2 2 2 1 ; 1 2 2 2 1],...
'Taper',[taylorwin(5)';taylorwin(5)']);
w = getTaper(array)
w = 10\times1

```
0.5181
0.5181
1.2029
1.2029
1.5581
1.5581
1.2029
1.2029
0.5181
0.5181

\section*{isPolarizationCapable}

System object: phased. HeterogeneousURA
Package: phased
Polarization capability

\section*{Syntax}
flag = isPolarizationCapable(h)

\section*{Description}
flag = isPolarizationCapable(h) returns a Boolean value, flag, indicating whether the array supports polarization. An array supports polarization if all of its constituent sensor elements support polarization.

\section*{Input Arguments}

\section*{h - Uniform rectangular array}

Uniform rectangular array specified as phased.HeterogeneousURA System object.

\section*{Output Arguments}

\section*{flag - Polarization-capability flag}

Polarization-capability flag returned as a Boolean value true if the array supports polarization or false if it does not.

\section*{Examples}

\section*{Short-Dipole Antenna Array Polarization}

Show that an array of short-dipole antenna element supports polarization.
```

antennal = phased.ShortDipoleAntennaElement('FrequencyRange',[100e6 1e9], ...
'AxisDirection','Z');
antenna2 = phased.ShortDipoleAntennaElement('FrequencyRange',[100e6 1e9],...
'AxisDirection','Y');
array = phased.HeterogeneousURA('ElementSet',{antennal,antenna2}, ...
'ElementIndices',[1 2 2 2 1 ; 1 2 2 2 1]);
isPolarizationCapable(array)
ans = logical
1

```

\section*{pattern}

System object: phased. HeterogeneousURA
Package: phased
Plot heterogeneous URA directivity and power pattern

\section*{Syntax}
```

pattern(sArray,FREQ)
pattern(sArray,FREQ,AZ)
pattern(sArray,FREQ,AZ,EL)
pattern(__,Name,Value)
[PAT,AZ_ANG,EL_ANG] = pattern(

```
\(\qquad\)
``` )
```


## Description

pattern(sArray, FREQ) plots the 3-D array directivity pattern (in dBi ) for the array specified in sArray. The operating frequency is specified in FREQ.

The integration used when computing array directivity has a minimum sampling grid of 0.1 degrees. If an array pattern has a beamwidth smaller than this, the directivity value will be inaccurate.
pattern (sArray, FREQ,AZ) plots the array directivity pattern at the specified azimuth angle.
pattern(sArray, FREQ, AZ, EL) plots the array directivity pattern at specified azimuth and elevation angles.
pattern( $\qquad$ , Name, Value) plots the array pattern with additional options specified by one or more Name, Value pair arguments.
[PAT,AZ_ANG,EL_ANG] = pattern (__ ) returns the array pattern in PAT. The AZ_ANG output contains the coordinate values corresponding to the rows of PAT. The EL_ANG output contains the coordinate values corresponding to the columns of PAT. If the 'CoordinateSystem' parameter is set to 'uv' , then AZ_ANG contains the $U$ coordinates of the pattern and EL_ANG contains the $V$ coordinates of the pattern. Otherwise, they are in angular units in degrees. $\bar{U} V$ units are dimensionless.

Note This method replaces the plotResponse method. See "Convert plotResponse to pattern" on page 1-645 for guidelines on how to use pattern in place of plotResponse.

## Input Arguments

## sArray - Heterogeneous URA

System object
Heterogeneous conformal array, specified as a phased. HeterogeneousURA System object.
Example: sArray= phased. HeterogeneousURA;

## FREQ - Frequency for computing directivity and patterns

positive scalar | 1-by-L real-valued row vector
Frequencies for computing directivity and patterns, specified as a positive scalar or 1-by-L realvalued row vector. Frequency units are in hertz.

- For an antenna, microphone, or sonar hydrophone or projector element, FREQ must lie within the range of values specified by the FrequencyRange or FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased. CustomAntennaElement and phased.CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

```
Example: [1e8 2e6]
```

Data Types: double

## AZ - Azimuth angles

[-180:180] (default) | 1-by- $N$ real-valued row vector
Azimuth angles for computing directivity and pattern, specified as a 1-by- $N$ real-valued row vector where $N$ is the number of azimuth angles. Angle units are in degrees. Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the $x y$ plane. When measured from the $x$-axis toward the $y$-axis, this angle is positive.

## Example: [-45:2:45]

Data Types: double

## EL - Elevation angles

[-90:90] (default) | 1-by-M real-valued row vector
Elevation angles for computing directivity and pattern, specified as a 1-by-M real-valued row vector where $M$ is the number of desired elevation directions. Angle units are in degrees. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

The elevation angle is the angle between the direction vector and $x y$-plane. The elevation angle is positive when measured towards the $z$-axis.

Example: [-75:1:70]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

```
CoordinateSystem - Plotting coordinate system
'polar' (default)|'rectangular'|'uv'
```

Plotting coordinate system of the pattern, specified as the comma-separated pair consisting of 'CoordinateSystem' and one of 'polar', 'rectangular', or 'uv'. When
'CoordinateSystem' is set to 'polar' or 'rectangular', the AZ and EL arguments specify the pattern azimuth and elevation, respectively. AZ values must lie between $-180^{\circ}$ and $180^{\circ}$. EL values must lie between $-90^{\circ}$ and $90^{\circ}$. If 'CoordinateSystem' is set to ' uv ', AZ and EL then specify $U$ and $V$ coordinates, respectively. AZ and EL must lie between -1 and 1 .
Example: 'uv'
Data Types: char

## Type - Displayed pattern type

'directivity' (default)|'efield'|'power'|'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb' - power pattern converted to dB.

Example: 'powerdb'
Data Types: char

## Orientation - Array orientation

[0;0;0]. (default) | 3-by-1 real-valued column vector
Array orientation, specified as a 3-by-1 real-valued column vector containing the rotation angles with respect to the $x$-, $y$-, and $z$-axes of the local coordinate system, respectively.

## Normalize - Display normalize pattern

true (default) | false
Display normalized pattern, specified as the comma-separated pair consisting of 'Normalize' and a Boolean. Set this parameter to true to display a normalized pattern. This parameter does not apply when you set 'Type' to 'directivity'. Directivity patterns are already normalized.
Data Types: logical

## ShowArray - View array geometry

false (default) | true
View the array geometry along with the 3D radiation pattern, specified as false or true.
Data Types: logical
ShowLocalCoordinates - Show local coordinate axes
true (default) | false
Show the local coordinate axes, specified as true or false.
Data Types: logical

## ShowColorbar - Show colorbar

true (default) | false

Show the colorbar, specified as true or false.

## Data Types: logical

## Parent - Handle to axis

scalar
Handle to the axes along which the array geometry is displayed specified as a scalar.

## PlotStyle - Plotting style

'overlay' (default)|'waterfall'
Plotting style, specified as the comma-separated pair consisting of 'Plotstyle' and either 'overlay' or 'waterfall'. This parameter applies when you specify multiple frequencies in FREQ in 2-D plots. You can draw 2-D plots by setting one of the arguments AZ or EL to a scalar.

## Data Types: char

## Polarization - Polarized field component

```
'combined' (default)| 'H' | 'V'
```

Polarized field component to display, specified as the comma-separated pair consisting of 'Polarization' and 'combined', 'H', or 'V'. This parameter applies only when the sensors are polarization-capable and when the 'Type' parameter is not set to 'directivity'. This table shows the meaning of the display options.

| 'Polarization ' | Display |
| :--- | :--- |
| 'combined ' | Combined $H$ and $V$ polarization components |
| ' $\mathrm{H}^{\prime}$ | $H$ polarization component |
| ' $\mathrm{V}^{\prime}$ | $V$ polarization component |

Example: 'V '

## Data Types: char

## PropagationSpeed - Signal propagation speed

speed of light (default) | positive scalar
Signal propagation speed, specified as the comma-separated pair consisting of
' PropagationSpeed ' and a positive scalar in meters per second.
Example: 'PropagationSpeed', physconst('LightSpeed')
Data Types: double

## Weights - Array weights

1 (default) | $N$-by-1 complex-valued column vector | $N$-by-L complex-valued matrix
Array weights, specified as the comma-separated pair consisting of 'Weights' and an N -by-1 complex-valued column vector or $N$-by- $L$ complex-valued matrix. Array weights are applied to the elements of the array to produce array steering, tapering, or both. The dimension $N$ is the number of elements in the array. The dimension $L$ is the number of frequencies specified by FREQ.

| Weights Dimension | FREQ Dimension | Purpose |
| :--- | :--- | :--- |
| $N$-by-1 complex-valued column <br> vector | Scalar or 1-by- $L$ row vector | Applies a set of weights for the <br> single frequency or for all $L$ <br> frequencies. |
| $N$-by- $L$ complex-valued matrix | 1-by- $L$ row vector | Applies each of the $L$ columns of <br> 'Weights ' for the <br> corresponding frequency in <br> FREQ. |

Note Use complex weights to steer the array response toward different directions. You can create weights using the phased. SteeringVector System object or you can compute your own weights. In general, you apply Hermitian conjugation before using weights in any Phased Array System Toolbox function or System object such as phased. Radiator or phased. Collector. However, for the directivity, pattern, patternAzimuth, and patternElevation methods of any array System object use the steering vector without conjugation.

Example: 'Weights', ones ( $\mathrm{N}, \mathrm{M}$ )
Data Types: double
Complex Number Support: Yes

## Output Arguments

## PAT - Array pattern

$M$-by- $N$ real-valued matrix
Array pattern, returned as an $M$-by- $N$ real-valued matrix. The dimensions of PAT correspond to the dimensions of the output arguments AZ_ANG and EL_ANG.

## AZ_ANG - Azimuth angles

scalar | 1-by- $N$ real-valued row vector
Azimuth angles for displaying directivity or response pattern, returned as a scalar or 1-by- $N$ realvalued row vector corresponding to the dimension set in AZ. The columns of PAT correspond to the values in AZ_ANG. Units are in degrees.

## EL_ANG - Elevation angles

scalar | 1-by-M real-valued row vector
Elevation angles for displaying directivity or response, returned as a scalar or 1-by-M real-valued row vector corresponding to the dimension set in EL. The rows of PAT correspond to the values in EL_ANG. Units are in degrees.

## Examples

## Azimuth Pattern and Directivity of Heterogeneous URA

Construct a 3-by-3 heterogeneous URA of short-dipole antenna elements with a rectangular lattice. Then, plot the array's azimuth pattern at 300 MHz .

```
sElement1 = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[2e8 5e8],...
    'AxisDirection','Z');
sElement2 = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[2e8 5e8],...
    'AxisDirection','Y');
sArray = phased.HeterogeneousURA(...
    'ElementSet',{sElement1,sElement2},...
    'ElementIndices',[1 1 1; 2 2 2; 1 1 1]);
fc = 300e6;
c = physconst('LightSpeed');
pattern(sArray,fc,[-180:180],0,...
    'PropagationSpeed',c,...
    'CoordinateSystem','rectangular',...
    'Type','powerdb',...
    'Normalize',true,...
    'Polarization','combined')
```



Plot the same result in polar form.

```
pattern(sArray,fc,[-180:180],0,...
    'PropagationSpeed',c,...
    'CoordinateSystem','polar',...
    'Type','powerdb',...
    'Normalize',true,...
    'Polarization','combined')
```



Normalized Power (dB), Broadside at $0.00^{\circ}$

Finally, plot the directivity.

```
pattern(sArray,fc,[-180:180],0,...
    'PropagationSpeed',c,...
    'CoordinateSystem','rectangular',...
    'Type','directivity')
```



## Azimuth Pattern of Heterogeneous URA for Two Sets of Weights

Construct a square 3-by-3 heterogeneous URA composed of 9 short-dipole antenna elements with different orientations. Plot the array azimuth pattern from -45 degrees to 45 degrees in 0.1 degree increments. The Weights parameter lets you display the array pattern simultaneously for different sets of weights: in this case a uniform set of weights and a tapered set.

```
sElement1 = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[2e8 5e8],...
    'AxisDirection','Z');
sElement2 = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[2e8 5e8],...
    'AxisDirection','Y');
sArray = phased.HeterogeneousURA(...
    'ElementSet',{sElement1,sElement2},...
    'ElementIndices',[1 1 1; 2 2 2; 1 1 1]);
fc = [3e8];
c = physconst('LightSpeed');
wts1 = ones(9,1)/9;
wts2 = [.7,.7,.7,.7,1,.7,.7,.7,.7]';
wts2 = wts2/sum(wts2);
pattern(sArray,fc,[-45:0.1:45],0,...
    'PropagationSpeed',c,...
    'CoordinateSystem','rectangular',...
```

```
'Type','powerdb',...
'Weights',[wts1,wts2],...
'Polarization','combined')
```



## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\text {rad }}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Convert plotResponse to pattern

For antenna, microphone, and array System objects, the pattern method replaces the plotResponse method. In addition, two new simplified methods exist just to draw 2-D azimuth and elevation pattern plots. These methods are azimuthPattern and elevationPattern.

The following table is a guide for converting your code from using plotResponse to pattern. Notice that some of the inputs have changed from input arguments to Name-Value pairs and conversely. The general pattern method syntax is
pattern(H,FREQ,AZ,EL, 'Name1', 'Value1',...,' NameN', 'ValueN')

| plotResponse Inputs | plotResponse Description | pattern Inputs |
| :--- | :--- | :--- |
| H argument | Antenna, microphone, or array <br> System object. | H argument (no change) |
| FREQ argument | Operating frequency. | FREQ argument (no change) |
| V argument | Propagation speed. This argument <br> is used only for arrays. | 'PropagationSpeed ' name-value <br> pair. This parameter is only used for <br> arrays. |


| plotResponse Inputs | plotResponse Description |  | pattern Inputs |  |
| :---: | :---: | :---: | :---: | :---: |
| 'Format' and 'RespCut' namevalue pairs | These options work together to let you create a plot in angle space (line or polar style) or $U V$ space. They also determine whether the plot is 2-D or 3-D. This table shows you how to create different types of plots using plotResponse. |  | 'CoordinateSystem' name-value pair used together with the AZ and EL input arguments. <br> 'CoordinateSystem' has the same options as the plotResponse method 'Format ' name-value pair, except that 'line' is now named 'rectangular'. The table shows how to create different types of plots using pattern. |  |
|  | Display space |  |  |  |
|  | Angle space (2D) |  |  |  |
|  |  | Set 'RespCut'to 'Az' or'El'. Set'Format' to'line' or'polar'.Set the displayaxis using eitherthe'AzimuthAngleS' or'ElevationAngles' name-value pairs. | Display space |  |
|  |  |  | Angle space (2D) <br> Angle space (3D) | Set <br> 'Coordinate <br> System' to rectangular' or 'polar'. <br> Specify either AZ or EL as a scalar. |
|  |  |  |  | Set <br> 'Coordinate <br> System' to 'rectangular' |
|  | Angle space (3D) | Set 'RespCut' to '3D'. Set 'Format' to ' line' or 'polar'. <br> Set the display axis using both the 'AzimuthAngle ${ }^{\prime}$ and 'Elevation Angles ' namevalue pairs. |  | or 'polar'. <br> Specify both AZ and EL as vectors. |
|  |  |  | UV space (2D) | Set <br> 'Coordinate <br> System' to 'uv'. Use AZ to specify a $U$ space vector. Use EL to specify a $V$-space scalar. |
|  |  |  | UV space (3D) | Set |
|  | UV space (2D) | Set 'RespCut' to'U'. Set 'Format' to 'UV '. Set the display range using the 'UGrid' namevalue pair. |  | System' to 'uv'. Use AZ to specify a $U$ space vector. <br> Use EL to specify a $V$-space vector. |
|  |  |  | If you set CoordinateSystem to 'uv', enter the UV grid values using AZ and EL . |  |
|  | UV space (3D) | $\begin{aligned} & \text { Set 'RespCut' } \\ & \text { to'3D'. Set } \\ & \text { 'Format' to } \end{aligned}$ |  |  |


| plotResponse Inputs | plotResponse Description |  | pattern Inputs |
| :---: | :---: | :---: | :---: |
|  | Display space |  |  |
|  |  | 'UV'. Set the display range using both the 'UGrid' and 'VGrid' namevalue pairs. |  |
| 'CutAngle' name-value pair | Constant angle at to take an azimuth or elevation cut. When producing a 2-D plot and when 'RespCut' is set to 'Az' or 'El', use 'CutAngle' to set the slice across which to view the plot. |  | No equivalent name-value pair. To create a cut, specify either AZ or EL as a scalar, not a vector. |
| 'NormalizeResponse' namevalue pair | Normalizes the plot. When 'Unit' is set to 'dbi', you cannot specify 'NormalizeResponse'. |  | Use the 'Normalize' name-value pair. When 'Type' is set to 'directivity' you cannot specify 'Normalize'. |
| 'OverlayFreq' name-value pair | Plot multiple frequencies on the same 2-D plot. Available only when 'Format' is set to 'line' or 'uv' and 'RespCut' is not set to '3D'. The value true produces an overlay plot and the value false produces a waterfall plot. |  | 'PlotStyle' name-value pair plots multiple frequencies on the same 2-D plot. <br> The values 'overlay' and 'waterfall' correspond to 'OverlayFreq' values of true and false. The option 'waterfall' is allowed only when 'CoordinateSystem' is set to 'rectangular' or 'uv'. |
| 'Polarization' name-value pair | Determines how to plot polarized fields. Options are 'None', 'Combined', 'H', or 'V'. |  | 'Polarization' name-value pair determines how to plot polarized fields. The 'None ' option is removed. The options 'Combined ', 'H', or 'V' are unchanged. |
| 'Unit ' name-value pair | Determines the plot units. Choose 'db', 'mag', 'pow', or 'dbi', where the default is ' db '. |  | 'Type ' name-value pair, uses equivalent options with different names |
|  |  |  | plotResponse pattern |
|  |  |  | 'db' 'powerdb' <br> 'mag' 'efield' <br> 'pow' 'power' <br> 'dbi' 'directivity' |
| 'Weights ' name-value pair | Array element tapers (or weights). |  | 'Weights ' name-value pair (no change). |
| 'AzimuthAngles ' name-value pair | Azimuth angles used to display the antenna or array response. |  | AZ argument |


| plotResponse Inputs | plotResponse Description | pattern Inputs |
| :--- | :--- | :--- |
| 'ElevationAngles ' name-value <br> pair | Elevation angles used to display the <br> antenna or array response. | EL argument |
| 'UGrid' name-value pair | Contains $U$ coordinates in $U V$ - <br> space. | AZ argument when <br> 'CoordinateSystem ' name-value <br> pair is set to ' uv ' |
| 'VGrid' name-value pair | Contains V-coordinates in $U V$-space. | EL argument when <br> 'CoordinateSystem ' name-value <br> pair is set to 'uv ' |

## Version History <br> Introduced in R2015a

See Also<br>patternAzimuth | patternElevation

## patternAzimuth

System object: phased. HeterogeneousURA
Package: phased
Plot heterogeneous URA directivity or pattern versus azimuth

## Syntax

```
patternAzimuth(sArray,FREQ)
patternAzimuth(sArray,FREQ,EL)
patternAzimuth(sArray,FREQ,EL,Name,Value)
PAT = patternAzimuth(
```

$\qquad$

``` )
```


## Description

patternAzimuth (sArray, FREQ) plots the 2-D array directivity pattern versus azimuth (in dBi) for the array sArray at zero degrees elevation angle. The argument FREQ specifies the operating frequency.

The integration used when computing array directivity has a minimum sampling grid of 0.1 degrees. If an array pattern has a beamwidth smaller than this, the directivity value will be inaccurate.
patternAzimuth(sArray, FREQ,EL), in addition, plots the 2-D array directivity pattern versus azimuth (in dBi) for the array sArray at the elevation angle specified by $E L$. When $E L$ is a vector, multiple overlaid plots are created.
patternAzimuth(sArray, FREQ,EL,Name, Value) plots the array pattern with additional options specified by one or more Name, Value pair arguments.

PAT = patternAzimuth ( _ _ ) returns the array pattern. PAT is a matrix whose entries represent the pattern at corresponding sampling points specified by the 'Azimuth ' parameter and the EL input argument.

## Input Arguments

## sArray - Heterogeneous URA

System object
Heterogeneous URA, specified as a phased. HeterogeneousURA System object.

```
Example: sArray= phased.HeterogeneousURA;
```


## FREQ - Frequency for computing directivity and pattern

positive scalar
Frequency for computing directivity and pattern, specified as a positive scalar. Frequency units are in hertz.

- For an antenna or microphone element, FREQ must lie within the range of values specified by the FrequencyRange or the FrequencyVector property of the element. Otherwise, the element
produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased.CustomMic rophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: 1e8
Data Types: double

## EL - Elevation angles

1 -by- $N$ real-valued row vector
Elevation angles for computing sensor or array directivities and patterns, specified as a 1-by- $N$ realvalued row vector. The quantity $N$ is the number of requested elevation directions. Angle units are in degrees. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

The elevation angle is the angle between the direction vector and the $x y$ plane. When measured toward the $z$-axis, this angle is positive.
Example: [0, 10, 20]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Type - Displayed pattern type

'directivity' (default)|'efield'|'power'|'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb' - power pattern converted to dB.

Example: 'powerdb'
Data Types: char

## PropagationSpeed - Signal propagation speed

## speed of light (default) | positive scalar

Signal propagation speed, specified as the comma-separated pair consisting of ' PropagationSpeed ' and a positive scalar in meters per second.
Example: 'PropagationSpeed', physconst('LightSpeed')
Data Types: double

## Weights - Array weights

M-by-1 complex-valued column vector
Array weights, specified as the comma-separated pair consisting of 'Weights' and an $M$-by-1 complex-valued column vector. Array weights are applied to the elements of the array to produce array steering, tapering, or both. The dimension $M$ is the number of elements in the array.

Note Use complex weights to steer the array response toward different directions. You can create weights using the phased. SteeringVector System object or you can compute your own weights. In general, you apply Hermitian conjugation before using weights in any Phased Array System Toolbox function or System object such as phased. Radiator or phased. Collector. However, for the directivity, pattern, patternAzimuth, and patternElevation methods of any array System object use the steering vector without conjugation.

Example: 'Weights', ones (10,1)
Data Types: double
Complex Number Support: Yes

## Azimuth - Azimuth angles

[-180:180] (default) | 1-by-P real-valued row vector
Azimuth angles, specified as the comma-separated pair consisting of 'Azimuth' and a 1-by-P realvalued row vector. Azimuth angles define where the array pattern is calculated.
Example: 'Azimuth', [-90:2:90]
Data Types: double

## Parent - Handle to axis

scalar
Handle to the axes along which the array geometry is displayed specified as a scalar.

## Output Arguments

## PAT - Array directivity or pattern

$L$-by- $N$ real-valued matrix
Array directivity or pattern, returned as an $L$-by- $N$ real-valued matrix. The dimension $L$ is the number of azimuth values determined by the 'Azimuth' name-value pair argument. The dimension $N$ is the number of elevation angles, as determined by the EL input argument.

## Examples

## Azimuth Directivity of Heterogeneous URA

Construct a square 4-by-4 heterogeneous URA composed of a mix of crossed-dipole and short-dipole antenna elements with short dipoles in the center. Plot the array azimuth directivity for two different elevation angles. Set the operating frequency to 400 MHz .

```
sElement1 = phased.CrossedDipoleAntennaElement(...
    'FrequencyRange',[200e6 500e6]);
```

```
sElement2 = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[200e6 500e6],...
    'AxisDirection','Z');
elemindices = ones(4,4);
elemindices(2:3,2:3) = 2;
sArray = phased.HeterogeneousURA(...
    'ElementSet',{sElement1,sElement2},...
    'ElementIndices',elemindices);
fc = 400e6;
c = physconst('LightSpeed');
patternAzimuth(sArray,fc,[0 30],...
    'PropagationSpeed',c,...
    'Type','directivity')
```



Directivity (dBi), Broadside at $0.00^{\circ}$

## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \Pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Version History

Introduced in R2015a

## See Also

pattern| patternElevation

## patternElevation

System object: phased. HeterogeneousURA
Package: phased
Plot heterogeneous ULA directivity or pattern versus elevation

## Syntax

```
patternElevation(sArray,FREQ)
patternElevation(sArray,FREQ,AZ)
patternElevation(sArray,FREQ,AZ,Name,Value)
PAT = patternElevation(
```

$\qquad$

``` )
```


## Description

patternElevation(sArray, FREQ) plots the 2-D array directivity pattern versus elevation (in dBi ) for the array sArray at zero degrees azimuth angle. When AZ is a vector, multiple overlaid plots are created. The argument FREQ specifies the operating frequency.

The integration used when computing array directivity has a minimum sampling grid of 0.1 degrees. If an array pattern has a beamwidth smaller than this, the directivity value will be inaccurate.
patternElevation(sArray, FREQ, AZ), in addition, plots the 2-D element directivity pattern versus elevation (in dBi ) at the azimuth angle specified by $A Z$. When $A Z$ is a vector, multiple overlaid plots are created.
patternElevation(sArray,FREQ,AZ,Name, Value) plots the array pattern with additional options specified by one or more Name, Value pair arguments.

PAT = patternElevation ( _ ) returns the array pattern. PAT is a matrix whose entries represent the pattern at corresponding sampling points specified by the 'Elevation' parameter and the AZ input argument.

## Input Arguments

## sArray - Heterogeneous URA

System object
Heterogeneous URA array, specified as a phased. HeterogeneousURA System object.
Example: sArray= phased.HeterogeneousURA;
FREQ - Frequency for computing directivity and pattern
positive scalar
Frequency for computing directivity and pattern, specified as a positive scalar. Frequency units are in hertz.

- For an antenna or microphone element, FREQ must lie within the range of values specified by the FrequencyRange or the FrequencyVector property of the element. Otherwise, the element
produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased.CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: 1e8
Data Types: double

## AZ - Azimuth angles for computing directivity and pattern

1-by- $N$ real-valued row vector
Azimuth angles for computing sensor or array directivities and patterns, specified as a 1 -by- $N$ realvalued row vector where $N$ is the number of desired azimuth directions. Angle units are in degrees. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the $x y$ plane. This angle is positive when measured from the $x$-axis toward the $y$-axis.
Example: [0,10,20]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Type - Displayed pattern type

'directivity' (default)|'efield'|'power'|'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb' - power pattern converted to dB.

Example: 'powerdb'
Data Types: char

## PropagationSpeed - Signal propagation speed

speed of light (default) | positive scalar
Signal propagation speed, specified as the comma-separated pair consisting of ' PropagationSpeed ' and a positive scalar in meters per second.
Example: 'PropagationSpeed', physconst('LightSpeed')
Data Types: double

## Weights - Array weights

M-by-1 complex-valued column vector
Array weights, specified as the comma-separated pair consisting of 'Weights' and an $M$-by-1 complex-valued column vector. Array weights are applied to the elements of the array to produce array steering, tapering, or both. The dimension $M$ is the number of elements in the array.
$\overline{\text { Note Use complex weights to steer the array response toward different directions. You can create }}$ weights using the phased. SteeringVector System object or you can compute your own weights. In general, you apply Hermitian conjugation before using weights in any Phased Array System Toolbox function or System object such as phased.Radiator or phased. Collector. However, for the directivity, pattern, patternAzimuth, and patternElevation methods of any array System object use the steering vector without conjugation.

Example: 'Weights', ones (10,1)
Data Types: double
Complex Number Support: Yes

## Elevation - Elevation angles

[-90:90] (default) | 1-by-P real-valued row vector
Elevation angles, specified as the comma-separated pair consisting of 'Elevation' and a 1-by-P real-valued row vector. Elevation angles define where the array pattern is calculated.
Example: 'Elevation', [-90:2:90]
Data Types: double

## Parent - Handle to axis

scalar
Handle to the axes along which the array geometry is displayed specified as a scalar.

## Output Arguments

## PAT - Array directivity or pattern

L-by- $N$ real-valued matrix

Array directivity or pattern, returned as an $L$-by- $N$ real-valued matrix. The dimension $L$ is the number of elevation angles determined by the 'Elevation' name-value pair argument. The dimension $N$ is the number of azimuth angles determined by the AZ argument.

## Examples

## Elevation Directivity of Heterogeneous URA

Construct a square 4-by-4 heterogeneous URA composed of a mix of crossed-dipole and short-dipole antenna elements with short dipoles in the center. Plot the array elevation directivity for two different azimuth angles. Set the operating frequency to 400 MHz .

```
sElement1 = phased.CrossedDipoleAntennaElement(...
    'FrequencyRange',[200e6 500e6]);
```

```
sElement2 = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[200e6 500e6],...
    'AxisDirection','Z');
elemindices = ones(4,4);
elemindices(2:3,2:3) = 2;
sArray = phased.HeterogeneousURA(...
    'ElementSet',{sElement1,sElement2},...
    'ElementIndices',elemindices);
fc = 400e6;
c = physconst('LightSpeed');
patternElevation(sArray,fc,[0 75],...
    'PropagationSpeed',c,...
    'Type','directivity')
```



Directivity (dBi), Broadside at $0.00^{\circ}$

## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \Pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\mathrm{total}}}
$$

where $U_{\text {rad }}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Version History

Introduced in R2015a

## See Also

pattern| patternAzimuth

## plotResponse

System object: phased. HeterogeneousURA
Package: phased
Plot response pattern of array

## Syntax

plotResponse(H, FREQ, V)
plotResponse(H, FREQ, V, Name, Value)
hPlot = plotResponse( $\qquad$ )

## Description

plotResponse ( $\mathrm{H}, \mathrm{FREQ}, \mathrm{V}$ ) plots the array response pattern along the azimuth cut, where the elevation angle is 0 . The operating frequency is specified in FREQ. The propagation speed is specified in $V$.
plotResponse(H, FREQ, V,Name, Value) plots the array response with additional options specified by one or more Name, Value pair arguments.
hPlot = plotResponse( $\qquad$ ) returns handles of the lines or surface in the figure window, using any of the input arguments in the previous syntaxes.

## Input Arguments

## H

Array object

## FREQ

Operating frequency in Hertz specified as a scalar or 1-by-K row vector. Values must lie within the range specified by a property of H . That property is named FrequencyRange or FrequencyVector, depending on the type of element in the array. The element has no response at frequencies outside that range. If you set the 'RespCut ' property of $H$ to ' $3 D^{\prime}$ ' FREQ must be a scalar. When FREQ is a row vector, plotResponse draws multiple frequency responses on the same axes.

## V

Propagation speed in meters per second.

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## CutAngle

Cut angle as a scalar. This argument is applicable only when RespCut is ' Az ' or ' El '. If RespCut is 'Az' , CutAngle must be between -90 and 90. If RespCut is 'El', CutAngle must be between -180 and 180.

Default: 0

## Format

Format of the plot, using one of 'Line', 'Polar', or 'UV '. If you set Format to 'UV ', FREQ must be a scalar.

Default: 'Line'

## NormalizeResponse

Set this value to true to normalize the response pattern. Set this value to false to plot the response pattern without normalizing it. This parameter is not applicable when you set the Unit parameter value to 'dbi'.

## Default: true

## OverlayFreq

Set this value to true to overlay pattern cuts in a 2-D line plot. Set this value to false to plot pattern cuts against frequency in a 3-D waterfall plot. If this value is false, FREQ must be a vector with at least two entries.

This parameter applies only when Format is not 'Polar' and RespCut is not '3D '.

## Default: true

## Polarization

Specify the polarization options for plotting the array response pattern. The allowable values are |'None' | 'Combined' | 'H' | 'V' | where

- 'None' specifies plotting a nonpolarized response pattern
- 'Combined ' specifies plotting a combined polarization response pattern
- 'H' specifies plotting the horizontal polarization response pattern
- 'V ' specifies plotting the vertical polarization response pattern

For arrays that do not support polarization, the only allowed value is 'None '. This parameter is not applicable when you set the Unit parameter value to ' dbi ' .

Default: 'None'

## RespCut

Cut of the response. Valid values depend on Format, as follows:

- If Format is 'Line' or 'Polar', the valid values of RespCut are 'Az', 'El', and '3D'. The default is ' Az '.
- If Format is 'UV', the valid values of RespCut are 'U' and '3D'. The default is 'U'.

If you set RespCut to ' 3D' , FREQ must be a scalar.

## Unit

The unit of the plot. Valid values are 'db', 'mag', 'pow', or 'dbi'. This parameter determines the type of plot that is produced.

| Unit value | Plot type |
| :--- | :--- |
| db | power pattern in dB scale |
| mag | field pattern |
| pow | power pattern |
| dbi | directivity |

Default: 'db'

## Weights

Weight values applied to the array, specified as a length- $N$ column vector or $N$-by- $M$ matrix. The dimension $N$ is the number of elements in the array. The interpretation of $M$ depends upon whether the input argument FREQ is a scalar or row vector.

| Weights Dimensions | FREQ Dimension | Purpose |
| :--- | :--- | :--- |
| $N$-by-1 column vector | Scalar or 1-by- $M$ row vector | Apply one set of weights for the <br> same single frequency or all $M$ <br> frequencies. |
| $N$-by- $M$ matrix | Scalar | Apply all of the $M$ different <br> columns in Weights for the <br> same single frequency. |
|  |  | Apply each of the $M$ different <br> columns in Weights for the <br> corresponding frequency in <br> FREQ. |
|  |  |  |

## AzimuthAngles

Azimuth angles for plotting array response, specified as a row vector. The AzimuthAngles parameter sets the display range and resolution of azimuth angles for visualizing the radiation pattern. This parameter is allowed only when the RespCut parameter is set to 'Az' or '3D' and the Format parameter is set to 'Line' or 'Polar'. The values of azimuth angles should lie between $180^{\circ}$ and $180^{\circ}$ and must be in nondecreasing order. When you set the RespCut parameter to ' 3 D ', you can set the AzimuthAngles and ElevationAngles parameters simultaneously.

Default: [-180:180]

## ElevationAngles

Elevation angles for plotting array response, specified as a row vector. The ElevationAngles parameter sets the display range and resolution of elevation angles for visualizing the radiation pattern. This parameter is allowed only when the RespCut parameter is set to ' El ' or ' 3 D ' and the

Format parameter is set to 'Line' or 'Polar'. The values of elevation angles should lie between $90^{\circ}$ and $90^{\circ}$ and must be in nondecreasing order. When yous set the RespCut parameter to ' $3 \mathrm{D}^{\prime}$, you can set the ElevationAngles and AzimuthAngles parameters simultaneously.

Default: [-90:90]
UGrid
$U$ coordinate values for plotting array response, specified as a row vector. The UGrid parameter sets the display range and resolution of the $U$ coordinates for visualizing the radiation pattern in $U / V$ space. This parameter is allowed only when the Format parameter is set to 'UV' and the RespCut parameter is set to ' $U$ ' or ' $3 D$ '. The values of UGrid should be between -1 and 1 and should be specified in nondecreasing order. You can set the UGrid and VGrid parameters simultaneously.

Default: [-1:0.01:1]

## VGrid

$V$ coordinate values for plotting array response, specified as a row vector. The VGrid parameter sets the display range and resolution of the $V$ coordinates for visualizing the radiation pattern in $U / V$ space. This parameter is allowed only when the Format parameter is set to 'UV' and the RespCut parameter is set to ' $3 D^{\prime}$ '. The values of VGrid should be between -1 and 1 and should be specified in nondecreasing order. You can set VGrid and UGrid parameters simultaneously.

Default: [-1:0.01:1]

## Examples

## Azimuth Response and Directivity of Heterogeneous URA

Construct a 3-by-3 heterogeneous URA with a rectangular lattice, then plot the array's azimuth response at 300 MHz .

```
sElementl = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[2e8 5e8],...
    'AxisDirection','Z');
sElement2 = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[2e8 5e8],...
    'AxisDirection','Y');
sArray = phased.HeterogeneousURA(...
    'ElementSet',{sElement1,sElement2},...
    'ElementIndices',[1 1 1; 2 2 2; 1 1 1]);
fc = [3e8];
c = physconst('LightSpeed');
plotResponse(sArray,fc,c);
```



Plot the same result in polar form.
plotResponse(sArray,fc,c,'RespCut','Az','Format','Polar');


Normalized Power (dB), Broadside at $0.00^{\circ}$
Finally, plot the directivity.
plotResponse(sArray,fc, c,'RespCut','Az','Unit','dbi');


## Azimuth Responses of a Heterogeneous URA For Two Sets of Weights

Construct a square 3-by-3 heterogeneous URA composed of 9 short-dipole antenna elements with different orientations. Using the AzimuthAngles parameter, plot the array's azimuth response in the -45 degrees to 45 degrees in 0.1 degree increments. The Weights parameter lets you display the array's response simultaneously for different sets of weights: in this case a uniform set of weights and a tapered set.

```
sElement1 = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[2e8 5e8],...
    'AxisDirection','Z');
sElement2 = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[2e8 5e8],...
    'AxisDirection','Y');
sArray = phased.HeterogeneousURA(...
    'ElementSet',{sElement1,sElement2},...
    'ElementIndices',[1 1 1; 2 2 2; 1 1 1]);
fc = [3e8];
c = physconst('LightSpeed');
wts1 = ones(9,1)/9;
wts2 = [.7,.7,.7,.7,1,.7,.7,.7,.7]';
wts2 = wts2/sum(wts2);
plotResponse(sArray,fc,c,'RespCut','Az',...
    'Format','Line',...
```

```
'AzimuthAngles',[-45:0.1:45],...
'Weights',[wts1,wts2],'Unit','db');
```



## See Also

uv2azel|azel2uv

## step

System object: phased. HeterogeneousURA
Package: phased
Output responses of array elements

## Syntax

RESP = step(H,FREQ,ANG)

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step (obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.

RESP $=$ step ( $H$, FREQ , ANG) returns the array elements' responses RESP at operating frequencies specified in FREQ and directions specified in ANG.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## H

Array object

## FREQ

Operating frequencies of array in hertz. FREQ is a row vector of length $L$. Typical values are within the range specified by a property of H . Element. That property is named FrequencyRange or FrequencyVector, depending on the type of element in the array. The element has zero response at frequencies outside that range.

## ANG

Directions in degrees. ANG is either a 2 -by- $M$ matrix or a row vector of length $M$.
If ANG is a 2-by-M matrix, each column of the matrix specifies the direction in the form [azimuth; elevation]. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive.

If ANG is a row vector of length $M$, each element specifies the azimuth angle of the direction. In this case, the corresponding elevation angle is assumed to be $0^{\circ}$.

## Output Arguments

## RESP

Voltage responses of the phased array. The output depends on whether the array supports polarization or not.

- If the array is not capable of supporting polarization, the voltage response, RESP, has the dimensions $N$-by- $M$-by-L. $N$ is the number of elements in the array. The dimension $M$ is the number of angles specified in ANG. $L$ is the number of frequencies specified in FREQ. For any element, the columns of RESP contain the responses of the array elements for the corresponding direction specified in ANG. Each of the $L$ pages of RESP contains the responses of the array elements for the corresponding frequency specified in FREQ.
- If the array is capable of supporting polarization, the voltage response, RESP, is a MATLAB struct containing two fields, RESP.H and RESP.V. The field, RESP.H, represents the array's horizontal polarization response, while RESP. V represents the array's vertical polarization response. Each field has the dimensions $N$-by-M-by-L. $N$ is the number of elements in the array, and $M$ is the number of angles specified in ANG. $L$ is the number of frequencies specified in FREQ. Each column of RESP contains the responses of the array elements for the corresponding direction specified in ANG. Each of the $L$ pages of RESP contains the responses of the array elements for the corresponding frequency specified in FREQ.


## Examples

## Response of 2-by-2 Heterogeneous URA of Cosine Antennas

Construct a 2-by-2 rectangular lattice heterogeneous URA of cosine antenna elements. Find the response of each element at 30 degrees azimuth and 0 degrees elevation. Assume the operating frequency is 1 GHz . Then, plot the array directivity.

```
sElement1 = phased.CosineAntennaElement('CosinePower',1.5);
sElement2 = phased.CosineAntennaElement('CosinePower',1.8);
sArray = phased.HeterogeneousURA(...
    'ElementSet',{sElement1,sElement2},...
    'ElementIndices',[1 2; 2 1]);
fc = 1e9;
c = physconst('LightSpeed');
ang = [30;0];
resp = step(sArray,fc,ang)
resp = 4×1
    0.8059
    0.7719
    0.7719
    0.8059
```

Show the 3-D directivity pattern.
pattern(sArray,fc,[-180:180], [-90:90],...
'PropagationSpeed ', c, ...
'CoordinateSystem', 'rectangular', ...
'Type','directivity')


## See Also

uv2azel | phitheta2azel

## viewArray

System object: phased. HeterogeneousURA
Package: phased
View array geometry

## Syntax

```
viewArray(H)
viewArray(H,Name,Value)
hPlot = viewArray(
```

$\qquad$

``` )
```


## Description

viewArray (H) plots the geometry of the array specified in H .
viewArray ( $\mathrm{H}, \mathrm{Name}$, Value) plots the geometry of the array, with additional options specified by one or more Name, Value pair arguments.
hPlot = viewArray( $\qquad$ ) returns the handle of the array elements in the figure window. All input arguments described for the previous syntaxes also apply here.

## Input Arguments

## H

Array object.

## Name-Value Pair Arguments

Specify optional pairs of arguments as Namel=Value1, . . . ,NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Parent

Handle to the axes along which the array geometry is displayed.

## ShowNormals

Set this value to true to show the normal directions of all elements of the array. Set this value to false to plot the elements without showing normal directions.

Default: false

## ShowLocalCoordinates

Logical flag specifying whether to show the local coordinate axes.

Default: true

## ShowAnnotation

Logical flag specifying whether to show the annotations in the UI panel of the figure. Annotation shows aperture size and element spacing based on array axis of array.

Default: true

## Orientation

Orientation of the array, specified as a 3-by-1 column vector containing the rotation angles with respect to the $x-, y$-, and $z$-axes of the local coordinate system, respectively. The default value is [0;0;0].

Default: [0;0;0]

## ShowTaper

Set this value to true to specify whether to change the element color brightness in proportion to the element taper magnitude. When this value is set to false, all elements are drawn with the same color.

Default: false

## ShowIndex

Vector specifying the element indices to show in the figure. Each number in the vector must be an integer between 1 and the number of elements. You can also specify the value 'All ' to show the indices of all elements of the array or 'None' to suppress indices.

Default: 'None'

## Title

Character vector specifying the title of the plot.
Default: 'Array Geometry'

## Output Arguments

hPlot
Handle of array elements in figure window.

## Examples

## Geometry, Normal Directions, and Indices of Heterogeneous URA Elements

Display the element positions, normal directions, and indices for all elements of a 4-by-4 heterogeneous URA.

```
sElement1 = phased.CosineAntennaElement('CosinePower',1.5);
sElement2 = phased.CosineAntennaElement('CosinePower',1.8);
```

sArray = phased. HeterogeneousURA(...
'ElementSet', \{sElement1,sElement2\},...
'ElementIndices',[1111; $1221 ; 1221 ; 1111]) ;$
viewArray(sArray,'ShowIndex','all','ShowNormal',true);

## Array Geometry



## See Also

phased.ArrayResponse

## Topics

Phased Array Gallery

## phased.IntensityScope

Package: phased
Range-time-intensity (RTI) or Doppler-time-intensity (DTI) display

## Description

The phased. IntensityScope System object creates an intensity scope for viewing range-timeintensity (RTI) or Doppler-time-intensity (DTI) data. An intensity scope is a scrolling waterfall of intensity values as a function of time. Scan lines appear at the bottom of the display window and scroll off at the top. Each scan line represents signal intensity as a function of a parameter of interest, such as range or speed. You can also use this object to display angle-time-intensity data and spectral data. This figure shows an RTI display.


To create an intensity scope:
1 Define and set up the phased. IntensityScope System object. You can set any System object properties at this time or you can leave them at their default values. See "Construction" on page 1-674.
2 Call the step method to add intensity lines to the bottom of the display according to the properties of the phased. IntensityScope System object. Some properties are tunable and can be changed at any time. Non-tunable properties cannot be changed after the first call to step. Subsequent calls to step add more intensity lines.

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step (obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.

## Construction

sIS = phased.IntensityScope creates an intensity scope System object, sIS, having default property values.
sIS = phased.IntensityScope(Name, Value) returns an intensity scope System object, sIS, with each specified property Name set to a specified Value. Name must appear inside single quotes
(' ' ). You can specify several name-value pair arguments in any order as
Name1, Value1, ..., NameN, ValueN.

## Properties

## Name - Window name

'Intensity Scope' (default)| character vector
Intensity scope window name, specified as a character vector. Name property and Title are different properties. The title appears inside the display window, above the data. The name appears in the title bar of the window.

Example: 'Range Intensity'
Data Types: char

## XResolution - X-axis sample spacing

1 (default) | positive real-valued scalar
X-axis sample spacing, specified as a positive real-valued scalar. This quantity determines the width of each horizontal bin of the scan line. The units depend on the interpretation of the data. For example, if you are creating an RTI display, then setting XResolution to 0.5 is interpreted as 0.5 meters.
Example: 0.5
Data Types: double
XOffset - X-axis offset
0 (default) | real-valued scalar
X-axis offset, specified as a real-valued scalar. This quantity sets the value of the lowest bin of the scan line. The values of all other bins are equal to this value plus an integer multiple of Xresolution. The units depend upon the interpretation of the data. For example, if you are creating an RTI display, then setting XOffset to 100.0 is interpreted as 100 meters.
Example: -0.1
Data Types: double

## Xlabel - X-axis label

' ' (default) | character vector
$X$-axis label, specified as a character vector.
Example: 'Range (km)'
Data Types: char

## Title - Title of display

' ' (default) | character vector

Title of the intensity scope display, specified as a character vector. Title property and Name are different properties. The title appears inside the display window, above the data. The name appears in the title bar of the window.

## Example: 'Range vs Time'

Data Types: char

## TimeResolution - Time resolution

. 001 (default) | positive real-valued scalar
Time resolution of intensity line(s), specified as a positive real-valued scalar. Units are seconds.
Example: . 0001
Data Types: double

## TimeSpan - Time span of display window

0.1 (default) | positive real-valued scalar

Time span of intensity display, specified as a positive real-valued scalar. Units are seconds.
Example: 5.0
Data Types: double

## IntensityUnits - Intensity units label

'dB ' (default)| character vector
Intensity units label displayed in the color bar, specified as a character vector.
Example: 'Watts'
Data Types: char

## Position - Location and size of intensity scope window

depends on display-resolution (default) | 1-by-4 vector of positive values
Location and size of the intensity scope window, specified as a 1-by-4 vector having the form [ left bottom width height]. Units are in pixels.

- left and bottom specify the location of the bottom-left corner of the window.
- width and height specify the width and height of the window.

The default value of this property depends on the resolution of your display. This property is tunable.
Example: [100 100500 400]
Data Types: double

## Methods

hide Hide intensity scope window
reset Reset state of intensity scope System object
show Show intensity scope window
step Update intensity scope display

## Common to All System Objects

```
release Allow System object property value changes
```


## Examples

## RTI Display of Moving Target

Use a phased.IntensityScope System object ${ }^{\text {TM }}$ to display the echo intensity of a moving target as a function of range and time.

Run the simulation for 5 seconds at 0.1 second steps. In the display, each horizontal scan line shows the intensities of radar echo at each time step.

```
nsteps = 50;
dt = .1;
timespan = nsteps*dt;
```

Simulate a target at a range of 320.0 km and a range rate of $2.0 \mathrm{~km} / \mathrm{s}$. Echoes are resolved into range bins of 1 km resolution. The range bins span from 50 to 1000 km .

```
rngres = 1.0;
rngmin = 50.0;
rngmax = 1000.0;
tgtrange = 320.0;
rangerate = 2.0;
rngscan = [rngmin:rngres:rngmax];
```

Set up the Intensity Scope using these properties.

- Use the XResolution property to set the width of each scan line bin to the range resolution of 1 km.
- Use the XOffset property to set the value of the lowest range bin to the minimum range of 50 km.
- Use the TimeResolution property to set the value of the scan line time difference to 0.1 s .
- Use the TimeSpan property to set the height of the display window to the time duration of the simulation.
- Use the IntensityUnits property to set the display units to Watts.

```
scope = phased.IntensityScope('Name','IntensityScope Display',...
    'Title','Range vs. Time','XLabel','Range (km)',...
    'XResolution',rngres,'X0ffset',rngmin,...
    'TimeResolution',dt,'TimeSpan',timespan, ...
    'IntensityUnits','Watts','Position',[100,100,800,450]);
```

Update the current target bin and create entries for two adjacent range bins. Each call to the step method creates a new scan line.

```
for k = 1:nsteps
    bin = floor((tgtrange - rngmin)/rngres) + 1;
    scanline = zeros(size(rngscan));
    scanline(bin+[-1:1]) = 1;
    scope(scanline.');
    tgtrange = tgtrange + dt*rangerate;
```

```
        pause(.1);
end
```



## RTI Display of Three Moving Targets

Use the phased. IntensityScope System object ${ }^{\mathrm{TM}}$ to display the intensities of the echoes of three moving targets as functions of range and time.

## Create the Radar and Target System Objects

Set up the initial positions and velocities of the three targets. Use the phased.Platform System object to model radar and target motions. The radar is stationary while the targets undergo constant velocity motion. The simulation runs for 500 steps at 0.1 second increments, giving a total simulation time of 50 seconds.

```
nsteps = 500;
dt = .1;
timespan = nsteps*dt;
x1 = [60,0,0]';
x2 = [60,-80,40]';
x3 = [300,0,-300]';
v1 = [2,0,0]';
v2 = [10,5,6]';
```

```
v3 = [-10,2,-4]';
platform = phased.Platform([0,0,0]',[0,0,0]');
targets = phased.Platform([x1,x2,x3],[v1,v2,v3]);
```


## Set Up Range Bins

Each echo is put into a range bin. The range bin resolution is 1 meter and the range is from 50 to 1000 meters.

```
rngres = 1.0;
rngmin = 50.0;
rngmax = 1000.0;
rngscan = [rngmin:rngres:rngmax];
```


## Create the Gain Function

Define a range-dependent gain function to enhance the display of targets at larger ranges. The gain function amplifies the returned echo for visualization purposes only.

```
rangegain = @(rng)(1e12*rng^4);
```


## Create the Intensity Scope

Set up the Intensity Scope using these properties.

- Use the XResolution property to set the width of each scan line bin to the range resolution of 1 km.
- Use the XOffset property to set the value of the lowest range bin to the minimum range of 50 km.
- Use the TimeResolution property to set the value of the scan line time difference to 0.1 s .
- Use the TimeSpan property to set the height of the display window to the time duration of the simulation.
- Use the IntensityUnits property to set the display units to Watts.
scope = phased.IntensityScope('Name','IntensityScope Display',...
'Title','Ranges vs. Time','XLabel','Range (m)','XResolution', rngres,...
'X0ffset', rngmin, 'TimeResolution',dt,'TimeSpan',timespan, ...
'IntensityUnits','Watts','Position',[100,100,800,450]);


## Run Simulation Loop

1 In this loop, move the targets at constant velocity using the step method of the phased. Platform System object.
2 Compute the target ranges using the rangeangle function.
3 Compute the target range bins by quantizing the range values in integer multiples of rngres.
4 Fill each target range bin and neighboring bins with a simulated radar intensity value.
5 Add the signal from each target to the scan line.
6 Call the step method of the phased. IntensityScope System object to display the scan lines.

```
for k = 1:nsteps
    xradar = platform(dt);
    xtgts = targets(dt);
    [rngs] = rangeangle(xtgts,xradar);
    scanline = zeros(size(rngscan));
```

```
    rngindx = ceil((rngs(1) - rngmin)/rngres);
    scanline(rngindx + [-1:1]) = rangegain(rngs(1))/(rngs(1)^4);
    rngindx = ceil((rngs(2) - rngmin)/rngres);
    scanline(rngindx + [-1:1]) = rangegain(rngs(2))/(rngs(2)^4);
    rngindx = ceil((rngs(3) - rngmin)/rngres);
    scanline(rngindx + [-1:1]) = rangegain(rngs(3))/(rngs(3)^4);
    scope(scanline.');
    pause(.1);
end
```



## RTI and DTI Displays in Full Radar Simulation

Use the phased. IntensityScope System Object ${ }^{\text {TM }}$ to display the detection output of a radar system simulation. The radar scenario contains a stationary single-element monostatic radar and three moving targets.

## Set Radar Operating Parameters

Set the maximum range, peak power range resolution, operating frequency, transmitter gain, and target radar cross-section.

```
max_range = 5000;
range_res = 50;
fc = 10e9;
tx_gain = 20;
peāk_power = 5500.0;
```

Choose the signal propagation speed to be the speed of light, and compute the signal wavelength corresponding to the operating frequency.

```
c = physconst('LightSpeed');
lambda = c/fc;
```

Compute the pulse bandwidth from the range resolution. Set the sampling rate, fs , to twice the pulse bandwidth. The noise bandwidth is also set to the pulse bandwidth. The radar integrates a number of pulses set by num_pulse_int. The duration of each pulse is the inverse of the pulse bandwidth.

```
pulse_bw = c/(2*range_res);
pulse_length = 1/pulse_bw;
fs = \overline{2}}\mathrm{ *pulse_bw;
noise_bw = pulse_bw;
num_pulse_int = 10;
```

Set the pulse repetition frequency to match the maximum range of the radar.
prf = c/(2*max_range);

## Create System Objects for the Model

Choose a rectangular waveform.

```
waveform = phased.RectangularWaveform('PulseWidth',pulse_length,...
    'PRF',prf,'SampleRate',fs);
```

Set the receiver amplifier characteristics.

```
amplifier = phased.ReceiverPreamp('Gain',20,'NoiseFigure',0,...
    'SampleRate',fs,'EnableInputPort',true,'SeedSource','Property',...
    'Seed',2007);
transmitter = phased.Transmitter('Gain',tx_gain,'PeakPower',peak_power,...
    'InUseOutputPort',true);
```

Specify the radar antenna as a single isotropic antenna.

```
antenna = phased.IsotropicAntennaElement('FrequencyRange',[5e9 15e9]);
```

Set up a monostatic radar platform.

```
radarplatform = phased.Platform('InitialPosition',[0; 0; 0],...
    'Velocity',[0; 0; 0]);
```

Set up the three target platforms using a single System object.

```
targetplatforms = phased.Platform(...
    'InitialPosition',[2000.66 3532.63 3845.04; 0 0 0; 0 0 0], ...
    'Velocity',[150 -150 0; 0 0 0; 0 0 0]);
```

Create the radiator and collector System objects.

```
radiator = phased.Radiator('Sensor',antenna,'OperatingFrequency',fc);
collector = phased.Collector('Sensor',antenna,'OperatingFrequency',fc);
```

Set up the three target RCS properties.

```
targets = phased.RadarTarget('MeanRCS',[1.6 2.2 1.05],'OperatingFrequency',fc);
```

Create System object to model two-way freespace propagation.

```
channels= phased.FreeSpace('SampleRate',fs,'TwoWayPropagation',true,...
    'OperatingFrequency',fc);
```

Define a matched filter.

```
MFcoef = getMatchedFilter(waveform);
filter = phased.MatchedFilter('Coefficients',MFcoef,'Gain0utputPort',true);
```


## Create Range and Doppler Bins

Set up the fast-time grid. Fast time is the sampling time of the echoed pulse relative to the pulse transmission time. The range bins are the ranges corresponding to each bin of the fast time grid.

```
fast_time = unigrid(0,1/fs,1/prf,'[)');
range_bins = c*fast_time/2;
```

To compensate for range loss, create a time varying gain System Object.

```
gain = phased.TimeVaryingGain('RangeLoss',2*fspl(range_bins,lambda),...
    'ReferenceLoss',2*fspl(max_range,lambda));
```

Set up Doppler bins. Doppler bins are determined by the pulse repetition frequency. Create an FFT System object for Doppler processing.

```
DopplerFFTbins = 32;
DopplerRes = prf/DopplerFFTbins;
fft = dsp.FFT('FFTLengthSource','Property',...
    'FFTLength',DopplerFFTbins);
```


## Create Data Cube

Set up a reduced data cube. Normally, a data cube has fast-time and slow-time dimensions and the number of sensors. Because the data cube has only one sensor, it is two-dimensional.
rx_pulses = zeros(numel(fast_time),num_pulse_int);

## Create IntensityScope System Objects

Create two IntensityScope System objects, one for Doppler-time-intensity and the other for range-time-intensity.

```
dtiscope = phased.IntensityScope('Name','Doppler-Time Display',...
    'XLabel','Velocity (m/sec)', ...
    'XResolution',dop2speed(DopplerRes,c/fc)/2, ...
```

```
    'XOffset',dop2speed(-prf/2,c/fc)/2,...
    'TimeResolution',0.05,'TimeSpan',5,'IntensityUnits','Mag');
rtiscope = phased.IntensityScope('Name','Range-Time Display',...
    'XLabel','Range (m)', ...
    'XResolution',c/(2*fs), ...
    'TimeResolution',0.05,'TimeSpan',5,'IntensityUnits','Mag');
```

Run the Simulation Loop over Multiple Radar Transmissions
Transmit 2000 pulses. Coherently process groups of 10 pulses at a time.
For each pulse:
1 Update the radar position and velocity radarplatform
2 Update the target positions and velocities targetplatforms
3 Create the pulses of a single wave train to be transmitted transmitter
4 Compute the ranges and angles of the targets with respect to the radar
5 Radiate the signals to the targets radiator
6 Propagate the pulses to the target and back channels
7 Reflect the signals off the target targets
8 Receive the signal sCollector
9 Amplify the received signal amplifier
10 Form data cube
For each set of 10 pulses in the data cube:
1 Match filter each row (fast-time dimension) of the data cube.
2 Compute the Doppler shifts for each row (slow-time dimension) of the data cube.

```
pri = 1/prf;
nsteps = 200;
for k = 1:nsteps
    for m = 1:num_pulse_int
        [ant_pos,ant_ve\overline{l}] = radarplatform(pri);
        [tgt_pos,tgt vel] = targetplatforms(pri);
        sig = waveform();
        [s,tx_status] = transmitter(sig);
        [~,tgt_ang] = rangeangle(tgt_pos,ant_pos);
        tsig = radiator(s,tgt_ang);
        tsig = channels(tsig,ant_pos,tgt_pos,ant_vel,tgt_vel);
        rsig = targets(tsig);
        rsig = collector(rsig,tgt_ang);
        rx_pulses(:,m) = amplifier}(rsig,~(tx_status>0))
    end
    rx pulses = filter(rx pulses);
    MFdelay = size(MFcoef,1) - 1;
    rx_pulses = buffer(rx_pulses((MFdelay + 1):end), size(rx_pulses,1));
    rx_pulses = gain(rx_pulses);
    range = pulsint(rx_pulses,'noncoherent');
    rtiscope(range);
    dshift = fft(rx_pulses.');
    dshift = fftshift(abs(dshift),1);
```

dtiscope(mean(dshift,2));
radarplatform(.05);
targetplatforms(.05);
end



All of the targets lie on the x -axis. Two targets are moving along the x -axis and one is stationary. Because the radar is at the origin, you can read the target speed directly from the Doppler-Time Display window. The values agree with the specified velocities of $-150,150$, and $0 \mathrm{~m} / \mathrm{sec}$.

## Version History

Introduced in R2016a

## See Also

spectrogram

## Topics

"Measure Intensity Levels Using the Intensity Scope"

## phased.ATIScope

View angle-time array response

## Description

The phased.ATIScope System object creates an angle-time intensity (ATI) scope for displaying array response intensities as a function of time and angle of arrival. You can input two types of data -in-phase/quadrature (I/Q) data or intensity data. In either case, the scope displays signal magnitude or signal power.

- I/Q data - The data consists of fast-time I/Q samples of pulses and sweeps from multiple sensors. The scope creates intensity data and displays the array response map. To use I/Q data, set the IQDataInput property to true. In this mode, you can set the properties shown in "Properties Applicable for Processed I/Q Data" on page 1-694.
- Intensity data - The data consists of angle-time array intensity data. The scope displays the angletime intensity response map. For example, you can obtain time-angle intensity data from the output of a beamformer. To use intensity data, set the IQDataInput property to false. In this mode, you can set the properties shown in "Properties Applicable for Viewing Response Data" on page 1-694.

To display angle-time response data:
1 Create the phased.ATIScope object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

scope $=$ phased.ATIScope()
scope $=$ phased.ATIScope(Name=Value)

## Description

scope $=$ phased.ATIScope() creates an ATI System object for displaying the angle-time intensity response of an array.
scope $=$ phased.ATIScope(Name=Value) creates an ATI scope System object with each specified property set to the specified value. See Properties for a list of properties. You can specify additional name-value pair arguments in any order as (Name1=Value1, ... ,NameN=ValueN). For example,

```
scope = phased.ATIScope(IQDataInput=true,IntensityUnits="power", ...
    SensorArray=phased.URA(Size=[4,3]),OperatingFrequency=1e6)
```

creates an ATI scope System object that process I/Q data from a 4 -by-3 uniform rectangular array. The intensity is displayed in power units. The operating frequency is 1 MHz .

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## Name - Scope window name

'Angle-Time Intensity Scope' (default)|character vector | string
Scope window name, specified as a character vector or string. The name appears in the title bar of the window.

## Example: 'Multi-target Angle-Time Intensity Scope'

Tunable: Yes
Data Types: char | string

## Position - Location and size of intensity scope window

dependent on display-resolution (default) | 1-by-4 vector of positive values
Location and size of the intensity scope window, specified as a 1-by-4 vector having the form [left bottom width height].

- left and bottom specify the location of the bottom-left corner of the window.
- width and height specify the width and height of the window.

Units are in pixels.
The default value of this property depends on the resolution of your display. By default, the window is positioned in the center of the screen with a width of 800 pixels and a height of 450 pixels.
Example: [100 100500 400]
Tunable: Yes
Data Types: double

## IQDataInput - Input data type <br> false (default) | true

Input data type, specified as false or true. When true, the input consists of complex I/Q sample data and further processing is required to transform to the angle-time domain. When false, the input data is real response data that has already been transformed to the angle-time domain.

## Data Types: logical

## AngleLabel - Angle-axis label

'Angles (deg)' (default)| character vector | string

Angle-axis label, specified as a character vector or a string.
Example: 'Angles (rad)'
Tunable: Yes
Data Types: char | string

## AngleResolution - Angle difference between samples

1.0 (default) | positive scalar

Angle separation between samples, specified as a positive scalar. This property defines the angle difference between columns of the input matrix. Units are in degrees.

## Dependencies

To enable this property, set the IQDataInput property to false.

## Data Types: double

## AngleOffset - Angle offset

0.0 (default) | scalar

Angle offset, specified as a scalar. This property defines the angle value of the first column of the input matrix. Units are in degrees.

## Dependencies

To enable this property, set the IQDataInput property to false.
Data Types: double

## TimeResolution - Time difference between rows

0.001 (default) | positive scalar

Time interval between samples, specified as a positive scalar. This property defines the time interval between the rows of the scope. Units are in seconds.
Data Types: double

## TimeSpan - Time span of display

0.100 (default) | positive scalar

Time span of the intensity display, specified as a positive scalar. Units are in seconds.
Data Types: double
IntensityUnits - Response intensity units
'db' (default)|'magnitude' | 'power'
Response intensity units, specified as 'db', 'magnitude', or 'power'.
Data Types: char | string

## Title - Display title

'Angle vs. Time' (default) | character vector | string
Display title, specified as a character vector or string.
Tunable: Yes

## Data Types: char|string

## SensorArray - Sensor array

phased.ULA array with default array properties (default) | Phased Array System Toolbox array System object

Sensor array, specified as a Phased Array System Toolbox array System object. See phased.ULA for the default values of a uniform linear array.
Example: phased.URA

## Dependencies

To enable this property, set the IQDataInput to true.

## DOAMethod - Direction of arrival estimation method

'beamscan' (default)|'mvdr'|'music'
Direction of arrival estimation method, specified as 'beamscan','mvdr', or 'music'.

## Example: 'mvdr'

## Dependencies

To enable this property, set the IQDataInput property to true.
Data Types: char | string

## PropagationSpeed - Signal propagation speed

physconst('LightSpeed') (default) | positive scalar
Signal propagation speed, specified as a positive scalar. The default value of this property is the speed of light. See physconst. Units are in meters/second.

Example: 3e8

## Dependencies

To enable this property, set the IQDataInput property to true.
Data Types: double
OperatingFrequency - Operating frequency
300e6 (default) | positive scalar
Operating frequency of the system, specified as a positive scalar. Units are in Hz .
Example: 2e9

## Dependencies

To enable this property, set the IQDataInput property to true.
Data Types: double

## NumPhaseShifterBits - Number of phase shifter quantization bits <br> 0 (default) | non-negative scalar

The number of bits used to quantize the phase shift of the applied beamformer, specified as a nonnegative integer. A value of zero indicates that no quantization is performed.

## Example: 5

## Dependencies

To enable this property, set the IQDataInput property to true.
Data Types: double

## ForwardBackwardAveraging - Forward-backward averaging <br> false (default) | true

Set this property to true to allow forward-backward averaging to estimate the covariance matrix for sensor arrays having a conjugate-symmetric array manifold.

## Dependencies

To enable this property, set the IQDataInput property to true.

## Data Types: logical

## AzimuthScanAngles - Azimuth scan angles

-90:90 (default) | scalar | real-valued row vector
Azimuth scan angles, specified as a scalar or real-valued row vector. The angles must lie between $180^{\circ}$ and $180^{\circ}$, inclusive. Specify the angles in increasing order. At least one of the sets of angles defined in the AzimuthScanAngles and ElevationScanAngles properties must be a scalar. Units are in degrees.

Example: -20:20

## Dependencies

To enable this property, set the IQDataInput property to true.

## Data Types: double

## ElevationScanAngles - Elevation scan angles

0 (default) | scalar | real-valued row vector
Elevation scan angles, specified as a scalar or real-valued row vector. The angles must lie between $90^{\circ}$ and $90^{\circ}$, inclusive. Specify the angles in increasing order. At least one of the sets of angles defined in the AzimuthScanAngles and ElevationScanAngles properties must be a scalar. Units are in degrees.

## Dependencies

To enable this property, set the IQDataInput property to true.
Data Types: double
Usage

## Syntax

scope (X)

## Description

scope (X) displays an ATI scope of array response intensities derived from the data $X$. You can display magnitude or power values.

## Input Arguments

## X - Intensity or I/Q data

## $M$-by- $N$ real-valued matrix | $M$-by- $N$ complex-valued matrix

- When the IQDataInput property is false, X represents intensity data, specified as an $M$-by- $N$ real-valued matrix. Each column of the matrix represents an intensity vector from successive times. Each matrix row $M$ is the number of intensity values in an angle intensity vector and $N$ is the number of intensity vectors. $M$ should be greater than 1 and $N$ should be equal to or greater than 1 . The time between the intensity vectors is specified in the TimeResolution property.
- When the IQDataInput property is true, X represents I/Q data, specified as an $M$-by- $N$ complexvalued matrix. Each row contains the data samples for all sensors at a single time. Each column contains the I/Q data for one sensor for all times.

Data Types: double

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```


## Specific to phased.ATIScope

## hide Turn off visibility of scope

isVisible Visibility of scopes
show Turn on visibility of scopes

## Common to All System Objects

step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object

## Examples

## Display I/Q Data on Angle-Time Intensity Scope

Display the directions-of-arrival (DOA) of two signals arriving at a 10-by-5 uniform rectangular array (URA).

First, create a phased.URA array System object ${ }^{\text {TM }}$ containing phased.IsotropicAntennaElement System objects spaced 0.45 wavelengths apart.

```
fc = 200e6;
lambda = physconst('LightSpeed')/fc;
```

```
d = 0.45*lambda;
element = phased.IsotropicAntennaElement( ...
    FrequencyRange=[100e6,300e6]);
array = phased.URA(Element=element,Size=[10,5], ...
    ElementSpacing=[d,d]);
```

Then, create an ATIScope to process I/Q data.

```
scope = phased.ATIScope(IQDataInput=true, ...
    SensorArray=array, ...
    DOAMethod="mvdr", ...
    OperatingFrequency=fc, ...
    AzimuthScanAngles=-50:50, ...
    ElevationScanAngles=0, ...
    AngleLabel="Azimuth Angle (deg)", ...
    TimeSpan=100, ...
    TimeResolution=2);
```

Generate baseband signals at 300 and 400 Hz . The sampling rate of the baseband signals is 8 kHz .

```
fs = 8000;
t = (0:1/fs:1).';
x1 = exp(-1i*2*pi*t*300);
x2 = exp(-1i*2*pi*t*400);
```

Create two paths in azimuth-elevation space. The first path is a straight line starting at -45 degrees in azimuth and stopping at 25 degrees with 50 samples. The second path has constant azimuth of 30 degrees.

```
path1 = [linspace(-45,25,50); 0.0*ones(1,50)];
path2 = [-10*ones(1,50);zeros(1,50)];
xtot = [x1,x2];
for k = 1:size(path2,2)
    azel1 = [path1(:,k),path2(:,k)];
    x = collectPlaneWave(array,xtot,azell,fc);
    noise = 0.1*(randn(size(x)) + li*randn(size(x)));
    scope(x + noise);
end
```



## Display Array Response Using Angle-Time Intensity Scope

Display the directions-of-arrival (DOA) of two signals arriving at a 10-by-5 uniform rectangular array (URA).

First, create a phased.URA array System object ${ }^{\mathrm{TM}}$ composed of phased.IsotropicAntennaElement System objects.
fc = 200e6;
lambda = physconst('LightSpeed')/fc;
d = 0.45*lambda;
element = phased.IsotropicAntennaElement(FrequencyRange=[100e6,300e6]); array = phased.URA(Element=element,Size=[5,5],ElementSpacing=[d,d]);

Then, create a phased.ATIScope System object.
scope $=$ phased.ATIScope(IQDataInput=false, ... AngleLabel="Azimuth Angle (deg)", ...
TimeSpan=100,TimeResolution=2, ...
Angle0ffset=-70);
Generate baseband signals at 300 and 400 Hz . The sampling rate of the baseband signal is 8 kHz .
fs = 8000;
$\mathrm{t}=(0: 1 / \mathrm{fs}: 1) .{ }^{\prime} ;$
$x 1=\exp \left(-1 i^{*} 2 *\right.$ pi $\left.^{*} \mathrm{t}^{*} 300\right)$;
$x 2=\exp \left(-1 i * 2 * i^{*} * * 400\right) ;$

Create an MVDR beamformer System object. Specify the beamformer pointing angles.

```
azAngle = -50:50;
elAngle = zeros(size(azAngle));
bfAngle = [azAngle;elAngle];
beamformer = phased.MVDRBeamformer(SensorArray=array, ...
    PropagationSpeed=physconst('LightSpeed'), ...
    OperatingFrequency=fc,Direction=bfAngle, ...
    Weights0utputPort=false);
```

Create two of objects in azimuth-elevation space. The first path is a straight line starting at $-45^{\circ}$ in azimuth and ending at $25^{\circ}$. The second path is at a constant azimuth of $10^{\circ}$ degrees. Both paths have 50 samples.

```
path1 = [linspace(-45,25,50);zeros(1,50)];
path2 = [-10*ones(1,50);zeros(1,50)];
xtot = [x1,x2];
ymn = zeros(size(bfAngle,2));
for k = 1:size(path2,2)
    azel1 = [path1(:,k),path2(:,k)];
    x = collectPlaneWave(array,xtot,azel1,fc);
    noise = 0.1*(randn(size(x)) + li*randn(size(x)));
    y = beamformer(conj(x) + noise);
    ymn(k,:) = mean(abs(y),1);
    scope(ymn)
end
scope(ymn)
```



## More About

Properties Applicable for Processed I/Q Data
These properties are applicable when IQDataInput is true.

| Properties | Position |
| :--- | :--- |
| Name | TimeResolution |
| AngleLabel | IntensityUnits |
| TimeSpan | PropagationSpeed |
| Title | DOAMethod |
| SensorArray | ForwardBackwardAveraging |
| OperatingFrequency | AzimuthScanAngles |
| NumPhaseShifterBits |  |
| ElevationScanAngles |  |

## Properties Applicable for Viewing Response Data

These properties are applicable when IQDataInput is false.

| Properties | Position |
| :--- | :--- |
| Name | AngleResolution |
| AngleLabel | TimeResolution |
| AngleOffset | IntensityUnits |
| TimeSpan |  |
| Title |  |

## Version History

Introduced in R2022b

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder ${ }^{\mathrm{TM}}$.

## See Also

phased.BeamscanEstimator|phased.BeamscanEstimator2D|phased.MVDREstimator2D | phased.MVDREstimator|phased.MUSICEstimator2D | phased.MUSICEstimator| phased.AngleDopplerScope | phased.DTIScope | phased. IntensityScope | phased.RangeAngleScope | phased.RangeDopplerScope|phased.RTIScope

## phased.RTIScope

Package: phased
Range intensity scope

## Description

The phased.RTIScope System object creates a scrolling display of range response intensity as a function of time. Each row represents the range response for a pulse or FMCW signal. Sequential calls to the object add new rows to the bottom of the display window. Columns represent the responses at a specific range over all pulses. You can input two types of data - in-phase and quadrature (I/Q) data or response data.

- I/Q data - The input consists of fast-time I/Q samples for one or more pulses or FM sweeps. The scope computes the range response and adds it to the display. To use I/Q data, set the IQDataInput property to true. In this mode, you can set the properties shown in "Properties Applicable to I/Q Data" on page 1-703.
- Response data - The data consists of the range response itself. The scope adds the range response to the display. For example, you can obtain the range response from a phased. RangeResponse object. To use response data, set the IQDataInput property to false. In this mode, you can set the properties shown in "Properties Applicable to Response Data" on page 1-703.


To create and run a range-time intensity scope,
1 Create the phased.RTIScope object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

scope = phased.RTIScope
scope = phased.phased.RTIScope(Name,Value)

## Description

scope $=$ phased.RTIScope creates a range-time intensity scope System object, scope. This object displays the intensity of the range-time response for the input data.
scope = phased.phased.RTIScope(Name, Value) creates a range-time intensity scope, scope, with each specified property set to the specified value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN). Enclose property names in quotes. For example,

```
scope = phased.RTIScope('IQDataInput',true,'RangeMethod', ...
    'FFT','SampleRate',1e6,'TimeResolution',0.5,'TimeSpan',10.0, ...
    'RangeFFTLength',1024);
```

creates a scope object that uses FFT-based range processing for I/Q data having a sample rate of 1 MHz . The time resolution is 0.5 seconds and the time span is 10 seconds. The range FFT length is 1024 samples.

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## Name - Display caption

'Range Time Intensity Scope' (default)|character vector
Display caption, specified as a character vector. The caption appears in the title bar of the window.

## Example: 'Multi-target Range Time Intensity Scope'

Tunable: Yes
Data Types: char

## Position - Location and size of intensity scope window

depends on display-resolution (default) | 1-by-4 vector of positive values
Location and size of the intensity scope window, specified as a 1-by-4 vector having the form [left bottom width height].

- left and bottom specify the location of the bottom-left corner of the window.
- width and height specify the width and height of the window.

Units are in pixels.
The default value of this property depends on the resolution of your display. By default, the window is positioned in the center of the screen, with a width and height of 800 and 450 pixels, respectively.
Example: [100 100500 400]
Tunable: Yes
Data Types: double

## IQDataInput - Type of input data <br> false (default)| true

Type of input data, specified as false or true. When true, the object assumes that the input consists of I/Q sample data and further processing is required in the range domain. When false, the object assumes that the data is response data that has already been processed.
Data Types: logical

## RangeLabel - Range axis label

'Range (m)' (default) | character vector
Range-axis label, specified as a character vector.
Example: 'Range (km)'
Tunable: Yes
Data Types: char

## RangeResolution - Range difference between samples

1.0 (default) | positive scalar

Range distance between samples, specified as a positive scalar. This property defines the distance between columns of the scope. Units are in meters.

Data Types: double

## RangeOffset - Range offset

0.0 (default) | positive scalar

Range offset, specified as a positive scalar. This property defines the range value of the first column of the display. Units are in meters.
Data Types: double

## TimeResolution - Time difference between rows

0.001 (default) | positive scalar

Time interval between samples, specified as a positive scalar. This property defines the time interval between the rows of the scope. Units are in seconds.
Data Types: double
TimeSpan - Time span of display
0.100 (default) | positive scalar

Time span of the intensity display, specified as a positive scalar. Units are in seconds.

Data Types: double
IntensityUnits - Response intensity units
'db' (default)|'magnitude' | 'power'
Response intensity units, specified as a 'db', 'magnitude', or 'power'.
Data Types: char
RangeMethod - Range processing method
'Matched filter' (default)|'FFT'
Range-processing method, specified as 'Matched filter' or 'FFT'.

| 'Matched filter' | The object applies a matched filter to the incoming signal. This <br> approach is commonly used with pulsed signals, where the matched <br> filter is a time-reversed replica of the transmitted signal. |
| :--- | :--- |
| 'FFT' | Algorithm performs range processing by applying an FFT to the <br> input signal. This approach is commonly used with FMCW <br> continuous signals and linear FM pulsed signals. |

## Dependencies

To enable this property, set the IQDataInput property to true.

## PropagationSpeed - Signal propagation speed

physconst('LightSpeed') (default) | positive scalar
Signal propagation speed, specified as a positive scalar. The default value of this property is the speed of light. See physconst. Units are in meters/second.
Example: 3e8

## Dependencies

To enable this property, set the IQDataInput property to true.

## Data Types: double

## SampleRate - Sample rate

le6 (default) | positive scalar
Sample rate, specified as a positive scalar. Units are in Hz.
Example: 10e3

## Dependencies

To enable this property, set the IQDataInput property to true.

```
Data Types: double
```


## SweepSlope - FM sweep slope

1e9 (default) | scalar
Slope of the linear FM sweep, specified as a scalar. Units are in $\mathrm{Hz} / \mathrm{sec}$.

## Dependencies

To enable this property, set the IQDataInput property to true and the RangeMethod property to 'FFT'.

Data Types: double
DechirpInput - Dechirp input signal
false (default) | true
Set this property to true to dechirp the input signal before performing range processing. false indicates that the input signal is already dechirped and no dechirp operation is necessary.

## Dependencies

To enable this property, set the IQDataInput property to true and the RangeMethod property to 'FFT'.

Data Types: logical

## RangeFFTLength - FFT length used in range processing

1024 (default) | positive integer
FFT length used for range processing, specified as a positive integer.
Example: 128

## Dependencies

To enable this property, set the IQDataInput property to true and the RangeMethod property to 'FFT'.

Data Types: double
ReferenceRangeCentered - Set reference range at center of range span
true (default) | false
Set this property to true to set the reference range to the center of the range span. Set this property to false to set the reference range to the beginning of the range span.

## Dependencies

To enable this property, set the IQDataInput property to true and the RangeMethod property to 'FFT'.
Data Types: logical

## Usage

## Syntax

scope (X)
scope(X,Xref)

## Description

scope (X) adds new rows to the range-time intensity scope. The input $X$ can be I/Q sample data or range response data depending on the value of the IQDataInput property.
scope (X, Xref) also specifies a reference signal to use for dechirping the input signal, X. This syntax applies when you set the IQDataInput property to true, the RangeMethod property to ' $F F T$ ' , and the DechirpInput property to true. This syntax is most commonly used with FMCW signals. Xref is generally the transmitted signal.
scope (X, coeff) also specifies matched filter coefficients, coeff. This syntax applies when you set the IQDataInput property to true and the RangeMethod property to 'Matched Filter'. This syntax is most commonly used with pulsed signals.

## Input Arguments

## X - Input data

real-valued $N$-by-M matrix | complex-valued $N$-by- $M$ matrix
Input data, specified as a complex-valued $N$-by- $M$ matrix. The interpretation of the data depends on the setting of the IQDataInput property.

- When IQDataInput is true, each column contains $N$ fast-time I/Q samples for a pulse or an FMCW sweep. $M$ is the number of pulses in the case of pulsed signals or the number of dechirped frequency sweeps for FMCW signals. The scope computes and displays the range-response.
- When RangeMethod is set to 'FFT' and DechirpInput is false, X has previously been dechirped.
- When RangeMethod is set to 'FFT' and DechirpInput is false, X has not been previously dechirped. Use the syntax that includes XREF as input data.
- When RangeMethod is set to 'MatchedFilter', X has not been matched filtered. Use the syntax that includes COEF as input data.
- When IQDataInput is false, each column contains $N$ response samples for a pulse or an FMCW sweep such as that produced by the phased. RangeResponse. $M$ is the number of pulses in the case of pulsed signals or the number of dechirped frequency sweeps for FMCW signals. The scope only displays the range-response.


## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```


## Specific to Scope Objects

show Turn on visibility of scopes
hide Turn off visibility of scope
isVisible Visibility of scopes

## Common to All System Objects

step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object

## Examples

## Display Range Time Intensity Map for Three Targets

Create a scrolling display of intensity at each range as function of time. The intensity is a combination of intensities from three simulated targets. One target starts at a range of 250 m and moves outward to 950 m . The second target starts at 1000 m and moves inward to 300 m . The third stays at 400 m . The intensities are computed using the inline function rangePow. The targets move in steps of 10 m but the rangePow function spreads the intensity over nearby range bins which are spaced every meter.

The inline function rangePow simulates a spread target return having an intensity falling off with the fourth power of range.

```
txpow = 200;
gain = 2e8;
std = 5;
rangePow = @(rngbins,range) ...
    gain.*exp(-0.5*((rngbins-range)./std).^2).* ...
    txpow./(range.^4)./(sqrt(2*pi).*std);
```

Create an RTI Scope to view intensity data.

```
scope = phased.RTIScope( ...
    'IQDataInput',false,...
    'Name','Range-Time Intensity Scope',...
    'Position',[560 375 560 420],...
    'RangeLabel','Range (m)', ...
    'RangeResolution',1, ...
    'TimeResolution',0.05,'TimeSpan',6, ...
    'IntensityUnits','magnitude');
```

Create range bins for three targets.

```
rngbins = 0:900;
ranges(:,1) = 250:10:950;
ranges(:,2) = 1000:-10:300;
ranges(:,3) = 400;
```

Fill in all range bins by looping over all ranges and add each line at a time to the scope.

```
for k = 1:size(ranges,1)
    y = rangePow(rngbins,ranges(k,1)) + ...
        rangePow(rngbins,ranges(k,2)) + ...
        rangePow(rngbins,ranges(k,3));
    scope(y.');
    pause(.1);
end
```




## More About

## Properties Applicable to I/Q Data

These properties are applicable when IQDataInput is true.

| Properties | Position |
| :--- | :--- |
| Name | RangeResolution |
| RangeLabel | TimeResolution |
| RangeOffset | IntensityUnits |
| TimeSpan | PropagationSpeed |
| RangeMethod | SweepSlope |
| SampleRate | RangeFFTLength |
| DechirpInput |  |
| ReferenceRangeCentered |  |

## Properties Applicable to Response Data

These properties are applicable when IQDataInput is false.

| Properties | Position |
| :--- | :--- |
| Name | RangeResolution |
| RangeLabel | TimeResolution |
| RangeOffset | IntensityUnits |
| TimeSpan |  |

## Version History

Introduced in R2019a

## See Also

show | hide |isVisible | phased.RangeDopplerResponse | phased.RangeResponse | phased.DTIScope|phased.ATIScope| phased.AngleDopplerScope| phased.RangeAngleScope | phased. RangeDopplerScope

## phased.DTIScope

Package: phased
Doppler-time intensity scope

## Description

The phased.DTIScope System object creates a scrolling display of Doppler response intensity as a function of time. Each row represents the Doppler response for a pulse or FMCW signal. Sequential calls to the object add new rows to the bottom of the display window. Columns represent the responses at specific Doppler values as a function of time. You can input two types of data - in-phase and quadrature (I/Q) data or response data.

- I/Q data - The input consists of fast-time I/Q samples from one or more pulses or FM sweeps. The scope computes the Doppler response and adds it to the display. To use I/Q data, set the IQDataInput property to true. In this mode, you can set the properties listed in "Properties Applicable to I/Q Data" on page 1-703.
- Response data - The data consists of the Doppler response itself as a function of time. The scope only adds the Doppler response to the display. For example, you can obtain Doppler responses from the phased. RangeDopplerResponse System object. To use response data, set the IQDataInput property to false. In this mode, you can set the properties listed in "Properties Applicable to Response Data" on page 1-703.


To create and run a Doppler-time intensity scope,
1 Create the phased.DTIScope object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

scope = phased.DTIScope
scope = phased.phased.DTIScope(Name,Value)

## Description

scope = phased.DTIScope creates a Doppler time intensity scope System object, scope. This object displays the Doppler-time response intensity of the input data.
scope = phased.phased.DTIScope(Name, Value) creates a Doppler-time intensity scope object, scope, with each specified property set to the specified value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN). Enclose property names in quotes. For example,

```
scope = phased.DTIScope('IQInputData',false, ...
    'OperatingFrequency',1e6, ...
    'SampleRate',1e6,'DopplerOutput','Speed', ...
    'OperatingFrequency',10e6,'DopplerFFTLength',512);
```

creates a scope object that displays a 10 -second time span of data using a Doppler FFT size of 512 for I/Q data. The Doppler output units are speed in meters per second.

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## Name - Display caption

Doppler Time Intensiy Scope' (default)|character vector
Display caption, specified as a character vector. The caption appears in the title bar of the window.

## Example: 'Multi-target Doppler Time Intensiy Scope'

Tunable: Yes
Data Types: char

## Position - Location and size of intensity scope window

depends on display-resolution (default) | 1-by-4 vector of positive values
Location and size of the intensity scope window, specified as a 1-by-4 vector having the form [left bottom width height].

- left and bottom specify the location of the bottom-left corner of the window.
- width and height specify the width and height of the window.

Units are in pixels.
The default value of this property depends on the resolution of your display. By default, the window is positioned in the center of the screen, with a width and height of 800 and 450 pixels, respectively.
Example: [100 100500 400]
Tunable: Yes
Data Types: double
IQDataInput - Type of input data
false (default) | true
Type of input data, specified as true or false. When true, the object assumes that the input consists of I/Q sample data and further processing is required in the Doppler domain. When false, the object assumes that the data is response data that has already been processed.

Data Types: logical
DopplerResolution - Doppler interval between samples
1.0 (default) | positive scalar

Doppler interval between samples, specified as a positive scalar. This property defines the Doppler frequency difference between the scope columns. Units are in Hz .
Data Types: double

## DopplerOffset - Doppler axis offset

0.0 (default) | scalar

Doppler axis offset, specified as a scalar. This property apples a frequency offset to the Doppler axis. Units are in Hz .
Data Types: double

## TimeResolution - Time difference between rows

0.001 (default) | positive scalar

Time interval between samples, specified as a positive scalar. This property defines the time duration between rows of scope. Units are in seconds.

Data Types: double

## TimeSpan - Time duration of display

0.100 (default) | positive scalar

Time span of the intensity display, specified as a positive scalar. Units are in seconds.
Data Types: double
IntensityUnits - Response Intensity units
'db' (default)| 'magnitude' | 'power'
Response intensity units, specified as a 'db', 'magnitude', or 'power'.
Data Types: char

## DopplerOutput - Doppler output domain

'Frequency ' (default) | 'Speed '
Doppler output domain, specified as 'Frequency ' or 'Speed '. If you set this property to
'Frequency' , the Doppler domain is the Doppler shift. Units are in Hz. If you set this property to
'Speed ' ', the Doppler domain is the corresponding radial speed. Units are in $\mathrm{m} / \mathrm{s}$.

## Data Types: char

## PropagationSpeed - Signal propagation speed

physconst('LightSpeed') (default) | positive scalar
Signal propagation speed, specified as a positive scalar. The default value of this property is the speed of light. See physconst. Units are in meters/second.
Example: 3e8

## Dependencies

To enable this property, set the IQDataInput property to true.
Data Types: double
OperatingFrequency - Operating frequency
300e6 (default) | positive scalar
Operating frequency, specified as a positive scalar.

## Dependencies

To enable this property, set the IQDataInput property to true and the DopplerOutput to 'Speed'.
Data Types: double

## DopplerFFTLength - FFT length used in Doppler processing

1024 (default) | positive integer
FFT length used in Doppler processing, specified as a positive integer.

## Dependencies

To enable this property, set the IQDataInput property to true.
Data Types: double

## Usage

## Syntax

scope (X)

## Description

scope (X) updates and displays the Doppler-time intensity scope for the input data, $X$. The input $X$ can be I/Q sample data or Doppler response data depending on the value of the IQDataInput property.

## Input Arguments

## X - Input data

complex-valued $K$-by- $L$ matrix
Input data, specified as a complex-valued $K$-by- $L$ matrix. The interpretation of the data depends on the value of the IQDataInput property.

- When IQDataInput is true, the input consists of received fast-time and slow-time data for each PRI pulse or FMCW sweep. $K$ denotes the number of time samples. $L$ is the number of pulses in the case of pulsed signals or the number of dechirped frequency sweeps for FMCW signals. The scope computes and displays the Doppler response.
- When IQDataInput is false, the input already consists of response data in the Doppler domain such as that produced, for example, by phased. RangeDopplerResponse. Each row contains the set of Doppler responses. Each response corresponds to an element of the Dop vector. The scope serves only as a display of the Doppler response.


## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```


## Specific to Scope Objects

| show | Turn on visibility of scopes |
| :--- | :--- |
| hide | Turn off visibility of scope |
| isVisible | Visibility of scopes |

## Common to All System Objects

step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object

## Examples

## Display Doppler-Time Intensity Map for Three Targets

Create a phased.DTIScope object to view a scrolling Doppler-Time Intensity map.
Load the example data.

```
load('RTIDTIExampleData.mat')
rx_pulses = zeros(numel(fast_time),num_pulse_int);
```

Create the DTI scope.

```
scope = phased.DTIScope('IQDataInput',false,...
    'DopplerOutput','Speed',...
    'PropagationSpeed',c,...
```

```
'OperatingFrequency',fc,...
'Name','Doppler-Time Display',...
'DopplerResolution',DopplerRes, ...
'DopplerOffset',-prf/2,...
'TimeResolution',0.05,...
'TimeSpan',5,...
'IntensityUnits','magnitude',...
'Position',[560 375 560 420]);
```

Obtain the pulse repetition interval, 33.3564 microsec.

```
pri = 1/prf;
```

Transmit 2000 pulses and coherently process a train of 10 pulses at a time. There are 200 trains. After each pulse, move the target and radar platform. The radar reflects off three targets. The first moves along the $x$-axis at $-150 \mathrm{~m} / \mathrm{sec}$. The second moves along the $x$-axis at $+150 \mathrm{~m} / \mathrm{sec}$. The third target is stationary. After each pulse train, compute the Doppler response using an FFT.

```
nsteps = 200;
for k = 1:nsteps
    for m = 1:num_pulse_int
        [ant_pos,\overline{ant ve\overline{l}] = radarplatform(pri);}
        [tgt_pos,tgt_vel] = targetplatforms(pri);
        sig = waveform();
        [s,tx status] = transmitter(sig);
        [~,tgt_ang] = rangeangle(tgt_pos,ant_pos);
        tsig = radiator(s,tgt_ang);
        tsig = channels(tsig,ant_pos,tgt_pos,ant_vel,tgt_vel);
        rsig = targets(tsig);
        rsig = collector(rsig,tgt_ang);
        rx_pulses(:,m) = preamplifier(rsig,~(tx_status>0));
    end
    rx_pulses = gain(rx_pulses);
    dshift = fft(rx_pulses.');
    dshift = fftshift(abs(dshift),1);
    scope(mean(dshift,2));
    pause(0.1)
    radarplatform(.05);
    targetplatforms(.05);
end
```




## More About

## Properties Applicable to I/Q Data

These properties are applicable when IQDataInput is true.

| Properties | Position |
| :--- | :--- |
| Name | DopplerOffset |
| DopplerResolution | TimeSpan |
| TimeResolution | DopplerOutput |
| IntensityUnits | OperatingFrequency |
| PropagationSpeed |  |
| DopplerFFTLength |  |

## Properties Applicable to Response Data

These properties are applicable when IQDataInput is false.

| Properties |  |
| :--- | :--- |
| Name | Position |
| DopplerResolution | DopplerOffset |


| Properties | TimeSpan |
| :--- | :--- |
| TimeResolution | DopplerOutput |
| IntensityUnits | OperatingFrequency |
| PropagationSpeed |  |

## Version History

Introduced in R2019a

## See Also

show | hide |isVisible | phased. RangeDopplerResponse | phased. AngleDopplerScope | phased.RangeAngleScope | phased.RangeDopplerScope | phased.RTIScope|
phased.ATIScope

## hide

System object: phased. IntensityScope
Package: phased
Hide intensity scope window

## Syntax

hide(sIS)

## Description

hide(sIS) hides the display window of the phased. IntensityScope object, sIS.

## Input Arguments

## sIS - Intensity scope

phased.IntensityScope System object
Intensity scope, specified as a phased. IntensityScope System object.
Example: phased.IntensityScope

## Examples

## Hide and Show Intensity Scope

Create an angle-time-intensity scope. Use the phased.IntensityScope System object ${ }^{\text {TM }}$ to display simulated intensity as a function of the angular motion of a moving target. After five steps in the processing loop, use the hide method to hide the scope. At completion of the loop, use the show method to show the scope.

Simulate data for 5 seconds with a time interval of 0.5 seconds between scan lines.

```
nsteps = 10;
dt = 0.5;
timespan = nsteps*dt;
```


## Set Up IntensityScope System Object

Create an angle-time-intensity scope having azimuth angle bins spanning $-180^{\circ}$ to $180^{\circ}$ with $1^{\circ}$ resolution.

```
scanline = zeros(361,1);
angres = 1.0;
angmin = -180.0;
angmax = 180.0;
rtidisplay = phased.IntensityScope( ...
    'Name','IntensityScope Display',...
    'Title','Azimuth vs. Time',...
```

'XLabel','Azimuth (deg)', ...
'XResolution', angres,'X0ffset', angmin,...
'TimeResolution',dt,'TimeSpan',timespan, ...
'IntensityUnits','Watts',...
'Position',[100,100,800,450]);

## Loop Over Scan Updates

Simulate angular motion and fill the bin containing the current angular position of the signal. Hide the scope after the 5th step and show the scope at the end of the simulation.

```
for k = 1:nsteps
    ang = -130.0 + k;
    binindexdx = floor((ang - angmin)/angres) + 1;
    scanline(binindexdx) = 1;
    rtidisplay(scanline);
    scanline(binindexdx) = 0;
    if k == 5
        hide(rtidisplay)
    end
    pause(.1);
end
show(rtidisplay)
```



## Version History

Introduced in R2016a

## reset

System object: phased.IntensityScope
Package: phased
Reset state of intensity scope System object

## Syntax

reset(sIS)

## Description

reset(sIS) resets the internal state of the phased. IntensityScope System object, sIS, to its initial value.

## Input Arguments

sIS - Intensity scope
phased.IntensityScope System object
Intensity scope, specified as a phased. IntensityScope System object.
Example: phased.IntensityScope

## Version History <br> Introduced in R2016a

## show

System object: phased. IntensityScope
Package: phased
Show intensity scope window

## Syntax

show(sIS)

## Description

show(sIS) shows the display window of the phased. IntensityScope object, sIS.

## Input Arguments

## sIS - Intensity scope

phased.IntensityScope System object
Intensity scope, specified as a phased. IntensityScope System object.
Example: phased.IntensityScope

## Examples

## Hide and Show Intensity Scope

Create an angle-time-intensity scope. Use the phased.IntensityScope System object ${ }^{\text {TM }}$ to display simulated intensity as a function of the angular motion of a moving target. After five steps in the processing loop, use the hide method to hide the scope. At completion of the loop, use the show method to show the scope.

Simulate data for 5 seconds with a time interval of 0.5 seconds between scan lines.

```
nsteps = 10;
dt = 0.5;
timespan = nsteps*dt;
```


## Set Up IntensityScope System Object

Create an angle-time-intensity scope having azimuth angle bins spanning $-180^{\circ}$ to $180^{\circ}$ with $1^{\circ}$ resolution.

```
scanline = zeros(361,1);
angres = 1.0;
angmin = -180.0;
angmax = 180.0;
rtidisplay = phased.IntensityScope( ...
    'Name','IntensityScope Display',...
    'Title','Azimuth vs. Time',...
```

'XLabel','Azimuth (deg)', ...
'XResolution', angres,'X0ffset', angmin,...
'TimeResolution',dt,'TimeSpan',timespan, ...
'IntensityUnits','Watts',...
'Position',[100,100,800,450]);

## Loop Over Scan Updates

Simulate angular motion and fill the bin containing the current angular position of the signal. Hide the scope after the 5th step and show the scope at the end of the simulation.

```
for k = 1:nsteps
    ang = -130.0 + k;
    binindexdx = floor((ang - angmin)/angres) + 1;
    scanline(binindexdx) = 1;
    rtidisplay(scanline);
    scanline(binindexdx) = 0;
    if k == 5
        hide(rtidisplay)
    end
    pause(.1);
end
show(rtidisplay)
```



## Version History

Introduced in R2016a

## step

System object: phased. IntensityScope
Package: phased
Update intensity scope display

## Syntax

step(sIS,data)

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.
step(sIS, data) updates the intensity scope display with new scan lines from a real signal, data.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

sIS - Intensity scope display
phased.IntensityScope System object
Intensity scope display, specified as a phased.IntensityScope System object.
Example: phased.IntensityScope

## data - Displayed intensity values

real-valued $N$-by-M matrix
Displayed intensity values, specified as a real-valued $N$-by- $M$ matrix. The quantity $N$ specifies the number of intensity bins in data. The quantity $M$ specifies the number of intensity vectors in the data. Each column of the matrix creates a display line. Units are arbitrary. Specify the time interval between intensity vectors using the TimeResolution property.
Example: [5.0;5.1;5.0;4.9]
Data Types: double

## Examples

## RTI Display of Three Moving Targets

Use the phased. IntensityScope System object ${ }^{\text {tM }}$ to display the intensities of the echoes of three moving targets as functions of range and time.

## Create the Radar and Target System Objects

Set up the initial positions and velocities of the three targets. Use the phased. Platform System object to model radar and target motions. The radar is stationary while the targets undergo constant velocity motion. The simulation runs for 500 steps at 0.1 second increments, giving a total simulation time of 50 seconds.

```
nsteps = 500;
dt = .l;
timespan = nsteps*dt;
x1 = [60,0,0]';
x2 = [60,-80,40]';
x3 = [300,0,-300]';
v1 = [2,0,0]';
v2 = [10,5,6]';
v3 = [-10,2,-4]';
platform = phased.Platform([0,0,0]',[0,0,0]');
targets = phased.Platform([x1,x2,x3],[v1,v2,v3]);
```


## Set Up Range Bins

Each echo is put into a range bin. The range bin resolution is 1 meter and the range is from 50 to 1000 meters.

```
rngres = 1.0;
rngmin = 50.0;
rngmax = 1000.0;
rngscan = [rngmin:rngres:rngmax];
```


## Create the Gain Function

Define a range-dependent gain function to enhance the display of targets at larger ranges. The gain function amplifies the returned echo for visualization purposes only.

```
rangegain = @(rng)(1e12*rng^4);
```


## Create the Intensity Scope

Set up the Intensity Scope using these properties.

- Use the XResolution property to set the width of each scan line bin to the range resolution of 1 km.
- Use the XOffset property to set the value of the lowest range bin to the minimum range of 50 km.
- Use the TimeResolution property to set the value of the scan line time difference to 0.1 s .
- Use the TimeSpan property to set the height of the display window to the time duration of the simulation.
- Use the IntensityUnits property to set the display units to Watts.
scope $=$ phased.IntensityScope('Name','IntensityScope Display',...
'Title','Ranges vs. Time','XLabel','Range (m)','XResolution', rngres,...

```
'XOffset',rngmin,'TimeResolution',dt,'TimeSpan',timespan, ...
'IntensityUnits','Watts','Position',[100,100,800,450]);
```


## Run Simulation Loop

1 In this loop, move the targets at constant velocity using the step method of the phased. Platform System object.
2 Compute the target ranges using the rangeangle function.
3 Compute the target range bins by quantizing the range values in integer multiples of rngres.
4 Fill each target range bin and neighboring bins with a simulated radar intensity value.
5 Add the signal from each target to the scan line.
6 Call the step method of the phased. IntensityScope System object to display the scan lines.

```
for k = 1:nsteps
    xradar = platform(dt);
    xtgts = targets(dt);
    [rngs] = rangeangle(xtgts,xradar);
    scanline = zeros(size(rngscan));
    rngindx = ceil((rngs(1) - rngmin)/rngres);
    scanline(rngindx + [-1:1]) = rangegain(rngs(1))/(rngs(1)^4);
    rngindx = ceil((rngs(2) - rngmin)/rngres);
    scanline(rngindx + [-1:1]) = rangegain(rngs(2))/(rngs(2)^4);
    rngindx = ceil((rngs(3) - rngmin)/rngres);
    scanline(rngindx + [-1:1]) = rangegain(rngs(3))/(rngs(3)^4);
    scope(scanline.');
    pause(.1);
end
```



## RTI and DTI Displays in Full Radar Simulation

Use the phased.IntensityScope System Object ${ }^{T M}$ to display the detection output of a radar system simulation. The radar scenario contains a stationary single-element monostatic radar and three moving targets.

## Set Radar Operating Parameters

Set the maximum range, peak power range resolution, operating frequency, transmitter gain, and target radar cross-section.

```
max_range = 5000;
range_res = 50;
fc = \overline{1}0e9;
tx_gain = 20;
peak_power = 5500.0;
```

Choose the signal propagation speed to be the speed of light, and compute the signal wavelength corresponding to the operating frequency.
c = physconst('LightSpeed');
lambda $=\mathrm{c} / \mathrm{fc}$;

Compute the pulse bandwidth from the range resolution. Set the sampling rate, fs , to twice the pulse bandwidth. The noise bandwidth is also set to the pulse bandwidth. The radar integrates a number of pulses set by num_pulse_int. The duration of each pulse is the inverse of the pulse bandwidth.

```
pulse_bw = c/(2*range_res);
pulse_length = 1/pulse_bw;
fs = \overline{2*pulse bw;}
noise_bw = pulse bw;
num_pulse_int = 10;
```

Set the pulse repetition frequency to match the maximum range of the radar.

```
prf = c/(2*max_range);
```


## Create System Objects for the Model

Choose a rectangular waveform.

```
waveform = phased.RectangularWaveform('PulseWidth',pulse_length,...
    'PRF',prf,'SampleRate',fs);
```

Set the receiver amplifier characteristics.

```
amplifier = phased.ReceiverPreamp('Gain',20,'NoiseFigure',0,...
    'SampleRate',fs,'EnableInputPort',true,'SeedSource','Property',...
    'Seed',2007);
transmitter = phased.Transmitter('Gain',tx_gain,'PeakPower',peak_power,...
    'InUseOutputPort',true);
```

Specify the radar antenna as a single isotropic antenna.

```
antenna = phased.IsotropicAntennaElement('FrequencyRange',[5e9 15e9]);
```

Set up a monostatic radar platform.

```
radarplatform = phased.Platform('InitialPosition',[0; 0; 0],...
    'Velocity',[0; 0; 0]);
```

Set up the three target platforms using a single System object.

```
targetplatforms = phased.Platform(...
    'InitialPosition',[2000.66 3532.63 3845.04; 0 0 0; 0 0 0], ...
    'Velocity',[150 -150 0; 0 0 0; 0 0 0]);
```

Create the radiator and collector System objects.

```
radiator = phased.Radiator('Sensor',antenna,'OperatingFrequency',fc);
collector = phased.Collector('Sensor',antenna,'OperatingFrequency',fc);
```

Set up the three target RCS properties.

```
targets = phased.RadarTarget('MeanRCS',[1.6 2.2 1.05],'OperatingFrequency',fc);
```

Create System object to model two-way freespace propagation.

```
channels= phased.FreeSpace('SampleRate',fs,'TwoWayPropagation',true,...
    'OperatingFrequency',fc);
```

Define a matched filter.

MFcoef = getMatchedFilter(waveform);
filter = phased.MatchedFilter('Coefficients',MFcoef,'Gain0utputPort',true);

## Create Range and Doppler Bins

Set up the fast-time grid. Fast time is the sampling time of the echoed pulse relative to the pulse transmission time. The range bins are the ranges corresponding to each bin of the fast time grid.

```
fast_time = unigrid(0,1/fs,1/prf,'[)');
range_bins = c*fast_time/2;
```

To compensate for range loss, create a time varying gain System Object.

```
gain = phased.TimeVaryingGain('RangeLoss',2*fspl(range_bins,lambda),...
    'ReferenceLoss',2*fspl(max_range,lambda));
```

Set up Doppler bins. Doppler bins are determined by the pulse repetition frequency. Create an FFT System object for Doppler processing.

```
DopplerFFTbins = 32;
DopplerRes = prf/DopplerFFTbins;
fft = dsp.FFT('FFTLengthSource','Property',...
    'FFTLength',DopplerFFTbins);
```


## Create Data Cube

Set up a reduced data cube. Normally, a data cube has fast-time and slow-time dimensions and the number of sensors. Because the data cube has only one sensor, it is two-dimensional.

```
rx_pulses = zeros(numel(fast_time),num_pulse_int);
```


## Create IntensityScope System Objects

Create two IntensityScope System objects, one for Doppler-time-intensity and the other for range-time-intensity.

```
dtiscope = phased.IntensityScope('Name','Doppler-Time Display',...
    'XLabel','Velocity (m/sec)', ...
    'XResolution',dop2speed(DopplerRes,c/fc)/2, ...
    'X0ffset',dop2speed(-prf/2,c/fc)/2,...
    'TimeResolution',0.05,'TimeSpan',5,'IntensityUnits','Mag');
rtiscope = phased.IntensityScope('Name','Range-Time Display',...
    'XLabel','Range (m)', ...
    'XResolution',c/(2*fs), ...
    'TimeResolution',0.05,'TimeSpan',5,'IntensityUnits','Mag');
```


## Run the Simulation Loop over Multiple Radar Transmissions

Transmit 2000 pulses. Coherently process groups of 10 pulses at a time.
For each pulse:
1 Update the radar position and velocity radarplatform
2 Update the target positions and velocities targetplatforms
3 Create the pulses of a single wave train to be transmitted transmitter
4 Compute the ranges and angles of the targets with respect to the radar

5 Radiate the signals to the targets radiator
6 Propagate the pulses to the target and back channels
7 Reflect the signals off the target targets
8 Receive the signal sCollector
9 Amplify the received signal amplifier
10 Form data cube
For each set of 10 pulses in the data cube:
1 Match filter each row (fast-time dimension) of the data cube.
2 Compute the Doppler shifts for each row (slow-time dimension) of the data cube.
pri $=1 / p r f ;$
nsteps = 200;
for $k=1: n s t e p s$
for m = 1:num_pulse_int
[ant_pos, ant_vē] = radarplatform(pri);
[tgt_pos,tgt_vel] = targetplatforms(pri);
sig = waveform();
[s,tx_status] = transmitter(sig);
$\left[\sim, t g \bar{t} \_a n g\right]=$ rangeangle(tgt_pos,ant_pos);
tsig = radiator(s,tgt_ang);
tsig = channels(tsig,ant_pos,tgt_pos,ant_vel,tgt_vel);
rsig = targets(tsig);
rsig = collector(rsig,tgt_ang);
rx_pulses(:,m) = amplifier(rsig,~(tx_status>0));
end
rx_pulses = filter(rx_pulses);
MFdelay = size(MFcoef,1) - 1;
rx_pulses = buffer(rx_pulses((MFdelay + 1):end), size(rx_pulses,1));
rx_pulses = gain(rx_pulses);
range = pulsint(rx_pulses,'noncoherent');
rtiscope(range);
dshift = fft(rx_pulses.');
dshift = fftshift(abs(dshift), 1 );
dtiscope(mean(dshift,2));
radarplatform(.05);
targetplatforms(.05);
end



All of the targets lie on the x -axis. Two targets are moving along the x -axis and one is stationary. Because the radar is at the origin, you can read the target speed directly from the Doppler-Time Display window. The values agree with the specified velocities of $-150,150$, and $0 \mathrm{~m} / \mathrm{sec}$.

## Intensity Scope Display of Target Angular Motion

Use the phased.IntensityScope System object ${ }^{\mathrm{TM}}$ to display the angular motions of moving targets as functions of time. Each horizontal line (scan line) shows the strength of radar echoes at different azimuth angles. Azimuth space is divided into azimuth bins and each bin is filled with a simulated value depending upon the position of the targets.

## Create Radar and Target System Objects

Set up the initial positions and velocities of the three targets. Use the phased. Platform System object to model radar and target motions. The radar is stationary while the targets undergo constant velocity motion. The simulation runs for 200 steps at 0.5 second intervals, giving a total simulation time of 100 seconds.

```
nsteps = 200;
dt = 0.5;
timespan = nsteps*dt;
x1 = [60,0,0]';
```

```
x2 = [60,-80,40]';
x3 = [300,0,-300]';
x3 = [-300,0,-300]';
v1 = [2,0,0]';
v2 = [10,5,6]';
v3 = [-10,2,-4]';
radarplatform = phased.Platform([0,0,0]',[0,0,0]');
targets = phased.Platform([x1,x2,x3],[v1,v2,v3]);
```


## Set Up Azimuth Angle Bins

The signal for each echo is put into an angle bin and two adjacent bins. Bin resolution is 1 degree and the angle span is from -180 to 180 degrees.

```
angres = 1.0;
angmin = -180.0;
angmax = 180.0;
angscan = [angmin:angres:angmax];
na = length(angscan);
```


## Range Gain Function

Define a range-dependent gain function to enhance the display of targets at larger ranges. The gain function amplifies the returned echo for visualization purposes only.

```
rangegain = @(rng)(1e12*rng^4);
```


## Set Up Scope Viewer

The XResolution name-value pair specifies the width of each bin of the scan line. The XOffset sets the value of the lowest azimuth angle bin. The TimeResolution name-value pair specifies the time difference between scan lines. The TimeSpan name-value pair sets the height of the display window. A scan line is created with each call to the step method. Intensity units are amplitude units.

```
scope = phased.IntensityScope( ...
    'Name','IntensityScope Display',...
    'Title','Azimuth vs. Time',...
    'XLabel','Azimuth (deg)', ...
    'XResolution',angres,'X0ffset',angmin,...
    'TimeResolution',dt,'TimeSpan',timespan, ...
    'IntensityUnits','Watts',...
    'Position',[100,100,800,450]);
```


## Update-Display Loop

1 In this loop, move the targets at constant velocity using the step method of the phased. Platform System object.
2 Compute the target ranges and azimuth angles using the rangeangle function.
3 Compute the azimuth angle bins by quantizing the azimuth angle values in integer multiples of angres.
4 Fill each target azimuth bin and neighboring bins with a simulated radar intensity value.
5 Call the phased.IntensityScope step method to display the scan line.

```
for k = 1:nsteps
    xradar = radarplatform(dt);
```

```
    xtgts = targets(dt);
    [rngs,angs] = rangeangle(xtgts,xradar);
    scanline = zeros(size(angscan));
    angindx = ceil((angs(1,1) - angmin)/angres) + 1;
    idx = angindx + [-1:1];
    idx(idx>na)=[];
    idx(idx<1)=[];
    scanline(idx) = rangegain(rngs(1))/(rngs(1)^4);
    angindx = ceil((angs(1,2) - angmin)/angres) + 1;
    idx = angindx + [-1:1];
    idx(idx>na)=[];
    idx(idx<1)=[];
    scanline(idx) = rangegain(rngs(2))/(rngs(2)^4);
    angindx = ceil((angs(1,3) - angmin)/angres) + 1;
    idx = angindx + [-1:1];
    idx(idx>na)=[];
    idx(idx<1)=[];
    scanline(idx) = rangegain(rngs(3))/(rngs(3)^4);
    scope(scanline.');
    pause(.1);
end
```



## Version History

Introduced in R2016a

## phased.IsoSpeedUnderwaterPaths

Package: phased
Isospeed multipath sonar channel

## Description

The phased.IsoSpeedUnderwaterPaths System object creates an underwater acoustic channel to propagate narrowband sound from point to point. The channel has finite constant depth with airwater and water-bottom interfaces. Both interfaces are planar and horizontal. Sound speed is constant throughout the channel. The object generates multiple propagation paths in the channel using the acoustical method of images (see [3]). Because sound speed is constant, all propagation paths are straight lines between the source, boundaries, and receiver. There is always one direct line-of-sight path. For each propagation path, the object outputs range-dependent time delay, gain, Doppler factor, reflection loss, and spreading loss. You can use the channel data as input to the multipath sound propagator, phased.MultipathChannel.

To model an isospeed channel :
1 Define and set up the channel. You can set phased. IsoSpeedUnderwaterPaths System object properties at construction time or leave them to their default values. See "Construction" on page 1-733. Some properties that you set at construction time can be changed later. These properties are tunable.
2 To create the multipath channel, call the step method of phased. IsoSpeedUnderwaterPaths. The output of the method depends on the properties of the phased.IsoSpeedUnderwaterPaths System object. You can change tunable properties at any time.

Note Instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, $y=\operatorname{step}(o b j, x)$ and $y=$ obj $(x)$ perform equivalent operations.

## Construction

channel = phased.IsoSpeedUnderwaterPaths creates an isospeed multipath underwater channel System object, channel.
channel = phased.IsoSpeedUnderwaterPaths(Name,Value) creates an isospeed multipath underwater channel System object, channel, with each specified property Name set to the specified Value. You can specify additional name and value pair arguments in any order as
(Name1, Value1,...,NameN, ValueN).

## Properties

## ChannelDepth - Channel depth

100 (default) | positive scalar
Channel depth, specified as a positive scalar. Units are in meters.

## Example: 250.0

Data Types: double

## PropagationSpeed - Underwater sound propagation speed <br> 1520.0 (default) | positive scalar

Underwater sound propagation speed, specified as a positive scalar. Units are in meter per second. The default value is a commonly-used underwater sound propagation speed.

Example: 1502.0
Data Types: double

## NumPathsSource - Source of number of propagation paths <br> 'Auto' (default)|'Property'

The source of the number of propagation paths, specified as 'Auto' or 'Property '. If you set this property to 'Auto', the object automatically determines the number of paths based on spreading and reflection losses. If you set this property to 'Property', you specify the number of paths using the NumPaths property.

When NumPathsSource is set to 'Auto', only paths having a total loss greater than 20 dB below the direct path loss are returned.

Example: 'Property'
Data Types: char
NumPaths - Number of propagation paths
10 (default) | positive integer
The number of propagation paths, specified as a positive integer between 1 and 51 , inclusive.
Example: 11

## Dependencies

To enable this property, set the NumPathsSource property to 'Property '.
Data Types: double

## CoherenceTime - Channel coherence time

0 (default) | nonnegative scalar
Channel coherence time, specified as a nonnegative scalar. Coherence time is a measure of the temporal stability of the channel. The object keeps a record of cumulative step time. When the cumulative step time exceeds the coherence time, propagation paths are recomputed and the cumulative step time is reset to zero. If you set this quantity to zero, the propagation paths are update at each call to step. Units are in seconds.
Example: 5.0
Data Types: double

## BottomLoss - Bottom reflection loss

6 (default) | nonnegative scalar
Bottom reflection loss, specified as a nonnegative scalar. This value applies to each bottom reflection of a path. Units are in dB .

## Example: 10

Data Types: double

## LossFrequencies - Absorption loss frequencies

[1:100]*1000 (default) | positive real-valued vector
Frequencies for which to compute absorption loss, specified as a positive real-valued vector. Units are in Hz .

Example: [1000:100:3000]
Data Types: double

## TwoWayPropagation - Enable two-way propagation

## false (default) | true

Enable two-way propagation, specified as a false or true. Set this property to true to perform round-trip propagation between the signal origin and destination specified in step. Set this property to false to perform only one-way propagation from the origin to the destination.

## Example: true

Data Types: logical

## Methods

step Create propagation paths in an isospeed multipath sound channel
reset Reset state of System object

## Common to All System Objects

release Allow System object property value changes

## Examples

## Create One-Way Multipath Underwater Sound Channel

Create a 5 -path underwater sound channel and display the propagation path matrix. Assume the source is stationary and the receiver is moving along the $x$-axis towards the source at 20 kph . Assume one-way propagation.

```
speed = -20*1000/3600;
numpaths = 5;
channelpaths = phased.IsoSpeedUnderwaterPaths('ChannelDepth',200,'BottomLoss',10, ...
    'NumPathsSource','Property','NumPaths',numpaths,'CoherenceTime',5);
tstep = 1;
srcpos = [0;0;-160];
rcvpos = [500;0;-50];
srcvel = [0;0;0];
rcvvel = [speed;0;0];
pathmat = channelpaths(srcpos,rcvpos,srcvel,rcvvel,tstep);
disp(pathmat)
```

| 0.3356 | 0.3556 | 0.4687 | 0.3507 | 0.3791 |
| ---: | ---: | ---: | ---: | ---: |
| 1.0000 | -1.0000 | -0.3162 | 0.3162 | -0.3162 |
| 54.1847 | 54.6850 | 57.0766 | 54.5652 | 55.2388 |

The first row contains the time delay in seconds. The second row contains the bottom reflection loss coefficients, and the third row contains the spreading loss in dB . The reflection loss coefficient for the first path is 1.0 because the direct path has no boundary reflections. The reflection loss coefficient for the second path is -1.0 because the path has only a surface reflection.

## Create Two-Way Multipath Underwater Sound Channel

Create a 7-path underwater sound channel and display the propagation path matrix. Assume the source is stationary and the target is moving along the $x$-axis towards the source at 20 kph . Assume two-way propagation.

```
speed = -20*1000/3600;
numpaths = 7;
channelpaths = phased.IsoSpeedUnderwaterPaths('ChannelDepth',200,'BottomLoss',10, ...
    'NumPathsSource','Property','NumPaths',numpaths,'CoherenceTime',5,...
    'TwoWayPropagation',true);
tstep = 1;
srcpos = [0;0;-160];
tgtpos = [500;0;-50];
srcvel = [0;0;0];
tgtvel = [speed;0;0];
[pathmat,dop,aloss,tgtangs,srcangs] = channelpaths(srcpos,tgtpos,srcvel,tgtvel,tstep);
disp(pathmat)
\begin{tabular}{rrrrrrr}
0.6712 & 0.7112 & 0.9374 & 1.0354 & 0.7014 & 0.7581 & 1.0152 \\
1.0000 & 1.0000 & 0.1000 & 0.1000 & 0.1000 & 0.1000 & 0.0100 \\
\hline 8.3693 & 9.369 & 114.1531 & 15.8772 & 109.1304 & 110.4775 & 115.5355
\end{tabular}
```

The first row contains the time delay in seconds. The second row contains the bottom reflection loss coefficients, and the third row contains the spreading loss in dB . The reflection loss coefficient for the first path is 1.0 because the direct path has no boundary reflections. The reflection loss coefficient for the second path is -1.0 because the path has only a surface reflection.

## Propagate Sound in Channel Having Unknown Number of Paths

Create an underwater sound channel and plot the combined received signal. Automatically find the number of paths. Assume that the source is stationary and that the receiver is moving along the $x$-axis toward the source at $20 \mathrm{~km} / \mathrm{h}$. Assume the default one-way propagation.

```
speed = -20*1000/3600;
channel = phased.IsoSpeedUnderwaterPaths('ChannelDepth',200,'BottomLoss',5, ...
    'NumPathsSource','Auto','CoherenceTime',5);
tstep = 1;
srcpos = [0;0;-160];
rcvpos = [500;0;-50];
srcvel = [0;0;0];
rcvvel = [speed;0;0];
```

Compute the path matrix, Doppler factor, and losses. The propagator outputs 51 paths output but some paths can contain Nan values.
[pathmat,dop,absloss,rcvangs,srcangs] = channel(srcpos,rcvpos,srcvel,rcvvel,tstep);
Create of a 100 Hz signal with 500 samples. Assume that all the paths have the same signal. Use a phased.MultipathChannel System object ${ }^{\mathrm{TM}}$ to propagate the signals to the receiver.
phased.MultipathChannel accepts as input all paths produced by phased.IsoSpeedUnderwaterPaths but ignores paths that have NaN values.

```
fs = 1e3;
nsamp = 500;
propagator = phased.MultipathChannel('OperatingFrequency',10e3,'SampleRate',fs);
t = [0:(nsamp-1)]'/fs;
sig0 = sin(2*pi*100*t);
numpaths = size(pathmat,2);
sig = repmat(sig0,1,numpaths);
propsig = propagator(sig,pathmat,dop,absloss);
```

Plot the real part of the coherent sum of the propagated signals.
plot(t*1000, real(sum(propsig,2)))
xlabel('Time (millisec)')


## Doppler Stretching of Sonar Signal

Compare the duration of a propagated signal from a stationary sonar to that of a moving sonar. The moving sonar has a radial velocity of $25 \mathrm{~m} / \mathrm{s}$ away from the target. In each case, propagate the signal along a single path. Assume one-way propagation.

Define the sonar system parameters: maximum unambiguous range, required range resolution, operating frequency, and propagation speed.

```
maxrange = 5000.0;
rngres = 10.0;
fc = 20.0e3;
csound = 1520.0;
```

Use a rectangular waveform for the transmitted signal.

```
prf = csound/(2*maxrange);
pulseWidth = 8*rngres/csound;
pulseBW = 1/pulseWidth;
fs = 80*pulseBW;
waveform = phased.RectangularWaveform('PulseWidth',pulseWidth,'PRF',prf, ...
    'SampleRate',fs);
```

Specify the sonar positions.

```
sonarplatform1 = phased.Platform('InitialPosition',[0;0;-60],'Velocity',[0;0;0]);
sonarplatform2 = phased.Platform('InitialPosition',[0;0;-60],'Velocity',[0;-25;0]);
```

Specify the target position.

```
targetplatform = phased.Platform('InitialPosition',[0;500;-60],'Velocity',[0;0;0]);
```

Define the underwater path and propagation channel objects.

```
paths = phased.IsoSpeedUnderwaterPaths('ChannelDepth',100, ...
    'CoherenceTime',0,'NumPathsSource','Property','NumPaths',1, ...
    'PropagationSpeed',csound);
propagator = phased.MultipathChannel('SampleRate',fs,'OperatingFrequency',fc);
```

Create the transmitted waveform.

```
wav = waveform();
nsamp = size(wav,1);
rxpulses = zeros(nsamp,2);
t = (0:nsamp-1)/fs;
```

Transmit the signal and then receive the echo at the stationary sonar.

```
[pathmat,dop,aloss,~,~] = paths(sonarplatform1.InitialPosition, ...
    targetplatform.InitialPosition, sonarplatform1.InitialVelocity, ...
    targetplatform.InitialVelocity,1/prf);
rxpulses(:,1) = propagator(wav,pathmat,dop,aloss);
```

Transmit and receive at the moving sonar.

```
[pathmat,dop,aloss,~,~] = paths(sonarplatform2.InitialPosition, ...
    targetplatform.InitialPosition, sonarplatform2.Velocity, ...
    targetplatform.Velocity,1/prf);
rxpulses(:,2) = propagator(wav,pathmat,dop,aloss);
```

Plot the received pulses.
plot(abs(rxpulses))
xlim([490 650])
ylim([0 1.65e-3])
legend('Stationary sonar','Moving sonar')
xlabel('Received Sample Time (sec)')
ylabel('Integrated Received Pulses')


The signal received at the moving sonar has increased in duration compared to the stationary sonar.

## Version History

## Introduced in R2017a

## References

[1] Urick, R.J. Principles of Underwater Sound, 3rd Edition. New York: Peninsula Publishing, 1996.
[2] Sherman, C.S. and J.Butler Transducers and Arrays for Underwater Sound. New York: Springer, 2007.
[3] Allen, J.B. and D. Berkely, "Image method for efficiently simulating small-room acoustics", J. Acoust. Soc. Am, Vol 65, No. 4. April 1979.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
See "System Objects in MATLAB Code Generation" (MATLAB Coder).

## See Also

## Objects

phased.BackscatterSonarTarget | phased.IsotropicHydrophone |
phased.IsotropicProjector|phased.MultipathChannel
Topics
"Underwater Target Detection with an Active Sonar System"
"Locating an Acoustic Beacon with a Passive Sonar System"

## step

## System object: phased. IsoSpeedUnderwaterPaths <br> Package: phased

Create propagation paths in an isospeed multipath sound channel

## Syntax

pathmat = step(channel, srcpos,destpos,srcvel,destvel,T)
[pathmat,dop,aloss,destang,srcang] = step(channel,srcpos,destpos,srcvel,
destvel,T)

## Description

Note Instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, $\mathrm{y}=\mathrm{step}(\mathrm{obj}, \mathrm{x})$ and $\mathrm{y}=$ obj $(x)$ perform equivalent operations.
pathmat $=$ step(channel,srcpos,destpos,srcvel,destvel,T) returns the propagation paths matrix, pathmat, for a multipath underwater acoustic channel. The matrix describes one or two-way propagation from the signal source position, srcpos, to the signal destination position, destpos. The velocity of the signal source is specified in srcvel and the velocity of the signal destination is specified in destvel. T is the step time interval.

When you use this method for one-way propagation, srcpos refers to the origin of the signal and destpos to the receiver. One-way propagation modeling is useful for passive sonar and underwater communications.

When you use this method for two-way propagation, destpos now refers to the reflecting target, not the sonar receiver. A two-way path consists of a one-way path from source to target and then along an identical one-way path from target to receiver (which is collocated with the source). Two-way propagation modeling is useful for active sonar systems.
[pathmat,dop,aloss,destang,srcang] = step(channel,srcpos,destpos,srcvel, destvel, T ) also returns the Doppler factor, dop, the frequency dependent absorption loss, aloss, the receiver arrival angles, destang, and the srcang transmitting angles.

When you use this method for two-way propagation, destang now refers to the reflecting target, not the sonar receiver.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

Note Instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, $y=s t e p(o b j, x)$ and $y=$ obj (x) perform equivalent operations.

## Input Arguments

channel - Isospeed underwater channel path
phased.IsoSpeedUnderwaterPaths System object
Isospeed underwater channel paths, specified as a phased.IsoSpeedUnderwaterPaths System object.
Example: phased.IsoSpeedUnderwaterPaths
srcpos - Source of sonar signals
real-valued 3-by-1 column vector
Source of the sonar signal, specified as a real-valued 3-by-1 column vector. Position units are meters.
Example: [1000;100;500]
Data Types: double
destpos - Destination of signal
real-valued 3-by-1 column vector
Destination position of the signal, specified as a real-valued 3-by-1 column vector. Position units are in meters.

Example: [0;0;0]
Data Types: double

## srcvel - Velocity of signal source

real-valued 3-by-1 column vector
Velocity of signal source, specified as a real-valued 3-by-1 column vector. Velocity units are in meters per second.
Example: [10;0;5]
Data Types: double

## destvel - Velocity of signal destination

real-valued 3-by-1 column vector
Velocity of signal destination, specified as a real-valued 3-by-1 column vector. Velocity units are in meters per second.
Example: [0;0;0]
Data Types: double

## T - Elapsed time of current step <br> positive scalar

Elapsed time of current step, specified as a positive scalar. Time units are in seconds.

Example: 0.1
Data Types: double

## Output Arguments

## pathmat - Propagation paths matrix

real-valued 3 -by- $N$ matrix
Propagation paths matrix, returned as a real-valued 3-by- $N$ matrix. $N$ is the number of paths in the channel. Each column represents a path. When you set NumPathsSource to 'Auto',$N$ is 51 . In this case, any columns filled with NaN do not correspond to found paths. The matrix rows represent:

| Row | Data |
| :--- | :--- |
| 1 | Propagation delays for each path. Units are in seconds. |
| 2 | Total reflection coefficient for each path. Units are dimensionless |
| 3 | Spreading loss for each path. Units are in dB. |

Except for the direct path, paths consists of alternating surface and bottom reflections. The losses for multiple reflections are multiplied. Bottom loss per reflection is specified by the BottomLoss property. The loss at the surface is -1 indicating no loss, but only a $180^{\circ}$ phase change. This is because the air-water interface surface is a pressure-release surface.

Data Types: double

## dop - Doppler factor

real-valued $N$-by-1 row vector
Doppler factor, returned as a real-valued $N$-by- 1 row vector where $N$ is the number of paths. The Doppler factor multiplies the transmitted frequency to produce the Doppler-shifted received frequency for each path. The Doppler shift is defined as the difference between the transmitted frequency and the received frequency. The Doppler factor also defines the time compression or expansion of a signal. Units are dimensionless.
Data Types: double
aloss - Frequency-dependent absorption loss
real-valued $K$-by-( $N+1$ ) matrix
Frequency-dependent absorption loss, returned as a real-valued $K$-by-( $N+1$ ) matrix. $K$ is the number of frequencies specified in the LossFrequencies property. $N$ is the number of paths returned. The first column of aloss contains the absorption loss frequencies in Hz. You specify the frequencies using the LossFrequencies property. The remaining columns contain the absorption losses for each frequency. There is one column for each path. Units are in dB.

## Data Types: double

## destang - Angles of paths at destination

real-valued 2 -by- $N$ matrix
Angles of paths at destination, returned as a real-valued 2-by- $N$ matrix. Each column contains the direction of the received path with respect to the destination position as azimuth and elevation, [az;el]. Units are in degrees.
Data Types: double

## srcang - Angles of paths from source

real-valued 2-by- $N$ matrix
Angles of paths from source, returned as a real-valued 2-by- $N$ matrix. Each column contains the direction of the transmitted path with respect to the source position as azimuth and elevation, [az;el]. Units are in degrees.

Data Types: double

## Examples

## Create One-Way Multipath Underwater Sound Channel

Create a 5 -path underwater sound channel and display the propagation path matrix. Assume the source is stationary and the receiver is moving along the $x$-axis towards the source at 20 kph . Assume one-way propagation.

```
speed = -20*1000/3600;
numpaths = 5;
channelpaths = phased.IsoSpeedUnderwaterPaths('ChannelDepth',200,'BottomLoss',10, ...
    'NumPathsSource','Property','NumPaths',numpaths,'CoherenceTime',5);
tstep = 1;
srcpos = [0;0;-160];
rcvpos = [500;0;-50];
srcvel = [0;0;0];
rcvvel = [speed;0;0];
pathmat = channelpaths(srcpos,rcvpos,srcvel,rcvvel,tstep);
disp(pathmat)
\begin{tabular}{rrrrr}
0.3356 & 0.3556 & 0.4687 & 0.3507 & 0.3791 \\
1.0000 & -1.0000 & -0.3162 & 0.3162 & -0.3162
\end{tabular}
54.1847 54.6850 57.0766 54.5652 55.2388
```

The first row contains the time delay in seconds. The second row contains the bottom reflection loss coefficients, and the third row contains the spreading loss in dB . The reflection loss coefficient for the first path is 1.0 because the direct path has no boundary reflections. The reflection loss coefficient for the second path is -1.0 because the path has only a surface reflection.

## Create Two-Way Multipath Underwater Sound Channel

Create a 7-path underwater sound channel and display the propagation path matrix. Assume the source is stationary and the target is moving along the $x$-axis towards the source at 20 kph . Assume two-way propagation.

```
speed = -20*1000/3600;
numpaths = 7;
channelpaths = phased.IsoSpeedUnderwaterPaths('ChannelDepth',200,'BottomLoss',10, ...
    'NumPathsSource','Property','NumPaths',numpaths,'CoherenceTime',5,...
    'TwoWayPropagation',true);
tstep = 1;
srcpos = [0;0;-160];
tgtpos = [500;0;-50];
srcvel = [0;0;0];
```

tgtvel = [speed;0;0];
[pathmat,dop,aloss,tgtangs,srcangs] = channelpaths(srcpos,tgtpos,srcvel,tgtvel,tstep); disp(pathmat)

| 0.6712 | 0.7112 | 0.9374 | 1.0354 | 0.7014 | 0.7581 | 1.0152 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1.0000 | 1.0000 | 0.1000 | 0.1000 | 0.1000 | 0.1000 | 0.0100 |
| 108.3693 | 109.3699 | 114.1531 | 115.8772 | 109.1304 | 110.4775 | 115.5355 |

The first row contains the time delay in seconds. The second row contains the bottom reflection loss coefficients, and the third row contains the spreading loss in dB. The reflection loss coefficient for the first path is 1.0 because the direct path has no boundary reflections. The reflection loss coefficient for the second path is -1.0 because the path has only a surface reflection.

## Automatically Find the Number of Paths

Create an underwater sound channel and display the propagation paths which are found automatically. Assume the source is stationary and the receiver is moving along the $x$-axis towards the source at 20 kph . Assume two-way propagation.

```
speed = -20*1000/3600;
channelpaths = phased.IsoSpeedUnderwaterPaths('ChannelDepth',200,'BottomLoss',5, ...
    'NumPathsSource','Auto','CoherenceTime',5,'TwoWayPropagation',true);
tstep = 1;
srcpos = [0;0;-160];
tgtpos = [500;0;-50];
srcvel = [0;0;0];
tgtpos = [speed;0;0];
[pathmat,dop,aloss,rcvangs,srcangs] = channelpaths(srcpos,tgtpos,srcvel,tgtpos,tstep);
```

Display the first 7 columns of pathmat. Some columns are filled with NaNs.

```
disp(pathmat(:,1:7))
\begin{tabular}{rrrllll}
0.2107 & 0.2107 & NaN & NaN & NaN & NaN & NaN \\
1.0000 & 1.0000 & NaN & NaN & NaN & NaN & NaN \\
88.1753 & 88.1753 & NaN & NaN & NaN & NaN & NaN
\end{tabular}
```

Select the column indices of the valid paths from the entire matrix.

```
idx = find(~isnan(pathmat(1,:)))
idx = 1x4
    1 2 27 28
```

Display the valid paths information.

```
validpaths = pathmat(:,idx)
validpaths = 3×4
```

| 0.2107 | 0.2107 | 0.3159 | 0.3159 |
| ---: | ---: | ---: | ---: |
| 1.0000 | 1.0000 | 0.3162 | 0.3162 |
| 88.1753 | 88.1753 | 95.2131 | 95.2131 |

The first row contains the time delays in seconds. The second row contains the bottom reflected loss coefficients, and the third row contains the spreading losses.

## Version History

Introduced in R2017a

## reset

System object: phased.IsoSpeedUnderwaterPaths
Package: phased
Reset state of System object

## Syntax

reset (channel)

## Description

reset (channel) resets the internal state of the phased.IsoSpeedUnderwaterPaths object, channel. This method resets the coherence time clock.

## Input Arguments

## channel - Isospeed underwater channel path

phased.IsoSpeedUnderwaterPaths System object
Isospeed underwater channel paths, specified as a phased.IsoSpeedUnderwaterPaths System object.

Example: phased.IsoSpeedUnderwaterPaths

## Version History

Introduced in R2017a

# phased.IsotropicAntennaElement 

Package: phased
Isotropic antenna element

## Description

The phased.IsotropicAntennaElement object creates an antenna element with an isotropic response pattern. The object models an antenna element whose response is unity in all directions. An isotropic antenna does not support polarization.

To compute the response of the antenna element for specified directions:
1 Create the phased.IsotropicAntennaElement object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

```
antenna = phased.IsotropicAntennaElement
antenna = phased.IsotropicAntennaElement(Name,Value)
```


## Description

antenna = phased.IsotropicAntennaElement creates an isotropic antenna System object, antenna, with default property values.
antenna = phased.IsotropicAntennaElement(Name, Value) creates an isotropic antenna object, antenna, with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN).

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

FrequencyRange - Operating frequency range
[0 1e20] (default) | nonnegative, real-valued 1-by-2 row vector

Operating frequency range of the antenna, specified as a nonnegative, real-valued, 1-by-2 row vector in the form [LowerBound HigherBound]. The antenna element has no response outside the specified frequency range. Units are in Hz .

## Data Types: double

## BackBaffled - Backbaffle antenna element <br> false (default) | true

Backbaffle the antenna element, specified as false or true. Set this property to true to baffle the response on the backside of the antenna element. In this case, the antenna response to all azimuth angles beyond $\pm 90^{\circ}$ from broadside ( $0^{\circ}$ azimuth and $0^{\circ}$ elevation) is zero. When the value of this property is false, the back of the antenna element is not baffled.
Data Types: logical

## Usage

## Syntax

RESP = antenna(FREQ, ANG)

## Description

RESP = antenna (FREQ, ANG) returns the antenna voltage response RESP at operating frequencies specified in FREQ and in directions specified in ANG.

## Input Arguments

## FREQ - Operating frequency of antenna element

nonnegative scalar | nonnegative, real-valued 1-by- $L$ row vector
Operating frequency of the antenna element, specified as a nonnegative scalar or nonnegative, realvalued 1 -by- L row vector. Frequency units are in Hz .

FREQ must lie within the range of values specified by the FrequencyRange or the
FrequencyVector property of the element. Otherwise, the element produces no response and the response is returned as -Inf. Element objects use the FrequencyRange property, except for phased. CustomAntennaElement, which uses the FrequencyVector property.

Example: [1e8 2e6]
Data Types: double

## ANG - Azimuth and elevation angles of response directions

real-valued 1-by-M row vector | real-valued 2-by-M matrix
Azimuth and elevation angles of the response directions, specified as a real-valued 1-by- $M$ row vector or a real-valued 2-by- $M$ matrix, where $M$ is the number of angular directions. Angle units are in degrees. The azimuth angle must lie in the range $-180^{\circ}$ to $180^{\circ}$, inclusive. The elevation angle must lie in the range $-90^{\circ}$ to $90^{\circ}$, inclusive.

- If ANG is a 1 -by-M vector, each element specifies the azimuth angle of the direction. In this case, the corresponding elevation angle is assumed to be zero.
- If ANG is a 2-by-M matrix, each column of the matrix specifies the direction in the form [azimuth;elevation].

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the $x y$-plane. This angle is positive when measured from the $x$-axis toward the $y$-axis. The elevation angle is the angle between the direction vector and $x y$-plane. This angle is positive when measured toward the $z$-axis. See the definition of "Azimuth and Elevation Angles".

Example: [110 125; 15 10]
Data Types: double

## Output Arguments

RESP - Voltage response of antenna
complex-valued $M$-by- $L$ matrix
Voltage response of antenna element, returned as a complex-valued $M$-by- $L$ matrix. In this matrix, $M$ represents the number of angles specified in ANG and $L$ represents the number of frequencies specified in FREQ.
Data Types: double

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```


## Specific to Antenna and Transducer Element System Objects

beamwidth
directivity
isPolarizationCapable
pattern
patternAzimuth
patternElevation

Compute and display beamwidth of sensor element pattern
Directivity of antenna or transducer element
Antenna element polarization capability
Plot antenna or transducer element directivity and patterns
Plot antenna or transducer element directivity and pattern versus azimuth
Plot antenna or transducer element directivity and pattern versus elevation

## Common to All System Objects

step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object

## Examples

## Plot Isotropic Antenna Element Response

Create an isotropic antenna operating over a frequency range from 800 MHz to 1.2 GHz . The operating frequency is 1 GHz . Find the response of the antenna at boresight. Then, plot the polarpattern elevation response of the antenna.

```
antenna = phased.IsotropicAntennaElement( ...
    'FrequencyRange',[800e6 1.2e9]);
fc = 1e9;
```

Obtain the response at boresight.

```
resp = antenna(fc,[0;0])
resp = 1
```

Plot the response pattern.

```
pattern(antenna,fc,0,[-90:90],'CoordinateSystem','polar', ...
    'Type','powerdb','Normalize',true)
```



Normalized Power (dB), Broadside at $0.00^{\circ}$

## Isotropic Antenna Does Not Support Polarization

Create an isotropic antenna element using the phased.Isot ropicAntennaElement System object ${ }^{T M}$ and show that it does not support polarization.

```
antenna = phased.IsotropicAntennaElement('FrequencyRange',[1.0,10]*1e9);
isPolarizationCapable(antenna)
ans = logical
    0
```

The returned value 0 shows that the antenna element does not support polarization.

## Directivity of Isotropic Antenna Element

Compute the directivity of an isotropic antenna element in different directions.
Create an isotropic antenna element System object ${ }^{\mathrm{TM}}$.

```
antenna = phased.IsotropicAntennaElement();
```

First, specify that the directions of interest all at an elevation angle of zero degrees. The seven azimuth angles are centered around boresight (zero degrees azimuth and zero degrees elevation). Set the frequency to 1 GHz .

```
ang = [-30,-20,-10,0,10,20,30; 0,0,0,0,0,0,0];
freq = 1e9;
Compute the directivity along the constant elevation cut.
d = directivity(antenna,freq,ang)
d = 7x1
    0
    0
    0
    0
    0
    0
    0
```

Next, specify that the directions of interest all at an azimuth angle of zero degrees. All elevation angles are centered around boresight. The five elevation angles range from -20 to +20 degrees, inclusive. Set the frequency to 1 GHz .

```
ang = [0,0,0,0,0; -20,-10,0,10,20];
freq = 1e9;
Compute the directivity along the constant azimuth cut.
```

```
d = directivity(antenna,freq,ang)
```

d = directivity(antenna,freq,ang)
d = 5×1
0
0
0
0
0

```

For an isotropic antenna, the directivity is independent of direction.

\section*{Plot Pattern and Directivity of Isotropic Antenna}

Create an isotropic antenna element. Then, plot the antenna power pattern and directivity.
First, create the antenna.
antenna \(=\) phased.IsotropicAntennaElement;
Draw an azimuth cut of the power pattern at 0 degrees elevation. Assume the operating frequency is 1 GHz .
fc = 1e9;
pattern(antenna,fc,[-180:180],0,...
'Type','power',...
'CoordinateSystem', 'rectangular')


Draw the same azimuth cut of the antenna directivity.
pattern(antenna,fc, [-180:180],0,...
'Type','directivity',...
'CoordinateSystem','rectangular')


\section*{Elevation-Cut of Isotropic Antenna Pattern}

Construct an isotropic antenna operating in the frequency range from 800 MHz to 1.2 GHz . Compute the response at boresight at 1 GHz . Display the power pattern of the antenna at 1 GHz .
```

antenna = phased.IsotropicAntennaElement(...
'FrequencyRange',[800e6 1.2e9]);
fc = 1e9;
resp = antenna(fc,[0;0])
resp = 1

```

Plot the elevation power pattern of the antenna in polar coordinates.
```

pattern(antenna,fc,0,[-90:90],'Type','powerdb','CoordinateSystem','polar')

```


Normalized Power (dB), Broadside at \(0.00^{\circ}\)

\section*{3-D Isotropic Antenna Pattern}

Construct an isotropic antenna operating over a frequency range from 800 MHz to 1.2 GHz . Then, plot the 3-D antenna field pattern.

Construct an isotropic antenna element.
antenna \(=\) phased.IsotropicAntennaElement(...
'FrequencyRange',[800e6 1.2e9]);
Plot the 3-D magnitude pattern of the antenna at 1 GHz from -30 to 30 degrees in both azimuth and elevation in 0.1 degree increments.
fc = 1e9;
pattern(antenna,fc,[-30:0.1:30],[-30:0.1:30],...
'Type', 'efield',...
'CoordinateSystem', 'polar')


\section*{Directivity Pattern of Isotropic Antenna Element for Span of Azimuth Angles}

Plot an azimuth cut of the directivity of an isotropic antenna element at 0 degrees elevation for all azimuth angles and at 30 degrees elevation for a small span of azimuth angles. Assume the operating frequency is 500 MHz .

Create the antenna element.
```

fc = 500e6;

```
antenna = phased.IsotropicAntennaElement('FrequencyRange',[100,900]*1e6);

Plot the pattern for all azimuth angles at 0 degrees elevation.
patternAzimuth(antenna,fc, 0 )


Directivity (dBi), Broadside at \(0.00^{\circ}\)

Plot the pattern for a reduced span of azimuth angles using the Azimuth parameter.
patternAzimuth(antenna,fc,30,'Azimuth',[-20:20])


Directivity (dBi), Broadside at \(0.00^{\circ}\)

\section*{Directivity Pattern of Isotropic Antenna Element for Span of Elevation Angles}

Plot an elevation cut of directivity of an isotropic antenna element at 45 degrees azimuth for all elevation angles and at 45 degrees for a span of elevation angles. Assume the operating frequency is 500 MHz .

Create the antenna element.
fc = 500e6;
antenna \(=\) phased.IsotropicAntennaElement('FrequencyRange', [100, 900]*1e6);
Plot the directivity for all elevation angles.
patternElevation(antenna,fc,45)


Directivity (dBi), Broadside at \(0.00^{\circ}\)

Plot the directivity for a span of elevation angles using the Elevation parameter. patternElevation(antenna,fc,45,'Elevation',[-20:20])


Directivity (dBi), Broadside at \(0.00^{\circ}\)

\section*{Version History}

Introduced in R2011a

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder \(^{\text {TM }}\).
Usage notes and limitations:
- pattern, patternAzimuth, and patternElevation object functions are not supported.
- See "System Objects in MATLAB Code Generation" (MATLAB Coder).

\section*{See Also}
phased.ConformalArray | phased.CosineAntennaElement | phased.CrossedDipoleAntennaElement | phased.CustomAntennaElement| phased.CustomMicrophoneElement | phased.OmnidirectionalMicrophoneElement | phased. ShortDipoleAntennaElement | phased.ULA | phased.URA|uv2azel| phitheta2azel

\section*{directivity}

System object: phased. IsotropicAntennaElement
Package: phased
Directivity of isotropic antenna element

\section*{Syntax}

D = directivity(H,FREQ,ANGLE)

\section*{Description}

D = directivity (H,FREQ,ANGLE) returns the "Directivity (dBi)" on page 1-763 of an isotropic antenna element, H , at frequencies specified by FREQ and in direction angles specified by ANGLE.

\section*{Input Arguments}

\section*{H - Isotropic antenna element}

System object
Isotropic antenna element specified as a phased.IsotropicAntennaElement System object.
Example: H = phased.IsotropicAntennaElement;

\section*{FREQ - Frequency for computing directivity and patterns}
positive scalar | 1-by-L real-valued row vector
Frequencies for computing directivity and patterns, specified as a positive scalar or 1-by-L realvalued row vector. Frequency units are in hertz.
- For an antenna, microphone, or sonar hydrophone or projector element, FREQ must lie within the range of values specified by the FrequencyRange or FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased. CustomAntennaElement and phased.CustomMic rophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

\section*{Example: [1e8 2e6]}

Data Types: double

\section*{ANGLE - Angles for computing directivity}

1-by-M real-valued row vector | 2 -by- \(M\) real-valued matrix
Angles for computing directivity, specified as a 1-by- \(M\) real-valued row vector or a 2 -by- \(M\) real-valued matrix, where \(M\) is the number of angular directions. Angle units are in degrees. If ANGLE is a 2 -by- \(M\) matrix, then each column specifies a direction in azimuth and elevation, [az;el]. The azimuth angle must lie between \(-180^{\circ}\) and \(180^{\circ}\). The elevation angle must lie between \(-90^{\circ}\) and \(90^{\circ}\).

If ANGLE is a 1 -by- \(M\) vector, then each entry represents an azimuth angle, with the elevation angle assumed to be zero.

The azimuth angle is the angle between the \(x\)-axis and the projection of the direction vector onto the \(x y\) plane. This angle is positive when measured from the \(x\)-axis toward the \(y\)-axis. The elevation angle is the angle between the direction vector and xy plane. This angle is positive when measured towards the \(z\)-axis. See "Azimuth and Elevation Angles".
Example: [45 60; 0 10]
Data Types: double

\section*{Output Arguments}

\section*{D - Directivity}

M-by-L matrix
Directivity, returned as an \(M\)-by- \(L\) matrix. Each row corresponds to one of the \(M\) angles specified by ANGLE. Each column corresponds to one of the \(L\) frequency values specified in FREQ. Directivity units are in dBi where dBi is defined as the gain of an element relative to an isotropic radiator.

\section*{Examples}

\section*{Directivity of Isotropic Antenna Element}

Compute the directivity of an isotropic antenna element in different directions.
Create an isotropic antenna element System object \({ }^{\text {TM }}\).
antenna \(=\) phased.IsotropicAntennaElement();
First, specify that the directions of interest all at an elevation angle of zero degrees. The seven azimuth angles are centered around boresight (zero degrees azimuth and zero degrees elevation). Set the frequency to 1 GHz .
```

ang = [-30,-20,-10,0,10,20,30; 0,0,0,0,0,0,0];
freq = 1e9;

```

Compute the directivity along the constant elevation cut.
```

d = directivity(antenna,freq,ang)
d = 7x1

```
    0
    0
    0
    0
    0
    0
    0

Next, specify that the directions of interest all at an azimuth angle of zero degrees. All elevation angles are centered around boresight. The five elevation angles range from -20 to +20 degrees, inclusive. Set the frequency to 1 GHz .
```

ang = [0,0,0,0,0; -20,-10,0,10,20];
freq = 1e9;

```

Compute the directivity along the constant azimuth cut.
```

d = directivity(antenna,freq,ang)

```
\(d=5 \times 1\)

0
0
0
0
0

For an isotropic antenna, the directivity is independent of direction.

\section*{More About}

\section*{Directivity (dBi)}

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power
\[
D=4 \Pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
\]
where \(U_{\mathrm{rad}}(\theta, \varphi)\) is the radiant intensity of a transmitter in the direction \((\theta, \varphi)\) and \(P_{\text {total }}\) is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as \(d B i\). For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

\section*{See Also}
patternAzimuth | pattern | patternElevation

\section*{isPolarizationCapable}

System object: phased.Isot ropicAntennaElement
Package: phased
Polarization capability

\section*{Syntax}
flag = isPolarizationCapable(h)

\section*{Description}
flag = isPolarizationCapable(h) returns a Boolean value, flag, indicating whether the phased. IsotropicAntennaElement System object supports polarization. An antenna element supports polarization if it can create or respond to polarized fields. This object does not support polarization.

\section*{Input Arguments}
h - Isotropic antenna element
Isotropic antenna element specified as a phased.Isot ropicAntennaElement System object.

\section*{Output Arguments}

\section*{flag - Polarization-capability flag}

Polarization-capability returned as a Boolean value true if the antenna element supports polarization or false if it does not. Since the phased. IsotropicAntennaElement object does not support polarization, flag is always returned as false.

\section*{Examples}

\section*{Isotropic Antenna Does Not Support Polarization}

Create an isotropic antenna element using the phased. IsotropicAntennaElement System object \({ }^{\mathrm{TM}}\) and show that it does not support polarization.
```

antenna = phased.IsotropicAntennaElement('FrequencyRange',[1.0,10]*1e9);
isPolarizationCapable(antenna)
ans = logical
0

```

The returned value 0 shows that the antenna element does not support polarization.

\section*{pattern}

System object: phased. Isot ropicAntennaElement
Package: phased
Plot isotropic antenna element directivity and patterns

\section*{Syntax}
```

pattern(sElem,FREQ)
pattern(sElem,FREQ,AZ)
pattern(sElem,FREQ,AZ,EL)
pattern(
,Name,Value)
[PAT,AZ_ANG,EL_ANG] = pattern(

```
\(\qquad\)
``` )
```


## Description

pattern (sElem, FREQ) plots the 3-D array directivity pattern (in dBi) for the element specified in sElem. The operating frequency is specified in FREQ.
pattern(sElem, FREQ,AZ) plots the element directivity pattern at the specified azimuth angle.
pattern(sElem, FREQ,AZ,EL) plots the element directivity pattern at specified azimuth and elevation angles.
pattern(__,Name,Value) plots the element pattern with additional options specified by one or more Name, Value pair arguments.
[PAT,AZ_ANG,EL_ANG] = pattern( $\qquad$ ) returns the element pattern in PAT. The AZ_ANG output contains the coordinate values corresponding to the rows of PAT. The EL_ANG output contains the coordinate values corresponding to the columns of PAT. If the 'CoordinateSystem' parameter is set to ' uv', then AZ_ANG contains the $U$ coordinates of the pattern and EL_ANG contains the $V$ coordinates of the pattern. Otherwise, they are in angular units in degrees. $U V$ units are dimensionless.

Note This method replaces the plotResponse method. See "Convert plotResponse to pattern" on page 1-772 for guidelines on how to use pattern in place of plotResponse.

## Input Arguments

## sElem - Isotropic antenna element

System object
Isotropic antenna element, specified as a phased.IsotropicAntennaElement System object.
Example: sElem = phased.IsotropicAntennaElement;
FREQ - Frequency for computing directivity and patterns
positive scalar | 1-by-L real-valued row vector

Frequencies for computing directivity and patterns, specified as a positive scalar or 1-by-L realvalued row vector. Frequency units are in hertz.

- For an antenna, microphone, or sonar hydrophone or projector element, FREQ must lie within the range of values specified by the FrequencyRange or FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased. CustomAntennaElement and phased. CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.


## Example: [1e8 2e6]

Data Types: double

## AZ - Azimuth angles

[-180:180] (default) | 1-by- $N$ real-valued row vector
Azimuth angles for computing directivity and pattern, specified as a $1-b y-N$ real-valued row vector where $N$ is the number of azimuth angles. Angle units are in degrees. Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the $x y$ plane. When measured from the $x$-axis toward the $y$-axis, this angle is positive.

## Example: [-45:2:45]

Data Types: double

## EL - Elevation angles

[-90:90] (default) | 1-by-M real-valued row vector
Elevation angles for computing directivity and pattern, specified as a 1-by- $M$ real-valued row vector where $M$ is the number of desired elevation directions. Angle units are in degrees. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

The elevation angle is the angle between the direction vector and $x y$-plane. The elevation angle is positive when measured towards the $z$-axis.
Example: [-75:1:70]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## CoordinateSystem - Plotting coordinate system

'polar' (default)|'rectangular'|'uv'
Plotting coordinate system of the pattern, specified as the comma-separated pair consisting of
'CoordinateSystem' and one of 'polar', 'rectangular', or 'uv'. When
'CoordinateSystem' is set to 'polar' or 'rectangular', the AZ and EL arguments specify the
pattern azimuth and elevation, respectively. AZ values must lie between $-180^{\circ}$ and $180^{\circ}$. EL values must lie between $-90^{\circ}$ and $90^{\circ}$. If 'CoordinateSystem' is set to 'uv', AZ and EL then specify $U$ and $V$ coordinates, respectively. AZ and EL must lie between -1 and 1.
Example: 'uv'
Data Types: char

## Type - Displayed pattern type

'directivity' (default) | 'efield'|'power'|'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type ' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb ' - power pattern converted to dB.

Example: ' powerdb'
Data Types: char

## Normalize - Display normalize pattern

true (default) | false
Display normalized pattern, specified as the comma-separated pair consisting of 'Normalize' and a Boolean. Set this parameter to true to display a normalized pattern. This parameter does not apply when you set 'Type' to 'directivity'. Directivity patterns are already normalized.

Data Types: logical

## PlotStyle - Plotting style

'overlay' (default)| 'waterfall'
Plotting style, specified as the comma-separated pair consisting of 'Plotstyle' and either 'overlay' or 'waterfall'. This parameter applies when you specify multiple frequencies in FREQ in 2-D plots. You can draw 2-D plots by setting one of the arguments AZ or EL to a scalar.

## Data Types: char

## Output Arguments

## PAT - Element pattern

$N$-by-M real-valued matrix
Element pattern, returned as an $N$-by- $M$ real-valued matrix. The pattern is a function of azimuth and elevation. The rows of PAT correspond to the azimuth angles in the vector specified by EL_ANG. The columns correspond to the elevation angles in the vector specified by AZ_ANG.

## AZ_ANG - Azimuth angles

```
scalar | 1-by-N real-valued row vector
```

Azimuth angles for displaying directivity or response pattern, returned as a scalar or 1-by- $N$ realvalued row vector corresponding to the dimension set in AZ. The columns of PAT correspond to the values in AZ_ANG. Units are in degrees.

## EL_ANG - Elevation angles

scalar | 1-by-M real-valued row vector
Elevation angles for displaying directivity or response, returned as a scalar or 1-by-M real-valued row vector corresponding to the dimension set in EL. The rows of PAT correspond to the values in EL_ANG. Units are in degrees.

## Examples

## Plot Pattern and Directivity of Isotropic Antenna

Create an isotropic antenna element. Then, plot the antenna power pattern and directivity.
First, create the antenna.
antenna $=$ phased.IsotropicAntennaElement;
Draw an azimuth cut of the power pattern at 0 degrees elevation. Assume the operating frequency is 1 GHz .
fc = 1e9;
pattern(antenna,fc, [-180:180],0,...
'Type', 'power',...
'CoordinateSystem', 'rectangular')


Draw the same azimuth cut of the antenna directivity.
pattern(antenna,fc, [-180:180],0,...
'Type', 'directivity', ...
'CoordinateSystem', 'rectangular')


## Elevation-Cut of Isotropic Antenna Pattern

Construct an isotropic antenna operating in the frequency range from 800 MHz to 1.2 GHz . Compute the response at boresight at 1 GHz . Display the power pattern of the antenna at 1 GHz .

```
antenna = phased.IsotropicAntennaElement(...
```

'FrequencyRange',[800e6 1.2e9]);
fc = 1e9;
resp $=$ antenna(fc,[0;0])
resp $=1$
Plot the elevation power pattern of the antenna in polar coordinates.
pattern(antenna,fc,0,[-90:90],'Type','powerdb','CoordinateSystem','polar')


Normalized Power (dB), Broadside at $0.00^{\circ}$

## 3-D Isotropic Antenna Pattern

Construct an isotropic antenna operating over a frequency range from 800 MHz to 1.2 GHz . Then, plot the 3-D antenna field pattern.

Construct an isotropic antenna element.
antenna $=$ phased.IsotropicAntennaElement(...
'FrequencyRange',[800e6 1.2e9]);
Plot the 3-D magnitude pattern of the antenna at 1 GHz from -30 to 30 degrees in both azimuth and elevation in 0.1 degree increments.
fc = 1e9;
pattern(antenna,fc,[-30:0.1:30],[-30:0.1:30],...
'Type', 'efield',...
'CoordinateSystem', 'polar')


## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \Pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Convert plotResponse to pattern

For antenna, microphone, and array System objects, the pattern method replaces the plotResponse method. In addition, two new simplified methods exist just to draw 2-D azimuth and elevation pattern plots. These methods are azimuthPattern and elevationPattern.

The following table is a guide for converting your code from using plotResponse to pattern. Notice that some of the inputs have changed from input arguments to Name-Value pairs and conversely. The general pattern method syntax is
pattern(H,FREQ,AZ,EL,'Name1','Value1',...,' $N a m e N ', ' V a l u e N ') ~$

| plotResponse Inputs | plotResponse Description | pattern Inputs |
| :--- | :--- | :--- |
| H argument | Antenna, microphone, or array <br> System object. | H argument (no change) |
| FREQ argument | Operating frequency. | FREQ argument (no change) |
| V argument | Propagation speed. This argument <br> is used only for arrays. | 'PropagationSpeed ' name-value <br> pair. This parameter is only used for <br> arrays. |


| plotResponse Inputs | plotResponse Description |  | pattern Inputs |  |
| :---: | :---: | :---: | :---: | :---: |
| 'Format' and 'RespCut' namevalue pairs | These options work together to let you create a plot in angle space (line or polar style) or $U V$ space. They also determine whether the plot is 2-D or 3-D. This table shows you how to create different types of plots using plotResponse. |  | 'CoordinateSystem' name-value pair used together with the AZ and EL input arguments. <br> 'CoordinateSystem' has the same options as the plotResponse method 'Format ' name-value pair, except that ' line' is now named 'rectangular'. The table shows how to create different types of plots using pattern. |  |
|  | Display space <br> Angle space (2D) |  |  |  |
|  | Angle space (2D) | Set 'RespCut' <br> to 'Az' or |  |  |
|  |  | 'El'. Set <br> 'Format ' to <br> 'line' or 'polar'. | Display space |  |
|  |  | ' line' or 'polar'. <br> Set the display axis using either the 'AzimuthAngle | Angle space (2D) | Set <br> Coordinate <br> System' to <br> rectangular' <br> or 'polar' <br> Specify either AZ <br> or EL as a scalar. |
|  |  | s' or 'ElevationAng les' namevalue pairs. | Angle space (3D) | Set <br> 'Coordinate <br> System' to 'rectangular' |
|  | Angle space (3D) | Set 'RespCut' to '3D'. Set |  | or 'polar'. <br> Specify both AZ <br> and EL as <br> vectors. |
|  |  | 'polar'. <br> Set the display axis using both the 'AzimuthAngle s' and 'Elevation | $U V$ space (2D) | Set <br> Coordinate System' to uv'. Use AZ to specify a $U$ space vector. Use EL to specify a $V$-space scalar. |
|  |  | Angles' namevalue pairs. | UV space (3D) |  |
|  | UV space (2D) | Set 'RespCut' to'U'. Set 'Format ' to 'UV'. Set the display range using the 'UGrid' namevalue pair. |  | 'Coordinate <br> System' to <br> 'uv'. Use AZ to <br> specify a $U$ - <br> space vector. <br> Use EL to specify <br> a $V$-space vector. |
|  |  |  | If you set CoordinateSystem to 'uv ' , enter the UV grid values using $A Z$ and $E L$. |  |
|  | UV space (3D) | $\begin{aligned} & \text { Set 'RespCut' } \\ & \text { to'3D'. Set } \\ & \text { 'Format' to } \end{aligned}$ |  |  |


| plotResponse Inputs | plotResponse Description |  | pattern Inputs |
| :---: | :---: | :---: | :---: |
|  | Display space | 'UV '. Set the display range using both the 'UGrid' and 'VGrid ' namevalue pairs. |  |
| 'CutAngle' name-value pair | Constant angle at to take an azimuth or elevation cut. When producing a 2-D plot and when 'RespCut' is set to 'Az' or 'El', use 'CutAngle' to set the slice across which to view the plot. |  | No equivalent name-value pair. To create a cut, specify either AZ or EL as a scalar, not a vector. |
| 'NormalizeResponse' namevalue pair | Normalizes the plot. When 'Unit' is set to 'dbi' , you cannot specify 'NormalizeResponse'. |  | Use the 'Normalize' name-value pair. When 'Type' is set to 'directivity' you cannot specify 'Normalize'. |
| 'OverlayFreq' name-value pair | Plot multiple frequencies on the same 2-D plot. Available only when 'Format' is set to 'line' or 'uv and 'RespCut' is not set to '3D'. The value true produces an overlay plot and the value false produces a waterfall plot. |  | 'PlotStyle' name-value pair plots multiple frequencies on the same 2-D plot. <br> The values 'overlay' and 'waterfall' correspond to 'OverlayFreq' values of true and false. The option 'waterfall' is allowed only when 'CoordinateSystem' is set to 'rectangular' or 'uv'. |
| 'Polarization' name-value pair | Determines how to plot polarized fields. Options are 'None', 'Combined', 'H', or 'V'. |  | 'Polarization ' name-value pair determines how to plot polarized fields. The 'None ' option is removed. The options 'Combined ' , ' H ', or 'V' are unchanged. |
| ' Unit ' name-value pair | Determines the plot units. Choose 'db','mag', 'pow', or 'dbi', where the default is ' db ' |  | 'Type ' name-value pair, uses equivalent options with different names |
|  |  |  | plotResponse pattern |
|  |  |  | 'db' 'powerdb' <br> 'mag' 'efield' <br> 'pow' 'power' <br> 'dbi' 'directivity' |
| 'Weights ' name-value pair | Array element tapers (or weights). |  | 'Weights ' name-value pair (no change). |
| 'AzimuthAngles ' name-value pair | Azimuth angles used to display the antenna or array response. |  | AZ argument |


| plotResponse Inputs | plotResponse Description | pattern Inputs |
| :--- | :--- | :--- |
| 'ElevationAngles ' name-value <br> pair | Elevation angles used to display the <br> antenna or array response. | EL argument |
| ' UGrid' name-value pair | Contains $U$ coordinates in $U V$ - <br> space. | AZ argument when <br> 'CoordinateSystem ' name-value <br> pair is set to 'uv' |
| 'VGrid' name-value pair | Contains V-coordinates in $U V$-space. | EL argument when <br> 'CoordinateSystem ' name-value <br> pair is set to 'uv' |

## Version History <br> Introduced in R2015a

See Also<br>patternAzimuth|patternElevation

## patternAzimuth

System object: phased. Isot ropicAntennaElement
Package: phased
Plot isotropic antenna element directivity or pattern versus azimuth

## Syntax

```
patternAzimuth(sElem,FREQ)
patternAzimuth(sElem,FREQ,EL)
patternAzimuth(sElem,FREQ,EL,Name,Value)
PAT = patternAzimuth(
```

$\qquad$

## Description

patternAzimuth (sElem, FREQ) plots the 2-D element directivity pattern versus azimuth (in dBi) for the element sElem at zero degrees elevation angle. The argument FREQ specifies the operating frequency.
patternAzimuth(sElem, FREQ,EL), in addition, plots the 2-D element directivity pattern versus azimuth (in dBi ) at the elevation angle specified by EL . When EL is a vector, multiple overlaid plots are created.
patternAzimuth(sElem, FREQ,EL,Name, Value) plots the element pattern with additional options specified by one or more Name, Value pair arguments.

PAT = patternAzimuth( $\qquad$ ) returns the element pattern. PAT is a matrix whose entries represent the pattern at corresponding sampling points specified by the 'Azimuth' parameter and the EL input argument.

## Input Arguments

## sElem - Isotropic antenna element

System object
Isotropic antenna element, specified as a phased.IsotropicAntennaElement System object.

```
Example: sElem = phased.IsotropicAntennaElement;
```


## FREQ - Frequency for computing directivity and pattern

positive scalar
Frequency for computing directivity and pattern, specified as a positive scalar. Frequency units are in hertz.

- For an antenna or microphone element, FREQ must lie within the range of values specified by the FrequencyRange or the FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased. CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: 1e8
Data Types: double

## EL - Elevation angles

1-by- $N$ real-valued row vector
Elevation angles for computing sensor or array directivities and patterns, specified as a 1-by- $N$ realvalued row vector. The quantity $N$ is the number of requested elevation directions. Angle units are in degrees. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

The elevation angle is the angle between the direction vector and the xy plane. When measured toward the $z$-axis, this angle is positive.
Example: [0, 10, 20]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Type - Displayed pattern type

'directivity' (default) | 'efield' | 'power' | 'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power ' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb ' - power pattern converted to dB.

Example: 'powerdb'
Data Types: char

## Azimuth - Azimuth angles

[-180:180] (default) | 1-by-P real-valued row vector
Azimuth angles, specified as the comma-separated pair consisting of 'Azimuth' and a 1-by-P realvalued row vector. Azimuth angles define where the array pattern is calculated.
Example: 'Azimuth', [-90:2:90]
Data Types: double

## Output Arguments

## PAT - Element directivity or pattern

$P$-by- $N$ real-valued matrix
Element directivity or pattern, returned as an $P$-by- $N$ real-valued matrix. The dimension $P$ is the number of azimuth values determined by the 'Azimuth' name-value pair argument. The dimension $N$ is the number of elevation angles, as determined by the EL input argument.

## Examples

## Directivity Pattern of Isotropic Antenna Element for Span of Azimuth Angles

Plot an azimuth cut of the directivity of an isotropic antenna element at 0 degrees elevation for all azimuth angles and at 30 degrees elevation for a small span of azimuth angles. Assume the operating frequency is 500 MHz .

Create the antenna element.
$\mathrm{fc}=500 \mathrm{e} 6$;
antenna = phased.IsotropicAntennaElement('FrequencyRange',[100, 900]*1e6);
Plot the pattern for all azimuth angles at 0 degrees elevation.
patternAzimuth(antenna,fc, 0 )


Directivity (dBi), Broadside at $0.00^{\circ}$

Plot the pattern for a reduced span of azimuth angles using the Azimuth parameter.

```
patternAzimuth(antenna,fc,30,'Azimuth',[-20:20])
```



Directivity (dBi), Broadside at $0.00^{\circ}$

## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\text {rad }}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Version History

Introduced in R2015a

See Also<br>pattern| patternElevation

## patternElevation

System object: phased. IsotropicAntennaElement
Package: phased
Plot isotropic antenna element directivity or pattern versus elevation

## Syntax

```
patternElevation(sElem,FREQ)
patternElevation(sElem,FREQ,AZ)
patternElevation(sElem,FREQ,AZ,Name,Value)
PAT = patternElevation(
```

$\qquad$

## Description

patternElevation(sElem, FREQ) plots the 2-D element directivity pattern versus elevation (in dBi) for the element sElem at zero degrees azimuth angle. The argument FREQ specifies the operating frequency.
patternElevation(sElem,FREQ,AZ), in addition, plots the 2-D element directivity pattern versus elevation (in dBi ) at the azimuth angle specified by $A Z$. When $A Z$ is a vector, multiple overlaid plots are created.
patternElevation(sElem,FREQ,AZ,Name, Value) plots the element pattern with additional options specified by one or more Name, Value pair arguments.

PAT = patternElevation( $\qquad$ ) returns the element pattern. PAT is a matrix whose entries represent the pattern at corresponding sampling points specified by the 'Elevation' parameter and the $A Z$ input argument.

## Input Arguments

## sElem - Isotropic antenna element

System object
Isotropic antenna element, specified as a phased.IsotropicAntennaElement System object.

```
Example: sElem = phased.IsotropicAntennaElement;
```


## FREQ - Frequency for computing directivity and pattern

positive scalar
Frequency for computing directivity and pattern, specified as a positive scalar. Frequency units are in hertz.

- For an antenna or microphone element, FREQ must lie within the range of values specified by the FrequencyRange or the FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased.CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: 1e8
Data Types: double

## AZ - Azimuth angles for computing directivity and pattern

1-by- $N$ real-valued row vector
Azimuth angles for computing sensor or array directivities and patterns, specified as a 1-by- N realvalued row vector where $N$ is the number of desired azimuth directions. Angle units are in degrees. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the xy plane. This angle is positive when measured from the $x$-axis toward the $y$-axis.
Example: [0,10,20]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Type - Displayed pattern type

'directivity' (default) | 'efield' | 'power' | 'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power ' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb ' - power pattern converted to dB.

Example: 'powerdb'
Data Types: char

## Elevation - Elevation angles

[-90:90] (default)| 1-by-P real-valued row vector
Elevation angles, specified as the comma-separated pair consisting of 'Elevation' and a 1-by-P real-valued row vector. Elevation angles define where the array pattern is calculated.
Example: 'Elevation', [-90:2:90]
Data Types: double

## Output Arguments

## PAT - Element directivity or pattern

$P$-by- $N$ real-valued matrix
Element directivity or pattern, returned as an $P$-by- $N$ real-valued matrix. The dimension $P$ is the number of elevation angles determined by the 'Elevation' name-value pair argument. The dimension $N$ is the number of azimuth angles determined by the AZ argument.

## Examples

## Directivity Pattern of Isotropic Antenna Element for Span of Elevation Angles

Plot an elevation cut of directivity of an isotropic antenna element at 45 degrees azimuth for all elevation angles and at 45 degrees for a span of elevation angles. Assume the operating frequency is 500 MHz .

Create the antenna element.
$\mathrm{fc}=500 \mathrm{e} 6$;
antenna $=$ phased.IsotropicAntennaElement('FrequencyRange',[100,900]*1e6);
Plot the directivity for all elevation angles.
patternElevation(antenna,fc,45)


Directivity (dBi), Broadside at $0.00^{\circ}$

Plot the directivity for a span of elevation angles using the Elevation parameter.
patternElevation(antenna,fc,45,'Elevation', [-20:20])


Directivity (dBi), Broadside at $0.00^{\circ}$

## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \Pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\text {rad }}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Version History

Introduced in R2015a

See Also<br>patternAzimuth | pattern

## plotResponse

System object: phased. IsotropicAntennaElement
Package: phased
Plot response pattern of antenna

## Syntax

plotResponse(H,FREQ)
plotResponse(H,FREQ,Name, Value)
hPlot = plotResponse( $\qquad$ )

## Description

plotResponse( $\mathrm{H}, \mathrm{FREQ}$ ) plots the element response pattern along the azimuth cut, where the elevation angle is 0 . The operating frequency is specified in FREQ.
plotResponse(H, FREQ,Name, Value) plots the element response with additional options specified by one or more Name, Value pair arguments.
hPlot $=$ plotResponse ( __ $)$ returns handles of the lines or surface in the figure window, using any of the input arguments in the previous syntaxes.

## Input Arguments

## H

Element System object

## FREQ

Operating frequency in Hertz specified as a scalar or 1-by-K row vector. FREQ must lie within the range specified by the FrequencyVector property of H . If you set the 'RespCut ' property of H to ' 3D ' , FREQ must be a scalar. When FREQ is a row vector, plotResponse draws multiple frequency responses on the same axes.

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## CutAngle

Cut angle specified as a scalar. This argument is applicable only when RespCut is ' Az ' or ' El '. If RespCut is 'Az', CutAngle must be between -90 and 90. If RespCut is 'El', CutAngle must be between -180 and 180 .

## Default: 0

## Format

Format of the plot, using one of 'Line', 'Polar', or 'UV '. If you set Format to 'UV ' , FREQ must be a scalar.

Default: 'Line'

## NormalizeResponse

Set this value to true to normalize the response pattern. Set this value to false to plot the response pattern without normalizing it. This parameter is not applicable when you set the Unit parameter value to 'dbi'.

Default: true

## OverlayFreq

Set this value to true to overlay pattern cuts in a 2-D line plot. Set this value to false to plot pattern cuts against frequency in a 3-D waterfall plot. If this value is false, FREQ must be a vector with at least two entries.

This parameter applies only when Format is not 'Polar' and RespCut is not '3D '.

## Default: true

## Polarization

Specify the polarization options for plotting the antenna response pattern. The allowable values are |'None' | 'Combined' | 'H' | 'V' | where

- 'None' specifies plotting a nonpolarized response pattern
- 'Combined ' specifies plotting a combined polarization response pattern
- 'H' specifies plotting the horizontal polarization response pattern
- 'V ' specifies plotting the vertical polarization response pattern

For antennas that do not support polarization, the only allowed value is 'None'. This parameter is not applicable when you set the Unit parameter value to ' dbi ' .

Default: 'None'

## RespCut

Cut of the response. Valid values depend on Format, as follows:

- If Format is 'Line' or 'Polar', the valid values of RespCut are 'Az', 'El', and '3D'. The default is ' Az '.
- If Format is 'UV', the valid values of RespCut are 'U' and '3D'. The default is 'U'.

If you set RespCut to ' 3D' , FREQ must be a scalar.

## Unit

The unit of the plot. Valid values are 'db', 'mag', 'pow', or 'dbi'. This parameter determines the type of plot that is produced.

| Unit value | Plot type |
| :--- | :--- |
| db | power pattern in dB scale |
| mag | field pattern |
| pow | power pattern |
| dbi | directivity |

Default: 'db'

## AzimuthAngles

Azimuth angles for plotting element response, specified as a row vector. The AzimuthAngles parameter sets the display range and resolution of azimuth angles for visualizing the radiation pattern. This parameter is allowed only when the RespCut parameter is set to ' Az ' or ' $3 D^{\prime}$ and the Format parameter is set to 'Line' or 'Polar'. The values of azimuth angles should lie between $180^{\circ}$ and $180^{\circ}$ and must be in nondecreasing order. When you set the RespCut parameter to '3D ', you can set the AzimuthAngles and ElevationAngles parameters simultaneously.

Default: [-180:180]

## ElevationAngles

Elevation angles for plotting element response, specified as a row vector. The ElevationAngles parameter sets the display range and resolution of elevation angles for visualizing the radiation pattern. This parameter is allowed only when the RespCut parameter is set to ' $E l$ ' or ' $3 D^{\prime}$ ' and the Format parameter is set to 'Line' or 'Polar'. The values of elevation angles should lie between $90^{\circ}$ and $90^{\circ}$ and must be in nondecreasing order. When you set the RespCut parameter to ' 3D ', you can set the ElevationAngles and AzimuthAngles parameters simultaneously.

Default: [-90:90]

## UGrid

$U$ coordinate values for plotting element response, specified as a row vector. The UGrid parameter sets the display range and resolution of the $U$ coordinates for visualizing the radiation pattern in $U / V$ space. This parameter is allowed only when the Format parameter is set to 'UV' and the RespCut parameter is set to ' $U$ ' or ' $3 D$ '. The values of $U G r i d$ should be between -1 and 1 and should be specified in nondecreasing order. You can set the UGrid and VGrid parameters simultaneously.

Default: [-1:0.01:1]

## VGrid

$V$ coordinate values for plotting element response, specified as a row vector. The VGrid parameter sets the display range and resolution of the $V$ coordinates for visualizing the radiation pattern in $U / V$ space. This parameter is allowed only when the Format parameter is set to ' UV' and the RespCut parameter is set to ' 3 D '. The values of VGrid should be between -1 and 1 and should be specified in nondecreasing order. You can set the VGrid and UGrid parameters simultaneously.

Default: [-1:0.01:1]

## Examples

## Plot Response and Directivity of Isotropic Antenna

This example shows how to plot the response and the directivity of an isotropic antenna element.
Draw a line plot of an azimuth cut of the response of an isotropic antenna along 0 degrees elevation. Assume the operating frequency is 1 GHz .
sIso = phased.IsotropicAntennaElement; plotResponse(sIso,1e9,'Unit','pow');


Draw an azimuth cut of the antenna directivity.
plotResponse(sIso,1e9,'Unit','dbi');


## Plot Elevation-Cut of Isotropic Antenna Response

Construct an isotropic antenna operating in the frequency range from 800 MHz to 1.2 GHz . Find the response of the antenna at boresight at 1 GHz .

```
sIso = phased.IsotropicAntennaElement(...
    'FrequencyRange',[800e6 1.2e9]);
fc = 1e9;
resp = step(sIso,fc,[0;0])
resp = 1
```

Plot the polar-form of the elevation response of the antenna.

```
plotResponse(sIso,fc,'RespCut','El','Format','Polar');
```



Normalized Power (dB), Broadside at $0.00^{\circ}$

## Plot 3-D Response

This example shows how to construct an isotropic antenna operating over a frequency range from 800 MHz to 1.2 GHz and how to plot its response.

Construct the antenna element.

```
sIso = phased.IsotropicAntennaElement(...
    'FrequencyRange',[0.8e9 1.2e9]);
```

Plot the 3-D response of the antenna at 1 GHz from - 30 to 30 degrees in both azimuth and elevation at 0.1 degree increments.

```
fc = 1e9;
plotResponse(sIso,fc,'RespCut','3D','Format','Polar',...
    'Unit','mag','AzimuthAngles',[-30:.1:30],...
    'ElevationAngles',[-30:.1:30]);
```



See Also
uv2azel|azel2uv

## step

## System object: phased. IsotropicAntennaElement

Package: phased
Output response of antenna element

## Syntax

RESP = step(H,FREQ,ANG)

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step $(o b j, x)$ and $y=o b j(x)$ perform equivalent operations.

RESP $=$ step ( $H$, FREQ, ANG) returns the antenna's voltage response RESP at operating frequencies specified in FREQ and directions specified in ANG.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## H

Antenna element object.

## FREQ

Operating frequencies of antenna in hertz. FREQ is a row vector of length $L$.

## ANG

Directions in degrees. ANG can be either a 2-by-M matrix or a row vector of length M .
If ANG is a 2-by-M matrix, each column of the matrix specifies the direction in the form [azimuth; elevation]. The azimuth angle must be between -180 and 180 degrees, inclusive. The elevation angle must be between -90 and 90 degrees, inclusive.

If ANG is a row vector of length $M$, each element specifies a direction's azimuth angle. In this case, the corresponding elevation angle is assumed to be 0 .

## Output Arguments

## RESP

Voltage response of antenna element specified as an $M$-by- $L$, complex-valued matrix. In this matrix, $M$ represents the number of angles specified in ANG while $L$ represents the number of frequencies specified in FREQ.

## Examples

## Plot Isotropic Antenna Element Response

Create an isotropic antenna operating over a frequency range from 800 MHz to 1.2 GHz . The operating frequency is 1 GHz . Find the response of the antenna at boresight. Then, plot the polarpattern elevation response of the antenna.

```
antenna = phased.IsotropicAntennaElement( ...
    'FrequencyRange',[800e6 1.2e9]);
fc = 1e9;
```

Obtain the response at boresight.

```
resp = antenna(fc,[0;0])
resp = 1
```

Plot the response pattern.

```
pattern(antenna,fc,0,[-90:90],'CoordinateSystem','polar', ...
    'Type','powerdb','Normalize',true)
```



Normalized Power (dB), Broadside at $0.00^{\circ}$

## See Also

uv2azel| phitheta2azel

# phased.IsotropicHydrophone 

Package: phased

Isotropic hydrophone element

## Description

The phased.IsotropicHydrophone System object models an isotropic hydrophone for sonar applications. An isotropic hydrophone has the same response in all signal directions. The response is the output voltage of the hydrophone per unit sound pressure. The response of a hydrophone is also called its sensitivity. You can specify the response using the VoltageSensitivity property.

To compute the response of the isotropic hydrophone element for specified directions:
1 Create the phased. IsotropicHydrophone object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

hydrophone $=$ phased.IsotropicHydrophone
hydrophone = phased.IsotropicHydrophone(Name=Value)

## Description

hydrophone = phased.IsotropicHydrophone creates an isotropic hydrophone System object, hydrophone.
hydrophone = phased.IsotropicHydrophone(Name=Value) creates an Isotropic hydrophone object, hydrophone, with each specified property set to the specified value. You can specify additional name-value pair arguments in any order as (Namel=Value1,...,NameN=ValueN).

Example: hydrophone = phased.IsotropicHydrophone(FrequencyRange=[0
1000], BackBaffled=true) creates an isotropic hydrophone element with its frequency range specified between 0 and 1000 Hz .

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## FrequencyRange - Operating frequency range of hydrophone

[0 100e6] (default) | real-valued 1-by-2 vector
Operating frequency range of hydrophone, specified as a real-valued 1-by-2 row vector of the form [LowerBound HigherBound]. This property defines the frequency range over which the hydrophone has a response. The hydrophone element has zero response outside this frequency range. Units are in Hz .

Example: [0 1000]
Data Types: double

## VoltageSensitivity - Voltage sensitivity of hydrophone

- 120 (default) | scalar | real-valued 1-by-K row vector

Voltage sensitivity of hydrophone, specified as a scalar or real-valued 1-by-K row vector. When you specify the voltage sensitivity as a scalar, that value applies to the entire frequency range specified by FrequencyRange. When you specify the voltage sensitivity as a vector, the frequency range is divided into $\mathrm{K}-1$ equal intervals. The sensitivity values are assigned to the interval end points. The step method interpolates the voltage sensitivity for any frequency inside the frequency range. Units are in $\mathrm{dB} / / 1 \mathrm{~V} / \mu \mathrm{Pa}$. See "Hydrophone Sensitivity" on page 1-806 for more details.

Example: 10
Data Types: double

## BackBaffled - Back baffle hydrophone element

false (default) | true
Baffle the back direction of hydrophone element, specified as false or true. When true, the hydrophone responses to all azimuth angles beyond $\pm 90$ degrees from broadside (zero degrees azimuth and elevation) are zero.

When the value of this property is false, the back direction of the microphone element is not baffled.

## Usage

## Syntax

resp = hydrophone(freq, ang)
Description
resp = hydrophone(freq, ang) returns the voltage sensitivity for the hydrophone at the specified operating frequencies and in the specified directions of arriving signals.

## Input Arguments

## freq - Voltage sensitivity frequencies

positive real scalar | real-valued 1-by-L vector of positive values
Voltage sensitivity frequencies of hydrophone, specified as a positive real scalar or a real-valued 1-by$L$ vector of positive values. Units are in Hz .
Data Types: double

## ang - Direction of arriving signals

real-valued 1-by-M row vector | real-valued 2-by-M matrix
Direction of arriving signals, specified as a real-valued 1-by- $M$ row vector or 2-by-M matrix. When ang is a 2 -by- $M$ matrix, each column of the matrix specifies the direction in the form [azimuth; elevation]. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive.

When ang is a 1 -by- $M$ row vector, each element specifies the azimuth angle of the arriving signal. In this case, the corresponding elevation angle is assumed to be zero.

Data Types: double

## Output Arguments <br> resp - Voltage sensitivity of hydrophone <br> real-valued $M$-by- $L$ matrix

Voltage sensitivity of hydrophone, returned as a real-valued $M$-by- $L$ matrix. $M$ represents the number of angles specified in ang, and $L$ represents the number of frequencies specified in freq. Units are in V/Pa.

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```


## Specific to Antenna and Transducer Element System Objects

beamwidth
directivity
isPolarizationCapable
pattern
patternAzimuth
patternElevation

Compute and display beamwidth of sensor element pattern Directivity of antenna or transducer element Antenna element polarization capability Plot antenna or transducer element directivity and patterns Plot antenna or transducer element directivity and pattern versus azimuth Plot antenna or transducer element directivity and pattern versus elevation

## Common to All System Objects

| step | Run System object algorithm <br> release |
| :--- | :--- |
| Release resources and allow changes to System object property values and input <br> characteristics |  |
| reset | Reset internal states of System object |

## Examples

## Response of Isotropic Hydrophone

Compute the response of an isotropic hydrophone operating at 2 kHz . The hydrophone has default property values.

Obtain the voltage sensitivity at five different elevation angles: $-30^{\circ},-15^{\circ}, 0^{\circ}, 15^{\circ}$ and $30^{\circ}$. All azimuth angles are at $0^{\circ}$. The sensitivities are computed at the signal frequency of 2 kHz .
hydrophone $=$ phased.IsotropicHydrophone;
fc = 2e3;
resp $=$ hydrophone(fc,[0 $0000 ;-30-15015$ 30]);

## Response and Pattern of Isotropic Hydrophone for Single Frequency

Examine the response and patterns of an isotropic hydrophone operating between 1 kHz and 10 kHz .
Set up the hydrophone parameters. Obtain the voltage sensitivity at five different elevation angles: $-30^{\circ},-15^{\circ}, 0^{\circ}, 15^{\circ}$ and $30^{\circ}$. All azimuth angles are at $0^{\circ}$. The sensitivities are computed at the signal frequency of 2 kHz .

```
hydrophone = phased.IsotropicHydrophone('FrequencyRange', ...
    [1 10]*1e3);
fc = 2e3;
resp = hydrophone(fc,[0 0 0 0 0;-30 -15 0 15 30]);
```

Draw a 3-D plot of the voltage sensitivity.

```
pattern(hydrophone,fc,[-180:180],[-90:90], ...
```

    'CoordinateSystem', 'polar','Type', 'powerdb')
    

## Response and Pattern of Isotropic Hydrophone at Multiple Frequencies

Examine the response and patterns of an isotropic hydrophone at three different frequencies. The hydrophone operates between 1 kHz and 10 kHz . Specify the voltage sensitivity as a vector.

Set up the hydrophone parameters and obtain the voltage sensitivity at $45^{\circ}$ azimuth and $30^{\circ}$ elevation. Compute the sensitivities at the signal frequencies of 2,5 , and 7 kHz .

```
hydrophone = phased.IsotropicHydrophone('FrequencyRange',[1 10]*1e3, ...
    'VoltageSensitivity',[-100 -90 -100]);
fc = [2e3 5e3 7e3];
resp = hydrophone(fc,[45;30])
resp = 1\times3
    14.8051 29.2202 24.4152
```

Draw a 2-D plot of the voltage sensitivity as a function of azimuth.
pattern(hydrophone,fc,[-180:180],0, 'CoordinateSystem','rectangular',... 'Type','power')


## Directivity of Isotropic Hydrophone

Compute the directivity of an isotropic hydrophone in different directions. Assume the signal frequency is 3 kHz . First, set up the hydrophone parameters.

```
fc = 3e3;
hydrophone = phased.IsotropicHydrophone('FrequencyRange',[1,10]*1e3, ...
    'VoltageSensitivity',[-100,-90,-100]);
patternElevation(hydrophone,fc,45)
```



Directivity (dBi), Broadside at $0.00^{\circ}$
First, select the angles of interest to be constant elevation angle at zero degrees. The five azimuth angles are centered around boresight (zero degrees azimuth and zero degrees elevation).
ang $=[-20,-10,0,10,20 ; 0,0,0,0,0]$;
Compute the directivity along the constant elevation cut.
d = directivity(hydrophone,fc,ang)
$d=5 \times 1$
0
0
0
0
0

The directivity of an isotropic hydrophone is zero in every direction.

## Response and Pattern of Isotropic Hydrophone at Multiple Frequencies

Examine the response and patterns of an isotropic hydrophone at three different frequencies. The hydrophone operates between 1 kHz and 10 kHz . Specify the voltage sensitivity as a vector.

Set up the hydrophone parameters and obtain the voltage sensitivity at $45^{\circ}$ azimuth and $30^{\circ}$ elevation. Compute the sensitivities at the signal frequencies of 2,5 , and 7 kHz .

```
hydrophone = phased.IsotropicHydrophone('FrequencyRange',[1 10]*1e3, ...
    'VoltageSensitivity',[-100 -90 -100]);
fc = [2e3 5e3 7e3];
resp = hydrophone(fc,[45;30])
resp = 1\times3
    14.8051 29.2202 24.4152
```

Draw a 2-D plot of the voltage sensitivity as a function of azimuth.

```
pattern(hydrophone,fc,[-180:180],0,'CoordinateSystem','rectangular',...
```

    'Type', 'power')
    

## Azimuth Pattern of Isotropic Hydrophone

Examine the azimuth pattern of an isotropic hydrophone at $30^{\circ}$ elevation. The frequency range is between 1 kHz and 10 kHz . Specify the voltage sensitivity as a vector.

First, set up the hydrophone parameters.
fc = 3e3;
hydrophone = phased.IsotropicHydrophone('FrequencyRange', [1, 10]*1e3, ...
'VoltageSensitivity', [-100,-90,-100]);
patternAzimuth (hydrophone, fc, 30)


Directivity (dBi), Broadside at $0.00^{\circ}$

Plot a smaller range of azimuth angles using the Azimuth parameter.
patternAzimuth(hydrophone,fc, 30,'Azimuth', [-20:20])


Directivity (dBi), Broadside at $0.00^{\circ}$

## Elevation Pattern of Isotropic Hydrophone

Plot an elevation cut of directivity of an isotropic hydrophone at $45^{\circ}$ azimuth. Assume the signal frequency is 3 kHz . First, set up the hydrophone parameters.
$\mathrm{fc}=3 \mathrm{e} 3$;
hydrophone = phased.IsotropicHydrophone('FrequencyRange',[1,10]*1e3, ...
'VoltageSensitivity',[-100,-90,-100]);
patternElevation(hydrophone, fc, 45)


Directivity (dBi), Broadside at $0.00^{\circ}$

Plot a smaller range of elevation angles using the Elevation parameter. patternElevation(hydrophone,fc,45,'Elevation',-20:20)


Directivity (dBi), Broadside at $0.00^{\circ}$

## More About

## Hydrophone Sensitivity

Hydrophone sensitivity measures the response of a hydrophone to input sound pressure.
Hydrophone voltage sensitivity is the open circuit voltage (OCV) at the output of a hydrophone for a given input sound intensity. Another term for hydrophone sensitivity is open circuit receiving response (OCRR). Specifically, OCRR is the voltage generated by a hydrophone per $\mu \mathrm{Pa}$ of sound intensity. OCRR is generally a function of frequency. If the sound intensity level (SIL) is expressed in $\mathrm{dB} / / \mu \mathrm{Pa}$ and the output voltage is expressed in $\mathrm{dB} / / 1 \mathrm{~V}$, then OCRR is expressed in $\mathrm{dB} / / 1 \mathrm{~V} / \mu \mathrm{Pa}$. The output voltage of a hydrophone is related to the input sound level by
$\mathrm{VdB}=\mathrm{SIL}+\mathrm{OCRR}$.
Consider a hydrophone that has OCRR $=-160 \mathrm{~dB} / / 1 \mathrm{~V} / \mathrm{\mu Pa}$ at 10 kHz . Assume that the SIL at the hydrophone due to a nearby ship is $120 \mathrm{~dB} / / \mu \mathrm{Pa}$. Then, the output voltage of the hydrophone is
$\mathrm{VdB}=\mathrm{SIL}+\mathrm{OCRR}=120 \mathrm{~dB}+(-160) \mathrm{dB}=-40 \mathrm{~dB} / / 1 \mathrm{~V}$.
In linear units,
$\mathrm{V}=10^{\mathrm{VdB} / 10}=100 \mu \mathrm{~V}$.

## Algorithms

The total sensitivity of a hydrophone is a combination of its frequency sensitivity and spatial sensitivity. phased. Isot ropicHydrophone calculates both sensitivities using nearest neighbor interpolation, and then multiplies the sensitivities to form the total sensitivity.

## Version History

## Introduced in R2017a

## References

[1] Urick, R.J. Principles of Underwater Sound. 3rd Edition. New York: Peninsula Publishing, 1996.
[2] Sherman, C.S., and J. Butler. Transducers and Arrays for Underwater Sound. New York: Springer, 2007.
[3] Allen, J.B., and D. Berkely. "Image method for efficiently simulating small-room acoustics", Journal of the Acoustical Society of America. Vol. 65, No. 4. April 1979, pp. 943-950.
[4] Van Trees, H. Optimum Array Processing. New York: Wiley-Interscience, 2002, pp. 274-304.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:

- The pattern, patternAzimuth, and patternElevation methods are not supported.
- See "System Objects in MATLAB Code Generation" (MATLAB Coder).


## See Also

phased.ULA|phased.URA|phased.ConformalArray|phased.IsotropicProjector| phased.UnderwaterRadiatedNoise

## Topics

"Underwater Target Detection with an Active Sonar System"
"Locating an Acoustic Beacon with a Passive Sonar System"
Phased Array Gallery

## directivity

System object: phased. Isot ropicHydrophone
Package: phased
Directivity of isotropic hydrophone

## Syntax

D = directivity(hydrophone, FREQ,ANGLE)

## Description

D = directivity (hydrophone, FREQ, ANGLE) returns the "Directivity" on page 1-810 of the isotropic hydrophone, hydrophone, at frequencies specified by FREQ and in direction angles specified by ANGLE.

## Input Arguments

## hydrophone - Isotropic hydrophone

phased. IsotropicHydrophone System object
Isotropic hydrophone, specified as a phased. IsotropicHydrophone System object.

## Example: phased.IsotropicHydrophone

## FREQ - Frequency for computing directivity and patterns

positive scalar | 1-by-L real-valued row vector
Frequencies for computing directivity and patterns, specified as a positive scalar or 1-by-L realvalued row vector. Frequency units are in hertz.

- For an antenna, microphone, or sonar hydrophone or projector element, FREQ must lie within the range of values specified by the FrequencyRange or FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased.CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.


## Example: [1e8 2e6]

Data Types: double

## ANGLE - Angles for computing directivity

1-by-M real-valued row vector | 2 -by- $M$ real-valued matrix
Angles for computing directivity, specified as a 1-by- $M$ real-valued row vector or a 2 -by- $M$ real-valued matrix, where $M$ is the number of angular directions. Angle units are in degrees. If ANGLE is a 2-by- $M$ matrix, then each column specifies a direction in azimuth and elevation, [az;el]. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

If ANGLE is a 1 -by- $M$ vector, then each entry represents an azimuth angle, with the elevation angle assumed to be zero.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the xy plane. This angle is positive when measured from the $x$-axis toward the $y$-axis. The elevation angle is the angle between the direction vector and $x y$ plane. This angle is positive when measured towards the $z$-axis. See "Azimuth and Elevation Angles".
Example: [45 60; 0 10]
Data Types: double

## Output Arguments

## D - Directivity

$M$-by-L matrix
Directivity, returned as an $M$-by- $L$ matrix. Each row corresponds to one of the $M$ angles specified by ANGLE. Each column corresponds to one of the $L$ frequency values specified in FREQ. Directivity units are in dBi where dBi is defined as the gain of an element relative to an isotropic radiator.

## Examples

## Directivity of Isotropic Hydrophone

Compute the directivity of an isotropic hydrophone in different directions. Assume the signal frequency is 3 kHz . First, set up the hydrophone parameters.

```
fc = 3e3;
hydrophone = phased.IsotropicHydrophone('FrequencyRange',[1,10]*1e3, ...
    'VoltageSensitivity',[-100,-90,-100]);
patternElevation(hydrophone,fc,45)
```



Directivity (dBi), Broadside at $0.00^{\circ}$

First, select the angles of interest to be constant elevation angle at zero degrees. The five azimuth angles are centered around boresight (zero degrees azimuth and zero degrees elevation).
ang $=[-20,-10,0,10,20 ; 0,0,0,0,0] ;$
Compute the directivity along the constant elevation cut.
d = directivity(hydrophone,fc,ang)
$\mathrm{d}=5 \times 1$
0
0
0
0
0

The directivity of an isotropic hydrophone is zero in every direction.

## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Version History

Introduced in R2017a

See Also<br>pattern | patternAzimuth | patternElevation

## isPolarizationCapable

System object: phased. IsotropicHydrophone
Package: phased
Polarization capability

## Syntax

flag = isPolarizationCapable(hydrophone)

## Description

flag = isPolarizationCapable(hydrophone) returns a Boolean value, flag, indicating whether the phased. IsotropicHydrophone supports polarization. An element supports polarization if it can create or respond to polarized fields. This hydrophone does not support polarization.

## Input Arguments

## hydrophone - Isotropic hydrophone

phased.IsotropicHydrophone System object
Isotropic hydrophone, specified as a phased.IsotropicHydrophone System object.
Example: phased.IsotropicHydrophone

## Output Arguments

flag - Polarization-capability flag
true | false
Polarization-capability returned as a Boolean value true if the hydrophone supports polarization or false if it does not. Because the phased. IsotropicHydrophone object does not support polarization, flag is always returned as false.

## Version History

Introduced in R2017a

## pattern

System object: phased. IsotropicHydrophone
Package: phased
Plot isotropic hydrophone directivity and patterns

## Syntax

pattern(hydrophone, FREQ)
pattern(hydrophone, FREQ, AZ)
pattern(hydrophone, FREQ, AZ, EL)
pattern(
,Name, Value)
[PAT,AZ_ANG,EL_ANG] = pattern(___)

## Description

pattern (hydrophone, FREQ) plots the 3D directivity pattern (in dBi) for the hydrophone, hydrophone. The operating frequency is specified in FREQ.
pattern(hydrophone, FREQ,AZ) plots the directivity pattern at the specified azimuth angle.
pattern(hydrophone, FREQ , AZ , EL) plots the directivity pattern at specified azimuth and elevation angles.
pattern (__ ,Name, Value) plots the directivity pattern with additional options specified by one or more Name, Value pair arguments.
[PAT,AZ_ANG,EL_ANG] = pattern( $\qquad$ ) returns the array pattern in PAT. The AZ_ANG output contains the coordinate values corresponding to the rows of PAT. The EL_ANG output contains the coordinate values corresponding to the columns of PAT. If the 'CoordinateSystem' parameter is set to ' uv', then AZ_ANG contains the $U$ coordinates of the pattern and EL_ANG contains the $V$ coordinates of the pattern. Otherwise, they are in angular units in degrees. $U V$ units are dimensionless.

## Input Arguments

## hydrophone - Isotropic hydrophone

phased.IsotropicHydrophone System object
Isotropic hydrophone, specified as a phased. IsotropicHydrophone System object.

## Example: phased.IsotropicHydrophone

## FREQ - Frequency for computing directivity and patterns

positive scalar | 1-by-L real-valued row vector
Frequencies for computing directivity and patterns, specified as a positive scalar or 1-by-L realvalued row vector. Frequency units are in hertz.

- For an antenna, microphone, or sonar hydrophone or projector element, FREQ must lie within the range of values specified by the FrequencyRange or FrequencyVector property of the element.

Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased.CustomMic rophoneElement, which use the FrequencyVector property.

- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.


## Example: [1e8 2e6]

Data Types: double

## AZ - Azimuth angles

[-180:180] (default) | 1-by- $N$ real-valued row vector
Azimuth angles for computing directivity and pattern, specified as a 1-by- $N$ real-valued row vector where $N$ is the number of azimuth angles. Angle units are in degrees. Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the $x y$ plane. When measured from the $x$-axis toward the $y$-axis, this angle is positive.

## Example: [-45:2:45] <br> Data Types: double

## EL - Elevation angles

[-90:90] (default) | 1-by-M real-valued row vector
Elevation angles for computing directivity and pattern, specified as a 1-by-M real-valued row vector where $M$ is the number of desired elevation directions. Angle units are in degrees. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

The elevation angle is the angle between the direction vector and $x y$-plane. The elevation angle is positive when measured towards the $z$-axis.
Example: [-75:1:70]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Namel=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## CoordinateSystem - Plotting coordinate system <br> 'polar' (default)|'rectangular' | 'uv'

Plotting coordinate system of the pattern, specified as the comma-separated pair consisting of 'CoordinateSystem' and one of 'polar', 'rectangular', or 'uv'. When 'CoordinateSystem' is set to 'polar' or 'rectangular', the AZ and EL arguments specify the pattern azimuth and elevation, respectively. AZ values must lie between $-180^{\circ}$ and $180^{\circ}$. EL values must lie between $-90^{\circ}$ and $90^{\circ}$. If 'CoordinateSystem' is set to ' uv' , AZ and EL then specify $U$ and $V$ coordinates, respectively. AZ and EL must lie between -1 and 1.
Example: 'uv'

## Data Types: char

## Type - Displayed pattern type

'directivity' (default)|'efield'|'power'|'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb ' - power pattern converted to dB.


## Example: 'powerdb'

Data Types: char

## Normalize - Display normalize pattern

true (default) | false
Display normalized pattern, specified as the comma-separated pair consisting of 'Normalize' and a Boolean. Set this parameter to true to display a normalized pattern. This parameter does not apply when you set 'Type' to 'directivity'. Directivity patterns are already normalized.
Data Types: logical

## PlotStyle - Plotting style

'overlay' (default)|'waterfall'
Plotting style, specified as the comma-separated pair consisting of 'Plotstyle' and either 'overlay' or 'waterfall'. This parameter applies when you specify multiple frequencies in FREQ in 2-D plots. You can draw 2-D plots by setting one of the arguments AZ or EL to a scalar.

## Data Types: char

## Polarization - Polarized field component

'combined' (default) | 'H' | 'V'
Polarized field component to display, specified as the comma-separated pair consisting of 'Polarization' and 'combined ', 'H', or 'V'. This parameter applies only when the sensors are polarization-capable and when the 'Type' parameter is not set to 'directivity'. This table shows the meaning of the display options.

| 'Polarization' | Display |
| :--- | :--- |
| 'combined ' | Combined $H$ and $V$ polarization components |
| 'H' | $H$ polarization component |
| 'V' | $V$ polarization component |

Example: 'V '
Data Types: char

## Output Arguments

## PAT - Element pattern

$N$-by-M real-valued matrix
Element pattern, returned as an $N$-by- $M$ real-valued matrix. The pattern is a function of azimuth and elevation. The rows of PAT correspond to the azimuth angles in the vector specified by EL_ANG. The columns correspond to the elevation angles in the vector specified by AZ ANG.

## AZ_ANG - Azimuth angles

scalar | 1-by- $N$ real-valued row vector
Azimuth angles for displaying directivity or response pattern, returned as a scalar or 1-by- N realvalued row vector corresponding to the dimension set in AZ. The columns of PAT correspond to the values in AZ_ANG. Units are in degrees.

## EL_ANG - Elevation angles

scalar | 1-by-M real-valued row vector
Elevation angles for displaying directivity or response, returned as a scalar or 1-by-M real-valued row vector corresponding to the dimension set in EL. The rows of PAT correspond to the values in EL_ANG. Units are in degrees.

## Examples

## Response and Pattern of Isotropic Hydrophone for Single Frequency

Examine the response and patterns of an isotropic hydrophone operating between 1 kHz and 10 kHz .
Set up the hydrophone parameters. Obtain the voltage sensitivity at five different elevation angles: $-30^{\circ},-15^{\circ}, 0^{\circ}, 15^{\circ}$ and $30^{\circ}$. All azimuth angles are at $0^{\circ}$. The sensitivities are computed at the signal frequency of 2 kHz .

```
hydrophone = phased.IsotropicHydrophone('FrequencyRange', ...
    [1 10]*le3);
fc = 2e3;
resp = hydrophone(fc,[0 0 0 0 0;-30 -15 0 15 30]);
```

Draw a 3-D plot of the voltage sensitivity.

```
pattern(hydrophone,fc,[-180:180],[-90:90], ...
```

    'CoordinateSystem','polar','Type','powerdb')
    

## Response and Pattern of Isotropic Hydrophone at Multiple Frequencies

Examine the response and patterns of an isotropic hydrophone at three different frequencies. The hydrophone operates between 1 kHz and 10 kHz . Specify the voltage sensitivity as a vector.

Set up the hydrophone parameters and obtain the voltage sensitivity at $45^{\circ}$ azimuth and $30^{\circ}$ elevation. Compute the sensitivities at the signal frequencies of 2, 5, and 7 kHz .

```
hydrophone = phased.IsotropicHydrophone('FrequencyRange',[1 10]*1e3, ...
```

    'VoltageSensitivity',[-100 -90-100]);
    fc = [2e3 5e3 7e3];
resp $=$ hydrophone(fc,[45;30])
resp $=1 \times 3$
$14.8051 \quad 29.2202 \quad 24.4152$

Draw a 2-D plot of the voltage sensitivity as a function of azimuth.

```
pattern(hydrophone,fc,[-180:180],0,'CoordinateSystem','rectangular',...
    'Type','power')
```



## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as dBi. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Version History Introduced in R2017a

## See Also

patternAzimuth | patternElevation

## patternAzimuth

System object: phased. IsotropicHydrophone
Package: phased
Plot isotropic hydrophone directivity and response patterns versus azimuth

## Syntax

```
patternAzimuth(hydrophone,FREQ)
patternAzimuth(hydrophone,FREQ,EL)
patternAzimuth(hydrophone,FREQ,EL,Name,Value)
PAT = patternAzimuth(
```

$\qquad$

## Description

patternAzimuth (hydrophone, FREQ) plots the 2-D element directivity pattern versus azimuth (in dBi ) for the element hydrophone at zero degrees elevation angle. The argument FREQ specifies the operating frequency.
patternAzimuth (hydrophone, FREQ,EL), in addition, plots the 2-D element directivity pattern versus azimuth (in dBi ) at the elevation angle specified by EL. When EL is a vector, multiple overlaid plots are created.
patternAzimuth(hydrophone, FREQ, EL,Name, Value) plots the element pattern with additional options specified by one or more Name, Value pair arguments.

PAT $=$ patternAzimuth ( __ ) returns the element pattern. PAT is a matrix whose entries represent the pattern at corresponding sampling points specified by the 'Azimuth' parameter and the EL input argument.

## Input Arguments

## hydrophone - Isotropic hydrophone

phased.IsotropicHydrophone System object
Isotropic hydrophone, specified as a phased. IsotropicHydrophone System object.

## Example: phased.IsotropicHydrophone

## FREQ - Frequency for computing directivity and pattern

positive scalar
Frequency for computing directivity and pattern, specified as a positive scalar. Frequency units are in hertz.

- For an antenna or microphone element, FREQ must lie within the range of values specified by the FrequencyRange or the FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased. CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: 1e8
Data Types: double

## EL - Elevation angles

1-by- $N$ real-valued row vector
Elevation angles for computing sensor or array directivities and patterns, specified as a 1-by- $N$ realvalued row vector. The quantity $N$ is the number of requested elevation directions. Angle units are in degrees. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

The elevation angle is the angle between the direction vector and the xy plane. When measured toward the $z$-axis, this angle is positive.
Example: [0, 10, 20]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Type - Displayed pattern type

'directivity' (default) | 'efield' | 'power' | 'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power ' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb ' - power pattern converted to dB.

Example: 'powerdb'
Data Types: char

## Azimuth - Azimuth angles

[-180:180] (default) | 1-by-P real-valued row vector
Azimuth angles, specified as the comma-separated pair consisting of 'Azimuth' and a 1-by-P realvalued row vector. Azimuth angles define where the array pattern is calculated.
Example: 'Azimuth', [-90:2:90]
Data Types: double

## Output Arguments

## PAT - Element directivity or pattern

$P$-by- $N$ real-valued matrix
Element directivity or pattern, returned as an $P$-by- $N$ real-valued matrix. The dimension $P$ is the number of azimuth values determined by the 'Azimuth' name-value pair argument. The dimension $N$ is the number of elevation angles, as determined by the EL input argument.

## Examples

## Azimuth Pattern of Isotropic Hydrophone

Examine the azimuth pattern of an isotropic hydrophone at $30^{\circ}$ elevation. The frequency range is between 1 kHz and 10 kHz . Specify the voltage sensitivity as a vector.

First, set up the hydrophone parameters.
$\mathrm{fc}=3 \mathrm{e} 3$;
hydrophone = phased.IsotropicHydrophone('FrequencyRange',[1,10]*1e3, ...
'VoltageSensitivity', [-100, -90, -100]) ;
patternAzimuth(hydrophone,fc,30)


Directivity (dBi), Broadside at $0.00^{\circ}$
Plot a smaller range of azimuth angles using the Azimuth parameter.


Directivity (dBi), Broadside at $0.00^{\circ}$

## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \Pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Version History

Introduced in R2017a

See Also<br>pattern| patternElevation

## patternElevation

System object: phased. IsotropicHydrophone
Package: phased
Plot isotropic hydrophone directivity and response patterns versus elevation

## Syntax

```
patternElevation(hydrophone,FREQ)
patternElevation(hydrophone,FREQ,AZ)
patternElevation(hydrophone, FREQ,AZ,Name,Value)
PAT = patternElevation(
```

$\qquad$

``` )
```


## Description

patternElevation(hydrophone, FREQ) plots the 2-D element directivity pattern versus elevation (in dBi ) for the element hydrophone at zero degrees azimuth angle. The argument FREQ specifies the operating frequency.
patternElevation(hydrophone, FREQ,AZ), in addition, plots the 2-D element directivity pattern versus elevation (in dBi ) at the azimuth angle specified by $A Z$. When $A Z$ is a vector, multiple overlaid plots are created.
patternElevation(hydrophone, FREQ,AZ,Name, Value) plots the element pattern with additional options specified by one or more Name, Value pair arguments.

PAT = patternElevation $\qquad$ ) returns the element pattern. PAT is a matrix whose entries represent the pattern at corresponding sampling points specified by the 'Elevation' parameter and the $A Z$ input argument.

## Input Arguments

## hydrophone - Isotropic hydrophone

phased.IsotropicHydrophone System object
Isotropic hydrophone, specified as a phased. IsotropicHydrophone System object.

## Example: phased.IsotropicHydrophone

## FREQ - Frequency for computing directivity and pattern

positive scalar
Frequency for computing directivity and pattern, specified as a positive scalar. Frequency units are in hertz.

- For an antenna or microphone element, FREQ must lie within the range of values specified by the FrequencyRange or the FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased.CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: 1e8
Data Types: double

## AZ - Azimuth angles for computing directivity and pattern

1-by- $N$ real-valued row vector
Azimuth angles for computing sensor or array directivities and patterns, specified as a 1-by- N realvalued row vector where $N$ is the number of desired azimuth directions. Angle units are in degrees. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the xy plane. This angle is positive when measured from the $x$-axis toward the $y$-axis.
Example: [0,10,20]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Type - Displayed pattern type

'directivity' (default) | 'efield' | 'power' | 'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb ' - power pattern converted to dB.

Example: 'powerdb'
Data Types: char

## Elevation - Elevation angles

[-90:90] (default)| 1-by-P real-valued row vector
Elevation angles, specified as the comma-separated pair consisting of 'Elevation' and a 1-by-P real-valued row vector. Elevation angles define where the array pattern is calculated.
Example: 'Elevation', [-90:2:90]
Data Types: double

## Output Arguments

## PAT - Element directivity or pattern

$P-$ by- $N$ real-valued matrix
Element directivity or pattern, returned as an $P$-by- $N$ real-valued matrix. The dimension $P$ is the number of elevation angles determined by the 'Elevation' name-value pair argument. The dimension $N$ is the number of azimuth angles determined by the AZ argument.

## Examples

## Elevation Pattern of Isotropic Hydrophone

Plot an elevation cut of directivity of an isotropic hydrophone at $45^{\circ}$ azimuth. Assume the signal frequency is 3 kHz . First, set up the hydrophone parameters.

```
fc = 3e3;
hydrophone = phased.IsotropicHydrophone('FrequencyRange',[1,10]*1e3, ...
    'VoltageSensitivity',[-100,-90,-100]);
patternElevation(hydrophone,fc,45)
```



Directivity (dBi), Broadside at $0.00^{\circ}$
Plot a smaller range of elevation angles using the Elevation parameter.
patternElevation(hydrophone, fc,45,'Elevation',-20:20)


Directivity (dBi), Broadside at $0.00^{\circ}$

## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Version History Introduced in R2017a

## See Also

pattern|patternAzimuth

## step

System object: phased. Isot ropicHydrophone
Package: phased
Voltage sensitivity of isotropic hydrophone

## Syntax

resp $=$ step(hydrophone,freq,ang)

## Description

Note Instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, x) and y = obj $(x)$ perform equivalent operations.
resp $=$ step(hydrophone,freq, ang) returns the voltage sensitivity for the hydrophone at the specified operating frequencies and in the specified directions of arriving signals.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## hydrophone - Isotropic hydrophone

phased.IsotropicHydrophone System object
Isotropic hydrophone, specified as a phased. IsotropicHydrophone System object.

## Example: phased.IsotropicHydrophone

## freq - Voltage sensitivity frequencies

positive real scalar | real-valued 1 -by- $L$ vector of positive values
Voltage sensitivity frequencies of hydrophone, specified as a positive real scalar or a real-valued 1-by$L$ vector of positive values. Units are in Hz .

## Data Types: double

## ang - Direction of arriving signals

real-valued 1-by-M row vector | real-valued 2-by-M matrix
Direction of arriving signals, specified as a real-valued 1-by- $M$ row vector or 2-by-M matrix. When ang is a 2 -by- $M$ matrix, each column of the matrix specifies the direction in the form
[azimuth;elevation]. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive.

When ang is a 1 -by- $M$ row vector, each element specifies the azimuth angle of the arriving signal. In this case, the corresponding elevation angle is assumed to be zero.
Data Types: double

## Output Arguments

## resp - Voltage sensitivity of hydrophone

Voltage sensitivity of hydrophone, returned as a real-valued $M$-by- $L$ matrix. $M$ represents the number of angles specified in ang, and $L$ represents the number of frequencies specified in freq. Units are in V/Pa.

## Examples

## Response and Pattern of Isotropic Hydrophone for Single Frequency

Examine the response and patterns of an isotropic hydrophone operating between 1 kHz and 10 kHz .
Set up the hydrophone parameters. Obtain the voltage sensitivity at five different elevation angles: $-30^{\circ},-15^{\circ}, 0^{\circ}, 15^{\circ}$ and $30^{\circ}$. All azimuth angles are at $0^{\circ}$. The sensitivities are computed at the signal frequency of 2 kHz .
hydrophone $=$ phased.IsotropicHydrophone('FrequencyRange', ...
[1 10]*1e3);
fc = 2e3;
resp $=$ hydrophone(fc,[0 $0000 ;-30-15015$ 30]);
Draw a 3-D plot of the voltage sensitivity.
pattern(hydrophone,fc,[-180:180],[-90:90], ...
'CoordinateSystem','polar','Type','powerdb')


## Response and Pattern of Isotropic Hydrophone at Multiple Frequencies

Examine the response and patterns of an isotropic hydrophone at three different frequencies. The hydrophone operates between 1 kHz and 10 kHz . Specify the voltage sensitivity as a vector.

Set up the hydrophone parameters and obtain the voltage sensitivity at $45^{\circ}$ azimuth and $30^{\circ}$ elevation. Compute the sensitivities at the signal frequencies of 2,5 , and 7 kHz .

```
hydrophone = phased.IsotropicHydrophone('FrequencyRange',[1 10]*1e3, ...
```

    'VoltageSensitivity',[-100 -90-100]);
    fc = [2e3 5e3 7e3];
resp = hydrophone(fc,[45;30])
resp $=1 \times 3$
$14.8051 \quad 29.2202 \quad 24.4152$

Draw a 2-D plot of the voltage sensitivity as a function of azimuth.

```
pattern(hydrophone,fc,[-180:180],0,'CoordinateSystem','rectangular',...
    'Type','power')
```



## Algorithms

The total sensitivity of a hydrophone is a combination of its frequency sensitivity and spatial sensitivity. phased. IsotropicHydrophone calculates both sensitivities using nearest neighbor interpolation, and then multiplies the sensitivities to form the total sensitivity.

## See Also

uv2azel|phitheta2azel

# phased.IsotropicProjector 

Package: phased
Isotropic projector element

## Description

The phased. IsotropicProjector System object creates an isotropic sound projector used in sonar applications. An isotropic projector has the same response in all directions. The response is the radiated sound intensity per unit input voltage to the projector. You can change the response using the VoltageResponse property.

To compute the response of the isotropic projector for specified directions:
1 Create the phased.IsotropicProjector object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

projector $=$ phased.IsotropicProjector
projector = phased.IsotropProjector(Name=Value)

## Description

projector = phased.IsotropicProjector creates an isotropic projector System object, projector.
projector $=$ phased.IsotropProjector(Name=Value) creates an Isotropic projector object, projector, with each specified property set to the specified value. You can specify additional namevalue pair arguments in any order as (Namel=Value1,...,NameN=ValueN).

Example: projector = phased.IsotropicProjector(FrequencyRange=[0
1000], BackBaffled=true) creates an isotropic projector element with its frequency range specified between 0 and 1000 Hz .

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## FrequencyRange - Operating frequency range of projector

[0 100e6] (default) | real-valued 1-by-2 vector
Operating frequency range of projector, specified as a 1 -by- 2 row vector in the form of [LowerBound HigherBound]. This property defines the frequency range over which the projector has a response. The projector element has zero response outside this frequency range. Units are in Hz..
Example: [0 10e3]
Data Types: double

## VoltageResponse - Voltage response of projector

120 (default) | scalar | real-valued 1-by-K row vector
Voltage response of projector, specified as a scalar or real-valued 1-by-K row vector. When you specify voltage response as a scalar, that value applies to the entire frequency range specified by FrequencyRange. When you specify the voltage sensitivity as a vector, the frequency range is divided into K-1 equal intervals. The response values are assigned to the interval end points. Then, the step method interpolates the voltage response for any frequency inside the frequency range. Units are in dB ref: $1 \mu \mathrm{~Pa} / \mathrm{V}$. See "Projector Voltage Response" on page 1-844 for more details.
Example: 10
Data Types: double

## BackBaffled - Back baffle response of projector <br> false (default)| true

Back baffle response of projector, specified as false or true. Set this property to true to back baffle the projector response. When the projector is back baffled, the projector response for all azimuth angles beyond $\pm 90$ from broadside are zero. Broadside is defined as $0^{\circ}$ azimuth and $0^{\circ}$ elevation.

When the value of this property is false, the projector is not back baffled.

## Usage

## Syntax

resp $=$ projector(freq,ang)

## Description

resp $=$ projector(freq,ang) returns the voltage response resp for the projector at the specified operating frequencies freq and in the specified directions ang of arriving signals.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## freq - Voltage response frequencies <br> positive real scalar | real-valued 1-by-L vector of positive values

Voltage response frequencies of projector, specified as a positive real scalar or a real-valued 1-by-L vector of positive values. Units are in Hz .

Data Types: double

## ang - Direction of arriving signals

real-valued 1-by-M row vector | real-valued 2-by-M matrix
Direction of arriving signals, specified as a real-valued 1-by- $M$ row vector or 2-by-M matrix. When ang is a 2 -by- $M$ matrix, each column of the matrix specifies the direction in the form [azimuth; elevation]. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive.

When ang is a 1 -by- $M$ row vector, each element specifies the azimuth angle of the arriving signal. In this case, the corresponding elevation angle is assumed to be zero.

## Data Types: double

## Output Arguments

## resp - Voltage response of projector

real-valued $M$-by-L matrix
Voltage response of projector, returned as a real-valued $M$-by- $L$ matrix. $M$ represents the number of angles specified in ang, and $L$ represents the number of frequencies specified in freq. Units are in $\mathrm{V} / \mathrm{Pa}$.

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```


## Specific to Antenna and Transducer Element System Objects

beamwidth
directivity
isPolarizationCapable
pattern
patternAzimuth
patternElevation

Compute and display beamwidth of sensor element pattern Directivity of antenna or transducer element Antenna element polarization capability Plot antenna or transducer element directivity and patterns Plot antenna or transducer element directivity and pattern versus azimuth Plot antenna or transducer element directivity and pattern versus elevation

## Common to All System Objects

step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object

## Examples

## Response of Isotropic Projector

Find the response of an isotropic projector with default properties. Obtain the voltage response at five different elevation angles: $-30^{\circ},-15^{\circ}, 0^{\circ}, 15^{\circ}$ and $30^{\circ}$. All azimuth angles are set to $0^{\circ}$. The voltage response is computed at 2 kHz .

```
projector = phased.IsotropicProjector;
fc = 2e3;
resp = projector(fc,[0,0,0,0,0;-30,-15,0,15,30])
resp = 5×1
    1
    1
    1
    1
    1
```


## Response and Pattern of Isotropic Projector at Single Frequency

Examine the response and patterns of an isotropic projector operating between 1 kHz and 10 kHz .
Set the projector parameters and obtain the voltage response at five different elevation angles: $-30^{\circ}$, $-15^{\circ}, 0^{\circ}, 15^{\circ}$ and $30^{\circ}$. All elevation angles at $0^{\circ}$ azimuth angle. The voltage response is computed at 2 kHz .

```
projector = phased.IsotropicProjector('FrequencyRange',[1,10]*1e3);
fc = 2e3;
resp = projector(fc,[0,0,0,0,0;-30,-15,0,15,30]);
```

Draw a 3-D plot of the voltage response.
pattern(projector,fc,[-180:180],[-90:90],'CoordinateSystem','polar', ...
'Type','power')


Plot Beamwidth of Isotropic Projector
Find the beamwidth of an isotropic underwater projector at 10 kHz .
First, create an isotropic projector element.

```
projector = phased.IsotropicProjector('FrequencyRange',[10 12000])
projector =
    phased.IsotropicProjector with properties:
        VoltageResponse: 120
        FrequencyRange: [10 12000]
            BackBaffled: false
```

Then, use the beamwidth object function to plot the 3 dB beamwidth of the projector.
[bmw,angs] = beamwidth(projector,10000,'dbDown', 3)

```
bmw = 360
```

angs $=1 \times 2$
- 180180

Because the projector is isotropic, there is no 3 dB down point.

## Response and Pattern of Isotropic Projector at Multiple Frequencies

Examine the response and patterns of an isotropic projector at three different frequencies. The projector operates between 1 kHz and 10 kHz . Specify the voltage response as a vector.

Set up the projector parameters, and obtain the voltage response at $45^{\circ}$ azimuth and $30^{\circ}$ elevation. Compute the responses at signal frequencies of 2,5 , and 7 kHz .

```
projector = phased.IsotropicProjector('FrequencyRange',[1 10]*1e3, ...
    'VoltageResponse',[90 95 100 95 90]);
fc = [2e3 5e3 7e3];
resp = projector(fc,[45;30]);
resp
resp = 1\times3
    0.0426 0.0903 0.0708
```

Next, draw a 2-D plot of the voltage response as a function of azimuth.
pattern(projector,fc,[-180:180],0,'CoordinateSystem','rectangular', ... 'Type','power')


## Directivity of Isotropic Projector

Compute the directivity of an isotropic projector in different directions. Assume the signal frequency is 3 kHz . First, set the projector parameters.
fc = 3e3;
projector = phased.IsotropicProjector('FrequencyRange', [1,10]*1e3, ...
'VoltageResponse',[100,110,120,110,100]);
patternElevation(projector,fc,45)


Directivity (dBi), Broadside at $0.00^{\circ}$

Select the angles of interest to be constant elevation angle at zero degrees. The five azimuth angles are centered around boresight (zero degrees azimuth and zero degrees elevation).
ang $=[-20,-10,0,10,20 ; 0,0,0,0,0] ;$
Compute the directivity along the constant elevation cut.

```
d = directivity(projector,fc,ang)
d = 5\times1
```

0
0
0
0

0

The directivity of an isotropic projector is zero in every direction

## Azimuth Pattern of Isotropic Projector

Examine the azimuth pattern of an isotropic projector at $30^{\circ}$ elevation. The frequency range is between 1 kHz and 10 kHz . Specify the voltage response as a scalar.

Set the projector parameters.
$\mathrm{fc}=3 \mathrm{e}$;
projector = phased.IsotropicProjector('FrequencyRange',[1,10]*1e3, ...
'VoltageResponse',-115);
patternAzimuth(projector,fc,30)


Directivity (dBi), Broadside at $0.00^{\circ}$

Plot a smaller range of azimuth angles using the Azimuth parameter.
patternAzimuth(projector,fc,30,'Azimuth', [-20:20])


Directivity (dBi), Broadside at $0.00^{\circ}$

## Elevation Pattern of Isotropic Projector

Plot an elevation cut of the directivity of an isotropic projector at $45^{\circ}$ azimuth. Assume the signal frequency is 3 kHz .

Create the isotropic projector object and call the pattern object function.
fc = 3e3;
projector $=$ phased.IsotropicProjector('FrequencyRange', [1,10]*1e3, ... 'VoltageResponse',70);
patternElevation(projector,fc,45)


Directivity (dBi), Broadside at $0.00^{\circ}$

Plot a smaller range of elevation angles using the Elevation parameter. patternElevation(projector,fc, 45,'Elevation',-20:20)


Directivity (dBi), Broadside at $0.00^{\circ}$

## More About

## Projector Voltage Response

The voltage response of a projector relates the transmitted sound intensity to the input voltage.
For a sound projector, the transmitting voltage response (TVR) is the sound intensity in $\mu \mathrm{Pa}$ per volt, when measured at one meter from the projector. TVR is generally a function of frequency. If the sound intensity level (SIL) is expressed in $\mathrm{dB} / / \mu \mathrm{Pa}$ and the output voltage ( VdB ) is expressed in $d B / / 1 \mathrm{~V}$, then TVR is expressed in $\mathrm{dB} / / \mu \mathrm{Pa} / 1 \mathrm{~V}$. The output sound pressure level of a hydrophone is related to the input voltage level by

SIL $=\mathrm{TVR}+\mathrm{VdB}$.
Consider a projector that has $\mathrm{TVR}=160 \mathrm{~dB} / / \mu \mathrm{Pa} / 1 \mathrm{~V}$ at 10 kHz . If the projector input voltage is 200 V , then the VdB is 23 dB and the sound intensity level (SIL) at one meter is
$\mathrm{SIL}=\mathrm{TVR}+\mathrm{VdB}=160+23=173 \mathrm{~dB} / / \mu \mathrm{Pa}$.

## Version History

Introduced in R2017a

## References

[1] Urick, R.J. Principles of Underwater Sound. 3rd Edition. New York: Peninsula Publishing, 1996.
[2] Sherman, C.S., and J. Butler. Transducers and Arrays for Underwater Sound. New York: Springer, 2007.
[3] Allen, J.B., and D. Berkely. "Image method for efficiently simulating small-room acoustics", Journal of the Acoustical Society of America. Vol. 65, No. 4. April 1979, , pp. 943-950.
[4] Van Trees, H. Optimum Array Processing. New York: Wiley-Interscience, 2002, pp. 274-304.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:

- The pattern, patternAzimuth, and patternElevation methods are not supported.
- See "System Objects in MATLAB Code Generation" (MATLAB Coder).


## See Also

phased.ULA|phased.URA|phased.ConformalArray|phased.IsotropicHydrophone | phased.UnderwaterRadiatedNoise

Topics
"Underwater Target Detection with an Active Sonar System"
"Locating an Acoustic Beacon with a Passive Sonar System"
Phased Array Gallery

## directivity

System object: phased.IsotropicProjector
Package: phased
Directivity of isotropic projector

## Syntax

D = directivity(projector, FREQ,ANGLE)

## Description

D = directivity(projector, FREQ,ANGLE) returns the "Directivity" on page 1-848 of the isotropic projector, projector, at frequencies specified by FREQ and in the directions specified by ANGLE.

## Input Arguments

projector - Isotropic projector
phased.IsotropicProjector System object
Isotropic projector, specified as a phased.Isot ropicProjector System object.

## Example: phased.IsotropicProjector

## FREQ - Frequency for computing directivity and patterns

positive scalar | 1-by-L real-valued row vector
Frequencies for computing directivity and patterns, specified as a positive scalar or 1-by-L realvalued row vector. Frequency units are in hertz.

- For an antenna, microphone, or sonar hydrophone or projector element, FREQ must lie within the range of values specified by the FrequencyRange or FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased.CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.


## Example: [1e8 2e6]

Data Types: double

## ANGLE - Angles for computing directivity

1 -by-M real-valued row vector | 2 -by- $M$ real-valued matrix
Angles for computing directivity, specified as a 1-by- $M$ real-valued row vector or a 2 -by- $M$ real-valued matrix, where $M$ is the number of angular directions. Angle units are in degrees. If ANGLE is a 2-by- $M$ matrix, then each column specifies a direction in azimuth and elevation, [az;el]. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

If ANGLE is a 1 -by- $M$ vector, then each entry represents an azimuth angle, with the elevation angle assumed to be zero.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the xy plane. This angle is positive when measured from the $x$-axis toward the $y$-axis. The elevation angle is the angle between the direction vector and $x y$ plane. This angle is positive when measured towards the $z$-axis. See "Azimuth and Elevation Angles".

Example: [45 60; 0 10]
Data Types: double

## Output Arguments

## D - Directivity

$M$-by-L matrix
Directivity, returned as an $M$-by- $L$ matrix. Each row corresponds to one of the $M$ angles specified by ANGLE. Each column corresponds to one of the $L$ frequency values specified in FREQ. Directivity units are in dBi where dBi is defined as the gain of an element relative to an isotropic radiator.

## Examples

## Directivity of Isotropic Projector

Compute the directivity of an isotropic projector in different directions. Assume the signal frequency is 3 kHz . First, set the projector parameters.

```
fc = 3e3;
projector = phased.IsotropicProjector('FrequencyRange',[1,10]*1e3, ...
    'VoltageResponse', [100,110,120,110,100]);
patternElevation(projector,fc,45)
```



Directivity (dBi), Broadside at $0.00^{\circ}$

Select the angles of interest to be constant elevation angle at zero degrees. The five azimuth angles are centered around boresight (zero degrees azimuth and zero degrees elevation).
ang $=[-20,-10,0,10,20 ; 0,0,0,0,0] ;$
Compute the directivity along the constant elevation cut.
d = directivity(projector,fc,ang)
d $=5 \times 1$
0
0
0
0
0

The directivity of an isotropic projector is zero in every direction.

## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Version History

Introduced in R2017a

See Also<br>pattern | patternAzimuth | patternElevation

## isPolarizationCapable

System object: phased. Isot ropicProjector
Package: phased
Polarization capability

## Syntax

flag = isPolarizationCapable(projector)

## Description

flag = isPolarizationCapable(projector) returns a Boolean value, flag, indicating whether the phased.IsotropicProjector supports polarization. An element supports polarization if it can create or respond to polarized fields. This projector does not support polarization.

## Input Arguments

projector - Isotropic projector
phased.IsotropicProjector System object
Isotropic projector, specified as a phased.IsotropicProjector System object.
Example: phased.IsotropicProjector

## Output Arguments

flag - Polarization-capability flag
true | false
Polarization-capability returned as a Boolean value true if the projector supports polarization or false if it does not. Because the phased. IsotropicProjector object does not support polarization, flag is always returned as false.

## pattern

System object: phased. Isot ropicProjector
Package: phased
Plot isotropic projector directivity and patterns

## Syntax

```
pattern(projector,FREQ)
pattern(projector, FREQ,AZ)
pattern(projector, FREQ,AZ,EL)
pattern(___,Name,Value)
[PAT,AZ_ANG,EL_ANG] = pattern(___)
```


## Description

pattern (projector, FREQ) plots the 3D directivity pattern (in dBi ) for the projector specified in projector. The operating frequency is specified in FREQ.
pattern(projector, $\mathrm{FREQ}, \mathrm{AZ}$ ) plots the projector directivity pattern at the specified azimuth angle.
pattern(projector, $\mathrm{FREQ}, \mathrm{AZ}, \mathrm{EL}$ ) plots the projector directivity pattern at specified azimuth and elevation angles.
pattern (__ , Name, Value) plots the projector pattern with additional options specified by one or more Name, Value pair arguments.
[PAT,AZ_ANG,EL_ANG] = pattern (___ ) returns the projector pattern in PAT. The AZ_ANG output contains the coordinate values corresponding to the rows of PAT. The EL_ANG output contains the coordinate values corresponding to the columns of PAT. If the 'Coordinatesystem' parameter is set to ' $u v$ ', then AZ_ANG contains the $U$ coordinates of the pattern and EL_ANG contains the $V$ coordinates of the pattern. Otherwise, they are in angular units in degrees. $U \bar{V}$ units are dimensionless.

## Input Arguments

## FREQ - Frequency for computing directivity and patterns

positive scalar | 1-by-L real-valued row vector
Frequencies for computing directivity and patterns, specified as a positive scalar or 1-by-L realvalued row vector. Frequency units are in hertz.

- For an antenna, microphone, or sonar hydrophone or projector element, FREQ must lie within the range of values specified by the FrequencyRange or FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased.CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.


## Example: [1e8 2e6]

## Data Types: double

## AZ - Azimuth angles

[-180:180] (default) | 1-by- $N$ real-valued row vector
Azimuth angles for computing directivity and pattern, specified as a 1 -by- $N$ real-valued row vector where $N$ is the number of azimuth angles. Angle units are in degrees. Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the $x y$ plane. When measured from the $x$-axis toward the $y$-axis, this angle is positive.

## Example: [-45:2:45]

Data Types: double

## EL - Elevation angles

[-90:90] (default) | 1-by-M real-valued row vector
Elevation angles for computing directivity and pattern, specified as a 1 -by- $M$ real-valued row vector where $M$ is the number of desired elevation directions. Angle units are in degrees. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

The elevation angle is the angle between the direction vector and $x y$-plane. The elevation angle is positive when measured towards the $z$-axis.

Example: [-75:1:70]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Namel=Value1, ... ,NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## CoordinateSystem - Plotting coordinate system

'polar' (default)|'rectangular'|'uv'
Plotting coordinate system of the pattern, specified as the comma-separated pair consisting of 'CoordinateSystem' and one of 'polar', 'rectangular', or 'uv'. When
'CoordinateSystem' is set to 'polar' or 'rectangular', the AZ and EL arguments specify the pattern azimuth and elevation, respectively. AZ values must lie between $-180^{\circ}$ and $180^{\circ}$. EL values must lie between $-90^{\circ}$ and $90^{\circ}$. If 'CoordinateSystem' is set to ' uv ', AZ and EL then specify $U$ and $V$ coordinates, respectively. AZ and EL must lie between -1 and 1.
Example: 'uv'
Data Types: char

## Type - Displayed pattern type

'directivity' (default)|'efield'|'power'|'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb ' - power pattern converted to dB.


## Example: ' powerdb'

## Data Types: char

## Normalize - Display normalize pattern

true (default) | false
Display normalized pattern, specified as the comma-separated pair consisting of 'Normalize' and a Boolean. Set this parameter to true to display a normalized pattern. This parameter does not apply when you set 'Type' to 'directivity'. Directivity patterns are already normalized.

## Data Types: logical

## PlotStyle - Plotting style

'overlay' (default)| 'waterfall'
Plotting style, specified as the comma-separated pair consisting of 'Plotstyle' and either 'overlay' or 'waterfall'. This parameter applies when you specify multiple frequencies in FREQ in 2-D plots. You can draw 2-D plots by setting one of the arguments AZ or EL to a scalar.

## Data Types: char

## Polarization - Polarized field component

'combined' (default) | 'H' | 'V'
Polarized field component to display, specified as the comma-separated pair consisting of 'Polarization' and 'combined', 'H', or 'V'. This parameter applies only when the sensors are polarization-capable and when the 'Type' parameter is not set to 'directivity'. This table shows the meaning of the display options.

| 'Polarization' | Display |
| :--- | :--- |
| ' combined ' | Combined $H$ and $V$ polarization components |
| 'H' | $H$ polarization component |
| 'V' | $V$ polarization component |

Example: 'V '
Data Types: char

## Output Arguments

## PAT - Element pattern

$N$-by-M real-valued matrix
Element pattern, returned as an $N$-by- $M$ real-valued matrix. The pattern is a function of azimuth and elevation. The rows of PAT correspond to the azimuth angles in the vector specified by EL_ANG. The columns correspond to the elevation angles in the vector specified by AZ_ANG.

## AZ_ANG - Azimuth angles

scalar | 1-by- $N$ real-valued row vector
Azimuth angles for displaying directivity or response pattern, returned as a scalar or 1-by- $N$ realvalued row vector corresponding to the dimension set in AZ. The columns of PAT correspond to the values in AZ_ANG. Units are in degrees.

## EL_ANG - Elevation angles

scalar | 1-by-M real-valued row vector
Elevation angles for displaying directivity or response, returned as a scalar or 1-by-M real-valued row vector corresponding to the dimension set in EL. The rows of PAT correspond to the values in EL_ANG. Units are in degrees.

## Examples

## Response and Pattern of Isotropic Projector at Single Frequency

Examine the response and patterns of an isotropic projector operating between 1 kHz and 10 kHz .
Set the projector parameters and obtain the voltage response at five different elevation angles: $-30^{\circ}$, $-15^{\circ}, 0^{\circ}, 15^{\circ}$ and $30^{\circ}$. All elevation angles at $0^{\circ}$ azimuth angle. The voltage response is computed at 2 kHz .

```
projector = phased.IsotropicProjector('FrequencyRange',[1,10]*1e3);
```

fc = 2e3;
resp $=$ projector(fc, [0, 0, 0, 0, 0;-30,-15, $0,15,30]$ );

Draw a 3-D plot of the voltage response.

```
pattern(projector,fc,[-180:180],[-90:90],'CoordinateSystem','polar', ...
    'Type','power')
```



## Response and Pattern of Isotropic Projector at Multiple Frequencies

Examine the response and patterns of an isotropic projector at three different frequencies. The projector operates between 1 kHz and 10 kHz . Specify the voltage response as a vector.

Set up the projector parameters, and obtain the voltage response at $45^{\circ}$ azimuth and $30^{\circ}$ elevation. Compute the responses at signal frequencies of 2,5 , and 7 kHz .

```
projector = phased.IsotropicProjector('FrequencyRange',[1 10]*1e3, ...
    'VoltageResponse',[90 95 100 95 90]);
fc = [2e3 5e3 7e3];
resp = projector(fc,[45;30]);
resp
resp = 1\times3
    0.0426 0.0903 0.0708
```

Next, draw a 2-D plot of the voltage response as a function of azimuth.

```
pattern(projector,fc,[-180:180],0,'CoordinateSystem','rectangular', ...
    'Type','power')
```



## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Version History Introduced in R2017a

## See Also

patternAzimuth|patternElevation

## patternAzimuth

System object: phased. IsotropicProjector
Package: phased
Plot isotropic projector directivity and response patterns versus azimuth

## Syntax

```
patternAzimuth(projector,FREQ)
patternAzimuth(projector,FREQ,EL)
patternAzimuth(projector,FREQ,EL,Name,Value)
PAT = patternAzimuth(
```

$\qquad$

## Description

patternAzimuth(projector, FREQ) plots the 2-D element directivity pattern versus azimuth (in dBi ) for the projector, projector, at zero-degrees elevation angle. The argument FREQ specifies the operating frequency.
patternAzimuth(projector, FREQ,EL), in addition, plots the 2-D element directivity pattern versus azimuth (in dBi ) at the elevation angle specified by EL. When EL is a vector, multiple overlaid plots are created.
patternAzimuth(projector, FREQ, EL,Name, Value) plots the element pattern with additional options specified by one or more Name, Value pair arguments.

PAT $=$ patternAzimuth ( __ ) returns the element pattern. PAT is a matrix whose entries represent the pattern at corresponding sampling points specified by the 'Azimuth' parameter and the EL input argument.

## Input Arguments

## projector - Isotropic projector

phased.IsotropicProjector System object
Isotropic projector, specified as a phased.IsotropicProjector System object.
Example: phased.IsotropicProjector

## FREQ - Frequency for computing directivity and pattern

positive scalar
Frequency for computing directivity and pattern, specified as a positive scalar. Frequency units are in hertz.

- For an antenna or microphone element, FREQ must lie within the range of values specified by the FrequencyRange or the FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased. CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: 1e8
Data Types: double

## EL - Elevation angles

1-by- $N$ real-valued row vector
Elevation angles for computing sensor or array directivities and patterns, specified as a 1-by- $N$ realvalued row vector. The quantity $N$ is the number of requested elevation directions. Angle units are in degrees. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

The elevation angle is the angle between the direction vector and the xy plane. When measured toward the $z$-axis, this angle is positive.
Example: [0, 10, 20]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Type - Displayed pattern type

'directivity' (default) | 'efield' | 'power' | 'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power ' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb ' - power pattern converted to dB.

Example: 'powerdb'
Data Types: char

## Azimuth - Azimuth angles

[-180:180] (default) | 1-by-P real-valued row vector
Azimuth angles, specified as the comma-separated pair consisting of 'Azimuth' and a 1-by-P realvalued row vector. Azimuth angles define where the array pattern is calculated.
Example: 'Azimuth', [-90:2:90]
Data Types: double

## Output Arguments

## PAT - Element directivity or pattern

$P$-by- $N$ real-valued matrix
Element directivity or pattern, returned as an $P$-by- $N$ real-valued matrix. The dimension $P$ is the number of azimuth values determined by the 'Azimuth' name-value pair argument. The dimension $N$ is the number of elevation angles, as determined by the EL input argument.

## Examples

## Azimuth Pattern of Isotropic Projector

Examine the azimuth pattern of an isotropic projector at $30^{\circ}$ elevation. The frequency range is between 1 kHz and 10 kHz . Specify the voltage response as a scalar.

Set the projector parameters.

```
fc = 3e3;
projector = phased.IsotropicProjector('FrequencyRange',[1,10]*1e3, ...
    'VoltageResponse',-115);
patternAzimuth(projector,fc,30)
```



Directivity (dBi), Broadside at $0.00^{\circ}$
Plot a smaller range of azimuth angles using the Azimuth parameter.

```
patternAzimuth(projector,fc,30,'Azimuth',[-20:20])
```



Directivity (dBi), Broadside at $0.00^{\circ}$

## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as dBi. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

# Version History <br> Introduced in R2017a 

See Also<br>pattern| patternElevation

## patternElevation

System object: phased.IsotropicProjector
Package: phased
Plot isotropic projector directivity and response patterns versus elevation

## Syntax

```
patternElevation(projector,FREQ)
patternElevation(projector,FREQ,AZ)
patternElevation(projector,FREQ,AZ,Name,Value)
PAT = patternElevation(
```

$\qquad$

``` )
```


## Description

patternElevation(projector, FREQ) plots the 2D element directivity pattern versus elevation (in dBi) for the projector, projector, at zero-degrees azimuth angle. The argument FREQ specifies the operating frequency.
patternElevation(projector, FREQ,AZ), in addition, plots the 2D element directivity pattern versus elevation (in dBi ) at the azimuth angle specified by $A Z$. When $A Z$ is a vector, multiple overlaid plots are created.
patternElevation(projector,FREQ,AZ,Name, Value) plots the element pattern with additional options specified by one or more Name, Value pair arguments.

PAT = patternElevation $\qquad$ ) returns the element pattern. PAT is a matrix whose entries represent the pattern at corresponding sampling points specified by the 'Elevation' parameter and the $A Z$ input argument.

## Input Arguments

## projector - Isotropic projector

phased.IsotropicProjector System object
Isotropic projector, specified as a phased.IsotropicProjector System object.

## Example: phased.IsotropicProjector

## FREQ - Frequency for computing directivity and pattern

positive scalar
Frequency for computing directivity and pattern, specified as a positive scalar. Frequency units are in hertz.

- For an antenna or microphone element, FREQ must lie within the range of values specified by the FrequencyRange or the FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased.CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: 1e8
Data Types: double

## AZ - Azimuth angles for computing directivity and pattern

1-by- $N$ real-valued row vector
Azimuth angles for computing sensor or array directivities and patterns, specified as a 1-by- N realvalued row vector where $N$ is the number of desired azimuth directions. Angle units are in degrees. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the xy plane. This angle is positive when measured from the $x$-axis toward the $y$-axis.
Example: [0,10,20]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Type - Displayed pattern type

'directivity' (default) | 'efield' | 'power' | 'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power ' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb ' - power pattern converted to dB.

Example: 'powerdb'
Data Types: char

## Elevation - Elevation angles

[-90:90] (default)| 1-by-P real-valued row vector
Elevation angles, specified as the comma-separated pair consisting of 'Elevation' and a 1-by-P real-valued row vector. Elevation angles define where the array pattern is calculated.
Example: 'Elevation', [-90:2:90]
Data Types: double

## Output Arguments

## PAT - Element directivity or pattern

$P$-by- $N$ real-valued matrix
Element directivity or pattern, returned as an $P$-by- $N$ real-valued matrix. The dimension $P$ is the number of elevation angles determined by the 'Elevation' name-value pair argument. The dimension $N$ is the number of azimuth angles determined by the AZ argument.

## Examples

## Elevation Pattern of Isotropic Projector

Plot an elevation cut of the directivity of an isotropic projector at $45^{\circ}$ azimuth. Assume the signal frequency is 3 kHz .

Create the isotropic projector object and call the pattern object function.

```
fc = 3e3;
projector = phased.IsotropicProjector('FrequencyRange',[1,10]*1e3, ...
    'VoltageResponse',70);
patternElevation(projector,fc,45)
```



Directivity $(\mathrm{dBi})$, Broadside at $0.00^{\circ}$
Plot a smaller range of elevation angles using the Elevation parameter.
patternElevation(projector,fc,45,'Elevation',-20:20)


Directivity (dBi), Broadside at $0.00^{\circ}$

## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \Pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Version History

Introduced in R2017a

See Also<br>pattern| patternAzimuth

## step

System object: phased.IsotropicProjector
Package: phased
Voltage response of isotropic projector

## Syntax

resp = step(projector,freq,ang)

## Description

Note Instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, x) and y = obj $(x)$ perform equivalent operations.
resp $=$ step(projector, freq,ang) returns the voltage response for the projector at the specified operating frequencies and in the specified directions of arriving signals.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

projector - Isotropic projector
phased.IsotropicProjector System object
Isotropic projector, specified as a phased.IsotropicProjector System object.
Example: phased.IsotropicProjector

## freq - Voltage response frequencies

positive real scalar | real-valued 1-by-L vector of positive values
Voltage response frequencies of projector, specified as a positive real scalar or a real-valued 1-by-L vector of positive values. Units are in Hz .
Data Types: double

## ang - Direction of arriving signals

real-valued 1-by-M row vector | real-valued 2-by-M matrix
Direction of arriving signals, specified as a real-valued 1-by- $M$ row vector or 2-by-M matrix. When ang is a 2 -by- $M$ matrix, each column of the matrix specifies the direction in the form
[azimuth;elevation]. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive.

When ang is a 1 -by- $M$ row vector, each element specifies the azimuth angle of the arriving signal. In this case, the corresponding elevation angle is assumed to be zero.
Data Types: double

## Output Arguments

## resp - Voltage response of projector

real-valued M-by-L matrix
Voltage response of projector, returned as a real-valued $M$-by- $L$ matrix. $M$ represents the number of angles specified in ang, and $L$ represents the number of frequencies specified in freq. Units are in V/Pa.

## Examples

## Response and Pattern of Isotropic Projector at Single Frequency

Examine the response and patterns of an isotropic projector operating between 1 kHz and 10 kHz .
Set the projector parameters and obtain the voltage response at five different elevation angles: $-30^{\circ}$, $-15^{\circ}, 0^{\circ}, 15^{\circ}$ and $30^{\circ}$. All elevation angles at $0^{\circ}$ azimuth angle. The voltage response is computed at 2 kHz .

```
projector = phased.IsotropicProjector('FrequencyRange',[1,10]*1e3);
```

fc = 2e3;
resp $=$ projector(fc,[0,0,0,0,0;-30,-15,0,15,30]);

Draw a 3-D plot of the voltage response.

```
pattern(projector,fc,[-180:180],[-90:90],'CoordinateSystem','polar', ...
    'Type','power')
```



## Response and Pattern of Isotropic Projector at Multiple Frequencies

Examine the response and patterns of an isotropic projector at three different frequencies. The projector operates between 1 kHz and 10 kHz . Specify the voltage response as a vector.

Set up the projector parameters, and obtain the voltage response at $45^{\circ}$ azimuth and $30^{\circ}$ elevation. Compute the responses at signal frequencies of 2,5 , and 7 kHz .

```
projector = phased.IsotropicProjector('FrequencyRange',[1 10]*1e3, ...
    'VoltageResponse',[90 95 100 95 90]);
fc = [2e3 5e3 7e3];
resp = projector(fc,[45;30]);
resp
resp = 1×3
    0.0426 0.0903 0.0708
```

Next, draw a 2-D plot of the voltage response as a function of azimuth.

```
pattern(projector,fc,[-180:180],0,'CoordinateSystem','rectangular', ...
    'Type','power')
```



## Algorithms

The total response of a projector is a combination of its frequency response and spatial response. phased.IsotropicProjector calculates both responses using nearest neighbor interpolation, and then multiplies the responses to form the total response.

## See Also <br> uv2azel | phitheta2azel

# phased.LCMVBeamformer 

Package: phased
Narrowband LCMV beamformer

## Description

The phased.LCMVBeamformer object implements a narrowband linear-constraint minimum-variance (LCMV) beamformer for a sensor array. The LCMV beamformer belongs to the family of constrained optimization beamformers.

To beamform signals arriving at a sensor array:
1 Create the phased.LCMVBeamformer object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

beamformer = phased.LCMVBeamformer
beamformer $=$ phased.LCMVBeamformer(Name,Value)

## Description

beamformer $=$ phased.LCMVBeamformer creates an LCMV beamformer System object, beamformer, with default property values.
beamformer $=$ phased.LCMVBeamformer(Name, Value) creates an LCMV beamformer with each property Name set to a specified Value. You can specify additional name-value pair arguments in any order as (Namel,Value1,...,NameN,ValueN). Enclose each property name in single quotes.
Example: beamformer = phased.LCMVBeamformer('Constraint', [1;1]) sets the constraint matrix.

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## Constraint - Constraint matrix

[1;1] (default) | complex-valued $N$-by-K matrix

Constraint matrix, specified as a complex-valued $N$-by- $K$ matrix. Each column of the matrix represents a constraint. $N$ is the number of elements in the sensor array and $K$ is the number of constraints. $K$ must be less than or equal to $N, K \leq N$.
Example: [1 1i;1 1i]
Data Types: single|double
Complex Number Support: Yes

## DesiredResponse - Desired response

1 (default) | complex-valued K-by-1 vector
Desired response of the LCMV beamformer, specified as a complex-valued $K$-by- 1 vector, where $K$ is the number of constraints in the Constraint property. Each element in the vector defines the desired response of the constraint specified in the corresponding column of the Constraint property. A value of one creates a distortionless response and a value of zero creates a null response.

Example: [1;0]
Data Types: single | double
Complex Number Support: Yes

## DiagonalLoadingFactor - Diagonal loading factor <br> 0 (default) | nonnegative scalar

Diagonal loading factor, specified as a nonnegative scalar. Diagonal loading is a technique used to achieve robust beamforming performance, especially when the sample size is small. A small sample size can lead to an inaccurate estimate of the covariance matrix. Diagonal loading also provides robustness due to steering vector errors. The diagonal loading technique adds a positive scalar multiple of the identity matrix to the sample covariance matrix.

## Tunable: Yes

Data Types: single | double

## TrainingInputPort - Enable training data input <br> false (default) | true

Enable training data input, specified as false or true. When you set this property to true, use the training data input argument, XT , when running the object. Set this property to false to use the input data, X , as the training data.
Data Types: logical
WeightsOutputPort - Enable beamforming weights output
false (default) | true
Enable the output of beamforming weights, specified as false or true. To obtain the beamforming weights, set this property to true and use the corresponding output argument, W. If you do not want to obtain the weights, set this property to false.
Data Types: logical

## Usage

## Syntax

$\mathrm{Y}=$ beamformer(X)
$Y=$ beamformer (X,XT)
[ $\mathrm{Y}, \mathrm{W}$ ] = beamformer (__ )

## Description

$Y=$ beamformer $(X)$ performs LCMV beamforming on the input array data, $X$, and returns the beamformed output in Y .
$\mathrm{Y}=$ beamformer $(\mathrm{X}, \mathrm{XT})$ uses XT as training data to calculate the beamforming weights. To use this syntax, set the TrainingInputPort property to true.
$[Y, W]=$ beamformer (__ ) returns the beamforming weights $W$. To use this syntax, set the WeightsOutputPort property to true.

## Input Arguments

## X - Array element data

complex-valued $M$-by- $N$ matrix
Array element data, specified as an $M$-by- $N$ matrix where $N$ is the number of elements in the sensor array.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
Example: [1 0.5 2.6; 2-0.2 0]
Data Types: single | double

## XT - Training data

complex-valued $P$-by- $N$ matrix
Training data, specified as a $P$-by- $N$ matrix. $N$ is the number of elements of the sensor array. $P$ is the length of the training data and must be greater than $N$.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
Example: [1 0.5 2.6; 2 -0.2 0; 3-2 -1]

## Dependencies

To enable this argument, set the TrainingInputPort property to true.
Data Types: single | double

## Output Arguments

Y - Beamformed output
complex-valued $M$-by-1 vector

Beamformed output, returned as a complex-valued $M$-by- 1 vector.
Data Types: single | double
W - Beamformer weights
complex-valued N -by-1 vector
Beamformer weights, returned as a complex-valued $N$-by- 1 vector. $N$ is the number of elements in the sensor array.

## Dependencies

To enable this argument, set the WeightsOutputPort property to true.
Data Types: single | double

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:
release(obj)

## Common to All System Objects

step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object

## Examples

## LCMV Beamformer with One Constraint

Apply an LCMV beamformer to a 5 -element ULA of isotropic sensor elements, preserving the signal from a desired direction. The operating frequency is 300 MHz .

Simulate a low-frequency sinusoid signal in Gaussian noise.

```
f = 50;
t = (0:.001:.3)';
x = sin(2*pi*f*t);
c = physconst('LightSpeed');
fc = 300e6;
lambda = c/fc;
incidentAngle = [45;0];
antenna = phased.IsotropicAntennaElement('FrequencyRange',[20 20e8]);
array = phased.ULA('NumElements',5,'ElementSpacing',lambda/2,...
    'Element',antenna);
x = collectPlaneWave(array,x,incidentAngle,fc,c);
noise = 0.2*(randn(size(x)) + lj*randn(size(x)));
rx = x + noise;
```

Beamform the array.

```
steervec = phased.SteeringVector('SensorArray',array,...
    'PropagationSpeed',c);
beamformer = phased.LCMVBeamformer('Constraint',steervec(fc,incidentAngle),'DesiredResponse',1);
y = beamformer(rx);
```

Plot the original and beamformed signals.
plot(t, real(rx(: 3$)), ' r: ', t, r e a l(y), t, r e a l(x(:, 3)), ' g ')$
xlabel('Time (sec)')
ylabel('Amplitude')
legend('Signal at Sensor 3','Beamformed Signal','Noise Free Signal')


## Nulling with LCMV Beamformer

This example shows how to use an LCMV beamformer to point a null of the array response in the direction of an interfering source. The array is a 10 -element uniform linear array (ULA). By default, the ULA elements are isotropic antennas created by the phased. IsotropicAntennaElement System object ${ }^{\mathrm{TM}}$. Set the frequency range of the antenna elements so that the carrier frequency lies within the operating range. The carrier frequency is 1 GHz .

```
fc = 1e9;
lambda = physconst('LightSpeed')/fc;
array = phased.ULA('NumElements',10,'ElementSpacing',lambda/2);
array.Element.FrequencyRange = [8e8 1.2e9];
```

Simulate a test signal using a simple rectangular pulse.

```
t = linspace(0,0.3,300)';
testsig = zeros(size(t));
testsig(201:205) = 1;
```

Assume the rectangular pulse is incident on the ULA from an angle of $30^{\circ}$ azimuth and $0^{\circ}$ elevation. Use the collectPlaneWave function of the ULA System object to simulate reception of the pulse waveform from the incident angle.

```
angle of arrival = [30;0];
x = collectPlaneWave(array,testsig,angle_of_arrival,fc);
```

The signal $x$ is a matrix with ten columns. Each column represents the received signal at one of the array elements.

Construct a conventional phase-shift beamformer. Set the Weights0utputPort property to true to output the spatial filter weights.

```
convbeamformer = phased.PhaseShiftBeamformer('SensorArray',array,...
    'OperatingFrequency',1e9,'Direction',angle_of_arrival,...
    'Weights0utputPort',true);
```

Add complex-valued white Gaussian noise to the signal $x$. Set the default random number stream for reproducible results.

```
rng default
npower = 0.5;
x = x + sqrt(npower/2)*(randn(size(x)) + li*randn(size(x)));
```

Create a 10W interference source. Specify the barrage jammer to have an effective radiated power of 10 W . The interference signal from the barrage jammer is incident on the ULA from an angle of $120^{\circ}$ azimuth and $0^{\circ}$ elevation. Use the collectPlaneWave function of the ULA System object to simulate reception of the jammer signal.

```
jamsig = sqrt(10)*randn(300,1);
jammer_angle = [120;0];
jamsig = collectPlaneWave(array,jamsig,jammer_angle,fc);
```

Add complex-valued white Gaussian noise to simulate noise contributions not directly associated with the jamming signal. Again, set the default random number stream for reproducible results. This noise power is 0 dB below the jammer power. Beamform the signal using a conventional beamformer.

```
noisePwr = 1e-5;
rng(2008);
noise = sqrt(noisePwr/2)*...
    (randn(size(jamsig)) + 1j*randn(size(jamsig)));
jamsig = jamsig + noise;
rxsig = x + jamsig;
[yout,w] = convbeamformer(rxsig);
```

Implement the adaptive LCMV beamformer using the same ULA array. Use the target-free data, jamsig, as training data. Output the beamformed signal and the beamformer weights.

```
steeringvector = phased.SteeringVector('SensorArray',array,...
    'PropagationSpeed',physconst('LightSpeed'));
LCMVbeamformer = phased.LCMVBeamformer('DesiredResponse',1,...
    'TrainingInputPort',true,'WeightsOutputPort',true);
```

```
LCMVbeamformer.Constraint = steeringvector(fc,angle_of_arrival);
LCMVbeamformer.DesiredResponse = 1;
[yLCMV,wLCMV] = LCMVbeamformer(rxsig,jamsig);
```

Plot the conventional beamformer output and the adaptive beamformer output.

```
subplot(211)
plot(t,abs(yout))
axis tight
title('Conventional Beamformer')
ylabel('Magnitude')
subplot(212)
plot(t,abs(yLCMV))
axis tight
title('LCMV (Adaptive) Beamformer')
xlabel('Seconds')
ylabel('Magnitude')
```



The adaptive beamformer significantly improves the SNR of the rectangular pulse at 0.2 s . Using conventional and LCMV weights, plot the responses for each beamformer.

```
subplot(211)
pattern(array,fc,[-180:180],0,'PropagationSpeed',physconst('LightSpeed'),...
    'CoordinateSystem','rectangular','Type','powerdb','Normalize',true,...
    'Weights',w)
title('Array Response with Conventional Beamforming Weights');
subplot(212)
```

```
pattern(array,fc,[-180:180],0,'PropagationSpeed',physconst('LightSpeed'),...)
    'CoordinateSystem','rectangular','Type','powerdb','Normalize',true,...
    'Weights',wLCMV)
title('Array Response with LCMV Beamforming Weights');
```



Array Response with LCMV Beamforming Weights


The adaptive beamform places a null at the arrival angle of the interference signal, $120^{\circ}$.

## Algorithms

## Data Precision

This System object supports single and double precision for input data, properties, and arguments. If the input data X is single precision, the output data is single precision. If the input data X is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

## Version History

## Introduced in R2011a

## References

[1] Van Trees, H. Optimum Array Processing. New York: Wiley-Interscience, 2002.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
See "System Objects in MATLAB Code Generation" (MATLAB Coder).
This System object supports single and double precision for input data, properties, and arguments. If the input data X is single precision, the output data is single precision. If the input data X is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

## See Also

phased.MVDRBeamformer | phased.PhaseShiftBeamformer |
phased.TimeDelayLCMVBeamformer
Topics
"Adaptive Beamforming"

## step

System object: phased. LCMVBeamformer
Package: phased
Perform LCMV beamforming

## Syntax

Y = step (H, X)
Y $=\operatorname{step}(\mathrm{H}, \mathrm{X}, \mathrm{XT})$
[Y,W] = step( $\qquad$ )

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.
$\mathrm{Y}=\operatorname{step}(\mathrm{H}, \mathrm{X})$ performs LCMV beamforming on the input, X , and returns the beamformed output in Y . X is an M -by- N matrix where N is the number of elements of the sensor array. Y is a column vector of length M .

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
$\mathrm{Y}=$ step $(\mathrm{H}, \mathrm{X}, \mathrm{XT})$ uses XT as the training samples to calculate the beamforming weights. This syntax is available when you set the TrainingInputPort property to true. XT is a P-by-N matrix, where N is the number of elements of the sensor array. P must be greater than N .

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
$[\mathrm{Y}, \mathrm{W}]=\operatorname{step}(\ldots \quad$ ) returns the beamforming weights W . This syntax is available when you set the WeightsOutputPort property to true. W is a column vector of length N , where N is the number of elements in the sensor array.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Examples

## LCMV Beamformer with One Constraint

Apply an LCMV beamformer to a 5-element ULA of isotropic sensor elements, preserving the signal from a desired direction. The operating frequency is 300 MHz .

Simulate a low-frequency sinusoid signal in Gaussian noise.
f = 50;
t = (0:.001:.3)';
$\mathrm{x}=\sin (2 * \mathrm{pi} * \mathrm{f} * \mathrm{t})$;
c = physconst('LightSpeed');
fc = 300e6;
lambda = c/fc;
incidentAngle = [45;0];
antenna = phased.IsotropicAntennaElement('FrequencyRange',[20 20e8]);
array $=$ phased.ULA('NumElements',5,'ElementSpacing',lambda/2,...
'Element', antenna);
$x=$ collectPlaneWave(array, $x$, incidentAngle, $\mathrm{fc}, \mathrm{c}$ );
noise $=0.2^{*}(\operatorname{randn}(\operatorname{size}(x))+1 j * \operatorname{randn}(\operatorname{size}(x)))$;
rx = x + noise;
Beamform the array.

```
steervec = phased.SteeringVector('SensorArray',array,...
    'PropagationSpeed',c);
beamformer = phased.LCMVBeamformer('Constraint',steervec(fc,incidentAngle),'DesiredResponse',1);
y = beamformer(rx);
```

Plot the original and beamformed signals.

```
plot(t,real(rx(:,3)),'r:',t,real(y),t,real(x(:,3)),'g')
xlabel('Time (sec)')
ylabel('Amplitude')
legend('Signal at Sensor 3','Beamformed Signal','Noise Free Signal')
```



# phased.LinearFMWaveform 

Package: phased
Linear FM pulse waveform

## Description

The LinearFMWaveform System object creates a linear FM pulse waveform.
To create the waveform:
1 Create the phased.LinearFMWaveform object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

waveform = phased.LinearFMWaveform
waveform = phased.LinearFMWaveform(Name=Value)

## Description

waveform = phased.LinearFMWaveform creates a linear FM pulse waveform System object. Use this object to generate samples of a linear FM pulse waveform.
waveform = phased.LinearFMWaveform(Name=Value) creates a linear FM pulse waveform System object with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Name1=Value1,...,NameN=ValueN).

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## SampleRate - Signal sample rate

1e6 (default) | positive scalar
Signal sample rate, specified as a positive scalar. The ratio of sample rate to pulse repetition frequency must be a positive integer, so the number of samples in each pulse must be an integer value. Units are in Hertz.

## Example: 100e3

## Data Types: double

## DurationSpecification - Method to set pulse duration <br> 'Pulse width' (default)|'Duty cycle'

Method to set pulse duration (pulse width), specified as 'Pulse width' or 'Duty cycle'. This property determines how you set the pulse duration.

- When you set this property to 'Pulse width', set the pulse duration directly using the PulseWidth property.
- When you set this property to 'Duty cycle', set the pulse duration from the values of the PRF and DutyCycle properties. The pulse width is equal to the value of the DutyCycle property divided by the value of the PRF property.

Data Types: char | string

## PulseWidth - Pulse time duration

50e-6 (default) | positive scalar
Pulse time duration, specified as a positive scalar. The value must satisfy PulseWidth <= 1./PRF. Units are in seconds.

## Dependencies

To enable this property, set the DurationSpecification property to 'Pulse width'.
Data Types: double

## DutyCycle - Pulse duty cycle

0.5 (default) | positive scalar in the range [0,1]

Pulse duty cycle, specified as a positive scalar in the range $[0,1]$. The pulse width is the value of the DutyCycle property divided by the value of the PRF property. This quantity is dimensionless.
Example: 0.75

## Dependencies

To enable this property, set the DurationSpecification property to 'Duty cycle'.
Data Types: double

## PRF - Pulse repetition frequency

10e3 (default) | positive scalar | row vector of positive values
Pulse repetition frequency (PRF), specified as a scalar or a row vector. Units are in Hz . The pulse repetition interval (PRI) is the inverse of the pulse repetition frequency PRF value. The PRF must satisfy these restrictions:

- The product of PRF and PulseWidth must be less than or equal to one. This condition requires that the pulse width is less than one PRI. For the phase-coded waveform, the pulse width is the product of the values of the ChipWidth and NumChips properties.
- The ratio of SampleRate to PRF must be an integer. This condition requires that the number of samples in one PRI is an integer.

You can set the value of PRF using the PRF property settings alone or using property settings in conjunction with the prfidx input argument of the object.

- When PRFSelectionInputPort is false, you set the PRF using the PRF properties alone. You can:
- Implement a constant PRF by specifying the PRF property as a positive real-valued scalar.
- Implement a staggered PRF by specifying the PRF property as a row vector with positive realvalued elements. Each call to the object uses successive elements of this vector as the PRF. Once the object reaches the last element of the vector, it continues the process cyclically with the first element of the vector.
- When PRFSelectionInputPort is true, you can set the PRF value using the PRF property in conjunction with the prfidx input argument. You implement a selectable PRF by specifying the PRF property as a row vector with positive real-valued elements. When you execute the object, the object selects a PRF by using the index you specify in the prfidx input argument to index into the PRF vector.

In all cases, the number of output samples is fixed when you set the OutputFormat property to 'Samples'. When you use a varying PRF and also set the OutputFormat property to 'Pulses ', the number of samples can vary.
Data Types: double

## PRFSelectionInputPort - Enable PRF selection input

false (default) |true
Enable PRF selection input, specified as false or true. When you set this property to true, you can pass an index argument to the object to select a predefined value from the PRF property vector. When you set this property to false, the object uses the PRF property to define the PRF sequence used in the simulation.

Data Types: logical

## SweepBandwidth - Bandwidth of linear FM sweep

100e3 (default) | positive scalar
Bandwidth of linear FM sweep, specified as a positive scalar. Units are in Hz .

## Data Types: double

## SweepDirection - Direction of linear FM sweep

'Up' (default) | 'Down'
Direction of the linear FM sweep, specified as 'Up' or 'Down '.
Data Types: char \| string

## SweepInterval - Location of FM sweep interval

'Positive' (default)|'Symmetric'
Location of the FM sweep interval, specified as'Positive' or 'Symmetric'.

- If SweepInterval is 'Positive', the waveform sweeps the interval between 0 and $B$ where $B$ is the sweep bandwidth in the SweepBandwidth property.
- If SweepInterval is 'Symmetric', the waveform sweeps the interval between $-B / 2$ and $B / 2$.


## Data Types: char | string

## Envelope - Waveform envelope function

'Rectangular' (default)| 'Gaussian'
Waveform envelope function, specified as 'Rectangular' or 'Gaussian'.
Data Types: char | string
FrequencyOffsetSource - Source of frequency offset
'Property' (default)|'Input port'
Source of frequency offset, specified as 'Property' or 'Input port'.

- When you set this property to 'Property', the frequency offset is determined by the value of the FrequencyOffset property.
- When you set this property to 'Input port', the frequency offset is determined by the input argument freqoffset when calling the object.

Example: 'Input port'
Data Types: char | string

## FrequencyOffset - Frequency offset

0 (default) | scalar
Frequency offset, specified as a scalar. Units are in Hz.
Example: 150.0

## Dependencies

To enable this property, set the FrequencyOffsetSource property to 'Property '.
Data Types: double

## OutputFormat - Format of output signal

'Pulses' (default)|'Samples'
Format of output signal, specified as 'Pulses' or 'Samples'.

- When you set the OutputFormat property to 'Pulses ', the output of the object takes the form of multiple pulses specified by the value of the NumPulses property. The number of samples per pulse can vary if you change the PRF during the simulation.
- When you set the OutputFormat property to 'Samples ', the output of the object takes the form of multiple samples. In this case, the number of output signal samples is the value of the NumSamples property and is fixed.

Data Types: char | string

## NumSamples - Number of samples in output

100 (default) | positive integer
Number of samples in each output of the object, specified as a positive integer.

## Dependencies

To enable this property, set the OutputFormat property to 'Samples '.

Data Types: double

## NumPulses - Number of pulses in output

1 (default) | positive integer
Number of pulses in each output, specified as a positive integer.

## Dependencies

To enable this property, set the OutputFormat property to 'Pulses '.
Data Types: double
PRFOutputPort - Enable PRF output
false (default) | true
Enable PRF output, specified as false or true. Set this property to true to output the PRF.

## Dependencies

To enable this property, set the OutputFormat property to 'Pulses '.

## Data Types: logical

## CoefficientsOutputPort - Enable matched filter coefficients output false (default) | true

Enable matched filter coefficients output, specified as false or true. Set this property to true to enable the object the output of the matched filter coefficients of the waveform used during the simulation.
Data Types: logical

## Usage

## Syntax

Y = waveform()
$Y=$ waveform(prfidx)
$Y=$ waveform(freqoffset)
[Y,PRF] = waveform( $\qquad$
[Y,coeff] = waveform( $\qquad$ )

## Description

$Y=$ waveform() returns samples of the linear FM pulse in a column vector $Y$. $Y$ can contain either a certain number of pulses or a certain number of samples.
$Y=$ waveform(prfidx), specifies the index prfidx of the pulse repetition frequency (PRF). The index identifies selected entries in the PRF property. This syntax applies when you set the PRFSelectionInputPort property to true.

Use this syntax for the cases where the transmitted pulse needs to be dynamically selected. In such situations, the PRF property includes a list of predetermined choices of PRF's. Based on prfidx value input, one of the PRF's is selected as the PRF for the next transmission.

Note that the transmission always finishes the current pulse before starting the next pulse. Therefore, when you set the OutputFormat property to 'Samples' and then specify the NumSamples property to be shorter than a pulse, it is possible that during a given simulation step, if the entire output is needed to finish the previously transmitted pulse, the specified prfidx is ignored.

Y = waveform(freqoffset) generates a waveform with a frequency offset freqoffset. Use this syntax for cases where the transmit pulse frequency needs to be dynamically updated.

This syntax applies when you set the FrequencyOffsetSource property to 'Input port'.
[Y,PRF] = waveform( __ ) also returns the current pulse repetition frequency PRF. To enable this syntax, set the PRFOutputPort property to true and set the OutputFormat property to 'Pulses'.
[Y, coeff] = waveform (__ ) also returns the matched filter coefficients, coeff, for the current pulse. To enable this syntax, set the CoefficientsOutputPort property to true.

You can combine optional input and output arguments when their enabling properties are set. Optional inputs and outputs must be listed in the same order as the order of the enabling properties. For example,

```
[Y,PRF,coeff] = waveform(prfidx,freqoffset)
```

Input Arguments

## prfidx - index of pulse repetition frequency

positive integer
Index of pulse frequency, specified as a positive integer. The index identifies the entries in the PRF.

## Dependencies

To enable this argument, set the PRFSelectionInputPort property to true

## freqoffset - frequency offset

0 (default) | scalar
Frequency offset, specified as a scalar. The offset generates the waveform with a frequency offset. Use this argument for the cases where the transmit pulse frequency needs to be dynamically updated. Units are in Hz .

## Dependencies

To enable this argument, set the FrequencyOffsetSource property to 'Input port'.

## Data Types: double

## Output Arguments

## PRF - pulse repetition frequency

scalar
Pulse repetition frequency, returned as a scalar.

## Dependencies

To enable this argument, set the PRFOutputPort property to true and set the OutputFormat to 'Pulses'. When you set the PRF0utputPort property to true, the function returns the current PRF used by the system.

## coeff - matched filter coefficients

$N_{Z}$-by-1 complex-valued vector $\mid N_{Z}$-by- $M$ complex-valued matrix
Matched filter coefficients, returned as an $N_{Z}$-by- 1 complex-valued vector or an $N_{Z}$-by- $M$ complexvalued matrix.

- If you set OutputFormat to 'Pulses' and NumPulses is 1 , the object returns coeff as an $N_{Z^{-}}$ length vector. $N_{Z}$ corresponds to the pulse width.
- If you set OutputFormat to 'Pulses' with NumPulses greater than 1 or OutputFormat is 'Samples' and DurationSpecification is 'Pulse width', coeff is returned as an $N_{Z^{-}}$ length vector. $N_{Z}$ corresponds to the pulse width.
- If OutputFormat is set to 'Pulses' with NumPulses greater than 1 or OutputFormat is set to 'Samples' and DurationSpecification is set to 'Duty cycle' with only one unique PRF value, coeff is returned as an $N_{Z}$-length vector. $N_{Z}$ corresponds to the pulse width.
- If OutputFormat is 'Pulses' with NumPulses greater than 1 or OutputFormat is 'Samples' and DurationSpecification is 'Duty cycle', coeff is returned as an $N_{Z}$-by- $M$ matrix. $N_{Z}$ corresponds to the maximum pulse width and $M$ corresponds to the number of unique PRFs.


## Dependencies

To enable this argument, set the Coefficients0utputPort property to true.

## Data Types: double

Complex Number Support: Yes

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```


## Specific to waveform System objects

bandwidth Waveform bandwidth<br>getMatchedFilter Matched filter coefficients derived from waveform<br>getStretchProcessor Create stretch processor for waveform<br>plot<br>Plot pulse waveform

## Common to All System Objects

| step | Run System object algorithm |
| :--- | :--- |
| release | Release resources and allow changes to System object property values and input <br> characteristics |
| reset | Reset internal states of System object |

## Examples

## Create Linear FM Pulses

Construct a linear FM waveform having a sweep bandwidth of 300 kHz , a sample rate of 1 MHz , a pulse width of 50 microseconds, and a pulse repetition frequency of 10 kHz . Generate two pulses.

```
sLFM = phased.LinearFMWaveform('SweepBandwidth',3e5,...
    'OutputFormat','Pulses','SampleRate',1e6,...
    'PulseWidth',50e-6,'PRF',10e3,'NumPulses',2);
```

Obtain and plot the linear FM waveform.

```
wav = step(sLFM);
numpulses = size(wav,1);
t = [0:(numpulses-1)]/sLFM.SampleRate;
plot(t*le6,real(wav))
xlabel('Time (\mu sec)')
ylabel('Amplitude')
```



## Create Linear FM Pulses with Variable PRF

Construct six linear FM waveform pulses having a sweep bandwidth of 300 kHz , a sample rate of 1 MHz , a pulse width of 50 microseconds, and a duty cycle of $20 \%$. Vary the pulse repetition frequency.

Set the sample rate and PRF. The ratio of sample rate to PRF must be an integer.

```
fs = 1e6;
PRF = [10000,25000];
sLFM = phased.LinearFMWaveform('SweepBandwidth',3e5,...
    'OutputFormat','Pulses','SampleRate',fs,...
    'DurationSpecification','Duty Cycle','DutyCycle',.2,...
    'PRF',PRF,'NumPulses',1,'PRFSelectionInputPort',true);
```

Obtain and plot the linear FM waveforms. For the first three calls to the step method, set the PRF to 10 kHz using the PRF index. For the next three calls, set the PRF to 25 kHz .

```
wav = [];
for n = 1:6
    idx = floor((n-1)/3)+1;
    wav1 = step(sLFM,idx);
    wav = [wav;wav1];
end
nsamps = size(wav,1);
t = [0:(nsamps-1)]/sLFM.SampleRate;
plot(t*le6,real(wav))
xlabel('Time (\mu sec)')
ylabel('Amplitude')
```



## Plot LFM Waveform and Spectrum

Create and plot an upsweep linear FM pulse waveform. The sample rate is 500 kHz , the sweep bandwidth is 200 kHz and the pulse width is 1 millisecond (equal to the pulse repetition interval).

```
fs = 500e3;
sLFM = phased.LinearFMWaveform('SampleRate',fs,...
    'SweepBandwidth',200e3,...
    'PulseWidth',1e-3,'PRF',1e3);
```

Obtain and then plot the real part of the LFM waveform.

```
lfmwav = step(sLFM);
nsamp = size(lfmwav,1);
t = [0:(nsamp-1)]/fs;
plot(t*1000,real(lfmwav))
xlabel('Time (millisec)')
ylabel('Amplitude')
grid
```



Plot the Fourier transform of the complex signal.

```
nfft = 2^nextpow2(nsamp);
Z = fft(lfmwav,nfft);
fr = [0:(nfft/2-1)]/nfft*fs;
plot(fr/1000,abs(Z(1:nfft/2)),'.-')
xlabel('Frequency (kHz)')
```

ylabel('Amplitude')
grid


Plot a spectrogram of the function with window size of 64 samples and $50 \%$ overlap.
nfftl = 64;
nov = floor(0.5*nfft1);
spectrogram(lfmwav, hamming(nfft1), nov, nfft1,fs,'centered', 'yaxis')


This plot shows the increasing frequency of the signal.

## Apply Frequency Offset to Linear FM Waveform

Apply a frequency offset to an upsweep linear FM (LFM) pulse waveform. Plot the frequency spectrum of the waveform with and without applying a frequency offset.

Create an LFM waveform object, which is configured to set the frequency offset from an input when the object is executed.

```
fs = 500e3;
sLFM = phased.LinearFMWaveform('SampleRate',fs,'SweepBandwidth',200e3, ...
    'PulseWidth',2e-5,'PRF',1e3,'Frequency0ffsetSource','Input port');
```

Execute the object two times. First set the frequency offset to 0 Hz and then to 2 e 4 Hz .

```
lfmwav = sLFM(0);
lfmwav_foffset = sLFM(2e4);
```

Plot the frequency spectrum of the complex signals. The frequency offset signal is shifted to the right.

```
[Pxx,f] = pwelch(lfmwav,[],[],[],fs,'centered');
[Pxx_offset,foffset] = pwelch(lfmwav_foffset,[],[],[],fs,'centered');
plot(f/1000,Pxx,foffset/1000,Pxx_offset)
ylabel('PSD');
```

xlabel('Frequency (kHz)');
legend(\{'No offset','Offset applied'\},'Location','northwest'); grid on;


## Generate Matched Filter Coefficients of Linear FM Pulse Waveform

Generate output samples and matched filter coefficients of a linear FM pulse waveform at a 50 kHz frequency offset.

```
waveform = phased.LinearFMWaveform('SweepBandwidth',1e5, ...
    'PulseWidth',5e-5,'0utputFormat','Pulses', ...
    'Frequency0ffset',5e4,'Coefficients0utputPort',true);
```

[wav,coeff] = waveform();

Create a matched filter that applies the coefficients as an input argument. Use the coefficients when applying the matched filter to the waveform. Plot the waveform and matched filter outputs.

```
mf = phased.MatchedFilter('CoefficientsSource','Input port');
mfOut = mf(wav,coeff);
subplot(211),plot(real(wav));
xlabel('Samples'),ylabel('Amplitude'),title('Waveform Output');
subplot(212),plot(abs(mf0ut));
xlabel('Samples'),ylabel('Amplitude'),title('Matched Filter Output');
```



## Compute Linear FM Bandwidth

Determine the bandwidth of a linear FM pulse waveform. The default value for an LFM waveform is 100 kHz .
waveform = phased.LinearFMWaveform; bw = bandwidth(waveform)
$b w=100000$

## Version History <br> Introduced in R2011a

## References

[1] Levanon, N. and E. Mozeson. Radar Signals. Hoboken, NJ: John Wiley \& Sons, 2004.
[2] Richards, M. A. Fundamentals of Radar Signal Processing. New York: McGraw-Hill, 2005.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.
Usage notes and limitations:

- The plot method is not supported.
- See "System Objects in MATLAB Code Generation" (MATLAB Coder).


## See Also

phased.NonlinearFMWaveform | phased.CustomFMWaveform | phased.PhaseCodedWaveform | phased.RectangularWaveform | phased.SteppedFMWaveform

## Topics

"Waveform Analysis Using the Ambiguity Function"

## reset

System object: phased.LinearFMWaveform
Package: phased
Reset states of the linear FM waveform object

## Syntax

reset (H)

## Description

reset $(\mathrm{H})$ resets the states of the LinearFMWaveform object, H . Afterward, if the PRF property is a vector, the next call to step uses the first PRF value in the vector.

## step

System object: phased.LinearFMWaveform
Package: phased
Samples of linear FM pulse waveform

## Syntax

Y = step(sLFM)
Y = step(sLFM, prfidx)
Y = step(sRFM,freqoffset)
[Y,PRF] = step (___)
[Y,COEFF] = step( $\qquad$ )

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, $y=$ step (obj, x) and $y=o b j(x)$ perform equivalent operations. When the only argument to the step method is the System object itself, replace $y=\operatorname{step}(o b j)$ by $y=o b j()$.
$\mathrm{Y}=$ step(sLFM) returns samples of the linear FM pulse in a column vector Y .
$Y=$ step(sLFM, prfidx), uses the prfidx index to select the PRF from the predefined vector of values specified by in the PRF property. This syntax applies when you set the PRFSelectionInputPort property to true.
$Y=s t e p(s R F M, f r e q o f f s e t)$, uses the freqoffset to generate the waveform with an offset as specified at step time. Use this syntax for cases where the transmit pulse frequency needs to be dynamically updated. This syntax applies when you set the FrequencyOffsetSource property to 'Input port'.
[Y,PRF] = step( ) also returns the current pulse repetition frequency, PRF. To enable this syntax, set the PRFOutputPort property to true and set the OutputFormat property to 'Pulses'.
$[Y$, COEFF $]=\operatorname{step}(\ldots \quad$ ) returns the matched filter coefficients, COEFF, for the current pulse. To enable this syntax, set the CoefficientsOutputPort property to true. COEFF is returned as either an $N_{Z}$-by- 1 vector or an $N_{Z}$-by-M matrix.

- An $N_{Z}$-by-1 vector is returned when:
- The object has OutputFormat set to 'Pulses' and NumPulses is equal to $1 . N_{\mathrm{Z}}$ is the pulse width.
- The object is configured to generate constant pulse width waveforms
(DurationSpecification is set to 'Pulse width' or 'Duty cycle' and PRF has one unique value); and either OutputFormat is set to 'Pulses' and NumPulses is greater than 1, or the OutputFormat is set to 'Samples'. For this case, $N_{\mathrm{Z}}$ is the pulse width.
- An $N_{\mathrm{Z}}$-by-M matrix is returned when the object generates varying pulse widths (DurationSpecification property is set to 'Duty cycle' and PRF has more than one unique value); and either OutputFormat set to 'Pulses' and NumPulses is greater than 1, or OutputFormat is set to 'Samples '. For this case, $N_{\mathrm{Z}}$ is the maximum of the pulse widths, and $M$ is the number of unique PRFs.

You can combine optional input and output arguments when their enabling properties are set. Optional inputs and outputs must be listed in the same order as the order of the enabling properties. For example, [Y,PRF,COEFF] = step(sRFM, prfidx,freqoffset).

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Examples

## Create Linear FM Pulses

Construct a linear FM waveform having a sweep bandwidth of 300 kHz , a sample rate of 1 MHz , a pulse width of 50 microseconds, and a pulse repetition frequency of 10 kHz . Generate two pulses.

```
sLFM = phased.LinearFMWaveform('SweepBandwidth',3e5,...
    'OutputFormat','Pulses','SampleRate',1e6,...
    'PulseWidth',50e-6,'PRF',10e3,'NumPulses',2);
```

Obtain and plot the linear FM waveform.

```
wav = step(sLFM);
numpulses = size(wav,1);
t = [0:(numpulses-1)]/sLFM.SampleRate;
plot(t*le6,real(wav))
xlabel('Time (\mu sec)')
ylabel('Amplitude')
```



## Create Linear FM Pulses with Variable PRF

Construct six linear FM waveform pulses having a sweep bandwidth of 300 kHz , a sample rate of 1 MHz , a pulse width of 50 microseconds, and a duty cycle of $20 \%$. Vary the pulse repetition frequency.

Set the sample rate and PRF. The ratio of sample rate to PRF must be an integer.

```
fs = 1e6;
PRF = [10000,25000];
sLFM = phased.LinearFMWaveform('SweepBandwidth',3e5,...
    'OutputFormat','Pulses','SampleRate',fs,...
    'DurationSpecification','Duty Cycle','DutyCycle',.2,...
    'PRF',PRF,'NumPulses',1,'PRFSelectionInputPort',true);
```

Obtain and plot the linear FM waveforms. For the first three calls to the step method, set the PRF to 10 kHz using the PRF index. For the next three calls, set the PRF to 25 kHz .

```
wav = [];
for n = 1:6
    idx = floor((n-1)/3)+1;
    wav1 = step(sLFM,idx);
    wav = [wav;wav1];
end
nsamps = size(wav,1);
t = [0:(nsamps-1)]/sLFM.SampleRate;
```

plot(t*le6, real(wav))
xlabel('Time (\mu sec)')
ylabel('Amplitude')


## Generate Matched Filter Coefficients of Linear FM Pulse Waveform

Generate output samples and matched filter coefficients of a linear FM pulse waveform at a 50 kHz frequency offset.

```
waveform = phased.LinearFMWaveform('SweepBandwidth',1e5, ...
    'PulseWidth',5e-5,'OutputFormat','Pulses', ...
    'Frequency0ffset',5e4,'Coefficients0utputPort',true);
```

[wav,coeff] = waveform();

Create a matched filter that applies the coefficients as an input argument. Use the coefficients when applying the matched filter to the waveform. Plot the waveform and matched filter outputs.

```
mf = phased.MatchedFilter('CoefficientsSource','Input port');
mfOut = mf(wav,coeff);
subplot(211),plot(real(wav));
xlabel('Samples'),ylabel('Amplitude'),title('Waveform Output');
subplot(212),plot(abs(mf0ut));
xlabel('Samples'),ylabel('Amplitude'),title('Matched Filter Output');
```



# phased.NonlinearFMWaveform 

Package: phased
Nonlinear FM pulse waveform

## Description

The phased.NonlinearFMWaveform System object creates a frequency-modulated waveform whose frequency is a nonlinear function of time (NLFM). NLFM waveforms achieve low-range sidelobes by shaping the spectrum using frequency modulation. Four different waveforms are supported depending on the FrequencyModulation property:

- 'Polynomial ' - Generate a waveform with an instantaneous frequency that follows a polynomial function.
- 'Hyperbolic' - Generate a hyperbolic frequency modulated (HFM) waveform.
- 'Hybrid Linear-Tangent' - Generate a hybrid NLFM waveform that combines an LFM waveform with tan-FM waveform.
- 'Stepped Price' - Generate a stepped version of Price's NLFM waveform.

To create the waveforms:
1 Create the phased.NonlinearFMWaveform object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

```
waveform = phased.NonlinearFMWaveform
waveform = phased.NonlinearFMWaveform(Name = Value)
```


## Description

waveform = phased. NonlinearFMWaveform creates a nonlinear FM pulse waveform System object. By default, the waveform has a polynomial frequency modulation.
waveform = phased.NonlinearFMWaveform(Name = Value) creates a nonlinear FM pulse waveform System object with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Namel = Value1,...,NameN = ValueN).

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.

For more information on changing property values, see System Design in MATLAB Using System Objects.

## SampleRate - Signal sample rate

1e6 (default) | positive scalar
Signal sample rate, specified as a positive scalar. The ratio of sample rate to pulse repetition frequency must be a positive integer, so the number of samples in each pulse must be an integer value. Units are in Hertz.

Example: 100e3
Data Types: double

## DurationSpecification - Method to set pulse duration <br> 'Pulse width' (default)|'Duty cycle'

Method to set pulse duration (pulse width), specified as 'Pulse width' or 'Duty cycle'. This property determines how you set the pulse duration.

- When you set this property to 'Pulse width', set the pulse duration directly using the PulseWidth property.
- When you set this property to 'Duty cycle', set the pulse duration from the values of the PRF and DutyCycle properties. The pulse width is equal to the value of the DutyCycle property divided by the value of the PRF property.

Data Types: char|string

## PulseWidth - Pulse time duration

50e-6 (default) | positive scalar
Pulse time duration, specified as a positive scalar. The value must satisfy PulseWidth <= 1./PRF. Units are in seconds.

## Dependencies

To enable this property, set the DurationSpecification property to 'Pulse width'.

## Data Types: double

## DutyCycle - Pulse duty cycle

0.5 (default) | positive scalar in the range $[0,1]$

Pulse duty cycle, specified as a positive scalar in the range $[0,1]$. The pulse width is the value of the DutyCycle property divided by the value of the PRF property. This quantity is dimensionless.

## Example: 0.75

## Dependencies

To enable this property, set the DurationSpecification property to 'Duty cycle'.
Data Types: double

## PRF - Pulse repetition frequency

10e3 (default) | positive scalar | row vector of positive values

Pulse repetition frequency (PRF), specified as a scalar or a row vector. Units are in Hz. The pulse repetition interval (PRI) is the inverse of the pulse repetition frequency PRF value. The PRF must satisfy these restrictions:

- The product of PRF and PulseWidth must be less than or equal to one. This condition requires that the pulse width is less than one PRI. For the phase-coded waveform, the pulse width is the product of the values of the ChipWidth and NumChips properties.
- The ratio of SampleRate to PRF must be an integer. This condition requires that the number of samples in one PRI is an integer.

You can set the value of PRF using the PRF property settings alone or using property settings in conjunction with the prfidx input argument of the object.

- When PRFSelectionInputPort is false, you set the PRF using the PRF properties alone. You can:
- Implement a constant PRF by specifying the PRF property as a positive real-valued scalar.
- Implement a staggered PRF by specifying the PRF property as a row vector with positive realvalued elements. Each call to the object uses successive elements of this vector as the PRF. Once the object reaches the last element of the vector, it continues the process cyclically with the first element of the vector.
- When PRFSelectionInputPort is true, you can set the PRF value using the PRF property in conjunction with the prfidx input argument. You implement a selectable PRF by specifying the PRF property as a row vector with positive real-valued elements. When you execute the object, the object selects a PRF by using the index you specify in the prfidx input argument to index into the PRF vector.

In all cases, the number of output samples is fixed when you set the OutputFormat property to 'Samples'. When you use a varying PRF and also set the OutputFormat property to 'Pulses ', the number of samples can vary.
Data Types: double

## PRFSelectionInputPort - Enable PRF selection input

false (default) |true
Enable PRF selection input, specified as false or true. When you set this property to true, you can pass an index argument to the object to select a predefined value from the PRF property vector. When you set this property to false, the object uses the PRF property to define the PRF sequence used in the simulation.
Data Types: logical

## FrequencyModulation - Frequency modulation

'Polynomial' (default)|'Hyperbolic'|'Hybrid Linear-Tangent'|'Stepped Price'
Frequency modulation of the nonlinear FM waveform, specified as 'Polynomial', 'Hyperbolic', 'Hybrid Linear-Tangent', or 'Stepped Price'.

- When you set the property to 'Polynomial ' the System object generates a waveform with an instantaneous frequency that follows a polynomial function. You specify the coefficients in the PolynomialCoefficients property. The object normalizes the resulting frequency function such that each pulse sweeps the bandwidth you specify in SweepBandwidth. The SweepDirection property is inactive when FrequencyModulation is set to 'Polynomial' ''.
- When you set the property to 'Hyperbolic' the System object generates a hyperbolic frequency modulated (HFM) waveform. Use the HyperbolicStartFrequency property to set the start frequency of the hyperbolic sweep. The SweepInterval property is inactive in this case.
- When you set the property to 'Hybrid Linear-Tangent' System object generates a hybrid NLFM waveform that combines an LFM with a tan-FM as described by Collins and Atkins [1]. You specify the balance between LFM and tan-FM in the LinearTangentBalance property, and the portion of the $\tan (\mathrm{x})$ curve to used for tan-FM in the TangentCurvePortion property.
- When you set the property to 'Stepped Price' the System object generates a stepped version of the Price's NLFM waveform as given by Levanon and Mozeson [2]. The SweepBandwidth property is inactive in this case and the sweep bandwidth is determined by the bandwidth factors in the BandwidthFactors property and the number of frequency steps in the NumSteps property.

Example: 'Stepped Price'
Data Types: char \| string
PolynomialCoefficients - Coefficients of polynomial frequency function
[1 0 0] (default) | $(N+1)$-length real-valued vector
Coefficients of the polynomial frequency function, specified as a length- $(N+1)$ real-valued vector. The vector represents the coefficients of an $N$-th degree polynomial. The first entry in PolynomialCoefficients is the coefficient of the highest power $N$ of the polynomial. The last entry is the coefficient of the power zero term of the polynomial.
Example: [0.5,1,1,0.5]

## Dependencies

To enable this property, set the FrequencyModulation property to 'Polynomial ' .
Data Types: double

## LinearTangentBalance - Balance factor between linear FM and tan-FM functions

0.5 (default) | positive scalar

Balance factor between linear FM and tan-FM functions for a hybrid linear-tangent NLFM waveform, specified as a scalar. Units are dimensionless.

## Example: 0.66

## Dependencies

To enable this property, set the FrequencyModulation property to 'Hybrid Linear-Tangent '.

## Data Types: double

## TangentCurvePortion - Portion of $\tan (x)$ curve

## 1.4 (default) | real-valued scalar

Portion of the $\tan (\mathrm{x})$ curve between $-\pi / 2$ and $+\pi / 2$ to use as a tangent term in the hybrid lineartangent FM frequency function, specified as a scalar between 0 and $+\Pi / 2$.

## Example: 1.2

## Dependencies

To enable this property, set the FrequencyModulation property to 'Hybrid Linear-Tangent'.

## Data Types: double

## NumSteps - Number of frequency steps

50 (default) | positive integer
Number of frequency steps for the stepped form of Price's NLFM, specified as a positive integer.
Example: 10

## Dependencies

To enable this property, set the FrequencyModulation property to 'Stepped Price'.
Data Types: double

## BandwidthFactors - Bandwidth factors

[1e4 2e4] (default)| 2 -element positive-valued vector
Bandwidth factors for the stepped form of Price's NLFM, specified as a two-element positive-valued vector of the form [BL BC]. BL determines the bandwidth of the linear component of the waveform and $B C$ determines the bandwidth of the nonlinear component. The total sweep bandwidth is equal to $(M-1) / M^{*}\left(B L+B C^{*} M / \operatorname{sqrt}\left(2^{*} M-1\right)\right)$, where $M$ is the value of the NumSteps property. As $M$, increases the bandwidth of the linear component approximately equals $B L$, while the bandwidth of the nonlinear component grows with $M$.

## Dependencies

To enable this property, set the FrequencyModulation property to 'Stepped Price'.

## Data Types: double

## HyperbolicStartFrequency - Start frequency of hyperbolic FM waveform 200e3 (default) | positive scalar

Start frequency of the hyperbolic frequency modulated waveform, specified as a positive scalar. Units are in Hz .

## Dependencies

To enable this property, set the FrequencyModulation property to 'Hyperbolic'.
Data Types: double

## SweepBandwidth - Bandwidth of nonlinear FM sweep

100e3 (default) | positive scalar
Bandwidth of nonlinear FM sweep, specified as a positive scalar. Units are in Hz.

## Data Types: double

## SweepDirection - Direction of nonlinear FM sweep

'Up' (default)|'Down'
Direction of the nonlinear FM sweep, specified as 'Up' or 'Down'.
Data Types: char | string

```
SweepInterval - Location of FM sweep interval 'Positive' (default)|'Symmetric'
```

Location of the FM sweep interval, specified as'Positive' or 'Symmetric'.

- If SweepInterval is 'Positive', the waveform sweeps the interval between 0 and $B$ where $B$ is the sweep bandwidth in the SweepBandwidth property.
- If SweepInterval is 'Symmetric', the waveform sweeps the interval between $-B / 2$ and $B / 2$.


## Data Types: char|string

## Envelope - Waveform envelope function

'Rectangular' (default)|'Gaussian'|'Hamming'|'Chebyshev'|'Hann'|'Kaiser' |
'Taylor'|'Custom'
Waveform envelope function, specified as 'Rectangular', 'Gaussian', 'Hamming', 'Chebyshev', 'Hann', 'Kaiser', 'Taylor', or 'Custom'.

When Envelope is set to 'Custom' use the CustomEnvelope property to specify a custom envelope.

Example: 'Taylor'
Data Types: char|string

## EnvelopeSidelobeLevel - Envelope window sidelobe level

30 (default) | positive scalar
Sidelobe level of a Kaiser, Chebyshev, or Taylor window used as the waveform envelope, specified as a positive scalar. Units are in dB.

## Dependencies

To enable this property, set the Envelope property to 'Kaiser', 'Chebyshev', or 'Taylor'.
Data Types: double

## CustomEnvelope - User-defined waveform envelope

@gausswin (default) | function handle | cell array
User-defined waveform envelope, specified as a function handle or cell array.

- If CustomEnvelope is a function handle, the specified function uses the window length as input and generates appropriate window coefficients.
- If CustomEnvelope is a cell array, then the first cell must be a function handle. The specified function takes the window length as the first input argument, with other additional input arguments if necessary, and generates appropriate window coefficients. The remaining entries in the cell array serve as additional input arguments to the function.

Example: \{@chebwin,512,100\}

## Dependencies

To enable this property, set the Envelope property to 'Custom ' .
Data Types: cell|function_handle

## FrequencyOffsetSource - Source of frequency offset

'Property' (default)|'Input port'
Source of frequency offset, specified as 'Property' or 'Input port'.

- When you set this property to 'Property', the frequency offset is determined by the value of the Frequency0ffset property.
- When you set this property to 'Input port', the frequency offset is determined by the input argument freqoffset when calling the object.

Example: 'Input port'
Data Types: char|string
Frequency0ffset - Frequency offset
0 (default) | scalar
Frequency offset, specified as a scalar. Units are in Hz.
Example: 150.0

## Dependencies

To enable this property, set the Frequency0ffsetSource property to 'Property '.
Data Types: double

## OutputFormat - Format of output signal

'Pulses' (default)| 'Samples'
Format of output signal, specified as 'Pulses ' or 'Samples '.

- When you set the OutputFormat property to 'Pulses', the output of the object takes the form of multiple pulses specified by the value of the NumPulses property. The number of samples per pulse can vary if you change the PRF during the simulation.
- When you set the OutputFormat property to 'Samples', the output of the object takes the form of multiple samples. In this case, the number of output signal samples is the value of the NumSamples property and is fixed.

Data Types: char|string

## NumSamples - Number of samples in output

100 (default) | positive integer
Number of samples in each output of the object, specified as a positive integer.

## Dependencies

To enable this property, set the OutputFormat property to 'Samples '.
Data Types: double

## NumPulses - Number of pulses in output

1 (default) | positive integer
Number of pulses in each output, specified as a positive integer.

## Dependencies

To enable this property, set the OutputFormat property to 'Pulses'.
Data Types: double

## PRFOutputPort - Enable PRF output

false (default) |true
Enable PRF output, specified as false or true. Set this property to true to output the PRF.

## Dependencies

To enable this property, set the OutputFormat property to 'Pulses '.
Data Types: logical
CoefficientsOutputPort - Enable matched filter coefficients output false (default) | true

Enable matched filter coefficients output, specified as false or true. Set this property to true to enable the object the output of the matched filter coefficients of the waveform used during the simulation.

Data Types: logical

## Usage

## Syntax

```
Y = waveform()
Y = waveform(prfidx)
Y = waveform(freqoffset)
[Y,PRF] = waveform(__)
[Y,coeff]= waveform()
```


## Description

$Y=$ waveform() returns samples of the nonlinear FM pulse in a column vector $Y$. $Y$ can contain either a certain number of pulses or a certain number of samples.
$Y=$ waveform(prfidx) specifies the index of the pulse repetition frequency (PRF), prfidx. The index identifies the entries specified in the PRF property. This syntax applies when you set the PRFSelectionInputPort property to true.

Use this syntax for the cases where the transmitted pulse needs to be dynamically selected. In such situations, the PRF property includes a list of predetermined choices of PRF's. During the simulation, using prfidx, one of the PRFs is selected as the PRF for the next transmission.

Note that the transmission always finishes the current pulse before starting the next pulse. Therefore, when you set the OutputFormat property to 'Samples' and then specify the NumSamples property to be shorter than a pulse, it is possible that during a given simulation step, if the entire output is needed to finish the previously transmitted pulse, the specified prfidx is ignored.
$Y=$ waveform(freqoffset) specifies the value of the frequency offset freqoffset as a finite real value. The offset is used to generate the waveform with a frequency offset. Use this syntax for the cases where the transmit pulse frequency needs to be dynamically updated. To enable this syntax set the FrequencyOffsetSource property to 'Input port'.
[Y,PRF] = waveform( $\qquad$ ) also returns the current pulse repetition frequency, PRF. To enable this syntax, set the PRFOutputPort property to true and set the OutputFormat property to 'Pulses'.
[Y, coeff]= waveform() returns an additional output coeff, as the matched filter coefficients. To use this syntax, set the Coefficients0utputPort property to true.

You can combine optional input and output arguments when their enabling properties are set. Optional inputs and outputs must be listed in the same order as the order of the enabling properties. For example,

```
[Y,PRF,coeff] = waveform(prfidx,freqoffset)
```

Input Arguments
prfidx - index of pulse repetition frequency
positive integer
Index of pulse repetition frequency, specified as a positive integer. The index identifies the entries in the PRF property. This syntax applies when you set the PRFSelectionInputPort property to true. Use this argument for the case when the transmit pulse needs to be dynamically selected. Under such situations, the PRF property includes a list of predetermined choices of PRFs. During the simulation, based on the PRF index input, one of the PRFs is selected as the PRF for the next transmission.

## freqoffset - frequency offset

0 (default) | scalar
Frequency offset, specified as a scalar. This argument generates the waveform with a frequency offset when the object is called. Use this syntax for the cases where the transmit pulse frequency needs to be dynamically updated.

## Dependencies

To use this argument, set the Frequency0ffsetSource property to 'Input port'.
Data Types: double

## Output Arguments

## PRF - pulse repetition frequency

scalar
Pulse repetition frequency, returned as a scalar. Returns the current PRF used by the object. Units are in Hz .

## Dependencies

To enable this argument, set the PRF0utputPort property to true and set the OutputFormat to
'Pulses'.
coeff - matched filter coefficients
$N_{Z}$-by-1 complex-valued vector $\mid N_{Z}$-by- $M$ complex-valued matrix
Matched filter coefficients, returned as an $N_{Z}$-by- 1 complex-valued vector or an $N_{Z}$-by- $M$ complexvalued matrix.

- If you set OutputFormat to 'Pulses' and NumPulses is 1 , the object returns coeff as an $N_{Z^{-}}$ length vector. $N_{Z}$ corresponds to the pulse width.
- If you set OutputFormat to 'Pulses ' with NumPulses greater than 1 or OutputFormat is 'Samples' and DurationSpecification is 'Pulse width', coeff is returned as an $N_{Z^{-}}$ length vector. $N_{Z}$ corresponds to the pulse width.
- If OutputFormat is set to 'Pulses' with NumPulses greater than 1 or OutputFormat is set to 'Samples' and DurationSpecification is set to 'Duty cycle' with only one unique PRF value, coeff is returned as an $N_{Z}$-length vector. $N_{Z}$ corresponds to the pulse width.
- If OutputFormat is 'Pulses' with NumPulses greater than 1 or OutputFormat is 'Samples' and DurationSpecification is 'Duty cycle', coeff is returned as an $N_{Z}$-by- $M$ matrix. $N_{Z}$ corresponds to the maximum pulse width and $M$ corresponds to the number of unique PRFs.


## Dependencies

To enable this argument, set the Coefficients0utputPort property to true.
Data Types: double
Complex Number Support: Yes

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```


## Specific to waveform System objects

bandwidth Waveform bandwidth
getMatchedFilter Matched filter coefficients derived from waveform
plot
Plot pulse waveform

## Common to All System Objects

step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object

## Examples

## Create Nonlinear FM Waveform with Default Properties

Create a nonlinear FM waveform with the default polynomial frequency modulation.

```
waveform = phased.NonlinearFMWaveform()
waveform =
    phased.NonlinearFMWaveform with properties:
                            SampleRate: 1000000
        DurationSpecification: 'Pulse width'
            PulseWidth: 5.0000e-05
```

PRF: 10000
PRFSelectionInputPort: false
FrequencyModulation: 'Polynomial'
PolynomialCoefficients: [1 0 0]
SweepBandwidth: 100000
SweepInterval: 'Positive'
Envelope: 'Rectangular'
Frequency0ffsetSource: 'Property'
Frequency0ffset: 0
OutputFormat: 'Pulses'
NumPulses: 1
PRFOutputPort: false
CoefficientsOutputPort: false

Display the real part of the waveform.
plot(waveform)


## Plot Quadratic FM Pulse Waveform

Create and plot a quadratic FM pulse waveform. The pulse has a 10 MHz bandwidth and $50 \mu \mathrm{sec}$ duration. The pulse sample rate is 10 times the bandwidth.

BW = 10e6;
$\mathrm{T}=50 \mathrm{e}-6$;
waveform = phased.NonlinearFMWaveform( ...
'SampleRate', 10*BW, 'SweepBandwidth',BW, ...
'PulseWidth', T) ;
plot(waveform,PlotType='complex')



## Create Hybrid Linear-Tangent FM Waveform

Generate samples of a hybrid linear-tangent FM waveform with a bandwidth of 2 kHz and a pulse width of 100 ms . Set the pulse repetition frequency to 5 Hz and the sample frequency to 20 kHz . Set the factor controlling the balance between the linear and the nonlinear terms to 0.5. Set the factor controlling the portion of the $\tan (\mathrm{x})$ curve used for frequency modulation to 1.4. Plot the autocorrelation function to determine the resulting range sidelobe level.

BW = 2000;
$\mathrm{T}=100 \mathrm{e}-3$;
PRF = 5;
$\mathrm{fs}=10 * \mathrm{BW}$;
Set the balance between tan-FM and LFM to 0.5 and set the portion of $\tan (x)$ to use to 1.4.

```
alpha = 0.5;
gamma = 1.4;
```

Create the waveform and plot the real and imaginary parts.
waveform = phased.NonlinearFMWaveform('SampleRate',fs,'PulseWidth', T, ...
'PRF', PRF,'FrequencyModulation','Hybrid Linear-Tangent', ...
'LinearTangentBalance', alpha,'TangentCurvePortion',gamma, ...
'SweepBandwidth', BW, 'OutputFormat','Pulses','NumPulses', 2);
wav = waveform();
figure
plot(waveform, PlotType='complex')



Compute and plot the autocorrelation function.

```
[acf,delay] = ambgfun(wav,waveform.SampleRate,waveform.PRF, ...
    Cut='Doppler');
figure
plot(delay/waveform.PulseWidth,mag2db(acf),LineWidth=2)
grid on
xlim([-0.25 0.25])
ylim([-60 1])
xlabel('Delay (\tau/T)')
ylabel('Autocorrelation (dB)')
```



## Plot Stepped Version of Price's Waveform

Generate output samples of a nonlinear FM pulse waveform based on the stepped version of Price's waveform. The pulse width is $5 \mathrm{e}-6$ seconds. The waveform performs 50 frequency steps within one pulse. The time-bandwidth products of the linear and nonlinear components are 20 and 40 respectively. The start frequency of the sweep is 15 MHz . Generate matched filter coefficients and then apply the matched filter.

```
T = 5e-6;
M = 50;
BLT = 20;
BCT = 40;
bfs = [BLT BCT]/T;
fs = 100e6;
fstart = 15e6;
waveform = phased.NonlinearFMWaveform(SampleRate=fs, ...
    PulseWidth=T,FrequencyModulation='Stepped Price', ...
    BandwidthFactors=bfs,NumSteps=M,FrequencyOffset=fstart, ...
    OutputFormat='Pulses',CoefficientsOutputPort=true);
```

Plot the complex waveform.
figure
plot(waveform,PlotType=' complex')



Obtain the resulting sweep bandwidth (Hz)
bandwidth(waveform)
ans $=4.3317 e+07$
Find the matched filter coefficients. Then plot the filtered waveform.

```
[wav,coeff] = waveform();
mf = phased.MatchedFilter(CoefficientsSource='Input port');
mfout = mf(wav,coeff);
```

Plot the filter input and output.

```
figure
subplot(211)
plot(real(wav))
grid on
xlabel('Samples')
ylabel('Amplitude (V)')
title('Input Signal')
subplot(212)
plot(abs(mfout));
grid on
xlabel('Samples')
ylabel('Amplitude (V)')
title('Matched Filter Output')
```



Plot Spectrogram of Hyperbolic FM Waveform
Create a hyperbolic frequency modulated (HFM) waveform. The start and the stop frequencies of the sweep are 100 kHz and 20 kHz , respectively. The pulse width is 50 ms . The sample rate is 200 kHz . Plot the spectrogram.

```
f1 = 100e3;
f2 = 20e3;
BW = f1 - f2;
T = 50e-3;
fs = 2*f1;
```

Create a hyperbolic FM waveform.
waveform = phased.NonlinearFMWaveform( ...
SampleRate=fs,PulseWidth=T,SweepBandwidth=BW, ...
FrequencyModulation='Hyperbolic', ...
HyperbolicStartFrequency=f1, ...
SweepDirection='down', PRF=1/T);
sig = waveform();
spectrogram(sig, 256, 128, 1024, fs, 'yaxis')


## Version History <br> Introduced in R2023a

## References

[1] Collins, T., and P. Atkins. "Nonlinear frequency modulation chirps for active sonar." IEE Proceedings-Radar, Sonar and Navigation 146.6 (1999): 312-316.
[2] Levanon, Nadav, and Eli Mozeson. Radar signals. John Wiley \& Sons, 2004, pp. 92-93.
[3] Doerry, Armin Walter. "Generating nonlinear FM chirp waveforms for radar". No.
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[4] Cook, C. E. "A class of nonlinear FM pulse compression signals." Proceedings of the IEEE 52.11 (1964): 1369-1371.
[5] Yang, J., and T. K. Sarkar. "Doppler-invariant property of hyperbolic frequency modulated waveforms." Microwave and optical technology letters 48.6 (2006): 1174-1179.
[6] Melvin, William L., and James Scheer. Principles of modern radar: advanced techniques. SciTech Pub., 2013.
[7] Alphonse, Sebastian, and Geoffrey A. Williamson. "Evaluation of a class of NLFM radar signals." EURASIP Journal on Advances in Signal Processing 2019.1 (2019): 1-12.

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{rm}}$.

## See Also

phased.LinearFMWaveform | phased.CustomFMWaveform | phased. PhaseCodedWaveform | phased.RectangularWaveform|phased.SteppedFMWaveform|nlfmspec2freq

Topics
"Waveform Analysis Using the Ambiguity Function"

## phased.CustomFMWaveform

Package: phased
Custom FM pulse waveform

## Description

The phased.CustomFMWaveform System object lets you define a waveform with a user-defined frequency modulation (FM) and waveform envelope.

To create the waveform:
1 Create the phased.CustomFMWaveform object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

waveform = phased.CustomFMWaveform()
waveform = phased.CustomFMWaveform(Name=Value)

## Description

waveform = phased.CustomFMWaveform() creates a custom FM pulse waveform System object with linear frequency modulation and a rectangular envelope.
waveform = phased.CustomFMWaveform(Name=Value) sets additional properties using NameValue arguments. You can specify additional name-value pair arguments in any order as (Neme1=Value1,...,NameN=ValueN).

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## SampleRate - Signal sample rate

le6 (default) | positive scalar
Signal sample rate, specified as a positive scalar. The ratio of sample rate to pulse repetition frequency must be a positive integer, so the number of samples in each pulse must be an integer value. Units are in Hertz.

## Example: 100e3

## Data Types: double

## DurationSpecification - Method to set pulse duration

'Pulse width' (default)|'Duty cycle'
Method to set pulse duration (pulse width), specified as 'Pulse width' or 'Duty cycle'. This property determines how you set the pulse duration.

- When you set this property to 'Pulse width', set the pulse duration directly using the PulseWidth property.
- When you set this property to 'Duty cycle', set the pulse duration from the values of the PRF and DutyCycle properties. The pulse width is equal to the value of the DutyCycle property divided by the value of the PRF property.

Data Types: char | string

## PulseWidth - Pulse time duration

50e-6 (default) | positive scalar
Pulse time duration, specified as a positive scalar. The value must satisfy PulseWidth <= 1./PRF. Units are in seconds.

## Dependencies

To enable this property, set the DurationSpecification property to 'Pulse width'.
Data Types: double

## DutyCycle - Pulse duty cycle

0.5 (default) | positive scalar in the range [0,1]

Pulse duty cycle, specified as a positive scalar in the range $[0,1]$. The pulse width is the value of the DutyCycle property divided by the value of the PRF property. This quantity is dimensionless.
Example: 0.75

## Dependencies

To enable this property, set the DurationSpecification property to 'Duty cycle'.
Data Types: double

## PRF - Pulse repetition frequency

10e3 (default) | positive scalar | row vector of positive values
Pulse repetition frequency (PRF), specified as a scalar or a row vector. Units are in Hz. The pulse repetition interval (PRI) is the inverse of the pulse repetition frequency PRF value. The PRF must satisfy these restrictions:

- The product of PRF and PulseWidth must be less than or equal to one. This condition requires that the pulse width is less than one PRI. For the phase-coded waveform, the pulse width is the product of the values of the ChipWidth and NumChips properties.
- The ratio of SampleRate to PRF must be an integer. This condition requires that the number of samples in one PRI is an integer.

You can set the value of PRF using the PRF property settings alone or using property settings in conjunction with the prfidx input argument of the object.

- When PRFSelectionInputPort is false, you set the PRF using the PRF properties alone. You can:
- Implement a constant PRF by specifying the PRF property as a positive real-valued scalar.
- Implement a staggered PRF by specifying the PRF property as a row vector with positive realvalued elements. Each call to the object uses successive elements of this vector as the PRF. Once the object reaches the last element of the vector, it continues the process cyclically with the first element of the vector.
- When PRFSelectionInputPort is true, you can set the PRF value using the PRF property in conjunction with the prfidx input argument. You implement a selectable PRF by specifying the PRF property as a row vector with positive real-valued elements. When you execute the object, the object selects a PRF by using the index you specify in the prfidx input argument to index into the PRF vector.

In all cases, the number of output samples is fixed when you set the OutputFormat property to 'Samples'. When you use a varying PRF and also set the OutputFormat property to 'Pulses ', the number of samples can vary.

Data Types: double

## PRFSelectionInputPort - Enable PRF selection input

false (default) |true
Enable PRF selection input, specified as false or true. When you set this property to true, you can pass an index argument to the object to select a predefined value from the PRF property vector. When you set this property to false, the object uses the PRF property to define the PRF sequence used in the simulation.
Data Types: logical

## FrequencyModulation - Waveform frequency modulation

length- $M$ real-valued vector | function handle
Waveform frequency modulation, specified as a length- $M$ real-valued vector, function handle, or cell array.

- If the FrequencyModulation property is a vector, it specifies samples of the instantaneous frequency at $M$ points as $\left[f_{1}, f_{2}, \ldots, f_{\mathrm{M}}\right]$. The waveform sweeps the specified frequencies such that for the $k^{\text {th }}$ pulse with start time $t_{\mathrm{k}}$ and duration $T_{\mathrm{k}}$, the instantaneous frequency at time

$$
t_{m}=t_{k}+(m-1) T_{k} /(M-1)
$$

is equal to $f_{\mathrm{m}}$ where $t_{\mathrm{k}} \leqq t_{\mathrm{m}} \leqq t_{\mathrm{k}}+T_{\mathrm{k}}$ and $m=1 \ldots M$. The instantaneous frequencies between time $t_{\mathrm{m}}$ and $t_{\mathrm{m}+1}$ are found by linearly interpolating between $f_{\mathrm{m}}$ and $f_{\mathrm{m}+1}$. The resulting custom FM waveform is a piecewise linear FM (LFM) waveform consisting of M-1 LFM sections of equal duration.

- If the FrequencyModulation property is a function handle, the function must have the following syntax: $f=f m F c n(t)$ where $f$ is the instantaneous frequency at time $t$. $t$ is the time at which to compute the instantaneous frequency. The values in $t$ are between 0 and the pulse width.
- If the FrequencyModulation property is a cell array, then the first cell must be a function handle as specified above. The remaining entries in the cell array are the additional input arguments to the function, if any.

Data Types: double

## Envelope - Waveform envelope function

'Rectangular' (default)|'Gaussian' |'Hamming'|'Chebyshev' |'Hann'|'Kaiser' | 'Taylor'|'Custom'

Waveform envelope function, specified as 'Rectangular', 'Gaussian', 'Hamming', 'Chebyshev', 'Hann', 'Kaiser', 'Taylor', or 'Custom'.

When you set Envelope is set to 'Custom' must use the CustomEnvelope property to specify a custom envelope.

Example: 'Taylor'
Data Types: char | string

## EnvelopeSidelobeLevel - Envelope window sidelobe level

30 (default) | positive scalar
Sidelobe level for a Kaiser, Chebyshev, or Taylor window used as the waveform envelope, specified as a positive scalar. Units are in dB.

## Dependencies

To enable this property, set the Envelope property to 'Kaiser', 'Chebyshev', or 'Taylor'.
Data Types: double

## CustomEnvelope - User-defined waveform envelope

@gausswin (default) | function handle | cell array
User-defined waveform envelope, specified as a function handle or cell array.

- If CustomEnvelope is a function handle, the specified function uses the window length as input and generates appropriate window coefficients.
- If CustomEnvelope is a cell array, then the first cell must be a function handle. The specified function takes the window length as the first input argument, with other additional input arguments if necessary, and generates appropriate window coefficients. The remaining entries in the cell array serve as additional input arguments to the function.

Example: \{@chebwin,512,100\}

## Dependencies

To enable this property, set the Envelope property to 'Custom'.
Data Types: cell | function_handle
FrequencyOffsetSource - Source of frequency offset 'Property' (default)|'Input port'

Source of frequency offset, specified as 'Property' or 'Input port'.

- When you set this property to 'Property', the frequency offset is determined by the value of the Frequency0ffset property.
- When you set this property to 'Input port', the frequency offset is determined by the input argument freqoffset when calling the object.

Example: 'Input port'
Data Types: char|string
Frequency0ffset - Frequency offset
0 (default) | scalar
Frequency offset, specified as a scalar. Units are in Hz.
Example: 150.0

## Dependencies

To enable this property, set the Frequency0ffsetSource property to 'Property '.
Data Types: double

## OutputFormat - Format of output signal

'Pulses' (default)| 'Samples'
Format of output signal, specified as 'Pulses ' or 'Samples '.

- When you set the OutputFormat property to 'Pulses', the output of the object takes the form of multiple pulses specified by the value of the NumPulses property. The number of samples per pulse can vary if you change the PRF during the simulation.
- When you set the OutputFormat property to 'Samples', the output of the object takes the form of multiple samples. In this case, the number of output signal samples is the value of the NumSamples property and is fixed.

Data Types: char|string

## NumSamples - Number of samples in output

100 (default) | positive integer
Number of samples in each output of the object, specified as a positive integer.

## Dependencies

To enable this property, set the OutputFormat property to 'Samples '.
Data Types: double

## NumPulses - Number of pulses in output

1 (default) | positive integer
Number of pulses in each output, specified as a positive integer.

## Dependencies

To enable this property, set the OutputFormat property to 'Pulses'.
Data Types: double

## PRFOutputPort - Enable PRF output

false (default) |true
Enable PRF output, specified as false or true. Set this property to true to output the PRF.

## Dependencies

To enable this property, set the OutputFormat property to 'Pulses '.
Data Types: logical
CoefficientsOutputPort - Enable matched filter coefficients output false (default) | true

Enable matched filter coefficients output, specified as false or true. Set this property to true to enable the object the output of the matched filter coefficients of the waveform used during the simulation.

Data Types: logical

## Usage

## Syntax

```
Y = waveform()
Y = waveform(prfidx)
Y = waveform(freqoffset)
[Y,PRF] = waveform(__)
[Y,coeff]= waveform()
```


## Description

$\mathrm{Y}=$ waveform( ) returns samples of the custom nonlinear FM pulse in a column vector Y . Y can contain a certain number of pulses or a certain number of samples.
$\mathrm{Y}=$ waveform(prfidx) specifies the index of the PRF vector, prfidx. The object uses the index is used to identify the entries specified in the PRF property. To enable this syntax, set the PRFSelectionInputPort property to true.

Use this syntax for the cases where you need to dynamically select the transmitted pulse. In such situations, the PRF property includes a list of predetermined PRF values. During the simulation, based on PRF index input, the object selects one of the PRFs values for the PRF for the next transmission.

The transmission always finishes the current pulse before starting the next pulse. Therefore, when you set the OutputFormat property to 'Samples' and then specify the NumSamples property to be shorter than a pulse, the object can ignore the PRF index during a given simulation step if needs the entire output to finish the previously transmitted pulse.
$Y=$ waveform(freqoffset) specifies the value of the frequency offset freqoffset. The offset generates the waveform with a frequency offset. Use this syntax when you need to update the transmit pulse frequency dynamically. To enable this syntax, set the FrequencyOffsetSource property to 'Input port'.
[Y, PRF] = waveform (__ ) also returns the current PRF. To enable this syntax, set the PRFOutputPort property to true and set the OutputFormat property to 'Pulses'.
[ Y , coeff]= waveform() returns the matched filter coefficients coeff when you set the Coefficients0utputPort property to true.

You can combine optional input and output arguments when you set their enabling properties are set. List optional inputs and outputs in the same order as the order of the enabling properties. For example,
[Y,PRF, coeff] = waveform(prfidx,freqoffset)

## Input Arguments

prfidx - index of PRF
positive integer
Index of PRF, specified as a positive integer. The index identifies the entries in the PRF property. To enable this syntax, set the PRFSelectionInputPort property to true. Use this syntax when you need to dynamically select the transmit pulse. In such situations, the PRF property includes a list of predetermined values. During the simulation, based on the PRF index input, the object selects one of the PRFs is selected as the PRF for the next transmission.

## freqoffset - frequency offset

0 (default) | scalar
Frequency offset, specified as a finite scalar. The object generates the waveform with a frequency offset. Use this syntax when you need to update the transmit pulse frequency dynamically.

## Dependencies

To use this argument, set the Frequency0ffsetSource property to 'Input port '.

## Data Types: double

## Output Arguments

## PRF - pulse repetition frequency

scalar
Pulse repetition frequency, returned as a scalar. When you set the PRFOutputPort property to true it returns the current PRF used by the system. Units are in Hz.

## Dependencies

To enable this argument, set the PRFOutputPort property to true and set the OutputFormat to 'Pulses'.

## coeff - matched filter coefficients

$N_{Z}$-by-1 complex-valued vector $\mid N_{Z}$-by- $M$ complex-valued matrix
Matched filter coefficients, returned as an $N_{Z}$-by- 1 complex-valued vector or an $N_{Z}$-by- $M$ complexvalued matrix.

- If you set OutputFormat to 'Pulses' and NumPulses is 1 , the object returns coeff as an $N_{Z^{-}}$ length vector. $N_{Z}$ corresponds to the pulse width.
- If you set OutputFormat to 'Pulses' with NumPulses greater than 1 or OutputFormat is 'Samples' and DurationSpecification is 'Pulse width', coeff is returned as an $N_{Z^{-}}$ length vector. $N_{Z}$ corresponds to the pulse width.
- If OutputFormat is set to 'Pulses ' with NumPulses greater than 1 or OutputFormat is set to 'Samples' and DurationSpecification is set to 'Duty cycle' with only one unique PRF value, coeff is returned as an $N_{Z}$-length vector. $N_{Z}$ corresponds to the pulse width.
- If OutputFormat is 'Pulses' with NumPulses greater than 1 or OutputFormat is 'Samples' and DurationSpecification is 'Duty cycle', coeff is returned as an $N_{Z}$-by- $M$ matrix. $N_{Z}$ corresponds to the maximum pulse width and $M$ corresponds to the number of unique PRFs.


## Dependencies

To enable this argument, set the Coefficients0utputPort property to true.
Data Types: double
Complex Number Support: Yes

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```


## Specific to waveform System objects

| bandwidth | Waveform bandwidth |
| :--- | :--- |
| getMatchedFilter | Matched filter coefficients derived from waveform |
| plot | Plot pulse waveform |

## Common to All System Objects

step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object

## Examples

## Create Custom FM Waveform with Default Properties

Create a custom FM waveform with the default frequency modulation and envelope function.

```
waveform = phased.CustomFMWaveform()
waveform =
    phased.CustomFMWaveform with properties:
                            SampleRate: 1000000
        DurationSpecification: 'Pulse width'
                            PulseWidth: 5.0000e-05
                            PRF: 10000
        PRFSelectionInputPort: false
```

```
    FrequencyModulation: [0 100000]
    Envelope: 'Rectangular'
FrequencyOffsetSource: 'Property'
    FrequencyOffset: 0
            OutputFormat: 'Pulses'
            NumPulses: 1
        PRFOutputPort: false
CoefficientsOutputPort: false
```

Display the real part of the waveform.

```
plot(waveform)
```



## Display Sinusoidal Frequency Modulated Waveform

Create a sinusoidal frequency modulated waveform with a bandwidth of 200 Hz , a pulse width of 0.25 s, and a modulation frequency of 20 Hz .

```
BW = 200;
T = 0.25;
fm = 20;
fs = 10*BW;
freqfunc = @(t)(BW/2)*cos(2*pi*fm*t);
waveform = phased.CustomFMWaveform(SampleRate=fs, ...
```

PulseWidth=T,FrequencyModulation=freqfunc, $\mathrm{PRF}=1 / \mathrm{T}$ );
wav = waveform();
Display the spectrogram of the waveform.
spectrogram(wav, $32,30,512, f s, ' y a x i s ', ' c e n t e r e d ')$
title('Sinusoidal Frequency Modulated Waveform')


## Waveform Derived from Taylor Spectrum Window

Create a nonlinear FM waveform derived from a power spectral density function shaped as a Taylor window with -35 dB sidelobes. The pulse bandwidth is 120 MHz and the pulse duration is $10 \mu \mathrm{sec}$. Generate matched filter coefficients and then apply a matched filter. Plot the resulting matched filter output to display the range sidelobe levels.

```
BW = 120e6;
T = 10e-6;
fs = 10*BW;
```

Generate 200 points of a waveform with instantaneous frequency values defined by a Taylor window. The window has -35 dB sidelobe levels.

```
w = taylorwin(200,4,-35);
freq = nlfmspec2freq(BW,w);
waveform = phased.CustomFMWaveform('SampleRate',fs, ...
```

```
    'PulseWidth',T,'FrequencyModulation',freq, ...
    'OutputFormat','Pulses','CoefficientsOutputPort',true);
disp(['Bandwidth = ',num2str(bandwidth(waveform)/1e6),' MHz']);
Bandwidth = 119.9644 MHz
```

Obtain the matched filter coefficients from the waveform.

```
[wav,coeff] = waveform();
filter = phased.MatchedFilter('CoefficientsSource','Input port');
mfout = filter(wav,coeff);
```

Plot input signal and matched filter output.
$\mathrm{t}=(0$ : numel(wav)-1)/fs;
figure
subplot(121)
plot(t*le6, real(wav))
xlabel('Time (\mus)')
ylabel('Amplitude (V)')
title('Input Signal')
subplot(122)
plot(t*1e6,mag2db(abs(mfout)));
xlabel('Time (\mus)')
ylabel('Amplitude (dB)')
title('Matched Filter Output')
xlim([9 11]);
$y \lim ([0$ 100]);


## Version History

Introduced in R2023a

## References

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[2] Levanon, Nadav, and Eli Mozeson. Radar signals. John Wiley \& Sons, 2004, pp. 92-93.
[3] Doerry, Armin Walter. "Generating nonlinear FM chirp waveforms for radar". No.
SAND2006-5856. Sandia National Laboratories (SNL), Albuquerque, NM, and Livermore, CA (United States), 2006.
[4] Cook, C. E. "A class of nonlinear FM pulse compression signals." Proceedings of the IEEE 52.11 (1964): 1369-1371.
[5] Yang, J., and T. K. Sarkar. "Doppler-invariant property of hyperbolic frequency modulated waveforms." Microwave and optical technology letters 48.6 (2006): 1174-1179.
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[7] Alphonse, Sebastian, and Geoffrey A. Williamson. "Evaluation of a class of NLFM radar signals." EURASIP Journal on Advances in Signal Processing 2019.1 (2019): 1-12.

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

phased.LinearFMWaveform | phased.NonlinearFMWaveform | phased. PhaseCodedWaveform | phased.RectangularWaveform| phased.SteppedFMWaveform|nlfmspec2freq

## Topics

"Waveform Analysis Using the Ambiguity Function"

## phased.LOSChannel

Package: phased
Narrowband LOS propagation channel

## Description

The phased.LOSChannel models the propagation of narrowband electromagnetic signals through a line-of-sight (LOS) channel from a source to a destination. In an LOS channel, propagation paths are straight lines from point to point. The propagation model in the LOS channel includes free-space attenuation in addition to attenuation due to atmospheric gases, rain, fog, and clouds. You can use phased.LOSChannel to model the propagation of signals between multiple points simultaneously.

While the System object works for all frequencies, the attenuation models for atmospheric gases and rain are valid for electromagnetic signals in the frequency range $1-1000 \mathrm{GHz}$ only. The attenuation model for fog and clouds is valid for $10-1000 \mathrm{GHz}$. Outside these frequency ranges, the System object uses the nearest valid value.

The phased.LOSChannel System object applies range-dependent time delays to the signals, as well as gains or losses. When either the source or destination is moving, the System object applies Doppler shifts.

Like the phased. FreeSpace System object, the phased. LOSChannel System object supports twoway propagation.

To compute the propagation delay for specified source and receiver points:
1 Define and set up your LOS channel using the "Construction" on page 1-936 procedure. You can set the System object properties during construction or leave them at their default values. Some properties are tunable and can be changed at any time.
2 Call the step method to compute the propagated signal using the properties of the phased. LOSChannel System object.

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, $y=$ step (obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.

## Construction

sLOS $=$ phased. LOSChannel creates an LOS attenuating propagation channel System object, sLOS.
sLOS = phased.LOSChannel (Name, Value) creates a System object, sLOS, with each specified property Name set to the specified Value. You can specify additional name and value pair arguments in any order as (Name1, Value1,...,NameN, ValueN).

## Properties

PropagationSpeed - Signal propagation speed
physconst('LightSpeed') (default) | positive scalar
Signal propagation speed, specified as a positive scalar. Units are in meters per second. The default propagation speed is the value returned by physconst('LightSpeed'). See physconst for more information.

Example: 3e8
Data Types: double
OperatingFrequency - Operating frequency
300e6 (default) | positive scalar
Operating frequency, specified as a positive scalar. Units are in Hz .
Example: 1e9
Data Types: double

## SpecifyAtmosphere - Enable atmospheric attenuation model

false (default) |true
Option to enable the atmospheric attenuation model, specified as a false or true. Set this property to true to add signal attenuation caused by atmospheric gases, rain, fog, or clouds. Set this property to false to ignore atmospheric effects in propagation.

Setting SpecifyAtmosphere to true, enables the Temperature, DryAirPressure, WaterVapourDensity, LiquidWaterDensity, and RainRate properties.
Data Types: logical

## Temperature - Ambient temperature

15 (default) | real-valued scalar
Ambient temperature, specified as a real-valued scalar. Units are in degrees Celsius.
Example: 20.0

## Dependencies

To enable this property, set SpecifyAtmosphere to true.
Data Types: double

## DryAirPressure - Atmospheric dry air pressure

$101.325 e 3$ (default) | positive real-valued scalar
Atmospheric dry air pressure, specified as a positive real-valued scalar. Units are in pascals (Pa). The default value of this property corresponds to one standard atmosphere.

## Example: 101.0e3

## Dependencies

To enable this property, set SpecifyAtmosphere to true.
Data Types: double

## WaterVapourDensity - Atmospheric water vapor density

## 7.5 (default) | positive real-valued scalar

Atmospheric water vapor density, specified as a positive real-valued scalar. Units are in $\mathrm{g} / \mathrm{m}^{3}$.
Example: 7.4

## Dependencies

To enable this property, set SpecifyAtmosphere to true.
Data Types: double

## LiquidWaterDensity - Liquid water density

0.0 (default) | nonnegative real-valued scalar

Liquid water density of fog or clouds, specified as a nonnegative real-valued scalar. Units are in $\mathrm{g} / \mathrm{m}^{3}$. Typical values for liquid water density are 0.05 for medium fog and 0.5 for thick fog.

## Example: 0.1

## Dependencies

To enable this property, set SpecifyAtmosphere to true.
Data Types: double

## RainRate - Rainfall rate

0.0 (default) | nonnegative scalar

Rainfall rate, specified as a nonnegative scalar. Units are in $\mathrm{mm} / \mathrm{hr}$.
Example: 10.0

## Dependencies

To enable this property, set SpecifyAtmosphere to true.

## Data Types: double

TwoWayPropagation - Enable two-way propagation
false (default) | true
Enable two-way propagation, specified as a false or true. Set this property to true to perform round-trip propagation between the signal origin and destination specified in step. Set this property to false to perform only one-way propagation from the origin to the destination.

## Example: true

Data Types: logical

## SampleRate - Sample rate of signal

1e6 (default) | positive scalar
Sample rate of signal, specified as a positive scalar. Units are in Hz. The System object uses this quantity to calculate the propagation delay in units of samples.
Example: 1e6
Data Types: double

## MaximumDistanceSource - Source of maximum one-way propagation distance 'Auto' (default)|'Property'

Source of maximum one-way propagation distance, specified as 'Auto' or 'Property '. The maximum one-way propagation distance is used to allocate sufficient memory for signal delay computation. When you set this property to 'Auto' ' the System object automatically allocates memory. When you set this property to 'Property', you specify the maximum one-way propagation distance using the value of the MaximumDistance property.
Data Types: char

## MaximumDistance - Maximum one-way propagation distance

10000 (default) | positive real-valued scalar
Maximum one-way propagation distance, specified as a positive real-valued scalar. Units are in meters. Any signal that propagates more than the maximum one-way distance is ignored. The maximum distance must be greater than or equal to the largest position-to-position distance.
Example: 5000

## Dependencies

To enable this property, set the MaximumDistanceSource property to 'Property '.

```
Data Types: double
```


## Methods

| reset | Reset states of System object |
| :--- | :--- |
| step | Propagate signal in LOS channel |

## Common to All System Objects

| release | Allow System object property value changes |
| :--- | :--- | :--- |

## Examples

## Propagate Polarized Wave in LOS Channel

Propagate a polarized electromagnetic wave radiating from a short-dipole antenna element. The dipole is rotated $30^{\circ}$ around the $y$-axis. Set the orientation of the local axis to coincide with the dipole. Assume the dipole radiates at 30.0 GHz . Propagate the signal toward a target approximately 10 km away.

Create the short-dipole antenna element and radiator System objects. Set the Polarization property to 'Combined ' to generate polarized waves.

```
freq = 30.0e9;
c = physconst('LightSpeed');
antenna = phased.ShortDipoleAntennaElement('FrequencyRange',[100e6 40e9], ...
    'AxisDirection','Z');
radiator = phased.Radiator('Sensor',antenna, ...
    'PropagationSpeed',c, ...
    'OperatingFrequency',freq, ...
```

```
'Polarization','Combined', ...
'WeightsInputPort',false);
```

Create a signal to radiate. The signal envelope consists of several cycles of a 4 kHz sinusoid with amplitude set to unity. Set the sampling frequency to 1 MHz .

```
fsig = 4.0e3;
fs = 1.0e6;
t = [1:1000]/fs;
signal = sin(2*pi*fsig*t');
laxes = roty(30)*eye(3,3);
```

Use a phased. FreeSpace System object ${ }^{\mathrm{TM}}$ to propagate the field from the origin to the destination in free space.

```
fschannel = phased.FreeSpace('PropagationSpeed',c,...
    'OperatingFrequency',freq,...
    'TwoWayPropagation',false,...
    'SampleRate',fs);
```

Use a phased.LOSChannel System object to propagate the field from the origin to the destination in the LOS channel. Attenuation is due to atmospheric gases and fog.

```
loschannel = phased.LOSChannel('PropagationSpeed',c,...
    'OperatingFrequency',freq,...
    'TwoWayPropagation',false,...
    'SampleRate',fs,'SpecifyAtmosphere',true,'LiquidWaterDensity',0.5);
```

Set the signal origin, signal origin velocity, signal destination, and signal destination velocity.

```
source_pos = [0;0;0];
target_pos = [10000;200;0];
source_vel = [0;0;0];
target_vel = [0;0;0];
[~,radiatingAngles] = rangeangle(target_pos,source_pos,laxes);
```

Radiate the signal towards the target. The radiated signal is a struct containing the polarized field.

```
rad_sig = radiator(signal,radiatingAngles,laxes);
```

Propagate the signals to the target in free space.

```
prop_sig = fschannel(rad_sig,source_pos,target_pos,...
    source_vel,target_vel);
```

Propagate the signals to the target in the LOS channel.

```
prop_att_sig = loschannel(rad_sig,source_pos,target_pos,...
    source_vel,target_vel);
```

Plot the z -components of both the free-space and LOS-channel-propagated signals.

```
plot(le6*t,real(prop_sig.Z),1e6*t,real(prop_att_sig.Z))
grid
xlabel('Time (\mu sec)')
legend('z_{fsp}','z_{los}')
```



The LOS channel signal is attenuated as compared to the free-space signal.

## More About

## Path Attenuation or Loss

Attenuation or path loss in the LOS channel consists of four components. $L=L_{f s p} L_{g} L_{c} L_{r}$, where

- $L_{f s p}$ is the free space path attenuation
- $L_{g}$ is the atmospheric path attenuation
- $L_{c}$ is the fog and cloud path attenuation
- $L_{r}$ is the rain path attenuation

Each path attenuation is in magnitude units, not in dB.

## Free-space Time Delay and Path Loss

When the origin and destination are stationary relative to each other, you can write the output signal of a free-space channel as $Y(t)=x(t-\tau) / L_{f s p}$. The quantity $\tau$ is the signal delay and $L_{f s p}$ is the free-space path loss. The delay $\tau$ is given by $R / c$, where $R$ is the propagation distance and $c$ is the propagation speed. The free-space path loss is given by

$$
L_{f s p}=\frac{(4 \pi R)^{2}}{\lambda^{2}}
$$

where $\lambda$ is the signal wavelength.
This formula assumes that the target is in the far field of the transmitting element or array. In the near field, the free-space path loss formula is not valid and can result in a loss smaller than one, equivalent to a signal gain. Therefore, the loss is set to unity for range values, $R \leq \lambda / 4 \Pi$.

When the origin and destination have relative motion, the processing also introduces a Doppler frequency shift. The frequency shift is $v / \lambda$ for one-way propagation and $2 v / \lambda$ for two-way propagation. The quantity $v$ is the relative speed of the destination with respect to the origin.

For more details on free-space channel propagation, see [5].

## Atmospheric Gas Attenuation Model

This model calculates the attenuation of signals that propagate through atmospheric gases.
Electromagnetic signals attenuate when they propagate through the atmosphere. This effect is due primarily to the absorption resonance lines of oxygen and water vapor, with smaller contributions coming from nitrogen gas. The model also includes a continuous absorption spectrum below 10 GHz . The ITU model Recommendation ITU-R P.676-10: Attenuation by atmospheric gases is used. The model computes the specific attenuation (attenuation per kilometer) as a function of temperature, pressure, water vapor density, and signal frequency. The atmospheric gas model is valid for frequencies from 1-1000 GHz and applies to polarized and nonpolarized fields.

The formula for specific attenuation at each frequency is

$$
\gamma=\gamma_{0}(f)+\gamma_{w}(f)=0.1820 f N^{\prime \prime}(f) .
$$

The quantity $N^{\prime \prime}()$ is the imaginary part of the complex atmospheric refractivity and consists of a spectral line component and a continuous component:

$$
N^{\prime \prime}(f)=\sum_{i} S_{i} F_{i}+N^{\prime \prime}{ }_{D}(f)
$$

The spectral component consists of a sum of discrete spectrum terms composed of a localized frequency bandwidth function, $F(f)_{\mathrm{i}}$, multiplied by a spectral line strength, $S_{\mathrm{i}}$. For atmospheric oxygen, each spectral line strength is

$$
S_{i}=a_{1} \times 10^{-7}\left(\frac{300}{T}\right)^{3} \exp \left[a_{2}\left(1-\left(\frac{300}{T}\right)\right] P .\right.
$$

For atmospheric water vapor, each spectral line strength is

$$
S_{i}=b_{1} \times 10^{-1}\left(\frac{300}{T}\right)^{3.5} \exp \left[b_{2}\left(1-\left(\frac{300}{T}\right)\right] W .\right.
$$

$P$ is the dry air pressure, $W$ is the water vapor partial pressure, and $T$ is the ambient temperature. Pressure units are in hectoPascals ( hPa ) and temperature is in degrees Kelvin. The water vapor partial pressure, $W$, is related to the water vapor density, $\rho$, by

$$
W=\frac{\rho T}{216.7} .
$$

The total atmospheric pressure is $P+W$.

For each oxygen line, $S_{i}$ depends on two parameters, $a_{1}$ and $a_{2}$. Similarly, each water vapor line depends on two parameters, $b_{1}$ and $b_{2}$. The ITU documentation cited at the end of this section contains tabulations of these parameters as functions of frequency.

The localized frequency bandwidth functions $F_{i}(f)$ are complicated functions of frequency described in the ITU references cited below. The functions depend on empirical model parameters that are also tabulated in the reference.

To compute the total attenuation for narrowband signals along a path, the function multiplies the specific attenuation by the path length, $R$. Then, the total attenuation is $L_{g}=R\left(\gamma_{o}+\gamma_{w}\right)$.

You can apply the attenuation model to wideband signals. First, divide the wideband signal into frequency subbands, and apply attenuation to each subband. Then, sum all attenuated subband signals into the total attenuated signal.

## Fog and Cloud Attenuation Model

This model calculates the attenuation of signals that propagate through fog or clouds.
Fog and cloud attenuation are the same atmospheric phenomenon. The ITU model, Recommendation ITU-R P.840-6: Attenuation due to clouds and fog is used. The model computes the specific attenuation (attenuation per kilometer), of a signal as a function of liquid water density, signal frequency, and temperature. The model applies to polarized and nonpolarized fields. The formula for specific attenuation at each frequency is

$$
\gamma_{C}=K_{l}(f) M,
$$

where $M$ is the liquid water density in $\mathrm{gm} / \mathrm{m}^{3}$. The quantity $K_{l}(f)$ is the specific attenuation coefficient and depends on frequency. The cloud and fog attenuation model is valid for frequencies $10-1000 \mathrm{GHz}$. Units for the specific attenuation coefficient are $(\mathrm{dB} / \mathrm{km}) /\left(\mathrm{g} / \mathrm{m}^{3}\right)$.

To compute the total attenuation for narrowband signals along a path, the function multiplies the specific attenuation by the path length $R$. Total attenuation is $L_{c}=R \gamma_{c}$.

You can apply the attenuation model to wideband signals. First, divide the wideband signal into frequency subbands, and apply narrowband attenuation to each subband. Then, sum all attenuated subband signals into the total attenuated signal.

## Rainfall Attenuation Model

This model calculates the attenuation of signals that propagate through regions of rainfall. Rain attenuation is a dominant fading mechanism and can vary from location-to-location and from year-toyear.

Electromagnetic signals are attenuated when propagating through a region of rainfall. Rainfall attenuation is computed according to the ITU rainfall model Recommendation ITU-R P.838-3: Specific attenuation model for rain for use in prediction methods. The model computes the specific attenuation (attenuation per kilometer) of a signal as a function of rainfall rate, signal frequency, polarization, and path elevation angle. The specific attenuation, $\gamma_{R}$, is modeled as a power law with respect to rain rate

$$
\gamma_{R}=k R^{\alpha},
$$

where $R$ is rain rate. Units are in $\mathrm{mm} / \mathrm{hr}$. The parameter $k$ and exponent $\alpha$ depend on the frequency, the polarization state, and the elevation angle of the signal path. The specific attenuation model is valid for frequencies from 1-1000 GHz.

To compute the total attenuation for narrowband signals along a path, the function multiplies the specific attenuation by the an effective propagation distance, $d_{\text {eff. }}$. Then, the total attenuation is $L=$ $d_{\text {eff }} Y_{\mathrm{R}}$.

The effective distance is the geometric distance, $d$, multiplied by a scale factor

$$
r=\frac{1}{0.477 d^{0.633} R_{0.01}^{0.073 \alpha} f^{0.123}-10.579(1-\exp (-0.024 d))}
$$

where $f$ is the frequency. The article Recommendation ITU-R P.530-17 (12/2017): Propagation data and prediction methods required for the design of terrestrial line-of-sight systems presents a complete discussion for computing attenuation.

The rain rate, $R$, used in these computations is the long-term statistical rain rate, $R_{0.01}$. This is the rain rate that is exceeded $0.01 \%$ of the time. The calculation of the statistical rain rate is discussed in Recommendation ITU-R P.837-7 (06/2017): Characteristics of precipitation for propagation modelling. This article also explains how to compute the attenuation for other percentages from the $0.01 \%$ value.

You can apply the attenuation model to wideband signals. First, divide the wideband signal into frequency subbands and apply attenuation to each subband. Then, sum all attenuated subband signals into the total attenuated signal.

## Version History

## Introduced in R2016a

## References

[1] Radiocommunication Sector of the International Telecommunication Union. Recommendation ITUR P.676-10: Attenuation by atmospheric gases. 2013.
[2] Radiocommunication Sector of the International Telecommunication Union. Recommendation ITUR P.840-6: Attenuation due to clouds and fog. 2013.
[3] Radiocommunication Sector of the International Telecommunication Union. Recommendation ITUR P.838-3: Specific attenuation model for rain for use in prediction methods. 2005.
[4] Seybold, J. Introduction to RF Propagation. New York: Wiley \& Sons, 2005.
[5] Skolnik, M. Introduction to Radar Systems, 3rd Ed. New York: McGraw-Hill, 2001.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:

See "System Objects in MATLAB Code Generation" (MATLAB Coder).

## See Also

## Functions

rangeangle|fogpl|gaspl|rainpl|fspl
Objects
phased.FreeSpace| phased.RadarTarget | phased.BackscatterRadarTarget |
twoRayChannel|phased.WidebandFreeSpace | phased.WidebandLOSChannel

## reset

System object: phased. LOSChannel
Package: phased
Reset states of System object

## Syntax

reset(sLOS)

## Description

reset (sLOS) resets the internal state of the phased. LOSChannel System object, sLOS. If SeedSource is a property of this System object and has the value 'Property ', then this method resets the random number generator state.

## Input Arguments

sLOS - LOS channel
phased.LOSChannel System object
LOS channel, specified as a phased. LOSChannel System object.
Example: phased.LOSChannel

## Version History <br> Introduced in R2016a

## step

System object: phased. LOSChannel
Package: phased
Propagate signal in LOS channel

## Syntax

prop_sig = step(sLOS,sig,origin_pos,dest_pos,origin_vel,dest_vel)

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.
prop_sig = step(sLOS,sig,origin_pos,dest_pos,origin_vel,dest_vel) returns the resulting signal, prop_sig, when a narrowband signal, sig, propagates through a line-of-sight (LOS) channel from a source located at the origin_pos position to a destination at the dest_pos position. Only one of the origin_pos or dest_pos arguments can specify multiple positions. The other must contain a single position. The velocity of the signal origin is specified in origin_vel and the velocity of the signal destination is specified in dest_vel. The dimensions of origin_vel and dest_vel must match the dimensions of origin_pos and dest_pos, respectively.

Electromagnetic fields propagating through an LOS channel can be polarized or nonpolarized. For nonpolarized fields, the propagating signal field, sig, is a vector or matrix. For polarized fields, sig is an array of structures. The structure elements represent an electric field vector in Cartesian form.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

sLOS - LOS channel
phased.LOSChannel System object
LOS channel, specified as a phased. LOSChannel System object.
Example: phased. LOSChannel

## sig - Narrowband signal

$M$-by- $N$ complex-valued matrix | 1-by- $N$ struct array containing complex-valued fields

Narrowband signal, specified as a matrix or struct array, depending on whether is signal or polarized or nonpolarized. The quantity $M$ is the number of samples in the signal, and $N$ is the number of LOS channels. Each channel corresponds to a source-destination pair.

- Narrowband nonpolarized scalar signal. Specify sig as an $M$-by- $N$ complex-valued matrix. Each column contains one signal propagated along the line-of-sight path.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

- Narrowband polarized signal. Specify sig as a 1-by- $N$ struct array containing complex-valued fields. Each struct represents a polarized signal propagated along the line-of-sight path. Each struct element contains three $M$-by- 1 complex-valued column vectors, sig. X , sig. Y , and sig. $Z$. These vectors represent the $x, y$, and $z$ Cartesian components of the polarized signal.

The size of the first dimension of the matrix fields within the struct can vary to simulate a changing signal length such as a pulse waveform with variable pulse repetition frequency.

Example: [1, 1; j, 1;0.5,0]
Data Types: double
Complex Number Support: Yes

## origin_pos - Signal origins

3-by-1 real-valued column vector | 3 -by- $N$ real-valued matrix
Origin of signals, specified as a 3-by-1 real-valued column vector or 3-by- $N$ real-valued matrix. The quantity $N$ is the number of LOS channels. If origin_pos is a column vector, it takes the form [ $x ; y ; z$ ]. If origin_pos is a matrix, each column specifies a different signal origin and has the form [ $x ; y ; z]$. Units are in meters.

You cannot specify both origin_pos and dest_pos as matrices. At least one must be a 3-by-1 column vector.

## Example: [1000;100;500]

Data Types: double

## dest_pos - Signal destinations

3-by-1 real-valued column vector | 3 -by- $N$ real-valued matrix
Destination position of the signal or signals, specified as a 3-by-1 real-valued column vector or 3-by- $N$ real-valued matrix. The quantity $N$ is the number of LOS channels propagating from or to $N$ signal origins. If dest_pos is a 3-by-1 column vector, it takes the form [x;y;z]. If dest_pos is a matrix, each column specifies a different signal destination and takes the form [x;y;z] Position units are in meters.

You cannot specify both origin_pos and dest_pos as matrices. At least one must be a 3-by-1 column vector.

```
Example: [0;0;0]
Data Types: double
```

origin_vel - Velocities of signal origins
3-by-1 real-valued column vector | 3-by- $N$ real-valued matrix

Velocity of signal origin, specified as a 3-by-1 real-valued column vector or 3-by-N real-valued matrix. The dimensions of origin_vel must match the dimensions of origin_pos. If origin_vel is a column vector, it takes the form [ $\mathrm{Vx} ; \mathrm{Vy} ; \mathrm{Vz}$ ]. If origin_vel is a 3 -by- $N$ matrix, each column specifies a different origin velocity and has the form $[\mathrm{Vx} \overline{\mathrm{V} y} ; \mathrm{Vz}]$. Velocity units are in meters per second.

Example: [10;0;5]
Data Types: double
dest_vel - Velocities of signal destinations
3 -by-1 real-valued column vector | 3 -by- $N$ real-valued matrix
Velocity of signal destinations, specified as a 3-by-1 real-valued column vector or 3-by- N real-valued matrix. The dimensions of dest_vel must match the dimensions of dest_pos. If dest_vel is a column vector, it takes the form [ $\mathrm{Vx} ; \mathrm{Vy} ; \mathrm{Vz}$ ]. If dest_vel is a 3-by- $N$ matrix, each column specifies a different destination velocity and has the form [ $\mathrm{Vx} ; \overline{\mathrm{V} y ; V z] ~ V e l o c i t y ~ u n i t s ~ a r e ~ i n ~ m e t e r s ~ p e r ~ s e c o n d . ~}$
Example: [0;0;0]
Data Types: double

## Output Arguments

## prop_sig - Narrowband propagated signal

$M$-by- $N$ complex-valued matrix | 1 -by- $N$ struct array containing complex-valued fields
Narrowband signal, returned as a matrix or struct array, depending on whether signal is polarized or nonpolarized. The quantity $M$ is the number of samples in the signal and $N$ is the number of narrowband LOS channels. Each channel corresponds to a source-destination pair.

- Narrowband nonpolarized scalar signal. prop_sig is an $M$-by- $N$ complex-valued matrix.
- Narrowband polarized scalar signal. prop_sig is a 1 -by- $N$ struct array containing complexvalued fields. Each struct element contains three $M$-by- 1 complex-valued column vectors, sig. X , sig. Y , and sig.Z. These vectors represent the $x, y$, and $z$ Cartesian components of the polarized signal.

The prop_sig output contains signal samples arriving at the signal destination within the current time frame. The current time frame is the time frame of the input signals to step. Whenever it takes longer than the current time frame for the signal to propagate from the origin to the destination, the output might not contain all contributions from the input of the current time frame. The remaining output appears in the next call to step.

## Examples

## Propagate Signal in LOS Channel

Propagate a sinusoidal signal in a line of sight (LOS) channel from a radar at (1000,0,0) meters to a target at $(10000,4000,500)$ meters. Assume the signal propagates in medium fog specified by a liquid water density of $0.05 \mathrm{~g} / \mathrm{m}^{3}$. Assume that the radar and the target are stationary. The signal carrier frequency is 10 GHz . The signal frequency is 500 Hz and the sample rate is 8.0 kHz .

Set up the transmitted signal.

```
fs = 8.0e3;
dt = 1/fs;
fsig = 500.0;
fc = 10.0e9;
t = [0:dt:.01];
sig = sin(2*pi*fsig*t);
```

Set the liquid water density and specify the LOS channel System object ${ }^{\mathrm{TM}}$.
lwd $=0.05$;
channel = phased.LOSChannel('SampleRate',fs,'SpecifyAtmosphere',true,...
'LiquidWaterDensity',lwd,'OperatingFrequency',fc);
Set the origin and destination of the signal.

```
xradar = [1000,0,0].';
vradar = [0,0,0].';
xtgt = [10000,4000,500].';
vtgt = [0,0,0].';
```

Propagate the signal from origin to destination and plot the result.

```
prog_sig = channel(sig.',xradar,xtgt,vradar,vtgt);
plot(t*1000,real(prog_sig))
grid
xlabel('Time (milliseconds)')
ylabel('Amplitude')
```



## Version History

## Introduced in R2016a

## References

[1] Radiocommunication Sector of the International Telecommunication Union. Recommendation ITUR P.676-10: Attenuation by atmospheric gases. 2013.
[2] Radiocommunication Sector of the International Telecommunication Union. Recommendation ITUR P.840-6: Attenuation due to clouds and fog. 2013.
[3] Radiocommunication Sector of the International Telecommunication Union. Recommendation ITUR P.838-3: Specific attenuation model for rain for use in prediction methods. 2005.
[4] Seybold, J. Introduction to RF Propagation. New York: Wiley \& Sons, 2005.

# phased.MatchedFilter 

Package: phased
Matched filter

## Description

The MatchedFilter object implements matched filtering of an input signal.
To compute the matched filtered signal:
1 Define and set up your matched filter. See "Construction" on page 1-952.
2 Call step to perform the matched filtering according to the properties of phased.MatchedFilter. The behavior of step is specific to each object in the toolbox.

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.

## Construction

$H=$ phased.MatchedFilter creates a matched filter System object, $H$. The object performs matched filtering on the input data.

H = phased.MatchedFilter(Name,Value) creates a matched filter object, H, with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN).

## Properties

## CoefficientsSource

Source of matched filter coefficients
Specify whether the matched filter coefficients come from the Coefficients property of this object or from an input argument in step. Values of this property are:

| 'Property' | The Coefficients property of this object specifies the <br> coefficients. |
| :--- | :--- |
| 'Input port' | An input argument in each invocation of step specifies the <br> coefficients. |

Default: 'Property'
Coefficients
Matched filter coefficients

Specify the matched filter coefficients as a column vector. This property applies when you set the CoefficientsSource property to 'Property'. This property is tunable.

Default: [1;1]

## SpectrumWindow

Window for spectrum weighting
Specify the window used for spectrum weighting using one of 'None', 'Hamming', 'Chebyshev', 'Hann', 'Kaiser', 'Taylor', or 'Custom'. Spectrum weighting is often used with linear FM waveform to reduce the sidelobes in the time domain. The object computes the window length internally, to match the FFT length.

Default: 'None'

## CustomSpectrumWindow

User-defined window for spectrum weighting
Specify the user-defined window for spectrum weighting using a function handle or a cell array. This property applies when you set the SpectrumWindow property to 'Custom'.

If CustomSpectrumWindow is a function handle, the specified function takes the window length as the input and generates appropriate window coefficients.

If CustomSpectrumWindow is a cell array, then the first cell must be a function handle. The specified function takes the window length as the first input argument, with other additional input arguments if necessary, and generates appropriate window coefficients. The remaining entries in the cell array are the additional input arguments to the function, if any.

Default: @hamming

## SpectrumRange

Spectrum window coverage region
Specify the spectrum region on which the spectrum window is applied as a 1-by-2 vector in the form of [StartFrequency EndFrequency] (in hertz). This property applies when you set the SpectrumWindow property to a value other than 'None'.

Note that both StartFrequency and EndFrequency are measured in baseband. That is, they are within [-Fs/2 Fs/2], where Fs is the sample rate that you specify in the SampleRate property. StartFrequency cannot be larger than EndFrequency.

Default: [0 1e5]

## SampleRate

Coefficient sample rate
Specify the matched filter coefficients sample rate (in hertz) as a positive scalar. This property applies when you set the SpectrumWindow property to a value other than 'None'.

Default: le6

## SidelobeAttenuation

Window sidelobe attenuation level
Specify the sidelobe attenuation level (in decibels) of a Chebyshev or Taylor window as a positive scalar. This property applies when you set the SpectrumWindow property to 'Chebyshev' or 'Taylor'.

Default: 30

## Beta

Kaiser window parameter
Specify the parameter that affects the Kaiser window sidelobe attenuation as a nonnegative scalar. Please refer to kaiser for more details. This property applies when you set the SpectrumWindow property to 'Kaiser'.

## Default: 0.5

## Nbar

Number of nearly constant sidelobes in Taylor window
Specify the number of nearly constant level sidelobes adjacent to the mainlobe in a Taylor window as a positive integer. This property applies when you set the SpectrumWindow property to 'Taylor'.

## Default: 4

## GainOutputPort

Output gain
To obtain the matched filter gain, set this property to true and use the corresponding output argument when invoking step. If you do not want to obtain the matched filter gain, set this property to false.

Default: false

## Methods

step Perform matched filtering
Common to All System Objects
release Allow System object property value changes

## Examples

## Matched Filter for Linear FM Waveform

Construct a matched filter for a linear FM waveform.
waveform = phased.LinearFMWaveform('PulseWidth',1e-4,'PRF',5e3);
x = waveform();
filter = phased.MatchedFilter( ...
'Coefficients',getMatchedFilter(waveform));
y = filter(x);
subplot (2,1,1), plot(real(x))
xlabel('Samples')
ylabel('Amplitude')
title('Input Signal')
subplot ( $2,1,2$ ), plot (real(y))
xlabel('Samples')
ylabel('Amplitude')
title('Matched Filter Output')


## Matched Filter Using Hamming Window

Apply a matched filter, using a Hamming window to do spectrum weighting.

```
waveform = phased.LinearFMWaveform('PulseWidth',1e-4,'PRF',5e3);
x = waveform();
filter = phased.MatchedFilter( ...
    'Coefficients',getMatchedFilter(waveform), ...
    'SpectrumWindow','Hamming');
y = filter(x);
subplot(2,1,1)
```

```
plot(real(x))
xlabel('Samples')
ylabel('Amplitude')
title('Input Signal')
subplot(2,1,2)
plot(real(y))
xlabel('Samples')
ylabel('Amplitude')
title('Matched Filter Output')
```



## Matched Filter with Custom Window

Apply a matched filter, using a custom Gaussian window for spectrum weighting.

```
waveform = phased.LinearFMWaveform('PulseWidth',1e-4,'PRF',5e3);
x = waveform();
filter = phased.MatchedFilter( ...
    'Coefficients',getMatchedFilter(waveform), ...
    'SpectrumWindow','Custom', ...
    'CustomSpectrumWindow',{@gausswin,2.5});
y = filter(x);
subplot(2,1,1)
plot(real(x))
xlabel('Samples')
ylabel('Amplitude')
```

```
title('Input Signal')
subplot(2,1,2)
plot(real(y))
xlabel('Samples')
ylabel('Amplitude')
title('Matched Filter Output')
```



## Algorithms

The filtering operation uses the overlap-add method.
Spectrum weighting produces a transfer function

$$
H^{\prime}(F)=w(F) H(F)
$$

where $w(F)$ is the window and $H(F)$ is the original transfer function.
For further details on matched filter theory, see [1]or [2].

## Version History

Introduced in R2011a

## References

[1] Richards, M. A. Fundamentals of Radar Signal Processing. New York: McGraw-Hill, 2005.
[2] Skolnik, M. Introduction to Radar Systems, 3rd Ed. New York: McGraw-Hill, 2001.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.
Usage notes and limitations:

- The CustomSpectrumWindow property is not supported.
- See "System Objects in MATLAB Code Generation" (MATLAB Coder).


## See Also

phased.CFARDetector|pulsint | phased.StretchProcessor | phased.TimeVaryingGain | taylorwin

## step

System object: phased.MatchedFilter
Package: phased
Perform matched filtering

## Syntax

$Y=\operatorname{step}(H, X)$
Y = step (H, X, COEFF)
[Y,GAIN] = step( $\qquad$ )

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step $(o b j, x)$ and $y=o b j(x)$ perform equivalent operations.
$\mathrm{Y}=\operatorname{step}(\mathrm{H}, \mathrm{X})$ applies the matched filtering to the input X and returns the filtered result in Y . The filter is applied along the first dimension. Y and X have the same dimensions. The initial transient is removed from the filtered result.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
$Y=\operatorname{step}(H, X, C O E F F)$ uses the input COEFF as the matched filter coefficients. This syntax is available when you set the CoefficientsSource property to 'Input port'.
[Y, GAIN] = step (__ ) returns additional output GAIN as the gain (in decibels) of the matched filter. This syntax is available when you set the GainOutputPort property to true.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Examples

## Match Filter Linear FM Waveform

Construct a linear FM waveform with a sweep bandwidth of 300 kHz and a pulse width of $50 \mu \mathrm{~s}$. Obtain the matched filter coefficients using the getMatchedFilter method. Then, use the step to match-filter the waveform.

```
waveform = phased.LinearFMWaveform('SweepBandwidth',3e5,...
    'OutputFormat','Pulses','SampleRate',1e6,...
    'PulseWidth',50e-6,'PRF',1e4);
wav = waveform();
```

Plot the entire waveform. The length of the waveform is the pulse repetition interval ( 100 samples).
stem(real(wav))
xlabel('Samples')
title('Real Part of Waveform')


Obtain the matched filter coefficients for the linear FM waveform. The length of the matched filter coefficients is the length of the pulse.

```
mfcoeffs = getMatchedFilter(waveform);
stem(real(mfcoeffs))
xlabel('Samples')
title('Real Part of Matched Filter Coefficients')
```



Use phased. MatchedFilter step method to obtain the matched filter output.

```
filter = phased.MatchedFilter('Coefficients',mfcoeffs);
mfoutput = filter(wav);
stem(real(mfoutput))
xlabel('Samples')
title('Real Part of Matched Filter Output')
```



# phased.MonopulseEstimator 

Package: phased
Amplitude monopulse direction finding

## Description

The phased.MonopulseEstimator System object implements a target direction estimator using the amplitude monopulse technique with arbitrary array geometry. The object works with the sum and difference channels that are output from the phased.MonopulseFeed System object or your own sum-difference channel generator. The output is an estimate of the target direction in azimuth and elevation. You can use the object for target direction estimation and target tracking.

To create a monopulse estimator:
1 Create the phased.MonopulseEstimator object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

estimator $=$ phased.MonopulseEstimator estimator $=$ phased.MonopulseEstimator(Name,Value)

## Description

estimator = phased.MonopulseEstimator creates a monopulse estimator System object, estimator, with default property values.
estimator = phased.MonopulseEstimator(Name,Value) creates an estimator with each property Name set to a specified Value. You can specify additional name-value pair arguments in any order as (Namel,Value1,...,NameN,ValueN). Enclose each property name in single quotes.
Example: estimator = phased.MonopulseEstimator('SensorArray', phased.URA, 'OperatingFrequency', 300e6 ,' Coverage', 'Azimuth') sets the sensor array to a uniform rectangular array (URA) with default URA property values. The estimator estimates azimuth from the sum channel and azimuth difference channel. The estimator operates at 300 MHz .

Note You can also create a phased.MonopulseEstimator object from a phased.MonopulseFeed object using the getMonopulseEstimator object function.

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

SensorArray - Sensor array
phased. ULA array with default property values (default) | Phased Array System Toolbox array
Sensor array, specified as an array System object belonging to Phased Array System Toolbox. The sensor array can contain subarrays.
Example: phased.URA

## PropagationSpeed - Signal propagation speed

physconst('LightSpeed') (default) | positive scalar
Signal propagation speed, specified as a positive scalar. Units are in meters per second. The default propagation speed is the value returned by physconst('LightSpeed'). See physconst for more information.

## Example: 3e8

Data Types: double

## OperatingFrequency - Operating frequency <br> 300e6 (default) | positive scalar

Operating frequency, specified as a positive scalar. Units are in Hz.
Example: 1e9
Data Types: double

## Coverage - Monopulse coverage

'3D' (default) | 'Azimuth'
Coverage of monopulse estimator, specified as '3D' or 'Azimuth'. When you set this property to '3D' , the monopulse estimator uses the sum channel and both azimuth and elevation difference channels. When you set this property to 'Azimuth', the estimator uses the sum channel and the azimuth difference channel.

## SquintAngle - Squint angle

10 (default) | scalar | real-valued 2-by-1 vector
Squint angle, specified as a scalar or real-valued 2-by-1 vector. The squint angle is the separation angle or angles between the sum beam and the beams along the azimuth and elevation directions.

- When you set the Coverage property to 'Azimuth ', set the SquintAngle property to a scalar.
- When you set the Coverage property to '3D', you can specify the squint angle as either a scalar or vector. If you set the SquintAngle property to a scalar, then the squint angle is the same along both the azimuth and elevation directions. If you set the SquintAngle property to a 2-by-1 vector, its elements specify the squint angle along the azimuth and elevation directions.

Example: [20;5]

## OutputFormat - Output direction format

'Angle' (default)|'Angle offset'
Format of direction output, specified as 'Angle' or 'Angle offset'. When you set this property to 'Angle', the output angles are in the direction of the target. When you set this property to 'Angle offset ', the output is the angle offset from the array steering direction.

## SumDifferenceRatioOutputPort - Enable sum-difference ratio output <br> false (default)| true

Set this property to true to output the ratio of the sum and difference channels in the azimuth and elevation directions. Set this property to false to not output the ratios. The ratio is often used as an error control signal.

Data Types: logical

## Usage

## Syntax

```
angest = estimator(sumchan,diffazchan,steervec)
angest = estimator(sumchan,diffazchan,diffelchan,steervec)
[angest,dratio] = estimator(
```

$\qquad$

``` )
Description
```

angest $=$ estimator(sumchan,diffazchan,steervec) returns the estimated target angle, angest, derived from the sum channel signal, sumchan, and the azimuth difference channel signal, diffazchan. steervec specifies the array steering direction. To use this syntax, set the Coverage property to 'Azimuth'.
angest $=$ estimator(sumchan,diffazchan, diffelchan,steervec) also specifies the elevation difference channel signal, diffelchan. To use this syntax, set the Coverage property to '3D'.
[angest,dratio] = estimator( __ ) also returns the sum and difference ratio, dratio. To use this syntax, set the SumDifferenceRatioOutputPort property to true.

You can combine optional input arguments when their enabling properties are set. Optional inputs must be listed in the same order as the order of the enabling properties. For example:

```
[angest,dratio] = estimator(X,steervec)
```


## Input Arguments

## sumchan - Sum-channel signal

complex-valued $N$-by- 1 column vector
Sum-channel signal, specified as a complex-valued $N$-by-1 column vector. $N$ is the number of snapshots in the signal.

## diffazchan - Azimuth difference-channel signal <br> complex-valued $N$-by-1 column vector

Azimuth difference-channel signal, specified as a complex-valued $N$-by- 1 column vector. $N$ is the number of snapshots in the signal.

Data Types: double
Complex Number Support: Yes

## diffelchan - Elevation difference-channel signal

complex-valued $N$-by- 1 column vector
Elevation difference-channel signal, specified as a complex-valued $N$-by-1 column vector. $N$ is the number of snapshots in the signal.

## Dependencies

To enable this output argument, set the Coverage property to '3D '.

## Data Types: double <br> Complex Number Support: Yes

## steervec - Array steering direction

scalar | real-valued 2-by-1 column vector
Array steering direction, specified as a scalar or real-valued 2-by-1 column vector.

- When you set the Coverage property to 'Azimuth ', the steering direction is a scalar and represents the azimuth steering angle.
- When you set the Coverage property to '3D', the steering vector has the form [azimuthAngle; elevationAngle], where azimuthAngle is the azimuth steering angle and elevationAngle is the elevation steering angle.

Units are in degrees. Azimuth angles lie between $-180^{\circ}$ and $180^{\circ}$, inclusive and elevation angles must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive.
Example: [40;10]
Data Types: double

## Output Arguments

## angest - Estimated direction of target

real-valued 1 -by- $N$ vector | real-valued 2-by- $N$ matrix
Estimated direction of target, returned as a real-valued 1-by- $N$ vector or real-valued 2-by- $N$ matrix. $N$ is the number of snapshots in the signal. Units are in degrees.

- When you set the Coverage property to 'Azimuth ', angest is a real-valued 1 -by- $N$ vector. The elements contain the estimated target direction azimuth angle at each signal snapshot.
- When you set the Coverage property to ' 3 D ', angest is a real-valued 2 -by- $N$ matrix. Each column contains the estimated target direction in the form [azimuthAngle; elevationAngle], where azimuthAngle is the estimated azimuth angle, and elevationAngle is the estimated elevation angle.

If you set the OutputFormat property to 'Angle offset ', each element of the vector or matrix represent an offset from the steering vector direction.

## Data Types: double

## dratio - Ratio of sum and difference channels

real-valued 1-by- $N$ vector | real-valued 2-by- $N$ matrix
Ratio of sum and difference channels, returned as a real-valued 1 -by- $N$ vector or real-valued 2-by- $N$ matrix. $N$ is the number of snapshots in the signal. Units are in degrees.

- When you set the Coverage property to 'Azimuth ', dratio is a real-valued 1 -by- $N$ vector. The elements contain the ratio of the sum to azimuth difference channel at each signal snapshot.
- When you set the Coverage property to ' $3 D^{\prime}$ ', dratio is a real-valued 2 -by- $N$ matrix. The elements of the first row contain the ratio of the sum to azimuth difference channel at each signal snapshot. The elements of the second row contain the ratio of the sum to elevation difference channel at each signal snapshot.


## Dependencies

To enable this output argument, set the SumDifferenceRatioOutputPort property to true.
Data Types: double

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```


## Common to All System Objects

step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object

## Examples

## Create Sum and Difference Channels for URA

After creating sum and difference channels, determine the direction of a target at approximately 24 degrees azimuth and 40 degrees elevation with respect to a 5 -by- 5 uniform rectangular array.

Create a monopulse feed system based on a URA.

```
fc = 200e6;
c = physconst('LightSpeed');
lambda = c/fc;
array = phased.URA('Size',[5 5],'ElementSpacing',lambda/2);
feed = phased.MonopulseFeed('SensorArray',array,'OperatingFrequency', ...
    fc,'Coverage','3D','AngleOutputPort',true);
```

Create a signal using a steering vector.

```
steervector = phased.SteeringVector('SensorArray',array);
```

x = steervector(feed.OperatingFrequency,[24;40]).';

Obtain the sum and difference channels and the estimated target angle.

```
[sumch,azch,elch,est_dir] = feed(x,[30;35]);
disp(est_dir)
    24.3705
    41.1997
```

Use a derived phased. MonopulseEstimator object to also obtain the target angle.

```
estimator = getMonopulseEstimator(feed);
est_dir = estimator(sumch,azch,elch,[30;35])
est_dir = 2×1
    24.3705
    41.1997
```


## Find Direction of Target

Determine the direction of a target using monopulse processing of signals arriving on a URA. The target echo is first detected before applying monopulse processing.

```
array = phased.URA('Size',4);
collect = phased.Collector('Sensor',array);
feed = phased.MonopulseFeed('SensorArray',array,'Coverage','3D');
estimator = phased.MonopulseEstimator('SensorArray',array,'Coverage','3D');
% Create a 100-sample random source signal with a single spike to simulate
% an echo.
x = sqrt(0.01/2)*(randn(100,1)+1i*randn(100,1));
x(20) = 1;
targetangle = [31;9];
rx = collect(x,targetangle);
```

Point the monopulse in a different direction from the target. Then, create the sum and difference angles.

```
steerangle = [30;10];
[sumch,azch,elch] = feed(rx,steerangle);
% Detect the target by finding the peak of the sum channel.
[~,idx] = max(abs(sumch));
% Estimate the arrival angle using a monopulse estimator.
est_dir = estimator(sumch(idx),azch(idx),elch(idx),steerangle)
est_dir = 2×1
    31.1307
        9.0132
```


## Version History

Introduced in R2018b

## References

[1] Mahafza, B.R. Radar System Analysis and Design Using Matlab. Boca Raton: Chapman and Hall/ CRC, 2000.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:

- See "System Objects in MATLAB Code Generation" (MATLAB Coder).


## See Also

## Objects

phased.SumDifferenceMonopulseTracker|phased.SumDifferenceMonopulseTracker2D | phased.MonopulseFeed

Functions
getMonopulseEstimator

## phased.MonopulseFeed

Package: phased
Creates sum and difference channels

## Description

The phased.MonopulseFeed System object implements a monopulse feed system for the amplitude sum and difference monopulse tracker. This object combines received signals from an arbitrary array to form sum and difference channels. You can use this object as a feed for the phased.MonopulseEstimator System object.

To create a monopulse feed system:
1 Create the phased.MonopulseFeed object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

```
feed = phased.MonopulseFeed
feed = phased.MonopulseFeed(Name,Value)
```


## Description

feed = phased.MonopulseFeed creates a monopulse feed System object, feed, with default property values.
feed $=$ phased.MonopulseFeed(Name, Value) creates a feed system with each property Name set to a specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN). Enclose each property name in single quotes.

## Example: feed =

 phased.MonopulseFeed('SensorArray', phased.URA,'OperatingFrequency', 300e6, 'Cov erage', 'Azimuth') sets the sensor array to a uniform rectangular array (URA) with default URA property values. The feed forms only the sum channel and azimuth difference channel. The feed system operates at 300 MHz .
## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.

For more information on changing property values, see System Design in MATLAB Using System Objects.

## SensorArray - Sensor array

phased. ULA array with default property values (default) | Phased Array System Toolbox array
Sensor array, specified as an array System object belonging to Phased Array System Toolbox. The sensor array can contain subarrays.
Example: phased.URA
PropagationSpeed - Signal propagation speed
physconst('LightSpeed') (default) | positive scalar
Signal propagation speed, specified as a positive scalar. Units are in meters per second. The default propagation speed is the value returned by physconst('LightSpeed'). See physconst for more information.

Example: 3e8
Data Types: double
OperatingFrequency - Operating frequency
300e6 (default) | positive scalar
Operating frequency, specified as a positive scalar. Units are in Hz.
Example: 1e9
Data Types: double

## Coverage - Monopulse coverage

'3D' (default)| 'Azimuth'
Coverage directions of monopulse feed, specified as '3D' or 'Azimuth '. When you set this property to '3D' , the monopulse feed forms the sum channel and both azimuth and elevation difference channels. When you set this property to 'Azimuth' , the monopulse feed forms the sum channel and the azimuth difference channel.

## Example: 'Azimuth'

## SquintAngle - Squint angle

10 (default) | scalar | real-valued 2-by-1 vector
Squint angle, specified as a scalar or real-valued 2-by-1 vector. The squint angle is the separation angle or angles between the sum beam and the beams along the azimuth and elevation directions.

- When you set the Coverage property to 'Azimuth ' , set the SquintAngle property to a scalar.
- When you set the Coverage property to '3D', you can specify the squint angle as either a scalar or vector. If you set the SquintAngle property to a scalar, then the squint angle is the same along both the azimuth and elevation directions. If you set the SquintAngle property to a 2-by-1 vector, its elements specify the squint angle along the azimuth and elevation directions.


## Example: [20;5]

## AngleOutputPort - Enable angle estimate output <br> false (default) | true

Enable angle estimate output, specified as false or true. Set this property to true to output the angle estimate in addition to sum and difference channels. Set this property to false to only output sum and difference channels.

## Data Types: logical

## Usage

## Syntax

[sumchan,diffazchan] = feed(X,steervec)
[sumchan,diffazchan,diffelchan] = feed(X,steervec)
[ __ , angest] = feed (X,steervec)

## Description

[sumchan,diffazchan] $=$ feed(X,steervec) returns the sum channel signal, sumchan, and the azimuth difference channel signal, diffazchan, computed from the input signal, $X$. steervec specifies the array steering direction. To use this syntax, set the Coverage property to 'Azimuth '.
[sumchan, diffazchan, diffelchan] = feed(X,steervec) also returns the elevation difference channel signal, diffelchan. To use this syntax, set the Coverage property to '3D'.
$\qquad$ , angest] $=$ feed ( X, steervec) also returns the estimated direction angle, angest. To use this syntax, set the Angle0utputPort property to true.

## Input Arguments

## X - Input signal <br> complex-valued M-by-N matrix | -by- $N$ matrix

Input signal, specified as a complex-valued $M$-by- $N$ matrix, where $M$ is the number of samples or snapshots of data, and $N$ is the number of array elements. If the array contains subarrays, then $N$ is the number of subarrays.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

Data Types: double

## steervec - Array steering direction

scalar | real-valued 2-by-1 column vector
Array steering direction, specified as a scalar or real-valued 2-by-1 column vector.

- When you set the Coverage property to 'Azimuth', the steering direction is a scalar and represents the azimuth steering angle.
- When you set the Coverage property to ' $3 D^{\prime}$ ', the steering vector has the form [azimuthAngle; elevationAngle], where azimuthAngle is the azimuth steering angle and elevationAngle is the elevation steering angle.

Units are in degrees. Azimuth angles lie between $-180^{\circ}$ and $180^{\circ}$, inclusive and elevation angles must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive.

## Example: [40;10]

## Data Types: double

You can combine optional input arguments when their enabling properties are set. Optional inputs must be listed in the same order as the order of the enabling properties. For example,

```
array = phased.URA('Size',[5 5]);
feed = phased.MonopulseFeed('SensorArray',array,'Coverage','3D', ...
    'AngleOutputPort',true);
[sumch,dazch,delch,angest] = feed(X,steervec);
```


## Output Arguments

## sumchan - Sum-channel signal

complex-valued $M$-by- 1 column vector
Sum-channel signal, returned as a complex-valued $M$-by- 1 column vector, where $M$ is the number of rows of $X$.

Data Types: double
Complex Number Support: Yes

## diffazchan - Azimuth difference-channel signal

complex-valued M-by-1 column vector
Azimuth difference-channel signal, returned as a complex-valued $M$-by- 1 column vector, where $M$ is the number of rows of $X$.

Data Types: double
Complex Number Support: Yes

## diffelchan - Elevation difference-channel signal

complex-valued $M$-by-1 column vector
Elevation difference-channel signal, returned as a complex-valued $M$-by- 1 column vector, where $M$ is the number of rows of $X$.

## Dependencies

To enable this output argument, set the Coverage property to '3D ' .

## Data Types: double <br> Complex Number Support: Yes

## angest - Estimated direction of target

real-valued 2-by-1 vector
Estimated direction of target, returned as a real-valued 2-by-1 vector in the form [azimuth, elevation]. Units are in degrees.

## Dependencies

To enable this output argument, set the AngleOutputPort property to true.
Data Types: double

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```


## Specific to phased. MonopulseFeed

getMonopulseEstimator Create monopulse estimator from monopulse feed

## Common to All System Objects

step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object

## Examples

## Create Sum and Difference Channels for URA

After creating sum and difference channels, determine the direction of a target at approximately 24 degrees azimuth and 40 degrees elevation with respect to a 5 -by- 5 uniform rectangular array.

Create a monopulse feed system based on a URA.

```
fc = 200e6;
c = physconst('LightSpeed');
lambda = c/fc;
array = phased.URA('Size',[5 5],'ElementSpacing',lambda/2);
feed = phased.MonopulseFeed('SensorArray',array,'OperatingFrequency', ...
    fc,'Coverage','3D','AngleOutputPort',true);
```

Create a signal using a steering vector.
steervector = phased.SteeringVector('SensorArray',array);
$x=$ steervector(feed.OperatingFrequency, [24;40]).';

Obtain the sum and difference channels and the estimated target angle.

```
[sumch,azch,elch,est_dir] = feed(x,[30;35]);
disp(est_dir)
```

    24.3705
    41.1997
    Use a derived phased. MonopulseEstimator object to also obtain the target angle.

```
estimator = getMonopulseEstimator(feed);
est_dir = estimator(sumch,azch,elch,[30;35])
est_dir = 2×1
```

    24.3705
    
## Version History

Introduced in R2018b

## References

[1] Mahafza, B.R. Radar System Analysis and Design Using Matlab. Boca Raton: Chapman and Hall/ CRC, 2000.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\text {rm }}$.
Usage notes and limitations:

- See "System Objects in MATLAB Code Generation" (MATLAB Coder).


## See Also

## Objects

phased.SumDifferenceMonopulseTracker | phased.SumDifferenceMonopulseTracker2D | phased.MonopulseEstimator

# getMonopulseEstimator 

Package: phased

Create monopulse estimator from monopulse feed

## Syntax

```
estimator = getMonopulseEstimator(feed)
```


## Description

estimator = getMonopulseEstimator(feed) creates a phased.MonopulseEstimator System object, estimator, from a phased.MonopulseFeed System object, feed.

## Examples

## Create Sum and Difference Channels for URA

After creating sum and difference channels, determine the direction of a target at approximately 24 degrees azimuth and 40 degrees elevation with respect to a 5 -by- 5 uniform rectangular array.

Create a monopulse feed system based on a URA.

```
fc = 200e6;
c = physconst('LightSpeed');
lambda = c/fc;
array = phased.URA('Size',[5 5],'ElementSpacing',lambda/2);
feed = phased.MonopulseFeed('SensorArray',array,'OperatingFrequency', ...
    fc,'Coverage','3D','Angle0utputPort',true);
```

Create a signal using a steering vector.

```
steervector = phased.SteeringVector('SensorArray',array);
x = steervector(feed.OperatingFrequency,[24;40]).';
```

Obtain the sum and difference channels and the estimated target angle.

```
[sumch,azch,elch,est_dir] = feed(x,[30;35]);
disp(est_dir)
```

    24.3705
    41.1997
    Use a derived phased.MonopulseEstimator object to also obtain the target angle.

```
estimator = getMonopulseEstimator(feed);
est_dir = estimator(sumch,azch,elch,[30;35])
est_dir = 2×1
```

    24.3705
    
## Input Arguments

feed - Monopulse feed<br>phased. MonopulseFeed System object

Monopulse feed, specified as a System object.

## Output Arguments

estimator - Monopulse estimator
phased.MonopulseEstimator System object
Monopulse estimator, returned as a phased. MonopulseEstimator System object.

## Version History

Introduced in R2018b

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.

# phased.MFSKWaveform 

Package: phased
MFSK waveform

## Description

The multiple frequency shift keying (MFSK) waveform is used in automotive radar to improve simultaneous range and Doppler estimation of multiple targets. The MFSKWaveform System object creates the baseband representation of an MFSK waveform. An MFSK waveform consists of two interleaved sequences of increasing frequencies, as described in "Algorithms" on page 1-981.

To obtain waveform samples:
1 Define and set up the MFSK waveform. See "Construction" on page 1-978.
2 Call step to generate the MFSK waveform samples according to the properties of phased.MFSKWaveform. The behavior of step is specific to each object in the toolbox. The output of the step method is controlled by the OutputFormat property, which has no effect on the properties of the waveform.

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, $y=$ step $(\mathrm{obj}, \mathrm{x})$ and $\mathrm{y}=\mathrm{obj}(\mathrm{x})$ perform equivalent operations. When the only argument to the step method is the System object itself, replace $y=\operatorname{step}(o b j)$ by $y=o b j()$.

## Construction

sMFSK = phased.MFSKWaveform creates an MFSK waveform System object, sMFSK.
sMFSK = phased.MFSKWaveform(Name,Value) creates an MFSK waveform object, sMFSK, with additional properties specified by one or more Name-Value pair arguments. Name must appear inside single quotes (' ' ). You can specify several name-value pair arguments in any order as Name1, Value1, ..., NameN, ValueN.

## Properties

## SampleRate - Sample rate

1e6 (default) | positive scalar
Sample rate of the signal, specified as a positive scalar. Units are hertz.
Example: 96e6
Data Types: double

## SweepBandwidth - MFSK sweep bandwidth

1e5 (default) | positive scalar
MFSK sweep bandwidth, specified as a positive scalar. Units are in hertz. The sweep bandwidth is the difference between the highest and lowest frequencies of either sequence.

Example: 9e7
Data Types: double

## StepTime - Duration of frequency step

1e-4 (default) | positive scalar
Time duration of each frequency step, specified as a positive scalar in seconds.
Example: 0.2e-3
Data Types: double

## StepsPerSweep - Total number of frequency steps

64 (default) | even positive integer
Total number of frequency steps in a sweep, specified as an even positive integer.
Example: 16
Data Types: double
FrequencyOffset - Chirp offset frequency
1000 (default) | real scalar
Chirp offset frequency, specified as a real scalar. Units are in hertz. The offset determines the frequency translation between the two sequences.

## Example: 500

Data Types: double

## OutputFormat - Output signal grouping <br> 'Steps' (default)|'Sweeps'|'Samples'

Output signal grouping, specified as one of 'Steps', 'Sweeps ', or 'Samples'. This property has no effect on the waveform but determines the output form of the step method.

- 'Steps' - The output consists of all samples contained in an integer number of frequency steps, NumSteps.
- 'Samples ' - The output consists of an integer number of samples, NumSamples.
- 'Sweeps ' - The output consists of all samples contained in an integer number of sweeps, NumSweeps.

Example: 'Samples'
Data Types: char

## NumSamples - Number of samples in output

1 (default) | positive integer
Number of samples in output, specified as a positive integer. This property applies only when you set OutputFormat to 'Samples'.
Example: 200
Data Types: double

## NumSteps - Number of frequency steps in output

1 (default) | positive integer
Number of frequency steps in output, specified as a positive integer. This property applies only when you set OutputFormat to 'Steps'.
Example: 10
Data Types: double

## NumSweeps - Number of sweeps in output

1 (default) | positive integer
Number of sweeps in output, specified as a positive integer. This property applies only when you set OutputFormat to 'Sweeps'.

Example: 5
Data Types: double

## Methods

| plot | Plot continuous MFSK waveform |
| :--- | :--- |
| reset | Reset states of the MFSK waveform object |

## Common to All System Objects

release $\quad$ Allow System object property value changes

## Examples

## Plot MFSK Waveform

Construct an MFSK waveform with a sample rate of 1 MHz and a sweep bandwidth of 0.1 MHz . Assume 52 steps with a step time of 4 milliseconds. Set the frequency offset to 1 kHz . There are 4000 samples per step.

```
fs = 1e6;
fsweep = 1e5;
tstep = 4e-3;
numsteps = 52;
foffset = 1000;
noutputsteps = 4;
sMFSK = phased.MFSKWaveform('SampleRate',fs,...
    'SweepBandwidth',fsweep,...
    'StepTime',tstep,...
    'StepsPerSweep',numsteps,...
    'Frequency0ffset',foffset,...
    'OutputFormat','Steps',...
    'NumSteps',noutputsteps);
```

Plot the real and imaginary components of the second step of the waveform using the plot method. Set the plot color to red.

```
plot(sMFSK,'PlotType','complex','StepIdx',2,'r')
```



MFSK waveform: imaginary part, step 2


## Algorithms

An MFSK waveform consists of two interleaved stepped-frequency sequences, as shown in this timefrequency diagram.


Each sequence is a set of continuous waveform (CW) signals increasing in frequency. The offset, $F_{\text {offset }}$, between the two sequences is constant and can be positive or negative. A complete waveform consists of an even number of steps, $N$, of equal duration, $T_{\text {step }}$. Then, each sequence consists of $N / 2$ steps. The sweep frequency, $F_{\text {sweep, }}$, is the difference between the lowest and highest frequency of either sequence. $F_{\text {sweep }}$ is always positive, indicating increasing frequency. The frequency difference between successive steps of each sequence is given by
$F_{\text {step }}=F_{\text {sweep }} /(N / 2-1)$.
The lowest frequency of the first sequence is always 0 hertz and corresponds to the carrier frequency of the bandpass signal. The lowest frequency of the second sequence can be positive or negative and is equal to $F_{\text {offset }}$. Negative frequencies correspond to bandpass frequencies that are lower than the carrier frequency. The duration of the waveform is given by $T_{\text {sweep }}=N * T_{\text {step }}$. The System object properties corresponding to the signal parameters are

| Signal Parameter | Property |
| :--- | :--- |
| $F_{\text {sweep }}$ | 'SweepBandwidth' |
| $T_{\text {step }}$ | 'StepTime' |
| $N$ | 'StepsPerSweep ' |
| $F_{\text {offset }}$ | 'FrequencyOffset ' |

## References

[1] Meinecke, Marc-Michale, and Hermann Rohling, "Combination of LFMCW and FSK Modulation Principles for Automotive Radar Systems." German Radar Symposium GRS2000. 2000.
[2] Rohling, Hermann, and Marc-Michale Meinecke. "Waveform Design Principles for Automotive Radar Systems". CIE International Conference on Radar. 2001.

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:

- plot method is not supported.
- See "System Objects in MATLAB Code Generation" (MATLAB Coder).


## See Also

phased.LinearFMWaveform | phased.PhaseCodedWaveform | phased.RectangularWaveform | phased.SteppedFMWaveform | phased.FMCWWaveform | phased.MatchedFilter

Topics
"Simultaneous Range and Speed Estimation Using MFSK Waveform"

## plot

System object: phased.MFSKWaveform
Package: phased
Plot continuous MFSK waveform

## Syntax

```
plot(sMFSK)
plot(sMFSK,Name,Value)
plot(sMFSK,Name,Value,LineSpec)
h = plot(
```

$\qquad$

``` )
```


## Description

plot (sMFSK) plots the real part of the waveform specified by sMFSK.
plot (sMFSK, Name, Value) plots the waveform with additional options specified by one or more Name, Value pair arguments.
plot (sMFSK,Name,Value,LineSpec) specifies the same line color, line style, or marker options that are available in the MATLAB plot function.
$\mathrm{h}=\mathrm{plot}(\ldots \quad)$ returns the line handle in the figure.

## Input Arguments

## sMFSK - MFSK waveform

MFSK waveform System object
MFSK waveform, specified as a phased.MFSKWaveform System object.
Example: sMFSK = phased.MFSKWaveform;

## LineSpec - Plot style

' b' (default) | character vector
Plot style, specified as a character vector. You can specify the same line color, style, or marker options that are available in the MATLAB plot function. If you specify a PlotType value of ' complex', then LineSpec applies to both the real and imaginary subplots.
Example: 'k.'

## Name-Value Pair Arguments

Specify optional pairs of arguments as Namel=Value1, ... ,NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## PlotType - Waveform component to plot

'real' (default)|'imag' | 'complex'
Waveform component to plot, specified as the comma-separated pair consisting of 'PlotType' and one of the following:

- 'real ' - Plots the real part of the waveform
- 'imag' - Plots the imaginary part of the waveform
- ' complex' - Plots both parts of the waveform

Example: 'PlotType','complex'

## StepIdx - Index of step

1 (default) | positive integer
Index of the step to plot, specified as the comma-separated pair consisting of 'StepIdx' and a positive integer. If you specify a 'StepIdx' value greater than 'StepsPerSweep', the frequency corresponds to the mod('StepIdx','StepsPerSweep') value.

## Output Arguments

## h - Plot handle

double
Plot handle(s) to the line or lines in the figure, returned as a double. When PlotType is set to ' complex', h is a 2-by-1 column vector. The first and second elements of this vector are the handles to the lines in the real and imaginary subplots, respectively.

## Examples

## Plot MFSK Waveform

Construct an MFSK waveform with a sample rate of 1 MHz and a sweep bandwidth of 0.1 MHz . Assume 52 steps with a step time of 4 milliseconds. Set the frequency offset to 1 kHz . There are 4000 samples per step.

```
fs = 1e6;
fsweep = 1e5;
tstep = 4e-3;
numsteps = 52;
foffset = 1000;
noutputsteps = 4;
sMFSK = phased.MFSKWaveform('SampleRate',fs,...
    'SweepBandwidth',fsweep,...
    'StepTime',tstep,...
    'StepsPerSweep',numsteps,...
    'Frequency0ffset',foffset,...
    'OutputFormat','Steps',...
    'NumSteps',noutputsteps);
```

Plot the real and imaginary components of the second step of the waveform using the plot method. Set the plot color to red.

```
plot(sMFSK,'PlotType','complex','StepIdx',2,'r')
```



MFSK waveform: imaginary part, step 2

Version History
Introduced in R2015a

## reset

System object: phased.MFSKWaveform
Package: phased
Reset states of the MFSK waveform object

## Syntax

reset(sMFSK)

## Description

reset (sMFSK) resets the internal states of the phased.MFSKWaveform object, sMFSK, to their initial values.

## Input Arguments

sMFSK - MFSK waveform
System object
MFSK waveform, specified as a phased.MFSKWaveform System object.
Example: sMFSK= phased.MFSKWaveform;

## Version History

Introduced in R2015a

## step

System object: phased.MFSKWaveform
Package: phased
Samples of continuous MFSK waveform

## Syntax

Y = step(sMFSK)

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step $(o b j, x)$ and $y=o b j(x)$ perform equivalent operations. When the only argument to the step method is the System object itself, replace $y=\operatorname{step}(o b j)$ by $y=o b j()$.
$Y=$ step(sMFSK) returns samples of the MFSK waveform in a $N$-by-1 complex valued column vector, Y .

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## sMFSK - MFSK waveform

System object
MFSK waveform, specified as a phased.MFSKWaveform System object.
Example: sMFSK= phased.MFSKWaveform;

## Output Arguments

## Y - Output samples

$N$-by-1 complex valued vector
Output samples of MFSK waveform, returned as an $N$-by- 1 complex valued vector. When the step method reaches the end of the waveform, the output samples wrap around from the start of the waveform, yielding a periodic waveform.

## Examples

## Construct MFSK Step Output

Construct an MFSK waveform with a sample rate of 1 MHz and a sweep bandwidth of 0.1 MHz .
Assume 52 steps, with a step time of 4 milliseconds. Set the frequency offset to 1 kHz . There are 4000 samples per step.

```
fs = 1e6;
fsweep = le5;
tstep = 40e-4;
numsteps = 52;
foffset = 1000;
noutputsteps = 4;
sMFSK = phased.MFSKWaveform('SampleRate',fs,...
    'SweepBandwidth',fsweep,...
    'StepTime',tstep,...
    'StepsPerSweep',numsteps,...
    'Frequency0ffset',foffset,...
    'OutputFormat','Steps',...
    'NumSteps',noutputsteps);
```

Call the step method to retrieve the samples for the four steps.

```
z = step(sMFSK);
```

Plot the real and imaginary parts of the first two steps.

```
samplesperstep = fs*tstep;
disp(samplesperstep)
    4 0 0 0
idx = [1:2*samplesperstep]';
time = idx/fs*1000;
plot(time,real(z(idx)),'b',time,imag(z(idx)),'k');
xlabel('Time (millisec)')
```



Compute the FFT of all the data.
n = size(z,1);
nfft = 2^ceil(log2(n));
$Y=f f t s h i f t(f f t(z, n f f t)) ;$
Plot the magnitudes of the spectrum.

```
fmax = fs/2;
ft = [-nfft/2:nfft/2-1]*fmax/(nfft/2);
figure(2);
hp = plot(ft/1000,abs(Y));
axis([-2,8,-1,4000]);
xlabel('Frequency (kHz)')
grid
```



The plot shows two pairs of peaks. The first pair lies at 0 Hz and 1000 Hz . The second pair lies at 4000 Hz and 5000 Hz . The frequency offset is 1000 Hz .

Compute the frequency increase to the second pair off peaks.
fdelta $=$ fsweep $/($ numsteps/2-1);
disp(fdelta)
4000
The increase agrees with the location of the second pair of peaks in the FFT spectrum.

## MFSK Samples per Sweep

Construct an MFSK waveform with a sample rate of 1 MHz and a sweep bandwidth of 0.1 MHz . Assume 52 steps with a step time of 400 microseconds. Set the frequency offset to 1 kHz . Find the number of samples returned when the OutputFormat property is set to return the samples for one sweep.

```
fs = 1e6;
fsweep = 1e5;
tstep = 40e-4;
numsteps = 52;
foffset = 1000;
noutputsweeps = 1;
```

```
sMFSK = phased.MFSKWaveform('SampleRate',fs,...
    'SweepBandwidth',fsweep,...
    'StepTime',tstep,...
    'StepsPerSweep',numsteps,...
    'Frequency0ffset',foffset,...
    'OutputFormat','Sweeps',...
    'NumSweeps',noutputsweeps);
```

Call the step method to retrieve the samples for the four steps.
z = step(sMFSK);
Count the number of samples in a sweep.
samplespersweep = fs*tstep*numsteps;
disp(samplespersweep)
208000
Verify that this value agrees with the number of samples returned by the step method.
disp(size(z))
208000
1

## Version History <br> Introduced in R2015a

## phased.MVDRBeamformer

Package: phased

Narrowband minimum-variance distortionless-response beamformer

## Description

The phased.MVDRBeamformer System object implements a narrowband minimum-variance distortionless-response (MVDR) beamformer. The MVDR beamformer is also called the Capon beamformer. An MVDR beamformer belongs to the family of constrained optimization beamformers.

To beamform signals arriving at an array:
1 Create the phased.MVDRBeamformer object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

beamformer $=$ phased.MVDRBeamformer
beamformer $=$ phased.MVDRBeamformer(Name,Value)

## Description

beamformer = phased.MVDRBeamformer creates an MVDR beamformer System object, beamformer, with default property values.
beamformer = phased.MVDRBeamformer(Name, Value) creates an MVDR beamformer with each property Name set to a specified Value. You can specify additional name-value pair arguments in any order as (Namel,Valuel,...,NameN,ValueN). Enclose each property name in single quotes.

Example: beamformer =
phased.MVDRBeamformer('SensorArray',phased.URA,'OperatingFrequency' ,300e6) sets the sensor array to a uniform rectangular array (URA) with default URA property values. The beamformer has an operating frequency of 300 MHz .

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## SensorArray - Sensor array

phased.ULA array with default property values (default) | Phased Array System Toolbox array
Sensor array, specified as an array System object belonging to Phased Array System Toolbox. The sensor array can contain subarrays.

Example: phased.URA

## PropagationSpeed - Signal propagation speed

physconst('LightSpeed') (default)| real-valued positive scalar
Signal propagation speed, specified as a real-valued positive scalar. Units are in meters per second. The default propagation speed is the value returned by physconst ('LightSpeed').
Example: 3e8
Data Types: single | double

## OperatingFrequency - Operating frequency

300e6 (default) | positive scalar
Operating frequency, specified as a positive scalar. Units are in Hz.
Example: 1e9
Data Types: single | double

## DiagonalLoadingFactor - Diagonal loading factor

0 (default) | nonnegative scalar
Diagonal loading factor, specified as a nonnegative scalar. Diagonal loading is a technique used to achieve robust beamforming performance, especially when the sample size is small. A small sample size can lead to an inaccurate estimate of the covariance matrix. Diagonal loading also provides robustness due to steering vector errors. The diagonal loading technique adds a positive scalar multiple of the identity matrix to the sample covariance matrix.

Tunable: Yes
Data Types: single | double

## TrainingInputPort - Enable training data input

false (default) | true
Enable training data input, specified as false or true. When you set this property to true, use the training data input argument, XT , when running the object. Set this property to false to use the input data, X , as the training data.
Data Types: logical

## DirectionSource - Source of beamforming direction <br> 'Property' (default)|'Input port'

Source of beamforming direction, specified as 'Property' or 'Input port'. Specify whether the beamforming direction comes from the Direction property of this object or from the input argument, ANG. Values of this property are:

| 'Property' | Specify the beamforming direction using the Direction <br> property. |
| :--- | :--- |
| 'Input port' | Specify the beamforming direction using the input argument, <br> ANG. |

## Data Types: char

## Direction - Beamforming directions

[0;0] (default) | real-valued 2-by-1 vector | real-valued 2-by-L matrix
Beamforming directions, specified as a real-valued 2-by-1 vector or a real-valued 2-by-L matrix. For a matrix, each column specifies a different beamforming direction. Each column has the form [AzimuthAngle; ElevationAngle]. Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$ and elevation angles must lie between $-90^{\circ}$ and $90^{\circ}$. All angles are defined with respect to the local coordinate system of the array. Units are in degrees.

Example: [40;30]

## Dependencies

To enable this property, set the DirectionSource property to 'Property '.
Data Types: single|double

## NumPhaseShifterBits - Number of phase shifter quantization bits

0 (default) | nonnegative integer
The number of bits used to quantize the phase shift component of beamformer or steering vector weights, specified as a nonnegative integer. A value of zero indicates that no quantization is performed.

Example: 5
Data Types: single | double

## WeightsOutputPort - Enable beamforming weights output

## false (default) |true

Enable the output of beamforming weights, specified as false or true. To obtain the beamforming weights, set this property to true and use the corresponding output argument, $W$. If you do not want to obtain the weights, set this property to false.

```
Data Types: logical
```


## Usage

## Syntax

```
Y = beamformer(X)
Y = beamformer(X,XT)
Y = beamformer(X,ANG)
Y = beamformer(X,XT,ANG)
[Y,W] = beamformer(
```

$\qquad$

``` )
```


## Description

$Y=$ beamformer $(X)$ performs MVDR beamforming on the input signal, $X$, and returns the beamformed output in Y . This syntax uses X as training samples to calculate the beamforming weights.
$\mathrm{Y}=$ beamformer $(\mathrm{X}, \mathrm{XT})$ uses XT as training samples to calculate the beamforming weights. To use this syntax, set the TrainingInputPort property to true.
$\mathrm{Y}=$ beamformer (X,ANG) uses ANG as the beamforming direction. To use this syntax, set the DirectionSource property to 'Input port'.
$\mathrm{Y}=$ beamformer( $\mathrm{X}, \mathrm{XT}, \mathrm{ANG}$ ) combines all input arguments. To use this syntax, set the TrainingInputPort property to true and set the DirectionSource property to 'Input port'.
$[\mathrm{Y}, \mathrm{W}]=$ beamformer (__ ) returns the beamforming weights, W . To use this syntax, set the WeightsOutputPort property to true.

## Input Arguments

## X - Input signal

complex-valued $M$-by- $N$ matrix
Input signal, specified as a complex-valued $M$-by- $N$ matrix. $N$ is the number of array elements. If the sensor array contains subarrays, $N$ is the number of subarrays. If you set TrainingInputPort to false, $M$ must be larger than $N$; otherwise, $M$ can be any positive integer.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
Data Types: single | double
Complex Number Support: Yes

## XT — Training data

complex-valued $P$-by- $N$ matrix
Training data, specified as a complex-valued $P$-by- $N$ matrix. If the sensor array contains subarrays, $N$ is the number of subarrays; otherwise, $N$ is the number of elements. $P$ must be larger than $N$.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
Example: [1 0.5 2.6; 2 -0.2 0; 3-2 -1]

## Dependencies

To enable this argument, set the TrainingInputPort property to true.

## Data Types: single | double <br> Complex Number Support: Yes

## ANG - Beamforming directions

[0;0] (default) | real-valued 2-by-1 column vector | real-valued 2-by-L matrix
Beamforming directions, specified as a real-valued 2-by-1 column vector, or 2-by-L matrix. $L$ is the number of beamforming directions. Each column has the form [AzimuthAngle; ElevationAngle].

Units are in degrees. Each azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$, and each elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

Example: [40;10]

## Dependencies

To enable this argument, set the DirectionSource property to 'Input port '.
Data Types: single|double

## Output Arguments

Y - Beamformed output
complex-valued $M$-by- $L$ matrix
Beamformed output, returned as a complex-valued $M$-by- $L$ matrix, where $M$ is the number of rows of $X$ and $L$ is the number of beamforming directions.

```
Data Types: single|double
Complex Number Support: Yes
```

W - Beamforming weights
complex-valued $N$-by-L matrix.
Beamforming weights, returned as a complex-valued $N$-by- $L$ matrix. If the sensor array contains subarrays, $N$ is the number of subarrays; otherwise, $N$ is the number of elements. $L$ is the number of beamforming directions.

## Dependencies

To enable this output, set the WeightsOutputPort property to true.
Data Types: single|double
Complex Number Support: Yes

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```


## Common to All System Objects

step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object

## Examples

## MVDR Beamforming

Apply an MVDR beamformer to a 5-element ULA. The incident angle of the signal is 45 degrees in azimuth and 0 degree in elevation. The signal frequency is .01 hertz. The carrier frequency is 300 MHz.

```
t = [0:.1:200]';
fr = .01;
xm = sin(2*pi*fr*t);
c = physconst('LightSpeed');
fc = 300e6;
rng('default');
incidentAngle = [45;0];
array = phased.ULA('NumElements',5,'ElementSpacing',0.5);
x = collectPlaneWave(array,xm,incidentAngle,fc,c);
noise = 0.1*(randn(size(x)) + lj*randn(size(x)));
rx = x + noise;
```

Compute the beamforming weights.

```
beamformer = phased.MVDRBeamformer('SensorArray',array,...
    'PropagationSpeed', c, 'OperatingFrequency' ,fc,...
    'Direction',incidentAngle, 'Weights0utputPort',true);
[y,w] = beamformer(rx);
```

Plot the signals.

```
plot(t,real(rx(:,3)),'r:',t,real(y))
xlabel('Time')
ylabel('Amplitude')
legend('Original','Beamformed')
```



Plot the array response pattern using the MVDR weights.
pattern(array,fc,[-180:180],0,'PropagationSpeed' , c, ...
'Weights',w,'CoordinateSystem', 'rectangular',...
'Type', 'powerdb');


## Algorithms

## MVDR Beamforming

The MVDR beamformer maximizes the signal to noise ratio.
Start with a signal arriving at the elements of an array. Assume that $X$ is a complex-valued $N$-by- $M$ data matrix representing the arrival of signals at an array. $N$ is the number of sensors in the array and $M$ is the number of samples or snapshots per signal. For mathematical convenience, this matrix is the transpose of the matrix specified in the $X$ argument. Each row of $X$ represents a time series of data for the corresponding array. The signal-to-noise ratio of a signal is given here.

$$
S N R=\frac{\left|w^{H} S\right|^{2}}{w^{H} R_{I+N} w}
$$

Properly, the covariance matrix in the denominator is the covariance matrix for the noise and any interferers. You can vary the scale of $w$ without affecting the SNR. Therefore, you can choose the normalization for $w$ so that The MVDR estimator weights for beamforming are $w=R^{-1} v / v^{H} R v$ where $R$ is the data covariance matrix $R=E\left[x x^{H}\right]$.

## Diagonal Loading

Diagonal loading provides beamformer robustness due to small sample size and steering vector errors.

## Data Precision

This System object supports single and double precision for input data, properties, and arguments. If the input data X is single precision, the output data is single precision. If the input data X is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

## Version History

## Introduced in R2011a

## References

[1] Van Trees, H. Optimum Array Processing. New York: Wiley-Interscience, 2002.
[2] Frost, O. "An Algorithm For Linearly Constrained Adaptive Array Processing", Proceedings of the IEEE. Vol. 60, Number 8, August, 1972, pp. 926-935.

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:

- See "System Objects in MATLAB Code Generation" (MATLAB Coder).
- This System object supports single and double precision for input data, properties, and arguments. If the input data $X$ is single precision, the output data is single precision. If the input data $X$ is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.


## See Also

phased.FrostBeamformer|phased. PhaseShiftBeamformer | phased.LCMVBeamformer | phased.SubbandMVDRBeamformer

# phased.MVDREstimator 

Package: phased
MVDR (Capon) spatial spectrum estimator for ULA

## Description

The MVDREstimator object computes a minimum variance distortionless response (MVDR) spatial spectrum estimate for a uniform linear array. This DOA estimator is also referred to as a Capon DOA estimator.

To estimate the spatial spectrum:
1 Define and set up your MVDR spatial spectrum estimator. See "Construction" on page 1-1002.
2 Call step to estimate the spatial spectrum according to the properties of phased.MVDREstimator. The behavior of step is specific to each object in the toolbox.

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.

## Construction

H = phased.MVDREstimator creates an MVDR spatial spectrum estimator System object, H. The object estimates the incoming signal's spatial spectrum using a narrowband MVDR beamformer for a uniform linear array (ULA).

H = phased.MVDREstimator(Name, Value) creates object, H, with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN).

## Properties

## SensorArray

Handle to sensor array
Specify the sensor array as a handle. The sensor array must be a phased. ULA object.
Default: phased.ULA with default property values

## PropagationSpeed

Signal propagation speed
Specify the propagation speed of the signal, in meters per second, as a positive scalar.
Default: Speed of light

## OperatingFrequency

System operating frequency
Specify the operating frequency of the system in hertz as a positive scalar. The default value corresponds to 300 MHz .

Default: 3e8

## NumPhaseShifterBits

Number of phase shifter quantization bits
The number of bits used to quantize the phase shift component of beamformer or steering vector weights. Specify the number of bits as a non-negative integer. A value of zero indicates that no quantization is performed.

Default: 0

## ForwardBackwardAveraging

Perform forward-backward averaging
Set this property to true to use forward-backward averaging to estimate the covariance matrix for sensor arrays with conjugate symmetric array manifold.

Default: false

## SpatialSmoothing

Spatial smoothing
Specify the number of averaging used by spatial smoothing to estimate the covariance matrix as a nonnegative integer. Each additional smoothing handles one extra coherent source, but reduces the effective number of element by 1 . The maximum value of this property is $M-2$, where $M$ is the number of sensors.

Default: 0, indicating no spatial smoothing

## ScanAngles

Scan angles
Specify the scan angles (in degrees) as a real vector. The angles are broadside angles and must be between -90 and 90 , inclusive. You must specify the angles in ascending order.

Default: -90:90
DOAOutputPort
Enable DOA output
To obtain the signal's direction of arrival (DOA), set this property to true and use the corresponding output argument when invoking step. If you do not want to obtain the DOA, set this property to false.

Default: false

## NumSignals

Number of signals
Specify the number of signals for DOA estimation as a positive scalar integer. This property applies when you set the DOAOutputPort property to true.

## Default: 1

## Methods

| plotSpectrum <br> reset <br> step |
| :--- |
| Common to All System Objects <br> Reset states of MVDR spatial spectrum estimator object <br> Perform spatial spectrum estimation |
| release |

## Examples

## Estimate DOA of Two Signals Using MVDR

First, estimate the DOAs of two signals received by a standard 10-element ULA with element spacing of 1 meter. The antenna operating frequency is 150 MHz . The actual direction of the first signal is $10^{\circ}$ in azimuth and $20^{\circ}$ in elevation. The direction of the second signal is $60^{\circ}$ in azimuth and $-5^{\circ}$ in elevation. Then, plot the MVDR spatial spectrum.

Create the signals with added noise. Then, create the ULA System object ${ }^{\text {TM }}$.

```
fs = 8000;
t = (0:1/fs:1).';
x1 = cos(2*pi*t*300);
x2 = cos(2*pi*t*400);
array = phased.ULA('NumElements',10,'ElementSpacing',1);
array.Element.FrequencyRange = [100e6 300e6];
fc = 150.0e6;
x = collectPlaneWave(array,[x1 x2],[10 20;60 -5]',fc);
noise = 0.1*(randn(size(x)) + li*randn(size(x)));
```

Construct MVDR estimator System object.

```
estimator = phased.MVDREstimator('SensorArray',array,...
    'OperatingFrequency',fc,'DOAOutputPort',true,'NumSignals',2);
```

Estimate the DOAs.

```
[y,doas] = estimator(x + noise);
doas = broadside2az(sort(doas),[20 -5])
doas = 1\times2
```


## $9.5829 \quad 60.3813$

Plot the spectrum.
plotSpectrum(estimator)


## Version History

Introduced in R2011a

## References

[1] Van Trees, H. Optimum Array Processing. New York: Wiley-Interscience, 2002.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
See "System Objects in MATLAB Code Generation" (MATLAB Coder).

## See Also

broadside2az | phased.MVDREstimator2D

## plotSpectrum

System object: phased.MVDREstimator
Package: phased
Plot spatial spectrum

## Syntax

plotSpectrum(estimator)
plotSpectrum(estimator,Name, Value)
hl = plotSpectrum( $\qquad$ )

## Description

plotSpectrum(estimator) plots the spatial spectrum resulting from the most recent execution of the object.
plotSpectrum(estimator, Name, Value) plots the spatial spectrum with additional options specified by one or more Name, Value pair arguments.
hl = plotSpectrum( $\qquad$ ) returns the line handle in the figure.

## Input Arguments

H

Spatial spectrum estimator object.

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## NormalizeResponse

Set this value to true to plot the normalized spectrum. Setting this value to false plots the spectrum without normalization.

Default: false
Title
Character vector to use as figure title.

## Default: ' '

## Unit

Plot units, specified as 'db', 'mag', or 'pow'.
Default: 'db'

## Examples

## Estimate DOA of Two Signals Using MVDR

First, estimate the DOAs of two signals received by a standard 10-element ULA with element spacing of 1 meter. The antenna operating frequency is 150 MHz . The actual direction of the first signal is $10^{\circ}$ in azimuth and $20^{\circ}$ in elevation. The direction of the second signal is $60^{\circ}$ in azimuth and $-5^{\circ}$ in elevation. Then, plot the MVDR spatial spectrum.

Create the signals with added noise. Then, create the ULA System object ${ }^{\mathrm{TM}}$.

```
fs = 8000;
t = (0:1/fs:1).';
x1 = cos(2*pi*t*300);
x2 = cos(2*pi*t*400);
array = phased.ULA('NumElements',10,'ElementSpacing',1);
array.Element.FrequencyRange = [100e6 300e6];
fc = 150.0e6;
x = collectPlaneWave(array,[x1 x2],[10 20;60 -5]',fc);
noise = 0.1*(randn(size(x)) + 1i*randn(size(x)));
```

Construct MVDR estimator System object.

```
estimator = phased.MVDREstimator('SensorArray',array,...
    'OperatingFrequency',fc,'DOAOutputPort',true,'NumSignals',2);
```

Estimate the DOAs.

```
[y,doas] = estimator(x + noise);
doas = broadside2az(sort(doas),[20 -5])
doas = 1\times2
    9.5829 60.3813
```

Plot the spectrum.
plotSpectrum(estimator)


## reset

System object: phased.MVDREstimator
Package: phased
Reset states of MVDR spatial spectrum estimator object

## Syntax

reset (H)

## Description

reset $(\mathrm{H})$ resets the states of the MVDREstimator object, H .

## step

## System object: phased.MVDREstimator

Package: phased
Perform spatial spectrum estimation

## Syntax

Y $=\operatorname{step}(\mathrm{H}, \mathrm{X})$
[Y,ANG] = step(H,X)

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step $(o b j, x)$ and $y=o b j(x)$ perform equivalent operations.
$Y=\operatorname{step}(H, X)$ estimates the spatial spectrum from $X$ using the estimator $H . X$ is a matrix whose columns correspond to channels. Y is a column vector representing the magnitude of the estimated spatial spectrum.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
[ $\mathrm{Y}, \mathrm{ANG}$ ] $=\operatorname{step}(\mathrm{H}, \mathrm{X})$ returns additional output ANG as the signal's direction of arrival (DOA) when the DOAOutputPort property is true. ANG is a row vector of the estimated broadside angles (in degrees).

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Examples

## Estimate DOA of Two Signals Using MVDR

First, estimate the DOAs of two signals received by a standard 10 -element ULA with element spacing of 1 meter. The antenna operating frequency is 150 MHz . The actual direction of the first signal is $10^{\circ}$ in azimuth and $20^{\circ}$ in elevation. The direction of the second signal is $60^{\circ}$ in azimuth and $-5^{\circ}$ in elevation. Then, plot the MVDR spatial spectrum.

Create the signals with added noise. Then, create the ULA System object ${ }^{\mathrm{TM}}$.

```
fs = 8000;
t = (0:1/fs:1).';
x1 = cos(2*pi*t*300);
x2 = cos(2*pi*t*400);
array = phased.ULA('NumElements',10,'ElementSpacing',1);
array.Element.FrequencyRange = [100e6 300e6];
fc = 150.0e6;
x = collectPlaneWave(array,[x1 x2],[10 20;60 -5]',fc);
noise = 0.1*(randn(size(x)) + li*randn(size(x)));
```

Construct MVDR estimator System object.

```
estimator = phased.MVDREstimator('SensorArray',array,...
    'OperatingFrequency',fc,'DOAOutputPort',true,'NumSignals',2);
```

Estimate the DOAs.

```
[y,doas] = estimator(x + noise);
doas = broadside2az(sort(doas),[20 -5])
doas = 1×2
    9.5829 60.3813
```

Plot the spectrum.
plotSpectrum(estimator)

MVDR Spatial Spectrum


## phased.MVDREstimator2D

Package: phased
2-D MVDR (Capon) spatial spectrum estimator

## Description

The MVDREstimator2D object computes a 2-D minimum variance distortionless response (MVDR) spatial spectrum estimate. This DOA estimator is also referred to as a Capon estimator.

To estimate the spatial spectrum:
1 Define and set up your 2-D MVDR spatial spectrum estimator. See "Construction" on page 11014.

2 Call step to estimate the spatial spectrum according to the properties of phased.MVDREstimator2D. The behavior of step is specific to each object in the toolbox.

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.

## Construction

H = phased.MVDREstimator2D creates a 2-D MVDR spatial spectrum estimator System object, H . The object estimates the signal's spatial spectrum using a narrowband MVDR beamformer.

H = phased.MVDREstimator2D(Name,Value) creates object, H , with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN).

## Properties

## SensorArray

Handle to sensor array
Specify the sensor array as a handle. The sensor array must be an array object in the phased package. The array cannot contain subarrays.

Default: phased.ULA with default property values

## PropagationSpeed

Signal propagation speed
Specify the propagation speed of the signal, in meters per second, as a positive scalar. You can specify this property as single or double precision.

Default: Speed of light

## OperatingFrequency

System operating frequency
Specify the operating frequency of the system in hertz as a positive scalar. The default value corresponds to 300 MHz . You can specify this property as single or double precision.

Default: 3e8

## NumPhaseShifterBits

Number of phase shifter quantization bits
The number of bits used to quantize the phase shift component of beamformer or steering vector weights. Specify the number of bits as a non-negative integer. A value of zero indicates that no quantization is performed. You can specify this property as single or double precision.

Default: 0

## ForwardBackwardAveraging

Perform forward-backward averaging
Set this property to true to use forward-backward averaging to estimate the covariance matrix for sensor arrays with conjugate symmetric array manifold.

Default: false

## AzimuthScanAngles

Azimuth scan angles (degrees)
Specify the azimuth scan angles (in degrees) as a real vector. The angles must be between -180 and 180, inclusive. You must specify the angles in ascending order. You can specify this property as single or double precision.

Default: -90:90

## ElevationScanAngles

Elevation scan angles
Specify the elevation scan angles (in degrees) as a real vector or scalar. The angles must be between -90 and 90 , inclusive. You must specify the angles in ascending order. You can specify this property as single or double precision.

## Default: 0

## DOAOutputPort

Enable DOA output
To obtain the signal's direction of arrival (DOA), set this property to true and use the corresponding output argument when invoking step. If you do not want to obtain the DOA, set this property to false.

Default: false

## NumSignals

Number of signals
Specify the number of signals for DOA estimation as a positive scalar integer. This property applies when you set the DOAOutputPort property to true. You can specify this property as single or double precision.

## Default: 1

## Methods

| plotSpectrum | Plot spatial spectrum |
| :--- | :--- |
| reset | Reset states of 2-D MVDR spatial spectrum estimator object |
| step | Perform spatial spectrum estimation |

## Common to All System Objects

release Allow System object property value changes

## Examples

## Estimate DOA of Two Signals Arriving at URA

Estimate the DOAs of two signals received by a 50 -element URA with a rectangular lattice. The antenna operating frequency is 150 MHz . The actual direction of the first signal is $-37^{\circ}$ in azimuth and $0^{\circ}$ in elevation. The direction of the second signal is $17^{\circ}$ in azimuth and $20^{\circ}$ degrees in elevation. Then, plot the spatial spectrum.

Create the arriving signals.

```
fs = 8000;
t = (0:1/fs:1).';
x1 = cos(2*pi*t*300);
x2 = cos(2*pi*t*400);
array = phased.URA('Size',[5 10],'ElementSpacing',[1 0.6]);
array.Element.FrequencyRange = [100e6 300e6];
fc = 150e6;
x = collectPlaneWave(array,[x1 x2],[-37 0;17 20]',fc);
```

Add noise.

```
noise = 0.1*(randn(size(x))+1i*randn(size(x)));
```

Create the MVDR DOA estimator and estimate the DOAs.

```
estimator = phased.MVDREstimator2D('SensorArray',array,...
    'OperatingFrequency',fc,...
    'DOAOutputPort',true,'NumSignals',2,...
    'AzimuthScanAngles',-50:50,...
    'ElevationScanAngles',-30:30);
[~,doas] = estimator(x + noise);
```

Plot the spectrum.
plotSpectrum(estimator)


## Algorithms

## Data Precision

This System object supports single and double precision for input data, properties, and arguments. If the input data $X$ is single precision, the output data is single precision. If the input data $X$ is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

## Version History

Introduced in R2011a

## References

[1] Van Trees, H. Optimum Array Processing. New York: Wiley-Interscience, 2002.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
See "System Objects in MATLAB Code Generation" (MATLAB Coder).
This System object supports single and double precision for input data, properties, and arguments. If the input data X is single precision, the output data is single precision. If the input data X is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

## See Also

phased.MVDREstimator|uv2azel | phitheta2azel

## plotSpectrum

System object: phased.MVDREstimator2D
Package: phased
Plot spatial spectrum

## Syntax

plotSpectrum(estimator)
plotSpectrum(estimator, Name, Value)
hl = plotSpectrum( $\qquad$ )

## Description

plotSpectrum(estimator) plots the spatial spectrum resulting from the most recent execution of the object.
plotSpectrum(estimator, Name, Value) plots the spatial spectrum with additional options specified by one or more Name, Value pair arguments.
hl = plotSpectrum( $\qquad$ ) returns the line handle in the figure.

## Input Arguments

H

Spatial spectrum estimator object.

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## NormalizeResponse

Set this value to true to plot the normalized spectrum. Setting this value to false plots the spectrum without normalization.

Default: false
Title
Character vector to use as figure title.

## Default: ' '

## Unit

Plot units, specified as 'db', 'mag', or 'pow'.
Default: 'db'

## Examples

## Estimate DOA Using 2D MVDR

Estimate the DOAs of two signals received by a 50 -element URA with a rectangular lattice. The antenna operating frequency is 150 MHz . The actual direction of the first signal is $-37^{\circ}$ in azimuth and $0^{\circ}$ in elevation. The direction of the second signal is $17^{\circ}$ in azimuth and $20^{\circ}$ in elevation.

Create signals sampled at 8 kHz .
$\mathrm{fc}=150 \mathrm{e} 6$;
fs = 8000;
t = (0:1/fs:1).';
$\mathrm{x} 1=\cos \left(2 *\right.$ pi $\left.^{*} \mathrm{t} * 300\right)$;
$\mathrm{x} 2=\cos \left(2 *\right.$ pi*t*400 $\left.^{2}\right)$;
array = phased.URA('Size',[5 10],'ElementSpacing',[1 0.6]);
array.Element.FrequencyRange = [100e6 300e6];
x = collectPlaneWave(array,[x1 x2],[-37 0;17 20]',fc);
Add complex noise.

```
noise = 0.1*(randn(size(x))+1i*randn(size(x)));
```

Create the MVDR DOA estimator for URA.

```
estimator = phased.MVDREstimator2D('SensorArray',array,...
    'OperatingFrequency',fc,...
    'DOA0utputPort',true,'NumSignals',2,...
    'AzimuthScanAngles',-50:50,...
    'ElevationScanAngles',-30:30);
```

Use the step method to the DOA estimates.

```
[~,doas] = estimator(x + noise)
doas = 2×2
    17 -37
    20 0
```

Plot the spectrum.

```
plotSpectrum(estimator)
```



## reset

System object: phased.MVDREstimator2D
Package: phased
Reset states of 2-D MVDR spatial spectrum estimator object

## Syntax

reset (H)

## Description

reset $(\mathrm{H})$ resets the states of the MVDREstimator2D object, H .

## step

System object: phased.MVDREstimator2D
Package: phased
Perform spatial spectrum estimation

## Syntax

```
Y = step(H,X)
[Y,ANG] = step(H,X)
```


## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step (obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.
$\mathrm{Y}=\operatorname{step}(\mathrm{H}, \mathrm{X})$ estimates the spatial spectrum from X using the estimator $\mathrm{H} . \mathrm{X}$ is a matrix whose columns correspond to channels. Y is a matrix representing the magnitude of the estimated 2-D spatial spectrum. The row dimension of $Y$ is equal to the number of angles in the ElevationScanAngles and the column dimension of $Y$ is equal to the number of angles in the AzimuthScanAngles property. You can specify the argument, X , as single or double precision.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
[ $\mathrm{Y}, \mathrm{ANG}$ ] $=\operatorname{step}(\mathrm{H}, \mathrm{X})$ returns additional output ANG as the signal's direction of arrival (DOA) when the DOAOutputPort property is true. ANG is a two-row matrix where the first row represents estimated azimuth and the second row represents estimated elevation (in degrees).

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Examples

## Estimate DOA Using 2D MVDR

Estimate the DOAs of two signals received by a 50 -element URA with a rectangular lattice. The antenna operating frequency is 150 MHz . The actual direction of the first signal is $-37^{\circ}$ in azimuth and $0^{\circ}$ in elevation. The direction of the second signal is $17^{\circ}$ in azimuth and $20^{\circ}$ in elevation.

Create signals sampled at 8 kHz .

```
fc = 150e6;
fs = 8000;
t = (0:1/fs:1).';
x1 = cos(2*pi*t*300);
x2 = cos(2*pi*t*400);
array = phased.URA('Size',[5 10],'ElementSpacing',[1 0.6]);
array.Element.FrequencyRange = [100e6 300e6];
x = collectPlaneWave(array,[x1 x2],[-37 0;17 20]',fc);
```

Add complex noise.

```
noise = 0.1*(randn(size(x))+li*randn(size(x)));
```

Create the MVDR DOA estimator for URA.

```
estimator = phased.MVDREstimator2D('SensorArray',array,...
    'OperatingFrequency',fc,...
    'DOAOutputPort',true,'NumSignals',2,...
    'AzimuthScanAngles',-50:50,...
    'ElevationScanAngles',-30:30);
```

Use the step method to the DOA estimates.

```
[~,doas] = estimator(x + noise)
doas = 2\times2
    17 -37
    20 0
```

Plot the spectrum.
plotSpectrum(estimator)


## See Also

azel2uv|azel2phitheta

## phased.MultipathChannel

Package: phased
Propagate signals in multipath channel

## Description

The phased.MultipathChannel System object propagates a signal through a multipath channel. To run the object, you must provide characteristics for each path: time delay, gain, Doppler factor, reflection loss, and spreading loss.

For sonar applications, you can use the phased.IsoSpeedUnderwaterPaths System object to generate channel path characteristics. You can also supply these characteristics independently.

To model signal propagation through a multipath channel:
1 Define and set up the propagator. You can set phased. MultipathChannel properties at construction time or leave them to their default values. See "Construction" on page 1-1026. Some properties that you set at construction time can be changed later. These properties are tunable.
2 To compute the propagated signal, call the step method of phased.MultipathChannel. The output of the step method depends on the properties of the phased. MultipathChannel System object. You can change tunable properties at any time.

Note Instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, $y=s t e p(o b j, x)$ and $y=$ obj $(x)$ perform equivalent operations.

## Construction

propagator $=$ phased.MultipathChannel creates a signal propagator System object for a multipath underwater channel.
propagator $=$ phased.MultipathChannel(Name,Value) creates a signal propagator System object with each specified property Name set to the specified Value. You can specify additional name and value pair arguments in any order as (Name1, Value1,...,NameN, ValueN).

## Properties

## OperatingFrequency - Signal carrier frequency

20e3 (default) | positive real-valued scalar
Signal carrier frequency, specified as a positive real-valued scalar. Units are in Hz .
Example: 10000
Data Types: double

## SampleRate - Signal sample rate

1e3 (default) | positive real-valued scalar

Signal sample rate, specified as a positive real-valued scalar. Units are in Hz. The System object uses this quantity to calculate the propagation delay in units of samples.
Example: 3e3
Data Types: double
MaximumDelaySource - Source of maximum delay
'Auto' (default)|'Property'
Source of the maximum delay value, specified as 'Auto' or 'Property'. When you set this property to 'Auto', the channel automatically allocates enough memory to simulate the propagation delay. When you set this property to 'Property', you can specify the maximum delay by using the MaximumDelay property. Signals arriving after the maximum delay are ignored.

## MaximumDelay - Maximum signal delay

1 (default) | positive scalar
Maximum signal delay, specified as a positive scalar. Delays greater than this value are ignored. Units are in seconds.

## Dependencies

To enable this property, set the MaximumDelaySource property to 'Property'.
Data Types: double

## InterpolationMethod - Interpolation method to implement fractional delay <br> 'Linear' (default)|'Oversample'

Interpolation method used to implement signal fractional delay and Doppler time-dilation and compression, specified as 'Linear' or 'Oversample'. When this property is set to 'Linear', the input signal is linearly interpolated directly onto a uniform grid to propagate the signal. When this property is set to 'Oversample', the input signal is resampled to a higher rate before linear interpolation. For broadband signals, oversampling preserves spectral shape.

## Data Types: char

## Methods

step Propagate signal through multipath sound channel
reset Reset state of System object

## Common to All System Objects

| release | Allow System object property value changes |
| :--- | :--- |

## Examples

## One-Way Signal Propagation in Multipath Underwater Sound Channel

Create a five-path underwater sound channel and compute the propagation path matrix, the Doppler factor, and the absorption loss. Assume that the source is stationary and the receiver is moving along the $x$-axis toward the source at $20 \mathrm{~km} / \mathrm{h}$. Assume the default one-way propagation.

Create the channel and specify the source and receiver locations and velocities.

```
numpaths = 5;
channel = phased.IsoSpeedUnderwaterPaths('ChannelDepth',200,'BottomLoss',10, ...
    'NumPathsSource','Property','NumPaths',numpaths);
tstep = 1;
srcpos = [0;0;-160];
rcvpos = [100;0;-50];
speed = -20*1000/3600;
srcvel = [0;0;0];
rcvvel = [speed;0;0];
```

Compute the path matrix, Doppler factor, and losses.

```
[pathmat,dop,absloss] = channel(srcpos,rcvpos,srcvel,rcvvel,tstep);
```

Create 500 samples of a 100 Hz signal. Assume all the paths have the same signal. Propagate the signals to the receiver.

```
fs = 1e3;
nsamp = 500;
propagator = phased.MultipathChannel('OperatingFrequency',10e3,'SampleRate',fs);
t = [0:(nsamp-1)]'/fs;
sig0 = sin(2*pi*100*t);
sig = repmat(sig0,1,numpaths);
propsig = propagator(sig,pathmat,dop,absloss);
```

Plot the real part of the coherent sum of the propagated signals.

```
plot(t*1000,real(sum(propsig,2)))
xlabel('Time (millisec)')
```



## Two-Way Signal Propagation in Multipath Underwater Sound Channel

Create a seven-path underwater sound channel and display the propagation path matrix. Assume that the source is stationary and that the receiver is moving along the $x$-axis toward the source at 20 $\mathrm{km} / \mathrm{h}$. Assume two-way propagation.

```
speed = -20*1000/3600;
numpaths = 7;
csound = 1515.0;
channel = phased.IsoSpeedUnderwaterPaths('ChannelDepth',200, ...
    'PropagationSpeed',csound,'BottomLoss',10,'NumPathsSource','Property', ...
    'NumPaths',numpaths,'TwoWayPropagation',true);
tstep = 1;
srcpos = [0;0;-160];
tgtpos = [500;0;-50];
srcvel = [0;0;0];
tgtvel = [speed;0;0];
```

Obtain the path matrix, Doppler factor, loss, and target reflection and transmit angles.

```
[pathmat,dop,aloss,tgtangs,srcangs] = channel(srcpos,tgtpos,srcvel,tgtvel,tstep);
```

Create a 100 Hz signal with 500 samples. Assume that all the paths have the same signal but with different amplitudes. Then, propagate the signals to the target and back. You can use the angle
information to calculate any angular dependence of the source and target responses. Each channel can have a different amplitude. This example uses a simple cosine model.

```
fs = 1e3;
nsamp = 500;
propagator = phased.MultipathChannel('OperatingFrequency',10e3,'SampleRate',fs);
t = [0:(nsamp-1)]'/fs;
ampsrc = cosd(srcangs(2,:));
amptgt = cosd(tgtangs(2,:));
sig0 = sin(2*pi*100*t);
sig = repmat(sig0,1,numpaths);
amptotal = ampsrc.^2.*amptgt;
sig = bsxfun(@times,amptotal,sig);
```

Because of the finite propagation delay, the first call to the propagator does not return the signal. Call propagator twice to obtain the returned signal.

```
propsig = propagator(sig,pathmat,dop,aloss);
propsig = propagator(sig,pathmat,dop,aloss);
```

Plot the real part of the coherent sum of the propagated signals. Compute the round trip time.

```
rng = rangeangle(srcpos,tgtpos);
tr = rng/csound;
plot((t+tr)*1000,real(sum(propsig,2)))
xlabel('Time (millisec)')
```



## Propagate Sound in Channel Having Unknown Number of Paths

Create an underwater sound channel and plot the combined received signal. Automatically find the number of paths. Assume that the source is stationary and that the receiver is moving along the $x$-axis toward the source at $20 \mathrm{~km} / \mathrm{h}$. Assume the default one-way propagation.

```
speed = -20*1000/3600;
channel = phased.IsoSpeedUnderwaterPaths('ChannelDepth',200,'BottomLoss',5, ...
    'NumPathsSource','Auto','CoherenceTime',5);
tstep = 1;
srcpos = [0;0;-160];
rcvpos = [500;0;-50];
srcvel = [0;0;0];
rcvvel = [speed;0;0];
```

Compute the path matrix, Doppler factor, and losses. The propagator outputs 51 paths output but some paths can contain Nan values.

```
[pathmat,dop,absloss,rcvangs,srcangs] = channel(srcpos,rcvpos,srcvel,rcvvel,tstep);
```

Create of a 100 Hz signal with 500 samples. Assume that all the paths have the same signal. Use a phased.MultipathChannel System object ${ }^{\mathrm{TM}}$ to propagate the signals to the receiver.
phased. MultipathChannel accepts as input all paths produced by phased.IsoSpeedUnderwaterPaths but ignores paths that have NaN values.

```
fs = 1e3;
nsamp = 500;
propagator = phased.MultipathChannel('OperatingFrequency',10e3,'SampleRate',fs);
t = [0:(nsamp-1)]'/fs;
sig0 = sin(2*pi*100*t);
numpaths = size(pathmat,2);
sig = repmat(sig0,1,numpaths);
propsig = propagator(sig,pathmat,dop,absloss);
```

Plot the real part of the coherent sum of the propagated signals.
plot(t*1000, real(sum(propsig, 2)))
xlabel('Time (millisec)')


## Doppler Stretching of Sonar Signal

Compare the duration of a propagated signal from a stationary sonar to that of a moving sonar. The moving sonar has a radial velocity of $25 \mathrm{~m} / \mathrm{s}$ away from the target. In each case, propagate the signal along a single path. Assume one-way propagation.

Define the sonar system parameters: maximum unambiguous range, required range resolution, operating frequency, and propagation speed.

```
maxrange = 5000.0;
rngres = 10.0;
fc = 20.0e3;
csound = 1520.0;
```

Use a rectangular waveform for the transmitted signal.

```
prf = csound/(2*maxrange);
pulseWidth = 8*rngres/csound;
pulseBW = 1/pulseWidth;
fs = 80*pulseBW;
waveform = phased.RectangularWaveform('PulseWidth',pulseWidth,'PRF',prf, ...
    'SampleRate',fs);
```

Specify the sonar positions.

```
sonarplatform1 = phased.Platform('InitialPosition',[0;0;-60],'Velocity',[0;0;0]);
sonarplatform2 = phased.Platform('InitialPosition',[0;0;-60],'Velocity',[0;-25;0]);
```

Specify the target position.

```
targetplatform = phased.Platform('InitialPosition',[0;500;-60],'Velocity',[0;0;0]);
```

Define the underwater path and propagation channel objects.

```
paths = phased.IsoSpeedUnderwaterPaths('ChannelDepth',100, ...
    'CoherenceTime',0,'NumPathsSource','Property','NumPaths',1, ...
    'PropagationSpeed',csound);
propagator = phased.MultipathChannel('SampleRate',fs,'OperatingFrequency',fc);
```

Create the transmitted waveform.

```
wav = waveform();
nsamp = size(wav,1);
rxpulses = zeros(nsamp,2);
t = (0:nsamp-1)/fs;
```

Transmit the signal and then receive the echo at the stationary sonar.

```
[pathmat,dop,aloss,~,~] = paths(sonarplatform1.InitialPosition, ...
    targetplatform.InitialPosition,sonarplatform1.InitialVelocity, ...
    targetplatform.InitialVelocity,1/prf);
rxpulses(:,1) = propagator(wav,pathmat,dop,aloss);
```

Transmit and receive at the moving sonar.

```
[pathmat,dop,aloss,~,~] = paths(sonarplatform2.InitialPosition, ...
    targetplatform.InitialPosition,sonarplatform2.Velocity, ...
    targetplatform.Velocity,1/prf);
rxpulses(:,2) = propagator(wav,pathmat,dop,aloss);
```

Plot the received pulses.

```
plot(abs(rxpulses))
xlim([490 650])
ylim([0 1.65e-3])
legend('Stationary sonar','Moving sonar')
xlabel('Received Sample Time (sec)')
ylabel('Integrated Received Pulses')
```



The signal received at the moving sonar has increased in duration compared to the stationary sonar.

## Version History

## Introduced in R2017a

## References

[1] Urick, R.J. Principles of Underwater Sound, 3rd Edition. New York: Peninsula Publishing, 1996.
[2] Sherman, C.S. and J. Butler Transducers and Arrays for Underwater Sound. New York: Springer, 2007.
[3] Allen, J.B. and D. Berkely, "Image method for efficiently simulating small-room acoustics", J. Acoust. Soc. Am, Vol 65, No. 4. April 1979.

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:
See "System Objects in MATLAB Code Generation" (MATLAB Coder).

## See Also

## Objects

phased.BackscatterSonarTarget|phased.IsoSpeedUnderwaterPaths |
phased.IsotropicHydrophone| phased.IsotropicProjector

## Topics

"Underwater Target Detection with an Active Sonar System"
"Locating an Acoustic Beacon with a Passive Sonar System"
"Doppler Effect for Sound"

## step

System object: phased.MultipathChannel
Package: phased
Propagate signal through multipath sound channel

## Syntax

propsig = step(propagator,sig,pathmat,dop,aloss)

## Description

Note Instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, $y=s t e p(o b j, x)$ and $y=$ obj ( $x$ ) perform equivalent operations.
propsig = step(propagator,sig,pathmat,dop,aloss) returns a signal, propsig, propagated through a multipath channel. sig is the input signal to the channel. The pathmat matrix contains the path time delay, the total reflection coefficient, and the spreading loss. dop specifies the Doppler factor and aloss specifies the frequency-dependent absorption loss. The matrix can describe one-way or two-way propagation from the signal source position to the signal destination position.

- When you use this method for one-way propagation, the source refers to the origin of the signal and the destination refers to the receiver. You can use one-way propagation modeling to model passive sonar and underwater communications.
- When you use this method for two-way propagation, the destination refers to the reflecting target, not the sonar receiver. A two-way path consists of a two identical one-way paths from source to target and back to receiver (collocated with the source). You can use two-way propagation to model active sonar systems.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

Note Instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj,x) and y = obj $(x)$ perform equivalent operations.

## Input Arguments

## propagator - Multipath channel propagator

phased.MultipathChannel System object
Multipath channel propagator, specified as a phased.MultipathChannel System object.

Example: phased.MultipathChannel
sig - Channel input signal
complex-valued $M$-by- $N$ matrix
Channel input signal, specified as a complex-valued $M$-by- $N$ matrix. $M$ is the number of samples in the signal and $N$ is the number of paths.
Data Types: double

## pathmat - Propagation paths matrix

real-valued 3-by- $N$ matrix
Propagation paths matrix, specified as a real-valued 3 -by- $N$ matrix. $N$ is the number of paths in the channel. Each column represents a path. The matrix rows represent:

| Row | Data |
| :--- | :--- |
| 1 | Propagation delays for each path. Units are in seconds. |
| 2 | Total reflection coefficient for each path. Units are dimensionless |
| 3 | Spreading loss for each path. Units are in dB. |

Except for the direct path, paths consist of alternating surface and bottom reflections. The losses for multiple reflections at the boundaries are multiplied. When you use phased. IsoSpeedUnderwaterPaths to create a path matrix, some of the columns can contain NaN values. phased.MultipathChannel ignores these paths.
Data Types: double
dop - Doppler factor
real-valued $N$-by-1 row vector
Doppler factor, specified as a real-valued $N$-by- 1 row vector where $N$ is the number of paths. The Doppler factor multiplies the transmitted frequency to produce the Doppler-shifted frequency for each path. The factor also defines the time contraction or dilation of a signal. Units are dimensionless.
Data Types: double

## aloss - Frequency-dependent absorption loss

real-valued $K$-by- $N+1$ matrix
Frequency-dependent absorption loss, specified as a real-valued $K$-by- $N+1$ matrix. $K$ is the number of frequencies and $N$ is the number of paths. The first column of aloss contains the absorption-loss frequencies in Hz. The remaining columns contain the absorption losses for the corresponding frequency. Units are in dB .
Data Types: double

## Output Arguments

propsig - Channel output signal
complex-valued $M$-by- $N$ matrix

Channel output signal, returned as a complex-valued $M$-by- $N$ matrix. $M$ is the number of samples in the signal and $N$ is the number of paths. The output is the signal propagated through the channel. propsig has the same dimensions as the input signal, sig.

## Examples

## One-Way Signal Propagation in Multipath Underwater Sound Channel

Create a five-path underwater sound channel and compute the propagation path matrix, the Doppler factor, and the absorption loss. Assume that the source is stationary and the receiver is moving along the $x$-axis toward the source at $20 \mathrm{~km} / \mathrm{h}$. Assume the default one-way propagation.

Create the channel and specify the source and receiver locations and velocities.

```
numpaths = 5;
channel = phased.IsoSpeedUnderwaterPaths('ChannelDepth',200,'BottomLoss',10, ...
    'NumPathsSource','Property','NumPaths',numpaths);
tstep = 1;
srcpos = [0;0;-160];
rcvpos = [100;0;-50];
speed = -20*1000/3600;
srcvel = [0;0;0];
rcvvel = [speed;0;0];
Compute the path matrix, Doppler factor, and losses.
```

```
[pathmat,dop,absloss] = channel(srcpos,rcvpos,srcvel,rcvvel,tstep);
```

Create 500 samples of a 100 Hz signal. Assume all the paths have the same signal. Propagate the signals to the receiver.

```
fs = le3;
nsamp = 500;
propagator = phased.MultipathChannel('OperatingFrequency',10e3,'SampleRate',fs);
t = [0:(nsamp-1)]'/fs;
sig0 = sin(2*pi*100*t);
sig = repmat(sig0,1,numpaths);
propsig = propagator(sig,pathmat,dop,absloss);
```

Plot the real part of the coherent sum of the propagated signals.

```
plot(t*1000,real(sum(propsig,2)))
xlabel('Time (millisec)')
```



## Two-Way Signal Propagation in Multipath Underwater Sound Channel

Create a seven-path underwater sound channel and display the propagation path matrix. Assume that the source is stationary and that the receiver is moving along the $x$-axis toward the source at 20 $\mathrm{km} / \mathrm{h}$. Assume two-way propagation.

```
speed = -20*1000/3600;
numpaths = 7;
csound = 1515.0;
channel = phased.IsoSpeedUnderwaterPaths('ChannelDepth',200, ...
    'PropagationSpeed',csound,'BottomLoss',10,'NumPathsSource','Property', ...
    'NumPaths',numpaths,'TwoWayPropagation',true);
tstep = 1;
srcpos = [0;0;-160];
tgtpos = [500;0;-50];
srcvel = [0;0;0];
tgtvel = [speed;0;0];
```

Obtain the path matrix, Doppler factor, loss, and target reflection and transmit angles.

```
[pathmat,dop,aloss,tgtangs,srcangs] = channel(srcpos,tgtpos,srcvel,tgtvel,tstep);
```

Create a 100 Hz signal with 500 samples. Assume that all the paths have the same signal but with different amplitudes. Then, propagate the signals to the target and back. You can use the angle
information to calculate any angular dependence of the source and target responses. Each channel can have a different amplitude. This example uses a simple cosine model.

```
fs = 1e3;
nsamp = 500;
propagator = phased.MultipathChannel('OperatingFrequency',10e3,'SampleRate',fs);
t = [0:(nsamp-1)]'/fs;
ampsrc = cosd(srcangs(2,:));
amptgt = cosd(tgtangs(2,:));
sig0 = sin(2*pi*100*t);
sig = repmat(sig0,1,numpaths);
amptotal = ampsrc.^2.*amptgt;
sig = bsxfun(@times,amptotal,sig);
```

Because of the finite propagation delay, the first call to the propagator does not return the signal. Call propagator twice to obtain the returned signal.

```
propsig = propagator(sig,pathmat,dop,aloss);
propsig = propagator(sig,pathmat,dop,aloss);
```

Plot the real part of the coherent sum of the propagated signals. Compute the round trip time.

```
rng = rangeangle(srcpos,tgtpos);
tr = rng/csound;
plot((t+tr)*1000,real(sum(propsig,2)))
xlabel('Time (millisec)')
```



## Propagate Sound in Channel Having Unknown Number of Paths

Create an underwater sound channel and plot the combined received signal. Automatically find the number of paths. Assume that the source is stationary and that the receiver is moving along the $x$-axis toward the source at $20 \mathrm{~km} / \mathrm{h}$. Assume the default one-way propagation.

```
speed = -20*1000/3600;
channel = phased.IsoSpeedUnderwaterPaths('ChannelDepth',200,'BottomLoss',5, ...
    'NumPathsSource','Auto','CoherenceTime',5);
tstep = 1;
srcpos = [0;0;-160];
rcvpos = [500;0;-50];
srcvel = [0;0;0];
rcvvel = [speed;0;0];
```

Compute the path matrix, Doppler factor, and losses. The propagator outputs 51 paths output but some paths can contain Nan values.

```
[pathmat,dop,absloss,rcvangs,srcangs] = channel(srcpos,rcvpos,srcvel,rcvvel,tstep);
```

Create of a 100 Hz signal with 500 samples. Assume that all the paths have the same signal. Use a phased.MultipathChannel System object ${ }^{\mathrm{TM}}$ to propagate the signals to the receiver.
phased. MultipathChannel accepts as input all paths produced by phased.IsoSpeedUnderwaterPaths but ignores paths that have NaN values.

```
fs = 1e3;
nsamp = 500;
propagator = phased.MultipathChannel('OperatingFrequency',10e3,'SampleRate',fs);
t = [0:(nsamp-1)]'/fs;
sig0 = sin(2*pi*100*t);
numpaths = size(pathmat,2);
sig = repmat(sig0,1,numpaths);
propsig = propagator(sig,pathmat,dop,absloss);
```

Plot the real part of the coherent sum of the propagated signals.

```
plot(t*1000,real(sum(propsig,2)))
```

xlabel('Time (millisec)')


## Version History <br> Introduced in R2017a

## reset

System object: phased.MultipathChannel
Package: phased
Reset state of System object

## Syntax

reset (propagator)

## Description

reset (propagator) resets the internal state of the phased. MultipathChannel object, propagator.

## Input Arguments

propagator - Multipath channel
phased.MultipathChannel System object
Multipath channel, specified as a phased.MultipathChannel System object.
Example: phased.MultipathChannel

## Version History

Introduced in R2017a

## phased.MUSICEstimator

Package: phased
Estimate direction of arrival using narrowband MUSIC algorithm for ULA

## Description

The phased.MUSICEstimator System object implements the narrowband multiple signal classification (MUSIC) algorithm for uniform linear arrays (ULA). MUSIC is a high-resolution direction-finding algorithm capable of resolving closely-spaced signal sources. The algorithm is based on eigenspace decomposition of the sensor spatial covariance matrix.

To estimate directions of arrival (DOA):
1 Define and set up a phased.MUSICEstimator System object. See "Construction" on page 11044.

2 Call the step method to estimate the DOAs according to the properties of phased.MUSICEstimator.

Note Alternatively, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, $y=$ step $(o b j, x)$ and $y=o b j(x)$ perform equivalent operations.

## Construction

estimator $=$ phased.MUSICEstimator creates a MUSIC DOA estimator System object, estimator.
estimator = phased.MUSICEstimator(Name,Value) creates a System object, estimator, with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Namel,Value1,...,NameN,ValueN).

## Properties

## SensorArray - ULA sensor array

phased.ULA System object (default)
ULA sensor array, specified as a phased.ULA System object. If you do not specify any name-value pair properties for the ULA sensor array, the default properties of the array are used.

## PropagationSpeed - Signal propagation speed

physconst('LightSpeed') (default) | real-valued positive scalar
Signal propagation speed, specified as a real-valued positive scalar. Units are in meters per second. The default propagation speed is the value returned by physconst('LightSpeed').
Example: 3e8
Data Types: single | double

## OperatingFrequency - Operating frequency

300e6 (default) | positive scalar
Operating frequency, specified as a positive scalar. Units are in Hz .
Example: 1e9
Data Types: single | double

## ForwardBackwardAveraging - Enable forward-backward averaging

false (default)| true
Enable forward-backward averaging, specified as false or true. Set this property to true to use forward-backward averaging to estimate the covariance matrix for sensor arrays with a conjugate symmetric array manifold.
Data Types: logical

## ScanAngles - Broadside scan angles

[-90:90] (default) | real-valued $K$-length vector
Broadside scan angles, specified as a real-valued vector. Units are in degrees. Broadside angles are between the search direction and the ULA array axis. The angles lie between $-90^{\circ}$ and $90^{\circ}$, inclusive. Specify the angles in increasing value.
Example: [-20:20]
Data Types: single | double

## DOAOutputPort - Enable directions of arrival output

false (default) | true
Option to enable directions-of-arrival (DOA) output, specified as false or true. To obtain the DOA of signals, set this property to true. The DOAs are returned in the second output argument when the object is executed.
Data Types: logical

## NumSignalsSource - Source of number of signals

'Auto' (default)|'Property'
Source of the number of arriving signals, specified as 'Auto' or 'Property'.

- 'Auto ' - The System object estimates the number of arriving signals using the method specified in the NumSignalsMethod property.
- 'Property ' - Specify the number of arriving signals using the NumSignals property.

Data Types: char
NumSignalsMethod - Method used to estimate number of arriving signals
'AIC' (default) | 'MDL'
Method used to estimate the number of arriving signals, specified as 'AIC' or 'MDL'.

- 'AIC' - Akaike Information Criterion
- 'MDL' - Minimum Description Length criterion


## Dependencies

To enable this property, set NumSignalsSource to 'Auto '.
Data Types: char
NumSignals - Number of arriving signals
1 (default) | positive integer
Number of arriving signals for DOA estimation, specified as a positive integer.

## Example: 3

## Dependencies

To enable this property, set NumSignalsSource to 'Property '.

## Data Types: single | double

## SpatialSmoothing - Enable spatial smoothing

0 (default) | nonnegative integer
Option to enable spatial smoothing, specified as a nonnegative integer. Use spatial smoothing to compute the arrival directions of coherent signals. A value of zero specifies no spatial smoothing. A positive value represents the number of subarrays used to compute the smoothed (averaged) source covariance matrix. Each increment in this value lets you handle one additional coherent source, but reduces the effective number of array elements by one. The length of the smoothing aperture, $L$, depends on the array length, $M$, and the averaging number, $K$, by $L=M-K+1$. The maximum value of $K$ is $M-2$.

## Example: 5

Data Types: double

## Methods

| plotSpectrum | Plot MUSIC spectrum |
| :--- | :--- |
| reset | Reset states of System object |
| step | Estimate direction of arrival using MUSIC |

## Common to All System Objects

release $\quad$ Allow System object property value changes

## Examples

## Plot MUSIC Spectrum of Two Signals Arriving at ULA

Estimate the DOAs of two signals received by a standard 10-element ULA having an element spacing of 1 meter. Then plot the MUSIC spectrum.

Create the ULA array. The antenna operating frequency is 150 MHz .

```
fc = 150.0e6;
```

array $=$ phased.ULA('NumElements',10,'ElementSpacing',1.0);

Create the arriving signals at the ULA. The true direction of arrival of the first signal is $10^{\circ}$ in azimuth and $20^{\circ}$ in elevation. The direction of the second signal is $60^{\circ}$ in azimuth and $-5^{\circ}$ in elevation.
fs $=8000.0 ;$
$\mathrm{t}=(0: 1 / \mathrm{fs}: 1) .{ }^{\prime}$;
sig1 $=\cos \left(2 *\right.$ pi $\left.^{*} \mathrm{t} * 300.0\right)$;
sig2 $=\cos (2 *$ pi*t*400.0);
sig = collectPlaneWave(array,[sig1 sig2],[10 20; 60-5]',fc);
noise $=0.1^{*}($ randn(size(sig)) $+1 i * r a n d n(s i z e(s i g))) ;$
Estimate the DOAs.

```
estimator = phased.MUSICEstimator('SensorArray',array,...
    'OperatingFrequency',fc,...
    'DOAOutputPort',true,'NumSignalsSource','Property',...
    'NumSignals',2);
[y,doas] = estimator(sig + noise);
doas = broadside2az(sort(doas),[20 -5])
doas = 1\times2
    9.5829 60.3813
```

Plot the MUSIC spectrum.
plotSpectrum(estimator,'NormalizeResponse',true)


## Compute DOA of Two Nearby Signals Using MUSIC

First, estimate the DOAs of two signals received by a standard 10-element ULA having an element spacing of one-half wavelength. Then, plot the spatial spectrum.

The antenna operating frequency is 150 MHz . The arrival directions of the two signals are separated by $2^{\circ}$. The direction of the first signal is $30^{\circ}$ azimuth and $0^{\circ}$ elevation. The direction of the second signal is $32^{\circ}$ azimuth and $0^{\circ}$ elevation. Estimate the number of signals using the Minimum Description Length (MDL) criterion.

Create the signals arriving at the ULA.

```
fs = 8000;
t = (0:1/fs:1).';
f1 = 300.0;
f2 = 600.0;
sig1 = cos(2*pi*t*f1);
sig2 = cos(2*pi*t*f2);
fc = 150.0e6;
c = physconst('LightSpeed');
lam = c/fc;
array = phased.ULA('NumElements',10,'ElementSpacing',0.5*lam);
sig = collectPlaneWave(array,[sig1 sig2],[30 0; 32 0]',fc);
noise = 0.1*(randn(size(sig)) + li*randn(size(sig)));
Estimate the DOAs.
```

```
estimator = phased.MUSICEstimator('SensorArray',array,...
```

estimator = phased.MUSICEstimator('SensorArray',array,...
'OperatingFrequency',fc,'DOAOutputPort',true,...
'OperatingFrequency',fc,'DOAOutputPort',true,...
'NumSignalsSource','Auto','NumSignalsMethod','MDL');
'NumSignalsSource','Auto','NumSignalsMethod','MDL');
[y,doas] = estimator(sig + noise);
[y,doas] = estimator(sig + noise);
doas = broadside2az(sort(doas),[0 0])
doas = broadside2az(sort(doas),[0 0])
doas = 1\times2
doas = 1\times2
30.0000 32.0000

```
    30.0000 32.0000
```

Plot the MUSIC spectrum.

```
plotSpectrum(estimator,'NormalizeResponse',true)
```



## Algorithms

## MUSIC Algorithm

MUSIC is a high-resolution direction-finding algorithm that estimates directions of arrival (DOA) of signals at an array from the covariance matrix of array sensor data. MUSIC belongs to the subspacedecomposition family of direction-finding algorithms. Unlike conventional beamforming, MUSIC can resolve closely spaced signal sources.

Based on eigenspace decomposition of the sensor covariance matrix, MUSIC divides the observation space into orthogonal signal and noise subspaces. Eigenvectors corresponding to the largest eigenvalues span the signal subspace. Eigenvectors corresponding to the smaller eigenvalues span the noise subspace. Because arrival (or steering) vectors lie in the signal subspace, they are orthogonal to the noise subspace. For ULAs, arrival vectors are functions of the broadside direction angles of the sources. The algorithm searches a grid of arrival angles to find the arrival vectors that have zero or small projections into the noise subspace. These angles are the directions of the sources.

MUSIC requires that the number of source signals is known. If the number of specified sources does not match the actual number of sources, the algorithm degrades. Generally, you must provide an estimate of the number of sources or use one of the built-in source number estimation methods. For a description of the methods used to estimate the number of sources, see the aictest or mdltest functions.

In place of the true sensor covariance matrix, the algorithm computes the sample covariance matrix from the sensor data. MUSIC applies to noncoherent signals but can be extended to coherent signals
using spatial smoothing and/or forward-backward averaging techniques. For a high-level description of the algorithm, see "MUSIC Super-Resolution DOA Estimation".

## Data Precision

This System object supports single and double precision for input data, properties, and arguments. If the input data $X$ is single precision, the output data is single precision. If the input data $X$ is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

## Version History

## Introduced in R2016b

## References

[1] Van Trees, H. L. Optimum Array Processing. New York: Wiley-Interscience, 2002.

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
See "System Objects in MATLAB Code Generation" (MATLAB Coder).
This System object supports single and double precision for input data, properties, and arguments. If the input data X is single precision, the output data is single precision. If the input data X is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

## See Also

## Functions

aictest|broadside2az|mdltest|rootmusicdoa|spsmooth

## Objects

phased.MUSICEstimator2D|phased.RootMUSICEstimator
Topics
"MUSIC Super-Resolution DOA Estimation"
"Direction of Arrival Estimation with Beamscan, MVDR, and MUSIC"
"High Resolution Direction of Arrival Estimation"
"Spherical Coordinates"

## plotSpectrum

System object: phased.MUSICEstimator
Package: phased
Plot MUSIC spectrum

## Syntax

plotSpectrum(estimator)
output_args = plotSpectrum(estimator,Name, Value)
lh = plotSpectrum( ___ )

## Description

plotSpectrum(estimator) plots the MUSIC spectrum computed by the most recent step method execution for the phased.MUSICEstimator System object, estimator.
output_args = plotSpectrum(estimator, Name, Value) plots the MUSIC spatial spectrum with additional options specified by one or more Name, Value pair arguments.
lh = plotSpectrum( $\qquad$ ) returns the line handle to the figure.

## Input Arguments

## estimator - MUSIC estimator

phased.MUSICEstimator System object.
MUSIC estimator, specified as a phased.MUSICEstimator System object

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Unit - Units used for plotting

'db' (default) | 'mag' | 'pow'
Units used for plotting, specified as the comma-separated pair consisting of 'Unit' and 'db', 'mag', or 'pow'.
Data Types: char

## NormalizeResponse - Plot normalized spectrum

## false (default) |true

Plot a normalized spectrum, specified as the comma-separated pair consisting of 'NormalizedResponse' and false or true. Normalization sets the magnitude of the largest spectrum value to one.

## Data Types: char

## Title - Title of plot

'MUSIC Spatial Spectrum' (default)| character vector
Title of plot, specified as a comma-separated pair consisting of 'Title' and a character vector.
Example: true
Data Types: char

## Output Arguments

## lh - Line handle of plot

line handle
Line handle of plot.

## Examples

## Plot MUSIC Spectrum of Two Signals Arriving at ULA

Estimate the DOAs of two signals received by a standard 10-element ULA having an element spacing of 1 meter. Then plot the MUSIC spectrum.

Create the ULA array. The antenna operating frequency is 150 MHz .

```
fc = 150.0e6;
array = phased.ULA('NumElements',10,'ElementSpacing',1.0);
```

Create the arriving signals at the ULA. The true direction of arrival of the first signal is $10^{\circ}$ in azimuth and $20^{\circ}$ in elevation. The direction of the second signal is $60^{\circ}$ in azimuth and $-5^{\circ}$ in elevation.

```
fs = 8000.0;
t = (0:1/fs:1).';
sig1 = cos(2*pi*t*300.0);
sig2 = cos(2*pi*t*400.0);
sig = collectPlaneWave(array,[sig1 sig2],[10 20; 60 -5]',fc);
noise = 0.1*(randn(size(sig)) + li*randn(size(sig)));
Estimate the DOAs.
```

```
estimator = phased.MUSICEstimator('SensorArray',array,...
```

estimator = phased.MUSICEstimator('SensorArray',array,...
'OperatingFrequency',fc,...
'OperatingFrequency',fc,...
'DOAOutputPort',true,'NumSignalsSource','Property',...
'DOAOutputPort',true,'NumSignalsSource','Property',...
'NumSignals',2);
'NumSignals',2);
[y,doas] = estimator(sig + noise);
[y,doas] = estimator(sig + noise);
doas = broadside2az(sort(doas),[20 -5])
doas = broadside2az(sort(doas),[20 -5])
doas = 1\times2
doas = 1\times2
9.5829 60.3813

```
    9.5829 60.3813
```

Plot the MUSIC spectrum.
plotSpectrum(estimator,'NormalizeResponse',true)


## Version History

Introduced in R2016b

## reset

System object: phased.MUSICEstimator
Package: phased
Reset states of System object

## Syntax

reset(estimator)

## Description

reset (estimator) resets the internal state of the phased.MUSICEstimator System object, estimator.

## Input Arguments

estimator - MUSIC estimator
phased.MUSICEstimator System object
MUSIC estimator, specified as a phased.MUSICEstimator System object.

## Version History

Introduced in R2016b

## step

System object: phased.MUSICEstimator
Package: phased
Estimate direction of arrival using MUSIC

## Syntax

spectrum = step(estimator,X)
[spectrum,doa] = step(estimator,X)

## Description

Note Instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj,x) and y = obj (x) perform equivalent operations.
spectrum = step(estimator, X ) returns the MUSIC spectrum for a signal specified by X .
[spectrum,doa] = step(estimator, X) also returns the signal broadside directions of arrival, doa. To use this syntax, set the DOAOutputPort property to true.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## estimator - MUSIC estimator

phased.MUSICEstimator System object
MUSIC estimator, specified as a phased.MUSICEstimator System object.
Example: phased.MUSICEstimator

## X - Received signal

$M$-by- $N$ complex-valued matrix
Received signal, specified as an $M$-by- $N$ complex-valued matrix. The quantity $M$ is the number of sample values (snapshots) contained in the signal, and $N$ is the number of sensor elements in the array.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

Example: [[0;1;2;3;4;3;2;1;0],[1;2;3;4;3;2;1;0;0]]
Data Types: double
Complex Number Support: Yes

## Output Arguments

## spectrum - MUSIC spatial spectrum

nonnegative, real-valued $K$-length column vector
MUSIC spatial spectrum, returned as a non-negative, real-valued $K$-length column vector representing the magnitude of the estimated MUSIC spatial spectrum. Each entry corresponds to an angle specified by the ScanAngles property.

## doa - Directions of arrival

real-valued $L$-length row vector
Directions of arrival of the signals, returned as a real-valued $L$-length row vector. The direction of arrival angle is the angle between the source direction and the array axis or broadside angle. Angle units are in degrees. $L$ is the number of signals specified by the NumSignals property or computed using the method specified by the NumSignalsMethod property.

## Dependencies

To enable this output argument, set the DOAOutputPort property to true.

## Examples

## Plot MUSIC Spectrum of Two Signals Arriving at ULA

Estimate the DOAs of two signals received by a standard 10-element ULA having an element spacing of 1 meter. Then plot the MUSIC spectrum.

Create the ULA array. The antenna operating frequency is 150 MHz .

```
fc = 150.0e6;
array = phased.ULA('NumElements',10,'ElementSpacing',1.0);
```

Create the arriving signals at the ULA. The true direction of arrival of the first signal is $10^{\circ}$ in azimuth and $20^{\circ}$ in elevation. The direction of the second signal is $60^{\circ}$ in azimuth and $-5^{\circ}$ in elevation.

```
fs = 8000.0;
t = (0:1/fs:1).';
sig1 = cos(2*pi*t*300.0);
sig2 = cos(2*pi*t*400.0);
sig = collectPlaneWave(array,[sig1 sig2],[10 20; 60 -5]',fc);
noise = 0.1*(randn(size(sig)) + 1i*randn(size(sig)));
Estimate the DOAs.
```

```
estimator = phased.MUSICEstimator('SensorArray',array,...
```

estimator = phased.MUSICEstimator('SensorArray',array,...
'OperatingFrequency',fc,...
'OperatingFrequency',fc,...
'DOAOutputPort',true,'NumSignalsSource','Property',...
'DOAOutputPort',true,'NumSignalsSource','Property',...
'NumSignals',2);

```
    'NumSignals',2);
```

```
[y,doas] = estimator(sig + noise);
doas = broadside2az(sort(doas),[20 -5])
doas = 1\times2
    9.5829 60.3813
```

Plot the MUSIC spectrum.
plotSpectrum(estimator,'NormalizeResponse',true)


## Compute DOA of Two Nearby Signals Using MUSIC

First, estimate the DOAs of two signals received by a standard 10-element ULA having an element spacing of one-half wavelength. Then, plot the spatial spectrum.

The antenna operating frequency is 150 MHz . The arrival directions of the two signals are separated by $2^{\circ}$. The direction of the first signal is $30^{\circ}$ azimuth and $0^{\circ}$ elevation. The direction of the second signal is $32^{\circ}$ azimuth and $0^{\circ}$ elevation. Estimate the number of signals using the Minimum Description Length (MDL) criterion.

Create the signals arriving at the ULA.
fs = 8000;
$t=(0: 1 / f s: 1) . ' ;$

```
f1 = 300.0;
f2 = 600.0;
sig1 = cos(2*pi*t*f1);
sig2 = cos(2*pi*t*f2);
fc = 150.0e6;
c = physconst('LightSpeed');
lam = c/fc;
array = phased.ULA('NumElements',10,'ElementSpacing',0.5*lam);
sig = collectPlaneWave(array,[sig1 sig2],[30 0; 32 0]',fc);
noise = 0.1*(randn(size(sig)) + 1i*randn(size(sig)));
```

Estimate the DOAs.

```
estimator = phased.MUSICEstimator('SensorArray',array,...
    'OperatingFrequency',fc,'DOAOutputPort',true,...
    'NumSignalsSource','Auto','NumSignalsMethod','MDL');
[y,doas] = estimator(sig + noise);
doas = broadside2az(sort(doas),[0 0])
doas = 1\times2
    30.0000 32.0000
```

Plot the MUSIC spectrum.
plotSpectrum(estimator,'NormalizeResponse',true)


# Version History <br> Introduced in R2016b 

# phased.MUSICEstimator2D 

Package: phased
Estimate 2D direction of arrival using narrowband MUSIC algorithm

## Description

The phased.MUSICEstimator2D System object implements the narrowband multiple signal classification (MUSIC) algorithm for 2-D planar or 3-D arrays such as a uniform rectangular array (URA). MUSIC is a high-resolution direction-finding algorithm capable of resolving closely-spaced signal sources. The algorithm is based on the eigenspace decomposition of the sensor covariance matrix.

To estimate directions of arrival (DOA):
1 Define and set up a phased.MUSICEstimator2D System object. See "Construction" on page 11060.

2 Call the step method to estimate the DOAs according to the properties of phased.MUSICEstimator2D.

Note Instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, $\mathrm{y}=\mathrm{step}(\mathrm{obj}, \mathrm{x}$ ) and $\mathrm{y}=$ obj (x) perform equivalent operations.

## Construction

estimator = phased.MUSICEstimator2D creates a MUSIC DOA estimator System object, estimator.
estimator $=$ phased.MUSICEstimator2D(Name, Value) creates a System object, estimator, with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN).

## Properties

## SensorArray - Sensor array

phased.ULA array with default array properties (default) | Phased Array System Toolbox array System object

Sensor array, specified as a Phased Array System Toolbox array System object.
Example: phased.URA

## PropagationSpeed - Signal propagation speed

physconst('LightSpeed') (default)| real-valued positive scalar
Signal propagation speed, specified as a real-valued positive scalar. Units are in meters per second. The default propagation speed is the value returned by physconst('LightSpeed').

Example: 3e8
Data Types: single|double

## OperatingFrequency - Operating frequency

300e6 (default) | positive scalar
Operating frequency, specified as a positive scalar. Units are in Hz.
Example: 1e9
Data Types: single|double

## ForwardBackwardAveraging - Enable forward-backward averaging

## false (default) | true

Enable forward-backward averaging, specified as false or true. Set this property to true to use forward-backward averaging to estimate the covariance matrix for sensor arrays with a conjugate symmetric array manifold.

Data Types: logical

## AzimuthScanAngles - Azimuth scan angles

[-90:90] (default) | real-valued row vector
Azimuth scan angles, specified as a or real-valued row vector. Angle units are in degrees. The angle values must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive, and be in ascending order.
Example: [-30:20]
Data Types: single | double

## ElevationScanAngles - Elevation scan angles <br> 0 (default) | real-valued row vector

Elevation scan angles, specified as a real-valued row vector. Angle units are in degrees. The angle values must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive, and be in ascending order.
Example: [-70:75]
Data Types: single | double

## DOAOutputPort - Enable directions of arrival output <br> false (default) | true

Option to enable directions-of-arrival (DOA) output, specified as false or true. To obtain the DOA of signals, set this property to true. The DOAs are returned in the second output argument when the object is executed.

## Data Types: logical

## NumSignalsSource - Source of number of signals

'Auto' (default)|'Property'
Source of the number of arriving signals, specified as 'Auto' or 'Property'.

- 'Auto ' - The System object estimates the number of arriving signals using the method specified in the NumSignalsMethod property.
- 'Property ' - Specify the number of arriving signals using the NumSignals property.

Data Types: char
NumSignalsMethod - Method used to estimate number of arriving signals
'AIC' (default)|'MDL'
Method used to estimate the number of arriving signals, specified as 'AIC' or 'MDL'.

- 'AIC' - Akaike Information Criterion
- 'MDL' - Minimum Description Length criterion


## Dependencies

To enable this property, set NumSignalsSource to 'Auto '.
Data Types: char

## NumSignals - Number of arriving signals

1 (default) | positive integer
Number of arriving signals for DOA estimation, specified as a positive integer.
Example: 3
Dependencies
To enable this property, set NumSignalsSource to 'Property '.
Data Types: single | double

## Methods

| plotSpectrum | Plot 2-D MUSIC spectrum |
| :--- | :--- |
| reset | Reset states of System object |
| step | Estimate direction of arrival using 2-D MUSIC |

Common to All System Objects
release Allow System object property value changes

## Examples

## Estimate DOAs of Two Signals

Assume that two sinusoidal waves of frequencies 450 Hz and 600 Hz strike a URA from two different directions. Signals arrive from - $37^{\circ}$ azimuth, $0^{\circ}$ elevation and $17^{\circ}$ azimuth, $20^{\circ}$ elevation. Use 2-D MUSIC to estimate the directions of arrival of the two signals. The array operating frequency is 150 MHz and the signal sampling frequency is 8 kHz .
$\mathrm{f} 1=450.0$;
f2 = 600.0;
doal = [-37;0];
doa2 = [17;20];

```
fc = 150e6;
c = physconst('LightSpeed');
lam = c/fc;
fs = 8000;
```

Create the URA with default isotropic elements. Set the frequency response range of the elements.
array = phased.URA('Size',[11 11],'ElementSpacing',[lam/2 lam/2]);

```
array.Element.FrequencyRange = [50.0e6 500.0e6];
```

Create the two signals and add random noise.
$\mathrm{t}=(0: 1 / \mathrm{fs}: 1) \mathrm{I}^{\prime}$;
$\mathrm{x} 1=\cos (2 * \mathrm{pi} * \mathrm{t} * \mathrm{f} 1)$;
$x 2=\cos \left(2 *\right.$ pi $\left.^{*} t * f 2\right)$;
$\mathrm{x}=$ collectPlaneWave(array,[x1 x2],[doa1,doa2],fc);
noise $=0.1^{*}\left(\operatorname{randn}(\operatorname{size}(x))+1 i^{*}\right.$ randn(size(x)));

Create and execute the 2-D MUSIC estimator to find the directions of arrival.

```
estimator = phased.MUSICEstimator2D('SensorArray',array,...
    'OperatingFrequency',fc,...
    'NumSignalsSource','Property',...
    'DOAOutputPort',true,'NumSignals',2,...
    'AzimuthScanAngles',-50:.5:50,...
    'ElevationScanAngles',-30:.5:30);
[~,doas] = estimator(x + noise)
doas = 2\times2
    -37 17
        0 20
```

The estimated DOAs exactly match the true DOAs.
Plot the 2-D spatial spectrum.

```
plotSpectrum(estimator);
```



## Estimate DOAs of Two Signals at Disk Array

Assume that two sinusoidal waves of frequencies 1.6 kHz and 1.8 kHz strike a disk array from two different directions. The spacing between elements of the disk is $1 / 2$ wavelength. Signals arrive from $-31^{\circ}$ azimuth, $-11^{\circ}$ elevation and $35^{\circ}$ azimuth, $55^{\circ}$ elevation. Use 2-D MUSIC to estimate the directions of arrival of the two signals. The array operating frequency is 300 MHz and the signal sampling frequency is 8 kHz .

```
f1 = 1.6e3;
f2 = 1.8e3;
doal = [-31;-11];
doa2 = [35;55];
fc = 300e6;
c = physconst('LightSpeed');
lam = c/fc;
fs = 8.0e3;
```

Create a conformal array with default isotropic elements. First, create a URA to get the element positions.

```
uraarray = phased.URA('Size',[21 21],'ElementSpacing',[lam/2 lam/2]);
pos = getElementPosition(uraarray);
```

Extract a subset of these to form an inscribed disk.

```
radius = 10.5*lam/2;
pos(:,sum(pos.^2) > radius^2) = [];
```

Then, create the conformal array using these positions.

```
confarray = phased.ConformalArray('ElementPosition',pos);
viewArray(confarray)
```


## Array Geometry



Array Span:
X axis $=0.000 \mathrm{~m}$
$\mathrm{Y}_{\text {axis }}=9.993 \mathrm{~m}$
Z axis $=9.993 \mathrm{~m}$

Set the frequency response range of the elements.

```
confarray.Element.FrequencyRange = [50.0e6 600.0e6];
```

Create the two signals and add random noise.

```
t = (0:1/fs:1.5).';
x1 = cos(2*pi*t*f1);
x2 = cos(2*pi*t*f2);
x = collectPlaneWave(confarray,[x1 x2],[doa1,doa2],fc);
noise = 0.1*(randn(size(x)) + li*randn(size(x)));
```

Create and execute the 2-D MUSIC estimator to find the directions of arrival.

```
estimator = phased.MUSICEstimator2D('SensorArray',confarray,...
    'OperatingFrequency',fc,...
    'NumSignalsSource','Property',...
    'DOAOutputPort',true,'NumSignals',2,...
    'AzimuthScanAngles',-60:.1:60,...
    'ElevationScanAngles',-60:.1:60);
[~,doas] = estimator(x + noise)
```

```
doas = 2×2
    35 -31
    55 -11
```

The estimated DOAs exactly match the true DOAs.
Plot the 2-D spatial spectrum.
plotSpectrum(estimator);


## Algorithms

## MUSIC Algorithm

MUSIC stands for MUltiple SIgnal Classification. MUSIC is a high-resolution direction-finding algorithm that estimates directions of arrival (DOA) of signals at an array from the covariance matrix of array sensor data. MUSIC belongs to the subspace-decomposition family of direction-finding algorithms. Unlike conventional beamforming, MUSIC can resolve closely-spaced signal sources.

Based on eigenspace decomposition of the sensor covariance matrix, MUSIC divides the observation space into orthogonal signal and noise subspaces. Eigenvectors corresponding to the largest eigenvalues span the signal subspace. Eigenvectors corresponding to the smaller eigenvalues span the noise subspace. Because arrival (or steering) vectors lie in the signal subspace, they are
orthogonal to the noise subspace. The arrival vectors depend on the direction of arrival of a signals. For a 2-D or 3-D array. the directions are determined by the azimuth and elevation of the sources. By searching over a grid of arrival angles, the algorithm finds those arrival vectors whose projection into the noise subspace is zero or at least very small.

MUSIC requires that the number of source signals is known. The algorithm degrades if the number of specified sources does not match the actual number of sources. Generally, you must provide an estimate of the number of sources or use one of the built-in source number estimation methods. For a description of the methods used to estimate the number of sources, see the aictest or mdltest functions.

In place of the true sensor covariance matrix, the algorithm computes the sample covariance matrix from the sensor data. MUSIC applies to noncoherent signals but can be extended to coherent signals using forward-backward averaging techniques. For a high-level description of the algorithm, see "MUSIC Super-Resolution DOA Estimation".

## Data Precision

This System object supports single and double precision for input data, properties, and arguments. If the input data $X$ is single precision, the output data is single precision. If the input data $X$ is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

## Version History

## Introduced in R2016b

## References

[1] Van Trees, H. L., Optimum Array Processing. New York: Wiley-Interscience, 2002.

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
See "System Objects in MATLAB Code Generation" (MATLAB Coder).
This System object supports single and double precision for input data, properties, and arguments. If the input data $X$ is single precision, the output data is single precision. If the input data $X$ is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

## See Also

## Functions

aictest|mdltest|musicdoa|rootmusicdoa

## Objects

phased.MUSICEstimator|phased.RootMUSICEstimator

Topics<br>"MUSIC Super-Resolution DOA Estimation"<br>"Direction of Arrival Estimation with Beamscan, MVDR, and MUSIC"<br>"High Resolution Direction of Arrival Estimation"<br>"Spherical Coordinates"

## plotSpectrum

System object: phased.MUSICEstimator2D
Package: phased
Plot 2-D MUSIC spectrum

## Syntax

plotSpectrum(estimator)
output_args = plotSpectrum(estimator, Name, Value)
lh = plotSpectrum( ___ )

## Description

plotSpectrum(estimator) plots the 2-D MUSIC spatial spectrum computed by the most recent step method execution for the phased.MUSICEstimator2D, estimator.
output_args = plotSpectrum(estimator,Name, Value) plots the 2-D MUSIC spatial spectrum with additional options specified by one or more Name, Value pair arguments.
lh = plotSpectrum( $\qquad$ ) returns the line handle to the figure.

## Input Arguments

## estimator - 2-D MUSIC estimator

phased.MUSICEstimator2D System object
2-D MUSIC estimator, specified as a phased.MUSICEstimator2D System object.

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Unit - Units used for plotting

'db' (default) | 'mag' | 'pow'
Units used for plotting, specified as the comma-separated pair consisting of 'Unit' and 'db', 'mag', or 'pow'.
Data Types: char

## NormalizeResponse - Plot normalized spectrum

## false (default) |true

Plot a normalized spectrum, specified as the comma-separated pair consisting of 'NormalizedResponse' and false or true. Normalization sets the magnitude of the largest spectrum value to one.

## Example: true

## Data Types: char

## Title - Title of plot

'2D MUSIC Spatial Spectrum' (default)| character vector
Title of plot, specified as a comma-separated pair consisting of 'Title' and a character vector.
Example: true
Data Types: char

## Output Arguments

## lh - Line handle of plot

line handle
Line handle of plot.

## Examples

## Estimate DOAs of Two Signals

Assume that two sinusoidal waves of frequencies 450 Hz and 600 Hz strike a URA from two different directions. Signals arrive from - $37^{\circ}$ azimuth, $0^{\circ}$ elevation and $17^{\circ}$ azimuth, $20^{\circ}$ elevation. Use 2-D MUSIC to estimate the directions of arrival of the two signals. The array operating frequency is 150 MHz and the signal sampling frequency is 8 kHz .

```
f1 = 450.0;
f2 = 600.0;
doal = [-37;0];
doa2 = [17;20];
fc = 150e6;
c = physconst('LightSpeed');
lam = c/fc;
fs = 8000;
```

Create the URA with default isotropic elements. Set the frequency response range of the elements.

```
array = phased.URA('Size',[11 11],'ElementSpacing',[lam/2 lam/2]);
array.Element.FrequencyRange = [50.0e6 500.0e6];
```

Create the two signals and add random noise.

```
t = (0:1/fs:1).';
x1 = cos(2*pi*t*f1);
x2 = cos(2*pi*t*f2);
x = collectPlaneWave(array,[x1 x2],[doa1,doa2],fc);
noise = 0.1*(randn(size(x))+li*randn(size(x)));
```

Create and execute the 2-D MUSIC estimator to find the directions of arrival.

```
estimator = phased.MUSICEstimator2D('SensorArray',array,...
    'OperatingFrequency',fc,...
    'NumSignalsSource','Property',...
```

```
    'DOA0utputPort',true,'NumSignals',2,...
    'AzimuthScanAngles',-50:.5:50,...
    'ElevationScanAngles',-30:.5:30);
[~,doas] = estimator(x + noise)
doas = 2\times2
    -37 17
    0 20
```

The estimated DOAs exactly match the true DOAs.
Plot the 2-D spatial spectrum.
plotSpectrum(estimator) ;


## Version History

Introduced in R2016b

## reset

System object: phased.MUSICEstimator2D
Package: phased
Reset states of System object

## Syntax

reset(estimator)

## Description

reset (estimator) resets the internal state of the phased.MUSICEstimator2D System object, estimator.

## Input Arguments

estimator - 2-D MUSIC estimator
phased.MUSICEstimator2D System object
2-D MUSIC estimator, specified as a phased.MUSICEstimator2D System object.

## Version History

Introduced in R2016b

## step

System object: phased.MUSICEstimator2D
Package: phased
Estimate direction of arrival using 2-D MUSIC

## Syntax

spectrum = step(estimator,X)
[spectrum,doa] = step(estimator,X)

## Description

Note Instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj,x) and y = obj $(x)$ perform equivalent operations.
spectrum $=$ step(estimator, X ) returns the 2-D MUSIC spectrum of a signal specified in X .
[spectrum,doa] = step(estimator,X) also returns the signal directions of arrival angles, doa.
To use this syntax, set the DOAOutputPort property to true.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## estimator - 2-D MUSIC estimator

phased.MUSICEstimator2D System object
2-D MUSIC estimator, specified as a phased.MUSICEstimator2D System object.

## X - Received signal

$M$-by- $N$ complex-valued matrix
Received signal, specified as an $M$-by- $N$ complex-valued matrix. The quantity $M$ is the number of sample values (snapshots) contained in the signal and $N$ is the number of sensor elements in the array.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
Example: [[0;1;2;3;4;3;2;1;0],[1;2;3;4;3;2;1;0;0]]

Data Types: single|double
Complex Number Support: Yes

## Output Arguments

## spectrum - 2-D MUSIC spatial spectrum

nonnegative, real-valued $K$-length column vector
2-D MUSIC spatial spectrum, returned as a nonnegative, real-valued $K$-length column vector representing the magnitude of the estimated MUSIC spatial spectrum. Each entry corresponds to an angle specified by the AzimuthScanAngles and ElevationScanAngles properties.

## doa - Directions of arrival

real-valued 2-by-L matrix
Directions of arrival of the signals, returned as a real-valued 2-by-L matrix. The direction of arrival angle is defined by the azimuth and elevation angles of the source with respect to the array local coordinate system. The first row of the matrix contains the azimuth angles and the second row contains the elevation angles. Angle units are in degrees. $L$ is the number of signals specified by the NumSignals property or derived using the method specified by the NumSignalsMethod property.

## Dependencies

To enable this output argument, set the DOAOutputPort property to true.

## Examples

## Estimate DOAs of Two Signals

Assume that two sinusoidal waves of frequencies 450 Hz and 600 Hz strike a URA from two different directions. Signals arrive from $-37^{\circ}$ azimuth, $0^{\circ}$ elevation and $17^{\circ}$ azimuth, $20^{\circ}$ elevation. Use 2-D MUSIC to estimate the directions of arrival of the two signals. The array operating frequency is 150 MHz and the signal sampling frequency is 8 kHz .

```
f1 = 450.0;
f2 = 600.0;
doa1 = [-37;0];
doa2 = [17;20];
fc = 150e6;
c = physconst('LightSpeed');
lam = c/fc;
fs = 8000;
```

Create the URA with default isotropic elements. Set the frequency response range of the elements.

```
array = phased.URA('Size',[11 11],'ElementSpacing',[lam/2 lam/2]);
array.Element.FrequencyRange = [50.0e6 500.0e6];
```

Create the two signals and add random noise.

```
t = (0:1/fs:1).';
x1 = cos(2*pi*t*f1);
x2 = cos(2*pi*t*f2);
x = collectPlaneWave(array,[x1 x2],[doa1,doa2],fc);
noise = 0.1*(randn(size(x))+li*randn(size(x)));
```

Create and execute the 2-D MUSIC estimator to find the directions of arrival.

```
estimator = phased.MUSICEstimator2D('SensorArray',array,...
    'OperatingFrequency',fc,...
    'NumSignalsSource','Property ',...
    'DOAOutputPort',true,'NumSignals',2,...
    'AzimuthScanAngles',-50:.5:50,...
    'ElevationScanAngles',-30:.5:30);
[~,doas] = estimator(x + noise)
doas = 2\times2
    -37 17
    00
```

The estimated DOAs exactly match the true DOAs.
Plot the 2-D spatial spectrum.
plotSpectrum(estimator);


## Estimate DOAs of Two Signals at Disk Array

Assume that two sinusoidal waves of frequencies 1.6 kHz and 1.8 kHz strike a disk array from two different directions. The spacing between elements of the disk is $1 / 2$ wavelength. Signals arrive from
$-31^{\circ}$ azimuth, $-11^{\circ}$ elevation and $35^{\circ}$ azimuth, $55^{\circ}$ elevation. Use 2-D MUSIC to estimate the directions of arrival of the two signals. The array operating frequency is 300 MHz and the signal sampling frequency is 8 kHz .

```
f1 = 1.6e3;
f2 = 1.8e3;
doal = [-31;-11];
doa2 = [35;55];
fc = 300e6;
c = physconst('LightSpeed');
lam = c/fc;
fs = 8.0e3;
```

Create a conformal array with default isotropic elements. First, create a URA to get the element positions.

```
uraarray = phased.URA('Size',[21 21],'ElementSpacing',[lam/2 lam/2]);
pos = getElementPosition(uraarray);
```

Extract a subset of these to form an inscribed disk.

```
radius = 10.5*lam/2;
pos(:,sum(pos.^2) > radius^2) = [];
```

Then, create the conformal array using these positions.

```
confarray = phased.ConformalArray('ElementPosition',pos);
viewArray(confarray)
```


## Array Geometry




Set the frequency response range of the elements.

```
confarray.Element.FrequencyRange = [50.0e6 600.0e6];
```

Create the two signals and add random noise.

```
t = (0:1/fs:1.5).';
x1 = cos(2*pi*t*f1);
x2 = cos(2*pi*t*f2);
x = collectPlaneWave(confarray,[x1 x2],[doa1,doa2],fc);
noise = 0.1*(randn(size(x)) + li*randn(size(x)));
```

Create and execute the 2-D MUSIC estimator to find the directions of arrival.

```
estimator = phased.MUSICEstimator2D('SensorArray',confarray,...
    'OperatingFrequency',fc,...
    'NumSignalsSource','Property',...
    'DOAOutputPort',true,'NumSignals',2,...
    'AzimuthScanAngles',-60:.1:60,...
    'ElevationScanAngles',-60:.1:60);
[~,doas] = estimator(x + noise)
doas = 2\times2
    35 -31
    55 -11
```

The estimated DOAs exactly match the true DOAs.
Plot the 2-D spatial spectrum.
plotSpectrum(estimator);


Version History
Introduced in R2016b

## phased.NRAntennaElement

Package: phased
5G antenna element described in 3GPP TR 38.901 specification

## Description

The NRAntennaElement System object models an antenna designed to meet the 3GPP TR 38.901 standard [1].

To compute the response of the antenna element for specified directions:
1 Create the phased.NRAntennaElement object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

antenna = phased.NRAntennaElement antenna $=$ phased.NRAntennaElement (Name, Value)

## Description

antenna = phased.NRAntennaElement creates an NR antenna System object, antenna, that follows the standard specified in 3GPP TR 38.901 [1].
antenna = phased.NRAntennaElement (Name, Value) creates an NR antenna element object, antenna, and sets each specified property set to the specified value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN).

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## FrequencyRange - Operating frequency range

[0 le20] (default) | nonnegative, real-valued 1-by-2 row vector
Operating frequency range of the antenna, specified as a nonnegative, real-valued, 1-by-2 row vector in the form [LowerBound HigherBound]. The antenna element has no response outside the specified frequency range. Units are in Hz .

## Data Types: double

## PolarizationAngle - Polarization slant angle

0.0 (default) | real scalar

Polarization slant angle of the antenna, specified as a scalar. The polarization slant angle is defined in section 7.3.2 of the 3GPP TR 38.901 Release 14 [1]. Units are in degrees.

Example: 45.0
Data Types: double

## PolarizationModel - Polarization model

2 (default) | 1
Polarization model, specified as either 1 or 2 . The polarization models are defined in section 7.3 .2 of the 3GPP TR 38.901 Release 14 [1].

## Example: 1

Data Types: double

## Beamwidth - Beamwidth of antenna pattern

[65 65] (default) | scalar | 1-by-2 real-valued vector
Beamwidth of the antenna pattern, specified as either a scalar or a 1-by-2 real-valued vector. When the specified value is a 1-by-2 vector, it has the form of [AzimuthBeamwidth
ElevationBeamwidth]. If the specified value is a scalar, the azimuth and elevation beamwidths are equal. Units are in degrees.

Example: 40
Data Types: double

## SidelobeLevel - Attenuation of maximum sidelobe level

[30 30] (default) | positive scalar | 1-by-2 real-valued vector of positive numbers
Attenuation of maximum sidelobe level of the antenna pattern, specified as either a positive scalar or a 1-by-2 real-valued vector of positive numbers. When the specified value is a 1 -by- 2 vector, it has the form of [AzimuthSidelobe ElevationSidelobe]. If the specified value is a scalar, the azimuth and elevation sidelobe levels are equal. Units are in dB .

Example: 24
Data Types: double

## MaximumAttenuation - Maximum pattern attenuation

30 (default) | positive scalar
Maximum attenuation to the main lobe in the antenna pattern specified as a positive scalar. This value should be no less than the values specified in the SidelobeLevel property. Units are in dB.

Example: 28
Data Types: double
MaximumGain - Maximum gain in the main lobe
8 (default) | positive scalar
Maximum gain of the main lobe in the antenna pattern specified as a positive scalar. Units are in dB.

Example: 5
Data Types: double

## Usage

## Syntax

RESP = antenna(FREQ,ANG)

## Description

RESP = antenna(FREQ, ANG) returns the antenna voltage response RESP at the operating frequencies specified in FREQ and directions specified in ANG.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## FREQ - Operating frequency of antenna element

nonnegative scalar | nonnegative, real-valued 1-by- $L$ row vector
Operating frequency of the antenna element, specified as a nonnegative scalar or nonnegative, realvalued 1-by-L row vector. Frequency units are in Hz.

FREQ must lie within the range of values specified by the FrequencyRange or the FrequencyVector property of the element. Otherwise, the element produces no response and the response is returned as -Inf. Element objects use the FrequencyRange property, except for phased. CustomAntennaElement, which uses the FrequencyVector property.

Example: [1e8 2e6]
Data Types: double

## ANG - Azimuth and elevation angles of response directions

## real-valued 1-by- $M$ row vector | real-valued 2-by-M matrix

Azimuth and elevation angles of the response directions, specified as a real-valued 1-by- $M$ row vector or a real-valued 2-by- $M$ matrix, where $M$ is the number of angular directions. Angle units are in degrees. The azimuth angle must lie in the range $-180^{\circ}$ to $180^{\circ}$, inclusive. The elevation angle must lie in the range $-90^{\circ}$ to $90^{\circ}$, inclusive.

- If ANG is a 1-by- $M$ vector, each element specifies the azimuth angle of the direction. In this case, the corresponding elevation angle is assumed to be zero.
- If ANG is a 2-by-M matrix, each column of the matrix specifies the direction in the form [azimuth;elevation].

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the $x y$-plane. This angle is positive when measured from the $x$-axis toward the $y$-axis. The elevation angle
is the angle between the direction vector and $x y$-plane. This angle is positive when measured toward the $z$-axis. See the definition of "Azimuth and Elevation Angles".
Example: [110 125; 15 10]
Data Types: double

## Output Arguments

RESP - Voltage response of antenna
complex-valued $M$-by- $L$ matrix
Voltage response of the antenna element, returned as a complex-valued $M$-by- $L$ matrix. In this matrix, $M$ represents the number of angles specified in ANG and $L$ represents the number of frequencies specified in FREQ.
Data Types: double

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```


## Specific to Antenna and Transducer Element System Objects

beamwidth
directivity
isPolarizationCapable
pattern
patternAzimuth
patternElevation

Compute and display beamwidth of sensor element pattern Directivity of antenna or transducer element Antenna element polarization capability Plot antenna or transducer element directivity and patterns Plot antenna or transducer element directivity and pattern versus azimuth Plot antenna or transducer element directivity and pattern versus elevation

## Common to All System Objects

step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object

## Examples

## Create NR Antenna Element

Construct an antenna based on the 3GPP 38.901 standard and plot its elevation response at 6 MHz .

```
antenna = phased.NRAntennaElement;
fc = 6e9;
pattern(antenna,fc,-180:180,0,'CoordinateSystem','polar');
```



Directivity (dBi), Broadside at $0.00^{\circ}$

Find the response of the antenna at the boresight.

```
ang = [0;0];
resp = antenna(fc,ang)
resp = struct with fields:
    H: 0
    V: -2.5119
```


## Construct NR Antenna with Polarization Model

Construct an NR antenna based on the 3GPP 38.901 standard with its Polarization Model set to "1". Then, find its response at boresight. Finally, plot its antenna response as a function of azimuth angle at 6 GHz .

```
    element = phased.NRAntennaElement('PolarizationModel',1);
    fc = 6e9;
    ang = [0;0];
    resp = element(fc,ang)
resp = struct with fields:
    H: 0
    V: -2.5119
```

Plot the antenna pattern at 0 degrees elevation for all azimuth angles.
pattern(element,fc,-180:180,0,'CoordinateSystem','polar')


Directivity (dBi), Broadside at $0.00^{\circ}$

## Construct NR Antenna with Specified Beamwidth

Construct an NR antenna based on the 3GPP 38.901 standard. Set the antenna beamwidth to 45 degrees in azimuth and 30 degrees in elevation. Find the antenna response at boresight. Then, plot the antenna response as a function of azimuth and elevation at 6 GHz .

```
    element = phased.NRAntennaElement('Beamwidth',[45,30]);
    fc = 6.0e9;
    ang = [0;0];
    resp = element(fc,ang)
resp = struct with fields:
    H: 0
    V: -2.5119
```

Plot the 3D antenna pattern for all azimuth angles and elevation angles.

```
pattern(element,fc,-180:180,-90:90,'CoordinateSystem','polar')
```



## Version History

Introduced in R2021a

## References

[1] 5G: Study on channel model for frequencies from 0.5 to 100 GHz , 3GPP TR38.901 Version 14.0.0 Release 14.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{Tm}}$.
Usage notes and limitations:
"System Objects in MATLAB Code Generation" (MATLAB Coder)

## See Also

phased.NRRectangularPanelArray

# phased.NRRectangularPanelArray 

Package: phased

5G antenna array described in 3GPP TR 38.901 specification

## Description

The phased.NRRectangularPanelArray System object creates a rectangular antenna array designed to meet the 3GPP TR 38.901 standard. This object models an antenna pattern generated by multiple panels in a rectangular layout. Each panel is a heterogeneous array consisting of co-located antenna elements. The default set of antenna elements is a pair of phased. NRAntennaElement antenna elements having $+45^{\circ}$ and $-45^{\circ}$ as the polarization slant angles. The default configuration of each panel is a 2-by-2 antenna configuration. You can also create an array using other types of elements. Elements and panels lie in the $y z$-plane.

To compute the response of the antenna element for specified directions:
1 Create the phased.NRRectangularPanelArray object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

array = phased.NRRectangularPanelArray
array = phased.NRRectangularPanelArray(Name,Value)

## Description

array = phased.NRRectangularPanelArray creates an NR antenna panel array System object, array that follows the specification described in the 3GPP TR 38.901.
array = phased.NRRectangularPanelArray(Name,Value) creates an NR rectangular panel array object, array, with each specified property set to the specified value. You can specify additional name-value arguments in any order as (Name1,Value1,...,NameN,ValueN).

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## ElementSet - Antenna elements

1-by-2 cell array (default) | 1-by-1 cell array
Antenna elements, specified as a 1-by-2 cell array or 1 -by-1 cell array. The default value is a 1 -by- 2 cell array containing two phased.NRAntennaElement antenna elements with a selected polarization model of 2 - one with a $-45^{\circ}$ polarization angle and the other with a $+45^{\circ}$ polarization angle.

## Size - Sizes of element grid and panel grid

[2 $2 l^{2} 1$ 1] (default)| 1-by-4 vector of positive integer values
Sizes of element grid and panel grid, specified as a 1-by-4 vector of positive integer values. The first two entries represent the number of elements in a panel and the last two entries represent the number of panels in the array.. The default value is one panel grid with a panel size of 2-by-2 elements.

Example: [2 2422 2
Data Types: double

## Spacing - Spacing between elements and between panels

[0.5 0.5 1.0 1.0] (default)| 1-by-4 vector of real positive values
Spacing between elements and between panels, specified as a 1-by-4 positive vector. The first two entries represent the spacing between elements within the panel and the remaining values in the represent the spacing between panels in the array. Units are in meters.
Example: [0.75 0.75 1.0 1.0]
Data Types: double

## Taper - Array element tapers

1 (default) | complex scalar | length- $N$ complex-valued vector
Array element tapers, specified as a complex scalar or a length- $N$ complex-valued vector of weights applied to each element in the sensor array. $N$ is the number of elements in the array. If Taper is a scalar, identical weights are applied to each element. If Taper is a vector, each weight is applied to the corresponding array element.
Example: 1
Data Types: double
Complex Number Support: Yes

## Usage

## Syntax

RESP = array(FREQ,ANG)

## Description

RESP = array (FREQ,ANG) returns the array voltage response, RESP, at the operating frequencies specified in FREQ and in directions specified in ANG.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## FREQ - Operating frequency of antenna element

nonnegative scalar | nonnegative, real-valued 1-by-L row vector
Operating frequency of the antenna element, specified as a nonnegative scalar or nonnegative, realvalued 1 -by- L row vector. Frequency units are in Hz .

FREQ must lie within the range of values specified by the FrequencyRange or the FrequencyVector property of the element. Otherwise, the element produces no response and the response is returned as -Inf. Element objects use the FrequencyRange property, except for phased.CustomAntennaElement, which uses the FrequencyVector property.

Example: [1e8 2e6]
Data Types: double

## ANG - Azimuth and elevation angles of response directions

real-valued 1-by-M row vector | real-valued 2-by-M matrix
Azimuth and elevation angles of the response directions, specified as a real-valued 1-by-M row vector or a real-valued 2-by- $M$ matrix, where $M$ is the number of angular directions. Angle units are in degrees. The azimuth angle must lie in the range $-180^{\circ}$ to $180^{\circ}$, inclusive. The elevation angle must lie in the range $-90^{\circ}$ to $90^{\circ}$, inclusive.

- If ANG is a 1 -by- $M$ vector, each element specifies the azimuth angle of the direction. In this case, the corresponding elevation angle is assumed to be zero.
- If ANG is a 2 -by- $M$ matrix, each column of the matrix specifies the direction in the form [azimuth;elevation].

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the $x y$-plane. This angle is positive when measured from the $x$-axis toward the $y$-axis. The elevation angle is the angle between the direction vector and $x y$-plane. This angle is positive when measured toward the $z$-axis. See the definition of "Azimuth and Elevation Angles".

Example: [110 125; 15 10]
Data Types: double

## Output Arguments

## RESP - Voltage response of array

complex-valued M-by-L matrix
Voltage response of the array, returned as a complex-valued $M$-by- $L$ matrix. In this matrix, $M$ represents the number of angles specified in ANG and $L$ represents the number of frequencies specified in FREQ.
Data Types: double

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```


## Specific to Antenna and Transducer Array System Objects

| beamwidth | Compute and display beamwidth of an array |
| :--- | :--- |
| collectPlaneWave | Simulate received plane waves at array |
| directivity | Compute array directivity |
| getElementNormal | Normal vectors for array elements |
| getElementPosition | Positions of array elements |
| getNumElements | Number of elements in an array |
| getTaper | Array element tapers |
| isPolarizationCapable | Array polarization capability |
| pattern | Plot array directivity and patterns |
| patternAzimuth | Plot array directivity or pattern versus azimuth |
| patternElevation | Plot array directivity or pattern versus elevation |
| perturbations | Perturbations defined on array |
| perturbedArray | Apply perturbations to phased array |
| perturbedPattern | Display pattern of perturbed array |
| viewArray | View array geometry |

## Common to All System Objects

| step | Run System object algorithm |
| :--- | :--- |
| release | Release resources and allow changes to System object property values and input <br> characteristics |
| reset | Reset internal states of System object |

## Examples

## Plot Response of NR Rectangular Panel Array

Construct a 5G antenna array where the grid is 2-by-2 and each panel is a 4 -by-4 array. Each antenna element consists of two short-dipole antennas with different dipole axis directions. The antenna elements are spaced $1 / 2$ wavelength apart and the panels are spaced 3 wavelengths apart. Plot the response pattern of the array assuming an operating frequency of 6 GHz .

```
c = physconst('LightSpeed');
fc = 6e9;
lambda = c/fc;
antennal = phased.ShortDipoleAntennaElement('AxisDirection','Z');
antenna2 = phased.ShortDipoleAntennaElement('AxisDirection','X');
array = phased.NRRectangularPanelArray('ElementSet', ...
    {antenna1, antenna2},'Size',[4, 4, 2, 2],'Spacing', ...
    [0.5*lambda, 0.5*lambda,3*lambda, 3*lambda]);
pattern(array,fc,'ShowArray',true)
```



Use the Orientation property of pattern to change the orientation $80^{\circ}$ along the $x$-axis, $30^{\circ}$ along the $y$-axis and $60^{\circ}$ along the $z$-axis.
pattern(array,fc,'Orientation', [80;30;60],'ShowArray',true)


Disable the display of local coordinates and the colorbar.
pattern(array,fc,'ShowLocalCoordinate',false,'ShowColorBar',false)

## 3D Directivity Pattern



## Get Response of NR Rectangular Array

Construct a 5 G antenna array where the grid is 2 -by- 2 and each panel is a 3 -by-2 array. The antenna elements are two phased.NRAntennaElement objects having polarization angles of +45 and -45 degrees. Find the response of the array at boresight, assuming an operating frequency of 6 GHz . The elements are spaced $1 / 2$-wavelength apart and the panels are 3 -wavelengths apart.

```
    c = physconst('LightSpeed');
    fc = 6e9;2
ans = 2
    lambda = c/fc;
    array = phased.NRRectangularPanelArray('Size',[3, 2, 2, 2], ...
            'Spacing',[0.5*lambda,0.5*lambda,3*lambda,3*lambda]);
    resp = array(fc,[0;0])
resp = struct with fields:
    H: [48x1 double]
    V: [48x1 double]
```


## Version History

Introduced in R2021a

## References

[1] 5G: Study on channel model for frequencies from 0.5 to 100 GHz , 3GPP TR38.901 Version 14.0.0 Release 14.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:
"System Objects in MATLAB Code Generation" (MATLAB Coder)

## See Also

phased.NRAntennaElement

# phased.OmnidirectionalMicrophoneElement 

Package: phased
Omnidirectional microphone element

## Description

The phased.OmnidirectionalMicrophoneElement System object models a microphone element with an omnidirectional response pattern.

To compute the response of the microphone element for specified directions:
1 Create the phased.OmnidirectionalMicrophoneElement object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

microphone = phased.OmnidirectionalMicrophoneElement
microphone = phased.OmnidirectionalMicrophoneElement(Name=Value)

## Description

microphone = phased.OmnidirectionalMicrophoneElement creates an omnidirectional microphone System object, microphone, with default object properties.
microphone = phased.OmnidirectionalMicrophoneElement(Name=Value) creates an omnidirectional microphone object, microphone, with each specified property set to the specified value. You can specify additional name-value pair arguments in any order as (Namel=Value1,...,NameN=ValueN).
Example: microphone = phased.OmnidirectionalMicrophoneElement(FrequencyRange=[0 1000], BackBaffled=true) creates a back baffled omnidirectional microphone element with its frequency range specified between 0 and 1000 Hz .

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## FrequencyRange - Operating frequency range

[0 1e20] (default) | 1-by-2 real-valued row vector
Operating frequency range of the microphone element, specified as a 1-by-2 real-valued row vector in the form of [LowerBound HigherBound]. The microphone element has no response outside the specified frequency range. Units are in Hz .

Data Types: double

## BackBaffled - Baffle the back direction of microphone element <br> false (default) | true

Baffle the back direction of microphone element, specified as false or true. When true, the microphone responses to all azimuth angles beyond $\pm 90$ degrees from broadside (zero degrees azimuth and elevation) are zero.

When the value of this property is false, the back direction of the microphone element is not baffled.

Data Types: logical

## Usage

## Syntax

RESP = microphone(FREQ,ANG)

## Description

RESP = microphone(FREQ,ANG) returns the microphone's magnitude response, RESP, at frequencies specified in FREQ and directions specified in ANG.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## FREQ - Signal frequencies

1 -by- $P$ row vector of positive values
Signal frequencies, specified as a 1-by-P row vector of positive values. Units are Hz .

## ANG - Response directions

1-by- $Q$ vector of real-values | 2-by- $Q$ matrix of real-values
Response directions, specified as a 1-by- $Q$ vector of real-values or a 2-by- $Q$ matrix of real-values.

- If ANG is a 1 -by- $Q$ vector, each element specifies a direction's azimuth angle. The azimuth angle must be between $-180^{\circ}$ and $180^{\circ}$, inclusive. In this case, the corresponding elevation angle is assumed to be zero.
- If ANG is a 2-by-Q matrix, each column of the matrix specifies the direction in the form [azimuth; elevation]. The azimuth angle must be between $-180^{\circ}$ and $180^{\circ}$, inclusive. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive.

Units are in degrees.

## Output Arguments

## RESP - Microphone response

$Q$-by-P real-valued matrix
Microphone magnitude response, returned as an $Q$-by- $P$ real-valued matrix. The matrix contains the responses of the microphone element at the $Q$ angles specified in ANG and the $P$ frequencies specified in FREQ.

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```


## Specific to Antenna and Transducer Element System Objects

beamwidth directivity isPolarizationCapable pattern patternAzimuth patternElevation

Compute and display beamwidth of sensor element pattern Directivity of antenna or transducer element Antenna element polarization capability Plot antenna or transducer element directivity and patterns Plot antenna or transducer element directivity and pattern versus azimuth Plot antenna or transducer element directivity and pattern versus elevation

## Common to All System Objects

step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object

## Examples

## Display Omnidirectional Microphone Pattern

Create an omnidirectional microphone. Find the microphone response at 200, 300, and 400 Hz for the incident angle $0^{\circ}$ azimuth and $0^{\circ}$ elevation. Then, plot the azimuth response of the microphone at three frequencies.

```
microphone = phased.OmnidirectionalMicrophoneElement;
microphone.FrequencyRange=[20 2e3];
fc = [200 300 400];
ang = [0;0];
resp = microphone(fc,ang);
```

Plot the response pattern. The response patterns for at all three frequencies are the same.

```
pattern(microphone,fc,-180:180,0,'CoordinateSystem','polar','Type','power');
```



Normalized Power, Broadside at $0.00^{\circ}$

## Directivity of Omnidirectional Microphone Element

Compute the directivity of an omnidirectional microphone element for several different directions.
Create the omnidirectional microphone element system object.
myMic = phased.OmnidirectionalMicrophoneElement();
Select the angles of interest at constant elevation angle set equal to zero degrees. Select seven azimuth angles centered at boresight (zero degrees azimuth and zero degrees elevation). Finally, set the desired frequency to 1 kHz .

```
ang = [-30,-20,-10,0,10,20,30; 0,0,0,0,0,0,0];
freq = 1000;
```

Compute the directivity along the constant elevation cut.

```
d = directivity(myMic,freq,ang)
d = 7x1
```

0
0

Next select the angles of interest to be at constant azimuth angle at zero degrees. All elevation angles are centered around boresight. The five elevation angles range from -20 to +20 degrees. Set the desired frequency to 1 GHz .

```
ang = [0,0,0,0,0; -20,-10,0,10,20];
freq = 1000;
Compute the directivity along the constant azimuth cut.
d = directivity(myMic,freq,ang)
d = 5 < 1
    0
    0
    0
    0
    0
```

For an omnidirectional microphone, the directivity is independent of direction.

## Omnidirectional Microphone Element Does Not Support Polarization

Determine whether a phased.OmnidirectionalMicrophoneElement microphone element supports polarization.

```
microphone = phased.OmnidirectionalMicrophoneElement;
isPolarizationCapable(microphone)
ans = logical
    0
```

The returned value 0 shows that the omnidirectional microphone element does not support polarization.

## Magnitude and Directivity Patterns of Omnidirectional Microphone

Construct an omnidirectional microphone and plot the magnitude and directivity patterns. The microphone operating frequency spans the range 20 to 20000 Hz .

Construct the omnidirectional microphone.
sOmni = phased.OmnidirectionalMicrophoneElement(...
'FrequencyRange',[20 20e3]);

Plot the microphone magnitude pattern at 200 Hz .
$\mathrm{fc}=200$;
pattern(s0mni,fc,[-180:180],0,...
'CoordinateSystem', 'rectangular',...
'Type', 'efield')


Plot the microphone directivity.
pattern(s0mni,fc,[-180:180],0,...
'CoordinateSystem', 'rectangular', ...
'Type', 'directivity')


The directivity is 0 dbi as expected for an omnidirectional element.

## 3-D Magnitude Pattern of Omnidirectional Microphone

Construct an omnidirectional microphone with response in the frequency range $20-20000 \mathrm{~Hz}$. Then, plot the 3-D magnitude pattern over a range of angles.

Construct the microphone element.

```
sOmin = phased.OmnidirectionalMicrophoneElement(...
    'FrequencyRange',[20 20e3]);
```

Plot the 3-D pattern at 500 Hz between -30 to 30 degrees in both azimuth and elevation in 0.1 degree increments.

```
fc = 500;
pattern(sOmin,fc,[-30:0.1:30],[-30:0.1:30],...
    'CoordinateSystem','polar',...
    'Type','efield')
```



## Azimuth Pattern of Omnidirectional Microphone Element

Create an omnidirectional microphone element. Plot an azimuth cut of the directivity at 0 and 30 degrees elevation. Assume an operating frequency of 500 Hz .

Create the microphone element.
sOmni = phased.OmnidirectionalMicrophoneElement('FrequencyRange',[100,900]); $\mathrm{fc}=500$;

Plot the azimuth pattern.
patternAzimuth(sOmni,fc,[0 30])


Directivity (dBi), Broadside at $0.00^{\circ}$
Because of the omnidirectionality of the microphone, the two patterns coincide.
Plot a reduced range of azimuth angles using the Azimuth parameter.
patternAzimuth(s0mni,fc,[0 30],'Azimuth',[-20:20])


Directivity (dBi), Broadside at $0.00^{\circ}$

## Elevation Pattern of Omnidirectional Microphone Element

Construct an omnidirectional microphone element. Plot an elevation cut of the power 45 and 55 degrees azimuth. Assume the operating frequency is 500 Hz .

Create the microphone element.
fc = 500;
sOmni = phased.OmnidirectionalMicrophoneElement('FrequencyRange', [100, 900]);
Display the power pattern.

```
patternElevation(sOmni,fc,[45 55],'Type','powerdb')
```



Power (dB), Broadside at $0.00^{\circ}$

Because of the omnidirectionality, the two plots coincide.
Plot a reduced range of elevation angles using the Elevation parameter. patternElevation(sOmni,fc,[45 55],...
'Elevation', [-20:20],...
'Type','powerdb')


Power (dB), Broadside at $0.00^{\circ}$

## Version History <br> Introduced in R2011a

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:

- The pattern, patternAzimuth, and patternElevation methods are not supported.
- See "System Objects in MATLAB Code Generation" (MATLAB Coder).


## See Also

phased.IsotropicProjector|phased.IsotropicHydrophone| phased.CustomMicrophoneElement | phased.ULA|phased.URA|phased.ConformalArray| uv2azel| phitheta2azel

## directivity

System object: phased.OmnidirectionalMicrophoneElement
Package: phased
Directivity of omnidirectional microphone element

## Syntax

D = directivity(H,FREQ,ANGLE)

## Description

$\mathrm{D}=$ directivity ( $\mathrm{H}, \mathrm{FREQ}$, ANGLE) returns the "Directivity ( dBi )" on page 1-1108 of an omnidirectional microphone element, H , at frequencies specified by FREQ and in direction angles specified by ANGLE.

## Input Arguments

## H O Omnidirectional Microphone Element

System object
Omnidirectional microphone element specified as a phased. OmnidirectionalMicrophoneElement System object.
Example: H = phased.OmnidirectionalMicrophoneElement

## FREQ - Frequency for computing directivity and patterns

positive scalar | 1-by- $L$ real-valued row vector
Frequencies for computing directivity and patterns, specified as a positive scalar or 1-by-L realvalued row vector. Frequency units are in hertz.

- For an antenna, microphone, or sonar hydrophone or projector element, FREQ must lie within the range of values specified by the FrequencyRange or FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased.CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.


## Example: [1e8 2e6]

## Data Types: double

## ANGLE - Angles for computing directivity

1 -by- $M$ real-valued row vector | 2 -by- $M$ real-valued matrix
Angles for computing directivity, specified as a 1-by- $M$ real-valued row vector or a 2 -by- $M$ real-valued matrix, where $M$ is the number of angular directions. Angle units are in degrees. If ANGLE is a 2-by- $M$ matrix, then each column specifies a direction in azimuth and elevation, [az;el]. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

If ANGLE is a 1 -by- $M$ vector, then each entry represents an azimuth angle, with the elevation angle assumed to be zero.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the $x y$ plane. This angle is positive when measured from the $x$-axis toward the $y$-axis. The elevation angle is the angle between the direction vector and xy plane. This angle is positive when measured towards the $z$-axis. See "Azimuth and Elevation Angles".
Example: [45 60; 0 10]
Data Types: double

## Output Arguments

## D - Directivity

M-by-L matrix
Directivity, returned as an $M$-by- $L$ matrix. Each row corresponds to one of the $M$ angles specified by ANGLE. Each column corresponds to one of the $L$ frequency values specified in FREQ. Directivity units are in dBi where dBi is defined as the gain of an element relative to an isotropic radiator.

## Examples

## Directivity of Omnidirectional Microphone Element

Compute the directivity of an omnidirectional microphone element for several different directions.
Create the omnidirectional microphone element system object.
myMic = phased.OmnidirectionalMicrophoneElement();
Select the angles of interest at constant elevation angle set equal to zero degrees. Select seven azimuth angles centered at boresight (zero degrees azimuth and zero degrees elevation). Finally, set the desired frequency to 1 kHz .

```
ang = [-30,-20,-10,0,10,20,30; 0,0,0,0,0,0,0];
freq = 1000;
```

Compute the directivity along the constant elevation cut.

```
d = directivity(myMic,freq,ang)
d = 7x1
```

    0
    0
    0
    0
    0
    0
    0
    Next select the angles of interest to be at constant azimuth angle at zero degrees. All elevation angles are centered around boresight. The five elevation angles range from -20 to +20 degrees. Set the desired frequency to 1 GHz .

```
ang = [0,0,0,0,0; -20,-10,0,10,20];
freq = 1000;
```

Compute the directivity along the constant azimuth cut.

```
d = directivity(myMic,freq,ang)
d = 5x1
```

0
0
0
0
0

For an omnidirectional microphone, the directivity is independent of direction.

## More About

## Directivity (dBi)

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## See Also <br> patternElevation| patternAzimuth | pattern

## isPolarizationCapable

System object: phased.OmnidirectionalMicrophoneElement
Package: phased
Polarization capability

## Syntax

flag = isPolarizationCapable(microphone)

## Description

flag = isPolarizationCapable(microphone) returns a Boolean value, flag, indicating whether the phased.OmnidirectionalMicrophoneElement supports polarization. An element supports polarization if it can create or respond to polarized fields. This microphone element, as all microphone elements, does not support polarization.

## Input Arguments

## microphone - Omni-directional microphone element

Omni-directional microphone element specified as a phased.OmnidirectionalMicrophoneElement System object

## Output Arguments

## flag - Polarization-capability flag

Polarization-capability returned as a Boolean value true if the microphone element supports polarization or false if it does not. Because the phased. OmnidirectionalMicrophoneElement object does not support polarization, flag is always returned as false.

## Examples

## Omnidirectional Microphone Element Does Not Support Polarization

Determine whether a phased.OmnidirectionalMicrophoneElement microphone element supports polarization.

```
microphone = phased.OmnidirectionalMicrophoneElement;
isPolarizationCapable(microphone)
ans = logical
    0
```

The returned value 0 shows that the omnidirectional microphone element does not support polarization.

## pattern

System object: phased.OmnidirectionalMicrophoneElement
Package: phased
Plot omnidirectional microphone element directivity and patterns

## Syntax

pattern(sElem, FREQ)
pattern(sElem, FREQ,AZ)
pattern(sElem, FREQ,AZ, EL)
pattern (__ ,Name, Value)
[PAT,AZ_ANG,EL_ANG] = pattern( $\qquad$ )

## Description

pattern(sElem, FREQ) plots the 3-D array directivity pattern (in dBi) for the element specified in sElem. The operating frequency is specified in FREQ.
pattern(sElem, FREQ,AZ) plots the element directivity pattern at the specified azimuth angle.
pattern(sElem, FREQ,AZ,EL) plots the element directivity pattern at specified azimuth and elevation angles.
pattern(__, Name, Value) plots the element pattern with additional options specified by one or more Name, Value pair arguments.
[PAT,AZ_ANG,EL_ANG] = pattern (___) returns the element pattern in PAT. The AZ_ANG output contains the coordinate values corresponding to the rows of PAT. The EL_ANG output contains the coordinate values corresponding to the columns of PAT. If the 'CoordinateSystem' parameter is set to ' $u v$ ', then AZ_ANG contains the $U$ coordinates of the pattern and EL_ANG contains the $V$ coordinates of the pattern. Otherwise, they are in angular units in degrees. $\bar{U} V$ units are dimensionless.

Note This method replaces the plotResponse method. See "Convert plotResponse to pattern" on page 1-1118 for guidelines on how to use pattern in place of plotResponse.

## Input Arguments

## sElem - Omnidirectional microphone element

System object
Omnidirectional microphone element, specified as a phased.OmnidirectionalMicrophoneElement System object.
Example: sElem = phased.OmnidirectionalMicrophoneElement;
FREQ - Frequency for computing directivity and patterns
positive scalar | 1-by-L real-valued row vector

Frequencies for computing directivity and patterns, specified as a positive scalar or 1-by-L realvalued row vector. Frequency units are in hertz.

- For an antenna, microphone, or sonar hydrophone or projector element, FREQ must lie within the range of values specified by the FrequencyRange or FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased. CustomAntennaElement and phased. CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.


## Example: [1e8 2e6]

Data Types: double

## AZ - Azimuth angles

[-180:180] (default) | 1-by-N real-valued row vector
Azimuth angles for computing directivity and pattern, specified as a $1-b y-N$ real-valued row vector where $N$ is the number of azimuth angles. Angle units are in degrees. Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the $x y$ plane. When measured from the $x$-axis toward the $y$-axis, this angle is positive.

## Example: [-45:2:45]

Data Types: double

## EL - Elevation angles

[-90:90] (default) | 1-by-M real-valued row vector
Elevation angles for computing directivity and pattern, specified as a 1-by- $M$ real-valued row vector where $M$ is the number of desired elevation directions. Angle units are in degrees. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

The elevation angle is the angle between the direction vector and $x y$-plane. The elevation angle is positive when measured towards the $z$-axis.
Example: [-75:1:70]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## CoordinateSystem - Plotting coordinate system

'polar' (default)|'rectangular'|'uv'
Plotting coordinate system of the pattern, specified as the comma-separated pair consisting of
'CoordinateSystem' and one of 'polar', 'rectangular', or 'uv'. When
'CoordinateSystem' is set to 'polar' or 'rectangular', the AZ and EL arguments specify the
pattern azimuth and elevation, respectively. AZ values must lie between $-180^{\circ}$ and $180^{\circ}$. EL values must lie between $-90^{\circ}$ and $90^{\circ}$. If 'CoordinateSystem' is set to 'uv', AZ and EL then specify $U$ and $V$ coordinates, respectively. AZ and EL must lie between -1 and 1.
Example: 'uv'
Data Types: char

## Type - Displayed pattern type

'directivity' (default) | 'efield'|'power'|'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type ' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb ' - power pattern converted to dB.

Example: ' powerdb'
Data Types: char

## Normalize - Display normalize pattern

true (default) | false
Display normalized pattern, specified as the comma-separated pair consisting of 'Normalize' and a Boolean. Set this parameter to true to display a normalized pattern. This parameter does not apply when you set 'Type' to 'directivity'. Directivity patterns are already normalized.

Data Types: logical

## PlotStyle - Plotting style

'overlay' (default)| 'waterfall'
Plotting style, specified as the comma-separated pair consisting of 'Plotstyle' and either 'overlay' or 'waterfall'. This parameter applies when you specify multiple frequencies in FREQ in 2-D plots. You can draw 2-D plots by setting one of the arguments AZ or EL to a scalar.

## Data Types: char

## Output Arguments

## PAT - Element pattern

$N$-by-M real-valued matrix
Element pattern, returned as an $N$-by- $M$ real-valued matrix. The pattern is a function of azimuth and elevation. The rows of PAT correspond to the azimuth angles in the vector specified by EL_ANG. The columns correspond to the elevation angles in the vector specified by AZ_ANG.

## AZ_ANG - Azimuth angles

```
scalar | 1-by-N real-valued row vector
```

Azimuth angles for displaying directivity or response pattern, returned as a scalar or 1-by- $N$ realvalued row vector corresponding to the dimension set in AZ. The columns of PAT correspond to the values in AZ_ANG. Units are in degrees.

## EL_ANG - Elevation angles

scalar | 1-by-M real-valued row vector
Elevation angles for displaying directivity or response, returned as a scalar or 1-by-M real-valued row vector corresponding to the dimension set in EL. The rows of PAT correspond to the values in EL_ANG. Units are in degrees.

## Examples

## Magnitude and Directivity Patterns of Omnidirectional Microphone

Construct an omnidirectional microphone and plot the magnitude and directivity patterns. The microphone operating frequency spans the range 20 to 20000 Hz .

Construct the omnidirectional microphone.

```
sOmni = phased.OmnidirectionalMicrophoneElement(...
    'FrequencyRange',[20 20e3]);
```

Plot the microphone magnitude pattern at 200 Hz .
fc = 200;
pattern(sOmni,fc,[-180:180],0,...
'CoordinateSystem', 'rectangular',...
'Type','efield')


Plot the microphone directivity.
pattern(s0mni,fc,[-180:180],0,...
'CoordinateSystem', 'rectangular',...
'Type','directivity')


The directivity is 0 dbi as expected for an omnidirectional element.

## 3-D Magnitude Pattern of Omnidirectional Microphone

Construct an omnidirectional microphone with response in the frequency range $20-20000 \mathrm{~Hz}$. Then, plot the 3-D magnitude pattern over a range of angles.

Construct the microphone element.

```
sOmin = phased.OmnidirectionalMicrophoneElement(...
    'FrequencyRange',[20 20e3]);
```

Plot the 3-D pattern at 500 Hz between -30 to 30 degrees in both azimuth and elevation in 0.1 degree increments.

```
fc = 500;
pattern(s0min,fc,[-30:0.1:30],[-30:0.1:30],...
    'CoordinateSystem','polar',...
    'Type','efield')
```



## Plot Directivity of Crossed-Dipole Antenna

Create a crossed-dipole antenna. Assume the antenna works between 1 and 2 GHz and its operating frequency is 1.5 GHz . Then, plot the directivity at a constant azimuth of $0^{\circ}$.

```
antenna = phased.CrossedDipoleAntennaElement('FrequencyRange',[1e9 2e9]);
fc = 1.5e9;
pattern(antenna,fc,0,-90:90,'Type','directivity', ...
    'CoordinateSystem','rectangular')
```



The directivity is maximum at $0^{\circ}$ elevation and attains a value of approximately 1.75 dB .

## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Convert plotResponse to pattern

For antenna, microphone, and array System objects, the pattern method replaces the plotResponse method. In addition, two new simplified methods exist just to draw 2-D azimuth and elevation pattern plots. These methods are azimuthPattern and elevationPattern.

The following table is a guide for converting your code from using plotResponse to pattern. Notice that some of the inputs have changed from input arguments to Name-Value pairs and conversely. The general pattern method syntax is
pattern(H,FREQ,AZ,EL,'Name1','Value1',...,' $N a m e N ', ' V a l u e N ') ~$

| plotResponse Inputs | plotResponse Description | pattern Inputs |
| :--- | :--- | :--- |
| H argument | Antenna, microphone, or array <br> System object. | H argument (no change) |
| FREQ argument | Operating frequency. | FREQ argument (no change) |
| V argument | Propagation speed. This argument <br> is used only for arrays. | 'PropagationSpeed ' name-value <br> pair. This parameter is only used for <br> arrays. |


| plotResponse Inputs | plotResponse Description |  | pattern Inputs |  |
| :---: | :---: | :---: | :---: | :---: |
| 'Format' and 'RespCut' namevalue pairs | These options work together to let you create a plot in angle space (line or polar style) or $U V$ space. They also determine whether the plot is 2-D or 3-D. This table shows you how to create different types of plots using plotResponse. |  | 'CoordinateSystem' name-value pair used together with the AZ and EL input arguments. <br> 'CoordinateSystem' has the same options as the plotResponse method 'Format ' name-value pair, except that ' line' is now named 'rectangular'. The table shows how to create different types of plots using pattern. |  |
|  | Display space <br> Angle space (2D) |  |  |  |
|  | Angle space (2D) | Set 'RespCut' <br> to 'Az' or |  |  |
|  |  | 'El'. Set <br> 'Format ' to <br> 'line' or 'polar'. | Display space |  |
|  |  | ' line' or 'polar'. <br> Set the display axis using either the 'AzimuthAngle | Angle space (2D) | Set <br> Coordinate <br> System' to <br> rectangular' <br> or 'polar' <br> Specify either AZ <br> or EL as a scalar. |
|  |  | s' or 'ElevationAng les' namevalue pairs. | Angle space (3D) | Set <br> 'Coordinate <br> System' to 'rectangular' |
|  | Angle space (3D) | Set 'RespCut' to '3D'. Set |  | or 'polar'. <br> Specify both AZ <br> and EL as <br> vectors. |
|  |  | 'polar'. <br> Set the display axis using both the 'AzimuthAngle s' and 'Elevation | $U V$ space (2D) | Set <br> Coordinate System' to uv'. Use AZ to specify a $U$ space vector. Use EL to specify a $V$-space scalar. |
|  |  | Angles' namevalue pairs. | UV space (3D) |  |
|  | UV space (2D) | Set 'RespCut' to'U'. Set 'Format ' to 'UV'. Set the display range using the 'UGrid' namevalue pair. |  | 'Coordinate <br> System' to <br> 'uv'. Use AZ to <br> specify a $U$ - <br> space vector. <br> Use EL to specify <br> a $V$-space vector. |
|  |  |  | If you set CoordinateSystem to 'uv ' , enter the UV grid values using $A Z$ and $E L$. |  |
|  | UV space (3D) | $\begin{aligned} & \text { Set 'RespCut' } \\ & \text { to'3D'. Set } \\ & \text { 'Format' to } \end{aligned}$ |  |  |


| plotResponse Inputs | plotResponse Description |  | pattern Inputs |
| :---: | :---: | :---: | :---: |
|  | Display space | 'UV '. Set the display range using both the 'UGrid' and 'VGrid ' namevalue pairs. |  |
| 'CutAngle' name-value pair | Constant angle at to take an azimuth or elevation cut. When producing a 2-D plot and when 'RespCut' is set to 'Az' or 'El', use 'CutAngle' to set the slice across which to view the plot. |  | No equivalent name-value pair. To create a cut, specify either AZ or EL as a scalar, not a vector. |
| 'NormalizeResponse' namevalue pair | Normalizes the plot. When 'Unit' is set to 'dbi' , you cannot specify 'NormalizeResponse'. |  | Use the 'Normalize' name-value pair. When 'Type' is set to 'directivity' you cannot specify 'Normalize'. |
| 'OverlayFreq' name-value pair | Plot multiple frequencies on the same 2-D plot. Available only when 'Format' is set to 'line' or 'uv and 'RespCut' is not set to '3D'. The value true produces an overlay plot and the value false produces a waterfall plot. |  | 'PlotStyle' name-value pair plots multiple frequencies on the same 2-D plot. <br> The values 'overlay' and 'waterfall' correspond to 'OverlayFreq' values of true and false. The option 'waterfall' is allowed only when 'CoordinateSystem' is set to 'rectangular' or 'uv'. |
| 'Polarization' name-value pair | Determines how to plot polarized fields. Options are 'None', 'Combined', 'H', or 'V'. |  | 'Polarization ' name-value pair determines how to plot polarized fields. The 'None ' option is removed. The options 'Combined ' , ' H ', or 'V' are unchanged. |
| ' Unit ' name-value pair | Determines the plot units. Choose 'db','mag', 'pow', or 'dbi', where the default is ' db ' |  | 'Type ' name-value pair, uses equivalent options with different names |
|  |  |  | plotResponse pattern |
|  |  |  | 'db' 'powerdb' <br> 'mag' 'efield' <br> 'pow' 'power' <br> 'dbi' 'directivity' |
| 'Weights ' name-value pair | Array element tapers (or weights). |  | 'Weights ' name-value pair (no change). |
| 'AzimuthAngles ' name-value pair | Azimuth angles used to display the antenna or array response. |  | AZ argument |


| plotResponse Inputs | plotResponse Description | pattern Inputs |
| :--- | :--- | :--- |
| ' ElevationAngles ' name-value <br> pair | Elevation angles used to display the <br> antenna or array response. | EL argument |
| ' UGrid' name-value pair | Contains $U$ coordinates in $U V$ - <br> space. | AZ argument when <br> 'CoordinateSystem ' name-value <br> pair is set to 'uv ' |
| 'VGrid' name-value pair | Contains $V$-coordinates in $U V$-space. | EL argument when <br> 'CoordinateSystem ' name-value <br> pair is set to 'uv ' |

## Version History <br> Introduced in R2015a

See Also<br>patternElevation| patternAzimuth

## patternAzimuth

System object: phased.OmnidirectionalMicrophoneElement
Package: phased
Plot omnidirectional microphone element directivity or pattern versus azimuth

## Syntax

```
patternAzimuth(sElem,FREQ)
patternAzimuth(sElem,FREQ,EL)
patternAzimuth(sElem,FREQ,EL,Name,Value)
PAT = patternAzimuth(
```

$\qquad$

## Description

patternAzimuth (sElem, FREQ) plots the 2-D element directivity pattern versus azimuth (in dBi) for the element sElem at zero degrees elevation angle. The argument FREQ specifies the operating frequency.
patternAzimuth(sElem, FREQ,EL), in addition, plots the 2-D element directivity pattern versus azimuth (in dBi ) at the elevation angle specified by EL. When EL is a vector, multiple overlaid plots are created.
patternAzimuth(sElem, FREQ,EL,Name,Value) plots the element pattern with additional options specified by one or more Name, Value pair arguments.

PAT = patternAzimuth( $\qquad$ ) returns the element pattern. PAT is a matrix whose entries represent the pattern at corresponding sampling points specified by the 'Azimuth' parameter and the EL input argument.

## Input Arguments

## sElem - Omnidirectional microphone element

System object
Omnidirectional microphone element, specified as a phased.OmnidirectionalMicrophoneElement System object.
Example: sElem = phased.OmnidirectionalMicrophoneElement;

## FREQ - Frequency for computing directivity and pattern

positive scalar
Frequency for computing directivity and pattern, specified as a positive scalar. Frequency units are in hertz.

- For an antenna or microphone element, FREQ must lie within the range of values specified by the FrequencyRange or the FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased. CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: 1e8
Data Types: double

## EL - Elevation angles

1-by- $N$ real-valued row vector
Elevation angles for computing sensor or array directivities and patterns, specified as a 1-by- $N$ realvalued row vector. The quantity $N$ is the number of requested elevation directions. Angle units are in degrees. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

The elevation angle is the angle between the direction vector and the xy plane. When measured toward the $z$-axis, this angle is positive.
Example: [0, 10, 20]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Type - Displayed pattern type

'directivity' (default) | 'efield' | 'power' | 'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb ' - power pattern converted to dB.

Example: 'powerdb'
Data Types: char

## Azimuth - Azimuth angles

[-180:180] (default) | 1-by-P real-valued row vector
Azimuth angles, specified as the comma-separated pair consisting of 'Azimuth' and a 1-by-P realvalued row vector. Azimuth angles define where the array pattern is calculated.
Example: 'Azimuth', [-90:2:90]
Data Types: double

## Output Arguments

## PAT - Element directivity or pattern

$P$-by- $N$ real-valued matrix
Element directivity or pattern, returned as an $P$-by- $N$ real-valued matrix. The dimension $P$ is the number of azimuth values determined by the 'Azimuth ' name-value pair argument. The dimension $N$ is the number of elevation angles, as determined by the EL input argument.

## Examples

## Azimuth Pattern of Omnidirectional Microphone Element

Create an omnidirectional microphone element. Plot an azimuth cut of the directivity at 0 and 30 degrees elevation. Assume an operating frequency of 500 Hz .

Create the microphone element.

```
sOmni = phased.OmnidirectionalMicrophoneElement('FrequencyRange',[100,900]);
```

fc = 500;

Plot the azimuth pattern.
patternAzimuth(sOmni,fc,[0 30])


Directivity (dBi), Broadside at $0.00^{\circ}$

Because of the omnidirectionality of the microphone, the two patterns coincide.
Plot a reduced range of azimuth angles using the Azimuth parameter.
patternAzimuth(s0mni,fc,[0 30],'Azimuth',[-20:20])


Directivity (dBi), Broadside at $0.00^{\circ}$

## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \Pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\mathrm{total}}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or
array used for transmission. When converted to decibels, the directivity is denoted as dBi . For information on directivity, read the notes on "Element Directivity" and "Array Directivity",

## Version History

Introduced in R2015a

## See Also

patternElevation|pattern

## patternElevation

System object: phased.OmnidirectionalMicrophoneElement
Package: phased
Plot omnidirectional microphone element directivity or pattern versus elevation

## Syntax

```
patternElevation(sElem,FREQ)
patternElevation(sElem,FREQ,AZ)
patternElevation(sElem,FREQ,AZ,Name,Value)
PAT = patternElevation(
```

$\qquad$

## Description

patternElevation(sElem, FREQ) plots the 2-D element directivity pattern versus elevation (in dBi ) for the element sElem at zero degrees azimuth angle. The argument FREQ specifies the operating frequency.
patternElevation(sElem,FREQ,AZ), in addition, plots the 2-D element directivity pattern versus elevation (in dBi ) at the azimuth angle specified by AZ. When AZ is a vector, multiple overlaid plots are created.
patternElevation(sElem,FREQ,AZ,Name, Value) plots the element pattern with additional options specified by one or more Name, Value pair arguments.

PAT = patternElevation (__ ) returns the element pattern. PAT is a matrix whose entries represent the pattern at corresponding sampling points specified by the 'Elevation' parameter and the AZ input argument.

## Input Arguments

## sElem - Omnidirectional microphone element

System object
Omnidirectional microphone element, specified as a phased.OmnidirectionalMicrophoneElement System object.
Example: sElem = phased.OmnidirectionalMicrophoneElement;

## FREQ - Frequency for computing directivity and pattern

positive scalar
Frequency for computing directivity and pattern, specified as a positive scalar. Frequency units are in hertz.

- For an antenna or microphone element, FREQ must lie within the range of values specified by the FrequencyRange or the FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased.CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: 1e8
Data Types: double

## AZ - Azimuth angles for computing directivity and pattern

1-by- $N$ real-valued row vector
Azimuth angles for computing sensor or array directivities and patterns, specified as a 1-by- N realvalued row vector where $N$ is the number of desired azimuth directions. Angle units are in degrees. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the xy plane. This angle is positive when measured from the $x$-axis toward the $y$-axis.
Example: [0,10,20]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Type - Displayed pattern type

'directivity' (default) | 'efield' | 'power' | 'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb ' - power pattern converted to dB.

Example: 'powerdb'
Data Types: char

## Elevation - Elevation angles

[-90:90] (default)| 1-by-P real-valued row vector
Elevation angles, specified as the comma-separated pair consisting of 'Elevation' and a 1-by-P real-valued row vector. Elevation angles define where the array pattern is calculated.
Example: 'Elevation', [-90:2:90]
Data Types: double

## Output Arguments

## PAT - Element directivity or pattern

$P$-by- $N$ real-valued matrix
Element directivity or pattern, returned as an $P$-by- $N$ real-valued matrix. The dimension $P$ is the number of elevation angles determined by the 'Elevation' name-value pair argument. The dimension $N$ is the number of azimuth angles determined by the AZ argument.

## Examples

## Elevation Pattern of Omnidirectional Microphone Element

Construct an omnidirectional microphone element. Plot an elevation cut of the power 45 and 55 degrees azimuth. Assume the operating frequency is 500 Hz .

Create the microphone element.
fc = 500;
sOmni = phased.OmnidirectionalMicrophoneElement('FrequencyRange',[100,900]);
Display the power pattern.
patternElevation(s0mni,fc,[45 55],'Type','powerdb')


Power (dB), Broadside at $0.00^{\circ}$

Because of the omnidirectionality, the two plots coincide.
Plot a reduced range of elevation angles using the Elevation parameter.
patternElevation(s0mni,fc,[45 55],...
'Elevation', [-20:20],...
'Type', 'powerdb')


Power (dB), Broadside at $0.00^{\circ}$

## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\text {rad }}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that
the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as dBi . For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Version History

Introduced in R2015a

## See Also

patternAzimuth | pattern

## plotResponse

System object: phased.OmnidirectionalMicrophoneElement
Package: phased
Plot response pattern of microphone

## Syntax

plotResponse(H,FREQ)
plotResponse(H,FREQ, Name, Value)
hPlot = plotResponse( $\qquad$ )

## Description

plotResponse( $\mathrm{H}, \mathrm{FREQ}$ ) plots the element response pattern along the azimuth cut, where the elevation angle is 0 . The operating frequency is specified in FREQ.
plotResponse(H, FREQ,Name, Value) plots the element response with additional options specified by one or more Name, Value pair arguments.
hPlot $=$ plotResponse ( __ $)$ returns handles of the lines or surface in the figure window, using any of the input arguments in the previous syntaxes.

## Input Arguments

## H

Element System object

## FREQ

Operating frequency in Hertz specified as a scalar or 1-by-K row vector. FREQ must lie within the range specified by the FrequencyVector property of H . If you set the 'RespCut ' property of H to ' 3 D ' , FREQ must be a scalar. When FREQ is a row vector, plotResponse draws multiple frequency responses on the same axes.

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## CutAngle

Cut angle specified as a scalar. This argument is applicable only when RespCut is ' Az ' or ' El '. If RespCut is 'Az', CutAngle must be between -90 and 90. If RespCut is 'El', CutAngle must be between -180 and 180 .

## Default: 0

## Format

Format of the plot, using one of 'Line', 'Polar', or 'UV '. If you set Format to 'UV ' , FREQ must be a scalar.

Default: 'Line'

## NormalizeResponse

Set this value to true to normalize the response pattern. Set this value to false to plot the response pattern without normalizing it. This parameter is not applicable when you set the Unit parameter value to 'dbi'.

Default: true

## OverlayFreq

Set this value to true to overlay pattern cuts in a 2-D line plot. Set this value to false to plot pattern cuts against frequency in a 3-D waterfall plot. If this value is false, FREQ must be a vector with at least two entries.

This parameter applies only when Format is not 'Polar' and RespCut is not '3D '.

## Default: true

## Polarization

Specify the polarization options for plotting the antenna response pattern. The allowable values are |'None' | 'Combined' | 'H' | 'V' | where

- 'None' specifies plotting a nonpolarized response pattern
- 'Combined ' specifies plotting a combined polarization response pattern
- 'H' specifies plotting the horizontal polarization response pattern
- 'V ' specifies plotting the vertical polarization response pattern

For antennas that do not support polarization, the only allowed value is 'None'. This parameter is not applicable when you set the Unit parameter value to ' dbi ' .

Default: 'None'

## RespCut

Cut of the response. Valid values depend on Format, as follows:

- If Format is 'Line' or 'Polar', the valid values of RespCut are 'Az', 'El', and '3D'. The default is ' Az '.
- If Format is 'UV', the valid values of RespCut are 'U' and '3D'. The default is 'U'.

If you set RespCut to ' 3D' , FREQ must be a scalar.

## Unit

The unit of the plot. Valid values are 'db', 'mag', 'pow', or 'dbi'. This parameter determines the type of plot that is produced.

| Unit value | Plot type |
| :--- | :--- |
| db | power pattern in dB scale |
| mag | field pattern |
| pow | power pattern |
| dbi | directivity |

Default: 'db'

## AzimuthAngles

Azimuth angles for plotting element response, specified as a row vector. The AzimuthAngles parameter sets the display range and resolution of azimuth angles for visualizing the radiation pattern. This parameter is allowed only when the RespCut parameter is set to ' Az ' or ' $3 D^{\prime}$ and the Format parameter is set to 'Line' or 'Polar'. The values of azimuth angles should lie between $180^{\circ}$ and $180^{\circ}$ and must be in nondecreasing order. When you set the RespCut parameter to '3D ', you can set the AzimuthAngles and ElevationAngles parameters simultaneously.

Default: [-180:180]

## ElevationAngles

Elevation angles for plotting element response, specified as a row vector. The ElevationAngles parameter sets the display range and resolution of elevation angles for visualizing the radiation pattern. This parameter is allowed only when the RespCut parameter is set to ' $E l$ ' or ' $3 D^{\prime}$ ' and the Format parameter is set to 'Line' or 'Polar'. The values of elevation angles should lie between $90^{\circ}$ and $90^{\circ}$ and must be in nondecreasing order. When you set the RespCut parameter to ' 3D ', you can set the ElevationAngles and AzimuthAngles parameters simultaneously.

Default: [-90:90]
UGrid
$U$ coordinate values for plotting element response, specified as a row vector. The UGrid parameter sets the display range and resolution of the $U$ coordinates for visualizing the radiation pattern in $U / V$ space. This parameter is allowed only when the Format parameter is set to 'UV' and the RespCut parameter is set to ' $U$ ' or ' $3 D$ '. The values of $U G r i d$ should be between -1 and 1 and should be specified in nondecreasing order. You can set the UGrid and VGrid parameters simultaneously.

Default: [-1:0.01:1]

## VGrid

$V$ coordinate values for plotting element response, specified as a row vector. The VGrid parameter sets the display range and resolution of the $V$ coordinates for visualizing the radiation pattern in $U / V$ space. This parameter is allowed only when the Format parameter is set to ' UV' and the RespCut parameter is set to ' 3 D '. The values of VGrid should be between -1 and 1 and should be specified in nondecreasing order. You can set the VGrid and UGrid parameters simultaneously.

Default: [-1:0.01:1]

## Examples

## Plot Response and Directivity of Omnidirectional Microphone

This example shows how to construct an omnidirectional microphone and how to plot its response and directivity. The microphone operating frequency spans the range 20 to 20000 Hz .

Construct the omnidirectional microphone.
sOmni = phased.OmnidirectionalMicrophoneElement(...
'FrequencyRange',[20 20e3]);
Plot the microphone response at 200 Hz .
$\mathrm{fc}=200$;
plotResponse(s0mni,fc,'Unit','mag');


Plot the microphone directivity.
plotResponse(sOmni,fc,'Unit','dbi');


## Plot 3-D Response of Omnidirectional Microphone

This example shows how to construct an omnidirection microphone with response in the frequency range $20-20000 \mathrm{~Hz}$ and how to plot its 3-D response over a range of angles.

Construct the microphone element.
sOmin = phased.OmnidirectionalMicrophoneElement(...
'FrequencyRange',[20 20e3]);
Plot the 3-D response at 500 Hz . Show the response between - 30 to 30 degrees in both azimuth and elevation in 0.1 degree increments.
plotResponse(s0min,500,'Format','Polar',...
'RespCut','3D','Unit','mag',...
'AzimuthAngles', [-30:0.1:30],...
'ElevationAngles', [-30:0.1:30]);


See Also

uv2azel|azel2uv

## step

## System object: phased. OmnidirectionalMicrophoneElement

Package: phased
Output response of microphone

## Syntax

RESP = step(H,FREQ,ANG)

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = $\operatorname{step}(\mathrm{obj}, \mathrm{x})$ and $\mathrm{y}=\mathrm{obj}(\mathrm{x})$ perform equivalent operations.

RESP $=$ step ( $\mathrm{H}, \mathrm{FREQ}, \mathrm{ANG}$ ) returns the microphone's magnitude response, RESP, at frequencies specified in FREQ and directions specified in ANG.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## H

Microphone object.

## FREQ

Frequencies in hertz. FREQ is a row vector of length $L$.

## ANG

Directions in degrees. ANG can be either a 2-by-M matrix or a row vector of length M.
If ANG is a 2-by-M matrix, each column of the matrix specifies the direction in the form [azimuth; elevation]. The azimuth angle must be between -180 and 180 degrees, inclusive. The elevation angle must be between -90 and 90 degrees, inclusive.

If ANG is a row vector of length $M$, each element specifies a direction's azimuth angle. In this case, the corresponding elevation angle is assumed to be 0 .

## Output Arguments

## RESP

Response of microphone. RESP is an M-by-L matrix that contains the responses of the microphone element at the M angles specified in ANG and the L frequencies specified in FREQ.

## Examples

## Display Omnidirectional Microphone Pattern

Create an omnidirectional microphone. Find the microphone response at 200, 300, and 400 Hz for the incident angle $0^{\circ}$ azimuth and $0^{\circ}$ elevation. Then, plot the azimuth response of the microphone at three frequencies.

```
microphone = phased.OmnidirectionalMicrophoneElement;
microphone.FrequencyRange=[20 2e3];
fc = [200 300 400];
ang = [0;0];
resp = microphone(fc,ang);
```

Plot the response pattern. The response patterns for at all three frequencies are the same.

```
pattern(microphone,fc,-180:180,0,'CoordinateSystem','polar','Type','power');
```



Normalized Power, Broadside at $0.00^{\circ}$

## phased.PartitionedArray

Package: phased
Phased array partitioned into subarrays

## Description

The PartitionedArray object represents a phased array that is partitioned into one or more subarrays.

To obtain the response of the subarrays in a partitioned array:
1 Define and set up your partitioned array. See "Construction" on page 1-1141.
2 Call step to compute the response of the subarrays according to the properties of phased. PartitionedArray. The behavior of step is specific to each object in the toolbox.

You can also specify a PartitionedArray object as the value of the SensorArray or Sensor property of objects that perform beamforming, steering, and other operations.

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.

## Construction

H = phased. PartitionedArray creates a partitioned array System object, H. This object represents an array that is partitioned into subarrays.

H = phased.PartitionedArray(Name, Value) creates a partitioned array object, H, with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN).

## Properties

## Array

Sensor array
Sensor array, specified as any array System object belonging to Phased Array System Toolbox.
Default: phased.ULA('NumElements',4)

## SubarraySelection

Subarray definition matrix
Specify the subarray selection as an $M$-by- $N$ matrix. $M$ is the number of subarrays and $N$ is the number of elements in the array. Each row of the matrix corresponds to a subarray and each entry in the row indicates whether or not an element belongs to the subarray. When the entry is zero, the
element does not belong to the subarray. A nonzero entry represents a complex-valued weight applied to the corresponding element. Each row must contain at least one nonzero entry.

The phase center of each subarray is at the subarray geometric center. The SubarraySelection and Array properties determine the geometric center.

Default: [1 $100 ; 0011]$

## SubarraySteering

Subarray steering method
Specify the method of subarray steering as either 'None'|'Phase'|'Time'| 'Custom'.

- When you set this property to 'Phase ', a phase shifter is used to steer the subarray. Use the STEERANG argument of the step method to define the steering direction.
- When you set this property to 'Time', subarrays are steered using time delays. Use the STEERANG argument of the step method to define the steering direction.
- When you set this property to 'Custom', subarrays are steered by setting independent weights for all elements in each subarray. Use the WS argument of the step method to define the weights for all subarrays.

Default: 'None'

## PhaseShifterFrequency

Subarray phase shifter frequency
Specify the operating frequency of phase shifters that perform subarray steering. The property value is a positive scalar in hertz. This property applies when you set the SubarraySteering property to 'Phase'.

Default: 300e6
NumPhaseShifterBits
Number of phase shifter quantization bits
The number of bits used to quantize the phase shift component of beamformer or steering vector weights. Specify the number of bits as a non-negative integer. A value of zero indicates that no quantization is performed.

Default: 0

## Methods

Specific to phased. PartitionedArray Object

| beamwidth | Compute and display beamwidth for a subarray |
| :--- | :--- |
| collectPla <br> neWave | Simulate received plane waves |
| directivit <br> y | Directivity of partitioned array |


| Specific to phased. PartitionedArray Object |  |
| :--- | :--- |
| getElement <br> Position | Positions of array elements |
| getNumElem <br> ents | Number of elements in array |
| getNumSuba <br> rrays | Number of subarrays in array |
| getSubarra <br> yPosition | Positions of subarrays in array |
| isPolariza <br> tionCapabl <br> e | Polarization capability |
| pattern | Plot partitioned array directivity, field, and power patterns |
| patternAzi <br> muth | Plot partitioned array directivity or pattern versus azimuth |
| patternEle <br> vation | Plot partitioned array directivity or pattern versus elevation |
| plotRespon <br> se | Plot response pattern of array |
| step | Output responses of subarrays |
| viewArray | View array geometry |

## Common to All System Objects

| release | Allow System object property value changes |
| :--- | :--- | :--- |

## Examples

## Azimuth Response of Partitioned ULA

Plot the azimuth response of a 4 -element ULA partitioned into two 2 -element ULA's. The element spacing is one-half wavelength.

Create the ULA, and partition it into two 2-element ULA's.

```
sULA = phased.ULA('NumElements',4,'ElementSpacing',0.5);
sPA = phased.PartitionedArray('Array',sULA,...
    'SubarraySelection',[1 1 0 0;0 0 1 1]);
```

Plot the azimuth response of the array. Assume the operating frequency is 1 GHz and the propagation speed is the speed of light.

```
fc = le9;
pattern(sPA,fc,[-180:180],0,'Type','powerdb',...
    'CoordinateSystem','polar',...
    'Normalize',true)
```



Normalized Power (dB), Broadside at $0.00^{\circ}$

## Response of Subarrays of Partitioned ULA

Create a 4 -element ULA. Then partition the ULA into two 2 -element ULAs. Then, calculate the response at boresight of a 4 -element ULA partitioned into two 2-element ULAs.

```
sULA = phased.ULA('NumElements',4,'ElementSpacing',0.5);
sPA = phased.PartitionedArray('Array',sULA,...
    'SubarraySelection',[1 1 0 0;0 0 1 1]);
```

Calculate the response at 1 GHz . The signal propagation speed is the speed of light.
$\mathrm{fc}=1 \mathrm{e} 9$;
resp $=$ step(sPA,fc,[0;0],physconst('LightSpeed'))
resp $=2 \times 1$

2
2

## Subarray Element Weights for Partitioned Array

Create a partitioned URA array with three subarrays of different sizes. The subarrays have 8, 16, and 32 elements. Use different sets of subarray element weights for each subarray.

Create a 4-by-56 element URA.

```
antenna = phased.IsotropicAntennaElement;
```

fc = 300e6;
c = physconst('LightSpeed');
lambda $=\mathrm{c} / \mathrm{fc}$;
n1 = 2^3;
n2 = 2^4;
n3 = 2^5;
nrows = 4;
ncols = n1 + n2 + n3;
array = phased.URA('Element',antenna,'Size',[nrows,ncols]);

Select the three subarrays by setting the selection matrix.

```
sel1 = zeros(nrows,ncols);
sel2 = sel1;
sel3 = sel1;
sel = zeros(3,nrows*ncols);
for r = 1:nrows
    sel1(r,1:n1) = 1;
    sel2(r,(n1+1):(n1+n2)) = 1;
    sel3(r,((n1+n2)+1):ncols) = 1;
end
sel(1,:) = sel1(:);
sel(2,:) = sel2(:);
sel(3,:) = sel3(:);
```

Create the partitioned array.

```
partarray = phased.PartitionedArray('Array',array, ...
    'SubarraySelection',sel,'SubarraySteering','Custom');
viewArray(partarray,'ShowSubarray','All');
```


## Array Geometry



Set weights for each subarray and get the response of each subarray. Put the weights in a cell array.

```
wts1 = ones(nrows*n1,1);
wts2 = 1.5*ones(nrows*n2,1);
wts3 = 3*ones(nrows*n3,1);
resp = partarray(fc,[30;0],c,{wts1,wts2,wts3})
resp = 3x1 complex
    0.0246 + 0.0000i
    0.0738 - 0.0000i
    0.2951 - 0.0000i
```


## Version History

Introduced in R2012a

## References

[1] Van Trees, H.L. Optimum Array Processing. New York: Wiley-Interscience, 2002.

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.
Usage notes and limitations:

- pattern, patternAzimuth, patternElevation, plotResponse, and viewArray methods are not supported.
- See "System Objects in MATLAB Code Generation" (MATLAB Coder).


## See Also

## Objects

phased.ULA|phased.URA| phased.UCA|phased.ConformalArray|
phased.ReplicatedSubarray
Apps
Sensor Array Analyzer
Topics
Subarrays in Phased Array Antennas
Phased Array Gallery
"Subarrays Within Arrays"

## directivity

System object: phased. PartitionedArray
Package: phased
Directivity of partitioned array

## Syntax

D = directivity (H, FREQ,ANGLE)
D = directivity (H, FREQ, ANGLE, Name, Value)

## Description

D = directivity (H,FREQ, ANGLE) returns the "Directivity" on page 1-1151 of a partitioned array of antenna or microphone elements, H , at frequencies specified by FREQ and in angles of direction specified by ANGLE.

The integration used when computing array directivity has a minimum sampling grid of 0.1 degrees. If an array pattern has a beamwidth smaller than this, the directivity value will be inaccurate.

D = directivity (H, FREQ, ANGLE, Name, Value) returns the directivity with additional options specified by one or more Name, Value pair arguments.

## Input Arguments

## H - Partitioned array

System object
Partitioned array, specified as a phased. PartitionedArray System object.
Example: H = phased.PartitionedArray;

## FREQ - Frequency for computing directivity and patterns

positive scalar | 1-by-L real-valued row vector
Frequencies for computing directivity and patterns, specified as a positive scalar or 1-by-L realvalued row vector. Frequency units are in hertz.

- For an antenna, microphone, or sonar hydrophone or projector element, FREQ must lie within the range of values specified by the FrequencyRange or FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased. CustomAntennaElement and phased.CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: [1e8 2e6]
Data Types: double

## ANGLE - Angles for computing directivity

## 1-by-M real-valued row vector | 2-by-M real-valued matrix

Angles for computing directivity, specified as a 1-by- $M$ real-valued row vector or a 2 -by- $M$ real-valued matrix, where $M$ is the number of angular directions. Angle units are in degrees. If ANGLE is a 2 -by- $M$ matrix, then each column specifies a direction in azimuth and elevation, [az;el]. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

If ANGLE is a 1 -by- $M$ vector, then each entry represents an azimuth angle, with the elevation angle assumed to be zero.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the xy plane. This angle is positive when measured from the $x$-axis toward the $y$-axis. The elevation angle is the angle between the direction vector and xy plane. This angle is positive when measured towards the $z$-axis. See "Azimuth and Elevation Angles".
Example: [45 60; 0 10]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Namel=Value1, ... ,NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## PropagationSpeed - Signal propagation speed

speed of light (default) | positive scalar
Signal propagation speed, specified as the comma-separated pair consisting of
'PropagationSpeed ' and a positive scalar in meters per second.
Example: 'PropagationSpeed', physconst('LightSpeed')
Data Types: double
Weights - Subarray weights
1 (default) | $N$-by-1 complex-valued column vector | $N$-by- $L$ complex-valued matrix
Subarray weights, specified as the comma-separated pair consisting of 'Weights' and an $N$-by-1 complex-valued column vector or $N$-by- $M$ complex-valued matrix. The dimension $N$ is the number of subarrays in the array. The dimension $L$ is the number of frequencies specified by the FREQ argument.

| Weights dimension | FREQ dimension | Purpose |
| :--- | :--- | :--- |
| $N$-by-1 complex-valued column <br> vector | Scalar or 1-by-L row vector | Applies a set of weights for the <br> single frequency or for all $L$ <br> frequencies. |
| $N$-by- $L$ complex-valued matrix | 1-by-L row vector | Applies each of the $L$ columns of <br> 'Weights' for the <br> corresponding frequency in the <br> FREQ argument. |

Example: 'Weights', ones ( $\mathrm{N}, \mathrm{M}$ )

## Data Types: double

## SteerAngle - Subarray steering angle

[0;0] (default) | scalar | 2-element column vector
Subarray steering angle, specified as the comma-separated pair consisting of 'SteerAngle' and a scalar or a 2-by-1 column vector.

If 'SteerAngle' is a 2 -by- 1 column vector, it has the form [azimuth; elevation]. The azimuth angle must be between $-180^{\circ}$ and $180^{\circ}$, inclusive. The elevation angle must be between $-90^{\circ}$ and $90^{\circ}$, inclusive.

If 'SteerAngle' is a scalar, it specifies the azimuth angle only. In this case, the elevation angle is assumed to be 0 .

This option applies only when the 'SubarraySteering ' property of the System object is set to 'Phase' or 'Time'.

Example: 'SteerAngle', [20;30]
Data Types: double

## ElementWeights - Weights applied to elements within subarray

1 (default) | complex-valued $N_{S E}$-by- $N$ matrix | 1-by- $N$ cell array
Subarray element weights, specified as complex-valued $N_{S E}$-by- $N$ matrix or 1-by- $N$ cell array. Weights are applied to the individual elements within a subarray. Subarrays can have different dimensions and sizes.

If ElementWeights is a complex-valued $N_{S E}$-by- $N$ matrix, $N_{S E}$ is the number of elements in the largest subarray and $N$ is the number of subarrays. Each column of the matrix specifies the weights for the corresponding subarray. Only the first $K$ entries in each column are applied as weights where $K$ is the number of elements in the corresponding subarray.

If ElementWeights is a 1 -by- $N$ cell array. Each cell contains a complex-valued column vector of weights for the corresponding subarray. The column vectors have lengths equal to the number of elements in the corresponding subarray.

## Dependencies

To enable this name-value pair, set the SubarraySteering property of the array to 'Custom '.
Data Types: double
Complex Number Support: Yes

## Output Arguments

## D - Directivity

M-by-L matrix
Directivity, returned as an $M$-by- $L$ matrix. Each row corresponds to one of the $M$ angles specified by ANGLE. Each column corresponds to one of the $L$ frequency values specified in FREQ. Directivity units are in dBi where dBi is defined as the gain of an element relative to an isotropic radiator.

## Examples

## Directivity of Partitioned Array

Compute the directivity of a partitioned array formed from a single 20-element ULA with elements spaced one-quarter wavelength apart. The subarrays are then phase-steered towards 30 degrees azimuth. The directivities are computed at azimuth angles from 0 to 60 degrees.

```
c = physconst('LightSpeed');
fc = 3e8;
lambda = c/fc;
angsteer = [30;0];
ang = [0:10:60;0,0,0,0,0,0,0];
```

Create a partitioned ULA array using the SubarraySelection property.

```
myArray = phased.PartitionedArray('Array',...
    phased.ULA(20,lambda/4),'SubarraySelection',...
    [ones(1,10) zeros(1,10);zeros(1,10) ones(1,10)],...
    'SubarraySteering','Phase','PhaseShifterFrequency',fc);
```

Create the steering vector and compute the directivity.

```
myStv = phased.SteeringVector('SensorArray',myArray,...
    'PropagationSpeed',c);
d = directivity(myArray,fc,ang,'PropagationSpeed',c,'Weights',...
    step(myStv,fc,angsteer),'SteerAngle',angsteer)
d = 7\times1
    -7.5778
    -4.7676
    -2.0211
    10.0996
        0.9714
        -3.5575
    -10.8439
```


## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or
array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## See Also

pattern | patternAzimuth | patternElevation

## collectPlaneWave

System object: phased. PartitionedArray
Package: phased
Simulate received plane waves

## Syntax

```
Y = collectPlaneWave(H,X,ANG)
Y = collectPlaneWave(H,X,ANG,FREQ)
Y = collectPlaneWave(H,X,ANG,FREQ,C)
```


## Description

$Y=\operatorname{collectPlaneWave}(H, X, A N G)$ returns the received signals at the sensor array, $H$, when the input signals indicated by $X$ arrive at the array from the directions specified in ANG.
$Y=$ collectPlaneWave ( $H, X$, ANG, $F R E Q$ ), in addition, specifies the incoming signal carrier frequency in FREQ.
$Y=\operatorname{collectPlaneWave}(H, X, A N G, F R E Q, C)$, in addition, specifies the signal propagation speed in C.

## Input Arguments

## H

Array object.
X
Incoming signals, specified as an M-column matrix. Each column of $X$ represents an individual incoming signal.

## ANG

Directions from which incoming signals arrive, in degrees. ANG can be either a 2-by-M matrix or a row vector of length M .

If ANG is a 2-by-M matrix, each column specifies the direction of arrival of the corresponding signal in X. Each column of ANG is in the form [azimuth; elevation]. The azimuth angle must be between $-180^{\circ}$ and $180^{\circ}$, inclusive. The elevation angle must be between $-90^{\circ}$ and $90^{\circ}$, inclusive.

If ANG is a row vector of length M , each entry in ANG specifies the azimuth angle. In this case, the corresponding elevation angle is assumed to be $0^{\circ}$.

FREQ
Carrier frequency of signal in hertz. FREQ must be a scalar.
Default: 3e8

## C

Propagation speed of signal in meters per second.
Default: Speed of light

## Output Arguments

## Y

Received signals. Y is an N-column matrix, where N is the number of subarrays in the array H . Each column of $Y$ is the received signal at the corresponding subarray, with all incoming signals combined.

## Examples

## Plane Waves Received at Array Containing Subarrays

Simulate the received signal at a 16 -element ULA partitioned into four 4 -element ULAs.
Create a 16 -element ULA, and partition it into 4 -element ULAs.

```
ula = phased.ULA('NumElements',16);
array = phased.PartitionedArray('Array',ula,...
    'SubarraySelection',....
    [1 1 1 1 0 0 0 0 0 0 0 0 0 0 0 0;...
        0 0 0 0 1 1 1 1 0 0 0 0 0 0 0 0;...
        0 0 0 0 0 0 0 0 1 1 1 1 0 0 0 0;...
        0 0 0 0 0 0 0 0 0 0 0 0 1 1 1 1]);
```

Simulate received signals from $10^{\circ}$ and $30^{\circ}$ azimuth. Both signals have an elevation angle of $0^{\circ}$. Assume the propagation speed is the speed of light and the carrier frequency of the signal is 100 MHz.

```
sig = collectPlaneWave(array,randn(4,2),[10 30],1.0e8,physconst('LightSpeed'))
sig = 4×4 complex
\begin{tabular}{rrrr}
\(-0.0710-0.4765 i\) & \(0.6616-0.4676 i\) & \(0.6616+0.4676 i\) & \(-0.0710+0.4765 i\) \\
\(2.1529-1.6304 i\) & \(1.0607+0.4802 i\) & \(1.0607-0.4802 i\) & \(2.1529+1.6304 i\) \\
\(-0.6074+2.0037 i\) & \(-2.3274+1.1797 i\) & \(-2.3274-1.1797 i\) & \(-0.6074-2.0037 i\) \\
\(0.0547-0.7644 i\) & \(0.9768-0.6037 i\) & \(0.9768+0.6037 i\) & \(0.0547+0.7644 i\)
\end{tabular}
```


## Algorithms

collectPlaneWave modulates the input signal with a phase corresponding to the delay caused by the direction of arrival. This method does not account for the response of individual elements in the array and only models the array factor among subarrays. Therefore, the result does not depend on whether the subarray is steered.
uv2azel | phitheta2azel

## getElementPosition

System object: phased. PartitionedArray
Package: phased
Positions of array elements

## Syntax

POS = getElementPosition(H)

## Description

POS = getElementPosition $(H)$ returns the element positions in the array H .

## Input Arguments

H
Partitioned array object.

## Output Arguments

## POS

Element positions in array. POS is a 3-by-N matrix, where N is the number of elements in H . Each column of POS defines the position of an element in the local coordinate system, in meters, using the form [x; y; z].

## Examples

## Element Positions in Partitioned Array

Obtain the positions of the six elements in a partitioned array.

```
array = phased.PartitionedArray('Array',phased.URA('Size',[2 3]),...
    'SubarraySelection',[1 0 1 0 1 0; 0 1 0 1 0 1]);
pos = getElementPosition(array)
pos = 3\times6
```

| 0 | 0 | 0 | 0 | 0 | 0 |
| ---: | ---: | ---: | ---: | ---: | ---: |
| -0.5000 | -0.5000 | 0 | 0 | 0.5000 | 0.5000 |
| 0.2500 | -0.2500 | 0.2500 | -0.2500 | 0.2500 | -0.2500 |

## See Also

getSubarrayPosition

## getNumElements

System object: phased. PartitionedArray
Package: phased
Number of elements in array

## Syntax

N = getNumElements(H)

## Description

$\mathrm{N}=$ getNumElements $(\mathrm{H})$ returns the number of elements in the array object H .

## Input Arguments

H
Partitioned array object.

## Examples

## Number of Elements in Partitioned Array

Obtain the number of elements in an array that is partitioned into subarrays.

```
array = phased.PartitionedArray('Array',phased.URA('Size',[2 3]),...
    'SubarraySelection',[1 0 1 0 1 0; 0 1 0 1 0 1]);
N = getNumElements(array)
N = 6
```


## See Also

getNumSubarrays

## getNumSubarrays

System object: phased.PartitionedArray
Package: phased
Number of subarrays in array

## Syntax

N = getNumSubarrays(H)

## Description

$N=$ getNumSubarrays $(H)$ returns the number of subarrays in the array object H . This number matches the number of rows in the SubarraySelection property of H .

## Input Arguments

## H

Partitioned array object.

## Examples

## Number of Subarrays in Partitioned Array

Obtain the number of subarrays in a partitioned array.

```
array = phased.PartitionedArray('Array',...
    phased.ULA('NumElements',5),...
        'SubarraySelection',[1 1 1 0 0; 0 0 1 1 1]);
N = getNumSubarrays(array)
N = 2
```


## See Also

getNumElements

## getSubarrayPosition

System object: phased.PartitionedArray
Package: phased
Positions of subarrays in array

## Syntax

POS = getSubarrayPosition(H)

## Description

POS = getSubarrayPosition(H) returns the subarray positions in the array H .

## Input Arguments

H
Partitioned array object.

## Output Arguments

## POS

Subarrays positions in array. POS is a 3-by-N matrix, where N is the number of subarrays in H . Each column of POS defines the position of a subarray in the local coordinate system, in meters, using the form [x; y; z].

## Examples

## Subarray Positions in Partitioned Array

Obtain the positions of the two subarrays in a partitioned array.

```
array = phased.PartitionedArray('Array',phased.URA('Size',[2 3]),...
    'SubarraySelection',[1 0 1 0 1 0; 0 1 0 1 0 1]);
pos = getSubarrayPosition(array)
pos = 3\times2
```

| 0 | 0 |
| ---: | ---: |
| 0 | 0 |
| 0 | -0.2500 |

## See Also

getElementPosition

## isPolarizationCapable

System object: phased.PartitionedArray
Package: phased
Polarization capability

## Syntax

flag = isPolarizationCapable(h)

## Description

flag = isPolarizationCapable(h) returns a Boolean value, flag, indicating whether the array supports polarization. An array supports polarization if all its constituent sensor elements support polarization.

## Input Arguments

h - Partitioned array
Partitioned array specified as a phased. PartitionedArray System object.

## Output Arguments

## flag - Polarization-capability flag

Polarization-capability flag returned as a Boolean value. This value is true, if the array supports polarization or false, if it does not.

## Examples

## Partitioned Array of Short-Dipole Antenna Elements Supports Polarization

Determine whether a partitioned array of phased. ShortDipoleAntennaElements supports polarization.

```
antenna = phased.ShortDipoleAntennaElement('FrequencyRange',[le9 10e9]);
ulaarray = phased.ULA(4,'Element',antenna);
partitionedarray = phased.PartitionedArray('Array',ulaarray,...
    'SubarraySelection',[1 1 0 0; 0 0 1 1]);
isPolarizationCapable(partitionedarray)
ans = logical
    1
```

The returned value 1 shows that this array supports polarization.

## pattern

## System object: phased.PartitionedArray

Package: phased
Plot partitioned array directivity, field, and power patterns

## Syntax

```
pattern(sArray,FREQ)
pattern(sArray,FREQ,AZ)
pattern(sArray,FREQ,AZ,EL)
pattern(__,Name,Value)
[PAT,AZ_ANG,EL_ANG] = pattern(
```

$\qquad$

``` )
```


## Description

pattern(sArray, FREQ) plots the 3-D array directivity pattern (in dBi) for the array specified in sArray. The operating frequency is specified in FREQ.

The integration used when computing array directivity has a minimum sampling grid of 0.1 degrees. If an array pattern has a beamwidth smaller than this, the directivity value will be inaccurate.
pattern(sArray, FREQ, AZ) plots the array directivity pattern at the specified azimuth angle.
pattern(sArray, FREQ, AZ, EL) plots the array directivity pattern at specified azimuth and elevation angles.
pattern( $\qquad$ ,Name, Value) plots the array pattern with additional options specified by one or more Name, Value pair arguments.
[PAT,AZ_ANG,EL_ANG] = pattern( __ ) returns the array pattern in PAT. The AZ_ANG output contains the coordinate values corresponding to the rows of PAT. The EL_ANG output contains the coordinate values corresponding to the columns of PAT. If the 'CoordinateSystem' parameter is set to ' uv' , then AZ_ANG contains the $U$ coordinates of the pattern and EL_ANG contains the $V$ coordinates of the pattern. Otherwise, they are in angular units in degrees. $U V$ units are dimensionless.

Note This method replaces the plotResponse method. See "Convert plotResponse to pattern" on page 1-1169 for guidelines on how to use pattern in place of plotResponse.

## Input Arguments

## sArray - Partitioned array

System object
Partitioned array, specified as a phased. PartitionedArray System object.
Example: sArray= phased.PartitionedArray;

## FREQ - Frequency for computing directivity and patterns

positive scalar | 1-by-L real-valued row vector
Frequencies for computing directivity and patterns, specified as a positive scalar or 1-by-L realvalued row vector. Frequency units are in hertz.

- For an antenna, microphone, or sonar hydrophone or projector element, FREQ must lie within the range of values specified by the FrequencyRange or FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased.CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: [1e8 2e6]
Data Types: double

## AZ - Azimuth angles

[-180:180] (default) | 1-by- $N$ real-valued row vector
Azimuth angles for computing directivity and pattern, specified as a 1-by- $N$ real-valued row vector where $N$ is the number of azimuth angles. Angle units are in degrees. Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the $x y$ plane. When measured from the $x$-axis toward the $y$-axis, this angle is positive.

## Example: [-45:2:45]

Data Types: double

## EL - Elevation angles

[-90:90] (default) | 1-by-M real-valued row vector
Elevation angles for computing directivity and pattern, specified as a 1-by-M real-valued row vector where $M$ is the number of desired elevation directions. Angle units are in degrees. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

The elevation angle is the angle between the direction vector and $x y$-plane. The elevation angle is positive when measured towards the $z$-axis.
Example: [-75:1:70]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

```
CoordinateSystem - Plotting coordinate system
'polar' (default)|'rectangular'|'uv'
```

Plotting coordinate system of the pattern, specified as the comma-separated pair consisting of 'CoordinateSystem' and one of 'polar', 'rectangular', or 'uv'. When
'CoordinateSystem' is set to 'polar' or 'rectangular', the AZ and EL arguments specify the pattern azimuth and elevation, respectively. AZ values must lie between $-180^{\circ}$ and $180^{\circ}$. EL values must lie between $-90^{\circ}$ and $90^{\circ}$. If 'CoordinateSystem' is set to 'uv', AZ and EL then specify $U$ and $V$ coordinates, respectively. AZ and EL must lie between -1 and 1.
Example: 'uv'
Data Types: char

## Type - Displayed pattern type

'directivity' (default)| 'efield'|'power'|'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type ' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb' - power pattern converted to dB.

Example: 'powerdb'
Data Types: char

## Orientation - Array orientation

[0;0;0]. (default)|3-by-1 real-valued column vector
Array orientation, specified as a 3-by-1 real-valued column vector containing the rotation angles with respect to the $x-y$-, and $z$-axes of the local coordinate system, respectively.

## Normalize - Display normalize pattern

true (default) | false
Display normalized pattern, specified as the comma-separated pair consisting of 'Normalize' and a Boolean. Set this parameter to true to display a normalized pattern. This parameter does not apply when you set 'Type' to 'directivity'. Directivity patterns are already normalized.
Data Types: logical

## ShowArray - View array geometry

false (default)| true
View the array geometry along with the 3D radiation pattern, specified as false or true.
Data Types: logical
ShowLocalCoordinates - Show local coordinate axes
true (default) | false
Show the local coordinate axes, specified as true or false.
Data Types: logical

## ShowColorbar - Show colorbar

true (default) | false

Show the colorbar, specified as true or false.
Data Types: logical

## Parent - Handle to axis

scalar
Handle to the axes along which the array geometry is displayed specified as a scalar.

## PlotStyle - Plotting style

'overlay' (default)|'waterfall'
Plotting style, specified as the comma-separated pair consisting of 'Plotstyle' and either ' overlay' or 'waterfall'. This parameter applies when you specify multiple frequencies in FREQ in 2-D plots. You can draw 2-D plots by setting one of the arguments AZ or EL to a scalar.

## Data Types: char

## Polarization - Polarized field component

'combined' (default)|'H'|'V'
Polarized field component to display, specified as the comma-separated pair consisting of 'Polarization' and 'combined ', 'H' , or 'V'. This parameter applies only when the sensors are polarization-capable and when the 'Type' parameter is not set to 'directivity'. This table shows the meaning of the display options.

| 'Polarization' | Display |
| :--- | :--- |
| ' combined ' | Combined $H$ and $V$ polarization components |
| 'H' | $H$ polarization component |
| ' $\mathrm{V}^{\prime}$ | V polarization component |

Example: 'V '
Data Types: char
PropagationSpeed - Signal propagation speed
speed of light (default) | positive scalar
Signal propagation speed, specified as the comma-separated pair consisting of ' PropagationSpeed ' and a positive scalar in meters per second.
Example: 'PropagationSpeed', physconst('LightSpeed')
Data Types: double

## Weights - Subarray weights

1 (default) | $N$-by-1 complex-valued column vector | $N$-by-L complex-valued matrix
Subarray weights, specified as the comma-separated pair consisting of 'Weights' and an $N$-by-1 complex-valued column vector or $N$-by- $M$ complex-valued matrix. The dimension $N$ is the number of subarrays in the array. The dimension $L$ is the number of frequencies specified by the FREQ argument.

| Weights dimension | FREQ dimension | Purpose |
| :--- | :--- | :--- |
| $N$-by-1 complex-valued column <br> vector | Scalar or 1-by- $L$ row vector | Applies a set of weights for the <br> single frequency or for all $L$ <br> frequencies. |
| $N$-by- $L$ complex-valued matrix | 1-by- $L$ row vector | Applies each of the $L$ columns of <br> 'Weights' for the <br> corresponding frequency in the <br> FREQ argument. |

## Example: 'Weights', ones ( $\mathrm{N}, \mathrm{M}$ )

Data Types: double

## SteerAngle - Subarray steering angle

[0;0] (default) | scalar | 2-element column vector
Subarray steering angle, specified as the comma-separated pair consisting of 'SteerAngle' and a scalar or a 2-by-1 column vector.

If 'SteerAngle' is a 2 -by- 1 column vector, it has the form [azimuth; elevation]. The azimuth angle must be between $-180^{\circ}$ and $180^{\circ}$, inclusive. The elevation angle must be between $-90^{\circ}$ and $90^{\circ}$, inclusive.

If 'SteerAngle' is a scalar, it specifies the azimuth angle only. In this case, the elevation angle is assumed to be 0 .

This option applies only when the 'SubarraySteering ' property of the System object is set to 'Phase' or 'Time'.

Example: 'SteerAngle', [20;30]
Data Types: double

## ElementWeights - Weights applied to elements within subarray

1 (default) | complex-valued $N_{S E}-$ by- $N$ matrix | 1 -by- $N$ cell array
Subarray element weights, specified as complex-valued $N_{S E}$-by- $N$ matrix or 1-by- $N$ cell array. Weights are applied to the individual elements within a subarray. Subarrays can have different dimensions and sizes.

If ElementWeights is a complex-valued $N_{S E}$-by- $N$ matrix, $N_{S E}$ is the number of elements in the largest subarray and $N$ is the number of subarrays. Each column of the matrix specifies the weights for the corresponding subarray. Only the first $K$ entries in each column are applied as weights where $K$ is the number of elements in the corresponding subarray.

If ElementWeights is a 1-by- $N$ cell array. Each cell contains a complex-valued column vector of weights for the corresponding subarray. The column vectors have lengths equal to the number of elements in the corresponding subarray.

## Dependencies

To enable this name-value pair, set the SubarraySteering property of the array to 'Custom '.

## Output Arguments

## PAT - Array pattern

$M$-by- $N$ real-valued matrix
Array pattern, returned as an $M$-by- $N$ real-valued matrix. The dimensions of PAT correspond to the dimensions of the output arguments AZ_ANG and EL_ANG.

## AZ_ANG - Azimuth angles

scalar | 1-by-N real-valued row vector
Azimuth angles for displaying directivity or response pattern, returned as a scalar or 1-by- $N$ realvalued row vector corresponding to the dimension set in AZ. The columns of PAT correspond to the values in AZ_ANG. Units are in degrees.

## EL_ANG - Elevation angles

scalar | 1-by-M real-valued row vector
Elevation angles for displaying directivity or response, returned as a scalar or 1-by-M real-valued row vector corresponding to the dimension set in EL. The rows of PAT correspond to the values in EL_ANG. Units are in degrees.

## Examples

## Azimuth Response of Partitioned ULA

Plot the azimuth response of a 4 -element ULA partitioned into two 2 -element ULA's. The element spacing is one-half wavelength.

Create the ULA, and partition it into two 2-element ULA's.

```
sULA = phased.ULA('NumElements',4,'ElementSpacing',0.5);
sPA = phased.PartitionedArray('Array',sULA,...
    'SubarraySelection',[1 1 0 0;0 0 1 1]);
```

Plot the azimuth response of the array. Assume the operating frequency is 1 GHz and the propagation speed is the speed of light.

```
fc = 1e9;
pattern(sPA,fc,[-180:180],0,'Type','powerdb',...
    'CoordinateSystem','polar',...
    'Normalize',true)
```



Normalized Power (dB), Broadside at $0.00^{\circ}$

## Plot Pattern and Directivity of Partitioned URA Over Restricted Range of Angles

Convert a 2-by-6 URA of isotropic antenna elements into a 1-by-3 partitioned array so that each subarray of the partitioned array is a 2-by-2 URA. Assume that the frequency response of the elements lies between 1 and 6 GHz . The elements are spaced one-half wavelength apart corresponding to the highest frequency of the element response. Plot an azimuth cut from -50 to 50 degrees for different two sets of weights. For partitioned arrays, weights are applied to the subarrays instead of the elements.

## Create partitioned array

```
fmin = le9;
fmax = 6e9;
c = physconst('LightSpeed');
lam = c/fmax;
sIso = phased.IsotropicAntennaElement(...
    'FrequencyRange',[fmin,fmax],...
    'BackBaffled',false);
sURA = phased.URA('Element',sIso,'Size',[2,6],...
    'ElementSpacing',[lam/2,lam/2]);
subarraymap = [[1,1,1,1,0,0,0,0,0,0,0,0];...
    [0,0,0,0,1,1,1,1,0,0,0,0];...
    [0,0,0,0,0,0,0,0,1,1,1,1]];
```

```
sPA = phased.PartitionedArray('Array',sURA,...
    'SubarraySelection',subarraymap);
```


## Plot power pattern

Plot the response of the array at 5 GHz over the restricted range of azimuth angles.

```
fc = 5e9;
wts = [[1,1,1]',[.862,1.23,.862]'];
pattern(sPA,fc,[-50:0.1:50],0,...
    'Type','powerdb',...
    'CoordinateSystem','polar',...
    'Weights',wts)
```



Normalized Power (dB), Broadside at $0.00^{\circ}$
The plot of the response shows the broadening of the main lobe and the reduction of the strength of the sidelobes caused by the weight tapering.

## Plot directivity

Plot an azimuth cut of the directivity of the array at 5 GHz over the restricted range of azimuth angles for the two different sets of weights.

```
fc = 5e9;
wts = [[1,1,1]',[.862,1.23,.862]'];
pattern(sPA,fc,[-50:0.1:50],0,...
    'Type','directivity',...
    'CoordinateSystem','rectangular',...
    'Weights',wts)
```



## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \Pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Convert plotResponse to pattern

For antenna, microphone, and array System objects, the pattern method replaces the plotResponse method. In addition, two new simplified methods exist just to draw 2-D azimuth and elevation pattern plots. These methods are azimuthPattern and elevationPattern.

The following table is a guide for converting your code from using plotResponse to pattern. Notice that some of the inputs have changed from input arguments to Name-Value pairs and conversely. The general pattern method syntax is
pattern(H,FREQ,AZ,EL,'Name1','Value1',...,'NameN','ValueN')

| plotResponse Inputs | plotResponse Description | pattern Inputs |
| :--- | :--- | :--- |
| H argument | Antenna, microphone, or array <br> System object. | H argument (no change) |
| FREQ argument | Operating frequency. | FREQ argument (no change) |
| V argument | Propagation speed. This argument <br> is used only for arrays. | 'PropagationSpeed ' name-value <br> pair. This parameter is only used for <br> arrays. |


| plotResponse Inputs | plotResponse Description |  | pattern Inputs |  |
| :---: | :---: | :---: | :---: | :---: |
| 'Format' and 'RespCut' namevalue pairs | These options work together to let you create a plot in angle space (line or polar style) or $U V$ space. They also determine whether the plot is 2-D or 3-D. This table shows you how to create different types of plots using plotResponse. |  | 'CoordinateSystem' name-value pair used together with the AZ and EL input arguments. <br> 'CoordinateSystem' has the same options as the plotResponse method 'Format ' name-value pair, except that ' line' is now named 'rectangular'. The table shows how to create different types of plots using pattern. |  |
|  | Display space <br> Angle space (2D) |  |  |  |
|  | Angle space (2D) | Set 'RespCut' <br> to 'Az' or |  |  |
|  |  | 'El'. Set <br> 'Format ' to <br> 'line' or 'polar'. | Display space |  |
|  |  | ' line' or 'polar'. <br> Set the display axis using either the 'AzimuthAngle | Angle space (2D) | Set <br> Coordinate <br> System' to <br> rectangular' <br> or 'polar' <br> Specify either AZ <br> or EL as a scalar. |
|  |  | s' or 'ElevationAng les' namevalue pairs. | Angle space (3D) | Set <br> 'Coordinate <br> System' to 'rectangular' |
|  | Angle space (3D) | Set 'RespCut' to '3D'. Set |  | or 'polar'. <br> Specify both AZ <br> and EL as <br> vectors. |
|  |  | 'polar'. <br> Set the display axis using both the 'AzimuthAngle s' and 'Elevation | $U V$ space (2D) | Set <br> Coordinate System' to uv'. Use AZ to specify a $U$ space vector. Use EL to specify a $V$-space scalar. |
|  |  | Angles' namevalue pairs. | UV space (3D) |  |
|  | UV space (2D) | Set 'RespCut' to'U'. Set 'Format ' to 'UV'. Set the display range using the 'UGrid' namevalue pair. |  | 'Coordinate <br> System' to <br> 'uv'. Use AZ to <br> specify a $U$ - <br> space vector. <br> Use EL to specify <br> a $V$-space vector. |
|  |  |  | If you set CoordinateSystem to 'uv ' , enter the UV grid values using $A Z$ and $E L$. |  |
|  | UV space (3D) | $\begin{aligned} & \text { Set 'RespCut' } \\ & \text { to'3D'. Set } \\ & \text { 'Format' to } \end{aligned}$ |  |  |


| plotResponse Inputs | plotResponse Description |  | pattern Inputs |
| :---: | :---: | :---: | :---: |
|  | Display space | 'UV '. Set the display range using both the 'UGrid' and 'VGrid ' namevalue pairs. |  |
| 'CutAngle' name-value pair | Constant angle at to take an azimuth or elevation cut. When producing a 2-D plot and when 'RespCut' is set to 'Az' or 'El', use 'CutAngle' to set the slice across which to view the plot. |  | No equivalent name-value pair. To create a cut, specify either AZ or EL as a scalar, not a vector. |
| 'NormalizeResponse' namevalue pair | Normalizes the plot. When 'Unit' is set to 'dbi' , you cannot specify 'NormalizeResponse'. |  | Use the 'Normalize' name-value pair. When 'Type' is set to 'directivity' you cannot specify 'Normalize'. |
| 'OverlayFreq' name-value pair | Plot multiple frequencies on the same 2-D plot. Available only when 'Format' is set to 'line' or 'uv and 'RespCut' is not set to '3D'. The value true produces an overlay plot and the value false produces a waterfall plot. |  | 'PlotStyle' name-value pair plots multiple frequencies on the same 2-D plot. <br> The values 'overlay' and 'waterfall' correspond to 'OverlayFreq' values of true and false. The option 'waterfall' is allowed only when 'CoordinateSystem' is set to 'rectangular' or 'uv'. |
| 'Polarization' name-value pair | Determines how to plot polarized fields. Options are 'None', 'Combined', 'H', or 'V'. |  | 'Polarization ' name-value pair determines how to plot polarized fields. The 'None ' option is removed. The options 'Combined ' , ' H ', or 'V' are unchanged. |
| ' Unit ' name-value pair | Determines the plot units. Choose 'db','mag', 'pow', or 'dbi', where the default is ' db ' |  | 'Type ' name-value pair, uses equivalent options with different names |
|  |  |  | plotResponse pattern |
|  |  |  | 'db' 'powerdb' <br> 'mag' 'efield' <br> 'pow' 'power' <br> 'dbi' 'directivity' |
| 'Weights ' name-value pair | Array element tapers (or weights). |  | 'Weights ' name-value pair (no change). |
| 'AzimuthAngles ' name-value pair | Azimuth angles used to display the antenna or array response. |  | AZ argument |


| plotResponse Inputs | plotResponse Description | pattern Inputs |
| :--- | :--- | :--- |
| ' ElevationAngles ' name-value <br> pair | Elevation angles used to display the <br> antenna or array response. | EL argument |
| ' UGrid' name-value pair | Contains $U$ coordinates in $U V$ - <br> space. | AZ argument when <br> 'CoordinateSystem ' name-value <br> pair is set to 'uv ' |
| 'VGrid' name-value pair | Contains $V$-coordinates in $U V$-space. | EL argument when <br> 'CoordinateSystem ' name-value <br> pair is set to 'uv ' |

## Version History <br> Introduced in R2015a

See Also<br>patternAzimuth|patternElevation

## patternAzimuth

System object: phased. PartitionedArray
Package: phased
Plot partitioned array directivity or pattern versus azimuth

## Syntax

```
patternAzimuth(sArray,FREQ)
patternAzimuth(sArray,FREQ,EL)
patternAzimuth(sArray,FREQ,EL,Name,Value)
PAT = patternAzimuth(
```

$\qquad$

``` )
```


## Description

patternAzimuth (sArray, FREQ) plots the 2-D array directivity pattern versus azimuth (in dBi) for the array sArray at zero degrees elevation angle. The argument FREQ specifies the operating frequency.

The integration used when computing array directivity has a minimum sampling grid of 0.1 degrees. If an array pattern has a beamwidth smaller than this, the directivity value will be inaccurate.
patternAzimuth(sArray, FREQ,EL), in addition, plots the 2-D array directivity pattern versus azimuth (in dBi) for the array sArray at the elevation angle specified by EL. When EL is a vector, multiple overlaid plots are created.
patternAzimuth(sArray, FREQ,EL,Name, Value) plots the array pattern with additional options specified by one or more Name, Value pair arguments.

PAT = patternAzimuth ( _ _ ) returns the array pattern. PAT is a matrix whose entries represent the pattern at corresponding sampling points specified by the 'Azimuth ' parameter and the EL input argument.

## Input Arguments

## sArray - Partitioned array

System object
Partitioned array, specified as a phased.PartitionedArray System object.
Example: sArray= phased.PartitionedArray;

## FREQ - Frequency for computing directivity and pattern

positive scalar
Frequency for computing directivity and pattern, specified as a positive scalar. Frequency units are in hertz.

- For an antenna or microphone element, FREQ must lie within the range of values specified by the FrequencyRange or the FrequencyVector property of the element. Otherwise, the element
produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased.CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: 1e8
Data Types: double

## EL - Elevation angles

## 1-by- $N$ real-valued row vector

Elevation angles for computing sensor or array directivities and patterns, specified as a 1-by- $N$ realvalued row vector. The quantity $N$ is the number of requested elevation directions. Angle units are in degrees. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

The elevation angle is the angle between the direction vector and the xy plane. When measured toward the $z$-axis, this angle is positive.
Example: [0, 10, 20]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Type - Displayed pattern type

'directivity' (default)|'efield'|'power'|'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb' - power pattern converted to dB.

Example: 'powerdb'
Data Types: char

## PropagationSpeed - Signal propagation speed

## speed of light (default) | positive scalar

Signal propagation speed, specified as the comma-separated pair consisting of ' PropagationSpeed ' and a positive scalar in meters per second.
Example: 'PropagationSpeed', physconst('LightSpeed')
Data Types: double

## Weights - Subarray weights

M-by-1 complex-valued column vector
Subarray weights, specified as the comma-separated pair consisting of 'Weights ' and an $M$-by-1 complex-valued column vector. Subarray weights are applied to the subarrays of the array to produce array steering, tapering, or both. The dimension $M$ is the number of subarrays in the array.

Example: 'Weights', ones (10, 1)
Data Types: double
Complex Number Support: Yes

## SteerAngle - Subarray steering angle

[0;0] (default) | scalar | 2 -element column vector
Subarray steering angle, specified as the comma-separated pair consisting of 'SteerAngle' and a scalar or a 2-by-1 column vector.

If 'SteerAngle' is a 2 -by- 1 column vector, it has the form [azimuth; elevation]. The azimuth angle must be between $-180^{\circ}$ and $180^{\circ}$, inclusive. The elevation angle must be between $-90^{\circ}$ and $90^{\circ}$, inclusive.

If 'SteerAngle' is a scalar, it specifies the azimuth angle only. In this case, the elevation angle is assumed to be 0 .

This option applies only when the 'SubarraySteering ' property of the System object is set to 'Phase' or 'Time'.

Example: 'SteerAngle', [20;30]
Data Types: double

## ElementWeights - Weights applied to elements within subarray

1 (default) | complex-valued $N_{S E}$-by- $N$ matrix | 1-by- $N$ cell array
Subarray element weights, specified as complex-valued $N_{S E}$-by- $N$ matrix or 1-by- $N$ cell array. Weights are applied to the individual elements within a subarray. Subarrays can have different dimensions and sizes.

If ElementWeights is a complex-valued $N_{S E}$-by- $N$ matrix, $N_{S E}$ is the number of elements in the largest subarray and $N$ is the number of subarrays. Each column of the matrix specifies the weights for the corresponding subarray. Only the first $K$ entries in each column are applied as weights where $K$ is the number of elements in the corresponding subarray.

If ElementWeights is a 1 -by- $N$ cell array. Each cell contains a complex-valued column vector of weights for the corresponding subarray. The column vectors have lengths equal to the number of elements in the corresponding subarray.

## Dependencies

To enable this name-value pair, set the SubarraySteering property of the array to 'Custom '.

```
Data Types: double
Complex Number Support: Yes
```


## Azimuth - Azimuth angles

[-180:180] (default) | 1-by-P real-valued row vector

Azimuth angles, specified as the comma-separated pair consisting of 'Azimuth' and a 1-by-P realvalued row vector. Azimuth angles define where the array pattern is calculated.

## Example: 'Azimuth', [-90:2:90]

Data Types: double

## Parent - Handle to axis

scalar
Handle to the axes along which the array geometry is displayed specified as a scalar.

## Output Arguments

## PAT - Array directivity or pattern

## L-by- $N$ real-valued matrix

Array directivity or pattern, returned as an $L$-by- $N$ real-valued matrix. The dimension $L$ is the number of azimuth values determined by the 'Azimuth' name-value pair argument. The dimension $N$ is the number of elevation angles, as determined by the EL input argument.

## Examples

## Plot Azimuth Directivity of Partitioned URA

Convert a 2-by-6 URA of isotropic antenna elements into a 1-by-3 partitioned array so that each subarray of the partitioned array is a 2-by-2 URA. Assume that the frequency response of the elements lies between 1 and 6 GHz . The elements are spaced one-half wavelength apart corresponding to the highest frequency of the element response. Plot the azimuth directivity. For partitioned arrays, weights are applied to the subarrays instead of the elements.

## Create partitioned array

```
fmin = 1e9;
fmax = 6e9;
c = physconst('LightSpeed');
lam = c/fmax;
sIso = phased.IsotropicAntennaElement(...
    'FrequencyRange',[fmin,fmax],...
    'BackBaffled',false);
sURA = phased.URA('Element',sIso,'Size',[2,6],...
    'ElementSpacing',[lam/2,lam/2]);
subarraymap = [[1,1,1,1,0,0,0,0,0,0,0,0];...
    [0,0,0,0,1,1,1,1,0,0,0,0];...
    [0,0,0,0,0,0,0,0,1,1,1,1]];
sPA = phased.PartitionedArray('Array',sURA,...
    'SubarraySelection',subarraymap);
```


## Plot azimuth directivity pattern

Plot the response of the array at 5 GHz

```
fc = 5e9;
wts = [0.862,1.23,0.862]';
patternAzimuth(sPA,fc,0,...
```

```
'Type','directivity',...
'PropagationSpeed',physconst('LightSpeed'),...
'Weights',wts)
```



Directivity (dBi), Broadside at $0.00^{\circ}$

## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \Pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\mathrm{total}}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as dBi. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Version History

Introduced in R2015a

See Also<br>pattern| patternElevation

## patternElevation

System object: phased. PartitionedArray
Package: phased
Plot partitioned array directivity or pattern versus elevation

## Syntax

```
patternElevation(sArray,FREQ)
patternElevation(sArray,FREQ,AZ)
patternElevation(sArray,FREQ,AZ,Name,Value)
PAT = patternElevation(
```

$\qquad$

``` )
```


## Description

patternElevation(sArray, FREQ) plots the 2-D array directivity pattern versus elevation (in dBi ) for the array sArray at zero degrees azimuth angle. When AZ is a vector, multiple overlaid plots are created. The argument FREQ specifies the operating frequency.

The integration used when computing array directivity has a minimum sampling grid of 0.1 degrees. If an array pattern has a beamwidth smaller than this, the directivity value will be inaccurate.
patternElevation(sArray, FREQ, AZ), in addition, plots the 2-D element directivity pattern versus elevation (in dBi ) at the azimuth angle specified by $A Z$. When $A Z$ is a vector, multiple overlaid plots are created.
patternElevation(sArray, FREQ,AZ, Name, Value) plots the array pattern with additional options specified by one or more Name, Value pair arguments.

PAT = patternElevation ( _ ) returns the array pattern. PAT is a matrix whose entries represent the pattern at corresponding sampling points specified by the 'Elevation' parameter and the AZ input argument.

## Input Arguments

## sArray - Partitioned array

System object
Partitioned array, specified as a phased. PartitionedArray System object.
Example: sArray= phased.PartitionedArray;

## FREQ - Frequency for computing directivity and pattern

positive scalar
Frequency for computing directivity and pattern, specified as a positive scalar. Frequency units are in hertz.

- For an antenna or microphone element, FREQ must lie within the range of values specified by the FrequencyRange or the FrequencyVector property of the element. Otherwise, the element
produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased.CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: 1e8
Data Types: double

## AZ - Azimuth angles for computing directivity and pattern

1-by- $N$ real-valued row vector
Azimuth angles for computing sensor or array directivities and patterns, specified as a 1 -by- $N$ realvalued row vector where $N$ is the number of desired azimuth directions. Angle units are in degrees. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the $x y$ plane. This angle is positive when measured from the $x$-axis toward the $y$-axis.
Example: [0,10,20]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Type - Displayed pattern type

'directivity' (default)|'efield'|'power'|'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb' - power pattern converted to dB.

Example: 'powerdb'
Data Types: char

## PropagationSpeed - Signal propagation speed

speed of light (default) | positive scalar
Signal propagation speed, specified as the comma-separated pair consisting of ' PropagationSpeed ' and a positive scalar in meters per second.
Example: 'PropagationSpeed', physconst('LightSpeed')
Data Types: double

## Weights - Subarray weights

M-by-1 complex-valued column vector
Subarray weights, specified as the comma-separated pair consisting of 'Weights ' and an $M$-by-1 complex-valued column vector. Subarray weights are applied to the subarrays of the array to produce array steering, tapering, or both. The dimension $M$ is the number of subarrays in the array.

Example: 'Weights', ones (10, 1)
Data Types: double
Complex Number Support: Yes

## SteerAngle - Subarray steering angle

[0;0] (default) | scalar | 2 -element column vector
Subarray steering angle, specified as the comma-separated pair consisting of 'SteerAngle' and a scalar or a 2-by-1 column vector.

If 'SteerAngle' is a 2 -by- 1 column vector, it has the form [azimuth; elevation]. The azimuth angle must be between $-180^{\circ}$ and $180^{\circ}$, inclusive. The elevation angle must be between $-90^{\circ}$ and $90^{\circ}$, inclusive.

If 'SteerAngle' is a scalar, it specifies the azimuth angle only. In this case, the elevation angle is assumed to be 0 .

This option applies only when the 'SubarraySteering ' property of the System object is set to 'Phase' or 'Time'.

Example: 'SteerAngle', [20;30]
Data Types: double

## ElementWeights - Weights applied to elements within subarray

1 (default) | complex-valued $N_{S E}$-by- $N$ matrix | 1-by- $N$ cell array
Subarray element weights, specified as complex-valued $N_{S E}$-by- $N$ matrix or 1-by- $N$ cell array. Weights are applied to the individual elements within a subarray. Subarrays can have different dimensions and sizes.

If ElementWeights is a complex-valued $N_{S E}$-by- $N$ matrix, $N_{S E}$ is the number of elements in the largest subarray and $N$ is the number of subarrays. Each column of the matrix specifies the weights for the corresponding subarray. Only the first $K$ entries in each column are applied as weights where $K$ is the number of elements in the corresponding subarray.

If ElementWeights is a 1 -by- $N$ cell array. Each cell contains a complex-valued column vector of weights for the corresponding subarray. The column vectors have lengths equal to the number of elements in the corresponding subarray.

## Dependencies

To enable this name-value pair, set the SubarraySteering property of the array to 'Custom '.

## Data Types: double <br> Complex Number Support: Yes

## Elevation - Elevation angles

[-90:90] (default) | 1-by-P real-valued row vector

Elevation angles, specified as the comma-separated pair consisting of 'Elevation' and a 1-by-P real-valued row vector. Elevation angles define where the array pattern is calculated.
Example: 'Elevation', [-90:2:90]
Data Types: double

## Parent - Handle to axis

scalar
Handle to the axes along which the array geometry is displayed specified as a scalar.

## Output Arguments

## PAT - Array directivity or pattern

L-by- $N$ real-valued matrix
Array directivity or pattern, returned as an $L$-by- $N$ real-valued matrix. The dimension $L$ is the number of elevation angles determined by the 'Elevation' name-value pair argument. The dimension $N$ is the number of azimuth angles determined by the AZ argument.

## Examples

## Plot Elevation Directivity of Partitioned URA

Convert a 2-by-6 URA of isotropic antenna elements into a 1-by-3 partitioned array so that each subarray of the partitioned array is a 2-by-2 URA. Assume that the frequency response of the elements lies between 1 and 6 GHz . The elements are spaced one-half wavelength apart corresponding to the highest frequency of the element response. Plot the directivity for elevation angles from - 45 to 45 degrees. For partitioned arrays, weights are applied to the subarrays instead of the elements.

## Create partitioned array

```
fmin = 1e9;
fmax = 6e9;
c = physconst('LightSpeed');
lam = c/fmax;
sIso = phased.IsotropicAntennaElement(...
    'FrequencyRange',[fmin,fmax],...
    'BackBaffled',false);
sURA = phased.URA('Element',sIso,'Size',[2,6],\ldots.
    'ElementSpacing',[lam/2,lam/2]);
subarraymap = [[1,1,1,1,0,0,0,0,0,0,0,0];...
    [0,0,0,0,1,1,1,1,0,0,0,0];...
    [0,0,0,0,0,0,0,0,1,1,1,1]];
sPA = phased.PartitionedArray('Array',sURA,...
    'SubarraySelection',subarraymap);
```

Plot elevation directivity pattern
Plot the response of the array at 5 GHz

```
fc = 5e9;
wts = [0.862,1.23,0.862]';
```

```
azimangle = 0;
patternElevation(sPA,fc,azimangle,...
    'Type','directivity',...
    'PropagationSpeed',physconst('LightSpeed'),...
    'Elevation',[-45:45],...
    'Weights',wts)
```



Directivity (dBi), Broadside at $0.00^{\circ}$

## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \Pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\mathrm{total}}}
$$

where $U_{\text {rad }}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or
array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Version History

Introduced in R2015a

## See Also

pattern| patternAzimuth

## plotResponse

System object: phased. PartitionedArray
Package: phased
Plot response pattern of array

## Syntax

plotResponse( H, FREQ, V )
plotResponse(H, FREQ, V, Name, Value)
hPlot = plotResponse( $\qquad$ )

## Description

plotResponse ( $\mathrm{H}, \mathrm{FREQ}, \mathrm{V}$ ) plots the array response pattern along the azimuth cut, where the elevation angle is 0 . The operating frequency is specified in FREQ. The propagation speed is specified in $V$.
plotResponse(H, FREQ, V,Name, Value) plots the array response with additional options specified by one or more Name, Value pair arguments.
hPlot = plotResponse( $\qquad$ ) returns handles of the lines or surface in the figure window, using any of the input arguments in the previous syntaxes.

## Input Arguments

H
Array object.

## FREQ

Operating frequency in hertz. Typical values are within the range specified by a property of H.Array.Element. That property is named FrequencyRange or FrequencyVector, depending on the type of element in the array. The element has zero response at frequencies outside that range. If FREQ is a nonscalar row vector, the plot shows multiple frequency responses on the same axes.

## V

Propagation speed in meters per second.

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, ... , NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## CutAngle

Cut angle specified as a scalar. This argument is applicable only when RespCut is ' Az ' or ' El '. If RespCut is 'Az', CutAngle must be between -90 and 90. If RespCut is 'El', CutAngle must be between -180 and 180.

Default: 0

## Format

Format of the plot, using one of 'Line', 'Polar', or 'UV'. If you set Format to 'UV', FREQ must be a scalar.

## Default: 'Line'

## NormalizeResponse

Set this value to true to normalize the response pattern. Set this value to false to plot the response pattern without normalizing it. This parameter is not applicable when you set the Unit parameter value to 'dbi'.

## Default: true

## OverlayFreq

Set this value to true to overlay pattern cuts in a 2-D line plot. Set this value to false to plot pattern cuts against frequency in a 3-D waterfall plot. If this value is false, then FREQ must be a vector with at least two entries.

This parameter applies only when Format is not 'Polar' and RespCut is not '3D'.

## Default: true

## Polarization

Specify the polarization options for plotting the array response pattern. The allowable values are |'None' | 'Combined' | 'H' | 'V' | where:

- 'None ' specifies plotting a nonpolarized response pattern
- 'Combined ' specifies plotting a combined polarization response pattern
- 'H' specifies plotting the horizontal polarization response pattern
- 'V' specifies plotting the vertical polarization response pattern

For arrays that do not support polarization, the only allowed value is 'None '. This parameter is not applicable when you set the Unit parameter value to 'dbi'.

Default: 'None'

## RespCut

Cut of the response. Valid values depend on Format, as follows:

- If Format is 'Line' or 'Polar', the valid values of RespCut are 'Az', 'El', and '3D'. The default is ' Az '.
- If Format is 'UV', the valid values of RespCut are 'U' and '3D'. The default is 'U'.

If you set RespCut to ' 3 D ' , FREQ must be a scalar.

## SteerAng

Subarray steering angle. SteerAng can be either a 2 -element column vector or a scalar.
If SteerAng is a 2 -element column vector, it has the form [azimuth; elevation]. The azimuth angle must be between -180 and 180 degrees, inclusive. The elevation angle must be between -90 and 90 degrees, inclusive.

If SteerAng is a scalar, it specifies the azimuth angle. In this case, the elevation angle is assumed to be 0 .

This option is applicable only if the SubarraySteering property of H is 'Phase' or 'Time '.
Default: [0;0]

## Unit

The unit of the plot. Valid values are 'db', 'mag', 'pow', or 'dbi'. This parameter determines the type of plot that is produced.

| Unit value | Plot type |
| :--- | :--- |
| db | power pattern in dB scale |
| mag | field pattern |
| pow | power pattern |
| dbi | directivity |

Default: 'db'
Weights
Weight values applied to the array, specified as a length- $N$ column vector or $N$-by- $M$ matrix. The dimension $N$ is the number of subarrays in the array. The interpretation of $M$ depends upon whether the input argument FREQ is a scalar or row vector.

| Weights Dimension | FREQ Dimension | Purpose |
| :--- | :--- | :--- |
| $N$-by-1 column vector | Scalar or 1-by-M row vector | Apply one set of weights for the <br> same single frequency or all $M$ <br> frequencies. |
| $N$-by- $M$ matrix | Scalar | Apply all of the $M$ different <br> columns in Weights for the <br> same single frequency. |
|  | 1-by- $M$ row vector | Apply each of the $M$ different <br> columns in Weights for the <br> corresponding frequency in <br> FREQ. |

## AzimuthAngles

Azimuth angles for plotting subarray response, specified as a row vector. The AzimuthAngles parameter sets the display range and resolution of azimuth angles for visualizing the radiation pattern. This parameter is allowed only when the RespCut parameter is set to 'Az' or '3D' and the Format parameter is set to 'Line' or 'Polar'. The values of azimuth angles should lie between $180^{\circ}$ and $180^{\circ}$ and must be in nondecreasing order. When you set the RespCut parameter to ' 3 D ', you can set the AzimuthAngles and ElevationAngles parameters simultaneously.

Default: [-180:180]

## ElevationAngles

Elevation angles for plotting subarray response, specified as a row vector. The ElevationAngles parameter sets the display range and resolution of elevation angles for visualizing the radiation pattern. This parameter is allowed only when the RespCut parameter is set to 'El' or '3D' and the Format parameter is set to 'Line' or 'Polar'. The values of elevation angles should lie between $90^{\circ}$ and $90^{\circ}$ and must be in nondecreasing order. When you set the RespCut parameter to ' $3 \mathrm{D}^{\prime}$ ', you can set the ElevationAngles and AzimuthAngles parameters simultaneously.

Default: [-90:90]

## UGrid

$U$ coordinate values for plotting subarray response, specified as a row vector. The UGrid parameter sets the display range and resolution of the $U$ coordinates for visualizing the radiation pattern in $U / V$ space. This parameter is allowed only when the Format parameter is set to ' UV ' and the RespCut parameter is set to ' $U$ ' or ' $3 D$ '. The values of $U G$ rid should be between -1 and 1 and should be specified in nondecreasing order. You can set the UGrid and VGrid parameters simultaneously.

Default: [-1:0.01:1]

## VGrid

$V$ coordinate values for plotting subarray response, specified as a row vector. The VGrid parameter sets the display range and resolution of the $V$ coordinates for visualizing the radiation pattern in $U / V$ space. This parameter is allowed only when the Format parameter is set to 'UV' and the RespCut parameter is set to ' 3 D '. The values of VGrid should be between -1 and 1 and should be specified in nondecreasing order. You can set the VGrid and UGrid parameters simultaneously.

Default: [-1:0.01:1]

## Examples

## Azimuth Response of Partitioned ULA

Plot the azimuth response of a 4-element ULA partitioned into two 2 -element ULA's. The element spacing is one-half wavelength.

Create the ULA, and partition it into two 2-element ULA's.

```
sULA = phased.ULA('NumElements',4,'ElementSpacing',0.5);
sPA = phased.PartitionedArray('Array',sULA,...
    'SubarraySelection',[1 1 0 0;0 0 1 1]);
```

Plot the azimuth response of the array. Assume the operating frequency is 1 GHz and the propagation speed is the speed of light.

```
fc = 1e9;
pattern(sPA,fc,[-180:180],0,'Type','powerdb',...
    'CoordinateSystem','polar',...
    'Normalize',true)
```



Normalized Power (dB), Broadside at $0.00^{\circ}$

## Plot Response and Directivity of Partitioned URA over Restricted Range of Angles

Convert a 2-by-6 URA of isotropic antenna elements into a 1-by-3 partitioned array so that each subarray of the partitioned array is a 2-by-2 URA. Assume that the frequency response of the elements lies between 1 and 6 GHz . The elements are spaced one-half wavelength apart corresponding to the highest frequency of the element response. Plot an azimuth cut from -50 to 50 degrees for two different sets of weights. For partitioned arrays, weights are applied to the subarrays instead of the elements.

Set up the partitioned array.

```
fmin = 1e9;
fmax = 6e9;
c = physconst('LightSpeed');
lam = c/fmax;
s_iso = phased.IsotropicAntennaElement(...
```

```
    'FrequencyRange',[fmin,fmax],...
    'BackBaffled',false);
s_ura = phased.URA('Element',s_iso,'Size',[2,6],...
    'ElementSpacing',[lam/2,lam/2]);
subarraymap = [[1,1,1,1,0,0,0,0,0,0,0,0];...
    [0,0,0,0,1,1,1,1,0,0,0,0];...
    [0,0,0,0,0,0,0,0,1,1,1,1]];
s_pa = phased.PartitionedArray('Array',s_ura,...
    'SubarraySelection',subarraymap);
```

Plot the response of the array at 5 GHz over the restricted range of azimuth angles.

```
fc = 5e9;
wts = [[1,1,1]',[.862,1.23,.862]'];
plotResponse(s_pa,fc,c,'RespCut','Az',...
    'AzimuthAngles',[-50:0.1:50],...
    'Unit','db','Format','Polar',...
    'Weights',wts);
```



## Normalized Power (dB), Broadside at $0.00^{\circ}$

The plot of the response shows the broadening of the main lobe and the reduction of the strength of the sidelobes caused by the weight tapering.

Next, plot an azimuth cut of the directivity of the array at 5 GHz over the restricted range of azimuth angles for the two different sets of weights.

```
fc = 5e9;
wts = [[1,1,1]',[.862,1.23,.862]'];
plotResponse(s_pa,fc,c,'RespCut','Az',...
```

'AzimuthAngles', [-50:0.1:50],...
'Unit','dbi',...
'Weights',wts);


## See Also

uv2azel | azel2uv

## step

## System object: phased. PartitionedArray

Package: phased
Output responses of subarrays

## Syntax

RESP $=\operatorname{step}(H, F R E Q, A N G, V)$
RESP $=\operatorname{step}(\mathrm{H}, \mathrm{FREQ}, \mathrm{ANG}, \mathrm{V}, \mathrm{STEERANGLE})$
RESP $=\operatorname{step}(H, F R E Q, A N G, V, W S)$

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step (obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.

RESP $=$ step ( $H$, FREQ , ANG , V ) returns the responses RESP of the subarrays in the array, at operating frequencies specified in FREQ and directions specified in ANG. The phase center of each subarray is at its geometric center. V is the propagation speed. The elements within each subarray are connected to the subarray phase center using an equal-path feed.

RESP $=$ step ( H, FREQ, ANG, V, STEERANGLE) uses STEERANGLE as the steering direction of the subarray. This syntax is available when you set the SubarraySteering property to either 'Phase' or 'Time'.

RESP $=$ step ( $H$, FREQ, ANG , V, WS ) uses WS as the subarray element weights. This syntax is available when you set the SubarraySteering property to 'Custom'.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## H

Partitioned array object.

## FREQ

Operating frequencies of array in hertz. FREQ is a row vector of length $L$. Typical values are within the range specified by a property of H . Array. Element. That property is named FrequencyRange
or FrequencyVector, depending on the type of element in the array. The element has zero response at frequencies outside that range.

## ANG

Directions in degrees. ANG can be either a 2-by-M matrix or a row vector of length M.
If ANG is a 2-by-M matrix, each column of the matrix specifies the direction in the form [azimuth; elevation]. The azimuth angle must be between -180 and 180 degrees, inclusive. The elevation angle must be between -90 and 90 degrees, inclusive.

If ANG is a row vector of length M , each element specifies a direction's azimuth angle. In this case, the corresponding elevation angle is assumed to be 0 .

## V

Propagation speed in meters per second. This value must be a scalar.

## STEERANGLE

Subarray steering direction. STEERANGLE can be either a 2 -element column vector or a scalar.
If STEERANGLE is a 2-element column vector, it has the form [azimuth; elevation]. The azimuth angle must be between - 180 and 180 degrees, inclusive. The elevation angle must be between -90 and 90 degrees, inclusive.

If STEERANGLE is a scalar, it specifies the direction's azimuth angle. In this case, the elevation angle is assumed to be 0 .

WS
Subarray element weights
Subarray element weights, specified as a complex-valued $N_{S E}$-by- $N$ matrix or 1-by- $N$ cell array where $N$ is the number of subarrays.

Subarrays do not have to have the same dimensions and sizes. In this case, you specify subarray weights as

- an $N_{S E}$-by- $N$ matrix, where $N_{S E}$ is the number of elements in the largest subarray. The first $Q$ entries in each column are the element weights for the subarray where $Q$ is the number of elements in the subarray.
- a 1-by- $N$ cell array. Each cell contains a column vector of weights for the corresponding subarray. The column vectors have lengths equal to the number of elements in the corresponding subarray.


## Dependencies

To enable this argument, set the SubarraySteering to 'Custom '.

## Output Arguments

## RESP

Voltage responses of the subarrays of a phased array. The output depends on whether the array supports polarization or not.

- If the array is not capable of supporting polarization, the voltage response, RESP, has the dimensions $N$-by- $M$-by- $L$. The size $N$ represents the number of subarrays in the phased array, $M$ represents the number of angles specified in ANG, and $L$ represents the number of frequencies specified in FREQ. For a particular subarray, each column of RESP contains the responses of the subarray for the corresponding direction specified in ANG. Each of the $L$ pages of RESP contains the responses of the subarrays for the corresponding frequency specified in FREQ.
- If the array is capable of supporting polarization, the voltage response, RESP, is a MATLAB st ruct containing two fields, RESP. H and RESP.V. The field RESP. H represents the array's horizontal polarization response while RESP. V represents the array's vertical polarization response. Each field has the dimensions $N$-by- $M$-by- $L$. The size $N$ represents the number of subarrays in the phased array, $M$ represents the number of angles specified in ANG, and $L$ represents the number of frequencies specified in FREQ. For a particular subarray, each column of RESP contains the responses of the subarray for the corresponding direction specified in ANG. Each of the $L$ pages of RESP contains the responses of the subarrays for the corresponding frequency specified in FREQ.


## Examples

## Response of Subarrays in Partitioned ULA

Calculate the response at boresight of a 4-element ULA partitioned into two 2-element ULAs.
Set up the partitioned array.

```
hula = phased.ULA('NumElements',4,'ElementSpacing',0.5);
partitionedarray = phased.PartitionedArray('Array',hula,...
    'SubarraySelection',[1 1 0 0;0 0 1 1]);
```

Calculate the response of the subarrays at boresight. Assume the operating frequency is 1 GHz and the propagation speed is the speed of light.

```
resp = partitionedarray(1.0e9,[0;0],physconst('Lightspeed'))
resp = 2×1
    2
    2
```


## Subarray Element Weights for Partitioned Array

Create a partitioned URA array with three subarrays of different sizes. The subarrays have 8, 16, and 32 elements. Use different sets of subarray element weights for each subarray.

Create a 4-by-56 element URA.

```
antenna = phased.IsotropicAntennaElement;
fc = 300e6;
c = physconst('LightSpeed');
lambda = c/fc;
n1 = 2^3;
```

```
n2 = 2^4;
n3 = 2^5;
nrows = 4;
ncols = n1 + n2 + n3;
array = phased.URA('Element',antenna,'Size',[nrows,ncols]);
```

Select the three subarrays by setting the selection matrix.

```
sel1 = zeros(nrows,ncols);
sel2 = sel1;
sel3 = sel1;
sel = zeros(3,nrows*ncols);
for r = 1:nrows
    sel1(r,1:n1) = 1;
    sel2(r,(n1+1):(n1+n2)) = 1;
    sel3(r,((n1+n2)+1):ncols) = 1;
end
sel(1,:) = sel1(:);
sel(2,:) = sel2(:);
sel(3,:) = sel3(:);
```

Create the partitioned array.

```
partarray = phased.PartitionedArray('Array',array, ...
    'SubarraySelection',sel,'SubarraySteering','Custom');
viewArray(partarray,'ShowSubarray','All');
```


## Array Geometry



Set weights for each subarray and get the response of each subarray. Put the weights in a cell array.

```
wts1 = ones(nrows*n1,1);
wts2 = 1.5*ones(nrows*n2,1);
wts3 = 3*ones(nrows*n3,1);
resp = partarray(fc,[30;0],c,{wts1,wts2,wts3})
resp = 3x1 complex
    0.0246 + 0.0000i
    0.0738 - 0.0000i
    0.2951 - 0.0000i
```


## See Also

uv2azel | phitheta2azel

## viewArray

System object: phased. PartitionedArray
Package: phased
View array geometry

## Syntax

```
viewArray(H)
viewArray(H,Name,Value)
hPlot = viewArray(
```

$\qquad$

``` )
```


## Description

viewArray (H) plots the geometry of the array specified in H .
viewArray ( $\mathrm{H}, \mathrm{Name}$, Value) plots the geometry of the array, with additional options specified by one or more Name, Value pair arguments.
hPlot = viewArray( $\qquad$ ) returns the handles of the array elements in the figure window. All input arguments described for the previous syntaxes also apply here.

## Input Arguments

## H

Array object.

## Name-Value Pair Arguments

Specify optional pairs of arguments as Namel=Value1, . . . ,NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Parent

Handle to the axes along which the array geometry is displayed.

## ShowNormals

Set this value to true to show the normal directions of all elements of the array. Set this value to false to plot the elements without showing normal directions.

Default: false

## ShowLocalCoordinates

Logical flag specifying whether to show the local coordinate axes.

Default: true

## ShowAnnotation

Logical flag specifying whether to show the annotations in the UI panel of the figure. Annotation shows aperture size and element spacing based on array axis of array.

Default: true

## Orientation

Orientation of the array, specified as a 3-by-1 column vector containing the rotation angles with respect to the $x-, y$-, and $z$-axes of the local coordinate system, respectively. The default value is [0;0;0].

Default: [0;0;0]

## ShowTaper

Set this value to true to specify whether to change the element color brightness in proportion to the element taper magnitude. When this value is set to false, all elements are drawn with the same color. The default value is false.

Default: false

## ShowIndex

Vector specifying the element indices to show in the figure. Each number in the vector must be an integer between 1 and the number of elements. You can also specify the value 'All' to show indices of all elements of the array or 'None' to suppress indices.

Default: 'None'

## ShowSubarray

Vector specifying the indices of subarrays to highlight in the figure. Each number in the vector must be an integer between 1 and the number of subarrays. You can also specify the value 'All' to highlight all subarrays of the array or ' None' to suppress the subarray highlighting. The highlighting uses different colors for different subarrays, and white for elements that occur in multiple subarrays.

Default: 'All'

## Title

Character vector specifying the title of the plot.
Default: 'Array Geometry'

## Output Arguments

## hPlot

Handles of array elements in figure window.

## Examples

## Highlight Overlapped Subarrays

Display the geometry of a uniform linear array having overlapped subarrays.
Create a 16 -element ULA that has five 4 -element subarrays. Some elements occur in more than one subarray.

```
h = phased.ULA(16);
ha = phased.PartitionedArray('Array',h,...
    'SubarraySelection',...
    [1 1 1 1 0 0 0 0 0 0 0 0 0 0 0 0;...
    0 0 1 1 1 1 0 0 0 0 0 0 0 0 0 0;...
    0 0 0 0 1 1 1 1 0 0 0 0 0 0 0 0;...
    0 0 0 0 0 0 0 0 1 1 1 1 0 0 0 0;...
    0 0 0 0 0 0 0 0 0 0 0 0 1 1 1 1]);
```

Display the geometry of the array, highlighting all subarrays.
viewArray(ha);

## Array Geometry

O Overlap


Each color other than white represents a different subarray. White represents elements that occur in multiple subarrays.

Examine the overlapped subarrays by creating separate figures that highlight the first, second, and third subarrays. In each figure, dark blue represents the highlighted elements.

```
for idx = 1:3
    figure;
    viewArray(ha,'ShowSubarray',idx,...
        'Title',['Subarray #' num2str(idx)]);
end
```

Subarray \#1


[^5]Subarray \#2


Array Span:
X axis $=0.0 \mathrm{~m}$
Y axis $=7.5 \mathrm{~m}$
$Z$ axis $=0.0 \mathrm{~m}$


## See Also

phased.ArrayResponse

## Topics

"Phased Array Gallery"

# phased.PhaseCodedWaveform 

Package: phased
Phase-coded pulse waveform

## Description

The PhaseCodedWaveform object creates a phase-coded pulse waveform.
To obtain waveform samples:
1 Define and set up your phase-coded pulse waveform. See "Construction" on page 1-1204.
2 Call step to generate the phase-coded pulse waveform samples according to the properties of phased. PhaseCodedWaveform. The behavior of step is specific to each object in the toolbox.

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step $(o b j, x)$ and $y=o b j(x)$ perform equivalent operations. When the only argument to the step method is the System object itself, replace $y=$ step(obj) by $y=o b j()$.

## Construction

H = phased.PhaseCodedWaveform creates a phase-coded pulse waveform System object, H. The object generates samples of a phase-coded pulse.

H = phased.PhaseCodedWaveform(Name, Value) creates a phase-coded pulse waveform object, H, with additional options specified by one or more Name, Value pair arguments. Name is a property name on page 1-1204, and Value is the corresponding value. Name must appear inside single quotes (' '). You can specify several name-value pair arguments in any order as Name1, Value1, ...,NameN, ValueN.

## Properties

## SampleRate

Sample rate
Specify the sample rate in hertz as a positive scalar. The default value of this property corresponds to 1 MHz . The value of this property must satisfy these constraints:

- (SampleRate./PRF) is a scalar or vector that contains only integers - the number of samples in a pulse must be an integer.
- (SampleRate*ChipWidth) is an integer value - the number of samples in a chip must be an integer.


## Default: 1e6

## Code

Phase code type
Specify the phase code type used in phase modulation. Valid values are:

- 'Barker'
- 'Frank'
- 'P1'
- 'P2'
- 'P3'
- 'P4'
- 'Px'
- 'Zadoff-Chu'

Default: 'Frank'

## ChipWidth

Time duration of each chip
Specify the time duration of each chip in a phase-coded waveform as a positive scalar. Units are seconds. For this waveform, the pulse duration is equal to the product of the chip width and number of chips.

The value of this property must satisfy these constraints:

- ChipWidth is less than or equal to (1./(NumChips*PRF)) - the total time duration of all chips cannot exceed the duration of the pulse.
- (SampleRate*ChipWidth) is an integer value - the number of samples in a chip must be an integer.


## Default: 1e-5

## NumChips

Number of chips
Specify the number of chips per pulse in a phase-coded waveform as a positive integer. The value of this property must be less than or equal to (1./(ChipWidth*PRF)) - the total time duration of all chips cannot exceed the pulse repetition interval.

The table shows additional constraints on the number of chips for different code types.

| If the Code property is ... | Then the NumChips property must be... |
| :--- | :--- |
| ' Frank', 'P1', or 'Px' | A perfect square |
| 'P2' | An even number that is a perfect square |
| 'Barker' | $2,3,4,5,7,11$, or 13 |

## Default: 4

## SequenceIndex

Zadoff-Chu sequence index
Specify the sequence index used in Zadoff-Chu code as a positive integer. This property applies only when you set the Code property to 'Zadoff-Chu'. The value of SequenceIndex must be relatively prime to the value of the NumChips property.

## Default: 1

## PRF

Pulse repetition frequency
Pulse repetition frequency, $P R F$, specified as a scalar or a row vector. Units are in Hz . The pulse repetition interval, $P R I$, is the inverse of the pulse repetition frequency, $P R F$. ThePRF must satisfy these restrictions:

- The product of PRF and PulseWidth must be less than or equal to one. This condition expresses the requirement that the pulse width is less than one pulse repetition interval. For the phasecoded waveform, the pulse width is the product of the chip width and number of chips.
- The ratio of sample rate to any element of PRF must be an integer. This condition expresses the requirement that the number of samples in one pulse repetition interval is an integer.

You can select the value of $P R F$ using property settings alone or using property settings in conjunction with the prfidx input argument of the step method.

- When PRFSelectionInputPort is false, you set the PRF using properties only. You can
- implement a constant PRF by specifying PRF as a positive real-valued scalar.
- implement a staggered PRF by specifying PRF as a row vector with positive real-valued entries. Then, each call to the step method uses successive elements of this vector for the PRF. If the last element of the vector is reached, the process continues cyclically with the first element of the vector.
- When PRFSelectionInputPort is true, you can implement a selectable PRF by specifying PRF as a row vector with positive real-valued entries. But this time, when you execute the step method, select a PRF by passing an argument specifying an index into the $P R F$ vector.

In all cases, the number of output samples is fixed when you set the OutputFormat property to 'Samples'. When you use a varying PRF and set the OutputFormat property to 'Pulses', the number of samples can vary.

Default: 10e3

## PRFSelectionInputPort

Enable PRF selection input
Enable the PRF selection input, specified as true or false. When you set this property to false, the step method uses the values set in the PRF property. When you set this property to true, you pass an index argument into the step method to select a value from the PRF vector.

Default: false

## FrequencyOffsetSource

Source of frequency offset
Source of frequency offset for the waveform, specified as 'Property' or 'Input port'.

- When you set this property to 'Property', the offset is determined by the value of the FrequencyOffset property.
- When you set this property to 'Input port', the FrequencyOffset is determined by the freqoffset input argument.

Default: 'Property'

## FrequencyOffset

Frequency offset
Frequency offset in Hz , specified as a scalar.

## Dependencies

This property applies when you set the FrequencyOffsetSource property to 'Input port '.
Default: 0 Hz

## OutputFormat

Output signal format
Specify the format of the output signal as 'Pulses' or 'Samples '. When you set the OutputFormat property to 'Pulses', the output of the step method takes the form of multiple pulses specified by the value of the NumPulses property. The number of samples per pulse can vary if you change the pulse repetition frequency during the simulation.

When you set the OutputFormat property to 'Samples', the output of the step method is in the form of multiple samples. In this case, the number of output signal samples is the value of the NumSamples property and is fixed.

Default: 'Pulses'

## NumSamples

Number of samples in output
Specify the number of samples in the output of the step method as a positive integer. This property applies only when you set the OutputFormat property to 'Samples'.

Default: 100

## NumPulses

Number of pulses in output
Specify the number of pulses in the output of the step method as a positive integer. This property applies only when you set the OutputFormat property to 'Pulses '.

## Default: 1

## PRFOutputPort

Set this property to true to output the PRF for the current pulse using a step method argument.

## Dependencies

This property can be used only when the OutputFormat property is set to 'Pulses'.
Default: false

## CoefficientsOutputPort

Enable matched filter coefficients output port
Enable the matched filter coefficients output port, specified as false or true. When you set this property to false, the object does not provide the matched filter coefficients used during the simulation as an output. When you set this property to true, the object provides the matched filter coefficients used during the simulation as an output.

Default: false

## Methods

| bandwidth | Bandwidth of phase-coded waveform |
| :--- | :--- |
| getMatchedFilter | Matched filter coefficients for waveform |
| plot | Plot phase-coded pulse waveform |
| reset | Reset states of phase-coded waveform object |
| step | Samples of phase-coded waveform |

## Common to All System Objects

release Allow System object property value changes

## Examples

## Plot Phase-Coded Waveform and Spectrum

Create and plot a two-pulse phase-coded waveform that uses the Zadoff-Chu code.

```
sPCW = phased.PhaseCodedWaveform('Code','Zadoff-Chu',...
    'ChipWidth',5e-6,'NumChips',16,...
    'OutputFormat','Pulses','NumPulses',2);
fs = sPCW.SampleRate;
```

Generate signal samples and plot the magnitude and phase of the waveforms.

```
wav = step(sPCW);
nsamp = size(wav,1);
t = [0:(nsamp-1)]/fs;
plot(t*le6,abs(wav),'.-')
title('Magnitude')
xlabel('Time (\mu sec)')
ylabel('Amplitude')
```



```
plot(t*le6,180/pi*angle(wav))
title('Phase Angle')
xlabel('Time (\mu sec)')
ylabel('Phase Angle (deg)')
```



Plot the spectrum.

```
nsamp = size(wav,1);
nfft = 2^nextpow2(nsamp);
Z = fft(wav,nfft);
fr = [0:(nfft-1)]/nfft*fs;
fr = fr - fs/2;
plot(fr/1000,abs(fftshift(Z)))
xlabel('Frequency (kHz)')
ylabel('Amplitude')
grid
```



## Apply Frequency Offset to Phase-Coded Waveform

Apply a frequency offset to a phase-coded waveform that uses the Zadoff-Chu code. Plot the frequency spectrum of the waveform with and without a frequency offset applied.

Create a phase-coded waveform object which is configured to set the frequency offset from an input when the object is executed.

```
fs = 1e6;
sPCW = phased.PhaseCodedWaveform('SampleRate',fs,'Code','Zadoff-Chu', ...
    'ChipWidth',8e-6,'NumChips',4,'OutputFormat','Pulses', ...
    'NumPulses',1,'FrequencyOffsetSource','Input port');
```

Execute the object two times. First set the frequency offset set to 0 Hz , and then to 2 e 4 Hz .

```
pcwav = sPCW(0);
pcwav_foffset = sPCW(2e4);
```

Plot the frequency spectrum of the complex signals. The frequency offset signal is shifted to the right.

```
[Pxx,f] = pwelch(pcwav,[],[],[],fs,'centered');
[Pxx_offset,foffset] = pwelch(pcwav_foffset,[],[],[],fs,'centered');
plot(f/1000,Pxx,foffset/1000,Pxx_of\overline{fset)}
ylabel('PSD');
xlabel('Frequency (kHz)');
```

legend(\{'No offset','Offset applied'\},'Location','northwest'); grid on;


## Algorithms

A 2-chip Barker code can use [1-1] or [1 1] as the sequence of amplitudes. This software implements [1-1].

A 4-chip Barker code can use [11-1 1] or [1 $111-1$ ] as the sequence of amplitudes. This software implements [11-11].

A Zadoff-Chu code can use a clockwise or counterclockwise sequence of phases. This software implements the latter, such as $\Pi \cdot f(k) \cdot$ SequenceIndex/NumChips instead of $-\Pi \cdot f(k) \cdot$ SequenceIndex/NumChips. In these expressions, $k$ is the index of the chip and $f(k)$ is a function of $k$.

For further details, see [1].

## Version History

Introduced in R2011b

## References

[1] Levanon, N. and E. Mozeson. Radar Signals. Hoboken, NJ: John Wiley \& Sons, 2004.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder ${ }^{\text {rm }}$.
Usage notes and limitations:

- plot method is not supported.
- See "System Objects in MATLAB Code Generation" (MATLAB Coder).


## See Also

phased.LinearFMWaveform|phased.SteppedFMWaveform|phased.RectangularWaveform

## Topics

Waveform Analysis Using the Ambiguity Function
"Phase-Coded Waveforms"

## bandwidth

System object: phased. PhaseCodedWaveform
Package: phased
Bandwidth of phase-coded waveform

## Syntax

bw = bandwidth(waveform)

## Description

bw = bandwidth(waveform) returns the bandwidth (in hertz) of the pulses for the phase-coded pulse waveform, waveform. The bandwidth value is the reciprocal of the chip width.

## Input Arguments

waveform
Phase-coded waveform object.

## Output Arguments

bw
Bandwidth of the pulses, in hertz.

## Examples

## Phase-Coded Waveform Bandwidth

Determine the bandwidth of a Frank phased-coded waveform.
waveform = phased. PhaseCodedWaveform;
bw = bandwidth(waveform)
bw $=1.0000 \mathrm{e}+05$

## getMatchedFilter

System object: phased. PhaseCodedWaveform
Package: phased
Matched filter coefficients for waveform

## Syntax

Coeff = getMatchedFilter(H)
Coeff = getMatchedFilter(H,'FrequnecyOffset',FOFFSET)

## Description

Coeff = getMatchedFilter $(H)$ returns the matched filter coefficients for the phase-coded waveform object, H . Coeff is a column vector.

Coeff = getMatchedFilter(H,'FrequnecyOffset', FOFFSET) adds a frequency offset when matched filter coefficients are generated. FOFFSET must be a positive scalar. This option is available when you set the FrequencyOffsetSource property to 'Input port ' for the input object, H.

## Input Arguments

H

Phase-coded waveform object.

## Output Arguments

Coeff
Column vector containing coefficients of the matched filter for H .

## Examples

## Matched-Filter Coefficients for Pulse-Coded Waveform

Obtain the matched filter coefficients for a phase-coded pulse waveform that uses the Zadoff-Chu code.

```
waveform = phased.PhaseCodedWaveform('Code','Zadoff-Chu','ChipWidth',1e-6, ...
    'NumChips',16,'OutputFormat','Pulses','NumPulses',2);
coeff = getMatchedFilter(waveform);
stem(real(coeff))
title('Matched Filter Coefficients, Real Part')
axis([0 17 -1.1 1.1])
```



## plot

System object: phased.PhaseCodedWaveform
Package: phased
Plot phase-coded pulse waveform

## Syntax

```
plot(Hwav)
plot(Hwav,Name,Value)
plot(Hwav,Name,Value,LineSpec)
h = plot(
```

$\qquad$

``` )
```


## Description

plot (Hwav) plots the real part of the waveform specified by Hwav.
plot (Hwav, Name, Value) plots the waveform with additional options specified by one or more Name, Value pair arguments.
plot (Hwav, Name, Value, LineSpec) specifies the same line color, line style, or marker options as are available in the MATLAB plot function.
h = plot( $\qquad$ ) returns the line handle in the figure.

## Input Arguments

## Hwav

Waveform object. This variable must be a scalar that represents a single waveform object.

## LineSpec

Character vector to specifies the same line color, style, or marker options as are available in the MATLAB plot function. If you specify a PlotType value of ' complex', then LineSpec applies to both the real and imaginary subplots.

Default: 'b'

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## PlotType

Specifies whether the function plots the real part, imaginary part, or both parts of the waveform. Valid values are 'real','imag', and 'complex'.

Default: 'real'

## PulseIdx

Index of the pulse to plot. This value must be a scalar.
Default: 1
Frequency0ffset
Frequency offset
Frequency offset in Hz , specified as a scalar.

## Dependencies

This property applies when you set the FrequencyOffsetSource property to 'Input port '.
Default: 0 Hz

## Output Arguments

## h

Handle to the line or lines in the figure. For a PlotType value of ' complex' h is a column vector. The first and second elements of this vector are the handles to the lines in the real and imaginary subplots, respectively.

## Examples

## Plot Pulse-Coded Waveform

Create and plot a phase-coded pulse waveform that uses the Zadoff-Chu code.

```
waveform = phased.PhaseCodedWaveform('Code','Zadoff-Chu','ChipWidth',1e-6, ...
    'NumChips',16,'OutputFormat','Pulses','NumPulses',2);
plot(waveform)
```



## reset

System object: phased.PhaseCodedWaveform
Package: phased
Reset states of phase-coded waveform object

## Syntax

reset (H)

## Description

reset (H) resets the states of the PhaseCodedWaveform object, H. Afterward, the next call to step restarts the phase sequence from the beginning. Also, if the PRF property is a vector, the next call to step uses the first PRF value in the vector.

## step

System object: phased. PhaseCodedWaveform
Package: phased
Samples of phase-coded waveform

## Syntax

```
Y = step(sPCW)
Y = step(sPCW,prfidx)
Y = step(sRFM,freqoffset)
[Y,PRF] = step(__)
[Y,COEFF] = step(___)
```


## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, $y=$ step $(o b j, x)$ and $y=o b j(x)$ perform equivalent operations. When the only argument to the step method is the System object itself, replace $y=\operatorname{step}(o b j)$ by $y=o b j()$.
$\mathrm{Y}=$ step( $s P C W$ ) returns samples of the phase-coded pulse in a column vector, Y .
$Y=$ step(sPCW, prfidx), uses the prfidx index to select the PRF from the predefined vector of values specified by in the PRF property. This syntax applies when you set the PRFSelectionInputPort property to true.
$Y=$ step(sRFM,freqoffset), uses the freqoffset to generate the waveform with an offset as specified at step time. Use this syntax for cases where the transmit pulse frequency needs to be dynamically updated. This syntax applies when you set the FrequencyOffsetSource property to 'Input port'.
[Y, PRF] = step ( __ ) also returns the current pulse repetition frequency, PRF. To enable this syntax, set the PRFOutputPort property to true and set the OutputFormat property to 'Pulses'.
[Y,COEFF] = step (__ ) returns the matched filter coefficients, COEFF, for the current pulse. To enable this syntax, set CoefficientsOutputPort to true. COEFF is returned as an $N_{Z}$-by- 1 vector, where $N_{\mathrm{Z}}$ is the maximum of the nonzero pulse width.

You can combine optional input and output arguments when their enabling properties are set. Optional inputs and outputs must be listed in the same order as the order of the enabling properties. For example, [Y, PRF,COEFF] = step(sRFM, prfidx,freqoffset).

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## sPCW

Phase-coded waveform object.

## Output Arguments

Y

Column vector containing the waveform samples.

## Examples

## Create Pulse Coded Waveform

Generate samples of two pulses of a phase-coded pulse waveform that uses the Zadoff-Chu code.

```
sPCW = phased.PhaseCodedWaveform('Code','Zadoff-Chu',...
    'ChipWidth',1e-6,'NumChips',16,...
    'OutputFormat','Pulses','NumPulses',2);
wav = step(sPCW);
fs = sPCW.SampleRate;
nsamps = size(wav,1);
t = [0:(nsamps-1)]/fs;
plot(t*le6,real(wav))
title('Waveform: Real Part')
xlabel('Time (\mu sec)')
ylabel('Amplitude')
grid
```



## Create Phase-Coded Waveform with Variable PRF

Create and plot two-pulse phase-coded waveforms that uses the Zadoff-Chu code. Set the sample rate to 1 MHz , a chip width of 5 microseconds, 16 chips per pulse. Vary the pulse repetition frequency.

```
fs = 1e6;
PRF = [5000,10000];
waveform = phased.PhaseCodedWaveform('SampleRate',fs,...
    'Code','Zadoff-Chu','PRFSelectionInputPort',true,...
    'ChipWidth',5e-6,'NumChips',16,'PRF',PRF,...
    'OutputFormat','Pulses','NumPulses',2);
```

Obtain and plot the phase-coded waveforms. For the first call to the step method, set the PRF to 10 kHz using the PRF index. For the next call, set the PRF to 25 kHz . For the final call, set the PRF to 10 kHz .

```
wav = [];
wav1 = waveform(1);
wav = [wav; wav1];
wav1 = waveform(2);
wav = [wav; wav1];
wav1 = waveform(1);
wav = [wav; wav1];
nsamps = size(wav,1);
t = [0:(nsamps-1)]/fs;
```

plot(t*le6,real(wav))
xlabel('Time (\mu sec)')
ylabel('Amplitude')


## Generate Matched Filter Coefficients of Phase-Coded Waveform

Generate output samples and matched filter coefficients of a Barker coded waveform.

```
waveform = phased.PhaseCodedWaveform('Code','Barker','NumChips',5, ...
    'CoefficientsOutputPort',true,'PRF',[1e4 2e4],'ChipWidth',5e-6, ...
    'OutputFormat','Samples',''NumSamples',150);
[wav,coeff] = waveform();
```

Create a matched filter that applies the coefficients as an input argument. Use the coefficients when applying the matched filter to the waveform. Plot the waveform and matched filter outputs.

```
mf = phased.MatchedFilter('CoefficientsSource','Input port');
mfOut = mf(wav,coeff);
subplot(211),plot(real(wav));
xlabel('Samples'),ylabel('Amplitude'),title('Waveform Output');
subplot(212),plot(abs(mf0ut));
xlabel('Samples'),ylabel('Amplitude'),title('Matched Filter Output');
```



# phased.PhaseShiftBeamformer 

Package: phased
Narrowband phase shift beamformer

## Description

The phased.PhaseShiftBeamformer object implements a narrowband phase-shift beamformer. A phase-shift beamformer approximates a time-delay beamformer for narrowband signals by phaseshifting the arriving signal. A phase shift beamformer belongs to the family of conventional beamformers.

To beamform signals arriving at an array:
1 Create the phased. PhaseShiftBeamformer object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

beamformer = phased.PhaseShiftBeamformer
beamformer $=$ phased.PhaseShiftBeamformer(Name,Value)

## Description

beamformer = phased.PhaseShiftBeamformer creates a phase-shift beamformer System object, beamformer, with default property values.
beamformer $=$ phased. PhaseShiftBeamformer(Name,Value) creates a phase-shift beamformer with each property Name set to a specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN). Enclose each property name in single quotes.
Example: beamformer =
phased. PhaseShiftBeamformer('SensorArray', phased.URA, 'OperatingFrequency', 300
e6) sets the sensor array to a uniform rectangular array (URA) with default URA property values.
The beamformer has an operating frequency of 300 MHz .

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.

For more information on changing property values, see System Design in MATLAB Using System Objects.

## SensorArray - Sensor array

phased. ULA array with default property values (default) | Phased Array System Toolbox array
Sensor array, specified as an array System object belonging to Phased Array System Toolbox. The sensor array can contain subarrays.
Example: phased.URA
PropagationSpeed - Signal propagation speed
physconst('LightSpeed') (default)| real-valued positive scalar
Signal propagation speed, specified as a real-valued positive scalar. Units are in meters per second. The default propagation speed is the value returned by physconst('LightSpeed').
Example: 3e8
Data Types: single | double

## OperatingFrequency - Operating frequency

300e6 (default) | positive scalar
Operating frequency, specified as a positive scalar. Units are in Hz.
Example: 1e9
Data Types: single | double

## DirectionSource - Source of beamforming direction

'Property' (default)|'Input port'
Source of beamforming direction, specified as 'Property' or 'Input port'. Specify whether the beamforming direction comes from the Direction property of this object or from the input argument, ANG. Values of this property are:

| 'Property' | Specify the beamforming direction using the Direction <br> property. |
| :--- | :--- |
| 'Input port' | Specify the beamforming direction using the input argument, <br> ANG. |

## Data Types: char

## Direction - Beamforming directions

[0;0] (default) | real-valued 2-by-1 vector | real-valued 2-by-L matrix
Beamforming directions, specified as a real-valued 2-by-1 vector or a real-valued 2-by-L matrix. For a matrix, each column specifies a different beamforming direction. Each column has the form [AzimuthAngle; ElevationAngle]. Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$ and elevation angles must lie between $-90^{\circ}$ and $90^{\circ}$. All angles are defined with respect to the local coordinate system of the array. Units are in degrees.

Example: [40;30]

## Dependencies

To enable this property, set the DirectionSource property to 'Property'.

## Data Types: single|double

## NumPhaseShifterBits - Number of phase shifter quantization bits

0 (default) | nonnegative integer
The number of bits used to quantize the phase shift component of beamformer or steering vector weights, specified as a nonnegative integer. A value of zero indicates that no quantization is performed.
Example: 5
Data Types: single | double
WeightsNormalization - Approach for normalizing beamformer weights
'Distortionless' (default)|'Preserve power'
If you set this property value to 'Distortionless', the gain in the beamforming direction is 0 dB . If you set this property value to 'Preserve power', the norm of the weights is unity.
Example: 'Preserve power'
Data Types: char

## WeightsOutputPort - Enable beamforming weights output

```
false (default)| true
```

Enable the output of beamforming weights, specified as false or true. To obtain the beamforming weights, set this property to true and use the corresponding output argument, W. If you do not want to obtain the weights, set this property to false.

## Data Types: logical

## Usage

## Syntax

$Y$ = beamformer(X)
Y = beamformer(X,ANG)
$[\mathrm{Y}, \mathrm{W}]=$ beamformer( $\qquad$ )

## Description

$Y=$ beamformer ( X ) performs phase-shift beamforming on the input signal, X , and returns the beamformed output in Y. To use this syntax, set DirectionSource to 'Property ' and set the beamforming direction using the Direction property.
$\mathrm{Y}=$ beamformer(X,ANG) uses the ANG input argument to set the beamforming direction. To use this syntax, set the DirectionSource property to 'Input port'.
$[\mathrm{Y}, \mathrm{W}]=$ beamformer (__ ) returns the beamforming weights, W . To use this syntax, set the WeightsOutputPort property to true.

## Input Arguments

X - Input signal
complex-valued $M$-by- $N$ matrix

Input signal, specified as a complex-valued $M$-by- $N$ matrix. If the sensor array contains subarrays, $N$ is the number of subarrays; otherwise, $N$ is the number of array elements.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

Data Types: single|double
Complex Number Support: Yes

## ANG - Beamforming directions

[0;0] (default) | real-valued 2-by-1 column vector | real-valued 2-by-L matrix
Beamforming directions, specified as a real-valued 2-by-1 column vector, or 2-by- $L$ matrix. $L$ is the number of beamforming directions. Each column has the form [AzimuthAngle; ElevationAngle]. Units are in degrees. Each azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$, and each elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

Example: [40;10]

## Dependencies

To enable this argument, set the DirectionSource property to 'Input port '.
Data Types: single|double

## Output Arguments

Y - Beamformed output
complex-valued $M$-by- $L$ matrix
Beamformed output, returned as a complex-valued $M$-by- $L$ matrix, where $M$ is the number of rows of $X$ and $L$ is the number of beamforming directions.

Data Types: single | double
Complex Number Support: Yes
W - Beamforming weights
complex-valued $N$-by- $L$ matrix.
Beamforming weights, returned as a complex-valued $N$-by- $L$ matrix. If the sensor array contains subarrays, $N$ is the number of subarrays; otherwise, $N$ is the number of elements. $L$ is the number of beamforming directions.

## Dependencies

To enable this output, set the DirectionSource property to true.
Data Types: single|double
Complex Number Support: Yes

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```


## Common to All System Objects

step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object

## Examples

## Phase-Shift ULA Beamformer

Apply phase-shift beamforming to a sinewave signal received by a 7 -element ULA. The beamforming direction is $45^{\circ}$ azimuth and $0^{\circ}$ elevation. Assume the array operates at 300 MHz . Specify the beamforming direction using the Direction property.

Simulate the signal.

```
t = (0:1000)';
fsignal = 0.01;
x = sin(2*pi*fsignal*t);
c = physconst('Lightspeed');
fc = 300e6;
incidentAngle = [45;0];
array = phased.ULA('NumElements',7);
x = collectPlaneWave(array,x,incidentAngle,fc,c);
noise = 0.1*(randn(size(x)) + 1j*randn(size(x)));
rx = x + noise;
```

Set up a phase-shift beamformer and then beamform the input data.

```
beamformer = phased.PhaseShiftBeamformer('SensorArray',array,...
    'OperatingFrequency',fc,'PropagationSpeed',c,...
    'Direction',incidentAngle, 'WeightsOutputPort',true);
[y,w] = beamformer(rx);
```

Plot the original signal at the middle element and the beamformed signal.

```
plot(t,real(rx(:,4)),'r:',t,real(y))
xlabel('Time (sec)')
ylabel('Amplitude')
legend('Input','Beamformed')
```



Plot the array response pattern after applying the weights.
pattern(array,fc,[-180:180],0,'PropagationSpeed', c, 'Type',...
'powerdb','CoordinateSystem', 'polar','Weights', w)


Normalized Power (dB), Broadside at $0.00^{\circ}$

## Phase-Shift Beamformer Using ULA

Apply phase-shift beamforming to the signal received by a 5 -element ULA. The beamforming direction is $45^{\circ}$ azimuth and $0^{\circ}$ elevation. Assume the array operates at 300 MHz . Specify the beamforming direction using an input port.

Simulate a sinewave signal arriving at the array.

```
t = (0:1000)';
fsignal = 0.01;
x = sin(2*pi*fsignal*t);
c = physconst('LightSpeed');
fc = 300e6;
incidentAngle = [45;0];
array = phased.ULA('NumElements',5);
x = collectPlaneWave(array,x,incidentAngle,fc,c);
noise = 0.1*(randn(size(x)) + lj*randn(size(x)));
rx = x + noise;
```

Construct the phase-shift beamformer and then beamform the input data.
beamformer = phased.PhaseShiftBeamformer('SensorArray',array,...
'OperatingFrequency',fc,'PropagationSpeed', c, ...
'DirectionSource','Input port','WeightsOutputPort',true);

Obtain the beamformed signal and the beamformer weights.
[ $y, w]=$ beamformer(rx,incidentAngle);
Plot the original signal at the middle element and the beamformed signal.
plot(t,real(rx(:, 3$)), ' r: ', t, r e a l(y))$
xlabel('Time')
ylabel('Amplitude')
legend('Original','Beamformed')


Plot the array response pattern after applying the weights.
pattern(array,fc, [-180:180], 0, 'PropagationSpeed', c, 'CoordinateSystem', 'rectangular', 'Weights',w)


## Algorithms

## Phase Shift Beamforming

The phase shift beamformer uses the conventional delay-and-sum beamforming algorithm. The beamformer assumes the signal is narrowband, so a phase shift can approximate the required delay. The beamformer preserves the incoming signal power.

For more details, see [1].

## Data Precision

This System object supports single and double precision for input data, properties, and arguments. If the input data X is single precision, the output data is single precision. If the input data X is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

## Version History

Introduced in R2011a

## References

[1] Van Trees, H.L. Optimum Array Processing. New York, NY: Wiley-Interscience, 2002.
[2] Johnson, Don H. and D. Dudgeon. Array Signal Processing. Englewood Cliffs, NJ: Prentice Hall, 1993.
[3] Van Veen, B.D. and K. M. Buckley. "Beamforming: A versatile approach to spatial filtering". IEEE ASSP Magazine, Vol. 5 No. 2 pp. 4-24.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:

- See "System Objects in MATLAB Code Generation" (MATLAB Coder).
- This System object supports single and double precision for input data, properties, and arguments. If the input data $X$ is single precision, the output data is single precision. If the input data $X$ is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.


## See Also

phased.FrostBeamformer|phased.MVDRBeamformer | phased.LCMVBeamformer | phased.SubbandMVDRBeamformer

## step

## System object: phased. PhaseShiftBeamformer

Package: phased
Perform phase shift beamforming

## Syntax

```
Y = step(H,X)
Y = step(H,X,ANG)
[Y,W] = step(___)
```


## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step (obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.
$Y=$ step ( $\mathrm{H}, \mathrm{X}$ ) performs phase shift beamforming on the input, X , and returns the beamformed output in Y .
$\mathrm{Y}=\operatorname{step}(\mathrm{H}, \mathrm{X}, \mathrm{ANG})$ uses ANG as the beamforming direction. This syntax is available when you set the DirectionSource property to 'Input port'.
$[\mathrm{Y}, \mathrm{W}]=\operatorname{step}(\ldots \quad$ ) returns the beamforming weights, W . This syntax is available when you set the WeightsOutputPort property to true.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## H

Beamformer object.

## X

Input signal, specified as an $M$-by- $N$ matrix. If the sensor array contains subarrays, $N$ is the number of subarrays; otherwise, $N$ is the number of elements.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

## ANG

Beamforming directions, specified as a two-row matrix. Each column has the form [AzimuthAngle; ElevationAngle], in degrees. Each azimuth angle must be between -180 and 180 degrees, and each elevation angle must be between -90 and 90 degrees.

## Output Arguments

## Y

Beamformed output. $Y$ is an $M$-by- $L$ matrix, where $M$ is the number of rows of $X$ and $L$ is the number of beamforming directions.

## W

Beamforming weights. W is an $N$-by- $L$ matrix, where $L$ is the number of beamforming directions. If the sensor array contains subarrays, $N$ is the number of subarrays; otherwise, $N$ is the number of elements.

## Examples

## Phase-Shift Beamformer Using ULA

Apply phase-shift beamforming to the signal received by a 5 -element ULA. The beamforming direction is $45^{\circ}$ azimuth and $0^{\circ}$ elevation. Assume the array operates at 300 MHz . Specify the beamforming direction using an input port.

Simulate a sinewave signal arriving at the array.

```
t = (0:1000)';
fsignal = 0.01;
x = sin(2*pi*fsignal*t);
c = physconst('LightSpeed');
fc = 300e6;
incidentAngle = [45;0];
array = phased.ULA('NumElements',5);
x = collectPlaneWave(array,x,incidentAngle,fc,c);
noise = 0.1*(randn(size(x)) + lj*randn(size(x)));
rx = x + noise;
```

Construct the phase-shift beamformer and then beamform the input data.

```
beamformer = phased.PhaseShiftBeamformer('SensorArray',array,...
    'OperatingFrequency',fc,'PropagationSpeed',c,...
    'DirectionSource','Input port','WeightsOutputPort',true);
```

Obtain the beamformed signal and the beamformer weights.
[ $\mathrm{y}, \mathrm{w}$ ] = beamformer(rx,incidentAngle);
Plot the original signal at the middle element and the beamformed signal.

```
plot(t,real(rx(:,3)),'r:',t,real(y))
xlabel('Time')
```

ylabel('Amplitude')
legend('Original', 'Beamformed')


Plot the array response pattern after applying the weights.
pattern(array,fc,[-180:180],0,'PropagationSpeed', c, 'CoordinateSystem','rectangular','Weights',w)


## Algorithms

The phase shift beamformer uses the conventional delay-and-sum beamforming algorithm. The beamformer assumes the signal is narrowband, so a phase shift can approximate the required delay. The beamformer preserves the incoming signal power.

For further details, see [1].

## References

[1] Van Trees, H. Optimum Array Processing. New York: Wiley-Interscience, 2002.

## See Also <br> uv2azel| phitheta2azel

## phased.Platform

Package: phased
Model platform motion

## Description

The phased.Platform System object models the translational motion of one or more platforms in space. A platform can be a target such as a vehicle or airplane, or a sonar or radar transmitter and receiver. The model assumes that the platform undergoes translational motion at constant velocity or constant acceleration during each simulation step. Positions and velocities are always defined in the global coordinate system.

To model a moving platform:
1 Define and set up your platform using the "Construction" on page 1-1240 procedure.
2 Repeatedly call the step method to move the platform along a path determined by the phased.Platform properties.

The behavior of step is specific to each object in the toolbox.

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.

## Construction

sPlat = phased.Platform creates a platform System object, sPlat. The object models a stationary platform with position at the origin and velocity set to zero.
sPlat = phased.Platform(Name, Value) creates an object, sPlat, with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN).
sPlat = phased.Platform(pos,vel,Name,Value) creates a platform object, sPlat, with InitialPosition set to pos and Velocity set to vel. Other specified property Names are set to specified Values. The pos and vel arguments are value-only. Value-only arguments do not require a specified Name but are interpreted according to their argument positions. To specify any value-only argument, specify all preceding value-only arguments.

The motion model is either a constant velocity, a constant acceleration, or a custom trajectory. You can choose one of two motion models using the MotionModel property.

| MotionModel Value | Usage |
| :--- | :--- |
| 'Velocity' | If you set the VelocitySource property to <br> 'Property' , the platform moves with constant <br> velocity determined by the Velocity property. <br> You can specify the InitialPosition property <br> or leave it to its default value. You can change the <br> tunable Velocity property at any simulation <br> step. |
|  | When you set the VelocitySource property to <br> ' Input port' , you can input instantaneous <br> velocity as an argument to the step method. <br> Specify the initial position using the <br> InitialPosition property or leave it as a <br> default value. |
| 'Acceleration' | When you set the AccelerationSource <br> property to 'Property' , the platform moves <br> with constant acceleration determined by the <br> Acceleration property. You can specify the <br> InitialPosition and InitialVelocity <br> properties or leave them to their defaults. You <br> can change the tunable Acceleration property <br> at any simulation step. |
|  | When you set the AccelerationSource <br> property to ' Input port ', you can input <br> instantaneous acceleration as an argument to the <br> step method. Specify the InitialPosition <br> and InitialVelocity properties or leave them <br> as their defaults. |
| 'Custom' | Specify the platform motion using a series of <br> waypoints in the CustomTrajectory property. |

## Properties

## MotionModel

## Object motion model

Object motion model, specified as 'Velocity', 'Acceleration', or 'Custom'. When you set this property to 'Velocity', the platform follows a constant velocity trajectory during each simulation step. When you set this property to 'Acceleration', the platform follows a constant acceleration trajectory during each simulation step. When you set the property to 'Custom', the platform motion follows a sequence of waypoints specified by the CustomTrajectory property. The object performs a piecewise cubic interpolation on the waypoints to derive the position and velocity at each time step.

Default: 'Velocity'

## InitialPosition

Initial position of platform

Initial position of platform, specified as a real-valued 3-by-1 column vector in the form of $[x ; y ; z]$ or a real-valued 3 -by- $N$ matrix where $N$ is the number of platforms. Each column takes the form
[x;y;z]. Position units are meters.
Default: [0;0;0]

## InitialVelocity

Initial velocity of platform
Initial velocity of platform, specified as a real-valued 3-by-1 column vector in the form of [vx; vy;vz] or a real-valued 3 -by- $N$ matrix where $N$ is the number of platforms. Each column taking the form [vx;vy;vz]. Velocity units are meters per second.

This property only applies when you set the MotionModel property to 'Velocity' and the VelocitySource to 'Input port', or when you set the MotionModel property to 'Acceleration'.

Default: [0;0;0]
VelocitySource
Source of velocity data
Source of velocity data, specified as one of 'Property' or 'Input port'. When you set the value of this property to 'Property', use Velocity property to set the velocity. When you set this property to 'Input port', use an input argument of the step method to set the velocity.

This property applies when you set the MotionModel property to 'Velocity'.
Default: 'Property'

## Velocity

## Current velocity of platform

Specify the current velocity of the platform as a 3-by-1 real-valued column vector in the form of [vx;vy;vz] or a 3-by-N real-valued matrix for multiple platforms. Each column taking the form [vx;vy;vz]. Velocity units are meters/sec. The dimension $N$ is the number of platforms.

This property applies when you set the MotionModel property to 'Velocity' and the VelocitySource to 'Property'. This property is tunable.

Default: [0;0;0]

## AccelerationSource

Source of acceleration data
Source of acceleration data, specified as one of 'Property' or 'Input port'. When you set the value of this property to 'Property', specify the acceleration using the Acceleration property. When you set this property to 'Input port', use an input argument of the step method to set the acceleration.

This property applies when you set the MotionModel property to 'Acceleration'.

Default: 'Property'

## Acceleration

Acceleration of platform
Specify the current acceleration of the platform as a real-valued 3-by-1 column vector in the form [ax;ay;az] or a real-valued 3 -by- $N$ matrix with each column taking the form [ax;ay;az]. The dimension $N$ is the number of platforms. Acceleration units are meters $/ \mathrm{sec} / \mathrm{sec}$.

This property applies when you set the MotionModel property to 'Acceleration' and AccelerationSource to 'Property'. This property is tunable.

Default: [0;0;0]

## CustomTrajectory

Custom trajectory waypoints.
Custom trajectory waypoints, specified as a real-valued $M$-by- $L$ matrix, or $M$-by- $L$-by- $N$ array. $M$ is the number of waypoints. $L$ is either 4 or 7.

- When $L$ is 4 , the first column indicates the times at which the platform position is measured. Columns 2-4 are position measurements in $\mathrm{x}, \mathrm{y}$, and z coordinates. The velocity is derived from the position measurements.
- When $L$ is 7, columns 5-7 in the matrix are velocity measurements in $\mathrm{x}, \mathrm{y}$, and z coordinates.

When you set the CustomTrajectory property to a three-dimensional array, the number of pages, $N$, represent the number of platforms. Time units are in seconds, position units are in meters, and velocity units are in meters per second.

To enable this property, set the MotionModel property to 'Custom '.

## ScanMode

Mechanical scanning mode
Mechanical scan mode for platform, specified as 'None', 'Circular'', or 'Sector', where 'None' is the default. When you set the ScanMode property to 'Circular', the platform scan clockwise 360 degrees continuously in the azimuthal direction of the platform orientation axes. When you set the ScanMode property to 'Sector', the platform scans clockwise in the azimuthal direction in the platform orientation axes within a range specified by the AzimuthSpan property. When the platform scan reaches the span limits, the scan reverses direction and scans back to the other scan limit. Scanning happens within the orientation axes of the platform.

## InitialScanAngle

Initial scan angle of platform
Initial scan angle of platform, specified as a 1 -by- $N$ vector where $N$ is the number of platforms. The scanning occurs in the local coordinate system of the platform. The InitialOrientationAxes specifies the original local coordinate system. At the start of the simulation, the orientation axes specified by the InitialOrientationAxes are rotated by the angle specified in the InitialScanAngle property. The default value is zero. Units are in degrees. This property applies when you set the ScanMode property to 'Circular' or 'Sector'.

## Example: [30 40]

## AzimuthSpan

Azimuth span
The azimuth angle span, specified as an $N$-by-2 matrix where $N$ is the number of platforms. Each row of the matrix specifies the scan range of the corresponding platform in the form
[ScanAngleLowerBound ScanAngleHigherBound]. The default value is [-60 60]. Units are in degrees. To enable this property, set the ScanMode to 'Sector'.

## AzimuthScanRate

Azimuth scan rate
Azimuth scan rate, specified as a 1 -by- $N$ vector where $N$ is the number of platforms. Each entry in the vector is the azimuth scan rate for the corresponding platform. The default value is 10 degrees/ second. Units are in degrees/second. To enable this property, set the ScanMode property to 'Circular' or 'Sector'.

## InitialOrientationAxes

Initial orientation axes of platform
Initial orientation axes of platform, specified as a 3-by-3 real-valued orthonormal matrix for a single platform or as a 3 -by-3-by- $N$ real-valued matrix for multiple platforms. The dimension $N$ is the number of platforms. When the orientation matrix is 3 -by-3, the three columns represent the axes of the local coordinate system ( $x y z$ ). When the orientation matrix is 3 -by-3-by- $N$, for each page index, the resulting 3 -by- 3 matrix represents the axes of a local coordinate system.

Default: [1 0 0;0 1 0;0 0 1]

## OrientationAxesOutputPort

Output orientation axes
To obtain the instantaneous orientation axes of the platform, set this property to true and use the corresponding output argument when invoking step. If you do not want to obtain the orientation axes of the platform, set this property to false.

Default: false

## Methods

reset Reset platform to initial position
step Output current position, velocity, and orientation axes of platform

```
Common to All System Objects
release Allow System object property value changes
```


## Examples

## Simulate Motion of a Platform

Create a platform at the origin having a velocity of $(100,100,0)$ meters per second. Simulate the motion of the platform for two time steps, assuming the time elapsed for each step is one second. The position of the platform is updated after each step.

```
sPlat = phased.Platform([0; 0; 0],[100; 100; 0]);
T = 1;
```

At the first call to step, the position is at its initial value.

```
[pos,v] = step(sPlat,T);
pos
pos = 3\times1
    0
    0
    0
```

At the second call to step, the position changes.

```
[pos,v] = step(sPlat,T);
pos
pos = 3\times1
    100
    100
        0
```


## Model Motion of Circling Airplane

Start with an airplane moving along a circular track with a radius of 10 km at a horizontal speed of $100 \mathrm{~m} / \mathrm{s}$ and descending at a rate of $1 \mathrm{~m} / \mathrm{sec}$. To create circular motion, specify a radially-inward acceleration and constrain the acceleration to lie in the horizontal plane. The acceleration of a body moving in a circle is $\frac{v^{2}}{r}$. The rate of descent is constant. Set the initial orientation axes matrix of the platform to the identity matrix.

## Set up the initial conditions

```
alt = 10000;
radcirc = 10000; % 10 km
phi = 60;
initPos = [cosd(phi)*radcirc;sind(phi)*radcirc;alt];
vs = 100.0;
vx = vs*sind(phi);
vy = -vs*cosd(phi);
vz = -1;
initVel = [vx,vy,vz]';
airplane = phased.Platform('MotionModel','Acceleration', ....
    'AccelerationSource','Input port','InitialPosition',initPos, ...
```

```
    'InitialVelocity',initVel,'OrientationAxes0utputPort',true, ...
    'InitialOrientationAxes',eye(3));
accelmag = vs^2/radcirc;
initPos1 = [cosd(phi)*radcirc;sind(phi)*radcirc;0];
unitvec = initPosl/radcirc;
accel = -accelmag*unitvec;
```


## Compute the trajectory

Compute the trajectory for 20000 integration steps at $\mathrm{T}=0.1 \mathrm{~s}$ intervals

```
N = 20000;
tstep = .10;
posmat = zeros(3,N);
for n = 1:N
    [pos,vel,oax] = airplane(tstep,accel);
    velcirc2 = vel(1)^2 + vel(2)^2;
    vmag = sqrt(velcirc2);
    pos1 = [pos(1),pos(2),0]';
    radcirc = sqrt(pos1'*pos1);
    unitvec = posl/radcirc;
    accelmag = velcirc2/radcirc;
    accel = -accelmag*unitvec;
    posmat(:,n) = pos;
end
```

Display the final orientation of the local coordinate system.
disp(oax)

| 0.1271 | 0.9919 | 0.0001 |
| ---: | ---: | ---: |
| -0.9919 | 0.1271 | 0.0003 |
| 0.0003 | -0.0001 | 1.0000 |

## Plot the trajectory

```
plot3(posmat(1,:)/1000,posmat(2,:)/1000,posmat(3,:)/1000,'b.')
xlabel('X (km)')
ylabel('Y (km)')
zlabel('Z (km)')
axis equal
grid
```



## Define Platform Motion Using Waypoints

This example shows
Create waypoints from parabolic motion.

```
x0 = 100;
y0 = -150;
z0 = 0;
vx = 5;
vy = 10;
vz = 0;
ax = 1;
ay = -1;
t = [0:2:20];
x = x0 + vx*t + ax/2*t.^2;
y = y0 + vy*t + ay/2*t.^2;
z = z0*ones(size(t));
wpts = [t.' x.' y.' z.'];
```

Create a platform object with motion determined using waypoints.

```
pltfm = phased.Platform('MotionModel','Custom','CustomTrajectory',wpts);
```

tstep = .5;

```
nsteps = 40;
X = [];
```

Advance the platform in time steps of one half second;

```
for k = 1:nsteps
    [pos,vel] = pltfm(tstep);
    X = [X;pos'];
end
plot(x,y,'o'); hold on
plot(X(:,1),X(:,2),'.')
hold off;
```



## More About

## Platform Orientation

A platform has an associated local coordinate system defined by three orthonormal axis vectors. The direction and magnitude of the velocity vector can change with each call to the step method. When the platform undergoes curvilinear motion, the orientation of the local coordinate system axes rotates with the motion of the platform. The change of direction of the velocity vector defines a rotation matrix. The same rotation matrix is then used to rotate the local coordinate system as well. When the velocity vector maintains a constant direction, the rotation matrix is the identity matrix. The initial orientation of the local coordinate system is specified using the InitialOrientationAxes property. When you specify multiple platforms, each platform rotates independently.

## Version History

Introduced in R2011a

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
See "System Objects in MATLAB Code Generation" (MATLAB Coder).

## See Also

global2localcoord|local2globalcoord | phased.Collector|phased.Radiator | rangeangle

## Topics

"Motion Modeling in Phased Array Systems"

## reset

System object: phased.Platform
Package: phased
Reset platform to initial position

## Syntax

reset (H)

## Description

reset $(\mathrm{H})$ resets the initial position of the Platform object, H .

## step

System object: phased. Platform
Package: phased
Output current position, velocity, and orientation axes of platform

## Syntax

[Pos,Vel] = step(sPlat,T)
[Pos,Vel] = step(sPlat,T,V)
[Pos,Vel] = step(sPlat,T,A)
[Pos,Vel,Laxes] = step( ___)

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step $(o b j, x)$ and $y=o b j(x)$ perform equivalent operations.
[Pos, Vel] = step(sPlat, T ) returns the current position, Pos, and velocity, Vel, of the platform. The method then updates the position and velocity. When the MotionModel property is set to 'Velocity ' and the VelocitySource property is set to 'Property' , the position is updated using the equation Pos $=$ Pos $+V e \|^{*} T$ where $T$ specifies the elapsed time (in seconds) for the current step. When the MotionModel property is set to 'Acceleration' and the AccelerationSource property is set to 'Property' , the position and velocity are updated using the equations Pos $=$ Pos + $V e{ }^{*} T+1 / 2 A c l^{*} T^{\wedge} 2$ and $\mathrm{Vel}=\mathrm{Vel}+A c l^{*} T$ where $T$ specifies the elapsed time (in seconds) for the current step.
[Pos, Vel] = step(sPlat, $\mathrm{T}, \mathrm{V}$ ) returns the current position, Pos, and the current velocity, Vel, of the platform. The method then updates the position and velocity using the equation Pos $=$ Pos + $V e{ }^{*} T$ where $T$ specifies the elapsed time (in seconds) for the current step. This syntax applies when you set the MotionModel property to 'Velocity' and the VelocitySource property to 'Input port'.
[Pos, Vel] = step(sPlat, T, A) returns the current position, Pos, and the current velocity, Vel, of the platform. The method then updates the position and velocity using the equations Pos $=$ Pos + $V e l * T+1 / 2 A c l^{*} T^{\wedge} 2$ and $\mathrm{Vel}=\mathrm{Vel}+A c l^{*} T$ where $T$ specifies the elapsed time (in seconds) for the current step. This syntax applies when you set the MotionModel property to 'Acceleration' and the AccelerationSource property to 'Input port'.
[Pos,Vel,Laxes] = step (__ ) returns the additional output Laxes as the platform's orientation axes when you set the OrientationAxesOutputPort property to true.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## sPlat

Platform
Platform, specified as a phased.Plat form System object.
T
Step time
Step time, specified as a real-valued scalar. Units are seconds

## V

Platform velocity
Platform velocity, specified as a real-valued 3-by- $N$ matrix where $N$ is the number of platforms to model. This argument applies when you set the MotionModel property to 'Velocity' and the VelocitySource property to 'Input port'. Units are meters per second.

A
Platform acceleration
Platform acceleration, specified as a real-valued 3-by- $N$ matrix where $N$ is the number of platforms to model. This argument applies when you set the MotionModel property to 'Acceleration' and the AccelerationSource property to 'Input port'. Units are meters per second-squared.

## Output Arguments

## Pos

Current platform position
Current position of platform, specified as a real-valued 3-by-1 column vector in the form of [x;y;z] or a real-valued 3 -by- $N$ matrix where $N$ is the number of platforms to model. Each column takes the form [x;y;z]. Units are meters.

## Vel

Current platform velocity
Current velocity of platform, specify as a real-valued 3-by-1 column vector in the form of [vx; vy; vz] or a real-valued 3 -by- $N$ matrix where $N$ is the number of platforms to model. Each column taking the form [vx;vy;vz]. Velocity units are meters per second.

## Laxes

Current platform orientation axes
Current platform orientation axes, returned as real-valued 3 -by- 3 -by- $N$ matrix where $N$ is the number of platforms to model. Each 3-by-3 submatrix is an orthonormal matrix. This output is enabled when
you set the OrientationAxesOutputPort property to true. The current platform axes rotate around the normal vector to the path of the platform.

## Examples

## Simulate Motion of Two Platforms

Create two moving platforms. The first platform, starting at the origin, has a velocity of $(100,100,0)$ meters per second. The second starts at ( $1000,0,0$ ) meters and has a velocity of $(0,200,0)$ meters per second. Next, specify different local coordinate axes for each platform defined by rotation matrices. Setting the OrientationAxes0utputPort property to true lets you retrieve the local coordinate axes at each step.

Set up the platform object.

```
pos0 = [[0;0;0],[1000;0;0]];
vel0 = [[100;100;0],[0;200;0]];
R1 = rotx(30);
R2 = roty(45);
laxes(:,:,1) = R1;
laxes(:,:,2) = R2;
sPlat = phased.Platform(pos0,vel0,...
    'OrientationAxesOutputPort',true,...
    'InitialOrientationAxes',laxes);
```

Simulate the motion of the platform for two time steps, assuming the time elapsed for each step is one second. The position of the platform is updated after each step.

T = 1;
At the first step, the position and velocity equal the initial values.

```
[pos,v,lax] = step(sPlat,T);
pos
pos = 3\times2
    0 1000
0 0
0 0
lax
lax =
lax(:,:,1) =
\begin{tabular}{rrr}
1.0000 & 0 & 0 \\
0 & 0.8660 & -0.5000 \\
0 & 0.5000 & 0.8660
\end{tabular}
lax(:,:,2) =
    0.7071 0 0.7071
        0 1.0000 0
```

-0.7071
0
0.7071

At the second step, the position is updated.

```
[pos,v,lax] = step(sPlat,T);
pos
pos = 3\times2
\begin{tabular}{rr}
100 & 1000 \\
100 & 200 \\
0 & 0
\end{tabular}
```

lax
lax =
$\operatorname{lax}(:,:, 1)=$

| 1.0000 | 0 | 0 |
| ---: | ---: | ---: |
| 0 | 0.8660 | -0.5000 |
| 0 | 0.5000 | 0.8660 |

$\operatorname{lax}(:,:, 2)=$

| 0.7071 | 0 | 0.7071 |
| ---: | ---: | ---: |
| 0 | 1.0000 | 0 |
| -0.7071 | 0 | 0.7071 |

## Free Falling Accelerating Platform

Find the trajectory of a platform which starts with some initial upward velocity but accelerates downward with a constant gravitational acceleration of $-9.8 \mathrm{~m} / \mathrm{sec} / \mathrm{sec}$. Update the platform position and velocity every two seconds.

Construct the platform System object ${ }^{\text {TM }}$.
platform = phased.Platform('MotionModel','Acceleration','InitialPosition',[2000,100,3000]',...
InitialVelocity',[300,150,20]','AccelerationSource','Property','Acceleration',[0,0,-9.8]');
T = 2;
$\mathrm{N}=100$;
Call the step method for 100 time samples.

```
posmat = zeros(3,N);
for n = 1:N
    [pos,vel] = platform(T);
    posmat(:,n) = pos;
end
```

Plot the trajectory.

```
plot3(posmat(1,:),posmat(2,:),posmat(3,:),'b.')
```

axis equal
xlabel('m') ylabel('m') zlabel('m') grid


# phased.RadarTarget 

Package: phased
Radar target

## Description

The RadarTarget System object models how a signal is reflected from a radar target. The quantity that determines the response of a target to incoming signals is called the radar target cross-section (RCS). While all electromagnetic radar signals are polarized, you can sometimes ignore polarization and process them as if they were scalar signals. To ignore polarization, specify the EnablePolarization property as false. To utilize polarization, specify the EnablePolarization property as true. For non-polarized processing, the radar cross section is encapsulated in a single scalar quantity called the MeanRCS. For polarized processing, specify the radar cross-section as a 2-by-2 scattering matrix in the ScatteringMatrix property. For both polarization processing types, there are several Swerling models available that can generate random fluctuations in the RCS.
Choose these models using the Model property. The SeedSource and Seed properties control the random fluctuations.

The properties that you can use to model the radar cross-section or scattering matrix depend upon the polarization type.

| EnablePolarization Value | Use These Properties |
| :---: | :---: |
| false | - MeanRCSSource <br> - MeanRCS |
| true | - ScatteringMatrixSource <br> - ScatteringMatrix <br> - Mode |

To compute the signal reflected from a radar target:
1 Define and set up your radar target. See "Construction" on page 1-1256.
2 Call step to compute the reflected signal according to the properties of phased.RadarTarget. The behavior of step is specific to each object in the toolbox.

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.

## Construction

$\mathrm{H}=$ phased.RadarTarget creates a radar target System object, H , that computes the reflected signal from a target.

H = phased.RadarTarget (Name, Value) creates a radar target object, H, with each specified property set to the specified value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN).

## Properties

## EnablePolarization

Allow polarized signals
Set this property to true to allow the target to simulate the reflection of polarized radiation. Set this property to false to ignore polarization.

Default: false

## Mode

Target scattering mode
Target scattering mode specified as one of 'Monostatic' or 'Bistatic'. If you set this property to 'Monostatic', the reflected signal direction is opposite to its incoming direction. If you set this property to 'Bistatic', the reflected direction of the signal differs from its incoming direction. This property applies when you set the EnablePolarization property to true.

Default: 'Monostatic'

## ScatteringMatrixSource

Sources of mean scattering matrix of target
Source of mean scattering matrix of target specified as one of 'Property' or 'Input port'. If you set the ScatteringMatrixSource property to 'Property', the target's mean scattering matrix is determined by the value of the ScatteringMatrix property. If you set this property to 'Input port ', the mean scattering matrix is determined by an input argument of the step method. This property applies only when you set the EnablePolarization property to true. When the EnablePolarization property is set to false, use the MeanRCSSource property instead, together with the MeanRCS property, if needed.

Default: 'Property'

## ScatteringMatrix

Mean radar scattering matrix for polarized signal
Mean radar scattering matrix specified as a complex-valued 2-by-2 matrix. This matrix represents the mean value of the target's radar cross-section. Units are in square meters. The matrix has the form [s_hh s_hv;s_vh s_vv]. In this matrix, the component s_hv specifies the complex scattering response when the input signal is vertically polarized and the reflected signal is horizontally polarized. The other components are defined similarly. This property applies when you set the ScatteringMatrixSource property to 'Property' and the EnablePolarization property to true. When the EnablePolarization property is set to false, use the MeanRCS property instead, together with the MeanRCSSource property. This property is tunable.

Default: [1 0;0 1i]
MeanRCSSource
Source of mean radar cross section

Specify whether the mean RCS value of the target comes from the MeanRCS property of this object or from an input argument in step. Values of this property are:

| 'Property' | The MeanRCS property of this object specifies the mean RCS <br> value(s). |
| :--- | :--- |
| 'Input port' | An input argument in each invocation of step specifies the <br> mean RCS value. |

When EnablePolarization property is set to true, use the ScatteringMatrixSource property together with the ScatteringMatrix property.

Default: 'Property'

## MeanRCS

Mean radar cross section
Specify the mean value of the target's radar cross section as a nonnegative scalar or as a 1 -by- $M$ realvalued, nonnegative row vector. Units are in square meters. Using a vector lets you simultaneously process multiple targets. The quantity $M$ is the number of targets. This property is used when MeanRCSSource is set to 'Property'. This property is tunable.

When EnablePolarization property is set to true, use the ScatteringMatrix property together with the ScatteringMatrixSource.

## Default: 1

## Model

Target statistical model
Specify the statistical model of the target as one of 'Nonfluctuating', 'Swerling1',
'Swerling2', 'Swerling3', or 'Swerling4'. If you set this property to a value other than
'Nonfluctuating', you must use the UPDATERCS input argument when invoking step. You can set the mean value of the radar cross-section model by specifying MeanRCS or use its default value.

## Default: 'Nonfluctuating'

## PropagationSpeed

Signal propagation speed
Specify the propagation speed of the signal, in meters per second, as a positive scalar.
Default: Speed of light

## OperatingFrequency

Signal carrier frequency
Specify the carrier frequency of the signal you are reflecting from the target, as a scalar in hertz.
Default: 3e8

## SeedSource

Source of seed for random number generator
Specify how the object generates random numbers. Values of this property are:

| 'Auto' | The default MATLAB random number generator produces the <br> random numbers. Use 'Auto' if you are using this object with <br> Parallel Computing Toolbox software. |
| :--- | :--- |
| 'Property' | The object uses its own private random number generator to <br> produce random numbers. The Seed property of this object <br> specifies the seed of the random number generator. Use <br> 'Property' if you want repeatable results and are not using this <br> object with Parallel Computing Toolbox software. |

The random numbers are used to model random RCS values. This property applies when the Model property is 'Swerling1','Swerling2','Swerling3', or 'Swerling4'.

Default: 'Auto'

## Seed

Seed for random number generator
Specify the seed for the random number generator as a scalar integer between 0 and $2^{32}-1$. This property applies when you set the SeedSource property to 'Property'.

## Default: 0

## Methods

| reset | Reset states of radar target object |
| :--- | :--- |
| step | Reflect incoming signal |

## Common to All System Objects

```
release Allow System object property value changes
```


## Examples

## Compute Reflected Signal from a Non-fluctuating Radar Target

Create a simple signal and compute the value of the reflected signal from a target having a radar cross section of $10 \mathrm{~m}^{2}$. Set the radar cross section using the MeanRCS property. Set the radar operating frequency to 600 MHz .

```
x = ones(10,1);
target = phased.RadarTarget('Model','Nonfluctuating',...
    'MeanRCS',10,...
    'OperatingFrequency',600e6);
y = target(x);
disp(y(1:3))
```

This value agrees with the formula $y=\sqrt{G} x$ where

$$
G=4 \pi \sigma / \lambda^{2}
$$

## Algorithms

For a narrowband nonpolarized signal, the reflected signal, $Y$, is

$$
Y=\sqrt{G} \cdot X,
$$

where:

- $X$ is the incoming signal.
- $G$ is the target gain factor, a dimensionless quantity given by

$$
G=\frac{4 \Pi \sigma}{\lambda^{2}} .
$$

- $\sigma$ is the mean radar cross-section (RCS) of the target.
- $\lambda$ is the wavelength of the incoming signal.

The incident signal on the target is scaled by the square root of the gain factor.
For narrowband polarized waves, the single scalar signal, $X$, is replaced by a vector signal, $\left(E_{H}, E_{V}\right)$, with horizontal and vertical components. The scattering matrix, $S$, replaces the scalar cross-section, $\sigma$. Through the scattering matrix, the incident horizontal and vertical polarized signals are converted into the reflected horizontal and vertical polarized signals.

$$
\left[\begin{array}{l}
E_{H}^{(s c a t)} \\
E_{V}^{(s c a t)}
\end{array}\right]=\sqrt{\frac{4 \pi}{\lambda^{2}}}\left[\begin{array}{ll}
S_{H H} & S_{V H} \\
S_{H V} & S_{V V}
\end{array}\right]\left[\begin{array}{l}
E_{H}^{(i n c)} \\
E_{V}^{(i n c)}
\end{array}\right]=\sqrt{\frac{4 \pi}{\lambda^{2}}}[S]\left[\begin{array}{l}
E_{H}^{(i n c)} \\
E_{V}^{(\text {inc) }}
\end{array}\right]
$$

For further details, see Mott, [1] or Richards, [2] .

## Version History

## Introduced in R2011a

## References

[1] Mott, H., Antennas for Radar and Communications, John Wiley \& Sons, 1992.
[2] Richards, M. A. Fundamentals of Radar Signal Processing. New York: McGraw-Hill, 2005.
[3] Skolnik, M. Introduction to Radar Systems, 3rd Ed. New York: McGraw-Hill, 2001.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
See "System Objects in MATLAB Code Generation" (MATLAB Coder).

## See Also

phased.FreeSpace|phased.Platform|phased.BackscatterRadarTarget| phased.BackscatterSonarTarget|phased.WidebandBackscatterRadarTarget| backscatterPedestrian

## Topics

"Radar Target"

## reset

System object: phased.RadarTarget
Package: phased
Reset states of radar target object

## Syntax

reset (H)

## Description

reset (H) resets the states of the RadarTarget object, H. This method resets the random number generator state if the SeedSource property is applicable and has the value 'Property'.

## step

System object: phased. RadarTarget
Package: phased
Reflect incoming signal

## Syntax

```
Y = step(H,X)
Y = step(H,X,MEANRCS)
Y = step(H,X,UPDATERCS)
Y = step(H,X,MEANRCS,UPDATERCS)
Y = step(H,X,ANGLE_IN,LAXES)
Y = step(H,X,ANGLE_IN,ANGLE_OUT,LAXES)
Y = step(H,X,ANGLE_IN,LAXES,SMAT)
Y = step(H,X,ANGLE_IN,LAXES,UPDATESMAT)
Y = step(H,X,ANGLE_IN,ANGLE_OUT,LAXES,SMAT,UPDATESMAT)
```


## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step $(o b j, x)$ and $y=o b j(x)$ perform equivalent operations.
$Y=\operatorname{step}(H, X)$ returns the reflected signal $Y$ due to the incident signal $X$. The argument $X$ is a complex-valued $N$-by- 1 column vector or $N$-by- $M$ matrix. The value $M$ is the number of signals. Each signal corresponds to a different target. The value $N$ is the number of samples in each signal. Use this syntax when you set the Model property of H to 'Nonfluctuating '. In this case, the value of the MeanRCS property is used as the Radar cross-section (RCS) value. This syntax applies only when the EnablePolarization property is set to false. If you specify $M$ incident signals, you can specify the radar cross-section as a scalar or as a 1 -by- $M$ vector. For a scalar, the same value will be applied to all signals.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
$\mathrm{Y}=$ step ( $\mathrm{H}, \mathrm{X}$, MEANRCS) uses MEANRCS as the mean RCS value. This syntax is available when you set the MeanRCSSource property to 'Input port' and set Model to 'Nonfluctuating'. The value of MEANRCS must be a nonnegative scalar or 1 -by-M row vector for multiple targets. This syntax applies only when the EnablePolarization property is set to false.
$\mathrm{Y}=\operatorname{step}(\mathrm{H}, \mathrm{X}, \mathrm{UPDATERCS})$ uses UPDATERCS as the indicator of whether to update the RCS value. This syntax is available when you set the Model property to 'Swerling1', 'Swerling2', 'Swerling3' , or 'Swerling4'. If UPDATERCS is true, a new RCS value is generated. If UPDATERCS is false, the previous RCS value is used. This syntax applies only when the

EnablePolarization property is set to false. In this case, the value of the MeanRCS property is used as the radar cross-section (RCS) value.
$\mathrm{Y}=\operatorname{step}(\mathrm{H}, \mathrm{X}$, MEANRCS, UPDATERCS $)$ lets you can combine optional input arguments when their enabling properties are set. In this syntax, MeanRCSSource is set to 'Input port' and Model is set to one of the Swerling models. This syntax applies only when the EnablePolarization property is set to false. For this syntax, changes in MEANRCS will be ignored after the first call to the step method.

Y = step ( $\mathrm{H}, \mathrm{X}$, ANGLE_IN, LAXES) returns the reflected signal Y from an incident signal X . This syntax applies only when the EnablePolarization property is set to true. The input argument, ANGLE_IN, specifies the direction of the incident signal with respect to the target's local coordinate system. The input argument, LAXES, specifies the direction of the local coordinate axes with respect to the global coordinate system. This syntax requires that you set the Model property to 'Nonfluctuating' and the Mode property to 'Monostatic'. In this case, the value of the ScatteringMatrix property is used as the scattering matrix value.
$X$ is a 1-by- $M$ row array of MATLAB struct type, each member of the array representing a different signal. The struct contains three fields, X.X, X.Y, and X.Z. Each field corresponds to the $x, y$, and $z$ components of the polarized input signal. Polarization components are measured with respect to the global coordinate system. Each field is a column vector representing a sequence of values for each incoming signal. The X.X, X.Y, and Y. Z fields must all have the same dimension. The argument, ANGLE_IN, is a 2-by- $M$ matrix representing the signals' incoming directions with respect to the target's local coordinate system. Each column of ANGLE_IN specifies the incident direction of the corresponding signal in the form [AzimuthAngle; ElevationAngle]. Angle units are in degrees. The number of columns in ANGLE_IN must equal the number of signals in the $X$ array. The argument, LAXES, is a 3-by-3 matrix. The columns are unit vectors specifying the local coordinate system's orthonormal $x, y$, and $z$ axes, respectively, with respect to the global coordinate system. Each column is written in $[x ; y ; z]$ form.
$Y$ is a row array of struct type having the same size as $X$. Each struct contains the three reflected polarized fields, Y.X, Y.Y, and Y.Z. Each field corresponds to the $x, y$, and $z$ component of the signal. Polarization components are measured with respect to the global coordinate system. Each field is a column vector representing one reflected signal.

The size of the first dimension of the matrix fields within the struct can vary to simulate a changing signal length such as a pulse waveform with variable pulse repetition frequency.

Y = step( $\mathrm{H}, \mathrm{X}$, ANGLE_IN, ANGLE_OUT, LAXES), in addition, specifies the reflection angle, ANGLE_OUT, of the reflected signal when you set the Mode property to 'Bistatic'. This syntax applies only when the EnablePolarization property is set to true. ANGLE_OUT is a 2 -row matrix representing the reflected direction of each signal. Each column of ANGLE_OUT specifies the reflected direction of the signal in the form [AzimuthAngle; ElevationAngle]. Angle units are in degrees. The number of columns in ANGLE_OUT must equal the number of members in the $X$ array. The number of columns in ANGLE_OUT must equal the number of elements in the X array.

Y = step(H,X,ANGLE_IN,LAXES, SMAT) specifies SMAT as the scattering matrix. This syntax applies only when the EnablePolarization property is set to true. The input argument SMAT is a 2-by-2 matrix. You must set the ScatteringMatrixSource property 'Input port' to use SMAT.
 update the scattering matrix when you set the Model property to 'Swerling1', 'Swerling2 ' ', 'Swerling3', or 'Swerling4'. This syntax applies only when the EnablePolarization property
is set to true. If UPDATESMAT is set to true, a scattering matrix value is generated. If UPDATESMAT is false, the previous scattering matrix value is used.
$Y=\operatorname{step}\left(H, X, A N G L E \_I N, A N G L E \_O U T, L A X E S, S M A T, U P D A T E S M A T\right)$. You can combine optional input arguments when their enabling properties are set. Optional inputs must be listed in the same order as the order of their enabling properties.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Examples

## Compute Reflected Signals from Two Non-Fluctuating Radar Targets

Create two sinusoidal signals and compute the value of the reflected signals from targets having radar cross sections of $5 \mathrm{~m}^{2}$ and $10 \mathrm{~m}^{2}$, respectively. Set the radar cross sections in the step method by choosing Input port for the value of the MeanRCSSource property. Set the radar operating frequency to 600 MHz .

```
sRadarTarget = phased.RadarTarget('Model','Nonfluctuating',...
    'MeanRCSSource','Input port',...
    'OperatingFrequency',600e6);
t = linspace(0,1,1000);
x = [cos(2*pi*250*t)',10*sin(2*pi*250*t)'];
y = step(sRadarTarget,x,[5,10]);
disp(y(1:3,1:2))
\begin{tabular}{rr}
15.8643 & 0 \\
-0.0249 & 224.3546 \\
-15.8642 & -0.7055
\end{tabular}
```


## Algorithms

For a narrowband nonpolarized signal, the reflected signal, $Y$, is

$$
Y=\sqrt{G} \cdot X
$$

where:

- $X$ is the incoming signal.
- $G$ is the target gain factor, a dimensionless quantity given by

$$
G=\frac{4 \Pi \sigma}{\lambda^{2}}
$$

- $\sigma$ is the mean radar cross-section (RCS) of the target.
- $\lambda$ is the wavelength of the incoming signal.

The incident signal on the target is scaled by the square root of the gain factor.
For narrowband polarized waves, the single scalar signal, $X$, is replaced by a vector signal, $\left(E_{H}, E_{V}\right)$, with horizontal and vertical components. The scattering matrix, $S$, replaces the scalar cross-section, $\sigma$. Through the scattering matrix, the incident horizontal and vertical polarized signals are converted into the reflected horizontal and vertical polarized signals.

$$
\left[\begin{array}{l}
E_{H}^{(s c a t)} \\
E_{V}^{(s c a t)}
\end{array}\right]=\sqrt{\frac{4 \pi}{\lambda^{2}}}\left[\begin{array}{ll}
S_{H H} & S_{V H} \\
S_{H V} & S_{V V}
\end{array}\right]\left[\begin{array}{l}
E_{H}^{(i n c)} \\
E_{V}^{(i n c)}
\end{array}\right]=\sqrt{\frac{4 \pi}{\lambda^{2}}}[S]\left[\begin{array}{l}
E_{H}^{(i n c)} \\
E_{V}^{(i n c)}
\end{array}\right]
$$

For further details, see Mott [1] or Richards[2].

## References

[1] Mott, H. Antennas for Radar and Communications.John Wiley \& Sons, 1992.
[2] Richards, M. A. Fundamentals of Radar Signal Processing. New York: McGraw-Hill, 2005.
[3] Skolnik, M. Introduction to Radar Systems, 3rd Ed. New York: McGraw-Hill, 2001.

## See Also

## Topics

"Swerling 1 Target Models"
"Swerling Target Models"
"Swerling 3 Target Models"
"Swerling 4 Target Models"

## phased.Radiator

Package: phased
Narrowband signal radiator

## Description

The phased. Radiator System object implements a narrowband signal radiator. A radiator converts signals into radiated wavefields transmitted from arrays and individual sensor elements such as antennas, microphone elements, and sonar transducers. The radiator output represents the fields at a reference distance of one meter from the phase center of the element or array. You can then propagate the signals to the far field using, for example, the phased. FreeSpace, phased.LOSChannel, or twoRayChannel System objects.

The object radiates fields in one of two ways controlled by the CombineRadiatedSignals property.

- If the CombineRadiatedSignals is set to true, the radiated field in a specified directions is the coherent sum of the delayed radiated fields from all elements (or subarrays when subarrays are supported). The object uses the phase-shift approximation of time delays for narrowband signals.
- If the CombineRadiatedSignals is set to false, each element can radiate in an independent direction.

You can use this object to

- model electromagnetic radiated signals as polarized or non-polarized fields depending upon whether the element or array supports polarization and the value of the "Polarization" on page 10 property. Using polarization, you can transmit a signal as a polarized electromagnetic field, or transmit two independent signals using dual polarizations.
- model acoustic radiated fields by using nonpolarized microphone and sonar transducer array elements and by setting the "Polarization" on page 1-0 to 'None '. You must also set the PropagationSpeed to a value appropriate for the medium.
- radiate fields from subarrays created by the phased.ReplicatedSubarray and phased.PartitionedArray objects. You can steer all subarrays in the same direction using the steering angle argument, STEERANG, or steer each subarray in a different direction using the Subarray element weights argument, WS. The radiator distributes the signal powers equally among the elements of each subarray. You cannot set the CombineRadiatedSignals property to false for subarrays.

To radiate signals:
1 Create the phased.Radiator object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

radiator = phased. Radiator
radiator $=$ phased.Radiator(Name,Value)
Description
radiator $=$ phased. Radiator creates a narrowband signal radiator object, radiator, with default property values.
radiator $=$ phased.Radiator(Name, Value) creates a narrowband signal radiator with each property Name set to a specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN). Enclose each property name in single quotes.
Example: radiator $=$ phased.Radiator('Sensor', phased.URA, 'OperatingFrequency' ,300e6) sets the sensor array to a uniform rectangular array (URA) with default URA property values. The beamformer has an operating frequency of 300 MHz .

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## Sensor - Sensor element or sensor array

phased.ULA array with default property values (default) | Phased Array System Toolbox sensor or array

Sensor element or sensor array, specified as a System object belonging to Phased Array System Toolbox. A sensor array can contain subarrays.

Example: phased.URA

## PropagationSpeed - Signal propagation speed

physconst('LightSpeed') (default) | positive scalar
Signal propagation speed, specified as a positive scalar. Units are in meters per second. The default propagation speed is the value returned by physconst('LightSpeed'). See physconst for more information.
Example: 3e8
Data Types: double

## OperatingFrequency - Operating frequency

300e6 (default) | positive scalar
Operating frequency, specified as a positive scalar. Units are in Hz.

Example: 1e9
Data Types: double
CombineRadiatedSignals - Combine radiated signals
true (default) | false
Combine radiated signals, specified as true or false. This property enables the coherent summation of the radiated signals from all elements of an array to produce plane waves. Set this property to false to obtain individual radiated signal for each radiating element.

- If the CombineRadiatedSignals is set to true, the radiated field in a specified directions is the coherent sum of the delayed radiated fields from all elements (or subarrays when subarrays are supported). The object uses the phase-shift approximation of time delays for narrowband signals.
- If the CombineRadiatedSignals is set to false, each element can radiate in an independent direction. If the Sensor property is an array that contains subarrays, you cannot set the CombineRadiatedSignals property to 'false.


## Data Types: logical

## SensorGainMeasure - Specify sensor gain <br> 'dB' (default)|'dBi'

Sensor gain measure, specified as 'dB' or 'dBi'.

- When you set this property to 'dB' , the input signal power is scaled by the sensor power pattern (in dB ) at the corresponding direction and then combined.
- When you set this property to ' dBi ' , the input signal power is scaled by the directivity pattern (in $\mathrm{dBi})$ at the corresponding direction and then combined. This option is useful when you want to compare results with the values computed by the radar equation that uses $d B i$ to specify the antenna gain. The computation using the 'dBi' option is expensive as it requires an integration over all directions to compute the total radiated power of the sensor.


## Dependencies

To enable this property, set the CombineRadiatedSignals property to true.

## Data Types: char

## Polarization - Polarization configuration

'None' (default) | 'Combined' | 'Dual'
Polarization configuration, specified as 'None', 'Combined ', or 'Dual'. When you set this property to 'None', the output field is considered a scalar field. When you set this property to 'Combined ', the radiated fields are polarized and are interpreted as a single signal in the sensor's inherent polarization. When you set this property to 'Dual ', the $H$ and $V$ polarization components of the radiated field are independent signals.
Example: 'Dual'
Data Types: char

## WeightsInputPort - Enable weights input <br> false (default) | true

Enable weights input, specified as false or true. When true, use the object input argument $W$ to specify weights. Weights are applied to individual array elements (or at the subarray level when subarrays are supported).

## Data Types: logical

## Usage

## Syntax

```
Y = radiator(X,ANG)
Y = radiator(X,ANG,LAXES)
Y = radiator(XH,XV,ANG,LAXES)
Y = radiator(, W)
Y = radiator(__,STEERANG)
Y = radiator(__,WS)
Y = radiator(\overline{X,ANG,LAXES,W,STEERANG)}
```


## Description

$Y=$ radiator (X,ANG) radiates the fields, $Y$, derived from signals, $X$ in the directions specified by ANG.
$Y=$ radiator (X, ANG, LAXES) also specifies LAXES as the local coordinate system axes directions. To use this syntax, set the "Polarization" on page 1-0 property to 'Combined '.
$Y=$ radiator (XH,XV,ANG,LAXES) specifies a horizontal-polarization port signal, XH, and a vertical-polarization port signal, XV. To use this syntax, set the "Polarization" on page 1-0 property to 'Dual'.
$\mathrm{Y}=$ radiator (__ W ) also specifies W as element or subarray weights. To use this syntax, set the WeightsInputPort property to true.
$\mathrm{Y}=$ radiator (__ , STEERANG) also specifies STEERANG as the subarray steering angle. To use this syntax, set the Sensor property to an array that supports subarrays and set the SubarraySteering property of that array to either 'Phase' or 'Time'.
$Y=$ radiator $($ $\qquad$ ,WS) also specifies WS as weights applied to each element within each subarray.
To use this syntax, set the Sensor property to an array that supports subarrays and set the SubarraySteering property of the array to 'Custom'.

You can combine optional input arguments when their enabling properties are set, for example, $\mathrm{Y}=$ radiator ( $\mathrm{X}, \mathrm{ANG}$, LAXES , W , STEERANG) combines several input arguments. Optional inputs must be listed in the same order as the order of the enabling properties.

## Input Arguments

## X - Signal to radiate

complex-valued $M$-by-1 vector | complex-valued $M$-by- $N$ matrix
Signal to radiate, specified as a complex-valued $M$-by- 1 vector or complex-valued $M$-by- $N$ matrix. $M$ is the length of the signal, and $N$ is the number of array elements (or subarrays when subarrays are supported).

## Dimensions of $\mathbf{X}$

| Dimension | Signal |
| :--- | :--- |
| $M$-by-1 vector | The same signal is radiated from all array <br> elements (or all subarrays when subarrays are <br> supported). |
| $M$-by $-N$ matrix | Each column corresponds to the signal radiated <br> by the corresponding array element (or <br> corresponding subarrays when subarrays are <br> supported). |

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

## Dependencies

To enable this argument, set the Polarization property to 'None ' or 'Combined '.
Data Types: double
Complex Number Support: Yes

## ANG - Radiating directions of signals

real-valued 2-by-L matrix
Radiating directions of signals, specified as a real-valued 2-by-L matrix. Each column specifies a radiating direction in the form [AzimuthAngle; ElevationAngle]. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive. When the CombineRadiatedSignals property is false, the number of angles must equal the number of array elements, $N$. Units are in degrees.

Example: [30, 20;45,0]
Data Types: double
LAXES - Local coordinate system
real-valued 3-by-3 orthogonal matrix
Local coordinate system, specified as a real-valued 3-by-3 orthogonal matrix. The matrix columns specify the local coordinate system's orthonormal $x, y$, and $z$ axes with respect to the global coordinate system.
Example: rotx (30)

## Dependencies

To enable this argument, set the Polarization property to 'Combined ' or 'Dual'.
Data Types: double
XH - H-polarization port signal to radiate
complex-valued $M$-by- 1 vector | complex-valued $M$-by- $N$ matrix
H-polarization port signal to radiate, specified as a complex-valued $M$-by-1 vector or complex-valued $M$-by- $N$ matrix. $M$ is the length of the signal, and $N$ is the number of array elements (or subarrays when subarrays are supported).

Dimensions of XH

| Dimension | Signal |
| :--- | :--- |
| $M$-by-1 vector | The same signal is radiated from all array <br> elements (or all subarrays when subarrays are <br> supported). |
| $M$-by- $N$ matrix | Each column corresponds to the signal radiated <br> by the corresponding array element (or <br> corresponding subarrays when subarrays are <br> supported). |

The dimensions and sizes of XH and XV must be the same.
The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

## Dependencies

To enable this argument, set the Polarization property to 'Dual ' .

## Data Types: double

Complex Number Support: Yes

## XV - V-polarization port signal to radiate

complex-valued $M$-by-1 vector | complex-valued $M$-by- $N$ matrix
V-polarization port signal to radiate, specified as a complex-valued $M$-by-1 vector or complex-valued $M$-by- $N$ matrix. $M$ is the length of the signal, and $N$ is the number of array elements (or subarrays when subarrays are supported).

Dimensions of XV

| Dimension | Signal |
| :--- | :--- |
| $M$-by-1 vector | The same signal is radiated from all array <br> elements (or all subarrays when subarrays are <br> supported). |
| $M$-by $-N$ matrix | Each column corresponds to the signal radiated <br> by the corresponding array element (or <br> corresponding subarrays when subarrays are <br> supported). |

The dimensions and sizes of XH and XV must be the same.
The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

## Dependencies

To enable this argument, set the Polarization property to 'Dual ' .
Data Types: double
Complex Number Support: Yes

## W - Element or subarray weights

$N$-by-1 column vector
Element or subarray weights, specified as a complex-valued $N$-by- 1 column vector where $N$ is the number of array elements (or subarrays when the array supports subarrays).

## Dependencies

To enable this argument, set the WeightsInputPort property to true.
Data Types: double
Complex Number Support: Yes

## WS - Subarray element weights

complex-valued $N_{\text {SE }}$-by- $N$ matrix | 1-by- $N$ cell array
Subarray element weights, specified as complex-valued $N_{\text {SE }}$-by- $N$ matrix or 1-by- $N$ cell array where $N$ is the number of subarrays. These weights are applied to the individual elements within a subarray.

## Subarray element weights

| Sensor Array | Subarray weights |
| :--- | :--- |
| phased. ReplicatedSubarray | All subarrays have the same dimensions and <br> sizes. Then, the subarray weights form an $N_{\text {SE }}$-by- <br> $N$ matrix. $N_{\text {SE }}$ is the number of elements in each <br> subarray and $N$ is the number of subarrays. Each <br> column of WS specifies the weights for the <br> corresponding subarray. |
| phased. PartitionedArray | Subarrays may not have the same dimensions and <br> sizes. In this case, you can specify subarray <br> weights as |
|  | an $N_{\text {SE }}$-by- $N$ matrix, where $N_{\mathrm{SE}}$ is now the <br> number of elements in the largest subarray. <br> The first $Q$ entries in each column are the <br> element weights for the subarray where $Q$ is <br> the number of elements in the subarray. <br> a 1-by- $N$ cell array. Each cell contains a <br> column vector of weights for the <br> corresponding subarray. The column vectors <br> have lengths equal to the number of elements <br> in the corresponding subarray. |

## Dependencies

To enable this argument, set the Sensor property to an array that contains subarrays and set the SubarraySteering property of the array to 'Custom'.
Data Types: double
Complex Number Support: Yes

## STEERANG - Subarray steering angle

real-valued 2-by-1 vector

Subarray steering angle, specified as a length- 2 column vector. The vector has the form [azimuthAngle;elevationAngle]. The azimuth angle must be between $-180^{\circ}$ and $180^{\circ}$, inclusive. The elevation angle must be between $-90^{\circ}$ and $90^{\circ}$, inclusive. Units are in degrees.

## Example: [20;15]

## Dependencies

To enable this argument, set the Sensor property to an array that supports subarrays and set the SubarraySteering property of that array to either 'Phase' or 'Time'
Data Types: double

## Output Arguments

## Y - Radiated signals

complex-valued $M$-by-L matrix | complex-valued 1-by-L cell array of structures
Radiated signals, specified as a complex-valued $M$-by- $L$ matrix or a 1-by- $L$ cell array, where $L$ is the number of radiating angles, ANG. $M$ is the length of the input signal, $X$.

- If the Polarization property value is set to 'None', the output argument $Y$ is an $M$-by- $L$ matrix.
- If the Polarization property value is set to 'Combined ' or 'Dual ', Y is a 1 -by-L cell array of structures. Each cell corresponds to a separate radiating signal. Each struct contains three column vectors containing the $X, Y$, and $Z$ components of the polarized fields defined with respect to the global coordinate system.

Data Types: double

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```


## Common to All System Objects

step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object

## Examples

## Radiation from 5-Element ULA

Propagate and combine radiation from five isotropic antenna elements. Set up a uniform line array of five isotropic antennas.

First construct a ULA array.

```
array = phased.ULA('NumElements',5);
```

Construct a radiator object.

```
radiator = phased.Radiator('Sensor',array,...
    'OperatingFrequency',300e6,'CombineRadiatedSignals',true);
```

Create a simple signal to radiate.
$\mathrm{x}=[1 ;-1 ; 1 ;-1 ; 1 ;-1]$;
Specify the azimuth and elevation of the radiating direction.

```
radiatingAngle = [30;10];
```

Radiate the signal.

```
y = radiator(x,radiatingAngle)
y = 6x1 complex
    -0.9523 - 0.0000i
    0.9523 + 0.0000i
    -0.9523 - 0.0000i
    0.9523 + 0.0000i
    -0.9523 - 0.0000i
    0.9523 + 0.0000i
```


## Radiation from 5-Element ULA of Polarized Antennas

Propagate and combine the radiation from five short-dipole antenna elements.
Set up a uniform line array of five short-dipole antennas with polarization enabled. Then, construct the radiator object.

```
antenna = phased.ShortDipoleAntennaElement;
array = phased.ULA('Element',antenna,'NumElements',5);
radiator = phased.Radiator('Sensor',array,'OperatingFrequency',300e6,...
    'CombineRadiatedSignals',true,'Polarization','Combined');
```

Rotate the local coordinate system from the global coordinates by $10^{\circ}$ around the x-axis. Demonstrate that the output represents a polarized field.

Specify a simple signal to radiate and specify the radiating direction in azimuth and elevation. Radiate the fields in two directions.

```
x = [1;-1;1;-1;1;-1];
radiatingAngles = [30 30; 0 20];
y = radiator(x,radiatingAngles,rotx(10))
y=1\times2 struct array with fields:
    X
    Y
    Z
```

Show the y-component of the polarized field radiating in the first direction.

```
disp(y(1).Y)
```

```
-0.2131 + 0.0000i
    0.2131 - 0.0000i
-0.2131 + 0.0000i
    0.2131 - 0.0000i
-0.2131 + 0.0000i
    0.2131 - 0.0000i
```


## Radiate Signal from Isotropic Antenna

Radiate a signal from a single isotropic antenna.

```
antenna = phased.IsotropicAntennaElement;
radiator = phased.Radiator('Sensor',antenna,'OperatingFrequency',300e6);
sig = [1;1];
radiatingAngles = [30 10]';
y = radiator(sig,radiatingAngles);
```

Radiate a far-field signal in two directions from a 5 -element array.

```
array = phased.ULA('NumElements',5);
radiator = phased.Radiator('Sensor',array,'OperatingFrequency',300e6);
sig = [1;1];
radiatingAngles = [30 10; 20 0]';
y = radiator(sig,radiatingAngles);
```

Radiate signals from a 3-element antenna array. Each antenna radiates a separate signal in a separate direction.

```
array = phased.ULA('NumElements',3);
radiator = phased.Radiator('Sensor',array,'OperatingFrequency',1e9,...
    'CombineRadiatedSignals',false);
sig = [1 2 3; 2 8 -1];
radiatingAngles = [10 0; 20 5; 45 2]';
y = radiator(sig,radiatingAngles)
y = 2x3
    2 3
    1
```


## Measure Target Scattering Matrix Using Dual Polarization

Use a dual-polarization system to obtain target scattering information. Simulate a transmitter and receiver where the vertical and horizontal components are transmitted successively using the input ports of the transmitter. The signals from the two polarization output ports of the receiver are then used to determine the target scattering matrix.

```
scmat = [0 1i; 1i 2];
radiator = phased.Radiator('Sensor', ...
    phased.CustomAntennaElement('SpecifyPolarizationPattern',true), ...
    'Polarization','Dual');
target = phased.RadarTarget('EnablePolarization',true,'ScatteringMatrix', ...
```

scmat);
collector = phased.Collector('Sensor', ...
phased.CustomAntennaElement('SpecifyPolarizationPattern',true), ...
'Polarization','Dual');
xh = 1;
$x v=1$;
Transmit a horizontal component and display the reflected Shh and Svh polarization components.

```
x = radiator(xh,0,[0;0],eye(3));
xrefl = target(x,[0;0],eye(3));
[Shh,Svh] = collector(xrefl,[0;0],eye(3))
Shh = 0
Svh = 0.0000 + 3.5474i
```

Transmit a vertical component and display the reflected Shv and Svv polarization components.

```
x = radiator(0,xv,[0;0],eye(3));
xrefl = target(x,[0;0],eye(3));
[Shv,Svv] = collector(xrefl,[0;0],eye(3))
Shv = 0.0000 + 3.5474i
Svv = 7.0947
```


## Version History

## Introduced in R2011a

## References

[1] Van Trees, H. Optimum Array Processing. New York: Wiley-Interscience, 2002.

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
See "System Objects in MATLAB Code Generation" (MATLAB Coder).

## See Also

phased.WidebandRadiator|phased.WidebandCollector|phased.Collector| phased.FreeSpace | twoRayChannel

## step

System object: phased. Radiator
Package: phased
Radiate signals

## Syntax

```
Y = step(H,X,ANG)
Y = step(H,X,ANG,LAXES)
Y = step(H,X,ANG,WEIGHTS)
Y = step(H,X,ANG,STEERANGLE)
Y = step(H,X,ANG,LAXES,WEIGHTS,STEERANGLE)
```


## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step (obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.
$\mathrm{Y}=\operatorname{step}(\mathrm{H}, \mathrm{X}, \mathrm{ANG})$ radiates signal X in the direction ANG. Y is the radiated signal. The radiating process depends on the CombineRadiatedSignals property of H , as follows:

- If CombineRadiatedSignals has the value true, each radiating element or subarray radiates $X$ in all the directions in ANG. $Y$ combines the outputs of all radiating elements or subarrays. If the Sensor property of H contains subarrays, the radiating process distributes the power equally among the elements of each subarray.
- If CombineRadiatedSignals has the value false, each radiating element radiates $X$ in only one direction in ANG. Each column of $Y$ contains the output of the corresponding element. The false option is available when the Sensor property of H does not contain subarrays.
$Y=$ step ( $\mathrm{H}, \mathrm{X}, \mathrm{ANG}, \mathrm{LAXES}$ ) uses LAXES as the local coordinate system axes directions. This syntax is available when you set the EnablePolarization property to true.

Y = step( $\mathrm{H}, \mathrm{X}$, ANG, WEIGHTS) uses WEIGHTS as the weight vector. This syntax is available when you set the WeightsInputPort property to true.
$\mathrm{Y}=\operatorname{step}(\mathrm{H}, \mathrm{X}$, ANG, STEERANGLE) uses STEERANGLE as the subarray steering angle. This syntax is available when you configure H so that H . Sensor is an array that contains subarrays and H.Sensor.SubarraySteering is either 'Phase' or 'Time'.
$\mathrm{Y}=\operatorname{step}(\mathrm{H}, \mathrm{X}$, ANG, LAXES, WEIGHTS, STEERANGLE) combines all input arguments. This syntax is available when you configure H so that H . EnablePolarization is true, H . WeightsInputPort is true, H.Sensor is an array that contains subarrays, and H.Sensor. SubarraySteering is either 'Phase' or 'Time'.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of
the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## H

Radiator object.

## X

Signals to radiate. X can be either a vector or a matrix.
If X is a vector, that vector is radiated through all radiating elements or subarrays. The computation does not divide the signal's power among elements or subarrays, but rather treats the $X$ vector the same as a matrix in which each column equals this vector.

If X is a matrix, the number of columns of X must equal the number of subarrays if H . Sensor is an array that contains subarrays, or the number of radiating elements otherwise. Each column of X is radiated by the corresponding element or subarray.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

## ANG

Radiating directions of signals. ANG is a two-row matrix. Each column specifies a radiating direction in the form [AzimuthAngle;ElevationAngle], in degrees.

## LAXES

Local coordinate system. LAXES is a 3-by-3 matrix whose columns specify the local coordinate system's orthonormal $x, y$, and $z$ axes, respectively. Each axis is specified in terms of $[x ; y ; z]$ with respect to the global coordinate system. This argument is only used when the EnablePolarization property is set to true.

## WEIGHTS

Vector of weights. WEIGHTS is a column vector whose length equals the number of radiating elements or subarrays.

## STEERANGLE

Subarray steering angle, specified as a length- 2 column vector. The vector has the form [azimuth; elevation], in degrees. The azimuth angle must be between -180 and 180 degrees, inclusive. The elevation angle must be between $-90^{\circ}$ and $90^{\circ}$, inclusive.

## Output Arguments

Y
Radiated signals

- If the EnablePolarization property value is set to false, the output argument $Y$ is a matrix. The number of columns of the matrix equals the number of radiating signals. Each column of $Y$ contains a separate radiating signal. The number of radiating signals depends upon the CombineRadiatedSignals property of H .
- If the EnablePolarization property value is set to true, Y is a row vector of elements of MATLAB struct type. The length of the struct vector equals the number of radiating signals. Each struct contains a separate radiating signal. The number of radiating signals depends upon the CombineRadiatedSignals property of H . Each struct contains three column-vector fields, $X, Y$, and $Z$. These fields represent the $x, y$, and $z$ components of the polarized wave vector signal in the global coordinate system.


## Examples

## Radiation from 5-Element ULA

Propagate and combine radiation from five isotropic antenna elements. Set up a uniform line array of five isotropic antennas.

First construct a ULA array.
array $=$ phased.ULA('NumElements',5);
Construct a radiator object.

```
radiator = phased.Radiator('Sensor',array,...
```

    'OperatingFrequency', 300e6, 'CombineRadiatedSignals', true);
    Create a simple signal to radiate.

```
x = [1;-1;1;-1;1;-1];
```

Specify the azimuth and elevation of the radiating direction.

```
radiatingAngle = [30;10];
```

Radiate the signal.

```
y = radiator(x,radiatingAngle)
y = 6x1 complex
    -0.9523 - 0.0000i
    0.9523 + 0.0000i
    -0.9523 - 0.0000i
        0.9523 + 0.0000i
    -0.9523 - 0.0000i
    0.9523 + 0.0000i
```


## Radiation from 5-Element ULA of Polarized Antennas

Propagate and combine the radiation from five short-dipole antenna elements.

Set up a uniform line array of five short-dipole antennas with polarization enabled. Then, construct the radiator object.

```
antenna = phased.ShortDipoleAntennaElement;
array = phased.ULA('Element',antenna,'NumElements',5);
radiator = phased.Radiator('Sensor',array,'OperatingFrequency',300e6,...
    'CombineRadiatedSignals',true,'Polarization','Combined');
```

Rotate the local coordinate system from the global coordinates by $10^{\circ}$ around the x -axis. Demonstrate that the output represents a polarized field.

Specify a simple signal to radiate and specify the radiating direction in azimuth and elevation. Radiate the fields in two directions.

```
x = [1;-1;1;-1;1;-1];
radiatingAngles = [30 30; 0 20];
y = radiator(x,radiatingAngles,rotx(10))
y=1\times2 struct array with fields:
    X
    Y
    Z
```

Show the y-component of the polarized field radiating in the first direction.

```
disp(y(1).Y)
    -0.2131 + 0.0000i
    0.2131 - 0.0000i
    -0.2131 + 0.0000i
    0.2131 - 0.0000i
    -0.2131 + 0.0000i
    0.2131 - 0.0000i
```


# phased.RangeAngleResponse 

Package: phased

Range-angle response

## Description

The phased.RangeAngleResponse System object creates an range-angle response object. This object calculate the range-angle response of a signal using either a matched filter or an FFT.

The input to the range-angle response object is a data cube. The organization of the data cube follows the Phased Array System Toolbox convention. The first dimension of the cube represents the fast-time samples or ranges of the received signals. The second dimension represents multiple channels such as sensors or beams. The third dimension, slow time, represents pulses or sweeps. If the data contains only one channel, for example, the data cube can contain fewer than three dimensions. Range processing operates along the first dimension of the cube. Angle processing operates along the second dimension.

The output of the object is also a data cube with the same number of dimensions as the input. The first dimension contains range-processed data but its length can differ from the first dimension of the input. The second dimension contains angle-processed data. Its length can differ from the last dimension of the input.

To obtain the range-angle response:
1 Create the phased. RangeAngleResponse object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

response = phased. RangeAngleResponse
response $=$ phased.RangeAngleResponse(Name,Value)

## Description

response = phased.RangeAngleResponse creates a phased.RangeAngleResponse System object, response, with default property values.
response $=$ phased.RangeAngleResponse(Name,Value) sets properties for the phased. RangeAngleResponse object using one or more name-value pairs. For example, response = phased.RangeAngleResponse('RangeMethod','FFT','SampleRate',1e6) creates an object that uses an FFT range processing method at a sample rate of 1 MHz . Enclose property names in quotes.

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## SensorArray - Sensor array

phased.ULA array with default array properties (default) | Phased Array System Toolbox array System object

Sensor array, specified as a Phased Array System Toolbox array System object.
Example: phased.URA
RangeMethod - Range processing method
'Matched filter' (default)|'FFT'
Range processing method, specified as 'Matched filter' or 'FFT'.

- 'Matched filter' - The object match-filters the incoming signal. This approach is commonly used for pulsed signals, where the matched filter is the time reverse of the transmitted signal.
- 'FFT' - The object applies an FFT to the input signal. This approach is commonly used for chirped signals such as FMCW and linear FM pulsed signals.

Example: 'Matched filter'
Data Types: char

## PropagationSpeed - Signal propagation speed

physconst('LightSpeed') (default)| positive scalar
Signal propagation speed, specified as a positive scalar. Units are in meters per second. The default propagation speed is the value returned by physconst('LightSpeed'). See physconst for more information.

Example: 3e8
Data Types: double

## OperatingFrequency - Operating frequency

300e6 (default) | positive scalar
Operating frequency, specified as a positive scalar. Units are in Hz .
Example: 1e9
Data Types: double

## SampleRate - Signal sample rate

le6 (default) | positive real-valued scalar
Signal sample rate, specified as a positive real-valued scalar. Units are in hertz.
Example: 1e6

## Data Types: double

## SweepSlope - Linear FM sweep slope

## 1.0e9 (default) | scalar

Linear FM sweep slope, specified as a scalar. The fast-time dimension of the signal input argument to step must correspond to sweeps having this slope.
Example: 1.5e9

## Dependencies

To enable this property, set the RangeMethod property to ' FFT'.

```
Data Types: double
```


## DechirpInput - Enable dechirping of input signals <br> false (default) |true

Option to enable dechirping of input signals, specified as false or true. Set this property to false to indicate that the input signal is already dechirped and no dechirp operation is necessary. Set this property to true when the input signal requires dechirping.

## Dependencies

To enable this property, set the RangeMethod property to ' $\mathrm{FFT}^{\text {' }}$.
Data Types: logical

## DecimationFactor - Decimation factor for dechirped signals

1 (default) | positive integer
Decimation factor for dechirped signals, specified as a positive integer. The decimation algorithm uses a 30th-order FIR filter generated by firl( $30,1 / D$ ), where $D$ is the decimation factor. The default value of 1 implies no decimation.

When processing FMCW signals, decimating the dechirped signal is useful for reducing the load on A/D converters.

## Dependencies

To enable this property, set the RangeMethod property to 'FFT' and the DechirpInput property to true.

Data Types: double

## RangeFFTLengthSource - Source of FFT length for range processing of dechirped signals 'Auto (default)|'Property'

Source of the FFT length used for the range processing of dechirped signals, specified as 'Auto ' or 'Property'.

- 'Auto ' - The FFT length equals the length of the fast-time dimension of the input data cube.
- 'Property ' - Specify the FFT length by using the RangeFFTLength property.


## Dependencies

To enable this property, set the RangeMethod property to ' $F$ FT' .

## Data Types: char

## RangeFFTLength - FFT length used for range processing <br> 1024 (default) | positive integer

FFT length used for range processing, specified as a positive integer.

## Dependencies

To enable this property, set the RangeMethod property to 'FFT ' and the RangeFFTLengthSource property to 'Property'
Data Types: double

## RangeWindow - FFT weighting window for range processing

'None' (default)|'Hamming'|'Chebyshev'|'Hann'|'Kaiser'|'Taylor' |'Custom'
FFT weighting window for range processing, specified as 'None', 'Hamming', 'Chebyshev',
'Hann', 'Kaiser', 'Taylor', or 'Custom'.
If you set this property to 'Taylor' , the generated Taylor window has four nearly constant sidelobes next to the mainlobe.

## Dependencies

To enable this property, set the RangeMethod property to ' FFT '.
Data Types: char
RangeSidelobeAttenuation - Sidelobe attenuation for range processing
30 (default) | positive scalar
Sidelobe attenuation for range processing, specified as a positive scalar. Attenuation applies to Kaiser, Chebyshev, or Taylor windows. Units are in dB.

## Dependencies

To enable this property, set the RangeMethod property to 'FFT' and the RangeWindow property to 'Kaiser', 'Chebyshev', or 'Taylor'.

## CustomRangeWindow - Custom window for range processing

@hamming (default) | function handle | cell array
Custom window for range processing, specified as a function handle or a cell array containing a function handle as its first entry. If you do not specify a window length, the object computes the window length and passes that into the function. If you specify a cell array, the remaining cells of the array can contain arguments to the function. If you use only the function handle without passing in arguments, all arguments take their default values.

If you write your own window function, the first argument must be the length of the window.

Note Instead of using a cell array, you can pass in all arguments by constructing a handle to an anonymous function. For example, you can set the value of CustomRangeWindow to @(n)taylorwin(n, nbar, sll), where you have previously set the values of nbar and sll.

Example: \{@taylor,5,-35\}

## Dependencies

To enable this property, set the RangeMethod property to 'FFT' and the RangeWindow property to 'Custom'.

Data Types: function_handle | cell

## ReferenceRangeCentered - Set reference range at center of range grid true (default) | false

Set reference range at center of range grid, specified as true or false. Setting this property to true enables you to set the reference range at the center of the range grid. Setting this property to false sets the reference range to the beginning of the range grid.

## Dependencies

To enable this property, set the RangeMethod to ' FFT ' .

## Data Types: logical

## ReferenceRange - Reference range of range grid

0.0 (default) | nonnegative scalar

Reference range of the range grid, specified as a nonnegative scalar.

- If you set the RangeMethod property to 'Matched filter', the reference range is set to the start of the range grid.
- If you set the RangeMethod property to ' FFT ', the reference range is determined by the ReferenceRangeCentered property.
- When you set the ReferenceRangeCentered property to true, the reference range is set to the center of the range grid.
- When you set the ReferenceRangeCentered property to false, the reference range is set to the start of the range grid.

Units are in meters.
This property is tunable.
Example: 1000. 0
Data Types: double

## MaximumNumInputSamplesSource - Source of maximum number of input signal samples

'Auto' (default)|'Property'
Source of the maximum number of input signal samples, specified as 'Auto' or 'Property'. When you set this property to 'Auto', the object automatically allocates enough memory to buffer the first input signal. When you set this property to 'Property' , you specify the maximum number of samples in the input signal using the MaximumNumInputSamples property. Any input signal longer than that value is truncated.

To use this object with a variable-size signal in a MATLAB Function Block in Simulink, set this property to 'Property ' and set a value for the MaximumNumInputSamples property.

## Dependencies

To enable this property, set the MaximumDistanceSource property to 'Property'.

## MaximumNumInputSamples - Maximum number of input signal samples

## 100 (default) | positive integer

Maximum number of samples in the input signal, specified as a positive integer. This property limits the size of the input signal. The input signal is the first argument to the object. The number of samples is the number of rows in the input. An input signal longer than this value is truncated.

Example: 1024

## Dependencies

To enable this property, set the RangeMethod property to 'Matched filter' and set the MaximumNumInputSamplesSource property to 'Property'.
Data Types: double
ElevationAngleSource - Source of elevation angle
'Property' (default)|'Input port'
Source of elevation angle, specified as 'Property' or 'Input port'.

| 'Property' | The elevation angle comes from the ElevationAngle <br> property. |
| :--- | :--- |
| 'Input port' | The elevation angle comes from an input argument. |

## ElevationAngle - Elevation angle

0 (default) | scalar
Specify the elevation angle in degrees used to calculate the range-angle response as a scalar. The angle must lie in the range from $-90^{\circ}$ to $90^{\circ}$. Units are in degrees.
Example: 45.0

## Dependencies

To enable this property, set the ElevationAngleSource property to 'Property'.

## Data Types: double

## AngleSpan - Angle response span

[-90 90] (default) | real-valued 1-by-2 vector
Angle response span, specified as a real-valued 2-by-1 vector. The object calculates the range-angle response within the angle range, [min_angle max_angle].

## Example: [-45 45]

Data Types: double

## NumAngleSamples - Number of samples in angle span

positive integer greater than two
Number of samples in angle span used to calculate range-angle response, specified as a positive integer greater than two.
Example: [256]
Data Types: double

You can combine optional input arguments when their enabling properties are set. Optional inputs must be listed in the same order as the order of the enabling properties. For example,

```
[RESP,RANGE,ANG] = response(X,XREF,EL)
```

or
[RESP,RANGE,ANG] = response(X,COEFF,EL)

## Usage

## Syntax

[RESP,RANGE,ANG] = response(X)
[RESP,RANGE,ANG] = response(X,XREF)
[RESP,RANGE,ANG] = response(X,COEFF)
[RESP,RANGE,ANG] = response( $\qquad$ , EL)

## Description

[RESP,RANGE,ANG] = response(X) returns the range-angle response, RESP, the ranges, RANGE, and the angles, ANG. X is a dechirped signal. This syntax applies when you set the RangeMethod property to 'FFT' and the DechirpInput property to false. This syntax is often applied to FMCW signals.
[RESP,RANGE, ANG] = response(X,XREF) also specifies the reference signal, XREF to dechirped the signal. This syntax applies when you set the RangeMethod property to 'FFT' and the DechirpInput property to true. This syntax is often applied to FMCW signals. Then, the reference signal can be the transmitted signal.
[RESP,RANGE,ANG] = response( $\mathrm{X}, \mathrm{COEFF}$ ) also specifies COEFF as matched filter coefficients. This syntax applies when you set the RangeMethod property to 'MatchedFilter'. This syntax is often applied to pulsed signals.
[RESP,RANGE,ANG] = response( __, EL) also specifies EL as the elevation angle. This syntax applies when you set the ElevationAngleSource property to 'Input port'.

## Input Arguments

## X - Input signal data cube

complex-valued $K$-by- $N$ matrix | complex-valued $K$-by- $N$-by- $L$ array
Input signal cube, specified as a complex-valued $K$-by- $N$ matrix or complex-valued $K$-by- $N$-by- $L$ array. The contents of the data cube depend on the type of range-angle processing specified by the different syntaxes.

- $K$ is the number of fast-time or range samples.
- $N$ is the number of independent spatial channels such as sensors or beams.
- $L$ is the slow-time dimension that corresponds to the number of pulses or sweeps in the input signal.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

## XREF - Reference signal used for dechirping

complex-valued $K$-by- 1 column vector
Reference signal used for dechirping, specified as a complex-valued $K$-by- 1 column vector. The number of rows must equal the length of the fast-time dimension of $X$.

## Dependencies

To enable this input argument, set the value of RangeMethod to 'FFT' and DechirpInput to true.
Data Types: double

## COEFF - Matched filter coefficients

complex-valued $P$-by-1 column vector
Matched filter coefficients, specified as a complex-valued $P$-by-1 column vector. $P$ must be less than or equal to $K . K$ is the number of fast-time or range sample.

## Dependencies

To enable this input argument, set the value of RangeMethod to 'Matched filter'.

## Data Types: double

## EL - Elevation angle <br> scalar

Elevation angle of response, specified as a scalar between $-90^{\circ}$ and $+90^{\circ}$. The range-angle response is computed for this elevation. Units are in degrees.

## Dependencies

To enable this argument, set the ElevationAngleSource property to 'Input port'.
Data Types: double

## Output Arguments

## RESP - Range response data cube

complex-valued $M$-element column vector | complex-valued $M$-by- $L$ matrix | complex-valued $M$-by- $N$ by-L array

Range response data cube, returned as one of the following:

- Complex-valued $M$-element column vector
- Complex-valued $M$-by- $L$ matrix
- Complex-valued $M$-by- $N$ by- $L$ array

The value of $M$ depends on the type of processing

| RangeMethod Property | DechirpInput Property | Value of $\boldsymbol{M}$ |
| :--- | :--- | :--- |
| ' FFT' | false | If you set the RangeFFTLength <br> property to 'Auto ',$M=K$, the <br> length of the fast-time <br> dimension of $x$. Otherwise, $M$ <br> equals the value of the <br> RangeFFTLength property. |
|  |  | true |
| 'Matched filter' | $M$ equals the quotient of the <br> number of rows, $K$, of the input <br> signal by the value of the <br> decimation factor, $D$, specified <br> in DecimationFactor. |  |

Data Types: double

## RANGE - Range values along range dimension

real-valued $M$-by-1 column vector
Range values along range dimension, returned as a real-valued $M$-by- 1 column vector. rnggrid defines the ranges corresponding to the fast-time dimension of the RESP output data cube. $M$ is the length of the fast-time dimension of RESP. Range values are monotonically increasing and equally spaced. Units are in meters.

## Data Types: double

## ANG - Angle values along angle direction

$P$-by-1 real-valued vector
Angle values along angle direction, returned as a $P$-by-1 real-valued vector. Units are in degrees.
Data Types: double

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```


## Specific to phased.RangeAngleResponse

plotResponse Plot range-angle response

## Common to All System Objects

step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object

## Examples

## Range Angle Response of Antenna Array

Calculate the range-angle response from a pulsed radar transmitting a rectangular waveform using the matched filter approach. The signal includes three target returns. Two are approximately 2000 m away and the third is approximately 3500 m away. In addition, two targets are stationary relative to the radar while the third is moving away from the radar at approximately $100 \mathrm{~m} / \mathrm{s}$. The signals arrive at an 8-element uniform linear array.

First, load the example data.

```
load('RangeAngleResponseExampleData','rectdata');
fs = rectdata.fs;
propspeed = rectdata.propspeed;
fc = rectdata.fc;
rxdata = rectdata.rxdata;
mfcoeffs = rectdata.mfcoeffs;
%noisepower = rectdata.noisepower;
antennaarray = rectdata.antennaarray;
```

Second, create the range-angle response object for matched filter processing.

```
rngangresp = phased.RangeAngleResponse(...
    'SensorArray',antennaarray,'OperatingFrequency',fc,...
    'SampleRate',fs,'PropagationSpeed',propspeed);
```

Obtain the range-angle map.
[resp,rng_grid,ang_grid] = rngangresp(rxdata,mfcoeffs);
Plot the response.

```
plotResponse(rngangresp,rxdata,mfcoeffs,'Unit','db');
```



## Algorithms

## Range-Angle Response

The object generates the response by first processing the input signal in the range domain using either a matched filter or a dechirp operation and then by processing along azimuth angles.

## Version History <br> Introduced in R2018b

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:

- The CustomRangeWindow property is not supported.
- The plotResponse object function is not supported.
- See "System Objects in MATLAB Code Generation" (MATLAB Coder).


## See Also

## Functions

bw2 range|firl|chebwin|dechirp|hann|hamming|kaiser|taylorwin|rangeangle Objects
phased.RangeResponse | phased.RangeDopplerResponse | phased.AngleDopplerResponse | phased.MatchedFilter| phased.DopplerEstimator|phased.RangeEstimator|
phased.CFARDetector | phased.CFARDetector2D

## plotResponse

Package: phased
Plot range-angle response

## Syntax

plotResponse(response, X)
plotResponse(response, X, XREF)
plotResponse(response, $X$, COEFF)
plotResponse( $\qquad$ , 'Unit', unit)

## Description

plotResponse(response, $X$ ) plots the range response of a dechirped input signal, $X$, from the phased.RangeAngleResponse object, response. This syntax applies when you set the RangeMethod property to 'FFT' and the DechirpInput property to false.
plotResponse(response, $\mathrm{X}, \mathrm{XREF}$ ) plots the range response X , after performing a dechirp operation using the reference signal, XREF. This syntax applies when you set the RangeMethod property to 'FFT' and the DechirpInput property to true.
plotResponse (response, $X$, COEFF) plots the range response of $X$ after match filtering using the match filter coefficients, coeff. This syntax applies when you set the RangeMethod property to 'Matched filter'.
plotResponse( __ , 'Unit', unit) plots the response in the units specified by units.

## Examples

## Range Angle Response of Antenna Array

Calculate the range-angle response from a pulsed radar transmitting a rectangular waveform using the matched filter approach. The signal includes three target returns. Two are approximately 2000 m away and the third is approximately 3500 m away. In addition, two targets are stationary relative to the radar while the third is moving away from the radar at approximately $100 \mathrm{~m} / \mathrm{s}$. The signals arrive at an 8-element uniform linear array.

First, load the example data.

```
load('RangeAngleResponseExampleData','rectdata');
fs = rectdata.fs;
propspeed = rectdata.propspeed;
fc = rectdata.fc;
rxdata = rectdata.rxdata;
mfcoeffs = rectdata.mfcoeffs;
%noisepower = rectdata.noisepower;
antennaarray = rectdata.antennaarray;
```

Second, create the range-angle response object for matched filter processing.

```
rngangresp = phased.RangeAngleResponse(...
    'SensorArray',antennaarray,'OperatingFrequency',fc,...
    'SampleRate',fs,'PropagationSpeed',propspeed);
```

Obtain the range-angle map.

```
[resp,rng_grid,ang_grid] = rngangresp(rxdata,mfcoeffs);
```

Plot the response.
plotResponse(rngangresp,rxdata,mfcoeffs,'Unit','db');


## Input Arguments

## response - Range-angle response object

phased. RangeAngleResponse System object
Range-angle response object, specified as a phased.RangeAngleResponse System object.

## X - Input data

complex-valued K-by- $N$ matrix
Input data, specified as a complex-valued $K$-by- $N$ matrix. The contents of the data cube depend on the type of range-angle processing specified by the different syntaxes. $K$ always specifies the number of fast-time samples and $N$ is always the number of channels, either array elements or beams.

- $K$ is the number of fast-time or range samples.
- $N$ is the number of independent spatial channels such as sensors or directions.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

## XREF - Reference signal used for dechirping

complex-valued $K$-by- 1 column vector
Reference signal used for dechirping, specified as a complex-valued $K$-by- 1 column vector. The number of rows must equal the length of the fast-time dimension of $X$.

## Dependencies

To enable this input argument, set the value of RangeMethod to ' FFT ' and DechirpInput to true.
Data Types: double

## COEFF - Matched filter coefficients

complex-valued $P$-by-1 column vector
Matched filter coefficients, specified as a complex-valued $P$-by- 1 column vector. $P$ must be less than or equal to $K$. $K$ is the number of fast-time or range sample.

## Dependencies

To enable this input argument, set the value of RangeMethod to 'Matched filter'.
Data Types: double

## unit - Plot units

```
'db' (default)|'mag' | 'pow'
```

Plot units, specified as 'db', 'mag', or 'pow'. who

- 'db ' - plot the response power in $d B$.
- 'mag' - plot the magnitude of the response.
- 'pow' - plot the response power.

Example: 'mag'
Data Types: char|string

Version History<br>Introduced in R2018b

## phased.RangeDopplerScope

Package: phased
Range-Doppler scope

## Description

The phased.RangeDopplerScope System object creates a scope for viewing a range- response map. The map is a 2-D image of response intensity as a function of range and (or speed). You can input two types of data - in-phase and quadrature (I/Q) data and response data.

- I/Q data - The data consists of fast-time and slow-time I/Q samples of pulses or sweeps. The scope computes and displays the response map. To use I/Q data, set the IQDataInput property to true. In this mode, you can set the properties shown in "Properties Applicable to I/Q Data" on page 11307.
- Response data - The data consists of the range- response itself. The scope displays the rangeresponse map. For example, you can obtain range- response from phased.RangeDopplerResponse object. To use response data, set the IQDataInput property to false. In this mode, you can set the properties shown in "Properties Applicable to Response Data" on page 1-1308.


To display a range-Doppler response map using the scope,
1 Create the phased.RangeDopplerScope object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

scope $=$ phased.RangeDopplerScope
scope $=$ phased.phased.RangeDopplerScope(Name,Value)

## Description

scope $=$ phased. RangeDopplerScope creates a range-Doppler scope System object, scope. This object displays the range-Doppler response of the input data.
scope $=$ phased.phased. RangeDopplerScope(Name, Value) creates a range-Doppler scope object, scope, with each specified property set to the specified value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN). Enclose property names in quotes. For example,

```
scope = phased.RangeDopplerScope('IQInputData',true,'RangeMethod', ...
    'FFT','SampleRate',1e6,'DopplerOutput','Speed', ...
    'OperatingFrequency',10e6,'SpeedUnits','km/h');
```

creates a scope object that uses FFT-based range processing for I/Q data having a sample rate of 1 MHz . The Doppler output units are speed in kilometers per hour.

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## Name - Display caption

'Range-Doppler Scope' (default)| character vector
Display caption, specified as a character vector. The caption appears in the title bar of the window.
Example: 'Aircraft Range-Doppler Response'
Tunable: Yes
Data Types: char

## Position - Location and size of intensity scope window

depends on display-resolution (default) | 1-by-4 vector of positive values
Location and size of the intensity scope window, specified as a 1-by-4 vector having the form [ left bottom width height].

- left and bottom specify the location of the bottom-left corner of the window.
- width and height specify the width and height of the window.

Units are in pixels.
The default value of this property depends on the resolution of your display. By default, the window is positioned in the center of the screen, with a width and height of 800 and 450 pixels, respectively.

Example: [100 100500 400]
Tunable: Yes

## Data Types: double

## IQDataInput - Type of input data <br> true (default) | false

Type of input data, specified as true or false. When true, the object assumes that the input consists of I/Q sample data and further processing is required in the range and Doppler domains. When false, the object assumes that the data is response data that has already been processed.

Data Types: logical

## ResponseUnits - Response units label

'db' (default) | 'magnitude'| 'power'
Response units, specified as 'db','magnitude', or 'power'.
Data Types: char

## RangeLabel - Range-axis label

'Range (m)' (default)| character vector
Range-axis label, specified as a character vector.
Example: 'Range (km)'
Tunable: Yes
Dependencies
To enable this property, set the IQDataInput to false.
Data Types: char
DopplerLabel - Doppler-axis label
'Doppler Frequency (Hz)' (default)| character vector
Doppler-axis label, specified as a character vector.
Example: 'Doppler Frequency (kHz)'
Tunable: Yes

## Dependencies

To enable this property, set the IQDataInput to false.
Data Types: char

## RangeMethod - Range processing method

'Matched filter' (default)| 'FFT'
Range-processing method, specified as 'Matched filter' or 'FFT'.

| 'Matched filter' | The object applies a matched filter to the incoming signal. This <br> approach is commonly used with pulsed signals, where the matched <br> filter is a time-reversed replica of the transmitted signal. |
| :--- | :--- |


| 'FFT' | Algorithm performs range processing by applying an FFT to the <br> input signal. This approach is commonly used with FMCW <br> continuous signals and linear FM pulsed signals. |
| :--- | :--- |

## Dependencies

To enable this property, set the IQDataInput property to true.

## RangeUnits - Range units

'm' (default) | 'km' | 'mi' | 'nmi'
Range units, specified as:

- 'm' - meters
- ' km' - kilometers
- 'mi' - miles
- 'nmi' - nautical miles

Example: 'mi'

## Dependencies

To enable this property, set the IQDataInput property to true.
Data Types: char

## PropagationSpeed - Signal propagation speed

physconst('LightSpeed') (default) | positive scalar
Signal propagation speed, specified as a positive scalar. The default value of this property is the speed of light. See physconst. Units are in meters/second.
Example: 3e8

## Dependencies

To enable this property, set the IQDataInput property to true.

## Data Types: double

## SampleRate - Sample rate

1e6 (default) | positive scalar
Sample rate, specified as a positive scalar. Units are in Hz.

## Example: 10e3

## Dependencies

To enable this property, set the IQDataInput property to true.

## Data Types: double

## SweepSlope - FM sweep slope

1e9 (default) | scalar
Slope of the linear FM sweep, specified as a scalar. Units are in $\mathrm{Hz} / \mathrm{sec}$.

## Dependencies

To enable this property, set the IQDataInput property to true and the RangeMethod property to 'FFT'.

Data Types: double

## DechirpInput - Dechirp input signal

false (default) | true
Set this property to true to dechirp the input signal before performing range processing. false indicates that the input signal is already dechirped and no dechirp operation is necessary.

## Dependencies

To enable this property, set the IQDataInput property to true and the RangeMethod property to 'FFT'.

Data Types: logical
RangeFFTLength - FFT length used in range processing
1024 (default) | positive integer
FFT length used for range processing, specified as a positive integer.
Example: 128

## Dependencies

To enable this property, set the IQDataInput property to true and the RangeMethod property to 'FFT'.

Data Types: double
ReferenceRangeCentered - Set reference range at center of range span
true (default) | false
Set this property to true to set the reference range to the center of the range span. Set this property to false to set the reference range to the beginning of the range span.

## Dependencies

To enable this property, set the IQDataInput property to true and the RangeMethod property to 'FFT'.

```
Data Types: logical
```


## ReferenceRange - Reference range

## 0.0 (default) | nonnegative scalar

Reference range of the range span, specified as a nonnegative scalar.

- If you set the RangeMethod property to 'Matched filter', the reference range marks the start of the range span.
- If you set the RangeMethod property to 'FFT' , the position of the reference range depends on the ReferenceRangeCentered property.
- If you set the ReferenceRangeCentered property to true, the reference range marks the center of the range span.
- If you set the ReferenceRangeCentered property to false, the reference range marks the start of the range span.

Units are in meters.
Example: 1000. 0
Tunable: Yes

## Dependencies

To enable this property, set the IQDataInput property to true.
Data Types: double

## PRFSource - Source of pulse repetition frequency

## 'Auto' (default)|'Property'

Source of the pulse repetition frequency (PRF) of the input signal, specified as 'Auto' or
'Property '. When you set this property to 'Auto', the PRF is a function of the number of rows in the input signal and the value of the SampleRate property. When you set this property to 'Property', you can specify the PRF using the PRF property.

## Dependencies

To enable this property, set the IQDataInput property to true.

## Data Types: char

PRF - Pulse repetition frequency of input signal
10e3 (default) | positive scalar
Pulse repetition frequency of input signal, specified as a positive scalar. Units are in Hz .
Example: 1.4e3

## Dependencies

To enable this property, set the IQDataInput property to true and set the PRFSource property to 'Property'.

Data Types: double

## DopplerFFTLength - FFT length used in Doppler processing

1024 (default) | positive integer
FFT length used in Doppler processing, specified as a positive integer.

## Example: 67

## Dependencies

To enable this property, set the IQDataInput property to true.

## Data Types: double

## DopplerOutput - Doppler output

'Frequency ' (default) | 'Speed '

Doppler output, specified as 'Frequency' or 'Speed '. If you set this property to 'Frequency', the Doppler output, Dop, at object execution time is the Doppler shift. If you set this property to ' Speed ' , the Doppler output is the equivalent radial speed.

## Dependencies

To enable this property, set the IQDataInput property to true.
Data Types: char
OperatingFrequency - Operating frequency
300e6 (default) | positive scalar
Operating frequency, specified as a positive scalar.

## Dependencies

To enable this property, set the IQDataInput property to true and the DopplerOutput to 'Speed'.
Data Types: double
NormalizeDoppler - Normalize Doppler
false (default)| true
Set this property to true to plot the range-Doppler response with normalized Doppler frequency. Set this property to false to plot the range-Doppler response without normalizing the Doppler frequency.

## Dependencies

To enable this property, set the IQDataInput property to true and the DopplerOutput to 'Frequency'.
Data Types: logical

## SpeedUnits - Doppler speed units

'm/s' (default)|'km/h'|'mph'|'kt'
Doppler speed units:

- 'm/s' - meters per second
- 'km/h' - kilometers per hour
- 'mph' - miles per hour
- 'kt ' - knots or nautical miles per hour

Example: 'mph'

## Dependencies

To enable this property, set the IQDataInput property to true and the DopplerOutput property to 'Speed'.

Data Types: char

## FrequencyUnits - Doppler frequency units

' Hz ' (default) | ' $\left.\mathrm{kHz}{ }^{\prime}\right|^{\prime} \mathrm{MHz}{ }^{\prime}$

Doppler frequency units, specified as ' Hz ', ' kHz ', or ' MHz '.

## Example: 'MHz'

## Dependencies

To enable this property, set the IQDataInput property to true, the DopplerOutput to
' Frequency ', and the NormalizedDoppler property to false.

## Data Types: char

## Usage

## Syntax

```
scope(X,Range,Dop)
scope(X)
scope(X,XREF)
scope(X,COEFF)
```


## Description

scope ( X , Range, Dop) displays a range-Doppler response map, X , at the ranges, Range, and Doppler shifts, Dop. This syntax applies when you set the IQDataInput to false.
scope (X) computes and displays the range-Doppler response map. This syntax applies when you set the IQDataInput property to true, the RangeMethod property to ' $\mathrm{FFT}^{\prime}$ ', and the DechirpInput property to false. This syntax is most commonly used with FMCW signals. All sweeps in X are assumed to be contiguous. If the sweeps are not contiguous, set the PRF by setting the PRFSource property to 'Property' and the PRF of the input data to the PRF.
scope ( $\mathrm{X}, \mathrm{XREF}$ ) also specifies a reference signal to use for dechirping the input signal, X . This syntax applies when you set the IQDataInput property to true, the RangeMethod property to ' FFT ' , and the DechirpInput property to true. This syntax is most commonly used with FMCW signals. XREF is generally the transmitted signal.
scope (X,COEFF) also specifies matched filter coefficients, COEFF. This syntax applies when you set the IQDataInput property to true and the RangeMethod property to 'Matched Filter'. This syntax is most commonly used with pulsed signals.

## Input Arguments

## X - Input data

complex-valued K-by-L matrix
Input data, specified as a complex-valued $K$-by- $L$ matrix. The interpretation of the data depends on the value of the IQDataInput property.

- When IQDataInput is true, the input consists of received fast-time (range) samples for each PRI pulse or FMCW sweep. $K$ denotes the number of fast-time samples. $L$ is the number of Doppler samples. The number of Doppler samples is the number of pulses in the case of pulsed signals or the number of dechirped frequency sweeps for FMCW signals. The scope computes and displays the range-Doppler response.
- When RangeMethod is set to 'FFT' and DechirpInput is false, X has previously been dechirped.
- When RangeMethod is set to ' FFT ' and DechirpInput is true, X has not been previously dechirped. Use the syntax that includes XREF as input data.
- When RangeMethod is set to 'MatchedFilter', X has not been match filtered. Use the syntax that includes COEFF as input data.
- When IQDataInput is false, the input already consists of response data in the range-Doppler domain such as that produced by phased. RangeDopplerResponse. Each row of the response map corresponds to an element of the Range vector. Each column corresponds to an element of the Dop vector. The scope serves only as a display of the range-Doppler response.


## Range - Range grid values of range-Doppler response map

real-valued $K$-by-1 column vector
Range grid values of response map, specified as a real-valued $K$-by- 1 column vector. Range denotes the range values at which the response has been computed. Elements of Range correspond to the rows of $X$.

## Dependencies

To enable this argument, set the IQInputData property to false.
Data Types: double

## Dop - Doppler grid values of range-Doppler response map

real-valued $L$-by-1 column vector
Doppler grid values of response map, specified as a real-valued $L$-by- 1 column vector. Dop denotes the Doppler values at which the response has been computed. Elements of Dop correspond to the columns of $X$. Dop can contain either Doppler or speed values at which the range-Doppler response is evaluated.

## Dependencies

To enable this argument, set the IQInputData property to false.
Data Types: double

## XREF - Reference signal

complex-valued $K$-by- 1 column vector
Reference signal used to dechirp X. XREF must be a column vector with the same number of rows as X.

## Dependencies

To enable this argument, set the IQDataInput property to true, the RangeMethod property to
' FFT' and the DechirpInput property to false
Data Types: double
Complex Number Support: Yes

## COEFF - Matched filter coefficients

complex-valued column vector
Matched filter coefficients, specified as a complex-valued column vector.

## Dependencies

To enable this argument, set the IQDataInput property to true and the RangeMethod property to 'Matched Filter'.

Data Types: double
Complex Number Support: Yes

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```


## Specific to Scope Objects

show Turn on visibility of scopes
hide Turn off visibility of scope
isVisible Visibility of scopes

## Common to All System Objects

step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object

## Examples

## View Target Response Using Range-Doppler Scope

Calculate and visualize the range-Doppler response from a pulsed radar transmitting a rectangular waveform. Compute the response using matched filtering. The signal contains returns from three targets. One target is approximately 2000 m away and is stationary relative to the radar. The second target is approximately 3500 m away and is also stationary relative to the radar. The third is approximately 2000 m away and is moving away from the radar at approximately $100 \mathrm{~m} / \mathrm{s}$.

Load the IQ data and obtain the signals and parameters.

```
load('RangeDopplerResponseExampleData','rectdata');
fs = rectdata.fs;
c = rectdata.propspeed;
fc = rectdata.fc;
rxdata = rectdata.rxdata;
mfcoeffs = rectdata.mfcoeffs;
```

Create the range-Doppler scope for matched filter processing and visualization. Set the Doppler FFT size to 1024. The display shows the three targets.

```
scope = phased.RangeDopplerScope( ...
    'IQDataInput',true,'RangeMethod','Matched filter', ...
    'Name','Range-Doppler Scope', ...
    'Position',[560 375 560 420],'ResponseUnits','db', ...
```

'RangeUnits','m','DopplerFFTLength',1024, ...
'DopplerOutput','Speed','OperatingFrequency', fc, ...
'SampleRate',fs,'PropagationSpeed', c);
scope(rxdata,mfcoeffs);


## More About

## Properties Applicable to I/Q Data

These properties are applicable when IQDataInput is true.

| Properties | Position |
| :--- | :--- |
| Name | RangeMethod |
| ResponseUnits | PropagationSpeed |
| RangeUnits | SweepSlope |
| SampleRate | RangeFFTLength |
| DechirpInput | ReferenceRange |
| ReferenceRangeCentered | PRF |
| PRFSource | DopplerOutput |
| DopplerFFTLength |  |


| Properties | NormalizeDoppler |
| :--- | :--- |
| OperatingFrequency | FrequencyUnits |
| SpeedUnits |  |

## Properties Applicable to Response Data

These properties are applicable when IQDataInput is false.

| Properties | Position |
| :--- | :--- |
| Name | RangeLabel |
| ResponseUnits |  |
| DopplerLabel |  |

## Version History

Introduced in R2019a

## See Also

show | hide |isVisible | phased.RangeDopplerResponse | phased.AngleDopplerScope | phased.RangeAngleScope

## phased.RangeAngleScope

Package: phased
View range-angle response

## Description

The phased.RangeAngleScope System object creates a scope for displaying a range-angle response map. The map is a 2-D representation of response intensity as a function of range and angle of arrival. You can input two types of data - in-phase and quadrature (I/Q) data and response data.

- I/Q data - The data consists of fast-time I/Q samples of pulses or sweeps from multiple sensors. The scope computes and displays the response map. To use I/Q data, set the IQDataInput property to true. In this mode, you can set the properties shown in "Properties Applicable to I/Q Data" on page 1-1318.
- Response data - The data consists of the range-angle response itself. The scope displays the range-angle response map. You can obtain range-angle response data from the RangeAngleResponse object. To use response data, set the IQDataInput property to false. In this mode, you can set the properties shown in "Properties Applicable to Response Data" on page 1-1319.


To display a range-angle response map using a scope,
1 Create the phased.RangeAngleScope object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

scope $=$ phased.RangeAngleScope
scope $=$ phased. RangeAngleScope(Name, Value)

## Description

scope $=$ phased. RangeAngleScope creates a range-angle scope System object for displaying the range-angle response.
scope $=$ phased. RangeAngleScope(Name, Value) creates a range-angle scope with each specified property set to the specified value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN). Enclose property names in quotes. For example,

```
scope = phased.RangeAngleScope('IQInputData',true,'RangeMethod', ...
    'FFT','SampleRate',1e6)
```

creates a scope object that uses FFT-based range processing to process I/Q data with a sample rate of 1 MHz .

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## Name - Display caption

'Range-Angle Scope' (default)| character vector
Display caption, specified as a character vector. The caption appears in the title bar of the window.
Example: 'Aircraft Range-Angle Response'
Tunable: Yes
Data Types: char
Position - Location and size of intensity scope window
depends on display-resolution (default) | 1-by-4 vector of positive values
Location and size of the intensity scope window, specified as a 1-by-4 vector having the form [left bottom width height].

- left and bottom specify the location of the bottom-left corner of the window.
- width and height specify the width and height of the window.

Units are in pixels.
The default value of this property depends on the resolution of your display. By default, the window is positioned in the center of the screen, with a width and height of 800 and 450 pixels, respectively.

Example: [100 100500 400]
Tunable: Yes
Data Types: double

## IQDataInput - Type of input data <br> true (default) | false

Type of input data, specified as true or false. When true, the object assumes that the input consists of I/Q sample data and further processing is required in the range and angle domains. When false, the object assumes that the data is response data that has already been processed.
Data Types: logical

## ResponseUnits - Response units label

'db' (default)|'magnitude'|'power'
Response units, specified as 'db', 'magnitude', or 'power'.
Data Types: char
RangeLabel - Range-axis label
'Range (m)' (default)| character vector
Range-axis label, specified as a character vector.
Example: 'Range (km)'
Tunable: Yes

## Dependencies

To enable this property, set the IQDataInput to false.

## Data Types: char

## AngleLabel - Angle-axis label

'Angle (degrees)' (default) | character vector
Angle-axis label, specified as a character vector.

```
Example: 'Angle Span (degrees)'
```

Tunable: Yes

## Dependencies

To enable this property, set the IQDataInput to false.
Data Types: char

## SensorArray - Sensor array

phased.ULA array with default array properties (default) | Phased Array System Toolbox array
System object
Sensor array, specified as a Phased Array System Toolbox array System object. See phased.ULA for the default values of a uniform linear array.
Example: phased. URA

## Dependencies

To enable this property, set the IQDataInput to true.

## RangeMethod - Range processing method

## 'Matched filter' (default)|'FFT'

Range-processing method, specified as 'Matched filter' or 'FFT'.

| 'Matched filter' | The object applies a matched filter to the incoming signal. This <br> approach is commonly used with pulsed signals, where the matched <br> filter is a time-reversed replica of the transmitted signal. |
| :--- | :--- |
| 'FFT' | Algorithm performs range processing by applying an FFT to the <br> input signal. This approach is commonly used with FMCW <br> continuous signals and linear FM pulsed signals. |

## Dependencies

To enable this property, set the IQDataInput property to true.

## RangeUnits - Range units

'm' (default) |'km' | 'mi'|'nmi'
Range units, specified as:

- 'm'-meters
- 'km' - kilometers
- 'mi'-miles
- 'nmi' - nautical miles

Example: 'mi'

## Dependencies

To enable this property, set the IQDataInput property to true.
Data Types: char

## PropagationSpeed - Signal propagation speed

physconst('LightSpeed') (default) | positive scalar
Signal propagation speed, specified as a positive scalar. The default value of this property is the speed of light. See physconst. Units are in meters/second.
Example: 3e8

## Dependencies

To enable this property, set the IQDataInput property to true.

## Data Types: double

## OperatingFrequency - Operating frequency

## 300e6 (default) | positive scalar

Operating frequency, specified as a positive scalar. Units are in Hz .

## Dependencies

To enable this property, set the IQDataInput property to true.

## Data Types: double

## SampleRate - Sample rate

1e6 (default) | positive scalar
Sample rate, specified as a positive scalar. Units are in Hz .

## Example: 10e3

## Dependencies

To enable this property, set the IQDataInput property to true.
Data Types: double
SweepSlope - FM sweep slope
1e9 (default) | scalar
Slope of the linear FM sweep, specified as a scalar. Units are in $\mathrm{Hz} / \mathrm{sec}$.

## Dependencies

To enable this property, set the IQDataInput property to true and the RangeMethod property to 'FFT'.
Data Types: double

## DechirpInput - Dechirp input signal <br> false (default) | true

Set this property to true to dechirp the input signal before performing range processing. false indicates that the input signal is already dechirped and no dechirp operation is necessary.

## Dependencies

To enable this property, set the IQDataInput property to true and the RangeMethod property to 'FFT'.

Data Types: logical

## RangeFFTLength - FFT length used in range processing

1024 (default) | positive integer
FFT length used for range processing, specified as a positive integer.

## Example: 128

## Dependencies

To enable this property, set the IQDataInput property to true and the RangeMethod property to 'FFT'.

Data Types: double
ReferenceRangeCentered - Set reference range at center of range span
true (default) | false
Set this property to true to set the reference range to the center of the range span. Set this property to false to set the reference range to the beginning of the range span.

## Dependencies

To enable this property, set the IQDataInput property to true and the RangeMethod property to 'FFT'.

Data Types: logical

## ReferenceRange - Reference range

0.0 (default) | nonnegative scalar

Reference range of the range span, specified as a nonnegative scalar.

- If you set the RangeMethod property to 'Matched filter', the reference range marks the start of the range span.
- If you set the RangeMethod property to ' $\mathrm{FFT}^{\prime}$ ', the position of the reference range depends on the ReferenceRangeCentered property.
- If you set the ReferenceRangeCentered property to true, the reference range marks the center of the range span.
- If you set the ReferenceRangeCentered property to false, the reference range marks the start of the range span.

Units are in meters.
Example: 1000. 0
Tunable: Yes

## Dependencies

To enable this property, set the IQDataInput property to true.

## Data Types: double

## ElevationAngle - Elevation angle of response <br> 0 (default) | scalar

Elevation angle at which to calculate the response, specified as a scalar. The elevation angle must lie in the interval from $-90^{\circ}$ to $90^{\circ}$, inclusive. Units are in degrees.
Example: 45 . 0

## Dependencies

To enable this property, set the IQDataInput property to true.

## Data Types: double

## AngleSpan - Azimuth angle span of response

[-90 90] (default) | real-valued 1-by-2 vector
Azimuth angle span at which to calculate response, specified as a real-valued 1-by-2 row vector. The object calculates the range-angle response within the angle range, [min_angle max_angle].
Angles must lie in the interval from $-90^{\circ}$ to $90^{\circ}$, inclusive. Units are in degrees.
Example: [-45 45]

## Dependencies

To enable this property, set the IQDataInput property to true.

## Data Types: double

## NumAngleSamples - Number of samples in azimuth angle span

256 (default) | positive integer greater than two
Number of samples in the azimuth angle span at which to calculate the range-angle response, specified as a positive integer greater than two.

## Example: 256

## Dependencies

To enable this property, set the IQDataInput property to true.
Data Types: double

## Usage

## Syntax

scope(X,Range,Ang)
scope (X)
scope (X,XREF)
scope(X,COEFF)

## Description

scope ( X , Range, Ang) displays a range-angle response map, X , at the ranges, Range, and angles, Ang. This syntax applies when you set the IQDataInput to false.
scope $(X)$ computes and displays the range-angle response map for the dechirped signal $X$. This syntax applies when you set the IQDataInput property to true, the RangeMethod property to ' FFT ', and the DechirpInput property to false. This syntax is most commonly used with FMCW signals.
scope ( $\mathrm{X}, \mathrm{XREF}$ ) also specifies a reference signal to use for dechirping the input signal, X . This syntax applies when you set the IQDataInput property to true, the RangeMethod property to ' $F F T$ ' , and the DechirpInput property to true. This syntax is most commonly used with FMCW signals. XREF is generally the transmitted signal.
scope ( X, COEFF) also specifies matched filter coefficients, COEFF. This syntax applies when you set the IQDataInput property to true and the RangeMethod property to 'Matched Filter'. This syntax is most commonly used with pulsed signals.

## Input Arguments

## X - Input data

complex-valued $K$-by-L matrix
Input data, specified as a complex-valued $K$-by- $L$ matrix. The interpretation of the data depends on the value of the IQDataInput property.

- When IQDataInput is true, the input consists of received fast-time data samples for each PRI pulse or FMCW sweep and for each array or subarray element. $K$ denotes the number of fast-time (range) samples. $L$ is the number of elements. If SensorArray contains subarrays, $L$ is the number of subarrays. The scope computes and displays the range-angle response.
- When RangeMethod is set to 'FFT' and DechirpInput is false, X has previously been dechirped.
- When RangeMethod is set to ' FFT ' and DechirpInput is true, X has not been previously dechirped. Use the syntax that includes XREF as input data.
- When RangeMethod is set to 'MatchedFilter', X has not been match filtered. Use the syntax that includes COEFF as input data.
- When IQDataInput is false, the input already consists of response data in the range-angle domain, such as the data produced, for example, by RangeAngleResponse. Each row of the response map corresponds to an element of the Range vector. $K$ is the number of range samples. Each column of the response map corresponds to an element of the Ang vector. $L$ is the number of angles. The scope serves only as a display of the range-angle response.


## Range - Range grid values of range-angle response map

real-valued $K$-by-1 column vector
Range grid values of range-angle response map, specified as a real-valued $K$-by- 1 column vector. Range denotes the range values at which the response has been computed. Elements of Range correspond to the rows of X .

## Dependencies

To enable this argument, set the IQInputData property to false.
Data Types: double

## Ang - Angle grid values of range-angle response map

real-valued $L$-by-1 column vector
Angle grid values of response map, specified as a real-valued $K$-by- 1 column vector. Ang denotes the angle values at which the response has been computed. Elements of Ang correspond to the columns of X .

## Dependencies

To enable this argument, set the IQInputData property to false.
Data Types: double

## XREF - Reference signal

complex-valued K-by-1 column vector
Reference signal used to dechirp X. XREF must be a column vector with the same number of rows as X.

## Dependencies

To enable this argument, set the IQDataInput property to true, the RangeMethod property to 'FFT' and the DechirpInput property to false

## COEFF - Matched filter coefficients

complex-valued column vector
Matched filter coefficients, specified as a complex-valued column vector.

## Dependencies

To enable this argument, set the IQDataInput property to true and the RangeMethod property to 'Matched Filter'.

Data Types: double
Complex Number Support: Yes

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```


## Specific to Scope Objects

| show | Turn on visibility of scopes |
| :--- | :--- |
| hide | Turn off visibility of scope |
| isVisible | Visibility of scopes |

## Common to All System Objects

step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object

## Examples

## View Target Response Using Range-Angle Scope

Calculate and visualize the range-angle response from a pulsed radar transmitting a rectangular waveform using a matched filter. One target is approximately 2000 m away and is stationary relative to the radar. The second target is approximately 3500 m away and is also stationary relative to the radar. The third is approximately 2000 m away and is moving away from the radar at approximately $100 \mathrm{~m} / \mathrm{s}$. The signals arrive at an 8 -element uniform linear array.

Load the data to obtain signals and parameters.

```
load('RangeAngleResponseExampleData','rectdata');
fs = rectdata.fs;
c = rectdata.propspeed;
fc = rectdata.fc;
rxdata = rectdata.rxdata;
mfcoeffs = rectdata.mfcoeffs;
noisepower = rectdata.noisepower;
array = rectdata.antennaarray;
```

Create a range-angle scope for processing.
scope $=$ phased.RangeAngleScope(
'IQDataInput',true,'RangeMethod','Matched filter', ...
'Name','Range-Angle Scope','ResponseUnits','magnitude', ...
'Position',[560 375560 420],'RangeUnits','m', ...
'SensorArray', array,'OperatingFrequency',fc, ...
'SampleRate',fs,'PropagationSpeed ', c);
Call the scope to display the response map.
scope(rxdata,mfcoeffs)


## More About

## Properties Applicable to I/Q Data

These properties are applicable when IQDataInput is true.

| Properties | Position |
| :--- | :--- |
| Name | SensorArray |
| ResponseUnits | PropagationSpeed |
| RangeMethod | RangeUnits |
| OperatingFrequency |  |


| Properties |  |
| :--- | :--- |
| SampleRate | SweepSlope |
| DechirpInput | RangeFFTLength |
| ReferenceRangeCentered | ReferenceRange |
| ElevationAngle | AngleSpan |
| NumAngleSamples |  |

## Properties Applicable to Response Data

These properties are applicable when IQDataInput is false.

| Properties | Position |
| :--- | :--- |
| Name | RangeLabel |
| ResponseUnits |  |
| AngleLabel |  |

## Version History

## Introduced in R2019a

## See Also

show | hide | isVisible | phased. RangeDopplerScope | phased.AngleDopplerScope | RangeAngleResponse

## phased.AngleDopplerScope

Package: phased
Angle-Doppler scope

## Description

The phased.AngleDopplerScope System object creates a scope for displaying an angle-Doppler response map. The map is a 2-D representation of response intensity as a function of angle and Doppler shift. You can input two types of data - in-phase and quadrature (I/Q) data and response data.

- I/Q data - The data consists of I/Q samples at the same range from multiple sensors over all pulses or sweeps. The scope computes and displays the response map. To use I/Q data, set the IQDataInput property to true. In this mode, you can set the properties listed in "Properties Applicable to I/Q Data" on page 1-1328.
- Response data - The data consists of the angle-Doppler response itself. The scope only displays the angle-Doppler response map. You can obtain angle-Doppler response data from the phased. AngleDopplerResponse object. To display response data, set the IQDataInput property to false. In this mode, you can set the properties listed in "Properties Applicable to Response Data" on page 1-1328.


To display an angle-Doppler response map using a scope,
1 Create the phased.AngleDopplerScope object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

scope = phased.AngleDopplerScope

```
scope = phased.phased.AngleDopplerScope(Name,Value)
```


## Description

scope = phased.AngleDopplerScope creates an angle-Doppler scope System object for displaying the angle-Doppler response map.
scope = phased.phased.AngleDopplerScope(Name,Value)creates an angle-Doppler scope with each specified property set to the specified value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN). Enclose property names in quotes. For example,

```
scope = phased.AngleDopplerScope('IQInputData',true, ...
    'NumAngleSamples',128,'NumDopplerSamples',64)
```

creates a scope object that computes and displays the angle-Doppler response at 128 angle values and 64 Doppler values from I/Q data input.

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## Name - Display caption

'Angle-Doppler Scope' (default) | character vector
Display caption, specified as a character vector. The caption appears in the title bar of the window.

## Example: 'Aircraft Angle-Doppler Response'

Tunable: Yes
Data Types: char

## Position - Location and size of intensity scope window

depends on display-resolution (default) | 1-by-4 vector of positive values
Location and size of the intensity scope window, specified as a 1-by-4 vector having the form [left bottom width height].

- left and bottom specify the location of the bottom-left corner of the window.
- width and height specify the width and height of the window.

Units are in pixels.
The default value of this property depends on the resolution of your display. By default, the window is positioned in the center of the screen, with a width and height of 800 and 450 pixels, respectively.
Example: [100 100500 400]
Tunable: Yes

Data Types: double
IQDataInput - Type of input data
true (default) | false
Type of input data, specified as true or false. When true, the object assumes that the input consists of $I / Q$ sample data and further processing is required in the range, angle, or Doppler domains. When false, the object assumes that the data is response data that has already been processed.

Data Types: logical
ResponseUnits - Response units label
'db' (default)| 'magnitude'|'power'
Response units, specified as 'db', 'magnitude', or 'power'.
Data Types: char

## AngleLabel - Angle-axis label

'Angle (degrees)' (default)| character vector
Angle-axis label, specified as a character vector.
Example: 'Angle Span (degrees)'
Tunable: Yes

## Dependencies

To enable this property, set the IQDataInput to false.
Data Types: char

## DopplerLabel - Doppler-axis label

'Doppler Frequency (Hz)' (default)| character vector
Doppler-axis label, specified as a character vector.
Example: 'Doppler Frequency (kHz)'
Tunable: Yes

## Dependencies

To enable this property, set the IQDataInput to false.
Data Types: char

## SensorArray - Sensor array

phased. ULA array with default array properties (default) | Phased Array System Toolbox array System object

Sensor array, specified as a Phased Array System Toolbox array System object. See phased.ULA for the default values of a uniform linear array.
Example: phased.URA

## Dependencies

To enable this property, set the IQDataInput to true.

## PropagationSpeed - Signal propagation speed <br> physconst('LightSpeed') (default) | positive scalar

Signal propagation speed, specified as a positive scalar. The default value of this property is the speed of light. See physconst. Units are in meters/second.

## Example: 3e8

## Dependencies

To enable this property, set the IQDataInput property to true.
Data Types: double
OperatingFrequency - Operating frequency
300e6 (default) | positive scalar
Operating frequency, specified as a positive scalar. Units are in Hz .

## Dependencies

To enable this property, set the IQDataInput property to true.
Data Types: double
PRF - Pulse repetition frequency of input signal
1 (default) | positive scalar
Pulse repetition frequency of input signal, specified as a positive scalar. Units are in Hz .
Example: 1.4e3

## Dependencies

To enable this property, set the IQDataInput property to true.

## Data Types: double

## ElevationAngle - Elevation angle of response

0 (default) | scalar
Elevation angle at which to calculate the response, specified as a scalar. The elevation angle must lie in the interval from $-90^{\circ}$ to $90^{\circ}$, inclusive. Units are in degrees.
Example: 45.0

## Dependencies

To enable this property, set the IQDataInput property to true.
Data Types: double

## NumAngleSamples - Number of bins in angle span <br> 256 (default) | positive integer greater than two

Number of bins in the angle span at which to calculate the response, specified as a positive integer greater than two.

## Example: 256

## Dependencies

To enable this property, set the IQDataInput property to true.
Data Types: double
NumDopplerSamples - Number of Doppler bins
256 (default) | positive integer greater than two
Number of bins in the Doppler domain used to calculate angle-Doppler response, specified as a positive integer greater than two.

Example: 512

## Dependencies

To enable this property, set the IQDataInput property to true.
Data Types: double
NormalizeDoppler - Normalize Doppler
false (default) | true
Set this property to true to plot the angle-Doppler response at the normalized Doppler frequency. Set this property to false to plot the angle-Doppler response without normalizing the Doppler frequency.

## Dependencies

To enable this property, set the IQDataInput property to true.
Data Types: logical

## FrequencyUnits - Doppler frequency units

'Hz' (default) | 'kHz' | 'MHz'
Doppler frequency units, specified as 'Hz', 'kHz', or 'MHz'.

## Example: 'MHz'

## Dependencies

To enable this property, set the IQDataInput property to true and the NormalizedDoppler property to false.
Data Types: char

## Usage

## Syntax

```
scope(X,Ang,Dop)
scope(X)
```


## Description

scope ( $\mathrm{X}, \mathrm{Ang}, \mathrm{Dop}$ ) displays an angle-Doppler response map for the response data, scope, for direction azimuth angles, Ang, and Doppler shifts, Dop. This syntax applies when you set the IQDataInput to false.
scope ( X ) computes and displays the angle-Doppler response map of the I/Q data $X$. This syntax applies when you set the IQDataInput property to true.

## Input Arguments

## X - Input data

real-valued $P$-by- $Q$ matrix | complex-valued $P$-by- $Q$ matrix | complex-valued $L$-by-1 column vector
Input data, specified as a real-valued $P$-by- $Q$ or complex-valued $P$-by- $Q$ matrix. The processing of the data depends on the value of the IQDataInput property.

- When IQDataInput is true, $x$ consists of I/Q samples at fixed range of pulses or sweeps from multiple elements or subarrays. $P$ is the number of array elements. If SensorArray contains subarrays, $P$ is the number of subarrays. $Q$ is the number of pulses. The scope computes and displays the angle-Doppler response.

When x is a column vector, $L$ must be equal to an integer multiple of $P$.

- When IQDataInput is false, x consists of real-valued angle-Doppler response data such as the data produced by phased. AngleDopplerResponse. $P$ is the number of Doppler samples and $Q$ is the number of angle samples. Each row represents a Doppler value corresponding to an element of Dop. Each column represents an angle value corresponding to an element of the Ang vector. The scope serves only as a display of the angle-Doppler response.


## Ang - Azimuth angle grid values of response map

real-valued $Q$-by-1 column vector
Azimuth angle grid values of response map, specified as a real-valued $Q$-by-1 column vector. Ang contains the angle values corresponding to the columns of X .

## Dependencies

To enable this argument, set the IQInputData property to false.

## Data Types: double

## Dop - Doppler grid values of response map

real-valued $P$-by-1 column vector
Doppler grid values of response map, specified as a real-valued $P$-by-1 column vector. Dop contains the Doppler values corresponding to the rows of $X$.

## Dependencies

To enable this argument, set the IQInputData property to false.

```
Data Types: double
```


## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:
release(obj)

## Specific to Scope Objects

show Turn on visibility of scopes
hide Turn off visibility of scope
isVisible Visibility of scopes

## Common to All System Objects

step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object

## Examples

## View Target Response Using Angle-Doppler Scope

Calculate and visualize the angle-Doppler response at a single range cell of a collected data cube.
Load the I/Q data and analyze the 43th range cell.
load STAPExampleData;
x = shiftdim(STAPEx_ReceivePulse(43,:,:));
Create a scope object that processes I/Q data.

```
scope = phased.AngleDopplerScope( ...
    'IQDataInput', true, ...
    'Name','Angle-Doppler Scope', ...
    'Position',[560 375 560 420], ...
    'NormalizeDoppler',false, ...
    'ResponseUnits','db', ...
    'SensorArray',STAPEx_HArray, ...
    'OperatingFrequency',STAPEx_OperatingFrequency, ...
    'PropagationSpeed',STAPEx_PropagationSpeed, ...
    'PRF',STAPEx_PRF,'NumDopp\̄erSamples',512);
```

Compute and visualize the angle-Doppler response.
scope(x)



## More About

## Properties Applicable to I/Q Data

These properties are applicable when IQDataInput is true.

| Properties | Position |
| :--- | :--- |
| Name | SensorArray |
| ResponseUnits | OperatingFrequency |
| PropagationSpeed | NumDopplerSamples |
| NumAngleSamples | ElevationAngle |
| PRF | FrequencyUnits |
| NormalizeDoppler |  |

## Properties Applicable to Response Data

These properties are applicable when IQDataInput is false.

## Properties

| Name | Position |
| :--- | :--- |
| ResponseUnits | DopplerLabel |

## Properties

AngleLabel

## Version History

Introduced in R2019a

## See Also

show | hide |isVisible | phased.AngleDopplerResponse | phased.RangeAngleScope | phased.RangeDopplerScope

## hide

Package: phased
Turn off visibility of scope

## Syntax

hide(scope)

## Description

hide(scope) hides the display window of the scope System object.

## Input Arguments

```
scope - Scope system object
```

scope System object
Scope, specified as a scope System object such as RangeDopplerScope.

## Version History

Introduced in R2019a

## See Also

show |isVisible | phased.RangeAngleScope | phased.RangeDopplerScope | phased.AngleDopplerScope|phased.RTIScope|phased.DTIScope

## isVisible

Package: phased
Visibility of scopes

## Syntax

vis = isVisible(scope)

## Description

vis = isVisible(scope) returns the visibility of the scope System object.

## Input Arguments

## scope - Scope system object

scope System object
Scope, specified as a scope System object such as RangeDopplerScope.

## Output Arguments

vis - Visibility of scope
true |false
Visibility of scope, returned as true or false. When true, scope is visible. When false, scope is hidden.

Data Types: logical

## Version History

Introduced in R2019a

## See Also

show | hide | phased.RangeAngleScope | phased.RangeDopplerScope |
phased.AngleDopplerScope|phased.RTIScope|phased.DTIScope

## show

Package: phased
Turn on visibility of scopes

## Syntax

show(scope)

## Description

show (scope) shows the display window of the scope System object.

## Input Arguments

## scope - Scope system object

scope System object
Scope, specified as a scope System object such as RangeDopplerScope.

## Version History

Introduced in R2019a

## See Also <br> hide |isVisible |phased.RangeAngleScope | phased.RangeDopplerScope | phased.AngleDopplerScope|phased.RTIScope|phased.DTIScope

# phased.RangeDopplerResponse 

Package: phased
Range-Doppler response

## Description

The phased.RangeDopplerResponse System object calculates the filtered response to fast-time and slow-time data. or equivalently, range data, using either a matched filter or an FFT.

The input to the Doppler response object is a data cube. The organization of the data cube follows the Phased Array System Toolbox convention. The first dimension of the cube represents the fast-time samples or ranges of the received signals. The second dimension represents multiple channels such as sensors or beams. The third dimension, slow time, represent pulses. If the data contains only one channel or pulse, the data cube can contain fewer than three dimensions. Range processing operates along the first dimension of the cube. Doppler processing operates along the last dimension.

The output of the object is also a data cube with the same number of dimensions as the input. The first dimension contains range-processed data but its length can differ from the first dimension of the input. The last dimension contains Doppler processed data. Its length can differ from the last dimension of the input.

To compute the range-Doppler response:
1 Define and set up your phased.RangeDopplerResponse System object. See "Construction" on page 1-1333.

2 Call step to compute the range-Doppler response of the input signal according to the properties of phased.RangeDopplerResponse. The behavior of step is specific to each object in the toolbox.

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step $(o b j, x)$ and $y=o b j(x)$ perform equivalent operations.

## Construction

H = phased.RangeDopplerResponse creates a range-Doppler response System object, H. The object calculates the range-Doppler response of the input data.

H = phased.RangeDopplerResponse(Name, Value) creates a range-Doppler response object, H, with additional options specified by one or more Name, Value pair arguments. Name is a property name on page 1-1334, and Value is the corresponding value. Name must appear inside single quotes (' '). You can specify several name-value pair arguments in any order as Name1, Value1, ..., NameN, ValueN.

## Properties

## RangeMethod

Range processing method
Specify the method of range processing as 'Matched filter' or 'FFT'.

| 'Matched filter' | Algorithm applies a matched filter to the incoming signal. This <br> approach is common with pulsed signals, where the matched filter <br> is the time reverse of the transmitted signal. |
| :--- | :--- |
| 'FFT' | Algorithm performs range processing by applying an FFT to the <br> input signal. This approach is commonly used with FMCW and <br> linear FM pulsed signals. |

## Default: 'Matched filter'

## PropagationSpeed

Signal propagation speed
Specify the propagation speed of the signal, in meters per second, as a positive scalar. You can specify this property as single or double precision.

Default: Speed of light

## SampleRate

Sample rate
Specify the sample rate, in hertz, as a positive scalar. This property can be specified as single or double precision. The default value corresponds to 1 MHz .

Default: 1e6

## SweepSlope

FM sweep slope
Specify the slope of the linear FM sweeping, in hertz per second, as a scalar. The $x$ data you provide to step or plotResponse must correspond to sweeps having this slope. This property can be specified as single or double precision.

To enable this property, set the RangeMethod property to 'FFT '.
Default: 1e9

## DechirpInput

Option to dechirp input signal
Set this property to true to have the range-Doppler response object dechirp the input signal. Set this property to false to indicate that the input signal is already dechirped and no dechirp operation is necessary.

To enable this property, set the RangeMethod property to 'FFT'.
Default: false

## DecimationFactor

Decimation factor for dechirped signal
Specify the decimation factor for the dechirped signal as a positive integer. When processing FMCW signals, you can often decimate the dechirped signal to reduce the requirements on the analog-todigital converter.

To enable this property, set the RangeMethod property to ' FFT ' and the DechirpInput property to true. This property can be specified as single or double precision. The default value indicates no decimation.

## Default: 1

## RangeFFTLengthSource

Source of FFT length used in range processing
Specify how the object determines the FFT length used in range processing. Values of this property are:

| 'Auto' | The FFT length equals the number of rows of the input signal. |
| :--- | :--- |
| 'Property' | The RangeFFTLength property of this object specifies the FFT <br> length. |

To enable this property, set the RangeMethod property to ' FFT '.

## Default: 'Auto'

## RangeFFTLength

FFT length in range processing
Specify the FFT length in the range domain as a positive integer. This property can be specified as single or double precision.

To enable this property, set the RangeMethod property to 'FFT' and the RangeFFTLengthSource property to 'Property'.

## Default: 1024

## RangeWindow

Window for range weighting
Specify the window used for range processing using one of 'None', 'Hamming', 'Chebyshev', 'Hann', 'Kaiser', 'Taylor', or 'Custom'. If you set this property to 'Taylor', the generated Taylor window has four nearly constant sidelobes adjacent to the mainlobe.

To enable this property, set the RangeMethod property to 'FFT'.
Default: 'None'

## RangeSidelobeAttenuation

Sidelobe attenuation level for range processing
Specify the sidelobe attenuation level of a Kaiser, Chebyshev, or Taylor window in range processing as a positive scalar, in decibels. This property can be specified as single or double precision.

To enable this property, set the RangeMethod property to 'FFT' and the RangeWindow property to 'Kaiser', 'Chebyshev', or 'Taylor'.

## Default: 30

## CustomRangeWindow

User-defined window for range processing
Specify the user-defined window for range processing using a function handle or a cell array.
To enable this property, set the RangeMethod property to 'FFT' and the RangeWindow property to 'Custom'.

If CustomRangeWindow is a function handle, the specified function takes the window length as the input and generates appropriate window coefficients.

If CustomRangeWindow is a cell array, then the first cell must be a function handle. The specified function takes the window length as the first input argument, with other additional input arguments, if necessary. The function then generates appropriate window coefficients. The remaining entries in the cell array are the additional input arguments to the function, if any.

Default: @hamming

## ReferenceRangeCentered

Set reference range at center of range grid, specified as true or false. Setting this property to true enables you to set the reference range at the center of the range grid. Setting this property to false sets the reference range to the beginning of the range grid.

## Dependencies

To enable this property, set the RangeMethod to ' FFT ' .
Default: true

## ReferenceRange

Reference range of the range grid, specified as a nonnegative scalar.

- If you set the RangeMethod property to 'Matched filter', the reference range is set to the start of the range grid.
- If you set the RangeMethod property to ' $F F T$ ' , the reference range is determined by the ReferenceRangeCentered property.
- When you set the ReferenceRangeCentered property to true, the reference range is set to the center of the range grid.
- When you set the ReferenceRangeCentered property to false, the reference range is set to the start of the range grid.

This property can be specified as single or double precision. Units are in meters.
This property is tunable.
Example: 1000.0
Default: 0.0

## PRFSource

Source of pulse repetition frequency
Source of pulse repetition frequency, specified as

- 'Auto ' - You assume that the pulse repetition frequency (PRF) is the inverse of the duration of the input signal to the step method. Then the PRF equals the sample rate of the signal divided by the number of rows in the input signal.
- 'Property ' - specify the pulse repetition frequency using the PRF property.
- 'Input port ' - specify the PRF using an input argument of the step method.

Use the 'Property' or 'Input port' option when the pulse repetition frequency cannot be determined by the signal duration, as is the case with range-gated data.

Default: 'Auto'
PRF
Pulse repetition frequency of input signal
Pulse repetition frequency of the input signal, specified as a positive scalar. PRF must be less than or equal to the sample rate divided by the number of rows of the input signal to the step method. When the signal length is variable, use the maximum possible number of rows of the input signal instead. This property can be specified as single or double precision.

To enable this property, set the PRFSource property to 'Property ' .
Default: 10e3

## DopplerFFTLengthSource

Source of FFT length in Doppler processing
Specify how the object determines the FFT length in Doppler processing. Values of this property are:

| 'Auto' | The FFT length is equal to the number of rows of the input signal. |
| :--- | :--- |
| 'Property ' | The DopplerFFTLength property of this object specifies the FFT <br> length. |

To enable this property, set the RangeMethod property to ' $F F T$ '.

## Default: 'Auto'

## DopplerFFTLength

FFT length for Doppler processing

FFT length for Doppler processing, specified as a positive integer. This property can be specified as single or double precision.

To enable this property, set the RangeMethod property to 'FFT ' and the DopplerFFTLengthSource property to 'Property'.

Default: 1024
DopplerWindow
Window for Doppler weighting
Specify the window used for Doppler processing using one of 'None', 'Hamming', 'Chebyshev', 'Hann', 'Kaiser', 'Taylor', or 'Custom'. If you set this property to 'Taylor', the generated Taylor window has four nearly constant sidelobes adjacent to the mainlobe.

To enable this property, set the RangeMethod property to ' $F F T$ '.
Default: 'None'

## DopplerSidelobeAttenuation

Sidelobe attenuation level for Doppler processing
Specify the sidelobe attenuation level of a Kaiser, Chebyshev, or Taylor window in Doppler processing as a positive scalar, in decibels. This property can be specified as single or double precision.

To enable this property, set the RangeMethod property to 'FFT' and the DopplerWindow property to 'Kaiser', 'Chebyshev', or 'Taylor'.

Default: 30

## CustomDopplerWindow

User-defined window for Doppler processing
Specify the user-defined window for Doppler processing using a function handle or a cell array..
If CustomDopplerWindow is a function handle, the specified function takes the window length as the input and generates appropriate window coefficients.

If CustomDopplerWindow is a cell array, then the first cell must be a function handle. The specified function takes the window length as the first input argument, with other additional input arguments, if necessary. The function then generates appropriate window coefficients. The remaining entries in the cell array are the additional input arguments to the function, if any.

To enable this property, set the RangeMethod property to 'FFT' and the DopplerWindow property to 'Custom'

Default: @hamming

## DopplerOutput

Doppler domain output

Specify the Doppler domain output as 'Frequency ' or 'Speed '. The Doppler domain output is the DOP_GRID argument of step.

| ' Frequency ' | DOP_GRID is the Doppler shift, in hertz. |
| :--- | :--- |
| 'Speed ' | DOP_GRID is the radial speed corresponding to the Doppler shift, in <br> meters per second. |

## Default: 'Frequency' <br> OperatingFrequency

Signal carrier frequency
Specify the carrier frequency, in hertz, as a scalar. The default value of this property corresponds to 300 MHz . This property can be specified as single or double precision.

To enable this property, set the DopplerOutput property to 'Speed '
Default: 3e8

## MaximumNumInputSamplesSource

Source of maximum number of samples
The source of the maximum number of samples of the input signal, specified as 'Auto' or 'Property'. When you set this property to 'Auto' ' the object automatically allocates enough memory to buffer the first input signal. When you set this property to 'Property', specify the maximum number of samples in the input signal using the MaximumNumInputSamples property. Any input signal longer than that value is truncated.

## Default: 'Auto'

## MaximumNumInputSamples

Maximum number of input signal samples
Maximum number of samples in the input signal, specified as a positive integer. This property limits the size of the input signal. Any input signal longer than this value is truncated. The input signal is the first argument to the step method. The number of samples is the number of rows in the input. This property can be specified as single or double precision.

To enable this property, set the RangeMethod property to 'Matched filter' and set the MaximumNumInputSamplesSource property to 'Property'.

Default: 100

## Methods

plotResponse
Plot range-Doppler response
step
Calculate range-Doppler response

## Common to All System Objects

```
release Allow System object property value changes
```


## Examples

## Range-Doppler Response Using Matched Filter

Compute the range-doppler response of a pulsed radar signal using a matched filter.
Load data for a pulsed radar signal. The signal includes three target returns. Two targets are approximately 2000 m away, while the third is approximately 3500 m away. In addition, two of the targets are stationary relative to the radar. The third is moving away from the radar at about $100 \mathrm{~m} / \mathrm{s}$.

```
load RangeDopplerExampleData;
```

Create a range-Doppler response object.

```
response = phased.RangeDopplerResponse('DopplerFFTLengthSource','Property', ...
    'DopplerFFTLength',RangeDopplerEx MF NFFTDOP,
    'SampleRate',RangeDopplerEx_MF_Fs,'DopplerOutput','Speed', ...
    'OperatingFrequency',RangeDopplerEx_MF_Fc);
```

Calculate the range-Doppler response.

```
[resp,rng_grid,dop_grid] = response(RangeDopplerEx_MF_X, ...
    RangeDopplerEx_MF_Coeff);
```

Plot the range-Doppler response.

```
imagesc(dop_grid,rng_grid,mag2db(abs(resp)));
xlabel('Speed (m/s)');
ylabel('Range (m)');
title('Range-Doppler Map');
```



## Range-Doppler Response of FMCW Signal

Compute the range-Doppler response of an FMCW signal using an FFT.
Load data for an FMCW signal that has not been dechirped. The signal contains the return from a target about 2200 m away. The signal has a normalized Doppler frequency of approximately -0.36 relative to the radar.
load RangeDopplerExampleData;
Create a range-Doppler response object.
hrdresp $=$ phased.RangeDopplerResponse(...
'RangeMethod', 'FFT', ...
'PropagationSpeed' , RangeDopplerEx_Dechirp_PropSpeed,...
'SampleRate', RangeDopplerEx_Dechirp_Fs,...
'DechirpInput', true,...
'SweepSlope' , RangeDopplerEx_Dechirp_SweepSlope);
Plot the range-Doppler response.
plotResponse(hrdresp,...
RangeDopplerEx_Dechirp_X,RangeDopplerEx_Dechirp_Xref,...
'Unit','db','NormalizeDoppler',true)


## Estimate Doppler and Range with Specified PRF

Estimate the Doppler and range responses for three targets. Two targets are approximately 2000 m away, while the third is approximately 3500 m away. In addition, two of the targets are stationary relative to the radar. The third is moving away from the radar at about $100 \mathrm{~m} / \mathrm{s}$. Specify the pulse repetition frequency.

Load data for a pulsed radar signal.
load RangeDopplerExampleData;
Create a range-Doppler response object. Set the PRF to 25 kHz .

```
response = phased.RangeDopplerResponse('DopplerFFTLengthSource','Property', ...
    'DopplerFFTLength',RangeDopplerEx_MF_NFFTDOP,'SampleRate', ...
    RangeDopplerEx_MF_Fs,'DopplerOutput','Speed','OperatingFrequency', ...
    RangeDopplerEx_MF_Fc,'PRFSource','Property','PRF',25.0e3);
```

Calculate the range-Doppler response.
[resp,rng_grid,dop_grid] = response(RangeDopplerEx_MF_X, ...
RangeDopplerEx_MF_Coeff);
Plot the range-Doppler response.

```
plotResponse(response,RangeDopplerEx_MF_X,RangeDopplerEx_MF_Coeff,'Unit','db')
```



## Algorithms

## Response Algorithm

The phased.RangeDopplerResponse object generates a response as follows:
1 Processes the input signal in the fast-time dimension using either a matched filter or dechirp/FFT operation.
2 Processes the input signal in the pulse dimension using an FFT.
The decimation algorithm uses a 30th order FIR filter generated by firl(30,1/R), where $R$ is the value of the DecimationFactor property.

## Data Precision

This System object supports single and double precision for input data, properties, and arguments. If the input data X is single precision, the output data is single precision. If the input data X is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

## Version History

Introduced in R2012b

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:

- The CustomRangeWindow and CustomDopplerWindow properties are not supported.
- The plotResponse method is not supported.
- See "System Objects in MATLAB Code Generation" (MATLAB Coder).

This System object supports single and double precision for input data, properties, and arguments. If the input data X is single precision, the output data is single precision. If the input data X is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

## See Also

## Functions

bw2 range | fir1|chebwin | dechirp|hann | hamming | kaiser | taylorwin | rangeangle

```
Objects
phased.RangeAngleResponse | phased.RangeResponse| phased.AngleDopplerResponse|
phased.MatchedFilter|phased.DopplerEstimator|phased.RangeEstimator|
phased.CFARDetector| phased.CFARDetector2D
```


## Topics

"Automotive Adaptive Cruise Control Using FMCW Technology" (Radar Toolbox)
"Radar Data Cube Concept"

## plotResponse

System object: phased. RangeDopplerResponse
Package: phased
Plot range-Doppler response

## Syntax

```
plotResponse(H,x)
plotResponse(H,x,xref)
plotResponse(H,x,coeff)
plotResponse(___,Name,Value)
hPlot = plotResponse(____)
```


## Description

plotResponse ( $H, x$ ) plots the range-Doppler response of the input signal, $x$, in decibels. This syntax is available when you set the RangeMethod property to 'FFT' and the DechirpInput property to false.
plotResponse( $\mathrm{H}, \mathrm{x}, \mathrm{xref}$ ) plots the range-Doppler response after performing a dechirp operation on x using the reference signal, xref. This syntax is available when you set the RangeMethod property to 'FFT' and the DechirpInput property to true.
plotResponse ( $\mathrm{H}, \mathrm{x}$, coeff) plots the range-Doppler response after performing a matched filter operation on $x$ using the matched filter coefficients in coeff. This syntax is available when you set the RangeMethod property to 'Matched filter'.
plotResponse( $\qquad$ ,Name, Value) plots the angle-Doppler response with additional options specified by one or more Name, Value pair arguments.
hPlot = plotResponse( $\qquad$ ) returns the handle of the image in the figure window, using any of the input arguments in the previous syntaxes.

## Input Arguments

## H

Range-Doppler response object.
x
Input data. Specific requirements depend on the syntax:

- In the syntax plotResponse $(H, x)$, each column of the matrix $x$ represents a dechirped signal from one frequency sweep. The function assumes all sweeps in $x$ are consecutive.
- In the syntax plotResponse ( $H, x, x r e f$ ), each column of the matrix $x$ represents a signal from one frequency sweep. The function assumes all sweeps in $x$ are consecutive and have not been dechirped yet.
- In the syntax plotResponse(H,x, coeff), each column of the matrix $x$ represents a signal from one pulse. The function assumes all pulses in x are consecutive.

In the case of an FMCW waveform with a triangle sweep, the sweeps alternate between positive and negative slopes. However, phased. RangeDopplerResponse is designed to process consecutive sweeps of the same slope. To apply phased.RangeDopplerResponse for a triangle-sweep system, use one of the following approaches:

- Specify a positive SweepSlope property value, with x corresponding to upsweeps only. In the plot, change the tick mark labels on the horizontal axis to reflect that the Doppler or speed values are half of what the plot shows by default.
- Specify a negative SweepSlope property value, with x corresponding to downsweeps only. In the plot, change the tick mark labels on the horizontal axis to reflect that the Doppler or speed values are half of what the plot shows by default.

You can specify this argument as single or double precision.

## xref

Reference signal, specified as a column vector having the same number of rows as x . You can specify this argument as single or double precision.
coeff
Matched filter coefficients, specified as a column vector. You can specify this argument as single or double precision.

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## NormalizeDoppler

Set this value to true to normalize the Doppler frequency. Set this value to false to plot the rangeDoppler response without normalizing the Doppler frequency. This parameter applies when you set the DopplerOutput property of H to 'Frequency '.

Default: false

## Unit

The unit of the plot. Valid values are 'db', 'mag', and 'pow'.
Default: 'db'

## Examples

## Range-Doppler Response of FMCW Signal

Compute the range-Doppler response of an FMCW signal using an FFT.

Load data for an FMCW signal that has not been dechirped. The signal contains the return from a target about 2200 m away. The signal has a normalized Doppler frequency of approximately -0.36 relative to the radar.

```
load RangeDopplerExampleData;
```

Create a range-Doppler response object.

```
hrdresp = phased.RangeDopplerResponse(...
    'RangeMethod','FFT',...
    'PropagationSpeed ',RangeDopplerEx_Dechirp_PropSpeed,...
    'SampleRate',RangeDopplerEx_Dechirp_Fs,...
    'DechirpInput',true,...
    'SweepSlope',RangeDopplerEx_Dechirp_SweepSlope);
```

Plot the range-Doppler response.
plotResponse(hrdresp,...
RangeDopplerEx_Dechirp_X,RangeDopplerEx_Dechirp_Xref,...
'Unit','db','NormalizeDoppler',true)


## See Also

## Topics

"Automotive Adaptive Cruise Control Using FMCW Technology" (Radar Toolbox)

## step

System object: phased. RangeDopplerResponse
Package: phased
Calculate range-Doppler response

## Syntax

[resp,rnggrid, dopgrid] $=\operatorname{step}(H, x)$
[resp,rnggrid,dopgrid] = step(H,x,xref)
[resp,rnggrid,dopgrid] = step(H,x,coeff)
[resp,rnggrid,dopgrid] = step(H, __ , prf)

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step (obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.
[resp,rnggrid,dopgrid] = step ( $\mathrm{H}, \mathrm{x}$ ) calculates the range-Doppler response of the input signal, $x$. resp is the complex range-Doppler response. rnggrid and dopgrid provide the range samples and Doppler samples, respectively, at which the range-Doppler response is evaluated. This syntax is available when you set the RangeMethod property to 'FFT' and the DechirpInput property to false. This syntax is most commonly used with FMCW signals.
[resp,rnggrid,dopgrid] = step( $\mathrm{H}, \mathrm{x}, \mathrm{xref}$ ) uses xref as the reference signal to dechirp x . This syntax is available when you set the RangeMethod property to ' $F F T$ ' and the DechirpInput property to true. This syntax is most commonly used with FMCW signals, where the reference signal is typically the transmitted signal.
[resp,rnggrid,dopgrid] = step(H,x,coeff) uses coeff as the matched filter coefficients. This syntax is available when you set the RangeMethod property to 'Matched filter'. This syntax is most commonly used with pulsed signals, where the matched filter is the time reverse of the transmitted signal.
[resp,rnggrid,dopgrid] = step(H, , prf) uses prf as the pulse repetition frequency. These syntaxes are available when you set the PRFSource property to 'Input port'. This syntax is most commonly used with pulsed signals, where the matched filter is the time reverse of the transmitted signal.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## H

Range-Doppler response System object

## x

Input data, specified as a complex-valued $K$-by- $L$ matrix or $K$-by- $N$-by- $L$ array where

- $K$ denotes the number of fast-time samples.
- $N$ denotes the number of channels such as beams or sensors. When $N$ is one, only a single data channel is present.
- $L$ denotes the number of pulses for matched-filter processing and the number of sweeps for FFT processing.

Specific requirements depend on the syntax:

- In the syntax step $(H, x)$, each column of $x$ represents a dechirped signal from one frequency sweep. The function assumes all sweeps in $x$ are consecutive.
- In the syntax $\operatorname{step}(H, x, x r e f)$, each column of $x$ represents a signal from one frequency sweep. The function assumes all sweeps in $x$ are consecutive and are not dechirped.
- In the syntax step ( $H, x$, coeff), each column of the matrix $x$ represents a signal from one pulse. The function assumes all pulses in x are consecutive.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

In the case of an FMCW waveform with a triangle sweep, the sweeps alternate between positive and negative slopes. However, phased. RangeDopplerResponse is designed to process consecutive sweeps of the same slope. To apply phased.RangeDopplerResponse for a triangle-sweep system, use one of the following approaches:

- Specify a positive SweepSlope property value, with x corresponding to upsweeps only. After obtaining the Doppler or speed values, divide them by 2.
- Specify a negative SweepSlope property value, with x corresponding to downsweeps only. After obtaining the Doppler or speed values, divide them by 2.

You can specify this argument as single or double precision.

## xref

Reference signal, specified as a column vector having the same number of rows as $x$. You can specify this argument as single or double precision.

## coeff

Matched filter coefficients, specified as a column vector. You can specify this argument as single or double precision.
prf
Pulse repetition frequency, specified as a positive scalar. prf must be less than or equal to the sample rate specified in the SampleRate property divided by the length of the first dimension of the input signal, $x$. You can specify this argument as single or double precision.

To enable this argument, set the PRFSource property to 'Input port'.

## Output Arguments

## resp

Range-Doppler response of $x$, returned as a complex-valued $M$-by- $P$ matrix or a $M$-by- $N$-by- $P$ array. The values of $P$ and $M$ depend on the syntax. $N$ has the same value as for the input argument, $x$.

| Syntax | Values of $\boldsymbol{M}$ and $P$ |
| :---: | :---: |
| step(H, x) | If you set the RangeFFTLength property to 'Auto',$M=K$, the length of the first dimension of $x$. Otherwise, $M$ equals the value of the RangeFFTLength property. <br> If you set the DopplerFFTLength property to 'Auto',$P=L$, the length of the last dimension of $x$. Otherwise, $P$ equals the value of the DopplerFFTLength property. |
| step(H,x,xref) | $M$ is the quotient of the length of the first dimension of $x$ divided by the value of the DecimationFactor property. <br> If you set the DopplerFFTLength property to 'Auto ',$P=L$, the length of the last dimension of $x$. Otherwise, $P$ equals the value of the DopplerFFTLength property. |
| step( $\mathrm{H}, \mathrm{x}, \mathrm{coeff}$ ) | $M$ is the number of rows of $x$. <br> If you set the DopplerFFTLength property to 'Auto ',$P=L$, the length of the last dimension of $x$. Otherwise, $P$ equals the value of the DopplerFFTLength property. |

## rnggrid

Range samples at which the range-Doppler response is evaluated. rnggrid is a column vector of length $M$.

## dopgrid

Doppler samples or speed samples at which the range-Doppler response is evaluated. dopgrid is a column vector of length $P$. Whether dopgrid contains Doppler or speed samples depends on the DopplerOutput property of H.

## Examples

## Range-Doppler Response Using Matched Filter

Compute the range-doppler response of a pulsed radar signal using a matched filter.
Load data for a pulsed radar signal. The signal includes three target returns. Two targets are approximately 2000 m away, while the third is approximately 3500 m away. In addition, two of the targets are stationary relative to the radar. The third is moving away from the radar at about $100 \mathrm{~m} / \mathrm{s}$.

```
load RangeDopplerExampleData;
```

Create a range-Doppler response object.

```
response = phased.RangeDopplerResponse('DopplerFFTLengthSource','Property', ...
    'DopplerFFTLength',RangeDopplerEx_MF_NFFTDOP, ...
    'SampleRate',RangeDopplerEx_MF_Fs,'DōpplerOutput','Speed', ...
    'OperatingFrequency',RangeDopplerEx_MF_Fc);
```

Calculate the range-Doppler response.

```
[resp,rng_grid,dop_grid] = response(RangeDopplerEx_MF_X, ...
    RangeD
```

Plot the range-Doppler response.

```
imagesc(dop_grid,rng_grid,mag2db(abs(resp)));
xlabel('Speed (m/s)');
ylabel('Range (m)');
title('Range-Doppler Map');
```



## Estimate Doppler and Range from Range-Doppler Response

Estimate the Doppler and range values of a single target from the range-Doppler response.
Load data for an FMCW signal that has not yet been dechirped. The signal contains the return from one target.
load RangeDopplerExampleData;
Create a range-Doppler response object.
hrdresp = phased.RangeDopplerResponse(...
'RangeMethod', 'FFT', . . .
'PropagationSpeed ',RangeDopplerEx_Dechirp_PropSpeed,...
'SampleRate', RangeDopplerEx_Dechirp_Fs,...
'DechirpInput',true,...
'SweepSlope' , RangeDopplerEx_Dechirp_SweepSlope);
Obtain the range-Doppler response data.
[resp,rng_grid,dop_grid] = step(hrdresp,...
RangeDopplerEx_Dechirp_X,RangeDopplerEx_Dechirp_Xref);
Estimate the range and Doppler by finding the location of the maximum response.

```
[x_temp,idx_temp] = max(abs(resp));
[~,dop_idx] = max(x_temp);
rng_idx = idx_temp(\overline{dop_idx);}
dop_est = dop_grid(dop_idx)
dop_est = -712.8906
rng_est = rng_grid(rng_idx)
rng_est = 2250
```

The target is approximately 2250 meters away, and is moving fast enough to cause a Doppler shift of approximately -713 Hz .

# phased.RangeEstimator 

Package: phased

Range estimation

## Description

The phased.RangeEstimator System object estimates the ranges of targets. Input to the estimator consists of a range-response or range-Doppler response data cube, and detection locations from a detector. When information about clusters of detections is available, the ranges are computed using cluster information. Clustering associates multiple detections into one extended detection.

To compute the detections for a range-response or range-Doppler cube:
1 Define and set up a range estimator using the "Construction" on page 1-1354 procedure that follows.
2 Call the step method to compute the range, using the properties you specify for the phased.RangeEstimator System object.

Note Instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, x) and y = obj $(x)$ perform equivalent operations.

## Construction

estimator $=$ phased.RangeEstimator creates a range estimator System object, estimator.
estimator = phased.RangeEstimator(Name, Value) creates a System object, estimator, with each specified property Name set to the specified Value. You can specify additional name and value pair arguments in any order as (Name1, Value1,...,NameN, ValueN).

## Properties

## NumEstimatesSource - Source of number of range estimates to report <br> 'Auto ' (default)|'Property'

Source of the number of range estimates to report, specified as 'Auto' or 'Property'.
If you set this property to 'Auto ', the number of reported estimates is determined from the number of columns in the detidx input to the step method. If cluster IDs are provided, the number of estimates is determined from the number of unique cluster IDs in the clusterids input to the step method.

If you set this property to 'Property', the number of reported estimates is obtained from the value of the NumEstimates property.
Data Types: char

## NumEstimates - Maximum number of estimates

## 1 (default) positive integer

The maximum number of range estimates to report, specified as a positive integer. The number of requested estimates can be greater than the number of columns in the detidx argument or the number of unique IDs in the clusterids argument of the step method. In that case, the remainder is filled with NaN .

## Dependencies

To enable this property, set the NumEstimatesSource property to 'Property'.
Data Types: single | double

## ClusterInputPort - Accept cluster IDs as input <br> false (default) | true

Option to accept cluster IDs as an input argument to the step method, specified as false or true. Setting this property to true enables the clusterids input argument.

## Data Types: logical

## VarianceOutputPort - Output variance for range estimates

false (default) | true
Option to enable output of range estimate variances, specified as false or true. Range variances are returned by the rngvar output argument of the step method.
Data Types: logical

## RMSResolution - Root-mean-square range resolution

1.0 (default) | positive scalar

Root-mean-square range resolution of the detection, specified as a positive scalar. The value of the RMSResolution must have the same units as the rangegrid input argument of the step method.

## Dependencies

To enable this property, set the value of the Variance0utputPort property to true.
Data Types: single | double

## NoisePowerSource - Source of noise power values <br> 'Property' (default)|'Input port'

Source of noise power values, specified as 'Property ' or 'Input port'. Noise power is used to compute range estimation variance and SNR. If you set this property to 'Property', the value of the NoisePower property represents the noise power at the detection locations. If you set this property to 'Input port', you can specify noise power using the noisepower input argument, of the step method.

Data Types: char
NoisePower - Noise power
1.0 (default) | positive scalar

Constant noise power value over the range-response or range-Doppler response data cube, specified as a positive real scalar. Noise power units are linear. The same noise power value is applied to all detections.

## Dependencies

To enable this property, set the value of the VarianceOutputPort property to true and set NoisePowerSource to 'Property'.

Data Types: single | double

## Methods

step Estimate target range

## Common to All System Objects

| release | Allow System object property value changes |
| :--- | :--- | :--- |

## Examples

## Estimate Range and Speed of Three Targets

To estimate the range and speed of three targets, create a range-Doppler map using the phased.RangeDopplerResponse System object ${ }^{\text {TM }}$. Then use the phased.RangeEstimator and phased.DopplerEstimator System objects to estimate range and speed. The transmitter and receiver are collocated isotropic antenna elements forming a monostatic radar system.

The transmitted signal is a linear FM waveform with a pulse repetition interval (PRI) of $7.0 \mu \mathrm{~s}$ and a duty cycle of $2 \%$. The operating frequency is 77 GHz and the sample rate is 150 MHz .

```
fs = 150e6;
c = physconst('LightSpeed');
fc = 77.0e9;
pri = 7e-6;
prf = 1/pri;
```

Set up the scenario parameters. The transmitter and receiver are stationary and located at the origin. The targets are 500,530, and 750 meters from the radar along the $x$-axis. The targets move along the $x$-axis at speeds of $-60,20$, and $40 \mathrm{~m} / \mathrm{s}$. All three targets have a nonfluctuating radar cross-section (RCS) of 10 dB . Create the target and radar platforms.

```
Numtgts = 3;
tgtpos = zeros(Numtgts);
tgtpos(1,:) = [500 530 750];
tgtvel = zeros(3,Numtgts);
tgtvel(1,:) = [-60 20 40];
tgtrcs = db2pow(10)*[1 1 1];
tgtmotion = phased.Platform(tgtpos,tgtvel);
target = phased.RadarTarget('PropagationSpeed',c,'OperatingFrequency',fc, ...
    'MeanRCS',tgtrcs);
radarpos = [0;0;0];
radarvel = [0;0;0];
radarmotion = phased.Platform(radarpos,radarvel);
```

Create the transmitter and receiver antennas.

```
txantenna = phased.IsotropicAntennaElement;
rxantenna = clone(txantenna);
```

Set up the transmitter-end signal processing. Create an upsweep linear FM signal with a bandwidth of one half the sample rate. Find the length of the PRI in samples and then estimate the rms bandwidth and range resolution.

```
bw = fs/2;
waveform = phased.LinearFMWaveform('SampleRate',fs, ...
    'PRF',prf,'OutputFormat','Pulses','NumPulses',1,'SweepBandwidth',fs/2, ...
    'DurationSpecification','Duty cycle','DutyCycle',0.02);
sig = waveform();
Nr = length(sig);
bwrms = bandwidth(waveform)/sqrt(12);
rngrms = c/bwrms;
```

Set up the transmitter and radiator System object properties. The peak output power is 10 W and the transmitter gain is 36 dB .

```
peakpower = 10;
txgain = 36.0;
transmitter = phased.Transmitter( ...
    'PeakPower',peakpower, ...
    'Gain',txgain, ...
    'InUseOutputPort',true);
radiator = phased.Radiator( ...
    'Sensor',txantenna,...
    'PropagationSpeed',c,...
    'OperatingFrequency',fc);
```

Set up the free-space channel in two-way propagation mode.

```
channel = phased.FreeSpace( ...
    'SampleRate',fs, ...
    'PropagationSpeed',c, ...
    'OperatingFrequency',fc, ...
    'TwoWayPropagation',true);
```

Set up the receiver-end processing. Set the receiver gain and noise figure.

```
collector = phased.Collector( ...
    'Sensor',rxantenna, ...
    'PropagationSpeed',c, ...
    'OperatingFrequency',fc);
rxgain = 42.0;
noisefig = 1;
receiver = phased.ReceiverPreamp( ...
    'SampleRate',fs, ...
    'Gain',rxgain, ...
    'NoiseFigure',noisefig);
```

Loop over the pulses to create a data cube of 128 pulses. For each step of the loop, move the target and propagate the signal. Then put the received signal into the data cube. The data cube contains the received signal per pulse. Ordinarily, a data cube has three dimensions where the last dimension corresponds to antennas or beams. Because only one sensor is used, the cube has only two dimensions.

The processing steps are:
1 Move the radar and targets.
2 Transmit a waveform.
3 Propagate the waveform signal to the target.
4 Reflect the signal from the target.
5 Propagate the waveform back to the radar. Two-way propagation enables you to combine the return propagation with the outbound propagation.

6 Receive the signal at the radar.
7 Load the signal into the data cube.
Np = 128;
dt = pri;
cube $=$ zeros(Nr,Np);
for $n=1: N p$
[sensorpos,sensorvel] = radarmotion(dt);
[tgtpos,tgtvel] = tgtmotion(dt);
[tgtrng,tgtang] = rangeangle(tgtpos,sensorpos);
sig = waveform();
[txsig,txstatus] = transmitter(sig);
txsig = radiator(txsig,tgtang);
txsig = channel(txsig, sensorpos,tgtpos,sensorvel,tgtvel);
tgtsig = target(txsig);
rxcol = collector(tgtsig,tgtang);
rxsig = receiver(rxcol);
cube(:,n) = rxsig;
end
Display the data cube containing signals per pulse.

```
imagesc([0:(Np-1)]*pri*1e6,[0:(Nr-1)]/fs*1e6,abs(cube))
xlabel('Slow Time {\mu}s')
ylabel('Fast Time {\mu}s')
axis xy
```



Create and display the range-Doppler image for 128 Doppler bins. The image shows range vertically and speed horizontally. Use the linear FM waveform for match filtering. The image is here is the range-Doppler map.

```
ndop = 128;
rangedopresp = phased.RangeDopplerResponse('SampleRate',fs, ...
    'PropagationSpeed',c,'DopplerFFTLengthSource','Property', ...
    'DopplerFFTLength',ndop,'DopplerOutput','Speed', ...
    'OperatingFrequency',fc);
matchingcoeff = getMatchedFilter(waveform);
[rngdopresp,rnggrid,dopgrid] = rangedopresp(cube,matchingcoeff);
imagesc(dopgrid,rnggrid,10*log10(abs(rngdopresp)))
xlabel('Closing Speed (m/s)')
ylabel('Range (m)')
axis xy
```



Because the targets lie along the positive $x$-axis, positive velocity in the global coordinate system corresponds to negative closing speed. Negative velocity in the global coordinate system corresponds to positive closing speed.

Estimate the noise power after matched filtering. Create a constant noise background image for simulation purposes.

```
mfgain = matchingcoeff'*matchingcoeff;
dopgain = Np;
noisebw = fs;
noisepower = noisepow(noisebw,receiver.NoiseFigure,receiver.ReferenceTemperature);
noisepowerprc = mfgain*dopgain*noisepower;
noise = noisepowerprc*ones(size(rngdopresp));
Create the range and Doppler estimator objects.
```

```
rangeestimator = phased.RangeEstimator('NumEstimatesSource','Auto', ...
```

rangeestimator = phased.RangeEstimator('NumEstimatesSource','Auto', ...
'VarianceOutputPort',true,'NoisePowerSource','Input port', ...
'VarianceOutputPort',true,'NoisePowerSource','Input port', ...
'RMSResolution',rngrms);
'RMSResolution',rngrms);
dopestimator = phased.DopplerEstimator('VarianceOutputPort',true, ...
dopestimator = phased.DopplerEstimator('VarianceOutputPort',true, ...
'NoisePowerSource','Input port','NumPulses',Np);

```
    'NoisePowerSource','Input port','NumPulses',Np);
```

Locate the target indices in the range-Doppler image. Instead of using a CFAR detector, for simplicity, use the known locations and speeds of the targets to obtain the corresponding index in the rangeDoppler image.

```
detidx = NaN(2,Numtgts);
tgtrng = rangeangle(tgtpos,radarpos);
```

```
tgtspd = radialspeed(tgtpos,tgtvel,radarpos,radarvel);
tgtdop = 2*speed2dop(tgtspd,c/fc);
for m = 1:numel(tgtrng)
    [~,iMin] = min(abs(rnggrid-tgtrng(m)));
    detidx(1,m) = iMin;
    [~,iMin] = min(abs(dopgrid-tgtspd(m)));
    detidx(2,m) = iMin;
end
```

Find the noise power at the detection locations.

```
ind = sub2ind(size(noise),detidx(1,:),detidx(2,:));
```

Estimate the range and range variance at the detection locations. The estimated ranges agree with the postulated ranges.

```
[rngest,rngvar] = rangeestimator(rngdopresp,rnggrid,detidx,noise(ind))
rngest = 3×1
```

    499.7911
    529.8380
    750.0983
    rngvar = $3 \times 1$
$10^{-4} \times$
0.0273
0.0276
0.2094

Estimate the speed and speed variance at the detection locations. The estimated speeds agree with the predicted speeds.

```
[spdest,spdvar] = dopestimator(rngdopresp,dopgrid,detidx,noise(ind))
spdest = 3\times1
```

    60.5241
    - 19.6167
    -39. 5838
    spdvar = 3×1
$10^{-5} \times$
0.0806
0.0816
0.6188

## More About

## Date Cube

One input to the range estimator is a response data cube. To create a response data cube, use the phased.RangeDopplerResponse or phased.RangeResponse System objects. The first dimension
of the cube represents the range. Only the first dimension is used to estimate range. All other dimensions are ignored. To interpret the detection location, you must pass in the rnggrid vector corresponding to the range values along this dimension. See "Radar Data Cube Concept".

## Algorithms

## Range Estimation

The phased. RangeEstimator System object estimates the range of a detection by following these steps:

1 Input a range-processed response data cube obtained from either the phased.RangeResponse or phased.RangeDopplerResponse System object. The first dimension of the cube represents the fast-time or equivalent range of the returned signal samples. Only this dimension is used to estimate detection range. All others are ignored.
2 Input a matrix of detection indices that specify the location of detections in the data cube. Each column denotes a separate detection. The row entries designate indices into the data cube. You can obtain detection indices as an output of the phased. CFARDetector or phased. CFARDetector2D detectors. To return these indices, set the OutputFormat property of either CFAR detector to 'Detection index'.
3 Optionally input a row vector of cluster IDs. This vector is equal in length to the number of detections. Each element of this vector assigns an ID to a corresponding detection. To form clusters of detections, the same ID can be assigned to more than one detection. To enable this option, set the ClusterInputPort property to true.
4 When ClusterInputPort is false, the object computes the range for each detection. The algorithm finds the response values at the detection location and at two adjacent indices in the cube along the range dimension. Then, the algorithm fits a quadratic curve to the magnitudes of the range response at these three locations and finds the location of the peak. When detections occur at the first or last sample in the range dimension, the range response is estimated from a two-point centroid. The estimation is at the location of the detection index and at the sample adjacent to the detection index.

When ClusterInputPort is true, the object computes range for each cluster. The algorithm finds the indices of the largest response value in the cluster and fits a quadratic formula to that detection in the same way as for individual detections.
5 Convert the fractional index values of the fitted peak locations to range. To convert the indices, choose appropriate units for the rnggrid input argument of the step method. You can use values for rnggrid obtained from either the phased. RangeResponse or phased.RangeDopplerResponse System objects.

The object computes the estimated range variance using the Ziv-Zakai bound.

## Data Precision

This System object supports single and double precision for input data, properties, and arguments. If the input data X is single precision, the output data is single precision. If the input data X is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

## Version History

Introduced in R2017a

## References

[1] Richards, M. Fundamentals of Radar Signal Processing. 2nd ed. McGraw-Hill Professional Engineering, 2014.
[2] Richards, M., J. Scheer, and W. Holm. Principles of Modern Radar: Basic Principles. SciTech Publishing, 2010.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\text {TM }}$.
Usage notes and limitations:

- See "System Objects in MATLAB Code Generation" (MATLAB Coder).
- This System object supports single and double precision for input data, properties, and arguments. If the input data $X$ is single precision, the output data is single precision. If the input data $X$ is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.


## See Also

## Functions

rangeangle | bw2 range

## Objects

phased.DopplerEstimator|phased.RangeResponse | phased.RangeDopplerResponse|
phased.CFARDetector|phased.CFARDetector2D

## Topics

"Radar Data Cube Concept"

## step

System object: phased.RangeEstimator
Package: phased
Estimate target range

## Syntax

```
rngest = step(estimator,resp,rnggrid,detidx)
[rngest,rngvar] = step(estimator,resp,rnggrid,detidx,noisepower)
[rngest,rngvar] = step(estimator,resp,rnggrid,detidx,clusterids)
[rngest,rngvar] = step(estimator,resp,rnggrid,detidx,noisepower,clusterids)
```


## Description

Note Instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, x) and y = obj (x) perform equivalent operations.
rngest $=$ step(estimator, resp,rnggrid,detidx) estimates ranges from detections derived from the range response data cube, resp. Range estimates are computed for each detection position reported in detidx. The rnggrid argument sets the units for the range dimension of the response data cube.
[rngest,rngvar] = step(estimator,resp,rnggrid,detidx, noisepower) also specifies the noise power. This syntax applies when you set the VarianceOutputPort property to true and the NoisePowerSource property to 'Input port'.
[rngest,rngvar] = step(estimator,resp,rnggrid,detidx,clusterids) also specifies the cluster IDs for the detections. This syntax applies when you set the ClusterInputPort to true.

You can combine optional input and output arguments when their enabling properties are set. Optional inputs and outputs must be listed in the same order as the order of the enabling properties. For example, [rngest,rngvar] = step(estimator, resp,rnggrid,detidx, noisepower, clusterids).

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

estimator - Range estimator
phased.RangeEstimator System object

Range estimator, specified as a phased.RangeEstimator System object.
Example: phased.RangeEstimator
resp - Range-processed response data cube
complex-valued $M$-by-1 column vector | complex-valued $M$-by- $N$ matrix | complex-valued $M$-by- $N$-by- $P$ matrix

Range-processed response data cube, specified as a complex-valued $M$-by- 1 column vector, a complexvalued $M$-by- $N$ matrix, or a complex-valued $M$-by- $N$-by- $P$ array. $M$ is the number of fast-time or range samples. $N$ is the number of spatial elements, such as sensor elements or beams, $P$ is the number of Doppler bins or pulses, depending on whether the data cube has been Doppler processed.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
Data Types: single | double

## rnggrid - Range values along range dimension

real-valued $M$-by- 1 column vector
Range values along range dimension of the resp argument, specified as a real-valued $M$-by- 1 column vector. rnggrid defines the range values corresponding to the fast-time or range dimension. Range values must be monotonically increasing and equally spaced. Units are in meters.
Example: [0.1, 0.2,0.3]
Data Types: single | double

## detidx - Detection indices

real-valued $N_{d}$-by- $Q$ matrix
Detection indices, specified as a real-valued $N_{d}$-by- $Q$ matrix. $Q$ is the number of detections and $N_{d}$ is the number of dimensions of the response data cube, resp. Each column of detidx contains the $N_{d}$ indices of the detection in the response data cube.

To generate detection indices, you can use the phased. CFARDetector object or phased.CFARDetector2D object.
Data Types: single | double

## noisepower - Noise power at detection locations

positive scalar | real-valued 1-by-Q row vector of positive values
Noise power at detection locations, specified as a positive scalar or real-valued 1-by-Q row vector where $Q$ is the number of detections specified in detidx.

## Dependencies

To enable this input argument, set the value of the NoisePowerSource property to 'Input port '.
Data Types: single | double
clusterids - Cluster IDs
real-valued 1-by- $Q$ row vector of positive values

Cluster IDs, specified as a real-valued 1-by- $Q$ row vector, where $Q$ is the number of detections specified in detidx. Each element of clusterids corresponds to a column in detidx. Detections with the same cluster ID are in the same cluster.

## Dependencies

To enable this input argument, set the value of the ClusterInputPort property to true.
Data Types: single|double

## Output Arguments

## rngest - Range estimates

real-valued K-by-1 column vector
Range estimates, returned as a real-valued $K$-by- 1 column vector.

- When ClusterInputPort is false, Doppler estimates are computed for each detection location in the detidx argument. Then $K$ equals the column dimension, $Q$, of detidx.
- When ClusterInputPort is true, Doppler estimates are computed for each cluster ID in the clusterids argument. Then $K$ equals the number of unique cluster IDs, $Q$.

Data Types: single | double
rngvar - Range estimation variance
positive, real-valued $K$-by-1 column vector
Range estimation variance, returned as a positive, real-valued $K$-by- 1 column vector, where $K$ is the dimension of rngest. Each element of rngvar corresponds to an element of rngest. The estimator variance is computed using the Ziv-Zakai bound.

Data Types: single | double

## Examples

## Estimate Range and Speed of Three Targets

To estimate the range and speed of three targets, create a range-Doppler map using the phased.RangeDopplerResponse System object ${ }^{\text {TM }}$. Then use the phased.RangeEstimator and phased.DopplerEstimator System objects to estimate range and speed. The transmitter and receiver are collocated isotropic antenna elements forming a monostatic radar system.

The transmitted signal is a linear FM waveform with a pulse repetition interval (PRI) of 7.0 s and a duty cycle of $2 \%$. The operating frequency is 77 GHz and the sample rate is 150 MHz .

```
fs = 150e6;
c = physconst('LightSpeed');
fc = 77.0e9;
pri = 7e-6;
prf = 1/pri;
```

Set up the scenario parameters. The transmitter and receiver are stationary and located at the origin. The targets are 500, 530, and 750 meters from the radar along the $x$-axis. The targets move along the
$x$-axis at speeds of $-60,20$, and $40 \mathrm{~m} / \mathrm{s}$. All three targets have a nonfluctuating radar cross-section (RCS) of 10 dB . Create the target and radar platforms.

```
Numtgts = 3;
tgtpos = zeros(Numtgts);
tgtpos(1,:) = [500 530 750];
tgtvel = zeros(3,Numtgts);
tgtvel(1,:) = [-60 20 40];
tgtrcs = db2pow(10)*[ll 1 1];
tgtmotion = phased.Platform(tgtpos,tgtvel);
target = phased.RadarTarget('PropagationSpeed',c,'OperatingFrequency',fc, ...
    'MeanRCS',tgtrcs);
radarpos = [0;0;0];
radarvel = [0;0;0];
radarmotion = phased.Platform(radarpos,radarvel);
```

Create the transmitter and receiver antennas.

```
txantenna = phased.IsotropicAntennaElement;
rxantenna = clone(txantenna);
```

Set up the transmitter-end signal processing. Create an upsweep linear FM signal with a bandwidth of one half the sample rate. Find the length of the PRI in samples and then estimate the rms bandwidth and range resolution.

```
bw = fs/2;
waveform = phased.LinearFMWaveform('SampleRate',fs, ...
    'PRF',prf,'OutputFormat','Pulses','NumPulses',1,'SweepBandwidth',fs/2, ...
    'DurationSpecification','Duty cycle','DutyCycle',0.02);
sig = waveform();
Nr = length(sig);
bwrms = bandwidth(waveform)/sqrt(12);
rngrms = c/bwrms;
```

Set up the transmitter and radiator System object properties. The peak output power is 10 W and the transmitter gain is 36 dB .

```
peakpower = 10;
txgain = 36.0;
transmitter = phased.Transmitter( ...
    'PeakPower',peakpower, ...
    'Gain',txgain, ...
    'InUseOutputPort',true);
radiator = phased.Radiator( ...
    'Sensor',txantenna,...
    'PropagationSpeed',c,...
    'OperatingFrequency',fc);
```

Set up the free-space channel in two-way propagation mode.

```
channel = phased.FreeSpace( ...
    'SampleRate',fs, ...
    'PropagationSpeed',c, ...
    'OperatingFrequency',fc, ...
    'TwoWayPropagation',true);
```

Set up the receiver-end processing. Set the receiver gain and noise figure.

```
collector = phased.Collector( ...
    'Sensor',rxantenna, ...
    'PropagationSpeed',c, ...
    'OperatingFrequency',fc);
rxgain = 42.0;
noisefig = 1;
receiver = phased.ReceiverPreamp( ...
    'SampleRate',fs, ...
    'Gain',rxgain, ...
    'NoiseFigure',noisefig);
```

Loop over the pulses to create a data cube of 128 pulses. For each step of the loop, move the target and propagate the signal. Then put the received signal into the data cube. The data cube contains the received signal per pulse. Ordinarily, a data cube has three dimensions where the last dimension corresponds to antennas or beams. Because only one sensor is used, the cube has only two dimensions.

The processing steps are:
1 Move the radar and targets.
2 Transmit a waveform.
3 Propagate the waveform signal to the target.
4 Reflect the signal from the target.
5 Propagate the waveform back to the radar. Two-way propagation enables you to combine the return propagation with the outbound propagation.
6 Receive the signal at the radar.
7 Load the signal into the data cube.

```
Np = 128;
dt = pri;
cube = zeros(Nr,Np);
for n = 1:Np
    [sensorpos,sensorvel] = radarmotion(dt);
    [tgtpos,tgtvel] = tgtmotion(dt);
    [tgtrng,tgtang] = rangeangle(tgtpos,sensorpos);
    sig = waveform();
    [txsig,txstatus] = transmitter(sig);
    txsig = radiator(txsig,tgtang);
    txsig = channel(txsig,sensorpos,tgtpos,sensorvel,tgtvel);
    tgtsig = target(txsig);
    rxcol = collector(tgtsig,tgtang);
    rxsig = receiver(rxcol);
    cube(:,n) = rxsig;
end
```

Display the data cube containing signals per pulse.

```
imagesc([0:(Np-1)]*pri*1e6,[0:(Nr-1)]/fs*1e6,abs(cube))
xlabel('Slow Time {\mu}s')
ylabel('Fast Time {\mu}s')
axis xy
```



Create and display the range-Doppler image for 128 Doppler bins. The image shows range vertically and speed horizontally. Use the linear FM waveform for match filtering. The image is here is the range-Doppler map.

```
ndop = 128;
rangedopresp = phased.RangeDopplerResponse('SampleRate',fs, ...
    'PropagationSpeed',c,'DopplerFFTLengthSource','Property', ...
    'DopplerFFTLength',ndop,'DopplerOutput','Speed', ...
    'OperatingFrequency',fc);
matchingcoeff = getMatchedFilter(waveform);
[rngdopresp,rnggrid,dopgrid] = rangedopresp(cube,matchingcoeff);
imagesc(dopgrid,rnggrid,10*log10(abs(rngdopresp)))
xlabel('Closing Speed (m/s)')
ylabel('Range (m)')
axis xy
```



Because the targets lie along the positive $x$-axis, positive velocity in the global coordinate system corresponds to negative closing speed. Negative velocity in the global coordinate system corresponds to positive closing speed.

Estimate the noise power after matched filtering. Create a constant noise background image for simulation purposes.

```
mfgain = matchingcoeff'*matchingcoeff;
dopgain = Np;
noisebw = fs;
noisepower = noisepow(noisebw,receiver.NoiseFigure,receiver.ReferenceTemperature);
noisepowerprc = mfgain*dopgain*noisepower;
noise = noisepowerprc*ones(size(rngdopresp));
Create the range and Doppler estimator objects.
```

```
rangeestimator = phased.RangeEstimator('NumEstimatesSource','Auto', ...
```

rangeestimator = phased.RangeEstimator('NumEstimatesSource','Auto', ...
'VarianceOutputPort',true,'NoisePowerSource','Input port', ...
'VarianceOutputPort',true,'NoisePowerSource','Input port', ...
'RMSResolution',rngrms);
'RMSResolution',rngrms);
dopestimator = phased.DopplerEstimator('VarianceOutputPort',true, ...
dopestimator = phased.DopplerEstimator('VarianceOutputPort',true, ...
'NoisePowerSource','Input port','NumPulses',Np);

```
    'NoisePowerSource','Input port','NumPulses',Np);
```

Locate the target indices in the range-Doppler image. Instead of using a CFAR detector, for simplicity, use the known locations and speeds of the targets to obtain the corresponding index in the rangeDoppler image.

```
detidx = NaN(2,Numtgts);
tgtrng = rangeangle(tgtpos,radarpos);
```

```
tgtspd = radialspeed(tgtpos,tgtvel,radarpos,radarvel);
tgtdop = 2*speed2dop(tgtspd,c/fc);
for m = 1:numel(tgtrng)
    [~,iMin] = min(abs(rnggrid-tgtrng(m)));
    detidx(1,m) = iMin;
    [~,iMin] = min(abs(dopgrid-tgtspd(m)));
    detidx(2,m) = iMin;
end
```

Find the noise power at the detection locations.

```
ind = sub2ind(size(noise),detidx(1,:),detidx(2,:));
```

Estimate the range and range variance at the detection locations. The estimated ranges agree with the postulated ranges.

```
[rngest,rngvar] = rangeestimator(rngdopresp,rnggrid,detidx,noise(ind))
rngest = 3\times1
    499.7911
    529.8380
    750.0983
rngvar = 3x1
10-4 x
    0.0273
    0.0276
    0.2094
```

Estimate the speed and speed variance at the detection locations. The estimated speeds agree with the predicted speeds.

```
[spdest,spdvar] = dopestimator(rngdopresp,dopgrid,detidx,noise(ind))
spdest = 3\times1
    60.5241
    -19.6167
    -39.5838
spdvar = 3x1
10-5}
    0.0806
    0.0816
    0.6188
```


# phased.RangeResponse 

Package: phased

Range response

## Description

The phased.RangeResponse System object performs range filtering on fast-time (range) data, using either a matched filter or an FFT-based algorithm. The output is typically used as input to a detector. Matched filtering improves the SNR of pulsed waveforms. For continuous FM signals, FFT processing extracts the beat frequency of FMCW waveforms. Beat frequency is directly related to range.

The input to the range response object is a radar data cube. The organization of the data cube follows the Phased Array System Toolbox convention.

- The first dimension of the cube represents the fast-time samples or ranges of the received signals.
- The second dimension represents multiple spatial channels, such as different sensors or beams.
- The third dimension, slow-time, represent pulses.

Range filtering operates along the fast-time dimension of the cube. Processing along the other dimensions is not performed. If the data contains only one channel or pulse, the data cube can contain fewer than three dimensions. Because this object performs no Doppler processing, you can use the object to process noncoherent radar pulses.

The output of the range response object is also a data cube with the same number of dimensions as the input. Its first dimension contains range-processed data but its length can differ from the first dimension of the input data cube.

To compute the range response:
1 Define and set up your phased. RangeResponse System object. See "Construction" on page 11372.

2 Call the step method to compute the range response using the properties you specify for the phased.RangeResponse System object.

Note Instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj,x) and y = obj ( $x$ ) perform equivalent operations.

## Construction

response $=$ phased. RangeResponse creates a range response System object, response.
response = phased.RangeResponse(Name,Value) creates a System object, response, with each specified property Name set to the specified Value. You can specify additional name and value pair arguments in any order as (Name1, Value1,...,NameN, ValueN).

## Properties

RangeMethod - Range processing method
'Matched filter' (default)|'FFT'
Range processing method, specified as 'Matched filter' or 'FFT'.

- 'Matched filter' - The object match-filters the incoming signal. This approach is commonly used for pulsed signals, where the matched filter is the time reverse of the transmitted signal.
- 'FFT' - The object applies an FFT to the input signal. This approach is commonly used for chirped signals such as FMCW and linear FM pulsed signals.

Example: 'Matched filter'
Data Types: char

## PropagationSpeed - Signal propagation speed

physconst('LightSpeed') (default) | real-valued positive scalar
Signal propagation speed, specified as a real-valued positive scalar. Units are in meters per second. The default propagation speed is the value returned by physconst('LightSpeed').

Example: 3e8
Data Types: single | double

## SampleRate - Signal sample rate

1e6 (default) | positive real-valued scalar
Signal sample rate, specified as a positive real-valued scalar. Units are in hertz.
Example: 1e6
Data Types: single | double

## SweepSlope - Linear FM sweep slope

1.0e9 (default) | scalar

Linear FM sweep slope, specified as a scalar. The fast-time dimension of the signal input argument to step must correspond to sweeps having this slope.

## Example: 1.5e9

## Dependencies

To enable this property, set the RangeMethod property to ' $\mathrm{FFT}^{\prime}$.
Data Types: single | double

## DechirpInput - Enable dechirping of input signals

false (default) |true
Option to enable dechirping of input signals, specified as false or true. Set this property to false to indicate that the input signal is already dechirped and no dechirp operation is necessary. Set this property to true when the input signal requires dechirping.

## Dependencies

To enable this property, set the RangeMethod property to ' $\mathrm{FFT}^{\text {' }}$.

## Data Types: logical

## DecimationFactor - Decimation factor for dechirped signals

1 (default) | positive integer
Decimation factor for dechirped signals, specified as a positive integer. The decimation algorithm uses a 30th-order FIR filter generated by firl( $30,1 / D$ ), where $D$ is the decimation factor. The default value of 1 implies no decimation.

When processing FMCW signals, decimating the dechirped signal is useful for reducing the load on A/D converters.

## Dependencies

To enable this property, set the RangeMethod property to 'FFT' and the DechirpInput property to true.

Data Types: single | double

## RangeFFTLengthSource - Source of FFT length for range processing of dechirped signals 'Auto (default)|'Property'

Source of the FFT length used for the range processing of dechirped signals, specified as 'Auto' or 'Property'.

- 'Auto ' - The FFT length equals the length of the fast-time dimension of the input data cube.
- 'Property ' - Specify the FFT length by using the RangeFFTLength property.


## Dependencies

To enable this property, set the RangeMethod property to ' $F F T$ '.
Data Types: char

## RangeFFTLength - FFT length used for range processing

1024 (default) | positive integer
FFT length used for range processing, specified as a positive integer.

## Dependencies

To enable this property, set the RangeMethod property to 'FFT' and the RangeFFTLengthSource property to 'Property'
Data Types: single|double

## RangeWindow - FFT weighting window for range processing

'None' (default)|'Hamming'|'Chebyshev'|'Hann' | 'Kaiser' | 'Taylor' | 'Custom'
FFT weighting window for range processing, specified as 'None', 'Hamming', 'Chebyshev ',
'Hann', 'Kaiser', 'Taylor', or 'Custom'.
If you set this property to 'Taylor' , the generated Taylor window has four nearly constant sidelobes next to the mainlobe.

## Dependencies

To enable this property, set the RangeMethod property to ' FFT ' .

## Data Types: char

## RangeSidelobeAttenuation - Sidelobe attenuation for range processing <br> 30 (default) | positive scalar

Sidelobe attenuation for range processing, specified as a positive scalar. Attenuation applies to Kaiser, Chebyshev, or Taylor windows. Units are in dB.

## Dependencies

To enable this property, set the RangeMethod property to 'FFT' and the RangeWindow property to 'Kaiser', 'Chebyshev', or 'Taylor'.

Data Types: single | double

## CustomRangeWindow - Custom window for range processing <br> @hamming (default) | function handle | cell array

Custom window for range processing, specified as a function handle or a cell array containing a function handle as its first entry. If you do not specify a window length, the object computes the window length and passes that into the function. If you specify a cell array, the remaining cells of the array can contain arguments to the function. If you use only the function handle without passing in arguments, all arguments take their default values.

If you write your own window function, the first argument must be the length of the window.

Note Instead of using a cell array, you can pass in all arguments by constructing a handle to an anonymous function. For example, you can set the value of CustomRangeWindow to @(n)taylorwin( $n, n b a r, s l l)$, where you have previously set the values of nbar and sll.

Example: \{@taylor,5,-35\}

## Dependencies

To enable this property, set the RangeMethod property to 'FFT' and the RangeWindow property to 'Custom'.

Data Types: function_handle | cell

## ReferenceRangeCentered - Set reference range at center of range grid

true (default) | false
Set reference range at center of range grid, specified as true or false. Setting this property to true enables you to set the reference range at the center of the range grid. Setting this property to false sets the reference range to the beginning of the range grid.

## Dependencies

To enable this property, set the RangeMethod to ' FFT ' .
Data Types: logical
ReferenceRange - Reference range of range grid
0.0 (default) | nonnegative scalar

Reference range of the range grid, specified as a nonnegative scalar.

- If you set the RangeMethod property to 'Matched filter', the reference range is set to the start of the range grid.
- If you set the RangeMethod property to ' $F F T$ ' , the reference range is determined by the ReferenceRangeCentered property.
- When you set the ReferenceRangeCentered property to true, the reference range is set to the center of the range grid.
- When you set the ReferenceRangeCentered property to false, the reference range is set to the start of the range grid.

Units are in meters.
This property is tunable.
Example: 1000.0
Data Types: single | double

## MaximumNumInputSamplesSource - Source of maximum number of samples

'Auto ' (default)|'Property'
The source of the maximum number of samples the input signal, specified as 'Auto ' or 'Property'. When you set this property to 'Auto ', the object automatically allocates enough memory to buffer the first input signal. When you set this property to 'Property' , you specify the maximum number of samples in the input signal using the MaximumNumInputSamples property. Any input signal longer than that value is truncated.

To use this object with variable-size input signals in a MATLAB Function Block in Simulink, set the MaximumNumInputSamplesSource property to 'Property' and set a value for the MaximumNumInputSamples property.

Example: 'Property'

## MaximumNumInputSamples - Maximum number of input signal samples

100 (default) | positive integer
Maximum number of samples in the input signal, specified as a positive integer. Any input signal longer than this value is truncated. The input signal is the first argument to the step method. The number of samples is the number of rows in the input.
Example: 2048

## Dependencies

To enable this property, set the RangeMethod property to 'Matched filter' and set the MaximumNumInputSamplesSource property to 'Property'.
Data Types: single | double

## Methods

plotResponse
Plot range response
step
Range response

Common to All System Objects

```
release Allow System object property value changes
```


## Examples

## Range Response of Three Targets

Compute the radar range response of three targets by using the phased. RangeResponse System object $^{\text {tm }}$. The transmitter and receiver are collocated isotropic antenna elements forming a monostatic radar system. The transmitted signal is a linear FM waveform with a pulse repetition interval of $7.0 \mu \mathrm{~s}$ and a duty cycle of $2 \%$. The operating frequency is 77 GHz and the sample rate is 150 MHz .

```
fs = 150e6;
c = physconst('LightSpeed');
fc = 77e9;
pri = 7e-6;
prf = 1/pri;
```

Set up the scenario parameters. The radar transmitter and receiver are stationary and located at the origin. The targets are 500,530 , and 750 meters from the radars on the $x$-axis. The targets move along the $x$-axis at speeds of $-60,20$, and $40 \mathrm{~m} / \mathrm{s}$. All three targets have a nonfluctuating radar crosssection (RCS) of 10 dB .

Create the target and radar platforms.

```
Numtgts = 3;
tgtpos = zeros(Numtgts);
tgtpos(1,:) = [500 530 750];
tgtvel = zeros(3,Numtgts);
tgtvel(1,:) = [-60 20 40];
tgtrcs = db2pow(10)*[1 1 1];
tgtmotion = phased.Platform(tgtpos,tgtvel);
target = phased.RadarTarget('PropagationSpeed',c,'OperatingFrequency',fc, ...
    'MeanRCS',tgtrcs);
radarpos = [0;0;0];
radarvel = [0;0;0];
radarmotion = phased.Platform(radarpos,radarvel);
```

Create the transmitter and receiver antennas.

```
txantenna = phased.IsotropicAntennaElement;
rxantenna = clone(txantenna);
```

Set up the transmitter-end signal processing. Create an upsweep linear FM signal with a bandwidth of half the sample rate. Find the length of the pri in samples and then estimate the rms bandwidth and range resolution.

```
bw = fs/2;
waveform = phased.LinearFMWaveform('SampleRate',fs, ...
    'PRF',prf,'OutputFormat','Pulses','NumPulses',1,'SweepBandwidth',fs/2, ...
    'DurationSpecification','Duty cycle','DutyCycle',0.02);
sig = waveform();
Nr = length(sig);
```

```
bwrms = bandwidth(waveform)/sqrt(12);
rngrms = c/bwrms;
```

Set up the transmitter and radiator System object properties. The peak output power is 10 W and the transmitter gain is 36 dB .

```
peakpower = 10;
txgain = 36.0;
transmitter = phased.Transmitter( ...
    'PeakPower',peakpower, ...
    'Gain',txgain, ...
    'InUseOutputPort',true);
radiator = phased.Radiator( ...
    'Sensor',txantenna, ...
    'PropagationSpeed',c, ...
    'OperatingFrequency',fc);
```

Create a free-space propagation channel in two-way propagation mode.

```
channel = phased.FreeSpace( ...
    'SampleRate',fs, ...
    'PropagationSpeed',c, ...
    'OperatingFrequency',fc, ...
    'TwoWayPropagation',true);
```

Set up the receiver-end processing. The receiver gain is 42 dB and noise figure is 10 .

```
collector = phased.Collector( ...
    'Sensor',rxantenna, ...
    'PropagationSpeed',c, ...
    'OperatingFrequency',fc);
rxgain = 42.0;
noisefig = 10;
receiver = phased.ReceiverPreamp( ...
    'SampleRate',fs, ...
    'Gain',rxgain, ...
    'NoiseFigure',noisefig);
```

Loop over 128 pulses to build a data cube. For each step of the loop, move the target and propagate the signal. Then put the received signal into the data cube. The data cube contains the received signal per pulse. Ordinarily, a data cube has three dimensions, where last dimension corresponds to antennas or beams. Because only one sensor is used in this example, the cube has only two dimensions.

The processing steps are:
1 Move the radar and targets.
2 Transmit a waveform.
3 Propagate the waveform signal to the target.
4 Reflect the signal from the target.
5 Propagate the waveform back to the radar. Two-way propagation mode enables you to combine the returned propagation with the outbound propagation.
6 Receive the signal at the radar.
7 Load the signal into the data cube.

```
Np = 128;
cube = zeros(Nr,Np);
for n = 1:Np
    [sensorpos,sensorvel] = radarmotion(pri);
    [tgtpos,tgtvel] = tgtmotion(pri);
    [tgtrng,tgtang] = rangeangle(tgtpos,sensorpos);
    sig = waveform();
    [txsig,txstatus] = transmitter(sig);
    txsig = radiator(txsig,tgtang);
    txsig = channel(txsig,sensorpos,tgtpos,sensorvel,tgtvel);
    tgtsig = target(txsig);
    rxcol = collector(tgtsig,tgtang);
    rxsig = receiver(rxcol);
    cube(:,n) = rxsig;
end
```

Display the image of the data cube containing signals per pulse.
imagesc([0:(Np-1)]*pri*1e6,[0:(Nr-1)]/fs*1e6, abs(cube))
xlabel('Slow Time \{\mu\}s')
ylabel('Fast Time \{\mu\}s')


Create a phased.RangeResponse System object in matched filter mode. Then, display the range response image for the 128 pulses. The image shows range vertically and pulse number horizontally.

```
matchingcoeff = getMatchedFilter(waveform);
```

ndop = 128;
rangeresp = phased.RangeResponse('SampleRate',fs,'PropagationSpeed',c);
[resp,rnggrid] = rangeresp(cube,matchingcoeff);
imagesc([1:Np],rnggrid,abs(resp))
xlabel('Pulse')
ylabel('Range (m)')


Integrate 20 pulses noncoherently.

```
intpulse = pulsint(resp(:,1:20),'noncoherent');
plot(rnggrid,abs(intpulse))
xlabel('Range (m)')
title('Noncoherent Integration of 20 Pulses')
```



## Algorithms

## Data Precision

This System object supports single and double precision for input data, properties, and arguments. If the input data X is single precision, the output data is single precision. If the input data X is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

## Version History

Introduced in R2017a

## References

[1] Richards, M. Fundamentals of Radar Signal Processing, 2nd ed. McGraw-Hill Professional Engineering, 2014.
[2] Richards, M., J. Scheer, and W. Holm, Principles of Modern Radar: Basic Principles. SciTech Publishing, 2010.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.
Usage notes and limitations:

- The CustomRangeWindow property is not supported.
- The plotResponse method is not supported.
- See "System Objects in MATLAB Code Generation" (MATLAB Coder).

This System object supports single and double precision for input data, properties, and arguments. If the input data $X$ is single precision, the output data is single precision. If the input data $X$ is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

## See Also

## Functions

bw2 range | fir1|chebwin|dechirp|hann | hamming| kaiser|taylorwin| rangeangle

## Objects

phased.RangeAngleResponse|phased.RangeDopplerResponse|
phased.AngleDopplerResponse|phased.MatchedFilter|phased.DopplerEstimator| phased.RangeEstimator|phased.CFARDetector|phased.CFARDetector2D

## Topics

"Radar Data Cube"

## plotResponse

System object: phased. RangeResponse
Package: phased
Plot range response

## Syntax

plotResponse(response, x)
plotResponse(response, x, xref)
plotResponse(response, $x$, coeff)
plotResponse(response, $\qquad$ ,Name, Value)

## Description

$p l o t R e s p o n s e(r e s p o n s e, x$ ) plots the range response of a dechirped input signal, $x$. This syntax applies when you set the RangeMethod property to 'FFT' and the DechirpInput property to false.
plotResponse(response, $x$, xref) plots the range response x , after performing a dechirp operation using the reference signal, xref. This syntax applies when you set the RangeMethod property to 'FFT' and the DechirpInput property to true.
plotResponse (response, $x$, coeff) plots the range response of $x$ after match filtering using the match filter coefficients, coeff. This syntax applies when you set the RangeMethod property to 'Matched filter'.
plotResponse(response,__, Name, Value) plots the range response with additional options specified by one or more Name, Value pair arguments.

## Input Arguments

## response - Range response

phased. RangeResponse System object
Range response, specified as a phased. RangeResponse System object.
Example: phased. RangeResponse

## x - Input radar data cube

complex-valued $K$-element column vector | complex-valued $K$-by- $L$ matrix | complex-valued $K$-by- $N$-by$L$ array

Input radar data cube, specified as a complex-valued $K$-by- 1 column vector, a $K$-by- $L$ matrix, or $K$-by-$N$-by-L array.

- $K$ is the number of fast-time or range samples.
- $N$ is the number of independent spatial channels such as sensors or directions.
- $L$ is the slow-time dimension that corresponds to the number of pulses or sweeps in the input signal.

See "Radar Data Cube".
Each $K$-element fast-time dimension is processed independently.
For FMCW waveforms with a triangle sweep, the sweeps alternate between positive and negative slopes. However, phased. RangeResponse is designed to process consecutive sweeps of the same slope. To apply phased.RangeResponse for a triangle-sweep system, use one of the following approaches:

- Specify a positive SweepSlope property value, with x corresponding to upsweeps only. After obtaining the Doppler or speed values, divide them by 2.
- Specify a negative SweepSlope property value, with x corresponding to downsweeps only. After obtaining the Doppler or speed values, divide them by 2.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

## Data Types: single | double

xref - Reference signal used for dechirping
complex-valued $K$-by- 1 column vector
Reference signal used for dechirping, specified as a complex-valued $K$-by- 1 column vector. The value of $K$ must equal the length of the first dimension of $x$.

Dependencies
To enable this input argument, set the value of RangeMethod to ' FFT ' and DechirpInput to true.
Data Types: single | double
coeff - Matched filter coefficients
complex-valued $P$-by-1 column vector
Matched filter coefficients, specified as a complex-valued $P$-by- 1 column vector. $P$ must be less than or equal to $K$, the length of the fast-time dimension.

## Dependencies

To enable this input argument, set RangeMethod property to 'Matched filter'.
Data Types: single | double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Unit - Vertical axes units

'db' (default)|'mag'|'pow'
Units for vertical axis of plot, specified as 'db', 'mag', or 'pow'.
Example: 'pow'

## Data Types: char

## Examples

## Plot Range Response of Three Targets

Plot the radar range response of three targets using the plotResponse method of the phased.RangeResponse System object ${ }^{\mathrm{Tm}}$. The transmitter and receiver are collocated isotropic antenna elements forming a monostatic radar system. The transmitted signal is a linear FM waveform with a pulse repetition interval of $7.0 \mu \mathrm{~s}$ and a duty cycle of $2 \%$. The operating frequency is 77 GHz and the sample rate is 150 MHz .

```
fs = 150e6;fs = 150e6;
c = physconst('LightSpeed');
fc = 77e9;
pri = 7e-6;
prf = 1/pri;
```

Set up the scenario parameters. The radar transmitter and receiver are stationary and located at the origin. The targets are 500,530 , and 750 meters from the radars on the $x$-axis. The targets move along the $x$-axis at speeds of $-60,20$, and $40 \mathrm{~m} / \mathrm{s}$. All three targets have a nonfluctuating RCS of 10 dB .

Create the target and radar platforms.

```
Numtgts = 3;
tgtpos = zeros(Numtgts);
tgtpos(1,:) = [500 530 750];
tgtvel = zeros(3,Numtgts);
tgtvel(1,:) = [-60 20 40];
tgtrcs = db2pow(10)*[[1 1 1];
tgtmotion = phased.Platform(tgtpos,tgtvel);
target = phased.RadarTarget('PropagationSpeed',c,'OperatingFrequency',fc, ...
    'MeanRCS',tgtrcs);
radarpos = [0;0;0];
radarvel = [0;0;0];
radarmotion = phased.Platform(radarpos,radarvel);
```

Create the transmitter and receiver antennas.

```
txantenna = phased.IsotropicAntennaElement;
rxantenna = clone(txantenna);
```

Set up the transmitter-end signal processing. Construct an upsweep linear FM signal with a bandwidth of half the sample rate. Find the rms bandwidth and rms range resolution.

```
bw = fs/2;
waveform = phased.LinearFMWaveform('SampleRate',fs,...
    'PRF',prf,'OutputFormat','Pulses','NumPulses',1,'SweepBandwidth',fs/2,...
    'DurationSpecification','Duty cycle','DutyCycle',.02);
sig = waveform();
Nr = length(sig);
bwrms = bandwidth(waveform)/sqrt(12);
rngrms = c/bwrms;
```

Set up the transmitter and radiator System object properties. The peak output power is 10 W and the transmitter gain is 36 dB .

```
peakpower = 10;
txgain = 36.0;
transmitter = phased.Transmitter(...
    'PeakPower', peakpower,...
    'Gain',txgain,...
    'InUseOutputPort',true);
radiator = phased.Radiator(...
    'Sensor',txantenna,...
    'PropagationSpeed',c,...
    'OperatingFrequency',fc);
```

Create a free-space propagation channel in two-way propagation mode.

```
channel = phased.FreeSpace(...
    'SampleRate',fs,...
    'PropagationSpeed',c,...
    'OperatingFrequency',fc,...
    'TwoWayPropagation',true);
```

Set up the receiver-end processing. The receiver gain is 42 dB and noise figure is 10 .

```
collector = phased.Collector(...
    'Sensor',rxantenna,...
    'PropagationSpeed',c,...
    'OperatingFrequency',fc);
rxgain = 42.0;
noisefig = 10;
receiver = phased.ReceiverPreamp(...
    'SampleRate',fs,...
    'Gain',rxgain,...
    'NoiseFigure',noisefig);
```

Loop over 128 pulses to build a data cube. For each step of the loop, move the target and propagate the signal. Then put the received signal into the data cube. The data cube contains the received signal per pulse. Ordinarily, a data cube has three dimensions. The last dimension corresponds to antennas or beams. Because only one sensor is used in this example, the cube has only two dimensions.

The processing steps are:
1 Move the radar and targets.
2 Transmit a waveform.
3 Propagate the waveform signal to the target.
4 Reflect the signal from the target.
5 Propagate the waveform back to the radar. Two-way propagation mode allows the return propagation to be combined with the outbound propagation.
6 Receive the signal at the radar.
7 Load the signal into the data cube.

```
Np = 128;
cube = zeros(Nr,Np);
for n = 1:Np
```

```
    [sensorpos,sensorvel] = radarmotion(pri);
    [tgtpos,tgtvel] = tgtmotion(pri);
    [tgtrng,tgtang] = rangeangle(tgtpos,sensorpos);
    sig = waveform();
    [txsig,txstatus] = transmitter(sig);
    txsig = radiator(txsig,tgtang);
    txsig = channel(txsig,sensorpos,tgtpos,sensorvel,tgtvel);
    tgtsig = target(txsig);
    rxcol = collector(tgtsig,tgtang);
    rxsig = receiver(rxcol);
    cube(:,n) = rxsig;
```

end

Create a phased.RangeResponse System object in matched filter mode. Then, call the plotResponse method to show the first 20 pulses.
matchcoeff = getMatchedFilter(waveform);
rangeresp = phased.RangeResponse('SampleRate',fs,'PropagationSpeed', c);
plotResponse(rangeresp,cube(:,1:20), matchcoeff);


## Version History

Introduced in R2017a

## step

System object: phased.RangeResponse
Package: phased
Range response

## Syntax

[resp,rnggrid] = step(response, x)
[resp,rnggrid] = step(response, $x, x r e f$ )
[resp,rnggrid] = step(response, $x$, coeff)

## Description

Note Instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, x) and y = obj $(x)$ perform equivalent operations.
[resp,rnggrid] = step(response, x) computes the range response, resp, for the input signal, $x$, and the range values, rnggrid, corresponding to the response. This syntax applies when you set RangeMethod to 'FFT ' and DechirpInput to false. This syntax assumes that the input signal has already been dechirped. This syntax is most commonly used with FMCW signals.
[resp,rnggrid] = step(response, $x, x r e f$ ) computes the range response of the input signal, $x$ using the reference signal, xref. This syntax applies when you set RangeMethod to 'FFT' and DechirpInput to true. Often, the reference signal is the transmitted signal. This syntax assumes that the input signal has not been dechirped. This syntax is most commonly used with FMCW signals.
[resp,rnggrid] = step(response, $x$, coeff) computes the range response of $x$ using the matched filter coeff. This syntax applies when you set RangeMethod to 'Matched filter'. This syntax is most commonly used with pulsed signals.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

response - Range response
phased. RangeResponse System object
Range response, specified as a phased.RangeResponse System object.
Example: phased. RangeResponse

## x - Input radar data cube

complex-valued $K$-element column vector | complex-valued $K$-by- $L$ matrix | complex-valued $K$-by- $N$-by$L$ array

Input radar data cube, specified as a complex-valued $K$-by- 1 column vector, a $K$-by- $L$ matrix, or $K$-by-$N$-by-L array.

- $K$ is the number of fast-time or range samples.
- $N$ is the number of independent spatial channels such as sensors or directions.
- $L$ is the slow-time dimension that corresponds to the number of pulses or sweeps in the input signal.

See "Radar Data Cube".
Each $K$-element fast-time dimension is processed independently.
For FMCW waveforms with a triangle sweep, the sweeps alternate between positive and negative slopes. However, phased. RangeResponse is designed to process consecutive sweeps of the same slope. To apply phased. RangeResponse for a triangle-sweep system, use one of the following approaches:

- Specify a positive SweepSlope property value, with x corresponding to upsweeps only. After obtaining the Doppler or speed values, divide them by 2.
- Specify a negative SweepSlope property value, with x corresponding to downsweeps only. After obtaining the Doppler or speed values, divide them by 2.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

## Data Types: single|double

## xref - Reference signal used for dechirping

complex-valued $K$-by- 1 column vector
Reference signal used for dechirping, specified as a complex-valued $K$-by- 1 column vector. The number of rows must equal the length of the fast-time dimension of $x$.

## Dependencies

To enable this input argument, set the value of RangeMethod to 'FFT' and DechirpInput to true.
Data Types: single|double

## coeff - Matched filter coefficients

complex-valued $P$-by- 1 column vector
Matched filter coefficients, specified as a complex-valued $P$-by- 1 column vector. $P$ must be less than or equal to $K . K$ is the number of fast-time or range sample.

## Dependencies

To enable this input argument, set the value of RangeMethod to 'Matched filter'.
Data Types: double

## Output Arguments

## resp - Range response data cube

complex-valued $M$-element column vector | complex-valued $M$-by- $L$ matrix | complex-valued $M$-by- $N$ by-L array

Range response data cube, returned as one of the following:

- Complex-valued $M$-element column vector
- Complex-valued $M$-by- $L$ matrix
- Complex-valued $M$-by- $N$ by- $L$ array

The value of $M$ depends on the type of processing

| RangeMethod Property | DechirpInput Property | Value of M |
| :---: | :---: | :---: |
| 'FFT' | false | If you set the RangeFFTLength property to 'Auto',$M=K$, the length of the fast-time dimension of $x$. Otherwise, $M$ equals the value of the RangeFFTLength property. |
|  | true | $M$ equals the quotient of the number of rows, $K$, of the input signal by the value of the decimation factor, $D$, specified in DecimationFactor. |
| 'Matched filter' | n/a | $M=K$, the length of the fasttime dimension of x . |

## Data Types: single | double

## rnggrid - Range values along range dimension

real-valued $M$-by- 1 column vector
Range values along range dimension, returned as a real-valued $M$-by- 1 column vector. rnggrid defines the ranges corresponding to the fast-time dimension of the resp output data cube. $M$ is the length of the fast-time dimension of resp. Range values are monotonically increasing and equally spaced. Units are in meters.
Example: [0, 0.1, 0.2,0.3]
Data Types: single | double

## Examples

## Range Response of Three Targets

Compute the radar range response of three targets by using the phased. RangeResponse System object $^{\mathrm{TM}}$. The transmitter and receiver are collocated isotropic antenna elements forming a monostatic radar system. The transmitted signal is a linear FM waveform with a pulse repetition interval of $7.0 \mu \mathrm{~s}$ and a duty cycle of $2 \%$. The operating frequency is 77 GHz and the sample rate is 150 MHz .

```
fs = 150e6;
c = physconst('LightSpeed');
fc = 77e9;
pri = 7e-6;
prf = 1/pri;
```

Set up the scenario parameters. The radar transmitter and receiver are stationary and located at the origin. The targets are 500,530, and 750 meters from the radars on the $x$-axis. The targets move along the $x$-axis at speeds of $-60,20$, and $40 \mathrm{~m} / \mathrm{s}$. All three targets have a nonfluctuating radar crosssection (RCS) of 10 dB .

Create the target and radar platforms.

```
Numtgts = 3;
tgtpos = zeros(Numtgts);
tgtpos(1,:) = [500 530 750];
tgtvel = zeros(3,Numtgts);
tgtvel(1,:) = [-60 20 40];
tgtrcs = db2pow(10)*[[1 1 1];
tgtmotion = phased.Platform(tgtpos,tgtvel);
target = phased.RadarTarget('PropagationSpeed',c,'OperatingFrequency',fc, ...
    'MeanRCS',tgtrcs);
radarpos = [0;0;0];
radarvel = [0;0;0];
radarmotion = phased.Platform(radarpos,radarvel);
```

Create the transmitter and receiver antennas.

```
txantenna = phased.IsotropicAntennaElement;
rxantenna = clone(txantenna);
```

Set up the transmitter-end signal processing. Create an upsweep linear FM signal with a bandwidth of half the sample rate. Find the length of the pri in samples and then estimate the rms bandwidth and range resolution.

```
bw = fs/2;
waveform = phased.LinearFMWaveform('SampleRate',fs, ...
    'PRF',prf,'OutputFormat','Pulses','NumPulses',1,'SweepBandwidth',fs/2, ...
    'DurationSpecification','Duty cycle','DutyCycle',0.02);
sig = waveform();
Nr = length(sig);
bwrms = bandwidth(waveform)/sqrt(12);
rngrms = c/bwrms;
```

Set up the transmitter and radiator System object properties. The peak output power is 10 W and the transmitter gain is 36 dB .

```
peakpower = 10;
txgain = 36.0;
transmitter = phased.Transmitter( ...
    'PeakPower',peakpower, ...
    'Gain',txgain, ...
    'InUseOutputPort',true);
radiator = phased.Radiator( ...
    'Sensor',txantenna, ...
    'PropagationSpeed',c, ...
    'OperatingFrequency',fc);
```

Create a free-space propagation channel in two-way propagation mode.

```
channel = phased.FreeSpace( ...
    'SampleRate',fs, ...
    'PropagationSpeed',c, ...
    'OperatingFrequency',fc, ...
    'TwoWayPropagation',true);
```

Set up the receiver-end processing. The receiver gain is 42 dB and noise figure is 10 .

```
collector = phased.Collector( ...
    'Sensor',rxantenna, ...
    'PropagationSpeed',c, ...
    'OperatingFrequency',fc);
rxgain = 42.0;
noisefig = 10;
receiver = phased.ReceiverPreamp( ...
    'SampleRate',fs, ...
    'Gain',rxgain, ...
    'NoiseFigure',noisefig);
```

Loop over 128 pulses to build a data cube. For each step of the loop, move the target and propagate the signal. Then put the received signal into the data cube. The data cube contains the received signal per pulse. Ordinarily, a data cube has three dimensions, where last dimension corresponds to antennas or beams. Because only one sensor is used in this example, the cube has only two dimensions.

The processing steps are:
1 Move the radar and targets.
2 Transmit a waveform.
3 Propagate the waveform signal to the target.
4 Reflect the signal from the target.
5 Propagate the waveform back to the radar. Two-way propagation mode enables you to combine the returned propagation with the outbound propagation.
6 Receive the signal at the radar.
7 Load the signal into the data cube.

```
Np = 128;
cube = zeros(Nr,Np);
for n = 1:Np
    [sensorpos,sensorvel] = radarmotion(pri);
    [tgtpos,tgtvel] = tgtmotion(pri);
    [tgtrng,tgtang] = rangeangle(tgtpos,sensorpos);
    sig = waveform();
    [txsig,txstatus] = transmitter(sig);
    txsig = radiator(txsig,tgtang);
    txsig = channel(txsig,sensorpos,tgtpos,sensorvel,tgtvel);
    tgtsig = target(txsig);
    rxcol = collector(tgtsig,tgtang);
    rxsig = receiver(rxcol);
    cube(:,n) = rxsig;
end
```

Display the image of the data cube containing signals per pulse.

```
imagesc([0:(Np-1)]*pri*le6,[0:(Nr-1)]/fs*1e6,abs(cube))
xlabel('Slow Time {\mu}s')
ylabel('Fast Time {\mu}s')
```



Create a phased.RangeResponse System object in matched filter mode. Then, display the range response image for the 128 pulses. The image shows range vertically and pulse number horizontally.

```
matchingcoeff = getMatchedFilter(waveform);
ndop = 128;
rangeresp = phased.RangeResponse('SampleRate',fs,'PropagationSpeed',c);
[resp,rnggrid] = rangeresp(cube,matchingcoeff);
imagesc([1:Np],rnggrid,abs(resp))
xlabel('Pulse')
ylabel('Range (m)')
```



Integrate 20 pulses noncoherently.
intpulse $=$ pulsint(resp(:,1:20),'noncoherent');
plot(rnggrid, abs(intpulse))
xlabel('Range (m)')
title('Noncoherent Integration of 20 Pulses')


## Version History <br> Introduced in R2017a

## phased.ReceiverPreamp

Package: phased
Receiver preamp

## Description

The ReceiverPreamp System object implements a model of a receiver preamplifier. The object receives incoming signals, multiplies them by the amplifier gain and divides by system losses. Finally, Gaussian white noise is added to the signal.

To model a receiver preamp:
1 Define and set up your receiver preamp. See "Construction" on page 1-1396.
2 Call step to amplify the input signal according to the properties of phased. ReceiverPreamp. The behavior of step is specific to each object in the toolbox.

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step $(o b j, x)$ and $y=o b j(x)$ perform equivalent operations.

## Construction

H = phased. ReceiverPreamp creates a receiver preamp System object, H.
H = phased. ReceiverPreamp (Name, Value) creates a receiver preamp object, H, with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN).

## Properties

## Gain

Gain of receiver
A scalar containing the gain (in decibels) of the receiver preamp.
Default: 20

## LossFactor

Loss factor of receiver
A scalar containing the loss factor (in decibels) of the receiver preamp.
Default: 0
NoiseMethod
Noise specification method

Specify how to compute noise power using one of 'Noise power' | 'Noise temperature'. If you set this property to 'Noise temperature', complex baseband noise is added to the input signal with noise power computed from the ReferenceTemperature, NoiseFigure, and SampleRate properties. If you set this property to 'Noise power', noise is added to the signal with power specified in the NoisePower property.

Default: 'Noise temperature'

## NoiseFigure

Noise figure of receiver
A scalar containing the noise figure (in decibels) of the receiver preamp. If the receiver has multiple channels/sensors, the noise figure applies to each channel/sensor. This property is only applicable when you set the NoiseMethod property to 'Noise temperature'.

## Default: 0

## ReferenceTemperature

Reference temperature of receiver
A scalar containing the reference temperature of the receiver (in kelvin). If the receiver has multiple channels/sensors, the reference temperature applies to each channel/sensor. This property is only applicable when you set the NoiseMethod property to 'Noise temperature'.

Default: 290

## SampleRate

Sample rate
Specify the sample rate, in hertz, as a positive scalar. This property is only applicable when you set the NoiseMethod property to 'Noise temperature'. The SampleRate property also specifies the noise bandwidth.

## Default: 1e6

## NoisePower

Noise power
Specify the noise power (in Watts) as a positive scalar. This property is only applicable when you set the NoiseMethod property to 'Noise power'.

Default: 1.0

## NoiseComplexity

Noise complexity
Specify the noise complexity as one of 'Complex'|'Real'. When you set this property to 'Complex', the noise power is evenly divided between real and imaginary channels. Usually, complex-valued baseband signals require the addition of complex-valued noise. On occasion, when the signal is real-valued, you can use this option to specify that the noise is real-valued as well.

Default: 'Complex'

## EnableInputPort

Add input to specify enabling signal
To specify a receiver enabling signal, set this property to true and use the corresponding input argument when you invoke step. If you do not want to specify a receiver enabling signal, set this property to false.

Default: false

## PhaseNoiseInputPort

Add input to specify phase noise
To specify the phase noise for each incoming sample, set this property to true and use the corresponding input argument when you invoke step. You can use this information to emulate coherent-on-receive systems. If you do not want to specify phase noise, set this property to false.

Default: false

## SeedSource

Source of seed for random number generator
Specify how the object generates random numbers. Values of this property are:

| 'Auto' | The default MATLAB random number generator produces the <br> random numbers. Use 'Auto ' if you are using this object with <br> Parallel Computing Toolbox software. |
| :--- | :--- |
| 'Property' | The object uses its own private random number generator to <br> produce random numbers. The Seed property of this object <br> specifies the seed of the random number generator. Use <br> 'Property' if you want repeatable results and are not using this <br> object with Parallel Computing Toolbox software. |

## Default: 'Auto'

## Seed

Seed for random number generator
Specify the seed for the random number generator as a scalar integer between 0 and $2^{32}-1$. This property applies when you set the SeedSource property to 'Property'.

## Default: 0

## Methods

reset Reset random number generator for noise generation
step Receive incoming signal

## Common to All System Objects

```
release Allow System object property value changes
```


## Examples

## Preamplify Signal

This example shows how to use the phased. ReceiverPreamp System object ${ }^{\text {TM }}$ to amplify a sine wave.

Create a phased.ReceiverPreamp System object with a sample rate of 100 Hz . Assume a receiver noise figure of 60 dB .

```
fs = 100;
```

receiver = phased.ReceiverPreamp('NoiseFigure',60, ...
'SampleRate',fs,'NoiseComplexity', 'Real');

Create the input signal.

```
t = linspace(0,1-1/fs,100);
x = 1e-6*sin(2*pi*5*t);
```

Amplify the signal and compare it with the input signal.

```
y = receiver(x);
plot(t,x,t,real(y))
xlabel('Time (s)')
ylabel('Amplitude')
legend('Input signal','Amplified signal')
```



## Version History <br> Introduced in R2011a

## References

[1] Richards, M. A. Fundamentals of Radar Signal Processing. New York: McGraw-Hill, 2005.
[2] Skolnik, M. Introduction to Radar Systems, 3rd Ed. New York: McGraw-Hill, 2001.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:
See "System Objects in MATLAB Code Generation" (MATLAB Coder).

## See Also

phased.Collector| phased.Transmitter

## Topics

"Receiver Preamp"

## reset

System object: phased. ReceiverPreamp
Package: phased
Reset random number generator for noise generation

## Syntax

reset (H)

## Description

reset (H) resets the states of the ReceiverPreamp object, H. This method resets the random number generator state if the SeedSource property is set to 'Property'.

## step

System object: phased. ReceiverPreamp
Package: phased
Receive incoming signal

## Syntax

$Y=\operatorname{step}(H, X)$
Y = step(H,X,EN_RX)
Y = step(H,X,PHNOISE)
Y $=\operatorname{step}\left(H, X, E N \_R X, P H N O I S E\right)$

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step $(o b j, x)$ and $y=o b j(x)$ perform equivalent operations.
$Y=\operatorname{step}(H, X)$ applies the receiver gain and the receiver noise to the input signal, $X$, and returns the resulting output signal, Y .

Y = step (H,X,EN_RX) uses input EN_RX as the enabling signal when the EnableInputPort property is set to true.
$\mathrm{Y}=$ step ( $\mathrm{H}, \mathrm{X}, \mathrm{PH} N O I S E)$ uses input PHNOISE as the phase noise for each sample in X when the PhaseNoiseInputPort is set to true. The phase noise is the same for all channels in $X$. The elements in PHNOISE represent the random phases the transmitter adds to the transmitted pulses. The receiver preamp object removes these random phases from all received samples returned within corresponding pulse intervals. Such setup is often referred to as coherent on receive.
$\mathrm{Y}=\operatorname{step}\left(\mathrm{H}, \mathrm{X}, \mathrm{EN} \_\right.$RX, PHNOISE) combines all input arguments. This syntax is available when you configure H so that $\overline{\mathrm{H}}$. EnableInputPort is true and H . PhaseNoiseInputPort is true.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## H

Receiver object.

## X

Input signal
The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

EN_RX
Enabling signal, specified as a column vector whose length equals the number of rows in $X$. The data type of EN_RN is double or logical. Every element of EN_RX that equals 0 or false indicates that the receiver is turned off, and no input signal passes through the receiver. Every element of EN_RX that is nonzero or true indicates that the receiver is turned on, and the input passes through.

## PHNOISE

Phase noise for each sample in $X$, specified as a column vector whose length equals the number of rows in X. You can obtain PHNOISE as an optional output argument from the step method of phased.Transmitter.

## Output Arguments

## Y

Output signal. Y has the same dimensions as X .

## Examples

## Preamplify Cosine Signal

This example shows how to construct a phased. ReceiverPreamp System object ${ }^{\mathrm{TM}}$ with a noise figure of 5 dB and a bandwidth of 1 MHz . Then use the object to amplify the signal.

Construct the Receiver Preamp System object.

```
receiver = phased.ReceiverPreamp('NoiseFigure',5,'SampleRate',1e6);
```

Create the signal.

```
Fs = 1e3;
t = linspace(0,1,1e3);
x = cos(2*pi*200*t)';
```

Use the step method to amplify the signal and then plot the first 100 samples.

```
y = receiver(x);
idx = [1:100];
plot(t(idx),x(idx),t(idx),real(y(idx)))
xlabel('Time (s)')
ylabel('Amplitude')
legend('Original signal','Received signal')
```



# phased.RectangularWaveform 

Package: phased
Rectangular pulse waveform

## Description

The RectangularWaveform object creates a rectangular pulse waveform.
To obtain waveform samples:
1 Define and set up your rectangular pulse waveform. See "Construction" on page 1-1406.
2 Call step to generate the rectangular pulse waveform samples according to the properties of phased. RectangularWaveform. The behavior of step is specific to each object in the toolbox.

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step (obj, x) and $y=o b j(x)$ perform equivalent operations. When the only argument to the step method is the System object itself, replace $y=\operatorname{step}(o b j)$ by $y=o b j()$.

## Construction

H = phased.RectangularWaveform creates a rectangular pulse waveform System object, H. The object generates samples of a rectangular pulse.

H = phased.RectangularWaveform(Name, Value) creates a rectangular pulse waveform object, H, with each specified property Name set to the specified Value. You can specify additional namevalue pair arguments in any order as (Name1,Value1,...,NameN,ValueN).

## Properties

## SampleRate

Sample rate
Signal sample rate, specified as a positive scalar. Units are Hertz. The ratio of sample rate to pulse repetition frequency ( $P R F$ ) must be a positive integer - each pulse must contain an integer number of samples.

Default: 1e6

## DurationSpecification

Method to set pulse duration
Method to set pulse duration (pulse width), specified as 'Pulse width' or 'Duty cycle'. This property determines how you set the pulse duration. When you set this property to 'Pulse width', then you set the pulse duration directly using the PulseWidth property. When you set this property
to 'Duty cycle', you set the pulse duration from the values of the PRF and DutyCycle properties. The pulse width is equal to the duty cycle divided by the $P R F$.

Default: 'Pulse width'

## PulseWidth

Pulse width
Specify the length of each pulse (in seconds) as a positive scalar. The value must satisfy PulseWidth $<=1 . /$ PRF.

Default: 50e-6
DutyCycle
Waveform duty cycle
Waveform duty cycle, specified as a scalar from 0 to 1 , exclusive. This property applies when you set the DurationSpecification property to 'Duty cycle'. The pulse width is the value of the DutyCycle property divided by the value of the PRF property.

Default: 0.5
PRF
Pulse repetition frequency
Pulse repetition frequency, $P R F$, specified as a scalar or a row vector. Units are in Hz . The pulse repetition interval, $P R I$, is the inverse of the pulse repetition frequency, $P R F$. ThePRF must satisfy these restrictions:

- The product of PRF and PulseWidth must be less than or equal to one. This condition expresses the requirement that the pulse width is less than one pulse repetition interval. For the phasecoded waveform, the pulse width is the product of the chip width and number of chips.
- The ratio of sample rate to any element of PRF must be an integer. This condition expresses the requirement that the number of samples in one pulse repetition interval is an integer.

You can select the value of $P R F$ using property settings alone or using property settings in conjunction with the prfidx input argument of the step method.

- When PRFSelectionInputPort is false, you set the PRF using properties only. You can
- implement a constant PRF by specifying PRF as a positive real-valued scalar.
- implement a staggered $P R F$ by specifying PRF as a row vector with positive real-valued entries. Then, each call to the step method uses successive elements of this vector for the PRF. If the last element of the vector is reached, the process continues cyclically with the first element of the vector.
- When PRFSelectionInputPort is true, you can implement a selectable $P R F$ by specifying PRF as a row vector with positive real-valued entries. But this time, when you execute the step method, select a $P R F$ by passing an argument specifying an index into the $P R F$ vector.

In all cases, the number of output samples is fixed when you set the OutputFormat property to
'Samples'. When you use a varying PRF and set the OutputFormat property to 'Pulses', the number of samples can vary.

Default: 10e3

## PRFSelectionInputPort

Enable PRF selection input
Enable the PRF selection input, specified as true or false. When you set this property to false, the step method uses the values set in the PRF property. When you set this property to true, you pass an index argument into the step method to select a value from the PRF vector.

Default: false

## FrequencyOffsetSource

Source of frequency offset
Source of frequency offset for the waveform, specified as 'Property' or 'Input port'.

- When you set this property to 'Property', the offset is determined by the value of the FrequencyOffset property.
- When you set this property to 'Input port ', the FrequencyOffset is determined by the freqoffset input argument.

Default: 'Property'

## FrequencyOffset

Frequency offset
Frequency offset in Hz , specified as a scalar.

## Dependencies

This property applies when you set the FrequencyOffsetSource property to 'Input port'.
Default: 0 Hz

## OutputFormat

Output signal format
Specify the format of the output signal as 'Pulses' or 'Samples'. When you set the OutputFormat property to 'Pulses', the output of the step method takes the form of multiple pulses specified by the value of the NumPulses property. The number of samples per pulse can vary if you change the pulse repetition frequency during the simulation.

When you set the OutputFormat property to 'Samples', the output of the step method is in the form of multiple samples. In this case, the number of output signal samples is the value of the NumSamples property and is fixed.

Default: 'Pulses'

## NumSamples

Number of samples in output

Specify the number of samples in the output of the step method as a positive integer. This property applies only when you set the OutputFormat property to 'Samples'.

Default: 100

## NumPulses

Number of pulses in output
Specify the number of pulses in the output of the step method as a positive integer. This property applies only when you set the OutputFormat property to 'Pulses'.

## Default: 1

## PRFOutputPort

Set this property to true to output the PRF for the current pulse using a step method argument.

## Dependencies

This property can be used only when the OutputFormat property is set to 'Pulses '.
Default: false

## Coefficients0utputPort

Enable matched filter coefficients output port
Enable the matched filter coefficients output port, specified as false or true. When you set this property to false, the object does not provide the matched filter coefficients used during the simulation as an output. When you set this property to true, the object provides the matched filter coefficients used during the simulation as an output.

Default: false

## Methods

| bandwidth | Bandwidth of rectangular pulse waveform |
| :--- | :--- |
| getMatchedFilter | Matched filter coefficients for waveform |
| plot | Plot rectangular pulse waveform |
| reset | Reset states of rectangular waveform object |
| step | Samples of rectangular pulse waveform |

## Common to All System Objects

```
release Allow System object property value changes
```


## Examples

Plot Rectangular Waveform and Spectrum
Create and plot a rectangular pulse waveform object and then plot its spectrum.

## Plot the waveform

Create and plot a pulse waveform. The sample rate is 500 kHz , the pulse width is 0.1 millisecond. The pulse repetition interval is twice the pulse duration.
fs = 500e3;
Create the rectangular waveform System object ${ }^{\mathrm{TM}}$.
sWF = phased.RectangularWaveform('SampleRate',fs,'PulseWidth',1e-4,'PRF',5000.0);
Use the step method to obtain the waveform. Then, plot the waveform.

```
rectwav = step(sWF);
nsamp = size(rectwav,1);
t = [0:(nsamp-1)]/fs;
plot(t*1000,real(rectwav))
xlabel('Time (millisec)')
ylabel('Amplitude')
grid
```



## Plot the spectrum

Compute the Fourier transform of the complex signal. Then show the spectrum.
nfft = 2^nextpow2(nsamp);
Z = fft(real(rectwav), nfft);
$\mathrm{fr}=$ [0:(nfft/2-1)]/nfft*fs;
plot(fr/1000,abs(Z(1:nfft/2)), ' . ' ' )
xlabel('Frequency (kHz)')
ylabel('Amplitude')
grid


## Plot the spectrogram

Plot a spectrogram of the function with a window size of 64 samples and $50 \%$ overlap. Window the signal with a Hamming function.
nfftl = 64;
nov $=$ floor(0.5*nfft1);
spectrogram(rectwav, hamming(nfft1), nov, nfft1,fs,'centered', 'yaxis')


This plot shows the constant frequency of the signal.

## Apply Frequency Offset to Rectangular Waveform

Apply a frequency offset to a rectangular pulse waveform. Plot the frequency spectrum of the waveform with and without a frequency offset applied.

Create a rectangular waveform object which is configured to set the frequency offset from an input when the object is executed.

```
fs = 500e3;
sRWF = phased.RectangularWaveform('SampleRate',fs,'PulseWidth',1e-4, ...
    'PRF',5000.0,'Frequency0ffsetSource','Input port');
```

Execute the object two times. First set the frequency offset set to 0 Hz , and then to 2 e 4 Hz .

```
rectwav = sRWF(0);
rectwav_foffset = sRWF(2e4);
```

Plot the frequency spectrum of the complex signals. The frequency offset signal is shifted to the right.

```
[Pxx,f] = pwelch(rectwav,[],[],[],fs,'centered');
[Pxx offset,foffset] = pwelch(rectwav foffset,[],[],[],fs,'centered');
plot(f/1000,Pxx,foffset/1000,Pxx_offset)
ylabel('PSD');
xlabel('Frequency (kHz)');
```

legend(\{'No offset','Offset applied'\},'Location','northwest'); grid on;


## Version History

Introduced in R2011a

## References

[1] Richards, M. A. Fundamentals of Radar Signal Processing. New York: McGraw-Hill, 2005.

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:

- The plot method is not supported.
- See "System Objects in MATLAB Code Generation" (MATLAB Coder).


## See Also

phased.LinearFMWaveform | phased.SteppedFMWaveform | phased. PhaseCodedWaveform

## Topics

Waveform Analysis Using the Ambiguity Function

## bandwidth

System object: phased.RectangularWaveform
Package: phased
Bandwidth of rectangular pulse waveform

## Syntax

BW = bandwidth(H)

## Description

$\mathrm{BW}=$ bandwidth(H) returns the bandwidth (in hertz) of the pulses for the rectangular pulse waveform, H . The bandwidth equals the reciprocal of the pulse width.

## Input Arguments

## H

Rectangular pulse waveform object.

## Output Arguments

BW
Bandwidth of the pulses, in hertz.

## Examples

## Find Bandwidth of Rectangular Pulse

Determine the bandwidth of a rectangular pulse waveform.

```
waveform = phased.RectangularWaveform;
```

bw = bandwidth(waveform)
$b w=20000$

## getMatchedFilter

System object: phased.RectangularWaveform
Package: phased
Matched filter coefficients for waveform

## Syntax

Coeff = getMatchedFilter(H)
Coeff = getMatchedFilter(H,'FrequencyOffset',FOFFSET)

## Description

Coeff = getMatchedFilter $(H)$ returns the matched filter coefficients for the rectangular waveform object H . Coeff is a column vector.

Coeff = getMatchedFilter(H,'FrequencyOffset', FOFFSET) adds a frequency offset when matched filter coefficients are generated. FOFFSET must be a scalar. This option is available when you set the FrequencyOffsetSource property to 'Input port' for the input object, H .

## Examples

## Matched Filter Coefficients for Rectangular Pulse

Get the matched filter coefficients for a rectangular pulse waveform.

```
waveform = phased.RectangularWaveform('PulseWidth',1e-5,\ldots.
    'OutputFormat','Pulses','NumPulses',1);
coeff = getMatchedFilter(waveform)
coeff = 10x1
```

    1
    1
    1
    1
    1
    1
    1
    1
    1
    1
    
## plot

System object: phased.RectangularWaveform
Package: phased
Plot rectangular pulse waveform

## Syntax

```
plot(Hwav)
plot(Hwav,Name,Value)
plot(Hwav,Name,Value,LineSpec)
h = plot(
```

$\qquad$

``` )
```


## Description

plot (Hwav) plots the real part of the waveform specified by Hwav.
plot (Hwav, Name, Value) plots the waveform with additional options specified by one or more Name, Value pair arguments.
plot (Hwav, Name, Value, LineSpec) specifies the same line color, line style, or marker options as are available in the MATLAB plot function.
h = plot( $\qquad$ ) returns the line handle in the figure.

## Input Arguments

## Hwav

Waveform object. This variable must be a scalar that represents a single waveform object.

## LineSpec

Character vector to specifies the same line color, style, or marker options as are available in the MATLAB plot function. If you specify a PlotType value of ' complex', then LineSpec applies to both the real and imaginary subplots.

Default: 'b'

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## PlotType

Specifies whether the function plots the real part, imaginary part, or both parts of the waveform. Valid values are 'real','imag', and 'complex'.

Default: 'real'

## PulseIdx

Index of the pulse to plot. This value must be a scalar.
Default: 1
FrequencyOffset
Frequency offset
Frequency offset in Hz , specified as a scalar.

## Dependencies

This property applies when you set the FrequencyOffsetSource property to 'Input port '.
Default: 0 Hz

## Output Arguments

## h

Handle to the line or lines in the figure. For a PlotType value of ' complex' h is a column vector. The first and second elements of this vector are the handles to the lines in the real and imaginary subplots, respectively.

## Examples

## Plot Rectangular Waveform

Create and plot a $100 \mu \mathrm{~s}$ rectangular pulse waveform.

```
waveform = phased.RectangularWaveform('PulseWidth',100e-6);
```

plot(waveform);


## reset

System object: phased.RectangularWaveform
Package: phased
Reset states of rectangular waveform object

## Syntax

reset (H)

## Description

reset $(\mathrm{H})$ resets the states of the RectangularWaveform object, H . Afterward, if the PRF property is a vector, the next call to step uses the first PRF value in the vector.

## step

System object: phased.RectangularWaveform
Package: phased
Samples of rectangular pulse waveform

## Syntax

$Y$ = step(sRFM)
Y = step(sRFM, prfidx)
$Y=$ step(sRFM,freqoffset)
[Y,PRF] = step (___)
[Y,COEFF] $=\operatorname{step}($ $\qquad$ )

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step (obj, x) and $y=o b j(x)$ perform equivalent operations. When the only argument to the step method is the System object itself, replace $y=\operatorname{step}(o b j)$ by $y=o b j()$.
$\mathrm{Y}=$ step(sRFM) returns samples of a rectangular pulse in the column vector Y .
$Y=$ step(sRFM, prfidx), uses the prfidx index to select the PRF from the predefined vector of values specified by the PRF property. This syntax applies when you set the PRFSelectionInputPort property to true.
$Y=s t e p(s R F M, f r e q o f f s e t)$, uses the freqoffset to generate the waveform with an offset as specified at step time. Use this syntax for cases where the transmit pulse frequency needs to be dynamically updated. This syntax applies when you set the FrequencyOffsetSource property to 'Input port'.
[Y,PRF] = step( ) also returns the current pulse repetition frequency, PRF. To enable this syntax, set the PRFOutputPort property to true and set the OutputFormat property to 'Pulses'.
[Y,COEFF] = step (__ ) returns the matched filter coefficients, COEFF, for the current pulse. To enable this syntax, set CoefficientsOutputPort to true. COEFF is returned as either an $N_{Z}$-by-1 vector or an $N_{\mathrm{Z}}$-by- M matrix.

- An $N_{Z}$-by-1 vector is returned when:
- The object has OutputFormat set to 'Pulses' and NumPulses is equal to $1 . N_{\mathrm{Z}}$ is the pulse width.
- The object is configured to generate constant pulse width waveforms
(DurationSpecification is set to 'Pulse width' or 'Duty cycle' and PRF has one unique value); and either OutputFormat is set to 'Pulses ' and NumPulses is greater than 1, or OutputFormat is set to 'Samples '. For this case, $N_{\mathrm{Z}}$ is the pulse width.
- An $N_{Z}$-by-M matrix is returned when the object generates varying pulse widths (DurationSpecification is set to 'Duty cycle' and PRF has more than one unique value); and either OutputFormat set to 'Pulses' and NumPulses is greater than 1, or OutputFormat is set to 'Samples'. For this case, $N_{Z}$ is the pulse width, and $M$ is the number of sub-pulses, NumSteps.

You can combine optional input and output arguments when their enabling properties are set. Optional inputs and outputs must be listed in the same order as the order of the enabling properties. For example, [Y,PRF,COEFF] = step(sRFM, prfidx,freqoffset).

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Examples

## Create Rectangular Waveform Pulse

Construct a 10 microseconds rectangular pulse with a pulse repetition interval of 100 microseconds.

```
Pulsewidth = 10e-6;
PRI = 100e-6;
sRFM = phased.RectangularWaveform('PulseWidth',Pulsewidth,...
    'OutputFormat','Pulses','NumPulses',1,...
    'SampleRate',1e6,'PRF',1/PRI);
wav = step(sRFM);
plot(wav)
xlabel('Time (\mu sec)')
ylabel('Amplitude')
grid
```



## Create Rectangular Pulses with Variable PRF

Construct rectangular waveforms with two pulses each. Set the sample rate to 1 MHz , a pulse width of 50 microseconds, and a duty cycle of $20 \%$. Vary the pulse repetition frequency.

Set the sample rate and PRF. The ratio of sample rate to PRF must be an integer.

```
fs = 1e6;
PRF = [10000,25000];
waveform = phased.RectangularWaveform('OutputFormat','Pulses','SampleRate',fs,...
    'DurationSpecification','Duty Cycle','DutyCycle',.2,...
    'PRF',PRF,'NumPulses',2,'PRFSelectionInputPort',true);
```

Obtain and plot the rectangular waveforms. For the first call to the step method, set the PRF to 10 kHz using the PRF index. For the next call, set the PRF to 25 kHz . For the final call, set the PRF to 10 kHz .

```
wav = [];
wav1 = waveform(1);
wav = [wav; wav1];
wav1 = waveform(2);
wav = [wav; wav1];
wav1 = waveform(1);
wav = [wav; wav1];
nsamps = size(wav,1);
```

```
t = [0:(nsamps-1)]/waveform.SampleRate;
plot(t*le6,real(wav))
xlabel('Time (\mu sec)')
ylabel('Amplitude')
grid
```



## Generate Matched Filter Coefficients of Rectangular Pulse Waveform

Generate output samples and matched filter coefficients of a rectangular pulse waveform.

```
waveform = phased.RectangularWaveform('CoefficientsOutputPort',true, ...
    'PRF',[1e4 2e4],'DurationSpecification','Duty cycle','DutyCycle',0.5, ...
    'OutputFormat','Pulses','NumPulses',2,'PRFSelectionInputPort',true);
[wav,coeff] = waveform(1);
```

Create a matched filter that applies the coefficients as an input argument. Use the coefficients when applying the matched filter to the waveform. Plot the waveform and matched filter outputs.

```
mf = phased.MatchedFilter('CoefficientsSource','Input port');
mf0ut = mf(wav,coeff(:,1));
subplot(211),plot(real(wav));
xlabel('Samples'),ylabel('Amplitude'),title('Waveform Output');
subplot(212),plot(abs(mf0ut));
xlabel('Samples'),ylabel('Amplitude'),title('Matched Filter Output');
```



## phased.ReplicatedSubarray

Package: phased
Phased array formed by replicated subarrays

## Description

The ReplicatedSubarray object represents a phased array that contains copies of a subarray created by replicating a single specified array.

To obtain the response of the subarrays:
1 Define and set up your phased array containing replicated subarrays. See "Construction" on page 1-1426.
2 Call step to compute the response of the subarrays according to the properties of phased.ReplicatedSubarray. The behavior of step is specific to each object in the toolbox.

You can also use a ReplicatedSubarray object as the value of the SensorArray or Sensor property of objects that perform beamforming, steering, and other operations.

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step $(\mathrm{obj}, \mathrm{x})$ and $\mathrm{y}=\mathrm{obj}(\mathrm{x})$ perform equivalent operations.

## Construction

H = phased.ReplicatedSubarray creates a replicated subarray System object, H. This object represents an array that contains copies of a subarray.

H = phased.ReplicatedSubarray(Name, Value) creates a replicated subarray object, H, with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN).

## Properties

## Subarray

Subarray to replicate
Specify the subarray you use to form the array. The subarray must be a phased.ULA, phased.URA, or phased. ConformalArray object.

Default: phased.ULA with default property values

## Layout

Layout of subarrays
Specify the layout of the replicated subarrays as 'Rectangular' or 'Custom'.

## Default: 'Rectangular'

## GridSize

Size of rectangular grid
Specify the size of the rectangular grid as a single positive integer or 1-by-2 positive integer row vector. This property applies only when you set the Layout property to 'Rectangular'.

If GridSize is a scalar, the array has the same number of subarrays in each row and column.
If GridSize is a 1-by-2 vector, the vector has the form [NumberOfRows, NumberOfColumns]. The first entry is the number of subarrays along each column, while the second entry is the number of subarrays in each row. A row is along the local $y$-axis, and a column is along the local $z$-axis. This figure shows how a 3-by-2 URA subarray is replicated using a GridSize value of [1,2].
$3 \times 2$ Element URA
Replicated on a $1 \times 2$ Grid


Default: [1 2]

## GridSpacing

Spacing of rectangular grid
Specify the rectangular grid spacing of subarrays as a positive real-valued scalar, a 1-by-2 row vector, or 'Auto'. This property applies only when you set the Layout property to 'Rectangular'. Grid spacing units are expressed in meters.

If GridSpacing is a scalar, the spacing along the row and the spacing along the column is the same.
If GridSpacing is a length- 2 row vector, it has the form [SpacingBetweenRows,
SpacingBetweenColumn]. The first entry specifies the spacing between rows along a column. The second entry specifies the spacing between columns along a row.

If GridSpacing is 'Auto' , the replication preserves the element spacing in both row and column. This option is available only if you use a phased.ULA or phased. URA object as the subarray.

Default: 'Auto'
SubarrayPosition
Subarray positions in custom grid

Specify the positions of the subarrays in the custom grid. This property value is a 3-by-N matrix, where N indicates the number of subarrays in the array. Each column of the matrix represents the position of a single subarray in the array's local coordinate system, in meters, using the form [x; y; z].

This property applies when you set the Layout property to 'Custom '.
Default: [0 0; -0.5 0.5; 0 0]

## SubarrayNormal

Subarray normal directions in custom grid
Specify the normal directions of the subarrays in the array. This property value is a 2 -by- N matrix, where N is the number of subarrays in the array. Each column of the matrix specifies the normal direction of the corresponding subarray, in the form [azimuth; elevation]. Each angle is in degrees and is defined in the local coordinate system.

You can use the SubarrayPosition and SubarrayNormal properties to represent any arrangement in which pairs of subarrays differ by certain transformations. The transformations can combine translation, azimuth rotation, and elevation rotation. However, you cannot use transformations that require rotation about the normal.

This property applies when you set the Layout property to 'Custom '.
Default: [0 0; 0 0]

## SubarraySteering

Subarray steering method
Specify the method of subarray steering as either 'None'|'Phase'|'Time'|'Custom'.

- When you set this property to 'Phase', a phase shifter is used to steer the subarray. Use the STEERANG argument of the step method to define the steering direction.
- When you set this property to 'Time', subarrays are steered using time delays. Use the STEERANG argument of the step method to define the steering direction.
- When you set this property to 'Custom', subarrays are steered by setting independent weights for all elements in each subarray. Use the WS argument of the step method to define the weights for all subarrays.

Default: 'None'

## PhaseShifterFrequency

Subarray phase shifter frequency
Specify the operating frequency of phase shifters that perform subarray steering. The property value is a positive scalar in hertz. This property applies when you set the SubarraySteering property to 'Phase'.

Default: 3e8
NumPhaseShifterBits
Number of phase shifter quantization bits

The number of bits used to quantize the phase shift component of beamformer or steering vector weights. Specify the number of bits as a non-negative integer. A value of zero indicates that no quantization is performed.

## Default: 0

## Methods

| Specific to phased. ReplicatedSubarray Object |  |
| :--- | :--- |
| beamwidth | Compute and display beamwidth for a subarray |
| collectPla <br> neWave | Simulate received plane waves |
| directivit <br> y | Directivity of replicated subarray |
| getElement <br> Position | Positions of array elements |
| getNumElem <br> ents | Number of elements in array |
| getNumSuba <br> rrays | Number of subarrays in array |
| getSubarra <br> yPosition | Positions of subarrays in array |
| isPolariza <br> tionCapabl <br> e | Polarization capability |
| pattern | Plot replicated subarray directivity and patterns |
| patternAzi <br> muth | Plot replicated subarray directivity or pattern versus azimuth |
| patternEle <br> vation | Plot replicated subarray directivity or pattern versus elevation |
| plotRespon <br> se | Plot response pattern of array |
| step | Output responses of subarrays |
| viewArray | View array geometry |

## Common to All System Objects

| release | Allow System object property value changes |
| :--- | :--- |

## Examples

## Azimuth Response of Array with Subarrays

Plot the azimuth response of a 4 -element ULA composed of two 2-element ULAs. By default, the antenna elements are isotropic.

```
sArray = phased.ULA('NumElements',2,'ElementSpacing',0.5);
sRSA = phased.ReplicatedSubarray('Subarray',sArray,...
    'Layout','Rectangular','GridSize',[1 2],...
    'GridSpacing','Auto');
```

Plot the azimuth response of the array. Assume the operating frequency is 1 GHz and the wave propagation speed is the speed of light.

```
fc = 1.0e9;
pattern(sRSA,fc,[-180:180],0,...
    'PropagationSpeed',physconst('LightSpeed'),...
    'Type','powerdb',...
    'Normalize',true,...
    'CoordinateSystem','polar')
```



Normalized Power (dB), Broadside at $0.00^{\circ}$

## Response of Subarrays with Polarized Antenna Elements

Create a 4 -element ULA from two 2 -element ULA subarrays consisting of short-dipole antenna elements. Then, calculate the response at boresight. Because the array elements support polarization, the response consists of horizontal and vertical components.

Create the arrays from subarrays.
sSD = phased.ShortDipoleAntennaElement;
sULA = phased.ULA('Element',sSD,...

```
    'NumElements',2,...
    'ElementSpacing',0.5);
sRSA = phased.ReplicatedSubarray('Subarray',sULA,...
    'Layout','Rectangular',...
    'GridSize',[1 2],...
    'GridSpacing','Auto');
```

Show the vertical polarization response for the subarrays.

```
fc = 1.0e9;
ang = [0;0];
resp = step(sRSA,fc,ang,physconst('LightSpeed'));
disp(resp.V)
```

    -2.4495
    -2.4495
    
## Independently Steered Replicated Subarrays

Create an array consisting of three copies of a 4-element ULA having elements spaced $1 / 2$ wavelength apart. The array operates at 300 MHz .

```
c = physconst('LightSpeed');
fc = 300e6;
lambda = c/fc;
subarray = phased.ULA(4,0.5*lambda);
```

Steer all subarrays by a common phase shift to 10 degrees azimuth.

```
array = phased.ReplicatedSubarray('Subarray',subarray,'GridSize',[1 3], ...
    SubarraySteering','Phase','PhaseShifterFrequency',fc);
steer_ang = [10;0];
sv_ar`
    'PropagationSpeed',c);
wts_array = sv_array(fc,steer_ang);
pat\overline{t}ern(array,\overline{fc,-90:90,0,'CoōrdinateSystem','Rectangular',...}
    'Type','powerdb','PropagationSpeed',c,'Weights',wts_array,...
    'SteerAngle',steer_ang);
legend('phase-shifted subarrays')
```



Compute independent subarray weights from subarray steering vectors. The weights point to 5,15 , and 30 degrees azimuth. Set the SubarraySteering property to 'Custom ' .
steer_ang_subarrays = [5 15 30;0 0 0];
sv_sub̄array = phased.SteeringVector('SensorArray', subarray,...
'PropagationSpeed',c);
wc = sv_subarray(fc,steer_ang_subarrays);
array.SūbarraySteering = 'Custom';
pattern(array,fc,-90:90,0,'CoordinateSystem', 'Rectangular',...
'Type','powerdb','PropagationSpeed', c, 'Weights',wts_array,...
'ElementWeight', conj(wc));
legend('independent subarrays')
hold off


## Version History

Introduced in R2012a

## References

[1] Mailloux, Robert J. Electronically Scanned Arrays. San Rafael, CA: Morgan \& Claypool Publishers, 2007.
[2] Mailloux, Robert J. Phased Array Antenna Handbook, 2nd Ed. Norwood, MA: Artech House, 2005.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:

- pattern, patternAzimuth, patternElevation, plotResponse, and viewArray methods are not supported.
- See "System Objects in MATLAB Code Generation" (MATLAB Coder).


## See Also

## Objects

phased.ULA | phased.URA | phased.UCA | phased.ConformalArray |
phased. PartitionedArray

## Apps <br> Sensor Array Analyzer

## Topics

Subarrays in Phased Array Antennas
Phased Array Gallery
"Subarrays Within Arrays"

## directivity

System object: phased.ReplicatedSubarray
Package: phased
Directivity of replicated subarray

## Syntax

D = directivity (H,FREQ,ANGLE)
D = directivity (H, FREQ, ANGLE, Name, Value)

## Description

D = directivity ( $\mathrm{H}, \mathrm{FREQ}$, ANGLE) returns the "Directivity (dBi)" on page 1-1437 of a replicated array of antenna or microphone element, H , at frequencies specified by FREQ and in angles of direction specified by ANGLE.

The integration used when computing array directivity has a minimum sampling grid of 0.1 degrees. If an array pattern has a beamwidth smaller than this, the directivity value will be inaccurate.

D = directivity (H, FREQ, ANGLE, Name, Value) returns the directivity with additional options specified by one or more Name, Value pair arguments.

## Input Arguments

## H - Replicated subarray

System object
Replicated subarray, specified as a phased.ReplicatedSubarray System object.
Example: H = phased.ReplicatedSubarray;

## FREQ - Frequency for computing directivity and patterns

positive scalar | 1-by-L real-valued row vector
Frequencies for computing directivity and patterns, specified as a positive scalar or 1-by-L realvalued row vector. Frequency units are in hertz.

- For an antenna, microphone, or sonar hydrophone or projector element, FREQ must lie within the range of values specified by the FrequencyRange or FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased.CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: [1e8 2e6]
Data Types: double

## ANGLE - Angles for computing directivity

## 1-by-M real-valued row vector | 2-by-M real-valued matrix

Angles for computing directivity, specified as a 1-by- $M$ real-valued row vector or a 2 -by- $M$ real-valued matrix, where $M$ is the number of angular directions. Angle units are in degrees. If ANGLE is a 2 -by- $M$ matrix, then each column specifies a direction in azimuth and elevation, [az;el]. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

If ANGLE is a 1 -by- $M$ vector, then each entry represents an azimuth angle, with the elevation angle assumed to be zero.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the xy plane. This angle is positive when measured from the $x$-axis toward the $y$-axis. The elevation angle is the angle between the direction vector and xy plane. This angle is positive when measured towards the $z$-axis. See "Azimuth and Elevation Angles".
Example: [45 60; 0 10]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Namel=Value1, ... ,NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## PropagationSpeed - Signal propagation speed

speed of light (default) | positive scalar
Signal propagation speed, specified as the comma-separated pair consisting of
'PropagationSpeed ' and a positive scalar in meters per second.
Example: 'PropagationSpeed', physconst('LightSpeed')
Data Types: double
Weights - Subarray weights
1 (default) | $N$-by-1 complex-valued column vector | $N$-by- $L$ complex-valued matrix
Subarray weights, specified as the comma-separated pair consisting of 'Weights' and an $N$-by-1 complex-valued column vector or $N$-by- $M$ complex-valued matrix. The dimension $N$ is the number of subarrays in the array. The dimension $L$ is the number of frequencies specified by the FREQ argument.

| Weights dimension | FREQ dimension | Purpose |
| :--- | :--- | :--- |
| $N$-by-1 complex-valued column <br> vector | Scalar or 1-by-L row vector | Applies a set of weights for the <br> single frequency or for all $L$ <br> frequencies. |
| $N$-by- $L$ complex-valued matrix | 1-by-L row vector | Applies each of the $L$ columns of <br> 'Weights' for the <br> corresponding frequency in the <br> FREQ argument. |

Example: 'Weights', ones ( $\mathrm{N}, \mathrm{M}$ )

## Data Types: double

## SteerAngle - Subarray steering angle

[0;0] (default) | scalar | 2-element column vector
Subarray steering angle, specified as the comma-separated pair consisting of 'SteerAngle' and a scalar or a 2-by-1 column vector.

If 'SteerAngle' is a 2 -by- 1 column vector, it has the form [azimuth; elevation]. The azimuth angle must be between $-180^{\circ}$ and $180^{\circ}$, inclusive. The elevation angle must be between $-90^{\circ}$ and $90^{\circ}$, inclusive.

If 'SteerAngle' is a scalar, it specifies the azimuth angle only. In this case, the elevation angle is assumed to be 0 .

This option applies only when the 'SubarraySteering ' property of the System object is set to 'Phase' or 'Time'.

Example: 'SteerAngle', [20;30]
Data Types: double

## ElementWeights - Weights applied to elements within subarray <br> 1 (default) | complex-valued $N_{S E}$-by- $N$ matrix

Subarray element weights, specified as complex-valued $N_{S E}$-by- $N$ matrix. Weights are applied to the individual elements within a subarray. All subarrays have the same dimensions and sizes. $N_{S E}$ is the number of elements in each subarray and $N$ is the number of subarrays. Each column of the matrix specifies the weights for the corresponding subarray.

## Dependencies

To enable this name-value pair, set the SubarraySteering property of the array to 'Custom '.

```
Data Types: double
Complex Number Support: Yes
```


## Output Arguments

## D - Directivity

$M$-by-L matrix
Directivity, returned as an $M$-by- $L$ matrix. Each row corresponds to one of the $M$ angles specified by ANGLE. Each column corresponds to one of the $L$ frequency values specified in FREQ. Directivity units are in dBi where dBi is defined as the gain of an element relative to an isotropic radiator.

## Examples

## Directivity of Replicated Subarray

Compute the directivity of an array built up from ULA subarrays. Determine the directivity of the replicated subarray when the array is steered to towards 30 degrees azimuth.

Set the signal propagation speed to the speed of light. Set the signal frequency to 300 MHz .

```
c = physconst('LightSpeed');
fc = 3e8;
lambda = c/fc;
```

Create a 4-element ULA of isotropic antenna elements spaced 0.4 -wavelength apart.

```
myArray = phased.ULA;
myArray.NumElements = 4;
myArray.ElementSpacing = 0.4*lambda;
```


## Construct a 2-by-1 replicated subarray.

```
myRepArray = phased.ReplicatedSubarray;
myRepArray.Subarray = myArray;
myRepArray.Layout = 'Rectangular';
myRepArray.GridSize = [2 1];
myRepArray.GridSpacing = 'Auto';
myRepArray.SubarraySteering = 'Time';
```

Steer the array to 30 degrees azimuth and zero degrees elevation.

```
ang = [30;0];
mySV = phased.SteeringVector;
mySV.SensorArray = myRepArray;
mySV.PropagationSpeed = c;
```

Find the directivity at 30 degrees azimuth.

```
d = directivity(myRepArray,fc,ang,...
    'PropagationSpeed',c,...
    'Weights',step(mySV,fc,ang),...
    'SteerAngle',ang)
d = 7.4776
```


## More About

## Directivity (dBi)

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## See Also

patternElevation | patternAzimuth | pattern

## collectPlaneWave

System object: phased.ReplicatedSubarray
Package: phased
Simulate received plane waves

## Syntax

```
Y = collectPlaneWave(H,X,ANG)
Y = collectPlaneWave(H,X,ANG,FREQ)
Y = collectPlaneWave(H,X,ANG,FREQ,C)
```


## Description

$Y=\operatorname{collectPlaneWave}(H, X, A N G)$ returns the received signals at the sensor array, $H$, when the input signals indicated by $X$ arrive at the array from the directions specified in ANG.
$Y=$ collectPlaneWave ( $H, X$, ANG, $F R E Q$ ), in addition, specifies the incoming signal carrier frequency in FREQ.
$Y=\operatorname{collectPlaneWave}(H, X, A N G, F R E Q, C)$, in addition, specifies the signal propagation speed in C.

## Input Arguments

## H

Array object.
X
Incoming signals, specified as an M-column matrix. Each column of $X$ represents an individual incoming signal.

## ANG

Directions from which incoming signals arrive, in degrees. ANG can be either a 2-by-M matrix or a row vector of length $M$.

If ANG is a 2-by-M matrix, each column specifies the direction of arrival of the corresponding signal in X. Each column of ANG is in the form [azimuth; elevation]. The azimuth angle must be between $-180^{\circ}$ and $180^{\circ}$, inclusive. The elevation angle must be between $-90^{\circ}$ and $90^{\circ}$, inclusive.

If ANG is a row vector of length M , each entry in ANG specifies the azimuth angle. In this case, the corresponding elevation angle is assumed to be $0^{\circ}$.

FREQ
Carrier frequency of signal in hertz. FREQ must be a scalar.
Default: 3e8

## C

Propagation speed of signal in meters per second.
Default: Speed of light

## Output Arguments

## Y

Received signals. Y is an N -column matrix, where N is the number of subarrays in the array H. Each column of $Y$ is the received signal at the corresponding subarray, with all incoming signals combined.

## Examples

## Plane Waves Received at Array of Subarrays

Simulate the received signal at a 16 -element ULA composed of four 4 -element ULAs.

```
array = phased.ULA('NumElements',4);
subarrays = phased.ReplicatedSubarray('Subarray',array,'GridSize',[4 1]);
```

Simulate two signals received from $10^{\circ}$ azimuth and $30^{\circ}$ azimuth. Both signals have an elevation angle of $0^{\circ}$. Assume the propagation speed is the speed of light and the carrier frequency of the signal is 100 MHz .

```
y = collectPlaneWave(subarrays,randn(4,2),[10 30],100.0e6,...
    physconst('LightSpeed'));
```


## Algorithms

collectPlaneWave modulates the input signal with a phase corresponding to the delay caused by the direction of arrival. This method does not account for the response of individual elements in the array and only models the array factor among subarrays. Therefore, the result does not depend on whether the subarray is steered.

## See Also <br> uv2azel | phitheta2azel

## getElementPosition

System object: phased.ReplicatedSubarray
Package: phased
Positions of array elements

## Syntax

POS = getElementPosition(H)

## Description

POS = getElementPosition $(H)$ returns the element positions in the array $H$.

## Input Arguments

H
Array object consisting of replicated subarrays.

## Output Arguments

## POS

Element positions in array. POS is a 3-by-N matrix, where N is the number of elements in H . Each column of POS defines the position of an element in the local coordinate system, in meters, using the form [ $\mathrm{x} ; \mathrm{y} ; \mathrm{z}$ ].

## Examples

## Positions of Elements in Array with Replicated Subarrays

Create an array with two copies of a 3-element ULA, and obtain the positions of the elements.
subarrays $=$ phased.ReplicatedSubarray('Subarray',...
phased.ULA('NumElements',3),'GridSize',[1 2]);
pos $=$ getElementPosition(subarrays)
pos $=3 \times 6$
$-1.2500$
0 - 0
$\begin{array}{llllll}0 & 0 & 0 & 0 & 0 & 0\end{array}$
0
-0.7500
0
-0.2500
0
0.2500
0
0.7500
1.2500

## See Also

getSubarrayPosition

## getNumElements

System object: phased.ReplicatedSubarray
Package: phased
Number of elements in array

## Syntax

N = getNumElements(H)

## Description

$N=$ getNumElements( $H$ ) returns the number of elements in the array object $H$. This number includes the elements in all subarrays of the array.

## Input Arguments

## H

Array object consisting of replicated subarrays.

## Examples

## Number of Elements in Array with Replicated Subarrays

Create an array with two copies of a 3 -element ULA, and obtain the total number of elements.
subarray $=$ phased.ReplicatedSubarray('Subarray',...
phased.ULA('NumElements',3),'GridSize',[1 2]);
$\mathrm{N}=$ getNumElements(subarray)
$N=6$

## See Also

getNumSubarrays

## getNumSubarrays

System object: phased.ReplicatedSubarray
Package: phased
Number of subarrays in array

## Syntax

N = getNumSubarrays(H)

## Description

$N=$ getNumSubarrays(H) returns the number of subarrays in the array object H .

## Input Arguments

H
Array object consisting of replicated subarrays.

## Examples

## Number of Subarrays in Array

Create an array by tiling copies of a ULA in a 2 -by- 5 grid. Then, obtain the number of subarrays.
subarrays $=$ phased.ReplicatedSubarray('Subarray',...
phased.ULA('NumElements',3),'GridSize',[2 5]);
$\mathrm{N}=$ getNumSubarrays(subarrays)
$\mathrm{N}=10$

## See Also

getNumElements

## getSubarrayPosition

System object: phased.ReplicatedSubarray
Package: phased
Positions of subarrays in array

## Syntax

POS = getSubarrayPosition(H)

## Description

POS = getSubarrayPosition(H) returns the subarray positions in the array H .

## Input Arguments

H
Partitioned array object.

## Output Arguments

## POS

Subarrays positions in array. POS is a 3-by-N matrix, where N is the number of subarrays in H. Each column of POS defines the position of a subarray in the local coordinate system, in meters, using the form [ $\mathrm{x} ; \mathrm{y} ; \mathrm{z}$ ].

## Examples

## Replicated Subarray Positions

Create an array with two copies of a 3 -element ULA, and obtain the positions of the subarrays.

```
subarray = phased.ReplicatedSubarray('Subarray',...
    phased.ULA('NumElements',3),'GridSize',[1 2]);
pos = getSubarrayPosition(subarray)
pos = 3\times2
```

| 0 | 0 |
| ---: | ---: |
| -0.7500 | 0.7500 |
| 0 | 0 |

## See Also

getElementPosition

## isPolarizationCapable

System object: phased.ReplicatedSubarray
Package: phased
Polarization capability

## Syntax

flag = isPolarizationCapable(h)

## Description

flag = isPolarizationCapable(h) returns a Boolean value, flag, indicating whether the array supports polarization. An array supports polarization if all of its constituent sensor elements support polarization.

## Input Arguments

## h - Replicated subarray

Replicated subarray specified as a phased.ReplicatedSubarray System object.

## Output Arguments

## flag - Polarization-capability flag

Polarization-capability flag returned as a Boolean value true if the array supports polarization or false if it does not.

## Examples

## Replicated Array of Short Dipoles Supports Polarization

Verify that a replicated subarray of short-dipole antenna elements supports polarization.

```
antenna = phased.ShortDipoleAntennaElement('FrequencyRange',[le9 10e9]);
array = phased.URA([3,2],'Element',antenna);
reparray = phased.ReplicatedSubarray('Subarray',array, ...
    'Layout','Rectangular','GridSize',[1,2],'GridSpacing','Auto');
isPolarizationCapable(reparray)
ans = logical
    1
```


## pattern

System object: phased. ReplicatedSubarray
Package: phased
Plot replicated subarray directivity and patterns

## Syntax

```
pattern(sArray,FREQ)
pattern(sArray,FREQ,AZ)
pattern(sArray,FREQ,AZ,EL)
pattern(__,Name,Value)
[PAT,AZ_ANG,EL_ANG] = pattern(
```

$\qquad$

``` )
```


## Description

pattern (sArray, FREQ) plots the 3-D array directivity pattern (in dBi) for the array specified in sArray. The operating frequency is specified in FREQ.

The integration used when computing array directivity has a minimum sampling grid of 0.1 degrees. If an array pattern has a beamwidth smaller than this, the directivity value will be inaccurate.
pattern(sArray, FREQ, AZ) plots the array directivity pattern at the specified azimuth angle.
pattern(sArray, $\mathrm{FREQ}, \mathrm{AZ}, \mathrm{EL}$ ) plots the array directivity pattern at specified azimuth and elevation angles.
pattern( $\qquad$ ,Name, Value) plots the array pattern with additional options specified by one or more Name, Value pair arguments.
[PAT,AZ_ANG,EL_ANG] = pattern( __ ) returns the array pattern in PAT. The AZ_ANG output contains the coordinate values corresponding to the rows of PAT. The EL_ANG output contains the coordinate values corresponding to the columns of PAT. If the 'CoordinateSystem' parameter is set to ' $u v$ ' , then AZ_ANG contains the $U$ coordinates of the pattern and EL_ANG contains the $V$ coordinates of the pattern. Otherwise, they are in angular units in degrees. $U V$ units are dimensionless.

Note This method replaces the plotResponse method. See "Convert plotResponse to pattern" on page 1-1454 for guidelines on how to use pattern in place of plotResponse.

## Input Arguments

## sArray - Replicated subarray

System object
Replicated subarray, specified as a phased.ReplicatedSubarray System object.
Example: sArray= phased.ReplicatedSubarray;

## FREQ - Frequency for computing directivity and patterns

positive scalar | 1-by-L real-valued row vector
Frequencies for computing directivity and patterns, specified as a positive scalar or 1-by-L realvalued row vector. Frequency units are in hertz.

- For an antenna, microphone, or sonar hydrophone or projector element, FREQ must lie within the range of values specified by the FrequencyRange or FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased. CustomAntennaElement and phased.CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

```
Example: [1e8 2e6]
```

Data Types: double

## AZ - Azimuth angles

[-180:180] (default) | 1-by- $N$ real-valued row vector
Azimuth angles for computing directivity and pattern, specified as a 1-by- $N$ real-valued row vector where $N$ is the number of azimuth angles. Angle units are in degrees. Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the $x y$ plane. When measured from the $x$-axis toward the $y$-axis, this angle is positive.

## Example: [-45:2:45]

Data Types: double

## EL - Elevation angles

[-90:90] (default) | 1-by-M real-valued row vector
Elevation angles for computing directivity and pattern, specified as a 1-by-M real-valued row vector where $M$ is the number of desired elevation directions. Angle units are in degrees. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

The elevation angle is the angle between the direction vector and $x y$-plane. The elevation angle is positive when measured towards the $z$-axis.

Example: [-75:1:70]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

```
CoordinateSystem - Plotting coordinate system
'polar' (default)|'rectangular'|'uv'
```

Plotting coordinate system of the pattern, specified as the comma-separated pair consisting of 'CoordinateSystem' and one of 'polar', 'rectangular', or 'uv'. When
'CoordinateSystem' is set to 'polar' or 'rectangular', the AZ and EL arguments specify the pattern azimuth and elevation, respectively. AZ values must lie between $-180^{\circ}$ and $180^{\circ}$. EL values must lie between $-90^{\circ}$ and $90^{\circ}$. If 'CoordinateSystem' is set to ' uv ', AZ and EL then specify $U$ and $V$ coordinates, respectively. AZ and EL must lie between -1 and 1 .
Example: 'uv'
Data Types: char

## Type - Displayed pattern type

'directivity' (default)|'efield'|'power'|'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb' - power pattern converted to dB.

Example: 'powerdb'
Data Types: char

## Orientation - Array orientation

[0;0;0]. (default) | 3-by-1 real-valued column vector
Array orientation, specified as a 3-by-1 real-valued column vector containing the rotation angles with respect to the $x-y$-, and $z$-axes of the local coordinate system, respectively.

## Normalize - Display normalize pattern

true (default) | false
Display normalized pattern, specified as the comma-separated pair consisting of 'Normalize' and a Boolean. Set this parameter to true to display a normalized pattern. This parameter does not apply when you set 'Type' to 'directivity'. Directivity patterns are already normalized.
Data Types: logical

## ShowArray - View array geometry

false (default) | true
View the array geometry along with the 3D radiation pattern, specified as false or true.
Data Types: logical
ShowLocalCoordinates - Show local coordinate axes
true (default) | false
Show the local coordinate axes, specified as true or false.
Data Types: logical

## ShowColorbar - Show colorbar <br> true (default) | false

Show the colorbar, specified as true or false.
Data Types: logical

## Parent - Handle to axis

scalar
Handle to the axes along which the array geometry is displayed specified as a scalar.

## PlotStyle - Plotting style

'overlay' (default)| 'waterfall'
Plotting style, specified as the comma-separated pair consisting of 'Plotstyle' and either ' overlay' or 'waterfall'. This parameter applies when you specify multiple frequencies in FREQ in 2-D plots. You can draw 2-D plots by setting one of the arguments AZ or EL to a scalar.

## Data Types: char

## Polarization - Polarized field component

'combined' (default) | 'H' | 'V'
Polarized field component to display, specified as the comma-separated pair consisting of 'Polarization' and 'combined ', 'H' , or 'V'. This parameter applies only when the sensors are polarization-capable and when the 'Type' parameter is not set to 'directivity'. This table shows the meaning of the display options.

| 'Polarization' | Display |
| :--- | :--- |
| ' combined ' | Combined $H$ and $V$ polarization components |
| 'H' | $H$ polarization component |
| ' $\mathrm{V}^{\prime}$ | $V$ polarization component |

Example: 'V '
Data Types: char
PropagationSpeed - Signal propagation speed
speed of light (default) | positive scalar
Signal propagation speed, specified as the comma-separated pair consisting of ' PropagationSpeed ' and a positive scalar in meters per second.
Example: 'PropagationSpeed', physconst('LightSpeed')
Data Types: double

## Weights - Subarray weights

1 (default) | $N$-by-1 complex-valued column vector | $N$-by-L complex-valued matrix
Subarray weights, specified as the comma-separated pair consisting of 'Weights' and an $N$-by- 1 complex-valued column vector or $N$-by- $M$ complex-valued matrix. The dimension $N$ is the number of subarrays in the array. The dimension $L$ is the number of frequencies specified by the FREQ argument.

| Weights dimension | FREQ dimension | Purpose |
| :--- | :--- | :--- |
| $N$-by-1 complex-valued column <br> vector | Scalar or 1-by- $L$ row vector | Applies a set of weights for the <br> single frequency or for all $L$ <br> frequencies. |
| $N$-by- $L$ complex-valued matrix | 1-by- $L$ row vector | Applies each of the $L$ columns of <br> 'Weights' for the <br> corresponding frequency in the <br> FREQ argument. |

## Example: 'Weights', ones ( $\mathrm{N}, \mathrm{M}$ )

Data Types: double

## SteerAngle - Subarray steering angle

[0;0] (default) | scalar | 2-element column vector
Subarray steering angle, specified as the comma-separated pair consisting of 'SteerAngle' and a scalar or a 2-by-1 column vector.

If 'SteerAngle' is a 2-by-1 column vector, it has the form [azimuth; elevation]. The azimuth angle must be between $-180^{\circ}$ and $180^{\circ}$, inclusive. The elevation angle must be between $-90^{\circ}$ and $90^{\circ}$, inclusive.

If 'SteerAngle' is a scalar, it specifies the azimuth angle only. In this case, the elevation angle is assumed to be 0 .

This option applies only when the 'SubarraySteering ' property of the System object is set to 'Phase' or 'Time'.
Example: 'SteerAngle', [20;30]
Data Types: double
ElementWeights - Weights applied to elements within subarray
1 (default) | complex-valued $N_{S E}$-by- $N$ matrix
Subarray element weights, specified as complex-valued $N_{S E}$-by- $N$ matrix. Weights are applied to the individual elements within a subarray. All subarrays have the same dimensions and sizes. $N_{S E}$ is the number of elements in each subarray and $N$ is the number of subarrays. Each column of the matrix specifies the weights for the corresponding subarray.

## Dependencies

To enable this name-value pair, set the SubarraySteering property of the array to 'Custom '.
Data Types: double
Complex Number Support: Yes

## Output Arguments

## PAT - Array pattern

$M$-by- $N$ real-valued matrix
Array pattern, returned as an $M$-by- $N$ real-valued matrix. The dimensions of PAT correspond to the dimensions of the output arguments AZ_ANG and EL_ANG.

## AZ_ANG - Azimuth angles

scalar | 1-by- $N$ real-valued row vector
Azimuth angles for displaying directivity or response pattern, returned as a scalar or 1-by-N realvalued row vector corresponding to the dimension set in AZ. The columns of PAT correspond to the values in AZ_ANG. Units are in degrees.

## EL_ANG - Elevation angles

scalar | 1-by-M real-valued row vector
Elevation angles for displaying directivity or response, returned as a scalar or 1-by-M real-valued row vector corresponding to the dimension set in EL. The rows of PAT correspond to the values in EL_ANG. Units are in degrees.

## Examples

## Azimuth Response of Array with Subarrays

Plot the azimuth response of a 4 -element ULA composed of two 2-element ULAs. By default, the antenna elements are isotropic.

```
sArray = phased.ULA('NumElements',2,'ElementSpacing',0.5);
sRSA = phased.ReplicatedSubarray('Subarray',sArray,...
    'Layout','Rectangular','GridSize',[1 2],...
    'GridSpacing','Auto');
```

Plot the azimuth response of the array. Assume the operating frequency is 1 GHz and the wave propagation speed is the speed of light.

```
fc = 1.0e9;
pattern(sRSA,fc,[-180:180],0,...
    'PropagationSpeed',physconst('LightSpeed'),...
    'Type','powerdb',...
    'Normalize',true,...
    'CoordinateSystem','polar')
```



Normalized Power (dB), Broadside at $0.00^{\circ}$

## Directivity of Array with Subarrays

Create a 2-by-2-element URA of isotropic antenna elements, and arrange four copies to form a 16element URA. Plot the 3-D directivity pattern.

## Create the array

```
fmin = 1e9;
fmax = 6e9;
c = physconst('LightSpeed');
lam = c/fmax;
sIso = phased.IsotropicAntennaElement(...
    'FrequencyRange',[fmin,fmax],...
    'BackBaffled',false);
sURA = phased.URA('Element',sIso,...
    'Size',[2 2],...
    'ElementSpacing',lam/2);
sRS = phased.ReplicatedSubarray('Subarray',sURA,...
    'Layout','Rectangular','GridSize',[2 2],...
    'GridSpacing','Auto');
```

Plot 3-D directivity pattern

```
fc = 1e9;
wts = [0.862,1.23,1.23,0.862]';
```

```
pattern(sRS,fc,[-180:180],[-90:90],...
    'PropagationSpeed',physconst('LightSpeed'), ....
    'Type','directivity',...
    'Weights',wts);
```



## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\text {rad }}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Convert plotResponse to pattern

For antenna, microphone, and array System objects, the pattern method replaces the plotResponse method. In addition, two new simplified methods exist just to draw 2-D azimuth and elevation pattern plots. These methods are azimuthPattern and elevationPattern.

The following table is a guide for converting your code from using plotResponse to pattern. Notice that some of the inputs have changed from input arguments to Name-Value pairs and conversely. The general pattern method syntax is
pattern(H,FREQ,AZ,EL,'Name1','Value1',...,' $N a m e N ', ' V a l u e N ') ~$

| plotResponse Inputs | plotResponse Description | pattern Inputs |
| :--- | :--- | :--- |
| H argument | Antenna, microphone, or array <br> System object. | H argument (no change) |
| FREQ argument | Operating frequency. | FREQ argument (no change) |
| V argument | Propagation speed. This argument <br> is used only for arrays. | 'PropagationSpeed ' name-value <br> pair. This parameter is only used for <br> arrays. |


| plotResponse Inputs | plotResponse Description |  | pattern Inputs |  |
| :---: | :---: | :---: | :---: | :---: |
| 'Format' and 'RespCut' namevalue pairs | These options work together to let you create a plot in angle space (line or polar style) or $U V$ space. They also determine whether the plot is 2-D or 3-D. This table shows you how to create different types of plots using plotResponse. |  | 'CoordinateSystem' name-value pair used together with the AZ and EL input arguments. <br> 'CoordinateSystem' has the same options as the plotResponse method 'Format ' name-value pair, except that ' line' is now named 'rectangular'. The table shows how to create different types of plots using pattern. |  |
|  | Display space <br> Angle space (2D) |  |  |  |
|  | Angle space (2D) | Set 'RespCut' <br> to 'Az' or |  |  |
|  |  | 'El'. Set <br> 'Format ' to <br> 'line' or 'polar'. | Display space |  |
|  |  | ' line' or 'polar'. <br> Set the display axis using either the 'AzimuthAngle | Angle space (2D) | Set <br> Coordinate <br> System' to <br> rectangular' <br> or 'polar' <br> Specify either AZ <br> or EL as a scalar. |
|  |  | s' or 'ElevationAng les' namevalue pairs. | Angle space (3D) | Set <br> 'Coordinate <br> System' to 'rectangular' |
|  | Angle space (3D) | Set 'RespCut' to '3D'. Set |  | or 'polar'. <br> Specify both AZ <br> and EL as <br> vectors. |
|  |  | 'polar'. <br> Set the display axis using both the 'AzimuthAngle s' and 'Elevation | $U V$ space (2D) | Set <br> Coordinate System' to uv'. Use AZ to specify a $U$ space vector. Use EL to specify a $V$-space scalar. |
|  |  | Angles' namevalue pairs. | UV space (3D) |  |
|  | UV space (2D) | Set 'RespCut' to'U'. Set 'Format ' to 'UV'. Set the display range using the 'UGrid' namevalue pair. |  | 'Coordinate <br> System' to <br> 'uv'. Use AZ to <br> specify a $U$ - <br> space vector. <br> Use EL to specify <br> a $V$-space vector. |
|  |  |  | If you set CoordinateSystem to 'uv ' , enter the UV grid values using $A Z$ and $E L$. |  |
|  | UV space (3D) | $\begin{aligned} & \text { Set 'RespCut' } \\ & \text { to'3D'. Set } \\ & \text { 'Format' to } \end{aligned}$ |  |  |


| plotResponse Inputs | plotResponse Description |  | pattern Inputs |
| :---: | :---: | :---: | :---: |
|  | Display space | 'UV '. Set the display range using both the 'UGrid' and 'VGrid ' namevalue pairs. |  |
| 'CutAngle' name-value pair | Constant angle at to take an azimuth or elevation cut. When producing a 2-D plot and when 'RespCut' is set to 'Az' or 'El', use 'CutAngle' to set the slice across which to view the plot. |  | No equivalent name-value pair. To create a cut, specify either AZ or EL as a scalar, not a vector. |
| 'NormalizeResponse' namevalue pair | Normalizes the plot. When 'Unit' is set to 'dbi' , you cannot specify 'NormalizeResponse'. |  | Use the 'Normalize' name-value pair. When 'Type' is set to 'directivity' you cannot specify 'Normalize'. |
| 'OverlayFreq' name-value pair | Plot multiple frequencies on the same 2-D plot. Available only when 'Format' is set to 'line' or 'uv and 'RespCut' is not set to '3D'. The value true produces an overlay plot and the value false produces a waterfall plot. |  | 'PlotStyle' name-value pair plots multiple frequencies on the same 2-D plot. <br> The values 'overlay' and 'waterfall' correspond to 'OverlayFreq' values of true and false. The option 'waterfall' is allowed only when 'CoordinateSystem' is set to 'rectangular' or 'uv'. |
| 'Polarization' name-value pair | Determines how to plot polarized fields. Options are 'None', 'Combined', 'H', or 'V'. |  | 'Polarization ' name-value pair determines how to plot polarized fields. The 'None ' option is removed. The options 'Combined ' , ' H ', or 'V' are unchanged. |
| ' Unit ' name-value pair | Determines the plot units. Choose 'db','mag', 'pow', or 'dbi', where the default is ' db ' |  | 'Type ' name-value pair, uses equivalent options with different names |
|  |  |  | plotResponse pattern |
|  |  |  | 'db' 'powerdb' <br> 'mag' 'efield' <br> 'pow' 'power' <br> 'dbi' 'directivity' |
| 'Weights ' name-value pair | Array element tapers (or weights). |  | 'Weights ' name-value pair (no change). |
| 'AzimuthAngles ' name-value pair | Azimuth angles used to display the antenna or array response. |  | AZ argument |


| plotResponse Inputs | plotResponse Description | pattern Inputs |
| :--- | :--- | :--- |
| ' ElevationAngles ' name-value <br> pair | Elevation angles used to display the <br> antenna or array response. | EL argument |
| ' UGrid' name-value pair | Contains $U$ coordinates in $U V$ - <br> space. | AZ argument when <br> 'CoordinateSystem ' name-value <br> pair is set to 'uv ' |
| 'VGrid' name-value pair | Contains $V$-coordinates in $U V$-space. | EL argument when <br> 'CoordinateSystem ' name-value <br> pair is set to 'uv ' |

## Version History <br> Introduced in R2015a

See Also<br>patternElevation| patternAzimuth

## patternAzimuth

System object: phased. ReplicatedSubarray
Package: phased
Plot replicated subarray directivity or pattern versus azimuth

## Syntax

```
patternAzimuth(sArray,FREQ)
patternAzimuth(sArray,FREQ,EL)
patternAzimuth(sArray,FREQ,EL,Name,Value)
PAT = patternAzimuth(
```

$\qquad$

``` )
```


## Description

patternAzimuth (sArray, FREQ) plots the 2-D array directivity pattern versus azimuth (in dBi) for the array sArray at zero degrees elevation angle. The argument FREQ specifies the operating frequency.

The integration used when computing array directivity has a minimum sampling grid of 0.1 degrees. If an array pattern has a beamwidth smaller than this, the directivity value will be inaccurate.
patternAzimuth(sArray, FREQ,EL), in addition, plots the 2-D array directivity pattern versus azimuth (in dBi) for the array sArray at the elevation angle specified by $E L$. When $E L$ is a vector, multiple overlaid plots are created.
patternAzimuth(sArray, FREQ,EL,Name, Value) plots the array pattern with additional options specified by one or more Name, Value pair arguments.

PAT = patternAzimuth( $\qquad$ ) returns the array pattern. PAT is a matrix whose entries represent the pattern at corresponding sampling points specified by the 'Azimuth ' parameter and the EL input argument.

## Input Arguments

## sArray - Replicated subarray

System object
Replicated subarray, specified as a phased.ReplicatedSubar ray System object.

```
Example: sArray= phased.ReplicatedSubarray;
```


## FREQ - Frequency for computing directivity and pattern

positive scalar
Frequency for computing directivity and pattern, specified as a positive scalar. Frequency units are in hertz.

- For an antenna or microphone element, FREQ must lie within the range of values specified by the FrequencyRange or the FrequencyVector property of the element. Otherwise, the element
produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased.CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: 1e8
Data Types: double

## EL - Elevation angles

## 1-by- $N$ real-valued row vector

Elevation angles for computing sensor or array directivities and patterns, specified as a 1-by- $N$ realvalued row vector. The quantity $N$ is the number of requested elevation directions. Angle units are in degrees. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

The elevation angle is the angle between the direction vector and the xy plane. When measured toward the $z$-axis, this angle is positive.
Example: [0, 10, 20]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Type - Displayed pattern type

'directivity' (default)|'efield'|'power'|'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb' - power pattern converted to dB.

Example: 'powerdb'
Data Types: char

## PropagationSpeed - Signal propagation speed

## speed of light (default) | positive scalar

Signal propagation speed, specified as the comma-separated pair consisting of ' PropagationSpeed ' and a positive scalar in meters per second.
Example: 'PropagationSpeed', physconst('LightSpeed')
Data Types: double

## Weights - Subarray weights

M-by-1 complex-valued column vector
Subarray weights, specified as the comma-separated pair consisting of 'Weights ' and an $M$-by-1 complex-valued column vector. Subarray weights are applied to the subarrays of the array to produce array steering, tapering, or both. The dimension $M$ is the number of subarrays in the array.

Example: 'Weights', ones (10,1)
Data Types: double
Complex Number Support: Yes

## SteerAngle - Subarray steering angle

[0;0] (default) | scalar | 2 -element column vector
Subarray steering angle, specified as the comma-separated pair consisting of 'SteerAngle' and a scalar or a 2-by-1 column vector.

If 'SteerAngle' is a 2 -by- 1 column vector, it has the form [azimuth; elevation]. The azimuth angle must be between $-180^{\circ}$ and $180^{\circ}$, inclusive. The elevation angle must be between $-90^{\circ}$ and $90^{\circ}$, inclusive.

If 'SteerAngle' is a scalar, it specifies the azimuth angle only. In this case, the elevation angle is assumed to be 0 .

This option applies only when the 'SubarraySteering ' property of the System object is set to 'Phase' or 'Time'.

Example: 'SteerAngle', [20;30]
Data Types: double

## ElementWeights - Weights applied to elements within subarray

1 (default) | complex-valued $N_{S E}$-by- $N$ matrix
Subarray element weights, specified as complex-valued $N_{S E}$-by- $N$ matrix. Weights are applied to the individual elements within a subarray. All subarrays have the same dimensions and sizes. $N_{S E}$ is the number of elements in each subarray and $N$ is the number of subarrays. Each column of the matrix specifies the weights for the corresponding subarray.

## Dependencies

To enable this name-value pair, set the SubarraySteering property of the array to 'Custom '.

```
Data Types: double
Complex Number Support: Yes
```

Azimuth - Azimuth angles
[-180:180] (default) | 1-by-P real-valued row vector
Azimuth angles, specified as the comma-separated pair consisting of 'Azimuth' and a 1-by-P realvalued row vector. Azimuth angles define where the array pattern is calculated.

Example: 'Azimuth', [-90:2:90]
Data Types: double

## Parent - Handle to axis

scalar

Handle to the axes along which the array geometry is displayed specified as a scalar.

## Output Arguments

## PAT - Array directivity or pattern

$L$-by- $N$ real-valued matrix
Array directivity or pattern, returned as an $L$-by- $N$ real-valued matrix. The dimension $L$ is the number of azimuth values determined by the 'Azimuth' name-value pair argument. The dimension $N$ is the number of elevation angles, as determined by the EL input argument.

## Examples

## Azimuth Pattern of Array with Subarrays

Create a 2-element ULA of isotropic antenna elements, and arrange three copies to form a 6 -element ULA. Plot the directivity azimuth pattern within a restricted range of azimuth angles from -30 to 30 degrees in 0.1 degree increments. Plot directivity for 0 degrees and 45 degrees elevation.

## Create the array

```
fmin = 1e9;
fmax = 6e9;
c = physconst('LightSpeed');
lam = c/fmax;
sIso = phased.IsotropicAntennaElement(...
    'FrequencyRange',[fmin,fmax],...
    'BackBaffled',false);
sULA = phased.ULA('Element',sIso,...
    'NumElements',2,'ElementSpacing',0.5);
sRS = phased.ReplicatedSubarray('Subarray',sULA,...
    'Layout','Rectangular','GridSize',[1 3],...
    'GridSpacing','Auto');
```


## Plot azimuth directivity pattern

```
fc = 1e9;
wts = [0.862,1.23,0.862]';
patternAzimuth(sRS,fc,[0,45],'PropagationSpeed',physconst('LightSpeed'),...
    'Azimuth',[-30:0.1:30],...
    'Type','directivity',...
    'Weights',wts);
```



Directivity (dBi), Broadside at $0.00^{\circ}$

## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Version History

Introduced in R2015a

## See Also

patternElevation|pattern

## patternElevation

System object: phased.ReplicatedSubarray
Package: phased
Plot replicated subarray directivity or pattern versus elevation

## Syntax

```
patternElevation(sArray,FREQ)
patternElevation(sArray,FREQ,AZ)
patternElevation(sArray,FREQ,AZ,Name,Value)
PAT = patternElevation(
```

$\qquad$

``` )
```


## Description

patternElevation(sArray, FREQ) plots the 2-D array directivity pattern versus elevation (in dBi ) for the array sArray at zero degrees azimuth angle. When AZ is a vector, multiple overlaid plots are created. The argument FREQ specifies the operating frequency.

The integration used when computing array directivity has a minimum sampling grid of 0.1 degrees. If an array pattern has a beamwidth smaller than this, the directivity value will be inaccurate.
patternElevation(sArray, FREQ, AZ), in addition, plots the 2-D element directivity pattern versus elevation (in dBi ) at the azimuth angle specified by $A Z$. When $A Z$ is a vector, multiple overlaid plots are created.
patternElevation(sArray, FREQ,AZ, Name, Value) plots the array pattern with additional options specified by one or more Name, Value pair arguments.

PAT = patternElevation ( _ ) returns the array pattern. PAT is a matrix whose entries represent the pattern at corresponding sampling points specified by the 'Elevation' parameter and the AZ input argument.

## Input Arguments

## sArray - Replicated subarray

System object
Replicated subarray, specified as a phased.ReplicatedSubarray System object.

```
Example: sArray= phased.ReplicatedSubarray;
```


## FREQ - Frequency for computing directivity and pattern

positive scalar
Frequency for computing directivity and pattern, specified as a positive scalar. Frequency units are in hertz.

- For an antenna or microphone element, FREQ must lie within the range of values specified by the FrequencyRange or the FrequencyVector property of the element. Otherwise, the element
produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased.CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: 1e8
Data Types: double

## AZ - Azimuth angles for computing directivity and pattern

1-by- $N$ real-valued row vector
Azimuth angles for computing sensor or array directivities and patterns, specified as a 1 -by- $N$ realvalued row vector where $N$ is the number of desired azimuth directions. Angle units are in degrees. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the $x y$ plane. This angle is positive when measured from the $x$-axis toward the $y$-axis.
Example: [0,10,20]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Type - Displayed pattern type

'directivity' (default)|'efield'|'power'|'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb' - power pattern converted to dB.

Example: 'powerdb'
Data Types: char

## PropagationSpeed - Signal propagation speed

speed of light (default) | positive scalar
Signal propagation speed, specified as the comma-separated pair consisting of ' PropagationSpeed ' and a positive scalar in meters per second.
Example: 'PropagationSpeed', physconst('LightSpeed')
Data Types: double

## Weights - Subarray weights

M-by-1 complex-valued column vector
Subarray weights, specified as the comma-separated pair consisting of 'Weights ' and an $M$-by-1 complex-valued column vector. Subarray weights are applied to the subarrays of the array to produce array steering, tapering, or both. The dimension $M$ is the number of subarrays in the array.

Example: 'Weights', ones (10,1)
Data Types: double
Complex Number Support: Yes

## SteerAngle - Subarray steering angle

[0;0] (default) | scalar | 2 -element column vector
Subarray steering angle, specified as the comma-separated pair consisting of 'SteerAngle' and a scalar or a 2-by-1 column vector.

If 'SteerAngle' is a 2 -by- 1 column vector, it has the form [azimuth; elevation]. The azimuth angle must be between $-180^{\circ}$ and $180^{\circ}$, inclusive. The elevation angle must be between $-90^{\circ}$ and $90^{\circ}$, inclusive.

If 'SteerAngle' is a scalar, it specifies the azimuth angle only. In this case, the elevation angle is assumed to be 0 .

This option applies only when the 'SubarraySteering ' property of the System object is set to 'Phase' or 'Time'.

Example: 'SteerAngle', [20;30]
Data Types: double

## ElementWeights - Weights applied to elements within subarray

1 (default) | complex-valued $N_{S E}$-by- $N$ matrix
Subarray element weights, specified as complex-valued $N_{S E}$-by- $N$ matrix. Weights are applied to the individual elements within a subarray. All subarrays have the same dimensions and sizes. $N_{S E}$ is the number of elements in each subarray and $N$ is the number of subarrays. Each column of the matrix specifies the weights for the corresponding subarray.

## Dependencies

To enable this name-value pair, set the SubarraySteering property of the array to 'Custom '.

## Data Types: double <br> Complex Number Support: Yes

## Elevation - Elevation angles

[-90:90] (default) | 1-by-P real-valued row vector
Elevation angles, specified as the comma-separated pair consisting of 'Elevation' and a 1-by-P real-valued row vector. Elevation angles define where the array pattern is calculated.

Example: 'Elevation', [-90:2:90]
Data Types: double

## Parent - Handle to axis

scalar

Handle to the axes along which the array geometry is displayed specified as a scalar.

## Output Arguments

## PAT - Array directivity or pattern

$L$-by- $N$ real-valued matrix
Array directivity or pattern, returned as an $L$-by- $N$ real-valued matrix. The dimension $L$ is the number of elevation angles determined by the 'Elevation' name-value pair argument. The dimension $N$ is the number of azimuth angles determined by the $A Z$ argument.

## Examples

## Elevation Pattern of Array with Subarrays

Create a 2-by-2-element URA of isotropic antenna elements, and arrange four copies to form a 16element URA. Plot the elevation directivity pattern within a restricted range of elevation angles from -45 to 45 degrees in 0.1 degree increments. Plot directivity for 0 degrees and 15 degrees azimuth.

## Create the array

```
fmin = 1e9;
fmax = 6e9;
c = physconst('LightSpeed');
lam = c/fmax;
sIso = phased.IsotropicAntennaElement(...
    'FrequencyRange',[fmin,fmax],...
    'BackBaffled',false);
sURA = phased.URA('Element',sIso,...
    'Size',[2 2],...
    'ElementSpacing',lam/2);
sRS = phased.ReplicatedSubarray('Subarray',sURA,...
    'Layout','Rectangular','GridSize',[2 2],...
    'GridSpacing','Auto');
```


## Plot elevation directivity pattern

```
fc = 1e9;
wts = [0.862,1.23,1.23,0.862]';
patternElevation(sRS,fc,[0,15],...
    'PropagationSpeed',physconst('LightSpeed'),...
    'Elevation',[-45:0.1:45],...
    'Type','directivity',...
    'Weights',wts);
```



Directivity (dBi), Broadside at $0.00^{\circ}$

## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Version History

Introduced in R2015a

## See Also

patternAzimuth | pattern

## plotResponse

System object: phased.ReplicatedSubarray
Package: phased
Plot response pattern of array

## Syntax

plotResponse( H, FREQ, V )
plotResponse(H, FREQ, V, Name, Value)
hPlot = plotResponse( $\qquad$ )

## Description

plotResponse ( $\mathrm{H}, \mathrm{FREQ}, \mathrm{V}$ ) plots the array response pattern along the azimuth cut, where the elevation angle is 0 . The operating frequency is specified in FREQ. The propagation speed is specified in $V$.
plotResponse(H, FREQ, V,Name, Value) plots the array response with additional options specified by one or more Name, Value pair arguments.
hPlot = plotResponse( $\qquad$ ) returns handles of the lines or surface in the figure window, using any of the input arguments in the previous syntaxes.

## Input Arguments

## H

Array object.

## FREQ

Operating frequency, in hertz. Typical values are within the range specified by a property of H.Subarray.Element. That property is named FrequencyRange or FrequencyVector, depending on the type of element in the array. The element has zero response at frequencies outside that range. If FREQ is a nonscalar row vector, the plot shows multiple frequency responses on the same axes.

## V

Propagation speed in meters per second.

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, ... , NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## CutAngle

Cut angle specified as a scalar. This argument is applicable only when RespCut is ' Az ' or ' El '. If RespCut is 'Az', CutAngle must be between -90 and 90. If RespCut is 'El', CutAngle must be between -180 and 180.

Default: 0

## Format

Format of the plot, using one of 'Line', 'Polar', or 'UV'. If you set Format to 'UV', FREQ must be a scalar.

## Default: 'Line'

## NormalizeResponse

Set this value to true to normalize the response pattern. Set this value to false to plot the response pattern without normalizing it. This parameter is not applicable when you set the Unit parameter value to 'dbi'.

## Default: true

## OverlayFreq

Set this value to true to overlay pattern cuts in a 2-D line plot. Set this value to false to plot pattern cuts against frequency in a 3-D waterfall plot. If this value is false, then FREQ must be a vector with at least two entries.

This parameter applies only when Format is not 'Polar' and RespCut is not '3D'.

## Default: true

## Polarization

Specify the polarization options for plotting the array response pattern. The allowable values are |'None' | 'Combined' | 'H' | 'V' | where:

- 'None ' specifies plotting a nonpolarized response pattern
- 'Combined ' specifies plotting a combined polarization response pattern
- 'H' specifies plotting the horizontal polarization response pattern
- 'V' specifies plotting the vertical polarization response pattern

For arrays that do not support polarization, the only allowed value is 'None '. This parameter is not applicable when you set the Unit parameter value to 'dbi'.

Default: 'None'

## RespCut

Cut of the response. Valid values depend on Format, as follows:

- If Format is 'Line' or 'Polar', the valid values of RespCut are 'Az', 'El', and '3D'. The default is ' Az '.
- If Format is 'UV', the valid values of RespCut are 'U' and '3D'. The default is 'U'.

If you set RespCut to ' 3 D ' , FREQ must be a scalar.

## SteerAng

Subarray steering angle. SteerAng can be either a 2 -element column vector or a scalar.
If SteerAng is a 2 -element column vector, it has the form [azimuth; elevation]. The azimuth angle must be between -180 and 180 degrees, inclusive. The elevation angle must be between -90 and 90 degrees, inclusive.

If SteerAng is a scalar, it specifies the azimuth angle. In this case, the elevation angle is assumed to be 0 .

This option is applicable only if the SubarraySteering property of H is 'Phase' or 'Time '.
Default: [0;0]

## Unit

The unit of the plot. Valid values are 'db', 'mag', 'pow', or 'dbi'. This parameter determines the type of plot that is produced.

| Unit value | Plot type |
| :--- | :--- |
| db | power pattern in dB scale |
| mag | field pattern |
| pow | power pattern |
| dbi | directivity |

Default: 'db'
Weights
Weight values applied to the array, specified as a length- $N$ column vector or $N$-by- $M$ matrix. The dimension $N$ is the number of subarrays in the array. The interpretation of $M$ depends upon whether the input argument FREQ is a scalar or row vector.

| Weights Dimension | FREQ Dimension | Purpose |
| :--- | :--- | :--- |
| $N$-by-1 column vector | Scalar or 1-by-M row vector | Apply one set of weights for the <br> same single frequency or all $M$ <br> frequencies. |
| $N$-by- $M$ matrix | Scalar | Apply all of the $M$ different <br> columns in Weights for the <br> same single frequency. |
|  | 1-by- $M$ row vector | Apply each of the $M$ different <br> columns in Weights for the <br> corresponding frequency in <br> FREQ. |

## AzimuthAngles

Azimuth angles for plotting subarray response, specified as a row vector. The AzimuthAngles parameter sets the display range and resolution of azimuth angles for visualizing the radiation pattern. This parameter is allowed only when the RespCut parameter is set to 'Az' or '3D' and the Format parameter is set to 'Line' or 'Polar'. The values of azimuth angles should lie between $180^{\circ}$ and $180^{\circ}$ and must be in nondecreasing order. When you set the RespCut parameter to ' 3 D ', you can set the AzimuthAngles and ElevationAngles parameters simultaneously.

Default: [-180:180]

## ElevationAngles

Elevation angles for plotting subarray response, specified as a row vector. The ElevationAngles parameter sets the display range and resolution of elevation angles for visualizing the radiation pattern. This parameter is allowed only when the RespCut parameter is set to 'El' or '3D' and the Format parameter is set to 'Line' or 'Polar'. The values of elevation angles should lie between $90^{\circ}$ and $90^{\circ}$ and must be in nondecreasing order. When you set the RespCut parameter to '3D ', you can set the ElevationAngles and AzimuthAngles parameters simultaneously.

Default: [-90:90]

## UGrid

$U$ coordinate values for plotting subarray response, specified as a row vector. The UGrid parameter sets the display range and resolution of the $U$ coordinates for visualizing the radiation pattern in $U / V$ space. This parameter is allowed only when the Format parameter is set to ' UV' and the RespCut parameter is set to ' $U$ ' or ' $3 D$ '. The values of $U G$ rid should be between -1 and 1 and should be specified in nondecreasing order. You can set the UGrid and VGrid parameters simultaneously.

Default: [-1:0.01:1]

## VGrid

$V$ coordinate values for plotting subarray response, specified as a row vector. The VGrid parameter sets the display range and resolution of the $V$ coordinates for visualizing the radiation pattern in $U / V$ space. This parameter is allowed only when the Format parameter is set to ' UV ' and the RespCut parameter is set to ' 3 D '. The values of VGrid should be between -1 and 1 and should be specified in nondecreasing order. You can set the VGrid and UGrid parameters simultaneously.

Default: [-1:0.01:1]

## Examples

## Azimuth Response and Directivity of ULA with Subarrays

Plot the azimuth response of a 4 -element ULA composed of two 2-element ULAs.
Create a 2 -element ULA, and arrange two copies to form a 4 -element ULA.

```
h = phased.ULA('NumElements',2,'ElementSpacing',0.5);
ha = phased.ReplicatedSubarray('Subarray',h,...
    'Layout','Rectangular','GridSize',[1 2],...
    'GridSpacing','Auto');
```

Plot the azimuth response of the array. Assume the operating frequency is 1 GHz and the wave propagation speed is $3 \mathrm{e} 8 \mathrm{~m} / \mathrm{s}$.

```
plotResponse(ha,1e9,3e8,'RespCut','Az','Format','Polar');
```



Normalized Power (dB), Broadside at $0.00^{\circ}$
Plot the azimuth directivity of the array.

```
plotResponse(ha,1e9,3e8,'RespCut','Az','Format','Polar','Unit','dbi');
```



Directivity (dBi), Broadside at $0.00^{\circ}$

## Display Azimuth Response of Array with Subarrays Between -30 and $\mathbf{3 0}$ Degrees

Create a 2 -element ULA, and arrange two copies to form a 4 -element ULA. Using the
AzimuthAngles parameter, plot the response within a restricted range of azimuth angles from -30 to 30 degrees in 0.1 degree increments.

```
h = phased.ULA('NumElements',2,'ElementSpacing',0.5);
ha = phased.ReplicatedSubarray('Subarray',h,...
    'Layout','Rectangular','GridSize',[1 2],...
    'GridSpacing','Auto');
plotResponse(ha,1e9,3e8,'RespCut','Az','Format','Polar',...
    'AzimuthAngles',[-30:0.1:30],'Unit','mag');
```



Normalized Magnitude, Broadside at $0.00^{\circ}$

## Apply Two Sets of Weights at a Single Frequency

Construct an array of replicated subarrays. Start with a 2 -element uniform line array (ULA), and duplicate it 5 times to create a 10 -element ULA. Apply both uniform weights and tapered weights. Then, use plotResponse to show that the tapered set of weights reduces the adjacent sidelobes while broadening the main lobe.

```
h = phased.ULA('NumElements',2,'ElementSpacing',0.2);
ha = phased.ReplicatedSubarray('Subarray',h,...
    'Layout','Rectangular','GridSize',[1 5],...
    'GridSpacing',0.4);
c = physconst('LightSpeed');
fc = 1e9;
wts1 = [0.2,0.2,0.2,0.2,0.2]';
wts2 = [0.1,0.23333,.33333,0.23333,0.1]';
plotResponse(ha,fc,c,'RespCut','Az','Format','Polar',...
    'Weights',[wts1,wts2]);
```



Normalized Power (dB), Broadside at $0.00^{\circ}$

## See Also

uv2azel|azel2uv

## step

System object: phased.ReplicatedSubarray<br>Package: phased<br>Output responses of subarrays

## Syntax

RESP $=$ step $(H, F R E Q, A N G, V)$
RESP $=\operatorname{step}(\mathrm{H}, \mathrm{FREQ}, \mathrm{ANG}, \mathrm{V}, \mathrm{STEERANGLE})$
RESP $=\operatorname{step}(H, F R E Q, A N G, V, W S)$

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.

RESP $=$ step ( $\mathrm{H}, \mathrm{FREQ}, \mathrm{ANG}, \mathrm{V}$ ) returns the responses, RESP, of the subarrays in the array, at operating frequencies specified in FREQ and directions specified in ANG. V is the propagation speed. The elements within each subarray are connected to the subarray phase center using an equal-path feed.

RESP $=$ step ( H, FREQ, ANG, V, STEERANGLE) uses STEERANGLE as the steering direction of the subarray. This syntax is available when you set the SubarraySteering property to either 'Phase' or 'Time'.

RESP $=$ step ( $H$, FREQ, ANG , V, WS ) uses WS as the subarray element weights. This syntax is available when you set the SubarraySteering property to 'Custom'.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## H

Phased array formed by replicated subarrays.

## FREQ

Operating frequencies of array in hertz. FREQ is a row vector of length $L$. Typical values are within the range specified by a property of H . Subarray. Element. That property is named

FrequencyRange or FrequencyVector, depending on the type of element in the array. The element has zero response at frequencies outside that range.

## ANG

Directions in degrees. ANG can be either a 2-by-M matrix or a row vector of length M.
If ANG is a 2 -by-M matrix, each column of the matrix specifies the direction in the form [azimuth; elevation]. The azimuth angle must be between -180 and 180 degrees, inclusive. The elevation angle must be between -90 and 90 degrees, inclusive.

If ANG is a row vector of length M , each element specifies a direction's azimuth angle. In this case, the corresponding elevation angle is assumed to be 0 .

## V

Propagation speed in meters per second. This value must be a scalar.

## STEERANGLE

Subarray steering direction. STEERANGLE can be either a 2 -element column vector or a scalar.
If this argument is a 2 -element column vector, it has the form [azimuth; elevation]. The azimuth angle must be between $-180^{\circ}$ and $180^{\circ}$, inclusive. The elevation angle must be between $-90^{\circ}$ and $90^{\circ}$, inclusive.

If STEERANGLE is a scalar, it specifies the direction's azimuth angle. In this case, the elevation angle is assumed to be $0^{\circ}$.

## Dependencies

To enable this argument, set the SubarraySteering to 'Phase' or 'Time'.

## WS

Subarray element weights
Subarray element weights, specified as complex-valued $N_{S E}$-by- $N$ matrix. Weights are applied to the individual elements within a subarray. All subarrays have the same dimensions and sizes. $N_{S E}$ is the number of elements in each subarray and $N$ is the number of subarrays. Each column of the matrix specifies the weights for the corresponding subarray.

## Dependencies

To enable this argument, set the SubarraySteering to 'Custom ' .

## Output Arguments

## RESP

Voltage responses of the subarrays of the phased array. The output depends on whether the array supports polarization or not.

- If the array is not capable of supporting polarization, the voltage response, RESP, has the dimensions $N$-by- $M$-by- $L$. The first dimension, $N$, represents the number of subarrays in the phased array, the second dimension, $M$, represents the number of angles specified in ANG, while $L$
represents the number of frequencies specified in FREQ. Each column of RESP contains the responses of the subarrays for the corresponding direction specified in ANG. Each of the $L$ pages of RESP contains the responses of the subarrays for the corresponding frequency specified in FREQ.
- If the array is capable of supporting polarization, the voltage response, RESP, is a MATLAB struct containing two fields, RESP. H and RESP.V, each having dimensions $N$-by- $M$-by-L. The field, RESP.H, represents the array's horizontal polarization response, while RESP.V represents the array's vertical polarization response. The first dimension, $N$, represents the number of subarrays in the phased array, the second dimension, $M$, represents the number of angles specified in ANG, while $L$ represents the number of frequencies specified in FREQ. Each of the M columns contains the responses of the subarrays for the corresponding direction specified in ANG. Each of the $L$ pages contains the responses of the subarrays for the corresponding frequency specified in FREQ.


## Examples

## Subarray Response

Calculate the response at boresight for two 2 -element ULA arrays that form subarrays of a 4 -element ULA array of short-dipole antenna elements.

Create a two-element ULA of short-dipole antenna elements. Then, arrange two copies to form a 4element ULA.

```
antenna = phased.ShortDipoleAntennaElement;
array = phased.ULA('Element',antenna,'NumElements',2,'ElementSpacing',0.5);
replicatedarray = phased.ReplicatedSubarray('Subarray',array,...
    'Layout','Rectangular','GridSize',[1 2],...
    'GridSpacing','Auto');
```

Find the response of each subarray at boresight. Assume the operating frequency is 1 GHz and the wave propagation speed is the speed of light.

```
c = physconst('LightSpeed');
resp = replicatedarray(1.0e9,[0;0],c)
resp = struct with fields:
    H: [2x1 double]
    V: [2x1 double]
```


## Independently Steered Replicated Subarrays

Create an array consisting of three copies of a 4 -element ULA having elements spaced $1 / 2$ wavelength apart. The array operates at 300 MHz .

```
c = physconst('LightSpeed');
fc = 300e6;
lambda = c/fc;
subarray = phased.ULA(4,0.5*lambda);
```

Steer all subarrays by a common phase shift to 10 degrees azimuth.

```
array = phased.ReplicatedSubarray('Subarray',subarray,'GridSize',[1 3], ...
    'SubarraySteering','Phase','PhaseShifterFrequency',fc);
steer_ang = [10;0];
sv_array = phased.SteeringVector('SensorArray',array,...
    'PropagationSpeed',c);
wts_array = sv_array(fc,steer_ang);
pat\overline{t}ern(array,\overline{fc,-90:90,0,'CoōrdinateSystem','Rectangular',...}
    'Type','powerdb','PropagationSpeed',c,'Weights',wts_array,...
    'SteerAngle',steer_ang);
legend('phase-shifted subarrays')
```



Compute independent subarray weights from subarray steering vectors. The weights point to 5,15 , and 30 degrees azimuth. Set the SubarraySteering property to 'Custom ' .

```
steer_ang_subarrays = [5 15 30;0 0 0];
sv_su\overline{b}arräy = phased.SteeringVector('SensorArray',subarray,...
    'PropagationSpeed',c);
wc = sv_subarray(fc,steer_ang_subarrays);
array.SūbarraySteering = 'Custom';
pattern(array,fc,-90:90,0,'CoordinateSystem','Rectangular',...
    'Type','powerdb','PropagationSpeed ',c,'Weights',wts_array,...
    'ElementWeight',conj(wc));
legend('independent subarrays')
hold off
```



See Also
uv2azel | phitheta2azel

## viewArray

System object: phased.ReplicatedSubarray
Package: phased
View array geometry

## Syntax

```
viewArray(H)
viewArray(H,Name,Value)
hPlot = viewArray(
```

$\qquad$

``` )
```


## Description

viewArray (H) plots the geometry of the array specified in H .
viewArray ( $\mathrm{H}, \mathrm{Name}$, Value) plots the geometry of the array, with additional options specified by one or more Name, Value pair arguments.
hPlot = viewArray( $\qquad$ ) returns the handles of the array elements in the figure window. All input arguments described for the previous syntaxes also apply here.

## Input Arguments

## H

Array object.

## Name-Value Pair Arguments

Specify optional pairs of arguments as Namel=Value1, . . . ,NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Parent

Handle to the axes along which the array geometry is displayed.

## ShowNormals

Set this value to true to show the normal directions of all elements of the array. Set this value to false to plot the elements without showing normal directions.

Default: false

## ShowLocalCoordinates

Logical flag specifying whether to show the local coordinate axes.

Default: true

## ShowAnnotation

Logical flag specifying whether to show the annotations in the UI panel of the figure. Annotation shows aperture size and element spacing based on array axis of array.

Default: true

## Orientation

Orientation of the array, specified as a 3-by-1 column vector containing the rotation angles with respect to the $\mathrm{x}-\mathrm{y}$-, and z -axes of the local coordinate system, respectively. The default value is [0;0;0].

Default: [0;0;0]

## ShowTaper

Set this value to true to specify whether to change the element color brightness in proportion to the element taper magnitude. When this value is set to false, all elements are drawn with the same color.

Default: false

## ShowIndex

Vector specifying the element indices to show in the figure. Each number in the vector must be an integer between 1 and the number of elements. You can also specify the value as 'All' to show indices of all elements of the array or 'None' to suppress indices.

Default: 'None'

## ShowSubarray

Vector specifying the indices of subarrays to highlight in the figure. Each number in the vector must be an integer between 1 and the number of subarrays. You can also specify the value as 'All ' to highlight all subarrays of the array or 'None' to suppress subarray highlighting. Highlighting uses different colors for different subarrays.

Default: 'All'

## Title

Character vector specifying the title of the plot.
Default: 'Array Geometry'

## Output Arguments

## hPlot

Handles of array elements in figure window.

## Examples

## Array of Replicated Hexagonal Arrays on a Sphere

This example shows how to construct a full array by replicating subarrays.
Create a hexagonal array to use as a subarray.

```
Nmin = 9;
Nmax = 17;
dy = 0.5;
dz = 0.5*sin(pi/3);
rowlengths = [Nmin:Nmax Nmax-1:-1:Nmin];
numels_hex = sum(rowlengths);
stopvals = cumsum(rowlengths);
startvals = stopvals-rowlengths+1;
pos = zeros(3,numels_hex);
rowidx = 0;
for m = Nmin-Nmax:Nmax-Nmin
    rowidx = rowidx+1;
    idx = startvals(rowidx):stopvals(rowidx);
    pos(2,idx) = (-(rowlengths(rowidx)-1)/2:...
        (rowlengths(rowidx)-1)/2) * dy;
    pos(3,idx) = m*dz;
end
hexa = phased.ConformalArray('ElementPosition',pos,...
    'ElementNormal',zeros(2,numels_hex));
```

Arrange copies of the hexagonal array on a sphere.

```
radius = 9;
az = [-180 -180 -180 -120 -120 -60 -60 0 0 0 60 60 120 120 180];
el = [[-90 
numsubarrays = size(az,2);
[x,y,z] = sph2cart(deg2rad(az),deg2rad(el),...
    radius*ones(1,numsubarrays));
ha = phased.ReplicatedSubarray('Subarray',hexa,...
    'Layout','Custom',...
    'SubarrayPosition',[x; y; z], ...
    'SubarrayNormal',[az; el]);
```

Display the geometry of the array, highlighting selected subarrays with different colors.

```
viewArray(ha,'ShowSubarray', 3:2:13,...
    'Title','Hexagonal Subarrays on a Sphere');
view(0,90)
```

Hexagonal Subarrays on a Sphere


Array Span:
$X$ axis $=19.053 \mathrm{~m}$
$Y$ axis $=18.500 \mathrm{~m}$
$Z$ axis $=18.000 \mathrm{~m}$

## See Also

phased.ArrayResponse

## Topics

Phased Array Gallery

## phased.RootMUSICEstimator

Package: phased
Root MUSIC direction of arrival (DOA) estimator for ULA and UCA

## Description

The RootMUSICEstimator object implements the root multiple signal classification (root-MUSIC) direction of arrival estimator for uniform linear arrays (ULA) and uniform circular arrays (UCA). When a uniform circular array is used, the algorithm transforms the input to a ULA-like structure using the phase mode excitation technique [2].

To estimate the direction of arrival (DOA):
1 Define and set up your DOA estimator. See "Construction" on page 1-1487.
2 Call step to estimate the DOA according to the properties of phased.RootMUSICEstimator. The behavior of step is specific to each object in the toolbox.

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.

## Construction

H = phased.RootMUSICEstimator creates a root MUSIC DOA estimator System object, H. The object estimates the signal's direction of arrival using the root MUSIC algorithm with a uniform linear array (ULA).

H = phased.RootMUSICEstimator(Name, Value) creates object, H, with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN).

## Properties

## SensorArray

Sensor array System object
Sensor array specified as a System object. The sensor array must be a phased. ULA object or a phased.UCA object.

Default: phased.ULA with default property values

## PropagationSpeed

Signal propagation speed
Specify the propagation speed of the signal, in meters per second, as a positive scalar. You can specify this property as single or double precision.

Default: Speed of light
OperatingFrequency
System operating frequency
Specify the operating frequency of the system in hertz as a positive scalar. The default value corresponds to 300 MHz . You can specify this property as single or double precision.

Default: 3e8

## ForwardBackwardAveraging

Perform forward-backward averaging
Set this property to true to use forward-backward averaging to estimate the covariance matrix for sensor arrays with conjugate symmetric array manifold.

Default: false

## SpatialSmoothing

Spatial smoothing
The averaging number used by spatial smoothing to estimate the covariance matrix, specified as a strictly positive integer. Each additional smoothing value handles one additional coherent source, but reduces the effective number of elements by one. The maximum value of this property is $M-2$. For a ULA, $M$ is the number of sensors. For a UCA, $M$ is the size of the internal ULA-like array structure defined by the phase mode excitation technique. The default value of zero indicates that no spatial smoothing is employed. You can specify this property as single or double precision.

## Default: 0

## NumSignalsSource

Source of number of signals
Specify the source of the number of signals as one of 'Auto' or 'Property'. If you set this property to 'Auto', the number of signals is estimated by the method specified by the NumSignalsMethod property.

When spatial smoothing is employed on a UCA, you cannot set the NumSignalsSource property to 'Auto' to estimate the number of signals. You can use the functions aictest or mdltest independently to determine the number of signals.

Default: 'Auto'

## NumSignalsMethod

Method to estimate number of signals
Specify the method to estimate the number of signals as one of 'AIC' or 'MDL'. 'AIC' uses the Akaike Information Criterion and 'MDL' uses Minimum Description Length Criterion. This property applies when you set the NumSignalsSource property to 'Auto'.

Default: 'AIC'

## NumSignals

Number of signals
Specify the number of signals as a positive integer scalar. This property applies when you set the NumSignalsSource property to 'Property'. The number of signals must be smaller than the number of elements in the array specified in the SensorArray property. You can specify this property as single or double precision.

## Default: 1

## Methods

step
Perform DOA estimation

## Common to All System Objects

release Allow System object property value changes

## Examples

## Root-MUSIC Estimation of DOA for ULA

Estimate the DOA's of two signals received by a standard 10-element uniform linear array (ULA) having an element spacing of 1 meter. The antenna operating frequency is 150 MHz . The actual direction of the first signal is 10 degrees in azimuth and 20 degrees in elevation. The direction of the second signal is 45 degrees in azimuth and 60 degrees in elevation.

```
fs = 8000;
t = (0:1/fs:1).';
x1 = cos(2*pi*t*300);
x2 = cos(2*pi*t*400);
sULA = phased.ULA('NumElements',10,...
    'ElementSpacing',1);
sULA.Element.FrequencyRange = [100e6 300e6];
fc = 150e6;
x = collectPlaneWave(sULA,[x1 x2],[10 20;45 60]',fc);
rng default;
noise = 0.1/sqrt(2)*(randn(size(x))+li*randn(size(x)));
sDOA = phased.RootMUSICEstimator('SensorArray',sULA,...
    'OperatingFrequency',fc,...
    'NumSignalsSource','Property',...
    'NumSignals',2);
doas = step(sDOA,x + noise);
az = broadside2az(sort(doas),[20 60])
az = 1\times2
    10.0001 45.0107
```


## Algorithms

## Data Precision

This System object supports single and double precision for input data, properties, and arguments. If the input data $X$ is single precision, the output data is single precision. If the input data $X$ is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

## Version History

Introduced in R2011a

## References

[1] Van Trees, H. Optimum Array Processing. New York: Wiley-Interscience, 2002.
[2] Mathews, C.P., Zoltowski, M.D., "Eigenstructure techniques for 2-D angle estimation with uniform circular arrays." IEEE Transactions on Signal Processing, vol. 42, No. 9, pp. 2395-2407, Sept. 1994.

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
See "System Objects in MATLAB Code Generation" (MATLAB Coder).
This System object supports single and double precision for input data, properties, and arguments. If the input data $X$ is single precision, the output data is single precision. If the input data $X$ is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

## See Also

broadside2az|sensorcov|spsmooth|rootmusicdoa|phased.RootWSFEstimator

## step

System object: phased. RootMUSICEstimator
Package: phased
Perform DOA estimation

## Syntax

ANG $=\operatorname{step}(H, X)$
ANG $=$ step ( $\mathrm{H}, \mathrm{X}, \mathrm{El}$ Ang)

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.

ANG $=\operatorname{step}(H, X)$ estimates the direction of arrivals (DOAs) from a signal $X$ using the DOA estimator $\mathrm{H} . \mathrm{X}$ is a matrix whose columns correspond to the signal channels. ANG is a row vector of the estimated broadside angles (in degrees). You can specify the argument $X$ as single or double precision.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

ANG = step ( $\mathrm{H}, \mathrm{X}, \mathrm{El}$ Ang) specifies, in addition, the assumed elevation angles of the signals. This syntax is only applicable when the SensorArray property of the object specifies a uniform circular array (UCA). ElAng is a scalar between $-90^{\circ}$ and $90^{\circ}$ and is applied to all signals. The elevation angles for all signals must be the same as required by the phase mode excitation algorithm. You can specify the argument ElAng as single or double precision.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Examples

## Root-MUSIC Estimation of DOA for ULA

Estimate the DOA's of two signals received by a standard 10-element uniform linear array (ULA) having an element spacing of 1 meter. The antenna operating frequency is 150 MHz . The actual direction of the first signal is 10 degrees in azimuth and 20 degrees in elevation. The direction of the second signal is 45 degrees in azimuth and 60 degrees in elevation.

```
fs = 8000;
t = (0:1/fs:1).';
x1 = cos(2*pi*t*300);
x2 = cos(2*pi*t*400);
sULA = phased.ULA('NumElements',10,...
    'ElementSpacing',1);
sULA.Element.FrequencyRange = [100e6 300e6];
fc = 150e6;
x = collectPlaneWave(sULA,[x1 x2],[10 20;45 60]',fc);
rng default;
noise = 0.1/sqrt(2)*(randn(size(x))+1i*randn(size(x)));
sDOA = phased.RootMUSICEstimator('SensorArray',sULA,...
    'OperatingFrequency',fc,...
    'NumSignalsSource','Property',...
    'NumSignals',2);
doas = step(sDOA,x + noise);
az = broadside2az(sort(doas),[20 60])
az = 1\times2
    10.0001 45.0107
```


## Root-MUSIC Estimation of DOA for UCA

Using the root-MUSIC algorithm, estimate the azimuth angle of arrival of two signals received by a 15 -element UCA having a 1.5 meter radius. The antenna operating frequency is 150 MHz . The actual direction of arrival of the first signal is 10 degrees in azimuth and 4 degrees in elevation. The direction of arrival of the second signal is 45 degrees in azimuth and -2 degrees in elevation. In estimating the directions of arrival, assume the signals arrive from 0 degrees elevation.

Set the frequencies of the signals to 500 and 600 Hz . Set the sample rate to 8 kHz and the operating frequency to 150 MHz . Then, create the baseband signals, the UCA array and the plane wave signals.

```
fs = 8000;
fc = 150e6;
t = (0:1/fs:1).';
x1 = cos(2*pi*t*500);
x2 = cos(2*pi*t*600);
sUCA = phased.UCA('NumElements',15,...
    'Radius',1.5);
x = collectPlaneWave(sUCA,[x1 x2],[10 4; 45 -2]',fc);
```

Add random complex Gaussian white noise to the signals.

```
rs = RandStream('mt19937ar','Seed',0);
noise = 0.1/sqrt(2)*(randn(rs,size(x))+li*randn(rs,size(x)));
```

Create the phased.RootMUSICEstimator System object ${ }^{\mathrm{TM}}$.

```
sDOA = phased.RootMUSICEstimator('SensorArray',sUCA,...
    'OperatingFrequency',fc,...
    'NumSignalsSource','Property',...
    'NumSignals',2);
```

Solve for the azimuth angles for zero degrees elevation.
elang = 0;
doas = step(sDOA, $x+$ noise, elang);
az = sort(doas)
$a z=1 \times 2$
9.981544 .9986

1-1493

# phased.RootWSFEstimator 

Package: phased
Root WSF direction of arrival (DOA) estimator for ULA

## Description

The RootWSFEstimator object implements a root weighted subspace fitting direction of arrival algorithm.

To estimate the direction of arrival (DOA):
1 Define and set up your root WSF DOA estimator. See "Construction" on page 1-1494.
2 Call step to estimate the DOA according to the properties of phased.RootWSFEstimator. The behavior of step is specific to each object in the toolbox.

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, x ) and $\mathrm{y}=\mathrm{obj}(\mathrm{x})$ perform equivalent operations.

## Construction

H = phased.RootWSFEstimator creates a root WSF DOA estimator System object, H. The object estimates the signal's direction of arrival using the root weighted subspace fitting (WSF) algorithm with a uniform linear array (ULA).

H = phased.RootWSFEstimator(Name,Value) creates object, H, with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN).

## Properties

## SensorArray

Handle to sensor array
Specify the sensor array as a handle. The sensor array must be a phased. ULA object.
Default: phased.ULA with default property values

## PropagationSpeed

Signal propagation speed
Specify the propagation speed of the signal, in meters per second, as a positive scalar. You can specify this property as single or double precision.

Default: Speed of light

## OperatingFrequency

System operating frequency
Specify the operating frequency of the system in hertz as a positive scalar. The default value corresponds to 300 MHz . You can specify this property as single or double precision.

## Default: 3e8

## NumSignalsSource

Source of number of signals
Specify the source of the number of signals as one of 'Auto' or 'Property '. If you set this property to 'Auto', the number of signals is estimated by the method specified by the NumSignalsMethod property.

Default: 'Auto'

## NumSignalsMethod

Method to estimate number of signals
Specify the method to estimate the number of signals as one of 'AIC' or 'MDL'. 'AIC' uses the Akaike Information Criterion and 'MDL' uses the Minimum Description Length Criterion. This property applies when you set the NumSignalsSource property to 'Auto'.

## Default: 'AIC'

## NumSignals

Number of signals
Specify the number of signals as a positive integer scalar. This property applies when you set the NumSignalsSource property to 'Property'. You can specify this property as single or double precision.

## Default: 1

## Method

Iterative method
Specify the iterative method as one of 'IMODE' or 'IQML'.
Default: ' IMODE'

## MaximumIterationCount

Maximum number of iterations
Specify the maximum number of iterations as a positive integer scalar or 'Inf '. This property is tunable. You can specify this property as single or double precision.

Default: 'Inf'

## Methods

step
Perform DOA estimation

## Common to All System Objects

release $\quad$ Allow System object property value changes

## Examples

## Estimate DOA of Two Signals Using Root-WSF

First, estimate the DOAs of two signals received by a standard 10-element ULA with element spacing of 1 meter. The antenna operating frequency is 150 MHz . The actual direction of the first signal is $10^{\circ}$ in azimuth and $20^{\circ}$ in elevation. The direction of the second signal is $45^{\circ}$ in azimuth and $-5^{\circ}$ in elevation.

Create the signals with added noise. Then, create the ULA System object ${ }^{\text {TM }}$.

```
fs = 8000;
t = (0:1/fs:1).';
x1 = cos(2*pi*t*300);
x2 = cos(2*pi*t*400);
array = phased.ULA('NumElements',10,'ElementSpacing',1);
array.Element.FrequencyRange = [100e6 300e6];
fc = 150.0e6;
x = collectPlaneWave(array,[x1 x2],[10 20; 45 60]',fc);
noise = 0.1*(randn(size(x)) + li*randn(size(x)));
```

Construct WSF estimator System object.

```
estimator = phased.RootWSFEstimator('SensorArray',array, ...
    'OperatingFrequency',fc, ...
    'NumSignalsSource','Property','NumSignals',2);
```

Estimate the DOAs.

```
doas = estimator(x + noise);
doas = broadside2az(sort(doas),[20 -5])
doas =
    10.0002 20.7934
```


## Algorithms

## Data Precision

This System object supports single and double precision for input data, properties, and arguments. If the input data $X$ is single precision, the output data is single precision. If the input data $X$ is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

## Version History

Introduced in R2011a

## References

[1] Van Trees, H. Optimum Array Processing. New York: Wiley-Interscience, 2002.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:
See "System Objects in MATLAB Code Generation" (MATLAB Coder).

## See Also

broadside2az|phased.RootMUSICEstimator

## step

System object: phased.RootWSFEstimator
Package: phased
Perform DOA estimation

## Syntax

ANG $=$ step $(H, X)$

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = $\underline{\text { step }(o b j, x) \text { and } y=o b j(x) \text { perform equivalent operations. }}$

ANG $=\operatorname{step}(\mathrm{H}, \mathrm{X})$ estimates the DOAs from X using the DOA estimator $\mathrm{H} . \mathrm{X}$ is a matrix whose columns correspond to channels. ANG is a row vector of the estimated broadside angles (in degrees). You can specify the argument $X$ as single or double precision.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Examples

## Estimate DOA of Two Signals Using Root-WSF

First, estimate the DOAs of two signals received by a standard 10 -element ULA with element spacing of 1 meter. The antenna operating frequency is 150 MHz . The actual direction of the first signal is $10^{\circ}$ in azimuth and $20^{\circ}$ in elevation. The direction of the second signal is $45^{\circ}$ in azimuth and $-5^{\circ}$ in elevation.

Create the signals with added noise. Then, create the ULA System object ${ }^{\mathrm{TM}}$.

```
fs = 8000;
t = (0:1/fs:1).';
x1 = cos(2*pi*t*300);
x2 = cos(2*pi*t*400);
array = phased.ULA('NumElements',10,'ElementSpacing',1);
```

```
array.Element.FrequencyRange = [100e6 300e6];
fc = 150.0e6;
x = collectPlaneWave(array,[x1 x2],[10 20; 45 60]',fc);
noise = 0.1*(randn(size(x)) + li*randn(size(x)));
Construct WSF estimator System object.
estimator = phased.RootWSFEstimator('SensorArray',array, ...
    'OperatingFrequency',fc, ...
    'NumSignalsSource','Property','NumSignals',2);
```

Estimate the DOAs.
doas = estimator(x + noise);
doas = broadside2az(sort(doas),[20-5])
doas = $10.0002 \quad 20.7934$

# phased.ScenarioViewer 

Package: phased
Display motion of radars and targets

## Description

The phased.ScenarioViewer System object creates a 3-D viewer to display the motion of radars and targets that you model in your radar simulation. You can display current positions and velocities, object tracks, position and speed annotations, radar beam directions, and other object parameters. You can change radar features such as beam range and beam width during the simulation. You can use the phased. Plat form System object to model moving objects or you can supply your own dynamic models.

This figure shows a four-object scenario consisting of a ground radar, two airplanes, and a ground vehicle. You can view the code that generated this figure in the "Visualize Multiplatform Scenario" on page 1-1509 example.


To create a scenario viewer:
1 Define and set up the phased. ScenarioViewer System object. See "Construction" on page 11501. You can set System object properties at construction time or leave them to their default values. Some properties that you set at construction time can be changed later. These properties are tunable.

2 Call the step method to update radar and target displayed positions according to the properties of the phased. ScenarioViewer System object. You can change tunable properties at any time.

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step (obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.

## Construction

sIS = phased.ScenarioViewer creates a scenario viewer System object, sIS having default property values.
sIS = phased.ScenarioViewer(Name,Value) returns a scenario viewer System object, sIS, with any specified property Name set to a specified Value. Name must appear inside single quotes (' ' ). You can specify several name-value pair arguments in any order as
Name1, Value1, . . . ,NameN, ValueN.

## Properties

## Name - Window caption name

'Scenario Viewer' (default)| character vector
Window caption name, specified as a character vector. The Name property and the Title property are different.
Example: 'Multitarget Viewer'
Data Types: char

## ReferenceRadar - Reference radar index

1 (default) | positive integer
Reference radar index, specified as a positive integer. This property selects one of the radars as the reference radar. Its value must be less than or equal to the number of radars that you specify in the radar_pos argument of the step method. This property is tunable. Target range, radial speed, azimuth, and elevation are defined with respect to this radar.
Example: 2
Data Types: double

## ShowBeam - Show radar beams

'ReferenceRadar' (default)|'None' |'All'
Enable the display of radar beams, specified as 'ReferenceRadar', 'None', or 'All'. This option determines which radar beams to show.

| Option | Beams to show |
| :--- | :--- |
| 'ReferenceRadar' | Show the beam of the radar specified in the <br> ReferenceRadar property. |
| 'None' | Do not show any radar beams. |


| Option | Beams to show |
| :--- | :--- |
| 'All' | Show the beams for all radars. |

This property is tunable.
Example: 'All'
Data Types: char

## BeamWidth - Vertical and horizontal radar beam widths

15 (default) | positive, real-valued scalar | positive, real-valued 2-element column vector | positive, real-valued $N$-element row vector | positive, real-valued 2 -by- $N$ matrix

Vertical and horizontal radar beam widths, specified as a positive real-valued scalar, a 2-element column vector, an $N$-element row vector, or a 2 -by- $N$ matrix. $N$ is the number of radars. All scalar, vector, and matrix entries are positive, real-valued numbers between $0-360^{\circ}$. Units are in degrees.

| Value Specification | Interpretation |
| :--- | :--- |
| Scalar | The horizontal and vertical radar beam widths <br> are equal and identical for all radars. |
| 2-element column vector | The first row specifies the horizontal beam width. <br> The second row specifies the vertical beam width. <br> These values are identical for all radars. |
| $N$-element row vector | Each element applies to one radar. Vertical and <br> horizontal beam widths for each radar are equal. |
| 2-by-N matrix | Each column applies to one radar. The first row <br> specifies the horizontal beam width and the <br> second row specifies the vertical beam width for <br> each radar. |

When CameraPerspective is set to 'Radar', the System object uses this property to calculate the value of CameraViewAngle. This property is tunable.

Example: [20 10; 18 9]
Data Types: double

## BeamRange - Radar beam range

1000 (default) | positive scalar | real-valued $N$ - element row vector of positive values
Radar beam range, specified as a positive scalar or an $N$-element row vector, where $N$ is the number of radars. Units are in meters. When specified as a scalar, all radars have the same beam range. When specified as a vector, each element corresponds to one radar. This property is tunable.
Example: [1000 1500 850]
Data Types: double

## BeamSteering - Beam steering direction

[0;0] (default) | positive real-valued 2-element column vector | positive real-valued $N$-element row vector

Beam steering directions of radars, specified as a real-valued 2 -element column vector of positive values or 2-by- $N$ real-valued matrix of positive values. $N$ is the number of radars. Beam steering
angles are relative to the local coordinate axes of each radar. Units are in degrees. Each column takes the form [azimuthangle;elevationangle]. When only one column is specified, the beam steering directions of all radars are the same. Azimuth angles are from $-180^{\circ}$ to $180^{\circ}$, and the elevation angles are from $-90^{\circ}$ to $90^{\circ}$. This property is tunable.
Example: [20 60 35; 50 10]
Data Types: double

## VelocityInputPort - Enable velocity input

true (default) | false
Enable the velocity input arguments, radar_velocity and tgt_velocity, of the step method, specified as true or false. Setting this property to true enables the input arguments. When this property is false, velocity vectors are estimated from the position change between consecutive updates divided by the update interval. The update interval is the inverse of the UpdateRate value.

Example: false
Data Types: logical

## OrientationInputPort - Enable orientation input <br> false (default) |true

Enable the input of local coordinate system orientation axes, radar_laxes and tgt_laxes, to the step method, specified as false or true. Setting this property to true enables the input arguments. When this property is false, the orientation axes are aligned with the global coordinate axes.

Example: true
Data Types: logical
UpdateRate - Update rate of scenario viewer
1 (default)|positive scalar
Update rate of scenario viewer, specified as a positive scalar. Units are in hertz.

## Example: 2.5

Data Types: double

## Title - Display title

' ' (default) | character vector
Display title, specified as a character vector. The Title property and the Name property are different. The display title appears within the figure at the top. The name appears at the top of the figure window. This property is tunable.
Example: 'Radar and Target Display'
Data Types: char
PlatformNames - Names of radars and targets
'Auto ' (default) | 1-by-( $N+M$ ) cell array of character vectors
Names assigned to radars and targets, specified as a 1-by- $(N+M)$ cell array of character vectors. $N$ is the number of radars and $M$ is the number of targets. Order the cell entries by radar names, followed by target names. Names appear in the legend and annotations. When you set PlatformNames to
'Auto', names are created sequentially starting from 'Radar 1' for radars and 'Target 1' for targets.

Example: \{'Stationary Radar','Mobile Radar','Airplane'\}
Data Types: cell

## TrailLength - Length of visible tracks

500 (default) | positive integer | ( $N+M$ )-length vector of positive integers
Length of the visibility of object tracks, specified as a positive integer or $(N+M)$-length vector of positive integers. $N$ is the number of radars and $M$ is the number of targets. When TrailLength is a scalar, all tracks have the same length. When TrailLength is a vector, each element of the vector specifies the length of the corresponding radar or target trajectory. Order the entries by radars, followed by targets. Each call to the step method generates a new visible point. This property is tunable.

Example: [100, 150, 100]
Data Types: double

## CameraPerspective - Camera perspective

'Auto' (default) | 'Custom' | 'Radar'
Camera perspective, specified as 'Auto', 'Custom', or 'Radar'. When you set this property to 'Auto ', the System object estimates appropriate values for the camera position, orientation, and view angle to show all tracks. When you set this property to 'Custom' , you can set the camera position, orientation, and angles using camera properties or the camera toolbar. When you set this property to 'Radar', the System object determines the camera position, orientation, and angles from the radar position and the radar beam steering direction. This property is tunable.

## Example: 'Radar'

Data Types: char

## CameraPosition - Camera position

[ $x, y, z$ ] vector of real-values
Camera position, specified as an $[x, y, z]$ vector of real values. Units are in meters. This property applies when you set CameraPerspective to 'Custom'. When you do not specify this property, the System object chooses values based on your display configuration. This property is tunable.
Example: [100,50,40]
Data Types: double

## CameraOrientation - Camera orientation

[pan,tilt, roll] vector of positive, real values
Camera orientation, specified as a [pan, tilt, roll] vector of positive, real values. Units are in degrees. Pan and roll angles take values from $-180^{\circ}$ to $180^{\circ}$. The tilt angle takes values from $-90^{\circ}$ to $90^{\circ}$. Camera rotations are performed in the order: pan, tilt, and roll. This property applies when you set CameraPerspective to 'Custom'. When you do not specify this property, the System object chooses values based on your display configuration. This property is tunable.
Example: [180, 45, 30]
Data Types: double

## CameraViewAngle - Camera view angle

real-valued scalar from $0^{\circ}$ to $360^{\circ}$
Camera view angle, specified as a real-valued scalar. Units are in degrees. View angle values are in the range $0^{\circ}$ to $360^{\circ}$. This property applies when you set CameraPerspective to 'Custom ' . When you do not specify this property, the System object chooses values based on your display configuration. This property is tunable.

Example: 75
Data Types: double

## ShowLegend - Show viewer legend

false (default) | true
Option to show the viewer legend, specified as false or true. This property is tunable.
Example: true
Data Types: logical

## ShowGround - Show ground plane of scenario <br> true (default) | false

Option to show the ground plane of the viewer scenario, specified as true or false. This property is tunable.
Example: false
Data Types: logical

## ShowName - Option to annotate radar and target tracks with names true (default) | false

Annotate radar and target tracks with names, specified as true or false. You can define custom platform names using PlatformNames. This property is tunable.
Example: false
Data Types: logical

## ShowPosition - Annotate radar and target tracks with positions <br> false (default) | true

Option to annotate radar and target tracks with positions, specified as false or true. This property is tunable.

## Example: true

Data Types: logical

## ShowRange - Annotate radar and target tracks with ranges

false (default) | true
Option to annotate radar and target tracks with the range from the reference radar, specified as false or true. This property is tunable.
Example: true
Data Types: logical

## ShowAltitude - Annotate radar and target tracks with altitude

false (default) |true
Option to annotate radar and target tracks with altitude, specified as false or true. This property is tunable.

Example: true
Data Types: logical

## ShowSpeed - Annotate radar and target tracks with speed

false (default) | true
Option to annotate radar and target tracks with speed, specified as false or true. This property is tunable.

Example: true
Data Types: logical

## ShowRadialSpeed - Annotate radar and target tracks with radial speed <br> false (default) |true

Option to annotate radar and target tracks with radial speed, specified as false or true. Radial speed is relative to the reference radar. This property is tunable.
Example: true
Data Types: logical

## ShowAzEl - Annotate radar and target tracks with azimuth and elevation

false (default) | true
Option to annotate radar and target tracks with azimuth and elevation angles relative to the reference radar, specified as false or true. This property is tunable.

## Example: true

Data Types: logical

## Position - Viewer window size and position

[left bottom width height] vector of positive, real values
Scenario viewer window size and position, specified as a [left bottom width height] vector of positive, real values. Units are in pixels.

- left sets the position of the left edge of the window.
- bottom sets the position of the bottom edge of the window.
- width sets the width of the window.
- height sets the height of the window.

When you do not specify this property, the window is positioned at the center of the screen, with width and height taking the values 410 and 300 pixels, respectively. This property is tunable.
Example: [100, 200, 800,500]
Data Types: double

## ReducePlotRate - Enable reduced plot rate

## true (default) | false

Option to reduce the plot rate to improve performance, specified as true or false. Set this property to true to update the viewer at a reduced rate. Set this property to false to update the viewer with each call to the step method. This mode adversely affects viewer performance. This property is tunable.

Example: false
Data Types: logical

## Methods

| hide | Hide scenario viewer window |
| :--- | :--- |
| reset | Reset state of the System object |
| show | Show scenario viewer window |
| step | Update scenario viewer display |

## Common to All System Objects

release Allow System object property value changes

## Examples

## View Tracks of Stationary Radar and One Target

Visualize the tracks of a radar and a single airplane target. The radar is stationary and the airplane is moving in a straight line. Maintain the radar beam pointing at the airplane.

Create the radar and airplane platform System objects ${ }^{\mathrm{TM}}$. Set the update rate to 0.1 s .

```
updateRate = 0.1;
radarPlatform = phased.Platform(...
    'InitialPosition',[0;0;10], ...
    'Velocity',[0;0;0]);
airplanePlatforms = phased.Platform(...
    'InitialPosition',[5000.0;3500.0;6000.0],...
    'Velocity',[-300;0;0]);
```

Create the phased.ScenarioViewer System object. Show the radar beam and annotate the tracks with position, speed, and altitude.

```
sSV = phased.ScenarioViewer('BeamRange',5000.0,'UpdateRate',updateRate,...
    'PlatformNames',{'Ground Radar','Airplane'},'ShowPosition',true,...
    'ShowSpeed',true,'ShowAltitude',true,'ShowLegend',true);
```

Run the scenario. At each step, compute the angle to the target. Use that angle to steer the radar beam toward the target.

```
for i = 1:100
    [radar_pos,radar_vel] = step(radarPlatform,updateRate);
    [tgt_pos,tgt_vel] = step(airplanePlatforms,updateRate);
```

[rng,ang] = rangeangle(tgt_pos,radar_pos);
sSV.BeamSteering = ang;
step(sSV, radar_pos, radar_vel,tgt_pos,tgt_vel);
pause(0.1);
end


## View Tracks of Airborne Radar and Ground Target

Visualize the tracks of an airborne radar and a ground vehicle target. The airborne radar is carried by a drone flying at an altitude of 5 km .

Create the drone radar and ground vehicle using phased.Platform System objects ${ }^{\mathrm{TM}}$. Set the update rate to 0.1 s .
updateRate = 0.1;
drone $=$ phased.Platform(...
'InitialPosition', [100;1000;5000], ...
'Velocity',[400;0;0]);
vehicle $=$ phased.Platform('MotionModel','Acceleration',...
'InitialPosition',[5000.0;3500.0;0.0],...
'InitialVelocity', [40;5;0],'Acceleration', [0.1;0.1;0]);

Create the phased.ScenarioViewer System object. Show the radar beam and annotate the tracks with position, speed, and altitude.

```
viewer = phased.ScenarioViewer('BeamRange',8000.0,'BeamWidth',2,'UpdateRate',updateRate,...
    'PlatformNames',{'Drone Radar','Vehicle'},'ShowPosition',true,...
    'ShowSpeed',true,'ShowAltitude',true,'ShowLegend',true,'Title','Vehicle Tracking Radar');
```

Run the scenario. At each step, compute the angle to the target. Use that angle to steer the radar beam toward the target.

```
for i = 1:100
    [radar_pos,radar_vel] = step(drone,updateRate);
    [tgt_pos,tgt_vel] = step(vehicle,updateRate);
    [rng,ang] = 'rangeangle(tgt_pos,radar_pos);
    viewer.BeamSteering = ang;
    viewer(radar_pos,radar_vel,tgt_pos,tgt_vel)
    pause(.1)
end
```



## Visualize Multiplatform Scenario

This example shows how to create and display a multiplatform scenario containing a ground-based stationary radar, a turning airplane, a constant-velocity airplane, and a moving ground vehicle. The turning airplane follows a parabolic flight path while descending at a rate of $20 \mathrm{~m} / \mathrm{s}$.

Specify the scenario refresh rate at 0.5 Hz . For 150 steps, the time duration of the scenario is 300 s .

```
updateRate = 0.5;
N = 150;
```

Set up the turning airplane using the Acceleration model of the phased.Platform System object $^{\mathrm{Tm}}$. Specify the initial position of the airplane by range and azimuth from the ground-based radar and its elevation. The airplane is 10 km from the radar at $60^{\circ}$ azimuth and has an altitude of 6 km . The airplane is accelerating at $10 \mathrm{~m} / \mathrm{s}^{2}$ in the negative $x$-direction.

```
airplane1range = 10.0e3;
airplane1Azimuth = 60.0;
airplanelalt = 6.0e3;
airplane1Pos0 = [cosd(airplane1Azimuth)*airplane1range;...
    sind(airplane1Azimuth)*airplanelrange;airplanelalt];
airplane1Vel0 = [400.0;-100.0;-20];
airplanelAccel = [-10.0;0.0;0.0];
airplanelplatform = phased.Platform('MotionModel','Acceleration',...
    'AccelerationSource','Input port','InitialPosition',airplane1Pos0,...
    'InitialVelocity',airplane1Vel0,'OrientationAxes0utputPort',true,...
    'InitialOrientationAxes',eye(3));
```

Set up the stationary ground radar at the origin of the global coordinate system. To simulate a rotating radar, change the ground radar beam steering angle in the processing loop.

```
groundRadarPos = [0,0,0]';
groundRadarVel = [0,0,0]';
groundradarplatform = phased.Platform('MotionModel','Velocity',...
    'InitialPosition',groundRadarPos,'Velocity',groundRadarVel,...
    'InitialOrientationAxes',eye(3));
```

Set up the ground vehicle to move at a constant velocity.

```
groundVehiclePos = [5e3,2e3,0]';
groundVehicleVel = [50,50,0]';
groundvehicleplatform = phased.Platform('MotionModel','Velocity',...
    'InitialPosition',groundVehiclePos,'Velocity',groundVehicleVel,...
    'InitialOrientationAxes',eye(3));
```

Set up the second airplane to also move at constant velocity.

```
airplane2Pos = [8.5e3,1e3,6000]';
airplane2Vel = [-300,100,20]';
airplane2platform = phased.Platform('MotionModel','Velocity',...
    'InitialPosition',airplane2Pos,'Velocity',airplane2Vel,...
    'Initial0rientationAxes',eye(3));
```

Set up the scenario viewer. Specify the radar as having a beam range of 8 km , a vertical beam width of $30^{\circ}$, and a horizontal beam width of $2^{\circ}$. Annotate the tracks with position, speed, altitude, and range.

```
BeamSteering = [0;50];
viewer = phased.ScenarioViewer('BeamRange',8.0e3,'BeamWidth',[2;30],'UpdateRate',updateRate,...
```

```
'PlatformNames',{'Ground Radar','Turning Airplane','Vehicle','Airplane 2'},'ShowPosition',tr
'ShowSpeed',true,'ShowAltitude',true,'ShowLegend',true,'ShowRange',true,...
'Title','Multiplatform Scenario','BeamSteering',BeamSteering);
```

Step through the display processing loop, updating radar and target positions. Rotate the groundbased radar steering angle by four degrees at each step.

```
for n = 1:N
    [groundRadarPos,groundRadarVel] = groundradarplatform(updateRate);
    [airplanelPos,airplanelVel,airplane1Axes] = airplanelplatform(updateRate,airplanelAccel);
    [vehiclePos,vehicleVel] = groundvehicleplatform(updateRate);
    [airplane2Pos,airplane2Vel] = airplane2platform(updateRate);
    viewer(groundRadarPos,groundRadarVel,[airplane1Pos,vehiclePos,airplane2Pos],...
    [airplane1Vel,vehicleVel,airplane2Vel]);
    BeamSteering = viewer.BeamSteering(1);
    BeamSteering = mod(BeamSteering + 4,360.0);
    if BeamSteering > 180.0
        BeamSteering = BeamSteering - 360.0;
    end
    viewer.BeamSteering(1) = BeamSteering;
    pause(0.2);
end
```



## Version History

Introduced in R2016a

## See Also

phased. Platform| rangeangle

## Topics

"Scene Visualization for Phased Array System Simulation"

## hide

System object: phased.ScenarioViewer
Package: phased
Hide scenario viewer window

## Syntax

hide(sSV)

## Description

hide(sSV) hides the display window of the phased. ScenarioViewer System object, sSV.

## Input Arguments

sSV - Scenario viewer
phased. ScenarioViewer System object
Scenario viewer, specified as a phased. ScenarioViewer System object.
Example: phased.ScenarioViewer

## Version History

Introduced in R2016a

## reset

System object: phased.ScenarioViewer
Package: phased
Reset state of the System object

## Syntax

reset(sSV)

## Description

reset (sSV) resets the internal state of the phased. ScenarioViewer System object, sSV, to its initial value.

## Input Arguments

sSV - Scenario viewer
phased.ScenarioViewer System object
Scenario viewer, specified as a phased. ScenarioViewer System object.
Example: phased.ScenarioViewer

## Version History <br> Introduced in R2016a

## show

System object: phased.ScenarioViewer
Package: phased
Show scenario viewer window

## Syntax

show(sSV)

## Description

show(sSV) shows the display window of the phased. ScenarioViewer System object, sSV.

## Input Arguments

sSV - Scenario viewer
phased. ScenarioViewer System object
Scenario viewer, specified as a phased. ScenarioViewer System object.
Example: phased.ScenarioViewer

## Version History

Introduced in R2016a

## step

System object: phased. ScenarioViewer
Package: phased
Update scenario viewer display

## Syntax

```
step(sSV,radar_pos,tgt_pos)
step(sSV,radar_pos,tgt pos,radar_velocity,tgt_velocity)
step(sSV,radar_pos,radar_laxes,tg}t_pos,tgt la\overline{xes)
step(sSV,radar_pos,radar_velocity,radar_laxes,tgt_pos,tgt_velocity,tgt_laxes)
```


## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, $y=$ step (obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.
step(sSV, radar_pos,tgt_pos) updates the scenario viewer display with new radar positions, radar_pos, and target positions, tgt_pos. This syntax applies when VelocityInputPort and OrientationInputPort are set to false.
step(sSV,radar_pos,tgt_pos,radar_velocity,tgt_velocity) also specifies the radar velocity, radar_velocity, and target velocity, tgt_velocity. This syntax applies when VelocityInputPort is set to true and OrientationInputPort is set to false.
step(sSV,radar_pos,radar_laxes,tgt_pos,tgt_laxes) also specifies the radar orientation axes, radar_laxes, and the target orientation axes, tgt_laxes. This syntax applies when VelocityInputPort is set to false and OrientationInputPort is set to true.
step(sSV,radar_pos,radar_velocity,radar_laxes,tgt_pos,tgt_velocity,tgt_laxes) also specifies velocity and orientation axes when VelocityInputPort and OrientationInputPort are set to true.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## sSV - Scenario viewer

phased. ScenarioViewer System object
Scenario viewer, specified as a phased. ScenarioViewer System object.

## Example: phased.ScenarioViewer

## radar pos - Radar positions

real-valued $3-b y-N$ matrix
Radar positions, specified as a real-valued 3 -by- $N$ matrix. $N$ is the number of radar tracks and must be equal to or greater than one. Each column has the form $[x ; y ; z]$. Position units are in meters.

Example: [100, 250, 75; 0, 20, 49; 300, 5, 120]
Data Types: double

## tgt_pos - Target positions

real-valued 3-by-M matrix
Target positions, specified as a real-valued 3 -by- $N$ matrix. $M$ is the number of target tracks and must be equal to or greater than one. Each column has the form $[x ; y ; z]$. Position units are in meters.

## Example: [200, 40; 10, 40; 305, 15]

Data Types: double
radar_velocity - Radar velocities
real-valued 3-by- $N$ matrix
Radar velocities, specified as a real-valued 3-by- $N$ matrix. $N$ is the number of radar tracks and must be equal to or greater than one. Each column has the form [vx; vy; vz]. The dimensions of radar_velocity must match the dimensions of radar_pos. Velocity units are in meters per second.

Example: [100, 10, 0; 4, 0, 7; 100, 500, 0]
Data Types: double
tgt_velocity - Target velocities
real-valued 3-by-M matrix
Target velocities, specified as a real-valued 3-by- $M$ matrix. $M$ is the number of target tracks and must be equal to or greater than one. Each column has the form [vx; vy; vz]. The dimensions of tgt_velocity must match the dimensions of target_position. Velocity units are in meters per second.

Example: [100, 10, 0; 4, 0, 7;100,500, 0]
Data Types: double

## radar_laxes - Radar local coordinate axes

real-valued 3-by-3-by-N array
Local coordinate axes of radar, specified as a real-valued 3-by-3-by- $N$ array. $N$ is the number of radar tracks. Each page (third index) represents a 3-by-3 orthogonal matrix that specifies the local coordinate axes of one radar. The columns are the unit vectors that form the $x, y$, and $z$ axes of the local coordinate system. Array units are dimensionless.

Example: [100, 10, 0; 4, 0, 7; 100, 500, 0]
Data Types: double
tgt_laxes - Target local coordinate axes
real-valued 3-by-3-by-M array

Local coordinate axes of target, specified as a real-valued 3 -by- 3 -by- $M$ array. $M$ is the number of target tracks. Each page (third index) represents a 3-by-3 orthogonal matrix that specifies the local coordinate axes of one radar. The columns are the unit vectors that form the $x, y$, and $z$ axes of the local coordinate system. Array units are dimensionless.
Example: [100, 10, 0;4, 0, 7;100,500, 0]
Data Types: double

## Examples

## View Tracks of Stationary Radar and One Target

Visualize the tracks of a radar and a single airplane target. The radar is stationary and the airplane is moving in a straight line. Maintain the radar beam pointing at the airplane.

Create the radar and airplane platform System objects ${ }^{\mathrm{TM}}$. Set the update rate to 0.1 s .

```
updateRate = 0.1;
radarPlatform = phased.Platform(...
    'InitialPosition',[0;0;10], ...
    'Velocity',[0;0;0]);
airplanePlatforms = phased.Platform(...
    'InitialPosition',[5000.0;3500.0;6000.0],...
    'Velocity',[-300;0;0]);
```

Create the phased.ScenarioViewer System object. Show the radar beam and annotate the tracks with position, speed, and altitude.

```
sSV = phased.ScenarioViewer('BeamRange',5000.0,'UpdateRate',updateRate,...
    'PlatformNames',{'Ground Radar','Airplane'},'ShowPosition',true,...
    'ShowSpeed',true,'ShowAltitude',true,'ShowLegend',true);
```

Run the scenario. At each step, compute the angle to the target. Use that angle to steer the radar beam toward the target.

```
for i = 1:100
    [radar_pos,radar_vel] = step(radarPlatform,updateRate);
    [tgt_pos,tgt_vel] = step(airplanePlatforms,updateRate);
    [rng,ang] = rangeangle(tgt_pos,radar_pos);
    sSV.BeamSteering = ang;
    step(sSV,radar_pos,radar_vel,tgt_pos,tgt_vel);
    pause(0.1);
end
```



## View Tracks of Airborne Radar and Ground Target

Visualize the tracks of an airborne radar and a ground vehicle target. The airborne radar is carried by a drone flying at an altitude of 5 km .

Create the drone radar and ground vehicle using phased.Platform System objects ${ }^{\mathrm{TM}}$. Set the update rate to 0.1 s .

```
updateRate = 0.1;
drone = phased.Platform(...
    'InitialPosition',[100;1000;5000], ...
    'Velocity',[400;0;0]);
vehicle = phased.Platform('MotionModel','Acceleration',...
    'InitialPosition',[5000.0;3500.0;0.0],...
    'InitialVelocity',[40;5;0],'Acceleration',[0.1;0.1;0]);
```

Create the phased.ScenarioViewer System object. Show the radar beam and annotate the tracks with position, speed, and altitude.

```
viewer = phased.ScenarioViewer('BeamRange',8000.0,'BeamWidth',2,'UpdateRate',updateRate,...
    'PlatformNames',{'Drone Radar','Vehicle'},'ShowPosition',true,...
    'ShowSpeed',true,'ShowAltitude',true,'ShowLegend',true,'Title','Vehicle Tracking Radar');
```

Run the scenario. At each step, compute the angle to the target. Use that angle to steer the radar beam toward the target.

```
for i = 1:100
    [radar_pos,radar_vel] = step(drone,updateRate);
    [tgt_pos,tgt_vel] = step(vehicle,updateRate);
    [rng,ang] = rangeangle(tgt_pos,radar_pos);
    viewer.BeamSteering = ang;
    viewer(radar_pos,radar_vel,tgt_pos,tgt_vel)
    pause(.1)
end
```



## Visualize Multiplatform Scenario

This example shows how to create and display a multiplatform scenario containing a ground-based stationary radar, a turning airplane, a constant-velocity airplane, and a moving ground vehicle. The turning airplane follows a parabolic flight path while descending at a rate of $20 \mathrm{~m} / \mathrm{s}$.

Specify the scenario refresh rate at 0.5 Hz . For 150 steps, the time duration of the scenario is 300 s .

```
updateRate = 0.5;
N = 150;
```

Set up the turning airplane using the Acceleration model of the phased.Platform System object ${ }^{\mathrm{Tm}}$. Specify the initial position of the airplane by range and azimuth from the ground-based radar and its elevation. The airplane is 10 km from the radar at $60^{\circ}$ azimuth and has an altitude of 6 km . The airplane is accelerating at $10 \mathrm{~m} / \mathrm{s}^{2}$ in the negative $x$-direction.

```
airplanelrange = 10.0e3;
airplane1Azimuth = 60.0;
airplanelalt = 6.0e3;
airplane1Pos0 = [cosd(airplanelAzimuth)*airplane1range;...
    sind(airplane1Azimuth)*airplanelrange;airplanelalt];
airplane1Vel0 = [400.0;-100.0;-20];
airplanelAccel = [-10.0;0.0;0.0];
airplanelplatform = phased.Platform('MotionModel','Acceleration',...
    'AccelerationSource','Input port','InitialPosition',airplane1Pos0,...
    'InitialVelocity',airplane1Vel0,'OrientationAxesOutputPort',true,...
    'InitialOrientationAxes',eye(3));
```

Set up the stationary ground radar at the origin of the global coordinate system. To simulate a rotating radar, change the ground radar beam steering angle in the processing loop.

```
groundRadarPos = [0,0,0]';
groundRadarVel = [0,0,0]';
groundradarplatform = phased.Platform('MotionModel','Velocity',...
    'InitialPosition',groundRadarPos,'Velocity',groundRadarVel,...
    'InitialOrientationAxes',eye(3));
```

Set up the ground vehicle to move at a constant velocity.

```
groundVehiclePos = [5e3,2e3,0]';
```

groundVehicleVel = [50,50,0]';
groundvehicleplatform = phased.Platform('MotionModel','Velocity',...
'InitialPosition', groundVehiclePos, 'Velocity', groundVehicleVel,...
'InitialOrientationAxes', eye(3));

Set up the second airplane to also move at constant velocity.

```
airplane2Pos = [8.5e3,1e3,6000]';
airplane2Vel = [-300,100,20]';
airplane2platform = phased.Platform('MotionModel','Velocity',...
    'InitialPosition',airplane2Pos,'Velocity', airplane2Vel,....
    'InitialOrientationAxes',eye(3));
```

Set up the scenario viewer. Specify the radar as having a beam range of 8 km , a vertical beam width of $30^{\circ}$, and a horizontal beam width of $2^{\circ}$. Annotate the tracks with position, speed, altitude, and range.

```
BeamSteering = [0;50];
viewer = phased.ScenarioViewer('BeamRange',8.0e3,'BeamWidth',[2;30],'UpdateRate',updateRate,...
    'PlatformNames',{'Ground Radar','Turning Airplane','Vehicle','Airplane 2'},'ShowPosition',tr
    'ShowSpeed',true,'ShowAltitude',true, 'ShowLegend',true, 'ShowRange',true,...
    'Title','Multiplatform Scenario','BeamSteering',BeamSteering);
```

Step through the display processing loop, updating radar and target positions. Rotate the groundbased radar steering angle by four degrees at each step.

```
for n = 1:N
    [groundRadarPos,groundRadarVel] = groundradarplatform(updateRate);
    [airplane1Pos,airplane1Vel,airplane1Axes] = airplanelplatform(updateRate,airplane1Accel);
    [vehiclePos,vehicleVel] = groundvehicleplatform(updateRate);
    [airplane2Pos,airplane2Vel] = airplane2platform(updateRate);
    viewer(groundRadarPos,groundRadarVel,[airplane1Pos,vehiclePos,airplane2Pos],...
        [airplane1Vel,vehicleVel,airplane2Vel]);
    BeamSteering = viewer.BeamSteering(1);
    BeamSteering = mod(BeamSteering + 4,360.0);
    if BeamSteering > 180.0
        BeamSteering = BeamSteering - 360.0;
    end
    viewer.BeamSteering(1) = BeamSteering;
    pause(0.2);
end
```



Version History
Introduced in R2016a

# phased.STAPSMIBeamformer 

Package: phased
Sample matrix inversion (SMI) beamformer

## Description

The SMIBeamformer object implements a sample matrix inversion space-time adaptive beamformer. The beamformer works on the space-time covariance matrix.

To compute the space-time beamformed signal:
1 Define and set up your SMI beamformer. See "Construction" on page 1-1523.
2 Call step to execute the SMI beamformer algorithm according to the properties of phased.STAPSMIBeamformer. The behavior of step is specific to each object in the toolbox.

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, x ) and $\mathrm{y}=\mathrm{obj}(\mathrm{x})$ perform equivalent operations.

## Construction

H = phased.STAPSMIBeamformer creates a sample matrix inversion (SMI) beamformer System object, H. The object performs the SMI space-time adaptive processing (STAP) on the input data.

H = phased.STAPSMIBeamformer(Name, Value) creates an SMI object, H, with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN).

## Properties

## SensorArray

Sensor array
Sensor array specified as an array System object belonging to the phased package. A sensor array can contain subarrays.

Default: phased.ULA with default property values

## PropagationSpeed

Signal propagation speed
Specify the propagation speed of the signal, in meters per second, as a positive scalar. You can specify this property as single or double precision.

Default: Speed of light

## OperatingFrequency

System operating frequency
Specify the operating frequency of the system in hertz as a positive scalar. The default value corresponds to 300 MHz . You can specify this property as single or double precision.

Default: 3e8

## PRFSource

Source of pulse repetition frequency
Source of the PRF values for the STAP processor, specified as 'Property' or 'Input port '. When you set this property to 'Property', the PRF is determined by the value of the PRF property. When you set this property to 'Input port', the PRF is determined by an input argument to the step method at execution time.

Default: 'Property'
PRF
Pulse repetition frequency
Pulse repetition frequency (PRF) of the received signal, specified as a positive scalar. Units are in Hertz. This property can be specified as single or double precision.

## Dependencies

To enable this property, set the PRFSource property to 'Property ' .
Default: 1

## DirectionSource

Source of targeting direction
Specify whether the targeting direction for the STAP processor comes from the Direction property of this object or from an input argument in step. Values of this property are:

| 'Property' | The Direction property of this object specifies the targeting <br> direction. |
| :--- | :--- |
| 'Input port' | An input argument in each invocation of step specifies the <br> targeting direction. |

## Default: 'Property'

## Direction

Targeting direction
Specify the targeting direction of the SMI processor as a column vector of length 2 . The direction is specified in the format of [AzimuthAngle; ElevationAngle] (in degrees). Azimuth angle should be between -180 and 180. Elevation angle should be between -90 and 90. This property applies when you set the DirectionSource property to 'Property'. You can specify this property as single or double precision.

Default: [0; 0]
NumPhaseShifterBits
Number of phase shifter quantization bits
The number of bits used to quantize the phase shift component of beamformer or steering vector weights. Specify the number of bits as a non-negative integer. A value of zero indicates that no quantization is performed. You can specify this property as single or double precision.

## Default: 0

## DopplerSource

Source of targeting Doppler
Specify whether the targeting Doppler for the STAP processor comes from the Doppler property of this object or from an input argument in step. Values of this property are:

| 'Property' | The Doppler property of this object specifies the Doppler. |
| :--- | :--- |
| 'Input port ' | An input argument in each invocation of step specifies the Doppler. |

Default: 'Property'
Doppler

## Targeting Doppler frequency

Specify the targeting Doppler of the STAP processor as a scalar. This property applies when you set the DopplerSource property to 'Property'. You can specify this property as single or double precision.

Default: 0

## NumGuardCells

Number of guarding cells
Specify the number of guard cells used in the training as an even integer. This property specifies the total number of cells on both sides of the cell under test. You can specify this property as single or double precision.

Default: 2, indicating that there is one guard cell at both the front and back of the cell under test
NumTrainingCells
Number of training cells
Specify the number of training cells used in the training as an even integer. Whenever possible, the training cells are equally divided before and after the cell under test. You can specify this property as single or double precision.

Default: 2, indicating that there is one training cell at both the front and back of the cell under test

## WeightsOutputPort

Output processing weights
To obtain the weights used in the STAP processor, set this property to true and use the corresponding output argument when invoking step. If you do not want to obtain the weights, set this property to false.

Default: false

## Methods

step Perform SMI STAP processing on input data

## Common to All System Objects

```
release Allow System object property value changes
```


## Examples

## Process Data Cube Using SMI

Process a data cube using an SMI beamformer. The weights are calculated for the 71st cell of a collected data cube pointing in the azimuth and elevation direction $\left(45^{\circ},-35^{\circ}\right)$ and with a Doppler of 12.980 kHz .

Load the cube data and create the SMI beamformer.

```
load STAPExampleData;
beamformer = phased.STAPSMIBeamformer('SensorArray',STAPEx_HArray, ...
    'PRF',STAPEx_PRF,'PropagationSpeed',STAPEx_PropagationS̄peed, ...
    'OperatingFrequency',STAPEx_OperatingFrequency, ...
    'NumTrainingCells',100,'WeightsOutputPort',true, ...
    'DirectionSource','Input port','DopplerSource','Input port');
[y,w] = beamformer(STAPEx ReceivePulse,71,[45;-35],12.980e3);
```

Plot the angle-doppler response.

```
response = phased.AngleDopplerResponse( ...
    'SensorArray',beamformer.SensorArray, ...
    'OperatingFrequency',beamformer.OperatingFrequency, ...
    'PRF' ,beamformer.PRF,'PropagationSpeed',beamformer.PropagationSpeed);
plotResponse(response,w)
```



## Algorithms

## Weight Computation

The optimum beamformer weights are

$$
w=k R^{-1} v
$$

where:

- $k$ is a scalar
- $R$ represents the space-time covariance matrix
- $v$ indicates the space-time steering vector

Because the space-time covariance matrix is unknown, you must estimate that matrix from the data. The sample matrix inversion (SMI) algorithm estimates the covariance matrix by designating a number of range gates to be training cells. Because you use the training cells to estimate the interference covariance, these cells should not contain target returns. To prevent target returns from contaminating the estimate of the interference covariance, you can specify insertion of a number of guard cells before and after the designated target cell.

To use the general algorithm for estimating the space-time covariance matrix:

1 Assume you have a M-by-N-by-K matrix. M represents the number of slow-time samples, and N is the number of array sensors. K is the number of training cells (range gates for training). Also assume that the number of training cells is an even integer and that you can designate $\mathrm{K} / 2$ training cells before and after the target range gate excluding the guard cells. Reshape the M-by-N-by-K matrix into a MN-by-K matrix by letting X denote the MN-by-K matrix.
2 Estimate the space-time covariance matrix as
$\frac{1}{K} X X^{H}$
3 Invert the space-time covariance matrix estimate.
4 Obtain the beamforming weights by multiplying the sample space-time covariance matrix inverse by the space-time steering vector.

## Single Precision

This System object supports single and double precision for input data, properties, and arguments. If the input data $X$ is single precision, the output data is single precision. If the input data $X$ is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

## Version History

## Introduced in R2011a

## References

[1] Guerci, J. R. Space-Time Adaptive Processing for Radar. Boston: Artech House, 2003.
[2] Ward, J. "Space-Time Adaptive Processing for Airborne Radar Data Systems," Technical Report 1015, MIT Lincoln Laboratory, December, 1994.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\text {TM }}$.
Usage notes and limitations:

## See Also

phased.ADPCACanceller|phased.AngleDopplerResponse | phased.DPCACanceller| uv2azel | phitheta2azel

## step

System object: phased.STAPSMIBeamformer
Package: phased
Perform SMI STAP processing on input data

## Syntax

Y = step( $\mathrm{H}, \mathrm{X}$, CUTIDX)
Y = step(H,X,CUTIDX, PRF)
$Y=\operatorname{step}(H, X, C U T I D X, A N G)$
Y = step(H,X,CUTIDX,DOP)
$[\mathrm{Y}, \mathrm{W}]=\operatorname{step}($

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step (obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.
$\mathrm{Y}=\operatorname{step}(\mathrm{H}, \mathrm{X}$, CUTIDX) applies SMI processing to the input data, X . X must be a 3 -dimensional M -by- N -by- P numeric array whose dimensions are (range, channels, pulses). The processing weights are calculated according to the range cell specified by CUTIDX. The targeting direction and the targeting Doppler are specified by Direction and Doppler properties, respectively. Y is a column vector of length $M$. This syntax is available when the DirectionSource property is 'Property' and the DopplerSource property is 'Property'.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

Y = step ( $\mathrm{H}, \mathrm{X}$, CUTIDX, PRF) uses PRF as the pulse repetition frequency. This syntax is available when the PRFSource property is 'Input port'.
$\mathrm{Y}=$ step ( $\mathrm{H}, \mathrm{X}$, CUTIDX, ANG) uses ANG as the targeting direction. This syntax is available when the DirectionSource property is 'Input port '. ANG must be a 2 -by- 1 vector in the form of
[AzimuthAngle; ElevationAngle] (in degrees). The azimuth angle must be between -180 and 180. The elevation angle must be between -90 and 90 .

Y = step(H,X,CUTIDX, DOP) uses DOP as the targeting Doppler frequency (in hertz). This syntax is available when the DopplerSource property is 'Input port'. DOP must be a scalar.

You can combine optional input arguments when their enabling properties are set: $\mathrm{Y}=$ step (H, X, CUTIDX,ANG, DOP)
$[\mathrm{Y}, \mathrm{W}]=\operatorname{step}(\ldots \quad$ ) returns the additional output, W , as the processing weights. This syntax is available when the WeightsOutputPort property is true. W is a column vector of length $N^{*} P$.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Examples

## Process Data Cube Using SMI

Process a data cube using an SMI beamformer. The weights are calculated for the 71st cell of a collected data cube pointing in the azimuth and elevation direction $\left(45^{\circ},-35^{\circ}\right)$ and with a Doppler of 12.980 kHz .

Load the cube data and create the SMI beamformer.

```
load STAPExampleData;
beamformer = phased.STAPSMIBeamformer('SensorArray',STAPEx_HArray, ...
    'PRF',STAPEx_PRF,'PropagationSpeed',STAPEx_PropagationSpeed, ...
    'OperatingFrēquency',STAPEx_OperatingFrequēncy, ...
    'NumTrainingCells',100,'Weights0utputPort',true, ...
    'DirectionSource','Input port','DopplerSource','Input port');
[y,w] = beamformer(STAPEx_ReceivePulse,71,[45;-35],12.980e3);
```

Plot the angle-doppler response.

```
response = phased.AngleDopplerResponse( ...
    'SensorArray',beamformer.SensorArray, ...
    'OperatingFrequency',beamformer.OperatingFrequency, ...
    'PRF',beamformer.PRF,'PropagationSpeed ',beamformer.PropagationSpeed);
plotResponse(response,w)
```



## See Also

uv2azel|phitheta2azel

# phased.ShortDipoleAntennaElement 

Package: phased
Short-dipole antenna element

## Description

The phased. ShortDipoleAntennaElement object models a short-dipole antenna element. A shortdipole antenna is a center-fed wire whose length is much shorter than one wavelength. This antenna object only supports polarized fields.

To compute the response of the antenna element for specified directions:
1 Create the phased.ShortDipoleAntennaElement object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

```
antenna = phased.ShortDipoleAntennaElement
antenna = phased.ShortDipoleAntennaElement(Name,Value)
RESP = antenna(H,FREQ,ANG)
```

Description
antenna = phased. ShortDipoleAntennaElement creates the system object, h , to model a shortdipole antenna element.
antenna $=$ phased.ShortDipoleAntennaElement(Name,Value) creates the system object, antenna, with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN).

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

FrequencyRange - Antenna operating frequency range
[0 1e20] (default) | real-valued 1-by-2 row vector

Antenna operating frequency range specified as a 1-by-2 row vector in the form of [LowerBound HigherBound]. This vector defines the frequency range over which the antenna has a response. The antenna element has zero response outside this specified frequency range.

## Data Types: double

## AxisDirection - Dipole axis direction

'Z' (default)| 'Y'|'Z'|'Custom'
Dipole axis direction, specified as one of ' $X^{\prime}$, ' $Y^{\prime}$, ' $Z$ ', or 'Custom'. The dipole axis defines the direction of the dipole current with respect to the local coordinate system. ' $X$ ' specifies a dipole along the $x$-axis, ' $Y$ ' specifies a dipole along the $y$-axis, and ' $Z$ ' specifies a dipole along the $z$-axis. An $x$-axis or $y$-axis direction is equivalent to a horizontal dipole and a $z$-axis direction is equivalent to a vertical dipole. When you set the AxisDirection property to 'Custom', you can specify the dipole axis using the CustomAxisDirection property.
Data Types: char

## CustomAxisDirection - Custom dipole axis direction

[0;0;1] (default) | real-valued 3-element column vector
Custom axis direction of the dipole antenna, specified as a real-valued 3-element column vector. Each entry in the vector represents the component of the dipole axis along the $x, y$, and $z$ axes in the local coordinate system.
Dependencies
To enable this property, set the AxisDirection property to 'Custom'.
Data Types: double

## Usage

## Syntax

RESP = antenna( $\mathrm{H}, \mathrm{FREQ}, \mathrm{ANG})$

## Description

RESP $=$ antenna( $H, F R E Q, A N G)$ returns the antenna's voltage response, RESP, at the operating frequencies specified in FREQ and in the directions specified in ANG. For the short-dipole antenna element object, RESP is a MATLAB struct containing two fields, RESP. H and RESP.V, representing the horizontal and vertical polarization components of the antenna's response. Each field is an $M$-by- $L$ matrix containing the antenna response at the $M$ angles specified in ANG and at the $L$ frequencies specified in FREQ.

## Input Arguments

## FREQ - Operating frequency of antenna element

nonnegative scalar | nonnegative, real-valued 1-by-L row vector
Operating frequency of the antenna element, specified as a nonnegative scalar or nonnegative, realvalued 1-by- $L$ row vector. Frequency units are in Hz.

FREQ must lie within the range of values specified by the FrequencyRange or the FrequencyVector property of the element. Otherwise, the element produces no response and the
response is returned as -Inf. Element objects use the FrequencyRange property, except for phased.CustomAntennaElement, which uses the FrequencyVector property.

Example: [1e8 2e6]
Data Types: double

## ANG - Azimuth and elevation angles of response directions

real-valued 1-by-M row vector | real-valued 2-by-M matrix
Azimuth and elevation angles of the response directions, specified as a real-valued 1-by-M row vector or a real-valued 2 -by- $M$ matrix, where $M$ is the number of angular directions. Angle units are in degrees. The azimuth angle must lie in the range $-180^{\circ}$ to $180^{\circ}$, inclusive. The elevation angle must lie in the range $-90^{\circ}$ to $90^{\circ}$, inclusive.

- If ANG is a 1 -by- $M$ vector, each element specifies the azimuth angle of the direction. In this case, the corresponding elevation angle is assumed to be zero.
- If ANG is a 2 -by- $M$ matrix, each column of the matrix specifies the direction in the form [azimuth;elevation].

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the $x y$-plane. This angle is positive when measured from the $x$-axis toward the $y$-axis. The elevation angle is the angle between the direction vector and $x y$-plane. This angle is positive when measured toward the $z$-axis. See the definition of "Azimuth and Elevation Angles".
Example: [110 125; 15 10]
Data Types: double

## Output Arguments

## RESP - Antenna voltage response

struct
Voltage response of antenna element returned as a MATLAB struct with fields RESP.H and RESP.V. Both RESP.H and RESP.V contain responses for the horizontal and vertical polarization components of the antenna radiation pattern. Both RESP. H and RESP.V are $M$-by- $L$ matrices. In these matrices, $M$ represents the number of angles specified in ANG, and $L$ represents the number of frequencies specified in FREQ.
Data Types: double

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```


## Specific to Antenna and Transducer Element System Objects

beamwidth
directivity
isPolarizationCapable
pattern

Compute and display beamwidth of sensor element pattern Directivity of antenna or transducer element
Antenna element polarization capability
Plot antenna or transducer element directivity and patterns
patternAzimuth patternElevation

Plot antenna or transducer element directivity and pattern versus azimuth Plot antenna or transducer element directivity and pattern versus elevation

## Common to All System Objects

step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object

## Examples

## Response of Short-Dipole Antenna

Find the response of a short-dipole antenna element at boresight, $\left(0^{\circ}, 0^{\circ}\right)$, and off boresight, $\left(30^{\circ}, 0^{\circ}\right)$. The antenna operates at 256 MHz .

```
antenna = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[100 900]*le6,'AxisDirection','Y');
ang = [0 30;0 0];
fc = 250e6;
resp = antenna(fc,ang)
resp = struct with fields:
    H: [2x1 double]
    V: [2x1 double]
```

Horizontal response.

```
disp(resp.H)
```

    -1. 2247
    -1.0607
    Vertical response.

```
disp(resp.V)
```

0
0

## Short-Dipole Antenna Aligned Along the Y-Axis

Specify a short-dipole antenna with the dipole oriented along the $y$-axis and operating at 250 MHz . Then, plot the 3-D responses for both the horizontal and vertical polarizations.

```
antenna = phased.ShortDipoleAntennaElement( . ..
    'FrequencyRange',[100e6,600e6],'AxisDirection', 'Y');
fc = 250.0e6;
```

Plot the horizontal polarization response.
pattern(antenna,fc,-180:180,[-90:90],'CoordinateSystem','polar', ...
'Type', 'powerdb', 'Polarization','H');


Plot the vertical polarization response.
pattern(antenna,fc,-180:180,[-90:90],'CoordinateSystem','polar', ...
'Type', 'powerdb', 'Polarization', 'V');


Plot the combined response.
pattern(antenna,fc,-180:180,[-90:90],'CoordinateSystem','polar',...
'Type', 'powerdb', 'Polarization', 'C');


## Short-Dipole Antenna Aligned Along Arbitrary Axis

Specify a short-dipole antenna with the dipole oriented along a custom axis and operating at 250 MHz . Then, plot the 3-D responses for both the horizontal and vertical polarizations.

Create the short-dipole antenna element System object ${ }^{\mathrm{Tm}}$. An easy way to create a custom axis is to rotate a unit vector using rotation functions.

```
v = rotx(30)*rotz(45)*[0;0;1];
antenna = phased.ShortDipoleAntennaElement( ...
    'FrequencyRange',[100e6,600e6],'AxisDirection','Custom', ...
    'CustomAxisDirection',v);
```

Plot the horizontal polarization response.

```
fc = 250.0e6;
pattern(antenna,fc,-180:180,[-90:90],'CoordinateSystem','polar', ...
    'Type','powerdb','Polarization','H');
```



Plot the vertical polarization response.
pattern(antenna,fc,-180:180,[-90:90],'CoordinateSystem','polar', ...
'Type', 'powerdb', 'Polarization', 'V');


Plot the combined response.
pattern(antenna,fc,-180:180,[-90:90],'CoordinateSystem','polar', ...
'Type', 'powerdb', 'Polarization', 'C');


## Algorithms

The total response of a short-dipole antenna element is a combination of its frequency response and spatial response. This System object calculates both responses using nearest neighbor interpolation and then multiplies the responses to form the total response.

## Version History

Introduced in R2013a

## References

[1] Mott, H., Antennas for Radar and Communications, John Wiley \& Sons, 1992.

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:

- pattern, patternAzimuth, patternElevation, and plotResponse methods are not supported.
- See "System Objects in MATLAB Code Generation" (MATLAB Coder).


## See Also

phased.CosineAntennaElement | phased.CrossedDipoleAntennaElement | phased.CustomAntennaElement | phased.IsotropicAntennaElement|phased.ULA| phased.URA|phased.ConformalArray|uv2azelpat|phitheta2azelpat|uv2azel| phitheta2azel

## directivity

System object: phased. ShortDipoleAntennaElement
Package: phased
Directivity of short-dipole antenna element

## Syntax

D = directivity (H,FREQ,ANGLE)

## Description

D = directivity (H, FREQ, ANGLE) returns the "Directivity (dBi)" on page 1-1545 of a short-dipole antenna element, H , at frequencies specified by FREQ and in direction angles specified by ANGLE.

## Input Arguments

## H - Short-dipole antenna element

System object
Short-dipole antenna element specified as a phased.ShortDipoleAntennaElement System object.
Example: H = phased.ShortDipoleAntennaElement;

## FREQ - Frequency for computing directivity and patterns

positive scalar | 1-by-L real-valued row vector
Frequencies for computing directivity and patterns, specified as a positive scalar or 1-by-L realvalued row vector. Frequency units are in hertz.

- For an antenna, microphone, or sonar hydrophone or projector element, FREQ must lie within the range of values specified by the FrequencyRange or FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased. CustomAntennaElement and phased.CustomMic rophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.


## Example: [1e8 2e6]

Data Types: double

## ANGLE - Angles for computing directivity

1-by-M real-valued row vector | 2 -by- $M$ real-valued matrix
Angles for computing directivity, specified as a 1-by- $M$ real-valued row vector or a 2 -by- $M$ real-valued matrix, where $M$ is the number of angular directions. Angle units are in degrees. If ANGLE is a 2 -by- $M$ matrix, then each column specifies a direction in azimuth and elevation, [az;el]. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

If ANGLE is a 1 -by- $M$ vector, then each entry represents an azimuth angle, with the elevation angle assumed to be zero.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the xy plane. This angle is positive when measured from the $x$-axis toward the $y$-axis. The elevation angle is the angle between the direction vector and $x y$ plane. This angle is positive when measured towards the $z$-axis. See "Azimuth and Elevation Angles".

Example: [45 60; 0 10]
Data Types: double

## Output Arguments

## D - Directivity

$M$-by-L matrix
Directivity, returned as an $M$-by- $L$ matrix. Each row corresponds to one of the $M$ angles specified by ANGLE. Each column corresponds to one of the $L$ frequency values specified in FREQ. Directivity units are in dBi where dBi is defined as the gain of an element relative to an isotropic radiator.

## Examples

## Directivity of Short-Dipole Antenna Element

Compute the directivity of a z-directed short-dipole antenna element as a function of elevation.
Create the crossed-dipole antenna element System object ${ }^{\mathrm{Tm}}$.

```
myAnt = phased.ShortDipoleAntennaElement;
myAnt.AxisDirection = 'Z';
myAnt.FrequencyRange = [0,10e9];
```

Select the desired angles of interest to be at constant azimuth angle at zero degrees. Set the elevation angles to center around boresight (zero degrees azimuth and zero degrees elevation). Set the frequency to 1 GHz .

```
elev = [-30:30];
azm = zeros(size(elev));
ang = [azm;elev];
freq = 1e9;
```

Plot the directivity along the constant azimuth cut.

```
d = directivity(myAnt,freq,ang);
plot(elev,d)
xlabel('Elevation (deg)');
ylabel('Directivity (dBi)');
```



## More About

## Directivity (dBi)

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\text {rad }}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## See Also

pattern | patternElevation | patternAzimuth

## isPolarizationCapable

System object: phased. ShortDipoleAntennaElement
Package: phased
Polarization capability

## Syntax

flag = isPolarizationCapable(h)

## Description

flag = isPolarizationCapable(h) returns a Boolean value, flag, indicating whether the phased.ShortDipoleAntennaElement antenna element supports polarization or not. An antenna element supports polarization if it can create or respond to polarized fields. The phased. ShortDipoleAntennaElement object always supports polarization.

## Input Arguments

## h - Short-dipole antenna element

Short-dipole antenna element specified as a phased.ShortDipoleAntennaElement System object.

## Output Arguments

## flag - Polarization-capability flag

Polarization-capability returned as a Boolean value true if the antenna element supports polarization or false if it does not. Because the short-dipole antenna element supports polarization, the returned value is always true.

## Examples

## Short-Dipole Antenna Supports Polarization

Show that a phased. ShortDipoleAntennaElement antenna supports polarization.

```
antenna = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[100e6 1e9],...
    'AxisDirection','Z');
isPolarizationCapable(antenna)
ans = logical
    1
```

The returned value of 1 shows that this antenna supports polarization.

## pattern

System object: phased. ShortDipoleAntennaElement
Package: phased
Plot short-dipole antenna element directivity and patterns

## Syntax

pattern(sElem,FREQ)
pattern(sElem, FREQ,AZ)
pattern(sElem, FREQ,AZ, EL)
pattern(__, Name, Value)
[PAT,AZ_ANG,EL_ANG] = pattern( $\qquad$ )

## Description

pattern(sElem, FREQ) plots the 3-D array directivity pattern (in dBi) for the element specified in sElem. The operating frequency is specified in FREQ.
pattern(sElem, FREQ,AZ) plots the element directivity pattern at the specified azimuth angle.
pattern(sElem, FREQ,AZ,EL) plots the element directivity pattern at specified azimuth and elevation angles.
pattern(__, Name, Value) plots the element pattern with additional options specified by one or more Name, Value pair arguments.
[PAT,AZ_ANG,EL_ANG] = pattern (___) returns the element pattern in PAT. The AZ_ANG output contains the coordinate values corresponding to the rows of PAT. The EL_ANG output contains the coordinate values corresponding to the columns of PAT. If the 'CoordinateSystem' parameter is set to ' $u v$ ', then AZ_ANG contains the $U$ coordinates of the pattern and EL_ANG contains the $V$ coordinates of the pattern. Otherwise, they are in angular units in degrees. $U V$ units are dimensionless.

Note This method replaces the plotResponse method. See "Convert plotResponse to pattern" on page 1-1554 for guidelines on how to use pattern in place of plotResponse.

## Input Arguments

## sElem - Short-dipole antenna element

System object
Short-dipole antenna element, specified as a phased.ShortDipoleAntennaElement System object.

```
Example: sElem = phased.ShortDipoleAntennaElement;
```

FREQ - Frequency for computing directivity and patterns

Frequencies for computing directivity and patterns, specified as a positive scalar or 1-by-L realvalued row vector. Frequency units are in hertz.

- For an antenna, microphone, or sonar hydrophone or projector element, FREQ must lie within the range of values specified by the FrequencyRange or FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased. CustomAntennaElement and phased. CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.


## Example: [1e8 2e6]

Data Types: double

## AZ - Azimuth angles

[-180:180] (default) | 1-by-N real-valued row vector
Azimuth angles for computing directivity and pattern, specified as a $1-b y-N$ real-valued row vector where $N$ is the number of azimuth angles. Angle units are in degrees. Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the $x y$ plane. When measured from the $x$-axis toward the $y$-axis, this angle is positive.

## Example: [-45:2:45]

Data Types: double

## EL - Elevation angles

[-90:90] (default) | 1-by-M real-valued row vector
Elevation angles for computing directivity and pattern, specified as a 1-by- $M$ real-valued row vector where $M$ is the number of desired elevation directions. Angle units are in degrees. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

The elevation angle is the angle between the direction vector and $x y$-plane. The elevation angle is positive when measured towards the $z$-axis.
Example: [-75:1:70]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## CoordinateSystem - Plotting coordinate system

'polar' (default)|'rectangular'|'uv'
Plotting coordinate system of the pattern, specified as the comma-separated pair consisting of
'CoordinateSystem' and one of 'polar', 'rectangular', or 'uv'. When
'CoordinateSystem' is set to 'polar' or 'rectangular', the AZ and EL arguments specify the
pattern azimuth and elevation, respectively. AZ values must lie between $-180^{\circ}$ and $180^{\circ}$. EL values must lie between $-90^{\circ}$ and $90^{\circ}$. If 'CoordinateSystem' is set to 'uv', AZ and EL then specify $U$ and $V$ coordinates, respectively. AZ and EL must lie between -1 and 1.
Example: 'uv'
Data Types: char

## Type - Displayed pattern type

'directivity' (default) |'efield'|'power'|'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type ' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb' - power pattern converted to dB.

Example: 'powerdb'
Data Types: char

## Normalize - Display normalize pattern

true (default) | false
Display normalized pattern, specified as the comma-separated pair consisting of 'Normalize' and a Boolean. Set this parameter to true to display a normalized pattern. This parameter does not apply when you set 'Type' to 'directivity'. Directivity patterns are already normalized.
Data Types: logical

## PlotStyle - Plotting style

'overlay' (default)|'waterfall'
Plotting style, specified as the comma-separated pair consisting of 'Plotstyle' and either 'overlay' or 'waterfall '. This parameter applies when you specify multiple frequencies in FREQ in 2-D plots. You can draw 2-D plots by setting one of the arguments AZ or EL to a scalar.

## Data Types: char

## Polarization - Polarized field component

'combined' (default) | 'H' | 'V'
Polarized field component to display, specified as the comma-separated pair consisting of 'Polarization' and 'combined ', 'H' , or 'V'. This parameter applies only when the sensors are polarization-capable and when the 'Type' parameter is not set to 'directivity'. This table shows the meaning of the display options.

| 'Polarization ' | Display |
| :--- | :--- |
| 'combined ' | Combined $H$ and $V$ polarization components |
| 'H' | $H$ polarization component |
| ' $\mathrm{V}^{\prime}$ | $V$ polarization component |

Example: 'V '

Data Types: char

## Output Arguments

## PAT - Element pattern

$N$-by- $M$ real-valued matrix
Element pattern, returned as an $N$-by- $M$ real-valued matrix. The pattern is a function of azimuth and elevation. The rows of PAT correspond to the azimuth angles in the vector specified by EL_ANG. The columns correspond to the elevation angles in the vector specified by AZ_ANG.

## AZ_ANG - Azimuth angles

scalar | 1-by-N real-valued row vector
Azimuth angles for displaying directivity or response pattern, returned as a scalar or 1-by- N realvalued row vector corresponding to the dimension set in AZ. The columns of PAT correspond to the values in AZ_ANG. Units are in degrees.

## EL_ANG - Elevation angles

scalar | 1-by-M real-valued row vector
Elevation angles for displaying directivity or response, returned as a scalar or 1-by-M real-valued row vector corresponding to the dimension set in EL. The rows of PAT correspond to the values in EL_ANG. Units are in degrees.

## Examples

## Pattern of Short-Dipole Antenna Oriented Along the Z-Axis

Specify a short-dipole antenna element with its dipole axis pointing along the $z$-axis. To do so, set the 'AxisDirection' value to ' $Z$ '.

```
sSD = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[100 900]*le6,'AxisDirection','Z');
```

Plot the antenna's vertical polarization power pattern at 200 MHz as a 3-D polar plot.

```
fc = 200e6;
pattern(sSD,fc,[-180:180],[-90:90],...
    'CoordinateSystem','polar',...
    'Type','powerdb',...
    'Polarization','V')
```



As the above figure shows, the antenna pattern is that of a vertically-oriented dipole and has its maximum at the equator and nulls at the poles.

## Short-Dipole Antenna Element Pattern over Selected Range

Specify a short-dipole antenna element with its dipole axis pointing along the $z$-axis. Then, plot the magnitude pattern over a selected range of angles. The antenna operating frequency spans the range 100 to 900 MHz .

To construct a z-directed short-dipole antenna, set the 'AxisDirection ' value to ' $Z$ '.

```
sSD = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[100 900]*1e6,...
    'AxisDirection','Z');
```

Plot the antenna's vertical polarization response at 200 MHz as an elevation cut at zero degrees azimuth angle. Restrict the plot from -60 to 60 degrees elevation in 0.1 degree increments.

```
fc = 200e6;
pattern(sSD,fc,0,[-60:0.1:60],...
    'CoordinateSystem','polar',...
    'Type','efield',...
    'Polarization','V')
```



Normalized Magnitude, Broadside at $0.00^{\circ}$

## Short-Dipole Antenna Element Directivity

Specify a short-dipole antenna element with its dipole axis pointing along the $y$-axis. Then, plot the directivity. The antenna operating frequency spans the range 100 to 900 MHz .

Construct a y-directed short-dipole antenna by setting the 'AxisDirection' value to ' Y '.
sSD = phased. ShortDipoleAntennaElement(...
'FrequencyRange',[100 900]*1e6,...
'AxisDirection','Y');
Plot the antenna's directivity at 500 MHz as an elevation cut at zero degrees azimuth angle.

```
fc = 500e6;
pattern(sSD,fc,0,[-90:90],...
    'CoordinateSystem','rectangular',...
    'Type','directivity')
```



## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \Pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as dBi. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Convert plotResponse to pattern

For antenna, microphone, and array System objects, the pattern method replaces the plotResponse method. In addition, two new simplified methods exist just to draw 2-D azimuth and elevation pattern plots. These methods are azimuthPattern and elevationPattern.

The following table is a guide for converting your code from using plotResponse to pattern. Notice that some of the inputs have changed from input arguments to Name-Value pairs and conversely. The general pattern method syntax is
pattern(H,FREQ,AZ,EL,'Name1','Value1',...,' $N a m e N ', ' V a l u e N ') ~$

| plotResponse Inputs | plotResponse Description | pattern Inputs |
| :--- | :--- | :--- |
| H argument | Antenna, microphone, or array <br> System object. | H argument (no change) |
| FREQ argument | Operating frequency. | FREQ argument (no change) |
| V argument | Propagation speed. This argument <br> is used only for arrays. | 'PropagationSpeed ' name-value <br> pair. This parameter is only used for <br> arrays. |


| plotResponse Inputs | plotResponse Description |  | pattern Inputs |  |
| :---: | :---: | :---: | :---: | :---: |
| 'Format' and 'RespCut' namevalue pairs | These options work together to let you create a plot in angle space (line or polar style) or $U V$ space. They also determine whether the plot is 2-D or 3-D. This table shows you how to create different types of plots using plotResponse. |  | 'CoordinateSystem' name-value pair used together with the AZ and EL input arguments. <br> 'CoordinateSystem' has the same options as the plotResponse method 'Format ' name-value pair, except that 'line' is now named 'rectangular'. The table shows how to create different types of plots using pattern. |  |
|  | Display space |  |  |  |
|  | Angle space (2D) |  |  |  |
|  |  | Set 'RespCut'to 'Az' or'El'. Set'Format' to'line' or'polar'.Set the displayaxis using eitherthe'AzimuthAngleS' or'ElevationAngles' name-value pairs. | Display space |  |
|  |  |  | Angle space (2D) <br> Angle space (3D) | Set <br> 'Coordinate <br> System' to rectangular' or 'polar'. <br> Specify either AZ or EL as a scalar. |
|  |  |  |  | Set <br> 'Coordinate <br> System' to 'rectangular' |
|  | Angle space (3D) | Set 'RespCut' to '3D'. Set 'Format' to ' line' or 'polar'. <br> Set the display axis using both the 'AzimuthAngle ${ }^{\prime}$ and 'Elevation Angles ' namevalue pairs. |  | or 'polar'. <br> Specify both AZ and EL as vectors. |
|  |  |  | UV space (2D) | Set <br> 'Coordinate <br> System' to 'uv'. Use AZ to specify a $U$ space vector. Use EL to specify a $V$-space scalar. |
|  |  |  | UV space (3D) | Set |
|  | UV space (2D) | Set 'RespCut' to'U'. Set 'Format' to 'UV '. Set the display range using the 'UGrid' namevalue pair. |  | System' to 'uv'. Use AZ to specify a $U$ space vector. <br> Use EL to specify a $V$-space vector. |
|  |  |  | If you set CoordinateSystem to 'uv', enter the UV grid values using AZ and EL . |  |
|  | UV space (3D) | $\begin{aligned} & \text { Set 'RespCut' } \\ & \text { to'3D'. Set } \\ & \text { 'Format' to } \end{aligned}$ |  |  |


| plotResponse Inputs | plotResponse Description |  | pattern Inputs |
| :---: | :---: | :---: | :---: |
|  | Display space | 'UV '. Set the display range using both the 'UGrid' and 'VGrid ' namevalue pairs. |  |
| 'CutAngle' name-value pair | Constant angle at to take an azimuth or elevation cut. When producing a 2-D plot and when 'RespCut' is set to 'Az' or 'El', use 'CutAngle' to set the slice across which to view the plot. |  | No equivalent name-value pair. To create a cut, specify either AZ or EL as a scalar, not a vector. |
| 'NormalizeResponse' namevalue pair | Normalizes the plot. When 'Unit' is set to 'dbi' , you cannot specify 'NormalizeResponse'. |  | Use the 'Normalize' name-value pair. When 'Type' is set to 'directivity' you cannot specify 'Normalize'. |
| 'OverlayFreq' name-value pair | Plot multiple frequencies on the same 2-D plot. Available only when 'Format' is set to 'line' or 'uv and 'RespCut' is not set to '3D'. The value true produces an overlay plot and the value false produces a waterfall plot. |  | 'PlotStyle' name-value pair plots multiple frequencies on the same 2-D plot. <br> The values 'overlay' and 'waterfall' correspond to 'OverlayFreq' values of true and false. The option 'waterfall' is allowed only when 'CoordinateSystem' is set to 'rectangular' or 'uv'. |
| 'Polarization' name-value pair | Determines how to plot polarized fields. Options are 'None', 'Combined', 'H', or 'V'. |  | 'Polarization ' name-value pair determines how to plot polarized fields. The 'None ' option is removed. The options 'Combined ' , ' H ', or 'V' are unchanged. |
| ' Unit ' name-value pair | Determines the plot units. Choose 'db','mag', 'pow', or 'dbi', where the default is ' db ' |  | 'Type ' name-value pair, uses equivalent options with different names |
|  |  |  | plotResponse pattern |
|  |  |  | 'db' 'powerdb' <br> 'mag' 'efield' <br> 'pow' 'power' <br> 'dbi' 'directivity' |
| 'Weights ' name-value pair | Array element tapers (or weights). |  | 'Weights ' name-value pair (no change). |
| 'AzimuthAngles ' name-value pair | Azimuth angles used to display the antenna or array response. |  | AZ argument |


| plotResponse Inputs | plotResponse Description | pattern Inputs |
| :--- | :--- | :--- |
| ' ElevationAngles ' name-value <br> pair | Elevation angles used to display the <br> antenna or array response. | EL argument |
| ' UGrid' name-value pair | Contains $U$ coordinates in $U V$ - <br> space. | AZ argument when <br> 'CoordinateSystem ' name-value <br> pair is set to 'uv ' |
| 'VGrid' name-value pair | Contains $V$-coordinates in $U V$-space. | EL argument when <br> 'CoordinateSystem ' name-value <br> pair is set to 'uv ' |

## Version History <br> Introduced in R2015a

See Also<br>patternElevation| patternAzimuth

## patternAzimuth

System object: phased. ShortDipoleAntennaElement
Package: phased
Plot short-dipole antenna element directivity or pattern versus azimuth

## Syntax

patternAzimuth(sElem, FREQ)
patternAzimuth(sElem,FREQ,EL)
patternAzimuth(sElem, FREQ, EL, Name, Value)
PAT = patternAzimuth( $\qquad$

## Description

patternAzimuth (sElem, FREQ) plots the 2-D element directivity pattern versus azimuth (in dBi) for the element sElem at zero degrees elevation angle. The argument FREQ specifies the operating frequency.
patternAzimuth (sElem, FREQ,EL), in addition, plots the 2-D element directivity pattern versus azimuth (in dBi ) at the elevation angle specified by EL. When EL is a vector, multiple overlaid plots are created.
patternAzimuth(sElem, FREQ,EL,Name,Value) plots the element pattern with additional options specified by one or more Name, Value pair arguments.

PAT = patternAzimuth( $\qquad$ ) returns the element pattern. PAT is a matrix whose entries represent the pattern at corresponding sampling points specified by the 'Azimuth' parameter and the EL input argument.

## Input Arguments

## sElem - Short-dipole antenna element

System object
Short-dipole antenna element, specified as a phased.ShortDipoleAntennaElement System object.

```
Example: sElem = phased.ShortDipoleAntennaElement;
```


## FREQ - Frequency for computing directivity and pattern

positive scalar
Frequency for computing directivity and pattern, specified as a positive scalar. Frequency units are in hertz.

- For an antenna or microphone element, FREQ must lie within the range of values specified by the FrequencyRange or the FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased. CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: 1e8
Data Types: double

## EL - Elevation angles

1-by- $N$ real-valued row vector
Elevation angles for computing sensor or array directivities and patterns, specified as a 1-by- $N$ realvalued row vector. The quantity $N$ is the number of requested elevation directions. Angle units are in degrees. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

The elevation angle is the angle between the direction vector and the xy plane. When measured toward the $z$-axis, this angle is positive.
Example: [0, 10, 20]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Type - Displayed pattern type

'directivity' (default) | 'efield' | 'power' | 'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power ' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb ' - power pattern converted to dB.

Example: 'powerdb'
Data Types: char

## Azimuth - Azimuth angles

[-180:180] (default) | 1-by-P real-valued row vector
Azimuth angles, specified as the comma-separated pair consisting of 'Azimuth' and a 1-by-P realvalued row vector. Azimuth angles define where the array pattern is calculated.
Example: 'Azimuth', [-90:2:90]
Data Types: double

## Output Arguments

## PAT - Element directivity or pattern

$P$-by- $N$ real-valued matrix
Element directivity or pattern, returned as an $P$-by- $N$ real-valued matrix. The dimension $P$ is the number of azimuth values determined by the 'Azimuth' name-value pair argument. The dimension $N$ is the number of elevation angles, as determined by the EL input argument.

## Examples

## Azimuth Directivity of Short-Dipole Antenna Element at Two Elevations

Specify a short-dipole antenna element having a direction along the $y$-axis. Then, plot an azimuth cut of the directivity at 0 and 30 degrees elevation. Assume the operating frequency is 500 MHz .

Create the antenna element.
fc = 500e6;
sSD = phased.ShortDipoleAntennaElement('FrequencyRange',[100,900]*1e6,...
'AxisDirection', 'y');
patternAzimuth(sSD,fc,[0 30])


Directivity (dBi), Broadside at $0.00^{\circ}$
Plot a reduced range of azimuth angles using the Azimuth parameter. Notice the change in scale.
patternAzimuth(sSD,fc,[0 30],'Azimuth',[-20:20])


Directivity (dBi), Broadside at $0.00^{\circ}$

## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \Pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Version History

Introduced in R2015a

See Also<br>pattern| patternElevation

## patternElevation

System object: phased. ShortDipoleAntennaElement
Package: phased
Plot short-dipole antenna element directivity or pattern versus elevation

## Syntax

```
patternElevation(sElem,FREQ)
patternElevation(sElem,FREQ,AZ)
patternElevation(sElem,FREQ,AZ,Name,Value)
PAT = patternElevation(
```

$\qquad$

## Description

patternElevation(sElem, FREQ) plots the 2-D element directivity pattern versus elevation (in dBi ) for the element sElem at zero degrees azimuth angle. The argument FREQ specifies the operating frequency.
patternElevation(sElem,FREQ,AZ), in addition, plots the 2-D element directivity pattern versus elevation (in dBi ) at the azimuth angle specified by $A Z$. When $A Z$ is a vector, multiple overlaid plots are created.
patternElevation(sElem,FREQ,AZ,Name, Value) plots the element pattern with additional options specified by one or more Name, Value pair arguments.

PAT = patternElevation (__ ) returns the element pattern. PAT is a matrix whose entries represent the pattern at corresponding sampling points specified by the 'Elevation' parameter and the AZ input argument.

## Input Arguments

## sElem - Short-dipole antenna element

System object
Short-dipole antenna element, specified as a phased.ShortDipoleAntennaElement System object.

```
Example: sElem = phased.ShortDipoleAntennaElement;
```


## FREQ - Frequency for computing directivity and pattern

positive scalar
Frequency for computing directivity and pattern, specified as a positive scalar. Frequency units are in hertz.

- For an antenna or microphone element, FREQ must lie within the range of values specified by the FrequencyRange or the FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased.CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: 1e8
Data Types: double

## AZ - Azimuth angles for computing directivity and pattern

1-by- $N$ real-valued row vector
Azimuth angles for computing sensor or array directivities and patterns, specified as a 1-by- N realvalued row vector where $N$ is the number of desired azimuth directions. Angle units are in degrees. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the xy plane. This angle is positive when measured from the $x$-axis toward the $y$-axis.
Example: [0,10,20]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Type - Displayed pattern type

'directivity' (default) | 'efield' | 'power' | 'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb ' - power pattern converted to dB.

Example: 'powerdb'
Data Types: char

## Elevation - Elevation angles

[-90:90] (default)| 1-by-P real-valued row vector
Elevation angles, specified as the comma-separated pair consisting of 'Elevation' and a 1-by-P real-valued row vector. Elevation angles define where the array pattern is calculated.
Example: 'Elevation', [-90:2:90]
Data Types: double

## Output Arguments

## PAT - Element directivity or pattern

$P$-by- $N$ real-valued matrix
Element directivity or pattern, returned as an $P$-by- $N$ real-valued matrix. The dimension $P$ is the number of elevation angles determined by the 'Elevation' name-value pair argument. The dimension $N$ is the number of azimuth angles determined by the AZ argument.

## Examples

## Plot Elevation Pattern of Crossed-Dipole Antenna Element

Plot the elevation directivity pattern of a crossed-dipole antenna at two different azimuths: $45^{\circ}$ and $55^{\circ}$. Assume the operating frequency is 500 MHz .
fc = 500e6;
sCD = phased.CrossedDipoleAntennaElement('FrequencyRange',[100,900]*1e6); patternElevation(sCD,fc,[45 55])


Directivity (dBi), Broadside at $0.00^{\circ}$

Plot a reduced range of elevation angles using the Elevation parameter. Notice the change in scale. patternElevation(sCD,fc,[45 55],'Elevation',-20:20)


Directivity (dBi), Broadside at $0.00^{\circ}$

## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Version History

Introduced in R2015a

## See Also

pattern|patternAzimuth

## plotResponse

System object: phased. ShortDipoleAntennaElement
Package: phased
Plot response pattern of antenna

## Syntax

plotResponse(H,FREQ)
plotResponse(H,FREQ,Name, Value)
hPlot = plotResponse( $\qquad$ )

## Description

plotResponse( $\mathrm{H}, \mathrm{FREQ}$ ) plots the element response pattern along the azimuth cut, where the elevation angle is 0 . The operating frequency is specified in FREQ.
plotResponse(H, FREQ,Name, Value) plots the element response with additional options specified by one or more Name, Value pair arguments.
hPlot $=$ plotResponse ( __ $)$ returns handles of the lines or surface in the figure window, using any of the input arguments in the previous syntaxes.

## Input Arguments

## H

Element System object

## FREQ

Operating frequency in Hertz specified as a scalar or 1-by-K row vector. FREQ must lie within the range specified by the FrequencyVector property of $\mathbf{H}$. If you set the 'RespCut ' property of H to ' 3 D ' , FREQ must be a scalar. When FREQ is a row vector, plotResponse draws multiple frequency responses on the same axes.

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## CutAngle

Cut angle specified as a scalar. This argument is applicable only when RespCut is ' Az ' or ' El '. If RespCut is 'Az', CutAngle must be between -90 and 90. If RespCut is 'El', CutAngle must be between -180 and 180 .

## Default: 0

## Format

Format of the plot, using one of 'Line', 'Polar', or 'UV '. If you set Format to 'UV ' , FREQ must be a scalar.

Default: 'Line'

## NormalizeResponse

Set this value to true to normalize the response pattern. Set this value to false to plot the response pattern without normalizing it. This parameter is not applicable when you set the Unit parameter value to 'dbi'.

Default: true

## OverlayFreq

Set this value to true to overlay pattern cuts in a 2-D line plot. Set this value to false to plot pattern cuts against frequency in a 3-D waterfall plot. If this value is false, FREQ must be a vector with at least two entries.

This parameter applies only when Format is not 'Polar' and RespCut is not '3D '.

## Default: true

## Polarization

Specify the polarization options for plotting the antenna response pattern. The allowable values are |'None' | 'Combined' | 'H' | 'V' | where

- 'None' specifies plotting a nonpolarized response pattern
- 'Combined ' specifies plotting a combined polarization response pattern
- 'H' specifies plotting the horizontal polarization response pattern
- 'V ' specifies plotting the vertical polarization response pattern

For antennas that do not support polarization, the only allowed value is 'None'. This parameter is not applicable when you set the Unit parameter value to ' dbi ' .

Default: 'None'

## RespCut

Cut of the response. Valid values depend on Format, as follows:

- If Format is 'Line' or 'Polar', the valid values of RespCut are 'Az', 'El', and '3D'. The default is ' Az '.
- If Format is 'UV', the valid values of RespCut are 'U' and '3D'. The default is 'U'.

If you set RespCut to ' 3D' , FREQ must be a scalar.

## Unit

The unit of the plot. Valid values are 'db', 'mag', 'pow', or 'dbi'. This parameter determines the type of plot that is produced.

| Unit value | Plot type |
| :--- | :--- |
| db | power pattern in dB scale |
| mag | field pattern |
| pow | power pattern |
| dbi | directivity |

Default: 'db'

## AzimuthAngles

Azimuth angles for plotting element response, specified as a row vector. The AzimuthAngles parameter sets the display range and resolution of azimuth angles for visualizing the radiation pattern. This parameter is allowed only when the RespCut parameter is set to ' Az ' or ' $3 D^{\prime}$ and the Format parameter is set to 'Line' or 'Polar'. The values of azimuth angles should lie between $180^{\circ}$ and $180^{\circ}$ and must be in nondecreasing order. When you set the RespCut parameter to '3D ', you can set the AzimuthAngles and ElevationAngles parameters simultaneously.

Default: [-180:180]

## ElevationAngles

Elevation angles for plotting element response, specified as a row vector. The ElevationAngles parameter sets the display range and resolution of elevation angles for visualizing the radiation pattern. This parameter is allowed only when the RespCut parameter is set to ' $E l$ ' or ' $3 D^{\prime}$ ' and the Format parameter is set to 'Line' or 'Polar'. The values of elevation angles should lie between $90^{\circ}$ and $90^{\circ}$ and must be in nondecreasing order. When you set the RespCut parameter to ' 3D ', you can set the ElevationAngles and AzimuthAngles parameters simultaneously.

Default: [-90:90]

## UGrid

$U$ coordinate values for plotting element response, specified as a row vector. The UGrid parameter sets the display range and resolution of the $U$ coordinates for visualizing the radiation pattern in $U / V$ space. This parameter is allowed only when the Format parameter is set to 'UV' and the RespCut parameter is set to ' $U$ ' or ' $3 D$ '. The values of $U G r i d$ should be between -1 and 1 and should be specified in nondecreasing order. You can set the UGrid and VGrid parameters simultaneously.

Default: [-1:0.01:1]

## VGrid

$V$ coordinate values for plotting element response, specified as a row vector. The VGrid parameter sets the display range and resolution of the $V$ coordinates for visualizing the radiation pattern in $U / V$ space. This parameter is allowed only when the Format parameter is set to ' UV' and the RespCut parameter is set to ' 3 D '. The values of VGrid should be between -1 and 1 and should be specified in nondecreasing order. You can set the VGrid and UGrid parameters simultaneously.

Default: [-1:0.01:1]

## Examples

## Response of Short-Dipole Antenna Oriented Along the Z-Axis

Specify a short-dipole antenna element with its dipole axis pointing along the $z$-axis. To do so, set the
'AxisDirection' value to 'Z'.

```
sSD = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[100 900]*le6,'AxisDirection','Z');
```

Plot the antenna's vertical polarization response at 200 MHz as a 3-D polar plot.

```
fc = 200e6;
plotResponse(sSD,fc,'Format','Polar',...
    'RespCut','3D','Polarization','V');
```



As the above figure shows, the antenna pattern is that of a vertically-oriented dipole and has its maximum at the equator and nulls at the poles.

## Plot Short-Dipole Antenna Element Response over Selected Range

This example shows how to construct a short-dipole antenna element with its dipole axis pointing along the z -axis and how to plot the response over a selected range of angles. The antenna operating frequency spans the range 100 to 900 MHz .

To construct a z-directed short-dipole antenna, set the 'AxisDirection' value to ' $Z$ '.

```
sSD = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[100 900]*1e6,'AxisDirection','Z');
```

Plot the antenna's vertical polarization response at 200 MHz as an elevation cut at a fixed azimuth angle. Use the 'ElevationAngles' property to restrict the plot from - 60 to 60 degrees elevation in 0.1 degree increments.

```
plotResponse(sSD,200e6,'Format','Polar',...
    'RespCut','El','Polarization','V',...
    'ElevationAngles',[-60:0.1:60],'Unit','mag');
```



Normalized Magnitude, Broadside at $0.00^{\circ}$

## Plot Short-Dipole Antenna Element Directivity

This example shows how to construct a short-dipole antenna element with its dipole axis pointing along the $y$-axis and how to plot the directivity. The antenna operating frequency spans the range 100 to 900 MHz .

To construct a y-directed short-dipole antenna, set the 'AxisDirection' value to ' Y '.

```
sSD = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[100 900]*1e6,'AxisDirection','Y');
```

Plot the antenna's directivity at 500 MHz as an elevation cut at a fixed azimuth angle.
plotResponse(sSD,500e6,'Format', 'Line', ..
'RespCut','El','Unit','dbi');


## See Also

uv2azel|azel2uv

## step

System object: phased.ShortDipoleAntennaElement<br>Package: phased<br>Output response of antenna element

## Syntax

RESP $=$ step (H,FREQ,ANG)

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step (obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.

RESP = step (H,FREQ,ANG) returns the antenna's voltage response, RESP, at the operating frequencies specified in FREQ and in the directions specified in ANG. For the short-dipole antenna element object, RESP is a MATLAB struct containing two fields, RESP.H and RESP.V, representing the horizontal and vertical polarization components of the antenna's response. Each field is an $M$-by- $L$ matrix containing the antenna response at the $M$ angles specified in ANG and at the $L$ frequencies specified in FREQ.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## H

Antenna element object.

## FREQ

Operating frequencies of antenna in hertz. FREQ is a row vector of length $L$.

## ANG

Directions in degrees. ANG can be either a 2-by-M matrix or a row vector of length M.
If ANG is a 2 -by-M matrix, each column of the matrix specifies the direction in the form [azimuth; elevation]. The azimuth angle must be between -180 and 180 degrees, inclusive. The elevation angle must be between -90 and 90 degrees, inclusive.

If ANG is a row vector of length $M$, each element specifies a direction's azimuth angle. In this case, the corresponding elevation angle is assumed to be 0 .

## Output Arguments

## RESP

Voltage response of antenna element returned as a MATLAB struct with fields RESP.H and RESP.V. Both RESP.H and RESP.V contain responses for the horizontal and vertical polarization components of the antenna radiation pattern. Both RESP. H and RESP.V are $M$-by- $L$ matrices. In these matrices, $M$ represents the number of angles specified in ANG, and $L$ represents the number of frequencies specified in FREQ.

## Examples

## Response of Short-Dipole Antenna

Find the response of a short-dipole antenna element at boresight, $\left(0^{\circ}, 0^{\circ}\right)$, and off boresight, $\left(30^{\circ}, 0^{\circ}\right)$. The antenna operates at 256 MHz .

```
antenna = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[100 900]*le6,'AxisDirection','Y');
ang = [0 30;0 0];
fc = 250e6;
resp = antenna(fc,ang)
resp = struct with fields:
    H: [2x1 double]
    V: [2x1 double]
```

Horizontal response.

```
disp(resp.H)
```

$-1.2247$
$-1.0607$
Vertical response.
disp(resp.v)
0
0

## Algorithms

The total response of a short-dipole antenna element is a combination of its frequency response and spatial response. This System object calculates both responses using nearest neighbor interpolation and then multiplies the responses to form the total response.

# phased.ScatteringMIMOChannel 

Package: phased<br>Scattering MIMO channel

## Description

The phased.ScatteringMIMOChannel System object models a multipath propagation channel in which radiated signals from a transmitting array are reflected from multiple scatterers back toward a receiving array. In this channel, propagation paths are line of sight from point to point. The object models range-dependent time delay, gain, Doppler shift, phase change, and atmospheric loss due to gases, rain, fog, and clouds.

The attenuation models for atmospheric gases and rain are valid for electromagnetic signals in the frequency range from 1 through 1000 GHz . The attenuation model for fog and clouds is valid from 10 through 1000 GHz . Outside of these frequency ranges, the object uses the nearest valid value.

To compute the multipath propagation for specified source and receiver points:
1 Define and set up your scattering MIMO channel using the "Construction" on page 1-1577 procedure. You can set the System object properties during construction or leave them at their default values.
2 Call the step method to compute the propagated signals using the properties of the phased.ScatteringMIMOChannel System object. You can change tunable properties before or after any call to the step method.

Note Instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, $\mathrm{y}=\mathrm{step}(\mathrm{obj}, \mathrm{x})$ and $\mathrm{y}=$ obj ( $x$ ) perform equivalent operations.

## Construction

channel = phased.ScatteringMIMOChannel creates a scattering MIMO propagation channel System object, channel.
channel = phased.ScatteringMIMOChannel (Name, Value) creates a System object, channel, with each specified property Name set to the specified Value. You can specify additional name and value pair arguments in any order as (Name1, Value1,...,NameN, ValueN).

## Properties

## TransmitArray - Transmitting array

phased.ULA (default)| Phased Array System Toolbox antenna array System object
Transmitting array, specified as a Phased Array System Toolbox antenna array System object. The default value for this property is a phased. ULA array with its default property values.
Example: phased.URA

## ReceiveArray - Receiving array

phased. ULA (default) | Phased Array System Toolbox antenna array System object
Receiving array, specified as a Phased Array System Toolbox antenna array System object. The default value for this property is a phased. ULA array with its default property values.

Example: phased.URA
PropagationSpeed - Signal propagation speed
physconst('LightSpeed') (default) | positive scalar
Signal propagation speed, specified as a positive scalar. Units are in meters per second. The default propagation speed is the value returned by physconst ('LightSpeed'). See physconst for more information.

Example: 3e8
Data Types: double
CarrierFrequency - Signal carrier frequency
300e6 (default) | positive real-valued scalar
Signal carrier frequency, specified as a positive real-valued scalar. Units are in Hz.
Example: 100e6
Data Types: double

## Polarization - Polarization configuration

'None' (default) | 'Combined ' | 'Dual'
Polarization configuration, specified as 'None', 'Combined', or 'Dual'. When you set this property to 'None', the output field is considered a scalar field. When you set this property to 'Combined ', the radiated fields are polarized and are interpreted as a single signal in the sensor's inherent polarization. When you set this property to 'Dual ' , the $H$ and $V$ polarization components of the radiated field are independent signals.
Example: 'Dual'
Data Types: char

## SpecifyAtmosphere - Enable atmospheric attenuation model

false (default)|true
Option to enable the atmospheric attenuation model, specified as a false or true. Set this property to true to add signal attenuation caused by atmospheric gases, rain, fog, or clouds. Set this property to false to ignore atmospheric effects in propagation.

Setting SpecifyAtmosphere to true, enables the Temperature, DryAirPressure, WaterVapourDensity, LiquidWaterDensity, and RainRate properties.
Data Types: logical

## Temperature - Ambient temperature

15 (default) | real-valued scalar
Ambient temperature, specified as a real-valued scalar. Units are in degrees Celsius.
Example: 20.0

## Dependencies

To enable this property, set SpecifyAtmosphere to true.

## Data Types: double

## DryAirPressure - Atmospheric dry air pressure

101.325 e 3 (default) | positive real-valued scalar

Atmospheric dry air pressure, specified as a positive real-valued scalar. Units are in pascals (Pa). The default value of this property corresponds to one standard atmosphere.
Example: 101.0e3

## Dependencies

To enable this property, set SpecifyAtmosphere to true.

## Data Types: double

## WaterVapourDensity - Atmospheric water vapor density

7.5 (default) | positive real-valued scalar

Atmospheric water vapor density, specified as a positive real-valued scalar. Units are in $\mathrm{g} / \mathrm{m}^{3}$.
Example: 7.4

## Dependencies

To enable this property, set SpecifyAtmosphere to true.
Data Types: double

## LiquidWaterDensity - Liquid water density

0.0 (default) | nonnegative real-valued scalar

Liquid water density of fog or clouds, specified as a nonnegative real-valued scalar. Units are in $\mathrm{g} / \mathrm{m}^{3}$. Typical values for liquid water density are 0.05 for medium fog and 0.5 for thick fog.
Example: 0.1

## Dependencies

To enable this property, set SpecifyAtmosphere to true.
Data Types: double

## RainRate - Rainfall rate

0.0 (default) | nonnegative scalar

Rainfall rate, specified as a nonnegative scalar. Units are in $\mathrm{mm} / \mathrm{hr}$.
Example: 10.0

## Dependencies

To enable this property, set SpecifyAtmosphere to true.
Data Types: double

## SampleRate - Sample rate of signal

1e6 (default) | positive scalar

Sample rate of signal, specified as a positive scalar. Units are in Hz. The System object uses this quantity to calculate the propagation delay in units of samples.

Example: 1e6
Data Types: double

## SimulateDirectPath - Enable propagation along direct path <br> false (default) | true

Option to enable signal propagation along the direct path, specified as false or true. The direct path is a line-of-sight path from the transmitting array to the receiving array with no scattering.

## Data Types: logical

## ChannelResponseOutputPort - Enable output of channel response <br> false (default) | true

Option to enable output of channel response, specified as false or true. Set this property to trueto output the channel response and time delay by using the chmatrix and tau output arguments of the step method.

## Data Types: logical

## MaximumDelaySource - Source of maximum delay

'Auto' (default)|'Property'
Source of the maximum delay value, specified as 'Auto' or 'Property '. When you set this property to 'Auto', the channel automatically allocates enough memory to simulate the propagation delay. When you set this property to 'Property', you can specify the maximum delay by using the MaximumDelay property. Signals arriving after the maximum delay are ignored.

## MaximumDelay - Maximum signal delay

10e-6 (default) | positive scalar
Maximum signal delay, specified as a positive scalar. Delays greater than this value are ignored. Units are in seconds.

## Dependencies

To enable this property, set the MaximumDelaySource property to 'Property'.
Data Types: double

## TransmitArrayMotionSource - Source of transmitting array motion parameters 'Property' (default)|'Input port'

Source of the transmitting array motion parameters, specified as 'Property' or 'Input port'.

- When you set this property to 'Property', the transmitting array is stationary. Then, you can specify the location and orientation of the array using the TransmitArrayPosition and TransmitArrayOrientationAxes properties.
- When you set this property to 'Input port', specify the transmitting array location, velocity, and orientation by using the txpos, txvel, and txaxes input arguments of the step method.

Data Types: char

TransmitArrayPosition - Position of transmitting array phase center
[0;0;0] (default) | real-valued three-element vector
Position of the transmitting array phase center, specified as a real-valued three-element vector in Cartesian form, $[x ; y ; z]$, with respect to the global coordinate system. Units are in meters.
Example: [1000;-200;55]

## Dependencies

To enable this property, set the TransmitArrayMotionSource property to 'Property'.
Data Types: double
TransmitArrayOrientationAxes - Orientation of transmitting array
eye $(3,3)$ (default) | real-valued 3-by-3 orthonormal matrix
Orientation of transmitting array, specified as a real-valued 3-by-3 orthonormal matrix. The matrix specifies the three axes, $(x, y, z)$, that define the local coordinate system of the array with respect to the global coordinate system. Matrix columns correspond to the axes of the local array coordinate system.
Example: rotz (45)

## Dependencies

To enable this property, set the TransmitArrayMotionSource property to 'Property'.
Data Types: double

## ReceiveArrayMotionSource - Source of receiving array motion parameters 'Property' (default)|'Input port'

Source of the receiving array motion parameters, specified as 'Property' or 'Input port'.

- When you set this property to 'Property ', the receiving array is stationary. Then, you can specify the location and orientation of the array by using the ReceiveArrayPosition and ReceiveArrayOrientationAxes properties.
- When you set this property to 'Input port', you can specify the receiving array location, velocity, and orientation by using the rxpos, rxvel, and rxaxes input arguments of the step method.


## Data Types: char

## ReceiveArrayPosition - Position of receiving array

[0;0;0] (default) | real-valued three-element vector
Position of the receiving array phase center, specified as a real-valued three-element vector in Cartesian form, $[x ; y ; z]$, with respect to the global coordinate system. Units are in meters.
Example: [1000;-200;55]

## Dependencies

To enable this property, set the ReceiveArrayMotionSource property to 'Property'.
Data Types: double

## ReceiveArrayOrientationAxes - Orientation of receiving array

eye (3,3) (default) | real-valued 3-by-3 orthonormal matrix
Orientation of receiving array, specified as a real-valued 3-by-3 orthonormal matrix. The matrix specifies the three axes, $(x, y, z)$, that define the local coordinate system of the array with respect to the global coordinate system. Matrix columns correspond to the axes of the local array coordinate system.

## Example: roty (60)

## Dependencies

To enable this property, set the ReceiveArrayMotionSource property to 'Property '.

## Data Types: double

## ScattererSpecificationSource - Source of scatterer parameters

'Auto' (default)|'Property'|'Input port'
Source of scatterer parameters, specified as 'Auto','Property','Input port'.

- When you set this property to 'Auto', all scatterer positions and coefficients are randomly generated. Scatterer velocities are zero. The generated positions are contained within the region defined by the ScattererPositionBoundary. To set the number of scatterers, use the NumScatterers property.
- When you set this property to 'Property ', you can set the scatterer positions by using the ScattererPosition property and the scattering coefficients by using the ScattererCoefficient property. All scatterer velocities are zero.
- When you set this property to 'Input port ', you can specify the scatterer positions, velocities, and scattering coefficients using the scatpos, scatvel, and scatcoef input arguments of the step method.

Example: 'Input port'
Data Types: char

## NumScatterers - Number of scatterers

1 (default) | nonnegative integer
Number of scatterers, specified as a nonnegative integer.

## Example: 9

## Dependencies

To enable this property, set the ScattererSpecificationSource property to 'Auto'.

## Data Types: double

## ScattererPositionBoundary - Boundary of scatterer positions

[0, 1000] (default) | 1-by-2 real-valued vector | 3-by-2 real-valued matrix
Boundary of the scatterer positions, specified as a 1-by-2 real-valued row vector or a 3-by-2 realvalued matrix. The vector specifies the minimum and maximum, [minbdry maxbdry], for all three dimensions. The matrix specifies boundaries in all three dimensions in the form [x_minbdry x_maxbdry;y_minbdry y_maxbdry; z_minbdry z_maxbdry].
Example: [-1000 500;-100 100;-200 0]

## Dependencies

To enable this property, set the ScattererSpecificationSource property to 'Auto'.

## Data Types: double

## ScattererPosition - Positions of scatterers

## [0;0;0] (default)| real-valued 3-by-K matrix

Positions of the scatterers, specified as real-valued 3-by-K matrix. $K$ is the number of scatterers. Each column represents a different scatterer and has the Cartesian form [x;y;z] with respect to the global coordinate system. Units are in meters.
Example: [1050-100;-300 55;0 -75]

## Dependencies

To enable this property, set the ScattererSpecificationSource property to 'Property'.
Data Types: double

## ScattererCoefficient - Scattering coefficients

1 (default) | complex-valued 1-by-K vector
Scattering coefficients, specified as a complex-valued 1-by- $K$ vector. $K$ is the number of scatterers. Units are dimensionless.

Example: 2+1i

## Dependencies

To enable this property, set the ScattererSpecificationSource property to 'Property'.
Data Types: double

## ScatteringMatrix - Scattering matrices

[1 0;0 1] |complex-valued 2-by-2-by- $N_{s}$ array
Scattering matrices of the scatterers, specified as a complex-valued 2-by-2-by- $N_{\mathrm{s}}$ array where $N_{\mathrm{s}}$ is the number of scatterers. Each page of this array represents the scattering matrix of a scatterer. Each scattering matrix has the form [s_hh s_hv;s_vh s_vv]. For example, the component s_hv specifies the complex scattering response when the input signal is vertically polarized and the reflected signal is horizontally polarized. The other components are defined similarly. Units are in square meters.

## Dependencies

To enable this property, set the ScatteringMatrixSource property to 'Property ' and the Polarization property to 'Combined ' or 'Dual'.
Data Types: double

## ScattererOrientationAxes - Orientation of scatterers

[1 0 0;0 1 0;0 0 1] (default) |real-valued 3-by-3-by- $N_{\mathrm{s}}$ array
Orientation of the scatterers, specified as a real-valued 3-by-3-by- $N_{\mathrm{s}}$ array where $N_{\mathrm{s}}$ is the number of scatterers. Each page of this array is an orthonormal matrix. Matrix columns represent the axis of the local coordinates $(x, y, z)$ of the scatterer with respect to the global coordinate system.
Example: roty (45)

## Dependencies

To enable this property, set the ScatteringMatrixSource property to 'Property' and the Polarization property to 'Combined' or 'Dual'.

## Data Types: double

## SeedSource - Source of random number generator seed

## 'Auto' (default)| 'Property'

Source of random number generator seed, specified as 'Auto' or 'Property'.

- When you set this property to 'Auto', random numbers are generated using the default MATLAB random number generator.
- When you set this property to 'Property', the object uses a private random number generator with the seed specified by the value of the Seed property.

To use this object with Parallel Computing Toolbox software, set this property to 'Auto '.

## Dependencies

To enable this property, set the ScattererSpecificationSource property to 'Auto'.

## Seed - Random number generator seed

0 (default) | nonnegative integer
Random number generator seed, specified as a nonnegative integer less than $2^{32}$.
Example: 5005

## Dependencies

To enable this property, set the ScattererSpecificationSource property to 'Auto' and the SeedSource property to 'Property'.
Data Types: double

## Methods

reset Reset state of the System object
step Propagate signals in scattering MIMO channel

## Common to All System Objects

release Allow System object property value changes

## Examples

## Propagate Signals in MIMO Channel

Create a 30 GHz MIMO channel with random scatterers. The scenario contains a stationary 21element transmitting ULA array and a stationary 15 -element receiving ULA array. The transmitting antennas have cosine responses and the receiving antennas are isotropic. Element spacing for both arrays is less than one-half wavelength. The channel has 50 randomly generated static scatterers
within a specified bounding box. The transmit array is located at [ $0 ; 20 ; 50$ ] meters and the receive array is located at $[200 ; 10 ; 10]$ meters. Compute the propagated signal through this channel. The sample rate for the signal is 10 MHz .

```
fc = 30e9;
c = physconst('LightSpeed');
lambda = c/fc;
fs = 10e6;
txarray = phased.ULA('Element',phased.CosineAntennaElement,...
    'NumElements',21,'ElementSpacing',0.45*lambda);
rxarray = phased.ULA('Element',phased.IsotropicAntennaElement,...
    'NumElements',15,'ElementSpacing',0.45*lambda);
channel = phased.ScatteringMIMOChannel('TransmitArray',txarray,...
    'ReceiveArray',rxarray,'PropagationSpeed',c,'CarrierFrequency',fc,...
    'SampleRate',fs,'TransmitArrayPosition',[0;20;50],...
    'ReceiveArrayPosition',[200;10;10],'NumScatterers',50,...
    'ScattererPositionBoundary',[10 180; -30 30; -30 30]);
```

Create a random data signal of ones and zeros for each transmitter.

```
x = randi(2,[100 21]) - 1;
```

Compute the received signals after propagating through the channel.
$y=$ channel( $x$ );

## Propagate Signals in MIMO Channel from Moving Transmitter

Create a MIMO channel containing 3 fixed scatterers. The scenario contains a 21 -element transmitting ULA array operating at 72 GHz , and a 15 -element receiving ULA array. The transmitting elements have cosine response shapes and the receiving antennas are isotropic. Only the transmitting antenna is moving. Element spacing for both arrays is less than one-half wavelength. The transmitting array starts at $(0,20,50)$ meters and moves towards the receiver at $2 \mathrm{~m} / \mathrm{s}$. The receiving array is located at $(200,10,10)$ meters. Compute the propagated signal through this channel. The sample rate for the signal is 10 MHz .

```
fc = 72e9;
c = physconst('LightSpeed');
lambda = c/fc;
fs = 10e6;
txplatform = phased.Platform('MotionModel','Velocity','InitialPosition', ...
    [0;20;50],'Velocity',[2;0;0]);
txarray = phased.ULA('Element',phased.CosineAntennaElement, ...
    'NumElements',21,'ElementSpacing',0.45*lambda);
rxarray = phased.ULA('Element',phased.IsotropicAntennaElement, ...
    'NumElements',15,'ElementSpacing',0.45*lambda);
channel = phased.ScatteringMIMOChannel('TransmitArray',txarray, ...
    'ReceiveArray',rxarray,'PropagationSpeed',c,'CarrierFrequency',fc,...
    'SampleRate',fs,'TransmitArrayMotionSource','Input port', ...
    'ReceiveArrayMotionSource','Property','ReceiveArrayPosition',[200;10;10],...
    'ReceiveArray0rientationAxes',rotz(180),...
    'ScattererSpecificationSource','Property','ScattererPosition', ...
    [75 100 120; -10 20 12; 5 -5 8],'ScattererCoefficient',[1i,2+3i,-1+1i]);
```

Move the platforms for two time steps at one second intervals. For each time instance:

- Create a random data signal of ones and zeros for each transmitter element.
- Move the transmitter and receiver. The orientations are fixed.
- Propagate the signals from transmitters to scatterers to receiver.

```
for k =1:2
    x = randi(2,[100 21]) - 1;
    [txpos,txvel] = txplatform(1);
    txaxes = eye(3);
    y = channel(x,txpos,txvel,txaxes);
end
```


## Propagate Signals Through MIMO Channel to Moving Receiver

Create a MIMO channel containing 3 fixed scatterers. The scenario contains a 21 -element transmitting ULA array and a 15 -element receiving ULA array. Both arrays operate at 72 GHz . The transmitting elements have cosine response shapes and the receiving antennas are isotropic. Only the receiving antenna is moving. Element spacing for both arrays is less than one-half wavelength. The transmitting array is located at $(0,20,50)$ meters. The receiving array starts at $(200,10,10)$ meters and moves toward the transmitter at $2 \mathrm{~m} / \mathrm{s}$. Compute the propagated signal through this channel. The sample rate for the signal is 10 MHz .

```
fc = 72e9;
c = physconst('LightSpeed');
lambda = c/fc;
fs = 10e6;
rxplatform = phased.Platform('MotionModel','Velocity','InitialPosition',...
    [200;10;10],'Velocity',[-2;0;0]);
txarray = phased.ULA('Element',phased.CosineAntennaElement, ...
    'NumElements',21,'ElementSpacing',0.45*lambda);
rxarray = phased.ULA('Element',phased.IsotropicAntennaElement, ...
    'NumElements',15,'ElementSpacing',0.45*lambda);
channel = phased.ScatteringMIMOChannel('TransmitArray',txarray, ...
    'ReceiveArray',rxarray,'PropagationSpeed',c,'CarrierFrequency',fc, ...
    'SampleRate',fs,'TransmitArrayMotionSource','Property',...
    'TransmitArrayPosition', [0;20;50],'TransmitArray0rientationAxes',eye(3,3), ...
    'ReceiveArrayMotionSource','Input port','ScattererSpecificationSource', ...
    'Property','ScattererPosition',[75 100 120; -10 20 12; 5 -5 8], ...
    'ScattererCoefficient',[1i,2+3i,-1+1i],'SpecifyAtmosphere',false);
```

Move the platforms for two time steps at one-second intervals. For each time instance:

- Create a random data signal of ones and zeros for each transmitter element.
- Move the transmitter and receiver. Fix the array orientations.
- Propagate the signals from transmitters to scatterers to receiver.

```
for k =1:2
    x = randi(2,[100 21]) - 1;
    [rxpos,rxvel] = rxplatform(1);
    rxaxes = rotz(45);
    y = channel(x,rxpos,rxvel,rxaxes);
end
```


## Propagate Polarized Signals in MIMO Channel

Create a MIMO channel at 30 GHz with a 16 -element transmit array and a 64 -element receive array. Assume the elements are short-dipole antennas and the arrays are uniform linear arrays. The transmit array is located at $[0 ; 0 ; 50]$ meters.

The receive array has an initial position at [200;0;0] meters and is moving at a speed of $[10 ; 0 ; 0$ ] meters/second. There are 200 static scatterers randomly located on the $x y$ plane within a square centered at $[200 ; 0 ; 0]$ and with a side length of 100 meters.

Use the channel to compute the propagated polarized signal. Assume the sample rate for the signal is 10 MHz and the frame length is 1000 samples. Collect 5 frames of received signal.

```
fc = 30e9;
c = 3e8;
lambda = c/fc;
fs = 10e6;
txarray = phased.ULA('Element',phased.ShortDipoleAntennaElement,...
    'NumElements',16,'ElementSpacing',lambda/2);
rxarray = phased.ULA('Element',phased.ShortDipoleAntennaElement,...
    'NumElements',64,'ElementSpacing',lambda/2);
Ns = 200;
scatpos = [100*rand(1,Ns) + 150; 100*rand(1,Ns) + 150; zeros(1,Ns)];
temp = randn(1,Ns) + 1i*randn(1,Ns);
scatcoef = repmat(eye(2),1,1,Ns).*permute(temp,[1 3 2]);
scatax = repmat(eye(3),1,1,Ns);
Nframesamp = 1000;
Tframe = Nframesamp/fs;
rxmobile = phased.Platform('InitialPosition',[200;0;0],...
    'Velocity',[10;0;0],'OrientationAxesOutputPort',true);
chan = phased.ScatteringMIMOChannel(...
    'TransmitArray',txarray,...
    'ReceiveArray',rxarray,...
    'PropagationSpeed',c,...
    'CarrierFrequency',fc,...
    'SampleRate',fs,...
    'Polarization','Dual',...
    'TransmitArrayPosition',[0;0;50],...
    'ReceiveArrayMotionSource','Input port',...
    'ScattererSpecificationSource','Property',...
    'ScattererPosition',scatpos,...
    'ScatteringMatrix',scatcoef,...
    'ScattererOrientationAxes',scatax);
xh = randi(2,[Nframesamp 16])-1;
xv = randi(2,[Nframesamp 16])-1;
for m = 1:5
    [rxpos,rxvel,rxax] = rxmobile(Tframe);
    [yh,yv] = chan(xh,xv,rxpos,rxvel,rxax);
end
```


## More About

## Attenuation and Loss Factors

Attenuation or path loss in the scattering MIMO channel consists of four components. $L=L_{f s p} L_{g} L_{c} L_{r}$, where:

- $L_{f s p}$ is the free-space path attenuation.
- $L_{g}$ is the atmospheric path attenuation.
- $L_{c}$ is the fog and cloud path attenuation.
- $L_{r}$ is the rain path attenuation.

Each component is in magnitude units, not in dB.

## Free-Space Time Delay and Loss

When the origin and destination are stationary relative to each other, you can write the output signal of a free-space channel as $Y(t)=x(t-\tau) / L_{f s p}$. The quantity $\tau$ is the signal delay and $L_{f s p}$ is the free-space path loss. The delay $\tau$ is given by $R / c$, where $R$ is the propagation distance and $c$ is the propagation speed. The free-space path loss is given by

$$
L_{f s p}=\frac{(4 \pi R)^{2}}{\lambda^{2}},
$$

where $\lambda$ is the signal wavelength.
This formula assumes that the target is in the far field of the transmitting element or array. In the near field, the free-space path loss formula is not valid and can result in a loss smaller than one, equivalent to a signal gain. Therefore, the loss is set to unity for range values, $R \leq \lambda / 4 \pi$.

When the origin and destination have relative motion, the processing also introduces a Doppler frequency shift. The frequency shift is $v / \lambda$ for one-way propagation and $2 v / \lambda$ for two-way propagation. The quantity $v$ is the relative speed of the destination with respect to the origin.

For more details on free space channel propagation, see [8]

## Atmospheric Gas Attenuation Model

This model calculates the attenuation of signals that propagate through atmospheric gases.
Electromagnetic signals attenuate when they propagate through the atmosphere. This effect is due primarily to the absorption resonance lines of oxygen and water vapor, with smaller contributions coming from nitrogen gas. The model also includes a continuous absorption spectrum below 10 GHz . The ITU model Recommendation ITU-R P.676-10: Attenuation by atmospheric gases is used. The model computes the specific attenuation (attenuation per kilometer) as a function of temperature, pressure, water vapor density, and signal frequency. The atmospheric gas model is valid for frequencies from 1-1000 GHz and applies to polarized and nonpolarized fields.

The formula for specific attenuation at each frequency is

$$
\gamma=\gamma_{o}(f)+\gamma_{w}(f)=0.1820 f N^{\prime \prime}(f) .
$$

The quantity $N^{\prime \prime}()$ is the imaginary part of the complex atmospheric refractivity and consists of a spectral line component and a continuous component:

$$
N^{\prime \prime}(f)=\sum_{i} S_{i} F_{i}+N^{\prime \prime}{ }_{D}(f)
$$

The spectral component consists of a sum of discrete spectrum terms composed of a localized frequency bandwidth function, $F(f)_{i}$, multiplied by a spectral line strength, $S_{i}$. For atmospheric oxygen, each spectral line strength is

$$
S_{i}=a_{1} \times 10^{-7}\left(\frac{300}{T}\right)^{3} \exp \left[a_{2}\left(1-\left(\frac{300}{T}\right)\right] P .\right.
$$

For atmospheric water vapor, each spectral line strength is

$$
S_{i}=b_{1} \times 10^{-1}\left(\frac{300}{T}\right)^{3.5} \exp \left[b_{2}\left(1-\left(\frac{300}{T}\right)\right] W .\right.
$$

$P$ is the dry air pressure, $W$ is the water vapor partial pressure, and $T$ is the ambient temperature. Pressure units are in hectoPascals ( hPa ) and temperature is in degrees Kelvin. The water vapor partial pressure, $W$, is related to the water vapor density, $\rho$, by

$$
W=\frac{\rho T}{216.7} .
$$

The total atmospheric pressure is $P+W$.
For each oxygen line, $S_{i}$ depends on two parameters, $a_{1}$ and $a_{2}$. Similarly, each water vapor line depends on two parameters, $b_{1}$ and $b_{2}$. The ITU documentation cited at the end of this section contains tabulations of these parameters as functions of frequency.

The localized frequency bandwidth functions $F_{i}(f)$ are complicated functions of frequency described in the ITU references cited below. The functions depend on empirical model parameters that are also tabulated in the reference.

To compute the total attenuation for narrowband signals along a path, the function multiplies the specific attenuation by the path length, $R$. Then, the total attenuation is $L_{g}=R\left(\gamma_{o}+\gamma_{w}\right)$.

You can apply the attenuation model to wideband signals. First, divide the wideband signal into frequency subbands, and apply attenuation to each subband. Then, sum all attenuated subband signals into the total attenuated signal.

For a complete description of this model, see [4].

## Fog and Cloud Attenuation Model

This model calculates the attenuation of signals that propagate through fog or clouds.
Fog and cloud attenuation are the same atmospheric phenomenon. The ITU model, Recommendation ITU-R P.840-6: Attenuation due to clouds and fog is used. The model computes the specific attenuation (attenuation per kilometer), of a signal as a function of liquid water density, signal frequency, and temperature. The model applies to polarized and nonpolarized fields. The formula for specific attenuation at each frequency is

$$
\gamma_{C}=K_{l}(f) M,
$$

where $M$ is the liquid water density in $\mathrm{gm} / \mathrm{m}^{3}$. The quantity $K_{l}(f)$ is the specific attenuation coefficient and depends on frequency. The cloud and fog attenuation model is valid for frequencies $10-1000 \mathrm{GHz}$. Units for the specific attenuation coefficient are $(\mathrm{dB} / \mathrm{km}) /\left(\mathrm{g} / \mathrm{m}^{3}\right)$.

To compute the total attenuation for narrowband signals along a path, the function multiplies the specific attenuation by the path length $R$. Total attenuation is $L_{c}=R \gamma_{c}$.

You can apply the attenuation model to wideband signals. First, divide the wideband signal into frequency subbands, and apply narrowband attenuation to each subband. Then, sum all attenuated subband signals into the total attenuated signal.

For a complete description of this model, see [5]

## Rainfall Attenuation Model

This model calculates the attenuation of signals that propagate through regions of rainfall. Rain attenuation is a dominant fading mechanism and can vary from location-to-location and from year-toyear.

Electromagnetic signals are attenuated when propagating through a region of rainfall. Rainfall attenuation is computed according to the ITU rainfall model Recommendation ITU-R P.838-3: Specific attenuation model for rain for use in prediction methods. The model computes the specific attenuation (attenuation per kilometer) of a signal as a function of rainfall rate, signal frequency, polarization, and path elevation angle. The specific attenuation, $\gamma_{\mathrm{R}}$, is modeled as a power law with respect to rain rate

$$
\gamma_{R}=k R^{\alpha},
$$

where $R$ is rain rate. Units are in $\mathrm{mm} / \mathrm{hr}$. The parameter $k$ and exponent $\alpha$ depend on the frequency, the polarization state, and the elevation angle of the signal path. The specific attenuation model is valid for frequencies from 1-1000 GHz.

To compute the total attenuation for narrowband signals along a path, the function multiplies the specific attenuation by the an effective propagation distance, $d_{\text {eff }}$. Then, the total attenuation is $L=$ $d_{\text {eff }} \gamma_{R}$.

The effective distance is the geometric distance, $d$, multiplied by a scale factor

$$
r=\frac{1}{0.477 d^{0.633} R_{0.01}^{0.073 \alpha} f^{0.123}-10.579(1-\exp (-0.024 d))}
$$

where $f$ is the frequency. The article Recommendation ITU-R P.530-17 (12/2017): Propagation data and prediction methods required for the design of terrestrial line-of-sight systems presents a complete discussion for computing attenuation.

The rain rate, $R$, used in these computations is the long-term statistical rain rate, $R_{0.01}$. This is the rain rate that is exceeded $0.01 \%$ of the time. The calculation of the statistical rain rate is discussed in Recommendation ITU-R P.837-7 (06/2017): Characteristics of precipitation for propagation modelling. This article also explains how to compute the attenuation for other percentages from the $0.01 \%$ value.

You can apply the attenuation model to wideband signals. First, divide the wideband signal into frequency subbands and apply attenuation to each subband. Then, sum all attenuated subband signals into the total attenuated signal.

## Version History

## Introduced in R2017a

## References

[1] Heath, R. Jr. et al. "An Overview of Signal Processing Techniques for Millimeter Wave MIMO Systems", arXiv.org:1512.03007 [cs.IT], 2015.
[2] Tse, D. and P. Viswanath, Fundamentals of Wireless Communications, Cambridge: Cambridge University Press, 2005.
[3] Paulraj, A. Introduction to Space-Time Wireless Communications, Cambridge: Cambridge University Press, 2003.
[4] Radiocommunication Sector of the International Telecommunication Union. Recommendation ITUR P.676-10: Attenuation by atmospheric gases. 2013.
[5] Radiocommunication Sector of the International Telecommunication Union. Recommendation ITUR P.840-6: Attenuation due to clouds and fog. 2013.
[6] Radiocommunication Sector of the International Telecommunication Union. Recommendation ITUR P.838-3: Specific attenuation model for rain for use in prediction methods. 2005.
[7] Seybold, J. Introduction to RF Propagation. New York: Wiley \& Sons, 2005.
[8] Skolnik, M. Introduction to Radar Systems, 3rd Ed. New York: McGraw-Hill, 2001.

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.
Usage notes and limitations:

- See "System Objects in MATLAB Code Generation" (MATLAB Coder).


## See Also

## Functions

rangeangle|fogpl|gaspl|rainpl|fspl|diagbfweights|scatteringchanmtx|
waterfill

## Objects

phased.FreeSpace|phased.RadarTarget|phased.BackscatterRadarTarget | twoRayChannel | phased.LOSChannel

## reset

System object: phased.ScatteringMIMOChannel
Package: phased
Reset state of the System object

## Syntax

reset (channel)

## Description

reset (channel) resets the internal state of the phased.ScatteringMIMOChannel System object, channel.

## Input Arguments

## channel - Spatial MIMO channel

phased.ScatteringMIMOChannel System object
Scattering MIMO channel, specified as a phased.ScatteringMIMOChannel System object.

## Version History

Introduced in R2017a

## step

System object: phased. ScatteringMIMOChannel
Package: phased
Propagate signals in scattering MIMO channel

## Syntax

```
Y = step(channel,X)
[YH,YV] = step(channel,[XH,XV])
[___] = step(
,txpos,txvel,txaxes)
[___] = step(
,rxpos,rxvel,rxaxes)
[__] ] = step(__,scatpos,scatvel,scatcoef)
[__] = step(__,scatpos,scatvel,scatmat,scataxes)
[ _ ,CR,TAU] = step(channel, )
[__,CR_HH,CR_HV,CR_VH,CR_V,TAU] = step(channel,
```

$\qquad$

``` )
\([\bar{Y}, C R, T A U]=\) step(channel, \(\bar{X}\), txpos,txvel,txaxes rxpos,rxvel,rxaxes,scatpos, scatvel,scatcoef)
```


## Description

Note Instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, $\mathrm{Y}=\operatorname{step}(\mathrm{obj}, \mathrm{X})$ and $\mathrm{Y}=$ obj $(X)$ perform equivalent operations.
$Y=$ step (channel, $X$ ) uses the scattering MIMO channel, channel, to propagate a signal, $X$, from a transmitting array towards multiple scatterers, and returns the scattered signals, $Y$, to a receiving array.

To enable this syntax, set the TransmitArrayMotionSource, ReceiveArrayMotionSource, and ScattererSpecificationSource properties to 'Property'.
[ $\mathrm{YH}, \mathrm{YV}$ ] = step(channel, $[\mathrm{XH}, \mathrm{XV}]$ ) propagates the polarized signals, XH and XV , through the $H$ port and $V$-port of the transmit array. The object returns the received signals, YH and YV to the $H$-port and $V$-port of the receive array.

To enable this syntax, set the Polarization property to 'Dual ' .
[___] = step(__ ,txpos,txvel,txaxes) also specifies the transmitting array position, velocity, and axes orientation.

To enable this syntax, set the ReceiveArrayMotionSource and ScattererSpecificationSource properties to 'Property' and set TransmitArrayMotionSource to 'Input port'.
[___] = step ( $\qquad$ , rxpos, rxvel, rxaxes) specifies the receiving array position, velocity, and axes orientation.

To enable this syntax, set the TransmitArrayMotionSource and ScattererSpecificationSource properties to 'Property' and set ReceiveArrayMotionSource to 'Input port'.
[___ ] = step( ___ , scatpos,scatvel, scatcoef) specifies the scatterer positions and velocities, and the scattering coefficients.

To enable this syntax, set the TransmitArrayMotionSource and ReceiveArrayMotionSource properties to 'Property', set ScattererSpecificationSource to 'Input port', and set the Polarization property to 'None'.
[ ___ ] = step( __ ,scatpos,scatvel, scatmat,scataxes) specifies the scatterer positions, scatpos, and velocities, scatvel, the scattering matrix, scatmat, and the scatterer orientation axes, scataxes.

To enable this syntax, set the TransmitArrayMotionSource and ReceiveArrayMotionSource properties to 'Property', set ScattererSpecificationSource to 'Input port', and set the Polarization property to 'Combined' or 'Dual'.
[ ___ CR, TAU] = step (channel, ___ ) also returns the channel response matrix, CR, and the channel path delays, TAU, using any of the previous input argument combinations.

To enable this syntax, set the ChannelResponseOutputPort property to true and set the Polarization property to 'None' or 'Combined'.
[ __ , CR_HH,CR_HV,CR_VH,CR_V,TAU] = step (channel, ___) also returns the channel response matrices, CR_HH, CR_HV, CR_VH, and CR_V, using any of the previous input argument combinations.

To enable this syntax, set the ChannelResponseOutputPort property to true and set the Polarization property to 'Dual'.

You can combine optional input arguments when their enabling properties are set. For example, [ Y , CR,TAU] = step(channel, $\mathrm{X}, \mathrm{t} \times \mathrm{pos}, \mathrm{txvel}, \mathrm{txaxes}$ rxpos,rxvel,rxaxes,scatpos, scatvel, scatcoef).

Note The object performs an initialization the first time the step method is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## channel - Scattering MIMO channel

phased. ScatteringMIMOChannel System object
Scattering MIMO channel, specified as a phased.ScatteringMIMOChannel System object.
Example: phased.ScatteringMIMOChannel
X - Transmitted narrowband signal
$M$-by- $N_{t}$ complex-valued matrix

Transmitted narrowband signal, specified as an $M$-by- $N_{t}$ complex-valued matrix. The quantity $M$ is the number of samples in the signal, and $N_{t}$ is the number of transmitting array elements. Each column represents the signal transmitted by the corresponding array element.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

Example: [1,1;j,1;0.5,0]

## Dependencies

To enable this argument, set the Polarization property to 'None' or 'Combined'.
Data Types: double
Complex Number Support: Yes

## XH - Transmitted narrowband H-polarization signal

$M$-by- $N_{t}$ complex-valued matrix
Transmitted narrowband $H$-polarization signal, specified as an $M$-by- $N_{t}$ complex-valued matrix. The quantity $M$ is the number of samples in the signal, and $N_{t}$ is the number of transmitting array elements. Each column represents the signal transmitted by the corresponding array element.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
Example: [1,1;j,1;0.5,0]

## Dependencies

To enable this argument, set the Polarization property to 'Dual '.

## Data Types: double

Complex Number Support: Yes

## XV - Transmitted narrowband V-polarization signal

$M$-by- $N_{t}$ complex-valued matrix
Transmitted narrowband $V$-polarization signal, specified as an $M$-by- $N_{t}$ complex-valued matrix. The quantity $M$ is the number of samples in the signal, and $N_{t}$ is the number of transmitting array elements. Each column represents the signal transmitted by the corresponding array element.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

```
Example: [1,1;j,1;0.5,0]
```


## Dependencies

To enable this argument, set the Polarization property to 'Dual ' .

```
Data Types: double
Complex Number Support: Yes
```


## txpos - Position of transmitting antenna array <br> real-valued three-element column vector

Position of transmitting antenna array, specified as real-valued three-element column vector taking the form $[x ; y ; z]$. The vector elements correspond to the $x, y$, and $z$ positions of the array. Units are in meters.

Example: [1000;100;500]

## Dependencies

To enable this argument, set the TransmitArrayMotionSource property to 'Input port'.

## Data Types: double

## txvel - Velocity of transmitting antenna array

real-valued three-element column vector
Velocity of transmitting antenna array, specified as a real-valued three-element column vector taking the form [ $\mathrm{vx} ; \mathrm{vy} ; \mathrm{vz}$ ]. The vector elements correspond to the $x, y$, and $z$ velocities of the array. Units are in meters per second.
Example: [10;0;5]

## Dependencies

To enable this argument, set the TransmitArrayMotionSource property to 'Input port'.
Data Types: double

## txaxes - Axes orientation of transmitting antenna array

real-valued 3-by-3 real orthonormal matrix
Axes orientation of transmitting antenna array, specified as a real-valued 3-by-3 real orthonormal matrix. The matrix defines the orientation of the array local coordinate system with respect to the global coordinates. Matrix columns correspond to the directions of the $x, y$, and $z$ axes of the local coordinate system. Units are dimensionless.

## Example: rotx (35)

## Dependencies

To enable this argument, set the TransmitArrayMotionSource property to 'Input port'.
Data Types: double

## rxpos - Position of receiving antenna array

real-valued three-element column vector
Position of receiving antenna array, specified as a real-valued three-element column vector taking the form $[x ; y ; z$ ]. The vector elements correspond to the $x, y$, and $z$ positions of the array. Units are in meters.

Example: [1000;100;500]

## Dependencies

To enable this argument, set the ReceiveArrayMotionSource property to 'Input port'.

## Data Types: double

## rxvel - Velocity of receiving antenna array

real-valued three-element column vector

Velocity of receiving antenna array, specified as a real-valued three-element column vector taking the form [vx;vy;vz]. The vector elements correspond to the $x, y$, and $z$ velocities of the array. Units are in meters per second.
Example: [10;0;5]

## Dependencies

To enable this argument, set the ReceiveArrayMotionSource property to 'Input port'.

## Data Types: double

rxaxes - Axes orientation of receiving antenna array
real-valued 3-by-3 real orthonormal matrix
Axes orientation of receiving antenna array, specified as a real-valued 3-by-3 real orthonormal matrix. The matrix defines the orientation of the array local coordinate system with respect to the global coordinates. Matrix columns correspond to the directions of the $x, y$, and $z$ axes of the local coordinate system. Units are dimensionless.
Example: rotx (35)

## Dependencies

To enable this argument, set the ReceiveArrayMotionSource property to 'Input port'.
Data Types: double
scatpos - Positions of scatterers
real-valued 3 -by- $N_{s}$ matrix
Positions of scatterers, specified as a real-valued 3 -by- $N_{s}$ matrix. The matrix contains the ( $x, y, z$ ) positions of scatterers. Each column of the matrix specifies a different scatterer and takes the form [ $x ; y ; z]$. Units are in meters.
Example: [1000;100;500]

## Dependencies

To enable this argument, set the ScattererSpecificationSource property to 'Input port '.

## Data Types: double

## scatvel - Velocities of scatterers

real-valued 3 -by- $N_{s}$ matrix
Velocities of scatterers, specified as a real-valued 3 -by- $N_{s}$ matrix. The matrix contains the ( $v_{x}, v_{y}, v_{z}$ ) positions of scatterers. Each column of the matrix specifies a different scatterer and takes the form [vx;vy;vz] Units are in meters per second.
Example: [1000;100;500]

## Dependencies

To enable this argument, set the ScattererSpecificationSource property to 'Input port '.

## Data Types: double

Scattering coefficients, specified as a complex-valued 1-by- $N_{s}$ row vector. Each vector element specifies the scattering coefficient of the corresponding scatterer. Units are dimensionless.
Example: [5+3*1i;4+1i;2]

## Dependencies

To enable this argument, set the ScattererSpecificationSource property to 'Input port' and the Polarization property to 'None'.
Data Types: double

## scatmat - Scattering matrices

[1 0;0 1] |complex-valued 2-by-2-by- $N_{\mathrm{s}}$ array
Scattering matrices of the scatterers, specified as a complex-valued 2-by-2-by- $N_{\mathrm{s}}$ array where $N_{\mathrm{s}}$ is the number of scatterers. Each page of this array represents the scattering matrix of a scatterer. Each scattering matrix has the form [s_hh s_hv;s_vh s_vv]. For example, the component s_hv specifies the complex scattering response when the input signal is vertically polarized and the reflected signal is horizontally polarized. The other components are defined similarly. Units are in square meters.

## Dependencies

To enable this property, set the ScattererSpecificationSource property to 'Input port' and the Polarization property to 'Combined' or 'Dual'.
Data Types: double

## scataxes - Scatterer orientation axes

real-valued 3-by-3-by- $N_{\text {s }}$ array
Scatterer orientation axes, specified as a real-valued 3-by-3-by- $N_{\mathrm{s}}$ array where $N_{\mathrm{s}}$ is the number of scatterers. Each page of this array represents the orientation axes matrix of a scatterer. The columns of the matrix represent the $x-y$-, and $z$-axes of the scatterer. Units are dimensionless.

## Dependencies

To enable this property, set the ScattererSpecificationSource property to 'Input port ' and the Polarization property to 'Combined' or 'Dual'.

Data Types: double

## Output Arguments

## Y - Received narrowband signal

complex-valued $M$-by- $N_{r}$ matrix
Received narrowband signal, returned as an $M$-by- $\mathrm{N}_{\mathrm{r}}$ complex-valued matrix. $M$ is the number of samples in the signal, and $N_{r}$ is the number of receiving array elements. Each column represents the signal received by the corresponding array element.
Example: [1,1;j,1;0.5,0]

## Dependencies

To enable this argument, set the Polarization property to 'None' or 'Combined'.
Data Types: double

## Complex Number Support: Yes

## YH - Received narrowband H-polarization signal

complex-valued $M$-by- $N_{r}$ matrix
Received narrowband $H$-polarization signal, returned as a complex-valued $M$-by- $N_{r}$ matrix. $M$ is the number of samples in the signal, and $N_{r}$ is the number of receiving array elements. Each column represents the signal received by the corresponding array element.
Example: [1,1;j,1;0.5,0]

## Dependencies

To enable this argument, set the Polarization property to 'Dual '.
Data Types: double
Complex Number Support: Yes

## YV - Received narrowband V-polarization signal

complex-valued $M$-by- $N_{r}$ matrix
Received narrowband $V$-polarization signal, returned as a complex-valued $M$-by- $N_{r}$ matrix. $M$ is the number of samples in the signal, and $N_{r}$ is the number of receiving array elements. Each column represents the signal received by the corresponding array element.
Example: [1, 1; j, 1;0.5,0]

## Dependencies

To enable this argument, set the Polarization property to 'Dual '.
Data Types: double
Complex Number Support: Yes

## CR - Channel response

complex-valued $N_{t}$-by- $N_{r}$-by- $N_{c}$ array
Channel response, returned as an $N_{t}$-by- $N_{r}$-by- $N_{c}$ complex-valued array.

- $N_{t}$ is the number of transmitting array elements.
- $N_{r}$ is the number of receiving array elements.
-     - When you specify SimulateDirectPath as false, $N_{c}=N_{s}$, the number of scatterers.
- When you specify SimulateDirectPath as true, $N_{c}=N_{s}+1$ to account for the direct path.

Each page of the array corresponds to the channel response matrix for a specific scatterer.

## Dependencies

To enable this argument, set the ChannelResponseOutputPort property to true and the Polarization property to 'None' or 'Combined'.
Data Types: double
Complex Number Support: Yes
CR_HH - Channel response for H-input to H-output
complex-valued $N_{t}$-by- $N_{r}$-by- $N_{c}$ array

Channel response from H-polarization input to H-polarization output returned as a complex-valued $N_{t}$-by- $N_{r}$-by- $N_{c}$ array.

- $N_{t}$ is the number of transmitting array elements.
- $N_{r}$ is the number of receiving array elements.
-     - When you specify SimulateDirectPath as false, $N_{c}=N_{s}$, the number of scatterers.
- When you specify SimulateDirectPath as true, $N_{c}=N_{s}+1$ to account for the direct path.

Each page of the array corresponds to the channel response matrix for a specific scatterer.
Dependencies
To enable this argument, set the ChannelResponseOutputPort property to true and the Polarization property to 'Dual'.
Data Types: double
Complex Number Support: Yes

## CR_HV - Channel response for H-input to V-output

complex-valued $N_{t}$-by- $N_{r}$-by- $N_{c}$ array
Channel response from H-polarization input to V-polarization output returned as a complex-valued $N_{t^{-}}$ by- $N_{r}$-by- $N_{c}$ array.

- $N_{t}$ is the number of transmitting array elements.
- $N_{r}$ is the number of receiving array elements.
-     - When you specify SimulateDirectPath as false, $N_{c}=N_{s}$, the number of scatterers.
- When you specify SimulateDirectPath as true, $N_{c}=N_{s}+1$ to account for the direct path.

Each page of the array corresponds to the channel response matrix for a specific scatterer.

## Dependencies

To enable this argument, set the ChannelResponseOutputPort property to true and the Polarization property to 'Dual'.
Data Types: double
Complex Number Support: Yes

## CR_VH - Channel response for V-input to H-output

complex-valued $N_{t}$-by- $N_{r}$-by- $N_{c}$ array
Channel response from V-polarization input to H-polarization output returned as a complex-valued $N_{t^{-}}$ by- $N_{r}$-by- $N_{c}$ array.

- $N_{t}$ is the number of transmitting array elements.
- $N_{r}$ is the number of receiving array elements.
-     - When you specify SimulateDirectPath as false, $N_{c}=N_{s}$, the number of scatterers.
- When you specify SimulateDirectPath as true, $N_{c}=N_{s}+1$ to account for the direct path.

Each page of the array corresponds to the channel response matrix for a specific scatterer.

## Dependencies

To enable this argument, set the ChannelResponseOutputPort property to true and the Polarization property to 'Dual'.

Data Types: double
Complex Number Support: Yes

## CR_VV - Channel response for V-input to V-output <br> complex-valued $N_{t}$-by- $N_{r}$-by- $N_{c}$ array

Channel response from V-polarization input to V-polarization output returned as a complex-valued $N_{t^{-}}$ by- $N_{r}$-by- $N_{c}$ array.

- $N_{t}$ is the number of transmitting array elements.
- $N_{r}$ is the number of receiving array elements.
-     - When you specify SimulateDirectPath as false, $N_{c}=N_{s}$, the number of scatterers.
- When you specify SimulateDirectPath as true, $N_{c}=N_{s}+1$ to account for the direct path.

Each page of the array corresponds to the channel response matrix for a specific scatterer.

## Dependencies

To enable this argument, set the ChannelResponseOutputPort property to true and the Polarization property to 'Dual'.
Data Types: double
Complex Number Support: Yes

## TAU - Path delays

1 -by- $N_{s}$ real-valued vector
Path delays, returned as a 1-by- $N_{C}$ real-valued vector. Each element corresponds to the path time delay from the transmitting array phase center to a scatterer and then to the receiving array phase center.

- When you specify SimulateDirectPath as false, $N_{c}=N_{s}$, the number of scatterers.
- When you specify SimulateDirectPath as true, $N_{c}=N_{s}+1$ to account for the direct path.


## Dependencies

To enable this argument, set the ChannelResponseOutputPort property to true.

## Data Types: double

## Examples

## Propagate Signals in MIMO Channel

Create a 30 GHz MIMO channel with random scatterers. The scenario contains a stationary 21element transmitting ULA array and a stationary 15 -element receiving ULA array. The transmitting antennas have cosine responses and the receiving antennas are isotropic. Element spacing for both arrays is less than one-half wavelength. The channel has 50 randomly generated static scatterers within a specified bounding box. The transmit array is located at $[0 ; 20 ; 50]$ meters and the receive
array is located at $[200 ; 10 ; 10]$ meters. Compute the propagated signal through this channel. The sample rate for the signal is 10 MHz .

```
fc = 30e9;
c = physconst('LightSpeed');
lambda = c/fc;
fs = 10e6;
txarray = phased.ULA('Element',phased.CosineAntennaElement,...
    'NumElements',21,'ElementSpacing',0.45*lambda);
rxarray = phased.ULA('Element',phased.IsotropicAntennaElement,...
    'NumElements',15,'ElementSpacing',0.45*lambda);
channel = phased.ScatteringMIMOChannel('TransmitArray',txarray,...
    'ReceiveArray',rxarray,'PropagationSpeed',c,'CarrierFrequency',fc,...
    'SampleRate',fs,'TransmitArrayPosition',[0;20;50],...
    'ReceiveArrayPosition',[200;10;10],'NumScatterers',50,...
    'ScattererPositionBoundary',[10 180; -30 30; -30 30]);
```

Create a random data signal of ones and zeros for each transmitter.
x = randi(2,[100 21]) - 1;
Compute the received signals after propagating through the channel.

```
y = channel(x);
```


## Propagate Signals in MIMO Channel from Moving Transmitter

Create a MIMO channel containing 3 fixed scatterers. The scenario contains a 21 -element transmitting ULA array operating at 72 GHz , and a 15 -element receiving ULA array. The transmitting elements have cosine response shapes and the receiving antennas are isotropic. Only the transmitting antenna is moving. Element spacing for both arrays is less than one-half wavelength. The transmitting array starts at $(0,20,50)$ meters and moves towards the receiver at $2 \mathrm{~m} / \mathrm{s}$. The receiving array is located at $(200,10,10)$ meters. Compute the propagated signal through this channel. The sample rate for the signal is 10 MHz .

```
fc = 72e9;
c = physconst('LightSpeed');
lambda = c/fc;
fs = 10e6;
txplatform = phased.Platform('MotionModel','Velocity','InitialPosition', ...
    [0;20;50],'Velocity',[2;0;0]);
txarray = phased.ULA('Element',phased.CosineAntennaElement, ...
        'NumElements',21,'ElementSpacing',0.45*lambda);
rxarray = phased.ULA('Element',phased.IsotropicAntennaElement, ...
        'NumElements',15,'ElementSpacing',0.45*lambda);
channel = phased.ScatteringMIMOChannel('TransmitArray',txarray, ...
        'ReceiveArray',rxarray,'PropagationSpeed',c,'CarrierFrequency',fc,...
        'SampleRate',fs,'TransmitArrayMotionSource','Input port', ...
        'ReceiveArrayMotionSource','Property','ReceiveArrayPosition',[200;10;10],...
        'ReceiveArray0rientationAxes',rotz(180),...
        'ScattererSpecificationSource','Property','ScattererPosition', ...
        [75 100 120; -10 20 12; 5 -5 8],'ScattererCoefficient',[1i,2+3i,-1+1i]);
```

Move the platforms for two time steps at one second intervals. For each time instance:

- Create a random data signal of ones and zeros for each transmitter element.
- Move the transmitter and receiver. The orientations are fixed.
- Propagate the signals from transmitters to scatterers to receiver.

```
for k =1:2
    x = randi(2,[100 21]) - 1;
    [txpos,txvel] = txplatform(1);
    txaxes = eye(3);
    y = channel(x,txpos,txvel,txaxes);
end
```


## Propagate Signals Through MIMO Channel to Moving Receiver

Create a MIMO channel containing 3 fixed scatterers. The scenario contains a 21 -element transmitting ULA array and a 15-element receiving ULA array. Both arrays operate at 72 GHz . The transmitting elements have cosine response shapes and the receiving antennas are isotropic. Only the receiving antenna is moving. Element spacing for both arrays is less than one-half wavelength. The transmitting array is located at $(0,20,50)$ meters. The receiving array starts at $(200,10,10)$ meters and moves toward the transmitter at $2 \mathrm{~m} / \mathrm{s}$. Compute the propagated signal through this channel. The sample rate for the signal is 10 MHz .

```
fc = 72e9;
c = physconst('LightSpeed');
lambda = c/fc;
fs = 10e6;
rxplatform = phased.Platform('MotionModel','Velocity','InitialPosition',...
    [200;10;10],'Velocity', [-2;0;0]);
txarray = phased.ULA('Element',phased.CosineAntennaElement, ...
    'NumElements',21,'ElementSpacing',0.45*lambda);
rxarray = phased.ULA('Element',phased.IsotropicAntennaElement, ...
    'NumElements',15,'ElementSpacing',0.45*lambda);
channel = phased.ScatteringMIMOChannel('TransmitArray',txarray, ...
    'ReceiveArray',rxarray,'PropagationSpeed',c,'CarrierFrequency',fc, ...
    'SampleRate',fs,'TransmitArrayMotionSource','Property',...
    'TransmitArrayPosition',[0;20;50],'TransmitArray0rientationAxes',eye(3,3), ...
    'ReceiveArrayMotionSource','Input port','ScattererSpecificationSource', ...
    'Property','ScattererPosition',[75 100 120; -10 20 12; 5 -5 8], ...
    'ScattererCoefficient',[1i,2+3i,-1+1i],'SpecifyAtmosphere',false);
```

Move the platforms for two time steps at one-second intervals. For each time instance:

- Create a random data signal of ones and zeros for each transmitter element.
- Move the transmitter and receiver. Fix the array orientations.
- Propagate the signals from transmitters to scatterers to receiver.

```
for k =1:2
    x = randi(2,[100 21]) - 1;
    [rxpos,rxvel] = rxplatform(1);
    rxaxes = rotz(45);
    y = channel(x,rxpos,rxvel,rxaxes);
end
```


## Compute Propagated Signals Through MIMO Channel with Moving Scatterers

Create a MIMO channel containing 3 moving scatterers. The scenario contains a 21 -element transmitting ULA array and a 15 -element receiving ULA array. Both arrays operate at 72 GHz . The transmitting elements have cosine responses and the receiving antennas are isotropic. Element spacing for both arrays is less than one-half wavelength. The transmitting array is located at $(0,20,50)$ meters. The receiving array is located at $(200,10,10)$ meters. Compute the propagated signal through this channel. The sample rate for the signal is 10 MHz . Obtain the channel response matrix and time delays.

```
fc = 30e9;
c = physconst('LightSpeed');
lambda = c/fc;
fs = 10e6;
txarray = phased.ULA('Element',phased.CosineAntennaElement, ...
    'NumElements',21,'ElementSpacing',0.45*lambda);
rxarray = phased.ULA('Element',phased.IsotropicAntennaElement, ...
    'NumElements',15,'ElementSpacing',0.45*lambda);
channel = phased.ScatteringMIMOChannel('TransmitArray',txarray, ...
    'ReceiveArray',rxarray,'PropagationSpeed',c,'CarrierFrequency',fc, ...
    'SampleRate',fs,'TransmitArrayPosition',[0;20;50], ...
    'ReceiveArrayPosition',[200;10;10],'ScattererSpecificationSource','Input port', ...
    'ChannelResponse0utputPort',true);
```

Create a random data signal of ones and zeros for each transmitter.

```
x = randi(2,[100 21]) - 1;
```

Compute the received signals after propagating through the channel. Also return the channel matrix and delays.

```
scatpos = [75 100 120; -10 20 12; 5 -5 8];
scatvel = [0 0.5 0; -0.1 1.2 0.04; .05 -0.45 0.8];
scatcoef = [1i,2+3i,-1+1i];
[y,chmat,delays] = channel(x,scatpos,scatvel,scatcoef);
```

Display the dimensions of the channel matrix.

```
size(chmat)
ans = 1\times3
    21 15 3
```

Display the time delays in microseconds.

```
delays*1e6
ans = 1\times3
    0.7310 0.7196 0.6919
```


## Propagate Polarized Signals in MIMO Channel

Create a MIMO channel at 30 GHz with a 16 -element transmit array and a 64 -element receive array. Assume the elements are short-dipole antennas and the arrays are uniform linear arrays. The transmit array is located at $[0 ; 0 ; 50]$ meters.

The receive array has an initial position at [200;0;0] meters and is moving at a speed of $[10 ; 0 ; 0]$ meters/second. There are 200 static scatterers randomly located on the $x y$ plane within a square centered at [200;0;0] and with a side length of 100 meters.

Use the channel to compute the propagated polarized signal. Assume the sample rate for the signal is 10 MHz and the frame length is 1000 samples. Collect 5 frames of received signal.

```
fc = 30e9;
c = 3e8;
lambda = c/fc;
fs = 10e6;
txarray = phased.ULA('Element',phased.ShortDipoleAntennaElement,...
    'NumElements',16,'ElementSpacing',lambda/2);
rxarray = phased.ULA('Element',phased.ShortDipoleAntennaElement,...
    'NumElements',64,'ElementSpacing',lambda/2);
Ns = 200;
scatpos = [100*rand(1,Ns) + 150; 100*rand(1,Ns) + 150; zeros(1,Ns)];
temp = randn(1,Ns) + 1i*randn(1,Ns);
scatcoef = repmat(eye(2),1,1,Ns).*permute(temp,[1 3 2]);
scatax = repmat(eye(3),1,1,Ns);
Nframesamp = 1000;
Tframe = Nframesamp/fs;
rxmobile = phased.Platform('InitialPosition',[200;0;0],...
    'Velocity',[10;0;0],'OrientationAxes0utputPort',true);
chan = phased.ScatteringMIMOChannel(...
    'TransmitArray',txarray,...
    'ReceiveArray',rxarray,...
    'PropagationSpeed',c,...
    'CarrierFrequency',fc,...
    'SampleRate',fs,...
    'Polarization','Dual',...
    'TransmitArrayPosition',[0;0;50],...
    'ReceiveArrayMotionSource','Input port',...
    'ScattererSpecificationSource','Property',...
    'ScattererPosition',scatpos,...
    'ScatteringMatrix',scatcoef,...
    'ScattererOrientationAxes',scatax);
xh = randi(2,[Nframesamp 16])-1;
xv = randi(2,[Nframesamp 16])-1;
for m = 1:5
    [rxpos,rxvel,rxax] = rxmobile(Tframe);
    [yh,yv] = chan(xh,xv,rxpos,rxvel,rxax);
end
```


# Version History <br> Introduced in R2017a 

## phased.SphericalWavefrontArrayResponse

Package: phased

Array response to spherical wavefront

## Description

The phased.SphericalWavefrontArrayResponse System object calculates the complex-valued response of a sensor array to a spherical wave.

To compute the response:
1 Create the phased.SphericalWavefrontArrayResponse object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

response = phased.SphericalWaveformArrayResponse
response = phased.SphericalWaveformArrayResponse(Name,Value)

## Description

The response = phased.SphericalWaveformArrayResponse creates a phased.SphericalWaveformArrayResponse System object response with default property values.
response = phased.SphericalWaveformArrayResponse(Name,Value) creates a phased. SphericalWaveformArrayResponse object with each property Name set to a specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN). Enclose each property name in single quotes.

## Example: response =

phased.SphericalWaveformArrayResponse('SensorArray', phased.URA([10, 20], 'Eleme ntSpacing',[0.25,0.25]),'PropagationSpeed', physconst('LightSpeed')) creates a phased.SphericalWaveformArrayResponse System object for a 10-by-20 uniform rectangular array (URA) with element spacing set to 0.25 meters The propagation speed set to the speed of light.

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.

For more information on changing property values, see System Design in MATLAB Using System Objects.

## SensorArray - Sensor array

phased.ULA array with default array properties (default) | Phased Array System Toolbox array System object

Sensor array, specified as a Phased Array System Toolbox array System object.
Example: phased.URA
PropagationSpeed - Signal propagation speed
physconst('LightSpeed') (default) | positive scalar
Signal propagation speed, specified as a positive scalar. Units are in meters per second. The default propagation speed is the value returned by physconst('LightSpeed'). See physconst for more information.

Example: 3e8
Data Types: double

## IncludeElementResponse - Include individual element responses in the steering vector false (default) | true

Option to include individual element responses in the steering vector, specified as false or true. If this property is set to true, the steering vector includes individual array element responses. If this property is set to false, the steering vector is computed assuming that the elements are isotropic, regardless of how the elements are specified. Set this property to true when using polarized signals.

When the array specified in the SensorArray property contains subarrays, the steering vector applies to subarrays. If SensorArray does not contain subarrays, the steering vector applies to the array elements.
Data Types: logical

## WeightsInputPort - Enable weights input <br> false (default) | true

Enable weights input, specified as false or true. When true, use the object input argument $W$ to specify weights. Weights are applied to individual array elements (or at the subarray level when subarrays are supported).
Data Types: logical

## EnablePolarization - Enable simulation of polarization false (default) |true

Enable polarization simulation, specified as false or true. Set this property to true to enable polarization and to false to ignore polarization. This property applies when the array specified in the SensorArray property is capable of simulating polarization and the IncludeElementResponse property of the array is set to true.
Data Types: logical

## Usage

## Syntax

RESP $=$ response(FREQ,ANG,RNG)
RESP $=$ response(FREQ,ANG,RNG,W)

## Description

RESP $=$ response (FREQ, ANG, RNG) returns the array response RESP at operating frequencies specified in FREQ, directions specified in ANG, and at range RNG.

RESP $=$ response (FREQ, ANG , RNG,$W$ ) applies weights $W$ to the sensor array. To enable this syntax, set the WeightsInputPort to true.

## Input Arguments

## FREQ - Frequency for computing directivity and patterns

positive scalar | 1-by-L real-valued row vector
Frequencies for computing directivity and patterns, specified as a positive scalar or 1-by- $L$ realvalued row vector. Frequency units are in hertz.

- For an antenna, microphone, or sonar hydrophone or projector element, FREQ must lie within the range of values specified by the FrequencyRange or FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased. CustomAntennaElement and phased. CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.


## Example: [1e8 2e6]

Data Types: double

## ANG - Angles for computing response

1-by- $M$ real-valued row vector | 2-by- $M$ real-valued matrix
Angles for computing response, specified as a 1-by- $M$ real-valued row vector or a 2-by- $M$ real-valued matrix, where $M$ is the number of angular directions. Angle units are in degrees. If ANGLE is a 2-by- $M$ matrix, then each column specifies a direction in azimuth and elevation, [az;el]. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

If ANGLE is a 1-by- $M$ vector, then each entry represents an azimuth angle, with the elevation angle assumed to be zero.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the $x y$ plane. This angle is positive when measured from the $x$-axis toward the $y$-axis. The elevation angle is the angle between the direction vector and $x y$ plane. This angle is positive when measured towards the $z$-axis. See "Azimuth and Elevation Angles".
Example: [45 60; 0 10]
Data Types: double

## RNG - Range

positive scalar | 1-by-M real-valued vector of positive values
Range, specified as a positive 1-by- $M$ real-valued vector of positive values. If ANG has more than one column, RNG must be a scalar or have the same number of columns as ANG. Units are in meters.

Data Types: double

## W - Array weights

1 (default) | complex length- $N$ column vector | complex $N$-by-L matrix
Weights applied to sensor array elements, specified as a complex-valued, length- $N$ column vector or a complex-valued, $N$-by- $L$ matrix. $N$ is the number of array elements and $L$ is the number of frequencies specified in FREQ. If $W$ is a vector, the same weight is applied at all frequencies. If $W$ is a matrix, each column of $W$ represents the weights used at the corresponding frequency specified in FREQ.

## Dependencies

To enable this argument, set the WeightsInputPort to true.

## Data Types: double

Complex Number Support: Yes

## Output Arguments

## RESP - Array response

complex-valued $M$-by-L matrix | struct
Array response, returned as a complex-valued $M$-by- $L$ complex-valued matrix or struct containing complex values. The response depends on whether the EnablePolarization property is set to true or false.

- If the EnablePolarization property is set to false, the voltage response, RESP, has the dimensions $M$-by-L. $M$ represents the number of angles specified in the input argument ANG while $L$ represents the number of frequencies specified in FREQ.
- If the EnablePolarization property is set to true, the voltage response, RESP, is a MATLAB struct containing two complex fields, RESP.H and RESP.V. The RESP. H field represents the array's horizontal polarization response, while RESP.V represents the array's vertical polarization response. Each field has the dimensions $M$-by-L. $M$ represents the number of angles specified in the input argument, ANG, while $L$ represents the number of frequencies specified in FREQ.


## Data Types: double

Complex Number Support: Yes

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:
release(obj)

## Common to All System Objects

step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object

## Examples

## Compute Spherical Wavefront Response for URA

Calculate and plot the azimuth response of a 4 -by- 8 uniform rectangular array at directions between $-90^{\circ}$ and $90^{\circ}$ in azimuth at a range of 1 km . Assume the array operating frequency is 300 MHz .

Create the array and the phased.SphericalWavefrontArrayResponse System object ${ }^{\mathrm{mm}}$.

```
array = phased.URA([4,8]);
response = phased.SphericalWavefrontArrayResponse( ...
    'SensorArray',array);
ang = -90:90;
rng = 1000.0;
fc = 300e6;
```

Compute and plot the response as a function of azimuth angle.

```
resp = response(fc,ang,rng);
plot(ang,abs(resp))
xlabel('Angle (degrees)')
ylabel('Magnitude')
title('Azimuth Response')
```



## Compute Spherical Wavefront Response for Weighted ULA

Calculate and plot the azimuth response of an 11-element uniform linear array at directions between $-90^{\circ}$ and $90^{\circ}$ in azimuth at a range of 1 km . Create a polarized field using short-dipole antenna elements. Assume the array operating frequency is 300 MHz .

Create the ULA array and the phased. SphericalWavefrontArrayResponse System object ${ }^{\text {Tm }}$.

```
antenna = phased.ShortDipoleAntennaElement;
array = phased.ULA(11,'Element',antenna);
response = phased.SphericalWavefrontArrayResponse( ...
    'SensorArray',array,'EnablePolarization', ...
    true,'WeightsInputPort',true);
ang = -90:90;
rng = 1000.0;
fc = 300e6;
w = taylorwin(11);
```

Compute and plot the response as a function of azimuth angle.

```
resp = response(fc,ang,rng,w);
plot(ang,abs(resp.V))
xlabel('Angle (degrees)')
ylabel('Magnitude')
title('Azimuth Response to Vertical Polarization')
```



## Version History

Introduced in R2021b

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.

## See Also

phased.ArrayResponse | phased.FocusedSteeringVector|phased.SteeringVector

## Topics

"Examine the Response of a Focused Phased Array"

# phased.SteeringVector 

Package: phased
Sensor array steering vector

## Description

The SteeringVector System object creates steering vectors for a sensor array for multiple directions and frequencies.

To compute the steering vector for an array for specified directions and frequency
1 Create the phased.SteeringVector object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

steervec = phased.SteeringVector
steervec = phased.SteeringVector(Name,Value)

## Description

steervec = phased.SteeringVector creates a steering vector System object, steervec, with default property values.
steervec = phased.SteeringVector(Name,Value) creates a steering vector with each property Name set to a specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN). Enclose each property name in single quotes.

Example: steervec = phased. SteeringVector('SensorArray', phased.URA, 'PropagationSpeed', physconst(' LightSpeed ') ) creates a steering vector object for a uniform rectangular array (URA) with default URA property values and sets the propagation speed to the speed of light.

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## SensorArray - Sensor array

phased. ULA array with default property values (default) | Phased Array System Toolbox array
Sensor array, specified as an array System object belonging to Phased Array System Toolbox. The sensor array can contain subarrays.

Example: phased.URA

## PropagationSpeed - Signal propagation speed

physconst('LightSpeed') (default)| positive scalar
Signal propagation speed, specified as a positive scalar. Units are in meters per second. The default propagation speed is the value returned by physconst('LightSpeed'). See physconst for more information.

Example: 3e8
Data Types: double

## IncludeElementResponse - Include individual element responses in the steering vector

 false (default) | trueOption to include individual element responses in the steering vector, specified as false or true. If this property is set to true, the steering vector includes individual array element responses. If this property is set to false, the steering vector is computed assuming that the elements are isotropic, regardless of how the elements are specified. Set this property to true when using polarized signals.

When the array specified in the SensorArray property contains subarrays, the steering vector applies to subarrays. If SensorArray does not contain subarrays, the steering vector applies to the array elements.

Data Types: logical

## NumPhaseShifterBits - Number of phase shifter quantization bits <br> 0 (default) | nonnegative integer

Number of phase shifter quantization bits, specified as a nonnegative integer. This number of bits is used to quantize the phase shift component of the beamformer or steering vector weights. A value of zero indicates that no quantization is performed.

Data Types: double
EnablePolarization - Enable polarized fields
false (default) |true
Option to enable polarized fields, specified as false or true. Set this property to true to enable polarization. Set this property to false to ignore polarization. Enabling polarization requires that the sensor array specified in the SensorArray property can simulate polarization.

If you set this property to false for an array that actually supports polarization, then all polarization information is discarded. A combined pattern from the $H$ and $V$ polarization components is used at each element to compute the steering vector.

Data Types: logical

## Usage

## Syntax

```
SV = steervec(FREQ,ANG)
SV = steervec(FREQ,ANG,STEERANG)
SV = steervec(FREQ,ANG,STEERANG,WS)
```


## Description

SV = steervec(FREQ,ANG) returns the steering vector, SV, pointing in the directions specified by ANG and for the operating frequencies specified in FREQ. The meaning of SV depends on the IncludeElementResponse property, as follows:

- If IncludeElementResponse is true, the components of SV include individual element responses.
- If IncludeElementResponse is false, the computation assumes that the elements are isotropic and SV does not include the individual element responses. If the array contains subarrays, SV is the array factor among the subarrays. The phase center of each subarray is at its geometric center. If SensorArray does not contain subarrays, SV is the array factor among the elements.

SV = steervec(FREQ,ANG,STEERANG) also specifies the subarray steering angle, STEERANG. To use this syntax, set the SensorArray property to an array type that contains subarrays and set the IncludeElementResponse to true. Arrays that contain subarrays are the phased. PartitionedArray and the phased.ReplicatedSubarray. In this case, set the SubarraySteering property of these arrays to either 'Phase' or 'Time'.

SV = steervec(FREQ,ANG,STEERANG,WS) also specifies WS as weights applied to each element within each subarray. To use this syntax, set the SensorArray property to an array that supports subarrays and set the SubarraySteering property of the array to 'Custom'.

## Input Arguments

## ANG - Steering vector direction

[0;0] (default) | real-valued length-M vector | real-valued 2-by-M matrix
Steering vector directions, specified as a real-valued, length- $M$ vector, or a real-valued 2-by- $M$ matrix. $M$ is the number of steering directions. When ANG is a 2-by-M matrix, each column of the matrix specifies the direction in space in the form [azimuth; elevation]. The azimuth angle must be between $-180^{\circ}$ and $180^{\circ}$, and the elevation angle must be between $-90^{\circ}$ and $90^{\circ}$. When ANG is a length- $M$ vector, its values correspond to the azimuth angles of the steering vector direction with elevation angles set to zero. Angle units are in degrees.
Example: $[50.0,17.0,-24.5 ; 0.4,4.0,23.9]$
Data Types: single | double

## FREQ - Operating frequencies

1 -by- $L$ vector of positive values
Operating frequencies, specified as a 1-by- $L$ vector of positive values. Units are in Hz .
Example: [4100.0,4200.0]
Data Types: single|double

## STEERANG - Subarray steering direction

scalar | real-valued 2-by-1 vector
Subarray steering direction, specified as a scalar or a real-valued 2 -by- 1 vector. When STEERANG is a 2 -by-1 vector, it specifies the subarray steering direction in the form [azimuth;elevation]. The azimuth angle must be between $-180^{\circ}$ and $180^{\circ}$, and the elevation angle must be between $-90^{\circ}$ and $90^{\circ}$. When STEERANG is a scalar, its value corresponds to the azimuth angle of the subarray steering direction with elevation angles set to zero. Angle units are in degrees.
Example: [50.0;10.0]
Data Types: single | double

## WS - Subarray element weights

complex-valued $N_{\text {SE }}$-by- $N$ matrix | 1-by- $N$ cell array
Subarray element weights, specified as complex-valued $N_{\text {SE }}$-by- $N$ matrix or 1-by- $N$ cell array where $N$ is the number of subarrays. These weights are applied to the individual elements within a subarray.

## Subarray element weights

| Sensor Array | Subarray weights |
| :--- | :--- |
| phased.ReplicatedSubarray | All subarrays have the same dimensions and <br> sizes. Then, the subarray weights form an $N_{\text {SE }}$-by- <br> $N$ matrix. $N_{\mathrm{SE}}$ is the number of elements in each <br> subarray and $N$ is the number of subarrays. Each <br> column of WS specifies the weights for the <br> corresponding subarray. |
| phased. PartitionedArray | Subarrays may not have the same dimensions and <br> sizes. In this case, you can specify subarray <br> weights as |
|  | an $N_{\mathrm{SE}}$-by- $N$ matrix, where $N_{\text {SE }}$ is now the <br> number of elements in the largest subarray. <br> The first $Q$ entries in each column are the <br> element weights for the subarray where $Q$ is <br> the number of elements in the subarray. |
|  | a 1-by- $N$ cell array. Each cell contains a <br> column vector of weights for the <br> corresponding subarray. The column vectors |
|  | have lengths equal to the number of elements |
| in the corresponding subarray. |  |

## Dependencies

To enable this argument, set the Sensor property to an array that contains subarrays and set the SubarraySteering property of the array to 'Custom'.
Data Types: single| double Complex Number Support: Yes

## Output Arguments

SV - Steering vector
complex-valued $N$-by- $M$-by- $L$ array | structures

Steering vector, returned as a complex-valued $N$-by- $M$-by- $L$ array or a structure containing arrays.
The form of the steering vector depends upon whether the EnablePolarization property is set to true or false.

- If EnablePolarization is set to false, the steering vector, SV, is an $N$-by- $M$-by- $L$ array. The length of the first dimension, $N$, is the number of elements of the phased array. If SensorArray contains subarrays, $N$ is the number of subarrays. The length of the second dimension, $M$, corresponding to the number of steering directions specified in the ANG argument. The length of the third dimension, $L$, is the number of frequencies specified in the FREQ argument.
- If EnablePolarization is set to true, SV is a MATLAB struct containing two fields, SV.H and SV.V. These two fields represent the horizontal $(H)$ and vertical $(V)$ polarization components of the steering vector. Each field is an $N$-by- $M$-by- $L$ array. The length of the first dimension, $N$, is the number of elements of the phased array. If SensorArray contains subarrays, $N$ is the number of subarrays. The length of the second dimension, $M$, corresponds to the number of steering directions specified in the ANG argument. The length of the third dimension, $L$, is the number of frequencies specified in the FREQ argument.

Simulating polarization also requires that the sensor array specified in the SensorArray property can simulate polarization, and that the IncludeElementResponse property is set to true.

Data Types: single | double

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```


## Common to All System Objects

```
step Run System object algorithm
release Release resources and allow changes to System object property values and input
    characteristics
reset Reset internal states of System object
```


## Examples

## Steering Vector for Uniform Linear Array

Calculate and display the steering vector for a 4 -element uniform linear array in the direction of 30 degrees azimuth and 20 degrees elevation. Assume the array's operating frequency is 300 MHz .

```
array = phased.ULA('NumElements',4);
steervec = phased.SteeringVector('SensorArray',array);
fc = 3e8;
ang = [30; 20];
sv = steervec(fc,ang)
sv = 4×1 complex
    -0.6011 - 0.7992i
```

```
0.7394 - 0.6732i
0.7394 + 0.6732i
-0.6011 + 0.7992i
```


## Beam Pattern with and Without Steering

Calculate the steering vector for a 4 -element uniform linear array (ULA) in the direction of 30 degrees azimuth and 20 degrees elevation. Assume the array operating frequency is 300 MHz .

```
fc = 300e6;
c = physconst('LightSpeed');
array = phased.ULA('NumElements',4);
steervec = phased.SteeringVector('SensorArray',array);
sv = steervec(fc,[30;20]);
```

Plot the beam patterns for the uniform linear array when no steering vector is applied (steered broadside) and when a steering vector is applied.

```
subplot(211)
pattern(array,fc,-180:180,0,'CoordinateSystem','rectangular', ...
    'PropagationSpeed ',c,'Type',' powerdb')
title('Without steering')
subplot(212)
pattern(array,fc,-180:180,0,'CoordinateSystem','rectangular', ...
    'PropagationSpeed',c,'Type','powerdb','Weights',sv)
title('With steering')
```



## Steering Vector for Uniform Linear Array

Calculate the steering vector for a uniform linear array in the direction of $30^{\circ}$ azimuth and $20^{\circ}$ elevation. Assume the array operates at 300 MHz .
array = phased.ULA('NumElements',2);
steeringvector = phased.SteeringVector('SensorArray',array);
fc = 300.0e6;
ang $=$ [30;20];
sv = steeringvector(fc,ang);

## Version History

Introduced in R2011a

## References

[1] Van Trees, H. Optimum Array Processing. New York: Wiley-Interscience, 2002.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.
Usage notes and limitations:

- See "System Objects in MATLAB Code Generation" (MATLAB Coder).


## See Also

phased.ArrayGain|phased.ArrayResponse|phased.ElementDelay|uv2azel| phitheta2azel

## step

System object: phased. SteeringVector
Package: phased
Calculate steering vector

## Syntax

SV = step( $\mathrm{H}, \mathrm{FREQ}, \mathrm{ANG}$ )
SV = step(H,FREQ,ANG,STEERANGLE)
SV $=\operatorname{step}(H, F R E Q, A N G, W S)$

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step $(o b j, x)$ and $y=o b j(x)$ perform equivalent operations.

SV = step( $\mathrm{H}, \mathrm{FREQ}, \mathrm{ANG}$ ) returns the steering vector SV of the array for the directions specified in ANG. The operating frequencies are specified in FREQ. The meaning of SV depends on the IncludeElementResponse property of H , as follows:

- If IncludeElementResponse is true, SV includes the individual element responses.
- If IncludeElementResponse is false, the computation assumes the elements are isotropic and SV does not include the individual element responses. Furthermore, if the SensorArray property of H contains subarrays, SV is the array factor among the subarrays and the phase center of each subarray is at its geometric center. If SensorArray does not contain subarrays, SV is the array factor among the elements.

SV = step(H,FREQ,ANG, STEERANGLE) uses STEERANGLE as the subarray steering angle. This syntax is available when you configure H so that H . Sensor is an array that contains subarrays, H.Sensor.SubarraySteering is either 'Phase' or 'Time', and H.IncludeElementResponse is true.

SV = step(H,FREQ,ANG,WS) uses WS as weights applied to each element within each subarray. To use this syntax, set the SensorArray property to an array that supports subarrays and set the SubarraySteering property of the array to 'Custom', and H.IncludeElementResponse is true.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## H

Steering vector object.

## FREQ

Operating frequencies in hertz. FREQ is a row vector of length L .

## ANG

Directions in degrees. ANG can be either a 2-by-M matrix or a row vector of length M.
If ANG is a 2-by-M matrix, each column of the matrix specifies the direction in space in the form [azimuth; elevation]. The azimuth angle must be between -180 degrees and 180 degrees, and the elevation angle must be between -90 degrees and 90 degrees.

If ANG is a row vector of length $M$, each element specifies the direction azimuth angle. In this case, the corresponding elevation angle is assumed to be 0 .

## STEERANGLE

Subarray steering angle in degrees. STEERANGLE can be a length-2 column vector or a scalar.
If STEERANGLE is a length -2 vector, it has the form [azimuth; elevation]. The azimuth angle must be between -180 degrees and 180 degrees, and the elevation angle must be between - 90 degrees and 90 degrees.

If STEERANGLE is a scalar, it represents the azimuth angle. In this case, the elevation angle is assumed to be 0 .

## WS

Subarray element weights
Subarray element weights, specified as complex-valued $N_{S E}$-by- $N$ matrix or 1-by- $N$ cell array where $N$ is the number of subarrays. These weights are applied to the individual elements within a subarray.

Subarray Element Weights

| Sensor Array | Subarray Weights |
| :--- | :--- |
| phased. ReplicatedSubarray | All subarrays have the same dimensions and <br> sizes. Then, the subarray weights form an $N_{S E}$-by- <br> $N$ matrix. $N_{S E}$ is the number of elements in each <br> subarray and $N$ is the number of subarrays. Each <br> column of WS specifies the weights for the <br> corresponding subarray. |
| phased. PartitionedArray | Subarrays cannot have the same dimensions and <br> sizes. In this case, you can specify subarray <br> weights as |
|  | an $N_{S E}$-by- $N$ matrix, where $N_{S E}$ is now the <br> number of elements in the largest subarray. <br> The first $Q$ entries in each column are the <br> element weights for the subarray where $Q$ is <br> the number of elements in the subarray. <br> a 1-by- $N$ cell array. Each cell contains a <br> column vector of weights for the <br> corresponding subarray. The column vectors <br> have lengths equal to the number of elements <br> in the corresponding subarray. |

## Dependencies

To enable this argument, set the SensorArray property to an array that contains subarrays and set the SubarraySteering property of the array to 'Custom', and H.IncludeElementResponse is true.

## Output Arguments

## SV

Steering vector. The form of the steering vector depends upon whether the EnablePolarization property is set to true or false.

- If EnablePolarization is set to false, the steering vector, SV, has the dimensions $N$-by- $M$-by$L$. The first dimension, $N$, is the number of elements of the phased array. If H.SensorArray contains subarrays, $N$ is the number of subarrays. Each column of SV contains the steering vector of the array for the corresponding direction specified in ANG. Each of the $L$ pages of SV contains the steering vectors of the array for the corresponding frequency specified in FREQ.

If you set the H . IncludeElementResponse property to true, the steering vector includes the individual element responses. If you set the H. IncludeElementResponse property to false, the elements are assumed to be isotropic. Then, the steering vector does not include individual element responses.

- If EnablePolarization is set to true, SV is a MATLAB struct containing two fields, SV.H and SV.V. These fields represent the steering vector horizontal and vertical polarization components. Each field has the dimensions $N$-by- $M$-by- $L$. The first dimension, $N$, is the number of elements of the phased array. If H . SensorArray contains subarrays, $N$ is the number of subarrays. Each column of SV contains the steering vector of the array for the corresponding direction specified in

ANG. Each of the $L$ pages of SV contains the steering vectors of the array for the corresponding frequency specified in FREQ.

If you set EnablePolarization to false for an array that supports polarization, then all polarization information is discarded. The combined pattern from both H and V polarizations is used at each element to compute the steering vector.

Simulating polarization also requires that the sensor array specified in the SensorArray property can simulate polarization, and the IncludeElementResponse property is set to true.

## Examples

## Steering Vector for Uniform Linear Array

Calculate the steering vector for a uniform linear array in the direction of $30^{\circ}$ azimuth and $20^{\circ}$ elevation. Assume the array operates at 300 MHz .

```
array = phased.ULA('NumElements',2);
steeringvector = phased.SteeringVector('SensorArray',array);
fc = 300.0e6;
ang = [30;20];
sv = steeringvector(fc,ang);
```

```
See Also
uv2azel|phitheta2azel
```


# phased.SteppedFMWaveform 

Package: phased
Stepped FM pulse waveform

## Description

The SteppedFMWaveform object creates a stepped FM pulse waveform.
To obtain waveform samples:
1 Define and set up your stepped FM pulse waveform. See "Construction" on page 1-1626.
2 Call step to generate the stepped FM pulse waveform samples according to the properties of phased.SteppedFMWaveform. The behavior of step is specific to each object in the toolbox.

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step (obj, x) and $y=o b j(x)$ perform equivalent operations. When the only argument to the step method is the System object itself, replace $y=\operatorname{step}(o b j)$ by $y=o b j()$.

## Construction

sSFM = phased.SteppedFMWaveform creates a stepped FM pulse waveform System object, sSFM. The object generates samples of a linearly stepped FM pulse waveform.
sSFM = phased.SteppedFMWaveform(Name,Value) creates a stepped FM pulse waveform object, sSFM, with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN).

## Properties

## SampleRate

Sample rate
Signal sample rate, specified as a positive scalar. Units are Hertz. The ratio of sample rate to pulse repetition frequency (PRF) must be a positive integer - each pulse must contain an integer number of samples.

Default: 1e6

## DurationSpecification

Method to set pulse duration
Method to set pulse duration (pulse width), specified as 'Pulse width' or 'Duty cycle'. This property determines how you set the pulse duration. When you set this property to 'Pulse width', then you set the pulse duration directly using the PulseWidth property. When you set this property
to 'Duty cycle', you set the pulse duration from the values of the PRF and DutyCycle properties. The pulse width is equal to the duty cycle divided by the $P R F$.

Default: 'Pulse width'

## PulseWidth

Pulse width
Specify the length of each pulse (in seconds) as a positive scalar. The value must satisfy PulseWidth < $=1 . /$ PRF.

Default: 50e-6
DutyCycle
Waveform duty cycle
Waveform duty cycle, specified as a scalar from 0 to 1 , exclusive. This property applies when you set the DurationSpecification property to 'Duty cycle'. The pulse width is the value of the DutyCycle property divided by the value of the PRF property.

Default: 0.5
PRF
Pulse repetition frequency
Pulse repetition frequency, $P R F$, specified as a scalar or a row vector. Units are in Hz . The pulse repetition interval, $P R I$, is the inverse of the pulse repetition frequency, $P R F$. ThePRF must satisfy these restrictions:

- The product of PRF and PulseWidth must be less than or equal to one. This condition expresses the requirement that the pulse width is less than one pulse repetition interval. For the phasecoded waveform, the pulse width is the product of the chip width and number of chips.
- The ratio of sample rate to any element of PRF must be an integer. This condition expresses the requirement that the number of samples in one pulse repetition interval is an integer.

You can select the value of $P R F$ using property settings alone or using property settings in conjunction with the prfidx input argument of the step method.

- When PRFSelectionInputPort is false, you set the PRF using properties only. You can
- implement a constant PRF by specifying PRF as a positive real-valued scalar.
- implement a staggered $P R F$ by specifying PRF as a row vector with positive real-valued entries. Then, each call to the step method uses successive elements of this vector for the PRF. If the last element of the vector is reached, the process continues cyclically with the first element of the vector.
- When PRFSelectionInputPort is true, you can implement a selectable $P R F$ by specifying PRF as a row vector with positive real-valued entries. But this time, when you execute the step method, select a $P R F$ by passing an argument specifying an index into the $P R F$ vector.

In all cases, the number of output samples is fixed when you set the OutputFormat property to 'Samples'. When you use a varying PRF and set the OutputFormat property to 'Pulses', the number of samples can vary.

Default: 10e3
PRFSelectionInputPort
Enable PRF selection input
Enable the PRF selection input, specified as true or false. When you set this property to false, the step method uses the values set in the PRF property. When you set this property to true, you pass an index argument into the step method to select a value from the PRF vector.

Default: false
FrequencyStep
Linear frequency step size
Specify the linear frequency step size (in hertz) as a positive scalar. The default value of this property corresponds to 20 kHz .

Default: 20e3

## NumSteps

Specify the number of frequency steps as a positive integer. When NumSteps is 1 , the stepped FM waveform reduces to a rectangular waveform.

## Default: 5

FrequencyOffsetSource
Source of frequency offset
Source of frequency offset for the waveform, specified as 'Property' or 'Input port'.

- When you set this property to 'Property', the offset is determined by the value of the FrequencyOffset property.
- When you set this property to 'Input port', the FrequencyOffset is determined by the freqoffset input argument.

Default: 'Property'
FrequencyOffset
Frequency offset
Frequency offset in Hz , specified as a scalar.

## Dependencies

This property applies when you set the FrequencyOffsetSource property to 'Input port '.
Default: 0 Hz

## OutputFormat

Output signal format

Specify the format of the output signal as 'Pulses' or 'Samples'. When you set the OutputFormat property to 'Pulses', the output of the step method takes the form of multiple pulses specified by the value of the NumPulses property. The number of samples per pulse can vary if you change the pulse repetition frequency during the simulation.

When you set the OutputFormat property to 'Samples', the output of the step method is in the form of multiple samples. In this case, the number of output signal samples is the value of the NumSamples property and is fixed.

Default: 'Pulses'

## NumSamples

Number of samples in output
Specify the number of samples in the output of the step method as a positive integer. This property applies only when you set the OutputFormat property to 'Samples'.

Default: 100

## NumPulses

Number of pulses in output
Specify the number of pulses in the output of the step method as a positive integer. This property applies only when you set the OutputFormat property to 'Pulses'.

## Default: 1

## PRFOutputPort

Set this property to true to output the PRF for the current pulse using a step method argument.

## Dependencies

This property can be used only when the OutputFormat property is set to 'Pulses '.
Default: false

## CoefficientsOutputPort

Enable matched filter coefficients output port
Enable the matched filter coefficients output port, specified as false or true. When you set this property to false, the object does not provide the matched filter coefficients used during the simulation as an output. When you set this property to true, the object provides the matched filter coefficients used during the simulation as an output.

Default: false

## Methods

| bandwidth | Bandwidth of stepped FM pulse waveform |
| :--- | :--- |
| getMatchedFilter | Matched filter coefficients for waveform |
| plot | Plot stepped FM pulse waveform |
| reset | Reset state of stepped FM pulse waveform object |
| step | Samples of stepped FM pulse waveform |

## Common to All System Objects

| release | Allow System object property value changes |
| :--- | :--- |

## Examples

## Plot Stepped-FM Waveform and Spectrum

Create a stepped frequency pulse waveform object. Assume the default value, 1 MHz , for the sample rate. Then, plot the waveform.

Create the SteppedFMWaveform System object ${ }^{\text {TM }}$ with 20 kHz frequency step size.
sSFM = phased.SteppedFMWaveform('NumSteps',3,'FrequencyStep',20e3);
fs = sSFM.SampleRate;
Plot the third pulse of the wave using the phased. SteppedFMWaveform. plot method. Pass in the pulse number using the 'PulseIdx' name-value pair.
plot(sSFM,'PulseIdx',3);


Alternatively, call the step method three times to obtain three pulses. Collect the three pulses in a single time series. Then plot the waveform using the plot function. You can see the full duty cycles of the pulses.

```
wavfull = [];
wav = step(sSFM);
wavfull = [wavfull;wav];
wav = step(sSFM);
wavfull = [wavfull;wav];
wav = step(sSFM);
wavfull = [wavfull;wav];
nsamps = size(wavfull,1);
t = [0:(nsamps-1)]/fs*le6;
plot(t,real(wavfull))
xlabel('Time (\mu sec)')
ylabel('Amplitude')
grid
```



Plot the spectrum using the spect rogram function. Assume an fft of 64 samples and a $50 \%$ overlap. Window the signal with a hamming function.

```
nfft1 = 64;
nov = floor(0.5*nfft1);
spectrogram(wavfull,hamming(nfft1),nov,nfft1,fs,'centered','yaxis')
```



## Apply Frequency Offset to Stepped FM Waveform

Apply a frequency offset to a stepped FM (SFM) pulse waveform. Plot the frequency spectrum of the waveform with and without a frequency offset applied.

Create an SFM waveform object which is configured to set the frequency offset from an input when the object is executed.

```
fs = 1e6;
```

```
sfmwav = sSFM(0);
```

sfmwav = sSFM(0);
sfmwav_foffset = sSFM(2e4);

```
sfmwav_foffset = sSFM(2e4);
```

sSFM = phased.SteppedFMWaveform('SampleRate',fs,'NumSteps',2, ...
'FrequencyStep',20e3,'NumPulses',2,'FrequencyOffsetSource','Input port');

Execute the object two times. First set the frequency offset set to 0 Hz , and then to 2 e 4 Hz .

Plot the frequency spectrum of the complex signals. The frequency offset signal is shifted to the right.

```
[Pxx,f] = pwelch(sfmwav,[],[],[],fs,'centered');
[Pxx_offset,foffset] = pwelch(sfmwav_foffset,[],[],[],fs,'centered');
plot(f/1000,Pxx,foffset/1000,Pxx_offset)
ylabel('PSD');
xlabel('Frequency (kHz)');
```

legend(\{'No offset','Offset applied'\},'Location','northwest'); grid on;


## More About

## Stepped FM Waveform

In a stepped FM waveform, a group of pulses together sweep a certain bandwidth. Each pulse in this group occupies a given center frequency and these center frequencies are uniformly located within the total bandwidth.

## Version History

Introduced in R2011a

## References

[1] Richards, M. A. Fundamentals of Radar Signal Processing. New York: McGraw-Hill, 2005.

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

Usage notes and limitations:

- The plot method is not supported.
- See "System Objects in MATLAB Code Generation" (MATLAB Coder).


## See Also

phased. LinearFMWaveform | phased. RectangularWaveform | phased. PhaseCodedWaveform

## Topics

"Waveform Analysis Using the Ambiguity Function"

## bandwidth

System object: phased.SteppedFMWaveform
Package: phased
Bandwidth of stepped FM pulse waveform

## Syntax

BW = bandwidth(H)

## Description

$\mathrm{BW}=$ bandwidth(H) returns the bandwidth (in hertz) of the pulses for the stepped FM pulse waveform H . If there are N frequency steps, the bandwidth equals N times the value of the
FrequencyStep property. If there is no frequency stepping, the bandwidth equals the reciprocal of the pulse width.

## Input Arguments

## H

Stepped FM pulse waveform object.

## Output Arguments

## BW

Bandwidth of the pulses, in hertz.

## Examples

## Bandwidth of Stepped FM Waveform

Determine the bandwidth of a stepped FM waveform.

```
waveform = phased.SteppedFMWaveform;
bw = bandwidth(waveform)
bw = 100000
```


## getMatchedFilter

System object: phased.SteppedFMWaveform
Package: phased
Matched filter coefficients for waveform

## Syntax

Coeff = getMatchedFilter(H)
Coeff = getMatchedFilter(H,'FrequencyOffset',FOFFSET)

## Description

Coeff $=$ getMatchedFilter $(H)$ returns the matched filter coefficients for the stepped FM waveform object H . Coeff is a matrix whose columns correspond to the different frequency pulses in the stepped FM waveform.

Coeff = getMatchedFilter (H,'FrequencyOffset', FOFFSET) adds a frequency offset when matched filter coefficients are generated. FOFFSET must be a scalar. This option is available when you set the FrequencyOffsetSource property to 'Input port' for the input object, H.

## Examples

## Matched Filter Coefficients for Stepped FM Pulse

Get the matched filter coefficients for a stepped FM pulse waveform.

```
waveform = phased.SteppedFMWaveform(...
    'NumSteps',3,'FrequencyStep',2e4,...
    'OutputFormat','Pulses','NumPulses',3);
coeff = getMatchedFilter(waveform);
```

Show the first four coefficients for each step.

```
coeff(1:4,:)
ans = 4×3 complex
```

| $1.0000+0.0000 i$ | $0.9921+0.1253 i$ | $0.9686+0.2487 i$ |
| :--- | :--- | :--- |
| $1.0000+0.0000 i$ | $0.9686+0.2487 i$ | $0.8763+0.4818 i$ |
| $1.0000+0.0000 i$ | $0.9298+0.3681 i$ | $0.7290+0.6845 i$ |
| $1.0000+0.0000 i$ | $0.8763+0.4818 i$ | $0.5358+0.8443 i$ |

## plot

System object: phased.SteppedFMWaveform
Package: phased
Plot stepped FM pulse waveform

## Syntax

```
plot(Hwav)
plot(Hwav,Name,Value)
plot(Hwav,Name,Value,LineSpec)
h = plot(
```

$\qquad$

``` )
```


## Description

plot (Hwav) plots the real part of the waveform specified by Hwav.
plot (Hwav, Name, Value) plots the waveform with additional options specified by one or more Name, Value pair arguments.
plot (Hwav, Name, Value, LineSpec) specifies the same line color, line style, or marker options as are available in the MATLAB plot function.
h = plot( $\qquad$ ) returns the line handle in the figure.

## Input Arguments

## Hwav

Waveform object. This variable must be a scalar that represents a single waveform object.

## LineSpec

Character vector to specifies the same line color, style, or marker options as are available in the MATLAB plot function. If you specify a PlotType value of ' complex', then LineSpec applies to both the real and imaginary subplots.

Default: 'b'

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## PlotType

Specifies whether the function plots the real part, imaginary part, or both parts of the waveform. Valid values are 'real','imag', and 'complex'.

Default: 'real'

## PulseIdx

Index of the pulse to plot. This value must be a scalar.
Default: 1
Frequency0ffset
Frequency offset
Frequency offset in Hz , specified as a scalar.

## Dependencies

This property applies when you set the FrequencyOffsetSource property to 'Input port '.
Default: 0 Hz

## Output Arguments

## h

Handle to the line or lines in the figure. For a PlotType value of 'complex', h is a column vector. The first and second elements of this vector are the handles to the lines in the real and imaginary subplots, respectively.

## Examples

## Plot Stepped FM Waveform

Create and plot a stepped frequency pulse waveform.

```
waveform = phased.SteppedFMWaveform('NumSteps',3);
plot(waveform);
```



## reset

System object: phased.SteppedFMWaveform
Package: phased
Reset state of stepped FM pulse waveform object

## Syntax

reset (H)

## Description

reset $(\mathrm{H})$ resets the states of the SteppedFMWaveform object, H . Afterward, if the PRF property is a vector, the next call to step uses the first PRF value in the vector.

## step

## System object: phased. SteppedFMWaveform <br> Package: phased

Samples of stepped FM pulse waveform

## Syntax

```
Y = step(sSFM)
Y = step(sSFM, prfidx)
Y = step(sRFM,freqoffset)
[Y,PRF] = step(
```

$\qquad$

``` )
[Y,COEFF] = step(
``` \(\qquad\)

\section*{Description}

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step \((o b j, x)\) and \(y=o b j(x)\) perform equivalent operations. When the only argument to the step method is the System object itself, replace \(y=\operatorname{step}(o b j)\) by \(y=o b j()\).
\(\mathrm{Y}=\) step (sSFM) returns samples of the stepped FM pulses in a column vector, Y . The output, Y , results from increasing the frequency of the preceding output by an amount specified by the FrequencyStep property. If the total frequency increase is larger than the value specified by the SweepBandwidth property, the samples of a rectangular pulse are returned.
\(Y=\) step(sSFM, prfidx), uses the prfidx index to select the PRF from the predefined vector of values specified by in the PRF property. This syntax applies when you set the PRFSelectionInputPort property to true.

Y = step(sRFM, freqoffset), uses the freqoffset to generate the waveform with an offset as specified at step time. Use this syntax for cases where the transmit pulse frequency needs to be dynamically updated. This syntax applies when you set the FrequencyOffsetSource property to 'Input port'.
[Y, PRF] = step( \(\qquad\) ) also returns the current pulse repetition frequency, PRF. To enable this syntax, set the PRFOutputPort property to true and set the OutputFormat property to 'Pulses'.
\([Y\), COEFF \(]=\operatorname{step}(\ldots \quad)\) returns the matched filter coefficients, COEFF, for the current pulse. To enable this syntax, set CoefficientsOutputPort to true. COEFF is returned as either an \(N_{Z}\)-by-1 vector or an \(N_{Z}\)-by-M matrix.
- An \(N_{Z}\)-by-1 vector is returned when the object has OutputFormat set to 'Pulses ' and NumPulses is equal to \(1 . N_{Z}\) is the pulse width.
- An \(N_{\mathrm{Z}}\)-by-M matrix is returned when either OutputFormat set to 'Pulses' and NumPulses is greater than 1, or OutputFormat is set to 'Samples'.
- When the object generates a constant pulse width waveform (DurationSpecification set to 'Pulse width' or 'Duty cycle' and PRF has one unique value), \(N_{\mathrm{Z}}\) is the pulse width and \(M\) is the number of sub-pulses, NumSteps.
- When the object generates a varying pulse width waveform (DurationSpecification is set to 'Duty cycle' and PRF has more than one unique value), \(N_{\mathrm{Z}}\) is the maximum of the pulse width and \(M\) is the product of NumSteps and the number of unique PRFs.

You can combine optional input and output arguments when their enabling properties are set. Optional inputs and outputs must be listed in the same order as the order of the enabling properties. For example, [Y, PRF,COEFF] = step(sRFM, prfidx,freqoffset).

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

\section*{Examples}

\section*{Create Stepped Frequency Pulse Waveform}

Create a stepped frequency pulse waveform object with a frequency step of 40 kHz and four frequency steps.
```

waveform = phased.SteppedFMWaveform(...
'NumSteps',4,'FrequencyStep',40e3,...
'OutputFormat','Pulses','NumPulses',1);
fs = waveform.SampleRate;

```

Use the waveform method to obtain the pulses.
First, generate pulse 1.
```

pulse1 = waveform();

```

Then, generate pulse 2, incremented by the frequency step 40 kHz .
```

pulse2 = waveform();

```

Next, generate pulse 3, incremented by the frequency step 40 kHz .
```

pulse3 = waveform();

```

Finally, generate pulse 4, incremented by the frequency step 40 kHz .
```

pulse4 = waveform();
nsamps = size(pulse4,1);
t = [0:(nsamps-1)]/fs*1e6;
plot(t,real(pulse4))
xlabel('Time (\mu sec)')
ylabel('Amplitude')
grid

```


\section*{Generate Matched Filter Coefficients of Stepped FM Pulse Waveform}

Generate output samples and matched filter coefficients of a stepped FM pulse waveform.
```

waveform = phased.SteppedFMWaveform('NumSteps',2,'NumPulses',1,...
'CoefficientsOutputPort',true,'PRF',[1e4 1e4 2e4 2e4],...
'DurationSpecification','Duty cycle','DutyCycle',0.5);
[wav1,coeff1] = waveform();
[wav2,coeff2] = waveform();
wav = [wav1 ; wav2];

```

Create a matched filter that applies the coefficients as an input argument. Use the coefficients when applying the matched filter to the waveform. Plot the waveform and matched filter outputs.
```

mf = phased.MatchedFilter('CoefficientsSource','Input port');
mf0ut1 = mf(wav1,coeff1);
mf0ut2 = mf(wav2,coeff2);
subplot(211),plot(real(wav));
xlabel('Samples'),ylabel('Amplitude'),title('Waveform Output');
subplot(212),plot(abs(mf0ut1+mf0ut2));
xlabel('Samples'),ylabel('Amplitude'),title('Matched Filter Output');

```


\section*{More About}

\section*{Stepped FM Waveform}

In a stepped FM waveform, a group of pulses together sweep a certain bandwidth. Each pulse in this group occupies a given center frequency and these center frequencies are uniformly located within the total bandwidth.

\section*{phased.StretchProcessor}

Package: phased
Stretch processor for linear FM waveform

\section*{Description}

The StretchProcessor object performs stretch processing on data from a linear FM waveform.
To perform stretch processing:
1 Define and set up your stretch processor. See "Construction" on page 1-1646.
2 Call step to perform stretch processing on input data according to the properties of phased. StretchProcessor. The behavior of step is specific to each object in the toolbox.

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step \((o b j, x)\) and \(y=o b j(x)\) perform equivalent operations.

\section*{Construction}

H = phased.StretchProcessor creates a stretch processor System object, H. The object performs stretch processing on data from a linear FM waveform.

H = phased.StretchProcessor(Name, Value) creates a stretch processor object, H, with additional options specified by one or more Name, Value pair arguments. Name is a property name on page 1-1646, and Value is the corresponding value. Name must appear inside single quotes ( ' ' ). You can specify several name-value pair arguments in any order as Name1, Value1, ..., NameN , ValueN.

\section*{Properties}

\section*{SampleRate}

Sample rate
Signal sample rate, specified as a positive scalar. Units are Hertz. The ratio of sample rate to pulse repetition frequency (PRF) must be a positive integer - each pulse must contain an integer number of samples. This property can be specified as single or double precision.

Default: 1e6

\section*{PulseWidth}

Pulse width
Specify the length of each pulse (in seconds) as a positive scalar. The value must satisfy PulseWidth \(<=1\)./PRF. This property can be specified as single or double precision.

Default: 50e-6

\section*{PRFSource}

Source of pulse repetition values
Source of the PRF values for the stretch processor, specified as 'Property', 'Auto', or 'Input port'. When you set this property to 'Property', the PRF is determined by the value of the PRF property. When you set this property to 'Input port', the PRF is determined by an input argument to the step method at execution time. When you set this property to 'Auto', the PRF is computed from the number of rows in the input signal.

Default: 'Property'
PRF
Pulse repetition frequency
Pulse repetition frequency (PRF) of the received signal, specified as a positive scalar. Units are in Hertz. This property can be specified as single or double precision.

\section*{Dependencies}

To enable this property, set the PRFSource property to 'Property'.

\section*{Default: 1}

\section*{SweepSlope}

FM sweep slope
Specify the slope of the linear FM sweeping, in hertz per second, as a scalar.
Default: 2e9

\section*{SweepInterval}

Location of FM sweep interval
Specify the linear FM sweeping interval using the value 'Positive' or 'Symmetric'. If SweepInterval is 'Positive', the waveform sweeps in the interval between 0 and B, where B is the sweep bandwidth. If SweepInterval is 'Symmetric', the waveform sweeps in the interval between \(-B / 2\) and \(B / 2\). This property can be specified as single or double precision.

Default: 'Positive'
PropagationSpeed
Signal propagation speed
Specify the propagation speed of the signal, in meters per second, as a positive scalar. You can specify this property as single or double precision.

Default: Speed of light

\section*{ReferenceRange}

Reference range of stretch processing

Specify the center of ranges of interest, in meters, as a positive scalar. The reference range must be within the unambiguous range of one pulse. This property can be specified as single or double precision. This property is tunable.

Default: 5000

\section*{RangeSpan}

Span of ranges of interest
Specify the length of the interval for ranges of interest, in meters, as a positive scalar. The range span is centered at the range value specified in the ReferenceRange property. This property can be specified as single or double precision.

Default: 500

\section*{Methods}
step Perform stretch processing for linear FM waveform

\section*{Common to All System Objects}
release \(\quad\) Allow System object property value changes

\section*{Examples}

\section*{Detect a Target Using Stretch Processing}

Use stretch processing to locate a target at a range of 4950 m .
Simulate the signal.
```

waveform = phased.LinearFMWaveform;
x = waveform();
c = physconst('LightSpeed');
rng = 4950.0;
num_samples = round(rng/(c/(2*waveform.SampleRate)));
x = circshift(x,num_samples);

```

Perform stretch processing.
```

stretchproc = getStretchProcessor(waveform,5000,200,c);
y = stretchproc(x);

```

Plot the spectrum of the resulting signal.
```

[Pxx,F] = periodogram(y,[],2048,stretchproc.SampleRate,'centered');
plot(F/1000,10*log10(Pxx))
grid
xlabel('Frequency (kHz)')
ylabel('Power/Frequency (dB/Hz)')
title('Periodogram Power Spectrum Density Estimate')

```


Detect the range.
```

[~,rngidx] = findpeaks(pow2db(Pxx/max(Pxx)),'MinPeakHeight',-5);
rngfreq = F(rngidx);
rng = stretchfreq2rng(rngfreq,stretchproc.SweepSlope,stretchproc.ReferenceRange,c)
rng = 4.9634e+03

```

\section*{Algorithms}

\section*{Data Precision}

This System object supports single and double precision for input data, properties, and arguments. If the input data X is single precision, the output data is single precision. If the input data X is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

\section*{Version History}

Introduced in R2012a

\section*{References}
[1] Richards, M. A. Fundamentals of Radar Signal Processing. New York: McGraw-Hill, 2005.

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® \({ }^{\circledR}\) Coder \(^{\mathrm{TM}}\).
Usage notes and limitations:
- See "System Objects in MATLAB Code Generation" (MATLAB Coder).
- This System object supports single and double precision for input data, properties, and arguments. If the input data \(X\) is single precision, the output data is single precision. If the input data \(X\) is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

\section*{See Also}
phased.LinearFMWaveform|phased.MatchedFilter|stretchfreq2rng
Topics
Range Estimation Using Stretch Processing
"Stretch Processing"

\section*{step}

System object: phased.StretchProcessor
Package: phased
Perform stretch processing for linear FM waveform

\section*{Syntax}
\(Y=\operatorname{step}(H, X)\)
Y = step(H,X,PRF)

\section*{Description}

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step \((o b j, x)\) and \(y=o b j(x)\) perform equivalent operations.
\(Y=\operatorname{step}(H, X)\) applies stretch processing along the first dimension of \(X\). Each column of \(X\) represents one receiving pulse.
\(\mathrm{Y}=\) step ( \(\mathrm{H}, \mathrm{X}, \mathrm{PRF}\) ) uses PRF as the pulse repetition frequency. This syntax is available when the PRFSource property is 'Input port'.

\section*{Input Arguments}

\section*{H}

Stretch processor object.

\section*{X}

Input signal matrix. Each column represents one received pulse.
The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

\section*{PRF}

Pulse repetition frequency specified as a positive scalar. To enable this argument, set the PRFSource property to 'Input port'. Units are in Hertz.

\section*{Output Arguments}

\section*{Y}

Result of stretch processing. The dimensions of \(Y\) match the dimensions of \(X\).

\section*{Examples}

\section*{Detect a Target Using Stretch Processing}

Use stretch processing to locate a target at a range of 4950 m .
Simulate the signal.
```

waveform = phased.LinearFMWaveform;
x = waveform();
c = physconst('LightSpeed');
rng = 4950.0;
num_samples = round(rng/(c/(2*waveform.SampleRate)));
x = circshift(x,num_samples);

```

Perform stretch processing.
```

stretchproc = getStretchProcessor(waveform,5000,200,c);

```
y = stretchproc(x);

Plot the spectrum of the resulting signal.
```

[Pxx,F] = periodogram(y,[],2048,stretchproc.SampleRate,'centered');
plot(F/1000,10*log10(Pxx))
grid
xlabel('Frequency (kHz)')
ylabel('Power/Frequency (dB/Hz)')
title('Periodogram Power Spectrum Density Estimate')

```


Detect the range.
```

[~,rngidx] = findpeaks(pow2db(Pxx/max(Pxx)),'MinPeakHeight',-5);
rngfreq = F(rngidx);
rng = stretchfreq2rng(rngfreq,stretchproc.SweepSlope,stretchproc.ReferenceRange,c)
rng = 4.9634e+03

```

\section*{See Also}
stretchfreq2rng

\section*{Topics}

Range Estimation Using Stretch Processing "Stretch Processing"

\title{
phased.SubbandMVDRBeamformer
}

\author{
Package: phased
}

Wideband minimum-variance distortionless-response beamformer

\section*{Description}

The phased. SubbandMVDRBeamformer System object implements a wideband minimum variance distortionless response beamformer (MVDR) based on the subband processing technique. This type of beamformer is also called a Capon beamformer.

To beamform signals arriving at an array:
1 Create the phased. SubbandMVDRBeamformer object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

\section*{Creation}

\section*{Syntax}
beamformer = phased.SubbandMVDRBeamformer
beamformer \(=\) phased.SubbandMVDRBeamformer(Name,Value)

\section*{Description}
beamformer = phased.SubbandMVDRBeamformer creates a subband MVDR beamformer System object, beamformer. The object performs subband MVDR beamforming on the received signal.
beamformer \(=\) phased.SubbandMVDRBeamformer(Name, Value) creates a subband MVDR beamformer System object, beamformer, with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as Name1,Value1,...,NameN,ValueN.

Example: beamformer = phased.SubbandMVDRBeamformer('SensorArray', phased.URA('Size', [5
5]), 'OperatingFrequency ' ,500e6) sets the sensor array to a 5 -by-5 uniform rectangular array (URA) with all other default URA property values. The beamformer has an operating frequency of 500 MHz.

\section*{Properties}

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.

For more information on changing property values, see System Design in MATLAB Using System Objects.

\section*{SensorArray - Sensor array}
phased. ULA array with default property values (default) | Phased Array System Toolbox array
Sensor array, specified as an array System object belonging to Phased Array System Toolbox. The sensor array can contain subarrays.

Example: phased.URA
PropagationSpeed - Signal propagation speed
physconst('LightSpeed') (default) | real-valued positive scalar
Signal propagation speed, specified as a real-valued positive scalar. Units are in meters per second. The default propagation speed is the value returned by physconst ('LightSpeed').
Example: 3e8
Data Types: single | double

\section*{OperatingFrequency - Operating frequency}

300e6 (default) | positive scalar
Operating frequency, specified as a positive scalar. Units are in Hz .
Example: 1e9
Data Types: single|double

\section*{SampleRate - Sample rate of signal}

1e6 (default) | positive scalar
Sample rate of signal, specified as a positive scalar. Units are in Hz. The System object uses this quantity to calculate the propagation delay in units of samples.
Example: 1e6
Data Types: single | double

\section*{NumSubbands - Number of processing subbands}

64 (default) | positive integer
Number of processing subbands, specified as a positive integer.
Example: 128
Data Types: double

\section*{DirectionSource - Source of beamforming direction}
'Property' (default)|'Input port'
Source of beamforming direction, specified as 'Property' or 'Input port'. Specify whether the beamforming direction comes from the Direction property of this object or from the input argument, ANG. Values of this property are:
\begin{tabular}{|l|l} 
'Property' & \begin{tabular}{l} 
Specify the beamforming direction using the Direction \\
property.
\end{tabular} \\
\hline
\end{tabular}
'Input port' \(\quad\) Specify the beamforming direction using the input argument, ANG.

\section*{Data Types: char}

\section*{Direction - Beamforming directions}
[0;0] (default) | real-valued 2-by-1 vector | real-valued 2-by-L matrix
Beamforming directions, specified as a real-valued 2-by-1 vector or a real-valued 2-by-L matrix. For a matrix, each column specifies a different beamforming direction. Each column has the form [AzimuthAngle;ElevationAngle]. Azimuth angles must lie between \(-180^{\circ}\) and \(180^{\circ}\) and elevation angles must lie between \(-90^{\circ}\) and \(90^{\circ}\). All angles are defined with respect to the local coordinate system of the array. Units are in degrees.
Example: [40;30]

\section*{Dependencies}

To enable this property, set the DirectionSource property to 'Property'.
Data Types: single | double

\section*{DiagonalLoadingFactor - Diagonal loading factor}

0 (default) | nonnegative scalar
Diagonal loading factor, specified as a nonnegative scalar. Diagonal loading is a technique used to achieve robust beamforming performance, especially when the sample size is small. A small sample size can lead to an inaccurate estimate of the covariance matrix. Diagonal loading also provides robustness due to steering vector errors. The diagonal loading technique adds a positive scalar multiple of the identity matrix to the sample covariance matrix.

Tunable: Yes
Data Types: single | double
TrainingInputPort - Enable training data input
false (default) | true
Enable training data input, specified as false or true. When you set this property to true, use the training data input argument, XT , when running the object. Set this property to false to use the input data, X , as the training data.
Data Types: logical

\section*{WeightsOutputPort - Enable beamforming weights output false (default) | true}

Enable the output of beamforming weights, specified as false or true. To obtain the beamforming weights, set this property to true and use the corresponding output argument, W. If you do not want to obtain the weights, set this property to false.

\section*{Data Types: logical}

\section*{SubbandsOutputPort - Option to enable output of subband center frequencies false (default) | true}

Option to enable output of subband center frequencies, specified as either true or false. To obtain the subband center frequencies, set this property to true and use the corresponding output argument FREQS when calling the object.

\section*{Data Types: logical}

\section*{Usage}

\section*{Syntax}
\(\mathrm{Y}=\) beamformer \((\mathrm{X})\)
\(Y=\) beamformer \((X, X T)\)
Y = beamformer(X,ANG)
\([\mathrm{Y}, \mathrm{W}]=\) beamformer (__ )
[Y,FREQS] = beamformer( \(\qquad\)
[Y,W,FREQS] = beamformer(X,XT,ANG)

\section*{Description}
\(Y\) = beamformer \((X)\) performs wideband MVDR beamforming on the input, \(X\), and returns the beamformed output in \(Y\). This syntax uses \(X\) for training samples to calculate the beamforming weights. Use the Direction property to specify the beamforming direction.
\(Y=\) beamformer \((X, X T)\) uses \(X T\) for training samples to calculate the beamforming weights.
Y = beamformer(X, ANG) uses ANG as the beamforming direction. This syntax applies when you set the DirectionSource property to 'Input port'.
\([\mathrm{Y}, \mathrm{W}]=\) beamformer (__ ) returns the beamforming weights, W . This syntax applies when you set the WeightsOutputPort property to true.
[ \(\mathrm{Y}, \mathrm{FREQS}]=\) beamformer \((\ldots \quad\) ) returns the center frequencies of the subbands, FREQS. This syntax applies when you set the SubbandsOutputPort property to true.

You can combine optional input arguments when you set their enabling properties. Optional input arguments must be listed in the same order as their enabling properties. For example, [ \(\mathrm{Y}, \mathrm{W}, \mathrm{FREQS}\) ] \(=\) beamformer (X,XT, ANG) is valid when you specify TrainingInputPort as true and set DirectionSource to 'Input port'.

\section*{Input Arguments}

\section*{X - Wideband input signal}
\(M\)-by- \(N\) complex-valued matrix
Wideband input signal, specified as an \(M\)-by- \(N\) matrix, where \(N\) is the number of array elements. \(M\) is the number of samples in the data. If the sensor array consists of subarrays, \(N\) is then the number of subarrays.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

If you set the TrainingInputPort to false, then the object uses \(X\) as training data. In this case, the dimension \(M\) must be greater than \(N \times N B\). where \(N B\) is the number of subbands specified in the NumSubbands.

If you set TrainingInputPort to true, use the XT argument to supply training data. In this case, the dimension \(M\) can be any positive integer.

Example: [1, 1; j, 1;0.5,0]
Data Types: single | double
Complex Number Support: Yes

\section*{XT - Wideband training samples}
\(P\)-by- \(N\) complex-valued matrix
Wideband training samples, specified as a \(P\)-by- \(N\) matrix where \(N\) is the number of elements. If the sensor array consists of subarrays, then \(N\) represents the number of subarrays.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

This argument applies when you set TrainingInputPort to true. The dimension \(P\) is the number of samples in the training data. \(P\) must be larger than \(N \times N B\), where \(N B\) is the number of subbands specified in the NumSubbands property.
Example: FT \(=[1,1 ; j, 1 ; 0.5,0]\)
Data Types: single | double
Complex Number Support: Yes

\section*{ANG - Beamforming direction}

\section*{2-by-L real-valued matrix}

Beamforming direction, specified as a 2 -by- \(L\) real-valued matrix, where \(L\) is the number of beamforming directions. This argument applies only when you set the DirectionSource property to 'Input port'. Each column takes the form of [AzimuthAngle; ElevationAngle]. Angle units are in degrees. The azimuth angle must lie between \(-180^{\circ}\) and \(180^{\circ}\). The elevation angle must lie between \(-90^{\circ}\) and \(90^{\circ}\). Angles are defined with respect to the local coordinate system of the array.

Example: [40 30;0 10]
Data Types: single | double

\section*{Output Arguments}

\section*{Y - Beamformed output}

M-by-L complex-valued matrix
Beamformed output, returned as an \(M\)-by- \(L\) complex-valued matrix. The quantity \(M\) is the number of signal samples and \(L\) is the number of beamforming directions specified in the ANG argument.

\section*{W - Beamforming weights}
\(N\)-by-K-by-L complex-valued matrix
Beamforming weights, returned as an \(N\)-by- \(K\)-by- \(L\) complex-valued matrix. The quantity \(N\) is the number of sensor elements or subarrays and \(K\) is the number of subbands specified by the

NumSubbands property. The quantity \(L\) is the number of beamforming directions. Each column of W contains the narrowband beamforming weights used in the corresponding subband for the corresponding directions.

\section*{Dependencies}

To return this output, set the WeightsOutputPort property to true.
Data Types: single | double
FREQS - Center frequencies of subbands
K-by-1 real-valued column vector
Center frequencies of subbands, returned as a \(K\)-by- 1 real-valued column vector. The quantity \(K\) is the number of subbands specified by the NumSubbands property.

\section*{Dependencies}

To return this output, set the SubbandsOutputPort property to true.
```

Data Types: single | double

```

\section*{Object Functions}

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:
release(obj)

\section*{Common to All System Objects}
step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object

\section*{Examples}

\section*{Subband MVDR Beamforming of ULA}

Apply subband MVDR beamforming to an underwater acoustic 11-element ULA. The incident angle of the signal is \(10^{\circ}\) azimuth and \(30^{\circ}\) elevation. The signal is an FM chirp having a bandwidth of 1 kHz . The speed of sound is \(1500 \mathrm{~m} / \mathrm{s}\).

\section*{Simulate signal}
```

array = phased.ULA('NumElements',11,'ElementSpacing',0.3);
fs = 2e3;
carrierFreq = 2000;
t = (0:1/fs:2)';
sig = chirp(t,0,2,fs/2);
c = 1500;
collector = phased.WidebandCollector('Sensor',array,'PropagationSpeed',c,...
'SampleRate',fs,'ModulatedInput',true,...
'CarrierFrequency',carrierFreq);

```
```

incidentAngle = [10;0];
sig1 = collector(sig,incidentAngle);
noise = 0.3*(randn(size(sig1)) + lj*randn(size(sig1)));
rx = sigl + noise;

```

\section*{Apply MVDR beamforming}
beamformer = phased.SubbandMVDRBeamformer('SensorArray', array,...
'Direction',incidentAngle,'OperatingFrequency', carrierFreq,...
'PropagationSpeed', c, 'SampleRate',fs,'TrainingInputPort',true, ...
'Subbands0utputPort', true, 'Weights0utputPort', true);
[y,w,subbandfreq] = beamformer(rx, noise);
Plot the signal that is input to the middle sensor (channel 6) vs the beamformer output.
plot(t(1:300), real(rx(1:300,6)), 'r:',t(1:300), real(y(1:300)))
xlabel('Time')
ylabel('Amplitude')
legend('Original','Beamformed');


\section*{Plot array response}

Plot the response pattern for five bands
pattern(array,subbandfreq(1:5).',-180:180,0,...
'PropagationSpeed',c,'Weights',w(:,1:5));


Directivity (dBi), Broadside at \(0.00^{\circ}\)

\section*{Subband MVDR Beamforming of Array with Interference}

Apply subband MVDR beamforming to an underwater acoustic 11-element ULA. Beamform the arriving signals to optimize the gain of a linear FM chirp signal arriving from 0 degrees azimuth and 0 degrees elevation. The signal has a bandwidth of 2.0 kHz . In addition, there unit amplitude 2.250 kHz interfering sine wave arriving from 28 degrees azimuth and 0 degrees elevation. Show how the MVDR beamformer nulls the interfering signal. Display the array pattern for several frequencies in the neighborhood of 2.250 kHz . The speed of sound is 1500 meters \(/ \mathrm{sec}\).

\section*{Simulate Arriving Signal and Noise}
```

array = phased.ULA('NumElements',11,'ElementSpacing',0.3);
fs = 2000;
carrierFreq = 2000;
t = (0:1/fs:2)';
sig = chirp(t,0,2,fs/2);
c = 1500;
collector = phased.WidebandCollector('Sensor',array,'PropagationSpeed',c,...
'SampleRate',fs,'ModulatedInput',true,...
'CarrierFrequency',carrierFreq);
incidentAngle = [0;0];
sig1 = collector(sig,incidentAngle);
noise = 0.3*(randn(size(sig1)) + lj*randn(size(sig1)));

```

\section*{Simulate Interfering Signal}

Combine both the desired and interfering signals.
```

fint = 250;
sigint = sin(2*pi*fint*t);
interfangle = [28;0];
sigint1 = collector(sigint,interfangle);
rx = sigl + sigintl + noise;

```

\section*{Apply MVDR Beamforming}

Use the combined noise and interfering signal as training data.
```

beamformer = phased.SubbandMVDRBeamformer('SensorArray',array,...
'Direction',incidentAngle,'OperatingFrequency',carrierFreq,...
'PropagationSpeed',c,'SampleRate',fs,'TrainingInputPort',true,...
'NumSubbands',64,...
'SubbandsOutputPort',true,'Weights0utputPort',true);
[y,w,subbandfreq] = beamformer(rx,sigint1 + noise);
tidx = [1:300];
plot(t(tidx),real(rx(tidx,6)),'r:',t(tidx),real(y(tidx)))
xlabel('Time')
ylabel('Amplitude')
legend('Original','Beamformed')

```


\section*{Plot Array Response Showing Beampattern Null}

Plot the response pattern for five bands near 2.250 kHz .
```

fdx = [5,7,9,11,13];
pattern(array,subbandfreq(fdx).',-50:50,0,...
'PropagationSpeed',c,'Weights',w(:,fdx),...
'CoordinateSystem','rectangular');

```


The beamformer places a null at 28 degrees for the subband containing 2.250 kHz .

\section*{More About}

\section*{Diagonal Loading}

Diagonal loading is a technique to improve beamformer robustness when stability issues arise from steering vector errors or finite sample size effects. This technique adds a positive real-valued multiple of the identity matrix to the correlation matrix of the received array data vector. You can apply diagonal loading using the DiagonalLoadingFactor property.

\section*{Algorithms}

\section*{Data Precision}

This System object supports single and double precision for input data, properties, and arguments. If the input data X is single precision, the output data is single precision. If the input data X is double
precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

\section*{Subband Frequency Processing}

Subband processing decomposes a wideband signal into multiple subbands and applies narrowband processing to the signal in each subband. The signals for all subbands are summed to form the output signal.

When using wideband frequency System objects or blocks, you specify the number of subbands, \(N_{\mathrm{B}}\), in which to decompose the wideband signal. Subband center frequencies and widths are automatically computed from the total bandwidth and number of subbands. The total frequency band is centered on the carrier or operating frequency, \(f_{c}\). The overall bandwidth is given by the sample rate, \(f_{s}\). Frequency subband widths are \(\Delta f=f_{\mathrm{s}} / N_{\mathrm{B}}\). The center frequencies of the subbands are
\[
f_{m}=\left\{\begin{array}{c}
f_{c}-\frac{f_{s}}{2}+(m-1) \Delta f, \quad N_{B} \text { even } \\
f_{c}-\frac{\left(N_{B}-1\right) f_{s}}{2 N_{B}}+(m-1) \Delta f, \quad N_{B} \text { odd }
\end{array}, m=1, \ldots, N_{B}\right.
\]

Some System objects let you obtain the subband center frequencies as output when you run the object. The returned subband frequencies are ordered consistently with the ordering of the discrete Fourier transform. Frequencies above the carrier appear first, followed by frequencies below the carrier.

\section*{Version History \\ Introduced in R2015b}

\section*{References}
[1] Van Trees, H. Optimum Array Processing. New York: Wiley-Interscience, 2002.

\section*{Extended Capabilities}

\section*{C/C++ Code Generation}

Generate C and \(\mathrm{C}++\) code using MATLAB® Coder \(^{\mathrm{TM}}\).
Usage notes and limitations:.
- See "System Objects in MATLAB Code Generation" (MATLAB Coder)
- This System object supports single and double precision for input data, properties, and arguments. If the input data \(X\) is single precision, the output data is single precision. If the input data \(X\) is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

\section*{See Also}
phased.MVDRBeamformer | phased.FrostBeamformer | phased. PhaseShiftBeamformer | phased.SubbandPhaseShiftBeamformer|phased.LCMVBeamformer | phased.WidebandCollector

\section*{reset}

System object: phased.SubbandMVDRBeamformer
Package: phased
Reset states of System object

\section*{Syntax}
reset(sMVDR)

\section*{Description}
reset (sMVDR) resets the internal state of the phased. SubbandMVDRBeamformer object, sWBFS. If the SeedSource property applies and has the value 'Property ', then this method resets the state of the random number generator.

\section*{Input Arguments}

\section*{sMVDR - Subband MVDR beamformer}

System object
Subband MVDR beamformer, specified as a System object.
Example: phased.SubbandMVDRBeamformer

\author{
Version History \\ Introduced in R2015b
}

\section*{step}

System object: phased.SubbandMVDRBeamformer
Package: phased
Wideband MVDR beamforming

\section*{Syntax}
\(Y=\) step(sMVDR,X)
\(Y=\) step (sMVDR, X,XT)
Y = step(sMVDR, X,ang)
[Y,Wts] = step(sMVDR, \(\qquad\)
[Y,Freq] = step(sMVDR,___)
[Y,Wts,Freq] = step(sMVDR,X,XT,ang)

\section*{Description}

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, \(x\) ) and \(y=o b j(x)\) perform equivalent operations.
\(Y=\) step (sMVDR, \(X\) ) performs wideband MVDR beamforming on the input, \(X\), and returns the beamformed output in Y . This syntax uses X for training samples to calculate the beamforming weights. Use the Direction property to specify the beamforming direction.
\(\mathrm{Y}=\) step (sMVDR, \(\mathrm{X}, \mathrm{XT}\) ) uses XT as the training samples to calculate the beamforming weights. This syntax applies only when you set the TrainingInputPort property to true. Use the Direction property to specify the beamforming direction.

Y = step(sMVDR,X,ang) uses ang as the beamforming direction. This syntax applies only when you set the DirectionSource property to 'Input port'.
[Y,Wts] = step(sMVDR, \(\qquad\) ) returns the beamforming weights, Wts, when you set the WeightsOutputPort property to true.
[Y,Freq] = step(sMVDR,__) returns the center frequencies of the subbands, Freq, when you set the SubbandsOutputPort property to true. Freq is a length- \(K\) column vector where, \(K\) is the number of subbands specified in the NumSubbands property.

You can combine optional input arguments when you set their enabling properties. Optional input arguments must be listed in the same order as their enabling properties. For example, [ \(\mathrm{Y}, \mathrm{Wts}, \mathrm{Freq}]=\operatorname{step}(\mathrm{sMVDR}, \mathrm{X}, \mathrm{XT}\), ang) is valid when you specify TrainingInputPort to true and specify DirectionSource to 'Input port'.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object
issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

\section*{Input Arguments}

\section*{sMVDR - Subband MVDR beamformer}

System object
Subband MVDR beamformer, specified as a System object.
Example: phased. SubbandMVDRBeamformer

\section*{X - Wideband input field}
\(M\)-by- \(N\) complex-valued matrix
Wideband input field, specified as an \(M\)-by- \(N\) matrix, where \(N\) is the number of array elements. If the sensor array consists of subarrays, \(N\) is then the number of subarrays. \(M\) is the number of samples in the data.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

If you set the TrainingInputPort to false, then step uses X as training data. In this case, the dimension \(M\) must be greater than \(N \times N B\). where \(N B\) is the number of subbands specified in the NumSubbands property.

If you set TrainingInputPort to true, use the XT argument to supply training data. In this case, the dimension \(M\) can be any positive integer.

Example: [1,1;j,1;0.5,0]
Data Types: double
Complex Number Support: Yes

\section*{XT - Wideband training samples}
\(P\)-by- \(N\) complex-valued matrix
Wideband training samples, specified as a \(P\)-by- \(N\) matrix where \(N\) is the number of elements. If the sensor array consists of subarrays, then \(N\) represents the number of subarrays.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

This argument applies when you set TrainingInputPort to true. The dimension \(P\) is the number of samples in the training data. \(P\) must be larger than \(N \times N B\), where \(N B\) is the number of subbands specified in the NumSubbands property.
Example: FT = [1,1;j,1;0.5,0]
Data Types: double
Complex Number Support: Yes

\section*{ang - Beamforming direction}

2-by-L real-valued matrix

Beamforming direction, specified as a 2 -by- \(L\) real-valued matrix, where \(L\) is the number of beamforming directions. This argument applies only when you set the DirectionSource property to 'Input port'. Each column takes the form of [AzimuthAngle;ElevationAngle]. Angle units are in degrees. The azimuth angle must lie between \(-180^{\circ}\) and \(180^{\circ}\). The elevation angle must lie between \(-90^{\circ}\) and \(90^{\circ}\). Angles are defined with respect to the local coordinate system of the array.
Example: \(F=\) [40 30; 0 10]
Data Types: double

\section*{Output Arguments}

\section*{Y - Beamformed output}
\(M\)-by-L complex-valued matrix
Beamformed output, returned as an \(M\)-by- \(L\) complex-valued matrix. The quantity \(M\) is the number of signal samples and \(L\) is the number of beamforming directions specified in the ang argument.

\section*{Wts - Beamforming weights}
\(N\)-by-K-by-L complex-valued matrix
Beamforming weights, returned as an \(N\)-by- K -by- \(L\) complex-valued matrix. The quantity \(N\) is the number of sensor elements or subarrays and \(K\) is the number of subbands specified by the NumSubbands property. The quantity \(L\) is the number of beamforming directions. Each column of Wts contains the narrowband beamforming weights used in the corresponding subband for the corresponding directions. This output applies only when you set the WeightsOutputPort property to true.

\section*{Freq - Center frequencies of subbands}

K-by-1 real-valued column vector
Center frequencies of subbands, returned as a \(K\)-by- 1 real-valued column vector. The quantity \(K\) is the number of subbands specified by the NumSubbands property. To return this output, set the SubbandsOutputPort property to true.

\section*{Examples}

\section*{Subband MVDR Beamforming of ULA}

Apply subband MVDR beamforming to an underwater acoustic 11-element ULA. The incident angle of the signal is \(10^{\circ}\) azimuth and \(30^{\circ}\) elevation. The signal is an FM chirp having a bandwidth of 1 kHz . The speed of sound is \(1500 \mathrm{~m} / \mathrm{s}\).

\section*{Simulate signal}
```

array = phased.ULA('NumElements',11,'ElementSpacing',0.3);
fs = 2e3;
carrierFreq = 2000;
t = (0:1/fs:2)';
sig = chirp(t,0,2,fs/2);
c = 1500;
collector = phased.WidebandCollector('Sensor',array,'PropagationSpeed',c,...
'SampleRate',fs,'ModulatedInput',true,...

```
'CarrierFrequency', carrierFreq);
```

incidentAngle = [10;0];

```
sigl = collector(sig,incidentAngle);
noise \(=0.3^{*}(\) randn(size(sig1)) \(+1 j *\) randn(size(sig1)));
rx = sigl + noise;

\section*{Apply MVDR beamforming}
```

beamformer = phased.SubbandMVDRBeamformer('SensorArray',array,...
'Direction',incidentAngle,'OperatingFrequency',carrierFreq,...
'PropagationSpeed',c,'SampleRate',fs,'TrainingInputPort',true, ...
'Subbands0utputPort',true,'Weights0utputPort',true);
[y,w,subbandfreq] = beamformer(rx, noise);

```

Plot the signal that is input to the middle sensor (channel 6) vs the beamformer output.
```

plot(t(1:300),real(rx(1:300,6)),'r:',t(1:300),real(y(1:300)))

```
xlabel('Time')
ylabel('Amplitude')
legend('Original','Beamformed');


\section*{Plot array response}

Plot the response pattern for five bands
```

pattern(array,subbandfreq(1:5).',-180:180,0,...

```
    'PropagationSpeed', c, 'Weights',w(:,1:5));


Directivity (dBi), Broadside at \(0.00^{\circ}\)

\section*{Subband MVDR Beamforming of Array with Interference}

Apply subband MVDR beamforming to an underwater acoustic 11-element ULA. Beamform the arriving signals to optimize the gain of a linear FM chirp signal arriving from 0 degrees azimuth and 0 degrees elevation. The signal has a bandwidth of 2.0 kHz . In addition, there unit amplitude 2.250 kHz interfering sine wave arriving from 28 degrees azimuth and 0 degrees elevation. Show how the MVDR beamformer nulls the interfering signal. Display the array pattern for several frequencies in the neighborhood of 2.250 kHz . The speed of sound is 1500 meters \(/ \mathrm{sec}\).

\section*{Simulate Arriving Signal and Noise}
```

array = phased.ULA('NumElements',11,'ElementSpacing',0.3);
fs = 2000;
carrierFreq = 2000;
t = (0:1/fs:2)';
sig = chirp(t,0,2,fs/2);
c = 1500;
collector = phased.WidebandCollector('Sensor',array,'PropagationSpeed',c,...
'SampleRate',fs,'ModulatedInput',true,...
'CarrierFrequency',carrierFreq);
incidentAngle = [0;0];
sig1 = collector(sig,incidentAngle);
noise = 0.3*(randn(size(sig1)) + lj*randn(size(sig1)));

```

\section*{Simulate Interfering Signal}

Combine both the desired and interfering signals.
```

fint = 250;
sigint = sin(2*pi*fint*t);
interfangle = [28;0];
sigint1 = collector(sigint,interfangle);
rx = sigl + sigint1 + noise;

```

\section*{Apply MVDR Beamforming}

Use the combined noise and interfering signal as training data.
```

beamformer = phased.SubbandMVDRBeamformer('SensorArray',array,...
'Direction',incidentAngle,'OperatingFrequency',carrierFreq,...
'PropagationSpeed',c,'SampleRate',fs,'TrainingInputPort',true,...
'NumSubbands',64,...
'Subbands0utputPort',true,'Weights0utputPort',true);
[y,w,subbandfreq] = beamformer(rx,sigint1 + noise);
tidx = [1:300];
plot(t(tidx),real(rx(tidx,6)),'r:',t(tidx),real(y(tidx)))
xlabel('Time')
ylabel('Amplitude')
legend('Original','Beamformed')

```


\section*{Plot Array Response Showing Beampattern Null}

Plot the response pattern for five bands near 2.250 kHz .
```

fdx = [5,7,9,11,13];
pattern(array,subbandfreq(fdx).',-50:50,0,...
'PropagationSpeed',c,'Weights',w(:,fdx),...
'CoordinateSystem','rectangular');

```


The beamformer places a null at 28 degrees for the subband containing 2.250 kHz .

\section*{Version History Introduced in R2015b}

\section*{References}
[1] Proakis, J. Digital Communications. New York: McGraw-Hill, 2001.
[2] Skolnik, M. Introduction to Radar Systems, 3rd Ed. New York: McGraw-Hill
[3] Saakian, A. Radio Wave Propagation Fundamentals. Norwood, MA: Artech House, 2011.
[4] Balanis, C. Advanced Engineering Electromagnetics. New York: Wiley \& Sons, 1989.
[5] Rappaport, T. Wireless Communications: Principles and Practice, 2nd Ed New York: Prentice Hall, 2002.

\title{
phased.SubbandPhaseShiftBeamformer
}

Package: phased
Subband phase shift beamformer

\section*{Description}

The SubbandPhaseShiftBeamformer object implements a subband phase shift beamformer.
To compute the beamformed signal:
1 Define and set up your subband phase shift beamformer. See "Construction" on page 1-1674.
2 Call step to perform the beamforming operation according to the properties of phased.SubbandPhaseShiftBeamformer. The behavior of step is specific to each object in the toolbox.

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = \(\underline{\text { step }(o b j, x) \text { and } y=o b j(x) \text { perform equivalent operations. }}\)

\section*{Construction}

H = phased. SubbandPhaseShiftBeamformer creates a subband phase shift beamformer System object, H. The object performs subband phase shift beamforming on the received signal.

H = phased.SubbandPhaseShiftBeamformer(Name,Value) creates a subband phase shift beamformer object, H, with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN).

\section*{Properties}

\section*{SensorArray}

Sensor array
Sensor array specified as an array System object belonging to the phased package. A sensor array can contain subarrays.

Default: phased.ULA with default property values

\section*{PropagationSpeed}

Signal propagation speed
Specify the propagation speed of the signal, in meters per second, as a positive scalar. You can specify this property as single or double precision.

Default: Speed of light

\section*{OperatingFrequency}

System operating frequency
Specify the operating frequency of the beamformer in hertz as a scalar. The default value of this property corresponds to 300 MHz . This property can be specified as single or double precision.

\section*{Default: 3e8}

\section*{SampleRate}

Signal sampling rate
Specify the signal sampling rate (in hertz) as a positive scalar. This property can be specified as single or double precision.

Default: 1e6

\section*{NumSubbands}

Number of subbands
Specify the number of subbands used in the subband processing as a positive integer. This property can be specified as single or double precision.

Default: 64

\section*{DirectionSource}

Source of beamforming direction
Specify whether the beamforming direction for the beamformer comes from the Direction property of this object or from an input argument in step. Values of this property are:
\begin{tabular}{|l|l|}
\hline 'Property' & \begin{tabular}{l} 
The Direction property of this object specifies the \\
beamforming direction.
\end{tabular} \\
\hline 'Input port' & \begin{tabular}{l} 
An input argument in each invocation of step specifies the \\
beamforming direction.
\end{tabular} \\
\hline
\end{tabular}

\section*{Default: 'Property'}

\section*{Direction}

\section*{Beamforming directions}

Specify the beamforming directions of the beamformer as a two-row matrix. Each column of the matrix has the form [AzimuthAngle; ElevationAngle] (in degrees). Each azimuth angle must be between -180 and 180 degrees, and each elevation angle must be between -90 and 90 degrees. This property applies when you set the DirectionSource property to 'Property'. This property can be specified as single or double precision.

Default: [0; 0]

\section*{WeightsOutputPort}

Output beamforming weights

To obtain the weights used in the beamformer, set this property to true and use the corresponding output argument when invoking step. If you do not want to obtain the weights, set this property to false.

\section*{Default: false}

\section*{Subbands0utputPort}

Output subband center frequencies
To obtain the center frequencies of each subband, set this property to true and use the corresponding output argument when invoking step. If you do not want to obtain the center frequencies, set this property to false.

Default: false

\section*{Methods}
step Beamforming using subband phase shifting

\section*{Common to All System Objects}
\begin{tabular}{|l|l} 
release & Allow System object property value changes
\end{tabular}

\section*{Examples}

\section*{Subband Phase-Shift Beamformer for Underwater ULA}

Apply subband phase-shift beamforming to an 11-element underwater ULA. The incident angle of a wideband signal is \(10^{\circ}\) in azimuth and \(30^{\circ}\) in elevation. The carrier frequency is 2 kHz .

Create the ULA.
```

antenna = phased.ULA('NumElements',11,'ElementSpacing',0.3);

```
antenna.Element.FrequencyRange = [20 20000];

Create a chirp signal with noise.
```

fs = 1e3;
carrierFreq = 2e3;
t = (0:1/fs:2)';
x = chirp(t,0,2,fs);
c = 1500;
collector = phased.WidebandCollector('Sensor',antenna, ...
'PropagationSpeed',c,'SampleRate',fs,...
'ModulatedInput',true,'CarrierFrequency' ,carrierFreq);
incidentAngle = [10;30];
x = collector(x,incidentAngle);
noise = 0.3*(randn(size(x)) + lj*randn(size(x)));
rx = x + noise;

```

Beamform in the direction of the incident angle.
```

beamformer = phased.SubbandPhaseShiftBeamformer('SensorArray',antenna, ...
'Direction',incidentAngle,'OperatingFrequency',carrierFreq, ...

```
```

    'PropagationSpeed',c,'SampleRate',fs,'SubbandsOutputPort',true, ...
    'Weights0utputPort',true);
    [y,w,subbandfreq] = beamformer(rx);

```

Plot the real part of the original and beamformed signals.
plot(t(1:300), real(rx(1:300,6)), 'r:',t(1:300), real(y(1:300)))
xlabel('Time')
ylabel('Amplitude')
legend('Original','Beamformed')


Plot the response pattern for five frequency bands.
```

pattern(antenna,subbandfreq(1:5).',[-180:180],0,'PropagationSpeed',c, ...
'CoordinateSystem','rectangular','Weights',w(:,1:5))
legend('location','SouthEast')

```


\section*{Algorithms}

\section*{Beamforming Algorithm}

The subband phase shift beamformer separates the signal into several subbands and applies narrowband phase shift beamforming to the signal in each subband. The beamformed signals in all the subbands are regrouped to form the output signal.

For further details, see [1].

\section*{Data Precision}

This System object supports single and double precision for input data, properties, and arguments. If the input data X is single precision, the output data is single precision. If the input data X is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

\section*{Version History}

\section*{Introduced in R2011a}

\section*{References}
[1] Van Trees, H. Optimum Array Processing. New York: Wiley-Interscience, 2002.

\section*{Extended Capabilities}

\section*{C/C++ Code Generation}

Generate C and \(\mathrm{C}++\) code using MATLAB® Coder \(^{\mathrm{rm}}\).
Usage notes and limitations:
See "System Objects in MATLAB Code Generation" (MATLAB Coder).
This System object supports single and double precision for input data, properties, and arguments. If the input data X is single precision, the output data is single precision. If the input data X is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

\section*{See Also}
phased.Collector|phased.PhaseShiftBeamformer | phased.TimeDelayBeamformer | phased.WidebandCollector|uv2azel | phitheta2azel

\section*{Topics}
"Wideband Beamforming"

\section*{step}

\section*{System object: phased. SubbandPhaseShiftBeamformer}

Package: phased
Beamforming using subband phase shifting

\section*{Syntax}
```

Y = step(H,X)
Y = step(H,X,ANG)
[Y,W] = step(
[Y,FREQ] = step(
[Y,W,FREQ] = step(

```
\(\qquad\)

\section*{Description}

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step (obj, \(x\) ) and \(y=o b j(x)\) perform equivalent operations.
\(Y=\) step \((H, X)\) performs subband phase shift beamforming on the input, \(X\), and returns the beamformed output in Y .
\(\mathrm{Y}=\operatorname{step}(\mathrm{H}, \mathrm{X}, \mathrm{ANG})\) uses ANG as the beamforming direction. This syntax is available when you set the DirectionSource property to 'Input port'.
\([\mathrm{Y}, \mathrm{W}]=\operatorname{step}(\ldots \quad\) ) returns the beamforming weights, W . This syntax is available when you set the WeightsOutputPort property to true.
[Y,FREQ] = step( \(\qquad\) ) returns the center frequencies of subbands, FREQ. This syntax is available when you set the SubbandsOutputPort property to true.
[ \(\mathrm{Y}, \mathrm{W}, \mathrm{FREQ}]=\) step ( ___ ) returns beamforming weights and center frequencies of subbands. This syntax is available when you set the WeightsOutputPort property to true and set the SubbandsOutputPort property to true.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

\section*{Input Arguments}

H
Beamformer object.

\section*{X}

Input signal, specified as an \(M\)-by- \(N\) matrix. If the sensor array contains subarrays, \(N\) is the number of subarrays; otherwise, \(N\) is the number of elements. This argument can be specified as single or double precision.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

\section*{ANG}

Beamforming directions, specified as a two-row matrix. Each column has the form [AzimuthAngle; ElevationAngle], in degrees. Each azimuth angle must be between -180 and 180 degrees, and each elevation angle must be between -90 and 90 degrees. This argument can be specified as single or double precision.

\section*{Output Arguments}

\section*{Y}

Beamformed output. Y is an \(M\)-by- \(L\) matrix, where \(M\) is the number of rows of X and \(L\) is the number of beamforming directions. This argument can be returned as single or double precision.

\section*{W}

Beamforming weights. W has dimensions \(N\)-by- \(K\)-by- \(L . K\) is the number of subbands in the NumSubbands property. \(L\) is the number of beamforming directions. If the sensor array contains subarrays, \(N\) is the number of subarrays; otherwise, \(N\) is the number of elements. Each column of \(W\) specifies the narrowband beamforming weights used in the corresponding subband for the corresponding direction. This argument can be returned as single or double precision.

\section*{FREQ}

Center frequencies of subbands. FREQ is a column vector of length \(K\), where \(K\) is the number of subbands in the NumSubbands property. This argument can be returned as single or double precision.

\section*{Examples}

\section*{Subband Phase-Shift Beamformer for Underwater ULA}

Apply subband phase-shift beamforming to an 11-element underwater ULA. The incident angle of a wideband signal is \(10^{\circ}\) in azimuth and \(30^{\circ}\) in elevation. The carrier frequency is 2 kHz .

Create the ULA.
```

antenna = phased.ULA('NumElements',11,'ElementSpacing',0.3);
antenna.Element.FrequencyRange = [20 20000];
Create a chirp signal with noise.

```
```

fs = 1e3;

```
fs = 1e3;
carrierFreq = 2e3;
```

```
t = (0:1/fs:2)';
x = chirp(t,0,2,fs);
c = 1500;
collector = phased.WidebandCollector('Sensor',antenna, ...
    'PropagationSpeed',c,'SampleRate',fs,...
    'ModulatedInput',true,'CarrierFrequency',carrierFreq);
incidentAngle = [10;30];
x = collector(x,incidentAngle);
noise = 0.3*(randn(size(x)) + lj*randn(size(x)));
rx = x + noise;
```

Beamform in the direction of the incident angle.

```
beamformer = phased.SubbandPhaseShiftBeamformer('SensorArray',antenna, ...
    'Direction',incidentAngle,'OperatingFrequency',carrierFreq, ...
    'PropagationSpeed',c,'SampleRate',fs,'Subbands0utputPort',true, ...
    'Weights0utputPort',true);
[y,w,subbandfreq] = beamformer(rx);
```

Plot the real part of the original and beamformed signals.

```
plot(t(1:300),real(rx(1:300,6)),'r:',t(1:300),real(y(1:300)))
xlabel('Time')
ylabel('Amplitude')
legend('Original','Beamformed')
```



Plot the response pattern for five frequency bands.
pattern(antenna,subbandfreq(1:5).',[-180:180],0,'PropagationSpeed', c, ...
'CoordinateSystem','rectangular','Weights',w(:,1:5))
legend('location','SouthEast')


## Algorithms

The subband phase shift beamformer separates the signal into several subbands and applies narrowband phase shift beamforming to the signal in each subband. The beamformed signals in all the subbands are regrouped to form the output signal.

For further details, see [1].

## References

[1] Van Trees, H. Optimum Array Processing. New York: Wiley-Interscience, 2002.

## See Also

uv2azel | phitheta2azel

# phased.SumDifferenceMonopulseTracker 

Package: phased
Sum and difference monopulse for ULA

## Description

The SumDifferenceMonopulseTracker object implements a sum and difference monopulse algorithm on a uniform linear array.

To estimate the direction of arrival (DOA):
1 Define and set up your sum and difference monopulse DOA estimator. See "Construction" on page 1-1684.
2 Call step to estimate the DOA according to the properties of phased.SumDifferenceMonopulseTracker. The behavior of step is specific to each object in the toolbox.

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.

## Construction

H = phased. SumDifferenceMonopulseTracker creates a tracker System object, H. The object uses sum and difference monopulse algorithms on a uniform linear array (ULA).

H = phased.SumDifferenceMonopulseTracker(Name, Value) creates a ULA monopulse tracker object, H, with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN).

## Properties

## SensorArray

Handle to sensor array
Specify the sensor array as a handle. The sensor array must be a phased. ULA object.
Default: phased.ULA with default property values

## PropagationSpeed

Signal propagation speed
Specify the propagation speed of the signal, in meters per second, as a positive scalar. You can specify this property as single or double precision.

Default: Speed of light

## OperatingFrequency

System operating frequency
Specify the operating frequency of the system in hertz as a positive scalar. The default value corresponds to 300 MHz . You can specify this property as single or double precision.

## Default: 3e8

## NumPhaseShifterBits

Number of phase shifter quantization bits
The number of bits used to quantize the phase shift component of beamformer or steering vector weights. Specify the number of bits as a non-negative integer. A value of zero indicates that no quantization is performed. You can specify this property as single or double precision.

## Default: 0

## Methods

step Perform monopulse tracking using ULA

## Common to All System Objects

| release | Allow System object property value changes |
| :--- | :--- |

## Examples

## Find Target Direction Using Monopulse Tracker

Determine the direction of a target at a $60.1^{\circ}$ broadside angle to a ULA starting with an approximate direction of $60^{\circ}$

```
array = phased.ULA('NumElements',4);
steervec = phased.SteeringVector('SensorArray',array);
tracker = phased.SumDifferenceMonopulseTracker('SensorArray',array);
x = steervec(tracker.OperatingFrequency,60.1).';
est_dir = tracker(x,60)
est_dir = 60.1000
```


## Algorithms

## Monopulse Algorithm

The sum-and-difference monopulse algorithm is used to the estimate the arrival direction of a narrowband signal impinging upon a uniform linear array (ULA). First, compute the conventional response of an array steered to an arrival direction $\varphi_{0}$. For a ULA, the arrival direction is specified by the broadside angle. To specify that the maximum response axis (MRA) point towards the $\varphi_{0}$ direction, set the weights to be

$$
\mathbf{w}_{S}=\left(1, e^{i k d \sin \phi_{0}}, e^{i k 2 d \sin \phi_{0}}, \ldots, e^{i k(N-1) d \sin \phi_{0}}\right)
$$

where $d$ is the element spacing and $k=2 \pi / \lambda$ is the wavenumber. An incoming plane wave, coming from any arbitrary direction $\varphi$, is represented by

$$
\mathbf{v}=\left(1, e^{i k d \sin \phi}, e^{i k 2 d \sin \phi}, \ldots, e^{i k(N-1) d \sin \phi}\right)
$$

The conventional response of this array to any incoming plane wave is given by $\mathbf{w}_{S}^{H} \mathbf{v}(\varphi)$ and is shown in the polar plot below as the Sum Pattern. The array is designed to steer towards $\varphi_{0}=30^{\circ}$.

The second pattern, called the Difference Pattern, is obtained by using phased-reversed weights. The weights are determined by phase-reversing the latter half of the conventional steering vector. For an array with an even number of elements, the phase-reversed weights are

$$
\mathbf{w}_{d}=-i\left(1, e^{i k d \sin \phi_{0}}, e^{i k 2 d \sin \phi_{0}}, \ldots, e^{i k N / 2 d \sin \phi_{0}},-e^{i k(N / 2+1) d \sin \phi_{0}}, \ldots,-e^{i k(N-1) d \sin \phi_{0}}\right)
$$

(For an array with an odd number of elements, the middle weight is set to zero). The multiplicative factor $-i$ is used for convenience. The response of the difference array to the incoming vector is

$$
\mathbf{w}_{d}^{H} \mathbf{v}(\varphi)
$$

This figure shows the sum and difference beam patterns of a four-element uniform linear array (ULA) steered $30^{\circ}$ from broadside. The array elements are spaced at one-half wavelength. The sum pattern shows that the array has its maximum response at $30^{\circ}$ and the difference pattern has a null at $30^{\circ}$.


The monopulse response curve is obtained by dividing the difference pattern by the sum pattern and taking the real part.

$$
R(\varphi)=\operatorname{Re}\left(\frac{\mathbf{w}_{d}^{H} \mathbf{v}(\varphi)}{\mathbf{w}_{S}^{H} \mathbf{v}(\varphi)}\right)
$$

To use the monopulse response curve to obtain the arrival angle, $\varphi$, of a narrowband signal, $\mathbf{x}$, compute

$$
z=\operatorname{Re}\left(\frac{\mathbf{w}_{d}^{H} \mathbf{x}}{\mathbf{w}_{S}^{H} \mathbf{x}}\right)
$$

and invert the response curve, $\varphi=R^{-1}(z)$, to obtain $\varphi$.
The response curve is not generally single valued and can only be inverted when arrival angles lie within the main lobe where it is single valued This figure shows the monopulse response curve within the main lobe of the four-element ULA array.


There are two desirable properties of the monopulse response curve. The first is that it have a steep slope. A steep slope insures robustness against noise. The second property is that the mainlobe be as wide as possible. A steep slope is ensure by a larger array but leads to a smaller mainlobe. You will need to trade off one property with the other.

For further details, see [1].

## Data Precision

This System object supports single and double precision for input data, properties, and arguments. If the input data X is single precision, the output data is single precision. If the input data X is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

## Version History

## Introduced in R2011a

## References

[1] Seliktar, Y. Space-Time Adaptive Monopulse Processing. Ph.D. Thesis. Georgia Institute of Technology, Atlanta, 1998.
[2] Rhodes, D. Introduction to Monopulse. Dedham, MA: Artech House, 1980.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
See "System Objects in MATLAB Code Generation" (MATLAB Coder).

See Also<br>phased.BeamscanEstimator|phased.SumDifferenceMonopulseTracker2D<br>Topics<br>"Target Tracking Using Sum-Difference Monopulse Radar"

## step

System object: phased. SumDifferenceMonopulseTracker
Package: phased
Perform monopulse tracking using ULA

## Syntax

ESTANG = step(H,X,STANG)

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.

ESTANG = step( $\mathrm{H}, \mathrm{X}, \mathrm{STANG}$ ) estimates the incoming direction ESTANG of the input signal, X , based on an initial guess of the direction.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## H

Tracker object of type phased. SumDifferenceMonopulseTracker.

## X

Input signal, specified as a row vector whose number of columns corresponds to number of channels. You can specify this argument as single or double precision.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

## STANG

Initial guess of the direction, specified as a scalar that represents the broadside angle in degrees. A typical initial guess is the current steering angle. The value of STANG is between -90 and 90. The angle is defined in the array's local coordinate system. For details regarding the local coordinate system of the ULA, type phased.ULA. coordinateSystemInfo. You can specify this argument as single or double precision.

## Output Arguments

## ESTANG

Estimate of incoming direction, returned as a scalar that represents the broadside angle in degrees. The value is between -90 and 90 . The angle is defined in the array's local coordinate system.

## Examples

## Find Target Direction Using Monopulse Tracker

Determine the direction of a target at a $60.1^{\circ}$ broadside angle to a ULA starting with an approximate direction of $60^{\circ}$

```
array = phased.ULA('NumElements',4);
steervec = phased.SteeringVector('SensorArray',array);
tracker = phased.SumDifferenceMonopulseTracker('SensorArray',array);
x = steervec(tracker.OperatingFrequency,60.1).';
est_dir = tracker(x,60)
est_dir = 60.1000
```


## Algorithms

The sum-and-difference monopulse algorithm is used to the estimate the arrival direction of a narrowband signal impinging upon a uniform linear array (ULA). First, compute the conventional response of an array steered to an arrival direction $\varphi_{0}$. For a ULA, the arrival direction is specified by the broadside angle. To specify that the maximum response axis (MRA) point towards the $\varphi_{0}$ direction, set the weights to be

$$
\mathbf{w}_{s}=\left(1, e^{i k d \sin \phi_{0}}, e^{i k 2 d \sin \phi_{0}}, \ldots, e^{i k(N-1) d \sin \phi_{0}}\right)
$$

where $d$ is the element spacing and $k=2 \pi / \lambda$ is the wavenumber. An incoming plane wave, coming from any arbitrary direction $\varphi$, is represented by

$$
\mathbf{v}=\left(1, e^{i k d \sin \phi}, e^{i k 2 d \sin \phi}, \ldots, e^{i k(N-1) d \sin \phi}\right)
$$

The conventional response of this array to any incoming plane wave is given by $\mathbf{w}_{s}^{H} \mathbf{v}(\varphi)$ and is shown in the polar plot below as the Sum Pattern. The array is designed to steer towards $\varphi_{0}=30^{\circ}$.

The second pattern, called the Difference Pattern, is obtained by using phased-reversed weights. The weights are determined by phase-reversing the latter half of the conventional steering vector. For an array with an even number of elements, the phase-reversed weights are

$$
\mathbf{w}_{d}=-i\left(1, e^{i k d \sin \phi_{0}}, e^{i k 2 d \sin \phi_{0}}, \ldots, e^{i k N / 2 d \sin \phi_{0}},-e^{i k(N / 2+1) d \sin \phi_{0}}, \ldots,-e^{i k(N-1) d \sin \phi_{0}}\right)
$$

(For an array with an odd number of elements, the middle weight is set to zero). The multiplicative factor $-i$ is used for convenience. The response of the difference array to the incoming vector is

$$
\mathbf{w}_{d}^{H} \mathbf{v}(\varphi)
$$

This figure shows the sum and difference beam patterns of a four-element uniform linear array (ULA) steered $30^{\circ}$ from broadside. The array elements are spaced at one-half wavelength. The sum pattern shows that the array has its maximum response at $30^{\circ}$ and the difference pattern has a null at $30^{\circ}$.


The monopulse response curve is obtained by dividing the difference pattern by the sum pattern and taking the real part.

$$
R(\varphi)=\operatorname{Re}\left(\frac{\mathbf{w}_{d}^{H} \mathbf{v}(\varphi)}{\mathbf{w}_{s}^{H} \mathbf{v}(\varphi)}\right)
$$

To use the monopulse response curve to obtain the arrival angle, $\varphi$, of a narrowband signal, $\mathbf{x}$, compute

$$
z=\operatorname{Re}\left(\frac{\mathbf{w}_{d}^{H} \mathbf{x}}{\mathbf{w}_{S}^{H} \mathbf{x}}\right)
$$

and invert the response curve, $\varphi=R^{-1}(z)$, to obtain $\varphi$.
The response curve is not generally single valued and can only be inverted when arrival angles lie within the main lobe where it is single valued This figure shows the monopulse response curve within the main lobe of the four-element ULA array.


There are two desirable properties of the monopulse response curve. The first is that it have a steep slope. A steep slope insures robustness against noise. The second property is that the mainlobe be as wide as possible. A steep slope is ensure by a larger array but leads to a smaller mainlobe. You will need to trade off one property with the other.

For further details, see [1].

## References

[1] Seliktar, Y. Space-Time Adaptive Monopulse Processing. Ph.D. Thesis. Georgia Institute of Technology, Atlanta, 1998.
[2] Rhodes, D. Introduction to Monopulse. Dedham, MA: Artech House, 1980.

## phased.SumDifferenceMonopulseTracker2D

Package: phased
Sum and difference monopulse for URA

## Description

The SumDifferenceMonopulseTracker2D object implements a sum and difference monopulse algorithm for a uniform rectangular array.

To estimate the direction of arrival (DOA):
1 Define and set up your sum and difference monopulse DOA estimator. See "Construction" on page 1-1693.
2 Call step to estimate the DOA according to the properties of phased.SumDifferenceMonopulseTracker2D. The behavior of step is specific to each object in the toolbox.

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.

## Construction

H = phased. SumDifferenceMonopulseTracker2D creates a tracker System object, H. The object uses sum and difference monopulse algorithms on a uniform rectangular array (URA).

H = phased.SumDifferenceMonopulseTracker2D(Name,Value) creates a URA monopulse tracker object, H, with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN).

## Properties

## SensorArray

Handle to sensor array
Specify the sensor array as a handle. The sensor array must be a phased. URA object.
Default: phased.URA with default property values

## PropagationSpeed

Signal propagation speed
Specify the propagation speed of the signal, in meters per second, as a positive scalar. You can specify this property as single or double precision.

Default: Speed of light

## OperatingFrequency

System operating frequency
Specify the operating frequency of the system in hertz as a positive scalar. The default value corresponds to 300 MHz . You can specify this property as single or double precision.

Default: 3e8

## NumPhaseShifterBits

Number of phase shifter quantization bits
The number of bits used to quantize the phase shift component of beamformer or steering vector weights. Specify the number of bits as a non-negative integer. A value of zero indicates that no quantization is performed. You can specify this property as single or double precision.

## Default: 0

## Methods

step Perform monopulse tracking using URA

## Common to All System Objects

release $\quad$ Allow System object property value changes

## Examples

## Find Target Direction Using Sum-Difference 2D Monopulse Tracker

Using a URA, determine the direction of a target at approximately $60^{\circ}$ azimuth and $20^{\circ}$ elevation.

```
array = phased.URA('Size',4);
steeringvec = phased.SteeringVector('SensorArray',array);
tracker = phased.SumDifferenceMonopulseTracker2D('SensorArray',array);
x = steeringvec(tracker.OperatingFrequency,[60.1; 19.5]).';
est_dir = tracker(x,[60; 20])
est_dir = 2×1
```

60.1000
19.5000

## Algorithms

## Monopulse Algorithm

The sum-and-difference monopulse algorithm is used to the estimate the arrival direction of a narrowband signal impinging upon a uniform linear array (ULA). First, compute the conventional response of an array steered to an arrival direction $\varphi_{0}$. For a ULA, the arrival direction is specified by
the broadside angle. To specify that the maximum response axis (MRA) point towards the $\varphi_{0}$ direction, set the weights to be

$$
\mathbf{w}_{S}=\left(1, e^{i k d \sin \phi_{0}}, e^{i k 2 d \sin \phi_{0}}, \ldots, e^{i k(N-1) d \sin \phi_{0}}\right)
$$

where $d$ is the element spacing and $k=2 \pi / \lambda$ is the wavenumber. An incoming plane wave, coming from any arbitrary direction $\varphi$, is represented by

$$
\mathbf{v}=\left(1, e^{i k d \sin \phi}, e^{i k 2 d \sin \phi}, \ldots, e^{i k(N-1) d \sin \phi}\right)
$$

The conventional response of this array to any incoming plane wave is given by $\mathbf{w}_{s}^{H} \mathbf{v}(\varphi)$ and is shown in the polar plot below as the Sum Pattern. The array is designed to steer towards $\varphi_{0}=30^{\circ}$.

The second pattern, called the Difference Pattern, is obtained by using phased-reversed weights. The weights are determined by phase-reversing the latter half of the conventional steering vector. For an array with an even number of elements, the phase-reversed weights are

$$
\mathbf{w}_{d}=-i\left(1, e^{i k d \sin \phi_{0}}, e^{i k 2 d \sin \phi_{0}}, \ldots, e^{i k N / 2 d \sin \phi_{0}},-e^{i k(N / 2+1) d \sin \phi_{0}}, \ldots,-e^{i k(N-1) d \sin \phi_{0}}\right)
$$

(For an array with an odd number of elements, the middle weight is set to zero). The multiplicative factor $-i$ is used for convenience. The response of the difference array to the incoming vector is

$$
\mathbf{w}_{d}^{H} \mathbf{v}(\varphi)
$$

This figure shows the sum and difference beam patterns of a four-element uniform linear array (ULA) steered $30^{\circ}$ from broadside. The array elements are spaced at one-half wavelength. The sum pattern shows that the array has its maximum response at $30^{\circ}$ and the difference pattern has a null at $30^{\circ}$.


The monopulse response curve is obtained by dividing the difference pattern by the sum pattern and taking the real part.

$$
R(\varphi)=\operatorname{Re}\left(\frac{\mathbf{w}_{d}^{H} \mathbf{v}(\varphi)}{\mathbf{w}_{S}^{H} \mathbf{v}(\varphi)}\right)
$$

To use the monopulse response curve to obtain the arrival angle, $\varphi$, of a narrowband signal, $\mathbf{x}$, compute

$$
z=\operatorname{Re}\left(\frac{\mathbf{w}_{d}^{H} \mathbf{x}}{\mathbf{w}_{s}^{H} \mathbf{x}}\right)
$$

and invert the response curve, $\varphi=R^{-1}(z)$, to obtain $\varphi$.
The response curve is not generally single valued and can only be inverted when arrival angles lie within the main lobe where it is single valued This figure shows the monopulse response curve within the main lobe of the four-element ULA array.


There are two desirable properties of the monopulse response curve. The first is that it have a steep slope. A steep slope insures robustness against noise. The second property is that the mainlobe be as wide as possible. A steep slope is ensure by a larger array but leads to a smaller mainlobe. You will need to trade off one property with the other.

For further details, see [1].

## Data Precision

This System object supports single and double precision for input data, properties, and arguments. If the input data $X$ is single precision, the output data is single precision. If the input data $X$ is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

## Version History

## Introduced in R2011a

## References

[1] Seliktar, Y. Space-Time Adaptive Monopulse Processing. Ph.D. Thesis. Georgia Institute of Technology, Atlanta, 1998.
[2] Rhodes, D. Introduction to Monopulse. Dedham, MA: Artech House, 1980.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
See "System Objects in MATLAB Code Generation" (MATLAB Coder).

## See Also <br> phased.BeamscanEstimator|phased.SumDifferenceMonopulseTracker

## step

System object: phased.SumDifferenceMonopulseTracker2D
Package: phased
Perform monopulse tracking using URA

## Syntax

ESTANG $=\operatorname{step}(\mathrm{H}, \mathrm{X}, \mathrm{STANG})$

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step (obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.

ESTANG $=\operatorname{step}(H, X$, STANG $)$ estimates the incoming direction ESTANG of the input signal, X , based on an initial guess of the direction.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## H

Tracker object of type phased. SumDifferenceMonopulseTracker2D.
X
Input signal, specified as a row vector whose number of columns corresponds to number of channels. You can specify this argument as single or double precision.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

## STANG

Initial guess of the direction, specified as a 2-by-1 vector in the form [AzimuthAngle;
ElevationAngle] in degrees. A typical initial guess is the current steering angle. Azimuth angles must be between -180 and 180. Elevation angles must be between -90 and 90. Angles are measured in the local coordinate system of the array. For details regarding the local coordinate system of the

URA, type phased.URA. coordinateSystemInfo. You can specify this argument as single or double precision.

## Output Arguments

## ESTANG

Estimate of incoming direction, returned as a 2-by-1 vector in the form [AzimuthAngle; ElevationAngle] in degrees. Azimuth angles are between -180 and 180. Elevation angles are between -90 and 90 . Angles are measured in the local coordinate system of the array.

## Examples

## Find Target Direction Using Sum-Difference 2D Monopulse Tracker

Using a URA, determine the direction of a target at approximately $60^{\circ}$ azimuth and $20^{\circ}$ elevation.

```
array = phased.URA('Size',4);
steeringvec = phased.SteeringVector('SensorArray',array);
tracker = phased.SumDifferenceMonopulseTracker2D('SensorArray',array);
x = steeringvec(tracker.OperatingFrequency,[60.1; 19.5]).';
est_dir = tracker(x,[60; 20])
est_dir = 2×1
    60.1000
    19.5000
```


## Algorithms

The sum-and-difference monopulse algorithm is used to the estimate the arrival direction of a narrowband signal impinging upon a uniform linear array (ULA). First, compute the conventional response of an array steered to an arrival direction $\varphi_{0}$. For a ULA, the arrival direction is specified by the broadside angle. To specify that the maximum response axis (MRA) point towards the $\varphi_{0}$ direction, set the weights to be

$$
\mathbf{w}_{s}=\left(1, e^{i k d \sin \phi_{0}}, e^{i k 2 d \sin \phi_{0}}, \ldots, e^{i k(N-1) d \sin \phi_{0}}\right)
$$

where $d$ is the element spacing and $k=2 \pi / \lambda$ is the wavenumber. An incoming plane wave, coming from any arbitrary direction $\varphi$, is represented by

$$
\mathbf{v}=\left(1, e^{i k d \sin \phi}, e^{i k 2 d \sin \phi}, \ldots, e^{i k(N-1) d \sin \phi}\right)
$$

The conventional response of this array to any incoming plane wave is given by $\mathbf{w}_{s}^{H} \mathbf{v}(\varphi)$ and is shown in the polar plot below as the Sum Pattern. The array is designed to steer towards $\varphi_{0}=30^{\circ}$.

The second pattern, called the Difference Pattern, is obtained by using phased-reversed weights. The weights are determined by phase-reversing the latter half of the conventional steering vector. For an array with an even number of elements, the phase-reversed weights are

$$
\mathbf{w}_{d}=-i\left(1, e^{i k d \sin \phi_{0}}, e^{i k 2 d \sin \phi_{0}}, \ldots, e^{i k N / 2 d \sin \phi_{0}},-e^{i k(N / 2+1) d \sin \phi_{0}}, \ldots,-e^{i k(N-1) d \sin \phi_{0}}\right)
$$

(For an array with an odd number of elements, the middle weight is set to zero). The multiplicative factor $-i$ is used for convenience. The response of the difference array to the incoming vector is

$$
\mathbf{w}_{d}^{H} \mathbf{v}(\varphi)
$$

This figure shows the sum and difference beam patterns of a four-element uniform linear array (ULA) steered $30^{\circ}$ from broadside. The array elements are spaced at one-half wavelength. The sum pattern shows that the array has its maximum response at $30^{\circ}$ and the difference pattern has a null at $30^{\circ}$.


The monopulse response curve is obtained by dividing the difference pattern by the sum pattern and taking the real part.

$$
R(\varphi)=\operatorname{Re}\left(\frac{\mathbf{w}_{d}^{H} \mathbf{v}(\varphi)}{\mathbf{w}_{S}^{H} \mathbf{v}(\varphi)}\right)
$$

To use the monopulse response curve to obtain the arrival angle, $\varphi$, of a narrowband signal, $\mathbf{x}$, compute

$$
z=\operatorname{Re}\left(\frac{\mathbf{w}_{d}^{H} \mathbf{x}}{\mathbf{w}_{s}^{H} \mathbf{x}}\right)
$$

and invert the response curve, $\varphi=R^{-1}(z)$, to obtain $\varphi$.

The response curve is not generally single valued and can only be inverted when arrival angles lie within the main lobe where it is single valued This figure shows the monopulse response curve within the main lobe of the four-element ULA array.


There are two desirable properties of the monopulse response curve. The first is that it have a steep slope. A steep slope insures robustness against noise. The second property is that the mainlobe be as wide as possible. A steep slope is ensure by a larger array but leads to a smaller mainlobe. You will need to trade off one property with the other.

For further details, see [1].

## References

[1] Seliktar, Y. Space-Time Adaptive Monopulse Processing. Ph.D. Thesis. Georgia Institute of Technology, Atlanta, 1998.
[2] Rhodes, D. Introduction to Monopulse. Dedham, MA: Artech House, 1980.

```
See Also
uv2azel|phitheta2azel| azel2uv | azel2phitheta
```


# phased.TimeDelayBeamformer 

Package: phased
Time delay beamformer

## Description

The TimeDelayBeamformer object implements a time delay beamformer.
To compute the beamformed signal:
1 Define and set up your time delay beamformer. See "Construction" on page 1-1703.
2 Call step to perform the beamforming operation according to the properties of phased.TimeDelayBeamformer. The behavior of step is specific to each object in the toolbox.

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step $(o b j, x)$ and $y=o b j(x)$ perform equivalent operations.

## Construction

H = phased.TimeDelayBeamformer creates a time delay beamformer System object, H. The object performs delay and sum beamforming on the received signal using time delays.

H = phased.TimeDelayBeamformer(Name,Value) creates a time delay beamformer object, H, with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN).

## Properties

## SensorArray

Handle to sensor array
Specify the sensor array as a handle. The sensor array must be an array object in the phased package. The array cannot contain subarrays.

Default: phased.ULA with default property values

## PropagationSpeed

Signal propagation speed
Specify the propagation speed of the signal, in meters per second, as a positive scalar. You can specify this property as single or double precision.

Default: Speed of light

## SampleRate

Signal sampling rate
Specify the signal sampling rate (in hertz) as a positive scalar. This property can be specified as single or double precision.

Default: 1e6

## DirectionSource

Source of beamforming direction
Specify whether the beamforming direction comes from the Direction property of this object or from an input argument in step. Values of this property are:

| 'Property' | The Direction property of this object specifies the <br> beamforming direction. |
| :--- | :--- |
| 'Input port' | An input argument in each invocation of step specifies the <br> beamforming direction. |

Default: 'Property'

## Direction

Beamforming direction
Specify the beamforming direction of the beamformer as a column vector of length 2 . The direction is specified in the format of [AzimuthAngle; ElevationAngle] (in degrees). The azimuth angle is between -180 and 180. The elevation angle is between -90 and 90. This property applies when you set the DirectionSource property to 'Property'. This property can be specified as single or double precision.

Default: [0; 0]

## WeightsOutputPort

Output beamforming weights
To obtain the weights used in the beamformer, set this property to true and use the corresponding output argument when invoking step. If you do not want to obtain the weights, set this property to false.

## Default: false

## Methods

step Perform time delay beamforming

## Common to All System Objects

```
release Allow System object property value changes
```


## Examples

## Time-Delay Beamformer Applied to ULA

Apply a time-delay beamformer to an 11 -element uniform linear acoustic array. The arrival angle of the signal is - 50 degrees in azimuth and 30 degrees in elevation. The arriving signal is a 0.3 second segment of a linear FM chirp having a 500 Hz bandwidth. Assume the speed of sound in air is 340.0 $\mathrm{m} / \mathrm{s}$.

Simulate the arriving signal at the wideband collector.

```
microphone = phased.CustomMicrophoneElement('FrequencyVector',[20,20000],'FrequencyResponse',[1,
array = phased.ULA('Element',microphone,'NumElements',11,'ElementSpacing',0.04);
fs = 8000;
t = 0:1/fs:0.3;
x = chirp(t,0,1,500);
c = 340;
collector = phased.WidebandCollector('Sensor',array,...
    'PropagationSpeed',c,'SampleRate',fs,'ModulatedInput',false);
incidentAngle = [-50;30];
x = collector(x.',incidentAngle);
```

Add white Gaussian random noise to the signal.

```
sigma = 0.2;
noise = sigma*randn(size(x));
rx = X + noise;
```

Beamform the incident signals using a time-delay beamformer.

```
beamformer = phased.TimeDelayBeamformer('SensorArray',array,...
    'SampleRate',fs,'PropagationSpeed',c,...
    'Direction',incidentAngle);
y = beamformer(rx);
```

Plot the beamformed signal against the incident signal at the middle sensor of the array.

```
plot(t,rx(:,6),'r:',t,y)
xlabel('Time (sec)')
ylabel('Amplitude')
legend('Original','Beamformed')
```



## Algorithms

## Data Precision

This System object supports single and double precision for input data, properties, and arguments. If the input data X is single precision, the output data is single precision. If the input data X is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

## Version History

Introduced in R2011a

## References

[1] Van Trees, H. Optimum Array Processing. New York: Wiley-Interscience, 2002.

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

Usage notes and limitations:

- Requires dynamic memory allocation. See "Limitations for System Objects that Require Dynamic Memory Allocation".
- See "System Objects in MATLAB Code Generation" (MATLAB Coder).
- This System object supports single and double precision for input data, properties, and arguments. If the input data $X$ is single precision, the output data is single precision. If the input data X is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.


## See Also

phased.FrostBeamformer | phased. PhaseShiftBeamformer |
phased.SubbandPhaseShiftBeamformer|phased.TimeDelayLCMVBeamformer|uv2azel | phitheta2azel

## Topics

"Wideband Beamforming"

## step

System object: phased.TimeDelayBeamformer
Package: phased
Perform time delay beamforming

## Syntax

```
Y = step(H,X)
Y = step(H,X,ANG)
[Y,W] = step(___)
```


## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.
$Y=$ step $(H, X)$ performs time delay beamforming on the input, $X$, and returns the beamformed output in Y . X is an M -by- N matrix where N is the number of elements of the sensor array. Y is a column vector of length M.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
$\mathrm{Y}=\operatorname{step}(\mathrm{H}, \mathrm{X}, \mathrm{ANG})$ uses ANG as the beamforming direction. This syntax is available when you set the DirectionSource property to 'Input port'. ANG is a column vector of length 2 in the form of [AzimuthAngle; ElevationAngle] (in degrees). The azimuth angle must be between -180 and 180 degrees, and the elevation angle must be between -90 and 90 degrees.
[ $\mathrm{Y}, \mathrm{W}$ ] = step( $\qquad$ ) returns additional output, W , as the beamforming weights. This syntax is available when you set the WeightsOutputPort property to true. W is a column vector of length N . For a time delay beamformer, the weights are constant because the beamformer simply adds all the channels together and scales the result to preserve the signal power.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

All input and output arguments can be single or double precision.

## Examples

## Time-Delay Beamformer Applied to ULA

Apply a time-delay beamformer to an 11-element uniform linear acoustic array. The arrival angle of the signal is - 50 degrees in azimuth and 30 degrees in elevation. The arriving signal is a 0.3 second segment of a linear FM chirp having a 500 Hz bandwidth. Assume the speed of sound in air is 340.0 $\mathrm{m} / \mathrm{s}$.

Simulate the arriving signal at the wideband collector.

```
microphone = phased.CustomMicrophoneElement('FrequencyVector',[20,20000],'FrequencyResponse',[1,'
array = phased.ULA('Element',microphone,'NumElements',11,'ElementSpacing',0.04);
fs = 8000;
t = 0:1/fs:0.3;
x = chirp(t,0,1,500);
c = 340;
collector = phased.WidebandCollector('Sensor',array,...
    'PropagationSpeed',c,'SampleRate',fs,'ModulatedInput',false);
incidentAngle = [-50;30];
x = collector(x.',incidentAngle);
```

Add white Gaussian random noise to the signal.

```
sigma = 0.2;
noise = sigma*randn(size(x));
rx = x + noise;
```

Beamform the incident signals using a time-delay beamformer.

```
beamformer = phased.TimeDelayBeamformer('SensorArray',array,...
    'SampleRate',fs,'PropagationSpeed',c,...
    'Direction',incidentAngle);
y = beamformer(rx);
```

Plot the beamformed signal against the incident signal at the middle sensor of the array.

```
plot(t,rx(:,6),'r:',t,y)
xlabel('Time (sec)')
ylabel('Amplitude')
legend('Original','Beamformed')
```



## See Also <br> uv2azel | phitheta2azel

# phased.TimeDelayLCMVBeamformer 

Package: phased
Time delay LCMV beamformer

## Description

The TimeDelayLCMVBeamformer object implements a time-delay linear constraint minimum variance beamformer.

To compute the beamformed signal:
1 Define and set up your time-delay LCMV beamformer. See "Construction" on page 1-1711.
2 Call step to perform the beamforming operation according to the properties of phased.TimeDelayLCMVBeamformer. The behavior of step is specific to each object in the toolbox.

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.

## Construction

H = phased.TimeDelayLCMVBeamformer creates a time-delay linear constraint minimum variance (LCMV) beamformer System object, H. The object performs time delay LCMV beamforming on the received signal.

H = phased.TimeDelayLCMVBeamformer(Name, Value) creates a time-delay LCMV beamformer object, H , with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN).

## Properties

## SensorArray

Handle to sensor array
Specify the sensor array as a handle. The sensor array must be an array object in the phased package. The array cannot contain subarrays.

Default: phased.ULA with default property values

## PropagationSpeed

Signal propagation speed
Specify the propagation speed of the signal, in meters per second, as a positive scalar. You can specify this property as single or double precision.

Default: Speed of light

## SampleRate

Signal sampling rate
Specify the signal sampling rate (in hertz) as a positive scalar. This property can be specified as single or double precision.

Default: 1e6

## FilterLength

FIR filter length
Specify the length of the FIR filter behind each sensor element in the array as a positive integer. This property can be specified as single or double precision.

## Default: 2

## Constraint

Constraint matrix
Specify the constraint matrix used for time-delay LCMV beamformer as an $M$-by- $K$ matrix. Each column of the matrix is a constraint and $M$ is the number of degrees of freedom of the beamformer. For a time-delay LCMV beamformer, the number of degrees of freedom is the product of the number of elements of the array and the filter length specified by the value of the FilterLength property. This property can be specified as single or double precision.

Default: [1;1]

## DesiredResponse

Desired response vector
Specify the desired response used for time-delay LCMV beamformer as a column vector of length $K$, where $K$ is the number of constraints in the Constraint property. Each element in the vector defines the desired response of the constraint specified in the corresponding column of the Constraint property. This property can be specified as single or double precision.

Default: 1, which is equivalent to a distortionless response

## DiagonalLoadingFactor

Diagonal loading factor
Specify the diagonal loading factor as a positive scalar. Diagonal loading is a technique used to achieve robust beamforming performance, especially when the sample support is small. This property is tunable. This property can be specified as single or double precision.

## Default: 0

## TrainingInputPort

Add input to specify training data

To specify additional training data, set this property to true and use the corresponding input argument when you invoke step. To use the input signal as the training data, set this property to false.

## Default: false

## DirectionSource

Source of beamforming direction
Specify whether the beamforming direction comes from the Direction property of this object or from an input argument in step. Values of this property are:

| 'Property' | The Direction property of this object specifies the <br> beamforming direction. |
| :--- | :--- |
| 'Input port' | An input argument in each invocation of step specifies the <br> beamforming direction. |

## Default: 'Property'

## Direction

Beamforming direction
Specify the beamforming direction of the beamformer as a column vector of length 2 . The direction is specified in the format of [AzimuthAngle; ElevationAngle] (in degrees). The azimuth angle is between $-180^{\circ}$ and $180^{\circ}$. The elevation angle is between $-90^{\circ}$ and $90^{\circ}$. This property applies when you set the DirectionSource property to 'Property'. This property can be specified as single or double precision.

Default: [0; 0]

## WeightsOutputPort

Output beamforming weights
To obtain the weights used in the beamformer, set this property to true and use the corresponding output argument when invoking step. If you do not want to obtain the weights, set this property to false.

Default: false

## Methods

step Perform time-delay LCMV beamforming

## Common to All System Objects

| release | Allow System object property value changes |
| :--- | :--- | :--- |

## Examples

## Time-Delay LCMV Beamformer

Apply a time delay LCMV beamformer to an 11-element acoustic ULA array. The elements are omnidirectional microphones. The incident angle of the signal is -50 degrees in azimuth and 30 degrees in elevation. The incident signal is an FM chirp with 500 Hz bandwidth. The propagation speed is a typical speed of sound in air, $340 \mathrm{~m} / \mathrm{s}$.

Simulate the signal and add noise.

```
nElem = 11;
microphone = phased.OmnidirectionalMicrophoneElement(...
    'FrequencyRange',[20 20000]);
array = phased.ULA('Element',microphone,'NumElements',nElem,'ElementSpacing',0.04);
fs = 8000;
t = 0:1/fs:0.3;
x = chirp(t,0,1,500);
c = 340;
collector = phased.WidebandCollector('Sensor',array,...
    'PropagationSpeed',c,'SampleRate',fs,...
    'ModulatedInput',false);
incidentAngle = [-50;30];
x = collector(x.',incidentAngle);
noise = 0.2*randn(size(x));
rx = x + noise;
```

Create and apply the time-delay LCMV beamformer. Specify a filterlength of 5 .

```
filterLength = 5;
constraintMatrix = kron(eye(filterLength),ones(nElem,1));
desiredResponseVector = eye(filterLength,1);
beamformer = phased.TimeDelayLCMVBeamformer('SensorArray',array,...
    'PropagationSpeed',c,'SampleRate',fs,'FilterLength',filterLength,...
    'Direction',incidentAngle,'Constraint',constraintMatrix,...
    'DesiredResponse',desiredResponseVector);
y = beamformer(rx);
```

Compare the beamformer output to the input to the middle sensor.

```
plot(t,rx(:,6),'r:',t,y)
xlabel('Time')
ylabel('Amplitude')
legend('Original','Beamformed')
```



## Algorithms

## Beamforming Algorithms

The beamforming algorithm is the time-domain counterpart of the narrowband linear constraint minimum variance (LCMV) beamformer. The algorithm does the following:

1 Steers the array to the beamforming direction.
2 Applies an FIR filter to the output of each sensor to achieve the specified constraints. The filter is specific to each sensor.

## Data Precision

This System object supports single and double precision for input data, properties, and arguments. If the input data $X$ is single precision, the output data is single precision. If the input data $X$ is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

## References

[1] Frost, O. "An Algorithm For Linearly Constrained Adaptive Array Processing", Proceedings of the IEEE. Vol. 60, Number 8, August, 1972, pp. 926-935.
[2] Van Trees, H. Optimum Array Processing. New York: Wiley-Interscience, 2002.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:

- Requires dynamic memory allocation. See "Limitations for System Objects that Require Dynamic Memory Allocation".
- See "System Objects in MATLAB Code Generation" (MATLAB Coder).
- This System object supports single and double precision for input data, properties, and arguments. If the input data $X$ is single precision, the output data is single precision. If the input data $X$ is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

```
See Also
phased.FrostBeamformer | phased.PhaseShiftBeamformer|
phased.SubbandPhaseShiftBeamformer|phased.TimeDelayBeamformer|uv2azel|
phitheta2azel
Topics
"Wideband Beamforming"
```


## step

System object: phased.TimeDelayLCMVBeamformer
Package: phased
Perform time-delay LCMV beamforming

## Syntax

$Y=\operatorname{step}(H, X)$
$Y=\operatorname{step}(H, X, X T)$
$Y=\operatorname{step}(H, X, A N G)$
$[\mathrm{Y}, \mathrm{W}]=\operatorname{step}($ )

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step (obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.
$Y=\operatorname{step}(H, X)$ performs time-delay LCMV beamforming on the input, $X$, and returns the beamformed output in Y . X is an $M$-by- $N$ matrix where $N$ is the number of elements of the sensor array. $M$ must be larger than the FIR filter length specified in the FilterLength property. Y is a column vector of length $M$.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
$\mathrm{Y}=$ step $(\mathrm{H}, \mathrm{X}, \mathrm{XT})$ uses XT as the training samples to calculate the beamforming weights when you set the TrainingInputPort property to true. XT is an $M$-by- $N$ matrix where $N$ is the number of elements of the sensor array. $M$ must be larger than the FIR filter length specified in the FilterLength property.
$\mathrm{Y}=\operatorname{step}(\mathrm{H}, \mathrm{X}, \mathrm{ANG})$ uses ANG as the beamforming direction, when you set the DirectionSource property to 'Input port'. ANG is a column vector of length 2 in the form of [AzimuthAngle; ElevationAngle] (in degrees). The azimuth angle must be between $-180^{\circ}$ and $180^{\circ}$, and the elevation angle must be between $-90^{\circ}$ and $90^{\circ}$.

You can combine optional input arguments when their enabling properties are set: $\mathrm{Y}=$ step (H, X, XT, ANG)
$[\mathrm{Y}, \mathrm{W}]=\operatorname{step}(\ldots \quad)$ returns additional output, W , as the beamforming weights when you set the WeightsOutputPort property to true. W is a column vector of length $L$, where $L$ is the number of degrees of freedom of the beamformer. For a time-delay LCMV beamformer, the number of degrees of freedom is given by the product of the number of elements of the array and the filter length specified by the value of the FilterLength property.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of
the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

All input and output arguments can be single or double precision.

## Examples

## Time-Delay LCMV Beamformer

Apply a time delay LCMV beamformer to an 11-element acoustic ULA array. The elements are omnidirectional microphones. The incident angle of the signal is -50 degrees in azimuth and 30 degrees in elevation. The incident signal is an FM chirp with 500 Hz bandwidth. The propagation speed is a typical speed of sound in air, $340 \mathrm{~m} / \mathrm{s}$.

Simulate the signal and add noise.

```
nElem = 11;
microphone = phased.OmnidirectionalMicrophoneElement(...
    'FrequencyRange',[20 20000]);
array = phased.ULA('Element',microphone,'NumElements',nElem,'ElementSpacing',0.04);
fs = 8000;
t = 0:1/fs:0.3;
x = chirp(t,0,1,500);
c = 340;
collector = phased.WidebandCollector('Sensor',array,...
    'PropagationSpeed',c,'SampleRate',fs,...
    'ModulatedInput',false);
incidentAngle = [-50;30];
x = collector(x.',incidentAngle);
noise = 0.2*randn(size(x));
rx = x + noise;
```

Create and apply the time-delay LCMV beamformer. Specify a filterlength of 5 .

```
filterLength = 5;
constraintMatrix = kron(eye(filterLength),ones(nElem,1));
desiredResponseVector = eye(filterLength,1);
beamformer = phased.TimeDelayLCMVBeamformer('SensorArray',array,...
    'PropagationSpeed',c,'SampleRate',fs,'FilterLength',filterLength,...
    'Direction',incidentAngle,'Constraint',constraintMatrix,...
    'DesiredResponse',desiredResponseVector);
y = beamformer(rx);
```

Compare the beamformer output to the input to the middle sensor.

```
plot(t,rx(:,6),'r:',t,y)
xlabel('Time')
ylabel('Amplitude')
legend('Original','Beamformed')
```



## Algorithms

The beamforming algorithm is the time-domain counterpart of the narrowband linear constraint minimum variance (LCMV) beamformer. The algorithm does the following:

1 Steers the array to the beamforming direction.
2 Applies an FIR filter to the output of each sensor to achieve the specified constraints. The filter is specific to each sensor.

## See Also

uv2azel|phitheta2azel

## phased.TimeVaryingGain

Package: phased
Time varying gain control

## Description

The TimeVaryingGain object applies a time varying gain to input signals. Time varying gain (TVG) is sometimes called automatic gain control (AGC).

To apply the time varying gain to the signal:
1 Define and set up your time varying gain controller. See "Construction" on page 1-1720.
2 Call step to apply the time varying gain according to the properties of phased.TimeVaryingGain. The behavior of step is specific to each object in the toolbox.

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.

## Construction

H = phased.TimeVaryingGain creates a time varying gain control System object, H. The object applies a time varying gain to the input signal to compensate for the signal power loss due to the range.

H = phased.TimeVaryingGain(Name,Value) creates an object, H , with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN).

## Properties

## RangeLossSource

Source of range losses
Specify the source of range losses as either 'Property' or 'Input port'. When you specify RangeLossSource as 'Property', the range loss for each sample is set in the RangeLoss property. When you specify the RangeLossSource as 'Input port', the range losses are specified using an input argument to the step method.

Default: 'Property'

## RangeLoss

Loss at each input sample range
Specify the loss due to range as a vector - elements correspond to the samples in the input signal. Units are in dB . This property can have single or double precision.

## Default: 0

## ReferenceLoss

Loss at reference range
Specify the loss at a given reference range as a scalar. Units are in dB . This property can have single or double precision.

## Default: 0

## Methods

step Apply time varying gains to input signal

## Common to All System Objects <br> release $\quad$ Allow System object property value changes

## Examples

## Apply Time Varying Gain to Adjust for Range Loss

Apply time varying gain to a signal to compensate for signal power loss due to range.
First, create a signal with range loss. Set the reference loss to 16 dB .

```
rngloss = 10:22;
refloss = 16;
t = (1:length(rngloss))';
x = 1./db2mag(rngloss(:));
```

Then add gain to compensate for range loss.

```
gain = phased.TimeVaryingGain('RangeLoss',rngloss,'ReferenceLoss',refloss);
y = gain(x);
```

Plot the signal with loss and the compensated signal.

```
tref = find(rngloss==refloss);
stem([t t],[abs(x) abs(y)])
hold on
stem(tref,x(tref),'filled','r')
xlabel('Time (s)'); ylabel('Magnitude (V)')
grid on
legend('Before time varying gain','After time varying gain',...
    'Reference range')
```



## Algorithms

## Data Precision

This System object supports single and double precision for input data, properties, and arguments. If the input data X is single precision, the output data is single precision. If the input data X is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.

## Version History

## Introduced in R2011a

## References

[1] Edde, B. Radar: Principles, Technology, Applications. Englewood Cliffs, NJ: Prentice Hall, 1993.
[2] Skolnik, M. Introduction to Radar Systems, 3rd Ed. New York: McGraw-Hill, 2001.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\text {TM }}$.
Usage notes and limitations:

- See "System Objects in MATLAB Code Generation" (MATLAB Coder).
- This System object supports single and double precision for input data, properties, and arguments. If the input data $X$ is single precision, the output data is single precision. If the input data X is double precision, the output data is double precision. The precision of the output is independent of the precision of the properties and other arguments.


## See Also

phased.MatchedFilter|pulsint

## step

System object: phased.TimeVaryingGain
Package: phased
Apply time varying gains to input signal

## Syntax

Y = step( $\mathrm{H}, \mathrm{X}$ )
Y = step(H,X,L)

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step (obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.
$Y=$ step $(H, X)$ applies time varying gains to the input signal matrix $X$. The process equalizes power levels across all samples to match a given reference range. The compensated signal is returned in Y . $X$ can be a column vector, a matrix, or a cube. The gain is applied to each column in $X$ independently. The number of rows in $X$ cannot exceed the length of the loss vector specified in the RangeLoss property. Y has the same dimensionality as X . X can be single or double precision.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
$\mathrm{Y}=\operatorname{step}(\mathrm{H}, \mathrm{X}, \mathrm{L})$ in addition, specifies the range loss, L as a columns vector. Use this argument only when you set the RangeLossSource property to 'Input port'. The length of $L$ must be equal to or greater than the number of rows of $X$. $L$ can be single or double precision.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Examples

## Apply Time Varying Gain to Adjust for Range Loss

Apply time varying gain to a signal to compensate for signal power loss due to range.
First, create a signal with range loss. Set the reference loss to 16 dB .
rngloss = 10:22;
refloss = 16;
t = (1:length(rngloss))';
$x=1 . / d b 2 m a g(r n g l o s s(:))$;
Then add gain to compensate for range loss.

```
gain = phased.TimeVaryingGain('RangeLoss',rngloss,'ReferenceLoss',refloss);
y = gain(x);
```

Plot the signal with loss and the compensated signal.

```
tref = find(rngloss==refloss);
stem([t t],[abs(x) abs(y)])
hold on
stem(tref,x(tref),'filled','r')
xlabel('Time (s)'); ylabel('Magnitude (V)')
grid on
legend('Before time varying gain','After time varying gain',...
    'Reference range')
```



# phased.Transmitter 

Package: phased
Transmitter

## Description

The Transmitter object implements a waveform transmitter.
To compute the transmitted signal:
1 Define and set up your waveform transmitter. See "Construction" on page 1-1726.
2 Call step to compute the transmitted signal according to the properties of phased.Transmitter. The behavior of step is specific to each object in the toolbox.

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step $(o b j, x)$ and $y=o b j(x)$ perform equivalent operations.

## Construction

$H=$ phased. Transmitter creates a transmitter System object, H. This object transmits the input waveform samples with specified peak power.

H = phased.Transmitter(Name, Value) creates a transmitter object, H, with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN).

## Properties

## PeakPower

Peak power
Specify the transmit peak power (in watts) as a positive scalar.
Default: 5000

## Gain

Transmit gain
Specify the transmit gain (in decibels) as a real scalar.
Default: 20
LossFactor
Loss factor

Specify the transmit loss factor (in decibels) as a nonnegative scalar.
Default: 0
InUseOutputPort
Enable transmitter status output
To obtain the transmitter in-use status for each output sample, set this property to true and use the corresponding output argument when invoking step. In this case, 1's indicate the transmitter is on, and 0's indicate the transmitter is off. If you do not want to obtain the transmitter in-use status, set this property to false.

Default: false
CoherentOnTransmit
Preserve coherence among pulses
Specify whether to preserve coherence among transmitted pulses. When you set this property to true, the transmitter does not introduce any random phase to the output pulses. When you set this property to false, the transmitter adds a random phase noise to each transmitted pulse. The random phase noise is introduced by multiplication of the pulse by $e^{i \phi}$ where $\phi$ is a uniform random variable on the interval $[0,2 \pi]$.

## Default: true

## PhaseNoiseOutputPort

Enable pulse phase noise output
To obtain the introduced transmitter random phase noise for each output sample, set this property to true and use the corresponding output argument when invoking step. You can use in the receiver to simulate coherent on receive systems. If you do not want to obtain the random phase noise, set this property to false. This property applies when you set the CoherentOnTransmit property to false.

Default: false

## SeedSource

Source of seed for random number generator

| 'Auto ' | The default MATLAB random number generator produces the <br> random numbers. Use 'Auto 'if you are using this object with <br> Parallel Computing Toolbox software. |
| :--- | :--- |
| 'Property ' | The object uses its own private random number generator to <br> produce random numbers. The Seed property of this object <br> specifies the seed of the random number generator. Use <br> 'Property if you want repeatable results and are not using this <br> object with Parallel Computing Toolbox software. |

This property applies when you set the CoherentOnTransmit property to false.
Default: 'Auto'

## Seed

Seed for random number generator
Specify the seed for the random number generator as a scalar integer between 0 and $2^{32}-1$. This property applies when you set the CoherentOnTransmit property to false and the SeedSource property to 'Property'.

Default: 0

## Methods

reset Reset states of transmitter object
step Transmit pulses
Common to All System Objects
release Allow System object property value changes

## Examples

## Transmit LFM Pulse

Transmit a pulse containing a linear FM waveform with a bandwidth of 5 MHz . The sample rate is 10 MHz and the pulse repetition frequency is 10 kHz .

```
fs = 1e7;
waveform = phased.LinearFMWaveform('SampleRate',fs, ...
    'PulseWidth',1e-5,'SweepBandwidth',5e6);
x = waveform();
transmitter = phased.Transmitter('PeakPower',5e3);
y = transmitter(x);
```


## Version History

Introduced in R2011a

## References

[1] Edde, B. Radar: Principles, Technology, Applications. Englewood Cliffs, NJ: Prentice Hall, 1993.
[2] Richards, M. A. Fundamentals of Radar Signal Processing. New York: McGraw-Hill, 2005.
[3] Skolnik, M. Introduction to Radar Systems, 3rd Ed. New York: McGraw-Hill, 2001.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

Usage notes and limitations:
See "System Objects in MATLAB Code Generation" (MATLAB Coder).
See Also
phased. Radiator | phased. ReceiverPreamp

## reset

System object: phased.Transmitter
Package: phased
Reset states of transmitter object

## Syntax

reset (H)

## Description

reset (H) resets the states of the Transmitter object, H. This method resets the random number generator state if the SeedSource property is applicable and has the value 'Property'.

## step

System object: phased.Transmitter
Package: phased
Transmit pulses

## Syntax

Y = step(H,X)
[Y,STATUS] = step(H,X)
[Y,PHNOISE] = $\operatorname{step}(H, X)$

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.
$Y=\operatorname{step}(H, X)$ returns the transmitted signal $Y$, based on the input waveform $X . Y$ is the amplified X where the amplification is based on the characteristics of the transmitter, such as the peak power and the gain.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
[ $\mathrm{Y}, \mathrm{STATUS}$ ] $=\operatorname{step}(\mathrm{H}, \mathrm{X})$ returns additional output STATUS as the on/off status of the transmitter when the InUseOutputPort property is true. STATUS is a logical vector where true indicates the transmitter is on for the corresponding sample time, and false indicates the transmitter is off.
[ $\mathrm{Y}, \mathrm{PHNOISE}]=\operatorname{step}(\mathrm{H}, \mathrm{X})$ returns the additional output PHNOISE as the random phase noise added to each transmitted sample when the CoherentOnTransmit property is false and the PhaseNoiseOutputPort property is true. PHNOISE is a vector which has the same dimension as Y. Each element in PHNOISE contains the random phase between 0 and $2 *$ pi, added to the corresponding sample in $Y$ by the transmitter.

You can combine optional output arguments when their enabling properties are set. Optional outputs must be listed in the same order as the order of the enabling properties. For example:
[Y,STATUS,PHNOISE] = step(H,X)

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Examples

## Transmit LFM Pulse

Transmit a pulse containing a linear FM waveform with a bandwidth of 5 MHz . The sample rate is 10 MHz and the pulse repetition frequency is 10 kHz .
fs $=1 \mathrm{e} 7$;
waveform = phased.LinearFMWaveform('SampleRate',fs, ...
'PulseWidth',1e-5, 'SweepBandwidth',5e6);
x = waveform();
transmitter = phased.Transmitter('PeakPower',5e3);
y = transmitter $(x)$;

## phased.UCA

Package: phased
Uniform circular array

## Description

The phased. UCA System object creates a uniform circular array (UCA). A UCA is formed from identical sensor elements equally spaced around a circle.

To compute the response for the array for specified directions:
1 Define and set up your uniform circular array. See "Construction" on page 1-1733.
2 Call step to compute the response according to the properties of phased.UCA. The behavior of step is specific to each object in the toolbox.

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = $\underline{\text { step }(o b j, x) \text { and } y=o b j(x) \text { perform equivalent operations. }}$

## Construction

sUCA $=$ phased. UCA creates a uniform circular array (UCA) System object, sUCA, consisting of five identical isotropic antenna elements, phased. IsotropicAntennaElement. The elements are equally spaced around a circle of radius 0.5 meters.
sUCA $=$ phased. UCA(Name, Value) creates a System object, sUCA, with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Name1, Value1,...,NameN, ValueN).
sUCA = phased.UCA( $N, R$ ) creates a UCA System object, sUCA, with the NumElements property set to N and the Radius property set to R . This syntax creates a UCA consisting of isotropic antenna elements, phased.IsotropicAntennaElement.
sUCA $=$ phased.UCA( $N, R$, Name, Value) creates a UCA System object, sUCA, with the NumElements property set to $\mathbf{N}$, the Radius property set to R, and other specified property Names set to the specified Values.

## Properties

## Element - phased array element

isotropic antenna element System object with default properties (default) | Phased Array System Toolbox antenna, microphone, or transducer element System object | Antenna Toolbox antenna System object

Phased array element, specified as a Phased Array System Toolbox antenna, microphone, or transducer element or Antenna Toolbox antenna.

Example: phased. CosineAntennaElement

## NumElements - Number of array elements

5 (default) | integer greater than one
Number of array elements, specified as an integer greater than one.
Example: 3

## Radius - Array radius

0.5 (default) | positive scalar

Array radius, specified as a positive scalar in meters.
Example: 2.5

## ArrayNormal - Array normal direction

```
'z' (default)| 'x'|'y'
```

Array normal direction, specified as one of ' $x$ ', ' $y$ ', or ' $z$ '. UCA elements lie in a plane orthogonal to the array normal direction. Element boresight vectors lie in the same plane and point radially outward from the origin.

| ArrayNormal Property Value | Element Positions and Boresight Directions |
| :--- | :--- |
| ' $x$ ' | Array elements lie on the $y z$-plane. All element <br> boresight vectors lie in the $y z$-plane and point <br> outward from the array center. |
| ' $y$ ' | Array elements lie on the $z x$-plane. All element <br> boresight vectors lie in the $z x$-plane and point <br> outward from the array center. |
| ' $z$ ' | Array elements lie on the $x y$-plane. All element <br> boresight vectors lie in the $x y$-plane and point <br> outward from the array center. |

Example: 'y '

## Taper - Element tapering

1 (default) | complex-valued scalar | complex-valued 1-by- $N$ row vector | complex-valued $N$-by- 1 column vector

Element tapering or weighting, specified as a complex-valued scalar, 1 -by- $N$ row vector, or $N$-by-1 column vector. The quantity $N$ represents the number of elements of the array. Tapers, also known as weights, are applied to each sensor element in the sensor array and modify both the amplitude and phase of the received data. If 'Taper' is a scalar, the same taper value is applied to all element. If 'Taper' is a vector, each taper value is applied to the corresponding sensor element.

## Example: [1 2321$]$

## Methods

| Specific to phased.UCA Object |  |
| :--- | :--- |
| beamwidth | Compute and display beamwidth of an array |
| collectPla <br> neWave | Simulate received plane waves |


| Specific to phased.UCA Object |  |
| :--- | :--- |
| directivit <br> y |  |
| getElement <br> Normal | Directivity of uniform circular array |
| getElement <br> Position | Positions of array elements |
| getElement <br> Spacing | Spacing between array elements |
| getNumElem <br> ents | Number of elements in array |
| getTaper | Array element tapers |
| isPolariza <br> tionCapabl <br> e | Polarization capability |
| pattern | Plot UCA array pattern |
| patternAzi <br> muth | Plot UCA array directivity or pattern versus azimuth |
| patternEle <br> vation | Plot UCA array directivity or pattern versus elevation |
| perturbati <br> ons | Perturbations defined on phased array |
| perturbedA <br> rray | Apply perturbations to phased array |
| perturbedP <br> attern | Compute and plot azimuth pattern of perturbed array |
| step | Output responses of array elements |
| viewArray | View array geometry |

## Common to All System Objects

release $\quad$ Allow System object property value changes

## Examples

## Pattern of 11-Element UCA Antenna Array

Create an 11 -element uniform circular array (UCA) having a 1.5 m radius and operating at 500 MHz .
The array consists of short-dipole antenna elements. First, display the vertical component of the response at 45 degrees azimuth and 0 degrees elevation. Then plot the azimuth and elevation directivities.

```
antenna = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[50e6,1000e6],...
    'AxisDirection','Z');
array = phased.UCA('NumElements',11,'Radius',1.5,'Element',antenna);
```

```
fc = 500e6;
ang = [45;0];
resp = array(fc,ang);
disp(resp.V)
    -1.2247
    -1.2247
    -1.2247
    -1.2247
    -1.2247
    -1.2247
    -1.2247
    -1.2247
    -1.2247
    -1.2247
    -1.2247
```

Display the azimuth directivity pattern at 500 MHz for azimuth angles between -180 and 180 degrees.
c = physconst('LightSpeed');
pattern(array,fc,[-180:180],0,'Type','directivity','PropagationSpeed', c)


Directivity (dBi), Broadside at $0.00^{\circ}$

Display the elevation directivity pattern at 500 MHz for elevation angles between -90 and 90 degrees.
pattern(array,fc,[0],[-90:90],'Type','directivity','PropagationSpeed', c)


Directivity (dBi), Broadside at $0.00^{\circ}$

## Algorithms

A UCA is formed from $N$ identical sensor elements equally spaced around a circle of radius $R$. The circle lies in the $x y$-plane of the local coordinate system whose origin lies at the center of the circle. The positions of the elements are defined with respect to the local array coordinate system. The circular array lies in the $x y$-plane of the coordinate system. The normal to the UCA plane lies along the positive $z$-axis. The elements are oriented so that their main response directions (normals) point radially outward in the $x y$-plane.


If the number of elements of the array is odd, the middle element lies on the $x$-axis. If the number of elements is even, the midpoint between the two middle elements lies on the $x$-axis. For an array of $N$ elements, the azimuth angle of the position of the nth element is given by

$$
\varphi_{n}=(-(N-1) / 2+n-1) \cdot 360 / N \quad n=1, \ldots, N
$$

The azimuth angle is defined as the angle, in the $x y$-plane, from the $x$-axis toward the $y$-axis. The elevation angle is defined as the angle from the $x y$-plane toward the $z$-axis. The angular distance between any two adjacent elements is $360 / \mathrm{N}$ degrees. Azimuth angle values are in degrees. Elevation angles for all array elements are zero.

## Version History

## Introduced in R2015a

## References

[1] Brookner, E., ed. Radar Technology. Lexington, MA: LexBook, 1996.
[2] Van Trees, H. Optimum Array Processing. New York: Wiley-Interscience, 2002, pp. 274-304.

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:

- pattern, patternAzimuth, patternElevation, plotResponse, and viewArray methods are not supported.
- See "System Objects in MATLAB Code Generation" (MATLAB Coder).


## See Also

phased.ULA | phased.URA | phased.ConformalArray | phased.CosineAntennaElement |
phased.CrossedDipoleAntennaElement|phased.CustomAntennaElement|
phased.IsotropicAntennaElement|phased.ShortDipoleAntennaElement|
phased.CustomMicrophoneElement| phased.OmnidirectionalMicrophoneElement

## Topics

"Phased Array Gallery"

## directivity

System object: phased. UCA
Package: phased
Directivity of uniform circular array

## Syntax

D = directivity(sArray, FREQ, ANGLE)
D = directivity(sArray, FREQ,ANGLE,Name, Value)

## Description

D = directivity (sArray, FREQ, ANGLE) returns the "Directivity (dBi)" on page 1-1743 of a uniform circular array (UCA) of antenna or microphone elements, sArray, at frequencies specified by FREQ and in angles of direction specified by ANGLE.

The integration used when computing array directivity has a minimum sampling grid of 0.1 degrees. If an array pattern has a beamwidth smaller than this, the directivity value will be inaccurate.

D = directivity(sArray, FREQ,ANGLE,Name, Value) returns the directivity with additional options specified by one or more Name, Value pair arguments.

## Input Arguments

## sArray - Uniform circular array

System object
Uniform circular array, specified as a phased. UCA System object.
Example: sArray= phased.UCA;

## FREQ - Frequency for computing directivity and patterns

positive scalar | 1-by-L real-valued row vector
Frequencies for computing directivity and patterns, specified as a positive scalar or 1-by-L realvalued row vector. Frequency units are in hertz.

- For an antenna, microphone, or sonar hydrophone or projector element, FREQ must lie within the range of values specified by the FrequencyRange or FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased. CustomAntennaElement and phased.CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: [1e8 2e6]
Data Types: double

## ANGLE - Angles for computing directivity

## 1-by- $M$ real-valued row vector | 2-by- $M$ real-valued matrix

Angles for computing directivity, specified as a 1-by- $M$ real-valued row vector or a 2 -by- $M$ real-valued matrix, where $M$ is the number of angular directions. Angle units are in degrees. If ANGLE is a 2 -by- $M$ matrix, then each column specifies a direction in azimuth and elevation, [az;el]. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

If ANGLE is a $1-b y-M$ vector, then each entry represents an azimuth angle, with the elevation angle assumed to be zero.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the xy plane. This angle is positive when measured from the $x$-axis toward the $y$-axis. The elevation angle is the angle between the direction vector and $x y$ plane. This angle is positive when measured towards the $z$-axis. See "Azimuth and Elevation Angles".
Example: [45 60; 0 10]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Namel=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## PropagationSpeed - Signal propagation speed

speed of light (default) | positive scalar
Signal propagation speed, specified as the comma-separated pair consisting of ' PropagationSpeed ' and a positive scalar in meters per second.
Example: 'PropagationSpeed', physconst('LightSpeed')
Data Types: double
Weights - Array weights
1 (default) $\mid N$-by-1 complex-valued column vector $\mid N$-by- $L$ complex-valued matrix
Array weights, specified as the comma-separated pair consisting of 'Weights' and an $N$-by- 1 complex-valued column vector or $N$-by- $L$ complex-valued matrix. Array weights are applied to the elements of the array to produce array steering, tapering, or both. The dimension $N$ is the number of elements in the array. The dimension $L$ is the number of frequencies specified by FREQ.

| Weights Dimension | FREQ Dimension | Purpose |
| :--- | :--- | :--- |
| $N$-by-1 complex-valued column <br> vector | Scalar or 1-by- $L$ row vector | Applies a set of weights for the <br> single frequency or for all $L$ <br> frequencies. |
| $N$-by- $L$ complex-valued matrix | 1-by- $L$ row vector | Applies each of the $L$ columns of <br> 'Weights ' for the <br> corresponding frequency in <br> FREQ. |

Note Use complex weights to steer the array response toward different directions. You can create weights using the phased.SteeringVector System object or you can compute your own weights. In general, you apply Hermitian conjugation before using weights in any Phased Array System Toolbox function or System object such as phased. Radiator or phased. Collector. However, for the directivity, pattern, patternAzimuth, and patternElevation methods of any array System object use the steering vector without conjugation.

## Example: 'Weights', ones ( $\mathrm{N}, \mathrm{M}$ )

Data Types: double
Complex Number Support: Yes

## Output Arguments

## D - Directivity <br> M-by-L matrix

Directivity, returned as an $M$-by- $L$ matrix. Each row corresponds to one of the $M$ angles specified by ANGLE. Each column corresponds to one of the $L$ frequency values specified in FREQ. Directivity units are in dBi where dBi is defined as the gain of an element relative to an isotropic radiator.

## Examples

## Directivity of UCA

Compute the directivity of two uniform circular arrays (UCA) at zero degrees azimuth and elevation. The first array consists of isotropic antenna elements. The second array consists of cosine antenna elements. In addition, compute the directivity of the cosine element array steered to a 45 degrees elevation.

## Array of isotropic antenna elements

First, create a 10 -element UCA with a radius of one-half meter consisting of isotropic antenna elements. Set the signal frequency to 300 MHz .

```
c = physconst('LightSpeed');
fc = 300e6;
sIso = phased.IsotropicAntennaElement;
sArray = phased.UCA('Element',sIso,'NumElements',10,'Radius',0.5);
ang = [0;0];
d = directivity(sArray,fc,ang,'PropagationSpeed',c)
d = -1.1423
```


## Array of cosine antenna elements

Next, create a 10 -element UCA of cosine antenna elements also with a 0.5 meter radius.

```
sCos = phased.CosineAntennaElement('CosinePower',[3,3]);
sArray1 = phased.UCA('Element',sCos,'NumElements',10,'Radius',0.5);
ang = [0;0];
d = directivity(sArray1,fc,ang,'PropagationSpeed',c)
d = 3.2550
```

The directivity is increased due to the added directivity of the cosine antenna elements.

## Steered array of cosine antenna elements

Finally, steer the cosine antenna array toward 45 degrees elevation, and then examine the directivity at 45 degrees.

```
ang = [0;45];
lambda = c/fc;
w = steervec(getElementPosition(sArray1)/lambda,ang);
d = directivity(sArray1,fc,ang,'PropagationSpeed',c,...
    'Weights',w)
d = -3.1410
```

The directivity is decreased because of the combined reduction of directivity of the elements and the array.

## More About

## Directivity (dBi)

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \Pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\mathrm{total}}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Version History

Introduced in R2015a

See Also<br>pattern | patternAzimuth | patternElevation

## collectPlaneWave

System object: phased. UCA
Package: phased
Simulate received plane waves

## Syntax

Y = collectPlaneWave(H,X,ANG)
$Y=$ collectPlaneWave( $\mathrm{H}, \mathrm{X}, \mathrm{ANG}, \mathrm{FREQ}$ )
Y = collectPlaneWave( $\mathrm{H}, \mathrm{X}, \mathrm{ANG}, \mathrm{FREQ}, \mathrm{C})$

## Description

$Y=$ collectPlaneWave $(H, X, A N G)$ returns the received signals at the sensor array, $H$, when the input signals indicated by $X$ arrive at the array from the directions specified in ANG.
$Y=$ collectPlaneWave( $H, X, A N G, F R E Q)$, in addition, specifies the incoming signal carrier frequency in FREQ.
$\mathrm{Y}=$ collectPlaneWave( $\mathrm{H}, \mathrm{X}, \mathrm{ANG}, \mathrm{FREQ}, \mathrm{C})$, in addition, specifies the signal propagation speed in C.

## Input Arguments

H - Uniform circular array
System object
Uniform circular array specified as a phased. UCA System object.
Example: $\mathrm{H}=$ phased.UCA();
X - Incoming signals
$M$-column matrix
Incoming signals, specified as an $M$-column matrix. Each column of $X$ represents an individual incoming signal.
Example: [1,5;2,10;3,10]
Data Types: double
Complex Number Support: Yes

## ANG - Arrival directions of incoming signals

1 -by- $M$ real-valued vector | 2 -by- $M$ real-valued matrix
Arrival directions of incoming signals, specified as a 1 -by- $M$ vector or a 2 -by- $M$ matrix, where $M$ is the number of incoming signals. Each column specifies the direction of arrival of the corresponding signal in X. If ANG is a 2-by-M matrix, each column specifies the direction in azimuth and elevation of the incoming signal [az;el]. Angular units are in degrees. The azimuth angle must lie between $180^{\circ}$ and $180^{\circ}$ and the elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

If ANG is a 1 -by- $M$ vector, then each entry represents a set of azimuth angles, with the elevation angles assumed to be zero.

The azimuth angle is the angle between the $x$-axis and the projection of the arrival direction vector onto the $x y$ plane. When measured from the $x$-axis toward the $y$-axis, the azimuth angle is positive.

The elevation angle is the angle between the arrival direction vector and the $x y$-plane. When measured toward the $z$ axis, the elevation angle is positive.

Example: [20, 30;15, 25]
Data Types: double

## FREQ - Signal carrier frequency

3e8 (default) | positive scalar
Signal carrier frequency, specified as a positive scalar in hertz.
Data Types: double

## C - Signal propagation speed

speed of light (default) | positive scalar
Signal propagation speed, specified as a positive scalar in meters per second.
Example: physconst('LightSpeed')
Data Types: double

## Output Arguments

## Y - Received signals

$N$-column complex-valued row vector
Received signals, returned as an $N$-column complex-valued row vector. The quantity $N$ is the number of elements in the array. Each column of $Y$ contains the combined received signals at the corresponding array element.

## Examples

## Simulate Received Signal at 5-Element UCA

Create a random signal arriving at a 5-element UCA from 10 degrees azimuth and 30 degrees azimuth. Both signals have an elevation angle of 0 degrees. Assume the propagation speed is the speed of light and the carrier frequency of the signal is 100 MHz . The signals are two random noise signals of three samples each.

```
sUCA = phased.UCA('NumElements',5,'Radius',2.0);
y = collectPlaneWave(sUCA,randn(3,2),[10 30],100e6,...
    physconst('LightSpeed'));
disp(y)
\begin{tabular}{rrrrrrr}
\(-0.8817+1.0528 i\) & \(1.0037-0.3636 i\) & \(-1.0579-0.8531 i\) & \(-1.0698+0.5187 i\) & \(-0.6388-0.9769 i\) \\
\(-1.6512+1.3471 i\) & \(1.7358+0.7662 i\) & \(-1.2932-1.6792 i\) & \(-1.0279+1.6997 i\) & \(-1.8283-0.7336 i\) \\
\(2.5071-2.4424 i\) & \(-2.7270-0.2435 i\) & \(2.4009+2.4977 i\) & \(2.1808-2.1178 i\) & \(2.3743+1.8105 i\)
\end{tabular}
```


## Algorithms

collectPlaneWave modulates the input signal with a phase corresponding to the delay caused by the direction of arrival. The method does not account for the response of individual elements in the array.

For further details, see [1].

## Version History

Introduced in R2015a

## References

[1] Van Trees, H. Optimum Array Processing. New York: Wiley-Interscience, 2002.

## See Also <br> uv2azel | phitheta2azel

## getElementNormal

System object: phased.UCA
Package: phased
Normal vectors for array elements

## Syntax

normvec = getElementNormal(sArray)
normvec = getElementNormal(sArray,elemidx)

## Description

normvec $=$ getElementNormal(sArray) returns the element normals of the phased. UCA System object, sArray. normv is a 2-by- $N$ matrix, where $N$ is the number of elements in sArray. Each column of normv specifies the normal direction of the corresponding element in the local coordinate system in the form [azimuth; elevation]. Units are degrees. For details regarding the local coordinate system of a UCA, type
phased.UCA.coordinateSystemInfo;
at the command line.
normvec $=$ getElementNormal(sArray, elemidx) returns only the normals of the elements that are specified in the element index vector elemidx.

## Input Arguments

## sArray - Uniform circular array

phased.UCA System object
Uniform circular array, specified as a phased.UCA System object.
Example: phased.UCA
elemidx - Element index vector
all elements (default) | vector of positive integers
Element index vector, specified as a vector of positive integers each of which takes a value from 1 to $N$. The dimension $N$ is the number of elements of the array.
Example: [1, 2, 3]

## Output Arguments

normvec - Normal vector
2-by-M real-valued matrix
Normal vector of array elements, returned as a 2-by- $M$ real matrix. Each column of normvec specifies the normal direction of the corresponding element in the local coordinate system in the form
[azimuth;elevation]. Units are degrees. If the input argument elemidx is not specified, $M$ is the number of elements of the array, $N$. If elemidx is specified, $M$ is the dimension of elemidx.

## Examples

## UCA Element Normal Vectors

Construct three different 7 -element UCA with a radius of 0.5 meters, and obtain the normal vectors of the middle three elements. Choose the array normal vectors to point along the $x-, y$-, and $z$-axes.

First, choose the array normal along the $x$-axis.

```
sUCA1 = phased.UCA('NumElements',7,'Radius',0.5,'ArrayNormal','x');
pos = getElementPosition(sUCA1,[3,4,5])
pos = 3\times3
\begin{tabular}{rrr}
0 & 0 & 0 \\
0.3117 & 0.5000 & 0.3117 \\
-0.3909 & 0 & 0.3909
\end{tabular}
normvec = getElementNormal(sUCA1,[3,4,5])
normvec = 2×3
\begin{tabular}{rrr}
90.0000 & 90.0000 & 90.0000 \\
-51.4286 & 0 & 51.4286
\end{tabular}
```

These outputs show that the array elements lie in the $y z$-plane. The normal vectors of the array elements also lie in the $y z$-plane and point outward like spokes on a wheel.

Next, choose the array normal along the $y$-axis.

```
sUCA2 = phased.UCA('NumElements',7,'Radius',0.5,'ArrayNormal','y');
pos = getElementPosition(sUCA2,[3,4,5])
pos = 3\times3
\begin{tabular}{rrr}
0.3117 & 0.5000 & 0.3117 \\
0 & 0 & 0 \\
-0.3909 & 0 & 0.3909
\end{tabular}
normvec = getElementNormal(sUCA2,[3,4,5])
normvec = 2×3
\begin{tabular}{rrr}
0 & 0 & 0 \\
-51.4286 & 0 & 51.4286
\end{tabular}
```

These outputs show that the array elements lie in the $z x$-plane. The normal vectors of the array elements also lie in the $z x$-plane and also point outward.

Finally, set the array normal along the $z$-axis. This is the default value of array normal.

```
sUCA3 = phased.UCA('NumElements',7,'Radius',0.5,'ArrayNormal','z');
pos = getElementPosition(sUCA3,[3,4,5])
pos = 3\times3
    0.3117 0.5000 0.3117
    -0.3909 0
normvec = getElementNormal(sUCA3,[3,4,5])
normvec = 2×3
    -51.4286 0 51.4286
        0 0 0
```

These outputs show that the array elements lie in the $x y$-plane. The normal vectors of the array elements also lie in the xy-plane and also point outward.

## Version History

Introduced in R2015a

## getElementPosition

System object: phased. UCA
Package: phased
Positions of array elements

## Syntax

pos $=$ getElementPosition(sUCA)
pos = getElementPosition(sUCA,elemidx)

## Description

pos $=$ getElementPosition (sUCA) returns the element positions of the phased.UCA System object, sUCA. pos is a 3-by- $N$ matrix, where $N$ is the number of elements in sUCA. Each column of pos defines the position of an element in the local coordinate system, in meters, using the form $[x ; y ; z]$. The origin of the local coordinate system is the center of the circular array.
pos = getElementPosition(sUCA, elemidx) returns only the positions of the elements that are specified in the element index vector elemidx.

## Input Arguments

## sUCA - Uniform circular array

phased.UCA System object
Uniform circular array, specified as a phased.UCA System object.
Example: phased. UCA

## elemidx - Element index vector

all elements (default) | vector of positive integers
Element index vector, specified as a vector of positive integers each of which takes a value from 1 to $N$. The quantity $N$ is the number of elements of the array.
Example: [1, 2, 3]

## Output Arguments

## pos - Positions of array elements

3-by-M real matrix
Positions of array elements, returned as a 3-by-M real matrix. If the input argument elemidx is not specified, $M$ is the number of elements of the array, $N$. If elemidx is specified, $M$ is the dimension of elemidx.

## Examples

## Positions of UCA Elements

Construct a 7 -element UCA with a radius of 0.5 meters, and obtain the positions of the middle three elements.
sArray = phased.UCA('NumElements',7,'Radius',0.5); pos $=$ getElementPosition(sArray,[3,4,5])
pos $=3 \times 3$

| 0.3117 | 0.5000 | 0.3117 |
| ---: | ---: | ---: |
| -0.3909 | 0 | 0.3909 |
| 0 | 0 | 0 |

The output verifies that the position of the middle element of an array with an odd number of elements lies on the x-axis.

## Version History <br> Introduced in R2015a

## getElementSpacing

System object: phased. UCA
Package: phased
Spacing between array elements

## Syntax

dist = getElementSpacing(sArray)
dist = getElementSpacing(sArray,disttype)

## Description

dist $=$ getElementSpacing(sArray) returns the arc length between adjacent elements of the phased. UCA System object, sArray.
dist = getElementSpacing(sArray,disttype) returns either the arc length or chord length between adjacent elements depending on the specification of disttype.

## Input Arguments

## sArray - Uniform circular array

phased.UCA System object
Uniform circular array, specified as a phased.UCA System object.
Example: phased.UCA()

## disttype - Distance type

'arc' (default)|'chord'
Distance type to define path between adjacent array elements, specified as a either 'arc' or ' chord'. If disttype is specified as 'arc', the returned distance is the arc length between adjacent elements. If disttype is specified as 'chord', the returned distance is the chord length between adjacent elements.

```
Example: 'chord'
```


## Output Arguments

## spacing - Spacing between elements

scalar
Spacing between elements, returned as a scalar. A uniform circular array has a unique distance between all pairs of adjacent elements. The distance depends only upon the radius of the array, $R$, and the angle between two adjacent elements, $\Delta \varphi$. The angle between two adjacent elements is computed from the number of elements, $\Delta \varphi=2 \pi / N$. If disttype is specified as 'arc', the method returns
$R \Delta \varphi$.

If disttype is specified as 'chord' ', the method returns
$2 R \sin (\Delta \varphi / 2)$.
The chord distance is always less than the arc distance.

## Examples

## Spacing Between UCA Elements

Construct a 10 -element UCA with a radius of 1.5 meters, and obtain the arc distance between any two adjacent elements. Then, obtain the chord distance.

```
sArray = phased.UCA('NumElements',10,'Radius',1.5);
dist = getElementSpacing(sArray,'arc')
dist = 0.9425
dist = getElementSpacing(sArray,'chord')
dist = 0.9271
```


## Version History

Introduced in R2015a

## getNumElements

System object: phased. UCA
Package: phased
Number of elements in array

## Syntax

$\mathrm{N}=$ getNumElements( H )

## Description

$\mathrm{N}=$ getNumElements $(\mathrm{H})$ returns the number of elements, $N$, in the UCA object H .

## Input Arguments

H - Uniform circular array
phased. UCA System object
Uniform circular array, specified as a phased. UCA System object.
Example: $\mathrm{H}=$ phased.UCA();

## Output Arguments

N - Number of elements
positive integer
Number of elements of array, returned as a positive integer.

## Examples

## Number of Elements of UCA

Create a UCA with the default number of elements. Verify that there are five elements.
sArray = phased.UCA();
$\mathrm{N}=$ getNumElements(sArray)
$\mathrm{N}=5$

## Version History

Introduced in R2015a

## getTaper

System object: phased. UCA
Package: phased
Array element tapers

## Syntax

WTS = getTaper(H)

## Description

WTS = getTaper(H) returns the tapers, WTS, applied to each element of the phased uniform circular array (UCA), H. Tapers are often referred to as weights.

## Input Arguments

## H - Uniform circular array

System object
Uniform circular array, specified as a phased. ULA System object.
Example: $\mathrm{H}=$ phased.UCA();

## Output Arguments

WTS - Array element tapers
$N$-by-1 complex-valued vector
Array element tapers, returned as an $N$-by- 1 complex-valued vector, where $N$ is the number of elements in the array.

## Examples

## Show UCA Element Tapers

Construct a 7 -element UCA array of isotropic antenna elements with a Taylor window taper. Design the array to have a radius of 0.5 meters. Then, draw the array showing the element taper shading.

```
Nelem = 7;
R = 0.5;
taper = taylorwin(Nelem);
sArray = phased.UCA(Nelem,R,'Taper',taper.');
w = getTaper(sArray)
w = 7x1
    0.4520
    0.9009
```

1.3680
1.5581
1.3680
0.9009
0.4520
viewArray(sArray,'ShowTaper',true);


Both the output and figure above shows that the taper magnitudes are largest near the middle element.

## Version History <br> Introduced in R2015a

## isPolarizationCapable

System object: phased.UCA
Package: phased
Polarization capability

## Syntax

flag = isPolarizationCapable(H)

## Description

flag = isPolarizationCapable(H) returns a Boolean value, flag, indicating whether the array supports polarization. An array supports polarization when all of its constituent sensor elements support polarization.

## Input Arguments

## H - Uniform line array

System object
Uniform line array specified as a phased. UCA System object.

## Output Arguments

## flag - Polarization-capability flag

boolean
Polarization-capability flag returned as a boolean value true when the array supports polarization or false when it does not.

## Examples

## Show UCA is Polarization Capable

Determine whether a UCA array of 7 short-dipole antenna elements supports polarization. The array radius is one-half meter.

```
antenna = phased.ShortDipoleAntennaElement('FrequencyRange',[le9 10e9]);
array = phased.UCA('NumElements',7,'Radius',0.5,'Element',antenna);
isPolarizationCapable(array)
ans = logical
    1
```

The returned value 1 from isPolarizationCapable shows that a UCA of short-dipole antenna elements supports polarization.

# Version History <br> Introduced in R2015a 

## pattern

System object: phased. UCA
Package: phased
Plot UCA array pattern

## Syntax

```
pattern(sArray,FREQ)
pattern(sArray,FREQ,AZ)
pattern(sArray,FREQ,AZ,EL)
pattern(__,Name,Value)
[PAT,AZ_ANG,EL_ANG] = pattern(
```

$\qquad$

``` )
```


## Description

pattern (sArray, FREQ) plots the 3-D array directivity pattern (in dBi) for the array specified in sArray. The operating frequency is specified in FREQ.

The integration used when computing array directivity has a minimum sampling grid of 0.1 degrees. If an array pattern has a beamwidth smaller than this, the directivity value will be inaccurate.
pattern(sArray, FREQ, AZ) plots the array directivity pattern at the specified azimuth angle.
pattern(sArray, FREQ, AZ, EL) plots the array directivity pattern at specified azimuth and elevation angles.
pattern(__, Name, Value) plots the array pattern with additional options specified by one or more Name, Value pair arguments.
[PAT,AZ_ANG,EL_ANG] = pattern( $\qquad$ ) returns the array pattern in PAT. The AZ_ANG output contains the coordinate values corresponding to the rows of PAT. The EL_ANG output contains the coordinate values corresponding to the columns of PAT. If the 'CoordinateSystem' parameter is set to ' $u v$ ', then AZ_ANG contains the $U$ coordinates of the pattern and EL_ANG contains the $V$ coordinates of the pattern. Otherwise, they are in angular units in degrees. $U V$ units are dimensionless.

## Input Arguments

## sArray - Uniform circular array

System object
Uniform circular array, specified as a phased.UCA System object.
Example: sArray= phased.UCA;

## FREQ - Frequency for computing directivity and patterns

positive scalar | 1-by-L real-valued row vector
Frequencies for computing directivity and patterns, specified as a positive scalar or 1-by-L realvalued row vector. Frequency units are in hertz.

- For an antenna, microphone, or sonar hydrophone or projector element, FREQ must lie within the range of values specified by the FrequencyRange or FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased.CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: [1e8 2e6]
Data Types: double

## AZ - Azimuth angles

[-180:180] (default) | 1-by-N real-valued row vector
Azimuth angles for computing directivity and pattern, specified as a 1-by- $N$ real-valued row vector where $N$ is the number of azimuth angles. Angle units are in degrees. Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the $x y$ plane. When measured from the $x$-axis toward the $y$-axis, this angle is positive.

```
Example: [-45:2:45]
```

Data Types: double

## EL - Elevation angles

[-90:90] (default) | 1-by-M real-valued row vector
Elevation angles for computing directivity and pattern, specified as a 1-by-M real-valued row vector where $M$ is the number of desired elevation directions. Angle units are in degrees. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

The elevation angle is the angle between the direction vector and $x y$-plane. The elevation angle is positive when measured towards the $z$-axis.

Example: [-75:1:70]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## CoordinateSystem - Plotting coordinate system <br> 'polar' (default) | 'rectangular' | 'uv'

Plotting coordinate system of the pattern, specified as the comma-separated pair consisting of 'CoordinateSystem' and one of 'polar', 'rectangular', or 'uv'. When 'CoordinateSystem' is set to 'polar' or 'rectangular', the AZ and EL arguments specify the pattern azimuth and elevation, respectively. AZ values must lie between $-180^{\circ}$ and $180^{\circ}$. EL values must lie between $-90^{\circ}$ and $90^{\circ}$. If 'CoordinateSystem' is set to ' $u v$ ', AZ and EL then specify $U$ and $V$ coordinates, respectively. AZ and EL must lie between -1 and 1 .

## Example: 'uv'

## Data Types: char

## Type - Displayed pattern type

'directivity' (default)|'efield'|'power'|'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb' - power pattern converted to dB.

Example: 'powerdb'
Data Types: char

## Orientation - Array orientation

[0;0;0]. (default)| 3-by-1 real-valued column vector
Array orientation, specified as a 3-by-1 real-valued column vector containing the rotation angles with respect to the $x-y$-, and $z$-axes of the local coordinate system, respectively.

## Normalize - Display normalize pattern

true (default) | false
Display normalized pattern, specified as the comma-separated pair consisting of 'Normalize' and a Boolean. Set this parameter to true to display a normalized pattern. This parameter does not apply when you set 'Type' to 'directivity'. Directivity patterns are already normalized.
Data Types: logical

## ShowArray - View array geometry

false (default) | true
View the array geometry along with the 3D radiation pattern, specified as false or true.
Data Types: logical
ShowLocalCoordinates - Show local coordinate axes
true (default) | false
Show the local coordinate axes, specified as true or false.
Data Types: logical

## ShowColorbar - Show colorbar <br> true (default) | false

Show the colorbar, specified as true or false.
Data Types: logical

## Parent - Handle to axis

scalar

Handle to the axes along which the array geometry is displayed specified as a scalar.

## PlotStyle - Plotting style

'overlay' (default)|'waterfall'
Plotting style, specified as the comma-separated pair consisting of 'Plotstyle' and either 'overlay' or 'waterfall'. This parameter applies when you specify multiple frequencies in FREQ in 2-D plots. You can draw 2-D plots by setting one of the arguments AZ or EL to a scalar.

## Data Types: char

## Polarization - Polarized field component

```
'combined' (default)|'H'| 'V'
```

Polarized field component to display, specified as the comma-separated pair consisting of 'Polarization' and 'combined ', 'H' , or 'V'. This parameter applies only when the sensors are polarization-capable and when the 'Type' parameter is not set to 'directivity'. This table shows the meaning of the display options.

| 'Polarization' | Display |
| :--- | :--- |
| 'combined ' | Combined $H$ and $V$ polarization components |
| 'H' | $H$ polarization component |
| ' $\mathrm{V}^{\prime}$ | V polarization component |

Example: 'V '

## Data Types: char

## PropagationSpeed - Signal propagation speed

speed of light (default) | positive scalar
Signal propagation speed, specified as the comma-separated pair consisting of ' PropagationSpeed ' and a positive scalar in meters per second.
Example: 'PropagationSpeed', physconst('LightSpeed')
Data Types: double

## Weights - Array weights

1 (default) | $N$-by-1 complex-valued column vector | $N$-by-L complex-valued matrix
Array weights, specified as the comma-separated pair consisting of 'Weights' and an $N$-by-1 complex-valued column vector or $N$-by- $L$ complex-valued matrix. Array weights are applied to the elements of the array to produce array steering, tapering, or both. The dimension $N$ is the number of elements in the array. The dimension $L$ is the number of frequencies specified by FREQ.

| Weights Dimension | FREQ Dimension | Purpose |
| :--- | :--- | :--- |
| $N$-by-1 complex-valued column <br> vector | Scalar or 1-by-L row vector | Applies a set of weights for the <br> single frequency or for all $L$ <br> frequencies. |


| Weights Dimension | FREQ Dimension | Purpose |
| :--- | :--- | :--- |
| $N$-by- $L$ complex-valued matrix | 1-by-L row vector | Applies each of the $L$ columns of <br> 'Weights' for the <br> corresponding frequency in <br> FREQ. |

$\overline{\text { Note Use complex weights to steer the array response toward different directions. You can create }}$ weights using the phased. SteeringVector System object or you can compute your own weights. In general, you apply Hermitian conjugation before using weights in any Phased Array System Toolbox function or System object such as phased.Radiator or phased. Collector. However, for the directivity, pattern, patternAzimuth, and patternElevation methods of any array System object use the steering vector without conjugation.

```
Example: 'Weights',ones( \(\mathrm{N}, \mathrm{M}\) )
```

Data Types: double
Complex Number Support: Yes

## Output Arguments

## PAT - Array pattern

$M$-by- $N$ real-valued matrix
Array pattern, returned as an $M$-by- $N$ real-valued matrix. The dimensions of PAT correspond to the dimensions of the output arguments AZ_ANG and EL_ANG.

## AZ_ANG - Azimuth angles

scalar | 1-by- $N$ real-valued row vector
Azimuth angles for displaying directivity or response pattern, returned as a scalar or 1-by- $N$ realvalued row vector corresponding to the dimension set in AZ. The columns of PAT correspond to the values in AZ_ANG. Units are in degrees.

## EL_ANG - Elevation angles

scalar | 1-by-M real-valued row vector
Elevation angles for displaying directivity or response, returned as a scalar or 1-by-M real-valued row vector corresponding to the dimension set in EL. The rows of PAT correspond to the values in EL_ANG. Units are in degrees.

## Examples

## Pattern of 11-Element UCA Antenna Array

Create an 11-element uniform circular array (UCA) having a 1.5 m radius and operating at 500 MHz . The array consists of short-dipole antenna elements. First, display the vertical component of the response at 45 degrees azimuth and 0 degrees elevation. Then plot the azimuth and elevation directivities.

```
antenna = phased.ShortDipoleAntennaElement(...
    'FrequencyRange' , [50e6,1000e6],...
```

```
    'AxisDirection','Z');
array = phased.UCA('NumElements',11,'Radius',1.5,'Element',antenna);
fc = 500e6;
ang = [45;0];
resp = array(fc,ang);
disp(resp.V)
    -1.2247
    -1.2247
    -1.2247
    -1.2247
    -1.2247
    -1.2247
    -1.2247
    -1.2247
    -1.2247
    -1.2247
    -1.2247
```

Display the azimuth directivity pattern at 500 MHz for azimuth angles between -180 and 180 degrees.
c = physconst('LightSpeed');
pattern(array,fc,[-180:180],0,'Type','directivity','PropagationSpeed', c)


Directivity (dBi), Broadside at $0.00^{\circ}$
Display the elevation directivity pattern at 500 MHz for elevation angles between -90 and 90 degrees.
pattern(array,fc,[0],[-90:90],'Type','directivity','PropagationSpeed', c)


Directivity (dBi), Broadside at $0.00^{\circ}$

## Pattern of 10-Element UCA Antenna Array in UV Space

Create a 10-element UCA antenna array consisting of cosine antenna elements. Display the 3-D power pattern in UV space.

```
sCos = phased.CosineAntennaElement('FrequencyRange',[100e6 le9],...
    'CosinePower',[2.5,2.5]);
sUCA = phased.UCA('NumElements',10,...
    'Radius',1.5,...
    'Element',sCos);
c = physconst('LightSpeed');
fc = 500e6;
pattern(sUCA,fc,[-1:.01:1],[-1:.01:1],...
    'CoordinateSystem','uv',...
    'Type','powerdb',...
    'PropagationSpeed',c)
```



## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Version History <br> Introduced in R2015a

## See Also

patternAzimuth|patternElevation

## patternAzimuth

System object: phased. UCA
Package: phased
Plot UCA array directivity or pattern versus azimuth

## Syntax

```
patternAzimuth(sArray,FREQ)
patternAzimuth(sArray,FREQ,EL)
patternAzimuth(sArray,FREQ,EL,Name,Value)
PAT = patternAzimuth(
```

$\qquad$

``` )
```


## Description

patternAzimuth (sArray, FREQ) plots the 2-D array directivity pattern versus azimuth (in dBi) for the array sArray at zero degrees elevation angle. The argument FREQ specifies the operating frequency.

The integration used when computing array directivity has a minimum sampling grid of 0.1 degrees. If an array pattern has a beamwidth smaller than this, the directivity value will be inaccurate.
patternAzimuth(sArray, FREQ,EL), in addition, plots the 2-D array directivity pattern versus azimuth (in dBi) for the array sArray at the elevation angle specified by EL. When EL is a vector, multiple overlaid plots are created.
patternAzimuth(sArray, FREQ,EL,Name, Value) plots the array pattern with additional options specified by one or more Name, Value pair arguments.

PAT = patternAzimuth ( _ _ ) returns the array pattern. PAT is a matrix whose entries represent the pattern at corresponding sampling points specified by the 'Azimuth ' parameter and the EL input argument.

## Input Arguments

## sArray - Uniform circular array

System object
Uniform circular array, specified as a phased. UCA System object.
Example: sArray= phased.UCA;

## FREQ - Frequency for computing directivity and pattern

positive scalar
Frequency for computing directivity and pattern, specified as a positive scalar. Frequency units are in hertz.

- For an antenna or microphone element, FREQ must lie within the range of values specified by the FrequencyRange or the FrequencyVector property of the element. Otherwise, the element
produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased.CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: 1e8
Data Types: double

## EL - Elevation angles

## 1-by- $N$ real-valued row vector

Elevation angles for computing sensor or array directivities and patterns, specified as a 1-by- $N$ realvalued row vector. The quantity $N$ is the number of requested elevation directions. Angle units are in degrees. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

The elevation angle is the angle between the direction vector and the xy plane. When measured toward the $z$-axis, this angle is positive.
Example: [0, 10, 20]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Type - Displayed pattern type

'directivity' (default)|'efield'|'power'|'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb' - power pattern converted to dB.

Example: 'powerdb'
Data Types: char

## PropagationSpeed - Signal propagation speed

## speed of light (default) | positive scalar

Signal propagation speed, specified as the comma-separated pair consisting of ' PropagationSpeed ' and a positive scalar in meters per second.
Example: 'PropagationSpeed', physconst('LightSpeed')
Data Types: double

## Weights - Array weights

M-by-1 complex-valued column vector
Array weights, specified as the comma-separated pair consisting of 'Weights' and an $M$-by-1 complex-valued column vector. Array weights are applied to the elements of the array to produce array steering, tapering, or both. The dimension $M$ is the number of elements in the array.
$\overline{\text { Note Use complex weights to steer the array response toward different directions. You can create }}$ weights using the phased. SteeringVector System object or you can compute your own weights. In general, you apply Hermitian conjugation before using weights in any Phased Array System Toolbox function or System object such as phased.Radiator or phased. Collector. However, for the directivity, pattern, patternAzimuth, and patternElevation methods of any array System object use the steering vector without conjugation.

Example: 'Weights', ones (10,1)
Data Types: double
Complex Number Support: Yes

## Azimuth - Azimuth angles

[-180:180] (default) | 1-by-P real-valued row vector
Azimuth angles, specified as the comma-separated pair consisting of 'Azimuth' and a 1-by-P realvalued row vector. Azimuth angles define where the array pattern is calculated.
Example: 'Azimuth', [-90:2:90]
Data Types: double

## Parent - Handle to axis

scalar
Handle to the axes along which the array geometry is displayed specified as a scalar.

## Output Arguments

## PAT - Array directivity or pattern

## L-by- $N$ real-valued matrix

Array directivity or pattern, returned as an $L$-by- $N$ real-valued matrix. The dimension $L$ is the number of azimuth values determined by the 'Azimuth' name-value pair argument. The dimension $N$ is the number of elevation angles, as determined by the EL input argument.

## Examples

## Plot Azimuth Pattern of UCA

Create a 6 -element UCA of short-dipole antenna elements. Design the array to have a radius of 0.5 meters. Plot an azimuth cut of directivity at 0 and 10 degrees elevation. Assume the operating frequency is 500 MHz .
fc = 500e6;
sCDant = phased. ShortDipoleAntennaElement('FrequencyRange',[100,900]*1e6);
sUCA = phased.UCA('NumElements',6,'Radius',0.5,'Element',sCDant); patternAzimuth(sUCA,fc,[0 30])


Directivity (dBi), Broadside at $0.00^{\circ}$
You can plot a smaller range of azimuth angles by setting the Azimuth property. patternAzimuth(sUCA,fc,[0 30],'Azimuth',[-90:90])


Directivity (dBi), Broadside at $0.00^{\circ}$

## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Version History Introduced in R2015a

## See Also

pattern| patternElevation

## patternElevation

System object: phased. UCA
Package: phased
Plot UCA array directivity or pattern versus elevation

## Syntax

```
patternElevation(sArray,FREQ)
patternElevation(sArray,FREQ,AZ)
patternElevation(sArray,FREQ,AZ,Name,Value)
PAT = patternElevation(
```

$\qquad$

``` )
```


## Description

patternElevation(sArray, FREQ) plots the 2-D array directivity pattern versus elevation (in dBi ) for the array sArray at zero degrees azimuth angle. When AZ is a vector, multiple overlaid plots are created. The argument FREQ specifies the operating frequency.

The integration used when computing array directivity has a minimum sampling grid of 0.1 degrees. If an array pattern has a beamwidth smaller than this, the directivity value will be inaccurate.
patternElevation(sArray, FREQ, AZ), in addition, plots the 2-D element directivity pattern versus elevation (in dBi ) at the azimuth angle specified by $A Z$. When $A Z$ is a vector, multiple overlaid plots are created.
patternElevation(sArray,FREQ,AZ,Name, Value) plots the array pattern with additional options specified by one or more Name, Value pair arguments.

PAT = patternElevation ( _ ) returns the array pattern. PAT is a matrix whose entries represent the pattern at corresponding sampling points specified by the 'Elevation' parameter and the AZ input argument.

## Input Arguments

## sArray - Uniform circular array

System object
Uniform circular array, specified as a phased.UCA System object.
Example: sArray= phased.UCA;
FREQ - Frequency for computing directivity and pattern
positive scalar
Frequency for computing directivity and pattern, specified as a positive scalar. Frequency units are in hertz.

- For an antenna or microphone element, FREQ must lie within the range of values specified by the FrequencyRange or the FrequencyVector property of the element. Otherwise, the element
produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased.CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: 1e8
Data Types: double

## AZ - Azimuth angles for computing directivity and pattern

1-by- $N$ real-valued row vector
Azimuth angles for computing sensor or array directivities and patterns, specified as a 1 -by- $N$ realvalued row vector where $N$ is the number of desired azimuth directions. Angle units are in degrees. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the $x y$ plane. This angle is positive when measured from the $x$-axis toward the $y$-axis.
Example: [0,10,20]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Type - Displayed pattern type

'directivity' (default)|'efield'|'power'|'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb' - power pattern converted to dB.

Example: 'powerdb'
Data Types: char

## PropagationSpeed - Signal propagation speed

speed of light (default) | positive scalar
Signal propagation speed, specified as the comma-separated pair consisting of ' PropagationSpeed ' and a positive scalar in meters per second.
Example: 'PropagationSpeed', physconst('LightSpeed')
Data Types: double

## Weights - Array weights

M-by-1 complex-valued column vector
Array weights, specified as the comma-separated pair consisting of 'Weights' and an $M$-by-1 complex-valued column vector. Array weights are applied to the elements of the array to produce array steering, tapering, or both. The dimension $M$ is the number of elements in the array.
$\overline{\text { Note Use complex weights to steer the array response toward different directions. You can create }}$ weights using the phased. SteeringVector System object or you can compute your own weights. In general, you apply Hermitian conjugation before using weights in any Phased Array System Toolbox function or System object such as phased.Radiator or phased. Collector. However, for the directivity, pattern, patternAzimuth, and patternElevation methods of any array System object use the steering vector without conjugation.

Example: 'Weights', ones (10,1)
Data Types: double
Complex Number Support: Yes

## Elevation - Elevation angles

[-90:90] (default) | 1-by-P real-valued row vector
Elevation angles, specified as the comma-separated pair consisting of 'Elevation' and a 1-by-P real-valued row vector. Elevation angles define where the array pattern is calculated.
Example: 'Elevation', [-90:2:90]
Data Types: double

## Parent - Handle to axis

scalar
Handle to the axes along which the array geometry is displayed specified as a scalar.

## Output Arguments

## PAT - Array directivity or pattern

L-by- $N$ real-valued matrix

Array directivity or pattern, returned as an $L$-by- $N$ real-valued matrix. The dimension $L$ is the number of elevation angles determined by the 'Elevation' name-value pair argument. The dimension $N$ is the number of azimuth angles determined by the AZ argument.

## Examples

## Plot Elevation Pattern of UCA

Create a 6 -element UCA of short-dipole antenna elements. Design the array to have a radius of 0.5 meters. Plot an elevation cut of directivity at 0 and 90 degrees azimuth. Assume the operating frequency is 500 MHz .
$\mathrm{fc}=500 \mathrm{e} 6$;
sCDant $=$ phased. ShortDipoleAntennaElement('FrequencyRange', [100,900]*1e6);
sUCA = phased.UCA('NumElements',6,'Radius',0.5,'Element',sCDant); patternElevation(sUCA,fc,[0 90])


Directivity (dBi), Broadside at $0.00^{\circ}$
You can plot a smaller range of elevation angles by setting the Elevation property. patternElevation(sUCA,fc,[0 45],'Elevation',[0:90])


Directivity (dBi), Broadside at $0.00^{\circ}$

## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Version History

Introduced in R2015a

## See Also

pattern| patternAzimuth

## step

System object: phased.UCA
Package: phased
Output responses of array elements

## Syntax

RESP = step(sArray,FREQ,ANG)

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.

RESP = step(sArray, FREQ, ANG) returns the responses, RESP, of the array elements, at operating frequencies specified in FREQ and directions specified in ANG.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## sArray - Uniform circular array

System object
Uniform circular array, specified as a phased. UCA System object.

```
Example: sArray= phased.UCA;
```


## FREQ - Operating frequency

positive scalar | 1-by-L real-valued row vector
Operating frequency of array specified, specified as a positive scalar or 1-by- $L$ real-valued row vector.
Frequency units are in hertz.

- For antenna or microphone elements, FREQ must lie within the range of values specified by the FrequencyRange or FrequencyVector property of the element. Otherwise, the element produces no response and the array response is returned as zero. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased.CustomMic rophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as zero.


## Example: [1e8 2e8]

Data Types: double

## ANG - Response directions

1-by- $M$ real-valued row vector | 2 -by- $M$ real-valued matrix
Response directions, specified as either a 2-by-M real-valued matrix or a real-valued row vector of length $M$.

If ANG is a 2-by-M matrix, each column of the matrix specifies the direction in the form [azimuth; elevation]. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive. Angle units are in degrees.

If ANG is a row vector of length $M$, each element specifies the azimuth angle of the direction. In this case, the corresponding elevation angle is assumed to be $0^{\circ}$.
Example: [20;15]
Data Types: double

## Output Arguments

## RESP - Voltage responses of phased array

complex-valued $N$-by- $M$-by-L matrix | complex-valued structure
Voltage responses of a phased array, specified as a complex-valued matrix or a struct with complexvalued fields. The output depends on whether the array supports polarization or not.

- If the array elements do not support polarization, the voltage response, RESP, has the dimensions $N$-by-M-by-L.
- $N$ (rows) is the number of elements in the array
- $M$ (columns) is the number of angles specified in ANG
- $L$ (pages) is the number of frequencies specified in FREQ

For each array element, the columns of RESP contain the array element responses for the corresponding direction specified in ANG. Each of the $L$ pages of RESP contains the array element responses for the corresponding frequency specified in FREQ.

- If the array supports polarization, RESP is a MATLAB struct containing two fields, RESP. H and RESP.V. The field, RESP.H, represents the array's horizontal polarization response, while RESP.V represents the array's vertical polarization response. Each field has the dimensions $N$-by- $M$-by- $L$.
- $\quad N$ (rows) is the number of elements in the array
- $M$ (columns) is the number of angles specified in ANG
- $L$ (pages) is the number of frequencies specified in FREQ

For each array element, the columns of RESP.H or RESP. V contain the array element responses for the corresponding direction specified in ANG. Each of the $L$ pages of RESP.H or RESP.V contains the array element responses for the corresponding frequency specified in FREQ.

## Examples

## Response of UCA Array

Create a 5 -element uniform circular array (UCA) of cosine antenna elements having a 0.5 meter radius. Find the element responses at the 0 degrees azimuth and elevation at a 300 MHz operating frequency.

```
c = physconst('LightSpeed');
fc = 300e6;
sCos = phased.CosineAntennaElement('CosinePower',[1,1]);
sArray = phased.UCA('Element',sCos,'NumElements',5,'Radius',0.5);
ang = [0;0];
resp = step(sArray,fc,ang)
resp = 5×1
    0
    0.3090
    1.0000
    0.3090
    0
```


## Version History

Introduced in R2015a

## viewArray

System object: phased. UCA
Package: phased
View array geometry

## Syntax

viewArray(H)
viewArray (H,Name, Value)
hPlot = viewArray( $\qquad$

## Description

viewArray (H) plots the geometry of the array specified in H .
viewArray (H,Name, Value) plots the geometry of the array, with additional options specified by one or more Name, Value pair arguments.
hPlot = viewArray( $\qquad$ ) returns the handle of the array elements in the figure window. All input arguments described for the previous syntaxes also apply here.

## Input Arguments

## H - Uniform circular array

System object
Uniform circular array specified as a phased. UCA System object.
Example: phased.UCA()

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Parent - Handle to axes

real-valued scalar
Handle to the axes along which the array geometry is displayed.

## ShowNormals - Option to show normal vectors

false (default) | true
Option to show normal directions, specified as the comma-separated pair consisting of 'ShowNormals ' and a Boolean value.

- true - show the normal directions of all elements in the array
- false - plot the elements without showing normal directions

Example: false
Data Types: logical

## ShowLocalCoordinates - Show local coordinates

true (default) | false
Logical flag specifying whether to show the local coordinate axes.

## Data Types: logical

## ShowAnnotation - Show aperture size and element spacing annotations <br> true (default) | false

Logical flag specifying whether to show the annotations in the UI panel of the figure. Annotation shows aperture size and element spacing based on array axis of array.
Data Types: logical

## Orientation - Array orientation

[0;0;0] (default)|3-by-1 real-valued vector
Orientation of the array, specified as a 3-by-1 column vector containing the rotation angles with respect to the $x-y$-, and $z$-axes of the local coordinate system, respectively.
Data Types: double

## ShowTaper - Option to show taper magnitude

false (default)|true
Option to show taper magnitude, specified as the comma-separated pair consisting of 'ShowTaper' and a Boolean value.

- true - change the element color brightness in proportion to the element taper magnitude
- false - plot all elements using the same color

Data Types: logical

## ShowIndex - Element indices to show

'None' (default) | vector of positive integers | 'All'
Element indices to show in the figure, specified as the comma-separated pair consisting of 'ShowIndex' and a vector of positive integers. Each number in the vector must be an integer between 1 and the number of elements. To show all of indices of the array, specify ' All '. To suppress all indices, specify ' None'.
Example: [1, 2, 3]
Data Types: double

## Title - Plot title

'Array Geometry' (default)| character vector
Plot title, specified as a character vector.

Example: 'My array plot'

## Output Arguments

## hPlot - Handle of array elements

scalar
Handle of array elements in the figure window, specified as a scalar.

## Examples

## View UCA Array

Construct an 7 -element UCA of isotropic antenna elements with a Taylor window taper. Design the array to have a radius of 0.5 meters. Then, draw the array showing the element normals, element indices, and element taper shading.

```
Nelem = 7;
R = 0.5;
taper = taylorwin(Nelem);
sArray = phased.UCA(Nelem,R,'Taper',taper.');
w = getTaper(sArray);
viewArray(sArray,'ShowNormals',true,'ShowIndex','All','ShowTaper',true);
```


## Array Geometry



# Version History 

Introduced in R2015a

## See Also

phased.ArrayResponse

## Topics

Phased Array Gallery

## phased.ULA

Package: phased
Uniform linear array

## Description

phased.ULA creates a uniform linear array (ULA) System object and computes its response.
To compute the response for each element in the array for specified directions:
1 Create the phased.ULA object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

array $=$ phased.ULA
array = phased.ULA(Name=Value)
array = phased.ULA(N,D,Name=Value)

## Description

array $=$ phased.ULA creates a uniform linear array (ULA) System object. In this syntax, the object models a ULA formed with identical isotropic phased array sensor elements. The origin of the local coordinate system is the phase center of the array. The positive $x$-axis is the direction normal to the array, and the elements of the array are located along the $y$-axis.
array $=$ phased.ULA(Name=Value) creates the object array with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Name1 = Value1, ... ,NameN = ValueN).
array $=$ phased.ULA(N, D, Name=Value) creates a ULA array object with the NumElements property set to $N$, the ElementSpacing property set to $D$, and other specified property Names set to the specified Values. $N$ and $D$ are value-only arguments. When specifying a value-only argument, specify all preceding value-only arguments. You can specify name-value pair arguments in any order.

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## Element - phased array element

isotropic antenna element System object with default properties (default) | Phased Array System
Toolbox antenna, microphone, or transducer element System object | Antenna Toolbox antenna System object

Phased array element, specified as a Phased Array System Toolbox antenna, microphone, or transducer element or Antenna Toolbox antenna.

Example: phased.CosineAntennaElement

## NumElements - Number of array elements

2 (default) | positive integer
Number of array elements, specified as a positive integer.

## Data Types: double

## ElementSpacing - Array element spacing

0.5 (default) | positive scalar

Spacing between two adjacent elements in the array, specified as a positive scalar. Units are in meters.
Data Types: double

## ArrayAxis - Axis of linear array

'y' (default)|'x' ${ }^{\prime}{ }^{\prime}$
Axis of linear array, specified as ' $y$ ', ' $x$ ', or ' $z$ '. Linear array elements are located along the selected coordinate system axis. The array axis determines the direction along which the element normal vectors point.

| ArrayAxis Property Value | Element Normal Direction |
| :--- | :--- |
| $' x^{\prime}$ | azimuth $=90^{\circ}$, elevation $=0^{\circ}(y$-axis $)$ |
| ' $y$ ' (default $)$ | azimuth $=0^{\circ}$, elevation $=0^{\circ}(x$-axis $)$ |
| ' $z^{\prime}$ | azimuth $=0^{\circ}$, elevation $=0^{\circ}(x$-axis $)$ |

Example: 'z'

## Data Types: char | string

## Taper - Array element tapers

1 (default) | complex-valued scalar | 1-by- $N$ complex-valued row vector | $N$-by-1 c column vector
Array element tapering, specified as a complex-valued scalar, 1-by- N complex-valued row vector, or N -by-1 complex-valued column vector. $N$ represents the number of elements of the array. Tapers, also known as weights, are applied to each sensor element in the sensor array and modify both the amplitude and phase of the received data. If 'Taper' is a scalar, the same taper value is applied to all elements. If 'Taper' is a vector, each taper value is applied to the corresponding sensor element.
Data Types: double

## Usage

## Syntax

resp = array(freq,ang)

## Description

resp = array(freq,ang) returns the array element responses, resp, at the operating frequencies specified in $f r e q$ and in directions specified in ang.

## Input Arguments

## freq - Array operating frequencies

length- $L$ row vector of positive values
Array operating frequencies, specified as a length- $L$ row vector. Typical values are within the range specified by a frequency range property of the array element. That property is called FrequencyRange or FrequencyVector, depending on the type of array element. The element has zero response at frequencies outside that range. Units are in Hz .
Data Types: double

## ang - Array response directions

length- $M$ row vector with real values | 2 -by- $M$ matrix with real values
Array response directions, specified as a 2 -by- $M$ matrix or length- $M$ row vector.
If ANG is a 2 -by- $M$ matrix, each column of the matrix specifies the direction in the form [azimuth; elevation]. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive.

If ang is a row vector of length $M$, each element specifies the azimuth angle of the direction. In this case, the corresponding elevation angle is assumed to be $0^{\circ}$.

Units are in degrees.

## Output Arguments

resp - Voltage responses of phased array
$N$-by-M-by-L complex-valued MATLAB array | MATLAB struct
Voltage responses of the phased array. The output depends on whether the array supports polarization or not.

- If the array is not capable of supporting polarization, the voltage response, resp, has the dimensions $N$-by- $M$-by- $L . N$ is the number of elements in the array. The dimension $M$ is the number of angles specified in ang. $L$ is the number of frequencies specified in freq. For any element, the columns of resp contain the responses of the array elements for the corresponding direction specified in ang. Each of the $L$ pages of resp contains the responses of the array elements for the corresponding frequency specified in freq.
- If the array is capable of supporting polarization, the voltage response, resp, is a MATLAB struct containing two fields, resp.H and resp.V. The field, resp.H, represents the array's horizontal polarization response, while resp.V represents the array's vertical polarization
response. Each field has the dimensions $N$-by-M-by-L. $N$ is the number of elements in the array, and $M$ is the number of angles specified in ang. $L$ is the number of frequencies specified in freq. Each column of resp contains the responses of the array elements for the corresponding direction specified in ang. Each of the $L$ pages of ang contains the responses of the array elements for the corresponding frequency specified in freq.


## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```


## Specific to phased. ULA and other array System objects

beamwidth
collectPlaneWave
directivity
getElementNormal
getElementPosition
getNumElements
getTaper
isPolarizationCapable
pattern
patternAzimuth
patternElevation
perturbations
perturbedArray
perturbedPattern
plotGratingLobeDiagram
viewArray

Compute and display beamwidth of an array
Simulate received plane waves at array
Compute array directivity
Normal vectors for array elements
Positions of array elements
Number of elements in an array
Array element tapers
Array polarization capability
Plot array directivity and patterns
Plot array directivity or pattern versus azimuth
Plot array directivity or pattern versus elevation
Perturbations defined on array
Apply perturbations to phased array
Display pattern of perturbed array
Plot grating lobe diagram of array
View array geometry

## Common to All System Objects

step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object

## Examples

## Directivity of Uniform Linear Array

Compute the directivities of two different uniform linear arrays (ULA). One array consists of isotropic antenna elements and the second array consists of cosine antenna elements. In addition, compute the directivity when the first array is steered in a specified direction. For each case, calculate the directivities for a set of seven different azimuth directions all at zero degrees elevation. Set the frequency to 800 MHz .

## Array of isotropic antenna elements

First, create a 10 -element ULA of isotropic antenna elements spaced 1/2-wavelength apart.

```
c = physconst('LightSpeed');
fc = 3e8;
lambda = c/fc;
ang = [-30,-20,-10,0,10,20,30; 0,0,0,0,0,0,0];
myAnt1 = phased.IsotropicAntennaElement;
myArray1 = phased.ULA(10,lambda/2,'Element',myAnt1);
Compute the directivity.
```

```
d = directivity(myArray1,fc,ang,'PropagationSpeed',c)
```

d = directivity(myArray1,fc,ang,'PropagationSpeed',c)
d = 7\times1
d = 7\times1
-6.9886
-6.9886
-6.2283
-6.2283
-6.5176
-6.5176
10.0011
10.0011
-6.5176
-6.5176
-6.2283
-6.2283
-6.9886

```
    -6.9886
```


## Array of cosine antenna elements

Next, create a 10-element ULA of cosine antenna elements spaced 1/2-wavelength apart.

```
myAnt2 = phased.CosineAntennaElement('CosinePower',[1.8,1.8]);
```

myArray2 = phased.ULA(10,lambda/2,'Element',myAnt2);

Compute the directivity.
$\mathrm{d}=$ directivity (myArray2,fc,ang,'PropagationSpeed ' c )
$d=7 \times 1$
-1.9838
0.0529
0.4968
17.2548
0.4968
0.0529
$-1.9838$

The directivity of the cosine ULA is greater than the directivity of the isotropic ULA because of the larger directivity of the cosine antenna element.

## Steered array of isotropic antenna elements

Finally, steer the isotropic antenna array to 30 degrees in azimuth and compute the directivity.

```
w = steervec(getElementPosition(myArray1)/lambda,[30;0]);
d = directivity(myArray1,fc,ang,'PropagationSpeed',c,...
    'Weights',w)
d = 7x1
    -297.2705
    -13.9783
```

The directivity is greatest in the steered direction.

## ULA Element Normals

Construct three ULAs with elements along the $x-, y$-, and $z$-axes. Obtain the element normals.
First, choose the array axis along the $x$-axis.

```
sULA1 = phased.ULA('NumElements',5,'ArrayAxis','x');
norm = getElementNormal(sULA1)
norm = 2×5
\begin{tabular}{rrrrr}
90 & 90 & 90 & 90 & 90 \\
0 & 0 & 0 & 0 & 0
\end{tabular}
```

The element normal vectors point along the $y$-axis.
Next, choose the array axis along the $y$-axis.

```
sULA2 = phased.ULA('NumElements',5,'ArrayAxis','y');
norm = getElementNormal(sULA2)
norm = 2×5
    0
    0}0
```

The element normal vectors point along the $x$-axis.
Finally, set the array axis along the $z$-axis. Obtain the normal vectors of the odd-numbered elements.

```
sULA3 = phased.ULA('NumElements',5,'ArrayAxis','z');
norm = getElementNormal(sULA3,[1,3,5])
norm = 2x3
    0 0 0
    0 0 0
```

The element normal vectors also point along the $x$-axis.

## ULA Element Positions

Construct a ULA with 5 elements along the $z$-axis. Obtain the element positions.
sULA = phased.ULA('NumElements',5,'ArrayAxis','z'); pos $=$ getElementPosition(sULA)
pos $=3 \times 5$

| 0 | 0 | 0 | 0 | 0 |
| ---: | ---: | ---: | ---: | ---: |
| 0 | 0 | 0 | 0 | 0 |
| -1.0000 | -0.5000 | 0 | 0.5000 | 1.0000 |

## Get Number of ULA Elements

Construct a default ULA and obtain the number of elements in that array.

```
array = phased.ULA;
N = getNumElements(array)
N = 2
```


## Geometry and Indices of ULA Elements

Draw a 6 -element ULA and use the 'ShowIndex ' parameter to show the indices of the first and third elements.
array = phased.ULA(6);
viewArray(array,'ShowIndex',[1 3],'ShowNormals',true, ...
'ShowLocalCoordinates',true,'Orientation', [60;100;45], ...
'ShowAnnotation', true)

## Array Geometry




Aperture Size:
Y axis $=3 \mathrm{~m}$
Element Spacing:
$\Delta y=500 \mathrm{~mm}$
Array Axis: $Y$ axis

## Construct ULA with Taylor Window

Construct a 5 -element ULA with a Taylor window taper. Then, obtain the element taper values.

```
taper = taylorwin(5)';
array = phased.ULA(5,'Taper',taper);
w = getTaper(array)
w = 5×1
    0.5181
    1.2029
    1.5581
    1.2029
    0.5181
```


## Short-Dipole Antenna ULA Supports Polarization

Show that an array of phased. ShortDipoleAntennaElement antenna elements supports polarization.

```
antenna = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[1e9 10e9]);
array = phased.ULA('NumElements',3,'Element',antenna);
isPolarizationCapable(array)
ans = logical
    1
```

The returned value of 1 shows that this array supports polarization.

## Plot Pattern of 4-Element Antenna Array

Create a 4 -element undersampled ULA and find the response of each element at boresight. Plot the array pattern at 1 GHz for azimuth angles between -180 and 180 degrees. The default element spacing is 0.5 meters.

```
array = phased.ULA('NumElements',4);
fc = 1e9;
ang = [0;0];
resp = array(fc,ang)
resp = 4×1
    1
    1
    1
    1
c = physconst('LightSpeed');
pattern(array,fc,-180:180,0,'PropagationSpeed',c,...
    'CoordinateSystem','rectangular',...
    'Type','powerdb','Normalize',true)
```



## Plot Pattern of 10-Element Microphone ULA

Construct a 10 -element uniform linear array of omnidirectional microphones spaced 3 cm apart.
Then, plot the array pattern at 100 Hz .
mic $=$ phased.OmnidirectionalMicrophoneElement(...
'FrequencyRange',[20 20e3]);
Nele = 10;
array $=$ phased.ULA('NumElements',Nele,...
'ElementSpacing', $3 \mathrm{e}-2, \ldots$
'Element',mic);
fc = 100;
ang $=[0 ; 0]$;
resp $=\operatorname{array}(f c, a n g)$;
c = 340;
pattern(array,fc,[-180:180],0,' PropagationSpeed', c, ...
'CoordinateSystem','polar',...
'Type', 'powerdb',...
'Normalize',true);


Normalized Power (dB), Broadside at $0.00^{\circ}$

## Plot Pattern of Array of Polarized Short-Dipole Antennas

Build a tapered uniform line array of 5 short-dipole sensor elements. Because short dipoles support polarization, the array should as well. Verify that it supports polarization by looking at the output of the isPolarizationCapable method.

```
antenna = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[100e6 le9],'AxisDirection','Z');
array = phased.ULA('NumElements',5,'Element',antenna,...
    'Taper',[.5,.7,1,.7,.5]);
isPolarizationCapable(array)
ans = logical
    1
```

Then, draw the array using the viewArray method.

```
viewArray(array,'ShowTaper',true,'ShowIndex','All')
```


## Array Geometry



Aperture Size:
Y axis $=2.5 \mathrm{~m}$ Element Spacing: $\Delta y=500 \mathrm{~mm}$ Array Axis: Y axis

Compute the horizontal and vertical responses.

```
fc = 150e6;
ang = [10];
resp = array(fc,ang);
```

Display the horizontal polarization response.
resp.H
ans $=5 \times 1$
0
0
0
0
0

Display the vertical polarization response.

```
resp.v
ans = 5\times1
    -0.6124
    -0.8573
    -1.2247
```

```
-0.8573
-0.6124
```

Plot an azimuth cut of the vertical polarization response.

```
c = physconst('LightSpeed');
pattern(array,fc,[-180:180],0,...
    'PropagationSpeed',c,...
    'CoordinateSystem','polar',...
    'Polarization','V',...
    'Type','powerdb',...
    'Normalize',true)
```



Normalized Power (dB), Broadside at $0.00^{\circ}$

## Plot Pattern of 9-Element ULA Antenna Array of Short Dipoles

Create an 9-element ULA of short dipole antenna elements spaced 0.2 meters apart. Display the azimuth and elevation directivities. The operating frequency is 500 MHz . Plot the directivities in polar coordinates.

Evaluate the fields at 45 degrees azimuth and 0 degrees elevation.

```
element = phased.ShortDipoleAntennaElement(...
```

'FrequencyRange', [50e6,1000e6],...
'AxisDirection','Z');

```
array = phased.ULA('NumElements',9,'ElementSpacing',1.5,'Element',element);
fc = 500e6;
ang = [45;0];
resp = array(fc,ang);
disp(resp.V)
    -1.2247
    -1.2247
    -1.2247
    -1.2247
    -1.2247
    -1.2247
    -1.2247
    -1.2247
    -1.2247
```

Display the azimuth directivity pattern at 500 MHz for azimuth angles between -180 and 180 degrees.

```
c = physconst('LightSpeed');
pattern(array,fc,[-180:180],0,...
    'Type','directivity',...
    'PropagationSpeed',c)
```



Directivity (dBi), Broadside at $0.00^{\circ}$
Display the elevation directivity pattern at 500 MHz for elevation angles between -90 and 90 degrees.

```
pattern(array,fc,[0],[-90:90],...
```

'Type','directivity',...
'PropagationSpeed ', c)


Directivity (dBi), Broadside at $0.00^{\circ}$

## Plot Pattern of 10-Element ULA Antenna Array in UV Space

Create a 10 -element ULA antenna array consisting of cosine antenna elements spaced 10 cm apart. Display the 3-D power pattern in UV space. The operating frequency is 500 MHz .

```
sCos = phased.CosineAntennaElement('FrequencyRange',[100e6 1e9],...
    'CosinePower',[2.5,2.5]);
sULA = phased.ULA('NumElements',10,...
    'ElementSpacing',.1,...
    'Element',sCos);
c = physconst('LightSpeed');
fc = 500e6;
pattern(sULA,fc,[-1:.01:1],[-1:.01:1],...
    'CoordinateSystem','uv',...
    'Type','powerdb',...
    'PropagationSpeed',c)
```



## Plot Azimuth Pattern of ULA

Create a 7-element ULA of short-dipole antenna elements spaced 10 cm apart. Plot an azimuth cut of directivity at 0 and 10 degrees elevation. Assume the operating frequency is 500 MHz .
$\mathrm{fc}=500 \mathrm{e} 6$;
sCDant = phased.ShortDipoleAntennaElement('FrequencyRange',[100,900]*1e6); sULA = phased.ULA('NumElements',7,'ElementSpacing',0.1,'Element',sCDant); patternAzimuth(sULA,fc,[0 30])


Directivity (dBi), Broadside at $0.00^{\circ}$
You can plot a smaller range of azimuth angles by setting the Azimuth property. patternAzimuth(sULA,fc,[0 30],'Azimuth',[-90:90])


Directivity (dBi), Broadside at $0.00^{\circ}$

## Plot Elevation Pattern of ULA

Create a 6-element ULA of short-dipole antenna elements with element spacing of 10 cm . Plot an elevation cut of directivity at 0 and 90 degrees azimuth. Assume the operating frequency is 500 MHz .
$\mathrm{fc}=500 \mathrm{e}$;
c = physconst('LightSpeed');
sSD = phased.ShortDipoleAntennaElement('FrequencyRange', [100,900]*1e6);
sULA = phased.ULA('NumElements',6,'ElementSpacing',0.1,'Element',sSD);
patternElevation(sULA,fc,[0 90],'PropagationSpeed',c)


Directivity (dBi), Broadside at $0.00^{\circ}$
You can plot a smaller range of elevation angles by setting the Elevation property. patternElevation(sULA,fc,[0 45],'Elevation',[0:90],'PropagationSpeed', c)


Directivity (dBi), Broadside at $0.00^{\circ}$

## Plot Beamwidth of Sonar Array

Plot the beamwidth of a sonar array operating at a frequency of 2 kHz when the propagation speed of sound in water is $1500 \mathrm{~m} / \mathrm{s}$.

The sonar array consists of a 20 -element uniform linear array (ULA). Consider the element of the ULA to be a backbaffled phased. IsotropicProjector with a VoltageResponse of 100 Volts and with a FrequencyRange from 10 Hz to 300 kHz . Create a phased. ULA object to model the uniform linear array.

```
projector = phased.IsotropicProjector('BackBaffled',true,...
            'VoltageResponse',100,'FrequencyRange',[10 300000])
projector =
    phased.IsotropicProjector with properties:
        VoltageResponse: 100
            FrequencyRange: [10 300000]
            BackBaffled: true
myArray = phased.ULA('Element',projector,'NumElements',20,...
            'ElementSpacing',1500/200e3/2)
myArray =
    phased.ULA with properties:
```

```
        Element: [1x1 phased.IsotropicProjector]
        NumElements: 20
ElementSpacing: 0.0037
    ArrayAxis: 'y'
        Taper: 1
```

Using the beamwidth function, calculate and plot the 6 dB beamwidth of the sonar array. beamwidth(myArray,200e3,'dBDown',6,'PropagationSpeed',1500)

## 6-dB Beamwidth @ Azimuth Cut (Elevation Angle $=0^{\circ}$ )



Power Pattern (dB), Broadside at $0.00^{\circ}$ @ 200 kHz
ans $=6.9200$

## Calculate Beamwidth and Angles of Uniform Linear Array (ULA)

Calculate the half-power beamwidth and angles of a 20 -element uniform linear array (ULA) of cosine antenna elements.

Create a phased.CosineAntennaElement object with the 'CosinePower' exponents set to 1.5.
myAnt $=$ phased.CosineAntennaElement
myAnt $=$
phased.CosineAntennaElement with properties:

```
FrequencyRange: [0 1.0000e+20]
    CosinePower: [1.5000 1.5000]
```

Create a phased. ULA object to model a 20 -element ULA of cosine antenna elements. These elements are spaced at 0.5 meters on the azimuth plane.

```
array = phased.ULA('Element',myAnt,'NumElements',20)
array =
    phased.ULA with properties:
            Element: [1x1 phased.CosineAntennaElement]
        NumElements: 20
        ElementSpacing: 0.5000
            ArrayAxis: 'y'
            Taper: 1
```

Compute the beamwidth and angles of the array when it is operating at 3 e 8 Hz . Specify the beamwidth to be computed along the elevation plane.
[BW,Ang] = beamwidth(array,3e8,'Cut','Elevation')
$\mathrm{BW}=74.8200$
Ang $=1 \times 2$
-37.4100 37.4100

## Response of Antenna ULA

Create a 4-element ULA of isotropic antenna elements and find the response of each element at boresight. Plot the array response at 1 GHz for azimuth angles between -180 and 180 degrees.

```
ha = phased.ULA('NumElements',4);
fc = 1e9;
ang = [0;0];
resp = step(ha,fc,ang);
c = physconst('LightSpeed');
pattern(ha,fc,[-180:180],0,...
    'PropagationSpeed ',c,...
    'CoordinateSystem','rectangular')
```



## Response of Microphone ULA Array

Find the response of a ULA array of 10 omnidirectional microphones spaced 1.5 meters apart. Set the frequency response of the microphone to the range 20 Hz to 20 kHz and choose the signal frequency to be 100 Hz . Using the step method, determine the response of each element at boresight: 0 degrees azimuth and 0 degrees elevation.

```
mic = phased.OmnidirectionalMicrophoneElement( ...
    'FrequencyRange',[20 20e3]);
Nelem = 10;
array = phased.ULA('NumElements',Nelem, ...
    'ElementSpacing',1.5,'Element',mic);
fc = 100;
ang = [0;0];
resp = array(fc,ang)
resp = 10×1
```

Plot the array directivity. Assume the speed of sound in air to be $340 \mathrm{~m} / \mathrm{s}$.
c = 340;
pattern(array,fc,[-180:180],0,'PropagationSpeed',c,'CoordinateSystem','polar')


Directivity (dBi), Broadside at $0.00^{\circ}$

## Simulate Received Signals at ULA

Simulate two received plane-wave random signals at a 4 -element ULA. The signals arrive from $10^{\circ}$ and $30^{\circ}$ azimuth. Both signals have an elevation angle of $0^{\circ}$. Assume the propagation speed is the speed of light and the carrier frequency of the signal is 100 MHz .
array = phased.ULA(4)
$y=$ collectPlaneWave(array, randn (4,2),[10 30],100e6,physconst('LightSpeed'))
$y=4 \times 4$ complex

| $0.7430-0.3705 i$ | $0.8433-0.1314 i$ | $0.8433+0.1314 i$ | $0.7430+0.3705 i$ |
| ---: | ---: | ---: | ---: | ---: |
| $0.8418+0.4308 i$ | $0.5632+0.1721 i$ | $0.5632-0.1721 i$ | $0.8418-0.4308 i$ |
| $-2.4817+0.9157 i$ | $-2.6683+0.3175 i$ | $-2.6683-0.3175 i$ | $-2.4817-0.9157 i$ |

## Create Grating Lobe Diagram for ULA

Plot the grating lobe diagram for a 4 -element uniform linear array having element spacing less than one-half wavelength. Grating lobes are plotted in $u-v$ coordinates.

Assume the operating frequency of the array is 3 GHz and the spacing between elements is 0.45 of the wavelength. All elements are isotropic antenna elements. Steer the array in the direction 45 degrees in azimuth and 0 degrees in elevation.

```
c = physconst('LightSpeed');
f = 3e9;
lambda = c/f;
sIso = phased.IsotropicAntennaElement;
sULA = phased.ULA('Element',sIso,'NumElements',4,...
    'ElementSpacing',0.45*lambda);
plotGratingLobeDiagram(sULA,f,[45;0],c);
```


## Grating Lobe Diagram in U Space



The main lobe of the array is indicated by a filled black circle. The grating lobes in the visible and nonvisible regions are indicated by empty black circles. The visible region is defined by the direction cosine limits between $[-1,1]$ and is marked by the two vertical black lines. Because the array spacing is less than one-half wavelength, there are no grating lobes in the visible region of space. There are
an infinite number of grating lobes in the nonvisible regions, but only those in the range $[-3,3]$ are shown.

The grating-lobe free region, shown in green, is the range of directions of the main lobe for which there are no grating lobes in the visible region. In this case, it coincides with the visible region.

The white area of the diagram indicates a region where no grating lobes are possible.

## Create Grating Lobe Diagram for Undersampled ULA

Plot the grating lobe diagram for a 4 -element uniform linear array having element spacing greater than one-half wavelength. Grating lobes are plotted in $u-v$ coordinates.

Assume the operating frequency of the array is 3 GHz and the spacing between elements is 0.65 of a wavelength. All elements are isotropic antenna elements. Steer the array in the direction 45 degrees in azimuth and 0 degrees in elevation.

```
c = physconst('LightSpeed');
f = 3e9;
lambda = c/f;
sIso = phased.IsotropicAntennaElement;
sULA = phased.ULA('Element',sIso,'NumElements',4,'ElementSpacing',0.65*lambda);
plotGratingLobeDiagram(sULA,f,[45;0],c);
```

Grating Lobe Diagram in U Space


The main lobe of the array is indicated by a filled black circle. The grating lobes in the visible and nonvisible regions are indicated by empty black circles. The visible region, marked by the two black vertical lines, corresponds to arrival angles between -90 and 90 degrees. The visible region is defined by the direction cosine limits $-1 \leq u \leq 1$. Because the array spacing is greater than one-half wavelength, there is now a grating lobe in the visible region of space. There are an infinite number of grating lobes in the nonvisible regions, but only those for which $-3 \leq u \leq 3$ are shown.

The grating-lobe free region, shown in green, is the range of directions of the main lobe for which there are no grating lobes in the visible region. In this case, it lies inside the visible region.

## Create Grating Lobe Diagram for ULA With Different Phase-Shifter Frequency

Plot the grating lobe diagram for a 4 -element uniform linear array having element spacing greater than one-half wavelength. Apply a phase-shifter frequency that differs from the signal frequency. Grating lobes are plotted in u-v coordinates.

Assume the signal frequency is 3 GHz and the spacing between elements is $0.65 \lambda$. All elements are isotropic antenna elements. The phase-shifter frequency is set to 3.5 GHz . Steer the array in the direction $45^{\circ}$ azimuth, $0^{\circ}$ elevation.

```
c = physconst('LightSpeed');
f = 3e9;
f0 = 3.5e9;
lambda = c/f;
sIso = phased.IsotropicAntennaElement;
sULA = phased.ULA('Element',sIso,'NumElements',4,...
    'ElementSpacing',0.65*lambda );
plotGratingLobeDiagram(sULA,f,[45;0],c,f0);
```


## Grating Lobe Diagram in U Space



As a result of adding the shifted frequency, the mainlobe shifts right towards larger $u$ values. The beam no longer points toward the actual source arrival angle.

The mainlobe of the array is indicated by a filled black circle. The grating lobes in the visible and nonvisible regions are indicated by empty black circles. The visible region, marked by the two black vertical lines, corresponds to arrival angles between $-90^{\circ}$ and $90^{\circ}$. The visible region is defined by the direction cosine limits $-1 \leq u \leq 1$. Because the array spacing is greater than one-half wavelength, there is now a grating lobe in the visible region of space. There are an infinite number of grating lobes in the nonvisible regions, but only those for which $-3 \leq u \leq 3$ are shown.

The grating-lobe free region, shown in green, is the range of directions of the main lobe for which there are no grating lobes in the visible region. In this case, it lies inside the visible region.

## Version History <br> Introduced in R2011a

## References

[1] Brookner, E., ed. Radar Technology. Lexington, MA: LexBook, 1996.
[2] Van Trees, H. Optimum Array Processing. New York: Wiley-Interscience, 2002.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.
Usage notes and limitations:

- pattern, patternAzimuth, patternElevation, plotResponse, and viewArray methods are not supported.
- See "System Objects in MATLAB Code Generation" (MATLAB Coder).


## See Also

phased.ReplicatedSubarray|phased.PartitionedArray|phased.ConformalArray| phased.CosineAntennaElement | phased.CustomAntennaElement | phased.CrossedDipoleAntennaElement | phased.IsotropicAntennaElement | phased.ShortDipoleAntennaElement | phased.URA | phased.UCA | phased.HeterogeneousULA | phased.HeterogeneousURA

Topics
Phased Array Gallery

## directivity

System object: phased. ULA
Package: phased
Directivity of uniform linear array

## Syntax

D = directivity (H, FREQ,ANGLE)
D = directivity (H, FREQ, ANGLE,Name, Value)

## Description

D = directivity ( $\mathrm{H}, \mathrm{FREQ}$, ANGLE) computes the "Directivity ( dBi )" on page 1-1819 of a uniform linear array (ULA) of antenna or microphone elements, H , at frequencies specified by FREQ and in angles of direction specified by ANGLE.

The integration used when computing array directivity has a minimum sampling grid of 0.1 degrees. If an array pattern has a beamwidth smaller than this, the directivity value will be inaccurate.

D = directivity (H, FREQ, ANGLE, Name, Value) returns the directivity with additional options specified by one or more Name, Value pair arguments.

## Input Arguments

## H - Uniform linear array

System object
Uniform linear array specified as a phased. ULA System object.
Example: $\mathrm{H}=$ phased.ULA;

## FREQ - Frequency for computing directivity and patterns

positive scalar | 1-by-L real-valued row vector
Frequencies for computing directivity and patterns, specified as a positive scalar or 1-by-L realvalued row vector. Frequency units are in hertz.

- For an antenna, microphone, or sonar hydrophone or projector element, FREQ must lie within the range of values specified by the FrequencyRange or FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased.CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: [1e8 2e6]
Data Types: double

## ANGLE - Angles for computing directivity

## 1-by- $M$ real-valued row vector | 2-by- $M$ real-valued matrix

Angles for computing directivity, specified as a 1-by- $M$ real-valued row vector or a 2 -by- $M$ real-valued matrix, where $M$ is the number of angular directions. Angle units are in degrees. If ANGLE is a 2 -by- $M$ matrix, then each column specifies a direction in azimuth and elevation, [az;el]. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

If ANGLE is a $1-b y-M$ vector, then each entry represents an azimuth angle, with the elevation angle assumed to be zero.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the xy plane. This angle is positive when measured from the $x$-axis toward the $y$-axis. The elevation angle is the angle between the direction vector and $x y$ plane. This angle is positive when measured towards the $z$-axis. See "Azimuth and Elevation Angles".
Example: [45 60; 0 10]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Namel=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## PropagationSpeed - Signal propagation speed

speed of light (default) | positive scalar
Signal propagation speed, specified as the comma-separated pair consisting of ' PropagationSpeed ' and a positive scalar in meters per second.
Example: 'PropagationSpeed', physconst('LightSpeed')
Data Types: double
Weights - Array weights
1 (default) $\mid N$-by-1 complex-valued column vector $\mid N$-by- $L$ complex-valued matrix
Array weights, specified as the comma-separated pair consisting of 'Weights' and an $N$-by-1 complex-valued column vector or $N$-by- $L$ complex-valued matrix. Array weights are applied to the elements of the array to produce array steering, tapering, or both. The dimension $N$ is the number of elements in the array. The dimension $L$ is the number of frequencies specified by FREQ.

| Weights Dimension | FREQ Dimension | Purpose |
| :--- | :--- | :--- |
| $N$-by-1 complex-valued column <br> vector | Scalar or 1-by- $L$ row vector | Applies a set of weights for the <br> single frequency or for all $L$ <br> frequencies. |
| $N$-by-L complex-valued matrix | 1-by-L row vector | Applies each of the $L$ columns of <br> 'Weights' for the <br> corresponding frequency in <br> FREQ. |

Note Use complex weights to steer the array response toward different directions. You can create weights using the phased.SteeringVector System object or you can compute your own weights. In general, you apply Hermitian conjugation before using weights in any Phased Array System Toolbox function or System object such as phased. Radiator or phased. Collector. However, for the directivity, pattern, patternAzimuth, and patternElevation methods of any array System object use the steering vector without conjugation.

Example: 'Weights',ones(N,M)
Data Types: double
Complex Number Support: Yes

## Output Arguments

## D - Directivity

M-by-L matrix
Directivity, returned as an $M$-by- $L$ matrix. Each row corresponds to one of the $M$ angles specified by ANGLE. Each column corresponds to one of the $L$ frequency values specified in FREQ. Directivity units are in dBi where dBi is defined as the gain of an element relative to an isotropic radiator.

## Examples

## Directivity of Uniform Linear Array

Compute the directivities of two different uniform linear arrays (ULA). One array consists of isotropic antenna elements and the second array consists of cosine antenna elements. In addition, compute the directivity when the first array is steered in a specified direction. For each case, calculate the directivities for a set of seven different azimuth directions all at zero degrees elevation. Set the frequency to 800 MHz .

## Array of isotropic antenna elements

First, create a 10 -element ULA of isotropic antenna elements spaced 1/2-wavelength apart.

```
c = physconst('LightSpeed');
fc = 3e8;
lambda = c/fc;
ang = [-30,-20,-10,0,10,20,30; 0,0,0,0,0,0,0];
myAnt1 = phased.IsotropicAntennaElement;
myArray1 = phased.ULA(10,lambda/2,'Element',myAnt1);
Compute the directivity.
d = directivity(myArray1,fc,ang,'PropagationSpeed',c)
d = 7x1
    -6.9886
    -6.2283
    -6.5176
    10.0011
    -6.5176
```


## Array of cosine antenna elements

Next, create a 10-element ULA of cosine antenna elements spaced 1/2-wavelength apart.

```
myAnt2 = phased.CosineAntennaElement('CosinePower',[1.8,1.8]);
```

myArray2 = phased.ULA(10,lambda/2,'Element',myAnt2);

Compute the directivity.

```
d = directivity(myArray2,fc,ang,'PropagationSpeed',c)
d = 7x1
    -1.9838
    0.0529
    0.4968
    17.2548
        0.4968
        0.0529
    -1.9838
```

The directivity of the cosine ULA is greater than the directivity of the isotropic ULA because of the larger directivity of the cosine antenna element.

## Steered array of isotropic antenna elements

Finally, steer the isotropic antenna array to 30 degrees in azimuth and compute the directivity.

```
w = steervec(getElementPosition(myArray1)/lambda,[30;0]);
d = directivity(myArray1,fc,ang,'PropagationSpeed',c,...
    'Weights',w)
d = 7\times1
    -297.2705
    -13.9783
    -9.5713
    -6.9897
    -4.5787
    -2.0536
    10.0000
```

The directivity is greatest in the steered direction.

## More About

## Directivity (dBi)

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\mathrm{total}}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## See Also

pattern | patternAzimuth | patternElevation

## collectPlaneWave

System object: phased. ULA
Package: phased
Simulate received plane waves

## Syntax

```
Y = collectPlaneWave(H,X,ANG)
Y = collectPlaneWave(H,X,ANG,FREQ)
Y = collectPlaneWave(H,X,ANG,FREQ,C)
```


## Description

$Y=\operatorname{collectPlaneWave}(H, X, A N G)$ returns the received signals at the sensor array, $H$, when the input signals indicated by $X$ arrive at the array from the directions specified in ANG.
$Y=$ collectPlaneWave ( $H, X$, ANG, $F R E Q$ ), in addition, specifies the incoming signal carrier frequency in FREQ.
$\mathrm{Y}=$ collectPlaneWave( $\mathrm{H}, \mathrm{X}, \mathrm{ANG}, \mathrm{FREQ}, \mathrm{C})$, in addition, specifies the signal propagation speed in C.

## Input Arguments

## H

Array object.
X
Incoming signals, specified as an M-column matrix. Each column of $X$ represents an individual incoming signal.

## ANG

Directions from which incoming signals arrive, in degrees. ANG can be either a 2-by-M matrix or a row vector of length $M$.

If ANG is a 2-by-M matrix, each column specifies the direction of arrival of the corresponding signal in X. Each column of ANG is in the form [azimuth; elevation]. The azimuth angle must be between $-180^{\circ}$ and $180^{\circ}$, inclusive. The elevation angle must be between $-90^{\circ}$ and $90^{\circ}$, inclusive.

If ANG is a row vector of length M , each entry in ANG specifies the azimuth angle. In this case, the corresponding elevation angle is assumed to be $0^{\circ}$.

FREQ
Carrier frequency of signal in hertz. FREQ must be a scalar.
Default: 3e8

## C

Propagation speed of signal in meters per second.
Default: Speed of light

## Output Arguments

## Y

Received signals. Y is an N-column matrix, where N is the number of elements in the array H. Each column of $Y$ is the received signal at the corresponding array element, with all incoming signals combined.

## Examples

## Simulate Received Signals at ULA

Simulate two received plane-wave random signals at a 4 -element ULA. The signals arrive from $10^{\circ}$ and $30^{\circ}$ azimuth. Both signals have an elevation angle of $0^{\circ}$. Assume the propagation speed is the speed of light and the carrier frequency of the signal is 100 MHz .

```
array = phased.ULA(4);
y = collectPlaneWave(array,randn(4,2),[10 30],100e6,physconst('LightSpeed'))
y = 4×4 complex
    0.7430-0.3705i 0.8433 - 0.1314i 0.8433 + 0.1314i 0.7430 + 0.3705i
    0.8418 + 0.4308i 0.5632 + 0.1721i 0.5632 - 0.1721i 0.8418 - 0.4308i
    -2.4817 + 0.9157i -2.6683 + 0.3175i -2.6683-0.3175i -2.4817 - 0.9157i
    1.0724-0.4748i 1.1895-0.1671i 1.1895 + 0.1671i 1.0724 + 0.4748i
```


## Algorithms

collectPlaneWave modulates the input signal with a phase corresponding to the delay caused by the direction of arrival. The method does not account for the response of individual elements in the array.

For further details, see [1].

## References

[1] Van Trees, H. Optimum Array Processing. New York: Wiley-Interscience, 2002.

## See Also

uv2azel | phitheta2azel

## getElementPosition

System object: phased. ULA
Package: phased
Positions of array elements

## Syntax

pos = getElementPosition(sULA)
pos = getElementPosition(sULA,elemidx)

## Description

pos = getElementPosition(sULA) returns the element positions of the phased.ULA System object, sULA. pos is a 3-by- $N$ matrix, where $N$ is the number of elements in sULA. Each column of pos defines the position of an element in the local coordinate system taking the form [ $x ; y ; z$ ]. Units are meters. The origin of the local coordinate system is the phase center of the array.
pos = getElementPosition(sULA, elemidx) returns only the positions of the elements that are specified in the element index vector elemidx. This syntax can use any of the input arguments in the previous syntax.

## Examples

## ULA Element Positions

Construct a ULA with 5 elements along the $z$-axis. Obtain the element positions.

```
sULA = phased.ULA('NumElements',5,'ArrayAxis','z');
pos = getElementPosition(sULA)
pos = 3\times5
```

| 0 | 0 | 0 | 0 | 0 |
| ---: | ---: | ---: | ---: | ---: |
| 0 | 0 | 0 | 0 | 0 |
| -1.0000 | -0.5000 | 0 | 0.5000 | 1.0000 |

## getElementNormal

System object: phased. ULA
Package: phased
Normal vector to array elements

## Syntax

normvec = getElementNormal(sULA)
normvec $=$ getElementNormal(sULA, elemidx)

## Description

normvec $=$ getElementNormal(sULA) returns the normal vectors of the array elements of the phased.ULA System object, sULA. The output argument normvec is a 2 -by- $N$ matrix, where $N$ is the number of elements in array, sULA. Each column of normvec defines the normal direction of an element in the local coordinate system in the form [az;el]. Units are degrees. Array elements are located along the axis selected in the ArrayAxis property. Element normal vectors are parallel to the array normal. The normal to a ULA array depends upon the selected ArrayAxis property.

| ArrayAxis Property Value | Array Normal Direction |
| :--- | :--- |
| $' x$ ' | azimuth $=90^{\circ}$, elevation $=0^{\circ}(y$-axis $)$ |
| ' $y$ ' | azimuth $=0^{\circ}$, elevation $=0^{\circ}(x$-axis $)$ |
| $' z{ }^{\prime}$ | azimuth $=0^{\circ}$, elevation $=0^{\circ}(x$-axis $)$ |

The origin of the local coordinate system is defined by the phase center of the array.
normvec $=$ getElementNormal(sULA,elemidx) returns only the normal vectors of the elements specified in the element index vector, elemidx. This syntax can use any of the input arguments in the previous syntax.

## Input Arguments

## sULA - Uniform line array

phased.ULA System object
Uniform line array, specified as a phased. ULA System object.
Example: sULA = phased.ULA
elemidx - Element indices
all array elements (default) | integer-valued 1 -by- $M$ row vector | integer-valued $M$-by-1 column vector
Element indices, specified as a 1 -by- $M$ or $M$-by-1 vector. Index values lie in the range 1 to $N$ where $N$ is the number of elements of the array. When elemidx is specified, getElementNormal returns the normal vectors of the elements contained in elemidx.
Example: [1,5,4]

## Output Arguments

## normvec - Element normal vectors

2-by-P real-valued vector
Element normal vectors, specified as a 2-by-P real-valued vector. Each column of normvec takes the form [az,el]. When elemidx is not specified, $P$ equals the array dimension. When elemidx is specified, $P$ equals the length of elemidx, $M$.

## Examples

## ULA Element Normals

Construct three ULAs with elements along the $x-, y$-, and $z$-axes. Obtain the element normals.
First, choose the array axis along the $x$-axis.

```
sULA1 = phased.ULA('NumElements',5,'ArrayAxis','x');
norm = getElementNormal(sULA1)
norm = 2×5
\begin{tabular}{rrrrr}
90 & 90 & 90 & 90 & 90 \\
0 & 0 & 0 & 0 & 0
\end{tabular}
```

The element normal vectors point along the $y$-axis.
Next, choose the array axis along the $y$-axis.

```
sULA2 = phased.ULA('NumElements',5,'ArrayAxis','y');
norm = getElementNormal(sULA2)
norm = 2×5
    0}00\quad0\quad0\quad
    0
```

The element normal vectors point along the $x$-axis.
Finally, set the array axis along the $z$-axis. Obtain the normal vectors of the odd-numbered elements.

```
sULA3 = phased.ULA('NumElements',5,'ArrayAxis','z');
norm = getElementNormal(sULA3,[1,3,5])
norm = 2×3
    0 0 0
    0 0 0
```

The element normal vectors also point along the $x$-axis.

# Version History <br> Introduced in R2016a 

## getNumElements

System object: phased. ULA
Package: phased
Number of elements in array

## Syntax

N = getNumElements(H)

## Description

$\mathrm{N}=$ getNumElements $(\mathrm{H})$ returns the number of elements, N , in the ULA object H .

## Examples

Get Number of ULA Elements
Construct a default ULA and obtain the number of elements in that array.
array = phased.ULA;
$N=$ getNumElements(array)
$N=2$

## getTaper

System object: phased.ULA
Package: phased
Array element tapers

## Syntax

wts = getTaper(h)

## Description

wts = getTaper(h) returns the tapers, wts, applied to each element of the phased uniform line array (ULA), h. Tapers are often referred to as weights.

## Input Arguments

h - Uniform line array
phased.ULA System object
Uniform line array specified as a phased.ULA System object.

## Output Arguments

wts - Array element tapers
$N$-by-1 complex-valued vector
Array element tapers returned as an $N$-by- 1 complex-valued vector, where $N$ is the number of elements in the array.

## Examples

## Construct ULA with Taylor Window

Construct a 5 -element ULA with a Taylor window taper. Then, obtain the element taper values.

```
taper = taylorwin(5)';
array = phased.ULA(5,'Taper',taper);
w = getTaper(array)
w = 5 < 1
    0.5181
    1.2029
    1.5581
    1.2029
    0.5181
```


## isPolarizationCapable

System object: phased.ULA
Package: phased
Polarization capability

## Syntax

flag = isPolarizationCapable(h)

## Description

flag = isPolarizationCapable(h) returns a Boolean value, flag, indicating whether the array supports polarization. An array supports polarization if all of its constituent sensor elements support polarization.

## Input Arguments

## h - Uniform line array

Uniform line array specified as a phased. ULA System object.

## Output Arguments

## flag - Polarization-capability flag

Polarization-capability flag returned as a Boolean value true if the array supports polarization or false if it does not.

## Examples

## Short-Dipole Antenna ULA Supports Polarization

Show that an array of phased.ShortDipoleAntennaElement antenna elements supports polarization.

```
antenna = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[1e9 10e9]);
array = phased.ULA('NumElements',3,'Element',antenna);
isPolarizationCapable(array)
ans = logical
    1
```

The returned value of 1 shows that this array supports polarization.

## plotResponse

System object: phased.ULA
Package: phased
Plot response pattern of array

## Syntax

plotResponse(H, FREQ, V)
plotResponse(H, FREQ, V, Name, Value)
hPlot = plotResponse( $\qquad$ )

## Description

plotResponse ( $\mathrm{H}, \mathrm{FREQ}, \mathrm{V}$ ) plots the array response pattern along the azimuth cut, where the elevation angle is 0 . The operating frequency is specified in FREQ. The propagation speed is specified in $V$.
plotResponse(H, FREQ, V,Name, Value) plots the array response with additional options specified by one or more Name, Value pair arguments.
hPlot = plotResponse( $\qquad$ ) returns handles of the lines or surface in the figure window, using any of the input arguments in the previous syntaxes.

## Input Arguments

## H

Array object

## FREQ

Operating frequency in Hertz specified as a scalar or 1-by-K row vector. Values must lie within the range specified by a property of H . That property is named FrequencyRange or FrequencyVector, depending on the type of element in the array. The element has no response at frequencies outside that range. If you set the 'RespCut ' property of H to ' 3 D ' , FREQ must be a scalar. When FREQ is a row vector, plot Response draws multiple frequency responses on the same axes.

## V

Propagation speed in meters per second.

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## CutAngle

Cut angle as a scalar. This argument is applicable only when RespCut is ' Az ' or ' El '. If RespCut is 'Az' , CutAngle must be between -90 and 90. If RespCut is 'El', CutAngle must be between -180 and 180.

Default: 0

## Format

Format of the plot, using one of 'Line', 'Polar', or 'UV '. If you set Format to 'UV ', FREQ must be a scalar.

Default: 'Line'

## NormalizeResponse

Set this value to true to normalize the response pattern. Set this value to false to plot the response pattern without normalizing it. This parameter is not applicable when you set the Unit parameter value to 'dbi'.

## Default: true

## OverlayFreq

Set this value to true to overlay pattern cuts in a 2-D line plot. Set this value to false to plot pattern cuts against frequency in a 3-D waterfall plot. If this value is false, FREQ must be a vector with at least two entries.

This parameter applies only when Format is not 'Polar' and RespCut is not '3D '.

## Default: true

## Polarization

Specify the polarization options for plotting the array response pattern. The allowable values are |'None' | 'Combined' | 'H' | 'V' | where

- 'None' specifies plotting a nonpolarized response pattern
- 'Combined ' specifies plotting a combined polarization response pattern
- 'H' specifies plotting the horizontal polarization response pattern
- 'V ' specifies plotting the vertical polarization response pattern

For arrays that do not support polarization, the only allowed value is 'None '. This parameter is not applicable when you set the Unit parameter value to ' dbi ' .

Default: 'None'

## RespCut

Cut of the response. Valid values depend on Format, as follows:

- If Format is 'Line' or 'Polar', the valid values of RespCut are 'Az', 'El', and '3D'. The default is ' Az '.
- If Format is 'UV', the valid values of RespCut are 'U' and '3D'. The default is 'U'.

If you set RespCut to ' 3D' , FREQ must be a scalar.

## Unit

The unit of the plot. Valid values are 'db', 'mag', 'pow', or 'dbi'. This parameter determines the type of plot that is produced.

| Unit value | Plot type |
| :--- | :--- |
| db | power pattern in dB scale |
| mag | field pattern |
| pow | power pattern |
| dbi | directivity |

Default: 'db'

## Weights

Weight values applied to the array, specified as a length- $N$ column vector or $N$-by- $M$ matrix. The dimension $N$ is the number of elements in the array. The interpretation of $M$ depends upon whether the input argument FREQ is a scalar or row vector.

| Weights Dimensions | FREQ Dimension | Purpose |
| :--- | :--- | :--- |
| $N$-by-1 column vector | Scalar or 1-by- $M$ row vector | Apply one set of weights for the <br> same single frequency or all $M$ <br> frequencies. |
| $N$-by- $M$ matrix | Scalar | Apply all of the $M$ different <br> columns in Weights for the <br> same single frequency. |
|  |  | Apply each of the $M$ different <br> columns in Weights for the <br> corresponding frequency in <br> FREQ. |
|  |  |  |

## AzimuthAngles

Azimuth angles for plotting array response, specified as a row vector. The AzimuthAngles parameter sets the display range and resolution of azimuth angles for visualizing the radiation pattern. This parameter is allowed only when the RespCut parameter is set to 'Az' or '3D' and the Format parameter is set to 'Line' or 'Polar'. The values of azimuth angles should lie between $180^{\circ}$ and $180^{\circ}$ and must be in nondecreasing order. When you set the RespCut parameter to ' 3 D ', you can set the AzimuthAngles and ElevationAngles parameters simultaneously.

Default: [-180:180]

## ElevationAngles

Elevation angles for plotting array response, specified as a row vector. The ElevationAngles parameter sets the display range and resolution of elevation angles for visualizing the radiation pattern. This parameter is allowed only when the RespCut parameter is set to ' El ' or ' 3 D ' and the

Format parameter is set to 'Line' or 'Polar'. The values of elevation angles should lie between $90^{\circ}$ and $90^{\circ}$ and must be in nondecreasing order. When yous set the RespCut parameter to ' $3 \mathrm{D}^{\prime}$ ', you can set the ElevationAngles and AzimuthAngles parameters simultaneously.

Default: [-90:90]

## UGrid

$U$ coordinate values for plotting array response, specified as a row vector. The UGrid parameter sets the display range and resolution of the $U$ coordinates for visualizing the radiation pattern in $U / V$ space. This parameter is allowed only when the Format parameter is set to 'UV' and the RespCut parameter is set to ' $U$ ' or ' $3 D$ '. The values of UGrid should be between -1 and 1 and should be specified in nondecreasing order. You can set the UGrid and VGrid parameters simultaneously.

Default: [-1:0.01:1]

## VGrid

$V$ coordinate values for plotting array response, specified as a row vector. The VGrid parameter sets the display range and resolution of the $V$ coordinates for visualizing the radiation pattern in $U / V$ space. This parameter is allowed only when the Format parameter is set to 'UV' and the RespCut parameter is set to ' $3 D^{\prime}$ '. The values of VGrid should be between -1 and 1 and should be specified in nondecreasing order. You can set VGrid and UGrid parameters simultaneously.

Default: [-1:0.01:1]

## Examples

## Plot Azimuth Response of 4-Element ULA

Construct a 4-element ULA of isotropic elements (the default) and plot its azimuth response in polar form. By default, the azimuth cut is at 0 degrees elevation. Assume the operating frequency is 1 GHz and the wave propagation speed is the speed of light. The nominal element spacing is $1 / 2$ meter which means that the array is undersampled at this frequency.

```
ha = phased.ULA(4);
fc = 1e9;
c = physconst('LightSpeed');
plotResponse(ha,fc,c,'RespCut','Az','Format','Polar');
```



Normalized Power (dB), Broadside at $0.00^{\circ}$

## Plot Response of ULA at Two Frequencies

This example shows how to plot an azimuth cut of the response of a uniform linear array at 0 degrees elevation using a line plot. The plot shows the responses at operating frequencies of 300 MHz and 400 MHz .
h = phased.ULA;
fc = [3e8 4e8];
$\mathrm{c}=$ physconst('LightSpeed'); plotResponse(h,fc, c);


## Plot Azimuth Response of Tapered 11-Element ULA

This example shows how to construct an 11-element ULA array of backbaffled omnidirectional microphones for beamforming the direction of arrival of sound in air. The elements are spaced four centimeters apart and have a frequency response lying in the $2000-8000 \mathrm{~Hz}$ frequency range. Use the plotResponse method to display an azimuth cut of the array's response at 5000 Hz . Use the 'Weights ' parameter to apply both uniform tapering and Taylor window tapering to the array at the same frequency. Finally, use the 'AzimuthAngles ' parameter to limit the display from - 45 to 45 degrees in 0.1 degree increments. A typical value for the speed of sound in air is 343 meters/second.

```
s_omni = phased.OmnidirectionalMicrophoneElement(...
    'FrequencyRange',[2000,8000],...
    'BackBaffled',true);
s_ula = phased.ULA(11,'Element',s_omni,...
    'ElementSpacing',0.04);
c = 343.0;
fc = 5000;
wts = taylorwin(11);
plotResponse(s_ula,fc,c,'RespCut','Az',...
    'Format','\overline{Polar',...}
    'Weights',[ones(11,1),wts],...
    'AzimuthAngles',[-45:.1:45]);
```



Normalized Power (dB), Broadside at $0.00^{\circ}$

The plot shows that the Taylor tapered set of weights reduces the adjacent sidelobes while broadening the main lobe compared to a uniformly tapered array.

## Plot Directivity of 11-Element ULA of Cosine Pattern Antennas

This example shows how to construct an 11-element ULA of cosine antenna elements that are spaced one-half wavelength apart. Then, using the plotResponse method, plot an azimuth cut of the array's directivity by setting the 'Unit' parameter to 'dbi' . Assume the operating frequency is 1.5 GHz and the wave propagation speed is the speed of light.

```
fc = 1.5e9;
c = physconst('Lightspeed');
lambda = c/fc;
sCos = phased.CosineAntennaElement('FrequencyRange',...
    [1e9 2e9],'CosinePower',[2.5,3.5]);
sULA = phased.ULA(11,0.5*lambda,'Element',sCos);
plotResponse(sULA,fc,c,'RespCut','Az','Unit','dbi');
```



## See Also

uv2azel|azel2uv

## pattern

System object: phased.ULA
Package: phased
Plot array pattern

## Syntax

```
pattern(sArray,FREQ)
pattern(sArray,FREQ,AZ)
pattern(sArray,FREQ,AZ,EL)
pattern(__,Name,Value)
[PAT,AZ_ANG,EL_ANG] = pattern(
```

$\qquad$

``` )
```


## Description

pattern(sArray, FREQ) plots the 3-D array directivity pattern (in dBi) for the array specified in sArray. The operating frequency is specified in FREQ.

The integration used when computing array directivity has a minimum sampling grid of 0.1 degrees. If an array pattern has a beamwidth smaller than this, the directivity value will be inaccurate.
pattern(sArray, FREQ,AZ) plots the array directivity pattern at the specified azimuth angle.
pattern(sArray, FREQ, AZ, EL) plots the array directivity pattern at specified azimuth and elevation angles.
pattern( $\qquad$ ,Name, Value) plots the array pattern with additional options specified by one or more Name, Value pair arguments.
[PAT,AZ_ANG,EL_ANG] = pattern( __ ) returns the array pattern in PAT. The AZ_ANG output contains the coordinate values corresponding to the rows of PAT. The EL_ANG output contains the coordinate values corresponding to the columns of PAT. If the 'CoordinateSystem' parameter is set to ' uv', then AZ_ANG contains the $U$ coordinates of the pattern and EL_ANG contains the $V$ coordinates of the pattern. Otherwise, they are in angular units in degrees. $U V$ units are dimensionless.

Note This method replaces the plotResponse method. See "Convert plotResponse to pattern" on page 1-1847 for guidelines on how to use pattern in place of plotResponse.

## Input Arguments

## sArray - Uniform linear array

System object
Uniform linear array, specified as a phased. ULA System object.
Example: sArray= phased.ULA;

## FREQ - Frequency for computing directivity and patterns

positive scalar | 1-by-L real-valued row vector
Frequencies for computing directivity and patterns, specified as a positive scalar or 1-by-L realvalued row vector. Frequency units are in hertz.

- For an antenna, microphone, or sonar hydrophone or projector element, FREQ must lie within the range of values specified by the FrequencyRange or FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased. CustomAntennaElement and phased.CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: [1e8 2e6]
Data Types: double

## AZ - Azimuth angles

[-180:180] (default) | 1-by- $N$ real-valued row vector
Azimuth angles for computing directivity and pattern, specified as a 1-by- $N$ real-valued row vector where $N$ is the number of azimuth angles. Angle units are in degrees. Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the $x y$ plane. When measured from the $x$-axis toward the $y$-axis, this angle is positive.

## Example: [-45:2:45]

Data Types: double

## EL - Elevation angles

[-90:90] (default) | 1-by-M real-valued row vector
Elevation angles for computing directivity and pattern, specified as a 1-by-M real-valued row vector where $M$ is the number of desired elevation directions. Angle units are in degrees. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

The elevation angle is the angle between the direction vector and $x y$-plane. The elevation angle is positive when measured towards the $z$-axis.

Example: [-75:1:70]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

```
CoordinateSystem - Plotting coordinate system
'polar' (default)|'rectangular'|'uv'
```

Plotting coordinate system of the pattern, specified as the comma-separated pair consisting of 'CoordinateSystem' and one of 'polar', 'rectangular', or 'uv'. When
'CoordinateSystem' is set to 'polar' or 'rectangular', the AZ and EL arguments specify the pattern azimuth and elevation, respectively. AZ values must lie between $-180^{\circ}$ and $180^{\circ}$. EL values must lie between $-90^{\circ}$ and $90^{\circ}$. If 'CoordinateSystem' is set to 'uv', AZ and EL then specify $U$ and $V$ coordinates, respectively. AZ and EL must lie between -1 and 1.
Example: 'uv'
Data Types: char

## Type - Displayed pattern type

'directivity' (default) |'efield'|'power'|'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type ' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb' - power pattern converted to dB.

Example: 'powerdb'
Data Types: char

## Orientation - Array orientation

[0;0;0]. (default)|3-by-1 real-valued column vector
Array orientation, specified as a 3-by-1 real-valued column vector containing the rotation angles with respect to the $x-y$-, and $z$-axes of the local coordinate system, respectively.

## Normalize - Display normalize pattern

true (default) | false
Display normalized pattern, specified as the comma-separated pair consisting of 'Normalize' and a Boolean. Set this parameter to true to display a normalized pattern. This parameter does not apply when you set 'Type' to 'directivity'. Directivity patterns are already normalized.
Data Types: logical

## ShowArray - View array geometry

false (default)| true
View the array geometry along with the 3D radiation pattern, specified as false or true.
Data Types: logical
ShowLocalCoordinates - Show local coordinate axes
true (default) | false
Show the local coordinate axes, specified as true or false.
Data Types: logical

## ShowColorbar - Show colorbar

true (default) | false

Show the colorbar, specified as true or false.
Data Types: logical

## Parent - Handle to axis

scalar
Handle to the axes along which the array geometry is displayed specified as a scalar.

## PlotStyle - Plotting style

'overlay' (default)|'waterfall'
Plotting style, specified as the comma-separated pair consisting of 'Plotstyle' and either 'overlay' or 'waterfall'. This parameter applies when you specify multiple frequencies in FREQ in 2-D plots. You can draw 2-D plots by setting one of the arguments AZ or EL to a scalar.

## Data Types: char

## Polarization - Polarized field component

'combined' (default) | 'H' | 'V'
Polarized field component to display, specified as the comma-separated pair consisting of 'Polarization' and 'combined ', 'H', or 'V'. This parameter applies only when the sensors are polarization-capable and when the 'Type' parameter is not set to 'directivity'. This table shows the meaning of the display options.

| 'Polarization ' | Display |
| :--- | :--- |
| ' combined ' | Combined $H$ and $V$ polarization components |
| 'H' | $H$ polarization component |
| 'V' | $V$ polarization component |

Example: 'V '

## Data Types: char

## PropagationSpeed - Signal propagation speed

speed of light (default) | positive scalar
Signal propagation speed, specified as the comma-separated pair consisting of
' PropagationSpeed ' and a positive scalar in meters per second.
Example: 'PropagationSpeed', physconst('LightSpeed')
Data Types: double

## Weights - Array weights

1 (default) | $N$-by-1 complex-valued column vector | $N$-by-L complex-valued matrix
Array weights, specified as the comma-separated pair consisting of 'Weights' and an N -by-1 complex-valued column vector or $N$-by- $L$ complex-valued matrix. Array weights are applied to the elements of the array to produce array steering, tapering, or both. The dimension $N$ is the number of elements in the array. The dimension $L$ is the number of frequencies specified by FREQ.

| Weights Dimension | FREQ Dimension | Purpose |
| :--- | :--- | :--- |
| $N$-by-1 complex-valued column <br> vector | Scalar or 1-by- $L$ row vector | Applies a set of weights for the <br> single frequency or for all $L$ <br> frequencies. |
| $N$-by- $L$ complex-valued matrix | 1-by- $L$ row vector | Applies each of the $L$ columns of <br> 'Weights' for the <br> corresponding frequency in <br> FREQ. |

Note Use complex weights to steer the array response toward different directions. You can create weights using the phased. SteeringVector System object or you can compute your own weights. In general, you apply Hermitian conjugation before using weights in any Phased Array System Toolbox function or System object such as phased. Radiator or phased. Collector. However, for the directivity, pattern, patternAzimuth, and patternElevation methods of any array System object use the steering vector without conjugation.

Example: 'Weights',ones(N,M)
Data Types: double
Complex Number Support: Yes

## Output Arguments

## PAT - Array pattern

$M$-by- $N$ real-valued matrix
Array pattern, returned as an $M$-by- $N$ real-valued matrix. The dimensions of PAT correspond to the dimensions of the output arguments AZ_ANG and EL_ANG.

## AZ_ANG - Azimuth angles

scalar | 1-by- $N$ real-valued row vector
Azimuth angles for displaying directivity or response pattern, returned as a scalar or 1-by- $N$ realvalued row vector corresponding to the dimension set in AZ. The columns of PAT correspond to the values in AZ_ANG. Units are in degrees.

## EL_ANG - Elevation angles

scalar | 1-by-M real-valued row vector
Elevation angles for displaying directivity or response, returned as a scalar or 1-by-M real-valued row vector corresponding to the dimension set in EL. The rows of PAT correspond to the values in EL_ANG. Units are in degrees.

## Examples

## Plot Pattern of 9-Element ULA Antenna Array of Short Dipoles

Create an 9-element ULA of short dipole antenna elements spaced 0.2 meters apart. Display the azimuth and elevation directivities. The operating frequency is 500 MHz . Plot the directivities in polar coordinates.

Evaluate the fields at 45 degrees azimuth and 0 degrees elevation.

```
element = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[50e6,1000e6],...
    'AxisDirection','Z');
array = phased.ULA('NumElements',9,'ElementSpacing',1.5,'Element',element);
fc = 500e6;
ang = [45;0];
resp = array(fc,ang);
disp(resp.V)
```

    -1. 2247
    -1.2247
    -1.2247
    -1. 2247
    -1.2247
    -1.2247
    -1. 2247
    -1.2247
    \(-1.2247\)
    Display the azimuth directivity pattern at 500 MHz for azimuth angles between -180 and 180 degrees.

```
c = physconst('LightSpeed');
pattern(array,fc,[-180:180],0,...
    'Type','directivity',...
    'PropagationSpeed',c)
```



Directivity (dBi), Broadside at $0.00^{\circ}$

Display the elevation directivity pattern at 500 MHz for elevation angles between -90 and 90 degrees.
pattern(array,fc,[0],[-90:90],...
'Type','directivity',...
'PropagationSpeed ', c)


Directivity (dBi), Broadside at $0.00^{\circ}$

## Plot Pattern of 10-Element ULA Antenna Array in UV Space

Create a 10-element ULA antenna array consisting of cosine antenna elements spaced 10 cm apart. Display the 3-D power pattern in UV space. The operating frequency is 500 MHz .

```
sCos = phased.CosineAntennaElement('FrequencyRange',[100e6 le9],...
    'CosinePower',[2.5,2.5]);
sULA = phased.ULA('NumElements',10,...
    'ElementSpacing',.1,...
    'Element',sCos);
c = physconst('LightSpeed');
fc = 500e6;
pattern(sULA,fc,[-1:.01:1],[-1:.01:1],...
    'CoordinateSystem','uv',...
    'Type','powerdb',...
    'PropagationSpeed',c)
```



## More About

## Directivity (dBi)

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \Pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Convert plotResponse to pattern

For antenna, microphone, and array System objects, the pattern method replaces the plotResponse method. In addition, two new simplified methods exist just to draw 2-D azimuth and elevation pattern plots. These are the azimuthPattern and elevationPattern methods.

The following table is a guide for converting your code from using plotResponse to pattern. You should notice that some of the inputs have changed from input arguments to Name-Value pairs and vice versa. The general pattern method syntax is

```
pattern(H,FREQ,AZ,EL,'Name1','Value1',...,''NameN','ValueN')
```

| plotResponse Inputs | plotResponse Description | pattern Inputs |
| :--- | :--- | :--- |
| H argument | Antenna, microphone, or array <br> System object. | H argument (no change) |
| FREQ argument | Operating frequency. | FREQ argument (no change) |
| V argument | Propagation speed. This argument <br> is used only for arrays. | 'PropagationSpeed ' name-value <br> pair. This parameter is only used for <br> arrays. |


| plotResponse Inputs | plotResponse Description |  | pattern Inputs |  |
| :---: | :---: | :---: | :---: | :---: |
| 'Format' and 'RespCut' namevalue pairs | These options work together to let you create a plot in angle space (line or polar style) or $U V$ space. They also determine whether the plot is 2-D or 3-D. This table shows you how to create different types of plots using plotResponse. |  | 'CoordinateSystem' name-value pair used together with the AZ and EL input arguments. <br> 'CoordinateSystem' has the same options as the plotResponse method 'Format ' name-value pair, except that 'line' is now named 'rectangular'. The table shows how to create different types of plots using pattern. |  |
|  | Display space |  |  |  |
|  | Angle space (2D) |  |  |  |
|  |  | Set 'RespCut'to 'Az' or'El'. Set'Format' to'line' or'polar'.Set the displayaxis using eitherthe'AzimuthAngleS' or'ElevationAngles' name-value pairs. | Display space |  |
|  |  |  | Angle space (2D) <br> Angle space (3D) | Set <br> 'Coordinate <br> System' to rectangular' or 'polar'. <br> Specify either AZ or EL as a scalar. |
|  |  |  |  | Set <br> 'Coordinate <br> System' to 'rectangular' |
|  | Angle space (3D) | Set 'RespCut' to '3D'. Set 'Format' to ' line' or 'polar'. <br> Set the display axis using both the 'AzimuthAngle ${ }^{\prime}$ and 'Elevation Angles ' namevalue pairs. |  | or 'polar'. <br> Specify both AZ and EL as vectors. |
|  |  |  | UV space (2D) | Set <br> 'Coordinate <br> System' to 'uv'. Use AZ to specify a $U$ space vector. Use EL to specify a $V$-space scalar. |
|  |  |  | UV space (3D) | Set |
|  | UV space (2D) | Set 'RespCut' to'U'. Set 'Format' to 'UV '. Set the display range using the 'UGrid' namevalue pair. |  | System' to 'uv'. Use AZ to specify a $U$ space vector. <br> Use EL to specify a $V$-space vector. |
|  |  |  | If you set CoordinateSystem to 'uv', enter the UV grid values using AZ and EL . |  |
|  | UV space (3D) | $\begin{aligned} & \text { Set 'RespCut' } \\ & \text { to'3D'. Set } \\ & \text { 'Format' to } \end{aligned}$ |  |  |



| plotResponse Inputs | plotResponse Description | pattern Inputs |
| :--- | :--- | :--- |
| 'ElevationAngles ' name-value <br> pair | Elevation angles used to display the <br> antenna or array response. | EL argument |
| 'UGrid' name-value pair | Contains $U$ coordinates in $U V$ - <br> space. | AZ argument when <br> 'CoordinateSystem ' name-value <br> pair is set to ' uv ' |
| 'VGrid' name-value pair | Contains V-coordinates in $U V$-space. | EL argument when <br> 'CoordinateSystem ' name-value <br> pair is set to 'uv ' |

## Version History <br> Introduced in R2015a

See Also<br>patternAzimuth | patternElevation

## patternAzimuth

System object: phased.ULA
Package: phased
Plot ULA array directivity or pattern versus azimuth

## Syntax

```
patternAzimuth(sArray,FREQ)
patternAzimuth(sArray,FREQ,EL)
patternAzimuth(sArray,FREQ,EL,Name,Value)
PAT = patternAzimuth(
```

$\qquad$

``` )
```


## Description

patternAzimuth (sArray, FREQ) plots the 2-D array directivity pattern versus azimuth (in dBi) for the array sArray at zero degrees elevation angle. The argument FREQ specifies the operating frequency.

The integration used when computing array directivity has a minimum sampling grid of 0.1 degrees. If an array pattern has a beamwidth smaller than this, the directivity value will be inaccurate.
patternAzimuth(sArray, FREQ,EL), in addition, plots the 2-D array directivity pattern versus azimuth (in dBi) for the array sArray at the elevation angle specified by EL. When EL is a vector, multiple overlaid plots are created.
patternAzimuth(sArray, FREQ,EL,Name, Value) plots the array pattern with additional options specified by one or more Name, Value pair arguments.

PAT = patternAzimuth( $\qquad$ ) returns the array pattern. PAT is a matrix whose entries represent the pattern at corresponding sampling points specified by the 'Azimuth ' parameter and the EL input argument.

## Input Arguments

## sArray - Uniform linear array

System object
Uniform linear array, specified as a phased. ULA System object.
Example: sArray= phased.ULA;

## FREQ - Frequency for computing directivity and pattern

positive scalar
Frequency for computing directivity and pattern, specified as a positive scalar. Frequency units are in hertz.

- For an antenna or microphone element, FREQ must lie within the range of values specified by the FrequencyRange or the FrequencyVector property of the element. Otherwise, the element
produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased.CustomMic rophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: 1e8
Data Types: double

## EL - Elevation angles

1 -by- $N$ real-valued row vector
Elevation angles for computing sensor or array directivities and patterns, specified as a 1-by- $N$ realvalued row vector. The quantity $N$ is the number of requested elevation directions. Angle units are in degrees. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

The elevation angle is the angle between the direction vector and the xy plane. When measured toward the $z$-axis, this angle is positive.
Example: [0, 10, 20]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Type - Displayed pattern type

'directivity' (default)|'efield'|'power'|'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb' - power pattern converted to dB.

Example: 'powerdb'
Data Types: char

## PropagationSpeed - Signal propagation speed

## speed of light (default) | positive scalar

Signal propagation speed, specified as the comma-separated pair consisting of ' PropagationSpeed ' and a positive scalar in meters per second.
Example: 'PropagationSpeed', physconst('LightSpeed')
Data Types: double

## Weights - Array weights

M-by-1 complex-valued column vector
Array weights, specified as the comma-separated pair consisting of 'Weights' and an $M$-by- 1 complex-valued column vector. Array weights are applied to the elements of the array to produce array steering, tapering, or both. The dimension $M$ is the number of elements in the array.

Note Use complex weights to steer the array response toward different directions. You can create weights using the phased. SteeringVector System object or you can compute your own weights. In general, you apply Hermitian conjugation before using weights in any Phased Array System Toolbox function or System object such as phased. Radiator or phased. Collector. However, for the directivity, pattern, patternAzimuth, and patternElevation methods of any array System object use the steering vector without conjugation.

Example: 'Weights', ones (10, 1)
Data Types: double
Complex Number Support: Yes

## Azimuth - Azimuth angles

[-180:180] (default) | 1-by-P real-valued row vector
Azimuth angles, specified as the comma-separated pair consisting of 'Azimuth' and a 1-by-P realvalued row vector. Azimuth angles define where the array pattern is calculated.
Example: 'Azimuth', [-90:2:90]
Data Types: double

## Parent - Handle to axis

scalar
Handle to the axes along which the array geometry is displayed specified as a scalar.

## Output Arguments

## PAT - Array directivity or pattern

L-by- $N$ real-valued matrix
Array directivity or pattern, returned as an $L$-by- $N$ real-valued matrix. The dimension $L$ is the number of azimuth values determined by the 'Azimuth' name-value pair argument. The dimension $N$ is the number of elevation angles, as determined by the EL input argument.

## Examples

## Plot Azimuth Pattern of ULA

Create a 7-element ULA of short-dipole antenna elements spaced 10 cm apart. Plot an azimuth cut of directivity at 0 and 10 degrees elevation. Assume the operating frequency is 500 MHz .

```
fc = 500e6;
sCDant = phased.ShortDipoleAntennaElement('FrequencyRange',[100,900]*1e6);
```

sULA = phased.ULA('NumElements',7,'ElementSpacing',0.1,'Element',sCDant); patternAzimuth(sULA,fc,[0 30])


Directivity (dBi), Broadside at $0.00^{\circ}$
You can plot a smaller range of azimuth angles by setting the Azimuth property. patternAzimuth(sULA,fc,[0 30],'Azimuth',[-90:90])


Directivity (dBi), Broadside at $0.00^{\circ}$

## More About

## Directivity (dBi)

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Version History Introduced in R2015a

## See Also

pattern| patternElevation

## patternElevation

System object: phased.ULA
Package: phased
Plot ULA array directivity or pattern versus elevation

## Syntax

```
patternElevation(sArray,FREQ)
patternElevation(sArray,FREQ,AZ)
patternElevation(sArray,FREQ,AZ,Name,Value)
PAT = patternElevation(
```

$\qquad$

``` )
```


## Description

patternElevation(sArray, FREQ) plots the 2-D array directivity pattern versus elevation (in dBi ) for the array sArray at zero degrees azimuth angle. When AZ is a vector, multiple overlaid plots are created. The argument FREQ specifies the operating frequency.

The integration used when computing array directivity has a minimum sampling grid of 0.1 degrees. If an array pattern has a beamwidth smaller than this, the directivity value will be inaccurate.
patternElevation(sArray, FREQ, AZ), in addition, plots the 2-D element directivity pattern versus elevation (in dBi ) at the azimuth angle specified by $A Z$. When $A Z$ is a vector, multiple overlaid plots are created.
patternElevation(sArray,FREQ,AZ,Name, Value) plots the array pattern with additional options specified by one or more Name, Value pair arguments.

PAT = patternElevation ( _ ) returns the array pattern. PAT is a matrix whose entries represent the pattern at corresponding sampling points specified by the 'Elevation' parameter and the AZ input argument.

## Input Arguments

## sArray - Uniform linear array

System object
Uniform linear array, specified as a phased. ULA System object.
Example: sArray= phased.ULA;

## FREQ - Frequency for computing directivity and pattern

positive scalar
Frequency for computing directivity and pattern, specified as a positive scalar. Frequency units are in hertz.

- For an antenna or microphone element, FREQ must lie within the range of values specified by the FrequencyRange or the FrequencyVector property of the element. Otherwise, the element
produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased.CustomMic rophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: 1e8
Data Types: double

## AZ - Azimuth angles for computing directivity and pattern

1 -by- $N$ real-valued row vector
Azimuth angles for computing sensor or array directivities and patterns, specified as a 1 -by- $N$ realvalued row vector where $N$ is the number of desired azimuth directions. Angle units are in degrees. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the $x y$ plane. This angle is positive when measured from the $x$-axis toward the $y$-axis.
Example: [0,10, 20]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Type - Displayed pattern type

'directivity' (default)|'efield'|'power'|'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb' - power pattern converted to dB.

Example: 'powerdb'
Data Types: char

## PropagationSpeed - Signal propagation speed

speed of light (default) | positive scalar
Signal propagation speed, specified as the comma-separated pair consisting of ' PropagationSpeed ' and a positive scalar in meters per second.
Example: 'PropagationSpeed', physconst('LightSpeed')
Data Types: double

## Weights - Array weights

M-by-1 complex-valued column vector
Array weights, specified as the comma-separated pair consisting of 'Weights' and an $M$-by- 1 complex-valued column vector. Array weights are applied to the elements of the array to produce array steering, tapering, or both. The dimension $M$ is the number of elements in the array.

Note Use complex weights to steer the array response toward different directions. You can create weights using the phased. SteeringVector System object or you can compute your own weights. In general, you apply Hermitian conjugation before using weights in any Phased Array System Toolbox function or System object such as phased. Radiator or phased. Collector. However, for the directivity, pattern, patternAzimuth, and patternElevation methods of any array System object use the steering vector without conjugation.

Example: 'Weights' , ones ( 10,1 )
Data Types: double
Complex Number Support: Yes

## Elevation - Elevation angles

[-90:90] (default) | 1-by-P real-valued row vector
Elevation angles, specified as the comma-separated pair consisting of 'Elevation' and a 1-by-P real-valued row vector. Elevation angles define where the array pattern is calculated.
Example: 'Elevation', [-90:2:90]
Data Types: double

## Parent - Handle to axis

scalar
Handle to the axes along which the array geometry is displayed specified as a scalar.

## Output Arguments

## PAT - Array directivity or pattern

L-by- $N$ real-valued matrix
Array directivity or pattern, returned as an $L$-by- $N$ real-valued matrix. The dimension $L$ is the number of elevation angles determined by the 'Elevation' name-value pair argument. The dimension $N$ is the number of azimuth angles determined by the $A Z$ argument.

## Examples

## Plot Elevation Pattern of ULA

Create a 6 -element ULA of short-dipole antenna elements with element spacing of 10 cm . Plot an elevation cut of directivity at 0 and 90 degrees azimuth. Assume the operating frequency is 500 MHz .
$\mathrm{fc}=500 \mathrm{e} 6$;
c = physconst('LightSpeed');
sSD = phased.ShortDipoleAntennaElement('FrequencyRange',[100,900]*1e6); sULA = phased.ULA('NumElements',6,'ElementSpacing',0.1,'Element',sSD); patternElevation(sULA,fc,[0 90],'PropagationSpeed', c)


Directivity (dBi), Broadside at $0.00^{\circ}$
You can plot a smaller range of elevation angles by setting the Elevation property. patternElevation(sULA,fc,[0 45],'Elevation',[0:90],'PropagationSpeed', c)


Directivity (dBi), Broadside at $0.00^{\circ}$

## More About

## Directivity (dBi)

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \Pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Version History Introduced in R2015a

## See Also

pattern| patternAzimuth

# plotGratingLobeDiagram 

System object: phased.ULA
Package: phased
Plot grating lobe diagram of array

## Syntax

```
plotGratingLobeDiagram(H,FREQ)
plotGratingLobeDiagram(H,FREQ,ANGLE)
plotGratingLobeDiagram(H,FREQ,ANGLE,C)
plotGratingLobeDiagram(H,FREQ,ANGLE,C,F0)
hPlot = plotGratingLobeDiagram(
```

$\qquad$

## Description

plotGratingLobeDiagram ( $\mathrm{H}, \mathrm{FREQ}$ ) plots the grating lobe diagram of an array in the $u$ - $v$ coordinate system. The System object H specifies the array. The argument FREQ specifies the signal frequency and phase-shifter frequency. The array, by default, is steered to $0^{\circ}$ azimuth and $0^{\circ}$ elevation.

A grating lobe diagram displays the positions of the peaks of the narrowband array pattern. The array pattern depends only upon the geometry of the array and not upon the types of elements which make up the array. Visible and nonvisible grating lobes are displayed as open circles. Only grating lobe peaks near the location of the mainlobe are shown. The mainlobe itself is displayed as a filled circle.
plotGratingLobeDiagram ( $\mathrm{H}, \mathrm{FREQ}, \mathrm{ANGLE}$ ), in addition, specifies the array steering angle, ANGLE.
plotGratingLobeDiagram( $\mathrm{H}, \mathrm{FREQ}, \mathrm{ANGLE}, \mathrm{C}$ ), in addition, specifies the propagation speed by C.
plotGratingLobeDiagram(H,FREQ, ANGLE , C, F0) , in addition, specifies an array phase-shifter frequency, F0, that differs from the signal frequency, FREQ. This argument is useful when the signal no longer satisfies the narrowband assumption and, allows you to estimate the size of beam squint.
hPlot = plotGratingLobeDiagram( $\qquad$ ) returns the handle to the plot for any of the input syntax forms.

## Input Arguments

## H

Antenna or microphone array, specified as a System object.

## FREQ

Signal frequency, specified as a scalar. Frequency units are hertz. Values must lie within a range specified by the frequency property of the array elements contained in H .Element. The frequency property is named FrequencyRange or FrequencyVector, depending on the element type.


#### Abstract

ANGLE Array steering angle, specified as either a 2 -by- 1 vector or a scalar. If ANGLE is a vector, it takes the form [azimuth; elevation]. The azimuth angle must lie in the range $\left[-180^{\circ}, 180^{\circ}\right]$. The elevation angle must lie in the range $\left[-90^{\circ}, 90^{\circ}\right]$. All angle values are specified in degrees. If the argument ANGLE is a scalar, it specifies only the azimuth angle where the corresponding elevation angle is $0^{\circ}$.


Default: [0;0]

## C

Signal propagation speed, specified as a scalar. Units are meters per second.
Default: Speed of light in vacuum

## F0

Phase-shifter frequency of the array, specified as a scalar. Frequency units are hertz When this argument is omitted, the phase-shifter frequency is assumed to be the signal frequency, FREQ.

Default: FREQ

## Examples

## Create Grating Lobe Diagram for ULA

Plot the grating lobe diagram for a 4 -element uniform linear array having element spacing less than one-half wavelength. Grating lobes are plotted in $u-v$ coordinates.

Assume the operating frequency of the array is 3 GHz and the spacing between elements is 0.45 of the wavelength. All elements are isotropic antenna elements. Steer the array in the direction 45 degrees in azimuth and 0 degrees in elevation.

```
c = physconst('LightSpeed');
f = 3e9;
lambda = c/f;
sIso = phased.IsotropicAntennaElement;
sULA = phased.ULA('Element',sIso,'NumElements',4,\ldots
    'ElementSpacing',0.45*lambda);
plotGratingLobeDiagram(sULA,f,[45;0],c);
```


## Grating Lobe Diagram in U Space



The main lobe of the array is indicated by a filled black circle. The grating lobes in the visible and nonvisible regions are indicated by empty black circles. The visible region is defined by the direction cosine limits between $[-1,1]$ and is marked by the two vertical black lines. Because the array spacing is less than one-half wavelength, there are no grating lobes in the visible region of space. There are an infinite number of grating lobes in the nonvisible regions, but only those in the range $[-3,3]$ are shown.

The grating-lobe free region, shown in green, is the range of directions of the main lobe for which there are no grating lobes in the visible region. In this case, it coincides with the visible region.

The white area of the diagram indicates a region where no grating lobes are possible.

## Create Grating Lobe Diagram for Undersampled ULA

Plot the grating lobe diagram for a 4-element uniform linear array having element spacing greater than one-half wavelength. Grating lobes are plotted in u-v coordinates.

Assume the operating frequency of the array is 3 GHz and the spacing between elements is 0.65 of a wavelength. All elements are isotropic antenna elements. Steer the array in the direction 45 degrees in azimuth and 0 degrees in elevation.

```
c = physconst('LightSpeed');
f = 3e9;
lambda = c/f;
```

```
sIso = phased.IsotropicAntennaElement;
```

sULA $=$ phased.ULA('Element',sIso,'NumElements',4,'ElementSpacing', $0.65 *$ lambda);
plotGratingLobeDiagram(sULA, f, [45;0], c) ;

Grating Lobe Diagram in U Space


The main lobe of the array is indicated by a filled black circle. The grating lobes in the visible and nonvisible regions are indicated by empty black circles. The visible region, marked by the two black vertical lines, corresponds to arrival angles between -90 and 90 degrees. The visible region is defined by the direction cosine limits $-1 \leq u \leq 1$. Because the array spacing is greater than one-half wavelength, there is now a grating lobe in the visible region of space. There are an infinite number of grating lobes in the nonvisible regions, but only those for which $-3 \leq u \leq 3$ are shown.

The grating-lobe free region, shown in green, is the range of directions of the main lobe for which there are no grating lobes in the visible region. In this case, it lies inside the visible region.

## Create Grating Lobe Diagram for ULA With Different Phase-Shifter Frequency

Plot the grating lobe diagram for a 4 -element uniform linear array having element spacing greater than one-half wavelength. Apply a phase-shifter frequency that differs from the signal frequency. Grating lobes are plotted in $u$-v coordinates.

Assume the signal frequency is 3 GHz and the spacing between elements is $0.65 \lambda$. All elements are isotropic antenna elements. The phase-shifter frequency is set to 3.5 GHz . Steer the array in the direction $45^{\circ}$ azimuth, $0^{\circ}$ elevation.

```
c = physconst('LightSpeed');
f = 3e9;
f0 = 3.5e9;
lambda = c/f;
sIso = phased.IsotropicAntennaElement;
sULA = phased.ULA('Element',sIso,'NumElements',4,...
    'ElementSpacing',0.65*lambda );
plotGratingLobeDiagram(sULA,f,[45;0],c,f0);
```

Grating Lobe Diagram in U Space


As a result of adding the shifted frequency, the mainlobe shifts right towards larger $u$ values. The beam no longer points toward the actual source arrival angle.

The mainlobe of the array is indicated by a filled black circle. The grating lobes in the visible and nonvisible regions are indicated by empty black circles. The visible region, marked by the two black vertical lines, corresponds to arrival angles between $-90^{\circ}$ and $90^{\circ}$. The visible region is defined by the direction cosine limits $-1 \leq u \leq 1$. Because the array spacing is greater than one-half wavelength, there is now a grating lobe in the visible region of space. There are an infinite number of grating lobes in the nonvisible regions, but only those for which $-3 \leq u \leq 3$ are shown.

The grating-lobe free region, shown in green, is the range of directions of the main lobe for which there are no grating lobes in the visible region. In this case, it lies inside the visible region.

## Concepts

## Grating Lobes

Spatial undersampling of a wavefield by an array gives rise to visible grating lobes. If you think of the wavenumber, $k$, as analogous to angular frequency, then you must sample the signal at spatial intervals smaller than $\Pi / k_{\max }$ (or $\lambda_{\text {min }} / 2$ ) in order to remove aliasing. The appearance of visible grating lobes is also known as spatial aliasing. The variable $k_{\max }$ is the largest wavenumber value present in the signal.

The directions of maximum spatial response of a ULA are determined by the peaks of the array's array pattern (alternatively called the beam pattern or array factor). Peaks other than the mainlobe peak are called grating lobes. For a ULA, the array pattern depends only on the wavenumber component of the wavefield along the array axis (the $y$-direction for the phased. ULA System object). The wavenumber component is related to the look-direction of an arriving wavefield by $k_{y}=-2 \Pi \sin \varphi /$ $\lambda$. The angle $\varphi$ is the broadside angle-the angle that the look-direction makes with a plane perpendicular to the array. The look-direction points away from the array to the wavefield source.

The array pattern possesses an infinite number of periodically-spaced peaks that are equal in strength to the mainlobe peak. If you steer the array to the $\varphi_{0}$ direction, the array pattern for a ULA has its mainlobe peak at the wavenumber value of $k_{y 0}=-2 \Pi \sin \varphi_{0} / \lambda$. The array pattern has strong grating lobe peaks at $k_{y m}=k_{y 0}+2 \pi m / d$, for any integer value $m$. Expressed in terms of direction cosines, the grating lobes occur at $u_{m}=u_{0}+m \lambda / d$, where $u_{0}=\sin \varphi_{0}$. The direction cosine, $u_{0}$, is the cosine of the angle that the look-direction makes with the $y$-axis and is equal to $\sin \varphi_{0}$ when expressed in terms of the look-direction.

In order to correspond to a physical look-direction, $u_{m}$ must satisfy, $-1 \leq u_{m} \leq 1$. You can compute a physical look-direction angle $\varphi_{m}$ from $\sin \varphi_{m}=u_{m}$ as long as $-1 \leq u_{m} \leq 1$. The spacing of grating lobes depends upon $\lambda / d$. When $\lambda / d$ is small enough, multiple grating lobe peaks can correspond to physical look-directions.

The presence or absence of visible grating lobes for the ULA is summarized in this table.

| Element Spacing | Grating Lobes |
| :--- | :--- |
| $\lambda / d \geq 2$ | No visible grating lobes for any mainlobe <br> direction. |
| $1 \leq \lambda / d<2$ | Visible grating lobes can exist for some range of <br> mainlobe directions. |
| $\lambda / d<1$ | Visible grating lobes exist for every mainlobe <br> direction. |

## References

[1] Van Trees, H.L. Optimum Array Processing. New York: Wiley-Interscience, 2002.

## See Also

uv2azel|azel2uv

## step

System object: phased. ULA
Package: phased
Output responses of array elements

## Syntax

RESP = step(H,FREQ,ANG)

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.

RESP = step (H, FREQ, ANG) returns the array element responses, RESP, at the operating frequencies specified in FREQ and in directions specified in ANG.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## H

Array object

## FREQ

Operating frequencies of array in hertz. FREQ is a row vector of length $L$. Typical values are within the range specified by a property of H . Element. That property is named FrequencyRange or FrequencyVector, depending on the type of element in the array. The element has zero response at frequencies outside that range.

## ANG

Directions in degrees. ANG is either a 2 -by- $M$ matrix or a row vector of length $M$.
If ANG is a 2 -by-M matrix, each column of the matrix specifies the direction in the form [azimuth; elevation]. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive.

If ANG is a row vector of length $M$, each element specifies the azimuth angle of the direction. In this case, the corresponding elevation angle is assumed to be $0^{\circ}$.

## Output Arguments

## RESP

Voltage responses of the phased array. The output depends on whether the array supports polarization or not.

- If the array is not capable of supporting polarization, the voltage response, RESP, has the dimensions $N$-by- $M$-by- $L$. $N$ is the number of elements in the array. The dimension $M$ is the number of angles specified in ANG. $L$ is the number of frequencies specified in FREQ. For any element, the columns of RESP contain the responses of the array elements for the corresponding direction specified in ANG. Each of the $L$ pages of RESP contains the responses of the array elements for the corresponding frequency specified in FREQ.
- If the array is capable of supporting polarization, the voltage response, RESP, is a MATLAB struct containing two fields, RESP.H and RESP.V. The field, RESP.H, represents the array's horizontal polarization response, while RESP.V represents the array's vertical polarization response. Each field has the dimensions $N$-by- $M$-by-L. $N$ is the number of elements in the array, and $M$ is the number of angles specified in ANG. $L$ is the number of frequencies specified in FREQ. Each column of RESP contains the responses of the array elements for the corresponding direction specified in ANG. Each of the $L$ pages of RESP contains the responses of the array elements for the corresponding frequency specified in FREQ.


## Examples

## Response of Antenna ULA

Create a 4 -element ULA of isotropic antenna elements and find the response of each element at boresight. Plot the array response at 1 GHz for azimuth angles between -180 and 180 degrees.

```
ha = phased.ULA('NumElements',4);
fc = 1e9;
ang = [0;0];
resp = step(ha,fc,ang);
c = physconst('LightSpeed');
pattern(ha,fc,[-180:180],0,...
    'PropagationSpeed',c,...
    'CoordinateSystem','rectangular')
```



## Response of Microphone ULA Array

Find the response of a ULA array of 10 omnidirectional microphones spaced 1.5 meters apart. Set the frequency response of the microphone to the range 20 Hz to 20 kHz and choose the signal frequency to be 100 Hz . Using the step method, determine the response of each element at boresight: 0 degrees azimuth and 0 degrees elevation.

```
mic = phased.OmnidirectionalMicrophoneElement( ...
    'FrequencyRange',[20 20e3]);
Nelem = 10;
array = phased.ULA('NumElements',Nelem, ...
    'ElementSpacing',1.5,'Element',mic);
fc = 100;
ang = [0;0];
resp = array(fc,ang)
resp = 10×1
```

Plot the array directivity. Assume the speed of sound in air to be $340 \mathrm{~m} / \mathrm{s}$.
c = 340;
pattern(array,fc,[-180:180],0,'PropagationSpeed',c,'CoordinateSystem','polar')


## See Also

uv2azel| phitheta2azel

## viewArray

System object: phased.ULA
Package: phased
View array geometry

## Syntax

```
viewArray(H)
viewArray(H,Name,Value)
hPlot = viewArray(
```

$\qquad$

``` )
```


## Description

viewArray (H) plots the geometry of the array specified in H .
viewArray ( $\mathrm{H}, \mathrm{Name}$, Value) plots the geometry of the array, with additional options specified by one or more Name, Value pair arguments.
hPlot = viewArray( $\qquad$ ) returns the handle of the array elements in the figure window. All input arguments described for the previous syntaxes also apply here.

## Input Arguments

## H

Array object.

## Name-Value Pair Arguments

Specify optional pairs of arguments as Namel=Value1, . . . ,NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Parent

Handle to the axes along which the array geometry is displayed.

## ShowNormals

Set this value to true to show the normal directions of all elements of the array. Set this value to false to plot the elements without showing normal directions.

Default: false

## ShowLocalCoordinates

Logical flag specifying whether to show the local coordinate axes.

Default: true

## ShowAnnotation

Logical flag specifying whether to show the annotations in the UI panel of the figure. Annotation shows aperture size and element spacing based on array axis of array.

Default: true

## Orientation

Orientation of the array, specified as a 3-by-1 column vector containing the rotation angles with respect to the $\mathrm{x}-, \mathrm{y}$-, and z -axes of the local coordinate system, respectively. The default value is [0;0;0].

Default: [0;0;0]

## ShowTaper

Set this value to true to specify whether to change the element color brightness in proportion to the element taper magnitude. When this value is set to false, all elements are drawn with the same color.

Default: false

## ShowIndex

Vector specifying the element indices to show in the figure. Each number in the vector must be an integer between 1 and the number of elements. You can also specify the value 'All' to show the indices of all elements of the array or 'None' to suppress indices.

Default: 'None'

## Title

Character vector specifying the title of the plot.
Default: 'Array Geometry'

## Output Arguments

## hPlot

Handle of array elements in figure window.

## Examples

## Geometry and Indices of ULA Elements

Draw a 6-element ULA and use the 'ShowIndex ' parameter to show the indices of the first and third elements.
array = phased.ULA(6);
viewArray(array,'ShowIndex', [1 3],'ShowNormals',true, ...

```
'ShowLocalCoordinates',true,'Orientation',[60;100;45], ...
```

'ShowAnnotation',true)

## Array Geometry



Aperture Size:
Y axis $=3 \mathrm{~m}$
Element Spacing:
$\Delta y=500 \mathrm{~mm}$
Array Axis: Y axis

## See Also

phased.ArrayResponse
Topics
Phased Array Gallery

## phased.UnderwaterRadiatedNoise

Package: phased
Radiate acoustic noise from underwater or surface sound source

## Description

The phased.UnderwaterRadiatedNoise System object creates a source of underwater radiated acoustic noise. The noise source can either be on the sea surface or underwater. The radiated noise consists of two components: broadband noise and tonal noise. Broadband noise fills the entire operating system bandwidth while tonal noise occurs at discrete frequencies within the bandwidth. In general, the intensity of the radiated noise depends on the noise spectrum and the source radiation pattern. The object lets you specify

- The spectral shape and levels of the broadband noise.
- The frequencies and levels of the tones.
- The noise source radiation pattern.

To propagate noise from a source to a receiver, use this object with the phased.IsoSpeedUnderwaterPaths and the phased.MultipathChannel objects.

To generate radiated underwater noise:
1 Create the phased.UnderwaterRadiatedNoise object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

noiseradiator = phased.UnderwaterRadiatedNoise
noiseradiator $=$ phased.UnderwaterRadiatedNoise(Name,Value)

## Description

noiseradiator = phased.UnderwaterRadiatedNoise creates an underwater radiated noise source with default property values.
noiseradiator $=$ phased.UnderwaterRadiatedNoise(Name,Value) creates an underwater radiated noise source with each property Name set to a specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN). Enclose each property name in single quotes.
Example: noiseradiator = phased.UnderwaterRadiatedNoise('TonalLevels', [4700 4900 5150],'SampleRate',500,'OperatingFrequency',5000) creates a noise source with tones at 4.7, 4.9, and 5.15 kHz . The sample rate is set to 0.5 kHz and the operating frequency is 5 kHz . The broadband noise levels are set to default values.

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

NumSamples - Number of output noise samples
100 (default) | positive integer
Number of output noise samples, specified as a positive integer.
Example: 500
Data Types: double

## SampleRate - Sample rate

1.0e3 (default) | positive scalar

Sample rate, specified as a positive scalar. The sample rate together with the operating frequency determines the operating frequency band. See "Input and Output Frequency Bands" on page 1-1886 for the definition of the operating frequency band. Units are in Hz .
Example: 2.0e3
Data Types: double

## OperatingFrequency - Signal operating frequency

20.0 e 3 (default) | positive scalar

Signal operating frequency, specified as a positive scalar. The operating frequency determines the center of the operating frequency band. See "Input and Output Frequency Bands" on page 1-1886 for the definition of the operating frequency band. Units are in Hz .

Example: 15.0e3
Data Types: double

## TonalFrequencies - Radiated tonal noise frequencies

[19700 20100 20300] (default) |real-valued vector of nonnegative values
Radiated tonal frequencies, specified as a vector of nonnegative values. Tonal frequencies must lie in the operating frequency band. Tonal frequencies outside this band are ignored. The length of the TonalFrequencies vector must match the length of the TonalLevels vector. Units are in Hz. See "Input and Output Frequency Bands" on page 1-1886 for the definition of the operating frequency band.

Example: [14900 15010 15200]
Data Types: double

## TonalLevels - Radiated tonal noise levels

[150 150 150] (default) | real-valued vector
Radiated tonal noise levels, specified as a vector of positive values. Units are in $\mathrm{dB} / / 1 \mu \mathrm{~Pa}$. The length of the TonalLevels vector must match the length of the TonalFrequencies vector.

Example: [50 20 170]
Data Types: double

## BroadbandLevel - Broadband noise spectrum level

130 (default) | vector of real values
Broadband noise spectrum level, specified as a vector of real-values. This vector specifies the noise spectrum at uniformly spaced frequencies in the operating system band. Units are in $\mathrm{dB} / \mathrm{Hz} / / 1 \mu \mathrm{~Pa}$.
Example: [140 145145 130]
Data Types: double

## AzimuthAngles - Elevation angles of source radiation pattern entries <br> -180: 180 (default) | vector of real values

Azimuth angles of source radiation pattern entries, specified as a length $-P$ vector. This property specifies the azimuth angles of the columns of the source radiation pattern, DirectionalPattern property. $P$ must be greater than 2 . Units are in degrees.
Example: [140 145145 130]
Data Types: double

## ElevationAngles - Elevation angles of directional radiation pattern

-90:90 (default) | length- $Q$ vector of real values
Elevation angles of the source radiation pattern entries, specified as a length- $Q$ vector. This property specifies the elevation angles of the rows of the source radiation pattern, DirectionalPattern . $Q$ must be greater than 2 . Units are in degrees.

## Example: [-45-30 045 30]

Data Types: double

## DirectionalPattern - Source radiation pattern

zeros $(181,361)$ (default) | real-valued $Q$-by-P matrix | real-valued $Q$-by- $P$-by-K array | 1-by-P-by-K array | real-valued $K$-by- $P$ matrix

Source radiation pattern, specified as a real-valued matrix or array. Units are in dB. The allowable pattern dimensions are:

Radiation Pattern Dimensions

| Dimensions | Application |
| :--- | :--- |
| $Q$-by- $P$ matrix | Specifies a directional pattern as a function of $Q$ <br> elevation angles and $P$ azimuth angles. The same <br> pattern is used for all frequencies. |
| $Q$-by- $P$-by- $K$ array | Specifies a directional pattern as a function of $Q$ <br> elevation angles, $P$ azimuth angles, and $K$ <br> frequencies. If $K=1$, the directional pattern is <br> equivalent to a $Q$-by- $P$ matrix. |
| 1 -by- $P$-by- $K$ array | Specifies a directional pattern as a function of $P$ <br> azimuth angles and $K$ frequencies. These <br> dimensions apply when there is only one <br> elevation angle. |
| $K$-by- $P$ matrix |  |

- $Q$ is the length of the vector specified by the ElevationAngles property.
- $\quad P$ is the length of the vector specified by the AzimuthAngles property.
- $K$ is the number of frequencies specified by the FrequencyVector property.


## Matrix and Array Specifications

| Application | Radiation Pattern Dimensions |
| :--- | :--- |
| One source and $M$ radiation directions specified <br> in the ang argument of the object function. | Specify one radiation pattern matrix or array for <br> all radiating angles. |
| $M$ sources with the same pattern and $M$ radiation <br> directions specified in the ang argument of the <br> object function. | Specify one radiation pattern matrix or array for <br> all radiating angles. |
| $M$ sources with individual radiation patterns and <br> $M$ radiation directions specified in the ang <br> argument of the object function. | $M$ radiation patterns in a cell array. All patterns <br> must have the same sizes and types. The number <br> of patterns must match the number of radiating <br> angles. |

Example: [1,3;5,-10]
Data Types: double

## FrequencyVector - Radiation pattern frequencies

[0 100e6] (default) | positive, real-valued 1-by-K vector
Radiation pattern frequencies, specified as a positive, real-valued 1-by-K vector. The vector defines the frequencies at which the DirectionalPattern property values are specified. The elements of the vector must be in strictly increasing order and frequencies must lie in the operating frequency band. See "Input and Output Frequency Bands" on page 1-1886 for the definition of the operating frequency band. Units are in Hz .

## Example: 1e6

Data Types: double

## SeedSource - Random number generator seed source <br> 'Auto' (default)|'Property'

Random number generator seed source, specified as 'Auto' or 'Property'. The random numbers are used to generate the noise. When you set this property to 'Auto', random numbers are generated using the default MATLAB random number generator. When you set this property to 'Property' , the object uses a private random number generator with a seed specified by the Seed property.

To use this object with Parallel Computing Toolbox software, set this property to 'Auto'.

## Data Types: char

## Seed - Random number generator seed

0 (default) | nonnegative integer less than $2^{32}$.
Random number generator seed, specified as a nonnegative integer less than $2^{32}$.
Example: 10223

## Dependencies

To enable this property, set the SeedSource property to 'Property '.
Data Types: double

## Usage

## Syntax

y = radiatednoise(ang)

## Description

$\mathrm{y}=$ radiatednoise(ang) returns the noise, y , radiated in the direction, ang.

## Input Arguments

## ang - Noise radiation directions

real-valued 2-by-M matrix
Noise radiation directions, specified as a real-valued 2-by-M matrix. Each column of ang specifies the direction of radiation of the corresponding noise signal in the form
[AzimuthAngle; ElevationAngle]. When ang represents multiple angles, the DirectionalPattern property can contain one pattern or $M$ patterns. In that case, each column of ang corresponds to one of the patterns. If there is only one pattern, then the multiple noise signals are generated using the same source pattern. Units are in degrees.

Example: [0 20; 35 -10]
Data Types: double

## Output Arguments

## y - Radiated noise

complex-valued $M$-by- $N$ matrix
Radiated noise, specified as a complex-valued $M$-by- $N$ matrix. $M$ is the number of angles specified in the ang argument. $N$ is the number of samples specified by the NumSamples property. Radiated noise
lies in the baseband range $[-f s / 2 f s / 2]$. $f_{s}$ represents the sample rate set by the SampleRate property. Noise units are in Pa.
Data Types: double

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:
release(obj)

## Common to All System Objects

step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object
The reset object function resets the random number generator state when the SeedSource property is set to 'Property'.

## Examples

## Radiate Underwater Noise from Surface Ship

Generate radiated noise from a surface ship. The sonar operating frequency is 5.0 kHz and the sampling rate is 1.0 kHz . By definition, broadband noise band lies in the band 4.5 kHz to 5.5 kHz . In addition, there are tonal noises at 4.6, 5.2, and 5.4 kHz .

```
shippos = [0;0;0];
rcvpos = [100;0;-50];
```

Compute the noise transmission angle from the ship to the receiver.

```
[~,ang] = rangeangle(rcvpos,shippos)
ang = 2\times1
```


## 0

$-26.5651$

Construct a phased.UnderwaterRadiatedNoise System object ${ }^{\mathrm{TM}}$ having a radiation pattern that depends only on elevation angle. Compute the noise radiated in the direction of the receiver. Create 10000 samples of the noise radiated towards the target.

```
azang = [-180:180];
elang = [-80:80];
pattern = mag2db(repmat (cosd(elang)',1,numel(azang)));
fs = 1000;
noiseradiator = phased.UnderwaterRadiatedNoise('NumSamples',10000, ...
    'SampleRate',fs,'TonalFrequencies',[4600 5200 5400],'TonalLevels',[200,200,200], ...
    'BroadbandLevels',[180 180 190 190 190 188 185],'AzimuthAngles',azang, ...
```

```
'ElevationAngles',elang,'DirectionalPattern',pattern, ...
'OperatingFrequency',5e3,'SeedSource','Property','Seed',2781);
```

Generate 10000 samples of noise.
y = noiseradiator(ang);
Plot the noise power spectral density (psd). Convert the psd to intensity referenced to 1 uPa .

```
[psd,fr] = pwelch(y,[],[],[],noiseradiator.SampleRate,'psd','centered');
plot(fr,10*log10(psd*1e12));
title('Power Spectral Density')
xlabel('frequency (Hz)')
ylabel('PSD //dB/Hz/luPa')
grid
```



The three tones appear over the broadband spectrum.

## Radiate Underwater Noise with Frequency-Dependent Pattern

Generate radiated noise from an underwater vehicle. Assume that the noise radiation pattern depends on frequency. The sonar operating frequency is 5.0 kHz and the sampling rate is 1.0 kHz . By definition, the broadband noise band is from 4.5 kHz to 5.5 kHz . In addition, there are tonal noises at $4.6,5.2$, and 5.3 kHz . Define the radiation pattern at three frequencies within this band. All three
patterns are multiples of the basic pattern. The frequencies of the radiation patterns are $4.6 \mathrm{kHz}, 5.0$ kHz , and 5.3 kHz .

First, specify the source and receiver positions.

```
srcpos = [0;50;-20];
rcvpos = [100;0;-50];
```

Compute the noise transmission angle from vehicle to receiver.

```
[~,ang] = rangeangle(rcvpos,srcpos)
ang = 2×1
    -26.5651
    -15.0203
```

Construct a phased.UnderwaterRadiatedNoise System object ${ }^{T M}$ with a radiation pattern that depends only on the azimuth angle and frequency. Compute the noise radiated in the direction of the receiver. Create 10000 samples of noise radiated from the vehicle.

```
azang = [-180:180];
elang = [-90:90];
fc = 5000.0;
```

Put the radiation pattern in a three-dimensional array.

```
basepattern = repmat(10*cosd(azang).^2,numel(elang),1);
pattern(:,:,1) = 0.5*basepattern;
pattern(:,:,2) = basepattern;
pattern(:,:,3) = 0.6*basepattern;
patterndb = mag2db(pattern);
noiseradiator = phased.UnderwaterRadiatedNoise('NumSamples',10000, ...
    'SampleRate',1e3,'TonalFrequencies',[4600,5200 5300], ...
    'TonalLevels',[200,210,200],'BroadbandLevels',[180 180 190 190 190 180 170], ...
    'AzimuthAngles',azang,'ElevationAngles',elang, ...
    'FrequencyVector',[4600,5000,5300],'DirectionalPattern',pattern, ...
    'OperatingFrequency',5e3,'SeedSource','Property','Seed',2081);
```

Generate 10000 samples of noise.

```
y = noiseradiator(ang);
```

Plot the noise power spectral density (psd). Convert the psd to intensity referenced to 1 uPa .

```
[psd,fr] = pwelch(y,[],[],[],noiseradiator.SampleRate,'psd','centered');
plot(fr,10*log10(psd*1e12));
title('Power Spectral Density')
xlabel('frequency (Hz)')
ylabel('PSD //dB/Hz/luPa')
grid
```



The three tones appear over the broadband spectrum.

## Radiate Underwater Noise from Two Sources

Generate radiated noise from a two underwater vehicles. Assume that the noise radiation pattern is different for each. The sonar operating frequency is 5.0 kHz and the sampling rate is 1.0 kHz . By definition, the broadband noise band is from 4.5 kHz to 5.5 kHz . In addition, there are tonal noises at $4.6,5.2$, and 5.3 kHz . The frequencies of the radiation patterns are $4.6 \mathrm{kHz}, 5.0 \mathrm{kHz}$, and 5.3 kHz .

First, specify the source and receiver positions.

```
srcpos1 = [0;50;-20];
srcpos2 = [200;50;-80];
rcvpos = [100;0;-50];
```

Compute the noise transmission angle from vehicle to receiver.
$[\sim$, ang1] $=$ rangeangle(rcvpos,srcpos1);
$[\sim$, ang2] $=$ rangeangle(rcvpos,srcpos2);
Construct a phased.UnderwaterRadiatedNoise System object ${ }^{\text {TM }}$ with a radiation pattern that depends only on the azimuth angle and frequency. Compute the noise radiated in the direction of the receiver. Create 10000 samples of noise radiated from the vehicle.

```
azang = [-180:180];
elang = [-90:90];
fc = 5000.0;
```

Put the radiation pattern in a three-dimensional array.

```
pattern1 = repmat(10*cosd(azang).^2,numel(elang),1);
pattern2 = ones(181,361);
pattern1db = mag2db(pattern1);
pattern2db = mag2db(pattern2);
noiseradiator = phased.UnderwaterRadiatedNoise('NumSamples',10000, ...
    'SampleRate',1e3,'TonalFrequencies',[4600,5200 5300], ...
    'TonalLevels',[200,210,200],'BroadbandLevels',[180 180 190 190 190 180 170], ...
    'AzimuthAngles',azang,'ElevationAngles',elang, ...
    'FrequencyVector',[4600,5000,5300],'DirectionalPattern',{pattern1,pattern2}, ...
    'OperatingFrequency',5e3,'SeedSource','Property','Seed', 2081);
```

Generate 10000 samples of noise.

```
y = noiseradiator([ang1,ang2]);
```

Plot the noise power spectral density (psd). Convert the psd to intensity referenced to 1 uPa .

```
[psd,fr] = pwelch(y,[],[],[],noiseradiator.SampleRate,'psd','centered');
plot(fr,10*log10(psd*1e12));
title('Power Spectral Density')
xlabel('frequency (Hz)')
ylabel('PSD //dB/Hz/1uPa')
grid
```



The three tones appear over the broadband spectrum.

## More About

## Input and Output Frequency Bands

The specified broadband and tonal noise frequencies must lie inside the operating frequency band,

$$
\left[f_{c}-f_{s} / 2, f_{c}+f_{s} / 2\right]
$$

$f_{s}$ represents the sample rate set by the SampleRate property and $f_{c}$ represents the operating frequency, set by the OperatingFrequency property.

However, the output noise spectrum lies in baseband:

$$
\left[-f_{s} / 2, f_{s} / 2\right]
$$

## Version History

Introduced in R2017b

## References

[1] Urick, R.J. Principles of Underwater Sound, 3rd Edition. New York: Peninsula Publishing, 1996.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{Tm}}$.
Usage notes and limitations:

- See "System Objects in MATLAB Code Generation" (MATLAB Coder).


## See Also

```
Objects
phased.BackscatterSonarTarget | phased.IsoSpeedUnderwaterPaths|
phased.IsotropicHydrophone|phased.IsotropicProjector|phased.MultipathChannel
Functions
range2tl|sonareqsl|sonareqsnr|sonareqtl|tl2range
```


## phased.URA

Package: phased
Uniform rectangular array

## Description

To create a Uniform Rectangular Array (URA) System object:
1 Create the phased.URA object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

array = phased.URA
array = phased.URA(Name,Value)
array $=$ phased.URA(SZ, D, Name, Value)

## Description

array $=$ phased. URA creates a uniform rectangular array (URA) System object that models a URA formed from identical isotropic phased array elements. Array elements are contained in the $y z$-plane in a rectangular lattice. The array look direction (boresight) points along the positive $x$-axis.
array $=$ phased.URA(Name,Value) creates an array object with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1, ..., NameN,ValueN). All properties needed to fully specify this object can be found in Properties."Response of 2-by-2 URA of Short-Dipole Antennas" on page 1-1891
array $=$ phased.URA(SZ,D,Name, Value) creates a phased.URA array System object with its Size property set to SZ and its ElementSpacing property set to D. Other specified property Names are set to the specified Values. SZ and D are value-only arguments. When specifying a value-only argument, specify all preceding value-only arguments. You can specify name-value pair arguments in any order.

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## Element - phased array element

isotropic antenna element System object with default properties (default) | Phased Array System Toolbox antenna, microphone, or transducer element System object | Antenna Toolbox antenna System object

Phased array element, specified as a Phased Array System Toolbox antenna, microphone, or transducer element or Antenna Toolbox antenna.

Example: phased. CosineAntennaElement

## Size - Array size

[2 2] (default) | positive scalar | 1-by-2 vector of positive values
Array size, specified as a 1-by-2 vector of integers or a single integer. containing the size of the array. If Size is a 1 -by-2 vector, the vector has the form [NumberOfRows, NumberOfColumns]. If Size is a scalar, the array has the same number of elements in each row and column. For a URA, array elements are indexed from top to bottom along a column and continuing to the next columns from left to right. In this illustration, a Size value of $[3,2]$ array has three rows and two columns.

## Size and Element Indexing Order

## for Uniform Rectangular Arrays

Example: Size = [3,2]


Example: $[3,2]$
Data Types: double

## ElementSpacing - Element spacing

[0.5 0.5] (default) | positive scalar | 1-by-2 vector of positive values
Element spacing, specified as a positive scalar or 1 -by-2 vector of positive values. If ElementSpacing is a 1 -by- 2 vector, it has the form
[SpacingBetweenRows, SpacingBetweenColumns]. See "Spacing Between Columns" on page 11907 and "Spacing Between Rows" on page 1-1907. If ElementSpacing is a scalar, both row and column spacings are equal. Units are in meters.
Example: [0.3, 0.5]
Data Types: double

## Lattice - Lattice type

'Rectangular' (default) | 'Triangular'
Element lattice type, specified as 'Rectangular' or 'Triangular'. When you set the Lattice property to 'Rectangular', all elements of the URA are aligned in both row and column directions. When you set the Lattice property to 'Triangular', elements in even rows are displaced toward the positive row axis direction. The displacement is one-half the element spacing along the row.

## Example: 'Triangular'

Data Types: char | string

## ArrayNormal - Array normal direction <br> ```'x' (default)| 'y'| 'z'```

Array normal direction, specified as one of ' $x$ ', ' $y$ ', or ' $z$ '. URA elements lie in a plane orthogonal to the selected array normal direction. Element boresight directions point along the array normal direction.

| ArrayNormal Property Value | Element Positions and Boresight Directions |
| :--- | :--- |
| ' $x^{\prime}$ | Array elements lie on the $y z$-plane. All element <br> boresight vectors point along the $x$-axis. This is <br> the default value. |
| $'^{\prime} y^{\prime}$ | Array elements lie on the $z x$-plane. All element <br> boresight vectors point along the $y$-axis. |
| ' $z{ }^{\prime}$ | Array elements lie on the $x y$-plane. All element <br> boresight vectors point along the $z$-axis. |

## Taper - Element tapers

1 (default) | complex-valued scalar | complex-valued 1-by-MN row vector
Element tapers, specified as a complex-valued scalar, complex-valued 1-by-MN vector, or complexvalued $M$-by- $N$ matrix. Tapers are applied to each element in the sensor array. Tapers are often referred to as element weights. $M$ is the number of elements along the $z$-axis, and $N$ is the number of elements along $y$-axis. $M$ and $N$ correspond to the values of [NumberofRows, NumberOfColumns] in the SIze property. If Taper is a scalar, the same taper value is applied to all elements. If the value of Taper is a vector or matrix, taper values are applied to the corresponding elements. Tapers are used to modify both the amplitude and phase of the received data.

## Example: [0.4 1 0.4]

Data Types: double

## Usage

## Syntax

RESP = array (FREQ,ANG)

## Description

RESP $=\operatorname{array}($ FREQ, ANG) returns the responses of the array elements, RESP, at the operating frequencies specified in FREQ and directions specified in ANG.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## FREQ - Array operating frequencies

length- $L$ row vector of positive values
Array operating frequencies, specified as a length- $L$ row vector. Typical values are within the range specified by a frequency range property of the array element. That property is called
FrequencyRange or FrequencyVector, depending on the type of array element. The element has zero response at frequencies outside that range. Units are in Hz .
Data Types: double

## ANG - Array response directions

length- $M$ row vector with real values | 2 -by- $M$ matrix with real values
Array response directions, specified as a 2 -by- $M$ matrix or length- $M$ row vector.
If ANG is a 2 -by-M matrix, each column of the matrix specifies the direction in the form [azimuth; elevation]. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive.

If ang is a row vector of length $M$, each element specifies the azimuth angle of the direction. In this case, the corresponding elevation angle is assumed to be $0^{\circ}$.

Units are in degrees.

## Output Arguments

## RESP - Voltage responses of phased array elements

$N$-by-M-by- complex-valued MATLAB array | MATLAB struct
Voltage responses of phased array elements. The output depends on whether or not the array supports polarization.

- If the array is not capable of supporting polarization, the voltage response, RESP, has the dimensions $N$-by- $M$-by- $L$. $N$ is the number of elements in the array. The dimension $M$ is the number of angles specified in ANG. $L$ is the number of frequencies specified in FREQ. For any element, the columns of RESP contain the responses of the array elements for the corresponding direction specified in ang. Each of the $L$ pages of RESP contains the responses of the array elements for the corresponding frequency specified in freq.
- If the array is capable of supporting polarization, the voltage response RESP is a MATLAB struct containing two fields, RESP.H and RESP.V. The field, RESP.H, represents the array's horizontal polarization response, while RESP.V represents the array's vertical polarization response. Each field has the dimensions $N$-by- $M$-by-L. $N$ is the number of elements in the array, and $M$ is the number of angles specified in ANG. $L$ is the number of frequencies specified in FREQ. Each column of RESP contains the responses of the array elements for the corresponding direction specified in ANG. Each of the $L$ pages of ANG contains the responses of the array elements for the corresponding frequency specified in FREQ.


## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:
release(obj)

## Specific to phased.URA and other array System objects

| beamwidth | Compute and display beamwidth of an array |
| :--- | :--- |
| collectPlaneWave | Simulate received plane waves at array |
| directivity | Compute array directivity |
| getElementNormal | Normal vectors for array elements |
| getElementPosition | Positions of array elements |
| getNumElements | Number of elements in an array |
| getTaper | Array element tapers |
| isPolarizationCapable | Array polarization capability |
| pattern | Plot array directivity and patterns |
| patternAzimuth | Plot array directivity or pattern versus azimuth |
| patternElevation | Plot array directivity or pattern versus elevation |
| perturbations | Perturbations defined on array |
| perturbedArray | Apply perturbations to phased array |
| perturbedPattern | Display pattern of perturbed array |
| plotGratingLobeDiagram | Plot grating lobe diagram of array |
| viewArray | View array geometry |

## Common to All System Objects

step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object

## Examples

## Response of 2-by-2 URA of Short-Dipole Antennas

Construct a 2-by-2 rectangular lattice URA of short-dipole antenna elements. Then, find the response of each element at boresight. Assume the operating frequency is 1 GHz .

```
sSD = phased.ShortDipoleAntennaElement;
sURA = phased.URA('Element',sSD,'Size',[2 2]);
fc = 1e9;
ang = [0;0];
resp = step(sURA,fc,ang);
disp(resp.V)
    -1.2247
    -1.2247
    -1.2247
    -1.2247
```


## Azimuth Response of a 3-by-2 URA at Boresight

Construct a 3-by-2 rectangular lattice URA. By default, the array consists of isotropic antenna elements. Find the response of each element at boresight, 0 degrees azimuth and elevation. Assume the operating frequency is 1 GHz .

```
array = phased.URA('Size',[3 2]);
fc = 1e9;
ang = [0;0];
resp = array(fc,ang);
disp(resp)
    1
1
1
1
1
1
```

Plot the azimuth pattern of the array.

```
c = physconst('LightSpeed');
pattern(array,fc,[-180:180],0,'PropagationSpeed',c, ...
    'CoordinateSystem','polar','Type','powerdb','Normalize',true)
```



Normalized Power (dB), Broadside at $0.00^{\circ}$

## Compare Triangular and Rectangular Lattice URAs

This example shows how to find and plot the positions of the elements of a 5 -row-by-6-column URA with a triangular lattice and a URA with a rectangular lattice. The element spacing is 0.5 meters for both lattices.

Create the arrays.
h_tri = phased.URA('Size',[5 6],'Lattice','Triangular');
h_rec = phased.URA('Size',[5 6],'Lattice','Rectangular');
Get the element $\mathrm{y}, \mathrm{z}$ positions for each array. All the x coordinates are zero.

```
pos tri = getElementPosition(h tri);
pos_rec = getElementPosition(h_rec);
pos_yz_tri = pos_tri(2:3,:);
pos_yz_rec = pos_rec(2:3,:);
```

Plot the element positions in the yz-plane.

```
figure;
gcf.Position = [100 100 300 400];
subplot(2,1,1);
plot(pos_yz_tri(1,:), pos_yz_tri(2,:), '.')
axis([-1.5 1.5 -2 2])
xlabel('y'); ylabel('z')
title('Triangular Lattice')
subplot(2,1,2);
plot(pos_yz_rec(1,:), pos_yz_rec(2,:), '.')
axis([-1.5 1.5 -2 2])
xlabel('y'); ylabel('z')
title('Rectangular Lattice')
```



## Adding Tapers to an Array

Construct a 5-by-2 element URA with a Taylor window taper along each column. The tapers form a 5-by-2 matrix.

```
taper = taylorwin(5);
ha = phased.URA([5,2],'Taper',[taper,taper]);
w = getTaper(ha)
w = 10\times1
    0.5181
    1.2029
    1.5581
    1.2029
    0.5181
    0.5181
    1.2029
    1.5581
    1.2029
    0.5181
```


## Simulate Received Signal at URA

Simulate two received random signals at a 6 -element URA. The array has a rectangular lattice with two elements in the row direction and three elements in the column direction. The signals arrive from $10^{\circ}$ and $30^{\circ}$ azimuth. Both signals have an elevation angle of $0^{\circ}$. Assume the propagation speed is the speed of light and the carrier frequency of the signal is 100 MHz .

```
array = phased.URA([2 3]);
fc = 100e6;
y = collectPlaneWave(array,randn(4,2),[10 30],fc,physconst('LightSpeed'));
```


## Directivity of Uniform Rectangular Array

Compute the directivity of two uniform rectangular arrays (URA). The first array consists of isotropic antenna elements. The second array consists of cosine antenna elements. In addition, compute the directivity of the first array steered to a specific direction.

## Array of isotropic antenna elements

First, create a 10-by-10-element URA of isotropic antenna elements spaced one-quarter wavelength apart. Set the signal frequency to 800 MHz .

```
c = physconst('LightSpeed');
fc = 3e8;
lambda = c/fc;
myAntIso = phased.IsotropicAntennaElement;
myArray1 = phased.URA;
myArray1.Element = myAntIso;
myArray1.Size = [10,10];
myArray1.ElementSpacing = [lambda*0.25,lambda*0.25];
ang = [0;0];
d = directivity(myArray1,fc,ang,'PropagationSpeed',c)
d = 15.7753
```


## Array of cosine antenna elements

Next, create a 10 -by-10-element URA of cosine antenna elements also spaced one-quarter wavelength apart.

```
myAntCos = phased.CosineAntennaElement('CosinePower',[1.8,1.8]);
myArray2 = phased.URA;
myArray2.Element = myAntCos;
myArray2.Size = [10,10];
myArray2.ElementSpacing = [lambda*0.25,lambda*0.25];
ang = [0;0];
d = directivity(myArray2,fc,ang,'PropagationSpeed',c)
d = 19.7295
```

The directivity is increased due to the directivity of the cosine antenna elements.

## Steered array of isotropic antenna elements

Finally, steer the isotropic antenna array to 30 degrees in azimuth and examine the directivity at the steered angle.

```
ang = [30;0];
w = steervec(getElementPosition(myArrayl)/lambda,ang);
d = directivity(myArray1,fc,ang,'PropagationSpeed',c,...
    'Weights',w)
d = 15.3309
```

The directivity is maximum in the steered direction and equals the directivity of the unsteered array at boresight.

## URA Element Normals

Construct three 2-by-2 URA's with element normals along the $x$-, $y$-, and $z$-axes. Obtain the element positions and normal directions.

First, choose the array normal along the $x$-axis.

```
sURA1 = phased.URA('Size',[2,2],'ArrayNormal','x');
pos = getElementPosition(sURA1)
pos = 3\times4
\begin{tabular}{rrrr}
0 & 0 & 0 & 0 \\
-0.2500 & -0.2500 & 0.2500 & 0.2500 \\
0.2500 & -0.2500 & 0.2500 & -0.2500
\end{tabular}
normvec = getElementNormal(sURA1)
normvec = 2×4
\begin{tabular}{llll}
0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0
\end{tabular}
```

All elements lie in the $y z$-plane and the element normal vectors point along the $x$-axis $\left(0^{\circ}, 0^{\circ}\right)$. Next, choose the array normal along the $y$-axis.

```
sURA2 = phased.URA('Size',[2,2],'ArrayNormal','y');
pos = getElementPosition(sURA2)
pos = 3\times4
\begin{tabular}{rrrr}
0.2500 & 0.2500 & -0.2500 & -0.2500 \\
0 & 0 & 0 & 0 \\
0.2500 & -0.2500 & 0.2500 & -0.2500
\end{tabular}
normvec = getElementNormal(sURA2)
normvec = 2×4
    90 90 90 90
    0 0 0 0
```

All elements lie in the $z x$-plane and the element normal vectors point along the $y$-axis $\left(90^{\circ}, 0^{\circ}\right)$.

Finally, set the array normal along the $z$-axis. Obtain the normal vectors of the odd-numbered elements.

```
sURA3 = phased.URA('Size',[2,2],'ArrayNormal','z');
pos = getElementPosition(sURA3)
pos = 3\times4
\begin{tabular}{rrrr}
-0.2500 & -0.2500 & 0.2500 & 0.2500 \\
0.2500 & -0.2500 & 0.2500 & -0.2500 \\
0 & 0 & 0 & 0
\end{tabular}
normvec = getElementNormal(sURA3,[1,3])
normvec = 2 <2
    0}
    90 90
```

All elements lie in the $x y$-plane and the element normal vectors point along the $z$-axis $\left(0^{\circ}, 90^{\circ}\right)$.

## Obtain URA Element Positions

Construct a default URA with a rectangular lattice, and obtain the element positions.

```
array = phased.URA;
pos = getElementPosition(array)
pos = 3×4
\begin{tabular}{rrrr}
0 & 0 & 0 & 0 \\
-0.2500 & -0.2500 & 0.2500 & 0.2500 \\
0.2500 & -0.2500 & 0.2500 & -0.2500
\end{tabular}
```


## Obtain Number of URA Elements

Construct a default URA, and obtain the number of elements.
array = phased.URA;
$\mathrm{N}=$ getNumElements(array)
$N=4$

## Create Tapered URA

Construct a 5-by-2 element URA with a Taylor window taper along each column. Then, draw the array showing the element taper shading.

```
taper = taylorwin(5);
array = phased.URA([5,2],'Taper',[taper,taper]);
w = getTaper(array)
w = 10x1
    0.5181
    1.2029
    1.5581
    1.2029
    0.5181
    0.5181
    1.2029
    1.5581
    1.2029
    0.5181
viewArray(array,'ShowTaper',true)
```


## Array Geometry



## Short-Dipole URA Supports Polarization

Show that a URA array of phased. ShortDipoleAntennaElement short-dipole antenna elements supports polarization.

```
antenna = phased.ShortDipoleAntennaElement('FrequencyRange',[le9 10e9]);
array = phased.URA([3,2],'Element',antenna);
isPolarizationCapable(array)
ans = logical
    1
```

The returned value 1 shows that this array supports polarization.

## Pattern of 5x7-Element URA Antenna Array

Create a 5 x 7 -element URA operating at 1 GHz . Assume the elements are spaced one-half wavelength apart. Show the 3-D array patterns.

## Create the array

```
sSD = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[50e6,1000e6],...
    'AxisDirection','Z');
fc = 500e6;
c = physconst('LightSpeed');
lam = c/fc;
sURA = phased.URA('Element',sSD,...
    'Size',[5,7],...
    'ElementSpacing',0.5*lam);
```


## Call the step method

Evaluate the fields of the first five elements at 45 degrees azimuth and 0 degrees elevation.

```
ang = [45;0];
resp = step(sURA,fc,ang);
disp(resp.V(1:5))
    -1.2247
    -1.2247
    -1.2247
    -1.2247
    -1.2247
```

Display the 3-D directivity pattern at $\mathbf{1} \mathbf{~ G H z}$ in polar coordinates

```
pattern(sURA,fc,[-180:180],[-90:90],...
    'CoordinateSystem','polar',...
    'Type','directivity','PropagationSpeed', c)
```



Display the 3-D directivity pattern at $\mathbf{1} \mathbf{G H z}$ in UV coordinates
pattern(sURA, fc, [-1.0:.01:1.0],[-1.0:.01:1.0],...
'CoordinateSystem', 'uv',...
'Type','directivity','PropagationSpeed', c)


## Azimuth Pattern of 5x7-Element URA Antenna Array

Create a 5x7-element URA of short-dipole antenna elements operating at 1 GHz . Assume the elements are spaced one-half wavelength apart. Plot the array azimuth directivity patterns for two different elevation angles, 0 and 15 degrees. The patternAzimuth method always plots the array pattern in polar coordinates.

## Create the array

```
sSD = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[50e6,1000e6],...
    'AxisDirection','Z');
fc = 1e9;
c = physconst('LightSpeed');
lam = c/fc;
sURA = phased.URA('Element',sSD,...
    'Size',[5,7],...
    'ElementSpacing',0.5*lam);
```


## Display the pattern

Display the azimuth directivity pattern at 1 GHz in polar coordinates

```
patternAzimuth(sURA,fc,[0 15],...
```

'PropagationSpeed', c, ...
'Type','directivity')


Directivity (dBi), Broadside at $0.00^{\circ}$

## Display a subset of angles

You can plot a smaller range of azimuth angles by setting the Azimuth parameter.
patternAzimuth(sURA,fc,[0 15],...
'PropagationSpeed', c,...
'Type','directivity',...
'Azimuth',[-45:45])


Directivity (dBi), Broadside at $0.00^{\circ}$

## Elevation Pattern of 7x7-Element Acoustic URA

Create a 7 x 7 -element URA of backbaffled omnidirectional transducer elements operating at 2 kHz . Assume the speed of sound in water is $1500 \mathrm{~m} / \mathrm{s}$. The elements are spaced less than one-half wavelength apart. Plot the array elevation directivity patterns for three different azimuth angles, -20 , 0 , and 15 degrees. The patternElevation method always plots the array pattern in polar coordinates.

## Create the array

```
element = phased.OmnidirectionalMicrophoneElement(...
    'FrequencyRange',[20,3000],...
    'BackBaffled',true);
fc = 1000;
c = 1500;
lam = c/fc;
array = phased.URA('Element',element,...
    'Size',[7,7],...
    'ElementSpacing',0.45*lam);
```


## Display the pattern

Display the azimuth directivity pattern at 1 GHz in polar coordinates.
patternElevation(array,fc,[-20, 0, 15],...
'PropagationSpeed', c, ...
'Type','directivity')


## Display a subset of elevation angles

You can plot a smaller range of elevation angles by setting the Elevation parameter.

```
patternElevation(array,fc,[-20, 0, 15],...
```

'PropagationSpeed', c, ...
'Type','directivity',...
'Elevation', [-45:45])


Directivity (dBi), Broadside at $0.00^{\circ}$

## Grating Lobe Diagram for Microphone URA

Plot the grating lobe diagram for an 11-by-9-element uniform rectangular array having element spacing equal to one-half wavelength.

Assume the operating frequency of the array is 10 kHz . All elements are omnidirectional microphone elements. Steer the array in the direction 20 degrees in azimuth and 30 degrees in elevation. The speed of sound in air is $344.21 \mathrm{~m} / \mathrm{s}$ at 21 deg C .

```
cair = 344.21;
f = 10.0e3;
lambda = cair/f;
microphone = phased.OmnidirectionalMicrophoneElement(...
    'FrequencyRange',[20 20000]);
array = phased.URA('Element',microphone,'Size',[11,9],...
    'ElementSpacing',0.5*lambda*[1,1]);
plotGratingLobeDiagram(array,f,[20;30],cair);
```



Plot the grating lobes. The main lobe of the array is indicated by a filled black circle. The grating lobes in visible and nonvisible regions are indicated by unfilled black circles. The visible region is the region in $u$-v coordinates for which $u^{2}+v^{2} \leq 1$. The visible region is shown as a unit circle centered at the origin. Because the array spacing is less than one-half wavelength, there are no grating lobes in the visible region of space. There are an infinite number of grating lobes in the nonvisible regions, but only those in the range $[-3,3]$ are shown.

The grating-lobe free region, shown in green, is the range of directions of the main lobe for which there are no grating lobes in the visible region. In this case, it coincides with the visible region.

The white areas of the diagram indicate a region where no grating lobes are possible.

## Geometry, Normal Directions, and Indices of URA Elements

This example shows how to display the element positions, normal directions, and indices for all elements of a 4-by-4 square URA.
ha = phased.URA(4);
viewArray(ha, 'ShowNormals',true,'ShowIndex','All');


## More About

## Spacing Between Columns

The spacing between columns is the distance between adjacent elements in the same row.

## Spacing Between Rows

The spacing between rows is the distance along the column axis direction between adjacent rows.


## Version History

Introduced in R2011a

## References

[1] Brookner, E., ed. Radar Technology. Lexington, MA: LexBook, 1996.
[2] Brookner, E., ed. Practical Phased Array Antenna Systems. Boston: Artech House, 1991.
[3] Mailloux, R. J. "Phased Array Theory and Technology," Proceedings of the IEEE, Vol., 70, Number 3s, pp. 246-291.
[4] Mott, H. Antennas for Radar and Communications, A Polarimetric Approach. New York: John Wiley \& Sons, 1992.
[5] Van Trees, H. Optimum Array Processing. New York: Wiley-Interscience, 2002.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.
Usage notes and limitations:

- pattern, patternAzimuth, patternElevation, and viewArray object functions are not supported.
- See "System Objects in MATLAB Code Generation" (MATLAB Coder).


## See Also

phased.ReplicatedSubarray|phased.PartitionedArray|phased.ConformalArray| phased.CosineAntennaElement | phased.CustomAntennaElement | phased.IsotropicAntennaElement | phased.ULA| phased.HeterogeneousULA| phased.HeterogeneousURA |uv2azel | phitheta2azel

## Topics

Phased Array Gallery

## directivity

System object: phased. URA
Package: phased
Directivity of uniform rectangular array

## Syntax

D = directivity (H,FREQ,ANGLE)
D = directivity (H, FREQ, ANGLE, Name, Value)

## Description

D = directivity ( $\mathrm{H}, \mathrm{FREQ}$, ANGLE) computes the "Directivity" on page 1-1913 of a uniform rectangular array (URA) of antenna or microphone elements, $H$, at frequencies specified by the FREQ and in angles of direction specified by the ANGLE.

The integration used when computing array directivity has a minimum sampling grid of 0.1 degrees. If an array pattern has a beamwidth smaller than this, the directivity value will be inaccurate.

D = directivity (H, FREQ, ANGLE, Name, Value) computes the directivity with additional options specified by one or more Name, Value pair arguments.

## Input Arguments

## H - Uniform rectangular array

System object
Uniform rectangular array specified as a phased. URA System object.
Example: H = phased.URA

## FREQ - Frequency for computing directivity and patterns

positive scalar | 1-by-L real-valued row vector
Frequencies for computing directivity and patterns, specified as a positive scalar or 1-by-L realvalued row vector. Frequency units are in hertz.

- For an antenna, microphone, or sonar hydrophone or projector element, FREQ must lie within the range of values specified by the FrequencyRange or FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased.CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: [1e8 2e6]
Data Types: double

## ANGLE - Angles for computing directivity

## 1-by- $M$ real-valued row vector | 2-by- $M$ real-valued matrix

Angles for computing directivity, specified as a 1-by- $M$ real-valued row vector or a 2 -by- $M$ real-valued matrix, where $M$ is the number of angular directions. Angle units are in degrees. If ANGLE is a 2 -by- $M$ matrix, then each column specifies a direction in azimuth and elevation, [az;el]. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

If ANGLE is a $1-b y-M$ vector, then each entry represents an azimuth angle, with the elevation angle assumed to be zero.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the xy plane. This angle is positive when measured from the $x$-axis toward the $y$-axis. The elevation angle is the angle between the direction vector and $x y$ plane. This angle is positive when measured towards the $z$-axis. See "Azimuth and Elevation Angles".
Example: [45 60; 0 10]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Namel=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## PropagationSpeed - Signal propagation speed

speed of light (default) | positive scalar
Signal propagation speed, specified as the comma-separated pair consisting of ' PropagationSpeed ' and a positive scalar in meters per second.

Example: 'PropagationSpeed', physconst('LightSpeed')
Data Types: double
Weights - Array weights
1 (default) $\mid N$-by-1 complex-valued column vector $\mid N$-by- $L$ complex-valued matrix
Array weights, specified as the comma-separated pair consisting of 'Weights' and an $N$-by- 1 complex-valued column vector or $N$-by- $L$ complex-valued matrix. Array weights are applied to the elements of the array to produce array steering, tapering, or both. The dimension $N$ is the number of elements in the array. The dimension $L$ is the number of frequencies specified by FREQ.

| Weights Dimension | FREQ Dimension | Purpose |
| :--- | :--- | :--- |
| $N$-by-1 complex-valued column <br> vector | Scalar or 1-by- $L$ row vector | Applies a set of weights for the <br> single frequency or for all $L$ <br> frequencies. |
| $N$-by- $L$ complex-valued matrix | 1-by-L row vector | Applies each of the $L$ columns of <br> 'Weights' for the <br> corresponding frequency in <br> FREQ. |

Note Use complex weights to steer the array response toward different directions. You can create weights using the phased.SteeringVector System object or you can compute your own weights. In general, you apply Hermitian conjugation before using weights in any Phased Array System Toolbox function or System object such as phased. Radiator or phased. Collector. However, for the directivity, pattern, patternAzimuth, and patternElevation methods of any array System object use the steering vector without conjugation.

## Example: 'Weights',ones(N,M)

Data Types: double
Complex Number Support: Yes

## Output Arguments

## D - Directivity

M-by-L matrix
Directivity, returned as an $M$-by- $L$ matrix. Each row corresponds to one of the $M$ angles specified by ANGLE. Each column corresponds to one of the $L$ frequency values specified in FREQ. Directivity units are in dBi where dBi is defined as the gain of an element relative to an isotropic radiator.

## Examples

## Directivity of Uniform Rectangular Array

Compute the directivity of two uniform rectangular arrays (URA). The first array consists of isotropic antenna elements. The second array consists of cosine antenna elements. In addition, compute the directivity of the first array steered to a specific direction.

## Array of isotropic antenna elements

First, create a 10-by-10-element URA of isotropic antenna elements spaced one-quarter wavelength apart. Set the signal frequency to 800 MHz .

```
c = physconst('LightSpeed');
fc = 3e8;
lambda = c/fc;
myAntIso = phased.IsotropicAntennaElement;
myArray1 = phased.URA;
myArrayl.Element = myAntIso;
myArrayl.Size = [10,10];
myArray1.ElementSpacing = [lambda*0.25,lambda*0.25];
ang = [0;0];
d = directivity(myArray1,fc,ang,'PropagationSpeed',c)
d = 15.7753
```


## Array of cosine antenna elements

Next, create a 10-by-10-element URA of cosine antenna elements also spaced one-quarter wavelength apart.

```
myAntCos = phased.CosineAntennaElement('CosinePower',[1.8,1.8]);
myArray2 = phased.URA;
```

```
myArray2.Element = myAntCos;
myArray2.Size = [10,10];
myArray2.ElementSpacing = [lambda*0.25,lambda*0.25];
ang = [0;0];
d = directivity(myArray2,fc,ang,'PropagationSpeed',c)
d = 19.7295
```

The directivity is increased due to the directivity of the cosine antenna elements.

## Steered array of isotropic antenna elements

Finally, steer the isotropic antenna array to 30 degrees in azimuth and examine the directivity at the steered angle.

```
ang = [30;0];
w = steervec(getElementPosition(myArray1)/lambda,ang);
d = directivity(myArray1,fc,ang,'PropagationSpeed',c,...
    'Weights',w)
d = 15.3309
```

The directivity is maximum in the steered direction and equals the directivity of the unsteered array at boresight.

## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \Pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## See Also

pattern| patternAzimuth | patternElevation

## collectPlaneWave

System object: phased. URA
Package: phased
Simulate received plane waves

## Syntax

```
Y = collectPlaneWave(H,X,ANG)
Y = collectPlaneWave(H,X,ANG,FREQ)
Y = collectPlaneWave(H,X,ANG,FREQ,C)
```


## Description

$Y=\operatorname{collectPlaneWave}(H, X, A N G)$ returns the received signals at the sensor array, $H$, when the input signals indicated by $X$ arrive at the array from the directions specified in ANG.
$Y=\operatorname{collectPlaneWave}(H, X, A N G, F R E Q)$, in addition, specifies the incoming signal carrier frequency in FREQ.
$\mathrm{Y}=$ collectPlaneWave( $\mathrm{H}, \mathrm{X}, \mathrm{ANG}, \mathrm{FREQ}, \mathrm{C})$, in addition, specifies the signal propagation speed in C.

## Input Arguments

## H

Array object.
X
Incoming signals, specified as an $M$-column matrix. Each column of $X$ represents an individual incoming signal.

## ANG

Directions from which incoming signals arrive, in degrees. ANG can be either a 2-by-M matrix or a row vector of length M .

If ANG is a 2-by-M matrix, each column specifies the direction of arrival of the corresponding signal in X. Each column of ANG is in the form [azimuth; elevation]. The azimuth angle must be between $-180^{\circ}$ and $180^{\circ}$, inclusive. The elevation angle must be between $-90^{\circ}$ and $90^{\circ}$, inclusive.

If ANG is a row vector of length M , each entry in ANG specifies the azimuth angle. In this case, the corresponding elevation angle is assumed to be $0^{\circ}$.

FREQ
Carrier frequency of signal in hertz. FREQ must be a scalar.
Default: 3e8

## C

Propagation speed of signal in meters per second.
Default: Speed of light

## Output Arguments

## Y

Received signals. Y is an N-column matrix, where N is the number of elements in the array H. Each column of $Y$ is the received signal at the corresponding array element, with all incoming signals combined.

## Examples

## Simulate Received Signal at URA

Simulate two received random signals at a 6 -element URA. The array has a rectangular lattice with two elements in the row direction and three elements in the column direction. The signals arrive from $10^{\circ}$ and $30^{\circ}$ azimuth. Both signals have an elevation angle of $0^{\circ}$. Assume the propagation speed is the speed of light and the carrier frequency of the signal is 100 MHz .
array = phased.URA([2 3]);
fc = 100e6;
$y=\operatorname{collectPlaneWave(array,randn(4,2),[1030],fc,physconst('LightSpeed'));~}$

## Algorithms

collectPlaneWave modulates the input signal with a phase corresponding to the delay caused by the direction of arrival. This method does not account for the response of individual elements in the array.

For further details, see [1].

## References

[1] Van Trees, H. Optimum Array Processing. New York: Wiley-Interscience, 2002.

## See Also <br> uv2azel | phitheta2azel

## getElementNormal

System object: phased.URA
Package: phased
Normal vector to array elements

## Syntax

normvec = getElementNormal(sURA)
normvec $=$ getElementNormal(sURA,elemidx)

## Description

normvec $=$ getElementNormal(sURA) returns the normal vectors of the array elements of the phased.URA System object, sURA. The output argument normvec is a 2 -by- $N$ matrix, where $N$ is the number of elements in array, sURA. Each column of normvec defines the normal direction of an element in the local coordinate system in the form [az;el]. Units are degrees. Array elements are located in the plane selected in the ArrayNormal property. Element normal vectors are parallel to the array normal. The normal to a URA array depends upon the selected ArrayNormal property.

| ArrayNormal Property Value | Array Normal Direction | Array Plane |
| :--- | :--- | :--- |
| ' $x$ ' | azimuth $=0^{\circ}$, elevation $=0^{\circ}(x-$ <br> axis $)$ | $y z$ |
| ' $y$ ' | azimuth $=90^{\circ}$, elevation $=0^{\circ}$ <br> $(y$-axis $)$ | $z x$ |
| ' $z$ ' | azimuth $=0^{\circ}$, elevation $=90^{\circ}$ <br> $(z$-axis $)$ | $x y$ |

The origin of the local coordinate system is defined by the phase center of the array.
normvec $=$ getElementNormal(sURA,elemidx) returns only the normal vectors of the elements specified in the element index vector, elemidx. This syntax can use any of the input arguments in the previous syntax.

## Input Arguments

## sURA - Uniform rectangular array

phased. sURA System object
Uniform line array, specified as a phased.URA System object.
Example: sULA = phased. URA

## elemidx - Element indices

all array elements (default) | integer-valued 1 -by-M row vector | integer-valued $M$-by-1 column vector
Element indices, specified as a 1 -by- $M$ or $M$-by-1 vector. Index values lie in the range 1 to $N$ where $N$ is the number of elements of the array. When elemidx is specified, getElementNormal returns the normal vectors of the elements contained in elemidx.

Example: [1,5,4]

## Output Arguments

## normvec - Element normal vectors

2-by-P real-valued vector
Element normal vectors, specified as a 2-by-P real-valued vector. Each column of normvec takes the form [az,el]. When elemidx is not specified, $P$ equals the array dimension. When elemidx is specified, $P$ equals the length of elemidx, $M$. You can determine element indices using the viewArray method.

## Examples

## URA Element Normals

Construct three 2-by-2 URA's with element normals along the $x$-, $y$-, and $z$-axes. Obtain the element positions and normal directions.

First, choose the array normal along the $x$-axis.

```
sURA1 = phased.URA('Size',[2,2],'ArrayNormal','x');
pos = getElementPosition(sURA1)
pos = 3\times4
\begin{tabular}{rrrr}
0 & 0 & 0 & 0 \\
-0.2500 & -0.2500 & 0.2500 & 0.2500 \\
0.2500 & -0.2500 & 0.2500 & -0.2500
\end{tabular}
normvec = getElementNormal(sURA1)
normvec = 2×4
    0 0 0 0
    0 0 0 0
```

All elements lie in the $y z$-plane and the element normal vectors point along the $x$-axis $\left(0^{\circ}, 0^{\circ}\right)$.
Next, choose the array normal along the $y$-axis.

```
sURA2 = phased.URA('Size',[2,2],'ArrayNormal','y');
pos = getElementPosition(sURA2)
pos = 3\times4
\begin{tabular}{rrrr}
0.2500 & 0.2500 & -0.2500 & -0.2500 \\
0 & 0 & 0 & 0 \\
0.2500 & -0.2500 & 0.2500 & -0.2500
\end{tabular}
normvec = getElementNormal(sURA2)
```

```
normvec = 2×4
```

| 90 | 90 | 90 | 90 |
| ---: | ---: | ---: | ---: |
| 0 | 0 | 0 | 0 |

All elements lie in the $z x$-plane and the element normal vectors point along the $y$-axis $\left(90^{\circ}, 0^{\circ}\right)$.
Finally, set the array normal along the $z$-axis. Obtain the normal vectors of the odd-numbered elements.

```
sURA3 = phased.URA('Size',[2,2],'ArrayNormal','z');
pos = getElementPosition(sURA3)
pos = 3\times4
\begin{tabular}{rrrr}
-0.2500 & -0.2500 & 0.2500 & 0.2500 \\
0.2500 & -0.2500 & 0.2500 & -0.2500 \\
0 & 0 & 0 & 0
\end{tabular}
normvec = getElementNormal(sURA3,[1,3])
normvec = 2×2
    0 0
    90 90
```

All elements lie in the $x y$-plane and the element normal vectors point along the $z$-axis $\left(0^{\circ}, 90^{\circ}\right)$.

## Version History <br> Introduced in R2016a

## getElementPosition

System object: phased. URA
Package: phased
Positions of array elements

## Syntax

POS = getElementPosition(H)
POS = getElementPosition(H,ELEIDX)

## Description

POS = getElementPosition (H) returns the element positions of the URA H. POS is a 3-by-N matrix where N is the number of elements in H . Each column of POS defines the position of an element in the local coordinate system, in meters, using the form [ $\mathrm{x} ; \mathrm{y} ; \mathrm{z}$ ].

For details regarding the local coordinate system of the URA, enter phased.URA.coordinateSystemInfo.

POS = getElementPosition(H,ELEIDX) returns the positions of the elements that are specified in the element index vector, ELEIDX. The index of a URA runs down each column, then to the next column to the right. For example, in a URA with 4 elements in each row and 3 elements in each column, the element in the third row and second column has an index value of 6.

## Examples

## Obtain URA Element Positions

Construct a default URA with a rectangular lattice, and obtain the element positions.

```
array = phased.URA;
pos = getElementPosition(array)
pos = 3\times4
\begin{tabular}{rrrr}
0 & 0 & 0 & 0 \\
-0.2500 & -0.2500 & 0.2500 & 0.2500 \\
0.2500 & -0.2500 & 0.2500 & -0.2500
\end{tabular}
```


## getNumElements

System object: phased. URA
Package: phased
Number of elements in array

## Syntax

N = getNumElements(H)

## Description

$\mathrm{N}=$ getNumElements $(\mathrm{H})$ returns the number of elements, N , in the URA object H .

## Examples

## Obtain Number of URA Elements

Construct a default URA, and obtain the number of elements.
array = phased.URA;
$\mathrm{N}=$ getNumElements(array)
$N=4$

## getTaper

System object: phased.URA
Package: phased
Array element tapers

## Syntax

wts = getTaper(h)

## Description

wts = getTaper(h) returns the tapers, wts, applied to each element of the phased uniform rectangular array (URA), h. Tapers are often referred to as weights.

## Input Arguments

h - Uniform rectangular array
phased.URA System object
Uniform rectangular array specified as aphased. URA System object.

## Output Arguments

## wts - Array element tapers

$N$-by-1 complex-valued vector
Array element tapers returned as an $N$-by-1, complex-valued vector, where $N$ is the number of elements in the array.

## Examples

## Create Tapered URA

Construct a 5-by-2 element URA with a Taylor window taper along each column. Then, draw the array showing the element taper shading.

```
taper = taylorwin(5);
array = phased.URA([5,2],'Taper',[taper,taper]);
w = getTaper(array)
w = 10\times1
    0.5181
    1.2029
    1.5581
    1.2029
    0.5181
    0.5181
```

```
    1.2029
    1.5581
    1.2029
    0.5181
viewArray(array,'ShowTaper',true)
```


## Array Geometry



[^6]
## pattern

System object: phased. URA
Package: phased
Plot URA array pattern

## Syntax

```
pattern(sArray,FREQ)
pattern(sArray,FREQ,AZ)
pattern(sArray,FREQ,AZ,EL)
pattern(__,Name,Value)
[PAT,AZ_ANG,EL_ANG] = pattern(
```

$\qquad$

``` )
```


## Description

pattern(sArray, FREQ) plots the 3-D array directivity pattern (in dBi) for the array specified in sArray. The operating frequency is specified in FREQ.

The integration used when computing array directivity has a minimum sampling grid of 0.1 degrees. If an array pattern has a beamwidth smaller than this, the directivity value will be inaccurate.
pattern(sArray, FREQ,AZ) plots the array directivity pattern at the specified azimuth angle.
pattern(sArray, FREQ, AZ, EL) plots the array directivity pattern at specified azimuth and elevation angles.
pattern( $\qquad$ ,Name, Value) plots the array pattern with additional options specified by one or more Name, Value pair arguments.
[PAT,AZ_ANG,EL_ANG] = pattern( __ ) returns the array pattern in PAT. The AZ_ANG output contains the coordinate values corresponding to the rows of PAT. The EL_ANG output contains the coordinate values corresponding to the columns of PAT. If the 'CoordinateSystem' parameter is set to ' uv' , then AZ_ANG contains the $U$ coordinates of the pattern and EL_ANG contains the $V$ coordinates of the pattern. Otherwise, they are in angular units in degrees. $U V$ units are dimensionless.

Note This method replaces the plotResponse method. See "Convert plotResponse to pattern" on page 1-1930 for guidelines on how to use pattern in place of plotResponse.

## Input Arguments

## sArray - Uniform rectangular array

System object
Uniform rectangular array, specified as a phased. URA System object.
Example: sArray= phased.URA;

## FREQ - Frequency for computing directivity and patterns

positive scalar | 1-by-L real-valued row vector
Frequencies for computing directivity and patterns, specified as a positive scalar or 1-by-L realvalued row vector. Frequency units are in hertz.

- For an antenna, microphone, or sonar hydrophone or projector element, FREQ must lie within the range of values specified by the FrequencyRange or FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased.CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: [1e8 2e6]
Data Types: double

## AZ - Azimuth angles

[-180:180] (default) | 1-by- $N$ real-valued row vector
Azimuth angles for computing directivity and pattern, specified as a 1-by- $N$ real-valued row vector where $N$ is the number of azimuth angles. Angle units are in degrees. Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the $x y$ plane. When measured from the $x$-axis toward the $y$-axis, this angle is positive.

## Example: [-45:2:45]

Data Types: double

## EL - Elevation angles

[-90:90] (default) | 1-by-M real-valued row vector
Elevation angles for computing directivity and pattern, specified as a 1-by-M real-valued row vector where $M$ is the number of desired elevation directions. Angle units are in degrees. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

The elevation angle is the angle between the direction vector and $x y$-plane. The elevation angle is positive when measured towards the $z$-axis.
Example: [-75:1:70]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

```
CoordinateSystem - Plotting coordinate system
'polar' (default)|'rectangular'|'uv'
```

Plotting coordinate system of the pattern, specified as the comma-separated pair consisting of 'CoordinateSystem' and one of 'polar', 'rectangular', or 'uv'. When
'CoordinateSystem' is set to 'polar' or 'rectangular', the AZ and EL arguments specify the pattern azimuth and elevation, respectively. AZ values must lie between $-180^{\circ}$ and $180^{\circ}$. EL values must lie between $-90^{\circ}$ and $90^{\circ}$. If 'CoordinateSystem' is set to 'uv', AZ and EL then specify $U$ and $V$ coordinates, respectively. AZ and EL must lie between -1 and 1.
Example: 'uv'
Data Types: char

## Type - Displayed pattern type

'directivity' (default) |'efield'|'power'|'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type ' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb' - power pattern converted to dB.

Example: 'powerdb'
Data Types: char

## Orientation - Array orientation

[0;0;0]. (default)|3-by-1 real-valued column vector
Array orientation, specified as a 3-by-1 real-valued column vector containing the rotation angles with respect to the $x-y$-, and $z$-axes of the local coordinate system, respectively.

## Normalize - Display normalize pattern

true (default) | false
Display normalized pattern, specified as the comma-separated pair consisting of 'Normalize' and a Boolean. Set this parameter to true to display a normalized pattern. This parameter does not apply when you set 'Type' to 'directivity'. Directivity patterns are already normalized.
Data Types: logical

## ShowArray - View array geometry

false (default)| true
View the array geometry along with the 3D radiation pattern, specified as false or true.
Data Types: logical
ShowLocalCoordinates - Show local coordinate axes
true (default) | false
Show the local coordinate axes, specified as true or false.
Data Types: logical

## ShowColorbar - Show colorbar

true (default) | false

Show the colorbar, specified as true or false.
Data Types: logical

## Parent - Handle to axis

scalar
Handle to the axes along which the array geometry is displayed specified as a scalar.

## PlotStyle - Plotting style

'overlay' (default)|'waterfall'
Plotting style, specified as the comma-separated pair consisting of 'Plotstyle' and either 'overlay' or 'waterfall'. This parameter applies when you specify multiple frequencies in FREQ in 2-D plots. You can draw 2-D plots by setting one of the arguments AZ or EL to a scalar.

## Data Types: char

## Polarization - Polarized field component

'combined' (default) | 'H' | 'V'
Polarized field component to display, specified as the comma-separated pair consisting of 'Polarization' and 'combined ', 'H', or 'V'. This parameter applies only when the sensors are polarization-capable and when the 'Type' parameter is not set to 'directivity'. This table shows the meaning of the display options.

| 'Polarization' | Display |
| :--- | :--- |
| ' combined ' | Combined $H$ and $V$ polarization components |
| 'H' | $H$ polarization component |
| ' $\mathrm{V}^{\prime}$ | $V$ polarization component |

Example: 'V '

## Data Types: char

## PropagationSpeed - Signal propagation speed

speed of light (default) | positive scalar
Signal propagation speed, specified as the comma-separated pair consisting of
' PropagationSpeed ' and a positive scalar in meters per second.
Example: 'PropagationSpeed', physconst('LightSpeed')
Data Types: double

## Weights - Array weights

1 (default) | $N$-by-1 complex-valued column vector | $N$-by-L complex-valued matrix
Array weights, specified as the comma-separated pair consisting of 'Weights' and an N -by-1 complex-valued column vector or $N$-by- $L$ complex-valued matrix. Array weights are applied to the elements of the array to produce array steering, tapering, or both. The dimension $N$ is the number of elements in the array. The dimension $L$ is the number of frequencies specified by FREQ.

| Weights Dimension | FREQ Dimension | Purpose |
| :--- | :--- | :--- |
| $N$-by-1 complex-valued column <br> vector | Scalar or 1-by- $L$ row vector | Applies a set of weights for the <br> single frequency or for all $L$ <br> frequencies. |
| $N$-by- $L$ complex-valued matrix | 1-by- $L$ row vector | Applies each of the $L$ columns of <br> 'Weights' for the <br> corresponding frequency in <br> FREQ. |

Note Use complex weights to steer the array response toward different directions. You can create weights using the phased. SteeringVector System object or you can compute your own weights. In general, you apply Hermitian conjugation before using weights in any Phased Array System Toolbox function or System object such as phased. Radiator or phased. Collector. However, for the directivity, pattern, patternAzimuth, and patternElevation methods of any array System object use the steering vector without conjugation.

Example: 'Weights',ones(N,M)
Data Types: double
Complex Number Support: Yes

## Output Arguments

## PAT - Array pattern

$M$-by- $N$ real-valued matrix
Array pattern, returned as an $M$-by- $N$ real-valued matrix. The dimensions of PAT correspond to the dimensions of the output arguments AZ_ANG and EL_ANG.

## AZ_ANG - Azimuth angles

scalar | 1-by-N real-valued row vector
Azimuth angles for displaying directivity or response pattern, returned as a scalar or 1-by- N realvalued row vector corresponding to the dimension set in AZ. The columns of PAT correspond to the values in AZ_ANG. Units are in degrees.

## EL_ANG - Elevation angles

scalar | 1-by-M real-valued row vector
Elevation angles for displaying directivity or response, returned as a scalar or 1-by-M real-valued row vector corresponding to the dimension set in EL. The rows of PAT correspond to the values in EL_ANG. Units are in degrees.

## Examples

## Pattern of 5x7-Element URA Antenna Array

Create a 5x7-element URA operating at 1 GHz . Assume the elements are spaced one-half wavelength apart. Show the 3-D array patterns.

```
Create the array
sSD = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[50e6,1000e6],...
    'AxisDirection','Z');
fc = 500e6;
c = physconst('LightSpeed');
lam = c/fc;
sURA = phased.URA('Element',sSD,...
    'Size',[5,7],...
    'ElementSpacing',0.5*lam);
```


## Call the step method

Evaluate the fields of the first five elements at 45 degrees azimuth and 0 degrees elevation.

```
ang = [45;0];
resp = step(sURA,fc,ang);
disp(resp.V(1:5))
    -1.2247
    -1.2247
    -1.2247
    -1.2247
    -1.2247
```

Display the 3-D directivity pattern at $\mathbf{1 ~ G H z}$ in polar coordinates

```
pattern(sURA,fc,[-180:180],[-90:90],...
    'CoordinateSystem','polar',...
    'Type','directivity','PropagationSpeed',c)
```



Display the 3-D directivity pattern at $1 \mathbf{G H z}$ in UV coordinates
pattern(sURA,fc,[-1.0:.01:1.0],[-1.0:.01:1.0],...
'CoordinateSystem','uv',...
'Type','directivity','PropagationSpeed', c)


## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \Pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as dBi . For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Convert plotResponse to pattern

For antenna, microphone, and array System objects, the pattern method replaces the plotResponse method. In addition, two new simplified methods exist just to draw 2-D azimuth and elevation pattern plots. These methods are the azimuthPattern and elevationPattern methods.

The following table is a guide for converting your code from using plotResponse to pattern. Notice that some of the inputs have changed from input arguments to Name-Value pairs and conversely. The general pattern method syntax is
pattern(H,FREQ,AZ,EL, 'Name1','Value1',...,'NameN', 'ValueN')

| plotResponse Inputs | plotResponse Description | pattern Inputs |
| :--- | :--- | :--- |
| H argument | Antenna, microphone, or array <br> System object. | H argument (no change) |
| FREQ argument | Operating frequency. | FREQ argument (no change) |
| V argument | Propagation speed. This argument <br> is used only for arrays. | 'PropagationSpeed ' name-value <br> pair. This parameter is only used for <br> arrays. |


| plotResponse Inputs | plotResponse Description |  | pattern Inputs |  |
| :---: | :---: | :---: | :---: | :---: |
| 'Format' and 'RespCut' namevalue pairs | These options work together to let you create a plot in angle space (line or polar style) or $U V$ space. They also determine whether the plot is 2-D or 3-D. This table shows you how to create different types of plots using plotResponse. |  | 'CoordinateSystem' name-value pair used together with the AZ and EL input arguments. <br> 'CoordinateSystem' has the same options as the plotResponse method 'Format ' name-value pair, except that ' line' is now named 'rectangular'. The table shows how to create different types of plots using pattern. |  |
|  | Display space |  |  |  |
|  | Angle space (2D) | Set 'RespCut' to 'Az' or 'El'. Set 'Format' to 'line' or 'polar'. |  |  |
|  |  |  | Display space |  |
|  |  | Set the display axis using either the 'AzimuthAngle s' or 'ElevationAng les ' namevalue pairs. | Angle space (2D) | Set <br> 'Coordinate System' to rectangular' or 'polar' Specify either AZ or EL as a scalar. |
|  |  |  | Angle space (3D) | Set 'Coordinate System' to 'rectangular' |
|  | Angle space (3D) | Set 'RespCut' to '3D'. Set 'Format' to 'line' or 'polar'. <br> Set the display axis using both the 'AzimuthAngle $s^{\prime}$ and 'Elevation Angles ' namevalue pairs. |  | or 'polar'. <br> Specify both AZ and EL as vectors. |
|  |  |  | UV space (2D) | Set Coordinate System' to 'uv '. Use AZ to specify a $U$ space vector. Use EL to specify a $V$-space scalar. |
|  |  |  | UV space (3D) | Set |
|  | UV space (2D) | Set 'RespCut' to'U'. Set 'Format ' to 'UV '. Set the display range using the 'UGrid' namevalue pair. |  | 'Coordinate <br> System' to 'uv'. Use AZ to specify a $U$ space vector. <br> Use EL to specify a $V$-space vector. |
|  |  |  | If you set CoordinateSystem to 'uv', enter the UV grid values using $A Z$ and $E L$. |  |
|  | UV space (3D) | $\begin{aligned} & \text { Set 'RespCut' } \\ & \text { to'3D'. Set } \\ & \text { 'Format' to } \end{aligned}$ |  |  |



| plotResponse Inputs | plotResponse Description | pattern Inputs |
| :--- | :--- | :--- |
| 'ElevationAngles ' name-value <br> pair | Elevation angles used to display the <br> antenna or array response. | EL argument |
| 'UGrid' name-value pair | Contains $U$ coordinates in $U V$ - <br> space. | AZ argument when <br> 'CoordinateSystem ' name-value <br> pair is set to ' uv ' |
| 'VGrid' name-value pair | Contains V-coordinates in $U V$-space. | EL argument when <br> 'CoordinateSystem ' name-value <br> pair is set to 'uv ' |

## Version History <br> Introduced in R2015a

See Also<br>patternAzimuth | patternElevation

## patternAzimuth

System object: phased.URA
Package: phased
Plot URA array directivity or pattern versus azimuth

## Syntax

```
patternAzimuth(sArray,FREQ)
patternAzimuth(sArray,FREQ,EL)
patternAzimuth(sArray,FREQ,EL,Name,Value)
PAT = patternAzimuth(
```

$\qquad$

``` )
```


## Description

patternAzimuth (sArray, FREQ) plots the 2-D array directivity pattern versus azimuth (in dBi) for the array sArray at zero degrees elevation angle. The argument FREQ specifies the operating frequency.

The integration used when computing array directivity has a minimum sampling grid of 0.1 degrees. If an array pattern has a beamwidth smaller than this, the directivity value will be inaccurate.
patternAzimuth(sArray, FREQ,EL), in addition, plots the 2-D array directivity pattern versus azimuth (in dBi) for the array sArray at the elevation angle specified by EL. When EL is a vector, multiple overlaid plots are created.
patternAzimuth(sArray, FREQ,EL,Name, Value) plots the array pattern with additional options specified by one or more Name, Value pair arguments.

PAT = patternAzimuth( $\qquad$ ) returns the array pattern. PAT is a matrix whose entries represent the pattern at corresponding sampling points specified by the 'Azimuth ' parameter and the EL input argument.

## Input Arguments

## sArray - Uniform rectangular array

System object
Uniform rectangular array, specified as a phased. URA System object.
Example: sArray= phased.URA;

## FREQ - Frequency for computing directivity and pattern

positive scalar
Frequency for computing directivity and pattern, specified as a positive scalar. Frequency units are in hertz.

- For an antenna or microphone element, FREQ must lie within the range of values specified by the FrequencyRange or the FrequencyVector property of the element. Otherwise, the element
produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased.CustomMic rophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: 1e8
Data Types: double

## EL - Elevation angles

## 1-by- $N$ real-valued row vector

Elevation angles for computing sensor or array directivities and patterns, specified as a 1-by- $N$ realvalued row vector. The quantity $N$ is the number of requested elevation directions. Angle units are in degrees. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

The elevation angle is the angle between the direction vector and the xy plane. When measured toward the $z$-axis, this angle is positive.
Example: [0, 10, 20]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Type - Displayed pattern type

'directivity' (default)|'efield'|'power'|'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb' - power pattern converted to dB.

Example: 'powerdb'
Data Types: char

## PropagationSpeed - Signal propagation speed

speed of light (default) | positive scalar
Signal propagation speed, specified as the comma-separated pair consisting of ' PropagationSpeed ' and a positive scalar in meters per second.
Example: 'PropagationSpeed', physconst('LightSpeed')
Data Types: double

## Weights - Array weights

M-by-1 complex-valued column vector
Array weights, specified as the comma-separated pair consisting of 'Weights' and an M-by-1 complex-valued column vector. Array weights are applied to the elements of the array to produce array steering, tapering, or both. The dimension $M$ is the number of elements in the array.

Note Use complex weights to steer the array response toward different directions. You can create weights using the phased. SteeringVector System object or you can compute your own weights. In general, you apply Hermitian conjugation before using weights in any Phased Array System Toolbox function or System object such as phased. Radiator or phased. Collector. However, for the directivity, pattern, patternAzimuth, and patternElevation methods of any array System object use the steering vector without conjugation.

Example: 'Weights', ones (10, 1)
Data Types: double
Complex Number Support: Yes

## Azimuth - Azimuth angles

[-180:180] (default) | 1-by-P real-valued row vector
Azimuth angles, specified as the comma-separated pair consisting of 'Azimuth' and a 1-by-P realvalued row vector. Azimuth angles define where the array pattern is calculated.

Example: 'Azimuth', [-90:2:90]
Data Types: double

## Parent - Handle to axis

scalar
Handle to the axes along which the array geometry is displayed specified as a scalar.

## Output Arguments

## PAT - Array directivity or pattern

L-by- $N$ real-valued matrix
Array directivity or pattern, returned as an $L$-by- $N$ real-valued matrix. The dimension $L$ is the number of azimuth values determined by the 'Azimuth' name-value pair argument. The dimension $N$ is the number of elevation angles, as determined by the EL input argument.

## Examples

## Azimuth Pattern of 5x7-Element URA Antenna Array

Create a 5 x 7 -element URA of short-dipole antenna elements operating at 1 GHz . Assume the elements are spaced one-half wavelength apart. Plot the array azimuth directivity patterns for two different elevation angles, 0 and 15 degrees. The patternAzimuth method always plots the array pattern in polar coordinates.

## Create the array

```
sSD = phased.ShortDipoleAntennaElement(...
    'FrequencyRange',[50e6,1000e6],...
    'AxisDirection','Z');
fc = 1e9;
c = physconst('LightSpeed');
lam = c/fc;
sURA = phased.URA('Element',sSD,...
    'Size',[5,7],...
    'ElementSpacing',0.5*lam);
```


## Display the pattern

Display the azimuth directivity pattern at 1 GHz in polar coordinates
patternAzimuth(sURA,fc,[0 15],...
'PropagationSpeed', c, ...
'Type','directivity')


Directivity (dBi), Broadside at $0.00^{\circ}$

## Display a subset of angles

You can plot a smaller range of azimuth angles by setting the Azimuth parameter.
patternAzimuth(sURA,fc,[0 15],...
'PropagationSpeed', c, ...
'Type', 'directivity',...
'Azimuth', [-45:45])


Directivity (dBi), Broadside at $0.00^{\circ}$

## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Version History

 Introduced in R2015a
## See Also

pattern| patternElevation

## patternElevation

System object: phased.URA
Package: phased
Plot URA array directivity or pattern versus elevation

## Syntax

```
patternElevation(sArray,FREQ)
patternElevation(sArray,FREQ,AZ)
patternElevation(sArray,FREQ,AZ,Name,Value)
PAT = patternElevation(
```

$\qquad$

``` )
```


## Description

patternElevation(sArray, FREQ) plots the 2-D array directivity pattern versus elevation (in dBi ) for the array sArray at zero degrees azimuth angle. When AZ is a vector, multiple overlaid plots are created. The argument FREQ specifies the operating frequency.

The integration used when computing array directivity has a minimum sampling grid of 0.1 degrees. If an array pattern has a beamwidth smaller than this, the directivity value will be inaccurate.
patternElevation(sArray, FREQ, AZ), in addition, plots the 2-D element directivity pattern versus elevation (in dBi ) at the azimuth angle specified by $A Z$. When $A Z$ is a vector, multiple overlaid plots are created.
patternElevation(sArray, FREQ,AZ,Name, Value) plots the array pattern with additional options specified by one or more Name, Value pair arguments.

PAT = patternElevation (__ ) returns the array pattern. PAT is a matrix whose entries represent the pattern at corresponding sampling points specified by the 'Elevation' parameter and the AZ input argument.

## Input Arguments

## sArray - Uniform rectangular array

System object
Uniform rectangular array, specified as a phased. URA System object.
Example: sArray= phased.URA;

## FREQ - Frequency for computing directivity and pattern

positive scalar
Frequency for computing directivity and pattern, specified as a positive scalar. Frequency units are in hertz.

- For an antenna or microphone element, FREQ must lie within the range of values specified by the FrequencyRange or the FrequencyVector property of the element. Otherwise, the element
produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased.CustomMic rophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: 1e8
Data Types: double

## AZ - Azimuth angles for computing directivity and pattern

1 -by- $N$ real-valued row vector
Azimuth angles for computing sensor or array directivities and patterns, specified as a 1 -by- $N$ realvalued row vector where $N$ is the number of desired azimuth directions. Angle units are in degrees. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the $x y$ plane. This angle is positive when measured from the $x$-axis toward the $y$-axis.
Example: [0,10, 20]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Type - Displayed pattern type

'directivity' (default)|'efield'|'power'|'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb' - power pattern converted to dB.

Example: 'powerdb'
Data Types: char

## PropagationSpeed - Signal propagation speed

speed of light (default) | positive scalar
Signal propagation speed, specified as the comma-separated pair consisting of ' PropagationSpeed ' and a positive scalar in meters per second.
Example: 'PropagationSpeed', physconst('LightSpeed')
Data Types: double

## Weights - Array weights

M-by-1 complex-valued column vector
Array weights, specified as the comma-separated pair consisting of 'Weights' and an $M$-by- 1 complex-valued column vector. Array weights are applied to the elements of the array to produce array steering, tapering, or both. The dimension $M$ is the number of elements in the array.

Note Use complex weights to steer the array response toward different directions. You can create weights using the phased. SteeringVector System object or you can compute your own weights. In general, you apply Hermitian conjugation before using weights in any Phased Array System Toolbox function or System object such as phased.Radiator or phased. Collector. However, for the directivity, pattern, patternAzimuth, and patternElevation methods of any array System object use the steering vector without conjugation.

Example: 'Weights' , ones (10,1)
Data Types: double
Complex Number Support: Yes

## Elevation - Elevation angles

[-90:90] (default) | 1-by-P real-valued row vector
Elevation angles, specified as the comma-separated pair consisting of 'Elevation' and a 1-by-P real-valued row vector. Elevation angles define where the array pattern is calculated.
Example: 'Elevation', [-90:2:90]
Data Types: double
Parent - Handle to axis
scalar
Handle to the axes along which the array geometry is displayed specified as a scalar.

## Output Arguments

## PAT - Array directivity or pattern

## L-by- $N$ real-valued matrix

Array directivity or pattern, returned as an $L$-by- $N$ real-valued matrix. The dimension $L$ is the number of elevation angles determined by the 'Elevation' name-value pair argument. The dimension $N$ is the number of azimuth angles determined by the AZ argument.

## Examples

## Elevation Pattern of 7x7-Element Acoustic URA

Create a 7x7-element URA of backbaffled omnidirectional transducer elements operating at 2 kHz . Assume the speed of sound in water is $1500 \mathrm{~m} / \mathrm{s}$. The elements are spaced less than one-half wavelength apart. Plot the array elevation directivity patterns for three different azimuth angles, -20 , 0 , and 15 degrees. The patternElevation method always plots the array pattern in polar coordinates.

## Create the array

element = phased.OmnidirectionalMicrophoneElement(...
'FrequencyRange', [20,3000], ...
'BackBaffled ',true);
fc = 1000;
c = 1500;
lam = c/fc;
array = phased.URA('Element',element,...
'Size',[7,7],...
'ElementSpacing',0.45*lam);

## Display the pattern

Display the azimuth directivity pattern at 1 GHz in polar coordinates.
patternElevation(array,fc,[-20, 0, 15],...
'PropagationSpeed', c, ...
'Type','directivity')


Directivity (dBi), Broadside at $0.00^{\circ}$

## Display a subset of elevation angles

You can plot a smaller range of elevation angles by setting the Elevation parameter.
patternElevation(array,fc,[-20, 0, 15],...
'PropagationSpeed', c, ...
'Type','directivity',...
'Elevation',[-45:45])


Directivity (dBi), Broadside at $0.00^{\circ}$

## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \Pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Version History

Introduced in R2015a

## See Also

pattern| patternAzimuth

## isPolarizationCapable

System object: phased. URA
Package: phased
Polarization capability

## Syntax

flag = isPolarizationCapable(h)

## Description

flag = isPolarizationCapable(h) returns a Boolean value, flag, indicating whether the array supports polarization. An array supports polarization if all of its constituent sensor elements support polarization.

## Input Arguments

## h - Uniform rectangular array

Uniform rectangular array specified as phased.URA System object.

## Output Arguments

## flag - Polarization-capability flag

Polarization-capability flag returned as a Boolean value, true, if the array supports polarization or, false, if it does not.

## Examples

## Short-Dipole URA Supports Polarization

Show that a URA array of phased. ShortDipoleAntennaElement short-dipole antenna elements supports polarization.

```
antenna = phased.ShortDipoleAntennaElement('FrequencyRange',[le9 10e9]);
array = phased.URA([3,2],'Element',antenna);
isPolarizationCapable(array)
ans = logical
    1
```

The returned value 1 shows that this array supports polarization.

## plotResponse

System object: phased.URA
Package: phased
Plot response pattern of array

## Syntax

plotResponse(H, FREQ, V)
plotResponse(H, FREQ, V, Name, Value)
hPlot = plotResponse( $\qquad$ )

## Description

plotResponse ( $\mathrm{H}, \mathrm{FREQ}, \mathrm{V}$ ) plots the array response pattern along the azimuth cut, where the elevation angle is 0 . The operating frequency is specified in FREQ. The propagation speed is specified in $V$.
plotResponse(H, FREQ, V,Name, Value) plots the array response with additional options specified by one or more Name, Value pair arguments.
hPlot = plotResponse( $\qquad$ ) returns handles of the lines or surface in the figure window, using any of the input arguments in the previous syntaxes.

## Input Arguments

## H

Array object

## FREQ

Operating frequency in Hertz specified as a scalar or 1-by-K row vector. Values must lie within the range specified by a property of H . That property is named FrequencyRange or FrequencyVector, depending on the type of element in the array. The element has no response at frequencies outside that range. If you set the 'RespCut ' property of $H$ to ' $3 D^{\prime}$ ' FREQ must be a scalar. When FREQ is a row vector, plotResponse draws multiple frequency responses on the same axes.

## V

Propagation speed in meters per second.

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## CutAngle

Cut angle as a scalar. This argument is applicable only when RespCut is ' Az ' or ' El '. If RespCut is 'Az', CutAngle must be between -90 and 90. If RespCut is ' El ' , CutAngle must be between -180 and 180.

Default: 0

## Format

Format of the plot, using one of 'Line', 'Polar', or 'UV '. If you set Format to 'UV ', FREQ must be a scalar.

## Default: 'Line'

## NormalizeResponse

Set this value to true to normalize the response pattern. Set this value to false to plot the response pattern without normalizing it. This parameter is not applicable when you set the Unit parameter value to 'dbi'.

## Default: true

## OverlayFreq

Set this value to true to overlay pattern cuts in a 2-D line plot. Set this value to false to plot pattern cuts against frequency in a 3-D waterfall plot. If this value is false, FREQ must be a vector with at least two entries.

This parameter applies only when Format is not 'Polar' and RespCut is not '3D '.

## Default: true

## Polarization

Specify the polarization options for plotting the array response pattern. The allowable values are |'None' | 'Combined' | 'H' | 'V' | where

- 'None' specifies plotting a nonpolarized response pattern
- 'Combined ' specifies plotting a combined polarization response pattern
- 'H' specifies plotting the horizontal polarization response pattern
- 'V ' specifies plotting the vertical polarization response pattern

For arrays that do not support polarization, the only allowed value is 'None'. This parameter is not applicable when you set the Unit parameter value to ' dbi ' .

Default: 'None'

## RespCut

Cut of the response. Valid values depend on Format, as follows:

- If Format is 'Line' or 'Polar', the valid values of RespCut are 'Az', 'El', and '3D'. The default is ' Az '.
- If Format is 'UV', the valid values of RespCut are 'U' and '3D'. The default is 'U'.

If you set RespCut to ' 3D' , FREQ must be a scalar.

## Unit

The unit of the plot. Valid values are 'db', 'mag', 'pow', or 'dbi'. This parameter determines the type of plot that is produced.

| Unit value | Plot type |
| :--- | :--- |
| db | power pattern in dB scale |
| mag | field pattern |
| pow | power pattern |
| dbi | directivity |

Default: 'db'

## Weights

Weight values applied to the array, specified as a length- $N$ column vector or $N$-by- $M$ matrix. The dimension $N$ is the number of elements in the array. The interpretation of $M$ depends upon whether the input argument FREQ is a scalar or row vector.

| Weights Dimensions | FREQ Dimension | Purpose |
| :--- | :--- | :--- |
| $N$-by-1 column vector | Scalar or 1-by-M row vector | Apply one set of weights for the <br> same single frequency or all $M$ <br> frequencies. |
| $N$-by- $M$ matrix | Scalar | Apply all of the $M$ different <br> columns in Weights for the <br> same single frequency. |
|  | 1-by- $M$ row vector | Apply each of the $M$ different <br> columns in Weights for the <br> corresponding frequency in <br> FREQ. |

## AzimuthAngles

Azimuth angles for plotting array response, specified as a row vector. The AzimuthAngles parameter sets the display range and resolution of azimuth angles for visualizing the radiation pattern. This parameter is allowed only when the RespCut parameter is set to 'Az' or '3D' and the Format parameter is set to 'Line' or 'Polar'. The values of azimuth angles should lie between $180^{\circ}$ and $180^{\circ}$ and must be in nondecreasing order. When you set the RespCut parameter to ' 3D ', you can set the AzimuthAngles and ElevationAngles parameters simultaneously.

Default: [-180:180]

## ElevationAngles

Elevation angles for plotting array response, specified as a row vector. The ElevationAngles parameter sets the display range and resolution of elevation angles for visualizing the radiation pattern. This parameter is allowed only when the RespCut parameter is set to ' El ' or ' 3 D ' and the

Format parameter is set to 'Line' or 'Polar'. The values of elevation angles should lie between $90^{\circ}$ and $90^{\circ}$ and must be in nondecreasing order. When yous set the RespCut parameter to ' 3 D ', you can set the ElevationAngles and AzimuthAngles parameters simultaneously.

## Default: [-90:90]

## UGrid

$U$ coordinate values for plotting array response, specified as a row vector. The UGrid parameter sets the display range and resolution of the $U$ coordinates for visualizing the radiation pattern in $U / V$ space. This parameter is allowed only when the Format parameter is set to 'UV' and the RespCut parameter is set to ' $U$ ' or ' $3 D$ '. The values of UGrid should be between -1 and 1 and should be specified in nondecreasing order. You can set the UGrid and VGrid parameters simultaneously.

Default: [-1:0.01:1]

## VGrid

$V$ coordinate values for plotting array response, specified as a row vector. The VGrid parameter sets the display range and resolution of the $V$ coordinates for visualizing the radiation pattern in $U / V$ space. This parameter is allowed only when the Format parameter is set to 'UV' and the RespCut parameter is set to ' $3 D^{\prime}$ '. The values of VGrid should be between -1 and 1 and should be specified in nondecreasing order. You can set VGrid and UGrid parameters simultaneously.

Default: [-1:0.01:1]

## Examples

## Azimuth Response of URA

This example shows how to construct a rectangular lattice 3-by-2 URA and plot that array's azimuth response.

```
ha = phased.URA('Size',[3 2]);
fc = 1e9;
c = physconst('LightSpeed');
plotResponse(ha,fc,c,'RespCut','Az','Format','Polar');
```



Normalized Power (dB), Broadside at $0.00^{\circ}$

## Array Response and Directivity of URA in U/V Space

This example shows how to construct a rectangular lattice 3-by-2 URA. Plot the $u$ cut of the array response in $u-v$ space.
ha = phased.URA('Size',[3 2]);
c = physconst('lightspeed');
plotResponse(ha,1e9, c, 'Format','UV');


Plot the directivity.
plotResponse(ha,le9,c,'Format','UV','Unit','dbi');


## Array Response of URA for Subrange of U-V Space

Construct a 5 -by- 5 square uniform rectangular array (URA) and then plot the 3D response in $u-v$ space. Restrict the $u-v$ range from -0.25 to 0.25 .
array $=$ phased.URA([5,5]);
fc = 500e6;
c = physconst('LightSpeed');
pattern(array,fc,[-0.25:.01:.25],[-0.25:.01:.25],'PropagationSpeed', c,'CoordinateSystem', 'uv')


## Array Response of URA with Two Sets of Weights

This example shows how to construct a square 5-by-5 URA array having elements spaced 0.3 meters apart. Apply both uniform weights and tapered weights at a single frequency using the Weights parameter. Choose the tapered weight values to be smallest at the edges and increasing towards the center. Then, show that the tapered weight set reduces the adjacent sidelobes while broadening the main lobe.

```
ha = phased.URA('Size',[5 5],'ElementSpacing',[0.3,0.3]);
fc = 1e9;
c = physconst('LightSpeed');
wts1 = ones(5,5);
wts1 = wts1(:);
wts1 = wts1/sum(wts1);
wts2 = 0.3*ones(5,5);
wts2(2:4,2:4) = 0.7;
wts2(3,3) = 1;
wts2 = wts2(:);
wts2 = wts2/sum(wts2);
plotResponse(ha,fc,c,'RespCut','Az','Format','Polar','Weights',[wts1,wts2]);
```



Normalized Power (dB), Broadside at $0.00^{\circ}$

## See Also

uv2azel|azel2uv

# plotGratingLobeDiagram 

System object: phased.URA
Package: phased
Plot grating lobe diagram of array

## Syntax

```
plotGratingLobeDiagram(H,FREQ)
plotGratingLobeDiagram(H,FREQ,ANGLE)
plotGratingLobeDiagram(H,FREQ,ANGLE,C)
plotGratingLobeDiagram(H,FREQ,ANGLE,C,F0)
hPlot = plotGratingLobeDiagram(
```

$\qquad$

## Description

plotGratingLobeDiagram ( $\mathrm{H}, \mathrm{FREQ}$ ) plots the grating lobe diagram of an array in the $u$ - $v$ coordinate system. The System object H specifies the array. The argument FREQ specifies the signal frequency and phase-shifter frequency. The array, by default, is steered to $0^{\circ}$ azimuth and $0^{\circ}$ elevation.

A grating lobe diagram displays the positions of the peaks of the narrowband array pattern. The array pattern depends only upon the geometry of the array and not upon the types of elements which make up the array. Visible and nonvisible grating lobes are displayed as open circles. Only grating lobe peaks near the location of the mainlobe are shown. The mainlobe itself is displayed as a filled circle.
plotGratingLobeDiagram ( $\mathrm{H}, \mathrm{FREQ}, \mathrm{ANGLE}$ ), in addition, specifies the array steering angle, ANGLE.
plotGratingLobeDiagram( $\mathrm{H}, \mathrm{FREQ}, \mathrm{ANGLE}, \mathrm{C}$ ), in addition, specifies the propagation speed by C.
plotGratingLobeDiagram(H,FREQ, ANGLE , C, F0) , in addition, specifies an array phase-shifter frequency, F0, that differs from the signal frequency, FREQ. This argument is useful when the signal no longer satisfies the narrowband assumption and, allows you to estimate the size of beam squint.
hPlot = plotGratingLobeDiagram( $\qquad$ ) returns the handle to the plot for any of the input syntax forms.

## Input Arguments

## H

Antenna or microphone array, specified as a System object.

## FREQ

Signal frequency, specified as a scalar. Frequency units are hertz. Values must lie within a range specified by the frequency property of the array elements contained in H .Element. The frequency property is named FrequencyRange or FrequencyVector, depending on the element type.


#### Abstract

ANGLE Array steering angle, specified as either a 2 -by- 1 vector or a scalar. If ANGLE is a vector, it takes the form [azimuth; elevation]. The azimuth angle must lie in the range $\left[-180^{\circ}, 180^{\circ}\right]$. The elevation angle must lie in the range $\left[-90^{\circ}, 90^{\circ}\right]$. All angle values are specified in degrees. If the argument ANGLE is a scalar, it specifies only the azimuth angle where the corresponding elevation angle is $0^{\circ}$.

Default: [0;0]

\section*{C}


Signal propagation speed, specified as a scalar. Units are meters per second.
Default: Speed of light in vacuum

## F0

Phase-shifter frequency of the array, specified as a scalar. Frequency units are hertz When this argument is omitted, the phase-shifter frequency is assumed to be the signal frequency, FREQ.

## Default: FREQ

## Examples

## Grating Lobe Diagram for Microphone URA

Plot the grating lobe diagram for an 11-by-9-element uniform rectangular array having element spacing equal to one-half wavelength.

Assume the operating frequency of the array is 10 kHz . All elements are omnidirectional microphone elements. Steer the array in the direction 20 degrees in azimuth and 30 degrees in elevation. The speed of sound in air is $344.21 \mathrm{~m} / \mathrm{s}$ at 21 deg C .

```
cair = 344.21;
f = 10.0e3;
lambda = cair/f;
microphone = phased.OmnidirectionalMicrophoneElement(...
    'FrequencyRange',[20 20000]);
array = phased.URA('Element',microphone,'Size',[11,9],...
    'ElementSpacing',0.5*lambda*[1,1]);
plotGratingLobeDiagram(array,f,[20;30],cair);
```



Plot the grating lobes. The main lobe of the array is indicated by a filled black circle. The grating lobes in visible and nonvisible regions are indicated by unfilled black circles. The visible region is the region in $u$-v coordinates for which $u^{2}+v^{2} \leq 1$. The visible region is shown as a unit circle centered at the origin. Because the array spacing is less than one-half wavelength, there are no grating lobes in the visible region of space. There are an infinite number of grating lobes in the nonvisible regions, but only those in the range $[-3,3]$ are shown.

The grating-lobe free region, shown in green, is the range of directions of the main lobe for which there are no grating lobes in the visible region. In this case, it coincides with the visible region.

The white areas of the diagram indicate a region where no grating lobes are possible.

## Create Grating Lobe Diagram for Undersampled Microphone URA

Plot the grating lobe diagram for an 11-by-9-element uniform rectangular array having element spacing greater than one-half wavelength. Grating lobes are plotted in $u$-v coordinates.

Assume the operating frequency of the array is 10 kHz and the spacing between elements is 0.75 of a wavelength. All elements are omnidirectional microphone elements. Steer the array in the direction 20 degrees in azimuth and 30 degrees in elevation. The speed of sound in air is $344.21 \mathrm{~m} / \mathrm{s}$ at 21 deg C.

```
cair = 344.21;
```

$\mathrm{f}=10000$;
lambda = cair/f;
sMic = phased.OmnidirectionalMicrophoneElement(...
'FrequencyRange',[20 20000]);
sURA = phased.URA('Element',sMic,'Size',[11,9],...
'ElementSpacing',0.75*lambda*[1,1]);
plotGratingLobeDiagram(sURA,f,[20;30],cair);


The main lobe of the array is indicated by a filled black circle. The grating lobes in visible and nonvisible regions are indicated by unfilled black circles. The visible region is the region in u-v coordinates for which $u^{2}+v^{2} \leq 1$. The visible region is shown as a unit circle centered at the origin. Because the array spacing is greater than one-half wavelength, there are grating lobes in the visible region of space. There are an infinite number of grating lobes in the nonvisible regions, but only those in the range $[-3,3]$ are shown.

The grating-lobe free region, shown in green, is the range of directions of the main lobe for which there are no grating lobes in the visible region. In this case, it lies inside the visible region. Because the mainlobe is outside the green area, there is a grating lobe within the visible region.

## Create Grating Lobe Diagram for Microphone URA with Frequency Shift

Plot the grating lobe diagram for an 11-by-9-element uniform rectangular array having element spacing greater than one-half wavelength. Apply a $20 \%$ phase-shifter frequency offset. Grating lobes are plotted in $u-v$ coordinates.

Assume the operating frequency of the array is 10 kHz and the spacing between elements is 0.75 of a wavelength. All elements are omnidirectional microphone elements. Steer the array in the direction 20 degrees in azimuth and 30 degrees in elevation. The shifted frequency is 12000 Hz . The speed of sound in air is $344.21 \mathrm{~m} / \mathrm{s}$ at 21 deg C .

```
cair = 344.21;
f = 10000;
f0 = 12000;
lambda = cair/f;
sMic = phased.OmnidirectionalMicrophoneElement(...
    'FrequencyRange',[20 20000]);
sURA = phased.URA('Element',sMic,'Size',[11,9],...
    'ElementSpacing',0.75*lambda*[1,1]);
plotGratingLobeDiagram(sURA,f,[20;30],cair,f0);
```



The mainlobe of the array is indicated by a filled black circle. The mainlobe has moved from its position in the previous example due to the frequency shift. The grating lobes in visible and nonvisible regions are indicated by unfilled black circles. The visible region is the region in $u-v$ coordinates for which $u^{2}+v^{2} \leq 1$. The visible region is shown as a unit circle centered at the origin. Because the array spacing is greater than one-half wavelength, there are grating lobes in the visible region of space. There are an infinite number of grating lobes in the nonvisible regions, but only those in the range $[-3,3]$ are shown.

The grating-lobe free region, shown in green, is the range of directions of the main lobe for which there are no grating lobes in the visible region. In this case, it lies inside the visible region. Because the mainlobe is outside the green area, there is a grating lobe within the visible region.

## Concepts

## Grating Lobes

Spatial undersampling of a wavefield by an array produces visible grating lobes. If you think of the wavenumber, $k$, as analogous to angular frequency, then you must sample the signal at spatial intervals smaller than $\Pi / k_{\max }$ (or $\lambda_{\min } / 2$ ) to remove aliasing. The appearance of visible grating lobes is also known as spatial aliasing. The variable $k_{\max }$ is the largest wavenumber value present in the signal.

The directions of maximum spatial response of a URA are determined by the peaks of the array pattern (alternatively called the beam pattern or array factor.) Peaks other than the main lobe peak are called grating lobes. For a URA, the array pattern depends only on the wavenumber component of the wavefield in the array plane (the $y$ and $z$ directions for the phased.URA System object). The wavenumber components are related to the look-direction of an arriving wavefield by $k_{y}=-2 \pi \sin a z$ $\cos e l / \lambda$ and $k_{z}=-2 \pi \sin \mathrm{el} / \lambda$. The angle $a z$ is azimuth angle of the arriving wavefield. The angle el is elevation angle of the arriving wavefield. The look-direction points away from the array to the wavefield source.

The array pattern possesses an infinite number of periodically spaced peaks that are equal in strength to the mainlobe peak. If you steer the array to the $a z_{0}, e l_{0}$ azimuth and elevation direction, the array pattern for the URA has its mainlobe peak at the wavenumber value, $k_{y 0}=-2 \pi \sin a z_{0} \cos$ $e l_{0} / \lambda, k_{z 0}=-2 \pi \sin e l_{/} / \lambda$. The array pattern has strong peaks at $k_{y m}=k_{y 0}+2 \pi \mathrm{~m} / d_{y}, k_{z n}=k_{z 0}+2 \pi n / d_{z}$ for integer values of $m$ and $n$. The quantities $d_{y}$ and $d_{z}$ are the inter-element spacings in the $y$ - and $z$ directions, respectively. Expressed in terms of direction cosines, the grating lobes occur at $u_{m}=u_{0}$ $m \lambda / d_{y}$ and $v_{n}=v_{0}-n \lambda / d_{z}$. The main lobe direction cosines are determined by $u_{0}=\sin a z_{0} \cos$ el $l_{0}$ and $v_{0}=\sin e l_{0}$ when expressed in terms of the look-direction.

Grating lobes can be visible or nonvisible, depending upon the value of $u_{m}{ }^{2}+v_{n}{ }^{2}$. When $u_{m}{ }^{2}+v_{n}{ }^{2} \leq 1$, the look direction represents a visible direction. When the value is greater than one, the grating lobe is non-visible. For each visible grating lobe, you can compute a look direction ( $a z_{m, n} e l_{m, n}$ ) from $u_{m}=$ $\sin a z_{m} \cos e l_{m}$ and $v_{n}=\sin e l_{n}$. The spacing of grating lobes depends upon $\lambda / d$. When $\lambda / d$ is small enough, multiple grating lobe peaks can correspond to physical look-directions.

## References

[1] Van Trees, H.L. Optimum Array Processing. New York: Wiley-Interscience, 2002.

## See Also

uv2azel|azel2uv

## step

System object: phased.URA
Package: phased
Output responses of array elements

## Syntax

RESP = step(H,FREQ,ANG)

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step (obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.

RESP $=$ step ( $\mathrm{H}, \mathrm{FREQ}, \mathrm{ANG}$ ) returns the responses of the array elements, RESP, at the operating frequencies specified in FREQ and directions specified in ANG.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## H

Array object

## FREQ

Operating frequencies of array in hertz. FREQ is a row vector of length $L$. Typical values are within the range specified by a property of H . Element. That property is named FrequencyRange or FrequencyVector, depending on the type of element in the array. The element has zero response at frequencies outside that range.

## ANG

Directions in degrees. ANG is either a 2 -by- $M$ matrix or a row vector of length $M$.
If ANG is a 2 -by-M matrix, each column of the matrix specifies the direction in the form [azimuth; elevation]. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive.

If ANG is a row vector of length $M$, each element specifies the azimuth angle of the direction. In this case, the corresponding elevation angle is assumed to be $0^{\circ}$.

## Output Arguments

## RESP

Voltage responses of the phased array. The output depends on whether the array supports polarization or not.

- If the array is not capable of supporting polarization, the voltage response, RESP, has the dimensions $N$-by- $M$-by- $L$. $N$ is the number of elements in the array. The dimension $M$ is the number of angles specified in ANG. $L$ is the number of frequencies specified in FREQ. For any element, the columns of RESP contain the responses of the array elements for the corresponding direction specified in ANG. Each of the $L$ pages of RESP contains the responses of the array elements for the corresponding frequency specified in FREQ.
- If the array is capable of supporting polarization, the voltage response, RESP, is a MATLAB struct containing two fields, RESP.H and RESP.V. The field, RESP.H, represents the array's horizontal polarization response, while RESP.V represents the array's vertical polarization response. Each field has the dimensions $N$-by- $M$-by-L. $N$ is the number of elements in the array, and $M$ is the number of angles specified in ANG. $L$ is the number of frequencies specified in FREQ. Each column of RESP contains the responses of the array elements for the corresponding direction specified in ANG. Each of the $L$ pages of RESP contains the responses of the array elements for the corresponding frequency specified in FREQ.


## Examples

## Response of 2-by-2 URA of Short-Dipole Antennas

Construct a 2-by-2 rectangular lattice URA of short-dipole antenna elements. Then, find the response of each element at boresight. Assume the operating frequency is 1 GHz .

```
sSD = phased.ShortDipoleAntennaElement;
sURA = phased.URA('Element',sSD,'Size',[2 2]);
fc = 1e9;
ang = [0;0];
resp = step(sURA,fc,ang);
disp(resp.V)
    -1.2247
    -1.2247
    -1.2247
    -1.2247
```


## See Also

uv2azel|phitheta2azel

## viewArray

System object: phased. URA
Package: phased
View array geometry

## Syntax

```
viewArray(H)
viewArray(H,Name,Value)
hPlot = viewArray(
```

$\qquad$

``` )
```


## Description

viewArray (H) plots the geometry of the array specified in H .
viewArray ( $\mathrm{H}, \mathrm{Name}$, Value) plots the geometry of the array, with additional options specified by one or more Name, Value pair arguments.
hPlot = viewArray( $\qquad$ ) returns the handle of the array elements in the figure window. All input arguments described for the previous syntaxes also apply here.

## Input Arguments

## H

Array object.

## Name-Value Pair Arguments

Specify optional pairs of arguments as Namel=Value1, . . . ,NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Parent

Handle to the axes along which the array geometry is displayed.

## ShowNormals

Set this value to true to show the normal directions of all elements of the array. Set this value to false to plot the elements without showing normal directions.

Default: false

## ShowLocalCoordinates

Logical flag specifying whether to show the local coordinate axes.

Default: true

## ShowAnnotation

Logical flag specifying whether to show the annotations in the UI panel of the figure. Annotation shows aperture size and element spacing based on array axis of array.

Default: true

## Orientation

Orientation of the array, specified as a 3-by-1 column vector containing the rotation angles with respect to the $\mathrm{x}-, \mathrm{y}$-, and z -axes of the local coordinate system, respectively. The default value is [0;0;0].

Default: [0;0;0]

## ShowTaper

Set this value to true to specify whether to change the element color brightness in proportion to the element taper magnitude. When this value is set to false, all elements are drawn with the same color.

Default: false

## ShowIndex

Vector specifying the element indices to show in the figure. Each number in the vector must be an integer between 1 and the number of elements. You can also specify the value ' All ' to show the indices of all elements of the array or 'None' to suppress indices.

Default: 'None'

## Title

Character vector specifying the title of the plot.
Default: 'Array Geometry'

## Output Arguments

## hPlot

Handle of array elements in figure window.

## Examples

## Geometry, Normal Directions, and Indices of URA Elements

This example shows how to display the element positions, normal directions, and indices for all elements of a 4 -by- 4 square URA.

```
ha = phased.URA(4);
viewArray(ha,'ShowNormals',true,'ShowIndex','All');
```



## See Also

phased.ArrayResponse

## Topics

"Phased Array Gallery"

# phased.WidebandBackscatterRadarTarget 

Package: phased
Backscatter wideband signal from radar target

## Description

The phased.WidebandBackscatterRadarTarget System object models backscattering of a wideband signal from a target. Backscattering is a special case of radar target scattering where the incident and reflected angles are the same. Use this object for monostatic radar configurations. The radar cross-section determines the backscattering response of a target to an incoming signal. This System object lets you specify an angle-dependent radar cross-section model that covers a range of incident angles. The wideband signal is decomposed into frequency subbands which are backscattered independently and then recombined.

This System object creates a backscattered signal for polarized or nonpolarized signals. Although electromagnetic radar signals are polarized, you can often ignore polarization in your simulation and process the signals as scalars. To ignore polarization, specify the EnablePolarization property as false. To employ polarization, specify EnablePolarization as true.

For nonpolarized signals, specify the radar cross section (RCS) as an array of values at discrete azimuth and elevation angles and discrete frequencies. The System object interpolates values for incident angles between array points. For polarized signals, specify the radar scattering matrix (SCM) using three arrays defined at discrete azimuth and elevation angles and discrete frequencies. These three arrays correspond to the $H H, H V$, and $V V$ polarization components. The $V H$ component is computed by applying the conjugate symmetry property of the $H V$ component. $H$ and $V$ stand for the horizontal and vertical polarization components, respectively.

For both nonpolarized and polarized signals, you can employ one of four Swerling models to generate random fluctuations in the RCS or radar scattering matrix. Choose the model using the Model property. Then, use the SeedSource and Seed properties to randomize the fluctuations.

| EnablePolarization | Radar cross-section patterns |
| :--- | :--- |
| false | RCSPattern |
| true | ShhPattern, SvvPattern, and ShvPattern |

To perform wideband target backscattering:
1 Create the phased.WidebandBackscatterRadarTarget object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

target = phased.WidebandBackscatterRadarTarget
target = phased.WidebandBackscatterRadarTarget(Name,Value)
Description
target $=$ phased.WidebandBackscatterRadarTarget creates a wideband backscatter radar target System object, .
target $=$ phased.WidebandBackscatterRadarTarget (Name, Value) creates a wideband backscatter radar target object, with each specified property Name set to the specified Value. You can specify additional name and value pair arguments in any order as
(Name1, Value1,...,NameN, ValueN).

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## EnablePolarization - Enable polarized signals <br> false (default)| true

Option to enable processing of polarized signals, specified as false or true. Set this property to true to allow the target to simulate the reflection of polarized radiation. Set this property to false to ignore polarization.

## Example: true

## FrequencyVector - Wideband backscatter pattern frequencies

[0,1e20] (default) | real-valued row vector in strictly increasing order
Specify the wideband backscatter pattern frequencies used in the RCS or SCM matrices. The elements of this vector must be in strictly increasing order. The target has no response outside this frequency range. Frequencies are defined with respect to the physical frequency band, not the baseband. Frequency units are in hertz.

## Example: [1e3,1e10]

## AzimuthAngles - Azimuth angles

[-180:180] (default) | 1-by-P real-valued row vector | $P$-by-1 real-valued column vector
Azimuth angles used to define the angular coordinates of each column of the matrices specified by the RCSPattern, ShhPattern, ShvPattern, or SvvPattern properties. Specify the azimuth angles as a length $P$ vector. $P$ must be greater than two. Angle units are in degrees.
Example: [-45:0.1:45]
Data Types: double

## ElevationAngles - Elevation angles

[-90:90] (default) | 1-by-Q real-valued row vector | $Q$-by-1 real-valued column vector

Elevation angles used to define the angular coordinates of each row of the matrices specified by the RCSPattern, ShhPattern, ShvPattern, or SvvPattern properties. Specify the elevation angles as a length $Q$ vector. $Q$ must be greater than two. Angle units are in degrees.

Example: [-30:0.1:30]
Data Types: double

## RCSPattern - Radar cross-section pattern

ones (181, 361) (default) | Q-by-P real-valued matrix | Q-by-P-by-K real-valued array | 1-by-P-by-K real-valued array | K-by-P real-valued matrix

Radar cross-section pattern, specified as a real-valued matrix or array.

| Dimensions | Application |
| :--- | :--- |
| $Q$-by- $P$ matrix | Specifies a matrix of RCS values as a function of <br> $Q$ elevation angles and $P$ azimuth angles. The <br> same RCS matrix is used for all frequencies. |
| $Q$-by- $P$-by- $K$ array | Specifies an array of RCS patterns as a function <br> of $Q$ elevation angles, $P$ azimuth angles, and $K$ <br> frequencies. If $K=1$, the RCS pattern is <br> equivalent to a $Q$-by- $P$ matrix. |
| 1-by- $P$-by- $K$ array | Specifies a matrix of RCS values as a function of <br> $P$ azimuth angles and $K$ frequencies. These <br> dimension formats apply when there is only one <br> elevation angle. |
| $K$-by- $P$ matrix |  |

- $Q$ is the length of the vector specified by the ElevationAngles property.
- $P$ is the length of the vector specified by the AzimuthAngles property.
- $K$ is the number of frequencies specified by the FrequencyVector property.

You can specify patterns for $L$ targets by putting $L$ patterns into a cell array. All patterns must have the same dimensions. The value of $L$ must match the column dimensions of the signals passed as input into the function. However, you can use one pattern to model $L$ targets.

RCS units are in square meters.
Example: [1,1;1,1]

## Dependencies

To enable this property, set the EnablePolarization property to false.
Data Types: double
ShhPattern - Radar scattering matrix HH polarization component
ones (181, 361) (default) | Q-by-P complex-valued matrix | Q-by-P-by-K complex-valued array | 1-by-$P$-by-K complex-valued array $\mid K$-by- $P$ complex-valued matrix

Radar scattering matrix (SCM) HH polarization component, specified as a complex-valued matrix or array.

| Dimensions | Application |
| :--- | :--- |
| $Q$-by- $P$ matrix | Specifies the scattering matrix polarization <br> component as a function of $Q$ elevation angles <br> and $P$ azimuth angles. The same SCM matrix is <br> used for all frequencies. |
| $Q$-by- $P$-by- $K$ array | Specifies the scattering matrix polarization <br> component as a function of $Q$ elevation angles, $P$ <br> azimuth angles, and $K$ frequencies. If $K=1$, the <br> RCS pattern is equivalent to a $Q$-by- $P$ matrix. |
| 1-by- $P$-by- $K$ array | Specifies the scattering matrix polarization <br> component as a function of $P$ azimuth angles and <br> $K$ frequencies. These dimension formats apply <br> when there is only one elevation angle. |
| K-by- $P$ matrix |  |

- $Q$ is the length of the vector specified by the ElevationAngles property.
- $\quad P$ is the length of the vector specified by the AzimuthAngles property.
- $K$ is the number of frequencies specified by the FrequencyVector property.

You can specify polarization component patterns for $L$ targets by putting $L$ patterns into a cell array. All patterns must have the same dimensions. The value of $L$ must match the column dimensions of the signals passed as input into the function. You can, however, use one pattern to model $L$ targets.

SCM units are in square-meters.
Example: [1,1;1i,1i]

## Dependencies

To enable this property, set the EnablePolarization property to true.
Data Types: double
Complex Number Support: Yes

## SvvPattern - Radar scattering matrix VV polarization component

ones $(181,361)$ (default) | $Q$-by- $P$ complex-valued matrix | $Q$-by- $P$-by- $K$ complex-valued array | 1-by-$P$-by- $K$ complex-valued array | $K$-by- $P$ complex-valued matrix

Radar scattering matrix VV-pol component, specified as a complex-valued vector, matrix, or array. Different dimension cases have different applications.

| Dimensions | Application |
| :--- | :--- |
| $Q$-by- $P$ matrix | Specifies the scattering matrix polarization <br> component as a function of $Q$ elevation angles <br> and $P$ azimuth angles. The same SCM matrix is <br> used for all frequencies. |
| $Q$-by- $P$-by- $K$ array | Specifies the scattering matrix polarization <br> component as a function of $Q$ elevation angles, $P$ <br> azimuth angles, and $K$ frequencies. If $K=1$, , the <br> RCS pattern is equivalent to a $Q$-by- $P$ matrix. |
| 1-by- $P$-by- $K$ array | Specifies the scattering matrix polarization <br> component as a function of $P$ azimuth angles and |

## Dimensions

$K$-by- $P$ matrix

## Application

$K$ frequencies. These dimension formats apply when there is only one elevation angle.

- $Q$ is the length of the vector specified by the ElevationAngles property.
- $P$ is the length of the vector specified by the AzimuthAngles property.
- $K$ is the number of frequencies specified by the FrequencyVector property.

You can specify polarization component patterns for $L$ targets by putting $L$ patterns into a cell array. All patterns must have the same dimensions. The value of $L$ must match the column dimensions of the signals passed as input into the function. You can, however, use one pattern to model $L$ targets.

SCM units are in square-meters.
Example: [1,1;1i,1i]

## Dependencies

To enable this property, set the EnablePolarization property to true.
Data Types: double
Complex Number Support: Yes
ShvPattern - Radar scattering matrix HV polarization component
ones $(181,361)$ (default) | $Q$-by- $P$ complex-valued matrix | $Q$-by- $P$-by-K complex-valued array | 1-by-$P$-by-K complex-valued vector | $K$-by- $P$ complex-valued matrix

Radar scattering matrix (SCM) HV-pol component, specified as a complex-valued vector, matrix, or array. Different dimension cases have different applications.

| Dimensions | Application |
| :--- | :--- |
| $Q$-by- $P$ matrix | Specifies the scattering matrix polarization <br> component as a function of $Q$ elevation angles <br> and $P$ azimuth angles. The same SCM matrix is <br> used for all frequencies. |
| $Q$-by- $P$-by- $K$ array | Specifies the scattering matrix polarization <br> component as a function of $Q$ elevation angles, $P$ <br> azimuth angles, and $K$ frequencies. If $K=1$, the <br> RCS pattern is equivalent to a $Q$-by- $P$ matrix. |
| 1 -by- $P$-by- $K$ array | Specifies the scattering matrix polarization <br> component as a function of $P$ azimuth angles and <br> $K$ frequencies. These dimension formats apply <br> when there is only one elevation angle. |
| $K$-by- $P$ matrix |  |

- $Q$ is the length of the vector specified by the ElevationAngles property.
- $P$ is the length of the vector specified by the AzimuthAngles property.
- $K$ is the number of frequencies specified by the FrequencyVector property.

You can specify polarization component patterns for $L$ targets by putting $L$ patterns into a cell array. All patterns must have the same dimensions. The value of $L$ must match the column dimensions of the signals passed as input into the function. You can, however, use one pattern to model $L$ targets.

SCM units are in square-meters.

Example: [1,1;1i,1i]

## Dependencies

To enable this property, set the EnablePolarization property to true.
Data Types: double
Complex Number Support: Yes

## Model - Target fluctuation model

'Nonfluctuating' (default)|'Swerling1'| 'Swerling2' | 'Swerling3'|'Swerling4'
Target fluctuation model, specified as 'Nonfluctuating', 'Swerling1', 'Swerling2', 'Swerling3', or 'Swerling4'. If you set this property to a value other than 'Nonfluctuating', use the update input argument when calling the function.

Example: 'Swerling3'
Data Types: char

## PropagationSpeed - Signal propagation speed

physconst('LightSpeed') (default)| positive scalar
Signal propagation speed, specified as a positive scalar. Units are in meters per second. The default propagation speed is the value returned by physconst('LightSpeed'). See physconst for more information.

Example: 3e8
Data Types: double

## OperatingFrequency - Operating frequency

300e6 (default) | positive scalar
Operating frequency, specified as a positive scalar. Units are in Hz.
Example: 1e9
Data Types: double

## SampleRate - Signal sample rate

le6 (default) | positive real-valued scalar
Signal sample rate, specified as a positive real-valued scalar. Units are in hertz.
Example: 1e6
Data Types: double

## NumSubbands - Number of processing subbands

64 (default) | positive integer
Number of processing subbands, specified as a positive integer.
Example: 128
Data Types: double

## SeedSource - Seed source of random number generator for RCS fluctuation model 'Auto' (default)|'Property'

Seed source of random number generator for RCS fluctuation model, specified as 'Auto ' or 'Property'. When you set this property to:

- 'Auto ', the object generates random numbers using the default MATLAB random number generator.
- 'Property ', you specify the random number generator seed using the Seed property.

When using this object with Parallel Computing Toolbox software, set this property to 'Auto '.
Dependencies
To enable this property, set the Model property to 'Swerling1', 'Swerling2', 'Swerling3', or
'Swerling4'.
Data Types: string

## Seed - Random number generator seed

0 (default) | nonnegative integer less than $2^{32}$
Random number generator seed, specified as a nonnegative integer less than $2^{32}$. .
Example: 32301

## Dependencies

To enable this property, set the SeedSource property to 'Property '.
Data Types: double

## Usage

## Syntax

refl_sig = target(sig,ang)
refl_sig = target(sig, ang, update)
refl_sig = target(sig,ang,laxes)
refl_sig = target(sig,ang,laxes,update)

## Description

refl_sig = target(sig,ang) returns the reflected signal, refl_sig, of an incident nonpolarized signal, sig. This syntax applies when you set the EnablePolarization property to false and the Model property to 'Nonfluctuating '. In this case, the values specified in the RCSPattern property are used to compute the RCS values for the incident and reflected directions, ang.
refl_sig = target(sig,ang, update) uses update to control whether to update the RCS values. This syntax applies when you set the EnablePolarization property to false and the Model property to one of the fluctuating RCS models: 'Swerling1', 'Swerling2', 'Swerling3', or 'Swerling4'. If update is true, a new RCS value is generated. If update is false, the previous RCS value is used.
refl_sig = target(sig,ang,laxes) returns the reflected signal, refl_sig, of an incident polarized signal, sig. This syntax applies when you set EnablePolarization to true and the

Model property to 'Nonfluctuating'. The values specified in the ShhPattern, SvvPattern, and ShvPattern properties are used to compute the backscattering matrices for the incident directions, ang. The laxes argument specifies a local coordinate system used to define the horizontal and vertical polarization components.
refl_sig = target(sig, ang,laxes, update) uses the update argument to control whether to update the scattering matrix values. This syntax applies when you set the EnablePolarization property to true and the Model property to one of the fluctuating RCS models: 'Swerling1', 'Swerling2', 'Swerling3', or 'Swerling4'. If update is true, a new RCS value is generated. If update is false, the previous RCS value is used.

## Input Arguments

## sig - Wideband signal

$N$-by-M complex-valued matrix | 1 -by- $M$ struct array containing complex-valued fields

- Wideband nonpolarized signal, specified as an $N$-by- $M$ complex-valued matrix. The quantity $N$ is the number of signal samples and $M$ is the number of independent signals reflecting off the target. Each column contains an independent signal reflected from the target.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

- Wideband polarized signal, specified as a 1 -by-M struct array containing complex-valued fields. Each struct element contains three $N$-by- 1 column vectors of electromagnetic field components (sig.X, sig.Y, sig.Z) representing the polarized signal that reflects from the target. Each struct element contains three $N$-by-1 complex-valued column vectors, sig. X , sig. Y , and sig. $Z$. These vectors represent the $x, y$, and $z$ Cartesian components of the polarized signal.

The size of the first dimension of the matrix fields within the struct can vary to simulate a changing signal length such as a pulse waveform with variable pulse repetition frequency.

Example: [1,1;j,1;0.5,0]
Data Types: double
Complex Number Support: Yes

## ang - Incident signal direction

2 -by-1 real-valued column vector | 2 -by- $M$ real-valued matrix
Incident signal direction, specified as a real-valued column 2-by-1 vector or 2-by-M matrix. Each column of ang specifies the incident direction of the corresponding signal in the form [AzimuthAngle;ElevationAngle]. The number of columns in ang must match the number of independent signals in sig. Units are in degrees.
Example: [30;45]
Data Types: double

## update - Update RCS

false (default) | true
Option to enable the RCS values for fluctuation models to update, specified as false or true. When update is true, a new RCS value is generated with each call to the function. If update is false, the RCS remains unchanged with each call to the function.

## Data Types: logical

## Laxes - Local coordinate matrix

## eye (3,3) (default) | 3-by-3 real-valued orthonormal matrix | 3-by-3-by-M real-valued array

Local coordinate system matrix, specified as a 3-by-3 real-valued orthonormal matrix or a 3-by-3-by-M real-valued array. The matrix columns specify the local coordinate system orthonormal $x$-axis, $y$-axis, and $z$-axis, respectively. Each axis is a vector of the form ( $x ; y ; z$ ) with respect to the global coordinate system. When sig has only one signal, laxes is a 3 -by- 3 matrix. When sig has multiple signals, you can use a single 3-by-3 matrix for multiple signals in sig. In this case, all targets have the same local coordinate systems. When you specify laxes as a 3-by-3-by-M array, each page (third index) defines a 3-by-3 local coordinate matrix for the corresponding target.

Example: [1,0,0;0,0.7071,-0.7071;0,0.7071,0.7071]
Data Types: double

## Output Arguments

## refl_sig - Wideband reflected signal

$N$-by- $M$ complex-valued matrix | 1 -by- $M$ struct array containing complex-valued fields

- Wideband nonpolarized signal, returned as an $N$-by- $M$ complex-valued matrix. Each column contains an independent signal reflected from the target.
- Wideband polarized signal, returned as a $1-$ by-M struct array containing complex-valued fields. Each struct element contains three $N$-by- 1 column vectors of electromagnetic field components (sig.X, sig.Y, sig.Z) representing the polarized signal that reflects from the target.

The quantity $N$ is the number of signal samples and $M$ is the number of signals reflecting off the target. Each column corresponds to a reflecting angle.

For polarized fields, the struct element contains three $N$-by- 1 complex-valued column vectors: sig.X, sig.Y, and sig.Z. These vectors represent the $x, y$, and $z$ Cartesian components of the polarized signal.

The output refl_sig contains signal samples arriving at the signal destination within the current input time frame. When the propagation time from source to destination exceeds the current time frame duration, the output does not contain all contributions from the input of the current time frame. The remaining output appears in the next call to the function.

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```


## Common to All System Objects

| step | Run System object algorithm <br> release |
| :--- | :--- |
| Release resources and allow changes to System object property values and input <br> characteristics |  |
| reset | Reset internal states of System object |

## Examples

## Backscatter Nonpolarized Wideband Signal

Calculate the reflected radar signal from a nonfluctuating point target having a peak RCS of 10.0 $\mathrm{m} \wedge 2$. Use a simple target RCS pattern for illustrative purposes. Real RCS patterns are more complicated. The RCS pattern covers a range of angles from 10-30 degrees in azimuth and 5-15 degrees in elevation. The RCS peaks at 20 degrees azimuth and 10 degrees elevation. The RCS also has a frequency dependence and is specified at 5 frequencies within the signal bandwidth. Assume that the radar operating frequency is 100 MHz and that the signal is a linear FM waveform having a 20 MHz bandwidth.

Create and plot the wideband signal.

```
c = physconst('LightSpeed');
fs = 50e6;
pw = 20e-6;
PRF = 1/(2*pw);
fc = 100e6;
bw = 20e6;
waveform = phased.LinearFMWaveform('SampleRate',fs,'PulseWidth',pw, ...
    'PRF',PRF,'OutputFormat','Pulses','NumPulses',1,'SweepBandwidth',bw, ...
    'SweepDirection','Down','Envelope','Rectangular','SweepInterval', ...
    'Symmetric');
wav = waveform();
n = size(wav,1);
plot([0:(n-1)]/fs*1e6,real(wav),'b')
xlabel('Time (\mu s)')
ylabel('Waveform Magnitude')
grid
```



Create an RCS pattern at five different frequencies within the signal bandwidth using a simplified frequency dependence. The frequency dependence is unity at the operating frequency and falls off outside that frequency. Realistic frequency dependencies are more complicated. Plot the RCS pattern for one of the frequencies.

```
fvec = fc + [-fs/2,-fs/4,0,fs/4,fs/2];
fdep = cos(3*(1 - fvec/fc));
azmax = 20.0;
elmax = 10.0;
azpattern = [10.0:0.5:30.0];
elpattern = [5.0:0.5:15.0];
rcspattern0 = 10.0*cosd(4*(elpattern - elmax))'*cosd(4*(azpattern - azmax));
for k = 1:5
    rcspattern(:,:,k) = rcspattern0*fdep(k);
end
imagesc(azpattern,elpattern,abs(rcspattern(:,:,1)))
axis image
axis tight
title('RCS')
xlabel('Azimuth (deg)')
ylabel('Elevation (deg)')
```



Create the phased.WidebandBackscatterRadarTarget System object ${ }^{\mathrm{TM}}$.

```
target = phased.WidebandBackscatterRadarTarget('Model','Nonfluctuating', ...
    'AzimuthAngles',azpattern,'ElevationAngles',elpattern,...
    'RCSPattern',rcspattern,'OperatingFrequency',fc,'NumSubbands',32, ...
    'FrequencyVector',fvec);
```

For a sequence of incident azimuth angles at constant elevation, find and plot the reflected signal amplitude.

```
az0 = 13.0;
el = 10.0;
az = az0 + [0:2:20];
naz = length(az);
magsig = zeros(1,naz);
for k = 1:naz
    y = target(wav,[az(k);el]);
    magsig(k) = max(abs(y));
end
plot(az,magsig,'r.')
xlabel('Azimuth (deg)')
ylabel('Scattered Signal Amplitude')
grid
```



## Backscatter Nonpolarized Wideband Signal from Fluctuating Target

Calculate the reflected radar signal from a Swerling 4 fluctuating point target with a peak RCS of 0.1 $\mathrm{m} \wedge 2$. Use a simple target RCS pattern for illustrative purposes. Real RCS patterns are more complicated. The RCS pattern covers a range of angles from $10-30$ degrees in azimuth and 5-15 degrees in elevation. The RCS peaks at 20 degrees in azimuth and 10 degrees in elevation at a value of $0.1 \mathrm{~m}^{\wedge} 2$. The RCS also has a frequency dependence and is specified at five frequencies within the signal bandwidth. Assume that the radar operating frequency is 100 MHz and that the signal is a linear FM waveform with a 20 MHz bandwidth. The sampling frequency is 50 MHz .

Create and plot the wideband signal.

```
c = physconst('LightSpeed');
fs = 50e6;
pw = 20e-6;
PRF = 1/(2*pw);
fc = 100.0e6;
bw = 20.0e6;
waveform = phased.LinearFMWaveform('SampleRate',fs,'PulseWidth',pw, ...
    'PRF',PRF,'OutputFormat','Pulses','NumPulses',1,'SweepBandwidth',bw, ...
    'SweepDirection','Down','Envelope','Rectangular','SweepInterval', ...
    'Symmetric');
wav = waveform();
```

Create an RCS pattern at five different frequencies within the signal bandwidth using a simple frequency dependence. The frequency dependence is designed to be unity at the operating frequency and fall off outside that band. Realistic frequency dependencies are more complicated.

```
fvec = fc + [-fs/2,-fs/4,0,fs/4,fs/2];
fdep = cos(3*(1 - fvec/fc));
azmax = 20.0;
elmax = 10.0;
azangs = [10.0:0.5:30.0];
elangs = [5.0:0.5:15.0];
rcspattern0 = 0.1*(cosd((elangs - elmax))'*cosd((azangs - azmax))).^2;
for k = 1:5
    rcspattern(:,:,k) = rcspattern0*fdep(k);
end
imagesc(azangs,elangs,abs(rcspattern(:,:,5)))
axis image
axis xy
axis tight
title('RCS')
xlabel('Azimuth (deg)')
ylabel('Elevation (deg)')
colorbar
```



Create the phased.WidebandBackscatterRadarTarget System object ${ }^{\mathrm{TM}}$.
target = phased.WidebandBackscatterRadarTarget('Model','Swerling4', ...
'SeedSource','Property','Seed',100213,'AzimuthAngles', azangs, ...

```
'ElevationAngles',elangs,'RCSPattern',rcspattern, ...
'OperatingFrequency',fc,'NumSubbands',32,'FrequencyVector',fvec);
```

Find and plot 100 samples of the incident signal and two sequential reflected signals at 10 degrees in azimuth and 10 degrees in elevation. Update the RCS at each execution of the System object ${ }^{\mathrm{TM}}$.
az $=10.0 ;$
el = 10.0;
refl_wav1 = target(wav,[az;el],true);
refl-wav2 = target(wav,[az;el],true);
$\mathrm{n}=100$;
plot([0:(n-1)]/fs*1e6, real(wav(1:n)))
hold on
plot([0:(n-1)]/fs*1e6, real(refl_wav1(1:n)),'.')
plot([0:(n-1)]/fs*1e6, real(refl_wav2(1:n)),'.')
hold off
legend('Incident Signal','First Backscattered Signal','Second Backscattered Signal') xlabel('Time (\mu s)')
ylabel('Waveform Magnitude')
title('Swerling 4 RCS')


## More About

## Backscattered Wideband Signals

Wideband signals are decomposed into narrowband signals which are reflected from the target independently.

For a narrowband nonpolarized signal, the reflected signal, $Y$, is

$$
Y=\sqrt{G} \cdot X,
$$

where:

- $X$ is the incoming signal.
- $G$ is the target gain factor, a dimensionless quantity given by

$$
G=\frac{4 \pi \sigma}{\lambda^{2}} .
$$

- $\sigma$ is the mean radar cross-section (RCS) of the target.
- $\lambda$ is the wavelength of the incoming signal.

The incident signal on the target is scaled by the square root of the gain factor.
For narrowband polarized waves, the single scalar signal, $X$, is replaced by a vector signal, $\left(E_{H}, E_{V}\right)$, with horizontal and vertical components. The scattering matrix, $S$, replaces the scalar cross-section, $\sigma$. Through the scattering matrix, the incident horizontal and vertical polarized signals are converted into the reflected horizontal and vertical polarized signals.

$$
\left[\begin{array}{l}
E_{H}^{(s c a t)} \\
E_{V}^{(s c a t)}
\end{array}\right]=\sqrt{\frac{4 \pi}{\lambda^{2}}}\left[\begin{array}{ll}
S_{H H} & S_{V H} \\
S_{H V} & S_{V V}
\end{array}\right]\left[\begin{array}{l}
E_{H}^{(\text {inc })} \\
E_{V}^{(\text {(inc) }}
\end{array}\right]=\sqrt{\frac{4 \pi}{\lambda^{2}}}[S]\left[\begin{array}{l}
E_{H}^{(\text {inc })} \\
E_{V}^{(i n c)}
\end{array}\right]
$$

For further details, see [1] or [2].

## Subband Frequency Processing

Subband processing decomposes a wideband signal into multiple subbands and applies narrowband processing to the signal in each subband. The signals for all subbands are summed to form the output signal.

When using wideband frequency System objects or blocks, you specify the number of subbands, $N_{\mathrm{B}}$, in which to decompose the wideband signal. Subband center frequencies and widths are automatically computed from the total bandwidth and number of subbands. The total frequency band is centered on the carrier or operating frequency, $f_{c}$. The overall bandwidth is given by the sample rate, $f_{s}$. Frequency subband widths are $\Delta f=f_{s} / N_{\mathrm{B}}$. The center frequencies of the subbands are

$$
f_{m}=\left\{\begin{array}{c}
f_{c}-\frac{f_{s}}{2}+(m-1) \Delta f, \quad N_{B} \text { even } \\
f_{c}-\frac{\left(N_{B}-1\right) f_{s}}{2 N_{B}}+(m-1) \Delta f, \quad N_{B} \text { odd }
\end{array}, m=1, \ldots, N_{B}\right.
$$

Some System objects let you obtain the subband center frequencies as output when you run the object. The returned subband frequencies are ordered consistently with the ordering of the discrete

Fourier transform. Frequencies above the carrier appear first, followed by frequencies below the carrier.

## Version History <br> Introduced in R2016b

## References

[1] Mott, H. Antennas for Radar and Communications. New York: John Wiley \& Sons, 1992.
[2] Richards, M. A. Fundamentals of Radar Signal Processing. New York: McGraw-Hill, 2005.
[3] Skolnik, M. Introduction to Radar Systems, 3rd Ed. New York: McGraw-Hill, 2001.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
See "System Objects in MATLAB Code Generation" (MATLAB Coder).

## See Also

phased.RadarTarget | phased.BackscatterRadarTarget | phased. BackscatterSonarTarget | backscatterPedestrian

Topics
"Modeling Target Radar Cross Section" (Radar Toolbox)
"Simulating Test Signals for a Radar Receiver"
"Swerling Target Models"

## reset

System object: phased.WidebandBackscatterRadarTarget
Package: phased
Reset states of System object

## Syntax

reset(target)

## Description

reset (target) resets the internal state of the phased. WidebandBackscatterRadarTarget object, target. This method resets the random number generator state if SeedSource is a property of this System object and has the value 'Property'.

## Input Arguments

## target - Wideband backscatter radar target <br> phased.WidebandBackscatterRadarTarget System object

Wideband backscatter radar target, specified as a phased.WidebandBackscatterRadarTarget System object.

Version History<br>Introduced in R2016b

## step

System object: phased. WidebandBackscatterRadarTarget
Package: phased
Backscatter wideband signal from radar target

## Syntax

```
refl_sig = step(target,sig,ang)
refl_sig = step(target,sig,ang,update)
refl_sig = step(target,sig,ang,laxes)
refl_sig = step(target,sig,ang,laxes,update)
```


## Description

Note Alternatively, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.
refl_sig = step(target,sig,ang) returns the reflected signal, refl_sig, of an incident nonpolarized signal, sig. This syntax applies when you set the EnablePolarization property to false and the Model property to 'Nonfluctuating'. In this case, the values specified in the RCSPattern property are used to compute the RCS values for the incident and reflected directions, ang.
refl_sig = step(target,sig,ang, update) uses update to control whether to update the RCS values. This syntax applies when you set the EnablePolarization property to false and the Model property to one of the fluctuating RCS models: 'Swerling1', 'Swerling2', 'Swerling3', or 'Swerling4'. If update is true, a new RCS value is generated. If update is false, the previous RCS value is used.
refl_sig $=$ step (target, sig, ang, laxes) returns the reflected signal, refl_sig, of an incident polarized signal, sig. This syntax applies when you set EnablePolarization to true and the Model property to 'Nonfluctuating'. The values specified in the ShhPattern, SvvPattern, and ShvPattern properties are used to compute the backscattering matrices for the incident directions, ang. The laxes argument specifies a local coordinate system used to define the horizontal and vertical polarization components.
refl_sig = step(target, sig,ang,laxes, update) uses the update argument to control whether to update the scattering matrix values. This syntax applies when you set the EnablePolarization property to true and the Model property to one of the fluctuating RCS models: 'Swerling1', 'Swerling2', 'Swerling3', or 'Swerling4'. If update is true, a new RCS value is generated. If update is false, the previous RCS value is used.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of
the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## target - Wideband backscatter radar target

phased.WidebandBackscatterRadarTarget System object
Backscatter target, specified as a phased.WidebandBackscatterRadarTarget System object.

## sig - Wideband signal

$N$-by- $M$ complex-valued matrix | 1 -by- $M$ struct array containing complex-valued fields

- Wideband nonpolarized signal, specified as an $N$-by- $M$ complex-valued matrix. The quantity $N$ is the number of signal samples and $M$ is the number of independent signals reflecting off the target. Each column contains an independent signal reflected from the target.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

- Wideband polarized signal, specified as a $1-b y-M$ struct array containing complex-valued fields. Each struct element contains three $N$-by- 1 column vectors of electromagnetic field components (sig.X, sig.Y,sig.Z) representing the polarized signal that reflects from the target. Each struct element contains three $N$-by- 1 complex-valued column vectors, sig.X, sig. Y , and sig. $Z$. These vectors represent the $x, y$, and $z$ Cartesian components of the polarized signal.

The size of the first dimension of the matrix fields within the struct can vary to simulate a changing signal length such as a pulse waveform with variable pulse repetition frequency.

Example: [1, 1; j, 1; 0.5, 0]
Data Types: double
Complex Number Support: Yes

## ang - Incident signal direction

2 -by-1 real-valued column vector of positive values | 2 -by- $M$ real-valued matrix of positive values
Incident signal direction, specified as a real-valued column 2-by-1 vector or 2-by-M matrix of positive values. Each column of ang specifies the incident direction of the corresponding signal in the form [AzimuthAngle;ElevationAngle]. The number of columns in ang must match the number of independent signals in sig. Units are in degrees.

## Example: [30;45]

Data Types: double

## update - Update RCS <br> false (default) | true

Option to enable the RCS values for fluctuation models to update, specified as false or true. When update is true, a new RCS value is generated with each call to the step method. If update is false, the RCS remains unchanged with each call to step.
Data Types: logical

## laxes - Local coordinate matrix

eye ( 3,3 ) (default) | 3-by-3 real-valued orthonormal matrix | 3-by-3-by-M real-valued array
Local coordinate system matrix, specified as a 3-by-3 real-valued orthonormal matrix or a 3-by-3-by-M real-valued array. The matrix columns specify the local coordinate system orthonormal $x$-axis, $y$-axis, and $z$-axis, respectively. Each axis is a vector of the form ( $x ; y ; z$ ) with respect to the global coordinate system. When sig has only one signal, laxes is a 3 -by-3 matrix. When sig has multiple signals, you can use a single 3-by-3 matrix for multiple signals in sig. In this case, all targets have the same local coordinate systems. When you specify laxes as a 3-by-3-by- $M$ array, each page (third index) defines a 3-by-3 local coordinate matrix for the corresponding target.

Example: [1,0,0;0,0.7071,-0.7071;0,0.7071,0.7071]
Data Types: double

## Output Arguments

## refl_sig - Wideband reflected signal

$N$-by- $M$ complex-valued matrix | 1 -by- $M$ struct array containing complex-valued fields

- Wideband nonpolarized signal, returned as an $N$-by- $M$ complex-valued matrix. Each column contains an independent signal reflected from the target.
- Wideband polarized signal, returned as a $1-$ by- $M$ struct array containing complex-valued fields. Each struct element contains three $N$-by- 1 column vectors of electromagnetic field components (sig.X, sig.Y, sig.Z) representing the polarized signal that reflects from the target.

The quantity $N$ is the number of signal samples and $M$ is the number of signals reflecting off the target. Each column corresponds to a reflecting angle.

For polarized fields, the struct element contains three $N$-by- 1 complex-valued column vectors: sig.X, sig.Y, and sig.Z. These vectors represent the $x, y$, and $z$ Cartesian components of the polarized signal.

The output refl_sig contains signal samples arriving at the signal destination within the current input time frame. When the propagation time from source to destination exceeds the current time frame duration, the output does not contain all contributions from the input of the current time frame. The remaining output appears in the next call to step.

## Examples

## Backscatter Nonpolarized Wideband Signal

Calculate the reflected radar signal from a nonfluctuating point target having a peak RCS of 10.0 $\mathrm{m}^{\wedge} 2$. Use a simple target RCS pattern for illustrative purposes. Real RCS patterns are more complicated. The RCS pattern covers a range of angles from 10-30 degrees in azimuth and 5-15 degrees in elevation. The RCS peaks at 20 degrees azimuth and 10 degrees elevation. The RCS also has a frequency dependence and is specified at 5 frequencies within the signal bandwidth. Assume that the radar operating frequency is 100 MHz and that the signal is a linear FM waveform having a 20 MHz bandwidth.

Create and plot the wideband signal.

```
c = physconst('LightSpeed');
fs = 50e6;
pw = 20e-6;
PRF = 1/(2*pw);
fc = 100e6;
bw = 20e6;
waveform = phased.LinearFMWaveform('SampleRate',fs,'PulseWidth',pw, ...
    'PRF',PRF,'OutputFormat','Pulses','NumPulses',1,'SweepBandwidth',bw, ...
    'SweepDirection','Down','Envelope','Rectangular','SweepInterval', ...
    'Symmetric');
wav = waveform();
n = size(wav,1);
plot([0:(n-1)]/fs*1e6,real(wav),'b')
xlabel('Time (\mu s)')
ylabel('Waveform Magnitude')
grid
```



Create an RCS pattern at five different frequencies within the signal bandwidth using a simplified frequency dependence. The frequency dependence is unity at the operating frequency and falls off outside that frequency. Realistic frequency dependencies are more complicated. Plot the RCS pattern for one of the frequencies.

```
fvec = fc + [-fs/2,-fs/4,0,fs/4,fs/2];
fdep = cos(3*(1 - fvec/fc));
azmax = 20.0;
elmax = 10.0;
azpattern = [10.0:0.5:30.0];
```

```
elpattern = [5.0:0.5:15.0];
rcspattern0 = 10.0*cosd(4*(elpattern - elmax))'*cosd(4*(azpattern - azmax));
for k = 1:5
        rcspattern(:,:,k) = rcspattern0*fdep(k);
end
imagesc(azpattern,elpattern,abs(rcspattern(:,:,1)))
axis image
axis tight
title('RCS')
xlabel('Azimuth (deg)')
ylabel('Elevation (deg)')
```



Create the phased.WidebandBackscatterRadarTarget System object ${ }^{\mathrm{Tm}}$.
target $=$ phased.WidebandBackscatterRadarTarget('Model','Nonfluctuating', ...
'AzimuthAngles', azpattern, 'ElevationAngles',elpattern,...
'RCSPattern', rcspattern,'OperatingFrequency',fc,'NumSubbands',32, ...
'FrequencyVector', fvec) ;

For a sequence of incident azimuth angles at constant elevation, find and plot the reflected signal amplitude.

```
az0 = 13.0;
el = 10.0;
az = az0 + [0:2:20];
naz = length(az);
magsig = zeros(1,naz);
for k = 1:naz
```

```
    y = target(wav,[az(k);el]);
    magsig(k) = max(abs(y));
end
plot(az,magsig,'r.')
xlabel('Azimuth (deg)')
ylabel('Scattered Signal Amplitude')
grid
```



## Backscatter Nonpolarized Wideband Signal from Fluctuating Target

Calculate the reflected radar signal from a Swerling 4 fluctuating point target with a peak RCS of 0.1 $\mathrm{m} \wedge 2$. Use a simple target RCS pattern for illustrative purposes. Real RCS patterns are more complicated. The RCS pattern covers a range of angles from $10-30$ degrees in azimuth and 5-15 degrees in elevation. The RCS peaks at 20 degrees in azimuth and 10 degrees in elevation at a value of $0.1 \mathrm{~m}^{\wedge} 2$. The RCS also has a frequency dependence and is specified at five frequencies within the signal bandwidth. Assume that the radar operating frequency is 100 MHz and that the signal is a linear FM waveform with a 20 MHz bandwidth. The sampling frequency is 50 MHz .

Create and plot the wideband signal.

```
c = physconst('LightSpeed');
fs = 50e6;
pw = 20e-6;
PRF = 1/(2*pw);
```

```
fc = 100.0e6;
bw = 20.0e6;
waveform = phased.LinearFMWaveform('SampleRate',fs,'PulseWidth',pw, ...
    'PRF',PRF,'OutputFormat','Pulses','NumPulses',1,'SweepBandwidth',bw, ...
    'SweepDirection','Down','Envelope','Rectangular','SweepInterval', ...
    'Symmetric');
wav = waveform();
```

Create an RCS pattern at five different frequencies within the signal bandwidth using a simple frequency dependence. The frequency dependence is designed to be unity at the operating frequency and fall off outside that band. Realistic frequency dependencies are more complicated.

```
fvec = fc + [-fs/2,-fs/4,0,fs/4,fs/2];
fdep = cos(3*(1 - fvec/fc));
azmax = 20.0;
elmax = 10.0;
azangs = [10.0:0.5:30.0];
elangs = [5.0:0.5:15.0];
rcspattern0 = 0.1*(cosd((elangs - elmax))'*cosd((azangs - azmax))).^2;
for k = 1:5
    rcspattern(:,:,k) = rcspattern0*fdep(k);
end
imagesc(azangs,elangs,abs(rcspattern(:,:,5)))
axis image
axis xy
axis tight
title('RCS')
xlabel('Azimuth (deg)')
ylabel('Elevation (deg)')
colorbar
```



Create the phased.WidebandBackscatterRadarTarget System object ${ }^{\text {TM }}$.

```
target = phased.WidebandBackscatterRadarTarget('Model','Swerling4', ...
    'SeedSource','Property','Seed',100213,'AzimuthAngles',azangs, ...
    'ElevationAngles',elangs,'RCSPattern',rcspattern, ...
    'OperatingFrequency',fc,'NumSubbands',32,'FrequencyVector',fvec);
```

Find and plot 100 samples of the incident signal and two sequential reflected signals at 10 degrees in azimuth and 10 degrees in elevation. Update the RCS at each execution of the System object ${ }^{\mathrm{TM}}$.

```
az = 10.0;
el = 10.0;
refl_wav1 = target(wav,[az;el],true);
refl_wav2 = target(wav,[az;el],true);
n = 100;
plot([0:(n-1)]/fs*le6,real(wav(1:n)))
hold on
plot([0:(n-1)]/fs*1e6,real(refl_wav1(1:n)),'.')
plot([0:(n-1)]/fs*le6,real(refl_wav2(1:n)),'.')
hold off
legend('Incident Signal','First Backscattered Signal','Second Backscattered Signal')
xlabel('Time (\mu s)')
ylabel('Waveform Magnitude')
title('Swerling 4 RCS')
```



## Version History <br> Introduced in R2016b

# phased.WidebandCollector 

Package: phased
Wideband signal collector

## Description

The phased.WidebandCollector System object implements a wideband signal collector. A collector converts incident wideband wave fields arriving from specified directions into signals to be further processed. Wave fields are incident on antenna and microphone elements, sensor arrays, or subarrays. The object collects signals in one of two ways controlled by the Wavef ront Wavefront property.

- If the Wavefront property is set to 'Plane', the collected signals at each element or subarray are the coherent sum of all incident plane wave fields sampled at each array element or subarray.
- If the Wavefront property is set to 'Unspecified ' , the collected signals are formed from an independent field incident on each individual sensor element.

You can use this object to

- model arriving signals as polarized or non-polarized fields depending upon whether the element or array supports polarization and the value of the Polarization property. Using polarization, you can receive a signal as a polarized electromagnetic field, or receive two independent signals using orthogonal polarization directions.
- model acoustic fields by using nonpolarized microphone and sonar transducer array elements and by setting the "Polarization" on page 1-0 to 'None '. You must also set the PropagationSpeed to a value appropriate for the medium.
- collect fields at subarrays created by the phased. ReplicatedSubarray and phased.PartitionedArray objects. You can steer all subarrays in the same direction using the steering angle argument, STEERANG, or steer each subarray in a different direction using the subarray element weights argument, WS. You cannot set the Wavefront property to 'Unspecified' for subarrays.

To collect arriving signals at the elements or arrays:
1 Create the phased.WidebandCollector object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

collector = phased.WidebandCollector
collector = phased.WidebandCollector(Name, Value)

## Description

collector $=$ phased. WidebandCollector creates a wideband signal collector object, collector, with default property values.
collector = phased.WidebandCollector(Name, Value) creates a wideband signal collector with each property Name set to a specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1,...,NameN,ValueN). Enclose each property name in single quotes.
Example: collector =
phased.WidebandCollector('Sensor', phased.URA, 'CarrierFrequency',300e6) sets the sensor array to a uniform rectangular array (URA) with default URA property values. The beamformer assumes a carrier frequency of 300 MHz .

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## Sensor - Sensor element or sensor array

phased.ULA array with default property values (default) | Phased Array System Toolbox sensor or array

Sensor element or sensor array, specified as a System object belonging to Phased Array System Toolbox. A sensor array can contain subarrays.
Example: phased.URA

## PropagationSpeed - Signal propagation speed

physconst('LightSpeed') (default) | positive scalar
Signal propagation speed, specified as a positive scalar. Units are in meters per second. The default propagation speed is the value returned by physconst('LightSpeed'). See physconst for more information.
Example: 3e8
Data Types: double

## SampleRate - Signal sample rate

1e6 (default) | positive real-valued scalar
Signal sample rate, specified as a positive real-valued scalar. Units are in hertz.

## Example: 1e6

Data Types: double

## ModulatedInput - Assume modulated input

true (default) | false

Set this property to true to indicate the input signal is demodulated at a carrier frequency.
Data Types: logical

## CarrierFrequency - Carrier frequency

le9 (default) | positive real-valued scalar
Carrier frequency, specified as a positive real-valued scalar. Units are in hertz.
Example: 1e6
Data Types: double
NumSubbands - Number of processing subbands
64 (default) | positive integer
Number of processing subbands, specified as a positive integer.
Example: 128
Data Types: double

## SensorGainMeasure - Specify sensor gain <br> 'dB' (default)|'dBi'

Sensor gain measure, specified as 'dB' or 'dBi'.

- When you set this property to ' dB ', the input signal power is scaled by the sensor power pattern (in dB ) at the corresponding direction and then combined.
- When you set this property to ' dBi ', the input signal power is scaled by the directivity pattern (in dBi ) at the corresponding direction and then combined. This option is useful when you want to compare results with the values predicted by the radar equation that uses dBi to specify the antenna gain. The computation using the ' dBi ' option is expensive as it requires an integration over all directions to compute the total radiated power of the sensor.


## Data Types: char

## Wavefront - Type of incoming wavefront

'Plane' (default)|'Unspecified'
The type of incoming wavefront, specified as 'Plane' or 'Unspecified ':

- 'Plane' - input signals are multiple plane waves impinging on the entire array. Each plane wave is received by all collecting elements.
- 'Unspecified ' - collected signals are independent fields incident on individual sensor elements. If the Sensor property is an array that contains subarrays, you cannot set the Wavefront property to 'Unspecified'.


## Data Types: char

## Polarization - Polarization configuration

'None' (default) |'Combined'| 'Dual'
Polarization configuration, specified as 'None', 'Combined ', or 'Dual'. When you set this property to 'None', the incident fields are considered scalar fields. When you set this property to 'Combined ', the incident fields are polarized and represent a single arriving signal whose
polarization reflects the sensor's inherent polarization. When you set this property to 'Dual ', the $H$ and $V$ polarization components of the fields are independent signals.

Example: 'Dual'
Data Types: char

## WeightsInputPort - Enable weights input

false (default) | true
Enable weights input, specified as false or true. When true, use the object input argument W to specify weights. Weights are applied to individual array elements (or at the subarray level when subarrays are supported).
Data Types: logical

## Usage

## Syntax

```
Y = collector(X,ANG)
Y = collector(X,ANG,LAXES)
[YH,YV] = collector(X,ANG,LAXES)
[___] = collector(___ ,W)
[___] = collector(___ ,STEERANG)
[___] = collector(___,WS)
```


## Description

$\mathrm{Y}=$ collector(X,ANG) collects the signals, X , arriving from the directions specified by ANG. Y contains the collected signals.
$\mathrm{Y}=$ collector (X,ANG,LAXES) also specifies LAXES as the local coordinate system axes directions. To use this syntax, set the property to 'Combined '.
[ $\mathrm{YH}, \mathrm{YV}$ ] $=$ collector ( $\mathrm{X}, \mathrm{ANG}, \mathrm{LAXES}$ ) returns an H -polarization component of the field, YH , and a V-polarization component, YV. To use this syntax, set the Polarization property to 'Dual'.
[__ ] = collector (__ W) also specifies W as array element or subarray weights. To use this syntax, set the WeightsInputPort property to true.
[___ ] = collector (__ , STEERANG) also specifies STEERANG as the subarray steering angle. To use this syntax, set the Sensor property to an array that supports subarrays and set the SubarraySteering property of that array to either 'Phase' or 'Time'.
[ _ ] = collector $\qquad$ ,WS) also specifies WS as the weights applied to each element within each subarray. To use this syntax, set the Sensor property to an array that supports subarrays and set the SubarraySteering of that array to 'Custom'.

## Input Arguments

## X - Arriving signals

complex-valued $M$-by- $L$ matrix | complex-valued 1-by- $L$ cell array of structures

Arriving signals, specified as a complex-valued $M$-by- $L$ matrix or complex-valued 1-by- $L$ cell array of structures. $M$ is the number of signal samples and $L$ is the number of arrival angles. This argument represents the arriving fields.

- If the Polarization property value is set to 'None', X is an $M$-by- $L$ matrix.
- If the Polarization property value is set to 'Combined ' or 'Dual', X is a 1 -by- L cell array of structures. Each cell corresponds to a separate arriving signal. Each struct contains three column vectors containing the $X, Y$, and $Z$ components of the polarized fields defined with respect to the global coordinate system.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

## Dependencies

To enable this argument, set the Polarization property to 'None' or 'Combined'.

## Data Types: double

Complex Number Support: Yes

## ANG - Arrival directions of signals

real-valued 2-by-L matrix
Arrival directions of signals, specified as a real-valued 2-by-L matrix. Each column specifies an arrival direction in the form [AzimuthAngle;ElevationAngle]. The azimuth angle must lie between $180^{\circ}$ and $180^{\circ}$, inclusive. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive. When the Wavefront property is false, the number of angles must equal the number of array elements, $N$. Units are in degrees.
Example: [30, 20;45,0]
Data Types: double

## LAXES - Local coordinate system

real-valued 3-by-3 orthogonal matrix
Local coordinate system, specified as a real-valued 3-by-3 orthogonal matrix. The matrix columns specify the local coordinate system's orthonormal $x, y$, and $z$ axes with respect to the global coordinate system.

## Example: rotx (30)

## Dependencies

To enable this argument, set the Polarization property to 'Combined ' or 'Dual '.

## Data Types: double

## W - Element or subarray weights

$N$-by-1 column vector
Element or subarray weights, specified as a complex-valued $N$-by-1 column vector where $N$ is the number of array elements (or subarrays when the array supports subarrays).

## Dependencies

To enable this argument, set the WeightsInputPort property to true.

## Data Types: double

Complex Number Support: Yes

## WS - Subarray element weights

complex-valued $N_{\text {SE }}$-by- $N$ matrix | 1-by- $N$ cell array
Subarray element weights, specified as complex-valued $N_{\mathrm{SE}}$-by- $N$ matrix or 1-by- $N$ cell array where $N$ is the number of subarrays. These weights are applied to the individual elements within a subarray.

## Subarray element weights

| Sensor Array | Subarray weights |
| :--- | :--- |
| phased. ReplicatedSubarray | All subarrays have the same dimensions and <br> sizes. Then, the subarray weights form an $N_{\mathrm{SE}}$-by- <br> $N$ matrix. $N_{\mathrm{SE}}$ is the number of elements in each <br> subarray and $N$ is the number of subarrays. Each <br> column of $W$ specifies the weights for the <br> corresponding subarray. |
| phased. PartitionedArray | Subarrays may not have the same dimensions and <br> sizes. In this case, you can specify subarray <br> weights as |
|  | an $N_{\mathrm{SE}}$-by- $N$ matrix, where $N_{\text {SE }}$ is now the <br> number of elements in the largest subarray. <br> The first $Q$ entries in each column are the <br> element weights for the subarray where $Q$ is <br> the number of elements in the subarray. |
|  | a 1-by- $N$ cell array. Each cell contains a <br> column vector of weights for the <br> corresponding subarray. The column vectors <br> have lengths equal to the number of elements <br> in the corresponding subarray. |

## Dependencies

To enable this argument, set the Sensor property to an array that contains subarrays and set the SubarraySteering property of the array to 'Custom'.
Data Types: double
Complex Number Support: Yes

## STEERANG - Subarray steering angle

real-valued 2-by-1 vector
Subarray steering angle, specified as a length-2 column vector. The vector has the form [azimuthAngle;elevationAngle]. The azimuth angle must be between $-180^{\circ}$ and $180^{\circ}$, inclusive. The elevation angle must be between $-90^{\circ}$ and $90^{\circ}$, inclusive. Units are in degrees.
Example: [20;15]

## Dependencies

To enable this argument, set the Sensor property to an array that supports subarrays and set the SubarraySteering property of that array to either 'Phase' or 'Time'

## Data Types: double

## Output Arguments

Y - Collected signal
complex-valued $M$-by- $N$ matrix
Collected signal, returned as a complex-valued $M$-by- $N$ matrix. $M$ is the length of the input signal. $N$ is the number of array elements (or subarrays when subarrays are supported). Each column corresponds to the signal collected by the corresponding array element (or corresponding subarrays when subarrays are supported).

## Dependencies

To enable this argument, set the Polarization property to 'None' or 'Combined'.

## Data Types: double

## YH - Collected horizontal polarization signal <br> complex-valued $M$-by- $N$ matrix

Collected horizontal polarization signal, returned as a complex-valued $M$-by- $N$ matrix. $M$ is the length of the input signal. $N$ is the number of array elements (or subarrays when subarrays are supported). Each column corresponds to the signal collected by the corresponding array element (or corresponding subarrays when subarrays are supported).

## Dependencies

To enable this argument, set the Polarization property to 'Dual '.

## Data Types: double

## YV - Collected vertical polarization signal

complex-valued $M$-by- $N$ matrix
Collected horizontal polarization signal, returned as a complex-valued $M$-by- $N$ matrix. $M$ is the length of the input signal. $N$ is the number of array elements (or subarrays when subarrays are supported). Each column corresponds to the signal collected by the corresponding array element (or corresponding subarrays when subarrays are supported).

## Dependencies

To enable this argument, set the Polarization property to 'Dual '.
Data Types: double

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:

```
release(obj)
```


## Common to All System Objects

step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object

## Examples

## Collect Wideband Signal at Single Antenna

Use the phased. WidebandCollector System object ${ }^{\mathrm{TM}}$ to construct a signal arriving at a single isotropic antenna from $10^{\circ}$ azimuth and $30^{\circ}$ elevation.

```
antenna = phased.IsotropicAntennaElement;
collector = phased.WidebandCollector('Sensor',antenna);
x = [1;0;-1];
incidentAngle = [10;30];
y = collector(x,incidentAngle);
disp(y)
    1.0000 + 0.0000i
    0.0000 + 0.0000i
    -1.0000 - 0.0000i
```


## Collect Wideband Signal at 5-Element ULA

Use the wideband collector to construct the signal impinging upon a 5-element ULA of isotropic antennas from 10 degrees azimuth and 30 degrees elevation.

```
array = phased.ULA('NumElements',5);
collector = phased.WidebandCollector('Sensor',array);
x = [1;1;1];
incidentAngle = [10;30];
y = collector(x,incidentAngle);
disp(y)
```

| $-0.9997+0.0102 i$ | $-0.0051-0.9999 i$ | $1.0000+0.0000 i$ | $-0.0051+1.0001 i$ | $-1.0002-0.0102 i$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $-0.9999+0.0102 i$ | $-0.0051-1.0000 i$ | $1.0000+0.0000 i$ | $-0.0051+1.0000 i$ | $-0.9999-0.0102 i$ |
| $-1.0002+0.0102 i$ | $-0.0051-1.0001 i$ | $1.0000-0.0000 i$ | $-0.0051+0.9999 i$ | $-0.9997-0.0102 i$ |

## Collect Different Signals at 3-Element ULA

Collect three signals incoming into a 3-element array of isotropic antenna elements. Each antenna collects a separate input signal from a separate direction.

```
array = phased.ULA('NumElements',3);
collector = phased.WidebandCollector('Sensor',array,...
    'Wavefront','Unspecified');
rng default
x = rand(10,3);
incidentAngles = [10 20 45; 0 5 2];
y = collector(x,incidentAngles);
disp(y)
```

| $0.8147+0.0000 i$ | $0.1576+0.0000 i$ | $0.6557-0.0000 i$ |
| :--- | :--- | :--- | :--- |
| $0.9058+0.0000 i$ | $0.9706+0.0000 i$ | $0.0357+0.0000 i$ |
| $0.1270-0.0000 i$ | $0.9572+0.0000 i$ | $0.8491-0.0000 i$ |
| $0.9134-0.0000 i$ | $0.4854+0.0000 i$ | $0.9340-0.0000 i$ |
| $0.6324+0.0000 i$ | $0.8003+0.0000 i$ | $0.6787-0.0000 i$ |
| $0.0975-0.0000 i$ | $0.1419+0.0000 i$ | $0.7577-0.0000 i$ |
| $0.2785+0.0000 i$ | $0.4218-0.0000 i$ | $0.7431-0.0000 i$ |
| $0.5469-0.0000 i$ | $0.9157-0.0000 i$ | $0.3922-0.0000 i$ |
| $0.9575+0.0000 i$ | $0.7922+0.0000 i$ | $0.6555+0.0000 i$ |
| $0.9649+0.0000 i$ | $0.9595+0.0000 i$ | $0.1712-0.0000 i$ |

## More About

## Subband Frequency Processing

Subband processing decomposes a wideband signal into multiple subbands and applies narrowband processing to the signal in each subband. The signals for all subbands are summed to form the output signal.

When using wideband frequency System objects or blocks, you specify the number of subbands, $N_{\mathrm{B}}$, in which to decompose the wideband signal. Subband center frequencies and widths are automatically computed from the total bandwidth and number of subbands. The total frequency band is centered on the carrier or operating frequency, $f_{c}$. The overall bandwidth is given by the sample rate, $f_{s}$. Frequency subband widths are $\Delta f=f_{\mathrm{s}} / N_{\mathrm{B}}$. The center frequencies of the subbands are

$$
f_{m}=\left\{\begin{array}{c}
f_{c}-\frac{f_{s}}{2}+(m-1) \Delta f, \quad N_{B} \text { even } \\
f_{c}-\frac{\left(N_{B}-1\right) f_{s}}{2 N_{B}}+(m-1) \Delta f, \quad N_{B} \text { odd }
\end{array}, m=1, \ldots, N_{B}\right.
$$

Some System objects let you obtain the subband center frequencies as output when you run the object. The returned subband frequencies are ordered consistently with the ordering of the discrete Fourier transform. Frequencies above the carrier appear first, followed by frequencies below the carrier.

The phased.WidebandCollector System object uses the narrowband phased approximation of the time delays across receiving elements in the far field for each subband.

## Algorithms

If the Wavefront property value is 'Plane', phased. WidebandCollector does the following for each plane wave signal:

1 Decomposes the signal into multiple subbands.
2 Uses the phase approximation of the time delays across collecting elements in the far field for each subband.
3 Regroups the collected signals in all the subbands to form the output signal.
If the Wavefront property value is 'Unspecified ', the object collects each channel independently.
For further details, see [1].

## Version History

Introduced in R2011a

## References

[1] Van Trees, H. Optimum Array Processing. New York: Wiley-Interscience, 2002.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.
Usage notes and limitations:

- Requires dynamic memory allocation. See "Limitations for System Objects that Require Dynamic Memory Allocation".
- See "System Objects in MATLAB Code Generation" (MATLAB Coder).


## See Also

phased.Collector|phased.WidebandRadiator|phased.Radiator

## step

System object: phased.WidebandCollector
Package: phased
Collect signals

## Syntax

Y = step( $\mathrm{H}, \mathrm{X}, \mathrm{ANG}$ )
Y = step(H,X,ANG,LAXES)
Y = step(H,X,ANG,WEIGHTS)
Y = step(H,X,ANG, STEERANGLE)
Y $=\operatorname{step}(H, X$, ANG, LAXES, WEIGHTS,STEERANGLE)

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.
$Y=$ step ( $\mathrm{H}, \mathrm{X}, \mathrm{ANG}$ ) collects signals X arriving from directions ANG. The collection process depends on the Wavefront property of H , as follows:

- If Wavefront has the value ' Plane', each collecting element collects all the far field signals in X . Each column of $Y$ contains the output of the corresponding element in response to all the signals in $X$.
- If Wavefront has the value 'Unspecified ', each collecting element collects only one impinging signal from $X$. Each column of $Y$ contains the output of the corresponding element in response to the corresponding column of $X$. The 'Unspecified ' option is available when the Sensor property of H does not contain subarrays.

Y = step ( $\mathrm{H}, \mathrm{X}, \mathrm{ANG}, \mathrm{LAXES}$ ) uses LAXES as the local coordinate system axes directions. This syntax is available when you set the EnablePolarization property to true.

Y = step ( $\mathrm{H}, \mathrm{X}$, ANG, WEIGHTS) uses WEIGHTS as the weight vector. This syntax is available when you set the WeightsInputPort property to true.
$\mathrm{Y}=\operatorname{step}(\mathrm{H}, \mathrm{X}$, ANG, STEERANGLE) uses STEERANGLE as the subarray steering angle. This syntax is available when you configure H so that H . Sensor is an array that contains subarrays and H.Sensor.SubarraySteering is either 'Phase' or 'Time'.
$Y=\operatorname{step}(H, X, A N G, L A X E S, W E I G H T S, S T E E R A N G L E)$ combines all input arguments. This syntax is available when you configure H so that H . WeightsInputPort is true, H . Sensor is an array that contains subarrays, and H.Sensor. SubarraySteering is either 'Phase' or 'Time'.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of
the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## H

Collector object.

## X

Arriving signals. Each column of X represents a separate signal. The specific interpretation of X depends on the Wavefront property of H .

| Wavefront Property <br> Value | Description |
| :--- | :--- |
| 'Plane ' | Each column of $X$ is a far field signal. |
| 'Unspecified ' | Each column of $X$ is the signal impinging on the corresponding element. <br> In this case, the number of columns in $X$ must equal the number of <br> collecting elements in the Sensor property. |

- If the EnablePolarization property value is set to false, X is a matrix. The number of columns of the matrix equals the number of separate signals.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

- If the EnablePolarization property value is set to true, X is a row vector of MATLAB struct type. The dimension of the struct array equals the number of separate signals. Each struct member contains three column-vector fields, $\mathrm{X}, \mathrm{Y}$, and Z , representing the $x, y$, and $z$ components of the polarized wave vector signals in the global coordinate system.

The size of the first dimension of the matrix fields within the struct can vary to simulate a changing signal length such as a pulse waveform with variable pulse repetition frequency.

## ANG

Incident directions of signals, specified as a two-row matrix. Each column specifies the incident direction of the corresponding column of X. Each column of ANG has the form [azimuth; elevation], in degrees. The azimuth angle must be between -180 and 180 degrees, inclusive. The elevation angle must be between -90 and 90 degrees, inclusive.

## LAXES

Local coordinate system. LAXES is a 3-by-3 matrix whose columns specify the local coordinate system's orthonormal $x, y$, and $z$ axes, respectively. Each axis is specified in terms of [x;y;z] with respect to the global coordinate system. This argument is only used when the EnablePolarization property is set to true.

## WEIGHTS

Vector of weights. WEIGHTS is a column vector of length $M$, where $M$ is the number of collecting elements.

Default: ones (M, 1)

## STEERANGLE

Subarray steering angle, specified as a length- 2 column vector. The vector has the form [azimuth; elevation], in degrees. The azimuth angle must be between -180 and 180 degrees, inclusive. The elevation angle must be between -90 and 90 degrees, inclusive.

## Output Arguments

## Y

Collected signals. Each column of Y contains the output of the corresponding element. The output is the response to all the signals in X , or one signal in X , depending on the Wavefront property of H .

## Examples

## Collect Wideband Signal at Single Antenna

Use the phased.WidebandCollector System object ${ }^{T M}$ to construct a signal arriving at a single isotropic antenna from $10^{\circ}$ azimuth and $30^{\circ}$ elevation.

```
antenna = phased.IsotropicAntennaElement;
collector = phased.WidebandCollector('Sensor',antenna);
x = [1;0;-1];
incidentAngle = [10;30];
y = collector(x,incidentAngle);
disp(y)
    1.0000 + 0.0000i
    0.0000 + 0.0000i
    -1.0000 - 0.0000i
```


## Collect Wideband Signal at 5-Element ULA

Use the wideband collector to construct the signal impinging upon a 5 -element ULA of isotropic antennas from 10 degrees azimuth and 30 degrees elevation.

```
array = phased.ULA('NumElements',5);
collector = phased.WidebandCollector('Sensor',array);
x = [1;1;1];
incidentAngle = [10;30];
y = collector(x,incidentAngle);
disp(y)
```

```
-0.9997 + 0.0102i -0.0051 - 0.9999i 1.0000 + 0.0000i -0.0051 + 1.0001i -1.0002 - 0.0102i
-0.9999 + 0.0102i -0.0051 - 1.0000i 1.0000 + 0.0000i -0.0051 + 1.0000i -0.9999 - 0.0102i
-1.0002 + 0.0102i -0.0051 - 1.0001i 1.0000-0.0000i -0.0051 + 0.9999i -0.9997 - 0.0102i
```


## Collect Different Signals at 3-Element ULA

Collect three signals incoming into a 3-element array of isotropic antenna elements. Each antenna collects a separate input signal from a separate direction.

```
array = phased.ULA('NumElements',3);
collector = phased.WidebandCollector('Sensor',array,...
    'Wavefront','Unspecified');
rng default
x = rand(10,3);
incidentAngles = [10 20 45; 0 5 2];
y = collector(x,incidentAngles);
disp(y)
```

| $0.8147+0.0000 i$ | $0.1576+0.0000 i$ | $0.6557-0.0000 i$ |
| :--- | :--- | :--- | :--- |
| $0.9058+0.0000 i$ | $0.9706+0.0000 i$ | $0.0357+0.0000 i$ |
| $0.1270-0.0000 i$ | $0.9572+0.0000 i$ | $0.8491-0.0000 i$ |
| $0.9134-0.0000 i$ | $0.4854+0.0000 i$ | $0.9340-0.0000 i$ |
| $0.6324+0.0000 i$ | $0.8003+0.0000 i$ | $0.6787-0.0000 i$ |
| $0.0975-0.0000 i$ | $0.1419+0.0000 i$ | $0.7577-0.0000 i$ |
| $0.2785+0.0000 i$ | $0.4218-0.0000 i$ | $0.7431-0.0000 i$ |
| $0.5469-0.0000 i$ | $0.9157-0.0000 i$ | $0.3922-0.0000 i$ |
| $0.9575+0.0000 i$ | $0.7922+0.0000 i$ | $0.6555+0.0000 i$ |
| $0.9649+0.0000 i$ | $0.9595+0.0000 i$ | $0.1712-0.0000 i$ |

## Algorithms

If the Wavefront property value is 'Plane', phased.WidebandCollector does the following for each plane wave signal:

1 Decomposes the signal into multiple subbands.
2 Uses the phase approximation of the time delays across collecting elements in the far field for each subband.
3 Regroups the collected signals in all the subbands to form the output signal.
If the Wavefront property value is 'Unspecified ', the object collects each channel independently.
For further details, see [1].

## References

[1] Van Trees, H. Optimum Array Processing. New York: Wiley-Interscience, 2002.

# phased.WidebandFreeSpace 

Package: phased
Wideband free-space propagation

## Description

The System object models wideband signal propagation from one point to another in a free-space environment. The System object applies range-dependent time delay, gain adjustment, and phase shift to the input signal. The object accounts for Doppler shift when either the source or destination is moving. A free-space environment is a boundary-free medium with a speed of signal propagation independent of position and direction. The signal propagates along a straight line from source to destination. For example, you can use this object to model the two-way propagation of a signal from a radar to a target.

For nonpolarized signals, the System object lets you propagate signals from a single point to multiple points or from multiple points to a single point. Multiple-point-to-multiple-point propagation is not supported.

To compute the propagated signal in free space:
1 Define and set up your wideband free space environment as shown in the "Construction" on page 1-2009 section.

2 Call step to propagate the signal through free space according to the properties of the System object. The behavior of step is specific to each object in the toolbox.

When propagating a round trip signal in free space, you can use one WidebandFreeSpace System object to compute the two-way propagation delay. Alternatively, you can use two separate WidebandFreeSpace System objects to compute one-way propagation delays in each direction. Due to filter distortion, the total round trip delay when you employ two-way propagation can differ from the delay when you use two one-way phased. WidebandFreeSpace System objects. It is more accurate to use a single two-way phased.WidebandFreeSpace System object. To set this option, use the TwoWayPropagation property.

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, $\mathrm{y}=$ step(obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.

## Construction

sWBFS = phased.WidebandFreeSpace creates a wideband free space System object, sWBFS.
sWBFS = phased.WidebandFreeSpace(Name,Value) creates a wideband free space System object, sWBFS, with each specified property Name set to the specified Value. You can specify additional name-value pair arguments in any order as Name1,Value1,...,NameN,ValueN.

## Properties

PropagationSpeed - Signal propagation speed
physconst('LightSpeed') (default) | positive scalar
Signal propagation speed, specified as a positive scalar. Units are in meters per second. The default propagation speed is the value returned by physconst('LightSpeed'). See physconst for more information.
Example: 3e8
Data Types: double
OperatingFrequency - Operating frequency
300e6 (default) | positive scalar
Operating frequency, specified as a positive scalar. Units are in Hz .
Example: 1e9
Data Types: double

## TwoWayPropagation - Enable two-way propagation

false (default) | true
Enable two-way propagation, specified as a false or true. Set this property to true to perform round-trip propagation between the signal origin and destination specified in step. Set this property to false to perform only one-way propagation from the origin to the destination.
Example: true
Data Types: logical

## SampleRate - Sample rate of signal

le6 (default) | positive scalar
Sample rate of signal, specified as a positive scalar. Units are in Hz. The System object uses this quantity to calculate the propagation delay in units of samples.
Example: 1e6
Data Types: double

## NumSubbands - Number of processing subbands

64 (default) | positive integer
Number of processing subbands, specified as a positive integer.
Example: 128
Data Types: double

## MaximumDistanceSource - Source of maximum one-way propagation distance 'Auto' (default)|'Property'

Source of maximum one-way propagation distance, specified as 'Auto' or 'Property'. The maximum one-way propagation distance is used to allocate sufficient memory for signal delay computation. When you set this property to 'Auto', the System object automatically allocates
memory. When you set this property to 'Property ', you specify the maximum one-way propagation distance using the value of the MaximumDistance property.

## Data Types: char

## MaximumDistance - Maximum one-way propagation distance <br> 10000 (default) | positive real-valued scalar

Maximum one-way propagation distance, specified as a positive real-valued scalar. Units are in meters. Any signal that propagates more than the maximum one-way distance is ignored. The maximum distance must be greater than or equal to the largest position-to-position distance.
Example: 5000

## Dependencies

To enable this property, set the MaximumDistanceSource property to 'Property '.
Data Types: double

## MaximumNumInputSamplesSource - Source of maximum number of samples <br> 'Auto' (default)|'Property'

The source of the maximum number of samples of the input signal, specified as 'Auto ' or 'Property'. When you set this property to 'Auto', the propagation model automatically allocates enough memory to buffer the input signal. When you set this property to 'Property', you specify the maximum number of samples in the input signal using the MaximumNumInputSamples property. Any input signal longer than that value is truncated.

To use this object with variable-size signals in a MATLAB Function Block in Simulink, set the MaximumNumInputSamplesSource property to 'Property' and set a value for the MaximumNumInputSamples property.
Example: 'Property'
Dependencies
To enable this property, set MaximumDistanceSource to 'Property '.

## Data Types: char

## MaximumNumInputSamples - Maximum number of input signal samples <br> 100 (default) | positive integer

Maximum number of input signal samples, specified as a positive integer. The input signal is the first argument of the step method, after the System object itself. The size of the input signal is the number of rows in the input matrix. Any input signal longer than this number is truncated. To process signals completely, ensure that this property value is greater than any maximum input signal length.

The waveform-generating System objects determine the maximum signal size:

- For any waveform, if the waveform OutputFormat property is set to 'Samples', the maximum signal length is the value specified in the NumSamples property.
- For pulse waveforms, if the OutputFormat is set to 'Pulses', the signal length is the product of the smallest pulse repetition frequency, the number of pulses, and the sample rate.
- For continuous waveforms, if the OutputFormat is set to 'Sweeps ', the signal length is the product of the sweep time, the number of sweeps, and the sample rate.


## Example: 2048

## Dependencies

To enable this property, set MaximumNumInputSamplesSource to 'Property '.
Data Types: double

## Methods

reset Reset states of phased.WidebandFreeSpace System object
step Propagate wideband signal from point to point using free-space channel model

## Common to All System Objects

release $\quad$ Allow System object property value changes

## Examples

## Free-Space Propagation of Wideband Signals

Propagate a wideband signal with three tones in an underwater acoustic with constant speed of propagation. You can model this environment as free space. The center frequency is 100 kHz and the frequencies of the three tones are $75 \mathrm{kHz}, 100 \mathrm{kHz}$, and 125 kHz , respectively. Plot the spectrum of the original signal and the propagated signal to observe the Doppler effect. The sampling frequency is 100 kHz .

```
c = 1500;
fc = 100e3;
fs = 100e3;
relfreqs = [-25000,0,25000];
```

Set up a stationary radar and moving target and compute the expected Doppler.

```
rpos = [0;0;0];
rvel = [0;0;0];
tpos = [30/fs*c; 0;0];
tvel = [45;0;0];
dop = -tvel(1)./(c./(relfreqs + fc));
```

Create a signal and propagate the signal to the moving target.

```
t = (0:199)/fs;
x = sum(exp(li*2*pi*t.'*relfreqs),2);
channel = phased.WidebandFreeSpace(...
    'PropagationSpeed ',c,...
    'OperatingFrequency',fc,...
    'SampleRate',fs);
y = channel(x,rpos,tpos,rvel,tvel);
```

Plot the spectra of the original signal and the Doppler-shifted signal.

```
periodogram([x y],rectwin(size(x,1)),1024,fs,'centered')
ylim([-150 0])
legend('original','propagated');
```



For this wideband signal, you can see that the magnitude of the Doppler shift increases with frequency. In contrast, for narrowband signals, the Doppler shift is assumed constant over the band.

## More About

## Free-space Time Delay and Path Loss

When the origin and destination are stationary relative to each other, you can write the output signal of a free-space channel as $Y(t)=x(t-\tau) / L_{f s p}$. The quantity $\tau$ is the signal delay and $L_{f s p}$ is the free-space path loss. The delay $\tau$ is given by $R / c$, where $R$ is the propagation distance and $c$ is the propagation speed. The free-space path loss is given by

$$
L_{f s p}=\frac{(4 \pi R)^{2}}{\lambda^{2}},
$$

where $\lambda$ is the signal wavelength.
This formula assumes that the target is in the far field of the transmitting element or array. In the near field, the free-space path loss formula is not valid and can result in a loss smaller than one, equivalent to a signal gain. Therefore, the loss is set to unity for range values, $R \leq \lambda / 4 \Pi$.

When the origin and destination have relative motion, the processing also introduces a Doppler frequency shift. The frequency shift is $v / \lambda$ for one-way propagation and $2 v / \lambda$ for two-way propagation. The quantity $v$ is the relative speed of the destination with respect to the origin.

For more details on free space channel propagation, see [2].

## Subband Frequency Processing

Subband processing decomposes a wideband signal into multiple subbands and applies narrowband processing to the signal in each subband. The signals for all subbands are summed to form the output signal.

When using wideband frequency System objects or blocks, you specify the number of subbands, $N_{\mathrm{B}}$, in which to decompose the wideband signal. Subband center frequencies and widths are automatically computed from the total bandwidth and number of subbands. The total frequency band is centered on the carrier or operating frequency, $f_{c}$. The overall bandwidth is given by the sample rate, $f_{s}$. Frequency subband widths are $\Delta f=f_{s} / N_{\mathrm{B}}$. The center frequencies of the subbands are

$$
f_{m}=\left\{\begin{array}{c}
f_{c}-\frac{f_{s}}{2}+(m-1) \Delta f, \quad N_{B} \text { even } \\
f_{c}-\frac{\left(N_{B}-1\right) f_{s}}{2 N_{B}}+(m-1) \Delta f, \quad N_{B} \text { odd }
\end{array}, m=1, \ldots, N_{B}\right.
$$

Some System objects let you obtain the subband center frequencies as output when you run the object. The returned subband frequencies are ordered consistently with the ordering of the discrete Fourier transform. Frequencies above the carrier appear first, followed by frequencies below the carrier.

The phased.WidebandFreeSpace System object uses narrowband time delay and loss algorithms for each subband.

## Version History

Introduced in R2015b

## References

[1] Proakis, J. Digital Communications. New York: McGraw-Hill, 2001.
[2] Skolnik, M. Introduction to Radar Systems, 3rd Ed. New York: McGraw-Hill, 2001.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:
See "System Objects in MATLAB Code Generation" (MATLAB Coder).

## See Also

twoRayChannel| phased.FreeSpace | phased.WidebandRadiator | phased.WidebandCollector|phased.RadarTarget |fspl

## reset

System object: phased.WidebandFreeSpace
Package: phased
Reset states of phased.WidebandFreeSpace System object

## Syntax

reset(sWBFS)

## Description

reset (sWBFS) resets the internal state of the phased.WidebandFreeSpace object, sWBFS. If the SeedSource property applies and has the value 'Property', then this method resets the random number generator state.

## Input Arguments

sWBFS - Wideband free space propagator
System object
Wideband free space propagator, specified as a System object.
Example: phased.WidebandFreeSpace

Version History<br>Introduced in R2015b

## step

System object: phased.WidebandFreeSpace
Package: phased
Propagate wideband signal from point to point using free-space channel model

## Syntax

prop_sig = step(sWBFS,sig,origin_pos,dest_pos,origin_vel,dest_vel)

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step (obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.
prop_sig = step(sWBFS,sig,origin_pos,dest_pos,origin_vel,dest_vel) returns the resulting signal, prop_sig, when a wideband signal sig propagates through a free-space channel from the origin_pos position to the dest_pos position. Either the origin_pos or dest_pos arguments can specify more than one point but you cannot specify both as having multiple points. The velocity of the signal origin is specified in origin_vel and the velocity of the signal destination is specified in dest_vel. The dimensions of origin_vel and dest_vel must agree with the dimensions of origin_pos and dest_pos, respectively.

Electromagnetic fields propagated through a free-space channel can be polarized or nonpolarized. For nonpolarized fields, such as acoustic fields, the propagating signal field, sig, is a vector or matrix. When the fields are polarized, sig is a struct array. Every structure element represents an electric field vector signal.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## sWBFS - Wideband free space propagator

System object
Wideband free space propagator, specified as a System object.

## Example: phased.WidebandFreeSpace

- Wideband nonpolarized signal, specified as an $M$-by- $N$ complex-valued matrix. Each column contains a signal propagated along one of the free-space paths.
- Wideband polarized signal, specified as a 1 -by- $N$ struct array containing complex-valued fields. Each struct element contains an $M$-by-1 column vector of electromagnetic field components (sig.X,sig.Y,sig.Z) representing a polarized signal propagating along one of the free-space paths.

The quantity $M$ is the number of signal samples and $N$ is the number of free-space channels. Each channel corresponds to a source-destination pair.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

For polarized fields, each struct element contains three $M$-by-1 complex-valued column vectors, sig. $X$, sig.Y, and sig. Z. These vectors represent the $x, y$, and $z$ Cartesian components of the polarized signal.

The size of the first dimension of the matrix fields within the struct can vary to simulate a changing signal length such as a pulse waveform with variable pulse repetition frequency.

Example: [1, 1; j, 1;0.5,0]
Data Types: double
Complex Number Support: Yes

## origin_pos - Signal origin

3-by-1 real-valued column vector | 3 -by- $N$ real-valued matrix
Origin of the signal or signals, specified as a 3-by-1 real-valued column vector or 3 -by- $N$ real-valued matrix. Position units are in meters. The quantity $N$ is the number of free-space channels. If origin_pos is a column vector, it takes the form [x;y;z]. If origin_pos is a matrix, each column specifies a different signal origin and has the form $[x ; y ; z]$.

You cannot specify both origin_pos and dest_pos as matrices. At least one must be a 3-by-1 column vector.
Example: [1000;100;500]
Data Types: double

## dest_pos - Signal destination

3 -by-1 real-valued column vector | 3 -by- $N$ real-valued matrix
Destination of the signal or signals, specified as a 3-by-1 real-valued column vector or 3-by- $N$ realvalued matrix. Position units are in meters. The quantity $N$ is the number of free-space channels. If dest_pos is a 3-by-1 column vector, it takes the form [x;y;z]. If dest_pos is a matrix, each column specifies a different signal destination and takes the form $[x ; y ; z]$.

You cannot specify both origin_pos and dest_pos as matrices. At least one must be a 3-by-1 column vector.

Example: [0;0;0]
Data Types: double

## origin_vel - Signal origin velocity

3 -by-1 real-valued column vector | 3 -by- $N$ real-valued matrix
Velocity of signal origin, specified as a real-valued 3-by-1 column vector or real-valued 3-by-N matrix. Velocity units are in meters per second. The dimension of origin_vel must match the dimension of origin_pos. If origin_vel is a column vector, it takes the form [ $\mathrm{Vx} ; \mathrm{Vy} ; \mathrm{Vz}$ ]. If origin_vel is a 3 -by- $N$ matrix, each column specifies a different origin velocity and has the form [ $\mathrm{Vx} ; \mathrm{Vy} ; \overline{\mathrm{Vz}}]$.

Example: [10;0;5]
Data Types: double

## dest_vel - Signal destination velocity <br> 3 -by- 1 real-valued column vector | 3 -by- $N$ real-valued matrix

Velocity of signal destinations, specified as a 3-by-1 column vector or 3-by- $N$ matrix. Velocity units are in meters per second. The dimension of dest_vel must match the dimension of dest_pos. If dest_vel is a column vector, it takes the form [ $\mathrm{Vx} ; \mathrm{Vy} ; \mathrm{Vz}$ ]. If dest_vel is a $3-\mathrm{by}-\mathrm{N}$ matrix, each column specifies a different destination velocity and has the form [ $\mathrm{Vx} ; \mathrm{Vy} ; \mathrm{Vz}$ ].
Example: [0;0;0]
Data Types: double

## Output Arguments

## prop_sig - Wideband propagated signal

$M$-by- $N$ complex-valued matrix | 1 -by- $N$ struct array containing complex-valued fields

- Wideband nonpolarized signal, specified as an $M$-by- $N$ complex-valued matrix. Each column contains a signal propagated along one of the free-space paths.
- Wideband polarized signal, specified as a 1 -by- $N$ struct array containing complex-valued fields. Each struct element contains an $M$-by-1 column vector of electromagnetic field components (sig.X, sig.Y,sig.Z) representing a polarized signal propagating along one of the free-space paths.

The output prop_sig contains signal samples arriving at the signal destination within the current steptime frame. Whenever it takes longer than the current time frame for the signal to propagate from the origin to the destination, the output may not contain all contribution from the input. The next call to step will return more of the propagated signal.

## Examples

## Free-Space Propagation of Wideband Signals

Propagate a wideband signal with three tones in an underwater acoustic with constant speed of propagation. You can model this environment as free space. The center frequency is 100 kHz and the frequencies of the three tones are $75 \mathrm{kHz}, 100 \mathrm{kHz}$, and 125 kHz , respectively. Plot the spectrum of the original signal and the propagated signal to observe the Doppler effect. The sampling frequency is 100 kHz .

```
c = 1500;
```

$\mathrm{fc}=100 \mathrm{e} 3$;

```
fs = 100e3;
relfreqs = [-25000,0,25000];
```

Set up a stationary radar and moving target and compute the expected Doppler.

```
rpos = [0;0;0];
rvel = [0;0;0];
tpos = [30/fs*c; 0;0];
tvel = [45;0;0];
dop = -tvel(1)./(c./(relfreqs + fc));
```

Create a signal and propagate the signal to the moving target.

```
t = (0:199)/fs;
x = sum(exp(li*2*pi*t.'*relfreqs),2);
channel = phased.WidebandFreeSpace(...
    'PropagationSpeed ', c, ...
    'OperatingFrequency',fc,...
    'SampleRate',fs);
y = channel(x,rpos,tpos,rvel,tvel);
```

Plot the spectra of the original signal and the Doppler-shifted signal.

```
periodogram([x y],rectwin(size(x,1)),1024,fs,'centered')
ylim([-150 0])
legend('original','propagated');
```



For this wideband signal, you can see that the magnitude of the Doppler shift increases with frequency. In contrast, for narrowband signals, the Doppler shift is assumed constant over the band.

## Version History

Introduced in R2015b

## References

[1] Proakis, J. Digital Communications. New York: McGraw-Hill, 2001.
[2] Skolnik, M. Introduction to Radar Systems. 3rd Ed. New York: McGraw-Hill
[3] Saakian, A. Radio Wave Propagation Fundamentals. Norwood, MA: Artech House, 2011.
[4] Balanis, C. Advanced Engineering Electromagnetics. New York: Wiley \& Sons, 1989.
[5] Rappaport, T. Wireless Communications: Principles and Practice. 2nd Ed. New York: Prentice Hall, 2002.

# phased.WidebandLOSChannel 

Package: phased
Wideband LOS propagation channel

## Description

The phased.WidebandLOSChannel models the propagation of narrowband electromagnetic signals through a line-of-sight (LOS) channel from a source to a destination. In an LOS channel, propagation paths are straight lines from point to point. The propagation model in the LOS channel includes freespace attenuation in addition to attenuation due to atmospheric gases, rain, fog, and clouds. You can use phased. WidebandLOSChannel to model the propagation of signals between multiple points simultaneously. The System object works for all frequencies.

While the attenuation models for atmospheric gases and rain are valid for electromagnetic signals in the frequency range 1-1000 GHz only, the attenuation model for fog and clouds is valid for 10-1000 GHz . Outside these frequency ranges, the System object uses the nearest valid value.

The phased.WidebandLOSChannel System object applies range-dependent time delays to the signals, as well as gains or losses. When either the source or destination is moving, the System object applies Doppler shifts.

Like the phased.WidebandFreeSpace System object, the phased.WidebandLOSChannel System object supports two-way propagation.

To compute the propagation delay for specified source and receiver points:
1 Define and set up your Wideband LOS channel using the "Construction" on page 1-2021 procedure. You can set the System object properties during construction or leave them at their default values.

2 Call the step method to compute the propagated signal using the properties of the phased.WidebandLOSChannel System object. You can change tunable properties before or after any call to the step method.

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step (obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.

## Construction

sWBLOS = phased.WidebandLOSChannel creates a Wideband LOS attenuating propagation channel System object, sWBLOS.
sWBLOS = phased.WidebandLOSChannel(Name,Value) creates a System object, sWBLOS, with each specified property Name set to the specified Value. You can specify additional name and value pair arguments in any order as (Name1, Value1,...,NameN, ValueN).

## Properties

PropagationSpeed - Signal propagation speed
physconst('LightSpeed') (default) | positive scalar
Signal propagation speed, specified as a positive scalar. Units are in meters per second. The default propagation speed is the value returned by physconst('LightSpeed'). See physconst for more information.

Example: 3e8
Data Types: double
OperatingFrequency - Operating frequency
300e6 (default) | positive scalar
Operating frequency, specified as a positive scalar. Units are in Hz.
Example: 1e9
Data Types: double

## SpecifyAtmosphere - Enable atmospheric attenuation model

false (default) |true
Option to enable the atmospheric attenuation model, specified as a false or true. Set this property to true to add signal attenuation caused by atmospheric gases, rain, fog, or clouds. Set this property to false to ignore atmospheric effects in propagation.

Setting SpecifyAtmosphere to true, enables the Temperature, DryAirPressure, WaterVapourDensity, LiquidWaterDensity, and RainRate properties.
Data Types: logical

## Temperature - Ambient temperature

15 (default) | real-valued scalar
Ambient temperature, specified as a real-valued scalar. Units are in degrees Celsius.
Example: 20.0

## Dependencies

To enable this property, set SpecifyAtmosphere to true.
Data Types: double

## DryAirPressure - Atmospheric dry air pressure

101.325 e 3 (default) | positive real-valued scalar

Atmospheric dry air pressure, specified as a positive real-valued scalar. Units are in pascals (Pa). The default value of this property corresponds to one standard atmosphere.

Example: 101.0e3

## Dependencies

To enable this property, set SpecifyAtmosphere to true.
Data Types: double

## WaterVapourDensity - Atmospheric water vapor density

## 7.5 (default) | positive real-valued scalar

Atmospheric water vapor density, specified as a positive real-valued scalar. Units are in $\mathrm{g} / \mathrm{m}^{3}$.
Example: 7.4

## Dependencies

To enable this property, set SpecifyAtmosphere to true.
Data Types: double

## LiquidWaterDensity - Liquid water density

0.0 (default) | nonnegative real-valued scalar

Liquid water density of fog or clouds, specified as a nonnegative real-valued scalar. Units are in $\mathrm{g} / \mathrm{m}^{3}$. Typical values for liquid water density are 0.05 for medium fog and 0.5 for thick fog.

## Example: 0.1

## Dependencies

To enable this property, set SpecifyAtmosphere to true.

## Data Types: double

## RainRate - Rainfall rate

0.0 (default) | non-negative real-valued scalar

Rainfall rate, specified as a nonnegative real-valued scalar. Units are in $\mathrm{mm} / \mathrm{hr}$. This property applies only when you set SpecifyAtmosphere to true.
Example: 10.0
Data Types: double

## TwoWayPropagation - Enable two-way propagation

false (default) | true
Enable two-way propagation, specified as a false or true. Set this property to true to perform round-trip propagation between the signal origin and destination specified in step. Set this property to false to perform only one-way propagation from the origin to the destination.
Example: true
Data Types: logical

## SampleRate - Sample rate of signal <br> le6 (default) | positive scalar

Sample rate of signal, specified as a positive scalar. Units are in Hz. The System object uses this quantity to calculate the propagation delay in units of samples.

Example: 1e6
Data Types: double
NumSubbands - Number of processing subbands
64 (default) | positive integer

Number of processing subbands, specified as a positive integer.
Example: 128
Data Types: double

## MaximumDistanceSource - Source of maximum one-way propagation distance 'Auto' (default)|'Property'

Source of maximum one-way propagation distance, specified as 'Auto' or 'Property'. The maximum one-way propagation distance is used to allocate sufficient memory for signal delay computation. When you set this property to 'Auto', the System object automatically allocates memory. When you set this property to 'Property ', you specify the maximum one-way propagation distance using the value of the MaximumDistance property.
Data Types: char
MaximumDistance - Maximum one-way propagation distance
10000 (default) | positive real-valued scalar
Maximum one-way propagation distance, specified as a positive real-valued scalar. Units are in meters. Any signal that propagates more than the maximum one-way distance is ignored. The maximum distance must be greater than or equal to the largest position-to-position distance.
Example: 5000

## Dependencies

To enable this property, set the MaximumDistanceSource property to 'Property'.

## Data Types: double

## MaximumNumInputSamplesSource - Source of maximum number of samples <br> 'Auto' (default)|'Property'

The source of the maximum number of samples of the input signal, specified as 'Auto ' or 'Property'. When you set this property to 'Auto', the propagation model automatically allocates enough memory to buffer the input signal. When you set this property to 'Property', you specify the maximum number of samples in the input signal using the MaximumNumInputSamples property. Any input signal longer than that value is truncated.

To use this object with variable-size signals in a MATLAB Function Block in Simulink, set the MaximumNumInputSamplesSource property to 'Property' and set a value for the MaximumNumInputSamples property.

## Example: 'Property'

## Dependencies

To enable this property, set MaximumDistanceSource to 'Property '.
Data Types: char

## MaximumNumInputSamples - Maximum number of input signal samples

100 (default) | positive integer
Maximum number of input signal samples, specified as a positive integer. The input signal is the first argument of the step method, after the System object itself. The size of the input signal is the
number of rows in the input matrix. Any input signal longer than this number is truncated. To process signals completely, ensure that this property value is greater than any maximum input signal length.

The waveform-generating System objects determine the maximum signal size:

- For any waveform, if the waveform OutputFormat property is set to 'Samples', the maximum signal length is the value specified in the NumSamples property.
- For pulse waveforms, if the OutputFormat is set to 'Pulses', the signal length is the product of the smallest pulse repetition frequency, the number of pulses, and the sample rate.
- For continuous waveforms, if the OutputFormat is set to 'Sweeps ', the signal length is the product of the sweep time, the number of sweeps, and the sample rate.


## Example: 2048

## Dependencies

To enable this property, set MaximumNumInputSamplesSource to 'Property'.

```
Data Types: double
```


## Methods

| reset | Reset states of System object |
| :--- | :--- |
| step | Propagate signal in Wideband LOS channel |


| Common to All System Objects |  |
| :--- | :--- |
| release | Allow System object property value changes |

## Examples

## Spectrum of Propagated Signal in Wideband LOS Channel

Propagate a wideband signal in a line-of-sight (LOS) channel from a radar at ( $0,0,0$ ) meters to a target at ( $35,0,0$ ) meters in medium fog. Set the fog liquid water density to $0.05 \mathrm{gm} / \mathrm{m} 3$. Assume rain is falling at $5 \mathrm{~mm} / \mathrm{hr}$. The signal carrier frequency is 20 GHz . The signal is a sum of four cw tones at $19.75,19.875,20.125$, and 20.25 GHz . Set the signal duration to $0.5 \mu \mathrm{~s}$ and the sample rate to 2.0 GHz . Assume the radar is stationary and the target approaches the radar at $40 \mathrm{~m} / \mathrm{s}$. The atmospheric temperature is $12^{\circ} \mathrm{C}$.

Set the signal parameters and create the transmitted signal.

```
c = physconst('LightSpeed');
fs = 2e9;
freq = [-0.25,-.125,0.125,0.25]*1e9;
fc = 20.0e9;
dt = 1/fs;
t = [0:dt:.5e-6];
sig = sum(exp(1i*2*pi*t.'*freq),2);
```

Specify the atmosphere parameters and create the phased.WidebandChannel System object ${ }^{\mathrm{TM}}$.

```
lwd = 0.05;
rainrate = 5.0;
```

```
temp = 12.0;
loschannel = phased.WidebandLOSChannel('SampleRate',fs,'PropagationSpeed',c,...
    'SpecifyAtmosphere',true,'OperatingFrequency',fc,'RainRate', rainrate,...
    'LiquidWaterDensity',lwd,'Temperature',temp);
```

Specify the radar and target positions and velocities.

```
xradar = [0,0,0].';
vradar = [0,0,0].';
xtgt = [35,0,0].';
vtgt = [-40,0,0].';
```

Propagate the signal using the step method.
prop_sig = loschannel(sig,xradar,xtgt,vradar,vtgt);
Plot the propagated signal. For a target range of 35 m , the propagation delay is $0.11 \mu \mathrm{~s}$ as seen in the plot.
plot(t*1e6,real(prop_sig))
grid
xlabel('Time (\{\mu\}s)')
ylabel('Amplitude')


Using the periodogram function with a Taylor window, plot the spectra of the original and propagated signals.

```
nfft = 1024;
nsamp = size(sig,1);
```

periodogram([sig prop_sig],taylorwin(nsamp),nfft,fs,'centered')
ylim([-200 0])
legend('transmitted','propagated')


## More About

## Attenuation and Loss Factors

Attenuation or path loss in the Wideband LOS channel consists of four components. $L=L_{f s p} L_{g} L_{c} L_{r}$, where

- $L_{f s p}$ is the free-space path attenuation
- $L_{g}$ is the atmospheric path attenuation
- $L_{c}$ is the fog and cloud path attenuation
- $L_{r}$ is the rain path attenuation

Each component is in magnitude units, not in dB.

## Free-space Time Delay and Loss

When the origin and destination are stationary relative to each other, you can write the output signal of a free-space channel as $Y(t)=x(t-\tau) / L_{f s p}$. The quantity $\tau$ is the signal delay and $L_{f s p}$ is the free-space path loss. The delay $\tau$ is given by $R / c$, where $R$ is the propagation distance and $c$ is the propagation speed. The free-space path loss is given by

$$
L_{f s p}=\frac{(4 \pi R)^{2}}{\lambda^{2}},
$$

where $\lambda$ is the signal wavelength.
This formula assumes that the target is in the far field of the transmitting element or array. In the near field, the free-space path loss formula is not valid and can result in a loss smaller than one, equivalent to a signal gain. Therefore, the loss is set to unity for range values, $R \leq \lambda / 4 \Pi$.

When the origin and destination have relative motion, the processing also introduces a Doppler frequency shift. The frequency shift is $v / \lambda$ for one-way propagation and $2 v / \lambda$ for two-way propagation. The quantity $v$ is the relative speed of the destination with respect to the origin.

For more details on free space channel propagation, see [5].

## Atmospheric Gas Attenuation Model

This model calculates the attenuation of signals that propagate through atmospheric gases.
Electromagnetic signals attenuate when they propagate through the atmosphere. This effect is due primarily to the absorption resonance lines of oxygen and water vapor, with smaller contributions coming from nitrogen gas. The model also includes a continuous absorption spectrum below 10 GHz . The ITU model Recommendation ITU-R P.676-10: Attenuation by atmospheric gases is used. The model computes the specific attenuation (attenuation per kilometer) as a function of temperature, pressure, water vapor density, and signal frequency. The atmospheric gas model is valid for frequencies from 1-1000 GHz and applies to polarized and nonpolarized fields.

The formula for specific attenuation at each frequency is

$$
\gamma=\gamma_{0}(f)+\gamma_{w}(f)=0.1820 f N^{\prime \prime}(f) .
$$

The quantity $N^{\prime \prime}()$ is the imaginary part of the complex atmospheric refractivity and consists of a spectral line component and a continuous component:

$$
N^{\prime \prime}(f)=\sum_{i} S_{i} F_{i}+N^{\prime \prime}{ }_{D}(f)
$$

The spectral component consists of a sum of discrete spectrum terms composed of a localized frequency bandwidth function, $F(f)_{\mathrm{i}}$, multiplied by a spectral line strength, $S_{\mathrm{i}}$. For atmospheric oxygen, each spectral line strength is

$$
S_{i}=a_{1} \times 10^{-7}\left(\frac{300}{T}\right)^{3} \exp \left[a_{2}\left(1-\left(\frac{300}{T}\right)\right] P .\right.
$$

For atmospheric water vapor, each spectral line strength is

$$
S_{i}=b_{1} \times 10^{-1}\left(\frac{300}{T}\right)^{3.5} \exp \left[b_{2}\left(1-\left(\frac{300}{T}\right)\right] W\right. \text {. }
$$

$P$ is the dry air pressure, $W$ is the water vapor partial pressure, and $T$ is the ambient temperature. Pressure units are in hectoPascals ( hPa ) and temperature is in degrees Kelvin. The water vapor partial pressure, $W$, is related to the water vapor density, $\rho$, by

$$
W=\frac{\rho T}{216.7} .
$$

The total atmospheric pressure is $P+W$.
For each oxygen line, $S_{i}$ depends on two parameters, $a_{1}$ and $a_{2}$. Similarly, each water vapor line depends on two parameters, $b_{1}$ and $b_{2}$. The ITU documentation cited at the end of this section contains tabulations of these parameters as functions of frequency.

The localized frequency bandwidth functions $F_{i}(f)$ are complicated functions of frequency described in the ITU references cited below. The functions depend on empirical model parameters that are also tabulated in the reference.

To compute the total attenuation for narrowband signals along a path, the function multiplies the specific attenuation by the path length, $R$. Then, the total attenuation is $L_{g}=R\left(\gamma_{o}+\gamma_{w}\right)$.

You can apply the attenuation model to wideband signals. First, divide the wideband signal into frequency subbands, and apply attenuation to each subband. Then, sum all attenuated subband signals into the total attenuated signal.

## Fog and Cloud Attenuation Model

This model calculates the attenuation of signals that propagate through fog or clouds.
Fog and cloud attenuation are the same atmospheric phenomenon. The ITU model, Recommendation ITU-R P.840-6: Attenuation due to clouds and fog is used. The model computes the specific attenuation (attenuation per kilometer), of a signal as a function of liquid water density, signal frequency, and temperature. The model applies to polarized and nonpolarized fields. The formula for specific attenuation at each frequency is

$$
\gamma_{C}=K_{l}(f) M,
$$

where $M$ is the liquid water density in $\mathrm{gm} / \mathrm{m}^{3}$. The quantity $K_{l}(f)$ is the specific attenuation coefficient and depends on frequency. The cloud and fog attenuation model is valid for frequencies $10-1000 \mathrm{GHz}$. Units for the specific attenuation coefficient are $(\mathrm{dB} / \mathrm{km}) /\left(\mathrm{g} / \mathrm{m}^{3}\right)$.

To compute the total attenuation for narrowband signals along a path, the function multiplies the specific attenuation by the path length $R$. Total attenuation is $L_{c}=R \gamma_{c}$.

You can apply the attenuation model to wideband signals. First, divide the wideband signal into frequency subbands, and apply narrowband attenuation to each subband. Then, sum all attenuated subband signals into the total attenuated signal.

## Rainfall Attenuation Model

This model calculates the attenuation of signals that propagate through regions of rainfall. Rain attenuation is a dominant fading mechanism and can vary from location-to-location and from year-toyear.

Electromagnetic signals are attenuated when propagating through a region of rainfall. Rainfall attenuation is computed according to the ITU rainfall model Recommendation ITU-R P.838-3: Specific attenuation model for rain for use in prediction methods. The model computes the specific attenuation (attenuation per kilometer) of a signal as a function of rainfall rate, signal frequency, polarization, and path elevation angle. The specific attenuation, $\gamma_{R}$, is modeled as a power law with respect to rain rate

$$
\gamma_{R}=k R^{\alpha},
$$

where $R$ is rain rate. Units are in $\mathrm{mm} / \mathrm{hr}$. The parameter $k$ and exponent $\alpha$ depend on the frequency, the polarization state, and the elevation angle of the signal path. The specific attenuation model is valid for frequencies from 1-1000 GHz.

To compute the total attenuation for narrowband signals along a path, the function multiplies the specific attenuation by the an effective propagation distance, $d_{\text {eff. }}$. Then, the total attenuation is $L=$ $d_{\text {eff }} Y_{R}$.

The effective distance is the geometric distance, $d$, multiplied by a scale factor

$$
r=\frac{1}{0.477 d^{0.633} R_{0.01}^{0.073 \alpha} f^{0.123}-10.579(1-\exp (-0.024 d))}
$$

where $f$ is the frequency. The article Recommendation ITU-R P.530-17 (12/2017): Propagation data and prediction methods required for the design of terrestrial line-of-sight systems presents a complete discussion for computing attenuation.

The rain rate, $R$, used in these computations is the long-term statistical rain rate, $R_{0.01}$. This is the rain rate that is exceeded $0.01 \%$ of the time. The calculation of the statistical rain rate is discussed in Recommendation ITU-R P.837-7 (06/2017): Characteristics of precipitation for propagation modelling. This article also explains how to compute the attenuation for other percentages from the $0.01 \%$ value.

You can apply the attenuation model to wideband signals. First, divide the wideband signal into frequency subbands and apply attenuation to each subband. Then, sum all attenuated subband signals into the total attenuated signal.

## Subband Frequency Processing

Subband processing decomposes a wideband signal into multiple subbands and applies narrowband processing to the signal in each subband. The signals for all subbands are summed to form the output signal.

When using wideband frequency System objects or blocks, you specify the number of subbands, $N_{\mathrm{B}}$, in which to decompose the wideband signal. Subband center frequencies and widths are automatically computed from the total bandwidth and number of subbands. The total frequency band is centered on the carrier or operating frequency, $f_{c}$. The overall bandwidth is given by the sample rate, $f_{s}$. Frequency subband widths are $\Delta f=f_{\mathrm{s}} / N_{\mathrm{B}}$. The center frequencies of the subbands are

$$
f_{m}=\left\{\begin{array}{c}
f_{c}-\frac{f_{s}}{2}+(m-1) \Delta f, \quad N_{B} \text { even } \\
f_{c}-\frac{\left(N_{B}-1\right) f_{s}}{2 N_{B}}+(m-1) \Delta f, \quad N_{B} \text { odd }
\end{array}, m=1, \ldots, N_{B}\right.
$$

Some System objects let you obtain the subband center frequencies as output when you run the object. The returned subband frequencies are ordered consistently with the ordering of the discrete Fourier transform. Frequencies above the carrier appear first, followed by frequencies below the carrier.

The phased.WidebandLOSChannel System object uses narrowband time delay and attenuation algorithms for each subband.

## Version History

Introduced in R2016a

## References

[1] Radiocommunication Sector of the International Telecommunication Union. Recommendation ITUR P.676-10: Attenuation by atmospheric gases. 2013.
[2] Radiocommunication Sector of the International Telecommunication Union. Recommendation ITUR P.840-6: Attenuation due to clouds and fog. 2013.
[3] Radiocommunication Sector of the International Telecommunication Union. Recommendation ITUR P.838-3: Specific attenuation model for rain for use in prediction methods. 2005.
[4] Seybold, J. Introduction to RF Propagation. New York: Wiley \& Sons, 2005.
[5] Skolnik, M. Introduction to Radar Systems, 3rd Ed. New York: McGraw-Hill, 2001.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:
See "System Objects in MATLAB Code Generation" (MATLAB Coder).

## See Also

## Functions

rangeangle|fogpl|gaspl|rainpl|fspl

## Objects

phased.FreeSpace| phased.RadarTarget | phased.BackscatterRadarTarget | twoRayChannel|phased.WidebandFreeSpace | phased.LOSChannel

## reset

System object: phased.WidebandLOSChannel
Package: phased
Reset states of System object

## Syntax

reset(sWBLOS)

## Description

reset (sWBLOS) resets the internal state of the phased.WidebandLOSChannel System object, sWBLOS. If SeedSource is a property of this System object and has the value 'Property ', then this method resets the random number generator state.

## Input Arguments

sWBLOS - Wideband LOS channel
phased.WidebandLOSChannel System object
Wideband LOS channel, specified as a phased.WidebandLOSChannel System object.
Example: phased.WidebandLOSChannel

## Version History <br> Introduced in R2016a

## step

## System object: phased.WidebandLOSChannel <br> Package: phased

Propagate signal in Wideband LOS channel

## Syntax

prop_sig = step(sLOS,sig,origin_pos,dest_pos,origin_vel,dest_vel)

## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.
prop_sig = step(sLOS,sig,origin_pos,dest_pos,origin_vel,dest_vel) returns the resulting signal, prop_sig, when a wideband signal, sig, propagates through a line-of-sight (LOS) channel from a source located at the origin_pos position to a destination at the dest_pos position. Only one of the origin_pos or dest_pos arguments can specify multiple positions. The other must contain a single position. The velocity of the signal origin is specified in origin_vel and the velocity of the signal destination is specified in dest_vel. The dimensions of origin_vel and dest_vel must match the dimensions of origin_pos and dest_pos, respectively.

Electromagnetic fields propagating through an LOS channel can be polarized or nonpolarized. For nonpolarized fields, the propagating signal field, sig, is a vector or matrix. For polarized fields, sig is an array of structures. The structure elements represent an electric field vector in Cartesian form.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## sWBLOS - Wideband LOS channel

phased.WidebandLOSChannel System object
Wideband LOS channel, specified as a phased.WidebandLOSChannel System object.
Example: phased. WidebandLOSChannel
sig - Wideband signal
$M$-by- $N$ complex-valued matrix | 1-by- $N$ struct array containing complex-valued fields

Wideband signal, specified as a matrix or struct array, depending on whether is signal or polarized or nonpolarized. The quantity $M$ is the number of samples in the signal, and $N$ is the number of wideband LOS channels. Each channel corresponds to a source-destination pair.

- Wideband nonpolarized scalar signal. Specify sig as an $M$-by- $N$ complex-valued matrix. Each column contains one signal propagated along the line-of-sight path.
- Wideband polarized signal. Specify sig as a 1 -by- $N$ struct array containing complex-valued fields. Each struct represents a polarized signal propagated along the line-of-sight path. Each struct element contains three $M$-by- 1 complex-valued column vectors, sig. $X$, sig. $Y$, and sig. $Z$. These vectors represent the $x, y$, and $z$ Cartesian components of the polarized signal.

Example: [1, 1; j, 1;0.5,0]
Data Types: double
Complex Number Support: Yes

## origin_pos - Signal origins

3-by-1 real-valued column vector | 3 -by- $N$ real-valued matrix
Origin of signals, specified as a 3-by-1 real-valued column vector or 3-by- N real-valued matrix. The quantity $N$ is the number of LOS channels. If origin_pos is a column vector, it takes the form [ $x ; y ; z]$. If origin_pos is a matrix, each column specifies a different signal origin and has the form [ $x ; y ; z]$. Units are in meters.

You cannot specify both origin_pos and dest_pos as matrices. At least one must be a 3-by-1 column vector.
Example: [1000;100;500]
Data Types: double

## dest_pos - Signal destinations

3 -by-1 real-valued column vector | 3 -by- N real-valued matrix
Destination position of the signal or signals, specified as a 3-by-1 real-valued column vector or 3-by- $N$ real-valued matrix. The quantity $N$ is the number of LOS channels propagating from or to $N$ signal origins. If dest_pos is a 3-by-1 column vector, it takes the form [x;y;z]. If dest_pos is a matrix, each column specifies a different signal destination and takes the form [x;y;z] Position units are in meters.

You cannot specify both origin_pos and dest_pos as matrices. At least one must be a 3-by-1 column vector.
Example: [0;0;0]
Data Types: double

## origin_vel - Velocities of signal origins

3 -by-1 real-valued column vector | 3 -by- N real-valued matrix
Velocity of signal origin, specified as a 3-by-1 real-valued column vector or 3-by- $N$ real-valued matrix. The dimensions of origin_vel must match the dimensions of origin_pos. If origin_vel is a
 specifies a different origin velocity and has the form [ $\mathrm{Vx} ; \mathrm{Vy} ; \mathrm{Vz}$ ]. Velocity units are in meters per second.

Example: [10;0;5]

## Data Types: double

## dest_vel - Velocities of signal destinations

3 -by- $\overline{1}$ real-valued column vector | 3 -by- $N$ real-valued matrix
Velocity of signal destinations, specified as a 3-by-1 real-valued column vector or 3-by- $N$ real-valued matrix. The dimensions of dest_vel must match the dimensions of dest_pos. If dest_vel is a column vector, it takes the form [ $\mathrm{Vx} ; \mathrm{Vy} ; \mathrm{Vz}$ ]. If dest_vel is a 3-by- $N$ matrix, each column specifies a different destination velocity and has the form [ $\mathrm{Vx} ; \mathrm{Vy} ; \mathrm{Vz}$ ] Velocity units are in meters per second.
Example: [0;0;0]
Data Types: double

## Output Arguments

## prop_sig - Wideband propagated signal

$M$-by- $N$ complex-valued matrix | 1-by- $N$ struct array containing complex-valued fields
Wideband signal, returned as a matrix or struct array, depending on whether the signal is polarized or nonpolarized. The quantity $M$ is the number of samples in the signal and $N$ is the number of wideband LOS channels. Each channel corresponds to a source-destination pair.

- Wideband nonpolarized scalar signal. prop_sig is an $M$-by- $N$ complex-valued matrix.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

- Wideband polarized scalar signal. prop_sig is a 1-by-N struct array containing complex-valued fields. Each struct element contains three $M$-by- 1 complex-valued column vectors, sig. $X$, sig.Y, and sig. Z. These vectors represent the $x, y$, and $z$ Cartesian components of the polarized signal.

The size of the first dimension of the matrix fields within the struct can vary to simulate a changing signal length such as a pulse waveform with variable pulse repetition frequency.

The prop_sig output contains signal samples arriving at the signal destination within the current time frame. The current time frame is the time frame of the input signals to step. Whenever it takes longer than the current time frame for the signal to propagate from the origin to the destination, the output might not contain all contributions from the input of the current time frame. The remaining output appears in the next call to step.

## Examples

## Propagate Wideband Signal in LOS Channel

Propagate a wideband signal in a line-of-sight (LOS) channel from a radar at ( $0,0,0$ ) meters to a target at $(60,0,0)$ meters in medium fog. Set the fog liquid water density to $0.05 \mathrm{~g} / \mathrm{m}^{3}$. Assume rain is falling at $5 \mathrm{~mm} / \mathrm{hr}$. The signal carrier frequency is 20 GHz . The signal is a sum of four cw tones at 19.75, $19.875,20.125$, and 20.25 GHz . Set the signal duration to 0.5 microsecond and the sample rate to 2.0 GHz . Assume the radar is stationary and the target approaches the radar at $40 \mathrm{~m} / \mathrm{s}$. The atmospheric temperature is $12^{\circ} \mathrm{C}$ and the dry air pressure is 101.300 kPa .

Set the signal parameters and create the transmitted signal.

```
c = physconst('LightSpeed');
fs = 2e9;
freq = [-0.25,-.125,0.0,0.125,0.25]*1e9;
fc = 20.0e9;
dt = 1/fs;
t = [0:dt:.5e-6];
sig = sum(exp(li*2*pi*t.'*freq),2);
```

Specify the atmosphere parameters and create the phased.WidebandChannel System object ${ }^{\mathrm{TM}}$.
lwd $=0.05$;

```
rainrate = 5.0;
```

dap = 101300.0;
temp = 12.0;
sWBLOS = phased.WidebandLOSChannel('SampleRate',fs,'PropagationSpeed', c, ...
'SpecifyAtmosphere',true,'OperatingFrequency',fc,'RainRate', rainrate,...
'LiquidWaterDensity',lwd,'Temperature',temp,'DryAirPressure',dap);

Specify the radar and target positions and velocities.

```
xradar = [0,0,0].';
vradar = [0,0,0].';
xtgt = [60,0,0].';
vtgt = [-40,0,0].';
```

Propagate the signal using the step method.
prop_sig $=$ step $(s W B L O S, s i g, x r a d a r, x t g t, v r a d a r, v t g t) ;$
Plot the propagated signal. For a target range of 60 m , the propagation delay is 0.20 s as shown in the plot.

```
plot(t*1e6,real(prop_sig))
grid
xlabel('Time (\mu sec)')
ylabel('Amplitude')
```



## Version History <br> Introduced in R2016a

## References

[1] Radiocommunication Sector of the International Telecommunication Union. Recommendation ITUR P.676-10: Attenuation by atmospheric gases. 2013.
[2] Radiocommunication Sector of the International Telecommunication Union. Recommendation ITUR P.840-6: Attenuation due to clouds and fog. 2013.
[3] Radiocommunication Sector of the International Telecommunication Union. Recommendation ITUR P.838-3: Specific attenuation model for rain for use in prediction methods. 2005.
[4] Seybold, J. Introduction to RF Propagation. New York: Wiley \& Sons, 2005.

# phased.WidebandRadiator 

Package: phased
Wideband signal radiator

## Description

The phased.WidebandRadiator System object implements a wideband signal radiator. A radiator converts signals into radiated wavefields transmitted from arrays and individual sensor elements such as antennas, microphone elements, and sonar transducers. The radiator output represents the fields at a reference distance of one meter from the phase center of the element or array. The algorithm divides the signal at each element into frequency subbands and applies a narrowband timedelay to each signal using the phase-shift approximation. Then, the delayed subbands are coherently added to create the output signal. You can then propagate the signals to the far field using, for example, the phased.WidebandFreeSpace or phased.WidebandLOSChannel System objects. You can use this object to

- model radiated signals as polarized or non-polarized fields depending upon whether the element or array supports polarization and the value of the Polarization property. Using polarization, you can transmit a signal as a polarized electromagnetic field, or transmit two independent signals using dual polarizations.
- model acoustic radiated fields by using nonpolarized microphone and sonar transducer array elements and by setting the "Polarization" on page 1-0 to 'None '. You must also set the PropagationSpeed to a value appropriate for the medium.
- radiate fields from subarrays created by the phased.ReplicatedSubarray and phased.PartitionedArray objects. You can steer all subarrays in the same direction using the Steering angle argument, STEERANG, or steer each subarray in a different direction using the Subarray element weights argument, WS. The radiator distributes the signal powers equally among the elements of each subarray.

To radiate signals:
1 Create the phased.WidebandRadiator object and set its properties.
2 Call the object with arguments, as if it were a function.
To learn more about how System objects work, see What Are System Objects?

## Creation

## Syntax

radiator $=$ phased.WidebandRadiator
radiator $=$ phased.WidebandRadiator(Name, Value)

## Description

radiator $=$ phased . WidebandRadiator creates a wideband signal radiator object, radiator, with default property values.
radiator $=$ phased.WidebandRadiator(Name, Value) creates a wideband signal radiator with each property Name set to a specified Value. You can specify additional name-value pair arguments in any order as (Namel,Valuel,...,NameN,ValueN). Enclose each property name in single quotes.

Example: radiator =
phased.WidebandRadiator('Sensor', phased.URA, 'CarrierFrequency', 300e6) sets the sensor array to a uniform rectangular array (URA) with default URA property values. The beamformer has a carrier frequency of 300 MHz .

## Properties

Unless otherwise indicated, properties are nontunable, which means you cannot change their values after calling the object. Objects lock when you call them, and the release function unlocks them.

If a property is tunable, you can change its value at any time.
For more information on changing property values, see System Design in MATLAB Using System Objects.

## Sensor - Sensor element or sensor array

phased. ULA array with default property values (default) | Phased Array System Toolbox sensor or array

Sensor element or sensor array, specified as a System object belonging to Phased Array System Toolbox. A sensor array can contain subarrays.

Example: phased.URA

## PropagationSpeed - Signal propagation speed

physconst('LightSpeed') (default) | positive scalar
Signal propagation speed, specified as a positive scalar. Units are in meters per second. The default propagation speed is the value returned by physconst('LightSpeed'). See physconst for more information.

Example: 3e8
Data Types: double

## SampleRate - Signal sample rate

1e6 (default) | positive real-valued scalar
Signal sample rate, specified as a positive real-valued scalar. Units are in hertz.
Example: 1e6
Data Types: double

## CarrierFrequency - Carrier frequency

le9 (default) | positive real-valued scalar
Carrier frequency, specified as a positive real-valued scalar. Units are in hertz.
Example: 1e6
Data Types: double

## NumSubbands - Number of processing subbands

## 64 (default) | positive integer

Number of processing subbands, specified as a positive integer.
Example: 128
Data Types: double

## SensorGainMeasure - Specify sensor gain <br> 'dB' (default)|'dBi'

Sensor gain measure, specified as 'dB' or 'dBi'.

- When you set this property to ' dB ', the input signal power is scaled by the sensor power pattern (in dB ) at the corresponding direction and then combined.
- When you set this property to ' dBi ' , the input signal power is scaled by the directivity pattern (in dBi ) at the corresponding direction and then combined. This option is useful when you want to compare results with the values computed by the radar equation that uses dBi to specify the antenna gain. The computation using the 'dBi' option is expensive as it requires an integration over all directions to compute the total radiated power of the sensor.


## Data Types: char

## Polarization - Polarization configuration

'None' (default) | 'Combined' | 'Dual'
Polarization configuration, specified as 'None', 'Combined', or 'Dual'. When you set this property to 'None', the output field is considered a scalar field. When you set this property to 'Combined ', the radiated fields are polarized and are interpreted as a single signal in the sensor's inherent polarization. When you set this property to 'Dual ', the $H$ and $V$ polarization components of the radiated field are independent signals.

## Example: 'Dual'

Data Types: char

## WeightsInputPort - Enable weights input

false (default) |true
Enable weights input, specified as false or true. When true, use the object input argument $W$ to specify weights. Weights are applied to individual array elements (or at the subarray level when subarrays are supported).
Data Types: logical

## Usage

## Syntax

```
Y = radiator(X,ANG)
Y = radiator(X,ANG,LAXES)
Y = radiator(XH,XV,ANG,LAXES)
Y = radiator(
,W)
Y = radiator(
                ,STEERANG)
```

$Y=$ radiator( $\qquad$ ,WS)
$Y$ = radiator(X,ANG,LAXES,W,STEERANG)

## Description

$Y=\operatorname{radiator}(X, A N G)$ radiates the signal $X$ in the directions specified by ANG. For each direction, the method computes the radiated signal, Y , by summing the contributions of each element or subarray.
$\mathrm{Y}=$ radiator (X, ANG, LAXES) also specifies the local coordinate system of the radiator, LAXES. This syntax applies when you set the Polarization property to 'Combined '.
$\mathrm{Y}=$ radiator $(\mathrm{XH}, \mathrm{XV}, \mathrm{ANG}, \mathrm{LAXES})$ specifies a horizontal-polarization port signal, XH, and a vertical-polarization port signal, XV. To use this syntax, set the Polarization property to 'Dual '.
$\mathrm{Y}=$ radiator $(\ldots, \mathrm{W})$ also specifies W as array element or subarray weights. To use this syntax, set the WeightsInputPort property to true.
$Y=$ radiator $($ $\qquad$ , STEERANG) also specifies STEERANG as the subarray steering angle. To use this syntax, set the Sensor property to an array that supports subarrays and set the SubarraySteering property of that array to either 'Phase' or 'Time'.
$Y=$ radiator $($ $\qquad$ ,WS) also specifies WS as the weights applied to each element within each subarray. To use this syntax, set the Sensor property to an array that supports subarrays and set the SubarraySteering of that array to 'Custom'.

You can combine optional input arguments when their enabling properties are set, for example, $\mathrm{Y}=$ radiator ( $\mathrm{X}, \mathrm{ANG}, \mathrm{LAXES}, \mathrm{W}, \mathrm{STEERANG}$ ) combines several input arguments. Optional inputs must be listed in the same order as the order of the enabling properties.

## Input Arguments

## X - Signal to radiate

complex-valued $M$-by-1 vector | complex-valued $M$-by- $N$ matrix
Signal to radiate, specified as a complex-valued $M$-by- 1 vector or complex-valued $M$-by- $N$ matrix. $M$ is the length of the signal, and $N$ is the number of array elements (or subarrays when subarrays are supported).

Dimensions of $X$

| Dimension | Signal |
| :--- | :--- |
| $M$-by-1 vector | The same signal is radiated from all array <br> elements (or all subarrays when subarrays are <br> supported). |
| $M$-by $-N$ matrix | Each column corresponds to the signal radiated <br> by the corresponding array element (or <br> corresponding subarrays when subarrays are <br> supported). |

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

## Dependencies

To enable this argument, set the Polarization property to 'None' or 'Combined '.

```
Data Types: double
Complex Number Support: Yes
```


## ANG - Radiating directions of signals

real-valued 2-by-L matrix
Radiating directions of signals, specified as a real-valued 2-by-L matrix. Each column specifies a radiating direction in the form [AzimuthAngle; ElevationAngle]. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive. Units are in degrees.
Example: [30,20;45,0]
Data Types: double

## LAXES - Local coordinate system

real-valued 3-by-3 orthogonal matrix
Local coordinate system, specified as a real-valued 3-by-3 orthogonal matrix. The matrix columns specify the local coordinate system's orthonormal $x, y$, and $z$ axes with respect to the global coordinate system.
Example: rotx (30)

## Dependencies

To enable this argument, set the Polarization property to 'Combined ' or 'Dual '.

## Data Types: double

## XH $\mathbf{- H}$-polarization port signal to radiate

complex-valued $M$-by-1 vector | complex-valued $M$-by- $N$ matrix
H-polarization port signal to radiate, specified as a complex-valued $M$-by-1 vector or complex-valued $M$-by- $N$ matrix. $M$ is the length of the signal, and $N$ is the number of array elements (or subarrays when subarrays are supported).

## Dimensions of XH

| Dimension | Signal |
| :--- | :--- |
| $M$-by-1 vector | The same signal is radiated from all array <br> elements (or all subarrays when subarrays are <br> supported). |
| $M$-by- $N$ matrix | Each column corresponds to the signal radiated <br> by the corresponding array element (or <br> corresponding subarrays when subarrays are <br> supported). |

The dimensions and sizes of XH and XV must be the same.
The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

## Dependencies

To enable this argument, set the Polarization property to 'Dual ' .
Data Types: double
Complex Number Support: Yes
XV - V-polarization port signal to radiate
complex-valued $M$-by- 1 vector | complex-valued $M$-by- $N$ matrix
V-polarization port signal to radiate, specified as a complex-valued $M$-by-1 vector or complex-valued $M$-by- $N$ matrix. $M$ is the length of the signal, and $N$ is the number of array elements (or subarrays when subarrays are supported).

Dimensions of XV

| Dimension | Signal |
| :--- | :--- |
| $M$-by-1 vector | The same signal is radiated from all array <br> elements (or all subarrays when subarrays are <br> supported). |
| $M$-by $-N$ matrix | Each column corresponds to the signal radiated <br> by the corresponding array element (or <br> corresponding subarrays when subarrays are <br> supported). |

The dimensions and sizes of XH and XV must be the same.
The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

## Dependencies

To enable this argument, set the Polarization property to 'Dual ' .
Data Types: double
Complex Number Support: Yes

## W - Element or subarray weights

$N$-by-1 column vector
Element or subarray weights, specified as a complex-valued $N$-by- 1 column vector where $N$ is the number of array elements (or subarrays when the array supports subarrays).

## Dependencies

To enable this argument, set the WeightsInputPort property to true.
Data Types: double
Complex Number Support: Yes

## WS - Subarray element weights

complex-valued $N_{\text {SE }}$-by- $N$ matrix | 1-by- $N$ cell array
Subarray element weights, specified as complex-valued $N_{\text {SE }}$-by- $N$ matrix or 1-by- $N$ cell array where $N$ is the number of subarrays. These weights are applied to the individual elements within a subarray.

Subarray element weights

| Sensor Array | Subarray weights |
| :---: | :---: |
| phased. ReplicatedSubarray | All subarrays have the same dimensions and sizes. Then, the subarray weights form an $N_{\mathrm{SE}^{-}}$-by$N$ matrix. $N_{\text {SE }}$ is the number of elements in each subarray and $N$ is the number of subarrays. Each column of WS specifies the weights for the corresponding subarray. |
| phased.PartitionedArray | Subarrays may not have the same dimensions and sizes. In this case, you can specify subarray weights as <br> - an $N_{\mathrm{SE}}-$ by- $N$ matrix, where $N_{\mathrm{SE}}$ is now the number of elements in the largest subarray. The first $Q$ entries in each column are the element weights for the subarray where $Q$ is the number of elements in the subarray. <br> - a 1-by- $N$ cell array. Each cell contains a column vector of weights for the corresponding subarray. The column vectors have lengths equal to the number of elements in the corresponding subarray. |

## Dependencies

To enable this argument, set the Sensor property to an array that contains subarrays and set the SubarraySteering property of the array to 'Custom'.

Data Types: double
Complex Number Support: Yes

## STEERANG - Subarray steering angle

real-valued 2-by-1 vector
Subarray steering angle, specified as a length-2 column vector. The vector has the form [azimuthAngle;elevationAngle]. The azimuth angle must be between $-180^{\circ}$ and $180^{\circ}$, inclusive. The elevation angle must be between $-90^{\circ}$ and $90^{\circ}$, inclusive. Units are in degrees.

## Example: [20;15]

## Dependencies

To enable this argument, set the Sensor property to an array that supports subarrays and set the SubarraySteering property of that array to either 'Phase' or 'Time'
Data Types: double

## Output Arguments

## Y - Radiated signals

complex-valued $M$-by-L matrix | complex-valued 1-by-L cell array of structures
Radiated signals, specified as a complex-valued $M$-by- $L$ matrix or a 1-by- $L$ cell array, where $L$ is the number of radiating angles, ANG. $M$ is the length of the input signal, X.

- If the Polarization property value is set to 'None', the output argument $Y$ is an $M$-by- $L$ matrix.
- If the Polarization property value is set to 'Combined ' or 'Dual', Y is a 1-by-L cell array of structures. Each cell corresponds to a separate radiating signal. Each struct contains three column vectors containing the $X, Y$, and $Z$ components of the polarized fields defined with respect to the global coordinate system.

Data Types: double

## Object Functions

To use an object function, specify the System object as the first input argument. For example, to release system resources of a System object named obj, use this syntax:
release(obj)

## Common to All System Objects

step Run System object algorithm
release Release resources and allow changes to System object property values and input characteristics
reset Reset internal states of System object

## Examples

## Radiate Wideband Energy from Array

Create a 5-by-5 URA and space the elements one-half wavelength apart. The wavelength corresponds to a design frequency of 300 MHz .

## Create 5-by-5 URA Array of Cosine Elements

```
c = physconst('LightSpeed');
fc = 100e6;
lam = c/fc;
antenna = phased.CosineAntennaElement('CosinePower',[2,2]);
array = phased.URA('Element',antenna,'Size',[5,5],'ElementSpacing',[0.5,0.5]*lam);
```


## Create and Radiate Wideband Signal

Radiate a wideband signal consisting of three sinusoids at 2,10 and 11 MHz . Set the sampling rate to 25 MHz . Radiate the fields into two directions: $(30,10)$ degrees azimuth and elevation and $(20,50)$ degrees azimuth and elevation.

```
fs = 25e6;
f1 = 2e6;
f2 = 10e6;
f3 = 11e6;
dt = 1/fs;
Tsig = 100e-6;
t = [0:dt:Tsig];
sig = 5.0*sin(2*pi*f1*t) + 2.0*sin(2*pi*f2*t + pi/10) + 4*sin(2*pi*f3*t + pi/2);
radiatingangles = [30 10; 20 50]';
radiator = phased.WidebandRadiator('Sensor',array,'CarrierFrequency',fc,'SampleRate',fs);
radsig = radiator(sig.',radiatingangles);
```


## Plot Radiated Signal

Plot the input signal to the radiator and the radiated signals.

```
plot(t(1:300)*1e6,real(sig(1:300)))
hold on
plot(t(1:300)*le6,real(radsig(1:300,1)))
plot(t(1:300)*1e6,real(radsig(1:300,2)))
hold off
xlabel('Time (\mu sec)')
ylabel('Amplitude')
legend('Input signal','Radiate to (30,10)','Radiate to (20,50)')
```



Plot the spectra of the signal that is radiated to $(30,10)$ degrees.
periodogram(real(radsig(:,1)),rectwin(size(radsig,1)),4096,fs);


## Radiate Wideband Polarized Fields from Array

Examine the polarized field produced by the wideband radiator from a five-element uniform line array (ULA) composed of short-dipole antenna elements.

Set up the ULA of five short-dipole antennas with polarization enabled. The element spacing is set to $1 / 2$ wavelength of the carrier frequency. Construct the wideband radiator System object ${ }^{\mathrm{TM}}$.

```
fc = 100e6;
c = physconst('LightSpeed');
lam = c/fc;
antenna = phased.ShortDipoleAntennaElement;
array = phased.ULA('Element',antenna,'NumElements',5,'ElementSpacing',lam/2);
```

Radiate a signal consisting of the sum of three sine waves. Radiate the signal into two different directions. Radiated angles are azimuth and elevation angles defined with respect to a local coordinate system. The local coordinate system is defined by 10 degree rotation around the x -axis from the global coordinates.

```
fs = 25e6;
f1 = 2e6;
f2 = 10e6;
f3 = 11e6;
dt = 1/fs;
fc = 100e6;
```

```
t = [0:dt:100e-6];
sig = 5.0*sin(2*pi*f1*t) + 2.0*sin(2*pi*f2*t + pi/10) + 4*sin(2*pi*f3*t + pi/2);
radiatingAngle = [30 30; 0 20];
laxes = rotx(10);
radiator = phased.WidebandRadiator('Sensor',array,'SampleRate',fs,...
    'CarrierFrequency',fc,'Polarization','Combined');
y = radiator(sig.',radiatingAngle,laxes);
```

Plot the first 200 samples of the $y$ and $z$ components of the polarized field propagating in the [30, 0] direction.

```
plot(10^6*t(1:200),real(y(1).Y(1:200)))
hold on
plot(10^6*t(1:200),real(y(1).Z(1:200)))
hold off
xlabel('Time (\mu sec)')
ylabel('Amplitude')
legend('Y Polarization','Z Polarization')
```



## More About

## Subband Frequency Processing

Subband processing decomposes a wideband signal into multiple subbands and applies narrowband processing to the signal in each subband. The signals for all subbands are summed to form the output signal.

When using wideband frequency System objects or blocks, you specify the number of subbands, $N_{\mathrm{B}}$, in which to decompose the wideband signal. Subband center frequencies and widths are automatically computed from the total bandwidth and number of subbands. The total frequency band is centered on the carrier or operating frequency, $f_{c}$. The overall bandwidth is given by the sample rate, $f_{s}$. Frequency subband widths are $\Delta f=f_{s} / N_{\mathrm{B}}$. The center frequencies of the subbands are

$$
f_{m}=\left\{\begin{array}{c}
f_{c}-\frac{f_{s}}{2}+(m-1) \Delta f, \quad N_{B} \text { even } \\
f_{c}-\frac{\left(N_{B}-1\right) f_{s}}{2 N_{B}}+(m-1) \Delta f, \quad N_{B} \text { odd }
\end{array}, m=1, \ldots, N_{B}\right.
$$

Some System objects let you obtain the subband center frequencies as output when you run the object. The returned subband frequencies are ordered consistently with the ordering of the discrete Fourier transform. Frequencies above the carrier appear first, followed by frequencies below the carrier.

## Version History

Introduced in R2015b

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\text {TM }}$.
Usage notes and limitations:
See "System Objects in MATLAB Code Generation" (MATLAB Coder).

## See Also

phased.Radiator| phased.Collector|phased.WidebandCollector|
phased.WidebandFreeSpace

## reset

System object: phased.WidebandRadiator
Package: phased
Reset states of System object

## Syntax

reset(sWBR)

## Description

reset ( $s W B R$ ) resets the internal state of the phased.WidebandRadiator object, sWBR. If the SeedSource property applies, and has the value 'Property', then this method resets the state of the random number generator.

## Input Arguments

sWBR - Wideband radiator
System object
Wideband radiator, specified as a System object.
Example: phased.WidebandRadiator

## Version History <br> Introduced in R2015b

## step

System object: phased.WidebandRadiator
Package: phased
Radiate wideband signals

## Syntax

```
sigrad = step(sWBR,sig,ang)
sigrad = step(sWBR,sig,ang,laxes)
sigrad = step(sWBR,sig,ang,wts)
sigrad = step(sWBR,sig,ang,steerang)
```


## Description

Note Starting in R2016b, instead of using the step method to perform the operation defined by the System object, you can call the object with arguments, as if it were a function. For example, y = step(obj, $x$ ) and $y=o b j(x)$ perform equivalent operations.
sigrad = step(sWBR, sig,ang) radiates the signal sig in the directions specified by ang. For each direction, the method computes the radiated signal, sigrad, by summing the contributions of each element or subarray.
sigrad = step(sWBR,sig,ang,laxes) radiates the signal using the specified the local coordinate system of the radiator, laxes. This syntax applies when you set the EnablePolarization property to true.
sigrad $=$ step(sWBR,sig,ang,wts) radiates the signal using wts as the weight vector when the WeightsInputPort property is true.
sigrad = step(sWBR,sig,ang,steerang) radiates the signal and uses steerang as the subarray steering angle. steerang must be a length-2 column vector in the form of [AzimuthAngle; ElevationAngle]. This syntax applies when you use a subarray as the Sensor property and set the SubarraySteering property of the sensor to 'Phase' or 'Time'.

You can combine optional input arguments when you set their enabling properties in the System object during construction. Optional inputs must be listed in the same order as their enabling properties. For example, sigrad $=$ step(sWBR, sig, laxes, wts, steerang) is valid when you set both EnablePolarization and WeightsInputPort to true and set the SubarraySteering property of the sensor.

Note The object performs an initialization the first time the object is executed. This initialization locks nontunable properties and input specifications, such as dimensions, complexity, and data type of the input data. If you change a nontunable property or an input specification, the System object issues an error. To change nontunable properties or inputs, you must first call the release method to unlock the object.

## Input Arguments

## sWBR - Wideband radiator

System object
Wideband radiator, specified as a phased.WidebandRadiator System object.
Example: phased.WidebandRadiator

## sig - Input signals

$M$-by-1 complex-valued column vector | $M$-by- $N$ complex-valued matrix
Input signals, specified as an $M$-by- 1 complex-valued column vector or $M$-by- $N$ complex-valued matrix. The quantity $M$ is the number of sample values (snapshots) of the signal. If sig is a column vector, the same signal is radiated through all elements. If sig is a matrix, $N$ is the number of sensor elements in the array. For subarrays, $N$ is the number of subarrays. Each column of sig represents the field radiated by the corresponding element or subarray.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

```
Example: [[0;1;2;3;4;3;2;1;0],[1;2;3;4;3;2;1;0;0]]
```

Data Types: double
Complex Number Support: Yes

## ang - Radiating directions

2-by-L real-valued matrix | 1-by-L real-valued row vector
Radiating directions of the signal, specified as 2 -by- $L$ real-valued matrix or 1-by-L real-valued row vector. The quantity $L$ is the number of directions to radiate. If ang is a matrix, each column has the form [azimuth;elevation]. If ang is a row vector, each entry represents the azimuthal direction. The elevation direction is zero degrees. Angle units are in degrees. Angles are defined with respect to the local coordinate system of the array.

When the sensory array is a uniform linear array, ang represents the broadside angle.

## Data Types: double

## laxes - Local coordinate system axes

eye $(3,3)$ (default) | 3-by-3 real-valued orthonormal matrix
Local coordinate system axes, specified as a 3-by-3 real-valued matrix orthonormal matrix. The matrix columns specify the $x, y$, and $z$ axes of the local coordinate system. Each column takes the form [ $x ; y ; z$ ] with respect to the global coordinate system. This argument only applies when the EnablePolarization property is set to true.
Data Types: double

## wts - Weight vector

ones ( $\mathrm{N}, 1$ ) (default) | $N$-by-1 complex-valued column vector
Weight vector, specified as an $N$-by-1 complex-valued column vector. Each weight vector element multiplies the signal at the corresponding element or subarray. $N$ is the number of radiating elements or subarrays. This argument only applies when the WeightsInputPort property is true.

## Data Types: double

Complex Number Support: Yes

## steerang - Subarray steering angle

2-by-1 real-valued column vector
Subarray steering angle, specified as a 2-by-1 real-valued column vector in the form of [AzimuthAngle; ElevationAngle]. This argument applies only when the Sensor property refers to a subarray and the SubarraySteering property of the sensor is set to 'Phased ' or 'Time'. Angles are defined with respect to the local coordinate system axes. Angle units are in degrees.
Data Types: double

## Output Arguments

## sigrad - Radiated signal

M-by-L complex-valued matrix | 1-by- $L$ array of struct type
Radiated signal, returned as an $M$-by- $L$ complex-valued matrix or 1-by- $L$ array of struct type depending on whether polarization is enabled. The radiated field is the combined far-field output from all elements or subarrays. The quantity $M$ is the number of sample values (snapshots) of the signal. The quantity $L$ is the number of entries in ang.

- If you set EnablePolarization to false, sigrad is an $M$-by- $L$ complex-valued matrix.
- If you set EnablePolarization is true, sigrad is a 1-by-L array of struct type. Each struct in the array has three data fields: sigrad.X, sigrad.Y, sigrad. $Z$ which correspond to the $x, y$, and $z$ components of the electromagnetic field. Electromagnetic field components are defined with respect to the global coordinate system. Each data field is an $M$-by- 1 column vector.


## Examples

## Radiate Wideband Energy from Array

Create a 5-by-5 URA and space the elements one-half wavelength apart. The wavelength corresponds to a design frequency of 300 MHz .

## Create 5-by-5 URA Array of Cosine Elements

```
c = physconst('LightSpeed');
fc = 100e6;
lam = c/fc;
antenna = phased.CosineAntennaElement('CosinePower',[2,2]);
array = phased.URA('Element',antenna,'Size',[5,5],'ElementSpacing',[0.5,0.5]*lam);
```


## Create and Radiate Wideband Signal

Radiate a wideband signal consisting of three sinusoids at 2,10 and 11 MHz . Set the sampling rate to 25 MHz . Radiate the fields into two directions: $(30,10)$ degrees azimuth and elevation and $(20,50)$ degrees azimuth and elevation.

```
fs = 25e6;
f1 = 2e6;
f2 = 10e6;
```

```
f3 = 11e6;
dt = 1/fs;
Tsig = 100e-6;
t = [0:dt:Tsig];
sig = 5.0*sin(2*pi*f1*t) + 2.0*sin(2*pi*f2*t + pi/10) + 4*sin(2*pi*f3*t + pi/2);
radiatingangles = [30 10; 20 50]';
radiator = phased.WidebandRadiator('Sensor',array,'CarrierFrequency',fc,'SampleRate',fs);
radsig = radiator(sig.',radiatingangles);
```


## Plot Radiated Signal

Plot the input signal to the radiator and the radiated signals.
plot(t(1:300)*le6, real(sig(1:300)))
hold on
plot(t(1:300)*1e6, real(radsig(1:300,1)))
plot(t(1:300)*le6, real(radsig(1:300,2)))
hold off
xlabel('Time (\mu sec)')
ylabel('Amplitude')
legend('Input signal','Radiate to $(30,10) ', ' R a d i a t e ~ t o ~(20,50) ')$


Plot the spectra of the signal that is radiated to $(30,10)$ degrees.
periodogram(real(radsig(:,1)),rectwin(size(radsig,1)),4096,fs);


## Radiate Wideband Polarized Fields from Array

Examine the polarized field produced by the wideband radiator from a five-element uniform line array (ULA) composed of short-dipole antenna elements.

Set up the ULA of five short-dipole antennas with polarization enabled. The element spacing is set to $1 / 2$ wavelength of the carrier frequency. Construct the wideband radiator System object ${ }^{\mathrm{TM}}$.

```
fc = 100e6;
c = physconst('LightSpeed');
lam = c/fc;
antenna = phased.ShortDipoleAntennaElement;
array = phased.ULA('Element',antenna,'NumElements',5,'ElementSpacing',lam/2);
```

Radiate a signal consisting of the sum of three sine waves. Radiate the signal into two different directions. Radiated angles are azimuth and elevation angles defined with respect to a local coordinate system. The local coordinate system is defined by 10 degree rotation around the x -axis from the global coordinates.

```
fs = 25e6;
f1 = 2e6;
f2 = 10e6;
f3 = 11e6;
dt = 1/fs;
fc = 100e6;
```

```
t = [0:dt:100e-6];
sig = 5.0*sin(2*pi*f1*t) + 2.0*sin(2*pi*f2*t + pi/10) + 4*sin(2*pi*f3*t + pi/2);
radiatingAngle = [30 30; 0 20];
laxes = rotx(10);
radiator = phased.WidebandRadiator('Sensor',array,'SampleRate',fs,...
    'CarrierFrequency',fc,'Polarization','Combined');
y = radiator(sig.',radiatingAngle,laxes);
```

Plot the first 200 samples of the $y$ and $z$ components of the polarized field propagating in the [ 30,0 ] direction.

```
plot(10^6*t(1:200),real(y(1).Y(1:200)))
hold on
plot(10^6*t(1:200),real(y(1).Z(1:200)))
hold off
xlabel('Time (\mu sec)')
ylabel('Amplitude')
legend('Y Polarization','Z Polarization')
```



## Version History

Introduced in R2015b

## See Also

phased.BeamscanEstimator|phased.Collector|phased.WidebandCollector | phased.Radiator| phased.RootMUSICEstimator

## polarpattern

Interactive plot of radiation patterns in polar format

## Description

The polarpattern object creates an interactive plot of antenna or array radiation patterns in polar format with uniformly spaced angles. You can also plot other types of polar data. Use this plot for interactive data visualization or measurement. To change the properties, zoom in, or add more data to the plot, right-click or scroll or drag the Polar Measurement window.


## Creation

## Syntax

polarpattern
polarpattern(data)
polarpattern(angle,magnitude)
polarpattern( ,Name, Value)
polarpattern(ax, )
$\mathrm{p}=$ polarpattern( $\qquad$ )

```
p = polarpattern('gco')
```


## Description

polarpattern creates an empty polar plot. You can add plots of antenna or array radiation patterns and other types of data to the plot by importing saved polari objects from MAT-files.
polarpattern(data) creates a polar plot with real magnitude values in the vector data with angles uniformly spaced on the unit circle starting at 0 degrees. Magnitudes may be negative when dB data units are used. For a matrix data, columns of data are independent datasets. For N -data arrays, dimensions 2 and greater are independent datasets. For complex values, magnitude and angle are derived from data.
polarpattern(angle, magnitude) creates a polar plot for a set of angles and corresponding magnitudes. You can also create polar plots from multiple sets of angle vectors in degrees and corresponding sets of magnitude using the syntax: polarpattern(angle1, magnitude1,..., angleN, magnitudeN).
polarpattern (__ ,Name, Value) creates a polar plot, with additional properties specified by one or more name-value pair arguments. Name is the property name and Value is the corresponding property value. You can specify several name-value pair arguments in any order as Name1, Value1, . . . NameN, ValueN. Unspecified properties retain their default values. To list all the property names and values, use details( p ). You can use the properties to extract data about the radiation pattern from the polar plot. For example, p = polarpattern(data,'Peaks',3) identifies and displays the three highest peaks in the pattern data.

For a list of properties, see PolarPattern.
polarpattern (ax, __ ) creates a polar plot using axes object, ax instead of the current axes object.
p = polarpattern( ___ ) creates a polari object using any combination of input arguments from the previous syntaxes. Use this syntax to customize the plot or add measurements.
$\mathrm{p}=$ polarpattern('gco') creates a polar plot object from the polar pattern in the current figure.

## Input Arguments

## data - Antenna or array data

real length- $M$ vector | real $M$-by- $N$ matrix | real multidimensional array | complex vector or matrix
Antenna or array data, specified as one of these options

- A real length- $M$ vector, containing $M$ magnitude values with angles their defined as $\frac{(0: M-1)}{M} \times 360^{\circ}$ degrees.
- A real $M$-by- $N$ matrix, containing $M$ magnitude values in a dataset and $N$ such independent data sets. Each column of the matrix has angles in degrees from the vector $\frac{(0: M-1)}{M} \times 360^{\circ}$.
- A real multidimensional array. Arrays with 2 or more dimensions contain independent data sets.
- A complex vector or matrix, that contains Cartesian coordinates ( $x, y$ ) of each point. $x$ contains the real part of the data and $y$ contains the imaginary part of the data.

When the data is in a logarithmic form, such as dB , magnitude values can be negative. In this case, polarpattern plots the smallest magnitude values at the origin of the polar plot and largest magnitude values at the maximum radius.

## Data Types: double

## angle - Set of angles

vector
Set of angles in degrees, specified as a vector.

## Data Types: double

## magnitude - Set of magnitude values

## vector | matrix

Set of magnitude values, specified as a vector or a matrix. If you specify this input as a matrix, each column is an independent set of magnitude values and corresponds to the same set of angles in the same column of the angle input.
Data Types: double

## ax - Axes of polar plot

axes object
Axes of the polar plot, specified as an axes object.

## Output Arguments

## p - polari object

polari object
Stores a polari object with a set of properties. Use p to modify properties of the plot after creation. For a list of all the properties, see PolarPattern Properties (Antenna Toolbox).
Example: $P=$ polarplot $(V)$

## Object Functions

## Examples

## Plot Cosine Pattern in Polar Coordinates

Specify a cosine antenna pattern from $0^{\circ}$ to $360^{\circ}$ in azimuth at $0^{\circ}$ elevation. Then, plot the antenna pattern using polarpattern.

Create the pattern.
az = [0:360];
$\mathrm{p}=\mathrm{abs}(\operatorname{cosd}(\mathrm{az}))$;
Plot the polar pattern of the antenna for an azimuth cut at $0^{\circ}$ elevation.

```
polarpattern(p,'TitleTopTextInterpreter','tex','TitleTop','Azimuth Cut (Elevation Angle = 0^{\ci
```



## Azimuth Pattern of a 3-by-2 URA

Construct a 3-by-2 rectangular lattice URA. By default, the array consists of isotropic antenna elements. Assume the operating frequency is 1 GHz . Then, plot the antenna pattern using polarpattern.

Create the array.
array = phased.URA('Size',[3 2]);
$\mathrm{fc}=1.0 \mathrm{e} 9$;
Plot the polar pattern of the array for an elevation cut at $0^{\circ}$ azimuth.

```
c = physconst('LightSpeed');
p = pattern(array,fc,[-180:180],0,'PropagationSpeed',c,'CoordinateSystem',...
    'polar','Type','powerdb','Normalize',true);
polarpattern([-180:180],p);
```



## Polar Pattern Display with Title for Short-Dipole Antenna

Specify a short-dipole antenna with the dipole oriented along the $z$-axis and operating at 250 MHz . Then, plot the antenna pattern using polarpattern and specifying a title.

Create the short-dipole antenna element System object ${ }^{\mathrm{TM}}$.
antenna = phased.ShortDipoleAntennaElement('FrequencyRange',[100e6,600e6],...
'AxisDirection','Z');
$\mathrm{fc}=250.0 \mathrm{e} 6$;
Plot the polar pattern of the antenna for an elevation cut at $0^{\circ}$ azimuth.

```
v = pattern(antenna,fc,0,-90:90);
polarpattern([-90:90],v,'TitleTopTextInterpreter','tex',...
    'TitleTop','Elevation Cut (Azimuth Angle = 0^{\circ})');
```



## Polar Pattern Properties

Specify a short-dipole antenna with the dipole oriented along the $z$-axis and operating at 250 MHz . Then, plot the antenna pattern using polarpattern and specifying a title.

Create the short-dipole antenna element System object ${ }^{\mathrm{TM}}$.
antenna = phased.ShortDipoleAntennaElement('FrequencyRange',[100e6,600e6],...
'AxisDirection','Z');
$\mathrm{fc}=250.0 \mathrm{e} 6$;
Create the polar pattern of the antenna for an elevation cut at $0^{\circ}$ azimuth.
p = pattern(antenna, fc, 0, -90:90);
P = polarpattern([-90:90], p,'TitleTopTextInterpreter','tex',...
'TitleTop','Elevation Cut (Azimuth Angle = 0^\{\circ\})');

## Elevation Cut (Azimuth Angle $=0^{\circ}$ )



Display the properties of the plot.

```
details(P)
```

    internal.polari handle with properties:
                        Interactive: 1
                LegendLabels:
                    AntennaMetrics: 0
                        CleanData: 0
                        AngleData: [181x1 double]
                            MagnitudeData: [181x1 double]
                            IntensityData: []
                            AngleMarkers: [0x1 struct]
                            CursorMarkers: [0x1 struct]
                    PeakMarkers: [0x1 struct]
                    ActiveDataset: 1
            AngleLimVisible: 0
                    LegendVisible: 0
                            Span: 0
                            TitleTop: 'Elevation Cut (Azimuth Angle = 0^\{\circ\})'
                TitleBottom:
                    Peaks: []
                    FontSize: 10
                MagnitudeLim: [-40 10]
                MagnitudeAxisAngle: 75
                    MagnitudeTick: [-40 -30 -20 -10 0 10]
    MagnitudeTickLabelColor: 'k'

AngleLim: [0 360]
AngleTickLabel: \{'0' '15' '30' '45' '60' '75' '90' '105' '120' '135'
AngleTickLabelColor: 'k'
TitleTopFontSizeMultiplier: 1.1000
TitleBottomFontSizeMultiplier: 0.9000
TitleTopFontWeight: 'bold'
TitleBottomFontWeight: 'normal'
TitleTopTextInterpreter: 'tex'
TitleBottomTextInterpreter: 'none'
TitleTopOffset: 0.1500
TitleBottomOffset: 0.1500
ToolTips: 1
MagnitudeLimBounds: [-Inf Inf]
MagnitudeFontSizeMultiplier: 0.9000
AngleFontSizeMultiplier: 1
AngleAtTop: 90
AngleDirection: 'ccw'
AngleResolution: 15
AngleTickLabelRotation: 0
AngleTickLabelFormat: '360'
AngleTickLabelColorMode: 'contrast'
PeaksOptions: \{\}
AngleTickLabelVisible: 1
Style: 'line'
DataUnits: 'dB'
DisplayUnits: 'dB'
NormalizeData: 0
ConnectEndpoints: 0
DisconnectAngleGaps: 0
EdgeColor: 'k'
LineStyle: '-'
LineWidth: 1
FontName: 'Helvetica'
FontSizeMode: 'auto'
GridForegroundColor: [0.8000 0.8000 0.8000]
GridBackgroundColor: 'w'
DrawGridToOrigin: 0
GridOverData: 0
GridAutoRefinement: 0
GridWidth: 0.5000
GridVisible: 1
ClipData: 1
TemporaryCursor: 1
MagnitudeLimMode: 'auto'
MagnitudeAxisAngleMode: 'auto'
MagnitudeTickMode: 'auto'
MagnitudeTickLabelColorMode: 'contrast'
MagnitudeTickLabelVisible: 1
MagnitudeUnits: ''
IntensityUnits: ''
Marker: 'none'
MarkerSize: 6
Parent: [1x1 Figure]
NextPlot: 'replace'
ColorOrder: [7x3 double]
ColorOrderIndex: 1
SectorsColor: [16x3 double]
SectorsAlpha: 0.5000

1-2065

View: 'full'<br>ZeroAngleLine: 0

# Version History 

Introduced in R2016a
See Also
PolarPattern Properties

## add

Add data to polar plot

## Syntax

```
add(p,d)
add(p,angle,magnitude)
```


## Description

$\operatorname{add}(\mathrm{p}, \mathrm{d})$ adds new antenna data to the polar plot, p based on the real amplitude values, data.
add ( $p$, angle, magnitude) adds data sets of angle vectors and corresponding magnitude matrices to polar plot $p$.

## Input Arguments

p - Polar plot
scalar handle
Polar plot, specified as a scalar handle.

## data - Antenna or array data

real length- $M$ vector | real $M$-by- $N$ matrix | real $N$ - $D$ array | complex vector or matrix
Antenna or array data, specified as one of the following:

- A real length- $M$ vector, where $M$ contains the magnitude values with angles assumed to be $\frac{(0: M-1)}{M} \times 360^{\circ}$ degrees.
- A real $M$-by- $N$ matrix, where $M$ contains the magnitude values and $N$ contains the independent data sets. Each column in the matrix has angles taken from the vector $\frac{(0: M-1)}{M} \times 360^{\circ}$ degrees. The set of each angle can vary for each column.
- A real $N-D$ array, where $N$ is the number of dimensions. Arrays with dimensions 2 and greater are independent data sets.
- A complex vector or matrix, where data contains Cartesian coordinates $((x, y)$ of each point. $x$ contains the real part of data and $y$ contains the imaginary part of data.

When data is in a logarithmic form such as dB , magnitude values can be negative. In this case,polarpattern plots the lowest magnitude values at the origin of the polar plot and highest magnitude values at the maximum radius.

## angle - Set of angles

vector in degrees
Set of angles, specified as a vector in degrees.

## magnitude - Set of magnitude values

vector | matrix
Set of magnitude values, specified as a vector or a matrix. For a matrix of magnitude values, each column is an independent set of magnitude values and corresponds to the same set of angles.

## Examples

## Add Data to Existing Polar Plot

Create a cosine-pattern antenna and plot the pattern from $0^{\circ}$ to $36^{\circ}$.
az = [0:360];
p1 = abs(cosd(az));
Plot the polar pattern.
P = polarpattern(p1);


Create a second cosine-pattern antenna rotated by $60^{\circ}$. Add this pattern to the existing pattern.
p2 = abs (cosd(az - 50)) ; add(P,p2);


## Add Second Plot to Polar Pattern

Create a cosine antenna and plot the polar pattern of its directivity at 75 MHz .
cosineantenna $=$ phased.CosineAntennaElement('FrequencyRange',[1.0e0 100.0e9],...
'CosinePower',[2,2]);
p1 = pattern(cosineantenna,75.0e6,[-90:90],0,'Type','Directivity');
P = polarpattern([-90:90], p1);


Create an isotropic antenna. Calculate the directivity of this antenna at 75 MHz .

```
isoantenna = phased.IsotropicAntennaElement('FrequencyRange',...
```

    [1.0e0 100.0e9]);
    p2 = pattern(isoantenna,75.0e6,[-180:180],0,'Type','Directivity');

Add the directivity plot of the isotropic antenna to the directivity plot of the cosine antenna. add(P,[-180:180],p2);


## Version History

Introduced in R2016a

## See Also

addCursor| animate |createLabels|findLobes|replace| showPeaksTable| showSpan

## addCursor

Add cursor to polar plot angle

## Syntax

```
addCursor(p,angle)
addCursor(p,angle,index)
id = addCursor(
```

$\qquad$

``` )
```


## Description

addCursor ( p , angle) adds a cursor to the active polar plot, p , at the data point closest to the specified angle. Angle units are in degrees.

The first cursor added is called ' C 1 ', the second ' C 2 ', and so on.
addCursor ( p , angle, index) adds a cursor at a specified data set index. index can be a vector of indices.
id = addCursor( $\qquad$ ) returns a cell array with one ID for each cursor created. You can specify any of the arguments from the previous syntaxes.

## Input Arguments

p - Polar plot
scalar handle
Polar plot, specified as a scalar handle.

## angle - Angle values

scalar in degrees | vector in degrees
Angle values at which the cursor is added, specified as a scalar or a vector in degrees.

## index - Data set index

scalar | vector
Data set index, specified as a scalar or a vector.

## Examples

## Add Cursors to Single Polar Pattern Plot

Create a cosine antenna and plot the polar pattern of its directivity at 75 MHz . Then add cursors at two $150^{\circ}$ and $270^{\circ}$.

```
cosineantenna = phased.CosineAntennaElement('FrequencyRange',[1.0e0 100.0e9],...
    'CosinePower',[2,2]);
p = pattern(cosineantenna,75.0e6,[-90:90],0,'Type','Directivity');
```

```
P = polarpattern([-90:90],p);
```

addCursor(P,[45 135]);


## Add Cursors to Multiple Polar Pattern Plots

Create a cosine antenna and plot the polar pattern of its directivity at 75 MHz . Then create an isotropic antenna. Also calculate the directivity of this antenna at 75 MHz . Add the directivity plot of the isotropic antenna to the directivity plot of the cosine antenna. Then add cursors at several points.

```
cosineantenna = phased.CosineAntennaElement('FrequencyRange',[1.0e0 100.0e9],...
    'CosinePower',[2,2]);
p1 = pattern(cosineantenna,75.0e6,[-90:90],0,'Type','Directivity');
P = polarpattern([-90:90],p1);
isoantenna = phased.IsotropicAntennaElement('FrequencyRange',...
    [1.0e0 100.0e9]);
p2 = pattern(isoantenna,75.0e6,[-180:180],0,'Type','Directivity');
add(P,[-180:180],p2);
```



Add a cursor at approximately $30^{\circ}$ to the cosine antenna pattern (designated by index 1) and at $150^{\circ}$ and $270^{\circ}$ to the isotropic polar pattern (designated by index 2).
addCursor(P,[30.5 149.0 314.7],[1 2 1]);


## Version History

Introduced in R2016a

## See Also

add|animate|createLabels|findLobes|replace|showPeaksTable| showSpan

## animate

Replace existing data with new data for animation

## Syntax

animate(p,data)
animate( p , angle, magnitude)

## Description

animate ( p , data) removes all the current data from polar plot, p and adds new data, based on real amplitude values, data.
animate( p , angle, magnitude) removes all the current data polar plot, p and adds new data sets of angle vectors and corresponding magnitude matrices.

## Input Arguments

## p - Polar plot

scalar handle
Polar plot, specified as a scalar handle.
data - Antenna or array data
real length- $M$ vector | real $M$-by- $N$ matrix | real $N-D$ array | complex vector or matrix
Antenna or array data, specified as one of the following:

- A real length $-M$ vector, where $M$ contains the magnitude values with angles assumed to be $\frac{(0: M-1)}{M} \times 360^{\circ}$ degrees.
- A real $M$-by- $N$ matrix, where $M$ contains the magnitude values and $N$ contains the independent data sets. Each column in the matrix has angles taken from the vector $\frac{(0: M-1)}{M} \times 360^{\circ}$ degrees. The set of each angle can vary for each column.
- A real $N-D$ array, where $N$ is the number of dimensions. Arrays with dimensions 2 and greater are independent data sets.
- A complex vector or matrix, where data contains Cartesian coordinates ( $(x, y)$ of each point. $x$ contains the real part of data and $y$ contains the imaginary part of data.

When data is in a logarithmic form such as dB , magnitude values can be negative. In this case,polarpattern plots the lowest magnitude values at the origin of the polar plot and highest magnitude values at the maximum radius.

## angle - Set of angles

vector in degrees
Set of angles, specified as a vector in degrees.

## magnitude - Set of magnitude values

vector | matrix
Set of magnitude values, specified as a vector or a matrix. For a matrix of magnitude values, each column is an independent set of magnitude values and corresponds to the same set of angles.

## Examples

## Animate Cosine Pattern Antenna Plot

Create a cosine-pattern antenna and plot the pattern from $0^{\circ}$ to $360^{\circ}$.
az = [0:360];
p1 $=$ abs(cosd(az));
Plot the polar pattern.

```
P = polarpattern(p1);
```



Create a second cosine-pattern antenna rotated by $60^{\circ}$. Animate the pattern by adding this pattern.

```
p2 = abs(cosd(az - 50));
animate(P,p2);
```



## Animate Existing Polar Azimuth Plot Data

Create a 15 -element ULA of cosine antennas with elements spaced one-half wavelength apart. Plot the directivity of the array at 20 GHz .
$\mathrm{fc}=20.0 \mathrm{e} 9$;
c = physconst('Lightspeed');
lam = c/fc;
angs $=$ [-180:1:180];
antenna $=$ phased.CosineAntennaElement('FrequencyRange',[1.0e9,100.0e9],...
'CosinePower',[2.5 2.5]);
array = phased.ULA('Element',antenna,'NumElements',15,'ElementSpacing',lam/2);
$\mathrm{a}=$ pattern(array,fc,angs,0);
P = polarpattern(angs,a);


Then, steer the array to $45^{\circ}$ and, using the animate method, replace the existing polar plot with the steered array directivity.

```
steervec = phased.SteeringVector('SensorArray',array,'PropagationSpeed',c,...
    'IncludeElementResponse',true);
sv = steervec(fc,[45;0]);
a1 = pattern(array,fc,angs,0,'Weights',sv);
animate(P,angs,al);
```



## Version History

Introduced in R2016a

## See Also

add |addCursor|createLabels|findLobes|replace|showPeaksTable|showSpan

## createLabels

Create legend labels for polar plot

## Syntax

createLabels(p,format, array)

## Description

createLabels( p , format, array) adds the specified format label to each array of the polar plot $p$. The labels are stored as a cell array in the LegendLabels property of $p$.

## Input Arguments

p - Polar plot
scalar handle
Polar plot, specified as a scalar handle.

## format - Format for legend label

cell array
Format for legend label added to the polar plot, specified as a cell array. For more information on legend label format see, legend.

Data Types: char
array - Values to apply to format
array
Values to apply to format, specified as an array. The values can be an array of angles or array of magnitude.

## Examples

## Add Legend Label to Polar Plot

Create a polar plot of cosine powers rotated in $30^{\circ}$ increments. Generate a legend label for this plot.

```
az = [0:359]';
a1 = abs(cosd(az).^5);
a2 = abs(cosd(az - 30).^5);
a3 = abs(cosd(az - 60).^5);
a4 = abs(cosd(az - 90).^5);
P = polarpattern([a1,a2,a3,a4],'Style','filled');
createLabels(P,'az = %d#deg',0:30:90)
```



## Version History

Introduced in R2016a

See Also<br>add | addCursor| animate | findLobes | replace | showPeaksTable| showSpan

## findLobes

Main, back, and side lobe data

## Syntax

$L=$ findLobes $(p)$
$L=$ findLobes $(p$, index)

## Description

$L=f i n d L o b e s(p)$ returns a structure, $L$, defining the main, back, and side lobes of the antenna or array radiation pattern in the specified polar plot, p .
$L=$ findLobes $(p$, index $)$ returns the radiation pattern lobes from the data set specified in index.

## Input Arguments

## p - Polar plot

scalar handle
Polar plot, specified as a scalar handle.

## index - Index of data set

scalar
Index of data set, specified as a scalar.

## Output Arguments

## L - Main,back, and side lobe data

structure
Main,back, and side lobe data, returned as a structure.

## Examples

## Find Lobes of Isotropic Antenna ULA

Create a 15 -element ULA of isotropic antenna with elements spaced one-half wavelength apart. Plot the directivity of the array at 20 GHz . Then, find the mainlobe, sidelobe, and backlobe directions of the array pattern.

```
fc = 20.0e9;
c = physconst('Lightspeed');
lam = c/fc;
angs = [-180:1:180];
antenna = phased.IsotropicAntennaElement('FrequencyRange',[1.0e9,100.0e9]);
array = phased.ULA('Element',antenna,'NumElements',15,'ElementSpacing',lam/2);
```

a = pattern(array,fc,angs,0);
$P=$ polarpattern(angs,a);


```
L = findLobes(P)
L = struct with fields:
    mainLobe: [1x1 struct]
    backLobe: [1x1 struct]
    sideLobes: [1x1 struct]
            FB: 0
            SLL: 0
            HPBW: 8.0000
            FNBW: 16.0000
            FBIdx: [181 1]
        SLLIdx: [181 361]
        HPBWIdx: [357 5]
        HPBWAng: [176 -176]
        FNBWIdx: [173 189]
```


## Find Lobes of Steered Isotropic Antenna ULA Patterns

Create a 15 -element ULA of isotropic antenna with elements spaced one-half wavelength apart. Plot the directivity of the array at 20 GHz . Then steer the array to $45^{\circ}$ azimuth and plot the directivity. Then, find the mainlobe, sidelobe, and backlobe directions of the array pattern.

```
fc = 20.0e9;
c = physconst('Lightspeed');
lam = c/fc;
angs = [-180:1:180];
antenna = phased.IsotropicAntennaElement('FrequencyRange',[1.0e9,100.0e9]);
array = phased.ULA('Element',antenna,'NumElements',15,'ElementSpacing',lam/2);
a = pattern(array,fc,angs,0);
P = polarpattern(angs,a);
```



Steer the array to $45^{\circ}$ azimuth and add the steered pattern to the polar plot.

```
steervec = phased.SteeringVector('SensorArray',array,'PropagationSpeed',c);
sv = steervec(fc,[45;0]);
a1 = pattern(array,fc,angs,0,'Weights',sv);
add(P,angs,al);
```



Find the lobes of the steered pattern.
$L=$ findLobes $(P, 2)$;
L.mainLobe

```
ans = struct with fields:
        index: 226
    magnitude: 11.7609
        angle: 45
        extent: [216 238]
```


## Version History

Introduced in R2016a

## See Also

add | addCursor|animate | createLabels | replace | showPeaksTable | showSpan

## replace

Replace polar plot data with new data

## Syntax

replace ( p , data)
replace( p , angle, magnitude)

## Description

replace ( p , data) removes all data from polar plot, p and adds new data based on real amplitude values, data.
replace ( $p$, angle, magnitude) removes all the current data and adds new data sets of angle vectors and corresponding magnitude matrices to the polar plot, $p$.

## Input Arguments

## p - Polar plot

scalar handle
Polar plot, specified as a scalar handle.
data - Antenna or array data
real length- $M$ vector | real $M$-by- $N$ matrix | real $N-D$ array | complex vector or matrix
Antenna or array data, specified as one of the following:

- A real length- $M$ vector, where $M$ contains the magnitude values with angles assumed to be $\frac{(0: M-1)}{M} \times 360^{\circ}$ degrees.
- A real $M$-by- $N$ matrix, where $M$ contains the magnitude values and $N$ contains the independent data sets. Each column in the matrix has angles taken from the vector $\frac{(0: M-1)}{M} \times 360^{\circ}$ degrees. The set of each angle can vary for each column.
- A real $N-D$ array, where $N$ is the number of dimensions. Arrays with dimensions 2 and greater are independent data sets.
- A complex vector or matrix, where data contains Cartesian coordinates ( $(x, y)$ of each point. $x$ contains the real part of data and $y$ contains the imaginary part of data.

When data is in a logarithmic form such as dB , magnitude values can be negative. In this case,polarpattern plots the lowest magnitude values at the origin of the polar plot and highest magnitude values at the maximum radius.

## angle - Set of angles

vector in degrees
Set of angles, specified as a vector in degrees.

## magnitude - Set of magnitude values

vector | matrix
Set of magnitude values, specified as a vector or a matrix. For a matrix of magnitude values, each column is an independent set of magnitude values and corresponds to the same set of angles.

## Examples

## Replace Cosine Polar Plot with Rotated Cosine Polar Plot

Plot cosine pattern in polar coordinates. Specify a cosine antenna pattern from $0^{\circ}$ to $360^{\circ}$ in azimuth at $0^{\circ}$ elevation. Then, plot the antenna pattern using polarpattern.

Create the pattern.
az = [0:360];
a = abs(cosd(az));
Plot the polar pattern of the antenna for an azimuth cut at $0^{\circ}$ elevation.

```
P = polarpattern(a,'TitleTopTextInterpreter','tex','TitleTop','Azimuth Cut (Elevation Angle = 0^.
```



Replace this plot with a rotated cosine pattern.
$a=a b s(\operatorname{cosd}(a z+30.0))$;
replace(P,a);


## Replace Polar Plot Data with New Angle-Magnitude Data

Create a 15 -element ULA of cosine antennas with elements spaced one-half wavelength apart. Plot the directivity of the array at 20 GHz .
$\mathrm{fc}=20.0 \mathrm{e} 9$;
c = physconst('Lightspeed');
lam = c/fc;
angs = [-180:1:180];
antenna $=$ phased.CosineAntennaElement('FrequencyRange',[1.0e9,100.0e9],...
'CosinePower',[2.5 2.5]);
array = phased.ULA('Element',antenna,'NumElements',15,'ElementSpacing',lam/2);
a = pattern(array,fc,angs,0);
P = polarpattern(angs,a);


Then, steer the array to $45^{\circ}$ and, using the replace method, replace the existing polar plot with the steered array directivity.

```
steervec = phased.SteeringVector('SensorArray',array,'PropagationSpeed',c,...
    'IncludeElementResponse',true);
sv = steervec(fc,[45;0]);
al = pattern(array,fc,angs,0,'Weights',sv);
replace(P,angs,al);
```



## Version History

Introduced in R2016a

```
See Also
add| addCursor| animate| createLabels| findLobes| showPeaksTable| showSpan
```


## showPeaksTable

Show or hide peak marker table

## Syntax

showPeaksTable(p,vis)

## Description

showPeaksTable( $\mathrm{p}, \mathrm{vis}$ ) shows or hides a table of the peak values. By default, the peak values table is visible.

## Input Arguments

p - Polar plot
scalar handle
Polar plot, specified as a scalar handle.
vis - Show or hide peaks table 0 | 1

Show or hide peaks table, specified as 0 or 1.

## Examples

## Peaks of ULA Array in Polar Pattern

Create a 15 -element ULA of cosine antennas with elements spaced one-half wavelength apart. Then, plot the directivity of the array at 20 GHz .

```
fc = 20.0e9;
c = physconst('Lightspeed');
lam = c/fc;
angs = [-180:1:180];
antenna = phased.CosineAntennaElement('FrequencyRange',[1.0e9,100.0e9],...
    CosinePower',[2.5 2.5]);
array = phased.ULA('Element',antenna,'NumElements',15,'ElementSpacing',lam/2);
```

Plot the polar pattern and show three peaks of the antenna. When creating a polarpattern plot, if you specify the Peaks property, the peaks table is displayed by default.

```
a = pattern(array,fc,angs,0);
P = polarpattern(angs,a,'Peaks',3);
```



Hide the table. When the peaks table is hidden, the peak markers display the peak values. showPeaksTable(P,0);


## Version History

Introduced in R2016a

## See Also

add | addCursor| animate | createLabels |findLobes | replace | showSpan

## PolarPattern Properties

Control appearance and behavior of polar plot

## Description

Polar pattern properties control the appearance and behavior of the polar pattern object. By changing property values, you can modify certain aspects of the polar plot. To change the default properties use:
p = polarpattern( $\qquad$ ,Name, Value)

To view all the properties of the polar pattern object use:

```
details(p)
```


## Properties

## Antenna Metrics

## 'AntennaMetrics' - Show antenna metric <br> 0 (default) | 1

Show antenna metrics, specified as a comma-separated pair consisting of 'AntennaMetrics ' and 0 or 1. Antenna metric displays main, back, and side lobes of antenna/array pattern passed as input.
Data Types: logical

## 'Peaks' - Maximum number of peaks to compute for each data set positive integer | vector of integers

Maximum number of peaks to compute for each data set, specified as a comma-separated pair consisting of 'Peaks ' and a positive scalar or vector of integers.
Data Types: double

## Angle Properties

'AngleAtTop ' - Angle at top of polar plot
90 (default) | scalar in degrees
Angle at the top of the polar plot, specified as a comma-separated pair consisting of 'AngleAtTop' and a scalar in degrees.
Data Types: double

## 'AngleLim' - Visible polar angle span

[0 360] (default) | 1-by-2 vector of real values
Visible polar angle span, specified as a comma-separated pair consisting of 'AngleLim' and a 1-by-2 vector of real values.

Data Types: double

```
'AngleLimVisible' - Show interactive angle limit cursors
0 (default) | 1
```

Show interactive angle limit cursors, specified as a comma-separated pair consisting of 'AngleLimVisible' and 0 or 1.

Data Types: logical
'AngleDirection ' - Direction of increasing angle
'ccw' (default)|'cw'
Direction of increasing angle, specified as a comma-separated pair consisting of 'AngleDirection' and 'ccw' (counterclockwise) or 'cw' (clockwise).

Data Types: char

## 'AngleResolution' - Number of degrees between radial lines <br> 15 (default) | scalar in degrees

Number of degrees between radial lines depicting angles in the polar plot, specified as a commaseparated pair consisting of 'AngleResolution' and a scalar in degrees.
Data Types: double

## 'AngleTickLabelRotation' - Rotate angle tick labels <br> 0 (default) | 1

Rotate angle tick labels, specified as a comma-separated pair consisting of 'AngleTickLabelRotation' and 0 or 1.

## Data Types: logical

'AngleTickLabelVisible' - Show angle tick labels
1 (default) | 0
Show angle tick labels, specified as a comma-separated pair consisting of
'AngleTickLabelVisible' and 0 or 1.
Data Types: logical

## 'AngleTickLabelFormat' - Format for angle tick labels

360 (default) | 180
Format for angle tick labels, specified as a comma-separated pair consisting of 'AngleTickLabelFormat' and 360 degrees or 180 degrees.

## Data Types: double

## 'AngleFontSizeMultiplier' - Scale factor of angle tick font <br> 1 (default) | numeric value greater than zero <br> Scale factor of angle tick font, specified as a comma-separated pair consisting of 'AngleFontSizeMultiplier' and a numeric value greater than zero.

## Data Types: double

[^7]Show angle span measurement, specified as a comma-separated pair consisting of 'Span' and 0 or 1.

Data Types: logical
'ZeroAngleLine' - Highlight radial line at zero degrees
0 (default) | 1
Highlight radial line at zero degrees, specified as a comma-separated pair consisting of 'ZeroAngleLine' and 0 or 1.

## Data Types: logical

'DisconnectAngleGaps ' - Show gaps in line plots with nonuniform angle spacing
1 (default) | 0
Show gaps in line plots with nonuniform angle spacing, specified as a comma-separated pair consisting of 'DisconnectAngleGaps ' and 0 or 1.

Data Types: logical

## Magnitude Properties

'MagnitudeAxisAngle' - Angle of magnitude tick label radial line
75 (default) | real scalar in degrees
Angle of magnitude tick label radial line, specified as a comma-separated pair consisting of 'MagnitudeAxisAngle' and real scalar in degrees.

## Data Types: double

## 'MagnitudeTick' - Magnitude ticks

[0 0.2 0.4 0.6 0.8] (default)| 1-by-N vector
Magnitude ticks, specified as a comma-separated pair consisting of 'MagnitudeTick' and a 1-by-N vector, where N is the number of magnitude ticks.
Data Types: double
'MagnitudeTickLabelVisible' - Show magnitude tick labels
1 (default) | 0
Show magnitude tick labels, specified as a comma-separated pair consisting of 'MagnitudeTickLabelVisible' and 0 or 1.

## Data Types: logical

## 'MagnitudeLim' - Minimum and maximum magnitude limits

[0 1] (default) | two-element vector of real values
Minimum and maximum magnitude limits, specified as a comma-separated pair consisting of 'MagnitudeLim' and a two-element vector of real values.
Data Types: double
'MagnitudeLimMode' - Determine magnitude dynamic range
'auto' (default)|'manual'

Determine magnitude dynamic range, specified as a comma-separated pair consisting of 'MagnitudeLimMode' and 'auto' or 'manual'.

Data Types: char
'MagnitudeAxisAngleMode' - Determine angle for magnitude tick labels
'auto' (default)|'manual'
Determine angle for magnitude tick labels, specified as a comma-separated pair consisting of 'MagnitudeAxisAngleMode' and 'auto' or 'manual'.
Data Types: char
'MagnitudeTickMode' - Determine magnitude tick locations
'auto' (default)|'manual'
Determine magnitude tick locations, specified as a comma-separated pair consisting of 'MagnitudeTickMode' and 'auto' or 'manual'.

Data Types: char
'MagnitudeUnits' - Magnitude units
'dB'|'dBLoss'
Magnitude units, specified as a comma-separated pair consisting of 'MagnitudeUnits' and 'db' or 'dBLoss'.

Data Types: char

## 'MagnitudeFontSizeMultiplier' - Scale factor of magnitude tick font <br> 0.9000 (default) | numeric value greater than zero

Scale factor of magnitude tick font, specified as a comma-separated pair consisting of 'MagnitudeFontSizeMultiplier' and a numeric value greater than zero.
Data Types: double

## Miscellaneous Properties

'View ' - View section of Smith plot
'full' (default)|'top' | 'bottom' | 'left'|'right'|'top-left'|'top-right'|
'bottom-left ' | 'bottom-right' | string scalar | character vector
View section of Smith plot, specified as a string scalar or character vector. Smith plot can be viewed by setting View property to one of property values in this table.

View Property Effect

| Property Value | Effect |
| :--- | :--- |
| ' full' | Full Smith plot is viewed. |
| 'top' | Top-half of the Smith plot is viewed. |
| 'bottom' | Bottom-half of the Smith plot is viewed. |
| ' left' | Left-half of the Smith plot is viewed. |
| 'right' | Right-half of the Smith plot is viewed. |
| 'top-left' | Top-left of the Smith plot is viewed. |
| 'top-right' | Top-right of the Smith plot is viewed. |
| 'bottom- left' | Bottom-left of the Smith plot is viewed. |
| 'bottom-right' | Bottom-right of the Smith plot is viewed. |

## Data Types: char \| string

## 'NormalizeData' - Normalize each data trace to maximum value <br> 0 (default) | 1

Normalize each data trace to maximum value, specified as a comma-separated pair consisting of 'NormalizeData' and 0 or 1.

## Data Types: logical

' ConnectEndpoints ' - Connect first and last angles
0 (default) | 1
Connect first and last angles, specified as a comma-separated pair consisting of 'ConnectEndpoints' and 0 or 1.

## Data Types: logical

## 'Style' - Style of polar plot display

'line' (default)|'filled'
Style of polar plot display, specified as a comma-separated pair consisting of 'Style' and 'line' or 'filled'.

Data Types: char
'TemporaryCursor' - Create temporary cursor
0 (default) | 1
Create a temporary cursor, specified as a comma-separated pair consisting of 'TemporaryCursor' and 0 or 1.

## Data Types: logical

## 'ToolTips' - Show tool tips

1 (default) | 0
Show tool tips when you hover over a polar plot element, specified as a comma-separated pair consisting of 'ToolTips' and 0 or 1.

Data Types: logical

## 'ClipData' - Clip data to outer circle <br> 0 (default) | 1

Clip data to outer circle, specified as a comma-separated pair consisting of 'ClipData' and 0 or 1.
Data Types: logical
'CleanData' - Cleans data
0 (default) | 1
Cleans data removing any Inf or NaN from the data. The property is specified as a comma-separated pair consisting of 'CleanData' and 0 or 1.
Data Types: logical
' NextPlot ' - Directive on how to add next plot
'replace' (default)|'new' | 'add'
Directive on how to add next plot, specified as a comma-separated pair consisting of 'NextPlot ' and one of the values in the table:

| Property Value | Effect |
| :--- | :--- |
| 'new' | Creates a figure and uses it as the current figure. |
| 'add' | Adds new graphics objects without clearing or <br> resetting the current figure. |
| 'replace' | Removes all axes objects and resets figure <br> properties to their defaults before adding new <br> graphics objects. |

## Legend and Title Properties

' LegendLabels ' - Data tables for legend annotation
character vector | cell array of character vectors
Data tables for legend annotation, specified as a comma-separated pair consisting of ' LegendLabels ' and a character vector or cell array of character vectors. (A) denotes the active line for interactive operation.
Data Types: char
'LegendVisible' - Show legend label
0 (default) | 1
Show legend label, specified as a comma-separated pair consisting of 'LegendVisible' and 0 or 1.
Data Types: logical

## 'TitleTop ' - Title to display above the polar plot <br> character vector

Title to display above the polar plot, specified as a comma-separated pair consisting of 'TitleTop ' and a character vector.

Data Types: char

## 'TitleBottom' - Title to display below the polar plot character vector

Title to display below the polar plot, specified as a comma-separated pair consisting of 'TitleBottom' and a character vector.

Data Types: char
'TitleTopOffset ' - Offset between top title and angle ticks
0.1500 (default) | scalar

Offset between top title and angle ticks, specified as a comma-separated pair consisting of 'TitleTopOffset' and a scalar. The value must be in the range [-0.5,0.5].

Data Types: double

## 'TitleBottomOffset' - Offset between bottom title and angle ticks

0.1500 (default) | scalar

Offset between bottom title and angle ticks, specified as a comma-separated pair consisting of 'TitleBottomOffset ' and a scalar. The value must be in the range [-0.5,0.5].
Data Types: double

## 'TitleTopFontSizeMultiplier' - Scale factor of top title font

1.1000 (default) | numeric value greater than zero

Scale factor of top title font, specified as a comma-separated pair consisting of 'TitleTopFontSizeMultiplier' and a numeric value greater than zero.
Data Types: double
'TitleBottomFontSizeMultiplier' - Scale factor of bottom title font
0.9000 (default) | numeric value greater than zero

Scale factor of bottom title font, specified as a comma-separated pair consisting of 'TitleBottomFontSizeMultiplier' and a numeric value greater than zero.
Data Types: double
'TitleTopFontWeight' - Thickness of top title font
'bold' (default)|'normal'
Thickness of top title font, specified as a comma-separated pair consisting of 'TitleTopFontWeight' and 'bold' or 'normal.

Data Types: char

## 'TitleBottomFontWeight' - Thickness of bottom title font 'normal' (default)|'bold'

Thickness of bottom title font, specified as a comma-separated pair consisting of 'TitleBottomFontWeight' and 'bold' or 'normal.
Data Types: char

```
'TitleTopTextInterpreter' - Interpretation of top title characters
'none' (default)|'tex'|'latex'
```

Interpretation of top title characters, specified as a comma-separated pair consisting of 'TitleTopTextInterpreter' and:

- 'tex' - Interpret using a subset of TeX markup
- ' latex' - Interpret using LaTeX markup
- 'none' - Display literal characters


## TeX Markup

By default, MATLAB supports a subset of TeX markup. Use TeX markup to add superscripts and subscripts, modify the text type and color, and include special characters in the text.

This table lists the supported modifiers when the TickLabelInterpreter property is set to 'tex', which is the default value. Modifiers remain in effect until the end of the text, except for superscripts and subscripts which only modify the next character or text within curly braces \{\}.

| Modifier | Description | Example |
| :---: | :---: | :---: |
| ^ $\{$ \} | Superscript | 'text^\{superscript\}' |
| _ $\{$ \} | Subscript | 'text_\{subscript\}' |
| \bf | Bold font | '\bf text' |
| \it | Italic font | '\it text' |
| \sl | Oblique font (rarely available) | '\sl text' |
| \rm | Normal font | '\} \mathrm { rm }  text'  |
| \fontname\{specifier\} | Set specifier as the name of a font family to change the font style. You can use this modifier with other modifiers. | ```'\fontname{Courier} text'``` |
| \fontsize\{specifier\} | Set specifier as a scalar numeric value to change the font size. | '\fontsize\{15\} text' |
| \color\{specifier\} | Set specifier as one of these colors: red, green, yellow, magenta, blue, black, white, gray, darkGreen, orange, or lightBlue. | '\color\{magenta\} text' |
| \color[rgb]\{specifier\} | Set specifier as a threeelement RGB triplet to change the font color. | $\begin{aligned} & \text { '\color[rgb]\{0,0.5,0.5\} } \\ & \text { text' } \end{aligned}$ |

## LaTeX Markup

To use LaTeX markup, set the TickLabel Interpreter property to ' latex'. The displayed text uses the default LaTeX font style. The FontName, FontWeight, and FontAngle properties do not have an effect. To change the font style, use LaTeX markup within the text.

The maximum size of the text that you can use with the LaTeX interpreter is 1200 characters. For multiline text, the maximum size reduces by about 10 characters per line.
Data Types: char

## 'TitleBottomTextInterpreter' - Interpretation of bottom title characters <br> 'none' (default)|'tex'|'latex'

Interpretation of bottom title characters, specified as a comma-separated pair consisting of 'TitleBottomTextInterpreter' and:

- 'tex' - Interpret using a subset of TeX markup
- 'latex' - Interpret using LaTeX markup
- 'none ' - Display literal characters


## TeX Markup

By default, MATLAB supports a subset of TeX markup. Use TeX markup to add superscripts and subscripts, modify the text type and color, and include special characters in the text.

This table lists the supported modifiers when the TickLabelInterpreter property is set to 'tex', which is the default value. Modifiers remain in effect until the end of the text, except for superscripts and subscripts which only modify the next character or the text within the curly braces \{\}.

| Modifier | Description | Example |
| :---: | :---: | :---: |
| $\wedge$ ^ \} | Superscript | 'text^\{superscript\}' |
| _ \{ \} | Subscript | 'text_\{subscript\}' |
| \bf | Bold font | '\bf text' |
| \it | Italic font | '\it text' |
| \sl | Oblique font (rarely available) | '\sl text' |
| \rm | Normal font | '\rm text' |
| \fontname\{specifier\} | Set specifier as the name of a font family to change the font style. You can use this modifier with other modifiers. | ```'\fontname{Courier}``` |
| \fontsize\{specifier\} | Set specifier as a scalar numeric value to change the font size. | '\fontsize\{15\} text' |
| \color\{specifier\} | Set specifier as one of these colors: red, green, yellow, magenta, blue, black, white, gray, darkGreen, orange, or lightBlue. | '\color\{magenta\} text' |
| \color[rgb]\{specifier\} | Set specifier as a threeelement RGB triplet to change the font color. | $\begin{aligned} & \text { '\color[rgb]\{0,0.5,0.5\} } \\ & \text { text ' } \end{aligned}$ |

## LaTeX Markup

To use LaTeX markup, set the TickLabelInterpreter property to ' latex'. The displayed text uses the default LaTeX font style. The FontName, FontWeight, and FontAngle properties do not have an effect. To change the font style, use LaTeX markup within the text.

The maximum size of the text that you can use with the LaTeX interpreter is 1200 characters. For multiline text, the maximum size reduces by about 10 characters per line.

## Data Types: char

## Grid Properties

'GridOverData' - Draw grid over data plots
0 (default) | 1
Draw grid over data plots, specified as a comma-separated pair consisting of 'GridOverData' and 0 or 1.

Data Types: logical

## 'DrawGridToOrigin' - Draw radial lines within innermost circle <br> 0 (default) | 1

Draw radial lines within innermost circle of the polar plot, specified as a comma-separated pair consisting of 'DrawGridToOrigin' and 0 or 1.
Data Types: logical

## 'GridAutoRefinement' - Increase angle resolution <br> 0 (default) | 1

Increase angle resolution in the polar plot, specified as a comma-separated pair consisting of 'GridAutoRefinement' and 0 or 1. This property increases angle resolution by doubling the number of radial lines outside each magnitude.
Data Types: logical

## 'GridWidth ' - Width of grid lines <br> 0.5000 (default) | positive scalar

Width of grid lines, specified as a comma-separated pair consisting of 'GridWidth ' and a positive scalar.

Data Types: double

## 'GridVisible' - Show grid lines <br> 1 (default) | 0

Show grid lines, including magnitude circles and angle radii, specified as a comma-separated pair consisting of 'GridVisible' and 0 or 1.
Data Types: logical

## 'GridForegroundColor' - Color of foreground grid lines

[0.8000 0.8000 0.8000] (default) |' none' | character vector of color names
Color of foreground grid lines, specified as a comma-separated pair consisting of
'GridForegroundColor' and an RGB triplet, character vector of color names, or 'none'.
RGB triplets and hexadecimal color codes are useful for specifying custom colors.

- An RGB triplet is a three-element row vector whose elements specify the intensities of the red, green, and blue components of the color. The intensities must be in the range [ 0,1 ; for example, [0.4 0.6 0.7].
- A hexadecimal color code is a character vector or a string scalar that starts with a hash symbol (\#) followed by three or six hexadecimal digits, which can range from 0 to F. The values are not case sensitive. Thus, the color codes '\#FF8800', '\#ff8800', '\#F80', and '\#f80' are equivalent.

Alternatively, you can specify some common colors by name. This table lists the named color options, the equivalent RGB triplets, and hexadecimal color codes.

| Color Name | Short Name | RGB Triplet | Hexadecimal <br> Color Code | Appearance |
| :--- | :--- | :--- | :--- | :--- |
| "red" | "r" | $\left[\begin{array}{lll}1 & 0 & 0\end{array}\right]$ | "\#FF0000" |  |
| "green" | "g" | $\left[\begin{array}{lll}0 & 1 & 0\end{array}\right]$ | $" \# 00 F F 00 "$ |  |
| "blue" | "b" | $\left[\begin{array}{lll}0 & 0 & 1\end{array}\right]$ | $" \# 0000$ FF" |  |
| "cyan" | "c" | $\left[\begin{array}{lll}0 & 1 & 1\end{array}\right]$ | $" \# 00 F F F F "$ |  |
| "magenta" | "m" | $\left[\begin{array}{lll}1 & 0 & 1\end{array}\right]$ | $" \# F F 00 F F "$ |  |
| "yellow" | "y" | $\left[\begin{array}{lll}1 & 1 & 0\end{array}\right]$ | $" \# F F F F 00 "$ |  |
| "black" | "k" | $\left[\begin{array}{lll}0 & 0 & 0\end{array}\right]$ | "\#000000" |  |
| "white" | "w" | $\left[\begin{array}{lll}1 & 1 & 1\end{array}\right]$ | $" \# F F F F F F "$ |  |

Here are the RGB triplets and hexadecimal color codes for the default colors MATLAB uses in many types of plots.

| RGB Triplet | Hexadecimal Color Code | Appearance |
| :--- | :--- | :--- |
| $\left[\begin{array}{llll}0 & 0.4470 & 0.7410] & \text { "\#0072BD" }\end{array}\right.$ |  |  |
| $\left[\begin{array}{lll}0.8500 & 0.3250 & 0.0980]\end{array}\right.$ | "\#D95319" |  |
| $\left[\begin{array}{lll}0.9290 & 0.6940 & 0.1250]\end{array}\right.$ | "\#EDB120" |  |
| $\left[\begin{array}{lll}0.4940 & 0.1840 & 0.5560]\end{array}\right.$ | "\#7E2F8E" |  |
| $\left[\begin{array}{lll}0.4660 & 0.6740 & 0.1880]\end{array}\right.$ | "\#77AC30" |  |
| $\left[\begin{array}{lll}0.3010 & 0.7450 & 0.9330]\end{array}\right.$ | "\#4DBEEE" |  |
| $\left[\begin{array}{lll}0.6350 & 0.0780 & 0.1840]\end{array}\right.$ | "\#A2142F" |  |

## Data Types: double | char

## 'GridBackGroundColor' - Color of background grid lines

'w' (default) | character vector of color names | 'none'
Color of background grid lines, specified as a comma-separated pair consisting of
'GridBackGroundColor' and an RGB triplet, character vector of color names, or 'none'.
RGB triplets and hexadecimal color codes are useful for specifying custom colors.

- An RGB triplet is a three-element row vector whose elements specify the intensities of the red, green, and blue components of the color. The intensities must be in the range [ 0,1 ]; for example, [0.4 0.6 0.7].
- A hexadecimal color code is a character vector or a string scalar that starts with a hash symbol (\#) followed by three or six hexadecimal digits, which can range from 0 to $F$. The values are not case sensitive. Thus, the color codes '\#FF8800', '\#ff8800', '\#F80', and '\#f80' are equivalent.

Alternatively, you can specify some common colors by name. This table lists the named color options, the equivalent RGB triplets, and hexadecimal color codes.

| Color Name | Short Name | RGB Triplet | Hexadecimal <br> Color Code | Appearance |
| :--- | :--- | :--- | :--- | :--- |
| "red" | "r" | $\left[\begin{array}{lll}1 & 0 & 0\end{array}\right]$ | "\#FF0000" |  |
| "green" | "g" | $\left[\begin{array}{lll}0 & 1 & 0\end{array}\right]$ | $" \# 00 F F 00 "$ |  |
| "blue" | "b" | $\left[\begin{array}{lll}0 & 0 & 1\end{array}\right]$ | $" \# 0000 F F "$ |  |
| "cyan" | "c" | $\left[\begin{array}{lll}0 & 1 & 1\end{array}\right]$ | $" \# 00 F F F F "$ |  |
| "magenta" | "m" | $\left[\begin{array}{lll}1 & 0 & 1\end{array}\right]$ | "\#FF00FF" |  |
| "yellow" | "y" | $\left[\begin{array}{lll}1 & 1 & 0\end{array}\right]$ | "\#FFFF00" |  |
| "black" | "k" | $\left[\begin{array}{lll}0 & 0 & 0\end{array}\right]$ | $" \# 000000 "$ |  |
| "white" | "w" | $\left[\begin{array}{lll}1 & 1 & 1\end{array}\right]$ | $" \# F F F F F F "$ |  |

Here are the RGB triplets and hexadecimal color codes for the default colors MATLAB uses in many types of plots.

| RGB Triplet | Hexadecimal Color Code | Appearance |
| :---: | :---: | :---: |
| [0 0.4470 0.7410] | "\#0072BD" |  |
| [0.8500 0.3250 0.0980] | "\#D95319" |  |
| [0.9290 0.6940 0.1250] | "\#EDB120" |  |
| [0.4940 0.1840 0.5560] | "\#7E2F8E" |  |
| [0.4660 0.6740 0.1880] | "\#77AC30" | $\square$ |
| [0.3010 0.7450 0.9330] | "\#4DBEEE" | $\square$ |
| [0.6350 0.0780 0.1840] | "\#A2142F" |  |

## Data Types: double | char

## Marker, Color, Line, and Font Properties

## 'Marker' - Marker symbol

'none' (default) | character vector of symbols
Marker symbol, specified as a comma-separated pair consisting of 'Marker' and either 'none ' or one of the symbols in this table. By default, a line does not have markers. Add markers at selected points along the line by specifying a marker.

| Marker | Description | Resulting Marker |
| :--- | :--- | :---: |
| "0" | Circle | $\bigcirc$ |
| "+" | Plus sign | + |
| "*" | Asterisk | * |
| "." | Point | • |


| Marker | Description | Resulting Marker |
| :--- | :--- | :---: |
| "x" | Cross | $\times$ |
| "_" | Horizontal line | - |
| " I" | Vertical line | $\mid$ |
| "square" | Square | $\square$ |
| "diamond" | Diamond | $\checkmark$ |
| "^" | Upward-pointing triangle | $\triangle$ |
| "v" | Downward-pointing triangle | $\nabla$ |
| ">" | Right-pointing triangle | $\searrow$ |
| "<" | Left-pointing triangle | $\triangleleft$ |
| "pentagram" | Pentagram | $\AA$ |
| "hexagram" | Hexagram | ¿ |
| "none" | No markers | Not applicable |

'MarkerSize' - Marker size
6 (default) | positive value
Marker size, specified as a comma-separated pair consisting of 'MarkerSize' and a positive value in point units.

## Data Types: double

## ' ColorOrder ' - Colors to use for multiline plots

seven predefined colors (default) | three-column matrix of RGB triplets
Colors to use for multi-line plots, specified as a comma-separated pair consisting of 'ColorOrder' and a three-column matrix of RGB triplets. Each row of the matrix defines one color in the color order.

Data Types: double
' ColorOrderIndex ' - Next color to use in color order
1 (default) | positive integer
Next color to use in color order, specified as a comma-separated pair consisting of 'ColorOrderIndex' and a positive integer. New plots added to the axes use colors based on the current value of the color order index.

Data Types: double

```
'EdgeColor' - Color of data lines
'k' (default) | RGB triplet vector
```

Color of data lines, specified as a comma-separated pair consisting of 'EdgeColor' and a character vector of color names or RGB triplet vector.

RGB triplets and hexadecimal color codes are useful for specifying custom colors.

- An RGB triplet is a three-element row vector whose elements specify the intensities of the red, green, and blue components of the color. The intensities must be in the range [ 0,1 ]; for example, [0.4 0.6 0.7].
- A hexadecimal color code is a character vector or a string scalar that starts with a hash symbol (\#) followed by three or six hexadecimal digits, which can range from 0 to $F$. The values are not case sensitive. Thus, the color codes '\#FF8800', '\#ff8800', '\#F80', and '\#f80' are equivalent.

Alternatively, you can specify some common colors by name. This table lists the named color options, the equivalent RGB triplets, and hexadecimal color codes.

| Color Name | Short Name | RGB Triplet | Hexadecimal <br> Color Code | Appearance |
| :--- | :--- | :--- | :--- | :--- |
| "red" | "r" | $\left[\begin{array}{lll}1 & 0 & 0\end{array}\right]$ | "\#FF0000" |  |
| "green" | "g" | $\left[\begin{array}{lll}0 & 1 & 0\end{array}\right]$ | $" \# 00 F F 00 "$ |  |
| "blue" | "b" | $\left[\begin{array}{lll}0 & 0 & 1\end{array}\right]$ | $" \# 0000$ FF" |  |
| "cyan" | "c" | $\left[\begin{array}{llll}0 & 1 & 1\end{array}\right]$ | $" \# 00 F F F F "$ |  |
| "magenta" | "m" | $\left[\begin{array}{lll}1 & 0 & 1\end{array}\right]$ | "\#FF00FF" |  |
| "yellow" | "y" | $\left[\begin{array}{lll}1 & 1 & 0\end{array}\right]$ | "\#FFFF00" |  |
| "black" | "k" | $\left[\begin{array}{lll}0 & 0 & 0\end{array}\right]$ | "\#000000" |  |
| "white" | "w" | $\left[\begin{array}{lll}1 & 1 & 1\end{array}\right]$ | "\#FFFFFF" |  |

Here are the RGB triplets and hexadecimal color codes for the default colors MATLAB uses in many types of plots.

| RGB Triplet | Hexadecimal Color Code | Appearance |
| :---: | :---: | :---: |
| [0 0.4470 0.7410] | "\#0072BD" | $\square$ |
| [0.8500 0.3250 0.0980] | "\#D95319" | $\square$ |
| [0.9290 0.6940 0.1250] | "\#EDB120" |  |
| [0.4940 0.1840 0.5560] | "\#7E2F8E" |  |
| [0.4660 0.6740 0.1880] | "\#77AC30" |  |
| [0.3010 0.7450 0.9330] | "\#4DBEEE" | $\square$ |
| [0.6350 0.0780 0.1840] | "\#A2142F" | - |

## Data Types: double | char

```
'LineStyle' - Line style of the plot
' -' (default)|'--' |':'|'- ''|'none'
```

Line style of the plot, specified as a comma-separated pair consisting of 'LineStyle' and one of the symbols in the table:

| Symbol | Line Style | Resulting Line |
| :---: | :---: | :---: |
| '- ' | Solid line |  |
| ' - ' | Dashed line | - - - - |
| ':' | Dotted line | $\ldots . . .1 . . . . . . . .$. |
| ' - . | Dash-dotted line | -------- |
| 'none ' | No line | No line |

'LineWidth ' - Line width of plot
1 (default) | positive scalar | positive vector
Line width of the plot, specified as a comma-separated pair consisting of 'LineWidth' and a positive scalar or vector.
'FontSize' - Font size of text in plot
10 (default) | positive scalar
Font size of text in the plot, specified as a comma-separated pair consisting of 'FontSize' and a positive scalar.
'FontSizeAutoMode' - Set font size
'auto' (default)|'manual'
Set font size, specified as a comma-separated pair consisting of 'FontSizeAutoMode' and 'auto' or 'manual'.

Data Types: char

## showSpan

Show or hide angle span between two markers

## Syntax

showSpan(p,id1,id2)
showSpan(p,id1,id2,true)
showSpan(p,vis)
showSpan(p)
d = showSpan( $\qquad$ )

## Description

showSpan( $\mathrm{p}, \mathrm{id} 1, \mathrm{id} 2$ ) displays the angle span between two angle markers, id1 and id2. The angle span is calculated counterclockwise.
showSpan( $p, i d 1, i d 2$, true) automatically reorders the angle markers such that the initial angle span is less than or equal to $180^{\circ}$ counterclockwise.
showSpan ( $p, v i s$ ) sets angle span visibility by setting vis to true or false.
showSpan ( $p$ ) toggles the angle span display on and off.
$\mathrm{d}=$ showSpan (__ ) returns angle span details in a structure, d using any of the previous syntaxes.

## Input Arguments

## p - Polar plot

scalar handle
Polar plot, specified as a scalar handle.
id1,id2 - Cursor or peak marker identifiers
character vector
Cursor or peak marker identifiers, specified as character vector. Adding cursors to the polar plot creates cursor marker identifiers. Adding peaks to the polar plot creates peak marker identifiers.
Example: showspan ( $\mathrm{p}, \mathrm{I}^{\prime} \mathrm{C} 1^{\prime}$, ' $\mathrm{C} 2{ }^{\prime}$ ) . Displays the angle span between cursors, C1 and C2 in polar plot, p.

## ExamplesShow Angle Span

Create a dipole antenna and plot the directivity at 270 MHz .

```
d = dipole;
D = pattern(d,270e6,0,0:1:360);
p = polarpattern(D);
```



Add cursors to the polar plot at approximately 60 and 150 degrees.
addCursor(p,[60 150]);


Show the angle span between the two angles.
showSpan(p,'C1','C2');


## Show Angle Span for Short-Dipole Antenna

Create a short-dipole antenna element and plot the field values at 250 MHz .
antenna = phased.ShortDipoleAntennaElement('FrequencyRange',[100,900]*1e6,...
'AxisDirection','Y');
angs $=$ [-180:1:180];
$\mathrm{fc}=250.0 \mathrm{e} 6$;
p = pattern(antenna,250.0e6,angs,0,'CoordinateSystem','polar','Type',...
'efield','Polarization','H');
$P=$ polarpattern(angs,abs(p));


Add cursors to the polar plot at $-30^{\circ}$ and $30^{\circ}$.
addCursor(P,[-30 30]);


Show the angle span between the two angles.
showSpan(P,'C1','C2');


## Version History

Introduced in R2016a

## See Also

add | addCursor| animate | createLabels |findLobes | replace | showPeaksTable

## AlphaBetaFilter

Alpha-beta filter for object tracking

## Description

The AlphaBetaFilter object represents an alpha-beta filter designed for object tracking. Use this tracker for platforms that follow a linear motion model and have a linear measurement model. Linear motion is defined by constant velocity or constant acceleration. Use the filter to predict the future location of an object, to reduce noise for a detected location, or to help associate multiple objects with their tracks.

## Creation

## Syntax

abf = AlphaBetaFilter
abf = AlphaBetaFilter(Name,Value,...)

## Description

abf = AlphaBetaFilter creates an alpha-beta filter for a discrete time, 2-D constant velocity system. The motion model of the filter corresponds to setting the MotionModel property to '2D Constant Velocity '. In this case, the filter state takes the form [x; vx; y; vy].
abf = AlphaBetaFilter(Name,Value, ...) specifies the properties of the filter using one or more Name, Value pair arguments. Any unspecified properties take default values.

## Properties

## MotionModel - Model of target motion

'2D Constant Velocity' (default)|'1D Constant Velocity'|'3D Constant Velocity'|
'1D Constant Acceleration'|'2D Constant Acceleration'|'3D Constant
Acceleration'
Model of target motion, specified as a character vector or string. Specifying 1D, 2D or 3D sets the dimensions of the targets motion. Specifying Constant Velocity assumes that the target motion has constant velocity at each simulation step. Specifying Constant Acceleration assumes that the target motion has constant acceleration at each simulation step.
Data Types: char | string

## State - Filter state

scalar | real-valued $M$-element vector
Filter state, specified as a scalar or a real-valued $M$-element vector. A scalar input is extended to an $M$-element vector. The state vector is the concatenated states from each dimension.

The state vectors for each motion model are column vectors:

| MotionModel Property | State Vector |
| :--- | :--- |
| '1D Constant Velocity' | $[x ; v x]$ |
| '2D Constant Velocity' | $[x ; v x ; y ; v y]$ |
| '3D Constant Velocity' | $[x ; v x ; y ; v y ; ~ z ; ~ v z]$ |
| '1D Constant Acceleration' | $[x ; v x ; a x]$ |
| '2D Constant Acceleration' | $[x ; v x ; a x ; y ; v y ; a y]$ |
| '3D Constant Acceleration' | $[x ; v x ; a x ; y ; v y ; a y ; z ; v z ; a z]$ |

where, for example, $v x$ denotes velocity in the $x$-direction and ax denotes acceleration in the $x$ direction.

Example: [200;0.2;150;0.1;0;0.25]
Data Types: double

## StateCovariance - State estimation error covariance

$M$-by-M matrix | scalar
State error covariance, specified as an $M$-by- $M$ matrix where $M$ is the size of the filter state. A scalar input is extended to an $M$-by- $M$ matrix. The covariance matrix represents the uncertainty in the filter state.

Example: eye (6)

## ProcessNoise - Process noise covariance

D-by-D matrix | scalar
Process noise covariance, specified as a scalar or an $D$-by- $D$ matrix where $D$ is the dimensionality of motion. For example, if MotionModel is ' 2 D Constant Velocity, then $D=2$. A scalar input is extended to an $D$-by- $D$ matrix.

Example: [20 0.1; 0.1 1]

## MeasurementNoise - Measurement noise covariance

$D$-by-D matrix | scalar
Measurement noise covariance, specified as a scalar or an $D$-by- $D$ matrix where $D$ is the dimensionality of motion. For example, if MotionModel is '2D Constant Velocity, then $D=2$. A scalar input is extended to an $M$-by- $M$ matrix.
Example: [20 0.1; 0.1 1]

## Coefficients - Alpha-beta filter coefficients

scalar | row vector of real values
Alpha-beta filter coefficients, specified as a scalar or row vector of real values. Any scalar input is extended to a row vector. If you specify constant velocity in the MotionModel property, the coefficients are [alpha beta]. If you specify constant acceleration in the MotionModel property, the coefficients are [alpha beta gamma].
Example: [20 0.1]

## Object Functions

predict Predict the state and state estimation error covariance
correct Correct the state and state estimation error covariance
distance Distances between measurements and predicted measurements
likelihood Likelihood of measurement
clone Create identical object

## Examples

## Track Constant-Velocity Target Using Alpha-Beta Filter

Apply the alpha-beta filter to track a target moving at constant velocity along the x -axis.

```
T = 0.1;
V0 = 100;
N = 100;
plat = phased.Platform('MotionModel','Velocity', ...
    'VelocitySource','Input port','InitialPosition',[100;0;0]);
abfilt = phased.AlphaBetaFilter('MotionModel','1D Constant Velocity');
Z = zeros(1,N);
Zp = zeros(1,N);
Zc = zeros(1,N);
for m = 1:N
    pos = plat(T,[100+20*randn;0;0]);
    Z(m) = pos(1);
    [~,~,Zp(m)] = predict(abfilt,T);
    [~,~,Zc(m)] = correct(abfilt,Z(m));
end
t = (0:N-1)*T;
plot(t,Z,t,Zp,t,Zc)
xlabel('Time (s)')
ylabel('Position (m)')
legend('True Track','Predicted Track','Corrected Track', ...
    'Location','Best')
```



## Track Constant-Acceleration Target Using Alpha-Beta Filter

Apply the alpha-beta filter to track a target moving at constant acceleration along the x -axis.

```
T = 0.1;
a0 = 100;
N = 100;
plat = phased.Platform('MotionModel','Acceleration', ...
    'AccelerationSource','Input port','InitialPosition',[100;0;0]);
abfilt = phased.AlphaBetaFilter( ...
    'MotionModel','1D Constant Acceleration', ...
    'Coefficients',[0.5 0.5 0.1]);
Z = zeros(1,N);
Zp = zeros(1,N);
Zc = zeros(1,N);
for m = 1:N
    pos = plat(T,[100+20*randn;0;0]);
    Z(m) = pos(1);
    [~,~,Zp(m)] = predict(abfilt,T);
    [~,~,Zc(m)] = correct(abfilt,Z(m));
end
t = (0:N-1)*T;
plot(t,Z,t,Zp,t,Zc)
xlabel('Time (s)')
ylabel('Position (m)');
```

```
legend('True Track','Predicted Track','Corrected Track', ...
    'Location','Best');
```



## Track Target in 3-D Using Alpha-Beta Filter

Apply the alpha-beta filter to track a target moving at constant velocity in three dimensions.

```
T = 0.1;
V0 = 100;
N = 100;
plat = phased.Platform('MotionModel','Velocity', ...
    'VelocitySource','Input port','InitialPosition',[100;0;0]);
abfilt = phased.AlphaBetaFilter('MotionModel', ...
    '3D Constant Velocity','State',zeros(6,1));
Z = zeros(3,N);
Zp = zeros(3,N);
Zc = zeros(3,N);
for m = 1:N
    Z(:,m) = plat(T,[V0+20*randn;0;0]);
    [~,~,Zp(:,m)] = predict(abfilt,T);
    [~,~,Zc(:,m)] = correct(abfilt,Z(:,m));
end
t = (0:N-1)*T;
plot(t,Z(1,:),t,Zp(1,:),t,Zc(1,:))
xlabel('Time (s)')
```

ylabel('Position along X (m)')
legend('True Track','Predicted Track','Corrected Track', ... 'Location', 'Best')


## Version History

Introduced in R2018b

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

## clone

Copy of alpha-beta tracking filter

## Syntax

```
abfilter2 = clone(abfilter)
```


## Description

abfilter2 = clone(abfilter) creates a copy, abfilter2, of the filter object, abfilter, with the same property values.

## Input Arguments

abfilter - Alpha-beta tracking filter
phased.AlphaBetaFilter object
Alpha-beta tracking filter, specified as a phased.AlphaBetaFilter object.

## Output Arguments

abfilter2 - Copy of alpha-beta tracking filter
phased.AlphaBetaFilter
Copy of alpha-beta tracking filter, returned as a phased.AlphaBetaFilter object.

## Version History

Introduced in R2018b

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

## Functions

predict | correct|distance|likelihood
Objects
phased.Platform

## correct

Correct the state and state estimation error covariance

## Syntax

xCorr = correct(abfilter,zMeas)
[xCorr, pCorr] = correct(abfilter,zMeas)
[xCorr,pCorr,zCorr] = correct(abfilter,zMeas)

## Description

$x$ Corr $=$ correct (abfilter, $z M e a s)$ returns the corrected the state, xCorr , of the tracking filter abfilter given the measurement, zMeas. Calling correct overwrites the internal states of the object.
[xCorr, pCorr] = correct(abfilter, zMeas) also returns the corrected state covariance matrix, pCorr.
[xCorr, pCorr,zCorr] = correct(abfilter,zMeas) also returns the corrected measurement, zCorr.

## Input Arguments

abfilter - Alpha-beta tracking filter
phased.AlphaBetaFilter object
Alpha-beta tracking filter, specified as a phased.AlphaBetaFilter object. Calling correct overwrites the internal states of the object.

## zMeas - Measurement of tracked object

K-by-1 vector
Measurement of tracked object, specified as a $K$-by- 1 vector, where $K$ is the size of the measurement.

## Output Arguments

## xCorr - Corrected state of the filter

L-by-1 vector
Corrected state of the filter, returned as an $L$-by- 1 vector. The corrected state overrides the value of the State property.

## pCorr - Corrected state covariance of the filter

L-by-L matrix
Corrected state covariance of the filter, returned as an L-by-L matrix. The corrected state covariance overrides the value of the StateCovariance property.

## zCorr - Corrected measurement of the filter

$K$-by-1 vector

Corrected measurement of the filter, returned as a $K$-by- 1 vector.

## Version History

Introduced in R2018b

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.

## See Also

## Functions

predict | distance|likelihood|clone
Objects
phased.Platform

## distance

Distances between measurements and predicted measurements

## Syntax

dist $=$ distance(abfilter, zMatrix)

## Description

dist = distance(abfilter, zMatrix) computes the distance between one or more predicted measurements given in zMatrix and the measurement predicted by the abfilter object.

## Input Arguments

abfilter - Alpha-beta tracking filter
phased.AlphaBetaFilter object
Alpha-beta tracking filter, specified as a phased.AlphaBetaFilter object.

## zMatrix - Measurements of tracked objects

N -by-K matrix
Measurements of tracked objects, specified as an $N$-by- $K$ matrix where $N$ is the number of measurements. Each row of the matrix contains a measurement vector. The number of columns, $K$, must match the measurement dimensions of the motion model. This computation takes into account the covariance of the predicted state and the process noise.

## Output Arguments

## dist - Distances between measurements and filter predictions

length- $N$ row vector
Distances between measurements and filter predictions, returned as a row vector. Each element corresponds to a distance between the predicted measurement coming from the abfilter object and a row of zMatrix.

Version History<br>Introduced in R2018b

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{Tm}}$.

## See Also

```
Functions
predict| correct|likelihood| clone
Objects
phased.Platform
```


## predict

Predict the state and state estimation error covariance

## Syntax

```
xPred = predict(abfilter,tstep)
[xPred,pPred] = predict(abfilter,tstep)
[xPred,pPred,zPred] = predict(abfilter,tstep)
```


## Description

xPred $=$ predict (abfilter, tstep) returns the predicted filter state, $x$ Pred, of the filter, abfilter, after the elapsed time, tstep.
[xPred,pPred] = predict(abfilter,tstep) also returns the estimated state covariance, pPred.
[xPred,pPred,zPred] = predict(abfilter,tstep) also returns the predicted measurements, zPred.

## Input Arguments

## abfilter - Alpha-beta tracking filter object

phased.AlphaBetaFilter object
Alpha-beta tracking filter, specified as a phased.AlphaBetaFilter object. Calling predict overwrites the internal states of the object.

## tstep - Time step

positive scalar
Time step for next prediction, specified as a positive scalar. The time step is the interval from the last prediction-correction to the current prediction. Units are in seconds.

## Output Arguments

## xPred - Predicted state of the filter

L-by-1 vector
Predicted state of the filter, returned as an $L$-by- 1 vector where $L$ is the size of the state vector. The predicted state overrides the value of the State property.

## pPred - Predicted state covariance of the filter

L-by-L matrix
Predicted state covariance of the filter, returned as an $L$-by- $L$ matrix. The predicted state covariance overrides the value of the StateCovariance property.

## zPred - Predicted measurement

K-by-1 vector

Predicted measurement, returned as a $K$-by- 1 vector, where $K$ is the size of the measurement.

## Version History

Introduced in R2018b

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.

## See Also

## Functions

correct | distance | likelihood | clone
Objects
phased.Platform

## likelihood

Likelihood of measurement

## Syntax

lk = likelihood(abfilter,zMeas)

## Description

lk = likelihood(abfilter, zMeas) computes the likelihood, lk, of the current measurement, zMeas, from the filter, abfilter.

## Input Arguments

abfilter - Alpha-beta tracking filter
phased.AlphaBetaFilter object
Alpha-beta tracking filter, specified as a phased.AlphaBetaFilter object.
zMeas - Measurements of tracked object
K-by-1 vector
Measurements of tracked object, specified as a $K$-by- 1 vector, where $K$ is the size of the measurement.

## Output Arguments

## lk - Likelihood of measurement

scalar
Likelihood of current measurement, returned as a scalar.

## Version History

Introduced in R2018b

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

## Functions

predict | correct | distance |clone

## Objects

phased.Platform

## directivity

Package: phased
Directivity of antenna or transducer element

## Syntax

D = directivity(element,FREQ,ANGLE)

## Description

D = directivity (element, FREQ, ANGLE) returns the "Directivity" on page 1-2132 of the antenna or transducer element, element, at frequencies specified by FREQ in direction angles specified by ANGLE.

## Input Arguments

## element - Antenna or transducer element

Phased Array System Toolbox System object
Antenna or transducer element, specified as a Phased Array System Toolbox System object.

## FREQ - Frequency for computing directivity and patterns

positive scalar | 1-by-L real-valued row vector
Frequencies for computing directivity and patterns, specified as a positive scalar or 1-by-L realvalued row vector. Frequency units are in hertz.

- For an antenna, microphone, or sonar hydrophone or projector element, FREQ must lie within the range of values specified by the FrequencyRange or FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased. CustomAntennaElement and phased. CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.


## Example: [1e8 2e6]

## Data Types: double

## ANGLE - Angles for computing directivity

1 -by- $M$ real-valued row vector | 2 -by- $M$ real-valued matrix
Angles for computing directivity, specified as a 1-by- $M$ real-valued row vector or a 2 -by- $M$ real-valued matrix, where $M$ is the number of angular directions. Angle units are in degrees. If ANGLE is a 2-by- $M$ matrix, then each column specifies a direction in azimuth and elevation, [az;el]. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

If ANGLE is a 1 -by- $M$ vector, then each entry represents an azimuth angle, with the elevation angle assumed to be zero.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the xy plane. This angle is positive when measured from the $x$-axis toward the $y$-axis. The elevation angle is the angle between the direction vector and xy plane. This angle is positive when measured towards the $z$-axis. See "Azimuth and Elevation Angles".
Example: [45 60; 0 10]
Data Types: double

## Output Arguments

## D - Directivity <br> M-by-L matrix

Directivity, returned as an $M$-by- $L$ matrix. Each row corresponds to one of the $M$ angles specified by ANGLE. Each column corresponds to one of the $L$ frequency values specified in FREQ. Directivity units are in dBi where dBi is defined as the gain of an element relative to an isotropic radiator.

## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Azimuth and Elevation Angles

The azimuth angle of a vector is the angle between the $x$-axis and the orthogonal projection of the vector onto the $x y$-plane. The angle is positive from the $x$-axis toward the $y$-axis. Azimuth angles lie between - 180 and 180 degrees. The elevation angle is the angle between the vector and its orthogonal projection onto the $x y$-plane. The angle is positive toward the positive $z$-axis from the $x y$ plane. By default, the boresight direction of an element or array is aligned with the positive $x$-axis. The boresight direction is the direction of the main lobe of an element or array.

Note The elevation angle is sometimes defined as the angle a vector makes with the positive $z$-axis. The MATLAB and Phased Array System Toolbox products do not use this definition.

This figure illustrates the azimuth and elevation angles of a direction vector.


## Version History

Introduced in R2019a

## See Also

pattern|patternAzimuth | patternElevation| beamwidth

## beamwidth

Package: phased
Compute and display beamwidth of an array

## Syntax

```
beamwidth(array,freq)
beamwidth(array,freq,Name,Value)
[bw,angles] = beamwidth(
```

$\qquad$

``` )
```


## Description

beamwidth (array, freq) plots the 2-D power pattern (in dB) of the array for all azimuth angles at a fixed elevation angle of zero degrees. The plot displays the half-power beamwidth (in degrees) at the frequency specified in freq (in Hz ) and the angles (in degrees) in azimuth at which the magnitude of the power pattern decreases by 3 dB from the peak of the main beam.
beamwidth (array, freq, Name, Value) plots the beamwidth with the specified parameter Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Name1, Value1, . . . , NameN, ValueN).
Example: beamwidth(array, 3e8, 'Cut' ', Elevation')
[bw, angles] = beamwidth ( ___ ) returns the angular beamwidth bw (in degrees). The function also returns the corresponding angle values (in degrees) that mark the beamwidth.

## Examples

## Plot Beamwidth of Sonar Array

Plot the beamwidth of a sonar array operating at a frequency of 2 kHz when the propagation speed of sound in water is $1500 \mathrm{~m} / \mathrm{s}$.

The sonar array consists of a 20 -element uniform linear array (ULA). Consider the element of the ULA to be a backbaffled phased.IsotropicProjector with a VoltageResponse of 100 Volts and with a FrequencyRange from 10 Hz to 300 kHz . Create a phased. ULA object to model the uniform linear array.

```
projector = phased.IsotropicProjector('BackBaffled',true,...
    'VoltageResponse',100,'FrequencyRange',[10 300000])
projector =
    phased.IsotropicProjector with properties:
        VoltageResponse: 100
        FrequencyRange: [10 300000]
            BackBaffled: true
```

```
myArray = phased.ULA('Element',projector,'NumElements',20,...
    'ElementSpacing',1500/200e3/2)
myArray =
    phased.ULA with properties:
            Element: [1x1 phased.IsotropicProjector]
        NumElements: 20
        ElementSpacing: 0.0037
            ArrayAxis: 'y'
                        Taper: 1
```

Using the beamwidth function, calculate and plot the 6 dB beamwidth of the sonar array. beamwidth(myArray, 200e3, 'dBDown' , 6, 'PropagationSpeed' , 1500)

## 6-dB Beamwidth @ Azimuth Cut (Elevation Angle $=0^{\circ}$ )



Power Pattern (dB), Broadside at $0.00^{\circ}$ @ 200 kHz
ans $=6.9200$

## Calculate Beamwidth and Angles of Uniform Linear Array (ULA)

Calculate the half-power beamwidth and angles of a 20 -element uniform linear array (ULA) of cosine antenna elements.

Create a phased.CosineAntennaElement object with the 'CosinePower' exponents set to 1.5.

```
myAnt = phased.CosineAntennaElement
myAnt =
    phased.CosineAntennaElement with properties:
        FrequencyRange: [0 1.0000e+20]
            CosinePower: [1.5000 1.5000]
```

Create a phased. ULA object to model a 20 -element ULA of cosine antenna elements. These elements are spaced at 0.5 meters on the azimuth plane.

```
array = phased.ULA('Element',myAnt,'NumElements',20)
array =
    phased.ULA with properties:
            Element: [1x1 phased.CosineAntennaElement]
        NumElements: 20
        ElementSpacing: 0.5000
            ArrayAxis: 'y'
                        Taper: 1
```

Compute the beamwidth and angles of the array when it is operating at 3 e 8 Hz . Specify the beamwidth to be computed along the elevation plane.

```
[BW,Ang] = beamwidth(array,3e8,'Cut','Elevation')
BW = 74.8200
Ang = 1\times2
    -37.4100 37.4100
```


## Input Arguments

## array - Array of sensor elements

Phased Array System Toolbox System object
Array of sensor elements, specified as one of the following System objects:

- phased.ULA
- phased.URA
- phased.UCA
- phased.ConformalArray
- phased.HeterogeneousULA
- phased.HeterogeneousURA
- phased.HeterogeneousConformalArray


## freq - Frequency used to calculate beamwidth

scalar in Hz

Frequency used to calculate the beamwidth, specified as a scalar in Hz .

## Example: 3e8

Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . ,NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.
Example: beamwidth(array, 3e8,'Cut','Azimuth' ' 'CutAngle', 45) plots the beamwidth of the array that is operating at a frequency of 0.3 GHz , with the slice direction set to 'Azimuth ', and the cut angle set to 45 degrees.

## Cut - Slice direction in azimuth-elevation space

'Azimuth' (default)|'Elevation'
The slice direction in azimuth-elevation space along which the beamwidth is computed, specified as the comma-separated pair consisting of 'Cut' and 'Azimuth' for the azimuth plane, and 'Cut' and 'Elevation' for the elevation plane.

## CutAngle - Angle for plane to get required 2-D cut

0 (default) | scalar
Corresponding angle (in degrees) for the plane to get the required 2-D cut, specified as the commaseparated pair consisting of 'CutAngle' and a scalar. If 'Cut' is specified as 'Azimuth', then 'CutAngle' (Elevation) should lie between [ $-90,90$ ] degrees. If 'Cut ' is specified as
'Elevation', then 'CutAngle' (Azimuth) should lie between [-180, 180] degrees.
Data Types: double

## dBDown - Power value from peak of main lobe

3 (default) | positive scalar
Power value (in dB) from the peak of the main lobe, specified as the comma-separated pair consisting of 'dBDown' and a positive scalar. The default value is 3 dB , which translates to half-power beamwidth. To calculate first-null beamwidth, specify the 'dBDown' value as Inf.
Data Types: single | double | int8| int16|int32|int64|uint8|uint16|uint32|uint64

## PropagationSpeed - Propagation speed

$3 \times 10^{\wedge} 8 \mathrm{~m} / \mathrm{s}$ (speed of light) (default) | positive scalar
Propagation speed, specified as the comma-separated pair consisting of 'PropagationSpeed ' and a positive scalar (in m/s).
Data Types: double

## Weights - Weights applied to array

length- $N$ column vector
Weights applied to the array of sensor elements, specified as the comma-separated pair consisting of 'Weights ' and a length- $N$ column vector, where $N$ is the number of elements in the array.

Data Types: double

## Output Arguments

bw - Angular beamwidth
scalar in degrees
Angular beamwidth of the array of sensor elements, returned as a scalar in degrees.
Data Types: double
angles - Angle values of beamwidth
1 -by-2 vector in degrees
Angle values of the beamwidth, returned as a 1-by- 2 vector. The two elements in the vector [ $a_{\text {min }}, a_{\text {max }}$ ] define the beamwidth bw as $a_{\max }-a_{\min }$.

## Version History <br> Introduced in R2020b

## See Also

Objects<br>phased.ULA|phased.URA|phased.UCA|phased.ConformalArray| phased.HeterogeneousULA | phased.HeterogeneousURA| phased.HeterogeneousConformalArray

## beamwidth

Package: phased
Compute and display beamwidth of a subarray

## Syntax

beamwidth(subarray, freq) beamwidth(subarray, freq, Name, Value)
[bw,angles] = beamwidth( $\qquad$ )

## Description

beamwidth (subarray, freq) plots the 2-D power pattern (in dB) of the subarray for all azimuth angles at a fixed elevation angle of zero degrees. The plot displays the half-power beamwidth (in degrees) at the frequency specified in freq (in Hz ) and the angles (in degrees) in azimuth at which the magnitude of the power pattern decreases by 3 dB from the peak of the main beam.
beamwidth(subarray,freq,Name,Value) computes and plots the beamwidth with the specified parameter Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Name1,Value1, ...,NameN, ValueN).
Example: beamwidth(subarray, 5e8, 'Cut', 'Elevation')
[bw, angles] = beamwidth ( ___ ) returns the angular beamwidth bw (in degrees). The function also returns the corresponding angle values (in degrees) of the beamwidth.

## Examples

## Plot Beamwidth of Rectangular Lattice Array

Plot the beamwidth of a rectangular lattice array composed of two uniform rectangular arrays. Consider the antenna elements of the array to be cosine antenna elements.

First, construct a phased.CosineAntennaElement object.

```
myAnt = phased.CosineAntennaElement
myAnt =
    phased.CosineAntennaElement with properties:
        FrequencyRange: [0 1.0000e+20]
            CosinePower: [1.5000 1.5000]
```

Next, construct a 5-by-5 uniform rectangular array by creating a phased. URA object.

```
myArray = phased.URA([5 5],[0.5 0.5],'Element',myAnt,...
    'ElementSpacing',[0.15 0.15])
myArray =
    phased.URA with properties:
```

```
        Element: [1x1 phased.CosineAntennaElement]
            Size: [5 5]
ElementSpacing: [0.1500 0.1500]
            Lattice: 'Rectangular'
    ArrayNormal: 'x'
            Taper: 1
```

Use two of these 5-by-5 uniform rectangular arrays to construct a 5-by-10 rectangular lattice. Construct the lattice using the phased. ReplicatedSubarray object.

```
myRSA = phased.ReplicatedSubarray('Subarray',myArray,...
'Layout','Rectangular','GridSize',[1 2],...
'GridSpacing','Auto','SubarraySteering','Phase')
myRSA =
    phased.ReplicatedSubarray with properties:
            Subarray: [1x1 phased.URA]
                            Layout: 'Rectangular'
                    GridSize: [1 2]
                GridSpacing: 'Auto'
                SubarraySteering: 'Phase'
        PhaseShifterFrequency: 300000000
            NumPhaseShifterBits: 0
```

Now visualize the 10dB beamwidth of the obtained lattice across the azimuth plane ( 0 degrees elevation). The subarray is phase steered toward 24 degrees azimuth. Assume the operating frequency of the array to be 1 GHz .

```
stv = phased.SteeringVector('SensorArray',myRSA);
beamwidth(myRSA,1e9,'dBDown',10,'SteerAngle',24,'Weights',stv(1e9,24))
```

10-dB Beamwidth @ Azimuth Cut (Elevation Angle $=0^{\circ}$ )


Power Pattern (dB), Broadside at $0.00^{\circ}$ @ 1 GHz

```
ans = 16.4600
```


## Calculate Beamwidth and Angles of Two ULAs

Calculate the 3 dB beamwidth of a 10 -element uniform linear array (ULA) composed of two 5-element ULAs across the azimuth plane and at 0 degrees elevation. By default, the antenna elements are isotropic. Assume the operating frequency of the array to be 500 MHz .

```
myArray = phased.ULA('NumElements',5)
myArray =
    phased.ULA with properties:
            Element: [1x1 phased.IsotropicAntennaElement]
            NumElements: 5
        ElementSpacing: 0.5000
            ArrayAxis: 'y'
                Taper: 1
myRSA = phased.ReplicatedSubarray('Subarray',myArray,...
'GridSize',[1 2])
myRSA =
    phased.ReplicatedSubarray with properties:
```

```
        Subarray: [1x1 phased.ULA]
            Layout: 'Rectangular'
        GridSize: [1 2]
    GridSpacing: 'Auto'
SubarraySteering: 'None'
[BW,Ang] = beamwidth(myRSA,5e8)
BW = 6.1200
Ang = 1\times2
    -3.0600 3.0600
```


## Input Arguments

## subarray - Subarray of sensor elements

Phased Array System Toolbox System object
Subarray of sensor elements, specified as one of the following System objects:

- phased.PartitionedArray
- phased.ReplicatedSubarray


## freq - Frequency used to calculate beamwidth

scalar in Hz
Frequency used to calculate the beamwidth, specified as a scalar in Hz .
Example: 5e8
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Namel=Value1, ... ,NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.
Example: beamwidth(subarray,5e8,'Cut','Azimuth','CutAngle', 45 ) plots the beamwidth of the subarray that is operating at a frequency of 0.5 GHz , with the slice direction set to 'Azimuth', and the cut angle set to 45 degrees.

## Cut - Slice direction in azimuth-elevation space

'Azimuth' (default)|'Elevation'
The slice direction in azimuth-elevation space along which the beamwidth is computed, specified as the comma-separated pair consisting of 'Cut ' and 'Azimuth' for the azimuth plane, and 'Cut' and 'Elevation' for the elevation plane.

## CutAngle - Angle for plane to get required 2-D cut

0 (default) | scalar
Corresponding angle (in degrees) for the plane to get the required 2-D cut, specified as the commaseparated pair consisting of 'CutAngle' and a scalar. If 'Cut' is specified as 'Azimuth', then 'CutAngle' (Elevation) should lie between [-90, 90] degrees. If 'Cut' is specified as 'Elevation', then 'CutAngle' (Azimuth) should lie between [-180, 180] degrees.
Data Types: double

## dBDown - Power value from peak of main lobe

3 (default) | Inf | positive scalar
Power value (in dB ) from the peak of the main lobe, specified as the comma-separated pair consisting of 'dBDown ' and a positive scalar. The default value is 3 dB , which translates to half-power beamwidth. To calculate the first-null beamwidth, specify the 'dBDown' value as Inf.
Data Types: single | double | int8 | int16 | int32 | int64 | uint8|uint16|uint32|uint64
PropagationSpeed - Propagation speed
$3 \times 10^{\wedge} 8 \mathrm{~m} / \mathrm{s}$ (speed of light) (default) | positive scalar
Propagation speed, specified as the comma-separated pair consisting of 'PropagationSpeed ' and a positive scalar (in m/s).

Data Types: double

## Weights - Weights applied to array

length- $N$ column vector
Weights applied to the array of sensor elements, specified as the comma-separated pair consisting of 'Weights ' and a length- $N$ column vector, where $N$ is the number of elements in the array.
Data Types: double

## SteerAngle - Subarray steering angle

[0; 0] (default) | scalar | length-2 column vector
Subarray steering angle (in degrees), specified as the comma-separated pair consisting of 'SteerAngle' and a scalar or a length-2 column vector. If the steering angle is a scalar, the value represents the azimuth angle and the elevation angle is assumed to be 0 . If the steering angle is a vector, the angle is specified in the form of [AzimuthAngle; ElevationAngle].

## Dependencies

This parameter is applicable when you set the SubarraySteering property of subarray object to either 'Phase' or 'Time'.
Data Types: double

## ElementWeights - Weights applied to each element in subarray matrix of all ones (default) | matrix | cell array

Weights applied to each element in the subarray, specified as the comma-separated pair consisting of 'ElementWeights ' and a matrix or a cell array.

For a ReplicatedSubarray object, ElementWeights must be a NSE-by-N matrix, where NSE is the number of elements in each individual subarray and $N$ is the number of subarrays. Each column in ElementWeights specifies the weights for the elements in the corresponding subarray.

For a PartitionedArray object, if the individual subarrays have the same number of elements, ElementWeights must be an NSE-by-N matrix, where NSE is the number of elements in each individual subarray and $N$ is the number of subarrays.

Each column in the WS property of the subarray object specifies the weights for the elements in the corresponding subarray. If subarrays in the PartitionedArray object have different number of elements, ElementWeights can be one of the following:

- $N S E-$ by- $N$ matrix -- NSE indicates the number of elements in the largest subarray and $N$ is the number of subarrays.
- 1-by- $N$ cell array $--N$ is the number of subarrays and each cell contains a column vector whose length is the same as the number of elements of the corresponding subarray.

If WS is a matrix, the first $K$ entries in each column specify the weights for the elements in the corresponding subarray. $K$ is the number of elements in the corresponding subarray. If WS is a cell array, each cell in the array is a column vector specifying the weights for the elements in the corresponding subarray.

## Dependencies

This parameter is applicable when you set the SubarraySteering property of subarray object to 'Custom'.
Data Types: double

## Output Arguments

## bw - Angular beamwidth

scalar in degrees
Angular beamwidth of the subarray, returned as a scalar in degrees.

## Data Types: double

## angles - Angle values of beamwidth

1 -by-2 vector in degrees
Angle values of the beamwidth, returned as a 1-by-2 vector. The two elements in the vector [ $a_{\text {min }}, a_{\text {max }}$ ] define the beamwidth bw as $a_{\max }-a_{\min }$.

## Version History

Introduced in R2020b

## See Also

## Objects

phased.PartitionedArray|phased.ReplicatedSubarray

## beamwidth

Package: phased
Compute and display beamwidth of sensor element pattern

## Syntax

beamwidth(element,freq)
beamwidth(element,freq,Name, Value)
[bw,angles] = beamwidth( $\qquad$ )

## Description

beamwidth(element, freq) plots the 2-D power pattern (in dB ) of the element for all azimuth angles at an elevation angle of zero degrees. The plot displays the half-power beamwidth (in degrees) at the frequency specified in freq (in Hz ) and the angles (in degrees) in azimuth at which the magnitude of the power pattern decreases by 3 dB from the peak of the main beam.
beamwidth (element, freq,Name, Value) plots the beamwidth with the specified parameter Name set to the specified Value. You can specify additional name-value pair arguments in any order as (Name1, Value1, . . . , NameN, ValueN).
Example: beamwidth(element,1e9,'Cut', 'Elevation)
[bw,angles] = beamwidth( $\qquad$ ) returns the angular beamwidth bw (in degrees). The function also returns the corresponding angle values (in degrees) that mark the beamwidth.

## Examples

## Plot Beamwidth of Isotropic Antenna

Plot the beamwidth for an isotropic antenna at 1 GHz .
Create an isotropic antenna using a phased. Isot ropicAntennaElement object.

```
antenna = phased.IsotropicAntennaElement('FrequencyRange',[800e6 1.2e9])
antenna =
    phased.IsotropicAntennaElement with properties:
        FrequencyRange: [800000000 1.2000e+09]
            BackBaffled: false
```

Using the beamwidth function, plot the half-power ( 3 dB ) beamwidth for the antenna. Use a frequency value of 1 GHz .
beamwidth (antenna, le9)


## Calculate Beamwidth and Angles of Cosine Antenna Element

Calculate the half-power beamwidth and angles of a cosine antenna element.
Create a phased.CosineAntennaElement object with the 'CosinePower' exponents set to 10.
myAnt = phased.CosineAntennaElement('CosinePower',[10 10])
myAnt =
phased.CosineAntennaElement with properties:
FrequencyRange: [0 1.0000e+20]
CosinePower: [10 10]

Compute the beamwidth and angles of the antenna element when it is operating at 1 GHz . Set 'dbDown' to 3 dB.
[BW,Ang] = beamwidth(myAnt,1e9,'dbDown',3)
$\mathrm{BW}=29.9600$
Ang $=1 \times 2$

## Input Arguments

## element - Antenna or microphone element

Phased Array System Toolbox System object
Antenna or microphone element, specified as a Phased Array System Toolbox System object.

## freq - Frequency used to calculate beamwidth <br> scalar in Hz

Frequency used to calculate the beamwidth, specified as a scalar in Hz .
Example: 1e9
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . , NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.
Example: beamwidth (element, 1e9, 'Cut','Azimuth', 'CutAngle', 45) plots the beamwidth of the antenna element that is operating at a frequency of 1 GHz , with the slice direction set to 'Azimuth ' , and the cut angle set to 45 degrees.

## Cut - Slice direction in azimuth-elevation space

'Azimuth' (default)|'Elevation'
The slice direction in azimuth-elevation space along which the beamwidth is computed, specified as the comma-separated pair consisting of 'Cut' and 'Azimuth' for the azimuth plane, and 'Cut 'and 'Elevation' for the elevation plane.

## CutAngle - Angle for plane to get required 2-D cut

0 (default) | scalar
Corresponding angle (in degrees) for the plane to get the required 2-D cut, specified as the commaseparated pair consisting of 'CutAngle' and a scalar. If 'Cut' is specified as 'Azimuth', then 'CutAngle' (Elevation) should lie between [-90, 90] degrees. If 'Cut' is specified as 'Elevation', then 'CutAngle' (Azimuth) should lie between [-180, 180] degrees.
Data Types: double

## dBDown - Power value from peak of main lobe

3 (default) | Inf | positive scalar
Power value from the peak of the main lobe, specified as the comma-separated pair consisting of 'dBDown ' and a positive scalar. The default value of 3 dB is equivalent to half-power beamwidth. To calculate the first-null beamwidth, specify the 'dBDown' value as Inf. Units are in dB.
Data Types: double

## Output Arguments

bw - Angular beamwidth
scalar in degrees
Angular beamwidth of the sensor element, returned as a scalar in degrees.
Data Types: double
angles - Angle values of beamwidth
1-by-2 vector in degrees
Angle values of the beamwidth, returned as a 1-by-2 vector. The two elements in the vector [ $a_{\min }, a_{\max }$ ] define the beamwidth bw as $a_{\max }-a_{\min }$.

## Version History

Introduced in R2020b

## See Also

Functions
directivity|isPolarizationCapable|pattern|patternAzimuth|patternElevation

## isPolarizationCapable

Package: phased
Antenna element polarization capability

## Syntax

capflag = isPolarizationCapable(element)

## Description

capflag = isPolarizationCapable(element) returns a Boolean value, capflag, indicating whether the antenna element supports polarization. An antenna element supports polarization if it can create or respond to polarized fields.

## Input Arguments

## element - Antenna or transducer element

Phased Array System Toolbox System object
Antenna or transducer element, specified as a Phased Array System Toolbox System object.

## Output Arguments

capflag - Polarization-capability flag
true |false
Polarization-capability flag returned as a Boolean value true if the antenna element supports polarization or false if it does not.

## Version History

Introduced in R2019a

## See Also

Functions
directivity | beamwidth | pattern | patternAzimuth | patternElevation

## pattern

Package: phased
Plot antenna or transducer element directivity and patterns

## Syntax

```
pattern(element,FREQ)
```

pattern(element, FREQ,AZ)
pattern(element, FREQ, AZ, EL)
pattern( _ , Name, Value)
[PAT,AZ_ANG,EL_ANG] = pattern( ___ )

## Description

pattern (element, FREQ) plots the 3-D array directivity pattern (in dBi) for the element specified in element. The operating frequency is specified in FREQ. You can use this function to display the patterns for antennas that support polarization.
pattern(element, FREQ,AZ) plots the element directivity pattern at the specified azimuth angle.
pattern(element, FREQ,AZ,EL) plots the element directivity pattern at specified azimuth and elevation angles.
pattern (__, Name, Value) plots the element pattern with additional options specified by one or more Name, Value pair arguments.
[PAT,AZ_ANG,EL_ANG] = pattern ( __ ) returns the element pattern in PAT. The AZ_ANG output contains the coordinate values corresponding to the rows of PAT. The EL_ANG output contains the coordinate values corresponding to the columns of PAT. If the 'CoordinateSystem' parameter is set to ' $u v$ ', then AZ_ANG contains the $U$ coordinates of the pattern and EL_ANG contains the $V$ coordinates of the pattern. Otherwise, they are in angular units in degrees. $U V$ units are dimensionless.

## Input Arguments

## element - Antenna or transducer element

Phased Array System Toolbox System object
Antenna or transducer element, specified as a Phased Array System Toolbox System object.

## FREQ - Frequency for computing directivity and patterns

positive scalar | 1-by- $L$ real-valued row vector
Frequencies for computing directivity and patterns, specified as a positive scalar or 1-by-L realvalued row vector. Frequency units are in hertz.

- For an antenna, microphone, or sonar hydrophone or projector element, FREQ must lie within the range of values specified by the FrequencyRange or FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most
elements use the FrequencyRange property except for phased.CustomAntennaElement and phased.CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.


## Example: [1e8 2e6]

Data Types: double

## AZ - Azimuth angles

[-180:180] (default) | 1-by-N real-valued row vector
Azimuth angles for computing directivity and pattern, specified as a 1-by- $N$ real-valued row vector where $N$ is the number of azimuth angles. Angle units are in degrees. Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the $x y$ plane. When measured from the $x$-axis toward the $y$-axis, this angle is positive.
Example: [-45:2:45]
Data Types: double

## EL - Elevation angles

[-90:90] (default) | 1-by-M real-valued row vector
Elevation angles for computing directivity and pattern, specified as a 1-by-M real-valued row vector where $M$ is the number of desired elevation directions. Angle units are in degrees. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

The elevation angle is the angle between the direction vector and $x y$-plane. The elevation angle is positive when measured towards the $z$-axis.

Example: [-75:1:70]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

```
Example: CoordinateSystem,'polar',Type,'directivity'
```

CoordinateSystem - Plotting coordinate system 'polar' (default)|'rectangular' | 'uv'

Plotting coordinate system of the pattern, specified as the comma-separated pair consisting of 'CoordinateSystem' and one of 'polar', 'rectangular', or 'uv'. When 'CoordinateSystem' is set to 'polar' or 'rectangular', the AZ and EL arguments specify the pattern azimuth and elevation, respectively. AZ values must lie between $-180^{\circ}$ and $180^{\circ}$. EL values must lie between $-90^{\circ}$ and $90^{\circ}$. If 'CoordinateSystem' is set to ' uv ', AZ and EL then specify $U$ and $V$ coordinates, respectively. AZ and EL must lie between -1 and 1.
Example: 'uv'

## Data Types: char

## Type - Displayed pattern type

'directivity' (default)|'efield' | 'power' | 'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb' - power pattern converted to dB.

Example: 'powerdb'
Data Types: char

## Normalize - Display normalize pattern

true (default) | false
Display normalized pattern, specified as the comma-separated pair consisting of 'Normalize' and a Boolean. Set this parameter to true to display a normalized pattern. This parameter does not apply when you set 'Type' to 'directivity'. Directivity patterns are already normalized.
Data Types: logical

## PlotStyle - Plotting style

'overlay' (default)|'waterfall'
Plotting style, specified as the comma-separated pair consisting of 'Plotstyle' and either ' overlay' or 'waterfall'. This parameter applies when you specify multiple frequencies in FREQ in 2-D plots. You can draw 2-D plots by setting one of the arguments AZ or EL to a scalar.

## Data Types: char

## Polarization - Polarization type

'combined' (default)|'H'|'V'
Polarization type, specified as the comma-separated pair consisting of 'Polarization' and either 'combined', 'H', or 'V'. If Polarization is 'combined', the horizontal and vertical polarization patterns are combined. If Polarization is ' H ' , only the horizontal polarization is displayed. If Polarization is ' V ', only the vertical polarization is displayed.

## Dependencies

To enable this property, set the element argument to an antenna that supports polarization: phased.CrossedDipoleAntennaElement, phased.ShortDipoleAntennaElement, or phased.CustomAntennaElement, and then set the 'Type' name-value pair to 'efield', 'power', or 'powerdb'.

Data Types: char | string

## Output Arguments

## PAT - Element pattern

$N$-by- $M$ real-valued matrix

Element pattern, returned as an $N$-by- $M$ real-valued matrix. The pattern is a function of azimuth and elevation. The rows of PAT correspond to the azimuth angles in the vector specified by EL_ANG. The columns correspond to the elevation angles in the vector specified by AZ_ANG.

## AZ_ANG - Azimuth angles

scalar | 1-by- $N$ real-valued row vector
Azimuth angles for displaying directivity or response pattern, returned as a scalar or 1-by- $N$ realvalued row vector corresponding to the dimension set in AZ. The columns of PAT correspond to the values in AZ_ANG. Units are in degrees.

## EL_ANG - Elevation angles

scalar | 1-by-M real-valued row vector
Elevation angles for displaying directivity or response, returned as a scalar or 1-by- $M$ real-valued row vector corresponding to the dimension set in EL. The rows of PAT correspond to the values in EL_ANG. Units are in degrees.

## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \Pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\text {rad }}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Azimuth and Elevation Angles

The azimuth angle of a vector is the angle between the $x$-axis and its orthogonal projection onto the $x y$-plane. The angle is positive when going from the $x$-axis toward the $y$-axis. Azimuth angles lie between $-180^{\circ}$ and $180^{\circ}$ degrees, inclusive. The elevation angle is the angle between the vector and its orthogonal projection onto the $x y$-plane. The angle is positive when going toward the positive $z$ axis from the $x y$-plane. Elevation angles lie between $-90^{\circ}$ and $90^{\circ}$ degrees, inclusive.


## Algorithms

## Convert plotResponse to Pattern

For antenna, transducer, and array System objects, the pattern function replaces the plotResponse function. In addition, two new simplified functions exist just to draw 2-D azimuth and elevation pattern plots. These functions are azimuthPattern and elevationPattern.

The following table is a guide for converting your code from using plotResponse to pattern. Notice that some of the inputs have changed from input arguments to Name-Value pairs and conversely. The general pattern method syntax is
pattern(H,FREQ,AZ,EL, 'Name1', 'Value1',...,' $N a m e N ', ~ ' V a l u e N ') ~$

| plotResponse Inputs | plotResponse Description | pattern Inputs |
| :--- | :--- | :--- |
| H argument | Antenna, microphone, or array <br> System object. | H argument (no change) |
| FREQ argument | Operating frequency. | FREQ argument (no change) |
| V argument | Propagation speed. This argument <br> is used only for arrays. | 'PropagationSpeed ' name-value <br> pair. This parameter is only used for <br> arrays. |


| plotResponse Inputs | plotResponse Description |  | pattern Inputs |  |
| :---: | :---: | :---: | :---: | :---: |
| 'Format' and 'RespCut' namevalue pairs | These options work together to let you create a plot in angle space (line or polar style) or $U V$ space. They also determine whether the plot is 2-D or 3-D. This table shows you how to create different types of plots using plotResponse. |  | 'CoordinateSystem' name-value pair used together with the AZ and EL input arguments. <br> 'CoordinateSystem' has the same options as the plotResponse method 'Format ' name-value pair, except that ' line' is now named 'rectangular'. The table shows how to create different types of plots using pattern. |  |
|  | Display space <br> Angle space (2D) |  |  |  |
|  | Angle space (2D) | Set 'RespCut' <br> to 'Az' or |  |  |
|  |  | 'El'. Set <br> 'Format ' to <br> 'line' or 'polar'. | Display space |  |
|  |  | ' line' or 'polar'. <br> Set the display axis using either the 'AzimuthAngle | Angle space (2D) | Set <br> Coordinate <br> System' to <br> rectangular' <br> or 'polar' <br> Specify either AZ <br> or EL as a scalar. |
|  |  | s' or 'ElevationAng les' namevalue pairs. | Angle space (3D) | Set <br> 'Coordinate <br> System' to 'rectangular' |
|  | Angle space (3D) | Set 'RespCut' to '3D'. Set |  | or 'polar'. <br> Specify both AZ <br> and EL as <br> vectors. |
|  |  | 'polar'. <br> Set the display axis using both the 'AzimuthAngle s' and 'Elevation | $U V$ space (2D) | Set <br> Coordinate System' to uv'. Use AZ to specify a $U$ space vector. Use EL to specify a $V$-space scalar. |
|  |  | Angles' namevalue pairs. | UV space (3D) |  |
|  | UV space (2D) | Set 'RespCut' to'U'. Set 'Format ' to 'UV'. Set the display range using the 'UGrid' namevalue pair. |  | 'Coordinate <br> System' to <br> 'uv'. Use AZ to <br> specify a $U$ - <br> space vector. <br> Use EL to specify <br> a $V$-space vector. |
|  |  |  | If you set CoordinateSystem to 'uv ' , enter the UV grid values using $A Z$ and $E L$. |  |
|  | UV space (3D) | $\begin{aligned} & \text { Set 'RespCut' } \\ & \text { to'3D'. Set } \\ & \text { 'Format' to } \end{aligned}$ |  |  |


| plotResponse Inputs | plotResponse Description |  | pattern Inputs |
| :---: | :---: | :---: | :---: |
|  | Display space | 'UV '. Set the display range using both the 'UGrid' and 'VGrid ' namevalue pairs. |  |
| 'CutAngle' name-value pair | Constant angle at to take an azimuth or elevation cut. When producing a 2-D plot and when 'RespCut' is set to 'Az' or 'El', use 'CutAngle' to set the slice across which to view the plot. |  | No equivalent name-value pair. To create a cut, specify either AZ or EL as a scalar, not a vector. |
| 'NormalizeResponse' namevalue pair | Normalizes the plot. When 'Unit' is set to 'dbi' , you cannot specify 'NormalizeResponse'. |  | Use the 'Normalize' name-value pair. When 'Type' is set to 'directivity' you cannot specify 'Normalize'. |
| 'OverlayFreq' name-value pair | Plot multiple frequencies on the same 2-D plot. Available only when 'Format' is set to 'line' or 'uv and 'RespCut' is not set to '3D'. The value true produces an overlay plot and the value false produces a waterfall plot. |  | 'PlotStyle' name-value pair plots multiple frequencies on the same 2-D plot. <br> The values 'overlay' and 'waterfall' correspond to 'OverlayFreq' values of true and false. The option 'waterfall' is allowed only when 'CoordinateSystem' is set to 'rectangular' or 'uv'. |
| 'Polarization' name-value pair | Determines how to plot polarized fields. Options are 'None', 'Combined', 'H', or 'V'. |  | 'Polarization ' name-value pair determines how to plot polarized fields. The 'None ' option is removed. The options 'Combined ' , ' H ', or 'V' are unchanged. |
| ' Unit ' name-value pair | Determines the plot units. Choose 'db','mag', 'pow', or 'dbi', where the default is ' db ' |  | 'Type ' name-value pair, uses equivalent options with different names |
|  |  |  | plotResponse pattern |
|  |  |  | 'db' 'powerdb' <br> 'mag' 'efield' <br> 'pow' 'power' <br> 'dbi' 'directivity' |
| 'Weights ' name-value pair | Array element tapers (or weights). |  | 'Weights ' name-value pair (no change). |
| 'AzimuthAngles ' name-value pair | Azimuth angles used to display the antenna or array response. |  | AZ argument |


| plotResponse Inputs | plotResponse Description | pattern Inputs |
| :--- | :--- | :--- |
| ' ElevationAngles ' name-value <br> pair | Elevation angles used to display the <br> antenna or array response. | EL argument |
| ' UGrid' name-value pair | Contains $U$ coordinates in $U V$ - <br> space. | AZ argument when <br> 'CoordinateSystem ' name-value <br> pair is set to 'uv ' |
| 'VGrid' name-value pair | Contains $V$-coordinates in $U V$-space. | EL argument when <br> 'CoordinateSystem ' name-value <br> pair is set to 'uv ' |

## Version History <br> Introduced in R2019a

## See Also <br> directivity|patternAzimuth|patternElevation|beamwidth

## patternAzimuth

Package: phased

Plot antenna or transducer element directivity and pattern versus azimuth

## Syntax

```
patternAzimuth(element,FREQ)
patternAzimuth(element,FREQ,EL)
patternAzimuth(element,FREQ,EL,Name,Value)
PAT = patternAzimuth(
```

$\qquad$

## Description

patternAzimuth (element, FREQ) plots the 2-D element directivity pattern versus azimuth (in dBi) for the element element at zero-degrees elevation angle. The argument FREQ specifies the operating frequency.
patternAzimuth(element, $\mathrm{FREQ}, \mathrm{EL}$ ), in addition, plots the 2-D element directivity pattern versus azimuth (in dBi) at the elevation angle specified by EL. When EL is a vector, multiple overlaid plots are created.
patternAzimuth(element, FREQ,EL,Name, Value) plots the element pattern with additional options specified by one or more Name, Value pair arguments.

PAT = patternAzimuth ( __ ) returns the element pattern. PAT is a matrix whose entries represent the pattern at corresponding sampling points specified by the 'Azimuth' parameter and the EL input argument.

## Input Arguments

## element - Antenna or transducer element

Phased Array System Toolbox System object
Antenna or transducer element, specified as a Phased Array System Toolbox System object.

## FREQ - Frequency for computing directivity and pattern <br> positive scalar

Frequency for computing directivity and pattern, specified as a positive scalar. Frequency units are in hertz.

- For an antenna or microphone element, FREQ must lie within the range of values specified by the FrequencyRange or the FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased.CustomMic rophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: 1e8
Data Types: double

## EL - Elevation angles

1-by- $N$ real-valued row vector
Elevation angles for computing sensor or array directivities and patterns, specified as a $1-b y-N$ realvalued row vector. The quantity $N$ is the number of requested elevation directions. Angle units are in degrees. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

The elevation angle is the angle between the direction vector and the xy plane. When measured toward the $z$-axis, this angle is positive.

Example: [0, 10, 20]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, ... , NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Example: Azimuth, [-90:90], Type,'directivity'

## Type - Displayed pattern type

'directivity' (default) |'efield'|'power'|'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type ' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb' - power pattern converted to dB.

Example: 'powerdb'
Data Types: char

## Azimuth - Azimuth angles

[-180:180] (default) | 1-by-P real-valued row vector
Azimuth angles, specified as the comma-separated pair consisting of 'Azimuth' and a 1-by-P realvalued row vector. Azimuth angles define where the array pattern is calculated.
Example: 'Azimuth', [-90:2:90]
Data Types: double

## Output Arguments

## PAT - Element directivity or pattern

$P$-by- $N$ real-valued matrix

Element directivity or pattern, returned as an $P$-by- $N$ real-valued matrix. The dimension $P$ is the number of azimuth values determined by the 'Azimuth ' name-value pair argument. The dimension $N$ is the number of elevation angles, as determined by the EL input argument.

## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Azimuth and Elevation Angles

The azimuth angle of a vector is the angle between the $x$-axis and its orthogonal projection onto the $x y$-plane. The angle is positive when going from the $x$-axis toward the $y$-axis. Azimuth angles lie between $-180^{\circ}$ and $180^{\circ}$ degrees, inclusive. The elevation angle is the angle between the vector and its orthogonal projection onto the $x y$-plane. The angle is positive when going toward the positive $z$ axis from the $x y$-plane. Elevation angles lie between $-90^{\circ}$ and $90^{\circ}$ degrees, inclusive.


## Version History

Introduced in R2019a

## See Also

directivity | pattern|patternElevation| beamwidth

## patternElevation

Package: phased
Plot antenna or transducer element directivity and pattern versus elevation

## Syntax

```
patternElevation(element,FREQ)
patternElevation(element,FREQ,AZ)
patternElevation(element,FREQ,AZ,Name,Value)
PAT = patternElevation(
```

$\qquad$

``` )
```


## Description

patternElevation(element, FREQ) plots the 2-D element directivity pattern versus elevation (in dBi ) for the element element at zero-degrees azimuth angle. The argument FREQ specifies the operating frequency.
patternElevation(element, FREQ,AZ), in addition, plots the 2-D element directivity pattern versus elevation (in dBi ) at the azimuth angle specified by $A Z$. When $A Z$ is a vector, multiple overlaid plots are created.
patternElevation(element, FREQ,AZ,Name, Value) plots the element pattern with additional options specified by one or more Name, Value pair arguments.

PAT = patternElevation ( _ _ ) returns the element pattern. PAT is a matrix whose entries represent the pattern at corresponding sampling points specified by the 'Elevation' parameter and the AZ input argument.

## Input Arguments

## element - Antenna or transducer element

Phased Array System Toolbox System object
Antenna or transducer element, specified as a Phased Array System Toolbox System object.

## FREQ - Frequency for computing directivity and pattern <br> positive scalar

Frequency for computing directivity and pattern, specified as a positive scalar. Frequency units are in hertz.

- For an antenna or microphone element, FREQ must lie within the range of values specified by the FrequencyRange or the FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased.CustomMic rophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.


## Example: 1e8

Data Types: double

## AZ - Azimuth angles for computing directivity and pattern

1-by- $N$ real-valued row vector
Azimuth angles for computing sensor or array directivities and patterns, specified as a 1 -by- N realvalued row vector where $N$ is the number of desired azimuth directions. Angle units are in degrees. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the $x y$ plane. This angle is positive when measured from the $x$-axis toward the $y$-axis.
Example: [0,10, 20]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, ... ,NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.

## Example: Azimuth, [-90:90], Type,' directivity'

## Type - Displayed pattern type

'directivity' (default)|'efield' | 'power' | 'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type' and one of

- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb' - power pattern converted to dB.

Example: 'powerdb'
Data Types: char

## Elevation - Elevation angles

[-90:90] (default)| 1-by-P real-valued row vector
Elevation angles, specified as the comma-separated pair consisting of 'Elevation' and a 1-by-P real-valued row vector. Elevation angles define where the array pattern is calculated.

Example: 'Elevation', [-90:2:90]
Data Types: double

## Output Arguments

## PAT - Element directivity or pattern

$P$-by- $N$ real-valued matrix

Element directivity or pattern, returned as an $P$-by- $N$ real-valued matrix. The dimension $P$ is the number of elevation angles determined by the 'Elevation' name-value pair argument. The dimension $N$ is the number of azimuth angles determined by the AZ argument.

## More About

## Directivity

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power

$$
D=4 \Pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\mathrm{total}}}
$$

where $U_{\mathrm{rad}}(\theta, \varphi)$ is the radiant intensity of a transmitter in the direction $(\theta, \varphi)$ and $P_{\text {total }}$ is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as $d B i$. For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

## Azimuth and Elevation Angles

The azimuth angle of a vector is the angle between the $x$-axis and its orthogonal projection onto the $x y$-plane. The angle is positive when going from the $x$-axis toward the $y$-axis. Azimuth angles lie between $-180^{\circ}$ and $180^{\circ}$ degrees, inclusive. The elevation angle is the angle between the vector and its orthogonal projection onto the $x y$-plane. The angle is positive when going toward the positive $z$ axis from the $x y$-plane. Elevation angles lie between $-90^{\circ}$ and $90^{\circ}$ degrees, inclusive.


## Version History

Introduced in R2019a

## See Also

directivity | pattern | patternAzimuth | beamwidth

## plotSpectrum

Package: phased
Plot spatial spectrum

## Syntax

plotSpectrum(estimator)
plotSpectrum(estimator,Name, Value)
hl = plotSpectrum( $\qquad$ )

## Description

plotSpectrum(estimator) plots the spatial spectrum resulting from the most recent execution of the estimator object.
plotSpectrum(estimator, Name, Value) plots the spatial spectrum with additional options specified by one or more Name, Value pair arguments.
hl = plotSpectrum( $\qquad$ ) returns the line handle of the spectrum plot in the figure.

## Input Arguments

## estimator - Spectrum estimator

System object
Spectrum estimator, specified as a Phased Array System Toolbox System object.

## Name-Value Pair Arguments

Specify optional pairs of arguments as Namel=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.
Example: 'NormalizedResponse',true,'Unit','pow'

## NormalizeResponse - Plot normalized response

false (default) | true
Option to enable plotting of normalized response, specified as false or true. Set this value to true to plot the normalized spectrum. Set this value to fal se to plot the spectrum without normalization.

## Data Types: logical

## Title - Title of plot figure

' ' (default) | character vector
Title of plot figure, specified as a character vector.
Example: 'Beamscan Spectrum'

Data Types: char
Unit - Plot units
'db' (default)|'mag' | 'pow'
Plot units, specified as

- 'db' - decibels
- 'mag' - magnitude
- 'pow' - power


## Output Arguments

hl - Line handle
line handle
Plot line, returned as a handle.

## Version History

Introduced in R2012a

## collectPlaneWave

Simulate received plane waves at array

## Syntax

$Y=$ collectPlaneWave(array, $X$, ang)
$Y$ = collectPlaneWave(array,X,ang,freq)
Y = collectPlaneWave(array, X, ang,freq, c)

## Description

$Y=$ collectPlaneWave(array, $X$, ang) returns the sum $Y$ of received signals $X$ arriving at the sensor array from the directions specified in ang.
$Y=$ collectPlaneWave(array, $X$, ang, freq ) also specifies the incoming signal carrier frequency freq.
$Y=\operatorname{collectPlaneWave(array,X,ang,freq,c)~also~specifies~the~signal~propagation~speed~} c$.

## Examples

## Simulate Received Signals at ULA

Simulate two received plane-wave random signals at a 4 -element ULA. The signals arrive from $10^{\circ}$ and $30^{\circ}$ azimuth. Both signals have an elevation angle of $0^{\circ}$. Assume the propagation speed is the speed of light and the carrier frequency of the signal is 100 MHz .

```
array = phased.ULA(4);
y = collectPlaneWave(array,randn(4,2),[10 30],100e6,physconst('LightSpeed'))
y = 4x4 complex
\begin{tabular}{rrrr}
\(0.7430-0.3705 i\) & \(0.8433-0.1314 i\) & \(0.8433+0.1314 i\) & \(0.7430+0.3705 i\) \\
\(0.8418+0.4308 i\) & \(0.5632+0.1721 i\) & \(0.5632-0.1721 i\) & \(0.8418-0.4308 i\) \\
\(-2.4817+0.9157 i\) & \(-2.6683+0.3175 i\) & \(-2.6683-0.3175 i\) & \(-2.4817-0.9157 i\) \\
\(1.0724-0.4748 i\) & \(1.1895-0.1671 i\) & \(1.1895+0.1671 i\) & \(1.0724+0.4748 i\)
\end{tabular}
```


## Input Arguments

## array - Phased array System object

System object
Phased array, specified as a Phased Array System Toolbox System object.

## X - Incoming signals

$P$-by- $M$ complex-valued matrix

Incoming signals in each direction, specified as a $P$-by- $M$ complex-valued matrix. $M$ is the number of signals impinging on the array. Each column of $X$ represents an individual incoming signal. $P$ is the number of signal samples. Each signal is assumed to arrive from the direction specified by the ang argument.
Example: [1, 5; 2, 10;3,10]
Data Types: double
Complex Number Support: Yes
ang - Arrival directions of incoming signals
1-by- $M$ real-valued vector | 2 -by- $M$ real-valued matrix
Arrival directions of incoming signals, specified as a 1-by- $M$ vector or a 2 -by- $M$ matrix, where $M$ is the number of incoming signals. Each column specifies the direction of arrival of the corresponding signal in $X$. If ANG is a 2-by- $M$ matrix, each column specifies the direction in azimuth and elevation of the incoming signal [az;el]. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$ and the elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$.

If ANG is a $1-b y-M$ vector, then each entry represents a set of azimuth angles, with the elevation angles assumed to be zero. Angle units are in degrees.

The azimuth angle is the angle between the $x$-axis and the projection of the arrival direction vector onto the xy plane. When measured from the $x$-axis toward the $y$-axis, the azimuth angle is positive.

The elevation angle is the angle between the arrival direction vector and the $x y$-plane. When measured toward the $z$ axis, the elevation angle is positive.

Example: [20, 30;15,25]
Data Types: double

## freq - Signal carrier frequency

3e8 (default) | positive scalar
Signal carrier frequency, specified as a positive scalar. Units are in Hz.
Data Types: double
c - Signal propagation speed
speed of light (default) | positive scalar
Signal propagation speed, specified as a positive scalar. Units are in meters per second.
Example: physconst('LightSpeed ')
Data Types: double

## Output Arguments

## $\mathbf{Y}$ - Combined received signals

$P$-by- $N$ complex-valued matrix
Combined received signals at each array element, returned as a $P$-by- $N$ complex-valued matrix where $N$ is the number of array elements. Each column of $Y$ contains the combined received signals at the corresponding array element. $P$ is the number of signal samples.

Data Types: double

## Algorithms

The collectPlaneWave modulates a signal by a phase delay caused by the direction of arrival. This is called the phase-shift approximation. The method does not account for the response of individual elements in the array.

For further details, see Van Trees [1] .

## Version History

Introduced in R2021a

## References

[1] Van Trees, H. Optimum Array Processing. New York: Wiley-Interscience, 2002.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{Tm}}$.

## See Also

uv2azel | phitheta2azel

## directivity

Compute array directivity

## Syntax

D = directivity (array, FREQ,ANGLE)
directivity( ,Name, Value)

## Description

D = directivity(array,FREQ,ANGLE) returns the "Directivity (dBi)" on page 1-1743 of an array of antenna or microphone elements, array, at frequencies specified by FREQ and in angles of direction specified by ANGLE.

The integration used when computing array directivity has a minimum sampling grid of 0.1 degrees. If an array pattern has a beamwidth smaller than this, the directivity value will be inaccurate.
directivity (__ , Name, Value) plots the array pattern with additional options specified by one or more Name, Value pair arguments.

## Examples

## Directivity of Uniform Linear Array

Compute the directivities of two different uniform linear arrays (ULA). One array consists of isotropic antenna elements and the second array consists of cosine antenna elements. In addition, compute the directivity when the first array is steered in a specified direction. For each case, calculate the directivities for a set of seven different azimuth directions all at zero degrees elevation. Set the frequency to 800 MHz .

## Array of isotropic antenna elements

First, create a 10 -element ULA of isotropic antenna elements spaced $1 / 2$-wavelength apart.

```
c = physconst('LightSpeed');
fc = 3e8;
lambda = c/fc;
ang = [-30,-20,-10,0,10,20,30; 0,0,0,0,0,0,0];
myAnt1 = phased.IsotropicAntennaElement;
myArray1 = phased.ULA(10,lambda/2,'Element',myAnt1);
Compute the directivity.
```

```
d = directivity(myArray1,fc,ang,'PropagationSpeed',c)
```

d = directivity(myArray1,fc,ang,'PropagationSpeed',c)
d = 7\times1
-6.9886
-6.2283
-6.5176

```

\section*{Array of cosine antenna elements}

Next, create a 10 -element ULA of cosine antenna elements spaced \(1 / 2\)-wavelength apart.
myAnt2 = phased.CosineAntennaElement('CosinePower',[1.8,1.8]);
myArray2 = phased.ULA(10,lambda/2,'Element',myAnt2);
Compute the directivity.
```

d = directivity(myArray2,fc,ang,'PropagationSpeed',c)
d = 7x1
-1.9838
0.0529
0.4968
17.2548
0.4968
0.0529
-1.9838

```

The directivity of the cosine ULA is greater than the directivity of the isotropic ULA because of the larger directivity of the cosine antenna element.

\section*{Steered array of isotropic antenna elements}

Finally, steer the isotropic antenna array to 30 degrees in azimuth and compute the directivity.
```

w = steervec(getElementPosition(myArray1)/lambda,[30;0]);
d = directivity(myArray1,fc,ang,'PropagationSpeed',c,...
'Weights',w)
d = 7x1
-297.2705
-13.9783
-9.5713
-6.9897
-4.5787
-2.0536
10.0000

```

The directivity is greatest in the steered direction.

\section*{Input Arguments}

\section*{array - Phased array}

Phased Array System Toolbox System object
Phased array, specified as a Phased Array System Toolbox System object.

\section*{FREQ - Frequency for computing directivity and patterns}
positive scalar | 1-by-L real-valued row vector
Frequencies for computing directivity and patterns, specified as a positive scalar or 1-by-L realvalued row vector. Frequency units are in hertz.
- For an antenna, microphone, or sonar hydrophone or projector element, FREQ must lie within the range of values specified by the FrequencyRange or FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased. CustomAntennaElement and phased. CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

\section*{Example: [1e8 2e6]}

Data Types: double

\section*{ANGLE - Angles for computing directivity}

1-by- \(M\) real-valued row vector | 2 -by- \(M\) real-valued matrix
Angles for computing directivity, specified as a 1-by- \(M\) real-valued row vector or a 2 -by- \(M\) real-valued matrix, where \(M\) is the number of angular directions. Angle units are in degrees. If ANGLE is a 2 -by- \(M\) matrix, then each column specifies a direction in azimuth and elevation, [az;el]. The azimuth angle must lie between \(-180^{\circ}\) and \(180^{\circ}\). The elevation angle must lie between \(-90^{\circ}\) and \(90^{\circ}\).

If ANGLE is a 1-by- \(M\) vector, then each entry represents an azimuth angle, with the elevation angle assumed to be zero.

The azimuth angle is the angle between the \(x\)-axis and the projection of the direction vector onto the \(x y\) plane. This angle is positive when measured from the \(x\)-axis toward the \(y\)-axis. The elevation angle is the angle between the direction vector and \(x y\) plane. This angle is positive when measured towards the \(z\)-axis. See "Azimuth and Elevation Angles".
Example: [45 60; 0 10]
Data Types: double

\section*{Name-Value Pair Arguments}

Specify optional pairs of arguments as Namel=Value1, . . , NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.
Example: CoordinateSystem, 'polar', Type, 'directivity'
PropagationSpeed - Signal propagation speed
speed of light (default) | positive scalar
Signal propagation speed, specified as the comma-separated pair consisting of ' PropagationSpeed ' and a positive scalar in meters per second.
Example: 'PropagationSpeed', physconst('LightSpeed')
Data Types: double

\section*{Weights - Array weights}

1 (default) | \(N\)-by-1 complex-valued column vector \(\mid N\)-by- \(L\) complex-valued matrix
Array weights, specified as the comma-separated pair consisting of 'Weights' and an \(N\)-by-1 complex-valued column vector or \(N\)-by- \(L\) complex-valued matrix. Array weights are applied to the elements of the array to produce array steering, tapering, or both. The dimension \(N\) is the number of elements in the array. The dimension \(L\) is the number of frequencies specified by FREQ.
\begin{tabular}{|l|l|l|}
\hline Weights Dimension & FREQ Dimension & Purpose \\
\hline \begin{tabular}{l}
\(N\)-by-1 complex-valued column \\
vector
\end{tabular} & Scalar or 1-by-L row vector & \begin{tabular}{l} 
Applies a set of weights for the \\
single frequency or for all \(L\) \\
frequencies.
\end{tabular} \\
\hline\(N\)-by- \(L\) complex-valued matrix & 1-by-L row vector & \begin{tabular}{l} 
Applies each of the \(L\) columns of \\
'Weights' for the \\
corresponding frequency in \\
FREQ.
\end{tabular} \\
\hline
\end{tabular}

Note Use complex weights to steer the array response toward different directions. You can create weights using the phased. SteeringVector System object or you can compute your own weights. In general, you apply Hermitian conjugation before using weights in any Phased Array System Toolbox function or System object such as phased.Radiator or phased. Collector. However, for the directivity, pattern, patternAzimuth, and patternElevation methods of any array System object use the steering vector without conjugation.

\section*{Example: 'Weights', ones ( \(\mathrm{N}, \mathrm{M}\) )}

Data Types: double
Complex Number Support: Yes

\section*{Output Arguments}

\section*{D - Directivity}

M-by-L matrix
Directivity, returned as an \(M\)-by- \(L\) matrix. Each row corresponds to one of the \(M\) angles specified by ANGLE. Each column corresponds to one of the \(L\) frequency values specified in FREQ. Directivity units are in dBi where dBi is defined as the gain of an element relative to an isotropic radiator.

\section*{More About}

\section*{Directivity (dBi)}

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power
\[
D=4 \pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
\]
where \(U_{\mathrm{rad}}(\theta, \varphi)\) is the radiant intensity of a transmitter in the direction \((\theta, \varphi)\) and \(P_{\text {total }}\) is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as \(d B i\). For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

\section*{Azimuth and Elevation Angles}

Define the azimuth and elevation conventions used in the toolbox.
The azimuth angle of a vector is the angle between the \(x\)-axis and its orthogonal projection onto the \(x y\)-plane. The angle is positive when going from the \(x\)-axis toward the \(y\)-axis. Azimuth angles lie between \(-180^{\circ}\) and \(180^{\circ}\) degrees, inclusive. The elevation angle is the angle between the vector and its orthogonal projection onto the \(x y\)-plane. The angle is positive when going toward the positive \(z\) axis from the \(x y\)-plane. Elevation angles lie between \(-90^{\circ}\) and \(90^{\circ}\) degrees, inclusive.


Version History
Introduced in R2021a

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® Coder \(^{\mathrm{TM}}\).

\section*{See Also}
pattern | patternAzimuth | patternElevation

\section*{getElementNormal}

Normal vectors for array elements

\section*{Syntax}
```

normvec = getElementNormal(array)
normvec = getElementNormal(array,elemidx)

```

\section*{Description}
normvec \(=\) getElementNormal(array) returns the normal vectors normvec to the array.
normvec \(=\) getElementNormal (array, elemidx) returns only the normals of the elements that are specified in the element index vector elemidx.

\section*{Examples}

\section*{ULA Element Normals}

Construct three ULAs with elements along the \(x\)-, \(y\)-, and \(z\)-axes. Obtain the element normals.
First, choose the array axis along the \(x\)-axis.
```

sULA1 = phased.ULA('NumElements',5,'ArrayAxis','x');
norm = getElementNormal(sULA1)
norm = 2 x5

| 90 | 90 | 90 | 90 | 90 |
| ---: | ---: | ---: | ---: | ---: |
| 0 | 0 | 0 | 0 | 0 |

```

The element normal vectors point along the \(y\)-axis.
Next, choose the array axis along the \(y\)-axis.
```

sULA2 = phased.ULA('NumElements',5,'ArrayAxis','y');
norm = getElementNormal(sULA2)
norm = 2\times5
0

```

The element normal vectors point along the \(x\)-axis.
Finally, set the array axis along the \(z\)-axis. Obtain the normal vectors of the odd-numbered elements.
sULA3 = phased.ULA('NumElements',5,'ArrayAxis','z');
norm = getElementNormal(sULA3, [1, 3,5])
```

norm = 2×3
0 0 0
0 0 0

```

The element normal vectors also point along the \(x\)-axis.

\section*{Input Arguments}

\section*{array - Phased array System object}

System object
Phased array, specified as a System object.
elemidx - Element index vector
all element indexes (default) | vector of positive integers
Element index vector, specified as a vector of positive integers each of which takes a value from 1 to \(N\). The dimension \(N\) is the number of elements of the array.
Example: [1, 2, 3]

\section*{Output Arguments}

\section*{normvec - Normal vector}

2-by-M real-valued matrix
Normal vector of array elements, returned as a 2-by-M real matrix. Each column of normvec specifies the normal direction of the corresponding element in the local coordinate system in the form [azimuth; elevation]. If the input argument elemidx is not specified, \(M\) is the number of elements of the array, \(N\). If elemidx is specified, \(M\) is the size of elemidx. The azimuth angle is defined as the angle from \(x\)-axis toward \(y\) axis. The elevation angle is defined as the angle from \(x y\) plane toward \(z\)-axis. Units are in degrees.

For uniform linear arrays, the normal vector depends upon the value of the ArrayAxis property.
\begin{tabular}{|l|l|}
\hline ArrayAxis Property Value & Array Normal Direction \\
\hline\(' x^{\prime}\) & azimuth \(=90^{\circ}\), elevation \(=0^{\circ}(y\)-axis \()\) \\
\hline\(' y\) ' & azimuth \(=0^{\circ}\), elevation \(=0^{\circ}(x\)-axis \()\) \\
\hline\(' z\) ' & azimuth \(=0^{\circ}\), elevation \(=0^{\circ}(x\)-axis \()\) \\
\hline
\end{tabular}
- For a conformal array, the origin of the local coordinate system, i.e., the phase center of the array, is defined at an arbitrary point. In local coordinate system, \(\mathrm{x}, \mathrm{y}\), and z axes are three orthogonal axes with x axis defines the normal direction of the conformal array. The elements are located in the 3D space.

\section*{Version History}

\section*{Introduced in R2021a}

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® \({ }^{\circledR}\) Coder \(^{\mathrm{TM}}\).

\section*{getElementPosition}

Positions of array elements

\section*{Syntax}
```

pos = getElementPosition(array)
pos = getElementPosition(array,elemidx)

```

\section*{Description}
pos \(=\) getElementPosition(array) returns the element positions pos of the System object array.
pos \(=\) getElementPosition(array,elemidx) returns only the positions of the elements that are specified in the element index vector elemidx.

\section*{Examples}

\section*{ULA Element Positions}

Construct a ULA with 5 elements along the \(z\)-axis. Obtain the element positions.
```

sULA = phased.ULA('NumElements',5,'ArrayAxis','z');
pos = getElementPosition(sULA)
pos = 3\times5

```
\begin{tabular}{rrrrr}
0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 \\
-1.0000 & -0.5000 & 0 & 0.5000 & 1.0000
\end{tabular}

\section*{Input Arguments}

\section*{array - Phased array System object}

System object
Phased array, specified as a System object.
elemidx - Element index vector
all element indexes (default) | vector of positive integers
Element index vector, specified as a vector of positive integers each of which takes a value from 1 to \(N\). The quantity \(N\) is the number of elements of the array.
Example: [1, 2, 3]

\section*{Output Arguments}

\section*{pos - Positions of array elements}

3-by-M real matrix
Positions of array elements, returned as a 3-by- \(M\) real matrix. Each column of pos defines the position of an element in the local coordinate system, using the form \([x ; y ; z\) ]. If the input argument elemidx is not specified, \(M\) is the number of elements of the array, \(N\). If elemidx is specified, \(M\) is the dimension of elemidx. Units are in meters

\section*{Version History}

Introduced in R2021a

\section*{Extended Capabilities}

\section*{C/C++ Code Generation}

Generate C and \(\mathrm{C}++\) code using MATLAB® Coder \(^{\mathrm{Tm}}\).

\section*{getNumElements}

Number of elements in an array

\section*{Syntax}

N = getNumElements(array)

\section*{Description}
\(\mathrm{N}=\) getNumElements(array) returns the number of elements N in the array array.

\section*{Examples}

\section*{Number of Elements of UCA}

Create a UCA with the default number of elements. Verify that there are five elements.
sArray = phased.UCA();
\(\mathrm{N}=\) getNumElements(sArray)
\(N=5\)

\section*{Input Arguments}

\section*{array - Phased array System object}

System object
Phased array, specified as a System object.

\section*{Output Arguments}

N - Number of array elements
positive integer
Number of elements of array, returned as a positive integer.

\section*{Version History}

Introduced in R2021a

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® Coder \(^{\mathrm{TM}}\).

\section*{getTaper}

Array element tapers

\section*{Syntax}
wts = getTaper(array)

\section*{Description}
wts = getTaper(array) returns the tapers wts applied to each element of the phased array array. Tapers are often referred to as weights.

\section*{Examples}

\section*{Construct ULA with Taylor Window}

Construct a 5 -element ULA with a Taylor window taper. Then, obtain the element taper values.
```

taper = taylorwin(5)';
array = phased.ULA(5,'Taper',taper);
w = getTaper(array)
w = 5 < 1
0.5181
1.2029
1.5581
1.2029
0.5181

```

\section*{Input Arguments}
array - Phased array System object
System object
Phased array, specified as a Phased Array System Toolbox System object.

\section*{Output Arguments}
wts - Array element tapers
\(N\)-by-1 complex-valued vector
Array element tapers, returned as an \(N\)-by- 1 complex-valued vector, where \(N\) is the number of elements in the array.

\section*{Version History}

Introduced in R2021a

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® Coder \(^{\mathrm{TM}}\).

\section*{isPolarizationCapable}

Array polarization capability

\section*{Syntax}
```

capflag = isPolarizationCapable(array)

```

\section*{Description}
capflag = isPolarizationCapable(array) returns a Boolean value, capflag, indicating whether the array supports polarization. An array supports polarization if it can create or respond to polarized fields.

\section*{Examples}

\section*{Short-Dipole Antenna ULA Supports Polarization}

Show that an array of phased.ShortDipoleAntennaElement antenna elements supports polarization.
```

antenna = phased.ShortDipoleAntennaElement(...
'FrequencyRange',[1e9 10e9]);
array = phased.ULA('NumElements',3,'Element',antenna);
isPolarizationCapable(array)
ans = logical
1

```

The returned value of 1 shows that this array supports polarization.

\section*{Input Arguments}
array - Array
Phased Array System Toolbox System object
Array, specified as a Phased Array System Toolbox System object.

\section*{Output Arguments}

\section*{capflag - Polarization-capability flag}
true |false
Polarization-capability flag returned as a Boolean value true if the array supports polarization or false if it does not.

\section*{Version History}

Introduced in R2021a

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® Coder \(^{\mathrm{TM}}\).

\section*{pattern}

Package: phased
Plot array directivity and patterns

\section*{Syntax}
```

pattern(array,FREQ)
pattern(array,FREQ,AZ)
pattern(array,FREQ,AZ,EL)
pattern(__, Name,Value)
[PAT,AZ_ANG,EL_ANG] = pattern(___)

```

\section*{Description}
pattern (array, FREQ) plots the 3-D array directivity pattern (in dBi) for the array specified in array. The operating frequency is specified in FREQ. You can use this function to display the patterns of arrays that support polarization.
pattern(array, FREQ,AZ) plots the array directivity pattern at the specified azimuth angle.
pattern(array, FREQ,AZ,EL) plots the array directivity pattern at specified azimuth and elevation angles.
pattern(__,Name, Value) plots the array pattern with additional options specified by one or more Name, Value pair arguments.
[PAT,AZ ANG,EL ANG] = pattern( \(\qquad\) ) returns the array pattern in PAT. The AZ_ANG output contains the coordinate values corresponding to the rows of PAT. The EL_ANG output contains the coordinate values corresponding to the columns of PAT. If the 'CoordinateSystem' parameter is set to ' uv', then AZ_ANG contains the \(U\) coordinates of the pattern and EL_ANG contains the \(V\) coordinates of the pattern. Otherwise, they are in angular units in degrees. \(U V\) units are dimensionless.

\section*{Examples}

\section*{Plot Response of NR Rectangular Panel Array}

Construct a 5G antenna array where the grid is 2-by-2 and each panel is a 4 -by-4 array. Each antenna element consists of two short-dipole antennas with different dipole axis directions. The antenna elements are spaced \(1 / 2\) wavelength apart and the panels are spaced 3 wavelengths apart. Plot the response pattern of the array assuming an operating frequency of 6 GHz .
```

c = physconst('LightSpeed');
fc = 6e9;
lambda = c/fc;
antenna1 = phased.ShortDipoleAntennaElement('AxisDirection','Z');
antenna2 = phased.ShortDipoleAntennaElement('AxisDirection','X');
array = phased.NRRectangularPanelArray('ElementSet', ...

```
\{antenna1, antenna2\},'Size',[4, 4, 2, 2],'Spacing', ...
[0.5*lambda, 0.5*lambda,3*lambda, 3*lambda]);
pattern(array,fc, 'ShowArray',true)


Use the Orientation property of pattern to change the orientation \(80^{\circ}\) along the \(x\)-axis, \(30^{\circ}\) along the \(y\)-axis and \(60^{\circ}\) along the \(z\)-axis.
pattern(array,fc,'Orientation',[80;30;60],'ShowArray',true)


Disable the display of local coordinates and the colorbar.
pattern(array,fc,'ShowLocalCoordinate',false,'ShowColorBar',false)

\section*{3D Directivity Pattern}


\section*{Input Arguments}

\section*{array - Phased array}

Phased Array System Toolbox System object
Phased array, specified as a Phased Array System Toolbox System object.

\section*{FREQ - Frequency for computing directivity and patterns}
positive scalar | 1-by-L real-valued row vector
Frequencies for computing directivity and patterns, specified as a positive scalar or 1-by-L realvalued row vector. Frequency units are in hertz.
- For an antenna, microphone, or sonar hydrophone or projector element, FREQ must lie within the range of values specified by the FrequencyRange or FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased. CustomAntennaElement and phased.CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: [1e8 2e6]
Data Types: double

\section*{AZ - Azimuth angles}
[-180:180] (default) | 1 -by- \(N\) real-valued row vector
Azimuth angles for computing directivity and pattern, specified as a 1-by- \(N\) real-valued row vector where \(N\) is the number of azimuth angles. Angle units are in degrees. Azimuth angles must lie between \(-180^{\circ}\) and \(180^{\circ}\).

The azimuth angle is the angle between the \(x\)-axis and the projection of the direction vector onto the \(x y\) plane. When measured from the \(x\)-axis toward the \(y\)-axis, this angle is positive.

Example: [-45:2:45]
Data Types: double

\section*{EL - Elevation angles}
[-90:90] (default) | 1-by-M real-valued row vector
Elevation angles for computing directivity and pattern, specified as a 1-by-M real-valued row vector where \(M\) is the number of desired elevation directions. Angle units are in degrees. The elevation angle must lie between \(-90^{\circ}\) and \(90^{\circ}\).

The elevation angle is the angle between the direction vector and \(x y\)-plane. The elevation angle is positive when measured towards the \(z\)-axis.
Example: [-75:1:70]
Data Types: double

\section*{Name-Value Pair Arguments}

Specify optional pairs of arguments as Namel=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.
Example: CoordinateSystem, 'polar', Type, 'directivity'

\section*{CoordinateSystem - Plotting coordinate system} 'polar' (default) | 'rectangular' | 'uv'

Plotting coordinate system of the pattern, specified as the comma-separated pair consisting of 'CoordinateSystem' and one of 'polar', 'rectangular', or 'uv'. When
'CoordinateSystem' is set to 'polar' or 'rectangular', the AZ and EL arguments specify the pattern azimuth and elevation, respectively. AZ values must lie between \(-180^{\circ}\) and \(180^{\circ}\). EL values must lie between \(-90^{\circ}\) and \(90^{\circ}\). If 'CoordinateSystem' is set to ' \(u v^{\prime}\) ', AZ and EL then specify \(U\) and \(V\) coordinates, respectively. AZ and EL must lie between -1 and 1 .
Example: 'uv'
Data Types: char

\section*{Type - Displayed pattern type}
'directivity' (default)|'efield' | 'power' | 'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type' and one of
- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb' - power pattern converted to dB.

Example: ' powerdb'
Data Types: char
Orientation - Array orientation
[0;0;0]. (default)|3-by-1 real-valued column vector
Array orientation, specified as a 3-by-1 real-valued column vector containing the rotation angles with respect to the \(x-y\)-, and \(z\)-axes of the local coordinate system, respectively.

\section*{Normalize - Display normalize pattern}
true (default) | false
Display normalized pattern, specified as the comma-separated pair consisting of 'Normalize' and a Boolean. Set this parameter to true to display a normalized pattern. This parameter does not apply when you set 'Type' to 'directivity'. Directivity patterns are already normalized.
Data Types: logical

\section*{ShowArray - View array geometry}
false (default) | true
View the array geometry along with the 3D radiation pattern, specified as false or true.
Data Types: logical

\section*{ShowLocalCoordinates - Show local coordinate axes \\ true (default) | false}

Show the local coordinate axes, specified as true or false.
Data Types: logical

\section*{ShowColorbar - Show colorbar \\ true (default) | false}

Show the colorbar, specified as true or false.
Data Types: logical

\section*{Parent - Handle to axis}
scalar
Handle to the axes along which the array geometry is displayed specified as a scalar.

\section*{PlotStyle - Plotting style}
'overlay' (default)| 'waterfall'
Plotting style, specified as the comma-separated pair consisting of 'Plotstyle' and either 'overlay' or 'waterfall'. This parameter applies when you specify multiple frequencies in FREQ in 2-D plots. You can draw 2-D plots by setting one of the arguments AZ or EL to a scalar.

\section*{Data Types: char}

\section*{Polarization - Polarization type}
'combined' (default)|'H'| 'V'
Polarization type, specified as the comma-separated pair consisting of 'Polarization' and either 'combined', 'H', or 'V'. If Polarization is 'combined', the horizontal and vertical polarization patterns are combined. If Polarization is ' H ' , only the horizontal polarization is displayed. If Polarization is ' V ', only the vertical polarization is displayed.

\section*{Dependencies}

To enable this property, set the array argument to an array that supports polarization and then set the 'Type' name-value pair to 'efield', 'power', or 'powerdb'.
Data Types: char \| string

\section*{PropagationSpeed - Signal propagation speed}
speed of light (default) | positive scalar
Signal propagation speed, specified as the comma-separated pair consisting of
' PropagationSpeed ' and a positive scalar in meters per second.
Example: 'PropagationSpeed', physconst('LightSpeed')
Data Types: double

\section*{Weights - Array weights}

1 (default) | \(N\)-by-1 complex-valued column vector | \(N\)-by-L complex-valued matrix
Array weights, specified as the comma-separated pair consisting of 'Weights' and an \(N\)-by- 1 complex-valued column vector or \(N\)-by- \(L\) complex-valued matrix. Array weights are applied to the elements of the array to produce array steering, tapering, or both. The dimension \(N\) is the number of elements in the array. The dimension \(L\) is the number of frequencies specified by FREQ.
\begin{tabular}{|l|l|l|}
\hline Weights Dimension & FREQ Dimension & Purpose \\
\hline \begin{tabular}{l}
\(N\)-by-1 complex-valued column \\
vector
\end{tabular} & Scalar or 1-by-L row vector & \begin{tabular}{l} 
Applies a set of weights for the \\
single frequency or for all \(L\) \\
frequencies.
\end{tabular} \\
\hline\(N\)-by- \(L\) complex-valued matrix & 1-by-L row vector & \begin{tabular}{l} 
Applies each of the \(L\) columns of \\
'Weights' for the \\
corresponding frequency in \\
FREQ.
\end{tabular} \\
\hline
\end{tabular}

Note Use complex weights to steer the array response toward different directions. You can create weights using the phased. SteeringVector System object or you can compute your own weights. In general, you apply Hermitian conjugation before using weights in any Phased Array System Toolbox function or System object such as phased.Radiator or phased. Collector. However, for the directivity, pattern, patternAzimuth, and patternElevation methods of any array System object use the steering vector without conjugation.

Example: 'Weights', ones ( \(\mathrm{N}, \mathrm{M}\) )
Data Types: double

\section*{Output Arguments}

\section*{PAT - array pattern}
\(N\)-by-M real-valued matrix
Array pattern, returned as an \(N\)-by- \(M\) real-valued matrix. The pattern is a function of azimuth and elevation. The rows of PAT correspond to the azimuth angles in the vector specified by EL_ANG. The columns correspond to the elevation angles in the vector specified by AZ_ANG.

\section*{AZ_ANG - Azimuth angles}
scalar | 1-by- \(N\) real-valued row vector
Azimuth angles for displaying directivity or response pattern, returned as a scalar or 1-by- N realvalued row vector corresponding to the dimension set in AZ. The columns of PAT correspond to the values in AZ_ANG. Units are in degrees.

\section*{EL_ANG - Elevation angles \\ scalar | 1-by-M real-valued row vector}

Elevation angles for displaying directivity or response, returned as a scalar or 1-by-M real-valued row vector corresponding to the dimension set in EL. The rows of PAT correspond to the values in EL_ANG. Units are in degrees.

\section*{More About}

\section*{Directivity}

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power
\[
D=4 \pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
\]
where \(U_{\mathrm{rad}}(\theta, \varphi)\) is the radiant intensity of a transmitter in the direction \((\theta, \varphi)\) and \(P_{\text {total }}\) is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as dBi . For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

\section*{Azimuth and Elevation Angles}

Define the azimuth and elevation conventions used in the toolbox.
The azimuth angle of a vector is the angle between the \(x\)-axis and its orthogonal projection onto the \(x y\)-plane. The angle is positive when going from the \(x\)-axis toward the \(y\)-axis. Azimuth angles lie between \(-180^{\circ}\) and \(180^{\circ}\) degrees, inclusive. The elevation angle is the angle between the vector and
its orthogonal projection onto the \(x y\)-plane. The angle is positive when going toward the positive \(z\) axis from the \(x y\)-plane. Elevation angles lie between \(-90^{\circ}\) and \(90^{\circ}\) degrees, inclusive.


\footnotetext{
Version History
Introduced in R2021a
}

\section*{patternAzimuth}

Package: phased
Plot array directivity or pattern versus azimuth

\section*{Syntax}
```

patternAzimuth(array,FREQ)
patternAzimuth(array,FREQ,EL)
patternAzimuth(array,FREQ,EL)
patternAzimuth(array, FREQ,EL,Name,Value)
PAT = patternAzimuth(

```

\section*{Description}
patternAzimuth (array, FREQ) plots the 2-D array directivity pattern versus azimuth (in dBi) for the array at zero degrees elevation angle. The argument FREQ specifies the operating frequency.

The integration used when computing array directivity has a minimum sampling grid of 0.1 degrees. If an array pattern has a beamwidth smaller than this, the directivity value will be inaccurate.
patternAzimuth (array, FREQ,EL), in addition, plots the 2-D array directivity pattern versus azimuth (in dBi ) for the array at the elevation angle specified by \(E L\). When \(E L\) is a vector, multiple overlaid plots are created.
patternAzimuth(array, FREQ,EL), in addition, plots the 2-D array directivity pattern versus azimuth (in dBi) for the array at the elevation angle specified by \(E L\). When \(E L\) is a vector, multiple overlaid plots are created.
patternAzimuth(array, FREQ,EL, Name, Value) plots the array pattern with additional options specified by one or more Name, Value pair arguments.

PAT = patternAzimuth( \(\qquad\) ) returns the array pattern. PAT is a matrix whose entries represent the pattern at corresponding sampling points specified by the 'Azimuth ' parameter and the EL input arguments.

\section*{Input Arguments}

\section*{array - Phased array}

Phased Array System Toolbox System object
Phased array, specified as a Phased Array System Toolbox System object.

\section*{FREQ - Frequency for computing directivity and patterns}
positive scalar | 1-by-L real-valued row vector
Frequencies for computing directivity and patterns, specified as a positive scalar or 1-by-L realvalued row vector. Frequency units are in hertz.
- For an antenna, microphone, or sonar hydrophone or projector element, FREQ must lie within the range of values specified by the FrequencyRange or FrequencyVector property of the element.

Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased. CustomAntennaElement and phased. CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

\section*{Example: [1e8 2e6]}

Data Types: double

\section*{EL - Elevation angles}

\section*{1-by-N real-valued row vector}

Elevation angles for computing sensor or array directivities and patterns, specified as a \(1-b y-N\) realvalued row vector. The quantity \(N\) is the number of requested elevation directions. Angle units are in degrees. The elevation angle must lie between \(-90^{\circ}\) and \(90^{\circ}\).

The elevation angle is the angle between the direction vector and the xy plane. When measured toward the \(z\)-axis, this angle is positive.
Example: [0, 10, 20]
Data Types: double

\section*{Name-Value Pair Arguments}

Specify optional pairs of arguments as Namel=Value1, . . . , NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.
Example: CoordinateSystem, 'polar', Type,'directivity'

\section*{Type - Displayed pattern type}
'directivity' (default)|'efield'|'power'|'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type' and one of
- 'directivity ' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power ' - power pattern of the sensor or array defined as the square of the field pattern.
- 'powerdb' - power pattern converted to dB.

Example: 'powerdb'
Data Types: char

\section*{PropagationSpeed - Signal propagation speed}
speed of light (default) | positive scalar
Signal propagation speed, specified as the comma-separated pair consisting of 'PropagationSpeed ' and a positive scalar in meters per second.
Example: 'PropagationSpeed', physconst('LightSpeed')

\section*{Data Types: double}

\section*{Weights - Array weights}

1 (default) | \(N\)-by-1 complex-valued column vector \(\mid N\)-by- \(L\) complex-valued matrix
Array weights, specified as the comma-separated pair consisting of 'Weights' and an N -by-1 complex-valued column vector or \(N\)-by- \(L\) complex-valued matrix. Array weights are applied to the elements of the array to produce array steering, tapering, or both. The dimension \(N\) is the number of elements in the array. The dimension \(L\) is the number of frequencies specified by FREQ.
\begin{tabular}{|l|l|l|}
\hline Weights Dimension & FREQ Dimension & Purpose \\
\hline \begin{tabular}{l}
\(N\)-by-1 complex-valued column \\
vector
\end{tabular} & Scalar or 1-by- \(L\) row vector & \begin{tabular}{l} 
Applies a set of weights for the \\
single frequency or for all \(L\) \\
frequencies.
\end{tabular} \\
\hline\(N\)-by- \(L\) complex-valued matrix & 1-by-L row vector & \begin{tabular}{l} 
Applies each of the \(L\) columns of \\
'Weights ' for the \\
corresponding frequency in \\
FREQ.
\end{tabular} \\
\hline
\end{tabular}

Note Use complex weights to steer the array response toward different directions. You can create weights using the phased. SteeringVector System object or you can compute your own weights. In general, you apply Hermitian conjugation before using weights in any Phased Array System Toolbox function or System object such as phased.Radiator or phased. Collector. However, for the directivity, pattern, patternAzimuth, and patternElevation methods of any array System object use the steering vector without conjugation.

\section*{Example: 'Weights', ones ( \(\mathrm{N}, \mathrm{M}\) )}

Data Types: double
Complex Number Support: Yes

\section*{Azimuth - Azimuth angles}
[-180:180] (default) | 1-by-P real-valued row vector
Azimuth angles, specified as the comma-separated pair consisting of 'Azimuth' and a 1-by-P realvalued row vector. Azimuth angles define where the array pattern is calculated.
Example: 'Azimuth', [-90:2:90]
Data Types: double

\section*{Parent - Handle to axis}
scalar
Handle to the axes along which the array geometry is displayed specified as a scalar.

\section*{Output Arguments}

\section*{PAT - Array directivity or pattern}

L-by- \(N\) real-valued matrix

Array directivity or pattern, returned as an \(L\)-by- \(N\) real-valued matrix. The dimension \(L\) is the number of azimuth values determined by the 'Azimuth' name-value pair argument. The dimension \(N\) is the number of elevation angles, as determined by the EL input argument.

\section*{More About}

\section*{Directivity (dBi)}

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power
\[
D=4 \Pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\mathrm{total}}}
\]
where \(U_{\mathrm{rad}}(\theta, \varphi)\) is the radiant intensity of a transmitter in the direction \((\theta, \varphi)\) and \(P_{\text {total }}\) is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as \(d B i\). For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

\section*{Azimuth and Elevation Angles}

Define the azimuth and elevation conventions used in the toolbox.
The azimuth angle of a vector is the angle between the \(x\)-axis and its orthogonal projection onto the \(x y\)-plane. The angle is positive when going from the \(x\)-axis toward the \(y\)-axis. Azimuth angles lie between \(-180^{\circ}\) and \(180^{\circ}\) degrees, inclusive. The elevation angle is the angle between the vector and its orthogonal projection onto the xy-plane. The angle is positive when going toward the positive \(z\) axis from the \(x y\)-plane. Elevation angles lie between \(-90^{\circ}\) and \(90^{\circ}\) degrees, inclusive.


\section*{Version History}

Introduced in R2021a

\section*{patternElevation}

\author{
Package: phased
}

Plot array directivity or pattern versus elevation

\section*{Syntax}
patternElevation(array,FREQ)
patternElevation(array, FREQ,AZ)
patternElevation(array, FREQ, AZ, Name, Value)
PAT = patternElevation( \(\qquad\)

\section*{Description}
patternElevation(array, FREQ) plots the 2-D array directivity pattern versus elevation (in dBi) for the array at zero degrees azimuth angle. When \(A Z\) is a vector, multiple overlaid plots are created. The argument FREQ specifies the operating frequency.
patternElevation(array, FREQ,AZ), in addition, plots the 2-D element directivity pattern versus elevation (in dBi) at the azimuth angle specified by \(A Z\). When \(A Z\) is a vector, multiple overlaid plots are created.
patternElevation(array, FREQ, AZ, Name, Value) plots the array pattern with additional options specified by one or more Name, Value pair arguments.

PAT = patternElevation ( __ ) returns the array pattern. PAT is a matrix whose entries represent the pattern at corresponding sampling points specified by the 'Elevation' parameter and the AZ input argument.

\section*{Input Arguments}

\section*{array - phased array}

System object
Phased array, specified as a System object.
Example: array = phased.UCA;

\section*{FREQ - Frequency for computing directivity and pattern}
positive scalar
Frequency for computing directivity and pattern, specified as a positive scalar. Frequency units are in hertz.
- For an antenna or microphone element, FREQ must lie within the range of values specified by the FrequencyRange or the FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased.CustomAntennaElement and phased.CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.

Example: 1e8
Data Types: double

\section*{AZ - Azimuth angles for computing directivity and pattern}

1-by- \(N\) real-valued row vector
Azimuth angles for computing sensor or array directivities and patterns, specified as a 1-by- \(N\) realvalued row vector where \(N\) is the number of desired azimuth directions. Angle units are in degrees. The azimuth angle must lie between \(-180^{\circ}\) and \(180^{\circ}\).

The azimuth angle is the angle between the \(x\)-axis and the projection of the direction vector onto the xy plane. This angle is positive when measured from the \(x\)-axis toward the \(y\)-axis.
Example: [0, 10, 20]
Data Types: double

\section*{Name-Value Pair Arguments}

Specify optional pairs of arguments as Namel=Value1, ... , NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.
Example: CoordinateSystem, 'polar', Type,'directivity'

\section*{Type - Displayed pattern type}
'directivity' (default) |'efield'|'power'|'powerdb'
Displayed pattern type, specified as the comma-separated pair consisting of 'Type' and one of
- 'directivity' - directivity pattern measured in dBi.
- 'efield' - field pattern of the sensor or array. For acoustic sensors, the displayed pattern is for the scalar sound field.
- 'power' - power pattern of the sensor or array defined as the square of the field pattern.
- ' powerdb' - power pattern converted to dB .

Example: ' powerdb'
Data Types: char
PropagationSpeed - Signal propagation speed
speed of light (default) | positive scalar
Signal propagation speed, specified as the comma-separated pair consisting of
' PropagationSpeed ' and a positive scalar in meters per second.
Example: 'PropagationSpeed', physconst('LightSpeed')
Data Types: double

\section*{Weights - Array weights}

M-by-1 complex-valued column vector

Array weights, specified as the comma-separated pair consisting of 'Weights' and an M-by-1 complex-valued column vector. Array weights are applied to the elements of the array to produce array steering, tapering, or both. The dimension \(M\) is the number of elements in the array.

Note Use complex weights to steer the array response toward different directions. You can create weights using the phased. SteeringVector System object or you can compute your own weights. In general, you apply Hermitian conjugation before using weights in any Phased Array System Toolbox function or System object such as phased. Radiator or phased. Collector. However, for the directivity, pattern, patternAzimuth, and patternElevation methods of any array System object use the steering vector without conjugation.

\section*{Example: 'Weights', ones(10,1)}

Data Types: double
Complex Number Support: Yes

\section*{Elevation - Elevation angles}
[-90:90] (default) | 1-by-P real-valued row vector
Elevation angles, specified as the comma-separated pair consisting of 'Elevation' and a 1-by-P real-valued row vector. Elevation angles define where the array pattern is calculated.
Example: 'Elevation', [-90:2:90]
Data Types: double

\section*{Parent - Handle to axis}
scalar
Handle to the axes along which the array geometry is displayed specified as a scalar.

\section*{Output Arguments}

\section*{PAT - Array directivity or pattern}
\(L\)-by- \(N\) real-valued matrix
Array directivity or pattern, returned as an \(L\)-by- \(N\) real-valued matrix. The dimension \(L\) is the number of elevation angles determined by the 'Elevation' name-value pair argument. The dimension \(N\) is the number of azimuth angles determined by the \(A Z\) argument.

\section*{More About}

\section*{Directivity}

Directivity describes the directionality of the radiation pattern of a sensor element or array of sensor elements.

Higher directivity is desired when you want to transmit more radiation in a specific direction. Directivity is the ratio of the transmitted radiant intensity in a specified direction to the radiant intensity transmitted by an isotropic radiator with the same total transmitted power
\[
D=4 \pi \frac{U_{\mathrm{rad}}(\theta, \varphi)}{P_{\text {total }}}
\]
where \(U_{\mathrm{rad}}(\theta, \varphi)\) is the radiant intensity of a transmitter in the direction \((\theta, \varphi)\) and \(P_{\text {total }}\) is the total power transmitted by an isotropic radiator. For a receiving element or array, directivity measures the sensitivity toward radiation arriving from a specific direction. The principle of reciprocity shows that the directivity of an element or array used for reception equals the directivity of the same element or array used for transmission. When converted to decibels, the directivity is denoted as \(d B i\). For information on directivity, read the notes on "Element Directivity" and "Array Directivity".

\section*{Azimuth and Elevation Angles}

Define the azimuth and elevation conventions used in the toolbox.
The azimuth angle of a vector is the angle between the \(x\)-axis and its orthogonal projection onto the \(x y\)-plane. The angle is positive when going from the \(x\)-axis toward the \(y\)-axis. Azimuth angles lie between \(-180^{\circ}\) and \(180^{\circ}\) degrees, inclusive. The elevation angle is the angle between the vector and its orthogonal projection onto the \(x y\)-plane. The angle is positive when going toward the positive \(z\) axis from the \(x y\)-plane. Elevation angles lie between \(-90^{\circ}\) and \(90^{\circ}\) degrees, inclusive.


\section*{Version History}

Introduced in R2021a

\section*{perturbations}

Perturbations defined on array

\section*{Syntax}
```

perts = perturbations(array)
perts = perturbations(array,prop)
perts = perturbations(array,prop,'None')
perts = perturbations(array,prop,'Normal',mean,sigma)
perts = perturbations(array,prop,'Uniform',minval,maxval)
perts = perturbations(array,prop,'RandomFail',failprob)

```

\section*{Description}
perts \(=\) perturbations(array) returns a table of all allowed perturbations perts defined for the array. This table contains a list of all properties that can be perturbed, the probability type of applied perturbation, and the parameters of the probability type.
perts = perturbations(array, prop) lets you view the current perturbation defined for the array property prop.
perts \(=\) perturbations(array, prop, 'None') specifies that the property prop is not perturbed.
perts = perturbations(array,prop,'Normal', mean,sigma) specifies that the perturbation is drawn from a normal probability distribution defined by its mean and standard deviation sigma. To use this syntax, set prop to 'ElementPositions', 'TaperMagnitude', or 'TaperPhase'.
perts = perturbations(array, prop,'Uniform', minval, maxval) specifies that the perturbation is drawn from a uniform probability distribution with a range defined by the interval [minval,maxval]. To use this syntax, set prop to 'ElementPositions', 'TaperMagnitude', or 'TaperPhase'.
perts = perturbations(array, prop,'RandomFail',failprob) specifies that the perturbation is a mask indicating whether an element is functioning based on the element fail property failprob. To use this syntax, set prop to 'ElementFailure'.

\section*{Examples}

\section*{Perturbations of Uniform Rectangular Array}

Create an 8 -by- 3 uniform rectangular array (URA). The array operates at 300 MHz and its elements are spaced one-half wavelength apart.
```

freq = 300.0e6;
lambda = physconst('Lightspeed')/freq;
d = lambda/2;
array = phased.URA(8,3,ElementSpacing=[d,d]);

```

Initially, there are no perturbations to the array.
```

perts = perturbations(array)
perts=4\times3 table
Property Type Value
{'ElementPosition'}
{'TaperMagnitude'
{'TaperPhase'
{'ElementFailure' }

| \{'None' $\}$ | $\{[\mathrm{NaN}]\}$ | $\{[\mathrm{NaN}]\}$ |
| :--- | :--- | :--- |
| \{'None' $\}$ | $\{[\mathrm{NaN}]\}$ | $\{[\mathrm{NaN}]\}$ |
| \{'None' $\}$ | $\{[\mathrm{NaN}]\}$ | $\{[\mathrm{NaN}]\}$ |
| $\{$ 'None' $\}$ | $\{[\mathrm{NaN}]\}$ | $\{[\mathrm{NaN}]\}$ |

```

Randomly perturb the element positions according to a normal distribution. Use a position variance of 16 th of a wavelength.
```

perts = perturbations(array,'ElementPosition','Normal',0,lambda/16)
perts=4\times3 table
Property
{'ElementPosition'} {'Normal'}
{'TaperMagnitude' } {'None' } {[NaN]} {[ NaN]}
{'TaperPhase' } {'None' } {[NaN]}
{'ElementFailure' } {'None' } {[NaN]} {[ NaN]}

```

Then perturb the magnitude of the element weights according to a normal distribution with a mean value of 0.1 and a variance of 0.02 .
```

perts = perturbations(array,'TaperMagnitude','Normal',0.1,0.02)
perts=4\times3 table
Property
{'ElementPosition'}
{'TaperMagnitude' }
{'TaperPhase' }
{'ElementFailure' }
Type
Value
{'Normal'}

| $0]\}$ | \{[0.062 |
| :---: | :---: |
| \{[0.1000]\} | \{[0.0200] |
| NaN]\} | \{[ NaN$]\}$ |
| NaN]\} | \{[ NaN$]$ |

```

Perturb the phase of the element weights according to a uniform distribution between -40 and 40 degrees.
```

perts = perturbations(array,'TaperPhase','Uniform',-40,40)
perts=4\times3 table
Property
{'ElementPosition'}
{'TaperMagnitude' } {'Normal' } {[0.1000]} {[0.0200]}
{'TaperPhase' } {'Uniform'} {[[ -40]}

```

Set a \(20 \%\) percent failure rate for the elements.
```

perts = perturbations(array,'ElementFailure','RandomFail',0.2)
perts=4\times3 table
Property
{'ElementPosition'}
{'TaperMagnitude' }
{'TaperPhase' }
{'ElementFailure' }

```

Type
-
\begin{tabular}{|c|c|c|}
\hline Normal' & 0] \} & \{[0.0625]\} \\
\hline \{'Normal' \} & \{[0.1000]\} & \{[0.0200]\} \\
\hline \{'Uniform' & \{[ -40]\} & \{[ 40]\} \\
\hline \{'RandomFail'\} & \{[0.2000]\} & \{[ NaN\(]\) \\
\hline
\end{tabular}

\section*{Input Arguments}

\section*{array - Phased array}

Phased Array System Toolbox System object
Phased array, specified as a Phased Array System Toolbox System object.
prop - Perturbed array property
'ElementPosition'|'TaperMagnitude'| 'TaperPhased'|'ElementFailure'
Perturbed property of array, specified as 'ElementPosition', 'TaperMagnitude', 'TaperPhased', or 'ElementFailure'.
Example: 'TaperPhased'
Data Types: string
mean - Mean value of normal distribution
scalar
Mean value of normal distribution, specified as a scalar. Units depend on the property prop.
\begin{tabular}{|l|l|}
\hline 'ElementPosition' & meters \\
\hline 'TaperMagnitude' & dimensionless \\
\hline 'TaperPhased ' & radians \\
\hline
\end{tabular}

Example: 12

\section*{Dependencies}

To enable this argument, set the perturbed array property prop to 'ElementPosition', 'TaperMagnitude', or 'TaperPhased' and the perturbation type to 'Normal'.

Data Types: double

\section*{sigma - Standard deviation of normal distribution}
positive scalar
Standard deviation of normal distribution, specified as a positive scalar. Units depend on the property prop.
\begin{tabular}{|l|l}
\hline ElementPosition' & meters \\
\hline
\end{tabular}
\begin{tabular}{|l|l|}
\hline 'TaperMagnitude' & dimensionless \\
\hline 'TaperPhased ' & radians \\
\hline
\end{tabular}

Example: 1.0

\section*{Dependencies}

To enable this argument, set the perturbed array property prop to 'ElementPosition ',
'TaperMagnitude', or 'TaperPhased' and the perturbation type to 'Normal'.
Data Types: double

\section*{minval - Minimum value of range of uniform probability distribution \\ scalar}

Minimum value of range of uniform probability distribution, specified as a scalar. When applied to the 'TaperPhase' property. the difference between minval and maxval should be less than or equal to \(2 \pi\). Units depend on the property prop.
\begin{tabular}{|l|l|}
\hline 'ElementPosition' & meters \\
\hline 'TaperMagnitude' & dimensionless \\
\hline 'TaperPhased ' & radians \\
\hline
\end{tabular}

\section*{Example: 0}

\section*{Dependencies}

To enable this argument, set the perturbed array property prop to 'ElementPosition',
'TaperMagnitude', or 'TaperPhased' and the perturbation type to 'Uniform'.
Data Types: double
maxval - Maximum value of range of uniform probability distribution
scalar
Maximum value of range of uniform probability distribution
Example: 1

\section*{Dependencies}

Maximum value of range of uniform probability distribution, specified as a scalar. When applied to the 'TaperPhase' property. the difference between minval and maxval should be less than or equal to \(2 \pi\). Units depend on the property prop.
\begin{tabular}{|l|l|}
\hline 'ElementPosition' & meters \\
\hline 'TaperMagnitude' & dimensionless \\
\hline 'TaperPhased' & radians \\
\hline
\end{tabular}

Data Types: double

\section*{failprob - Probability of failure}
positive scalar

Probability of failure, specified as a non-negative scalar greater than or equal to zero and less than one. Zero means that the elements will never fail. Otherwise, there is a some probability of failure.

Example: 0.01

\section*{Dependencies}

To enable this argument, set the array property prop to 'ElementFailure' and the perturbation type to 'RandomFail'.
Data Types: double

\section*{Output Arguments}

\section*{perts - List of possible perturbations}

MATLAB table
List of possible perturbations, returned as a MATLAB table. See "Perturbed properties and perturbation types" on page 1-2209 for a list of perturbations properties and types.
Data Types: table

\section*{More About}

\section*{Perturbed properties and perturbation types}

You can perturb the array by selecting one of the properties to be perturbed and then applying the type of perturbation. Each type of perturbation has specific arguments.
\begin{tabular}{|c|c|c|}
\hline Property & Perturbation Type & Arguments \\
\hline \multirow[t]{3}{*}{'ElementPosition'} & 'None' & - \\
\hline & 'Normal' & mean, sigma \\
\hline & 'Uniform' & minval, maxval \\
\hline \multirow[t]{3}{*}{'TaperMagnitude '} & 'None' & - \\
\hline & 'Normal' & mean, sigma \\
\hline & 'Uniform' & minval, maxval \\
\hline \multirow[t]{3}{*}{'TaperPhase'} & 'None' & - \\
\hline & 'Normal' & mean, sigma \\
\hline & 'Uniform' & minval, maxval \\
\hline \multirow[t]{2}{*}{'ElementFailure'} & 'None' & - \\
\hline & 'RandomFail' & probfail \\
\hline
\end{tabular}

\section*{Version History}

Introduced in R2022a

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® \({ }^{\circledR}\) Coder \(^{\mathrm{TM}}\).

\section*{See Also}
phased.ConformalArray|perturbedPattern|perturbedArray

\section*{perturbedArray}

Apply perturbations to phased array

\section*{Syntax}
arrayp = perturbedArray(array)
[arrayp,offsets] = perturbedArray(array)

\section*{Description}
arrayp = perturbedArray(array) creates a perturbed array arrayp from an original array. Use the perturbations function to apply one or perturbations to the array. Then create the perturbed array arrayp using the perturbedArray object function. The array perturbation are described in the perturbation table created by the perturbations object function. You can call this function many times to create a new perturbed array.
[arrayp,offsets] = perturbedArray(array) also returns the perturbation offsets used to create the perturbed arrayarrayp.

\section*{Examples}

\section*{Show Perturbed Uniform Linear Array}

Create an 11-element uniform linear array (ULA). The array operates at 300 MHz and its elements are spaced one-half wavelength apart. Perturb the element positions by \(1 / 20\) th of a wavelength. A second perturbation sets an element failure rate of \(10 \%\).
```

freq = 300.0e6;
lambda = physconst('LightSpeed')/freq;
d = lambda/2;
array = phased.ULA(11,ElementSpacing=d/2);

```

Display the appled perturbations.
```

rng(2001)
perturbations(array,'ElementPosition','Normal',0,lambda/20);
perturbations(array,'ElementFailure','RandomFail',0.1)
ans=4\times3 table
Property Type Value
{'ElementPosition'}
{'TaperMagnitude' }
{'TaperPhase' }
{'ElementFailure' }

| \{'Normal' | \{[ 0] | \{[0.0500] $\}$ |
| :---: | :---: | :---: |
| \{'None' \} | \{[ NaN]\} | \{[ NaN$]\}$ |
| \{'None' \} | \{[ NaN$]\}$ | \{[ NaN]\} |
| \{'RandomFail'\} | \{[0.1000]\} | \{[ NaN]\} |

```

Create the perturbed array. Show that the array is a conformal array.
arrayp = perturbedArray(array)
```

arrayp =
phased.ConformalArray with properties:
Element: [1x1 phased.IsotropicAntennaElement]
ElementPosition: [3x11 double]
ElementNormal: [2x11 double]
Taper: [11x1 double]

```

Find the perturbations themselves using the offsets output.
```

[arrayp,offsets] = perturbedArray(array);

```

Display the element position perturbations.
```

offsets(1)
ans = struct with fields:
Property: 'ElementPosition'
Offset: [3x11 double]
PerturbedValue: [3x11 double]

```
offsets(1).Offset
ans \(=3 \times 11\)
\begin{tabular}{rrrrrrrrr}
-0.0372 & 0.0107 & 0.0092 & -0.0774 & 0.0332 & -0.1940 & -0.0382 & 0.0454 & 0.0774 \\
-0.0177 & -0.0745 & 0.1042 & 0.0210 & -0.0359 & -0.0391 & 0.0281 & -0.0229 & 0.0281 \\
0.0048 & 0.0758 & 0.0528 & -0.0372 & -0.0066 & 0.0030 & 0.0323 & -0.1047 & -0.0887 \\
\hline
\end{tabular}
offsets(1).PerturbedValue
ans \(=3 \times 11\)
\begin{tabular}{rrrrrrrrr}
-0.0372 & 0.0107 & 0.0092 & -0.0774 & 0.0332 & -0.1940 & -0.0382 & 0.0454 & 0.0774 \\
-1.2668 & -1.0738 & -0.6452 & -0.4786 & -0.2858 & -0.0391 & 0.2780 & 0.4768 & 0.7776 \\
0.0048 & 0.0758 & 0.0528 & -0.0372 & -0.0066 & 0.0030 & 0.0323 & -0.1047 & -0.0887 \\
\hline .0 .0
\end{tabular}

Display the failed elements.
offsets(2)
ans = struct with fields:
Property: 'ElementFailure' Offset: [11x1 double]
PerturbedValue: [11×1 double]
offsets(2).Offset
ans \(=11 \times 1\)
1
1
1
1
1
```

        1
        1
        0
        1
        1
    offsets(2).PerturbedValue
ans = 11\times1

## Input Arguments

## array - Phased array

Phased Array System Toolbox System object
Phased array, specified as a Phased Array System Toolbox System object.

## Output Arguments

## arrayp - Perturbed phased array

phased.ConformalArray | phased. HeterogeneousConformalArray
Phased array, returned as a phased. ConformalArray or a phased. HeterogeneousConformalArray System object. arrayp is a heterogeneous conformal array if the input unperturbed array is a any heterogeneous array.

## offsets - Offsets used to define the perturbed array

array of structs
Perturbation offsets used to create the perturbed array, returned as an array of structs. Each struct describes one of the applied perturbations. The fields of each struct are:

| Property | Perturbed property of array |
| :--- | :--- |
| Offset | Numeric array containing the offset or change in <br> the property values. |
| PerturbedValue | Numeric array containing the newly perturbed <br> property values. |

Data Types: struct

# Version History 

Introduced in R2022a

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

phased.ConformalArray | phased.HeterogeneousConformalArray|perturbations | perturbedPattern

## perturbedPattern

Display pattern of perturbed array

## Syntax

```
pmc = perturbedPattern(array,freq)
pmc = perturbedPattern(array,freq,az)
pmc = perturbedPattern(array,freq,az,el)
pmc = perturbedPattern(
```

$\qquad$

``` , Name=Value)
[pmc,pnm,mpmc,varpmc] = perturbedPattern(array,
``` \(\qquad\)
``` )
perturbedPattern(array,
``` \(\qquad\)
``` )
```


## Description

pmc = perturbedPattern(array,freq) returns a set of perturbed azimuth array patterns pmc for an array generated from 100 Monte-Carlo runs. freq specifies the operating frequency at which the pattern is computed.
pmc = perturbedPattern(array,freq,az) also specifies the azimuth angles az used for computing the perturbed patterns.
pmc $=$ perturbedPattern(array,freq,az,el) also specifies the elevation angles el used for computing the perturbed patterns.
pmc $=$ perturbedPattern (__ , Name=Value) also sets the specified parameter Name to the specified Value. You can specify additional name-value pair arguments in any order as (Name1=Value1,...,NameN=ValueN). For example, NumTrials = 10000.
[pmc,pnm,mpmc,varpmc] = perturbedPattern(array, $\qquad$ ) also returns the nominal array response pattern pnm, the mean array response pattern mpmc, and the variance of the array response pattern varpmc.
perturbedPattern(array, $\qquad$ ) plots all perturbed patterns for all Monte-Carlo runs and overlays them with both the nominal array response pattern and the mean perturbed array response pattern.

## Examples

## Compute Power Pattern of Perturbed ULA for All Azimuth Angles

Create an 11 -element Uniform Linear Array. The array operates at 300 MHz and its elements are spaced one-half wavelength apart. Perturb the element positions by $1 / 20$ th of a wavelength. Use the default value of 100 Monte Carlo runs. Compute the pattern for the first simulation at all azimuth angles. Set the random number generator seed for reproducibility.

```
freq = 300.0e6;
lambda = physconst('LightSpeed')/freq;
d = lambda/2;
array = phased.ULA(11,ElementSpacing=d/2);
```

```
rng(10007)
perturbations(array,'ElementPosition','Normal',0,lambda/20);
perturbations(array,'TaperMagnitude','Normal',0,0.1);
pmc = perturbedPattern(array,freq);
```

Plot the array pattern vs azimuth angle.

```
plot(mag2db(abs(pmc(:,1))))
ylabel('Array Response (dB)')
xlabel('Azimith Angle (deg)')
title('Array Response')
grid on
xticks([0:30:180])
```



## Compute Power Pattern of Perturbed ULA for Span of Azimuth Angles

Create an 11-element uniform linear array (ULA). The array operates at 300 MHz and its elements are spaced one-half wavelength apart. Perturb the element positions by $1 / 20$ th of a wavelength. Use the default value of 100 Monte Carlo runs. Compute the pattern for the first simulation at azimuth angles from -45 to +45 degrees. Set the seed of the random number generator for reproducibilty.
freq $=300.0 \mathrm{e} 6$;
lambda = physconst('LightSpeed')/freq;
d = lambda/2;
array $=$ phased.ULA(11,ElementSpacing = d/2);

```
rng(230081)
perturbations(array,'ElementPosition','Normal',0,lambda/20);
perturbations(array,'TaperMagnitude','Normal',0,0.1);
```

Display the array response pattern for the first Monte Carlo run.

```
azang = -45:45;
pmc = perturbedPattern(array,freq,azang);
plot(azang,mag2db(abs(pmc(:,1))))
title('Response Pattern')
xlabel('Azimuth Angle (deg)')
ylabel('Array Response (dB)')
xticks([-45:15:45])
grid on
```



## Compute Power Pattern for Steered Array

Create an 11 -element Uniform Linear Array. The array operates at 300 MHz and its elements are spaced one-half wavelength apart. Perturb the element positions by $1 / 20$ th of a wavelength. Run 200 Monte Carlo simulations and steer the array 30 degrees in azimuth.

```
freq = 300e6;
```

lambda = physconst('Lightspeed')/freq;
d = lambda/2;
array $=$ phased.ULA(11,ElementSpacing=d/2);
pos = getElementPosition(array);
sv = steervec(pos,30);
perturbations(array,'ElementPosition', 'Normal', 0, lambda/20);
perturbations(array,'TaperMagnitude','Normal',0,0.1);
azang = -90:90;
elang = 0;
perturbedPattern(array,freq, azang, elang, Weights=sv,NumTrials=200);


## Input Arguments

## array - Phased array

Phased Array System Toolbox System object
Phased array, specified as a Phased Array System Toolbox System object.

## freq - Frequency used to compute array patterns

positive scalar
Frequency used to compute array patterns, specified as a positive scalar. Units are in Hz.
Data Types: double
az - Azimuth angles
scalar | length-M real-valued vector

Azimuth angles for computing power pattern, specified as a scalar or length- $M$ real-valued vector. Either az or el, must be a scalar. Units are in degrees.

Data Types: double

## el - Elevation angles

scalar | length-M real-valued vector
Elevation angles for computing power pattern, specified as a scalar or length- $N$ real-valued vector. Either az or el must be a scalar. Units are in degrees.

Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Namel=Value1, ... , NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.
Example: pmc = perturbedPatter(array,NumTrials = 1000)

## NumTrials - Number of Monte-Carlo trials

positive integer
Number of Monte-Carlo trials, specified as a positive integer.
Data Types: double

## Parent - Axes on which the pattern is displayed

axes handle
Axes on which the pattern is displayed, specified as an axis handle..
Data Types: double

## PropagationSpeed - Signal propagation speed

physconst('lightSpeed') (default) | positive scalar
Signal propagation speed, specified as a positive scalar. The default value is physconst('lightSpeed'). Units are in m/s.

Example: 300e6
Data Types: double
Weights - Element weights
length- $P$ complex-valued vector
Element weights, specified as a length- $P$ complex-valued vector. $P$ is the number of elements belonging to the array specified in the array argument.
Example: ones (11,1)
Data Types: double
Complex Number Support: Yes

## Output Arguments

## pmc - Perturbed array pattern

length- $Q$ vector
Perturbed array pattern, returned as an $M$-by- $Q$ or $N$-by- $Q$ complex-valued matrix. $M$ is the number of angles in the az argument. $N$ is the number of angles in the el argument. Either az or el must be a scalar. $Q$ is the number of Monte-Carlo trials. Each trial generates a different pattern. Units are in degrees.
Data Types: double
Complex Number Support: Yes
pnm - Nominal array pattern
length- $M$ real-valued vector | length- $N$ real-valued vector
Nominal array pattern, returned as an $M$ complex-valued vector or as an $N$-by- $Q$ complex-valued vector. $M$ is the number of angles in the az argument. $N$ is the number of angles in the al argument. Either az or el must be a scalar. Units are in degrees.

Data Types: double

## mpmc - Mean of array response pattern

length- $N$ real-valued vector | length- $N$ real-valued vector
Mean of array response pattern, returned as a length- $M$ real-valued vector or as an length- $N$ realvalued vector. $M$ is the number of angles in the az argument. $N$ is the number of angles in the al argument. Units are in degrees.
Data Types: double
varpmc - Variance of array response pattern
length- $N$ real-valued vector | length- $N$ real-valued vector
Variance of array response pattern, returned as a length- $M$ real-valued vector or as an length- $N$ realvalued vector. $M$ is the number of angles in the az argument. $N$ is the number of angles in the al argument. Units are in degrees.

## Version History

Introduced in R2022a

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder ${ }^{\mathrm{TM}}$.

## See Also

phased.ConformalArray | phased. HeterogeneousConformalArray | perturbedArray | perturbations

## plotGratingLobeDiagram

Plot grating lobe diagram of array

## Syntax

```
plotGratingLobeDiagram(array,freq)
plotGratingLobeDiagram(array,freq,c)
plotGratingLobeDiagram(array,freq,angle,c)
plotGratingLobeDiagram(array,freq,angle, c,f0)
hndl = plotGratingLobeDiagram(
```

$\qquad$

## Description

plotGratingLobeDiagram (array, freq) plots the grating lobe diagram of an array in the $u-v$ coordinate system. The System object array specifies the array. The argument freq specifies the signal frequency. The array, by default, is steered to $0^{\circ}$ azimuth and $0^{\circ}$ elevation.

A grating lobe diagram displays the positions of the peaks of the narrowband array pattern. The array pattern depends only upon the geometry of the array and not upon the types of elements which make up the array. Visible and non-visible grating lobes are displayed as open circles. Only grating lobe peaks near the location of the mainlobe are shown. The mainlobe itself is displayed as a filled circle.
plotGratingLobeDiagram(array, freq, c), in addition, specifies the array steering angle, angle.
plotGratingLobeDiagram(array,freq, angle, c), in addition, specifies the propagation speed by c .
plotGratingLobeDiagram(array,freq, angle, $c, f 0$ ), in addition, specifies an array phaseshifter frequency, f0, that differs from the signal frequency, freq. This argument is useful when the signal no longer satisfies the narrowband assumption and allows you to estimate the size of beam squint.
hndl = plotGratingLobeDiagram( $\qquad$ ) returns the handle hndl to the plot for any of the input syntaxes.

## Examples

## Create Grating Lobe Diagram for ULA

Plot the grating lobe diagram for a 4 -element uniform linear array having element spacing less than one-half wavelength. Grating lobes are plotted in u-v coordinates.

Assume the operating frequency of the array is 3 GHz and the spacing between elements is 0.45 of the wavelength. All elements are isotropic antenna elements. Steer the array in the direction 45 degrees in azimuth and 0 degrees in elevation.

```
c = physconst('LightSpeed');
f = 3e9;
```

```
lambda = c/f;
sIso = phased.IsotropicAntennaElement;
sULA = phased.ULA('Element',sIso,'NumElements',4,...
    'ElementSpacing',0.45*lambda);
plotGratingLobeDiagram(sULA,f,[45;0],c);
```


## Grating Lobe Diagram in U Space



The main lobe of the array is indicated by a filled black circle. The grating lobes in the visible and nonvisible regions are indicated by empty black circles. The visible region is defined by the direction cosine limits between $[-1,1]$ and is marked by the two vertical black lines. Because the array spacing is less than one-half wavelength, there are no grating lobes in the visible region of space. There are an infinite number of grating lobes in the nonvisible regions, but only those in the range [-3,3] are shown.

The grating-lobe free region, shown in green, is the range of directions of the main lobe for which there are no grating lobes in the visible region. In this case, it coincides with the visible region.

The white area of the diagram indicates a region where no grating lobes are possible.

## Input Arguments

array - Antenna, microphone, or transducer phased array
phased array
Antenna, microphone, or transducer phased array, specified as a System object.

## freq - Frequency for computing directivity and patterns

positive scalar | 1-by-L real-valued row vector
Frequencies for computing directivity and patterns, specified as a positive scalar or 1-by-L realvalued row vector. Frequency units are in hertz.

- For an antenna, microphone, or sonar hydrophone or projector element, FREQ must lie within the range of values specified by the FrequencyRange or FrequencyVector property of the element. Otherwise, the element produces no response and the directivity is returned as -Inf. Most elements use the FrequencyRange property except for phased. CustomAntennaElement and phased. CustomMicrophoneElement, which use the FrequencyVector property.
- For an array of elements, FREQ must lie within the frequency range of the elements that make up the array. Otherwise, the array produces no response and the directivity is returned as -Inf.


## Example: [1e8 2e6]

Data Types: double

## angle - array steering angle

[0;0] (default) | 2-by-1 real-valued vector | scalar
Array steering angle, specified as either a 2 -by-1 vector or a scalar. If angle is a vector, it takes the form [azimuth; elevation]. The azimuth angle must lie in the range [ $-180^{\circ}, 180^{\circ}$ ]. The elevation angle must lie in the range $\left[-90^{\circ}, 90^{\circ}\right.$ ]. All angle values are specified in degrees. If the argument angle is a scalar, it specifies only the azimuth angle where the corresponding elevation angle is $0^{\circ}$.
Data Types: double
c - signal propagation speed
speed of light (default) | positive scalar
Signal propagation speed, specified as a positive scalar. Units are m/s.
Data Types: double

## f0 - Phase-shifter frequency of array <br> freq (default) | scalar

Phase-shifter frequency of the array, specified as a scalar. When this argument is omitted, the phaseshifter frequency is assumed to be the signal frequency, freq. Units are Hz

Data Types: double

## Output Arguments

## hndl - plot handle

handle
Plot handle.

## Algorithms

## Grating Lobes

Spatial undersampling of a wavefield by an array gives rise to visible grating lobes. If you think of the wavenumber, $k$, as analogous to angular frequency, then you must sample the signal at spatial intervals smaller than $\Pi / k_{\max }$ ( or $\lambda_{\text {min }} / 2$ ) in order to remove aliasing. The appearance of visible grating lobes is also known as spatial aliasing. The variable $k_{\max }$ is the largest wavenumber value present in the signal.

The directions of maximum spatial response of a ULA are determined by the peaks of the array's array pattern (alternatively called the beam pattern or array factor). Peaks other than the mainlobe peak are called grating lobes. For a ULA, the array pattern depends only on the wavenumber component of the wavefield along the array axis (the $y$-direction for the phased. ULA System object). The wavenumber component is related to the look-direction of an arriving wavefield by $k_{y}=-2 \pi \sin \varphi /$ $\lambda$. The angle $\varphi$ is the broadside angle-the angle that the look-direction makes with a plane perpendicular to the array. The look-direction points away from the array to the wavefield source.

The array pattern possesses an infinite number of periodically-spaced peaks that are equal in strength to the mainlobe peak. If you steer the array to the $\varphi_{0}$ direction, the array pattern for a ULA has its mainlobe peak at the wavenumber value of $k_{y 0}=-2 \pi \sin \varphi_{0} / \lambda$. The array pattern has strong grating lobe peaks at $k_{y m}=k_{y 0}+2 \pi \mathrm{~m} / d$, for any integer value $m$. Expressed in terms of direction cosines, the grating lobes occur at $u_{m}=u_{0}+m \lambda / d$, where $u_{0}=\sin \varphi_{0}$. The direction cosine, $u_{0}$, is the cosine of the angle that the look-direction makes with the $y$-axis and is equal to $\sin \varphi_{0}$ when expressed in terms of the look-direction.

In order to correspond to a physical look-direction, $u_{m}$ must satisfy, $-1 \leq u_{m} \leq 1$. You can compute a physical look-direction angle $\varphi_{m}$ from $\sin \varphi_{m}=u_{m}$ as long as $-1 \leq u_{m} \leq 1$. The spacing of grating lobes depends upon $\lambda / d$. When $\lambda / d$ is small enough, multiple grating lobe peaks can correspond to physical look-directions.

The presence or absence of visible grating lobes for the ULA is summarized in this table.

| Element Spacing | Grating Lobes |
| :--- | :--- |
| $\lambda / d \geq 2$ | No visible grating lobes for any mainlobe <br> direction. |
| $1 \leq \lambda / d<2$ | Visible grating lobes can exist for some range of <br> mainlobe directions. |
| $\lambda / d<1$ | Visible grating lobes exist for every mainlobe <br> direction. |

## Version History

Introduced in R2022b

## References

[1] Van Trees, H.L. Optimum Array Processing. New York: Wiley-Interscience, 2002.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

## See Also

uv2azel|azel2uv

## viewArray

View array geometry

## Syntax

```
viewArray(array)
viewArray(array,Name,Value)
hndl = viewArray(
```

$\qquad$

``` -)
```


## Description

viewArray (array) displays the geometry of the array.
viewArray (array, Name, Value) displays the geometry of the array, with additional options specified by one or more Name, Value pair arguments.
hndl = viewArray( __ ) ) returns the handle of the array elements in the figure window. All input arguments described for the previous syntaxes also apply here.

## Examples

## Geometry of NR Rectangular Panel Array

Construct a 5 G antenna array where the grid is 2 -by- 2 and each panel is 4 -by- 4 array. Each antenna element consists of two short-dipole antennas with different dipole axis directions. The antenna elements are spaced $1 / 2$ wavelength apart and the panels are spaced 3 wavelengths apart. The array operates at 6 GHz .

```
c = physconst('LightSpeed');
fc = 6.0e9;
lambda = c/fc;
antennal = phased.ShortDipoleAntennaElement('AxisDirection','Z');
antenna2 = phased.ShortDipoleAntennaElement('AxisDirection','X');
array = phased.NRRectangularPanelArray('ElementSet', ...
    {antenna1, antenna2},'Size',[4, 4, 2, 2], ...
    'Spacing',[0.5*lambda,0.5*lambda,3*lambda,3*lambda]);
viewArray(array,'ShowNormals',true, ...
    'ShowLocalCoordinates',true,'Orientation',[60;100;45], ...
    'ShowAnnotation',true)
```


$\AA_{z}^{y}$
Array Span:
$X$ axis $=0.000 \mathrm{~mm}$
Y axis $=224.844 \mathrm{~mm}$
$Z$ axis $=224.844 \mathrm{~mm}$

## Input Arguments

## array - Phased array

System object
Phased array, specified as a System object.

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.
Example: 'ShowNormals',true,'ShowIndex','All', 'ShowTaper', true

## Parent - Handle to axes

real-valued scalar
Handle to the axes along which the array geometry is displayed.

## ShowNormals - Option to show normal vectors

false (default) | true

Option to show normal directions, specified as the comma-separated pair consisting of 'ShowNormals' and a Boolean value.

- true - show the normal directions of all elements in the array
- false - plot the elements without showing normal directions

Example: false
Data Types: logical

## ShowLocalCoordinates - Show local coordinates <br> true (default) | false

Logical flag specifying whether to show the local coordinate axes.

## Data Types: logical

## ShowAnnotation - Show aperture size and element spacing annotations <br> true (default) | false

Logical flag specifying whether to show the annotations in the UI panel of the figure. Annotation shows aperture size and element spacing based on array axis of array.
Data Types: logical

## Orientation - Orientation of the array

[0;0;0] (default) | 3-by-1 column vector with real values
Orientation of the array, specified as a 3-by-1 column vector containing the rotation angles with respect to the $\mathrm{x}-, \mathrm{y}$-, and z -axes of the local coordinate system, respectively. The default value is [0;0;0].

## Data Types: double

## ShowTaper - Option to show taper magnitude

## false (default) | true

Option to show taper magnitude, specified as the comma-separated pair consisting of 'ShowTaper' and a Boolean value.

- true - change the element color brightness in proportion to the element taper magnitude
- false - plot all elements using the same color

Example: true
Data Types: logical

## ShowIndex - Element indices to show

' None ' (default) | vector of positive integers | 'All'
Element indices to show in the figure, specified as the comma-separated pair consisting of 'ShowIndex' and a vector of positive integers. Each number in the vector must be an integer between 1 and the number of elements. To show all of indices of the array, specify 'All '. To suppress all indices, specify 'None'.
Example: [1,2,3]
Data Types: double

## Title - Plot title

'Array Geometry' (default)| character vector
Plot title, specified as a character vector.
Example: 'My array plot'
Data Types: char | string

## Output Arguments

hndl - Handle of array elements plot
scalar
Handle of array elements plot in the figure window, returned as a scalar.

## Version History <br> Introduced in R2021a

## bandwidth

Package: phased
Waveform bandwidth

## Syntax

BW = bandwidth(waveform)

## Description

$\mathrm{BW}=$ bandwidth(waveform) returns the bandwidth BW of the pulses for the waveform System object.

- For a linear FM waveform, the bandwidth equals the value of the SweepBandwidth property.
- For a rectangular waveform, the bandwidth equals the reciprocal of the pulse width.
- For the stepped FM waveform, If there are N frequency steps, the bandwidth equals N times the value of the FrequencyStep property. If there is no frequency stepping, the bandwidth equals the reciprocal of the pulse width.
- For phased coded waveform, The bandwidth value is the reciprocal of the chip width.


## Examples

## Compute Linear FM Bandwidth

Determine the bandwidth of a linear FM pulse waveform. The default value for an LFM waveform is 100 kHz .

```
waveform = phased.LinearFMWaveform;
bw = bandwidth(waveform)
bw = 100000
```


## Input Arguments

## waveform - Waveform object

waveform System object
Waveform, specified as a waveform System object.

## Output Arguments

## BW - Pulse bandwidth

scalar
Pulse bandwidth, returned as a positive scalar. Units are in Hz .

## Version History <br> Introduced in R2023a

## getStretchProcessor

Package: phased
Create stretch processor for waveform

## Syntax

strproc $=$ getStretchProcessor(waveform)
strproc $=$ getStretchProcessor(waveform, refrng)
strproc $=$ getStretchProcessor(waveform, refrng, rngspan)
strproc $=$ getStretchProcessor(waveform,refrng,rngspan,v)

## Description

strproc = getStretchProcessor(waveform) returns the stretch processor strproc for the waveform System object. By default the processor is set up so the reference range corresponds to $1 / 4$ of the maximum unambiguous range of a pulse. The range span corresponds to $1 / 10$ of the distance traveled by the wave within the pulse width. The propagation speed is the speed of light.
strproc = getStretchProcessor(waveform,refrng) also specifies the reference range.
strproc $=$ getStretchProcessor(waveform, refrng,rngspan) also specifies the range span rngspan. The reference interval is centered at refrng.
strproc = getStretchProcessor(waveform,refrng,rngspan,v) specifies the propagation speed v .

## Examples

## Detect a Target Using Stretch Processing

Use stretch processing to locate a target at a range of 4950 m .
Simulate the signal.

```
waveform = phased.LinearFMWaveform;
x = waveform();
c = physconst('LightSpeed');
rng = 4950.0;
num_samples = round(rng/(c/(2*waveform.SampleRate)));
x = circshift(x,num_samples);
```

Perform stretch processing.
stretchproc $=$ getStretchProcessor (waveform, 5000, 200, c) ;
$\mathrm{y}=$ stretchproc(x);

Plot the spectrum of the resulting signal.

```
[Pxx,F] = periodogram(y,[],2048,stretchproc.SampleRate,'centered');
```

plot(F/1000,10*log10(Pxx))
grid
xlabel('Frequency (kHz)')
ylabel('Power/Frequency (dB/Hz)')
title('Periodogram Power Spectrum Density Estimate')


Detect the range.

```
[~,rngidx] = findpeaks(pow2db(Pxx/max(Pxx)),'MinPeakHeight',-5);
rngfreq = F(rngidx);
rng = stretchfreq2rng(rngfreq,stretchproc.SweepSlope,stretchproc.ReferenceRange,c)
rng = 4.9634e+03
```


## Input Arguments

## waveform - Waveform

pulse waveform System object
Pulse waveform, specified as a Phased Array System Toolbox System object.
Example: phased.RectangularWaveform

## refrng - Reference range

$1 / 4$ of the maximum unambiguous range of a pulse (default) | positive scalar
Reference range, specified as a positive scalar. Units are in meters.

Data Types: double

## rngspan - Range span of interest

$1 / 10$ of the distance traveled by the wave within the pulse width (default) | positive scalar
Range span of interest, specfied as a positive scalar. The center of the interval is the range value specified in the refrng argument. Units are in meters.

Data Types: double
v - Propagation speed
speed of light (default) | positive scalar
Propagation speed, specified as a positive scalar. Units are in meters per second.
Example: 300.0
Data Types: double

## Output Arguments

## strproc - Stretch processor

stretch processor System object
Stretch processor, returned as a phased.StretchProcessor System object.

## Version History

Introduced in R2023a

## See Also

phased.StretchProcessor|stretchfreq2rng

## Topics

Range Estimation Using Stretch Processing "Stretch Processing"

## getMatchedFilter

Package: phased
Matched filter coefficients derived from waveform

## Syntax

coeff = getMatchedFilter(waveform)
coeff = getMatchedFilter(waveform,FrequencyOffset $=$ foffset)

## Description

coeff = getMatchedFilter(waveform) returns the matched filter coefficients coeff for the pulse FM waveform object.
coeff = getMatchedFilter(waveform,FrequencyOffset = foffset) also specifies a frequency offset foffset when matched filter coefficients are generated. To enable this syntax, set the FrequencyOffsetSource property of the waveform to 'Input port'.

## Examples

## Matched Filter Coefficients of Linear FM Waveform

Get the matched filter coefficients for a linear FM pulse.

```
waveform = phased.LinearFMWaveform('PulseWidth',5e-05,...
    'SweepBandwidth',1e5,'OutputFormat','Pulses');
coeff = getMatchedFilter(waveform);
stem(real(coeff))
title('Matched Filter Coefficients, Real Part')
```



## Input Arguments

waveform - Pulse waveform
pulse waveform System object
Pulse waveform, specified as a waveform System object.
Example: phased. RectangularWaveform
foffset - frequency offset
scalar
Frequency offset, specified as a scalar. Units are in Hz.
Example: 12000. 0
Data Types: double

## Output Arguments

## coeff - Matched filter coefficients

complex-valued column vector
Matched filter coefficients, returned as a complex-valued column vector. Units are dimensionless.

## Version History

Introduced in R2023a

## plot

Package: phased
Plot pulse waveform

## Syntax

plot(waveform)
plot(waveform,Name=Value)
plot(waveform,Name=Value,LineSpec)
hndl $=$ plot( $\qquad$ )

## Description

plot(waveform) plots the real part of the waveform.
plot (waveform, Name=Value) plots the waveform with additional options specified by one or more (Name=Value) pair arguments.
plot (waveform, Name=Value, LineSpec) specifies the same line color, line style, or marker options as are available in the MATLAB plot function.
hndl $=$ plot( $\qquad$ ) returns the line handle in the figure.

## Examples

## Plot Linear FM Pulse

Create and plot an upsweep linear FM pulse waveform.

```
waveform = phased.LinearFMWaveform('SweepBandwidth',1e5,'PulseWidth',1e-4);
``` plot(waveform);


\section*{Plot Quadratic FM Pulse Waveform}

Create and plot a quadratic FM pulse waveform. The pulse has a 10 MHz bandwidth and \(50 \mu \mathrm{sec}\) duration. The pulse sample rate is 10 times the bandwidth.
\(B W=10 e 6 ;\)
T = 50e-6;
waveform = phased.NonlinearFMWaveform( ...
'SampleRate', 10*BW, 'SweepBandwidth', BW, ...
'PulseWidth', T) ;
plot(waveform,PlotType='complex')


\section*{Input Arguments}

\section*{waveform - Pulse waveform}
waveform System object
Pulse waveform, specified as a System object.

\section*{LineSpec - Line properties}
' b ' (default) | character vector
Character vector to specifies the same line color, style, or marker options as are available in the MATLAB plot function. If you specify a PlotType value of ' complex', then LineSpec applies to both the real and imaginary subplots.

\section*{Name-Value Pair Arguments}

Specify optional pairs of arguments as Name1=Value1, . . . ,NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.
Example: plot(waveform,PlotType=' complex', pulseidx=4)

\section*{PlotType - plot type}
'real' (default)|'imag' | 'complex'

Specifies whether the function plots the real part, imaginary part, or both parts of the waveform. Valid values are 'real','imag', and 'complex'.
Example: 'complex'
Data Types: char|string

\section*{pulseidx - Index of pulse to plot}

1 (default) | positive integer
Index of the pulse to plot. This value must be a scalar.
Example: 4
Data Types: double

\section*{FrequencyOffset - Frequency offset}
0.0 (default) | scalar

Frequency offset, specified as a scalar. Units are in Hz .
Example: - 100
Data Types: double

\section*{FrequencyOffsetSource - Frequency offset source}
'Input port' (default)
Frequency offset source, specified as a scalar. Units are in Hz.
Example: 'Input port'
Data Types: double

\section*{Output Arguments}

\section*{hndl - Line handle}
scalar | positive valued column vector
Handle to the line or lines in the figure. For a PlotType value of ' complex' , hndl is a column vector. The first and second elements of this vector are the handles to the lines in the real and imaginary subplots, respectively.

\section*{Version History \\ Introduced in R2023a}

Functions

\section*{aictest}

Dimension of signal subspace

\section*{Syntax}
```

nsig = aictest(X)

```
nsig = aictest(X,'fb')

\section*{Description}
nsig = aictest(X) estimates the number of signals, nsig, present in a snapshot of data, X , that impinges upon the sensors in an array. The estimator uses the Akaike Information Criterion test (AIC). The input argument, X , is a complex-valued matrix containing a time sequence of data samples for each sensor. Each row corresponds to a single time sample for all sensors.
nsig = aictest(X,'fb') estimates the number of signals. Before estimating, it performs forwardbackward averaging on the sample covariance matrix constructed from the data snapshot, X. This syntax can use any of the input arguments in the previous syntax.

\section*{Examples}

\section*{Estimate the Signal Subspace Dimensions for Two Arriving Signals}

Construct a data snapshot for two plane waves arriving at a half-wavelength-spaced uniform line array with 10 elements. The plane waves arrive from \(0^{\circ}\) and \(-25^{\circ}\) azimuth, both with elevation angles of \(0^{\circ}\). Assume the signals arrive in the presence of additive noise that is both temporally and spatially Gaussian white. For each signal, the SNR is 5 dB . Take 300 samples to build a 300 -by- 10 data snapshot. Then, solve for the number of signals using aictest.
```

N = 10;
d = 0.5;
elementPos = (0:N-1)*d;
angles = [0 -25];
x = sensorsig(elementPos,300,angles,db2pow(-5));
nsig = aictest(x)
nsig = 2

```

The result shows that the number of signals is two, as expected.

\section*{Estimate the Signal Subspace Dimension Using Forward-Backward Smoothing}

Construct a data snapshot for two plane waves arriving at a half-wavelength-spaced uniform line array with 10 elements. Two correlated plane waves arrive from \(0^{\circ}\) and \(10^{\circ}\) azimuth, both with elevation angles of \(0^{\circ}\). Assume that the signals arrive in the presence of additive noise that is both temporally and spatially Gaussian white. For each signal, the SNR is 10 dB . Take 300 samples to build a 300-by-10 data snapshot. Then, solve for the number of signals using aictest.
```

N = 10;
d = 0.5;
elementPos = (0:N-1)*d;
angles = [0 10];
ncov = db2pow(-10);
scov = [1 .5]'*[1 .5];
x = sensorsig(elementPos,300,angles,ncov,scov);
Nsig = aictest(x)
Nsig = 1

```

This result shows that aictest cannot determine the number of signals correctly when the signals are correlated.

Use the forward-backward smoothing option.
Nsig \(=\) aictest(x,'fb')
Nsig \(=2\)
The addition of forward-backward smoothing yields the correct number of signals.
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\section*{Input Arguments}

\section*{X - Data snapshot \\ complex-valued \(K\)-by- \(N\) matrix}

Data snapshot, specified as a complex-valued, \(K\)-by- \(N\) matrix. A snapshot is a sequence of timesamples taken simultaneous at each sensor. In this matrix, \(K\) represents the number of time samples of the data, while \(N\) represents the number of sensor elements.
Example: [ \(-0.1211+1.2549 i, 0.1415+1.6114 i, 0.8932+0.9765 i ;]\)
Data Types: double
Complex Number Support: Yes

\section*{Output Arguments}

\section*{nsig - Dimension of signal subspace}
non-negative integer
Dimension of signal subspace, returned as a non-negative integer. The dimension of the signal subspace is the number of signals in the data.

\section*{More About}

\section*{Estimating the Number of Sources}

AIC and MDL tests
Direction finding algorithms such as MUSIC and ESPRIT require knowledge of the number of sources of signals impinging on the array or equivalently, the dimension, \(d\), of the signal subspace. The Akaike

Information Criterion (AIC) and the Minimum Description Length (MDL) formulas are two frequentlyused estimators for obtaining that dimension. Both estimators assume that, besides the signals, the data contains spatially and temporally white Gaussian random noise. Finding the number of sources is equivalent to finding the multiplicity of the smallest eigenvalues of the sampled spatial covariance matrix. The sample spatial covariance matrix constructed from a data snapshot is used in place of the actual covariance matrix.

A requirement for both estimators is that the dimension of the signal subspace be less than the number of sensors, \(N\), and that the number of time samples in the snapshot, \(K\), be much greater than \(N\).

A variant of each estimator exists when forward-backward averaging is employed to construct the spatial covariance matrix. Forward-backward averaging is useful for the case when some of the sources are highly correlated with each other. In that case, the spatial covariance matrix may be ill conditioned. Forward-backward averaging can only be used for certain types of symmetric arrays, called centro-symmetric arrays. Then the forward-backward covariance matrix can be constructed from the sample spatial covariance matrix, \(S\), using \(S_{F B}=S+J S^{*} J\) where \(J\) is the exchange matrix. The exchange matrix maps array elements into their symmetric counterparts. For a line array, it would be the identity matrix flipped from left to right.

All the estimators are based on a cost function
\[
L_{d}(d)=K(N-d) \ln \left\{\frac{\frac{1}{N-d} \sum_{i=d+1}^{N} \widehat{\lambda}_{i}}{\left\{\prod_{i=d+1}^{N} \widehat{\lambda}_{i}\right\}^{\frac{1}{N-d}}}\right\}
\]
plus an added penalty term. The value \(\lambda_{i}\) represent the smallest ( \(N-d\) ) eigenvalues of the spatial covariance matrix. For each specific estimator, the solution for \(d\) is given by
- AIC
\[
\widehat{d}_{A I C}=\underset{d}{\operatorname{argmin}}\left\{L_{d}(d)+d(2 N-d)\right\}
\]
- AIC for forward-backward averaged covariance matrices
\[
\widehat{d}_{A I C: F B}=\underset{d}{\operatorname{argmin}}\left\{L_{d}(d)+\frac{1}{2} d(2 N-d+1)\right\}
\]
- MDL
\[
\widehat{d}_{M D L}=\underset{d}{\operatorname{argmin}}\left\{L_{d}(d)+\frac{1}{2}(d(2 N-d)+1) \ln K\right\}
\]
- MDL for forward-backward averaged covariance matrices
\[
\widehat{d}_{M D L F B}=\underset{d}{\operatorname{argmin}}\left\{L_{d}(d)+\frac{1}{4} d(2 N-d+1) \ln K\right\}
\]

\section*{Version History}

\section*{Introduced in R2013a}

\section*{References}
[1] Van Trees, H.L. Optimum Array Processing. New York: Wiley-Interscience, 2002.

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder \(^{\text {TM }}\).
Usage notes and limitations:
Does not support variable-size inputs.

\author{
See Also \\ espritdoa|mdltest|rootmusicdoa|spsmooth
}

\section*{albersheim}

Required SNR using Albersheim's equation

\section*{Syntax}

SNR = albersheim(Pd,Pfa)
SNR = albersheim(Pd,Pfa,N)

\section*{Description}

SNR = albersheim(Pd,Pfa) returns the signal-to-noise ratio in decibels. This value indicates the ratio required to achieve the given probabilities of detection Pd and false alarm Pfa for a single sample.

SNR = albersheim(Pd,Pfa, N ) determines the required SNR for the noncoherent integration of N samples.

\section*{Examples}

\section*{Compute Required SNR for Probability of Detection}

Compute the required SNR of a single pulse to achieve a detection probability of 0.9 as a function of the fals- alarm probability.

Set the probability of detection to 0.9 and the probabilities of false alarm from 0.0001 to 0.01 .
Pd = 0.9;
Pfa \(=0.0001: 0.0001: .01 ;\)
Loop the Albersheim equation over all false-alarm probabilities.
```

snr = zeros(1,length(Pfa));
for j = 1:length(Pfa)
snr(j) = albersheim(Pd,Pfa(j));
end

```

Plot the SNR as a function of false-alarm probability.
```

semilogx(Pfa,snr)
grid
axis tight
xlabel("Probability of False Alarm")
ylabel("Required SNR (dB)")
title("Required SNR for P_D = "+Pd+" (N = 1)")

```


\section*{Compute Required SNR for Probability of Detection of 10 Pulses}

Compute the required SNR of 10 noncoherently integrated pulse to achieve a detection probability of 0.9 as a function of the false-alarm probability.

Set the probability of detection to 0.9 and the probabilities of false alarm from 0.0001 to 0.01 .
\(\mathrm{Pd}=0.9\);
Pfa \(=\) 0.0001:0.0001:.01;
Npulses = 10;
Loop over the Albersheim equation over all the false-alarm probabilities.
```

snr = zeros(1,length(Pfa));
for j = 1:length(Pfa)
snr(j) = albersheim(Pd,Pfa(j),Npulses);
end

```

Plot the SNR as a function of the false-alarm probability.
```

semilogx(Pfa,snr)
grid
axis tight
xlabel("Probability of False Alarm")

```
```

ylabel("Required SNR (dB)")
title("Required SNR for P_D = "+Pd+" (N = 10)")

```


\section*{Input Arguments}

\section*{Pd - Probability of detection}
positive scalar
Probability of detection, specified as a positive scalar.
Data Types: single | double

\section*{Pfa - Probability of false alarm}
positive scalar
Probability of false alarm, specified as a positive scalar.
Data Types: single | double

\section*{N - Number of pulses for noncoherent integration}

1 (default) | positive scalar
Number of pulses for noncoherent integration, specified as a positive scalar.
Data Types: single | double

\section*{More About}

\section*{Albersheim's Equation}

Albersheim's equation uses a closed-form approximation to calculate the SNR. This SNR value is required to achieve the specified detection and false-alarm probabilities for a nonfluctuating target in independent and identically distributed Gaussian noise. The approximation is valid for a linear detector and is extensible to the noncoherent integration of \(N\) samples.

Let
\[
A=\ln \frac{0.62}{P_{F A}}
\]
and
\[
B=\ln \frac{P_{D}}{1-P_{D}}
\]
where \(P_{F A}\) and \(P_{D}\) are the false-alarm and detection probabilities, respectively
Albersheim's equation for the required SNR in decibels is:
\[
\mathrm{SNR}=-5 \log _{10} N+[6.2+4.54 / \sqrt{N+0.44}] \log _{10}(A+0.12 A B+1.7 B)
\]
where \(N\) is the number of noncoherently integrated samples.

\section*{Version History}

Introduced in R2011a

\section*{Extended Capabilities}

\section*{C/C++ Code Generation}

Generate C and C++ code using MATLAB® Coder \({ }^{\text {TM }}\).
Usage notes and limitations:
Does not support variable-size inputs.

\section*{References}
[1] Richards, M. A. Fundamentals of Radar Signal Processing. New York: McGraw-Hill, 2005.
[2] Skolnik, M. Introduction to Radar Systems, 3rd Ed. New York: McGraw-Hill, 2001.

\section*{See Also}
shnidman

\section*{ambgfun}

Ambiguity and crossambiguity function

\section*{Syntax}
```

afmag = ambgfun(x,Fs,PRF)
afmag = ambgfun(x,y,Fs,PRF)
[afmag,delay,doppler] = ambgfun(

```
\(\qquad\)
``` )
[afmag,delay,doppler] = ambgfun(__,"Cut","2D")
[afmag,delay] = ambgfun( ___,"Cut","Doppler")
[afmag,delay] = ambgfun(
```

$\qquad$

``` "Cut" "Doppler"
                                ,"Cut", "Doppler", "CutValue",V)
[afmag,doppler] = ambgfun(
```

$\qquad$

``` ,"Cut","Delay")
[afmag,doppler] = ambgfun(
``` \(\qquad\)
``` ,"Cut","Delay","CutValue", V) ambgfun (
``` \(\qquad\)

\section*{Description}
afmag \(=\) ambgfun( \(x, F s, P R F)\) returns the magnitude of the normalized ambiguity function for the vector x . Fs is the sampling rate. PRF is the pulse repetition rate.
\(\operatorname{afmag}=\operatorname{ambg} f u n(x, y, F s, P R F)\) returns the magnitude of the normalized crossambiguity function between the pulse \(x\) and the pulse \(y\).
[afmag, delay,doppler] = ambgfun(__ ) or [afmag,delay,doppler] = ambgfun( , "Cut", "2D") returns the time delay vector, delay, and the Doppler frequency vector, doppler.
[afmag, delay] = ambgfun( \(\qquad\) , "Cut", "Doppler") returns delays from a zero-Doppler cut through the 2-D normalized ambiguity function magnitude.
[afmag, delay] = ambgfun(__,"Cut","Doppler","CutValue", V) returns delays from a nonzero Doppler cut through the 2-D normalized ambiguity function magnitude at Doppler value, V.
[afmag,doppler] = ambgfun( \(\qquad\) , "Cut","Delay") returns the Doppler values from zerodelay cut through the 2-D normalized ambiguity function magnitude.
[afmag, doppler] = ambgfun(__, "Cut","Delay","CutValue", V) returns the Doppler values from a one-dimensional cut through the 2-D normalized ambiguity function magnitude at a delay value of V .
ambgfun (__) , with no output arguments, plots the ambiguity or crossambiguity function. When "Cut" is " 2 D ", the function produces a contour plot of the periodic ambiguity function. When "Cut" is "Delay" or "Doppler", the function produces a line plot of the periodic ambiguity function cut.

\section*{Examples}

\section*{Plot Ambiguity Function of Rectangular Pulse}

Plot the ambiguity function magnitude of a rectangular pulse.
waveform = phased.RectangularWaveform;
x = waveform();
PRF = waveform.PRF;
[afmag,delay,doppler] = ambgfun(x,waveform.SampleRate,PRF);
contour(delay,doppler, afmag)
xlabel("Delay (seconds)")
ylabel("Doppler Shift (hertz)")


Use the ambgfun function with no output arguments to recreate the plot.
ambgfun(x, waveform.SampleRate, PRF)


\section*{Plot Autocorrelation Sequences of Rectangular and Linear FM Pulses}

This example shows how to plot zero-Doppler cuts of the autocorrelation sequences of rectangular and linear FM pulses of equal duration. Note the pulse compression exhibited in the autocorrelation sequence of the linear FM pulse.
```

hrect = phased.RectangularWaveform("PRF",2e4);
hfm = phased.LinearFMWaveform("PRF",2e4);
xrect = hrect();
xfm = hfm();
[ambrect,delayrect] = ambgfun(xrect,hrect.SampleRate,...,
hrect.PRF,"Cut","Doppler");
[ambfm,delayfm] = ambgfun(xfm,hfm.SampleRate,...,
hfm.PRF,"Cut","Doppler");
subplot(2,1,1)
stem(delayrect,ambrect)
title("Autocorrelation of Rectangular Pulse")
subplot(2,1,2)
stem(delayfm,ambfm)
xlabel("Delay (seconds)")
title("Autocorrelation of Linear FM Pulse")

```


Plot Nonzero-Doppler Cuts of Autocorrelation Sequences
Plot nonzero-Doppler cuts of the autocorrelation sequences of rectangular and linear FM pulses of equal duration. Both cuts are taken at a 5 kHz Doppler shift. Besides the reduction of the peak value, there is a strong shift in the position of the linear FM peak, evidence of range-doppler coupling.
```

hrect = phased.RectangularWaveform("PRF",2e4);
hfm = phased.LinearFMWaveform("PRF",2e4);
xrect = hrect();
xfm = hfm();
fd = 5000;
[ambrect,delayrect] = ambgfun(xrect,hrect.SampleRate,...,
hrect.PRF,"Cut","Doppler","CutValue",fd);
[ambfm,delayfm] = ambgfun(xfm,hfm.SampleRate,...,
hfm.PRF,"Cut","Doppler","CutValue",fd);
figure
subplot(2,1,1)
stem(delayrect*10^6,ambrect)
title("Autocorrelation of Rectangular Pulse at 5 kHz Doppler Shift")
subplot(2,1,2)
stem(delayfm*10^6,ambfm)
xlabel("Delay (\mu sec)")
title("Autocorrelation of Linear FM Pulse at 5 kHz Doppler Shift")

```


\section*{Plot Crossambiguity Function}

Plot the crossambiguity function between an LFM pulse and a delayed replica. Compare the crossambiguity function with the original ambiguity function. Set the sampling rate to 100 Hz , the pulse width to 0.5 sec , and the pulse repetition frequency to 1 Hz . The delay or lag is 10 samples equal to 100 ms . The bandwidth of the LFM signal is 10 Hz .
```

fs = 100.0;
bw1 = 10.0;
prf = 1;
nsamp = fs/prf;
pw = 0.5;
nlag = 10;

```

Create the original waveform and its delayed replica.
```

waveform1 = phased.LinearFMWaveform("SampleRate",fs,"PulseWidth",1,...
"SweepBandwidth",bwl,"SweepDirection", "Up", "PulseWidth", pw, "PRF", prf);
wav1 = waveform1();
wav2 = [zeros(nlag,1);wav1(1:(end-nlag))];

```

Plot the ambiguity and crossambiguity functions.
```

ambgfun(wav1,fs,prf,"Cut","Doppler","CutVal",5)

```
hold on
```

ambgfun(wav1,wav2,fs,[prf,prf],"Cut","Doppler","CutVal",5)
hold off
legend("Signal ambiguity","Crossambiguity")

```


\section*{Input Arguments}
x - Input pulse waveform
complex-valued row or column vector
Input pulse waveform, specified as a complex-valued row or column vector.
Example: wf = phased.LinearFMWaveform; wf()

\section*{y - Second input pulse waveform}
complex-valued row or column vector
Second input pulse waveform, specified as a complex-valued row or column vector.
Example: wf = phased.RectangularWaveform; wf()

\section*{Fs - Sample rate}
positive scalar
Sample rate in hertz, specified as a positive scalar.
Example: wf = phased.LinearFMWaveform; wf.SampleRate

Data Types: double

\section*{PRF - Pulse repetition frequency}
positive scalar
Pulse repetition frequency in hertz, specified as a positive scalar.
Example: wf = phased.LinearFMWaveform; wf.PRF
Data Types: double

\section*{Name-Value Pair Arguments}

Specify optional pairs of arguments as Name1=Value1, . . . ,NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.
Example: "Cut", "Doppler", "CutValue", 10 specifies that a vector of ambiguity function values be produced at a Doppler shift of 10 Hz .

\section*{Cut - Direction of one-dimensional cut through ambiguity function "2D" (default) | "Delay" | "Doppler"}

Used to generate an ambiguity surface or one-dimensional cut through the ambiguity diagram. The value "2D" generates a surface plot of the two-dimensional ambiguity function. The direction of the one-dimensional cut is determined by setting the value of "Cut" to "Delay" or "Doppler".

The choice of "Delay" generates a cut at zero time delay. In this case, the second output argument of ambgfuncontains the ambiguity function values at Doppler shifted values. You can create a cut at nonzero time delay using the name-value pair "CutValue".

The choice of "Doppler" generates a cut at zero Doppler shift. In this case, the second output argument of ambgfun contains the ambiguity function values at time-delayed values. You can create cut at nonzero Doppler using the name-value pair "CutValue".
Data Types: char | string

\section*{CutValue - Optional time delay or Doppler shift at which ambiguity function cut is taken 0 (default) | real-valued scalar}

When setting the name-value pair "Cut" to "Delay" or "Doppler", you can set "CutValue" to specify a cross-section that may not coincide with either zero time delay or zero Doppler shift. However, "CutValue" cannot be used when "Cut" is set to "2D".

When "Cut" is set to "Delay", "CutValue" is the time delay at which the cut is taken. Time delay units are in seconds.

When "Cut" is set to "Doppler", "CutValue" is the Doppler shift at which the cut is taken. Doppler units are in hertz.

Example: "CutValue",10.0
Data Types: double

\section*{Output Arguments}

\section*{afmag - Normalized ambiguity or crossambiguity function magnitudes}
matrix
Normalized ambiguity or crossambiguity function magnitudes, returned as a matrix. afmag is an \(M\) -by- \(N\) matrix where \(M\) is the number of Doppler frequencies and \(N\) is the number of time delays.

\section*{delay - Time delays}
vector
Time delays, returned as a vector. delay is an \(N\)-by- 1 vector of time delays.
For the ambiguity function, if \(N_{\chi}\) is the length of signal x , then the delay vector consist of \(N=2 N_{\chi}-1\) samples in the range, \(\left.-\left(N_{\star} / 2\right)-1, \ldots,\left(N_{\star} / 2\right)-1\right)\).

For the crossambiguity function, let \(N_{y}\) be the length of the second signal. The time delay vector consists of \(N=N_{x}+N_{y^{-}} 1\) equally spaced samples. For an even number of delays, the delay sample times are \(-(N / 2-1) / F s, \ldots,(N / 2-1)) / F s\). For an odd number of delays, if \(N_{f}=f l o o r(N / 2)\), the delay sample times are \(-N_{f} / F s, \ldots,\left(N_{f}-1\right) / F s\).

\section*{doppler - Doppler frequencies}

\section*{vector}

Doppler frequencies, returned as a vector. doppler is an \(M\)-by- 1 vector of Doppler frequencies. The Doppler frequency vector consists of \(M=2^{\text {ceillog2 } N)}\) equally-spaced samples. Frequencies are (- \((M /\) 2) \(\left.F_{s}, \ldots,(M / 2-1) F_{s}\right)\).

\section*{More About}

\section*{Normalized Ambiguity Function}

The normalized ambiguity function is
\[
\begin{aligned}
& A\left(t, f_{d}\right)=\frac{1}{E_{\chi}}\left|\int_{-\infty}^{\infty} x(u) e^{j 2 \pi f_{d} u} \chi^{*}(u-t) d u\right| \\
& E_{x}=\int_{-\infty}^{\infty} x(u) x^{*}(u) d u
\end{aligned}
\]
where \(E_{x}\) is the squared norm of the signal, \(x(t), t\) is the time delay, and \(f_{d}\) is the Doppler shift. The asterisk \({ }^{(*)}\) denotes the complex conjugate. The ambiguity function describes the effects of time delays and Doppler shifts on the output of a matched filter.

The magnitude of the ambiguity function achieves maximum value at \((0,0)\). At this point, there is perfect correspondence between the received waveform and the matched filter. The maximum value of the normalized ambiguity function is one.

The magnitude of the ambiguity function at zero time delay and Doppler shift, \(|A(0,0)|\), is the matched filter output when the received waveform exhibits the time delay and Doppler shift for which the matched filter is designed. Nonzero values of the time delay and Doppler shift variables indicate that the received waveform exhibits mismatches in time delay and Doppler shift from the matched filter.

The crossambiguity function between two different signals is
\[
\begin{aligned}
& A\left(t, f_{d}\right)=\frac{1}{\sqrt{E_{x} E_{y}}}\left|\int_{-\infty}^{\infty} x(u) e^{j 2 \pi f_{d} u} y^{*}(u-t) d u\right| \\
& E_{x}=\int_{-\infty}^{\infty} x(u) x^{*}(u) d u \\
& E_{x}=\int_{-\infty}^{\infty} y(u) y^{*}(u) d u
\end{aligned}
\]

The peak of the crossambiguity function is not necessarily unity.

\section*{Version History}

Introduced in R2011a

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® Coder \(^{\mathrm{Tm}}\).
Usage notes and limitations:
- Does not support variable-size inputs.
- Supported only when output arguments are specified.

\section*{References}
[1] Levanon, N. and E. Mozeson. Radar Signals. Hoboken, NJ: John Wiley \& Sons, 2004.
[2] Mahafza, B. R., and A. Z. Elsherbeni. MATLAB Simulations for Radar Systems Design. Boca Raton, FL: CRC Press, 2004.
[3] Richards, M. A. Fundamentals of Radar Signal Processing. New York: McGraw-Hill, 2005.

\section*{See Also}

\section*{Functions}
pambgfun

\section*{Objects}
phased.LinearFMWaveform | phased.MatchedFilter | phased.PhaseCodedWaveform | phased.RectangularWaveform| phased.SteppedFMWaveform

\section*{aperture2gain}

Convert effective aperture to gain

\section*{Syntax}

GdB \(=\) aperture2gain(A, lambda)

\section*{Description}

GdB = aperture2gain(A, lambda) returns the antenna gain GdB corresponding to an effective aperture A for an incident electromagnetic wave with wavelength lambda.

\section*{Examples}

\section*{Compute Antenna Gain}

An antenna has an effective aperture of 3 square meters. Find the antenna gain when used to capture an electromagnetic wave with a wavelength of 10 cm .
```

g = aperture2gain(3,0.1)
g = 35.7633

```

\section*{Input Arguments}

\section*{A - Antenna effective aperture}
positive scalar | \(N\)-element vector of positive values
Antenna effective aperture, specified as a positive scalar or as an \(N\)-element real-valued vector of positive values. If A is a vector, each element of A corresponds is the effective aperture of a different antenna. See "Gain and Effective Aperture" on page 2-20 for a discussion of aperture and gain. Units are in square meters.
Data Types: double

\section*{lambda - Wavelength of the incident electromagnetic wave positive scalar}

Wavelength of the incident electromagnetic wave, specified as a positive scalar. The same wavelength applies to all antennas in A. The wavelength of an electromagnetic wave is the ratio of the wave propagation speed to the frequency. Units are in meters.
Data Types: double

\section*{Output Arguments}

\section*{GdB - Antenna gain}
scalar | \(N\)-element real-valued vector

Antenna gain, returned as a scalar or as an \(N\)-element real-valued vector. The elements of GdB represent the gain corresponding to the elements in A . The size of GdB equals the size of A . Units are in dBi.

\section*{Data Types: double}

\section*{More About}

\section*{Gain and Effective Aperture}

The effective aperture describes how much energy is captured by an antenna from an incident electromagnetic plane wave. The effective area of the antenna and is not the same as the actual physical area. The array gain of an antenna \(G\) is related to its effective aperture \(A_{e}\) by:
\[
G=\frac{4 \pi}{\lambda^{2}} A_{e}
\]
where \(\lambda\) is the wavelength of the incident electromagnetic wave. For a fixed wavelength, the antenna gain is proportional to the effective aperture. For a fixed effective aperture, the antenna gain is inversely proportional to the square of the wavelength.

The gain expressed in \(\mathrm{dBi}(G d B)\) is
\[
G d B=10 \log _{10} G=10 \log _{10}\left(\frac{4 \pi A_{g}}{\lambda^{2}}\right)
\]

The effective antenna aperture can be derived from the gain in dB using
\[
A_{e}=10^{G d B / 10} \frac{\lambda^{2}}{4 \pi} .
\]

\section*{Version History \\ Introduced in R2011a}

\section*{References}
[1] Skolnik, M. Introduction to Radar Systems, 3rd Ed. New York: McGraw-Hill, 2001.
[2] Richards, M. Fundamentals of Radar Signal Processing, New York: McGraw-Hill, 2005.

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder \(^{\mathrm{TM}}\).
Usage notes and limitations:
Does not support variable-size inputs.

\section*{See Also}
gain2aperture

\section*{arrayfactor}

Array factor of sensor arrays

\section*{Syntax}
af = arrayfactor(pos,ang)
af \(=\) arrayfactor(pos,ang,wts)

\section*{Description}
af = arrayfactor(pos,ang) returns the array factor af for an array of elements located at positions pos and arrival directions ang.
af = arrayfactor(pos,ang,wts) also specifies array steering weights wts.

\section*{Examples}

\section*{Compute Array Factor of Unsteered ULA}

Compute the array factor for an unsteered 8-element ULA operating at 100 MHz . Elements are placed 0.4 wavelengths apart.
```

freq = 100e6;
c = physconst('LightSpeed');
lam = c/freq;
pos = (0:7)*0.4;
ang = -90:90;
af = arrayfactor(pos,ang);
plot(ang,mag2db(abs(af.')))
xlabel('Angle (deg)')
ylabel('Array pattern (dB)')
ylim([-30 20])
title('Array Factor of Unsteered Uniform Linear Array')

```


\section*{Display Beam Patterns of Array Factor}

Display the array beam patterns for an 8 -element ULA with half-wavelength spacing. Steer the array to \(-30,0\), and 30 degrees.

Set the positions of the ULA elements.
pos \(=(0: 7) * 0.5\);
Define the steering direction weights.
```

angsteer = [-30 0 30];
wsteer = steervec(pos,angsteer);

```

Compute the array factors for each steering direction for all angles.
```

ang = -90:90;
af = arrayfactor(pos,ang,wsteer);

```

Plot the array factor for each steering direction.
plot(ang, mag2db(abs(af.')))
xlabel('Angle (deg)')
ylabel('Beam pattern (dB)')
ylim([-50 20])



\section*{Input Arguments}

\section*{pos - Positions of array sensor elements}

1 -by- \(N\) real-valued vector | 2 -by- \(N\) real-valued matrix | 3 -by- \(N\) real-valued matrix
Positions of the elements of a sensor array, specified as a 1 -by- \(N\) vector, a 2 -by- \(N\) matrix, or a 3 -by- \(N\) matrix. In this vector or matrix, \(N\) represents the number of elements of the array. Each column of pos represents the coordinates of an element. If pos is a 1 -by- \(N\) vector, then it represents the \(y\) coordinate of the sensor elements of a line array. The \(x\) and \(z\)-coordinates are assumed to be zero. When pos is a 2 -by- \(N\) matrix, it represents the \((y, z)\)-coordinates of the sensor elements of a planar array. This array is assumed to lie in the \(y z\)-plane. The \(x\)-coordinates are assumed to be zero. When pos is a 3-by-N matrix, then the array can have an arbitrary shape. Sensor positions are in terms of signal wavelength.

Example: [0,0,0; 0.1,0.4,0.3; 1,1,1]
Data Types: double

\section*{ang - Arrival directions of incoming signals}

1-by- \(M\) real-valued vector | 2 -by- \(M\) real-valued matrix
Arrival directions of incoming signals specified as a 1 -by- \(M\) vector or a 2 -by- \(M\) matrix, where \(M\) is the number of incoming signals. If ang is a 2 -by- \(M\) matrix, each column specifies the direction in azimuth
and elevation of the incoming signal [az;el]. The azimuth angle must lie between \(-180^{\circ}\) and \(180^{\circ}\) and the elevation angle must lie between \(-90^{\circ}\) and \(90^{\circ}\). The azimuth angle is the angle between the \(x-\) axis and the projection of the arrival direction vector onto the \(x y\) plane. It is positive when measured from the \(x\)-axis toward the \(y\)-axis. The elevation angle is the angle between the arrival direction vector and \(x y\)-plane. It is positive when measured towards the \(z\) axis. If ang is a 1 -by- \(M\) vector, then it represents a set of azimuth angles with the elevation angles assumed to be zero. Angle units are specified in degrees.
Example: [45;0]
Data Types: double
wts - Array weights
ones ( \(\mathrm{N}, 1\) ) (default) | complex-valued \(N\)-by-1 vector | complex-valued \(N\)-by- \(L\) matrix
Array weights, specified as a complex-valued \(N\)-by- 1 vector or complex-valued \(N\)-by- \(L\) matrix. Each column of wts corresponds to a different set of weights for the array. \(L\) is the number of weight sets.
Data Types: double
Complex Number Support: Yes

\section*{Output Arguments}

\section*{af - Array factor of sensor array}

1-by-M complex-valued vector | \(L\)-by- \(M\) complex-valued matrix
Array factor of sensor array, returned as a 1-by- \(M\) complex-valued vector or \(L\)-by- \(M\) complex-valued matrix. Each column contains the array factor for a different set of weights wts. Each row corresponds to one of the angles specified in ang.

\section*{Version History}

Introduced in R2022a

\section*{References}
[1] Van Trees, Harry L. Detection, Estimation, and Modulation Theory. 4: Optimum Array Processing. Wiley, 2002.
[2] Johnson, Don H. and D. Dudgeon. Array Signal Processing. Englewood Cliffs, NJ: Prentice Hall, 1993.
[3] Van Veen, B.D. and K. M. Buckley. "Beamforming: A versatile approach to spatial filtering"

\section*{Extended Capabilities}

\section*{\(\mathbf{C} / \mathbf{C + +}\) Code Generation}

Generate C and \(\mathrm{C}++\) code using MATLAB® \(\mathrm{Coder}^{\mathrm{TM}}\).

\section*{See Also}
steervec | phased.SteeringVector

\section*{az2broadside}

Convert azimuth and elevation angle to broadside angle

\section*{Syntax}
bsang = az2broadside(az)
bsang = az2broadside(az,el)

\section*{Description}
bsang = az2broadside(az) returns the broadside angle on page 2-27, bsang, corresponding to the azimuth angle, az, and zero elevation angle. All angles are define with respect to the local coordinate system.
bsang = az2broadside(az,el) also specifies the elevation angle, el.

\section*{Examples}

\section*{Convert Azimuth Angle to Broadside Angle}

Return the broadside angle corresponding to \(45^{\circ}\) azimuth and \(0^{\circ}\) elevation.
```

bsang = az2broadside(45)
bsang = 45.0000

```

\section*{Convert Azimuth and Elevation to Broadside Angle}

Return the broadside angle corresponding to \(45^{\circ}\) azimuth and \(45^{\circ}\) elevation.
```

bsang = az2broadside(45,45)
bsang = 30.0000

```

\section*{Convert Multiple Azimuth and Elevation Angles to Broadside Angles}

Return broadside angles for 10 azimuth-elevation pairs.
```

az = (75:5:120)';
el = (45:5:90)';
bsang = az2broadside(az,el);

```

\section*{Input Arguments}

\section*{az - Azimuth angle}
scalar | vector of real values
Azimuth angle, specified as a scalar or vector of real values. Azimuth angles lie in the range from \(180^{\circ}\) to \(180^{\circ}\). Units are in degrees.
Example: [35;20;-10]

\section*{el - Elevation angle}

0 (default) | scalar | vector of real values
Elevation angle, specified as a scalar or vector. The elevation angle lie in the range from \(-90^{\circ}\) to \(90^{\circ}\). The length of el must equal the length of az. Units are in degrees.
Example: [5;2;-1]

\section*{Output Arguments}

\section*{bsang - Broadside angle}
scalar | vector of real values
Broadside angle, returned as a scalar or vector. The length of bsang equals the length of az. Units are in degrees.

\section*{More About}

\section*{Broadside Angle}

Broadside angles are useful in describing the response pattern of a uniform linear array (ULA).
For the definition of the broadside angle and how to convert between azimuth and elevation, and broadside angle see "Broadside Angles". For definitions of the azimuth and elevation angles, see "Azimuth and Elevation Angles".

\section*{Version History}

\section*{Introduced in R2011a}

\section*{Extended Capabilities}

\section*{C/C++ Code Generation}

Generate C and C++ code using MATLAB® \({ }^{\circledR}\) Coder \(^{\text {TM }}\).
Usage notes and limitations:
Does not support variable-size inputs.

\section*{See Also}
broadside2az|azel2uv|azel2phitheta

\section*{azel2phitheta}

Convert angles from azimuth-elevation form to phi-theta form

\section*{Syntax}

PhiTheta = azel2phitheta(AzEl)
PhiTheta = azel2phitheta(AzEl,RotAx)

\section*{Description}

PhiTheta = azel2phitheta(AzEl) converts the azimuth/elevation angle on page 2-29 pairs to their corresponding phi/theta angle on page 2-30 pairs.

PhiTheta \(=\) azel2phitheta(AzEl,RotAx) also specifies the choice of phi-theta angle convention using RotAx.

\section*{Examples}

\section*{Convert Azimuth-Elevation Coordinates to Phi-Theta Coordinates}

Find the phi-theta representation for \(30^{\circ}\) azimuth and \(10^{\circ}\) elevation for the convention where phi is defined from the \(y\)-axis to the \(z\)-axis, and theta is defined from the \(x\)-axis toward the \(y z\)-plane.
```

PhiTheta = azel2phitheta([30;10])
PhiTheta = 2×1
19.4254
31.4749

```

\section*{Azimuth-Elevation Coordinates to Alternative Phi-Theta Coordinates}

Find the phi-theta representation for \(30^{\circ}\) azimuth and \(10^{\circ}\) elevation for the convention with phi defined from the \(x\)-axis to the \(y\)-axis, and theta defined from the \(z\)-axis toward the \(x y\)-plane.
```

PhiTheta = azel2phitheta([30;10],false)
PhiTheta = 2×1
30
80

```

\section*{Input Arguments}

\section*{AzEl - Azimuth-elevation angle pairs}
two-row matrix
Azimuth and elevation angles, specified as a two-row matrix. Each column of the matrix represents an angle in degrees, in the form [azimuth; elevation].
Data Types: double

\section*{RotAx - Phi-theta angle convention selection}
true (default) | false
Phi-theta angle convention selection, specified as true or false.
- If RotAx is true, the phi angle is defined from the \(y\)-axis to the \(z\)-axis and the theta angle is defined from the \(x\)-axis toward the \(y z\)-plane.
- If RotAx is false, the phi angle is defined from the \(x\)-axis to the \(y\)-axis and the theta angle is defined from the \(z\)-axis toward the \(x y\) - plane. (see "Alternative Definition of Phi and Theta" on page 2-31).

Data Types: double

\section*{Output Arguments}

\section*{PhiTheta - Phi-theta angle pairs}
two-row matrix
Phi and theta angles, returned as a two-row matrix. Each column of the matrix represents an angle in degrees, in the form [phi; theta]. The matrix dimensions of PhiTheta are the same as those of AzEl.

\section*{More About}

\section*{Azimuth and Elevation Angles}

The azimuth angle of a vector is the angle between the \(x\)-axis and the orthogonal projection of the vector onto the \(x y\) plane. The angle is positive in going from the \(x\) axis toward the \(y\) axis. Azimuth angles lie between -180 and 180 degrees. The elevation angle is the angle between the vector and its orthogonal projection onto the \(x y\)-plane. The angle is positive when going toward the positive \(z\)-axis from the xy plane. By default, the boresight direction of an element or array is aligned with the positive \(x\)-axis. The boresight direction is the direction of the main lobe of an element or array.

Note The elevation angle is sometimes defined in the literature as the angle a vector makes with the positive \(z\)-axis. The MATLAB and Phased Array System Toolbox products do not use this definition.

This figure illustrates the azimuth angle and elevation angle for a vector shown as a green solid line.


\section*{Phi and Theta Angles}

The phi angle \((\varphi)\) is the angle from the positive \(y\)-axis to the vector's orthogonal projection onto the \(y z\) plane. The angle is positive toward the positive \(z\)-axis. The phi angle is between 0 and 360 degrees. The theta angle \((\theta)\) is the angle from the \(x\)-axis to the vector itself. The angle is positive toward the \(y z\) plane. The theta angle is between 0 and 180 degrees.

The figure illustrates phi and theta for a vector that appears as a green solid line.


The coordinate transformations between \(\varphi / \theta\) and \(a z / e l\) are described by the following equations
\[
\begin{aligned}
& \operatorname{sinel}=\sin \phi \sin \theta \\
& \tan a z=\cos \phi \tan \theta \\
& \cos \theta=\operatorname{cosel} \cos a z \\
& \tan \phi=\operatorname{tanel} / \sin a z
\end{aligned}
\]

This transformation applies when RotAx is true.

\section*{Alternative Definition of Phi and Theta}

The phi angle \((\varphi)\) is the angle from the positive \(x\)-axis to the vector's orthogonal projection onto the xy plane. The angle is positive toward the positive \(y\)-axis. The phi angle is between 0 and 360 degrees. The theta angle \((\theta)\) is the angle from the \(z\)-axis to the vector itself. The angle is positive toward the xy plane. The theta angle is between 0 and 180 degrees.

The figure illustrates \(\varphi\) and \(\theta\) for a vector that appears as a green solid line.


\section*{Version History}

Introduced in R2012a

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® Coder \(^{\mathrm{Tm}}\).
Usage notes and limitations:
Does not support variable-size inputs.
See Also
phitheta2azel

\section*{Topics}
"Spherical Coordinates"

\section*{azel2phithetapat}

Convert radiation pattern from azimuth-elevation coordinates to phi-theta coordinates

\section*{Syntax}
```

pat_phitheta = azel2phithetapat(pat_azel,az,el)
pat_phitheta = azel2phithetapat(pat_azel,az,el,phi,theta)
pat_phitheta = azel2phithetapat(__,'RotateZ2X',rotpatax)
[pat_phitheta,phi_pat,theta_pat] = azel2phithetapat(___)

```

\section*{Description}
pat_phitheta = azel2phithetapat(pat_azel, az,el) converts the antenna radiation pattern, pat_azel, from azimuth and elevation coordinates to the pattern, pat_phitheta, in phi and theta coordinates. az and el are the azimuth and elevation angles at which the pat azel values are defined. The pat phitheta matrix covers theta values from 0 to 180 degrees and phi values from 0 to 360 degrees in one degree increments. The function interpolates the pat_azel matrix to estimate the response of the antenna in a given phi-theta direction.
pat_phitheta = azel2phithetapat(pat_azel,az,el, phi,theta) also specifies phi and theta as the grid at which to sample pat_phitheta. To avoid interpolation errors, phi should cover the range \([0,180]\), and theta should cover the range [ 0,360 ].
pat_phitheta = azel2phithetapat \(\qquad\) , 'RotateZ2X', rotpatax) also specifies rotpatax to indicate the boresight direction of the pattern along the \(x\)-axis or the \(z\)-axis.
[pat phitheta, phi_pat,theta_pat] = azel2phithetapat( _ ) also returns vectors phi_pat and theta_pat containing the phi and theta angles at which pat_phitheta is sampled.

\section*{Examples}

\section*{Convert Radiation Pattern to Phi-Theta}

Convert a radiation pattern to \(\varphi / \theta\) form, with the \(\varphi\) and \(\theta\) angles spaced 1 degree apart.
Define the pattern in terms of azimuth and elevation.
```

az = -180:180;
el = -90:90;
pat_azel = mag2db(repmat(cosd(el)',1,numel(az)));

```

Convert the pattern to \(\varphi / \theta\) space.
pat_phitheta = azel2phithetapat(pat_azel,az,el);

\section*{Plot Converted Radiation Pattern}

Plot the result of converting a radiation pattern to \(\phi / \theta\) space with the \(\phi\) and \(\theta\) angles spaced 1 degree apart.

The radiation pattern is the cosine of the elevation.
```

az = -180:180;
el = -90:90;
pat_azel = repmat(cosd(el)',1,numel(az));

```

Convert the pattern to \(\phi / \theta\) space. Use the returned \(\phi\) and \(\theta\) angles for plotting.
[pat_phitheta,phi,theta] = azel2phithetapat(pat_azel,az,el);
Plot the result.
\(H=\operatorname{surf}(\) phi, theta, mag2db(pat_phitheta) \()\);
H.LineStyle = 'none';
xlabel('phi (degrees)');
ylabel('theta (degrees)');
zlabel('Pattern');


\section*{Convert Radiation Pattern to Alternate Phi-Theta Coordinates}

Convert a radiation pattern to the alternate phi-theta coordinates, with the phi and theta angles spaced one degree apart.

Create a simple radiation pattern in terms of azimuth and elevation. Add an offset to the pattern to suppress taking the logarithm of zero in mag2db.
```

az = -180:180;
el = -90:90;
pat_azel = mag2db(cosd(el).^2'*sind(az).^2 + 1);
imagesc(az,el,pat azel)
xlabel('Azimuth (deg)')
ylabel('Elevation (deg)')
colorbar

```


Convert the pattern to phi-theta space.
```

[pat_phitheta,phi_pat,theta_pat] = azel2phithetapat(pat_azel,az,el,'RotateZ2X',false);
imagesc(phi_pat,theta_pat,pat_phitheta)
xlabel('Phi'(deg)')
ylabel('Theta (deg)')
colorbar

```


\section*{Convert Radiation Pattern for Specific Phi/Theta Values}

Convert a radiation pattern to \(\phi / \theta\) space with \(\phi\) and \(\theta\) angles spaced 5 degrees apart.
The radiation pattern is the cosine of the elevation.
```

az = -180:180;
el = -90:90;
pat_azel = repmat(cosd(el)',1,numel(az));

```

Define the set of \(\phi\) and \(\theta\) angles at which to sample the pattern. Then, convert the pattern.
```

phi = 0:5:360;

```
theta = 0:5:180;
pat_phitheta = azel2phithetapat(pat_azel,az,el,phi,theta);

Plot the result.
```

H = surf(phi,theta,mag2db(pat_phitheta));
H.LineStyle = 'none';
xlabel('phi (degrees)');
ylabel('theta (degrees)');
zlabel('Pattern');

```


\section*{Input Arguments}

\section*{pat_azel - Antenna radiation pattern}
real-valued \(Q\)-by-P matrix
Antenna radiation pattern as a function of azimuth and elevation, specified as a real-valued \(Q\)-by- \(P\) matrix. pat_azel contains the magnitude pattern. \(P\) is the length of the az vector, and \(Q\) is the length of the el vector. Units are in dB .

Data Types: double

\section*{az - Azimuth angles}
real-valued length- \(P\) vector
Azimuth angles at which the pat_azel pattern is sampled, specified as a real-valued length- \(P\) vector. Azimuth angles lie between -180 and 180, inclusive. Units are in degrees.
Data Types: double

\section*{el - Elevation angles}
real-valued length-Q vector
Elevation angles at which the pat_azel pattern is sampled, specified as a real-valued length- \(Q\) vector. Azimuth angles lie between - 90 and 90, inclusive. Units are in degrees.
Data Types: double

\section*{phi - Phi angles}
[0:360] (default) | real-valued length- \(L\) vector
Phi angles at which the pat_phitheta pattern is sampled, specified as a real-valued length- \(L\) vector. Phi angles lie between 0 and 360, inclusive. Units are in degrees.
Data Types: double

\section*{theta - Theta angles}
[0:180] (default) | real-valued length- \(M\) vector
Theta angles at which the pat_phitheta pattern is sampled, specified as a real-valued length- \(M\) vector. Theta angles lie between 0 and 180, inclusive. Units are in degrees.
Data Types: double
rotpatax - Pattern boresight direction selector
true (default) | false
Pattern boresight direction selector, specified as true or false.
- If rotpatax is true, the pattern boresight is along the \(x\)-axis. In this case, the \(z\)-axis of phi-theta space is aligned with the \(x\)-axis of azimuth and elevation space. The phi angle is defined from the \(y\)-axis to the \(z\)-axis and the theta angle is defined from the \(x\)-axis toward the \(y z\)-plane. (See "Phi and Theta Angles" on page 2-41).
- If rotpatax is false, the phi angle is defined from the \(x\)-axis to the \(y\)-axis and the theta angle is defined from the \(z\)-axis toward the \(x y\)-plane. (See "Alternative Definition of Phi and Theta" on page 2-42).

Data Types: logical

\section*{Output Arguments}

\section*{pat_phitheta - Antenna radiation pattern in phi-theta coordinates}
real-valued \(M\)-by- \(L\) matrix
Antenna radiation pattern in phi-theta coordinates, returned as a real-valued \(M\)-by- \(L\) matrix. pat_phitheta represents the magnitude pattern. \(L\) is the length of the phi_pat vector, and \(M\) is the length of the theta_pat vector. Units are in dB .

\section*{phi_pat - Phi angles}
real-valued length- \(L\) vector
Phi angles at which the pat_phitheta pattern is sampled, returned as a real-valued length \(L\) vector. Units are in degrees.

\section*{theta_pat - Theta angles}
real-valued length- \(M\) vector
Theta angles at which the pat_phitheta pattern is sampled, returned as a real-valued length- \(M\) vector. Units are in degrees.

\section*{More About}

\section*{Azimuth and Elevation Angles}

The azimuth angle of a vector is the angle between the \(x\)-axis and the orthogonal projection of the vector onto the xy plane. The angle is positive in going from the \(x\) axis toward the \(y\) axis. Azimuth angles lie between -180 and 180 degrees. The elevation angle is the angle between the vector and its orthogonal projection onto the \(x y\)-plane. The angle is positive when going toward the positive \(z\)-axis from the xy plane. By default, the boresight direction of an element or array is aligned with the positive \(x\)-axis. The boresight direction is the direction of the main lobe of an element or array.

Note The elevation angle is sometimes defined in the literature as the angle a vector makes with the positive \(z\)-axis. The MATLAB and Phased Array System Toolbox products do not use this definition.

This figure illustrates the azimuth angle and elevation angle for a vector shown as a green solid line.


\section*{Phi and Theta Angles}

The phi angle \((\varphi)\) is the angle from the positive \(y\)-axis to the vector's orthogonal projection onto the \(y z\) plane. The angle is positive toward the positive \(z\)-axis. The phi angle is between 0 and 360 degrees The theta angle \((\theta)\) is the angle from the \(x\)-axis to the vector itself. The angle is positive toward the \(y z\) plane. The theta angle is between 0 and 180 degrees.

The figure illustrates phi and theta for a vector that appears as a green solid line.


The coordinate transformations between \(\varphi / \theta\) and \(a z / e l\) are described by the following equations
\[
\begin{aligned}
& \sin e l=\sin \phi \sin \theta \\
& \tan a z=\cos \phi \tan \theta \\
& \cos \theta=\cos e l \cos a z \\
& \tan \phi=\tan e l / \sin a z
\end{aligned}
\]

\section*{Alternative Definition of Phi and Theta}

The phi angle \((\varphi)\) is the angle from the positive \(x\)-axis to the vector's orthogonal projection onto the \(x y\) plane. The angle is positive toward the positive \(y\)-axis. The phi angle is between 0 and 360 degrees. The theta angle \((\theta)\) is the angle from the \(z\)-axis to the vector itself. The angle is positive toward the \(x y\) plane. The theta angle is between 0 and 180 degrees.

The figure illustrates \(\varphi\) and \(\theta\) for a vector that appears as a green solid line.

\[
\begin{aligned}
& \phi=a z \\
& \theta=90-e l \\
& a z=\phi \\
& e l=90-\theta
\end{aligned}
\]

\section*{Version History}

Introduced in R2012a

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® Coder \(^{\mathrm{TM}}\).
Usage notes and limitations:
Does not support variable-size inputs.

\section*{See Also}
phased.CustomAntennaElement|phitheta2azel|azel2phitheta|phitheta2azelpat
Topics
"Spherical Coordinates"

\section*{azel2uv}

Convert azimuth/elevation angles to \(u / v\) coordinates

\section*{Syntax}

UV = azel2uv(AzEl)

\section*{Description}

UV = azel2uv(AzEl) converts the azimuth/elevation angle on page 2-45 pairs to their corresponding coordinates in \(u / v\) space on page 2-46.

\section*{Examples}

\section*{Conversion of Azimuth and Elevation to UV}

Find the corresponding \(u v\) representation for \(30^{\circ}\) azimuth and \(0^{\circ}\) elevation.
```

uv = azel2uv([30;0])
uv = 2x1
0.5000
0

```

\section*{Input Arguments}

\section*{AzEl - Azimuth/elevation angle pairs}
two-row matrix
Azimuth and elevation angles, specified as a two-row matrix. Each column of the matrix represents an angle pair in the form [azimuth;elevation]. Azimuth angles must lie in the range [-90, 90]. Units are in degrees.

Data Types: double

\section*{Output Arguments}

\section*{UV - Angle in u/v space}
two-row matrix
Angle in \(u / v\) space, returned as a two-row matrix. Each column of the matrix represents an angle in the form \([u ; v]\). The matrix dimensions of UV are the same as those of AzEl.

\section*{More About}

\section*{Azimuth Angle, Elevation Angle}

The azimuth angle of a vector is the angle between the \(x\)-axis and the orthogonal projection of the vector onto the xy plane. The angle is positive in going from the \(x\) axis toward the \(y\) axis. Azimuth angles lie between -180 and 180 degrees. The elevation angle is the angle between the vector and its orthogonal projection onto the \(x y\)-plane. The angle is positive when going toward the positive \(z\)-axis from the xy plane. By default, the boresight direction of an element or array is aligned with the positive \(x\)-axis. The boresight direction is the direction of the main lobe of an element or array.

Note The elevation angle is sometimes defined in the literature as the angle a vector makes with the positive \(z\)-axis. The MATLAB and Phased Array System Toolbox products do not use this definition.

This figure illustrates the azimuth angle and elevation angle for a vector shown as a green solid line.


\section*{U/V Space}

The \(u / v\) coordinates for the positive hemisphere \(x \geq 0\) can be derived from the phi and theta angles on page 2-46.

The relation between these two coordinates systems is
\[
\begin{aligned}
& u=\sin \theta \cos \phi \\
& v=\sin \theta \sin \phi
\end{aligned}
\]

In these expressions, \(\varphi\) and \(\theta\) are the phi and theta angles, respectively.
To convert azimuth and elevation to \(u\) and \(v\) use the transformation
\[
\begin{aligned}
u & =\text { coselsinaz } \\
v & =\text { sinel }
\end{aligned}
\]
which is valid only in the range \(a b s(a z) \leq=90\).
The values of \(u\) and \(v\) satisfy the inequalities
\[
\begin{aligned}
& -1 \leq u \leq 1 \\
& -1 \leq v \leq 1 \\
& u^{2}+v^{2} \leq 1
\end{aligned}
\]

Conversely, the phi and theta angles can be written in terms of \(u\) and \(v\) using
\[
\begin{aligned}
& \tan \phi=v / u \\
& \sin \theta=\sqrt{u^{2}+v^{2}}
\end{aligned}
\]

The azimuth and elevation angles can also be written in terms of \(u\) and \(v\) :
\[
\begin{aligned}
& \operatorname{sinel}=v \\
& \tan a z=\frac{u}{\sqrt{1-u^{2}-v^{2}}}
\end{aligned}
\]

\section*{Phi Angle, Theta Angle}

The phi angle \((\varphi)\) is the angle from the positive \(y\)-axis to the vector's orthogonal projection onto the \(y z\) plane. The angle is positive toward the positive \(z\)-axis. The phi angle is between 0 and 360 degrees. The theta angle \((\theta)\) is the angle from the \(x\)-axis to the vector itself. The angle is positive toward the \(y z\) plane. The theta angle is between 0 and 180 degrees.

The figure illustrates phi and theta for a vector that appears as a green solid line.


The coordinate transformations between \(\varphi / \theta\) and \(a z / e l\) are described by the following equations
\[
\begin{aligned}
& \sin e l=\sin \phi \sin \theta \\
& \tan a z=\cos \phi \tan \theta \\
& \cos \theta=\operatorname{cosel} \cos a z \\
& \tan \phi=\tan e l / \sin a z
\end{aligned}
\]

\section*{Version History}

Introduced in R2012a

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® Coder \(^{\mathrm{TM}}\).
Usage notes and limitations:
Does not support variable-size inputs.

\section*{See Also}
uv2azel

\section*{Topics}
"Spherical Coordinates"

\section*{azel2uvpat}

Convert radiation pattern from azimuth/elevation form to \(u / v\) form

\section*{Syntax}
```

pat_uv = azel2uvpat(pat_azel,az,el)
pat_uv = azel2uvpat(pat_azel,az,el,u,v)
[pat_uv,u_pat,v_pat] = azel2uvpat(

```
\(\qquad\)
``` )
```


## Description

pat uv = azel2uvpat(pat azel, az, el) expresses the antenna radiation pattern pat azel in $u / v$ space on page 2-54 coordinates instead of azimuth/elevation angle on page 2-53 coordinates. pat_azel samples the pattern at azimuth angles in az and elevation angles in el. The pat_uv matrix uses a default grid that covers $u$ values from -1 to 1 and $v$ values from -1 to 1 . In this grid, pat_uv is uniformly sampled with a step size of 0.01 for $u$ and $v$. The function interpolates to estimate the response of the antenna at a given direction. Values in pat_uv are NaN for $u$ and $v$ values outside the unit circle because $u$ and $v$ are undefined outside the unit circle.
pat_uv = azel2uvpat (pat_azel, az,el, $u, v$ ) uses vectors $u$ and $v$ to specify the grid at which to sample pat_uv. To avoid interpolation errors, $u$ should cover the range $[-1,1]$ and $v$ should cover the range $[-1,1]$.
[pat_uv,u_pat,v_pat] = azel2uvpat( $\qquad$ ) returns vectors containing the $u$ and $v$ coordinates at which pat_uv samples the pattern, using any of the input arguments in the previous syntaxes.

## Examples

## Convert Radiation Pattern to UV Space

Convert a radiation pattern to $u-v$ space, with the $u$ and $v$ coordinates spaced by 0.01 .
Define the pattern in terms of azimuth and elevation.

```
az = -90:90;
el = -90:90;
pat_azel = mag2db(repmat(cosd(el)',1,numel(az)));
```

Convert the pattern to $u-v$ space.

```
pat_uv = azel2uvpat(pat_azel,az,el);
```


## Plot Converted Radiation Pattern

Plot the result of converting a radiation pattern to $u / v$ space with the $u$ and $v$ coordinates spaced by 0.01 .

The radiation pattern is the cosine of the elevation angle.

```
az = -90:90;
el = -90:90;
pat_azel = repmat(cosd(el)',1,numel(az));
```

Convert the pattern to $u / v$ space. Use the $u$ and $v$ coordinates for plotting.
[pat_uv,u,v] = azel2uvpat(pat_azel,az,el);
Plot the result.
$H=\operatorname{surf}\left(u, v, \operatorname{mag} 2 d b\left(p a t \_u v\right)\right)$;
H.LineStyle = 'none';
xlabel('u');
ylabel('v');
zlabel('Pattern');


## Convert Radiation Pattern for Specific U/V Values

Convert a radiation pattern to $u / v$ form, with the $u$ and $v$ coordinates spaced by 0.05 .
The radiation pattern is cosine of the elevation angle.

```
az = -90:90;
el = -90:90;
pat_azel = repmat(cosd(el)',1,numel(az));
```

Define the set of $u$ and $v$ coordinates at which to sample the pattern. Then, convert the pattern.

```
u = -1:0.05:1;
v = -1:0.05:1;
pat_uv = azel2uvpat(pat_azel,az,el,u,v);
```

Plot the result.
$H=\operatorname{surf}\left(u, v, m a g 2 d b\left(p a t \_u v\right)\right)$;
H.LineStyle = 'none';
xlabel('u');
ylabel('v');
zlabel('Pattern');


## Input Arguments

## pat_azel - Antenna radiation pattern in azimuth/elevation form

Q-by-P matrix
Antenna radiation pattern in azimuth/elevation form, specified as a Q-by-P matrix. pat_azel samples the 3-D magnitude pattern in decibels, in terms of azimuth and elevation angles. $P$ is the length of the az vector, and $Q$ is the length of the el vector.

Data Types: double
az - Azimuth angles
vector of length $P$
Azimuth angles at which pat_azel samples the pattern, specified as a vector of length P. Each azimuth angle is in degrees, between -90 and 90. Such azimuth angles are in the hemisphere for which $u$ and $v$ are defined.

Data Types: double
el - Elevation angles
vector of length Q
Elevation angles at which pat_azel samples the pattern, specified as a vector of length Q. Each elevation angle is in degrees, between -90 and 90 .
Data Types: double

## u-u coordinates

[-1:0.01:1] (default) | vector of length L
$u$ coordinates at which pat_uv samples the pattern, specified as a vector of length L. Each $u$ coordinate is between -1 and 1 .
Data Types: double
$\mathbf{v} \boldsymbol{- v}$ coordinates
[-1:0.01:1] (default) | vector of length M
$v$ coordinates at which pat_uv samples the pattern, specified as a vector of length M. Each $v$ coordinate is between -1 and 1 .
Data Types: double

## Output Arguments

## pat_uv - Antenna radiation pattern in u/v form <br> M-by-L matrix

Antenna radiation pattern in $u / v$ form, returned as an M-by-L matrix. pat_uv samples the 3-D magnitude pattern in decibels, in terms of $u$ and $v$ coordinates. Lis the length of the $u$ vector, and $M$ is the length of the $v$ vector. Values in pat_uv are NaN for $u$ and $v$ values outside the unit circle because $u$ and $v$ are undefined outside the unit circle.

## u_pat - u coordinates <br> vector of length $L$

$u$ coordinates at which pat_uv samples the pattern, returned as a vector of length $L$.

## v_pat - v coordinates

vector of length $M$
$v$ coordinates at which pat_uv samples the pattern, returned as a vector of length M .

## More About

## Azimuth Angle, Elevation Angle

The azimuth angle of a vector is the angle between the $x$-axis and the orthogonal projection of the vector onto the xy plane. The angle is positive in going from the $x$ axis toward the $y$ axis. Azimuth angles lie between -180 and 180 degrees. The elevation angle is the angle between the vector and its orthogonal projection onto the $x y$-plane. The angle is positive when going toward the positive $z$-axis from the xy plane. By default, the boresight direction of an element or array is aligned with the positive $x$-axis. The boresight direction is the direction of the main lobe of an element or array.

Note The elevation angle is sometimes defined in the literature as the angle a vector makes with the positive $z$-axis. The MATLAB and Phased Array System Toolbox products do not use this definition.

This figure illustrates the azimuth angle and elevation angle for a vector shown as a green solid line.


## U/V Space

The $u$ and $v$ coordinates are the direction cosines of a vector with respect to the $y$-axis and $z$-axis, respectively.

The $u / v$ coordinates for the hemisphere $x \geq 0$ are derived from the phi and theta angles on page 254 by:

$$
\begin{aligned}
& u=\sin \theta \cos \phi \\
& v=\sin \theta \sin \phi
\end{aligned}
$$

In these expressions, $\varphi$ and $\theta$ are the phi and theta angles, respectively.
To convert azimuth and elevation to $u$ and $v$ use the transformation

$$
\begin{aligned}
& u=\text { coselsin } a z \\
& v=\text { sinel }
\end{aligned}
$$

which is valid only in the range $a b s(a z) \leq=90$.
The values of $u$ and $v$ satisfy the inequalities

$$
\begin{aligned}
& -1 \leq u \leq 1 \\
& -1 \leq v \leq 1 \\
& u^{2}+v^{2} \leq 1
\end{aligned}
$$

Conversely, the phi and theta angles can be written in terms of $u$ and $v$ using

$$
\begin{aligned}
& \tan \phi=v / u \\
& \sin \theta=\sqrt{u^{2}+v^{2}}
\end{aligned}
$$

The azimuth and elevation angles can also be written in terms of $u$ and $v$ :

$$
\begin{aligned}
& \text { sine }=v \\
& \tan a z=\frac{u}{\sqrt{1-u^{2}-v^{2}}}
\end{aligned}
$$

## Phi Angle, Theta Angle

The phi angle $(\varphi)$ is the angle from the positive $y$-axis to the vector's orthogonal projection onto the $y z$ plane. The angle is positive toward the positive $z$-axis. The phi angle is between 0 and 360 degrees. The theta angle $(\theta)$ is the angle from the $x$-axis to the vector itself. The angle is positive toward the $y z$ plane. The theta angle is between 0 and 180 degrees.

The figure illustrates phi and theta for a vector that appears as a green solid line.


The coordinate transformations between $\varphi / \theta$ and $a z / e l$ are described by the following equations

$$
\begin{aligned}
& \sin e l=\sin \phi \sin \theta \\
& \tan a z=\cos \phi \tan \theta \\
& \cos \theta=\cos e l \cos a z \\
& \tan \phi=\tan e l / \sin a z
\end{aligned}
$$

## Version History

Introduced in R2012a

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
Does not support variable-size inputs.

## See Also

phased.CustomAntennaElement | azel2uv | uv2azel |uv2azelpat

## Topics

"Spherical Coordinates"

## azelcut2pat

Create 3-D response pattern from azimuth and elevation cuts

## Syntax

```
pat = azelcut2pat(azcut,elcut)
```


## Description

pat = azelcut2pat(azcut,elcut) creates a 3-D element response pattern, pat, from an azimuth cut, azcut, and an elevation cut, elcut. An azimuth cut consists of an antenna pattern over all azimuth angles at $0^{\circ}$ elevation. An elevation cut consists of the antenna pattern over all elevation angles at $0^{\circ}$ azimuth. You can specify cuts for different frequencies at the same time.

## Examples

## Create Custom Antenna Pattern from Azimuth and Elevations Cuts

Create a custom antenna pattern from azimuth and elevation cuts of a cosine-squared pattern.

```
az = -180:180;
azcut = mag2db(cosd(az).^2);
el = -90:90;
elcut = mag2db(cosd(el).^2);
pat = azelcut2pat(azcut,elcut);
antenna = phased.CustomAntennaElement('AzimuthAngles',az,...
    'ElevationAngles',el,'MagnitudePattern',pat,...
    'PhasePattern',zeros(size(pat)));
```

Display the antenna pattern for 200 MHz .

```
fs = 200.0e6;
pattern(antenna,fs);
```



## Input Arguments

## azcut - Azimuth pattern cut

zeros (1,361) (default) | real-valued 1-by- $Q$ vector | real-valued $L$-by- $Q$ matrix
Azimuth pattern cut, specified as a real-valued 1-by- $Q$ vector or a real-valued $L$-by- $Q$ matrix. $Q$ is the number of azimuth angles, and $L$ is the number of frequencies. Azimuth cuts are assumed to be made at $0^{\circ}$ elevation. When azcut is a matrix, each column represents a different azimuth angle, and each row represents a different frequency. Units are in dB .
Data Types: double

## elcut - Elevation pattern cut

zeros $(1,181)$ (default) | real-valued 1 -by- $P$ vector | real-valued $L$-by- $P$ matrix
Elevation pattern cut, specified as a real-valued 1-by- $P$ vector or a real-valued $L$-by- $P$ matrix. $P$ is the number of elevation angles, and $L$ is the number of frequencies. Elevation cuts are assumed to be made at $0^{\circ}$ azimuth. When elcut is a matrix, each column represents a different elevation angle, and each row represents a different frequency. Units are in dB .

Data Types: double

## Output Arguments

## pat - 3-D antenna pattern

real-valued $P$-by- $Q$ matrix | real-valued $P$-by- $Q$-by- $L$ array
3-D array or antenna pattern, returned as a real-valued $P$-by- $Q$ matrix or real-valued $P$-by- $Q$-by- $L$ MATLAB array. Units are in dB.

## Algorithms

The function returns a 3-D antenna pattern at the same azimuth and elevation angles used to define the azcut and elcut cuts. Because the cuts are specified in dB, the 3-D pattern is computed from the sum of the cut patterns.
pat(az,el) $=$ pat(az) + pat(el)

## Version History

Introduced in R2019a

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® $\mathrm{Coder}^{\mathrm{TM}}$.

## azelaxes

Spherical basis vectors in 3-by-3 matrix form

## Syntax

A = azelaxes(az,el)

## Description

$\mathrm{A}=$ azelaxes (az,el) returns a 3-by-3 matrix containing the components of the basis( $\left.\widehat{\mathbf{e}}_{R}, \widehat{\mathbf{e}}_{a z}, \widehat{\mathbf{e}}_{e l}\right)$ at each point on the unit sphere specified by azimuth, az, and elevation, el. The columns of A contain the components of basis vectors in the order of radial, azimuthal and elevation directions.

## Examples

## Compute Spherical Basis Vectors

At the point located at $45^{\circ}$ azimuth, $45^{\circ}$ elevation, compute the 3 -by- 3 matrix containing the components of the spherical basis.

```
A = azelaxes(45,45)
A = 3\times3
    0.5000 -0.7071 -0.5000
    0.5000 0.7071 -0.5000
    0.7071 0 0.7071
```

The first column of A contains the radial basis vector [0.5000; 0.5000; 0.7071]. The second and third columns are the azimuth and elevation basis vectors, respectively.

## Input Arguments

## az - Azimuth angle

scalar in range [-180,180]
Azimuth angle specified as a scalar in the closed range [-180,180]. Angle units are in degrees. To define the azimuth angle of a point on a sphere, construct a vector from the origin to the point. The azimuth angle is the angle in the $x y$-plane from the positive $x$-axis to the vector's orthogonal projection into the $x y$-plane. As examples, zero azimuth angle and zero elevation angle specify a point on the $x$-axis while an azimuth angle of $90^{\circ}$ and an elevation angle of zero specify a point on the $y$ axis.
Example: 45
Data Types: double

## el - Elevation angle

scalar in range [-90,90]
Elevation angle specified as a scalar in the closed range [-90,90]. Angle units are in degrees. To define the elevation of a point on the sphere, construct a vector from the origin to the point. The elevation angle is the angle from its orthogonal projection into the $x y$-plane to the vector itself. As examples, zero elevation angle defines the equator of the sphere and $\pm 90^{\circ}$ elevation define the north and south poles, respectively.

Example: 30
Data Types: double

## Output Arguments

## A - Spherical basis vectors

3-by-3 matrix
Spherical basis vectors returned as a 3-by-3 matrix. The columns contain the unit vectors in the radial, azimuthal, and elevation directions, respectively. Symbolically we can write the matrix as

$$
\left(\widehat{\mathbf{e}}_{R}, \widehat{\mathbf{e}}_{a z}, \widehat{\mathbf{e}}_{e l}\right)
$$

where each component represents a column vector.

## More About

## Spherical basis

Spherical basis vectors are a local set of basis vectors which point along the radial and angular directions at any point in space.

The spherical basis vectors ( $\widehat{\mathbf{e}}_{R}, \widehat{\mathbf{e}}_{a z}, \widehat{\mathbf{e}}_{e l}$ ) at the point (az,el) can be expressed in terms of the Cartesian unit vectors by

$$
\begin{aligned}
& \widehat{\mathbf{e}}_{\mathbf{R}}=\cos (e l) \cos (a z) \widehat{\mathbf{i}}+\cos (e l) \sin (a z) \widehat{\mathbf{j}}+\sin (e l) \widehat{\mathbf{k}} \\
& \widehat{\mathbf{e}}_{\mathbf{a z}}=-\sin (a z) \widehat{\mathbf{i}}+\cos (a z) \widehat{\mathbf{j}} \\
& \widehat{\mathbf{e}}_{\mathbf{e l}}=-\sin (e l) \cos (a z) \widehat{\mathbf{i}}-\sin (e l) \sin (a z) \widehat{\mathbf{j}}+\cos (e l) \widehat{\mathbf{k}}
\end{aligned} .
$$

This set of basis vectors can be derived from the local Cartesian basis by two consecutive rotations: first by rotating the Cartesian vectors around the $y$-axis by the negative elevation angle, -el, followed by a rotation around the $z$-axis by the azimuth angle, $a z$. Symbolically, we can write

$$
\begin{aligned}
& \widehat{\mathbf{e}}_{\mathbf{R}}=R_{z}(a z) R_{y}(-e l)\left[\begin{array}{l}
1 \\
0 \\
0
\end{array}\right] \\
& \widehat{\mathbf{e}}_{\mathbf{a z}}=R_{z}(a z) R_{y}(-e l)\left[\begin{array}{l}
0 \\
1 \\
0
\end{array}\right] \\
& \widehat{\mathbf{e}}_{\mathbf{e l}}=R_{z}(a z) R_{y}(-e l)\left[\begin{array}{l}
0 \\
0 \\
1
\end{array}\right]
\end{aligned}
$$

The following figure shows the relationship between the spherical basis and the local Cartesian unit vectors.


## Algorithms

MATLAB computes the matrix A from the equations

```
A = [cosd(el)*cosd(az), -sind(az), -sind(el)*cosd(az); ...
    cosd(el)*sind(az), cosd(az), -sind(el)*sind(az); ...
    sind(el), 0, cosd(el)];
```


## Version History

Introduced in R2013a

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
Does not support variable-size inputs.

## See Also

cart2sphvec|sph2cartvec

## beamwidth2gain

Compute antenna gain from azimuth and elevation beamwidths

## Syntax

```
g = beamwidth2gain(hpbw)
g = beamwidth2gain(hpbw,at)
```


## Description

$\mathrm{g}=$ beamwidth2gain(hpbw) returns the gain of an antenna given its half-power beamwidth, hpbw.
$\mathrm{g}=$ beamwidth2gain(hpbw, at) also specifies the type of antenna aperture.

## Examples

## Antenna Gain for Uniformly Illuminated Rectangular Aperture

Compute the antenna gain for a uniformly illuminated rectangular aperture. Specify an azimuth beamwidth of 1.4 degrees and an elevation beamwidth of 5 degrees.

```
BWaz = 1.4;
BWel = 5;
g = beamwidth2gain([BWaz;BWel],'UniformRectangular')
g = 36.6522
```


## Input Arguments

## hpbw - Antenna half-power beamwidth

row vector | two-row matrix
Antenna half-power beamwidth in degrees, specified as a row vector or a two-row matrix.

- If hpbw is a row vector, then beamwidth2gain assumes a symmetric aperture and each element of hpbw specifies the same beamwidth for both azimuth and elevation dimensions.
- If hpbw is a two-row matrix, then its first row contains azimuth beamwidth values and its second row contains elevation beamwidth values.


## Data Types: double | single

## at - Antenna aperture type

```
'IdealRectangular'(default)|'IdealElliptical'| 'IdealGaussian' |
'UniformRectangular'|'CosineRectangular'|'UniformCircular'|
'ParabolicCircular'|'PracticalGeneral'
```

Antenna aperture type, specified as one of these:

- 'IdealRectangular' - Rectangular beam with no sidelobes
- 'IdealElliptical' - Elliptical beam with no sidelobes
- 'IdealGaussian' - Gaussian beam with no sidelobes
- 'UniformRectangular' - Uniformly illuminated rectangular aperture
- 'CosineRectangular' - Cosine illuminated rectangular aperture
- 'UniformCircular' - Uniformly illuminated circular aperture. In this case, hpbw must be either a row vector or a two-row matrix with identical rows because the beamwidth is the same in the azimuth and elevation dimensions.
- 'ParabolicCircular' - Circular aperture parabolic-on-a-12 dB pedestal distribution. In this case, hpbw must be either a row vector or a two-row matrix with identical rows because the beamwidth is the same in the azimuth and elevation dimensions.
- 'PracticalGeneral' - General-use practical antenna with sidelobes and null fill. For more details, see [1].

Data Types: char | string

## Output Arguments

g - Antenna gain
vector
Antenna gain in dBi units, returned as a vector. The number of elements of $g$ equals the number of columns of hpbw.

## Version History

## Introduced in R2021a

## References

[1] Stutzman, Warren L., and Gary A. Thiele. Antenna Theory and Design. 3rd ed. Hoboken, NJ: Wiley, 2013.
[2] Stutzman, Warren L. "Estimating Directivity and Gain of Antennas." IEEE Antennas and Propagation Magazine 40, no. 4 (August 1998): 7-11. https://doi.org/10.1109/74.730532.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

aperture2gain | gain2aperture

## beat2range

Convert beat frequency to range

## Syntax

$r=$ beat 2 range(fb,slope)
$r=$ beat 2 range (fb,slope, $c$ )

## Description

$r=$ beat2range( $\mathrm{fb}, \mathrm{slope}$ ) converts the beat frequency on page 2-67 of a dechirped linear FMCW signal to its corresponding range. slope is the slope of the FMCW sweep.
$r=$ beat 2 range ( $\mathrm{fb}, \mathrm{slope}, \mathrm{c}$ ) specifies the signal propagation speed.

## Examples

## Range of Target in FMCW Radar System

Assume that an FMCW waveform sweeps a band of 3 MHz in 2 ms . The dechirped target return has a beat frequency of 1 kHz . Compute the target range.

```
slope = 30e6/(2e-3);
fb = 1e3;
r = beat2range(fb,slope)
r= 9.9931
```


## Input Arguments

## fb - Beat frequency of dechirped signal

M-by-1 vector | M-by-2 matrix
Beat frequency of dechirped signal, specified as an M-by-1 vector or M-by-2 matrix in hertz. If the FMCW signal performs an upsweep or downsweep, fb is a vector of beat frequencies.

If the FMCW signal has a triangular sweep, fb is an M-by-2 matrix in which each row represents a pair of beat frequencies. Each row has the form
[UpSweepBeatFrequency, DownSweepBeatFrequency].
Data Types: single | double

## slope - Sweep slope

nonzero scalar
Slope of FMCW sweep, specified as a nonzero scalar in hertz per second. If the FMCW signal has a triangular sweep, slope is the sweep slope of the up-sweep half. In this case, slope must be positive and the down-sweep half is assumed to have a slope of -slope.

Data Types: single | double
c - Signal propagation speed
speed of light (default) | positive scalar
Signal propagation speed, specified as a positive scalar in meters per second.
Data Types: single | double

## Output Arguments

## r - Range

M-by-1 column vector
Range, returned as an M-by-1 column vector in meters. Each row of $r$ is the range corresponding to the beat frequency in a row of $f b$.
Data Types: single | double

## More About

## Beat Frequency

For an up-sweep or down-sweep FMCW signal, the beat frequency is $F_{t}-F_{r}$. In this expression, $F_{t}$ is the transmitted signal's carrier frequency, and $F_{r}$ is the received signal's carrier frequency.

For an FMCW signal with triangular sweep, the upsweep and downsweep have separate beat frequencies.

## Algorithms

If fb is a vector, the function computes $\mathrm{c}^{*} \mathrm{fb} /\left(2^{*}\right.$ slope $)$.
If fb is an M-by-2 matrix with a row [UpSweepBeatFrequency, DownSweepBeatFrequency], the corresponding row in $r$ is $c^{*}((U p S w e e p B e a t F r e q u e n c y ~-~ D o w n S w e e p B e a t F r e q u e n c y) / 2) / ~$ (2*slope).

This function supports single and double precision for input data and arguments.

## Version History

Introduced in R2012b

## References

[1] Pace, Phillip. Detecting and Classifying Low Probability of Intercept Radar. Artech House, Boston, 2009.
[2] Skolnik, M.I. Introduction to Radar Systems. New York: McGraw-Hill, 1980.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

- Usage notes and limitations:
- Does not support variable-size inputs.
- This function supports single and double precision for input data and arguments.


## See Also

dechirp|range2beat | rdcoupling | phased. FMCWWaveform
Topics
"Automotive Adaptive Cruise Control Using FMCW Technology" (Radar Toolbox)

## jsdmbbweights

Create MU-MIMO baseband precoding weights

## Syntax

```
wpbb = jsdmbbweights(chaneff,ns,wprf)
wpbb = jsdmbbweights( _,'RegularizationFactor',alpha)
[wpbb,wc] = jsdmbbweights(
```

$\qquad$

## Description

wpbb = jsdmbbweights(chaneff,ns,wprf) returns baseband precoding weights, wpbb, for the effective channel, chaneff, to achieve orthogonality among users by Joint Spatial Division Multiplexing (JSDM). RF precoding weights, wprf, divide users into groups by their location information. ns is the number of data streams or users.
wpbb = jsdmbbweights(__, 'RegularizationFactor',alpha) specifies the regularization factor, alpha.
[wpbb,wc] = jsdmbbweights( $\qquad$ ) also returns combining weights wc for each user.

## Examples

## Find JSDM Baseband Precoding Weights

Find baseband precoding weights for a JSDM beamformer based on a base station with a 64 -element linear antenna array. Assume there are two user groups. The first group has two users and the second group has three users. Array elements are $1 / 2$ wavelength apart.

Set the number of array elements to 64 .

```
Nt = 64;
```

Find the array steering weights in the direction of the first user group. The user group is centered at $+10^{\circ}$ azimuth.

```
v1 = steervec((0:Nt-1)*0.5,[9 11]);
rcl = vl*v1';
```

Find the array steering weights in the direction of the second user group. The user group is centered $-5^{\circ}$ azimuth.

```
v2 = steervec((0:Nt-1)*0.5,[-4 -5 -6]);
rc2 = v2*v2';
```

Then, compute the RF weights from the channel covariance matrix.

```
ns = [2 3];
hcov = {rc1,rc2};
wprf = jsdmrfweights(hcov,ns);
```

Construct the instantaneous effective channel.

```
heff1 = wprf{1}*v1*eye(ns(1))*randn(ns(1),ns(1),'like',1i);
heff2 = wprf{2}*v2*eye(ns(2))*randn(ns(2),ns(2),'like',1i);
```

Compute baseband weights using per-group-processing.

```
[wpbb,wc] = jsdmbbweights({heff1,heff2},ns,wprf);
```

Verify orthogonality.

```
horthol = wpbb{1}*heff1*wc{1}
hortho1 = 2\times2 complex
    9.5489 - 0.0000i 0.0000 + 0.0000i
    0.0000 - 0.0000i 9.5489 + 0.0000i
hortho2 = wpbb{2}*heff2*wc{2}
hortho2 = 3\times3 complex
    2.8633 + 0.0000i 0.0000 - 0.0000i 0.0000 + 0.0000i
    -0.0000 + 0.0000i 2.8633 + 0.0000i -0.0000 - 0.0000i
    0.0000 - 0.0000i -0.0000 - 0.0000i 2.8633 - 0.0000i
```


## Input Arguments

## chaneff - Effective downlink channels

complex-valued Nsc-by-TotalNrtf-by-TotalNs array | 1-by-G cell array
Effective downlink channels, specified as a complex-valued Nsc-by-TotalNrtf-by-TotalNs array or 1-by$G$ cell array. The effective downlink channels map the streams in each group to the $G$ user groups.

- If chaneff is a 3-dimensional Nsc-by-TotalNtrf-by-TotalNs array, TotalNs is the total number of data streams, TotalNtrf is the sum of RF chains for all user groups, and Nsc is the number of subcarriers. This configuration corresponds to the joint group processing (JGP) scheme of JSDM.
- If chaneff is a $1-$ by- $G$ cell array, then the $g^{\text {th }}$ element in the cell array contains the individual effective channel from the allocated RF chain at the base station to the corresponding group of users as either:
- an $\operatorname{Nsc}$-by- $\operatorname{Ntrf}(g)$-by- $N S(g)$ array when ns is a vector, or
- an $N s c$-by- $\operatorname{Ntrf(g)-by-sum(NS\{ g\} )~array~when~ns~is~a~cell~array.~}$

This configuration corresponds to the per group processing (PGP) scheme of JSDM.
Data Types: double | cell
Complex Number Support: Yes
ns - Number of data streams
$G$-element row vector (default) | 1-by-G cell array
Number of data streams, specified as a $G$-element row vector or a 1-by- $G$ cell array.

- If ns is a vector, each element specifies the total number of data streams in the corresponding user group.
- If $n s$ is a cell array, each element in the cell array is a $K_{g}$-element row vector where $K_{g}$ is the number of users in the $g^{\text {th }}$ group. The elements in the $K_{g}$-element row vector specifies the number of receiving data streams for each user in that group.

Data Types: double | cell
wprf - RF precoding weights
1-by-G cell array
RF precoding weights, specified as an 1-by- $G$ cell array. The $g^{\text {th }}$ element in wprf is an $N \operatorname{trf}(g)$-by- $N t$ matrix that maps $N \operatorname{trf}(g) \mathrm{RF}$ chain to $N t$ antennas in the base station. $N \operatorname{trf}(g)$ is the number of RF chains dedicated to the $g^{\text {th }}$ group.

```
Data Types: cell | double
Complex Number Support: Yes
alpha - Regularization factor
0 (default) | nonnegative scalar
```

Regularization factor, specified as a nonnegative scalar. Units are dimensionless.
Data Types: double

## Output Arguments

## wpbb - Baseband precoding weights

Nsc-by-TotalNS-by-TotalNtrf array | 1-by-G cell array
Baseband precoding weights, returned as a complex-valued Nsc-by-TotalNS-by-TotalNtrf array or 1-by-G cell array.

- If chaneff is not a cell array, wpbb is an Nsc-by-TotalNS-by-TotalNtrf array.
- If chaneff is a cell array, then wpbb is a 1-by- $G$ cell array whose $g^{\text {th }}$ element is either an Nsc-by$N s(g)$-by- $N \operatorname{trf}(g)$ array when ns is a vector or an $N s c$-by-sum $(N S\{g\})$-by- $N \operatorname{trf}(g)$ array when ns is a cell array.


## wc - Recombining weights

1-by-G cell array
Recombining weights for each user, returned as a 1-by-G cell array. The structure of wc depends on the ns input argument.

- If ns is a vector, each cell in wc is an $N s c$-by- $N S(g)$-by- $N S(g)$ array.
- If ns is a cell array, then $\mathrm{wc}(g)$ is a 1 -by- $K_{\mathrm{g}}$ cell array where $K_{\mathrm{g}}$ is the number of users in the $g^{\text {th }}$ user group. Within the $K_{g}$-element cell array, each entry is an $N s c$-by-sum( $N s\{g\}$ )-by- $N s\{g\}(k)$ array where $N s\{g\}(k)$ is the number of data streams for the $k^{\text {th }}$ user in the $g^{\text {th }}$ user group.


## Version History

## Introduced in R2023a

## References

[1] Adhikary A., J. Nam, J-Y Ahn, and G. Caire. "Joint Spatial Division and Multiplexing - The LargeScale Array Regime." IEEE Transactions on Information Theory, Vol. 59, No. 10, October 2013, pp. 6441-6463.

## See Also

jsdmrfweights|blkdiagbfweights|omphybweights

## Topics

"Massive MIMO Hybrid Beamforming"

## jsdmrfweights

Create RF precoding weights

## Syntax

wprf = jsdmrfweights(hcov,ns)
wprf = jsdmrfweights(hcov,ns,ntrf)

## Description

wprf = jsdmrfweights(hcov,ns) returns the RF precoding weights, wprf, for the channel covariance matrix, hcov, to achieve orthogonality among users by Joint Spatial Division Multiplexing (JSDM). JSDM uses RF precoding weights to divide users into groups by their location information. The RF precoding weights, wprf, beamform the transmitted signal into each group.
wprf = jsdmrfweights(hcov,ns,ntrf) also specifies the desired number of RF chains ntrf.

## Examples

## Find JSDM RF Precoding Weights

Find RF precoding weights for a JSDM beamformer based on a base station with a 64 -element linear antenna array. Assume there are two user groups. The first group has two users and the second group has three users. Array elements are $1 / 2$ wavelength apart.

Set the number of array elements to 64 .

```
Nt = 64;
```

Find the array steering weights in the direction of the first user group. The user group is centered at $+10^{\circ}$ azimuth.

```
v1 = steervec((0:Nt-1)*0.5,[9 11]);
rcl = v1*v1';
```

Find the array steering weights in the direction of the second user group. The user group is centered $-5^{\circ}$ azimuth.

```
v2 = steervec((0:Nt-1)*0.5,[-4 -5 -6]);
rc2 = v2*v2';
```

Then, compute the RF weights from the channel covariance matrix.

```
hcov = {rc1,rc2};
wprf = jsdmrfweights(hcov,[2 3]);
```

Verify the orthogonality between the two user groups.

```
snr1 = pow2db(real(trace(wprf{1}*rc1*wprf{1}'))/real(trace(wprf{1}*rc2*wprf{1}')))
snr1 = 26.1255
```

```
snr2 = pow2db(real(trace(wprf{2}*rc2*wprf{2}'))/real(trace(wprf{2}*rc1*wprf{2}')))
snr2 = 26.1632
```


## Input Arguments

## hcov - Channel covariance matrix

1-by-G cell array
Channel covariance matrix, specified as 1-by- $G$ cell array where $G$ is the number of groups. Each cell in hcov an $N_{\mathrm{t}}$-by- $N_{\mathrm{t}}$ matrix representing the covariance of the channel between the base station and the corresponding group of the users. $N_{\mathrm{t}}$ is the number of elements in the base station array. Assume that hcov is the same for all users in the corresponding group across all subcarriers.
hcov for the $g^{\text {th }}$ user group is defined as the expected value of $H^{*} H^{\prime}$, where $H$ is an $N_{\mathrm{t}}$-by- $N_{\mathrm{r}}(g)$ matrix representing the instantaneous channel for that user group. $N_{\mathrm{r}}(g)$ is the number of receiving elements in the $g^{\text {th }}$ group.
Data Types: double
Complex Number Support: Yes
ns - Number of data streams
$G$-element row vector | 1 -by- $G$ cell array
Number of data streams, specified as a $G$-element row vector or a 1-by- $G$ cell array.

- If ns is a vector, each element specifies the total number of data streams in the corresponding user group.
- If ns is a cell array, each element in the cell array is a $K_{\mathrm{g}}$-element row vector where $K_{\mathrm{g}}$ is the number of users in the $g^{\text {th }}$ group. The elements in $K_{g}$-element row vector specify the number of receiving data streams for each user in that group.

This function assumes that the number of receiving elements in the $g^{\text {th }}$ user group, $N_{\mathrm{r}}(g)$, matches the total number of data streams for that group.
Data Types: double

## ntrf - Desired number of RF chains

number of data streams per group (default) | 1-by-G integer vector
Desired number of RF chains for each group, specified as a 1-by-G integer vector. Note that if nrtf is specified, then the dimension of wprf $(g)$ becomes $\operatorname{nrtf}(g)$-by- $N_{\mathrm{t}}$.

Data Types: double

## Output Arguments

## wprf - RF precoding weights

1-by-G cell array
RF precoding weights for the channel covariance matrix, returned as a 1-by-G cell array.

- When $n s$ is a vector, each cell in wprf is an $n s(g)$-by- $N_{\mathrm{t}}$ matrix that maps the $\mathrm{ns}(\mathrm{g}) \mathrm{RF}$ chain to $N t$ antennas in the base station.
- When $n s$ is a cell array, each cell in wprf is a $\operatorname{sum}(N S\{g\})$-by- $N t$ matrix that maps the total number of RF chains in the $g^{\text {th }}$ group to $N t$ antennas in the base station.


## Version History

## Introduced in R2023a

## References

[1] Adhikary A., J. Nam, J-Y Ahn, and G. Caire. "Joint Spatial Division and Multiplexing - The LargeScale Array Regime." IEEE Transactions on Information Theory, Vol. 59, No. 10, October 2013, pp. 6441-6463.

## See Also

jsdmbbweights|blkdiagbfweights|omphybweights

## Topics

"Massive MIMO Hybrid Beamforming"

## blkdiagbfweights

MIMO channel block diagonalized weights

## Syntax

[wp,wc] = blkdiagbfweights(chanmat,ns)
[wp,wc] = blkdiagbfweights(chanmat,ns,pt)

## Description

[wp,wc] = blkdiagbfweights(chanmat,ns) returns precoding weights, wp, and combining weights, wc, derived from the channel response matrices contained in a MATLAB cell array chanmat.

- You can specify multiple user channels by putting each channel in a chanmat cell. chanmat \{k\} represents the $k^{\text {th }}$ channel from the transmitter to the user.
- For a single frequency, specify the channel cell as a matrix.
- For multiple frequencies, specify the channel cell as a three-dimensional array where the rows represent different subcarriers.
- Specify multiple subchannels per channel using the ns argument. Subchannels represent different data streams. ns specifies the number of subchannels for each user channel. Multiply the data streams by the precoding weights, wp.

The precoding and combining weights diagonalize the channel into independent subchannels so that for the $k^{\text {th }}$ user, the matrix wp*chanmat $\{\mathrm{k}\}^{*} \mathrm{wc}\{\mathrm{k}\}$ is diagonal for each subcarrier.
[wp,wc] = blkdiagbfweights(chanmat,ns,pt) also specifies the total transmitted power, pt, per subcarrier.

## Examples

## Spatial Multiplexing with Block Diagonal Weights

Start with a base station consisting of a uniform linear array (ULA) with 16 antennas, and two users having receiver ULA arrays with 8 and 4 antennas, respectively. Show that using block diagonalization-based precoding and combining weights achieves spatial multiplexing, where the received signal at each user can be decoded without interference from the other user. Specify two data streams for each user.

Specify the transmitter location in txpos and two user receiver locations in rxpos1 and rxpos2. Array elements are spaced one-half wavelength apart.

```
txpos = (0:15)*0.5;
rxpos1 = (0:7)*0.5;
rxpos2 = (0:3)*0.5;
```

Create the channel matrix cell array using scatteringchanmtx and then compute the beamforming weights wp and wc. Each channel corresponds to a user. Assume that the channels have 10 scatterers. Each channel has two subchannels specified by the vector ns.

```
chanmat = {scatteringchanmtx(txpos,rxpos1,10), ...
    scatteringchanmtx(txpos,rxpos2,10)};
ns = [2 2];
[wp,wc] = blkdiagbfweights(chanmat,ns);
```

The weights diagonalize the channel matrices for each user.
For channel 1:

```
disp(wp*chanmat{1}*wc{1})
8.2269 - 0.0000i 0.0000 - 0.0000i
0.0000 + 0.0000i 6.1371 - 0.0000i
0.0000 - 0.0000i -0.0000 + 0.0000i
0.0000 - 0.0000i 0.0000 + 0.0000i
```

For channel 2:

```
disp(wp*chanmat{2}*wc{2})
\begin{tabular}{rr}
\(-0.0000+0.0000 i\) & \(-0.0000+0.0000 i\) \\
\(-0.0000+0.0000 i\) & \(-0.0000+0.0000 i\) \\
\(8.7543-0.0000 i\) & \(0.0000-0.0000 i\) \\
\(0.0000+0.0000 i\) & \(4.4372+0.0000 i\)
\end{tabular}
```

First create four subchannels to carry the data streams: two subchannels per channel. Each data stream contains 20 samples of $\pm 1$. Precode the input streams and combine the streams to produce the recovered signals.

```
x = 2*round(rand([20,4])) - 1;
xp = x*wp;
y1 = xp*chanmat{1} + 0.1*randn(20,8);
y2 = xp*chanmat{2} + 0.1*randn(20,4);
y = [y1*wc{1},y2*wc{2}];
```

Overlay stem plots of the input and recovered signals to show that the received user signals are the same as the transmitted signals.

```
for m = 1:4
    subplot(4,1,m)
    s = stem([x(:,m) 2*((real(y(:,m)) > 0) - 0.5)]);
    s(1).LineWidth = 2;
    s(2).MarkerEdgeColor = 'none';
    s(2).MarkerFaceColor = 'r';
    ylabel('Signal')
    title(sprintf('User %d Stream %d',ceil(m/2),rem(m-1,2) + 1))
    if m==1
        legend('Input','Recovered','Location','best')
    end
end
xlabel('Samples')
```



## Spatial Multiplexing with Specified Power

Start with a base station consisting of a uniform linear array (ULA) with 16 antennas, and two users having receiver ULA arrays with 8 and 5 antennas, respectively. Show how to use three-dimensional arrays of channel matrices to handle two subcarriers. Then, the channel matrix for the first user takes the form 2-by-16-by-8 and the channel matrix for the second user takes the form 2-by-16-by-5. Also assume that there are two data streams for each user.

Specify the transmitter location in txpos and two user receiver locations in rxpos1 and rxpos2. Array elements are spaced one-half wavelength apart.

```
nr1 = 8;
nr2 = 5;
txpos = (0:15)*0.5;
rxpos1 = (0:(nr1-1))*0.5;
rxpos2 = (0:(nr2-1))*0.5;
```

Create the channel matrices using scatteringchanmtx and put them in a cell array. To create a second subchannel for each receiver, duplicate each channel matrix. Assume 10 point scatterers in computing the channel matrix.

```
smtmp1 = scatteringchanmtx(txpos,rxpos1,10);
smtmp2 = scatteringchanmtx(txpos,rxpos2,10);
sm1 = zeros(2,16,8);
```

```
sm2 = zeros(2,16,5);
sm1(1,:,:) = smtmp1;
sm1(2,:,:) = smtmpl;
sm2(1,:,:) = smtmp2;
sm2(2,:,:) = smtmp2;
chanmat = {sm1,sm2};
```

Specify that there are two data streams for each user.
ns = [2 2];
Specify the transmitted powers for each subcarrier.

```
pt = [1.0 1.5];
```

Compute the beamforming weights.

```
[wp,wc] = blkdiagbfweights(chanmat,ns,pt);
```

Show that the channels are diagonalized for the first subcarrier.

```
ksubcr = 1;
wpx = squeeze(wp(ksubcr,:,:));
chanmat1 = squeeze(chanmat{1}(ksubcr,:,:));
chanmat2 = squeeze(chanmat{2}(ksubcr,:,:));
wc1 = squeeze(wc{1}(ksubcr,:,:));
wc2 = squeeze(wc{2}(ksubcr,:,:));
wpx*chanmat1*wcl
ans = 4×2 complex
    8.2104 + 0.0000i -0.0000 - 0.0000i
    0.0000 - 0.0000i 5.9732 - 0.0000i
    0.0000 - 0.0000i -0.0000 - 0.0000i
    0.0000 - 0.0000i 0.0000 - 0.0000i
```

wpx*chanmat2*wc2
ans $=4 \times 2$ complex
$-0.0000+0.0000 i \quad 0.0000+0.0000 i$
$-0.0000+0.0000 i \quad 0.0000+0.0000 i$
$8.8122+0.0000 i-0.0000+0.0000 i$
$0.0000+0.0000 i \quad 4.8186-0.0000 i$

Propagate the signals to each user and then decode. Generate four streams of random data containing -1 's and +1 's and having two columns for each user. Each stream is a subchannel.

```
x = 2*(round(rand([20 4]))) - 1;
```

Precode the data streams.

```
xp = x*wpx;
```

$y 1=x p *$ chanmat1 $+0.1 *$ randn $(20,8)$;
$y 2=x p *$ chanmat2 $+0.1 *$ randn $(20,5)$;

Decode the data streams.
$y=[y 1 * w c 1, y 2 * w c 2] ;$
Overlay stem plots of the input and recovered signals to show that the received user signals are the same as the transmitted signals.

```
for m = 1:4
    subplot(4,1,m)
    s = stem([x(:,m) 2*((real(y(:,m)) > 0) - 0.5)]);
    s(1).LineWidth = 2;
    s(2).MarkerEdgeColor = 'none';
    s(2).MarkerFaceColor = 'r';
    ylabel('Signal')
    title(sprintf('User %d Stream %d',ceil(m/2),rem(m-1,2) + 1))
    if m==1
        legend('Input','Recovered','Location','best')
    end
end
xlabel('Samples')
```



## Input Arguments

## chanmat - Channel response matrices

$N_{\mathrm{u}}$-element cell array
Channel response matrices, specified as an $N_{\mathrm{u}}$-element cell array. $N_{\mathrm{u}}$ is the number of receive arrays. Each cell corresponds to a different channel and contains a channel response matrix or a three
dimensional MATLAB array. The cell array must contain either all matrices or all arrays. For matrices, the number of rows for all matrices must be the same. For three-dimensional arrays, the number of rows and columns must be the same.

- If the $k^{\text {th }}$ cell is a matrix, the matrix has the size $N_{\mathrm{t}}-\mathrm{by}-\mathrm{N}_{\mathrm{r}}(k)$. $N_{\mathrm{t}}$ is the number of elements in the transmitting array and $N_{\mathrm{r}}(k)$ is the number of elements in the $k^{\text {th }}$ receiving array.
- If the $k^{\text {th }}$ cell is an array, the array has the size $L$-by- $N_{\mathrm{t}}$-by- $N_{\mathrm{r}}(k) . L$ is the number of subcarriers. $N_{\mathrm{t}}$ is the number of elements in the transmit array and $N_{\mathrm{r}}(k)$ is the number of elements in the $k^{\mathrm{th}}$ receive array.


## Data Types: double

Complex Number Support: Yes

## ns - Number of data streams per receive array

$N_{\mathrm{u}}$-element row vector of positive integers
Number of data streams per receive array, specified as an $N_{\mathrm{u}}$-element row vector of positive integers. $N_{\mathrm{u}}$ is the number of receive arrays.
Data Types: double

## pt - Total transmitted power per subcarrier

1 (default) | positive scalar | $L$-element vector of positive values
Total transmitted power per subcarrier, specified as a positive scalar or an $L$-element vector of positive values. $L$ is the number of subcarriers. If pt is a scalar, all subcarriers have the same transmitted power. If pt is a vector, each vector element specifies the transmitted power for the corresponding subcarrier. Power is in linear units.

## Data Types: double

## Output Arguments

## wp - Precoding weights

complex-valued $N_{\text {st }}$-by- $N_{\mathrm{t}}$ matrix | complex-valued $L$-by- $N_{\mathrm{st}}$-by- $N_{\mathrm{t}}$ MATLAB array
Precoding weights, returned as a complex-valued $N_{\mathrm{st}}$-by- $N_{\mathrm{t}}$ matrix or a complex-valued $L$-by- $N_{\mathrm{st}}$-by- $N_{\mathrm{t}}$ MATLAB array.

- If chanmat contains matrices, wp is a complex-valued $N_{\mathrm{st}}$-by- $N_{\mathrm{t}}$ matrix where $N_{\mathrm{st}}$ is the total number of data channels (sum(ns)).
- If chanmat contains three-dimensional MATLAB arrays, wp is a complex-valued $L$-by- $N_{s t}$-by- $N_{\mathrm{t}}$ MATLAB array where $N_{\text {st }}$ is the total number of data channels (sum(ns)).

Units are dimensionless.
Data Types: double
wc - Combining weights
$N_{\mathrm{u}}$-element cell array
Combining weights, returned as an $N_{\mathrm{u}}$-element cell array. Units are dimensionless.

- If chanmat contains matrices, the $k^{\text {th }}$ cell in wc contains a complex valued $N_{\mathrm{r}}(k)$-by- $N_{\mathrm{s}}(k)$ matrix. $N_{\mathrm{s}}(k)$ is the value of the argument ns for the $k^{\text {th }}$ receive array.
- If chanmat contains three-dimensional MATLAB arrays, the $k^{\text {th }}$ cell of wc contains a complexvalued $L$-by- $N_{\mathrm{r}}(k)$-by- $N_{\mathrm{s}}(k)$ MATLAB array. $N_{\mathrm{s}}(k)$ is the value of the $k^{\text {th }}$ entry of the ns vector.

Data Types: double

## Version History

## Introduced in R2020a

## References

[1] Heath, Robert W., et al. "An Overview of Signal Processing Techniques for Millimeter Wave MIMO Systems." IEEE Journal of Selected Topics in Signal Processing, vol. 10, no. 3, Apr. 2016, pp. 436-53. DOI.org (Crossref), doi:10.1109/JSTSP.2016.2523924. Bibliography
[2] Tse, D. and P. Viswanath, Fundamentals of Wireless Communications, Cambridge: Cambridge University Press, 2005.
[3] Paulraj, A. Introduction to Space-Time Wireless Communications, Cambridge: Cambridge University Press, 2003.
[4] Spencer, Q.H., et al. "Zero-Forcing Methods for Downlink Spatial Multiplexing in Multiuser MIMO Channels." IEEE Transactions on Signal Processing, Vol. 52, No. 2, February 2004, pp. 461-471. DOI.org (Crossref), doi:10.1109/TSP.2003.821107.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\text {TM }}$.
Usage notes and limitations:

- Does not support variable-size inputs.


## See Also

## Functions

diagbfweights|scatteringchanmtx|waterfill
Objects
phased.ScatteringMIMOChannel

## broadside2az

Convert broadside angle to azimuth angle

## Syntax

az = broadside2az(bsang)
$a z=b r o a d s i d e 2 a z(b s a n g, e l)$

## Description

az = broadside2az(bsang) returns the azimuth angle on page 2-84, az, corresponding to the broadside angle, bsang, for zero elevation angle. Angles are defined with respect to the local coordinate system.
$a z=b r o a d s i d e 2 a z(b s a n g, e l)$ also specifies the elevation angle, el.

## Examples

## Convert Broadside Angle to Azimuth Angle at Zero Elevation

Return the azimuth angle corresponding to a broadside angle of $45^{\circ}$ at $0^{\circ}$ elevation.

```
az = broadside2az(45.0)
az = 45.0000
```


## Convert Broadside Angle to Azimuth Angle

Return the azimuth angle corresponding to a broadside angle of $45^{\circ}$ and an elevation angle of $20^{\circ}$.
$\mathrm{az}=$ broadside2az $(45,20)$
$a z=48.8063$

## Convert Multiple Broadside Angles to Azimuth Angles

Return azimuth angles for 10 pairs of broadside angle and elevation angle.
BSang $=(45: 5: 90){ }^{\prime}$;
el = (45:-5:0)';
az = broadside2az(BSang,el);

## Input Arguments

## bsang - Broadside angle

scalar | vector of real values
Broadside angle, specified as a scalar or vector of real values. Units are in degrees. This argument supports single and double precision.
Example: [10;-22;-80]

## el - Elevation angle

0 (default) | scalar | vector of real values
Elevation angle, specified as a scalar or vector of real values. The length of el must match the length of bsang. Elevation angles lie in the range from $-90^{\circ}$ to $90^{\circ}$. Units are in degrees. This argument supports single and double precision.

Example: [5;2;-1]

## Output Arguments

## az - Azimuth angle

scalar | vector of real values
Azimuth angle, returned as a scalar or vector of real values. The length of azequals the length of bsang. Azimuth angles lie in the range from $-180^{\circ}$ to $180^{\circ}$. Units are in degrees.

## More About

## Broadside Angle

Broadside angles are useful in describing the response pattern of a uniform linear array (ULA).
For the definition of the broadside angle and how to convert between azimuth and elevation, and broadside angle see "Broadside Angles". For definitions of the azimuth and elevation angles, see "Azimuth and Elevation Angles".

## Version History

Introduced in R2011a

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{Tm}}$.
Usage notes and limitations:
Does not support variable-size inputs.

## See Also

az2broadside | uv2azel | phitheta2azel

## bw2range

Convert bandwidth to range resolution

## Syntax

rngres = bw2range(bw)
rngres = bw2range(bw, c)

## Description

Note The use of bw2range is not recommended. Use bw2rangeres instead.
rngres = bw2 range (bw) returns the range resolution of a signal corresponding to its bandwidth. Range resolution gives you the minimum range difference needed to distinguish two targets. The function applies to two-way propagation, as in a monostatic radar system.
rngres $=\mathrm{b} w 2$ range $(\mathrm{bw}, \mathrm{c})$ also specifies the signal propagation speed, c .

## Input Arguments

bw - Signal bandwidth
positive scalar | MATLAB array of positive real values
Signal bandwidth, specified as any array of array of positive real values. Units are in hertz.

## c - Signal propagation speed

speed of light (default) | positive scalar
Signal propagation speed, specified as a positive scalar. The default value is the output of physconst('LightSpeed'). Units are in meters per second.
Data Types: double

## Output Arguments

## rngres - Target range resolution

positive scalar | MATLAB array of positive real values
Target range resolution, returned as a scalar or MATLAB array of positive real numbers. The dimensions of rngres are the same as those of bw. Units are in meters.
Data Types: double

## Tips

- This function assumes two-way propagation. For one-way propagation, you can find the required range resolution by multiplying the output of this function by 2 .


## Algorithms

The function computes range resolution from rngres $=c /\left(2^{*} b w\right)$.

## Version History

Introduced in R2017a

## References

[1] Skolnik, M. Introduction to Radar Systems, 3rd Ed. New York: McGraw-Hill, 2001.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\text {TM }}$.
Usage notes and limitations:
Does not support variable-size inputs.

## See Also

time2range | range2bw | range2time | phased. FMCWWaveform
Topics
"Automotive Adaptive Cruise Control Using FMCW Technology" (Radar Toolbox)

## bw2rangeres

Convert bandwidth to range resolution

## Syntax

```
rangeres = bw2rangeres(bw)
rangeres = bw2rangeres(bw,c)
rangeres = bw2rangeres(___,'RangeBroadening',rb)
```


## Description

rangeres $=\mathrm{bw} 2$ rangeres ( bw ) returns the range resolution rangeres corresponding to the signal bandwidth bw. Range resolution gives the minimum range difference needed to distinguish two targets. The propagation is assumed to be two-way, as in a monostatic radar system.
rangeres $=\mathrm{bw} 2$ rangeres $(\mathrm{bw}, \mathrm{c})$ also specifies the signal propagation speed c .
rangeres = bw2rangeres( __ , 'RangeBroadening', rb) also specifies the range broadening factor rb .

## Examples

## Compute Range Resolution from Bandwidth

Assume you have a monostatic radar system that uses a rectangular waveform. Calculate the range resolution obtained using a signal bandwidth of 20 MHz .

```
bw = 20e6;
rngres = bw2rangeres(bw)
rngres = 7.4948
```


## Compute Sonar Range Resolution from Bandwidth

Calculate the range resolution of a two-way sonar system that uses a rectangular waveform. The signal bandwidth is 2 kHz . The speed of sound is $1520 \mathrm{~m} / \mathrm{s}$.

```
bw = 2e3;
c = 1520.0;
rngres = bw2rangeres(bw,c)
rngres = 0.3800
```


## Compute Range Resolution from Bandwidth with Range Broadening

Assume a monostatic radar system that uses a rectangular waveform. Calculate the range resolution for two signals with bandwidths of 10 and 20 MHz . Use a range broadening factor of 2.0.
bw = [10e6,20e6];
c = physconst('Lightspeed');
rngres $=$ bw2rangeres(bw,c,'RangeBroadening',2.0)
rngres $=1 \times 2$
$29.9792 \quad 14.9896$

## Input Arguments

## bw - Signal bandwidth

positive scalar
Signal bandwidth, specified as a positive scalar. Units are in Hz .
Example: 300e6
Data Types: double
c - Signal propagation speed
speed of light (default) | positive scalar
Signal propagation speed, specified as a positive scalar. Units are in $\mathrm{m} / \mathrm{s}$.
Example: 3.0e8
Data Types: double
rb - Range impulse broadening factor
1.0 (default) | real positive scalar

Range impulse broadening factor, specified as a real scalar. Range broadening occurs due to data weighting or windowing for side lobe control. Range broadening is the ratio of the actual -3 dB main lobe width with respect to the nominal width. Typical window functions such as hamming or hann exhibit range broadening in the range of 1 to 1.5 .
Example: 2.0
Data Types: double

## Output Arguments

## rangeres - Range resolution

positive scalar
Signal range resolution, returned as a positive scalar. Units are in meters.

## Algorithms

The range resolution (in meters) for a rectangular pulse of bandwidth $b w$ is $c /(b w \times 2)$, where $c$ is the propagation speed. The range resolution broadening factor $b$ yields a range resolution of $(c \times b) /(b w$ $\times 2$ ).

## Version History

Introduced in R2021a

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.

## See Also

rangeres2bw

## wavelen2freq

Convert wavelength to frequency

## Syntax

```
freq = wavelen2freq(wavelen)
freq = wavelen2freq(wavelen,c)
[freq,c] = wavelen2freq(
```

$\qquad$

## Description

freq = wavelen2freq(wavelen) converts wavelength wavelen to frequency freq using the speed of light in vacuum.
freq = wavelen2freq(wavelen,c) also specifies the signal propagation speed c .
[freq, c] = wavelen2freq( ___) also returns the propagation speed c used to compute frequency freq. Use this syntax with any of the input arguments in previous syntaxes.

## Examples

## Calculate Frequencies for Different Wavelengths

Calculate the frequencies corresponding to wavelengths of 1 and 4 cm . Use the default speed of propagation.

```
wavelen = [1e-2,4e-2];
freq = wavelen2freq(wavelen)
freq = 1\times2
1010 }
    2.9979 0.7495
```


## Obtain Propagation Speed Used for Frequency Conversion

Calculate the frequency corresponding to a wavelength of 2 cm . Obtain the propagation speed used to compute the frequency.

```
wavelen = 0.02;
[freq,c] = wavelen2freq(wavelen,3.0e8)
freq = 1.5000e+10
c = 300000000
```


## Input Arguments

## wavelen - Signal wavelength

positive scalar | length- $M$ vector of positive values
Signal wavelength, specified as a positive scalar or length- $M$ vector of positive values. Units are in meters.

## c - Signal propagation speed

speed of light in vacuum (default) | positive scalar
Signal propagation speed, specified as a positive scalar. The default value is obtained from physconst('Lightspeed'). Units are in m/s.
Example: 3.0e8
Data Types: double

## Output Arguments

## freq - Signal frequencies

positive scalar | length- $M$ vector of positive values
Signal frequency, specified as a positive scalar or a length- $M$ vector of positive values. The size of freq equals the size of wavelen. Units are in Hz .
Example: 10e6
Data Types: double
c - Signal propagation speed
speed of light in vacuum (default) | positive scalar
Signal propagation speed, returned as a positive scalar. Units are in m/s.
Data Types: double

## Version History

Introduced in R2021a

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\text {TM }}$.

## See Also

freq2wavelen

## freq2wavelen

Convert frequency to wavelength

## Syntax

```
wavelen = freq2wavelen(freq)
wavelen = freq2wavelen(freq,c)
[wavelen,c] = freq2wavelen(___)
```


## Description

wavelen = freq2wavelen(freq) converts the frequency freq to the wavelength wavelen using the speed of light in a vacuum.
wavelen $=$ freq2wavelen (freq, c) also specifies the signal propagation speed c.
[wavelen,c] = freq2wavelen( $\qquad$ ) also returns the propagation speed c used to compute wavelength wavelen.

## Examples

## Calculate Wavelengths for Different Frequencies

Calculate the wavelengths corresponding to frequencies of 3 and 4 GHz . Use the default speed of propagation.

```
freq = [3e9,4e9];
lambda = freq2wavelen(freq)
lambda = 1\times2
    0.0999 0.0749
```


## Obtain Propagation Speed Used for Wavelength Conversion

Calculate the wavelength corresponding to a frequency of 4 GHz . Obtain the propagation speed used to compute the wavelength.
freq $=4 e 9$;
[lambda, c] = freq2wavelen(freq,3.0e8)
lambda $=0.0750$
c $=300000000$

## Input Arguments

## freq - Signal frequencies

positive scalar | length- $M$ vector of positive values
Signal frequency, specified as a positive scalar or a length- $M$ vector of positive values. Units are in Hz.

Example: 10e6
Data Types: double
c - Signal propagation speed
speed of light in vacuum (default) | positive scalar
Signal propagation speed, specified as a positive scalar. The default value is obtained from physconst('Lightspeed'). Units are in m/s.

Example: 3.0e8
Data Types: double

## Output Arguments

## wavelen - Signal wavelength

positive scalar | length- $M$ vector of positive values
Signal wavelength, returned as a positive scalar or length- $M$ vector of positive values. The size of wavelen equals the size of freq. Units are in meters.

## c - Signal propagation speed positive scalar

Signal propagation speed, returned as a positive scalar. Units are in $\mathrm{m} / \mathrm{s}$.
Data Types: double

## Version History

Introduced in R2021a

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

wavelen2freq

## rangeres2bw

Convert range resolution to bandwidth

## Syntax

```
bw = rangeres2bw(rangeres)
bw = rangeres2bw(rangeres,c)
bw = rangeres2bw(
```

$\qquad$

``` , 'RangeBroadening' , rb)
```


## Description

bw = rangeres2bw(rangeres) returns the signal bandwidth bw corresponding to the range resolution rangeres. Signal bandwidth gives the maximum bandwidth needed to distinguish two targets in range. The propagation is assumed to be two-way, as in a monostatic radar system.
bw = rangeres2bw(rangeres,c) also specifies the signal propagation speed c.
bw = rangeres2bw( $\qquad$ , 'RangeBroadening ' ,rb) also specifies the range broadening factor rb.

## Examples

## Compute Bandwidth from Range Resolution

Assume you have a monostatic radar system that uses a rectangular waveform. Calculate the signal bandwidth needed to obtain a range resolution of 25 m . Use the default speed of light.

```
rangeres = 25.0;
bw = rangeres2bw(rangeres)
bw = 5.9958e+06
```


## Compute Sonar Bandwidth from Range Resolution

Calculate the bandwidth of a two-way sonar system that uses a rectangular waveform. The desired range resolution is one meter. The speed of sound is $1520 \mathrm{~m} / \mathrm{s}$.

```
rangeres = 1;
c = 1520.0;
bw = rangeres2bw(rangeres,c)
bw = 760
```


## Compute Bandwidth from Range Resolution with Range Broadening

Assume a monostatic radar system that uses a rectangular waveform. Calculate the bandwidths of two signals with range resolutions of 1 and 10 meters. The range broadening factor is 2.0.

```
res = [1.0,10.0];
```

c = physconst('Lightspeed');
bw = rangeres2bw(res,c,'RangeBroadening',2.0)
$\mathrm{bw}=1 \times 2$
$10^{8} \times$
2.99790 .2998

## Input Arguments

rangeres - Range resolution
positive scalar
Range resolution, specified as a positive scalar. Units are in meters.

## c - Signal propagation speed

speed of light (default) | positive scalar
Signal propagation speed, specified as a positive scalar. Units are in $\mathrm{m} / \mathrm{s}$.
Example: 3.0e8
Data Types: double
rb - Range impulse broadening factor
1.0 (default) | real positive scalar

Range impulse broadening factor, specified as a real scalar. Range broadening occurs due to data weighting or windowing for side lobe control. Range broadening is the ratio of the actual -3 dB main lobe width with respect to the nominal width. Typical window functions such as hamming or hann exhibit range broadening in the range of 1 to 1.5 .

Example: 2.0
Data Types: double

## Output Arguments

## bw - Signal bandwidth

positive scalar
Signal bandwidth, returned as a positive scalar. Units are in Hz .
Example: 300e6
Data Types: double

## Algorithms

The range resolution (in meters) for a rectangular pulse of bandwidth, $b w$, is $c / b w / 2$, where $c$ is the propagation speed. Using the range resolution broadening factor $b$ yields a range resolution of $c b / b w / 2$.

## Version History

Introduced in R2021a

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

bw2rangeres

## ap2beamwidth

Compute half-power beamwidth from aperture length

## Syntax

rlhpbw = ap2beamwidth(d,lambda)
rlhpbw = ap2beamwidth(d,lambda,azb)

## Description

rlhpbw = ap2beamwidth(d,lambda) computes the half-power, one-way beamwidth,rlhpbw for a real aperture. The quantity $d$ specifies the length of an unweighted antenna and lambda specifies the radar wavelength.
rlhpbw = ap2beamwidth(d,lambda,azb) also specifies the azimuth impulse broadening factor azb.

## Examples

## Compute Beamwidths of Multiple Antennas

Estimate the half-power beamwidths of side-looking airborne radars, each operating at wavelengths of 1,2 , and 3 centimeters. The radars have antenna aperture sizes of 2 and 3 meters in the azimuth direction.

```
lambda = [1,2,3]*1e-2;
daz = [2,3];
hpbw = ap2beamwidth(daz,lambda)
hpbw = 2×3
    0.2865 0.5730 0.8594
    0.1910 0.3820 0.5730
```


## Compute Beamwidth of Antenna with Azimuth Broadening

Estimate the half-power beamwidth of a radar operating at a wavelength of 2 cm . The radar has an antenna aperture dimension of 2 m in the azimuth direction. Use an azimuth broadening factor of 1.5.

```
lambda = 2e-2;
daz = 2;
azbf = 1.5;
hpbw = ap2beamwidth(daz,lambda,azbf)
hpbw = 0.8594
```


## Input Arguments

d - Length of unweighted antenna
positive scalar | length-J vector of positive values
Length of unweighted antenna, specified as a positive scalar or length- $J$ vector of positive values. Units are in meters.

Example: [3,4][
Data Types: double
lambda - Radar wavelength
positive real scalar | length-K vector of real values
Radar wavelength, specified as a positive real scalar or a length- $K$ vector of real values.
Example: 1.5
Data Types: double
azb - Azimuth impulse broadening factor
1.0 (default) | positive real scalar

Azimuth impulse broadening factor, specified as a positive real scalar. Broadening is due to data weighting or windowing for side lobe control. The quantity is the actual -3 dB main lobe width with respect to the nominal width. Typical window functions such as hamming or hann exhibit azimuth impulse broadening factors in the range of 1 to 1.5 .
Example: 1.2
Data Types: double

## Output Arguments

## rlhpbw - Half-power one-way beamwidth

positive scalar | J-by-K real-valued vector of positive values
Half-power one-way beamwidth, specified as a positive scalar or as a $J$-by- $K$ real-valued vector of positive values. Matrix rows correspond to the length of $d$ and columns correspond to the length of lambda. Units are in degrees.

## Algorithms

The half-power beamwidth (in degrees) for a rectangular aperture is $180 \lambda / \Pi d$ where $\lambda$ is the radar wavelength and $d$ is the aperture length. The azimuth broadening factor $b$ multiplies the beamwidth to produce a half-power beamwidth of $180 \mathrm{~b} \mathrm{\lambda} / \pi d$.

## Version History

## Introduced in R2021a

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

## See Also

beamwidth2ap

## beamwidth2ap

Computes aperture length of unweighted antenna from beamwidth

## Syntax

d = beamwidth2ap(hpbw,lambda)
d = beamwidth2ap(hpbw,lambda,azb)

## Description

$d$ = beamwidth2ap(hpbw, lambda) computes the aperture length $d$ of an unweighted antenna from its half-power one-way beamwidth hpbw. lambda specifies the radar wavelength.
$\mathrm{d}=$ beamwidth2ap(hpbw,lambda,azb) also specifies the azimuth impulse broadening factor azb.

## Examples

## Compute Aperture Length of Antenna from Beamwidth

Compute the aperture length of a radar from its half-power beamwidth. The radar is designed to operate at a wavelength of 2 centimeters. The radar has a half-power beamwidth of one degree. Use the default azimuth broadening factor.

```
lambda = 2e-2;
bw = 1;
aplen = beamwidth2ap(bw,lambda)
aplen = 1.1459
```


## Compute Aperture Lengths of Multiple Antennas from Beamwidths

Estimate the aperture lengths of two side-looking airborne radars operating at wavelengths of 1, 2, and 3 centimeters. The radars have beamwidths of 2 and 3 degrees in the azimuth dimension.

```
lambda = [1,2,3]*1e-2;
bw = [2,3];
aplen = beamwidth2ap(bw,lambda)
aplen = 2×3
    0.2865 0.5730 0.8594
    0.1910 0.3820 0.5730
```


## Compute Aperture Length of Antenna with Azimuth Broadening

Compute the aperture length of a radar operating at a wavelength of 2 centimeters. The radar has a beamwidth of 2 deg in the azimuth direction. Use an azimuth broadening factor of 1.5.

```
lambda = 2e-2;
bw = 2;
azbf = 1.5;
ap = beamwidth2ap(bw,lambda,azbf)
ap = 0.8594
```


## Compute Aperture Lengths of Rectangular Antenna

Estimate the aperture length of each side of a rectangular aperture antenna. The antenna operates at a wavelength of 10 cm . In this case, the input beamwidth array bw describes the two beamwidths of the same antenna. The radar has a half-power beamwidth of 1 degree along one dimension and a halfpower beamwidth of 2 degrees along the other.

```
bw = [1,2];
lambda = 0.01;
ap = beamwidth2ap(bw,lambda)
ap = 2×1
    0.5730
    0.2865
```


## Input Arguments

## hpbw - Half-power one-way beamwidth

positive scalar | J-by-K real-valued vector of positive values
Half-power one-way beamwidth, specified as a positive scalar or as a $J$-by- $K$ real-valued vector of positive values. Matrix rows correspond to the length of $d$ and columns correspond to the length of lambda. Units are in degrees.

## lambda - Radar wavelength

positive real scalar | length-K vector of real values
Radar wavelength, specified as a positive real scalar or a length- $K$ vector of real values.
Example: 1.5
Data Types: double

## azb - Azimuth impulse broadening factor

1.0 (default) | positive real scalar

Azimuth impulse broadening factor, specified as a positive real scalar due to data weighting or windowing for side lobe control. The quantity is the actual -3 dB main lobe width with respect to the nominal width. Typical window functions such as hamming or hann exhibit azimuth impulse broadening factors in the range of 1 to 1.5 .

Example: 1.2
Data Types: double

## Output Arguments

d - Length of unweighted antenna
positive scalar | length-J vector of positive values
Length of unweighted antenna, returned as a positive scalar or length-J vector of positive values. Units are in meters.

Example: [3.5,4.2]
Data Types: double

## Algorithms

The half-power beamwidth (in degrees) for a rectangular aperture is $180 \lambda / \pi d$ where $\lambda$ is the radar wavelength and $d$ is the aperture length. The azimuth broadening factor $b$ multiplies the beamwidth to produce a half-power beamwidth of $180 \mathrm{~b} \mathrm{\lambda} / \pi d$.

## Version History

Introduced in R2021b

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\text {TM }}$.

## See Also

ap2beamwidth

## cart2sphvec

Convert vector from Cartesian components to spherical representation

## Syntax

```
vs = cart2sphvec(vr,az,el)
```


## Description

$\mathrm{vs}=\mathrm{cart2sphvec}(\mathrm{vr}, \mathrm{az}, \mathrm{el})$ converts the components of a vector or set of vectors, vr , from their representation in a local Cartesian coordinate system to a spherical basis representation contained in vs. A spherical basis representation is the set of components of a vector projected into a basis given by ( $\widehat{\mathbf{e}}_{a z}, \widehat{\mathbf{e}}_{e l}, \widehat{\mathbf{e}}_{R}$ ). The orientation of a spherical basis depends upon its location on the sphere as determined by azimuth, az, and elevation, el.

## Examples

## Spherical Representation of Unit Z-Vector

Start with a vector in Cartesian coordinates pointing along the $z$-direction and located at $45^{\circ}$ azimuth, $45^{\circ}$ elevation. Compute its components with respect to the spherical basis at that point.

```
vr = [0;0;1];
vs = cart2sphvec(vr,45,45)
vs = 3\times1
```


## Input Arguments

## vr - Vector in Cartesian basis representation

3-by-1 column vector | 3-by-N matrix
Vector in Cartesian basis representation specified as a 3-by-1 column vector or 3-by-N matrix. Each column of $v r$ contains the three components of a vector in the right-handed Cartesian basis $x, y, x$.

## Example: [4.0; -3.5; 6.3]

Data Types: double
Complex Number Support: Yes

## az - Azimuth angle

scalar in range [-180,180]
Azimuth angle specified as a scalar in the closed range [-180,180]. Angle units are in degrees. To define the azimuth angle of a point on a sphere, construct a vector from the origin to the point. The
azimuth angle is the angle in the $x y$-plane from the positive $x$-axis to the vector's orthogonal projection into the $x y$-plane. As examples, zero azimuth angle and zero elevation angle specify a point on the $x$-axis while an azimuth angle of $90^{\circ}$ and an elevation angle of zero specify a point on the $y$ axis.
Example: 45
Data Types: double

## el - Elevation angle

scalar in range [-90,90]
Elevation angle specified as a scalar in the closed range [-90,90]. Angle units are in degrees. To define the elevation of a point on the sphere, construct a vector from the origin to the point. The elevation angle is the angle from its orthogonal projection into the $x y$-plane to the vector itself. As examples, zero elevation angle defines the equator of the sphere and $\pm 90^{\circ}$ elevation define the north and south poles, respectively.

Example: 30
Data Types: double

## Output Arguments

## vs - Vector in spherical basis

3-by-1 column vector | 3 -by-N matrix
Spherical representation of a vector returned as a 3-by-1 column vector or 3-by-N matrix having the same dimensions as vs. Each column of vs contains the three components of the vector in the righthanded ( $\widehat{\mathbf{e}}_{a z}, \widehat{\mathbf{e}}_{e l}, \widehat{\mathbf{e}}_{R}$ ) basis.

## More About

## Spherical basis representation of vectors

Spherical basis vectors are a local set of basis vectors which point along the radial and angular directions at any point in space.

The spherical basis is a set of three mutually orthogonal unit vectors ( $\widehat{\mathbf{e}}_{a z}, \widehat{\mathbf{e}}_{e l}, \widehat{\mathbf{e}}_{R}$ ) defined at a point on the sphere. The first unit vector points along lines of azimuth at constant radius and elevation. The second points along the lines of elevation at constant azimuth and radius. Both are tangent to the surface of the sphere. The third unit vector points radially outward.

The orientation of the basis changes from point to point on the sphere but is independent of $R$ so as you move out along the radius, the basis orientation stays the same. The following figure illustrates the orientation of the spherical basis vectors as a function of azimuth and elevation:


For any point on the sphere specified by $a z$ and $e l$, the basis vectors are given by:

$$
\begin{aligned}
& \widehat{\mathbf{e}}_{\mathbf{a z}}=-\sin (a z) \widehat{\mathbf{i}}+\cos (a z) \widehat{\mathbf{j}} \\
& \widehat{\mathbf{e}}_{\mathbf{e l}}=-\sin (e l) \cos (a z) \widehat{\mathbf{i}}-\sin (e l) \sin (a z) \widehat{\mathbf{j}}+\cos (e l) \widehat{\mathbf{k}} \\
& \widehat{\mathbf{e}}_{\mathbf{R}}=\cos (e l) \cos (a z) \widehat{\mathbf{i}}+\cos (e l) \sin (a z) \widehat{\mathbf{j}}+\sin (e l) \widehat{\mathbf{k}} .
\end{aligned}
$$

Any vector can be written in terms of components in this basis as $\mathbf{v}=v_{a z} \widehat{\mathbf{e}}_{\mathbf{a z}}+v_{e l} \widehat{\mathbf{e}}_{\mathbf{e l}}+v_{R} \widehat{\mathbf{e}}_{\mathbf{R}}$. The transformations between spherical basis components and Cartesian components take the form

$$
\left[\begin{array}{l}
v_{x} \\
v_{y} \\
v_{z}
\end{array}\right]=\left[\begin{array}{ccc}
-\sin (a z) & -\sin (e l) \cos (a z) & \cos (e l) \cos (a z) \\
\cos (a z) & -\sin (e l) \sin (a z) & \cos (e l) \sin (a z) \\
0 & \cos (e l) & \sin (e l)
\end{array}\right]\left[\begin{array}{c}
v_{a z} \\
v_{e l} \\
v_{R}
\end{array}\right]
$$

and

$$
\left[\begin{array}{l}
v_{a z} \\
v_{e l} \\
v_{R}
\end{array}\right]=\left[\begin{array}{ccc}
-\sin (a z) & \cos (a z) & 0 \\
-\sin (e l) \cos (a z) & -\sin (e l) \sin (a z) & \cos (e l) \\
\cos (e l) \cos (a z) & \cos (e l) \sin (a z) & \sin (e l)
\end{array}\right]\left[\begin{array}{c}
v_{x} \\
v_{y} \\
v_{z}
\end{array}\right] .
$$

## Version History

Introduced in R2013a

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
Does not support variable-size inputs.
See Also
sph2cartvec|azelaxes

## cbfweights

Conventional beamformer weights

## Syntax

```
wt = cbfweights(pos,ang)
wt = cbfweights(pos,ang,nqbits)
```


## Description

wt = cbfweights(pos,ang) returns narrowband conventional beamformer weights. When applied to the elements of a sensor array, these weights steer the response of the array to a specified arrival direction or set of directions. The pos argument specifies the sensor positions in the array. The ang argument specifies the azimuth and elevation angles of the desired response directions. The output weights, wt, are returned as an $N$-by- $M$ matrix. In this matrix, $N$ represents the number of sensors in the array while $M$ represents the number of arrival directions. Each column of wt contains the weights for the corresponding direction specified in the ang. The argument wt is equivalent to the output of the function steervec divided by $N$. All elements in the sensor array are assumed to be isotropic.
wt = cbfweights(pos,ang,nqbits) returns quantized narrowband conventional beamformer weights when the number of phase-shifter bits is set to nqbits.

## Examples

## Conventional Weights for Two Beamformer Directions

Specify a line array of five elements spaced 10 cm apart. Compute the weights for two directions: $30^{\circ}$ azimuth, $0^{\circ}$ elevation, and $45^{\circ}$ azimuth, $0^{\circ}$ elevation. Assume the array is tuned to plane waves having a frequency of 1 GHz .

```
elementPos = (0:.1:.4);
c = physconst('LightSpeed');
fc = 1e9;
lambda = c/fc;
ang = [30 45];
wt = cbfweights(elementPos/lambda,ang)
wt = 5*2 complex
    0.2000 + 0.0000i 0.2000 + 0.0000i
    0.0999 + 0.1733i 0.0177 + 0.1992i
    -0.1003 + 0.1731i -0.1969 + 0.0353i
    -0.2000 - 0.0004i -0.0527 - 0.1929i
    -0.0995 - 0.1735i 0.1875 - 0.0696i
```


## Quantized Weights for Two Beamformer Directions

Specify a line array of five elements spaced 10 cm apart. Compute the weights for two directions: $30^{\circ}$ azimuth, $0^{\circ}$ elevation, and $45^{\circ}$ azimuth, $0^{\circ}$ elevation. Assume the array is tuned to plane waves having a frequency of 1 GHz . Assume the weights are quantized to six bits.

```
elementPos = (0:.1:.4);
c = physconst('LightSpeed');
fc = 1e9;
lambda = c/fc;
ang = [30 45];
nqbits = 6;
wt = cbfweights(elementPos/lambda,ang,nqbits)
wt = 5x2 complex
    0.2000 + 0.0000i 0.2000 + 0.0000i
    0.0943 + 0.1764i 0.0196 + 0.1990i
    -0.0943 + 0.1764i -0.1962 + 0.0390i
    -0.2000 + 0.0000i -0.0581 - 0.1914i
    -0.0943 - 0.1764i 0.1848 - 0.0765i
```


## Input Arguments

pos - Positions of array sensor elements
1 -by- $N$ real-valued vector | 2 -by- $N$ real-valued matrix | 3 -by- $N$ real-valued matrix
Positions of the elements of a sensor array, specified as a 1 -by- $N$ vector, a 2 -by- $N$ matrix, or a 3 -by- $N$ matrix. In this vector or matrix, $N$ represents the number of elements of the array. Each column of pos represents the coordinates of an element. If pos is a 1 -by- $N$ vector, then it represents the $y$ coordinate of the sensor elements of a line array. The $x$ and $z$-coordinates are assumed to be zero. When pos is a 2-by- $N$ matrix, it represents the ( $y, z$ )-coordinates of the sensor elements of a planar array. This array is assumed to lie in the $y z$-plane. The $x$-coordinates are assumed to be zero. When pos is a 3 -by- $N$ matrix, then the array can have an arbitrary shape. Sensor positions are in terms of signal wavelength.

Example: [0,0,0; 0.1,0.4,0.3; 1,1,1]
Data Types: double

## ang - Beamforming directions

1-by- $M$ real-valued vector | 2 -by- $M$ real-valued matrix
Beamforming directions, specified as a 1 -by- $M$ vector or a 2 -by- $M$ matrix. In this vector or matrix, $M$ represents the number of incoming signals. If ang is a 2 -by- $M$ matrix, each column specifies the direction in azimuth and elevation of the beamforming direction as [az;el]. Angular units are specified in degrees. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$ and the elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$. The azimuth angle is the angle between the $x$-axis and the projection of the beamforming direction vector onto the $x y$ plane. The angle is positive when measured from the $x$-axis toward the $y$-axis. The elevation angle is the angle between the beamforming direction vector and $x y$-plane. It is positive when measured towards the positive $z$ axis. If ang is a $1-\mathrm{by}-M$ vector, then it represents a set of azimuth angles with the elevation angles assumed to be zero.

## Data Types: double

nqbits - Number of phase shifter quantization bits
0 (default) | non-negative integer
Number of bits used to quantize the phase shift in beamformer or steering vector weights, specified as a non-negative integer. A value of zero indicates that no quantization is performed.
Example: 5

## Output Arguments

## wt - Beamformer weights

$N$-by-M complex-valued matrix
Beamformer weights returned as an $N$-by- $M$ complex-valued matrix. In this matrix, $N$ represents the number of sensor elements of the array while $M$ represents the number of beamforming directions. Each column of wt corresponds to a beamforming direction specified in ang.

## Version History

Introduced in R2013a

## References

[1] Van Trees, H.L. Optimum Array Processing. New York, NY: Wiley-Interscience, 2002.
[2] Johnson, Don H. and D. Dudgeon. Array Signal Processing. Englewood Cliffs, NJ: Prentice Hall, 1993.
[3] Van Veen, B.D. and K. M. Buckley. "Beamforming: A versatile approach to spatial filtering". IEEE ASSP Magazine, Vol. 5 No. 2 pp. 4-24.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:
Does not support variable-size inputs.

## See Also

lcmvweights |mvdrweights | sensorcov|steervec|phased.PhaseShiftBeamformer

## circpol2pol

Convert circular component representation of field to linear component representation

## Syntax

$f v=c i r c p o l 2 p o l(c f v)$

## Description

$\mathrm{fv}=\operatorname{circpol2pol(cfv)}$ converts the circular polarization components of the field or fields contained in cfv to their linear polarization components contained in fv. Any polarized field can be expressed as a linear combination of horizontal and vertical components.

## Examples

## Convert Circular to Linear Polarization

Convert a horizontally polarized field, originally expressed in circular polarization components, into linear polarization components.

```
cfv = [1;1];
fv = circpol2pol(cfv)
fv = 2×1
    1.4142
    0
```

The vertical component of the output is zero for horizontally polarized fields.

## Convert Circular Polarization Ratio to Linear Polarization Ratio

Create a right circularly polarized field. Compute the circular polarization ratio and convert to a linear polarization ratio equivalent. Note that the input circular polarization ratio is Inf.

```
cfv = [0;1];
q = cfv(2)/cfv(1);
p = circpol2pol(q)
p = 0.0000 - 1.0000i
```


## Input Arguments

Field vector in its circular polarization representation specified as a 1 -by- $N$ complex row vector or a 2 -by- $N$ complex matrix. If cfv is a matrix, each column represents a field in the form of [ $\mathrm{El} ; \mathrm{Er}$ ], where El and Er are the left and right circular polarization components of the field. If cfv is a row vector, each column in cfv represents the polarization ratio, Er/El. For a row vector, the value Inf can designate the case when the ratio is computed for $\mathrm{El}=0$.
Example: [1;-1]
Data Types: double
Complex Number Support: Yes

## Output Arguments

## fv - Field vector in linear polarization representation or Jones vector

1 -by- $N$ complex-valued row vector or 2 -by- $N$ complex-valued matrix
Field vector in linear polarization representation or Jones vector returned as a 1-by- $N$ complex-valued row vector or 2 -by- $N$ complex-valued matrix. $f v$ has the same dimensions as $c f v$. If $c f v$ is a matrix, each column of fv contains the horizontal and vertical linear polarization components of the field in the form, [ $\mathrm{Eh} ; \mathrm{Ev}$ ]. If cfv is a row vector, each entry in fv contains the linear polarization ratio, defined as Ev/Eh.

## Version History

Introduced in R2013a

## References

[1] Mott, H., Antennas for Radar and Communications, John Wiley \& Sons, 1992.
[2] Jackson, J.D. , Classical Electrodynamics, 3rd Edition, John Wiley \& Sons, 1998, pp. 299-302
[3] Born, M. and E. Wolf, Principles of Optics, 7th Edition, Cambridge: Cambridge University Press, 1999, pp 25-32.

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:
Does not support variable-size inputs.

## See Also

pol2circpol|polellip|polratio|stokes

## coincidence

Coincidence algorithm

## Syntax

x = coincidence(res,div,maxval)
$\mathrm{x}=$ coincidence(res,div, maxval,tol)

## Description

$x=$ coincidence (res, div, maxval) returns the scalar $x$ that is less than or equal to maxval and is congruent to each remainder in res for the corresponding divisor in div. $x$ satisfies $\bmod (x, d i v)=$ res.
In other words, dividing $x$ by each element of div leaves as remainder the corresponding element of res.
$\mathrm{x}=$ coincidence(res, div, maxval, tol) also specifies the tolerance. In practice, there may be no value that satisfies all constraints in res and div exactly. In that case, coincidence identifies a set of candidates that approximately satisfy the constraints and are within an interval of width $2 \times$ tol centered at the candidates' median. The function then returns the median as x .

## Examples

## Coincidence Algorithm

Find a number smaller than 1000 that has a remainder of about 12 when divided by 19 , a remainder of about 13.1 when divided by 20.4 , and a remainder of about 6.1 when divided by 11 .

There is no number that satisfies the constraints exactly, so specify a tolerance of 1.

```
rems = [12 13.1 6.1];
divs = [19 20.4 11];
tol = 1;
x = coincidence(rems,divs,1000,tol)
x = 809.1000
```

Verify that the true remainders are within the specified tolerance.

```
tr = x - floor(x./divs).*divs
tr = 1\times3
    11.1000 13.5000 6.1000
```

Repeat the computation, but now specify a tolerance of 3. The number that satisfies the constraints decreases as the tolerance increases.

```
tol = 3;
x = coincidence(rems,divs,1000,tol)
x = 31
tr = x - floor(x./divs).*divs
tr = 1\times3
    12.0000 10.6000 9.0000
```

Increase the tolerance to 6 . The tolerance has to be smaller than the smallest specified remainder.
tol $=6$;
x = coincidence(rems,divs,1000,tol)
$x=12$
tr = x - floor(x./divs).*divs
$\mathrm{tr}=1 \times 3$
$12 \quad 12 \quad 1$

## Staggered PRF Radar with Maximum Range

In a staggered pulse repetition frequency (PRF) radar system, the first PRF corresponds to 70 range bins and the second PRF corresponds to 85 range bins. The target is detected at bin 47 for the first PRF and bin 12 for the second PRF. Assuming each range bin is 50 meters, compute the target range from these two measurements. Assume the farthest target can be 50 km away.

```
idx = coincidence([47 12],[70 85],50e3/50);
r = 50*idx
r = 30350
```


## Input Arguments

## res - Remainder array

row vector of nonnegative numbers
Remainder array, specified as a row vector of nonnegative numbers. res must have the same number of elements as div.

Data Types: single|double

## div - Divisor array

row vector of positive numbers
Divisor array, specified as a row vector of positive numbers. div must have the same number of elements as res.

Data Types: single | double
maxval - Upper bound
positive scalar
Upper bound, specified as a positive scalar.
Data Types: single|double
tol - Tolerance
0 (default) | nonnegative scalar
Tolerance, specified as a nonnegative scalar. tol must be smaller than the smallest element of res.
Data Types: single | double

## Output Arguments

$x$ - Congruent value
scalar
Congruent value, returned as a scalar.

## Version History

Introduced in R2021a

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

crt|iscoprime

## cranerainpl

RF signal attenuation due to rainfall using Crane model

## Syntax

L = cranerainpl(range,freq, rainrate)
L = cranerainpl(range,freq, rainrate, elev)
$\mathrm{L}=$ cranerainpl(range,freq, rainrate, elev,tau)

## Description

$L=$ cranerainpl(range,freq, rainrate) returns the signal attenuation, $L$, due to rain based on the Crane rain model [1]. Signal attenuation is a function of the signal path length, range, the signal frequency, freq, and the rain rate, rainrate. The rain rate is defined as the long-term statistical rain rate. The attenuation model applies only for frequencies from 1 GHz to 1000 GHz and is valid for ranges up to 22.5 km . The Crane model accounts for the cellular nature of rainstorms.
$L=c r a n e r a i n p l(r a n g e, f r e q, r a i n r a t e, e l e v)$ also specifies the elevation angle, elev, of the signal path.

L = cranerainpl(range,freq,rainrate,elev,tau) also specifies the polarization tilt angle, tau, of the signal.

## Examples

## Compare Attenuation for Two Rain Rates Using Crane Model

Use the Crane rain model to compute the signal attenuation caused by rain for a 20 GHz signal sent over a distance of 10 km . Use rain rates of 10.0 and $100.0 \mathrm{~mm} / \mathrm{hr}$.

First, set the rain rate to $10 \mathrm{~mm} / \mathrm{hr}$.

```
rr = 10.0;
L = cranerainpl(10e3,20.0e9,rr)
L = 12.5988
```

Repeat the computation using a rain rate of $100.0 \mathrm{~mm} / \mathrm{hr}$.

```
rr = 100.0;
L = cranerainpl(10e3,20.0e9,rr)
L = 73.1912
```


## Rain Attenuation as a Function of Frequency Using Crane Model

Plot the signal attenuation due to rain for signals in the frequency range from 1 to 1000 GHz . Use the Crane model to compute the attenuation for a rain rate of $30.0 \mathrm{~mm} / \mathrm{hr}$ and a signal path distance of 10 km .
$r r=30.0 ;$
freq = [1:1000]*1e9;
L = cranerainpl(10e3,freq,rr);
semilogx(freq/1e9, L)
grid
xlabel('Frequency (GHz)')
ylabel('Attenuation (dB)')


## Rain Attenuation as a Function of Elevation Using Crane Model

Plot the signal attenuation due to rain as a function of elevation angle. Elevation angles vary from 0 to 90 degrees. Assume a path distance of 10 km and a signal frequency of 10 GHz . The rain rate is $100 \mathrm{~mm} / \mathrm{hr}$.
rr = 100.0;
Set the elevation angles, frequency, and path length.

```
elev = [0:1:90];
freq = 10.0e9;
rng = 10e3*ones(size(elev));
```

Compute and plot the loss.

```
L = cranerainpl(rng,freq,rr,elev);
```

plot(elev, L)
grid
xlabel('Path Elevation (degrees)')
ylabel('Attenuation (dB)')


## Rain Attenuation as a Function of Polarization Using Crane Model

Plot the signal attenuation due to rainfall as a function of the polarization tilt angle. Assume a path distance of 10 km , a signal frequency of 10 GHz , and a path elevation angle of 0 degrees. Set the rainfall rate to $70 \mathrm{~mm} /$ hour. Plot the signal attenuation against polarization tilt angle.

Set the polarization tilt angle to vary from -90 to 90 degrees.

```
tau = -90:90;
```

Set the elevation angle, frequency, path distance, and rain rate.

```
elev = 0;
freq = 10.0e9;
```

```
rng = 10e3*ones(size(tau));
rr = 70.0;
```

Compute and plot the attenuation.

```
L = cranerainpl(rng,freq,rr,elev,tau);
plot(tau,L)
grid
xlabel('Tilt Angle (degrees)')
ylabel('Attenuation (dB)')
```



## Input Arguments

## range - Signal path length

positive scalar | real-valued 1-by- $M$ vector of positive values | real-valued $M$-by-1 vector of positive values

Signal path length, specified as a positive scalar, a real-valued 1-by- $M$ vector of positive values, or real-valued $M$-by-1 vector of positive values. Units are in meters.

Example: [13000.0,14000.0]

## freq - Signal frequency

positive scalar | real-valued 1 -by- $N$ vector of positive values | real-valued $N$-by-1 vector of positive values

Signal frequency, specified as a positive scalar, a real-valued 1-by- $N$ vector of positive values, or a real-valued $N$-by- 1 vector of positive values. Units are in Hz . Frequencies must lie in the range 11000 GHz .

Example: [2.0:2:10.0]*1e9]
rainrate - Rain rate
nonnegative scalar
Rain rate, specified as a nonnegative scalar. Rain rate represents the long-term statistical rainfall rate provided by Crane (see [1]). Units are in $\mathrm{mm} / \mathrm{hr}$.
Example: 100.5

## elev - Signal path elevation angle

0.0 (default) | scalar | real-valued 1-by- $M$ vector | real-valued $M$-by-1 vector

Signal path elevation angle, specified as a real-valued scalar, or real-valued $M$-by-1 or real-valued 1-by- $M$ vector. Units are in degrees between $-90^{\circ}$ and $90^{\circ}$.

- If elev is a scalar, all propagation paths have the same elevation angle.
- If elev is a vector, its length must match the length of range and each element in elev corresponds to a propagation range.

Example: [0,45]

## tau - Tilt angle of signal polarization ellipse

0.0 (default) | scalar | real-valued 1 -by- $M$ vector | real-valued $M$-by- 1 vector

Tilt angle of the signal polarization ellipse, specified as a scalar, a real-valued 1-by- $M$ vector, or a realvalued $M$-by- 1 vector. Tilt angle values are in the range $-90^{\circ}$ and $90^{\circ}$, inclusive. Units are in degrees.

- If tau is a scalar, all signals have the same tilt angle.
- If tau is a vector, its length must match the length of range. In that case, each element in tau corresponds to a propagation path in range.

The tilt angle is defined as the angle between the semimajor axis of the polarization ellipse and the $x$ axis. Because the ellipse is symmetrical, a tilt angle of $10^{\circ}$ corresponds to the same polarization state as a tilt angle of $-80^{\circ}$. Thus, the tilt angle need only be specified between $\pm 90^{\circ}$.
Example: [45, 30]

## Output Arguments

## L - Signal attenuation

real-valued $M$-by- $N$ matrix
Signal attenuation, returned as a real-valued $M$-by- $N$ matrix. Each matrix row represents a different path where $M$ is the number of paths. Each column represents a different frequency where $N$ is the number of frequencies. Units are in dB .

## More About

## Crane Rainfall Attenuation Model

The Crane model calculates the attenuation of signals that propagate through regions of rainfall. The model was developed for use on Earth-space or terrestrial propagation paths and is a commonly-used method for the calculation of rain attenuation. The model is based on observations of rain rate, rain structure, and the vertical variation of temperature in the atmosphere. The Crane model (see Electromagnetic Wave Propagation through Rain) is primarily applicable to North America. The Crane model generally predicts losses greater than those of the ITU rain attenuation model used in the rainpl function. However, the uncertainty of both models and the short-term variation of fade can be large.

The ITU and Crane models are very similar but have some differences. The ITU and Crane rain attenuation models both require statistical annual rainfall rates and utilize an effective path length reduction factor to account for the cellular nature of storms. The $0.01 \%$ rainfall rate tables provided by Crane and the ITU are different. The Crane rainfall zones are similar to the ITU zones but more zones are defined in the US than in the ITU model. The ITU rainfall zones are discussed in ITU-R P.838-3: Specific attenuation model for rain for use in prediction methods. The Crane model is more complex consisting of a piecewise combination of path profiles composed of exponential functions.

The Crane model utilizes two exponential functions to span the distance from 0 to 22.5 km .

- For $\delta<D<22.5$,

$$
L=\gamma\left(\frac{e^{y \delta}-1}{y}-\frac{b^{\alpha} e^{z \delta}}{z}+\frac{b^{\alpha} e^{z D}}{z}\right)
$$

- For $0<D<\delta$,

$$
L=\gamma\left(\frac{e^{y D}-1}{y}\right)
$$

where

- $L=$ path attenuation (dB)
- $\quad \mathrm{l}=$ propagation distance (km)
- $R=$ statistical $0.01 \%$ rain rate ( $\mathrm{mm} / \mathrm{hr}$ )
- $\gamma=$ specific attenuation identical to that calculated in rainpl.

$$
\gamma_{R}=k R^{\alpha},
$$

The parameters $k$ and $\alpha$ depend on the frequency, the polarization state, and the elevation angle of the signal path. These coefficients, given by both Crane Electromagnetic Wave Propagation through Rain and the ITU-R P.838-3: Specific attenuation model for rain for use in prediction methods, are identical and are valid from 1 GHz to 1000 GHz . The specific attenuation model is valid for frequencies from $1-1000 \mathrm{GHz}$. Rainfall specific attenuation is computed according to the ITU rainfall model in ITU-R P.838-3: Specific attenuation model for rain for use in prediction methods.

The remaining parameters are empirical constants defined as:

- $b=2.3 R^{-0.17}$
- $c=0.026-0.03 \ln R$
- $\delta=3.8-0.6 \ln R$
- $u=\ln \left(b e^{c \delta}\right) / \delta$
- $y=\alpha u$
- $z=\alpha c$

To compute the total attenuation for narrowband signals along a path, the function multiplies the specific attenuation by the propagation distance.

You can also apply the attenuation model to wideband signals. First, divide the wideband signal into frequency subbands and apply attenuation to each subband. Then, sum all attenuated subband signals into the total attenuated signal.

## Version History

Introduced in R2020a

## References

[1] Crane, Robert K. Electromagnetic Wave Propagation through Rain. Wiley, 1996.
[2] Radiocommunication Sector of International Telecommunication Union. Recommendation ITU-R P.838-3: Specific attenuation model for rain for use in prediction methods. P Series, Radiowave Propagation 2005.
[3] Radiocommunication Sector of International Telecommunication Union. Recommendation ITU-R P.530-17: Propagation data and prediction methods required for the design of terrestrial line-of-sight systems. 2017.
[4] Radiocommunication Sector of International Telecommunication Union. Recommendation ITU-R P.837-7: Characteristics of precipitation for propagation modelling. 6/2017

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\mathrm{Tm}}$.
Usage notes and limitations:
Does not support variable-size inputs.

## See Also

fspl|gaspl|fogpl|rainpl|LOSChannel | WidebandLOSChannel

## crt

Chinese remainder theorem

## Syntax

x = crt(res,div)

## Description

$x=\operatorname{crt}(r e s, d i v)$ returns the scalar integer $x$ that is congruent to each remainder in res for the corresponding divisor in div. $x$ satisfies
$\bmod (x, d i v)=$ res.
In other words, dividing $x$ by each element of div leaves as remainder the corresponding element of res.

## Examples

## Chinese Remainder Theorem

Find a number that has a remainder of 2 when divided by 9 , a remainder of 3 when divided by 10 , and a remainder of 6 when divided by 11 .

```
x = crt([2 3 6],[9 10 11])
x = 83
```

Use the mod function to verify the result.

```
ver = mod(x,[9 10 11])
ver = 1\times3
    2 3 6
```


## Staggered PRF Radar

In a staggered pulse repetition frequency (PRF) radar system, the first PRF corresponds to 70 range bins and the second PRF corresponds to 85 range bins. The target is detected at bin 47 for the first PRF and bin 12 for the second PRF. Assuming each range bin is 50 meters, compute the target range from these two measurements.

```
idx = crt([47 12],[70 85]);
r = 50*idx
r = 30350
```


## Input Arguments

## res - Remainder array

row vector of nonnegative integers
Remainder array, specified as a row vector of nonnegative integers. res must have the same number of elements as div.
Data Types: single | double
div - Divisor array
row vector of positive integers
Divisor array, specified as a row vector of positive integers. div must have the same number of elements as res.

Data Types: single | double

## Output Arguments

x-Congruent integer
scalar
Congruent integer, returned as a scalar.

## Version History

Introduced in R2021a

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\text {TM }}$.

See Also<br>coincidence|iscoprime

## dechirp

Perform dechirp operation on FMCW signal

## Syntax

$y=\operatorname{dechirp}(x, x r e f)$

## Description

$y=$ dechirp( $x, x r e f$ ) mixes the incoming signal, $x$, with the reference signal, xref. The signals can be complex baseband signals. In an FMCW radar system, x is the received signal and xref is the transmitted signal.

## Examples

## Dechirp FMCW Signal

Dechirp a delayed FMCW signal, and plot the spectrum before and after dechirping.
Create an FMCW signal.

```
Fs = 2e5; Tm = 0.001;
hwav = phased.FMCWWaveform('SampleRate',Fs,'SweepTime',Tm);
xref = step(hwav);
```

Dechirp a delayed copy of the signal.

```
x = [zeros(10,1); xref(1:end-10)];
y = dechirp(x,xref);
```

Plot the spectrum before dechirping.

```
[Pxx,F] = periodogram(x,[],1024,Fs,'centered');
plot(F/1000,10*log10(Pxx)); grid;
xlabel('Frequency (kHz)');
ylabel('Power/Frequency (dB/Hz)');
title('Periodogram Power Spectral Density Estimate Before Dechirping');
```



Plot the spectrum after dechirping.

```
[Pyy,F] = periodogram(y,[],1024,Fs,'centered');
plot(F/1000,10*log10(Pyy));
xlabel('Frequency (kHz)');
ylabel('Power/Frequency (dB/Hz)');
ylim([-100 -30]); grid
title('Periodogram Power Spectral Density Estimate After Dechirping');
```



## Input Arguments

## x - Incoming signal

$M$-by- $N$ matrix
Incoming signal, specified as an $M$-by- $N$ matrix. Each column of x is an independent signal and is individually mixed with xref.
Data Types: single | double
Complex Number Support: Yes
xref - Reference signal
M-by-1 vector
Reference signal, specified as an $M$-by-1 vector.
Data Types: single | double
Complex Number Support: Yes

## Output Arguments

## y - Dechirped signal

M-by-N matrix

Dechirped signal, returned as an $M$-by- $N$ matrix. Each column is the mixer output for the corresponding column of $x$.
Data Types: single | double

## Algorithms

For column vectors $x$ and $x$ ref, the mix operation is defined as xref .* conj $(x)$.
If $x$ has multiple columns, the mix operation applies the preceding expression to each column of $x$ independently.

The mix operation reverses the Doppler shift embedded in $x$, because of the mixing order of xref and $x$. The mixing order affects the sign of the imaginary part of the output argument, $y$. There is no consistent convention in the literature about the mixing order. This function and the beat2 range function use the same convention. If your program processes the output of dechirp in other ways, take the mixing order into account.

This function supports single and double precision for input data and arguments. If the input data, x , is single precision, the output data is single precision, regardless of the precision of the arguments. If the input data is double precision, the output data is double precision, regardless of the precision of the arguments.

## Version History <br> Introduced in R2012b

## References

[1] Pace, Phillip. Detecting and Classifying Low Probability of Intercept Radar. Boston: Artech House, 2009.
[2] Skolnik, M.I. Introduction to Radar Systems. New York: McGraw-Hill, 1980.

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:

- This function does not support variable-size inputs.
- This function supports single and double precision for input data and arguments. If the input data, $x$, is single precision, the output data is single precision, regardless of the precision of the arguments. If the input data is double precision, the output data is double precision, regardless of the precision of the arguments.


## See Also

beat2range | phased. RangeDopplerResponse

## Topics

"Automotive Adaptive Cruise Control Using FMCW Technology" (Radar Toolbox)

## delayseq

Delay or advance sequence

## Syntax

shifted_data = delayseq(data,delay)
shifted_data = delayseq(data,delay,fs)

## Description

shifted_data = delayseq(data, delay) delays or advances the signal in data by the number of samples specified in delay. Positive values of delay delay the signal, while negative values advance the signal. Noninteger values of delay represent fractional delays or advances. For fractional delays, the function interpolates between samples.

How the delayseq function operates on data depends on the dimensions of the data and delay arguments:

- When delay is a scalar, the function applies the same delay to each column of data.
- When delay is a vector:
- If data is a matrix, the length of the delay vector must equal the number of columns in the matrix. The function applies a delay to each column using the corresponding delay entry.
- If data is a column vector, the function creates a matrix where each column is the shift in the data vector by each entry in delay. The number of columns in shifted_data equals the length of the delay vector. The $k^{\text {th }}$ column of shifted_data is the result of shifting data by delay (k).
shifted_data $=$ delayseq (data, delay,fs) specifies delay in seconds. fs is the sampling frequency of data. If the product of delay and fs is not an integer, delayseq implements a fractional delay or advance of the signal using interpolation.


## Examples

## Delay Signal by Integer Number of Samples

Delay a 1 kHz cosine signal by an integer number of samples. Assume a sampling rate of 10 kHz .

```
fs = 1.0e4;
t = 0:1/fs:0.005;
signal = cos(2*pi*1000*t)';
```

Set the delay to 5 samples ( 0.5 ms ).

```
shifted_signal = delayseq(signal,5);
```

Plot the original and delayed signals.

```
subplot(2,1,1)
plot(t.*1000,signal)
```

```
title('Input')
subplot(2,1,2)
plot(t.*1000,shifted signal)
title('5 Sample Delay')
xlabel('msec')
```



## Delay Signal by Fractional Number of Samples

Delay a 1 kHz cosine signal by a fractional number of samples. Assume a sampling rate of 10 kHz .
$\mathrm{fs}=1 \mathrm{e} 4 ;$
$\mathrm{t}=0: 1 / \mathrm{fs}: 0.005$;
signal $=\cos (2 *$ pi*1000*t)';
Set the delay to 0.25 ms or 2.5 samples.
delayed_signal $=$ delayseq(signal, $0.25 e-3, f s)$;
Plot the original and delayed signals.

```
plot(t.*1000,signal)
title('Delayed Signal')
hold on
plot(t.*1000,delayed_signal,'r')
axis([0 5 -1.1 1.1])
```

```
xlabel('msec')
legend('Original Signal','Delayed Signal')
hold off
```



The delayed signal values differ from the original signal values because interpolation is used to implement the fractional delay.

## Input Arguments

## data - Input signal

real-valued length- $M$ vector $\mid$ complex-valued length- $M$ vector $\mid$ real-valued $M$-by- $N$ matrix | complexvalued $M$-by- $N$ matrix

Input signal, specified as a real-valued length- $M$ vector, complex-valued length- $M$ vector, real-valued $M$-by- $N$ matrix, or complex-valued $M$-by- $N$ matrix.
$M$ is the number of samples in data. When data is a matrix, $N$ is the number of independent signals.

## Data Types: single|double

Complex Number Support: Yes
delay - Signal delay or advance
scalar | real-valued $N$-length vector

Signal delay or advance, specified as a scalar or real-value $N$-length vector. If you specify the fs argument, delay units are in seconds. When delay is a scalar, the same delay is applied to all columns of data. delay units are in samples if fs is not specified and in seconds if fs is specified.
Data Types: single|double

## fs - Sampling frequency <br> 1 (default) | positive scalar

Sampling frequency of the signal, specified as a positive scalar. Units are in Hz .
Data Types: single | double

## Output Arguments

## shifted_data - Delayed or advanced signal

real-valued length- $M$ vector | complex-valued length- $M$ vector $\mid$ real-valued $M$-by- $N$ matrix | complexvalued $M$-by- $N$ matrix

Delayed or advanced signal, returned as a real-valued length- $M$ vector, complex-valued length- $M$ vector, real-valued $M$-by- $N$ matrix, or complex-valued $M$-by- $N$ matrix. shifted data has the same number of rows as data, with appropriate truncations or zero padding.

## Version History

Introduced in R2011a

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
Does not support variable-size inputs.

## See Also

phased.TimeDelayBeamformer

## diagbfweights

Diagonalize MIMO channel

## Syntax

[wp,wc] = diagbfweights(chanmat)
[wp,wc,P] = diagbfweights(chanmat)
[wp,wc, P, G] = diagbfweights(chanmat)
[wp,wc, P, G, C] = diagbfweights(chanmat)
[__ ] = diagbfweights(chanmat, Pt)
[___] = diagbfweights(chanmat,Pt, Pn)
[___] = diagbfweights(chanmat,Pt, Pn, powdistoption)

## Description

[wp,wc] = diagbfweights(chanmat) returns precoding weights, $w p$, and combining weights, wc, for the channel response matrix, chanmat. Together, these weights diagonalize the channel into subchannels so that the matrix wp*chanmat*wc is diagonal.
[wp,wc,P] = diagbfweights(chanmat) also returns the distributed power, P, for each element of the transmitting array.
[wp,wc, P, G] = diagbfweights(chanmat) also returns the subcarrier gains, G.
[wp,wc, P, G, C] = diagbfweights(chanmat) also returns the channel capacity sum, C.
[___ ] = diagbfweights(chanmat, Pt) also specifies total transmit power, Pt , and returned values any of the previous output argument combinations.
[___] = diagbfweights(chanmat, Pt, Pn) also specifies the noise power per transmitting antenna, Pn.
[___] = diagbfweights(chanmat, Pt, Pn, powdistoption) also specifies the noise distribution, powdistoption, across all transmitting antennas.

## Examples

## Compute and Diagonalize Channel Matrix

Compute the channel matrix for a 4 -by- 4 transmitting URA array and a 5-by-5 receiving URA array. Assume that three scatterers are randomly located within a specified angular range. The element spacing for both arrays is one-half wavelength. The receive array is 500 wavelengths away from the transmitting array along the $x$-axis. Constrain the angular span for the transmitting and receiving arrays. Diagonalize the channel matrix to compute the precoding and combining weights.

Specify the 4 -by- 4 transmitting array. Element spacing is in units of wavelength.

```
Nt = 4;
sp = 0.5;
```

```
ygridtx = (0:Nt-1)*sp - (Nt-1)/2*sp;
zgridtx = (0:Nt-1)*sp - (Nt-1)/2*sp;
[ytx,ztx] = meshgrid(ygridtx,zgridtx);
txpos = [zeros(1,Nt*Nt);ytx(:).';ztx(:).'];
```

Specify the 5-by-5 receiving array. Element spacing is in units of wavelength.

```
Nr = 5;
sp = 0.5;
ygridrx = (0:Nr-1)*sp - (Nr-1)/2*sp;
zgridrx = (0:Nr-1)*sp - (Nr-1)/2*sp;
[yrx,zrx] = meshgrid(ygridrx,zgridrx);
rxpos = [500*ones(1,Nr*Nr);yrx(:).';zrx(:).'];
```

Set the angular limits for transmitting and receiving.

- The azimuth angle limits for the transmitter are $-45^{\circ}$ to $+45^{\circ}$.
- The azimuth angle limits for the receiver are $-75^{\circ}$ to $+50^{\circ}$.
- The elevation angle limits for the transmitter are $-12^{\circ}$ to $+12^{\circ}$.
- The elevation angle limits for the receiver are $-30^{\circ}$ to $+30^{\circ}$.

```
angrange = [-45 45 -75 50; -12 12 -30 30];
```

Specify three scatterers and create the channel matrix.

```
numscat = 3;
chmat = scatteringchanmtx(txpos,rxpos,numscat,angrange);
```

Diagonalize the channel matrix.

```
[wp,wc] = diagbfweights(chmat);
z = wp*chmat*wc;
```

Show the first four diagonal elements.

```
z(1:4,1:4)
ans = 4×4 complex
\begin{tabular}{rrrrr}
\(23.3713+0.0000 i\) & \(0.0000+0.0000 i\) & \(0.0000+0.0000 i\) & \(0.0000-0.0000 i\) \\
\(0.0000+0.0000 i\) & \(10.7803+0.0000 i\) & \(-0.0000-0.0000 i\) & \(-0.0000-0.0000 i\) \\
\(0.0000+0.0000 i\) & \(0.0000+0.0000 i\) & \(1.0566+0.0000 i\) & \(0.0000+0.0000 i\) \\
\(0.0000+0.0000 i\) & \(-0.0000-0.0000 i\) & \(-0.0000+0.0000 i\) & \(0.0000+0.0000 i\)
\end{tabular}
```


## Distributed Power of Diagonalized Channel Matrix

Compute the channel matrix for a 4 -by- 4 transmitting URA array and a 5-by-5 receiving URA array. Assume that three scatterers are randomly located within a specified angular range. The element spacings for both arrays is one-half wavelength. The receive array is 500 wavelengths away along the $x$-axis. Diagonalize the channel matrix to compute the precoding and combining weights and the distributed power.

Specify the 4 -by- 4 transmitting array. Element spacing is in units of wavelength.

```
Nt = 4;
sp = 0.5;
ygridtx = (0:Nt-1)*sp - (Nt-1)/2*sp;
zgridtx = (0:Nt-1)*sp - (Nt-1)/2*sp;
[ytx,ztx] = meshgrid(ygridtx,zgridtx);
txpos = [zeros(1,Nt*Nt);ytx(:).';ztx(:).'];
```

Specify the 5 -by- 5 receiving array. Element spacing is in units of wavelength.

```
Nr = 5;
sp = 0.5;
ygridrx = (0:Nr-1)*sp - (Nr-1)/2*sp;
zgridrx = (0:Nr-1)*sp - (Nr-1)/2*sp;
[yrx,zrx] = meshgrid(ygridrx,zgridrx);
rxpos = [500*ones(1,Nr*Nr);yrx(:).';zrx(:).'];
```

Set the angular limits for transmitting and receiving.

- The azimuth angle limits for the transmitter are $-45^{\circ}$ to $+45^{\circ}$.
- The azimuth angle limits for the receiver are $-75^{\circ}$ to $+50^{\circ}$.
- The elevation angle limits for the transmitter are $-12^{\circ}$ to $+12^{\circ}$.
- The elevation angle limits for the receiver are $-30^{\circ}$ to $+30^{\circ}$.

```
angrange = [-45 45 -75 50; -12 12 -30 30];
```

Specify three scatterers and create the channel matrix.

```
numscat = 3;
chmat = scatteringchanmtx(txpos,rxpos,numscat,angrange);
```

Diagonalize the channel matrix and return the distributed power.

```
[wp,wc,P] = diagbfweights(chmat);
disp(P.')
    0.0625
    0.0625
    0.0625
    0.0625
    0.0625
    0.0625
    0.0625
    0.0625
    0.0625
    0.0625
    0.0625
    0.0625
    0.0625
    0.0625
    0.0625
    0.0625
```


## Subchannel Gains of Diagonalized Channel Matrix

Compute the channel matrix for an 11 -element transmitting ULA array and a 7 -element receiving ULA array. Assume that there are five randomly located scatterers. The element spacings for both
arrays is one-half wavelength. The receive array is 500 wavelengths away from the transmit array along the $x$-axis. Diagonalize the channel matrix to compute the precoding and combining weights, the distributed power, and the subchannel gains.

Specify the 11 -element transmitting ULA array. Element spacing is in units of wavelength.

```
Nt = 11;
sp = 0.5;
txpos = (0:Nt-1)*sp - (Nt-1)/2*sp;
```

Specify the 7 -element receiving ULA array. Element spacing is in units of wavelength.

```
Nr = 7;
sp = 0.5;
rxpos = (0:Nr-1)*sp - (Nr-1)/2*sp;
numscat = 5;
chmat = scatteringchanmtx(txpos,rxpos,numscat);
```

Diagonalize the channel matrix and return the subchannel gains.

```
[wp,wc,P,G] = diagbfweights(chmat);
disp(G.')
```

    221.8345
    56.8443
    47.6711
        0.8143
        0.0000
        0.0000
        0.0000
    
## Channel Capacity Sum of Diagonalized Channel Matrix

Compute the channel matrix for an 11 -element transmitting ULA array and a 7 -element receiving ULA array. Assume that there are five randomly located scatterers. The element spacings for both arrays is one-half wavelength. The receive array is 500 wavelengths away from the transmitting array along the $x$-axis. Create a channel matrix with two subcarriers. Diagonalize the channel matrix to compute the precoding and combining weights, the distributed power, the subchannel gains, and the channel capacity sum.

Specify the 11-element transmitting ULA array. Element spacing is in units of wavelength.

```
Nt = 11;
sp = 0.5;
txpos = (0:Nt-1)*sp - (Nt-1)/2*sp;
```

Specify the 7-element receiving ULA array. Element spacing is in units of wavelength.

```
Nr = 7;
sp = 0.5;
rxpos = (0:Nr-1)*sp - (Nr-1)/2*sp;
numscat = 5;
```

Create two subcarriers.

```
chmat1 = scatteringchanmtx(txpos,rxpos,numscat);
chmat2 = scatteringchanmtx(txpos,rxpos,numscat);
chmat(1,:,:) = chmat1;
chmat(2,:,:) = chmat2;
```

Diagonalize the channel matrix and return the subchannel gains.

```
[wp,wc,P,G,C] = diagbfweights(chmat);
disp(C.')
    9.5466 9.3605
```


## Diagonalize Channel Matrix with Specified Power

Compute the channel matrix for an 11-element transmitting ULA array and a 7 -element receiving ULA array. Specify the total transmitted power at 1000. Assume that there are five randomly located scatterers. The element spacings for both arrays is one-half wavelength. The receive array is 500 wavelengths away from the transmitting array along the $x$-axis. Create a channel matrix with two subcarriers. Diagonalize the channel matrix to compute the precoding and combining weights, the distributed power, the subchannel gains, and the channel capacity sum.

Specify the 11-element transmitting ULA array. Element spacing is in units of wavelength.

```
Nt = 11;
sp = 0.5;
txpos = (0:Nt-1)*sp - (Nt-1)/2*sp;
```

Specify the 7-element receiving ULA array. Element spacing is in units of wavelength.

```
Nr = 7;
sp = 0.5;
rxpos = (0:Nr-1)*sp - (Nr-1)/2*sp;
numscat = 5;
```

Create two subcarriers.

```
chmat1 = scatteringchanmtx(txpos,rxpos,numscat);
chmat2 = scatteringchanmtx(txpos,rxpos,numscat);
chmat(1,:,:) = chmat1;
chmat(2,:,:) = chmat2;
```

Diagonalize the channel matrix and return the distributed power for both subcarriers.

```
Pt = 1000.0;
disp(P.')
90.9091 90.9091
90.9091 90.9091
90.9091 90.9091
90.9091 90.9091
90.9091 90.9091
90.9091 90.9091
90.9091 90.9091
90.9091 90.9091
90.9091 90.9091
```

[wp,wc,P,G,C] = diagbfweights(chmat, Pt);

```
90.9091 90.9091
90.9091 90.9091
```


## Diagonalize Channel Matrix with Specified Noise Power

Compute the channel matrix for an 11 -element transmitting ULA array and a 7 -element receiving ULA array. Specify the total transmitted power at 1000 and the transmitting antenna noise power at 100. Assume that there are five randomly located scatterers. The element spacings for both arrays is one-half wavelength. The receive array is 500 wavelengths away from the transmit array along the $x$ axis. Create a channel matrix with two subcarriers. Diagonalize the channel matrix to compute the precoding and combining weights, the distributed power, subchannel gains, and channel capacity sum.

Specify the 11-element transmitting ULA array. Element spacing is in units of wavelength.

```
Nt = 11;
sp = 0.5;
txpos = (0:Nt-1)*sp - (Nt-1)/2*sp;
```

Specify the 7 -element receiving ULA array. Element spacing is in units of wavelength.

```
Nr = 7;
sp = 0.5;
rxpos = (0:Nr-1)*sp - (Nr-1)/2*sp;
numscat = 5;
```

Create two subcarriers.

```
chmat1 = scatteringchanmtx(txpos,rxpos,numscat);
chmat2 = scatteringchanmtx(txpos,rxpos,numscat);
chmat(1,:,:) = chmat1;
chmat(2,:,:) = chmat2;
```

Diagonalize the channel matrix and return the gain for both subcarriers.

```
Pt = 1000.0;
Pn = 100.0;
[wp,wc,P,G,C] = diagbfweights(chmat,Pt,Pn);
disp(G.')
    221.8345 119.7549
    56.8443 115.9814
    47.6711 24.9780
        0.8143 5.1025
        0.0000 0.0059
        0.0000 0.0000
        0.0000 0.0000
```


## Diagonalize Channel Matrix Using Waterfill Power Distribution

Compute the channel matrix for an 11-element transmitting ULA array and a 7 -element receiving ULA array. Specify the total transmitted power at 1000 and the transmitting antenna noise power at
100. Specify the transmitted power distribution as 'Waterfill'. Assume that there are five randomly located scatterers. The element spacing for both arrays is one-half wavelength. The receive array is 500 wavelengths away from the transmitting array along the $x$-axis. Create a channel matrix with two subcarriers. Diagonalize the channel matrix to compute the precoding and combining weights, the distributed power, the subchannel gains, and the channel capacity sum.

Specify the 11-element transmitting ULA array. Element spacing is in units of wavelength.

```
Nt = 11;
sp = 0.5;
txpos = (0:Nt-1)*sp - (Nt-1)/2*sp;
```

Specify the 7-element receiving ULA array. Element spacing is in units of wavelength.

```
Nr = 7;
sp = 0.5;
rxpos = (0:Nr-1)*sp - (Nr-1)/2*sp;
numscat = 5;
```

Create two subcarriers.

```
chmat1 = scatteringchanmtx(txpos,rxpos,numscat);
chmat2 = scatteringchanmtx(txpos,rxpos,numscat);
chmat(1,:,:) = chmat1;
chmat(2,:,:) = chmat2;
```

Diagonalize the channel matrix and return the gain for both subcarriers.

```
Pt = 1000.0;
Pn = 100.0;
[wp,wc,P,G,C] = diagbfweights(chmat,Pt,Pn,'Waterfill');
disp(G.')
    221.8345 119.7549
    56.8443 115.9814
    47.6711 24.9780
        0.8143 5.1025
        0.0000 0.0059
        0.0000 0.0000
        0.0000 0.0000
```


## Input Arguments

## chanmat - Channel response matrix

$N_{t}$-by- $N_{r}$ complex-valued matrix | $L$-by- $N_{t}$-by- $N_{r}$ complex-valued MATLAB array
Channel response matrix, specified as an $N_{t}$-by- $N_{r}$ complex-valued matrix or an $L$-by- $N_{t}$-by- $N_{r}$ complex-valued MATLAB array.

- $N_{t}$ is the number of elements in the transmitting array.
- $N_{r}$ is the number of elements in the receiving array.
- $L$ is the number of subcarriers.

When chanmat is a MATLAB array containing subcarriers, each subcarrier is decomposed independently into subchannels.

Data Types: double
Complex Number Support: Yes

## Pt - Total transmit power

1 (default) | positive scalar | $L$-element vector of positive values
Total transmit power, specified as a positive scalar or an $L$-element vector of positive values. Pt has the same units as the total distributed power, P .
Data Types: double
Pn - Noise power
1 (default) | positive scalar
Noise power in each receiving antenna, specified as a positive scalar. Pn has the same units as the total transmit power, Pt.
Data Types: double

## powdistoption - Power distribution option

'Uniform' (default)| 'Waterfill'
Power distribution option, specified as 'Uniform' or 'Waterfill'. When powdistoption is 'Uniform' , the transmit power is evenly distributed across all $N_{t}$ channels. If powdistoption is 'Waterfill', the transmit power is distributed across the $N_{t}$ channels using a waterfill algorithm.

Data Types: char

## Output Arguments

## wp - Precoding weights

$N_{t}$-by- $N_{t}$ complex-valued matrix | $L$-by- $N_{t}$-by- $N_{t}$ complex-valued MATLAB array
Precoding weights, returned as an $N_{t}$-by- $N_{t}$ complex-valued matrix or an $L$-by- $N_{t}$-by- $N_{t}$ complexvalued MATLAB array. Units are dimensionless.
Data Types: double

## wc - Combining weights

$N_{r}$-by- $N_{r}$ complex-valued matrix | L-by- $N_{r}$-by- $N_{r}$ complex-valued MATLAB array
Combining weights, returned as an $N_{r}$-by- $N_{r}$ complex-valued matrix or an $L$-by- $N_{r}$-by- $N_{r}$ complexvalued MATLAB array. Units are dimensionless.
Data Types: double

## P - Distributed power

1-by- $N_{t}$ real-valued row vector | $L$-by- $N_{t}$ real-valued matrix
Distributed power, returned as a vector or matrix.

- When chanmat is an $N_{t}$-by- $N_{r}$ real-valued matrix, P is a 1-by- $N_{t}$ real-valued row vector.
- When chanmat is an $L$-by- $N_{t}$-by- $N_{r}$ real-valued MATLAB array, P is an $L$-by- $N_{t}$ real-valued matrix.

Power units are linear.
Data Types: double

## G - Subchannel gains

1 -by- $N_{g}$ complex-valued row vector $\mid L$-by- $N_{g}$ complex-valued matrix
Subchannel gains, returned as a vector or matrix.

- When chanmat is an $N_{t}$-by- $N_{r}$ complex-valued matrix, G is a 1-by- $N_{g}$ complex-valued row vector.
- When chanmat is an $L$-by- $N_{t}$-by- $N_{r}$ complex-valued MATLAB array, G is an $L$-by- $N_{g}$ complex-valued matrix.
$N_{g}$ is the smaller of $N_{t}$ and $N_{r}$.
Gain units are linear.
Data Types: double


## C - Channel capacity sum for each subcarrier

scalar | L-by-1 vector
Channel capacity sum for each subcarrier, returned as a scalar or vector.

- When chanmat is an $N_{t}$-by- $N_{r}$ complex-valued matrix, C is a scalar.
- When chanmat is an $L$-by- $N_{t}$-by- $N_{r}$ complex-valued MATLAB array, C is an $L$-by- 1 vector.

Capacity units are in bps/Hz.
Data Types: double

## Version History

Introduced in R2017a

## References

[1] Heath, R. Jr. et al. "An Overview of Signal Processing Techniques for Millimeter Wave MIMO Systems", arXiv.org:1512.03007 [cs.IT], 2015.
[2] Tse, D. and P. Viswanath, Fundamentals of Wireless Communications, Cambridge: Cambridge University Press, 2005.
[3] Paulraj, A. Introduction to Space-Time Wireless Communications, Cambridge: Cambridge University Press, 2003.

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:

- Does not support variable-size inputs.


## See Also

## Functions

scatteringchanmtx|waterfill|blkdiagbfweights
Objects
phased.ScatteringMIMOChannel

## diffbfweights

Differential beamforming weights for ULA and UCA

## Syntax

```
wts = diffbfweights(nelem,elemspacing)
wts = diffbfweights(nelem,elemspacing,ArrayGeometry='ULA')
wts = diffbfweights(nelem,rad,ArrayGeometry='UCA')
wts = diffbfweights(nelem,elemspacing,angc,ArrayGeometry=ag)
wts = diffbfweights(nelem,elemspacing,angc,respc,ArrayGeometry=ag)
wts = diffbfweights( ___,SteerAngle=angs)
wts = diffbfweights(___,DiffuseNoiseCovariance=dncov)
wts = diffbfweights(___,DiagonalLoading=epsilon)
[wts,pos] = diffbfweights(___)
```


## Description

wts = diffbfweights(nelem,elemspacing) computes differential beamforming weights that steer a uniform linear array (ULA) to its endfire direction. nelem is the number of elements in the array and elemspacing is the distance between array elements. Differential weights can achieve frequency invariant beam patterns and are often used in microphone arrays.
wts = diffbfweights(nelem,elemspacing,ArrayGeometry='ULA') explicitly sets the array to a uniform linear array (ULA).
wts = diffbfweights(nelem,rad,ArrayGeometry='UCA') computes the differential beamforming weights for a uniform circular array (UCA). nelem is the number of elements in the array and rad is the radius ot the array.
wts = diffbfweights(nelem,elemspacing,angc,ArrayGeometry=ag) also specifies angles angc at which the array response is null. When ag equals 'ULA', elemspacing refers to the distance between array elements. When ag equals 'UCA', elemspacing refers to the array radius.
wts = diffbfweights(nelem,elemspacing,angc, respc,ArrayGeometry=ag) also specifies the desired responses, respc, at the angles specified in angc. When ag equals 'ULA', elemspacing refers to the number of array elements, When ag equals 'UCA', elemspacing refers to the array radius.
wts = diffbfweights (__ , SteerAngle=angs) also specifies the array steering angle angs.
wts = diffbfweights( $\qquad$ ,DiffuseNoiseCovariance=dncov) also specifies the diffuse noise covariance matrix dncov.
wts = diffbfweights( $\qquad$ ,DiagonalLoading=epsilon) also specifies the diagonal loading factor epsilon.
[wts,pos] = diffbfweights( ___ ) also returns the element positions pos.

## Examples

## Display Pattern of Differentially-Beamformed ULA

Display the pattern of a four-element uniform linear array. The element spacing is $1 / 10$ of the wavelength.
$\mathrm{N}=4 ;$
angp = -180:180;
[w, pos] = diffbfweights(N,0.1,ArrayGeometry='ULA');
bp = arrayfactor(pos,angp,w);
polarpattern(angp,mag2db(abs(bp)),'NormalizeData',true, ...
'MagnitudeLimMode','manual','MagnitudeLim', [-50 0])


## Display Pattern of Differentially-Beamformed UCA

Display the pattern of a six-element uniform circular array. The array radius is one wavelength.

```
N = 6;
angp = -180:180;
[w,pos] = diffbfweights(N,1,ArrayGeometry='UCA');
bp = arrayfactor(pos,angp,w);
polarpattern(angp,mag2db(abs(bp)),'NormalizeData',true, ...
    'MagnitudeLimMode','manual','MagnitudeLim',[-50 0])
```



## Cardioid Pattern from Differential Beamforming of ULA

Create a cardioid pattern for a four-element uniform linear array. The main beam points to the endfire direction, 90 degrees azimuth, and the null is in the opposite direction. The element spacing is set to be $1 / 10$ of the wavelength corresponding to the maximum frequency of interest.

```
N = 4;
angp = -180:180;
[w,pos] = diffbfweights(4,0.1,-90);
bp = arrayfactor(pos,angp,w);
polarpattern(angp,mag2db(abs(bp)),'NormalizeData',true, ...
    'MagnitudeLimMode','manual','MagnitudeLim',[-50 0])
```



## Cardioid Pattern of Four-Element ULA

Create a cardioid pattern with a four-element uniform linear array. Plot the pattern for both 1 kHz and 4 kHz . The main beam points to the broadside direction ( 0 degrees azimuth) and the null is at 70 degrees azimuth. The element spacing is set to be $1 / 10$ of the wavelength corresponding to the maximum frequency of interest,

```
N = 4;
c = 343;
fc = [1e3 4e3];
lambda = c./fc;
d = 0.1*lambda(2);
angp = -180:180;
for m = 2:-1:1
    [w,pos] = diffbfweights(N,d/lambda(m),70,SteerAngle=0);
    bp(:,m) = arrayfactor(pos,angp,w);
end
polarpattern(angp,mag2db(abs(bp)),'NormalizeData',true, ...
    'MagnitudeLimMode','manual','MagnitudeLim',[-50 0])
legend('1kHz','4kHz')
```



## Super-Cardioid from Three-Element UCA

Create a super-cardioid pattern with a 3 -element uniform circular array. Plot the pattern for both 1 kHz and 4 kHz . The main beam points to 0 degrees azimuth and the null is at 135 degrees azimuth.
The element spacing is set to be $1 / 10$ of the wavelength corresponding to the maximum frequency of interest.

```
N = 3;
c = 343;
fc = [1e3 4e3];
lambda = c./fc;
d = 0.1*lambda(2);
r = N*d/(2*pi);
angp = -180:180;
for m = 2:-1:1
    [w,pos] = diffbfweights(N,r/lambda(m),135,'ArrayGeometry','UCA');
    bp(:,m) = arrayfactor(pos,angp,w);
end
polarpattern(angp,mag2db(abs(bp)),'NormalizeData',true, ...
    'MagnitudeLimMode','manual','MagnitudeLim',[-50 0])
legend('1kHz','4kHz')
```



## Super-Cardioid from Four-Element UCA

Create a super-cardioid pattern with a four-element uniform circular array. Plot the pattern for both 1 kHz and 4 kHz . The main beam points to 50 degrees azimuth and the null is at 185 degrees azimuth. The radius is set to be $1 / 10$ of the wavelength corresponding to the maximum frequency of interest.

```
N = 4;
c = 343;
fc = [1e3 4e3];
lambda = c./fc;
r = 0.1*lambda(2);
angp = -180:180;
for m = 2:-1:1
    [w,pos] = diffbfweights(N,r/lambda(m),185, ...
        SteerAngle=50,ArrayGeometry='UCA');
    bp(:,m) = arrayfactor(pos,angp,w);
end
polarpattern(angp,mag2db(abs(bp)),'NormalizeData',true, ...
    'MagnitudeLimMode','manual','MagnitudeLim',[-50 0])
legend('1kHz','4kHz')
```



## Input Arguments

nelem - Number of array elements
positive integer
Number of array element, specified as a positive integer.
Data Types: double

## elemspacing - Element spacing of ULA

positive integer
Element spacing of a ULA array, specified as a positive scalar. Units are in wavelength.

## Dependencies

To enable this argument, set the ArrayGeometry property to 'ULA ' .
Data Types: double
rad - Radius of UCA
positive scalar
Radius of UCA, specified as a positive scalar. Units are in wavelength.

## Dependencies

To enable this argument, set the ArrayGeometry property to 'UCA '.
Data Types: double
ag - Array geometry
'ULA' (default)|'UCA'
Array geometry, specified as 'ULA' or 'UCA'. 'ULA' represent a uniform linear array and 'UCA' represents a uniform circular array. Use this argument to set the value of the ArrayGeometry property.
Data Types: double

## angc - Angular directions of null response

real-valued $P$-element row vector
Angular directions of null responses measured from broadside, specified as a real-valued $P$-element row vector. Angles must lie in the interval $[-90,90]$.
Data Types: double

## respc - Response at null directions

real-valued $P$-element row vector
Response at the null angles defined by angc, specified as a real-valued $P$-element row vector. The number of entries in respc must be equal to the number of entries in angc.
Data Types: double

## angs - Steering direction

scalar
Steering vector direction of the array, specified as a scalar in the interval [-90, 90]. The angle is measured from broadside. This argument sets the value of the SteerAngle property. Units are in degrees.
Data Types: double

## dncov - Diffuse covariance noise matrix

$N$-by- $N$ identity matrix (default) | $N$-by- $N$ matrix
Diffuse covariance noise matrix, specified as an $N$-by- $N$ matrix. Diffuse noise describes the noise presented at different directions. The default value is an identity matrix, indicating the diffuse noise is spatially white. This argument sets the value of the DiffuseNoiseCovariance property.

## Data Types: double

## epsilon - Diagonal loading factor

0 (default) | non-negative scalar
Diagonal loading factor, specified as as a nonnegative scalar. The diagonal loading is used to form a more robust estimate of the covariance. Units are dimensionless. This argument sets the value of the DiagonalLoading property.
Data Types: double

## Output Arguments

## wts - Array weights

$N$-element complex-valued vector
Array weights, returned as an $N$-element complex-valued vector. Values are dimensionless.

## pos - Array element positions

## 3-by- $N$ real-valued matrix

Array element positions, returned as a $3-b y-N$ real-valued matrix where $N$ is the number of array elements. Each column of pos represents the [x;y;z] coordinates of the corresponding element. For a ULA, the returned array is along $y$-axis, located at $(0: N-1) * D$. For a UCA, the returned array is in the $x-y$-plane, with its first element on zero degrees azimuth. Units are in wavelengths.

## Version History

## Introduced in R2022a

## References

[1] Benesty, Jacob, et al. Fundamentals of Differential Beamforming. Springer Singapore, 2016. DOI.org (Crossref), https://doi.org/10.1007/978-981-10-1046-0.
[2] Benesty, Jacob, and J. Chen. Study and Design of Differential Microphone Arrays. Springer, 2013.
[3] Jingdong Chen, Jacob Benesty, and Chao Pan, "On the design and implementation of linear differential microphone arrays", The Journal of the Acoustical Society of America, Vol 136, pp 3097, 2014.
[4] Jilu Jin, Gongping Huang, Xuehan Wang, Jingdong Chen, Jacob Benesty, and Israel Cohen, "Steering Study of Linear Differential Microphone Arrays", IEEE/ACM Transactions on Audio, Speech, and Language Processing, Vol 29, pp 158, 2020
[5] Jacob Benesty, Jingdong Chen, and Israel Cohen, Design of Circular Differential Microphone Arrays, Springer 2015.
[6] Gongping Huang, Israel Cohen, Jingdong Chen, and Jacob Benesty, "Continuously steerable differential beamformers with null constraints for circular microphone arrays", The Journal of the Acoustical Society of America, Vol 148, pp 1248, 2020.

## See Also

steervec|arrayfactor|polarpattern | phased.SteeringVector

## dop2speed

Convert Doppler shift to speed

## Syntax

radvel = dop2speed(dps,lambda)

## Description

radvel $=$ dop2speed $(\mathrm{dps}$, lambda) returns the radial velocity in meters per second. This value corresponds to the one-way Doppler shift dps for the wavelength lambda.

## Examples

## Calculate Speed of Car

Calculate the radial velocity of an automobile based on the Doppler shift of a continuous-wave radar. The radar carrier frequency is 24.15 GHz . Assume a doppler shift of 2.880 kHz .

```
f0 = 24.15e9;
lambda = physconst('LightSpeed')/f0;
dopshift = 2.880e3;
radvel = dop2speed(dopshift,lambda)
radvel = 35.7516
```

The radial velocity is 35.75 meters per second or 80 miles/hour.

## Input Arguments

```
dps - One-way Doppler shift
```

scalar | vector | matrix
One-way Doppler shift in hertz, specified as a scalar, vector, or matrix.
Data Types: single | double
lambda - Wavelength
positive scalar
Wavelength in meters, specified as a positive scalar.
Data Types: single | double

## Output Arguments

## radvel - Radial velocity

scalar | vector | matrix

Radial velocity in meters per second, returned as a scalar, vector, or matrix.

## More About

## Doppler-Radial Velocity Relation

The radial velocity of a source relative to a receiver can be computed from the one-way Doppler shift:

$$
V_{S, r}=\Delta f \lambda
$$

where $V_{s, r}$ denotes the radial velocity of the source relative to the receiver, $\Delta f$ is the Doppler shift in hertz, and $\lambda$ is the carrier frequency wavelength in meters.

## Version History <br> Introduced in R2011a

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
Does not support variable-size inputs.
This function supports single and double precision for input data and arguments.

## References

[1] Rappaport, T. Wireless Communications: Principles \& Practices. Upper Saddle River, NJ: Prentice Hall, 1996.
[2] Skolnik, M. Introduction to Radar Systems, 3rd Ed. New York: McGraw-Hill, 2001.

## See Also

dopsteeringvec|speed2dop

## dopsteeringvec

Doppler steering vector

## Syntax

DSTV = dopsteeringvec(dopplerfreq, numpulses)
DSTV = dopsteeringvec(dopplerfreq, numpulses,PRF)

## Description

DSTV = dopsteeringvec(dopplerfreq, numpulses) returns the temporal (time-domain)
Doppler steering vector for a target at a normalized Doppler frequency of dopplerfreq in hertz. The pulse repetition frequency is assumed to be 1 Hz .

DSTV = dopsteeringvec (dopplerfreq, numpulses, PRF) specifies the pulse repetition frequency, PRF.

## Examples

## Compute Steering Vector for Doppler Shift

Calculate the steering vector corresponding to a Doppler frequency of 200 Hz . Assume there are 10 pulses and the PRF is 1 kHz .

```
dstv = dopsteeringvec(200,10,1000)
dstv = 10x1 complex
    1.0000 + 0.0000i
    0.3090 + 0.9511i
    -0.8090 + 0.5878i
    -0.8090 - 0.5878i
    0.3090 - 0.9511i
    1.0000 - 0.0000i
    0.3090 + 0.9511i
    -0.8090 + 0.5878i
    -0.8090 - 0.5878i
    0.3090 - 0.9511i
```


## Input Arguments

## dopplerfreq - Doppler frequencies

scalar | vector
Doppler frequencies in hertz, specified as a scalar or vector. The normalized Doppler frequency is the Doppler frequency divided by the pulse repetition frequency. Every element of dopplerfreq must be smaller than or equal to one-half the pulse repetition frequency PRF.

## Data Types: single |double

## numpulses - Number of pulses

positive integer scalar
Number of pulses, specified as a positive integer scalar. The time-domain Doppler steering vector consists of numpulses samples taken at intervals of 1/PRF (slow-time samples).
Data Types: single|double

## PRF - Pulse repetition frequency

1 (default) | positive scalar
Pulse repetition frequency in hertz, specified as a positive scalar. The time-domain Doppler steering vector consists of numpulses samples taken at intervals of 1/PRF (slow-time samples). The normalized Doppler frequency is the Doppler frequency divided by the pulse repetition frequency.
Data Types: single | double

## Output Arguments

## DSTV - Temporal Doppler steering vector

column vector | matrix
Temporal Doppler steering vector, returned as a column vector or a matrix. DSTV has numpulses rows and a number of columns equal to the number of elements of dopplerfreq.

## More About

## Temporal Doppler Steering Vector

The temporal (time-domain) steering vector corresponding to a point scatterer is:

$$
e^{j 2 \pi f_{d} T_{p} n}
$$

where $n=0,1,2, \ldots, N-1$ are slow-time samples (one sample from each of $N$ pulses), $f_{d}$ is the Doppler frequency, and $T_{p}$ is the pulse repetition interval. The product of the Doppler frequency and the pulse repetition interval is the normalized Doppler frequency.

## Version History

## Introduced in R2011a

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:
This function supports single and double precision for input data and arguments.
This function does not support variable-size inputs.

## References

[1] Melvin, W. L. "A STAP Overview," IEEE ${ }^{\circledR}$ Aerospace and Electronic Systems Magazine, Vol. 19, Number 1, 2004, pp. 19-35.
[2] Richards, M. A. Fundamentals of Radar Signal Processing. New York: McGraw-Hill, 2005.

## See Also

dop2speed \| speed2dop

## espritdoa

Direction of arrival using TLS ESPRIT

## Syntax

```
ang = espritdoa(R,nsig)
ang = espritdoa(___,Name,Value)
```


## Description

ang = espritdoa( $\mathrm{R}, \mathrm{nsig}$ ) estimates the directions of arrival, ang, of a set of plane waves received on a uniform line array (ULA). The estimation employs the TLS ESPRIT, the total leastsquares ESPRIT, algorithm. The input arguments are the estimated spatial covariance matrix between sensor elements, R , and the number of arriving signals, nsig. In this syntax, sensor elements are spaced one-half wavelength apart.
ang = espritdoa( $\qquad$ ,Name, Value) estimates the directions of arrival with additional options specified by one or more Name, Value pair arguments. This syntax can use any of the input arguments in the previous syntax.

## Examples

## Three Signals Arriving at Half-Wavelength-Spaced ULA

Assume a half-wavelength spaced uniform line array with 10 elements. Three plane waves arrive from the $0^{\circ},-25^{\circ}$, and $30^{\circ}$ azimuth directions. Elevation angles are $0^{\circ}$. The noise is spatially and temporally white. The SNR for each signal is 5 dB . Find the arrival angles.

```
N = 10;
d = 0.5;
elementPos = (0:N-1)*d;
angles = [0 -25 30];
Nsig = 3;
R = sensorcov(elementPos,angles,db2pow(-5));
doa = espritdoa(R,Nsig)
doa = 1\times3
    30.0000 -0.0000 -25.0000
```

The espritdoa function returns the correct angles.

## Three Signals Arriving at 0.4-Wavelength-Spaced ULA

Assume a uniform line array with 10 elements. The element spacing is 0.4 wavelength. Three plane waves arrive from the $0^{\circ},-25^{\circ}$, and $30^{\circ}$ azimuth directions. Elevation angles are $0^{\circ}$. The noise is spatially and temporally white. The SNR for each signal is 5 dB . Find the arrival angles.

```
N = 10;
d = 0.4;
elementPos = (0:N-1)*d;
angles = [0 -25 30];
Nsig = 3;
R = sensorcov(elementPos,angles,db2pow(-5));
doa = espritdoa(R,Nsig,'ElementSpacing',d)
doa = 1\times3
    -25.0000 -0.0000 30.0000
```

espritdoa returns the correct angles.

## Input Arguments

## R - Spatial covariance matrix

complex-valued positive-definite $N$-by- $N$ matrix.
Spatial covariance matrix, specified as a complex-valued, positive-definite, $N$-by- $N$ matrix. In this matrix, $N$ represents the number of elements in the ULA array. If $R$ is not Hermitian, a Hermitian matrix is formed by averaging the matrix and its conjugate transpose, ( $R+R^{\prime}$ )/2.
Example: [ 4.3162, -0.2777-0.2337i; $-0.2777+0.2337 i$, 4.3162]
Data Types: double
Complex Number Support: Yes
nsig - Number of arriving signals
positive integer
Number of arriving signals, specified as a positive integer.
Example: 3
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.
Example: 'ElementSpacing', 0.45

## ElementSpacing - ULA element spacing

0.5 (default) | real-valued positive scalar

ULA element spacing, specified as a real-valued, positive scalar. Position units are measured in terms of signal wavelength.
Example: 0.4
Data Types: double

## RowWeighting - Row weights

1 (default) | real-valued positive scalar
Row weights specified as a real-valued positive scalar. These weights are applied to the selection matrices which determine the ESPRIT subarrays. A larger value is generally better but the value must be less than or equal to $\left(N_{s}-1\right) / 2$, where $N_{s}$ is the number of subarray elements. The number of subarray elements is $N_{s}=N-1$. The value of $N$ is the number of ULA elements, as specified by the dimensions of the spatial covariance matrix, R. A detailed discussion of selection matrices and row weighting can be found in Van Trees [1], p. 1178.
Example: 5
Data Types: double

## Output Arguments

## ang - Directions of arrival angles

real-valued 1-by-M row vector
Directions of arrival angle returned as a real-valued, 1-by- $M$ vector. The dimension $M$ is the number of arriving signals specified in the argument, nsig. This angle is the broadside angle. Angle units are degrees and angle values lie between $-90^{\circ}$ and $90^{\circ}$.

## Version History

Introduced in R2013a

## References

[1] Van Trees, H.L. Optimum Array Processing. New York: Wiley-Interscience, 2002.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\text {TM }}$.
Usage notes and limitations:
Does not support variable-size inputs.

See Also<br>aictest|mdltest|rootmusicdoa|spsmooth|phased.ESPRITEstimator

## fogpl

RF signal attenuation due to fog and clouds

## Syntax

$L=f o g p l(R, f r e q, T, d e n)$

## Description

$L=f o g p l(R, f r e q, T, d e n)$ returns attenuation, $L$, when signals propagate in fog or clouds. $R$ represents the signal path length. freq represents the signal carrier frequency, $T$ is the ambient temperature, and den specifies the liquid water density in the fog or cloud.

The fogpl function applies the International Telecommunication Union (ITU) cloud and fog attenuation model to calculate path loss of signals propagating through clouds and fog. See [1]. Fog and clouds are the same atmospheric phenomenon, differing only by height above ground. Both environments are parametrized by their liquid water density. Other model parameters include signal frequency and temperature. This function applies to cases when the signal path is contained entirely in a uniform fog or cloud environment. The liquid water density does not vary along the signal path. The attenuation model applies only for frequencies at $10-1000 \mathrm{GHz}$.

## Examples

## Attenuation in Cumulus Clouds

Compute the attenuation of signals propagating through a cloud that is 1 km long at 1000 meters altitude. Compute the attenuation for frequencies from 15 to 1000 GHz . A typical value for the cloud liquid water density is $0.5 \mathrm{~g} / \mathrm{m}^{3}$. Assume the atmospheric temperature at 1000 meters is $20^{\circ} \mathrm{C}$.

```
R = 1000.0;
freq = [15:5:1000]*1e9;
T = 20.0;
lwd = 0.5;
L = fogpl(R,freq,T,lwd);
```

Plot the specific attenuation as a function of frequency. Specific attenuation is the attenuation or loss per kilometer.

```
loglog(freq/le9,L)
grid
xlabel('Frequency (GHz)')
ylabel('Specific Attenuation (dB/km)')
```



## Input Arguments

## R - Signal path length

positive real-valued scalar | $M$-by-1 nonnegative real-valued vector | 1-by- $M$ nonnegative real-valued vector

Signal path length, specified as a scalar or as an $M$-by-1 or 1-by- $M$ vector of nonnegative real-values. Total attenuation is the specific attenuation multiplied by the path length. Units are meters.
Example: [1300.0,1400.0]

## freq - Signal frequency

positive real-valued scalar | $N$-by-1 nonnegative real-valued column vector | 1 -by- $N$ nonnegative realvalued row vector

Signal frequency, specified as a positive real-valued scalar or as an $N$-by-1 nonnegative real-valued vector or 1 -by- N nonnegative real-valued vector. Frequencies must lie in the range $10-1000 \mathrm{GHz}$. Units are in Hz .

Example: [14.0e9,15.0e9]

## T - Ambient temperature

real-valued scalar
Ambient temperature in fog or cloud, specified as a real-valued scalar. Units are in degrees Celsius.

Example: -10.0
den - Liquid water density
nonnegative real-valued scalar
Liquid water density, specified as a nonnegative real-valued scalar. Units are $\mathrm{g} / \mathrm{m}^{3}$. Typical values for liquid water density in fog range from approximately $0.05 \mathrm{~g} / \mathrm{m}^{3}$ for medium fog to approximately 0.5 $\mathrm{g} / \mathrm{m}^{3}$ for thick fog. For medium fog, visibility is about 300 meters. For heavy fog, visibility is about 50 meters. Cumulus cloud liquid water density is typically $0.5 \mathrm{~g} / \mathrm{m}^{3}$.
Example: 0.01

## Output Arguments

## L - Signal attenuation

real-valued $M$-by- $N$ matrix
Signal attenuation, returned as a real-valued $M$-by- $N$ matrix. Each matrix row represents a different path where $M$ is the number of paths. Each column represents a different frequency where $N$ is the number of frequencies. Units are in dB .

## More About

## Fog and Cloud Attenuation Model

This model calculates the attenuation of signals that propagate through fog or clouds.
Fog and cloud attenuation are the same atmospheric phenomenon. The ITU model, Recommendation ITU-R P.840-6: Attenuation due to clouds and fog is used. The model computes the specific attenuation (attenuation per kilometer), of a signal as a function of liquid water density, signal frequency, and temperature. The model applies to polarized and nonpolarized fields. The formula for specific attenuation at each frequency is

$$
\gamma_{C}=K_{l}(f) M,
$$

where $M$ is the liquid water density in $\mathrm{gm} / \mathrm{m}^{3}$. The quantity $K_{l}(f)$ is the specific attenuation coefficient and depends on frequency. The cloud and fog attenuation model is valid for frequencies $10-1000 \mathrm{GHz}$. Units for the specific attenuation coefficient are $(\mathrm{dB} / \mathrm{km}) /\left(\mathrm{g} / \mathrm{m}^{3}\right)$.

To compute the total attenuation for narrowband signals along a path, the function multiplies the specific attenuation by the path length $R$. Total attenuation is $L_{c}=R \gamma_{c}$.

You can apply the attenuation model to wideband signals. First, divide the wideband signal into frequency subbands, and apply narrowband attenuation to each subband. Then, sum all attenuated subband signals into the total attenuated signal.

## Version History

## Introduced in R2016a

## References

[1] Radiocommunication Sector of International Telecommunication Union. Recommendation ITU-R P.840-6: Attenuation due to clouds and fog. 2013.

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
Does not support variable-size inputs.

## See Also

fspl | rainpl | gaspl | LOSChannel | WidebandLOSChannel

## fspl

Free space path loss

## Syntax

$L=f s p l(R, l a m b d a)$

## Description

$L=f s p l(R, l a m b d a)$ returns the free space path loss in decibels for a waveform with wavelength lambda propagated over a distance of $R$ meters. The minimum value of $L$ is zero, indicating no path loss.

## Examples

## Calculate Free-Space Path Loss

Calculate the free-space path loss (in dB ) of a 10 GHz radar signal over a distance of 10 km .

```
fc = 10.0e9;
lambda = physconst('LightSpeed')/fc;
R = 10e3;
L = fspl(R,lambda)
L}=132.447
```


## Input Arguments

R - Propagation distance of signal
real-valued 1-by-M or $M$-by-1 vector
Units are in meters.

## lambda - Speed of propagation divided by the signal frequency

real-valued 1-by- N or N -by-1 vector
Wavelength units are meters.

## Output Arguments

## L - Path loss in decibels

$M$-by- $N$ non-negative matrix. A value of zero signifies no path loss.
When lambda is a scalar, L has the same dimensions as R .

## More About

## Free Space Path Loss

The free-space path loss, $L$, in decibels is:

$$
L=20 \log _{10}\left(\frac{4 \Pi R}{\lambda}\right)
$$

This formula assumes that the target is in the far-field of the transmitting element or array. In the near-field, the free-space path loss formula is not valid and can result in a loss smaller than 0 dB , equivalent to a signal gain. For this reason, the loss is set to 0 dB for range values $R \leq \lambda / 4 \Pi$.

## Version History

Introduced in R2011a

## References

[1] Proakis, J. Digital Communications. New York: McGraw-Hill, 2001.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{Tm}}$.
Usage notes and limitations:
Does not support variable-size inputs.

## See Also

gaspl|fogpl|rainpl|phased.FreeSpace

## gain2aperture

Convert gain to effective aperture

## Syntax

A = gain2aperture(GdB,lambda)

## Description

A = gain2aperture(GdB,lambda) returns the effective aperture of an antenna corresponding to an antenna gain of GdB for an incident electromagnetic wave with wavelength lambda.

## Examples

## Compute Effective Aperture

An antenna has a gain of 3 dB . Calculate the antenna's effective aperture when used to capture an electromagnetic wave with a wavelength of 10 cm .
a = gain2aperture(3,0.1)
$a=0.0016$

## Input Arguments

## GdB - Antenna gains

scalar | $N$-element real-valued vector
Antenna gains, specified as a scalar or as an $N$-element real-valued vector. If GdB is a vector, each element of GdB corresponds to the effective aperture of the same element in the output argument A . See "Gain and Effective Aperture" on page 2-20 for a discussion of aperture and gain. Units are in dBi.
Data Types: double

## lambda - Wavelength of the incident electromagnetic wave positive scalar

Wavelength of the incident electromagnetic wave, specified as a positive scalar. The wavelength of an electromagnetic wave is the ratio of the wave propagation speed to the frequency. Units are in meters.

Data Types: double

## Output Arguments

## A - Antenna effective aperture

positive scalar | $N$-element vector of positive values

Antenna effective aperture, returned as a positive scalar or as an $N$-element vector of positive values. The elements of A represent the effective apertures for the corresponding elements of GdB. The size of $A$ equals the size of $G d B$.

## Data Types: double

## More About

## Gain and Effective Aperture

The effective aperture describes how much energy is captured by an antenna from an incident electromagnetic plane wave. The effective area of the antenna and is not the same as the actual physical area. The array gain of an antenna $G$ is related to its effective aperture $A_{e}$ by:

$$
G=\frac{4 \Pi}{\lambda^{2}} A_{e}
$$

where $\lambda$ is the wavelength of the incident electromagnetic wave. For a fixed wavelength, the antenna gain is proportional to the effective aperture. For a fixed effective aperture, the antenna gain is inversely proportional to the square of the wavelength.

The gain expressed in $\mathrm{dBi}(G d B)$ is

$$
G d B=10 \log _{10} G=10 \log _{10}\left(\frac{4 \Pi A_{g}}{\lambda^{2}}\right)
$$

The effective antenna aperture can be derived from the gain in dB using

$$
A_{e}=10^{G d B / 10} \frac{\lambda^{2}}{4 \Pi}
$$

## Version History <br> Introduced in R2011a

## References

[1] Skolnik, M. Introduction to Radar Systems, 3rd Ed. New York: McGraw-Hill, 2001.
[2] Richards, M. Fundamentals of Radar Signal Processing, New York: McGraw-Hill, 2005.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
Does not support variable-size inputs.

## See Also

aperture2gain

## gaspl

RF signal attenuation due to atmospheric gases

## Syntax

$\mathrm{L}=$ gaspl(range,freq, $\mathrm{T}, \mathrm{P}, \mathrm{den})$

## Description

$\mathrm{L}=$ gaspl(range,freq, $\mathrm{T}, \mathrm{P}, \mathrm{den}$ ) returns the attenuation, L , of signals propagating through the atmosphere.

- range represents the signal path length.
- freq represents the signal carrier frequency.
- T represents the ambient temperature.
- Prepresents the atmospheric pressure.
- den represents the atmospheric water vapor density.

The gaspl function applies the International Telecommunication Union (ITU) atmospheric gas attenuation model [1] to calculate path loss for signals primarily due to oxygen and water vapor. The model computes attenuation as a function of ambient temperature, pressure, water vapor density, and signal frequency.

The function requires that the signal path is contained entirely in a homogeneous environment temperature T , atmospheric pressure P , and water vapor density den do not vary along the signal path. You can account for the variation of atmospheric parameters with height using the tropopl and atmositu functions in the Radar Toolbox.

The attenuation model applies only for frequencies at 1-1000 GHz.

## Examples

## Atmospheric Gas Attenuation Spectrum

Compute the attenuation spectrum from 1 to 1000 GHz for an atmospheric pressure of 101.300 kPa and a temperature of $15^{\circ} \mathrm{C}$. Plot the spectrum for a water vapor density of $7.5 \mathrm{~g} / \mathrm{m}^{3}$ and then plot the spectrum for dry air (zero water vapor density).

Set the attenuation frequencies.
freq = [1:1000]*1e9;
Assume a 1 km path distance.
R = 1000.0;
Compute the attenuation for air containing water vapor.

```
T = 15;
P = 101300.0;
W = 7.5;
L = gaspl(R,freq,T,P,W);
```

Compute the attenuation for dry air.

```
L0 = gaspl(R,freq,T,P,0.0);
```

Plot the attenuations.

```
semilogy(freq/le9,L)
hold on
semilogy(freq/1e9,L0)
grid
xlabel('Frequency (GHz)')
ylabel('Specific Attenuation (dB)')
hold off
```



Plot Attenuation Due to Atmospheric Gases and Free Space
First, plot the specific attenuation of atmospheric gases for frequencies from 1 GHz to 1000 GHz . Assume a sea-level dry air pressure of 101.325 e 5 kPa and a water vapor density of $7.5 \mathrm{~g} / \mathrm{m}^{3}$. The air temperature is $20^{\circ} \mathrm{C}$. Specific attenuation is defined as dB loss per kilometer. Then, plot the actual attenuation at 10 GHz for a span of ranges.

## Plot Specific Atmospheric Gas Attenuation

Set the atmosphere temperature, pressure, water vapor density.

```
T = 20.0;
Patm = 101.325e3;
rho wv = 7.5;
```

Set the propagation distance, speed of light, and frequencies.

```
km = 1000.0;
c = physconst('LightSpeed');
freqs = [1:1000]*1e9;
```

Compute and plot the atmospheric gas loss.

```
loss = gaspl(km,freqs,T,Patm,rho_wv);
semilogy(freqs/le9,loss)
grid on
xlabel('Frequency (GHz)')
ylabel('Specific Attenuation (dB/km)')
```



## Plot Actual Atmospheric and Free Space Attenuation

Compute both free space loss and atmospheric gas loss at 10 GHz for ranges from 1 to 100 km . The frequency corresponds to an $X$-band radar. Then, plot the free space loss and the total (atmospheric + free space) loss.

```
ranges = [1:100]*1000;
freq_xband = 10e9;
loss_gas = gaspl(ranges,freq_xband,T,Patm,rho_wv);
lambda = c/freq xband;
loss_fsp = fspl(ranges,lambda);
semilogx(ranges/1000,loss_gas + loss_fsp.',ranges/1000,loss_fsp)
legend('Atmospheric + Free Space Loss'','Free Space Loss','Lōcation','SouthEast')
```

xlabel('Range (km)')
ylabel('Loss (dB)')


## Input Arguments

## range - Signal path length

nonnegative real-valued scalar $\mid M$-by-1 nonnegative real-valued column vector | 1-by- $M$ nonnegative real-valued row vector

Signal path length used to compute attenuation, specified as a nonnegative real-valued scalar or vector. You can specify multiple path lengths simultaneously. Units are in meters.

Example: [13000.0,14000.0]

## freq - Signal frequency

positive real-valued scalar | $N$-by-1 nonnegative real-valued column vector | 1 -by- $N$ nonnegative realvalued row vector

Signal frequency, specified as a positive real-valued scalar, or as an $N$-by-1 nonnegative real-valued vector or 1 -by- $N$ nonnegative real-valued vector. You can specify multiple frequencies simultaneously. Frequencies must lie in the range $1-1000 \mathrm{GHz}$. Units are in hertz.

Example: [1.4e9,2.0e9]

## T - Ambient temperature

real-valued scalar

Ambient temperature, specified as a real-valued scalar. Units are in degrees Celsius.
Example: -10.0
P - Dry air pressure
positive real-valued scalar
Dry air pressure, specified as a positive real-valued scalar. Units are in Pa. One standard atmosphere at sea level is 101325 Pa .

Example: 101300.0
den - Water vapor density
nonnegative real-valued scalar
Water vapor density or absolute humidity, specified as a nonnegative real-valued scalar. Units are $\mathrm{g} / \mathrm{m}^{3}$. The maximum water vapor density of air at $30^{\circ} \mathrm{C}$ is approximately $30.0 \mathrm{~g} / \mathrm{m}^{3}$. The maximum water vapor density of air at $0^{\circ} \mathrm{C}$ is approximately $5.0 \mathrm{~g} / \mathrm{m}^{3}$.
Example: 4.0

## Output Arguments

## L - Signal attenuation

real-valued $M$-by- $N$ matrix
Signal attenuation, returned as a real-valued $M$-by- $N$ matrix. Each matrix row represents a different path where $M$ is the number of paths. Each column represents a different frequency where $N$ is the number of frequencies. Units are in dB.

## More About

## Atmospheric Gas Attenuation Model

This model calculates the attenuation of signals that propagate through atmospheric gases.
Electromagnetic signals attenuate when they propagate through the atmosphere. This effect is due primarily to the absorption resonance lines of oxygen and water vapor, with smaller contributions coming from nitrogen gas. The model also includes a continuous absorption spectrum below 10 GHz . The ITU model Recommendation ITU-R P.676-10: Attenuation by atmospheric gases is used. The model computes the specific attenuation (attenuation per kilometer) as a function of temperature, pressure, water vapor density, and signal frequency. The atmospheric gas model is valid for frequencies from 1-1000 GHz and applies to polarized and nonpolarized fields.

The formula for specific attenuation at each frequency is

$$
\gamma=\gamma_{0}(f)+\gamma_{w}(f)=0.1820 f N^{\prime \prime}(f) .
$$

The quantity $N^{\prime \prime}()$ is the imaginary part of the complex atmospheric refractivity and consists of a spectral line component and a continuous component:

$$
N^{\prime \prime}(f)=\sum_{i} S_{i} F_{i}+N^{\prime \prime}{ }_{D}(f)
$$

The spectral component consists of a sum of discrete spectrum terms composed of a localized frequency bandwidth function, $F(f)_{i}$, multiplied by a spectral line strength, $S_{\mathrm{i}}$. For atmospheric oxygen, each spectral line strength is

$$
S_{i}=a_{1} \times 10^{-7}\left(\frac{300}{T}\right)^{3} \exp \left[a_{2}\left(1-\left(\frac{300}{T}\right)\right] P .\right.
$$

For atmospheric water vapor, each spectral line strength is

$$
S_{i}=b_{1} \times 10^{-1}\left(\frac{300}{T}\right)^{3.5} \exp \left[b_{2}\left(1-\left(\frac{300}{T}\right)\right] W .\right.
$$

$P$ is the dry air pressure, $W$ is the water vapor partial pressure, and $T$ is the ambient temperature. Pressure units are in hectoPascals ( hPa ) and temperature is in degrees Kelvin. The water vapor partial pressure, $W$, is related to the water vapor density, $\rho$, by

$$
W=\frac{\rho T}{216.7} .
$$

The total atmospheric pressure is $P+W$.
For each oxygen line, $S_{i}$ depends on two parameters, $a_{1}$ and $a_{2}$. Similarly, each water vapor line depends on two parameters, $b_{1}$ and $b_{2}$. The ITU documentation cited at the end of this section contains tabulations of these parameters as functions of frequency.

The localized frequency bandwidth functions $F_{i}(f)$ are complicated functions of frequency described in the ITU references cited below. The functions depend on empirical model parameters that are also tabulated in the reference.

To compute the total attenuation for narrowband signals along a path, the function multiplies the specific attenuation by the path length, $R$. Then, the total attenuation is $L_{g}=R\left(\gamma_{o}+\gamma_{w}\right)$.

You can apply the attenuation model to wideband signals. First, divide the wideband signal into frequency subbands, and apply attenuation to each subband. Then, sum all attenuated subband signals into the total attenuated signal.

## Version History

## Introduced in R2016a

## References

[1] Radiocommunication Sector of International Telecommunication Union. Recommendation ITU-R P.676-10: Attenuation by atmospheric gases 2013.

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{Tm}}$.
Usage notes and limitations:
Does not support variable-size inputs.

## See Also

fspl|fogpl|rainpl|rainpl|phased.LOSChannel|phased.WidebandLOSChannel

## gccphat

Generalized cross-correlation

## Syntax

```
tau = gccphat(sig,refsig)
tau = gccphat(sig,refsig,fs)
[tau,R,lag] = gccphat(
```

$\qquad$

```
[___] = gccphat(sig)
[___] = gccphat(sig,fs)
```


## Description

tau $=$ gccphat (sig, refsig) computes the time delay, tau, between the signal, sig, and a reference signal, refsig. Both sig and refsig can have multiple channels. The function assumes that the signal and reference signal come from a single source. To estimate the delay, gccphat finds the location of the peak of the cross-correlation between sig and refsig. The cross-correlation is computed using the generalized cross-correlation phase transform (GCC-PHAT) algorithm. Time delays are multiples of the sample interval corresponding to the default sampling frequency of one hertz.
tau $=$ gccphat(sig,refsig,fs), specifies the sampling frequency of the signal. Time delays are multiples of the sample interval corresponding to the sampling frequency. All input signals should have the same sample rate.
[tau, R, lag] = gccphat (__ ) returns, in addition, the cross-correlation values and correlation time lags, using any of the arguments from previous syntaxes. The lags are multiples of the sampling interval. The number of cross-correlation channels equals the number of channels in sig.
[___] = gccphat(sig) or [___ ] = gccphat(sig,fs) returns the estimated delays and cross correlations between all pairs of channels in sig. If sig has $M$ columns, the resulting tau and $R$ have $M^{2}$ columns. In these syntaxes, no reference signal input is used. The first $M$ columns of tau and R contain the delays and cross correlations that use the first channel as the reference. The second $M$ columns contain the delays and cross-correlations that use the second channel as the reference, and so on.

## Examples

## Cross-Correlation Between Two Signals and Reference Signal

Load a gong sound signal. First, use the gong signal as a reference signal. Then, duplicate the signal twice, introducing time delays of 5 and 25 seconds. Leave the sampling rate to its default of one hertz. Use gccphat to estimate the time delays between the delayed signals and the reference signal.

```
load gong;
refsig = y;
delay1 = 5;
```

```
delay2 = 25;
sig1 = delayseq(refsig,delay1);
sig2 = delayseq(refsig,delay2);
tau_est = gccphat([sig1,sig2],refsig)
tau_est = 1\times2
    5 25
```


## Cross-Correlation Between Signal and Reference Signal

Load a gong sound signal. Use the gong signal as a reference signal. Then, duplicate the signal, introducing a time delays of 5 milliseconds. Use the sampling rate of 8192 Hz . Use gccphat to estimate the time delay between the delayed signal and the reference signal.

```
load gong;
delay = 0.005;
refsig = y;
sig = delayseq(refsig,delay,Fs);
tau_est = gccphat(sig,refsig,Fs)
tau_est = 0.0050
```


## Plot Cross-Correlation of Three Signals with Reference Signal

Load a musical sound signal with a sample rate is 8192 hertz. Then, duplicate the signal three times and introduce time delays between the signals. Estimate the time delays between the delayed signals and the reference signals. Plot the correlation values.

```
load handel;
dt = 1/Fs;
refsig = y;
```

Create three delayed versions of the signal.

```
delay1 = -5.2*dt;
delay2 = 10.3*dt;
delay3 = 7*dt;
sig1 = delayseq(refsig,delay1,Fs);
sig2 = delayseq(refsig,delay2,Fs);
sig3 = delayseq(refsig,delay3,Fs);
```

Cross-correlate the delayed signals with the reference signal.

```
[tau_est,R,lags] = gccphat([sig1,sig2,sig3],refsig,Fs);
```

The gccphat functions estimates the delay to the nearest sample interval.

```
disp(tau_est*Fs)
    -5
```

Plot the correlation functions.

```
plot(1000*lags,real(R(:,1)))
xlabel('Lag Times (ms)')
ylabel('Cross-correlation')
axis([-5,5,-.4,1.1])
hold on
plot(1000*lags,real(R(:,2)))
plot(1000*lags,real(R(:,3)))
hold off
```



## Plot Cross-Correlation of Several Signals

Load a musical sound signal with a sample rate is 8192 hertz. Then, duplicate the signal two times and introduce time delays between the two signals and the reference signal. Estimate the time delays and plot the cross-correlation function between all pairs of signals.

```
load handel;
dt = 1/Fs;
refsig = y;
```

Create three delayed versions of the signal.

```
delay1 = -5.7*dt;
delay2 = 10.2*dt;
sig1 = delayseq(refsig,delay1,Fs);
sig2 = delayseq(refsig,delay2,Fs);
```

Cross-correlate all signals with the other signal.
[tau_est,R,lags] = gccphat([refsig,sig1,sig2],Fs);
Show the time delays in units of sample interval. The algorithm estimates time delays quantized to the nearest sample interval. Cross-correlation of three signals produce 9 possible time delays, one for each possible signal pair.

```
disp(tau_est*Fs)
    0
```

A signal correlated with itself gives zero lag.
Plot the correlation functions.

```
for n=1:9
    plot(1000*lags,real(R(:,n)))
    if n==1
        hold on
        xlabel('Lag Times (ms)')
        ylabel('Correlation')
        axis([-5,5,-.4,1.1])
    end
end
hold off
```



## Input Arguments

## sig - Sensor signals

$N$-by-1 complex-valued column vector | $N$-by- $M$ complex-valued matrix
Sensor signals, specified as an $N$-by- 1 column vector or an $N$-by- $M$ matrix. $N$ is the number of time samples and $M$ is the number of channels. If sig is a matrix, each column is a different channel.
Example: [0, 1, 2, 3, 2, 1, 0]
Data Types: single | double
Complex Number Support: Yes

## refsig - Reference sensor signals

$N$-by-1 complex-valued column vector | $N$-by- $M$ complex-valued matrix
Reference signals, specified as an $N$-by- 1 complex-valued column vector or an $N$-by- $M$ complex-valued matrix. If refsig is a column vector, then all channels in sig use refsig as the reference signal when computing the cross-correlation.

If refsig is a matrix, then the size of refsig must match the size of sig. The gccphat function computes the cross-correlation between corresponding channels in sig and refsig. The signals can come from different sources.

Example: [1, 2, 3, 2, 1, 0, 0]
Data Types: single | double
Complex Number Support: Yes

## fs - Signal sample rate

1 (default) | positive real-valued scalar
Signal sample rate, specified as a positive real-valued scalar. All signals should have the same sample rate. Sample rate units are in hertz.

## Example: 8000

Data Types: single | double
Complex Number Support: Yes

## Output Arguments

## tau - Time delay

1-by-K real-valued row vector
Time delay, returned as a 1-by- $K$ real-valued row vector. The value of $K$ depends upon the input argument syntax.

- When a reference signal, refsig, is used, the value of $K$ equals the column dimension of sig, $M$. Each entry in tau specifies the estimated delay for the corresponding signal pairs in sig and refsig.
- When no reference signal is used, the value of $K$ equals the square of the column dimension of sig, $M^{2}$. Each entry in tau specifies the estimated delay for the corresponding signal pairs in sig.

Units are seconds.

## R - Cross-correlation between signals

(2N-1)-by-K complex-valued matrix
Cross-correlation between signals at different sensors, returned as a ( $2 N-1$ )-by- $K$ complex-valued matrix.

- When a reference signal, refsig, is used, the value of $K$ equals the column dimension of sig, $M$. Each column is the cross-correlation between the corresponding signal pairs in sig and refsig.
- When no reference signal is used, the value of $K$ equals the square of the column dimension of sig, $M^{2}$. Each column is the cross-correlation between the corresponding signal pairs in sig.


## lag - Cross-correlation lag times

## ( $2 N-1$ ) real-valued column vector

Correlation lag times, returned as a (2N-1) real-valued column vector. Each row of lag contains the lag time for the corresponding row of R. Lag values are constrained to be multiples of the sampling interval. Lag units are in seconds.

## More About

## Generalized Cross-Correlation

You can use generalized cross-correlation to estimate the time difference of arrival of a signal at two different sensors.

A model of a signal emitted by a source and received at two sensors is given by:

$$
\begin{aligned}
& r_{1}(t)=s(t)+n_{1}(t) \\
& r_{2}(t)=s(t-D)+n_{2}(t)
\end{aligned}
$$

where $D$ is the time difference of arrival (TDOA), or time lag, of the signal at one sensor with respect to the arrival time at a second sensor. You can estimate the time delay by finding the time lag that maximizes the cross-correlation between the two signals.

From the TDOA, you can estimate the broadside arrival angle of the plane wave with respect to the line connecting the two sensors. For two sensors separated by distance $L$, the broadside arrival angle, "Broadside Angles", is related to the time lag by

$$
\sin \beta=\frac{c \tau}{L}
$$

where $c$ is the propagation speed in the medium.
A common method of estimating time delay is to compute the cross-correlation between signals received at two sensors. To identify the time delay, locate the peak in the cross-correlation. When the signal-to-noise ratio (SNR) is large, the correlation peak, $\tau$, corresponds to the actual time delay $D$.

$$
\begin{aligned}
& R(\tau)=E\left\{r_{1}(t) r_{2}(t+\tau)\right\} \\
& \widehat{D}=\underset{\tau}{\operatorname{argmax}} R(\tau)
\end{aligned}
$$

When the correlation function is more sharply peaked, performance improves. You can sharpen a cross correlation peak using a weighting function that whitens the input signals. This technique is called generalized cross-correlation (GCC). One particular weighting function normalizes the signal
spectral density by the spectrum magnitude, leading to the generalized cross-correlation phase transform method (GCC-PHAT).

$$
\begin{aligned}
& S(f)=\int_{-\infty}^{\infty} R(\tau) e^{-i 2 \pi f \tau} d \tau \\
& \tilde{R}(\tau)=\int_{-\infty}^{\infty} \frac{S(f)}{|S(f)|} e^{+i 2 \pi f \tau} d f \\
& \tilde{D}=\operatorname{argmax}_{\tau}^{\arg (\tau)}
\end{aligned}
$$

If you use just one sensor pair, you can only estimate the broadside angle of arrival. However, if you use multiple pairs of non-collinear sensors, for example, in a URA, you can estimate the arrival azimuth and elevation angles of the plane wave using least-square estimation. For $N$ sensors, you can write the delay time $\tau_{k j}$ of a signal arriving at the $k^{\text {th }}$ sensor with respect to the $j^{\text {th }}$ sensor by

$$
\begin{aligned}
& c \tau_{k j}=-\left(\vec{x}_{k}-\vec{x}_{j}\right) \cdot \vec{u} \\
& \vec{u}=\cos \alpha \sin \theta \widehat{i}+\sin \alpha \sin \theta \widehat{j}+\cos \theta \widehat{k}
\end{aligned}
$$

where $u$ is the unit propagation vector of the plane wave. The angles $\alpha$ and $\theta$ are the azimuth and elevation angles of the propagation vector. All angles and vectors are defined with respect to the local axes. You can solve the first equation using least-squares to yield the three components of the unit propagation vector. Then, you can solve the second equation for the azimuth and elevation angles.

## Version History

## Introduced in R2015b

## References

[1] Knapp, C. H. and G.C. Carter, "The Generalized Correlation Method for Estimation of Time Delay." IEEE Transactions on Acoustics, Speech and Signal Processing. Vol. ASSP-24, No. 4, Aug 1976.
[2] G. C. Carter, "Coherence and Time Delay Estimation." Proceedings of the IEEE. Vol. 75, No. 2, Feb 1987.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:
Does not support variable-size inputs.

## See Also

phased.GCCEstimator

## global2localcoord

Convert global to local coordinates

## Syntax

lclCoord $=$ global2localcoord(gCoord)
lclCoord $=$ global2localcoord(gCoord,option)
lclCoord = global2localcoord(__, ,localOrigin)
lclCoord $=$ global2localcoord( $\qquad$ , localAxes)

## Description

lclCoord = global2localcoord(gCoord) converts the global rectangular coordinates gCoord to the local rectangular coordinates lclCoord. In this syntax, the global coordinate origin is located at $(0,0,0)$ and the coordinate axes are the unit vectors in the $x, y$, and $z$ directions.
lclCoord $=$ global2localcoord(gCoord,option) converts global coordinates to local coordinates using the coordinate transformation type option.
lclCoord = global2localcoord( $\qquad$ , localOrigin) specifies the origin of the local coordinate system localOrigin. Use this syntax with any of the input arguments in previous syntaxes.
lclCoord = global2localcoord( $\qquad$ , localAxes) specifies the axes of the local coordinate system localAxes. Use this syntax with any of the input arguments in previous syntaxes.

## Examples

## Convert Global Coordinates to Local Coordinates

Convert the global rectangular coordinates, ( $0,1,0$ ), to local rectangular coordinates. The local coordinate origin is $(1,1,1)$.

```
lclCoord = global2localcoord([0;1;0],"rr",[1;1;1])
lclCoord = 3x1
```

    -1
    0
    - 1
    Convert global spherical coordinates to local rectangular coordinates.
lclCoord $=$ global2localcoord([45;45;50],"sr",[50;50;50])
lclCoord $=3 \times 1$
-25. 0000
-25.0000

## Convert Two Vectors Between Local and Global Coordinates

Convert two vectors from global to local coordinates using the global2localcoord function. Then convert them back from local to global coordinates using the local2globalcoord function.

Start with two vectors in global coordinates, $(0,1,0)$ and $(1,1,1)$. The local coordinate origins are ( 1 , 5,2 ) and ( $-4,5,7$ ), respectively.
gCoord $=[01 ; 11 ; 01]$
gCoord $=3 \times 2$
$0 \quad 1$
$1 \quad 1$
$0 \quad 1$
lclOrig = [1 -4;5 5;2 7];
Construct two rotation matrices using the rotation functions.

```
lclAxes(:,:,1) = rotz(45)*roty(-15);
lclAxes(:,:,2) = roty(45)*rotx(35);
```

Convert the vectors from global coordinates to local coordinates.

```
lclCoord = global2localcoord(gCoord,"rr",lclOrig,lclAxes)
lclCoord = 3×2
```

    -3.9327 7.7782
    -2.1213 -3.6822
    -1.0168 1.7151
    Convert the vectors from local coordinates back to global coordinates.

```
gCoord1 = local2globalcoord(lclCoord,"rr",lclOrig,lclAxes)
```

gCoord1 $=3 \times 2$
-0.0000 1.0000
$1.0000 \quad 1.0000$
$0 \quad 1.0000$

## Input Arguments

## gCoord - Global coordinates in rectangular or spherical coordinate form

3-by-N matrix

Global coordinates in rectangular or spherical coordinate form, specified as a 3-by-N matrix. Each column represents one set of global coordinates.

If the coordinates are in rectangular form, each column contains the ( $x, y, z$ ) components. Units are in meters.

If the coordinates are in spherical form, each column contains ( $a z, e l, r$ ) components. $a z$ is the azimuth angle on page 2-186 in degrees, $e l$ is the elevation angle on page 2-186 in degrees, and $r$ is the radius in meters.

The origin of the global coordinate system is assumed to be ( $0,0,0$ ). The global system axes are the standard unit basis vectors in three-dimensional space, ( $1,0,0$ ), ( $0,1,0$ ), and ( $0,0,1$ ).

Data Types: double
option - Type of coordinate transformation
"rr" (default) | string scalar | character vector
Type of coordinate transformation, specified as a string scalar or character vector. Specify one of the following values.

| Value | Transformation |
| :--- | :--- |
| "rr" or 'rr' | Global rectangular to local rectangular |
| "rs" or 'rs' | Global rectangular to local spherical |
| "sr" or 'sr' | Global spherical to local rectangular |
| "ss" or 'ss' | Global spherical to local spherical |

## Data Types: string | char

## localOrigin - Origin of local coordinate system

[0;0;0] (default) | 3 -by- $N$ matrix
Origin of the local coordinate system, specified as a 3 -by- $N$ matrix containing the rectangular coordinates of the local coordinate system origin with respect to the global coordinate system. $N$ must match the number of columns of gCoord. Each column represents a separate origin. Alternatively, you can specify localOrigin as a 3-by-1 vector. If you do so, localOrigin expands to a 3-by- $N$ matrix with identical columns.
Data Types: double

## localAxes - Axes of local coordinate system

[1 0 0;0 1 0;0 0 1] (default)|3-by-3-by-N array
Axes of the local coordinate system, specified as a 3-by-3-by-N array. Each page contains a 3-by-3 matrix representing axes for a different local coordinate system. The columns of the 3-by-3 matrices specify the local $x, y$, and $z$ axes in rectangular form with respect to the global coordinate system. Alternatively, you can specify localAxes as a single 3-by-3 matrix. If you do so, localAxes expands to a 3-by-3-by- $N$ array with identical 3 -by- 3 matrices. The default value is the identity matrix.

Data Types: double

## Output Arguments

## lclCoord - Local coordinates in rectangular or spherical coordinate form

3-by- $N$ matrix
Local coordinates in rectangular or spherical coordinate form, returned as a 3 -by- $N$ matrix. The dimensions of lclCoord match the dimensions of gCoord.
Data Types: double

## More About

## Azimuth and Elevation Angles

The azimuth angle of a vector is the angle between the $x$-axis and the orthogonal projection of the vector onto the $x y$-plane. The angle is positive from the $x$-axis toward the $y$-axis. Azimuth angles lie between -180 and 180 degrees. The elevation angle is the angle between the vector and its orthogonal projection onto the $x y$-plane. The angle is positive toward the positive $z$-axis from the $x y$ plane. By default, the boresight direction of an element or array is aligned with the positive $x$-axis. The boresight direction is the direction of the main lobe of an element or array.

Note The elevation angle is sometimes defined as the angle a vector makes with the positive $z$-axis. The MATLAB and Phased Array System Toolbox products do not use this definition.

This figure illustrates the azimuth and elevation angles of a direction vector.


## Version History

Introduced in R2011a

## References

[1] Foley, J. D., A. van Dam, S. K. Feiner, and J. F. Hughes. Computer Graphics: Principles and Practice in C, 2nd Ed. Reading, MA: Addison-Wesley, 1995.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
Does not support variable-size inputs.

## See Also

local2globalcoord|uv2azel|phitheta2azel|azel2uv|azel2phitheta|rangeangle Topics
"Global and Local Coordinate Systems"

## iscoprime

Check coprime relation

## Syntax

```
iscp = iscoprime(x)
[iscp,ispcp,pidx,pgcd] = iscoprime(x)
```


## Description

iscp $=$ iscoprime $(x)$ returns true if all elements of $x$ are coprime and false if two or more elements of $x$ have a greatest common divisor (gcd) greater than 1.
[iscp,ispcp, pidx, pgcd] = iscoprime (x) checks if pairs of elements of $x$ have a greatest common divisor greater than 1 . This syntax also returns the indices of all pairs of elements of $x$ and the greatest common divisor of each pair.

## Examples

## Coprime Array Elements

Create an array x whose elements are $9=3 \times 3,15=3 \times 5$, and $25=5 \times 5$. Verify that all elements of $x$ are coprime.
$x=\left[\begin{array}{ll}15 & 25\end{array}\right] ;$

```
iscp = iscoprime(x)
```

iscp = logical
1

Verify that at least one pair of elements of $x$ has a greatest common divisor greater than 1. Output the pairs and their greatest common divisors.

```
[~,ispcp,pidx,pgcd] = iscoprime(x)
ispcp = logical
    0
pidx = 2×3
    1 1 2
    lll
pgcd = 1\times3
    3 1 5
```


## Input Arguments

x - Input array
row vector of positive integers
Input array, specified as a row vector of positive integers.
Example: [21 36 49]
Data Types: single |double

## Output Arguments

## iscp - True if all elements are coprime

logical scalar
True if all elements are coprime, returned as a logical scalar.

## ispcp - True if elements are pairwise coprime <br> logical scalar

True if all elements are pairwise coprime, returned as a logical scalar. ispcp is true if x has no two elements whose greatest common divisor is greater than 1. ispcp is false if any two elements of $x$ have as greatest common divisor a number greater than 1.

## pidx - Array pair indices

two-row matrix
Array pair indices, returned as a two-row matrix. pidx has $\binom{n}{2}=\frac{1}{2} n(n-1)$ columns. Each column of pidx specifies the indices of a pair of elements in $x$.

## pgcd - Pair greatest common divisors

row vector
Pair greatest common divisors, returned as a row vector with a number of elements equal to the number of columns of pidx. Each element of pgcd is the greatest common divisor of the two elements of x identified by the indices in the corresponding column of pidx.

## Version History

Introduced in R2021a

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

coincidence|crt

## Icmvweights

Narrowband linearly constrained minimum variance (LCMV) beamformer weights

## Syntax

```
wt = lcmvweights(constr,resp,cov)
```


## Description

wt = lcmvweights(constr, resp,cov) returns narrowband linearly-constrained minimum variance (LCMV) beamformer weights, wt, for a phased array. When applied to the elements of the array, these weights steer the response of the array toward a specific arrival direction or set of directions. LCMV beamforming requires that the beamformer response to signals from a direction of interest are passed with specified gain and phase delay. However, power from interfering signals and noise from all other directions is minimized. Additional constraints may be imposed to specifically nullify output power coming from known directions. The constraints are contained in the matrix, constr. Each column of constr represents a separate constraint vector. The desired response to each constraint is contained in the response vector, resp. The argument cov is the sensor spatial covariance matrix. All elements in the sensor array are assumed to be isotropic.

## Examples

## LCMV Beamformer with Nulls at -40 and $\mathbf{2 0}$ Degrees

Construct a 10 -element half-wavelength-spaced line array. Then, compute the LCMV weights for a desired arrival direction of 0 degrees azimuth. Impose three direction constraints: a null at -40 degrees, a unit desired response in the arrival direction 0 degrees, and another null at 20 degrees. The sensor spatial covariance matrix includes two signals arriving from -60 and 60 degrees and -10 dB isotropic white noise.

```
N = 10;
d = 0.5;
elementPos = (0:N-1)*d;
sv = steervec(elementPos,[-40 0 20]);
resp = [0 1 0]';
Sn = sensorcov(elementPos,[-60 60],db2pow(-10));
```

Compute the beamformer weights.
$\mathrm{w}=\mathrm{lcmvweights}(\mathrm{sv}, \mathrm{resp}, \mathrm{Sn})$;
Plot the array pattern for the computed weights.

```
vv = steervec(elementPos,[-90:90]);
plot([-90:90],mag2db(abs(w'*vv)))
grid on
axis([-90,90,-50,10]);
xlabel('Azimuth Angle (degrees)');
ylabel('Normalized Power (dB)');
title('LCMV Array Pattern');
```



The above figure shows that maximum gain is attained at 0 degrees as expected. In addition, the constraints impose nulls at -40 and 20 degrees and these can be seen in the plot. The nulls at - 60 and 60 degrees arise from the fundamental property of the LCMV beamformer of suppressing the power contained in the two plane waves that contributed to the sensor spatial covariance matrix.

## Input Arguments

## constr - Constraint matrix

$N$-by-K complex-valued matrix
Constraint matrix specified as a complex-valued, $N$-by- $K$, complex-valued matrix. In this matrix $N$ represents the number of elements in the sensor array while $K$ represents the number of constraints. Each column of the matrix specifies a constraint on the beamformer weights. The number of $K$ must be less than or equal to $N$.
Example: [0, 0, 0; .1, .2, .3; 0,0,0]
Data Types: double
Complex Number Support: Yes

## resp - Desired response

$K$-by-1 complex-valued column vector.
Desired response specified as complex-valued, $K$-by- 1 column vector where $K$ is the number of constraints. The value of each element in the vector is the desired response to the constraint specified in the corresponding column of constr.

## Example: [45;0]

Data Types: double
Complex Number Support: Yes

## cov - Sensor spatial covariance matrix

$N$-by- $N$ complex-valued matrix
Sensor spatial covariance matrix specified as a complex-valued, $N$-by- $N$ matrix. In this matrix, $N$ represents the number of sensor elements. The covariance matrix consists of the variances of the element data and the covariance between sensor elements. It contains contributions from all incoming signals and noise.
Example: [45;0]
Data Types: double
Complex Number Support: Yes

## Output Arguments

## wt - Beamformer weights

$N$-by-1 complex-valued vector
Beamformer weights returned as an $N$-by-1, complex-valued vector. In this vector, $N$ represents the number of elements in the array.

## More About

## Linear-Constrained Minimum Variance Beamformers

The LCMV beamformer computes weights that minimize the total output power of an array but that are subject to some constraints (see Van Trees [1], p. 527). In order to steer the response of the array to a particular arrival direction, weights are chosen to produce unit gain when applied to the steering vector for that direction. This requirement can be thought of as a constraint on the weights. Additional constraints may be applied to nullify the array response to signals from other arrival directions such as those containing noise sources. Let $\left(a z_{1}, e l_{1}\right),\left(a z_{2}, e l_{2}\right), \ldots,\left(a z_{K}, e l_{K}\right)$ be the set of directions for which a constraint is to be imposed. Each direction has a corresponding steering vector, $\mathbf{c}_{k}$, and the response of the array to that steering vector is given by $\mathbf{c}_{k}^{H} \mathbf{w}$. The transpose conjugate of a vector is denoted by the superscript symbol $H$. A constraint is imposed when a desired response is required when the beamformer weights act on a steering vector, $\mathbf{c}_{k}$,

$$
\mathbf{c}_{k}^{H} \mathbf{w}=r_{k}
$$

This response could be specified as unity to allow the array to pass through the signal from a certain direction. It could be zero to nullify the response from that direction. All the constraints can be collected into a single matrix, $C$, and all the response into a single column vector, $\mathbf{R}$. This allows the constraints to be represented together in matrix form

$$
C^{H} \mathbf{w}=\mathbf{R}
$$

The LCMV beamformer chooses weights to minimize the total output power

$$
P=\mathbf{w}^{H} S \mathbf{w}
$$

subject to the above constraints. $S$ denotes the sensor spatial correlation matrix. The solution to the power minimization is

$$
\mathbf{w}=S^{-1} C\left(C^{H} S^{-1} C\right)^{-1} \mathbf{R}
$$

and its derivation can be found in [2].

## Version History <br> Introduced in R2013a

## References

[1] Van Trees, H.L. Optimum Array Processing. New York, NY: Wiley-Interscience, 2002.
[2] Johnson, Don H. and D. Dudgeon. Array Signal Processing. Englewood Cliffs, NJ: Prentice Hall, 1993.
[3] Van Veen, B.D. and K. M. Buckley. "Beamforming: A versatile approach to spatial filtering". IEEE ASSP Magazine, Vol. 5 No. 2 pp. 4-24.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
Does not support variable-size inputs.

## See Also

cbfweights |mvdrweights | sensorcov | steervec| phased. LCMVBeamformer

## local2globalcoord

Convert local to global coordinates

## Syntax

gCoord = local2globalcoord(lclCoord)
gCoord $=$ local2globalcoord(lclCoord,option)
gCoord = local2globalcoord( $\qquad$ , localOrigin)
gCoord = local2globalcoord( $\qquad$ , localAxes)

## Description

gCoord $=$ local2globalcoord(lclCoord) converts the local rectangular coordinates lclCoord to the global rectangular coordinates gCoord.
gCoord = local2globalcoord(lclCoord,option) converts local coordinates to global coordinates using the coordinate transformation type option.
gCoord = local2globalcoord( $\qquad$ , local0rigin) specifies the origin of the local coordinate system localOrigin. Use this syntax with any of the input arguments in previous syntaxes.
gCoord = local2globalcoord( $\qquad$ , localAxes) specifies the axes of the local coordinate system localAxes. Use this syntax with any of the input arguments in previous syntaxes.

## Examples

## Convert Local Rectangular Coordinates to Global Rectangular Coordinates

Convert local rectangular coordinates to global rectangular coordinates. The local coordinate origin is $(1,1,1)$.

```
globalcoord = local2globalcoord([0;1;0],"rr",[1;1;1])
```

globalcoord $=3 \times 1$

1
2
1

## Convert Local Spherical Coordinates to Global Rectangular Coordinates

Convert local spherical coordinates to global rectangular coordinates.

```
globalcoord = local2globalcoord([30;45;4],"sr")
globalcoord = 3×1
```

2.4495
1.4142
2.8284

## Convert Two Vectors Between Local and Global Coordinates

Convert two vectors from global to local coordinates using the global2localcoord function. Then convert them back from local to global coordinates using the local2globalcoord function.

Start with two vectors in global coordinates, $(0,1,0)$ and $(1,1,1)$. The local coordinate origins are ( 1 , 5,2 ) and ( $-4,5,7$ ), respectively.

```
gCoord = [0 1;1 1;0 1]
```

gCoord $=3 \times 2$
$0 \quad 1$
11
01
lclOrig = [1 -4;5 5;2 7];

Construct two rotation matrices using the rotation functions.

```
lclAxes(:,:,1) = rotz(45)*roty(-15);
lclAxes(:,:,2) = roty(45)*rotx(35);
```

Convert the vectors from global coordinates to local coordinates.

```
lclCoord = global2localcoord(gCoord,"rr",lclOrig,lclAxes)
lclCoord = 3×2
```

| -3.9327 | 7.7782 |
| ---: | ---: |
| -2.1213 | -3.6822 |
| -1.0168 | 1.7151 |

Convert the vectors from local coordinates back to global coordinates.

```
gCoord1 = local2globalcoord(lclCoord,"rr",lclOrig,lclAxes)
```

gCoord1 = 3×2

| -0.0000 | 1.0000 |
| ---: | ---: |
| 1.0000 | 1.0000 |
| 0 | 1.0000 |

## Input Arguments

## lclCoord - Local coordinates in rectangular or spherical coordinate form

3-by-N matrix

Local coordinates in rectangular or spherical coordinate form, specified as a 3-by- $N$ matrix. Each column represents one set of local coordinates.

If the coordinates are in rectangular form, each column contains the $(x, y, z)$ components. Units are in meters.

If the coordinates are in spherical form, each column contains ( $a z, e l, r$ ) components. $a z$ is the azimuth angle on page 2-186 in degrees, $e l$ is the elevation angle on page 2-186 in degrees, and $r$ is the radius in meters.

Data Types: double

## option - Type of coordinate transformation

"rr" (default) | string scalar | character vector
Type of coordinate transformation, specified as a string scalar or character vector. Specify one of the following values.

| Value | Transformation |
| :--- | :--- |
| "rr" or 'rr' | Local rectangular to global rectangular |
| "rs" or 'rs' | Local rectangular to global spherical |
| "sr" or 'sr' | Local spherical to global rectangular |
| "ss" or 'ss' | Local spherical to global spherical |

Data Types: string | char

## localOrigin - Origin of local coordinate system

[0;0;0] (default)| 3 -by- $N$ matrix
Origin of the local coordinate system, specified as a 3 -by- $N$ matrix containing the rectangular coordinates of the local coordinate system origin with respect to the global coordinate system. $N$ must match the number of columns of gCoord. Each column represents a separate origin. Alternatively, you can specify localOrigin as a 3-by-1 vector. If you do so, localOrigin expands to a 3-by- $N$ matrix with identical columns.
Data Types: double

## localAxes - Axes of local coordinate system

[1 0 0;0 1 0;0 0 1] (default)|3-by-3-by-N array
Axes of the local coordinate system, specified as a 3-by-3-by-N array. Each page contains a 3-by-3 matrix representing axes for a different local coordinate system. The columns of the 3-by-3 matrices specify the local $x, y$, and $z$ axes in rectangular form with respect to the global coordinate system. Alternatively, you can specify localAxes as a single 3-by-3 matrix. If you do so, localAxes expands to a 3-by-3-by- $N$ array with identical 3 -by- 3 matrices. The default value is the identity matrix.
Data Types: double

## Output Arguments

gCoord - Global coordinates in rectangular or spherical coordinate form
3 -by- $N$ matrix

Global coordinates in rectangular or spherical coordinate form, returned as a 3-by- $N$ matrix. The dimensions of gCoord match the dimensions of lclCoord. The origin of the global coordinate system is assumed to be $(0,0,0)$. The global system axes are the standard unit basis vectors in threedimensional space, ( $1,0,0$ ), ( $0,1,0$ ), and ( $0,0,1$ ).
Data Types: double

## More About

## Azimuth and Elevation Angles

The azimuth angle of a vector is the angle between the $x$-axis and the orthogonal projection of the vector onto the $x y$-plane. The angle is positive from the $x$-axis toward the $y$-axis. Azimuth angles lie between - 180 and 180 degrees. The elevation angle is the angle between the vector and its orthogonal projection onto the $x y$-plane. The angle is positive toward the positive $z$-axis from the $x y$ plane. By default, the boresight direction of an element or array is aligned with the positive $x$-axis. The boresight direction is the direction of the main lobe of an element or array.

Note The elevation angle is sometimes defined as the angle a vector makes with the positive $z$-axis. The MATLAB and Phased Array System Toolbox products do not use this definition.

This figure illustrates the azimuth and elevation angles of a direction vector.


## Version History

Introduced in R2011a

## References

[1] Foley, J. D., A. van Dam, S. K. Feiner, and J. F. Hughes. Computer Graphics: Principles and Practice in C, 2nd Ed. Reading, MA: Addison-Wesley, 1995.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
Does not support variable-size inputs.

## See Also <br> global2localcoord | uv2azel | phitheta2azel | azel2uv|azel2phitheta|rangeangle Topics <br> "Global and Local Coordinate Systems"

## mdltest

Dimension of signal subspace

## Syntax

```
nsig = mdltest(X)
nsig = mdltest(X,'fb')
```


## Description

nsig $=$ mdltest $(X)$ estimates the number of signals, nsig, present in a snapshot of data, $X$, that impinges upon the sensors in an array. The estimator uses the Minimum Description Length (MDL) test. The input argument, $X$, is a complex-valued matrix containing a time sequence of data samples for each sensor. Each row corresponds to a single time sample for all sensors.
nsig $=$ mdltest (X,'fb') estimates the number of signals. Before estimating, it performs forwardbackward averaging on the sample covariance matrix constructed from the data snapshot, $X$. This syntax can use any of the input arguments in the previous syntax.

## Examples

## Estimate the Signal Subspace Dimensions for Two Arriving Signals

Construct a data snapshot of two plane waves arriving at a half-wavelength-spaced uniform line array having 10 elements. The plane waves arrive from $0^{\circ}$ and $-25^{\circ}$ azimuth, both with elevation angles of $0^{\circ}$. Assume the signals arrive in the presence of additive noise that is both temporally and spatially Gaussian white. For each signal, the SNR is 5 dB . Take 300 samples to build a 300-by-10 data snapshot. Then, solve for the number of signals using mdltest.

```
N = 10;
d = 0.5;
elementPos = (0:N-1)*d;
angles = [0 -25];
x = sensorsig(elementPos,300,angles,db2pow(-5));
Nsig = mdltest(x)
Nsig = 2
```

The result shows that the number of signals is two, as expected.

## Estimate the Signal Subspace Dimensions Using Forward-Backward Averaging

Construct a data snapshot for two plane waves arriving at a half-wavelength-spaced uniform line array with 10 elements. Correlated plane waves arrive from $0^{\circ}$ and $10^{\circ}$ azimuth, both with elevation angles of $0^{\circ}$. Assume the signals arrive in the presence of additive noise that is both temporally and spatially Gaussian white noise. For each signal, the SNR is 10 dB . Take 300 samples to build a 300-by-10 data snapshot. Then, solve for the number of signals using mdltest.

```
N = 10;
d = 0.5;
elementPos = (0:N-1)*d;
angles = [0 10];
ncov = db2pow(-10);
scov = [1 .5]'*[1 .5];
x = sensorsig(elementPos,300,angles,ncov,scov);
Nsig = mdltest(x)
Nsig = 1
```

This result shows that mdltest cannot determine the number of signals correctly when the signals are correlated.

Now, try the forward-backward smoothing option.
Nsig = mdltest(x,'fb')
Nsig $=2$
The addition of forward-backward smoothing yields the correct number of signals.

## Input Arguments

## X - Data snapshot <br> complex-valued $K$-by- $N$ matrix

Data snapshot, specified as a complex-valued, $K$-by- $N$ matrix. A snapshot is a sequence of timesamples taken simultaneous at each sensor. In this matrix, $K$ represents the number of time samples of the data, while $N$ represents the number of sensor elements.

Example: [ $-0.1211+1.2549 i, 0.1415+1.6114 i, 0.8932+0.9765 i ;$ ]
Data Types: double
Complex Number Support: Yes

## Output Arguments

## nsig - Dimension of signal subspace

non-negative integer
Dimension of signal subspace, returned as a non-negative integer. The dimension of the signal subspace is the number of signals in the data.

## More About

## Estimating the Number of Sources

AIC and MDL tests
Direction finding algorithms such as MUSIC and ESPRIT require knowledge of the number of sources of signals impinging on the array or equivalently, the dimension, $d$, of the signal subspace. The Akaike Information Criterion (AIC) and the Minimum Description Length (MDL) formulas are two frequentlyused estimators for obtaining that dimension. Both estimators assume that, besides the signals, the
data contains spatially and temporally white Gaussian random noise. Finding the number of sources is equivalent to finding the multiplicity of the smallest eigenvalues of the sampled spatial covariance matrix. The sample spatial covariance matrix constructed from a data snapshot is used in place of the actual covariance matrix.

A requirement for both estimators is that the dimension of the signal subspace be less than the number of sensors, $N$, and that the number of time samples in the snapshot, $K$, be much greater than $N$.

A variant of each estimator exists when forward-backward averaging is employed to construct the spatial covariance matrix. Forward-backward averaging is useful for the case when some of the sources are highly correlated with each other. In that case, the spatial covariance matrix may be ill conditioned. Forward-backward averaging can only be used for certain types of symmetric arrays, called centro-symmetric arrays. Then the forward-backward covariance matrix can be constructed from the sample spatial covariance matrix, $S$, using $S_{F B}=S+J S^{*} J$ where $J$ is the exchange matrix. The exchange matrix maps array elements into their symmetric counterparts. For a line array, it would be the identity matrix flipped from left to right.

All the estimators are based on a cost function

$$
L_{d}(d)=K(N-d) \ln \left\{\frac{\frac{1}{N-d} \sum_{i=d+1}^{N} \widehat{\lambda}_{i}}{\left\{\prod_{i=d+1}^{N} \widehat{\lambda}_{i}\right\}^{\frac{1}{N-d}}}\right\}
$$

plus an added penalty term. The value $\lambda_{i}$ represent the smallest ( $N-d$ ) eigenvalues of the spatial covariance matrix. For each specific estimator, the solution for $d$ is given by

- AIC

$$
\widehat{d}_{A I C}=\underset{d}{\operatorname{argmin}}\left\{L_{d}(d)+d(2 N-d)\right\}
$$

- AIC for forward-backward averaged covariance matrices

$$
\widehat{d}_{A I C: F B}=\underset{d}{\operatorname{argmin}}\left\{L_{d}(d)+\frac{1}{2} d(2 N-d+1)\right\}
$$

- MDL

$$
\widehat{d}_{M D L}=\underset{d}{\operatorname{argmin}}\left\{L_{d}(d)+\frac{1}{2}(d(2 N-d)+1) \ln K\right\}
$$

- MDL for forward-backward averaged covariance matrices

$$
\widehat{d}_{M D L F B}=\underset{d}{\operatorname{argmin}}\left\{L_{d}(d)+\frac{1}{4} d(2 N-d+1) \ln K\right\}
$$

## Version History

## Introduced in R2013a

## References

[1] Van Trees, H.L. Optimum Array Processing. New York: Wiley-Interscience, 2002.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
Does not support variable-size inputs.

See Also<br>aictest|espritdoa|rootmusicdoa|spsmooth

## mvdrweights

Minimum variance distortionless response (MVDR) beamformer weights

## Syntax

```
wt = mvdrweights(pos,ang,cov)
wt = mvdrweights(pos,ang,nqbits)
```


## Description

wt = mvdrweights(pos,ang,cov) returns narrowband minimum variance distortionless response (MVDR) beamformer weights for a phased array. When applied to the elements of an array, the weights steer the response of a sensor array in a specific arrival direction or set of directions. The pos argument specifies the sensor positions of the array. The ang argument specifies the azimuth and elevation angles of the desired response directions. cov is the sensor spatial covariance matrix between sensor elements. The output argument, wt, is a matrix contains the beamformer weights for each sensor and each direction. Each column of wt contains the weights for the corresponding direction specified in ang. All elements in the sensor array are assumed to be isotropic.
wt = mvdrweights(pos,ang,nqbits) returns quantized narrowband MVDR beamformer weights when the number of phase shifter bits is set to nqbits.

## Examples

## MVDR Beamformer with Arrival Directions of 30 and 45 Degrees

Construct a 10 -element, half-wavelength-spaced line array. Choose two arrival directions of interest one at $30^{\circ}$ azimuth and the other at $45^{\circ}$ azimuth. Assume both directions are at $0^{\circ}$ elevation. Compute the MVDR beamformer weights for each direction. Specify a sensor spatial covariance matrix that contains signals arriving from $-60^{\circ}$ and $60^{\circ}$ and noise at -10 dB .

Set up the array and sensor spatial covariance matrix.

```
N = 10;
d = 0.5;
elementPos = (0:N-1)*d;
Sn = sensorcov(elementPos,[-60 60],db2pow(-10));
```

Solve for the MVDR beamformer weights.

```
w = mvdrweights(elementPos,[30 45],Sn);
```

Plot the two MVDR array patterns.

```
plotangl = -90:90;
vv = steervec(elementPos,plotangl);
plot(plotangl,mag2db(abs(w'*vv)))
grid on
xlabel('Azimuth Angle (degrees)');
ylabel('Normalized Power (dB)');
```

```
legend('30 deg','45 deg');
```

title('MVDR Array Pattern')


The figure shows plots for each beamformer direction. One plot has the expected maximum gain at 30 degrees and the other at 45 degrees. The nulls at -60 and 60 degrees arise from the fundamental property of the MVDR beamformer of suppressing power in all directions except for the arrival direction.

## Quantized Weights in MVDR Beamformer

Construct a 10 -element, half-wavelength-spaced line array. Choose the arrival direction of interest to be $18.5^{\circ}$ azimuth and $10^{\circ}$ elevation. Compute the MVDR beamformer weights and then compute the weights for 3-bit quantization. Specify a sensor spatial covariance matrix that contains signals arriving from $-60^{\circ}$ and $60^{\circ}$ and noise at -10 dB .

Set up the array and the sensor spatial covariance matrix.

```
N = 10;
d = 0.5;
elementPos = (0:N-1)*d;
SN = sensorcov(elementPos,[-60 60],db2pow(-10));
```

Solve for the MVDR beamformer weights with and without quantization.
w = mvdrweights(elementPos,[18.5;10],SN);
$w q=$ mvdrweights(elementPos,[18.5;10],SN,3);
Plot both MVDR array patterns.
plotangl = -90:90;
vv = steervec(elementPos,plotangl);
plot(plotangl, mag2db(abs(w'*vv)))
hold on
plot(plotangl, mag2db(abs(wq'*vv)))
grid on
xlabel('Azimuth Angle (degrees)')
ylabel('Normalized Power (dB)')
legend('Non-Quantized Weights','Quantized Weights','Location','SouthWest'); title('Quantized vs Non-quantized Array Patterns')
hold off


## Input Arguments

## pos - Positions of array sensor elements

1 -by- $N$ real-valued vector | 2 -by- $N$ real-valued matrix | 3 -by- $N$ real-valued matrix
Positions of the elements of a sensor array, specified as a 1-by- $N$ vector, a 2 -by- $N$ matrix, or a 3 -by- $N$ matrix. In this vector or matrix, $N$ represents the number of elements of the array. Each column of pos represents the coordinates of an element. If pos is a $1-b y-N$ vector, then it represents the $y$ coordinate of the sensor elements of a line array. The $x$ and $z$-coordinates are assumed to be zero.

When pos is a 2-by- $N$ matrix, it represents the $(y, z)$-coordinates of the sensor elements of a planar array. This array is assumed to lie in the $y z$-plane. The $x$-coordinates are assumed to be zero. When pos is a 3 -by- $N$ matrix, then the array can have an arbitrary shape. Sensor positions are in terms of signal wavelength.
Example: [0,0,0; 0.1,0.4,0.3; 1,1,1]
Data Types: double

## ang - Beamforming directions

1-by-M real-valued vector | 2 -by-M real-valued matrix
Beamforming directions, specified as a 1 -by- $M$ vector or a 2 -by- $M$ matrix. In this vector or matrix, $M$ represents the number of incoming signals. If ang is a 2 -by- $M$ matrix, each column specifies the direction in azimuth and elevation of the beamforming direction as [az;el]. Angular units are specified in degrees. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$ and the elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$. The azimuth angle is the angle between the $x$-axis and the projection of the beamforming direction vector onto the $x y$ plane. The angle is positive when measured from the $x$-axis toward the $y$-axis. The elevation angle is the angle between the beamforming direction vector and $x y$-plane. It is positive when measured towards the positive $z$ axis. If ang is a $1-\mathrm{by}-\mathrm{M}$ vector, then it represents a set of azimuth angles with the elevation angles assumed to be zero.

## Example: [45;10]

Data Types: double

## cov - Sensor spatial covariance matrix

$N$-by- $N$ complex-valued matrix
Sensor spatial covariance matrix specified as an $N$-by- $N$, complex-valued matrix. In this matrix, $N$ represents the number of sensor elements.

Example: [5,0.1;0.1,2]
Data Types: double
Complex Number Support: Yes
nqbits - Number of phase shifter quantization bits
0 (default) | non-negative integer
Number of bits used to quantize the phase shift in beamformer or steering vector weights, specified as a non-negative integer. A value of zero indicates that no quantization is performed.

## Example: 5

## Output Arguments

## wt - Beamformer weights

$N$-by-M complex-valued matrix
Beamformer weights returned as a complex-valued, $N$-by- $M$ matrix. In this matrix, $N$ represents the number of sensor elements of the array while $M$ represents the number of beamforming directions. Each column of wt corresponds to a beamforming direction specified in ang.

## More About

## Minimum Variance Distortionless Response

MVDR beamformer weights minimize the total array output power while setting the gain in the desired response direction to unity (see Van Trees [1], p. 442). MVDR weights are given by

$$
\mathbf{w}=\frac{S^{-1 \mid} \mathbf{v}_{\mathbf{0}}}{\mathbf{v}_{\mathbf{0}} H S^{-1} \mathbf{v}_{\mathbf{0}}}
$$

where $\mathbf{v}_{0}$ is the steering vector corresponding to the desired response direction. $S$ is the spatial covariance matrix. The covariance matrix consists of the variances of the element data and the covariances of the data between the sensor elements. The covariance contains contributions from all incoming signals and noise.

## Version History

## Introduced in R2013a

## References

[1] Van Trees, H.L. Optimum Array Processing. New York, NY: Wiley-Interscience, 2002.
[2] Johnson, Don H. and D. Dudgeon. Array Signal Processing. Englewood Cliffs, NJ: Prentice Hall, 1993.
[3] Van Veen, B.D. and K. M. Buckley. "Beamforming: A versatile approach to spatial filtering". IEEE ASSP Magazine, Vol. 5 No. 2 pp. 4-24.

## Extended Capabilities

## $\mathbf{C} / \mathbf{C + +}$ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR} \operatorname{Coder}^{\mathrm{TM}}$.
Usage notes and limitations:
Does not support variable-size inputs.

See Also<br>steervec |cbfweights | lcmvweights | sensorcov | phased.MVDRBeamformer

## minvarweights

Weights for minimum-variance array pattern synthesis

## Syntax

```
wts = minvarweights(pos,ang)
wts = minvarweights(pos,ang,cov)
wts = minvarweights(
```

$\qquad$

``` , MaskAngle=angm)
wts = minvarweights(
``` \(\qquad\)
``` ,MaskSidelobeLevel=sllm)
wts = minvarweights(
``` \(\qquad\)
``` ,NullAngle=angn)
```


## Description

wts = minvarweights(pos,ang) computes the minimum-variance weights wts for synthesizing the pattern of a sensor array in the directions specified by ang. Array element positions are specified in pos. The function optimizes the beamforming weights using a second-order cone programming solver. This function requires Optimization Toolbox ${ }^{\text {TM }}$.
wts = minvarweights(pos,ang, cov) also specifies the spatial covariance matrix cov of the array elements.
wts = minvarweights( _ , MaskAngle=angm) also specifies angles angm at which mask sidelobe levels are defined in the sllm argument.
wts = minvarweights( $\qquad$ ,MaskSidelobeLevel=sllm) also specifies maximum allowable sidelobe levels sllm at the angles defined in angm.
wts = minvarweights( $\qquad$ , NullAngle=angn) also specifies null directions angn for the array.

## Examples

## Compute Optimized ULA Beamforming Weights

Compute optimized beamforming weights of a 31 -element half-wavelength spacing ULA in the direction of $-30^{\circ}$ degree in azimuth. Design the array to keep sidelobe levels less than -23 dB .

Create the optimized weights.

```
N = 31;
pos = (0:N-1)*0.5;
sll = -23;
wts = minvarweights(pos,-30,MaskSidelobeLevel=sll);
```

Apply the optimized weights and display the array pattern from $-90^{\circ}$ to $+90^{\circ}$ azimuth.

```
az = -90:.25:90;
pat_opt = arrayfactor(pos,az,wts);
plot(az,mag2db(abs(pat_opt)))
xlabel('Azimuth Angle (deg)')
```

```
ylabel('Beam Pattern (dB)')
```

xlim([-90,90])


## Optimized Tapered ULA Weights

Design an array to have a tapered beampattern, The array is a 51-element half-wavelength spacing ULA steered in the direction of $25^{\circ}$ in azimuth. The pattern synthesis goal is to achieve sidelobe levels smaller than a tapered mask decreasing linearly from -18 dB to -55 dB at $\pm 90^{\circ}$. Place nulls at $-35^{\circ}$, $-45^{\circ}$, and $40^{\circ}$ azimuth angle.

```
N = 51;
pos = (0:N-1)*0.5;
ANGmainBeam = 25;
angn = [-35 -45 40];
angm = [-90:.2:22 27:0.2:90];
sllm = [linspace(-55,-18,length(-90:.2:22)) ...
    linspace(-18,-55,length(27:.2:90))];
wts = minvarweights(pos,ANGmainBeam,'MaskAngle',angm, ...
    'MaskSidelobeLevel',sllm,'NullAngle',angn);
```

Apply optimized weights and display the array pattern from $-90^{\circ}$ to $+90^{\circ}$ in azimuth.

```
az = -90:.25:90;
pat_opt = arrayfactor(pos,az,wts);
```

```
plot(az,mag2db(abs(pat_opt)))
axis([-90 90 -125 5])
xlabel('Azimuth Angle (deg)')
ylabel('Beam Pattern (dB)')
```



Verify that nulls are placed at $-35^{\circ},-45^{\circ}$, and $40^{\circ}$ azimuth angle.

## Input Arguments

## pos - Positions of array sensor elements

1-by- $N$ real-valued vector | 2 -by- $N$ real-valued matrix | 3 -by- $N$ real-valued matrix
Positions of the elements of a sensor array, specified as a 1 -by- $N$ vector, a 2 -by- $N$ matrix, or a 3 -by- $N$ matrix. In this vector or matrix, $N$ represents the number of elements of the array. Each column of pos represents the coordinates of an element. If pos is a 1 -by- $N$ vector, then it represents the $y$ coordinate of the sensor elements of a line array. The $x$ and $z$-coordinates are assumed to be zero. When pos is a 2-by- $N$ matrix, it represents the ( $y, z$ )-coordinates of the sensor elements of a planar array. This array is assumed to lie in the $y z$-plane. The $x$-coordinates are assumed to be zero. When pos is a 3 -by- $N$ matrix, then the array can have an arbitrary shape. Sensor positions are in terms of signal wavelength.

Example: [0,0,0; 0.1,0.4,0.3; 1,1,1]
Data Types: double

## ang - Beamforming directions

1-by- $M$ real-valued vector | 2 -by- $M$ real-valued matrix
Beamforming directions, specified as a 1-by- $M$ vector or a 2 -by- $M$ matrix. In this vector or matrix, $M$ represents the number of incoming signals. If ang is a 2 -by- $M$ matrix, each column specifies the direction in azimuth and elevation of the beamforming direction as [az;el]. Angular units are specified in degrees. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$ and the elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$. The azimuth angle is the angle between the $x$-axis and the projection of the beamforming direction vector onto the $x y$ plane. The angle is positive when measured from the $x$-axis toward the $y$-axis. The elevation angle is the angle between the beamforming direction vector and $x y$-plane. It is positive when measured towards the positive $z$ axis. If ang is a 1-by- $M$ vector, then it represents a set of azimuth angles with the elevation angles assumed to be zero.
Example: [45;10]
Data Types: double
cov - Sensor spatial covariance matrix
eye (N) (default) | $N$-by- $N$ complex-valued matrix
Sensor spatial covariance matrix, specified as an $N$-by- $N$ complex-valued matrix. $N$ is the number of array sensor elements.
Example: [5, 0.1;0.1,2]
Data Types: double
Complex Number Support: Yes

## angm - Mask angles

[ ] (default) | real-valued 1-by-K vector | real-valued 2-by-K matrix
Angles at which mask sidelobe levels are defined, specified as a real-valued 1-by- $K$ vector or a realvalued 2 -by- $K$ matrix where $K$ is the number of mask sidelobe levels. If angm is a 1 -by- $K$ vector, then it contains the azimuth angles of the mask directions. If angm is a 2-by- $K$ matrix, each column specifies the direction in the form [az;el]. Angle units are in degrees.
Data Types: double
sllm - Maximum allowable mask sidelobe levels
non-positive scalar (default) | non-positive real-valued 1-by-K vector
Maximum allowable mask sidelobe levels, specified as a non-positive scalar or non-positive realvalued 1-by- $K$ vector. $K$ is the number of mask sidelobe levels. Sidelobe levels are always less then or equal to zero.

- If $s l l m$ is a scalar, then it contains a uniform mask for all sidelobe levels and angm must be empty.
- If $\operatorname{sllm}$ is a 1 -by- $K$ vector, then $s l l m$ and angm must have the same number of columns; and sllm contains the mask sidelobe levels for corresponding mask angles, angm.

An empty sllm vector means that there are no constraints on the sidelobe levels. Units are in dB .

## Data Types: double

## angn - Null direction angles

[ ] (default) | real-valued 1-by-P vector | real-valued 2-by-P matrix
Null direction angles, specified as either a 1-by- $P$ vector or a 2 -by- $P$ matrix where $P$ is the number of null directions. If angn is a 1-by- $P$ vector, then it contains only the azimuth angles of directions. If
angn is a 2-by-P matrix, each column specifies the null direction in the form [az; el]. Angle units are in degrees.

Data Types: double

## Output Arguments

## wts - Beamformer weights

$N$-by-1 complex-valued vector
Beamformer weights, returned as a complex-valued $N$-by- 1 vector. $N$ represents the number of sensor elements of the array.

## Version History <br> Introduced in R2022b

## References

[1] Lebret, H., and S. Boyd. "Antenna Array Pattern Synthesis via Convex Optimization." IEEE Transactions on Signal Processing, vol. 45, no. 3, Mar. 1997, pp. 526-32. DOI.org (Crossref), https://doi.org/10.1109/78.558465.
[2] Golbon-Haghighi, Mohammad-Hossein, et al. "Design of a Cylindrical Crossed Dipole Phased Array Antenna for Weather Surveillance Radars." IEEE Open Journal of Antennas and Propagation, vol. 2, 2021, pp. 402-11. DOI.org (Crossref), https://doi.org/10.1109/ OJAP.2021.3059471.

See Also<br>steervec |cbfweights | lcmvweights | sensorcov | phased.MVDRBeamformer |<br>phased.LCMVBeamformer

## musicdoa

Estimate arrival directions of signals using MUSIC

## Syntax

```
doas = musicdoa(covmat,nsig)
[doas,spec,specang] = musicdoa(covmat,nsig)
[___] = musicdoa(covmat,nsig,___,'ScanAngles',scanangle)
[___] = musicdoa(covmat,nsig,___,'ElementSpacing',dist)
```


## Description

doas = musicdoa(covmat,nsig) uses the MUSIC algorithm to estimate the directions of arrival, doas, of nsig plane waves received on a uniform linear array (ULA). The argument covmat is a positive-definite Hermitian matrix representing the sensor covariance matrix. Detected sources appear as peaks in the spatial spectrum. The argument nsig is the number of arriving signals. Sensor elements are spaced one-half wavelength apart in units of wavelengths. The function forces exact conjugate symmetry of covmat by averaging the covariance matrix with its conjugate transpose.
[doas,spec,specang] = musicdoa(covmat,nsig) also returns the spatial spectrum, spec, and the nsig angles of the spectrum peaks, specang.
[___] = musicdoa(covmat, nsig, $\qquad$ , 'ScanAngles', scanangle) specifies the grid of broadside angles to search for spectrum peaks.
[___] = musicdoa(covmat, nsig, ___ ,'ElementSpacing',dist) specifies the spacing between array elements.

## Examples

## Estimate DOA of Multiple Signals Using MUSIC

Calculate the directions of arrival of 3 uncorrelated signals arriving at an 11-element ULA with halfwavelength spacing. Assume the signals are coming from the broadside angles of $0^{\circ},-12^{\circ}$, and $85^{\circ}$. The noise at each element is Gaussian white noise and is uncorrelated between elements. The SNR is 5 dB .

Specify the number of ULA elements and the element spacing (in wavelengths).

```
nelem = 11;
d = 0.5;
snr = 5.0;
elementPos = (0:nelem-1)*d;
```

Specify the number of signals and their broadside arrival angles.

```
nsig = 3;
angles = [0.0 -12.0 85.0];
```

Create the sensor covariance matrix.

```
covmat = sensorcov(elementPos,angles,db2pow(-snr));
```

Estimate the broadside arrival angles.

```
doas = musicdoa(covmat,nsig)
doas = 1\times3
    85 0 - 12
```

The estimated angles match the specified angles.

## Display MUSIC Spectrum of Multiple Signals

Calculate the directions of arrival of 3 uncorrelated signals arriving at an 11-element ULA with halfwavelength spacing. Assume the signals are coming from the broadside angles of $0^{\circ},-12^{\circ}$, and $85^{\circ}$. The noise at each element is Gaussian white noise and is uncorrelated between elements. The SNR is 2 dB .

Specify the number of ULA elements and the element spacing (in wavelengths).

```
nelem = 11;
d = 0.5;
snr = 2.0;
elementPos = (0:nelem-1)*d;
```

Specify the number of signals and their broadside arrival angles.

```
nsig = 3;
angles = [0.0 -12.0 85.0];
```

Create the sensor covariance matrix.

```
covmat = sensorcov(elementPos,angles,db2pow(-snr));
```

Compute the MUSIC spectrum and estimate the broadside arrival angles.

```
[doas,spec,specang] = musicdoa(covmat,nsig);
```

Plot the MUSIC spectrum.

```
plot(specang,10*log10(spec))
xlabel('Arrival Angle (deg)')
ylabel('Magnitude (dB)')
title('MUSIC Spectrum')
grid
```



The estimated angles match the specified angles.

## Display MUSIC Spectrum Over Specified Direction Span

Calculate the directions of arrival of 4 uncorrelated signals arriving at an 11 -element ULA. The element spacing is 0.5 wavelengths. Assume the signals are coming from the broadside angles of -$60.2^{\circ},-20.7^{\circ}, 0.5^{\circ}$, and $84.8^{\circ}$. The noise at each element is Gaussian white noise and is uncorrelated between elements. The SNR is 0 dB .

Specify the number of ULA elements and the element spacing (in wavelengths).

```
nelem = 11;
d = 0.5;
snr = 5.0;
elementPos = (0:nelem-1)*d;
```

Specify the number of signals and their broadside arrival angles.

```
nsig = 4;
angles = [-60.2 -20.7 0.5 84.8];
```

Create the sensor covariance matrix.

```
covmat = sensorcov(elementPos,angles,db2pow(-snr));
```

Compute the MUSIC spectrum and estimate the broadside arrival angles in the range from $-70^{\circ}$ to $90^{\circ}$ in $0.1^{\circ}$ increments.

```
[doas,spec,specang] = musicdoa(covmat,nsig,'ScanAngles',[-70:.1:90]);
```

Plot the MUSIC spectrum.

```
plot(specang,10*log10(spec))
xlabel('Arrival Angle (deg)')
ylabel('Magnitude (dB)')
title('MUSIC Spectrum')
grid
```


disp(doas)
$\begin{array}{llll}-60.2000 & 84.8000 & 0.5000 & -20.7000\end{array}$

The estimated angles match the specified angles.

## Display MUSIC Spectrum with Specified Element Spacing

Calculate the directions of arrival of 4 uncorrelated signals arriving at an 11-element ULA. The element spacing is 0.4 wavelengths spacing. Assume the signals are coming from the broadside angles of $-60^{\circ},-20^{\circ}, 0^{\circ}$, and $85^{\circ}$. The noise at each element is Gaussian white noise and is uncorrelated between elements. The SNR is 0 dB .

Specify the number of ULA elements and the element spacing (in wavelengths).
nelem = 11;
$\mathrm{d}=0.4$;
snr = 0.0;
elementPos $=(0:$ nelem-1 $) * d$;
Specify the number of signals and their broadside arrival angles.

```
nsig = 4;
angles = [-60.0 -20.0 0.0 85.0];
```

Create the sensor covariance matrix.

```
covmat = sensorcov(elementPos,angles,db2pow(-snr));
```

Compute the MUSIC spectrum and estimate the broadside arrival angles.

```
[doas,spec,specang] = musicdoa(covmat,nsig,'ElementSpacing',d);
```

Plot the MUSIC spectrum.

```
plot(specang,10*log10(spec))
```

xlabel('Arrival Angle (deg)')
ylabel('Magnitude (dB)')
title('MUSIC Spectrum')
grid


The estimated angles match the specified angles.

# Input Arguments <br> covmat - Sensor covariance matrix <br> positive-definite complex-valued $M$-by- $M$ matrix 

Sensor covariance matrix, specified as a complex-valued, positive-definite $M$-by- $M$ matrix. The quantity $M$ is the number of elements in the ULA array. The function forces Hermiticity property by averaging the matrix and its conjugate transpose.
Data Types: double
Complex Number Support: Yes
nsig - Number of arriving signals
positive integer
Number of arriving signals, specified as a positive integer. The number of signals must be smaller than the number of elements in the ULA array.
Example: 2
Data Types: double

## scanangle - Broadside search angles

[-90:90] (default)| real-valued vector
Broadside search angles, specified as a real-valued vector. Angles must lie in the range ( $-90^{\circ}, 90^{\circ}$ ) and must be in increasing order.
Example: [-40:0.5:50]
Data Types: double

## dist - Distance between array elements

0.5 (default) | real-valued positive scalar

Distance between array elements, specified as a real-valued positive scalar.
Example: 0.45
Data Types: double

## Output Arguments

## doas - Directions of arrival angles

real-valued vector
Directions of arrival angle, returned as a real-valued 1-by- $D$ vector, where $D$ is the number of arriving signals specified in nsig. Angle units are in degrees. Angle values lie in the range specified by scanangle.
spec - Spatial spectrum
positive real-valued vector
Spatial spectrum, returned as a positive real-valued vector. The dimension of spec equals the dimension of scanangle.

## specang - Broadside angles of spectrum peaks

real-valued vector
Broadside angle of spectrum, returned as a real-valued vector. The dimension of specang equals the dimension of scanangle.

## Version History

Introduced in R2016b

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
Does not support variable-size inputs.

## See Also

```
Functions
az2broadside|broadside2az|db2pow|espritdoa|rootmusicdoa|sensorcov
Objects
phased.MUSICEstimator|phased.MUSICEstimator2D
Topics
"Spherical Coordinates"
"MUSIC Super-Resolution DOA Estimation"
```


## nlfmspec2freq

Instantaneous frequency of nonlinear frequency-modulated waveform

## Syntax

freq $=n l f m s p e c 2 f r e q(B W, S)$

## Description

freq $=\mathrm{nlfmspec} 2 \mathrm{freq}(\mathrm{BW}, \mathrm{S})$ returns samples of the instantaneous frequency freq for a nonlinear frequency modulated (NLFM) pulse waveform. The waveform sweeps the bandwidth BW and has a power spectrum shape $S$. The frequency values in freq are found by applying the principle of stationary phase to the power spectrum shape $S$.

## Examples

## Waveform Derived from Taylor Spectrum Window

Create a nonlinear FM waveform derived from a power spectral density function shaped as a Taylor window with -35 dB sidelobes. The pulse bandwidth is 120 MHz and the pulse duration is $10 \mu \mathrm{sec}$. Generate matched filter coefficients and then apply a matched filter. Plot the resulting matched filter output to display the range sidelobe levels.

```
BW = 120e6;
T = 10e-6;
fs = 10*BW;
```

Generate 200 points of a waveform with instantaneous frequency values defined by a Taylor window. The window has -35 dB sidelobe levels.

```
w = taylorwin(200,4,-35);
freq = nlfmspec2freq(BW,w);
waveform = phased.CustomFMWaveform('SampleRate',fs, ...
    'PulseWidth',T,'FrequencyModulation',freq, ...
    'OutputFormat','Pulses','CoefficientsOutputPort',true);
disp(['Bandwidth = ',num2str(bandwidth(waveform)/le6),' MHz']);
Bandwidth = 119.9644 MHz
```

Obtain the matched filter coefficients from the waveform.

```
[wav,coeff] = waveform();
filter = phased.MatchedFilter('CoefficientsSource','Input port');
mfout = filter(wav,coeff);
```

Plot input signal and matched filter output.

```
t = (0:numel(wav)-1)/fs;
figure
subplot(121)
plot(t*le6,real(wav))
```

```
xlabel('Time (\mus)')
ylabel('Amplitude (V)')
title('Input Signal')
subplot(122)
plot(t*1e6,mag2db(abs(mfout)));
xlabel('Time (\mus)')
ylabel('Amplitude (dB)')
title('Matched Filter Output')
xlim([9 11]);
ylim([0 100]);
```



## Input Arguments

BW - Pulse waveform bandwidth
positive scalar
Pulse waveform bandwidth, specified as a positive scalar. Units are in Hz .
Example: 10e3

Data Types: double

## S - Power spectrum shape <br> real-valued vector

Power spectrum shape, specified as a real-valued vector. Units are dimensionless.
Data Types: double

## Output Arguments

## freq - Instantaneous waveform frequencies

real-valued row vector
Instantaneous waveform frequencies, returned as a real-valued row vector. The instantaneous frequencies form a single up-sweep. freq has the same number of elements as S. Units are Hz.
Data Types: double

## Version History

## Introduced in R2023a

## References

[1] Collins, T., and P. Atkins. "Nonlinear frequency modulation chirps for active sonar" IEE Proceedings-Radar, Sonar and Navigation 146.6 (1999): 312-316.
[2] Levanon, Nadav, and Eli Mozeson. Radar signals. John Wiley \& Sons, 2004, pp. 92-93.
[3] Doerry, Armin Walter. "Generating nonlinear FM chirp waveforms for radar". No.
SAND2006-5856. Sandia National Laboratories (SNL), Albuquerque, NM, and Livermore, CA (United States), 2006.
[4] Cook, C. E. "A class of nonlinear FM pulse compression signals." Proceedings of the IEEE 52.11 (1964): 1369-1371.

## See Also

phased.NonlinearFMWaveform| phased.CustomFMWaveform

## Topics

"Waveform Analysis Using the Ambiguity Function"

## noisefigure

Receiver system noise figure of cascaded stages

## Syntax

```
cnf = noisefigure(nf,g)
[cnf,cg] = noisefigure(nf,g)
[cnf,cg,ctemp] = noisefigure(nf,g,reftemp)
```


## Description

$\mathrm{cnf}=$ noisefigure $(\mathrm{nf}, \mathrm{g})$ returns the scalar noise figure in decibels of the cascaded stages of a receiver system. The vector nf contains the noise figures for the different stages and the vector g contains the gains.
[ $\mathrm{cnf}, \mathrm{cg}]=$ noisefigure $(\mathrm{nf}, \mathrm{g})$ returns the scalar total gain in decibels of the cascaded system.
[cnf,cg,ctemp] = noisefigure(nf,g,reftemp) specifies the reference temperature in kelvins and returns the noise temperature of the cascaded receiver stages.

## Examples

## Cascaded Noise Figure of Receiver System

Compute the cascaded noise figure and total gain of a receiver system. The system has seven stages, with these values:

1 LNA with a noise figure of 1.0 dB and a gain of 15.0 dB
2 RF filter with a noise figure of 0.5 dB and a gain of -0.5 dB
3 Mixer with a noise figure of 5.0 dB and a gain of -7.0 dB
4 IF filter with a noise figure of 1.0 dB and a gain of -1.0 dB
5 IF preamplifier with a noise figure of 0.6 dB and a gain of -15.0 dB
6 IF stages with a noise figure of 1.0 dB and a gain of 20.0 dB
7 Phase detectors with a noise figure of 6.0 dB and a gain of -5.0 dB

```
nf = [1.0 0.5 5.0 1.0 0.6 1.0 6.0];
g = [15.0 -0.5 -7.0 -1.0 15.0 20.0 -5.0];
[cnf,ng] = noisefigure(nf,g)
cnf = 1.5252
ng = 36.5000
```

Compute the noise temperature of the cascaded receiver stages. Specify the reference temperature as 300 K .

```
rtemp = 300;
[~,~,ctemp] = noisefigure(nf,g,rtemp)
ctemp = 426.2281
```


## Input Arguments

nf - Stage-by-stage noise figures
vector
Stage-by-stage noise figures in decibels, specified as a vector.
Data Types: double
g - Stage-by-stage gains
vector
Stage-by-stage gains in decibels, specified as a vector.
Data Types: double
reftemp - Reference temperature
290 K (default) | nonnegative scalar
Reference temperature, specified as a nonnegative scalar in kelvins.
Data Types: double

## Output Arguments

## cnf - Noise figure of cascaded receiver stages

scalar
Noise figure of cascaded receiver stages, returned as a scalar in decibels.

## cg - Total gain of cascaded system

scalar
Total gain of cascaded system, returned as a scalar in decibels.
ctemp - Noise temperature of cascaded receiver stages
scalar
Noise temperature of cascaded receiver stages, returned as a scalar in kelvins.

## Version History

Introduced in R2021a

## References

[1] Barton, David K. Radar System Analysis and Modeling. Boston: Artech House, 2005.

## See Also

systemp

## noisepow

Receiver noise power

## Syntax

NPOWER = noisepow(NBW,NF,REFTEMP)

## Description

NPOWER = noisepow(NBW, NF, REFTEMP) returns the noise power, NPOWER, in watts for a receiver. This receiver has a noise bandwidth NBW in hertz, noise figure NF in decibels, and reference temperature REFTEMP in kelvins.

## Examples

## Compute Receiver Noise Power with Specified Temperature

Calculate the noise power of a receiver having a noise bandwidth of 10 kHz , a noise figure of 1 dB , and a reference temperature of 300 K .

```
npower = noisepow(10e3,1,300)
```

npower $=5.2144 \mathrm{e}-17$

## Input Arguments

## NBW - Noise bandwidth of the receiver

positive scalar
Noise bandwidth of the receiver in hertz, specified as a positive scalar. For a superheterodyne receiver, the noise bandwidth is approximately equal to the bandwidth of the intermediate frequency stages [1].

## Data Types: double

## NF - Noise figure

nonnegative scalar
Noise figure in decibels, specified as a nonnegative scalar. The noise figure is a dimensionless quantity that indicates how much a receiver deviates from an ideal receiver in terms of internal noise. An ideal receiver only produces the expected thermal noise power for a given noise bandwidth and temperature. A noise figure of $1(0 \mathrm{~dB})$ indicates that the noise power of a receiver equals the noise power of an ideal receiver. Because an actual receiver cannot exhibit a noise power value less than an ideal receiver, the noise figure is always greater than or equal to $1(0 \mathrm{~dB})$.

Data Types: double

## REFTEMP - Reference temperature

nonnegative scalar

Reference temperature in kelvins, specified as a nonnegative scalar. This argument specifies the temperature of the receiver. Typical values range from 290 to 300 kelvins.

Data Types: double

## Output Arguments

NPOWER - Noise power
nonnegative scalar
Noise power in watts, returned as a nonnegative scalar. The internal noise power contribution of the receiver to the signal-to-noise ratio.

## Version History <br> Introduced in R2011a

## References

[1] Skolnik, M. Introduction to Radar Systems. New York: McGraw-Hill, 1980.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
Does not support variable-size inputs.

## See Also

phased.ReceiverPreamp

## npwgnthresh

Detection SNR threshold for signal in white Gaussian noise

## Syntax

```
snrthresh = npwgnthresh(pfa)
snrthresh = npwgnthresh(pfa,numpulses)
snrthresh = npwgnthresh(pfa,numpulses,dettype)
snrthresh = npwgnthresh(pfa,numpulses,dettype,outscale)
```


## Description

snrthresh = npwgnthresh(pfa) calculates the "Detection SNR Threshold" on page 2-234 in decibels for detecting a deterministic signal in white Gaussian noise. The detection uses the NeymanPearson (NP) decision rule to achieve a specified probability of false alarm, pfa. This function uses a square-law detector.
snrthresh = npwgnthresh(pfa, numpulses) specifies numpulses as the number of pulses used in the pulse integration.
snrthresh = npwgnthresh(pfa, numpulses, dettype) specifies dettype as the type of detection. A square law detector is used in noncoherent detection.
snrthresh = npwgnthresh(pfa, numpulses,dettype,outscale) specifies the output scale.

## Examples

## Compute Detection Threshold from Pfa

Calculate the detection threshold that achieves a probability of false alarm (pfa) of 0.01 . Assume a single pulse with a real detection type. Then, verify that this threshold produces a pfa of approximately 0.01 . Do this by constructing 10000 real white gaussian noise (wgn) samples and computing the fraction of samples exceeding the threshold.

Compute the threshold from pfa. The detection threshold is expressed as a signal-to-noise ratio in db .

```
pfa = 0.01;
numpulses = 1;
snrthreshold = npwgnthresh(pfa,numpulses,"real")
snrthreshold = 7.3335
```

Compute fraction of simulated noise samples exceeding the threshold. The noise has unit power with 10000 samples.

```
noisepower = 1;
Ntrial = 10000;
noise = sqrt(noisepower)*randn(1,Ntrial);
```

Express the threshold in amplitude units.

```
threshold = sqrt(noisepower*db2pow(snrthreshold));
calculated_Pfa = sum(noise>threshold)/Ntrial
calculated_Pfa = 0.0107
```


## Detection Threshold Versus Number of Pulses

Plot the SNR detection threshold against the number of pulses, for real and complex noise. In each case, the SNR detection threshold is set for a probability of false alarm (pfa) of 0.001.

Compute detection threshold for 1 to 10 pulses of real and complex noise.

```
Npulses = 10;
snrcoh = zeros(1,Npulses);
snrreal = zeros(1,Npulses);
Pfa = 1e-3;
for num = 1:Npulses
    snrreal(num) = npwgnthresh(Pfa,num,"real");
    snrcoh(num) = npwgnthresh(Pfa,num,"coherent");
end
```

Plot the detection thresholds against number of pulses.

```
plot(snrreal,"o-")
hold on
plot(snrcoh,".-")
hold off
legend("Real data with integration",...
    "Complex data with coherent integration",...
    Location="southeast")
xlabel("Number of Pulses")
ylabel("SNR Required for Detection")
title("SNR Threshold for P_F_A = "+Pfa)
```



## Linear Detection Threshold Versus Number of Pulses

Plot the linear detection threshold against the number of pulses, for real and complex data. In each case, the threshold is set for a probability of false alarm of 0.001 .

Compute detection threshold for 1 to 10 pulses of real and complex noise.

```
Npulses = 10;
snrcoh = zeros(1,Npulses);
snrreal = zeros(1,Npulses);
Pfa = 1e-3;
for num = 1:Npulses
    snrreal(num) = npwgnthresh(Pfa,num,"real","linear");
    snrcoh(num) = npwgnthresh(Pfa,num,"coherent","linear");
end
```

Plot the detection thresholds against number of pulses.

```
plot(snrreal,"o-")
hold on
plot(snrcoh,".-")
hold off
legend("Real data with integration",...
    "Complex data with coherent integration",...
```

Location="southeast")
xlabel("Number of Pulses")
ylabel("Detection Threshold")
title("Linear Detection Threshold for P_F_A = "+Pfa)


## Input Arguments

pfa - Probability of false alarm
scalar in the range (0, 1)
Probability of false alarm, specified as a scalar in the range $(0,1)$.
Data Types: double
numpulses - Number of pulses
1 (default) | positive integer
Number of pulses used in the integration, specified as a positive integer.
Data Types: double
dettype - Type of pulse integration
"noncoherent" (default) | "coherent" | "real"

Specifies the type of pulse integration used in the NP decision rule, specified as "coherent", "noncoherent", or "real". "coherent" uses magnitude and phase information of complex-valued samples. "noncoherent" uses squared magnitudes. "real" uses real-valued samples.

## Data Types: char | string

outscale - Scale of the output value
"db" (default) | "linear"
Scale of the output value, specified as "db" or "linear". When outscale is set to "linear", the returned threshold represents amplitude.

Data Types: char|string

## Output Arguments

## snrthresh - Detection threshold

scalar
Detection threshold, returned as a scalar. The detection threshold is expressed in terms of the signal-to-noise ratio in decibels or in linear units if outscale is set to "linear". The relationship between the linear threshold and the threshold in dB is

$$
T_{d B}=20 \log _{10} T_{l i n}
$$

## More About

## Detection SNR Threshold

The output of npwgnthresh determines the detection threshold required to achieve a particular Pfa.
The threshold increases when pulse integration is used in the receiver. This threshold is not the single sample SNR that is used as an input to rocsnr or as the output of rocpfa, albersheim, and shnidman. For any fixed Pfa, you can decrease the single sample SNR required to achieve a particular Pd when pulse integration is used in the receiver. See "Signal Detection in White Gaussian Noise" and "Source Localization Using Generalized Cross Correlation" for examples of how to use npwgnthresh in a detection system.

## Detection in Real-Valued White Gaussian Noise

This function is designed for the detection of a nonzero mean in a sequence of Gaussian random variables. The function assumes that the random variables are independent and identically distributed, with zero mean. The linear detection threshold $\lambda$ for an NP detector is

$$
\frac{\lambda}{\sigma}=\sqrt{2 N} \operatorname{erfc}^{-1}\left(2 P_{f a}\right)
$$

This threshold can also be expressed as a signal-to-noise ratio in decibels

$$
10 \log _{10}\left(\frac{\lambda^{2}}{\sigma^{2}}\right)=10 \log _{10}\left(2 N\left(\operatorname{erfc}^{-1}\left(2 P_{f a}\right)\right)^{2}\right)
$$

In these equations

- $\sigma^{2}$ is the variance of the white Gaussian noise sequence
- $N$ is the number of samples
- $e r f c^{-1}$ is the inverse of the complementary error function
- $P_{f a}$ is the probability of false alarm

Note For probabilities of false alarm greater than or equal to $1 / 2$, the formula for detection threshold as SNR is invalid because erfc ${ }^{-1}$ is less than or equal to zero for values of its argument greater than or equal to one. In that case, use the linear output of the function invoked by setting outscale to'linear'.

## Detection in Complex-Valued White Gaussian Noise (Coherent Samples)

The NP detector for complex-valued signals is similar to that discussed in "Source Localization Using Generalized Cross Correlation". In addition, the function makes these assumptions:

- The variance of the complex-valued Gaussian random variable is divided equally among the real and imaginary parts.
- The real and imaginary parts are uncorrelated.

Under these assumptions, the linear detection threshold for an NP detector is

$$
\frac{\lambda}{\sigma}=\sqrt{N} \operatorname{erfc}^{-1}\left(2 P_{f a}\right)
$$

and expressed as a signal-to-noise ratio in decibels is:

$$
10 \log _{10}\left(\frac{\lambda^{2}}{\sigma^{2}}\right)=10 \log _{10}\left(N\left(\operatorname{erfc}^{-1}\left(2 P_{f a}\right)\right)^{2}\right)
$$

Note For probabilities of false alarm greater than or equal to $1 / 2$, the formula for detection threshold as SNR is invalid because erfc ${ }^{-1}$ is less than or equal to zero for when its argument is greater than or equal to one. In that case, select linear output for the function by setting outscale to 'linear'.

## Detection of Noncoherent Samples in White Gaussian Noise

For noncoherent samples in white Gaussian noise, detection of a nonzero mean leads to a square-law detector. For a detailed derivation, see [2], pp. 324-329.

The linear detection threshold for the noncoherent NP detector is:

$$
\frac{\lambda}{\sigma}=\sqrt{P^{-1}\left(N, 1-P_{f a}\right)}
$$

The threshold expressed as a signal-to-noise ratio in decibels is:

$$
10 \log _{10}\left(\frac{\lambda^{2}}{\sigma^{2}}\right)=10 \log _{10} P^{-1}\left(N, 1-P_{f a}\right)
$$

where $P^{-1}(x, y)$ is the inverse of the lower incomplete gamma function, $P_{f a}$ is the probability of false alarm, and $N$ is the number of pulses.

## Version History

Introduced in R2011a

## References

[1] Kay, S. M. Fundamentals of Statistical Signal Processing: Detection Theory. Upper Saddle River, NJ: Prentice Hall, 1998.
[2] Richards, M. A. Fundamentals of Radar Signal Processing. New York: McGraw-Hill, 2005.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
Does not support variable-size inputs.

## See Also

rocpfa|rocsnr|albersheim | shnidman
Topics
"Signal Detection in White Gaussian Noise"
"Signal Detection Using Multiple Samples"

## omphybweights

Compute hybrid beamforming weights using orthogonal matching pursuit

## Syntax

[wpbb,wprf] = omphybweights(chanmat,ns,ntrf,at)
[wpbb,wprf,wcbb,wcrf] = omphybweights(chanmat,ns,ntrf,at,nrrf,ar)
[ ] = omphybweights(chanmat,ns,ntrf,at,nrrf,ar,npow)

## Description

[wpbb,wprf] = omphybweights(chanmat,ns,ntrf,at) returns the hybrid precoding weights wpbb and wprf for the channel matrix chanmat. The weights are computed using an orthogonal matching pursuit algorithm. ns is the number of independent data streams propagated through the channel. ntrf specifies the number of RF chains in the transmit array. at is a collection of possible analog weights for wprf. Together, the precoding weights approximate the optimal full digital precoding weights of chanmat.
[wpbb,wprf,wcbb,wcrf] = omphybweights(chanmat,ns,ntrf,at,nrrf,ar) also returns the hybrid combining weights wcbb and wcrf. The input nrrf specifies the number of RF chains in the receive array. ar is a collection of possible analog weights for wcrf.
[___] = omphybweights(chanmat,ns,ntrf,at,nrrf,ar,npow) also specifies the noise power npow in each receive antenna element. All subcarriers are assumed to have the same noise power.

## Examples

## Calculate Effective Channel Matrix

Assume an 8-by-4 MIMO system with four RF chains in a transmit array and two RF chains in a receive array. Show that the hybrid weights can support transmitting two data streams simultaneously.

Specify the positions of the transmitters and receivers in uniform line arrays.

```
txpos = (0:7)*0.5;
rxpos = (0:3)*0.5;
```

Construct the channel matrix.
chanmat $=$ scatteringchanmtx(txpos,rxpos,10);
Specify the number of transmit and receive RF chains.

```
ntrf = 4;
nrrf = 2;
```

Specify two data streams.
ns $=2$;
Set up the steering vector dictionaries for the transmitting and receiving arrays.

```
txdict = steervec(txpos,-90:90);
rxdict = steervec(rxpos,-90:90);
```

Compute the precoding and combining weights.
[Fbb,Frf,Wbb,Wrf] = omphybweights(chanmat,ns,ntrf,txdict,nrrf,rxdict);
Calculate the effective channel matrix from the weights. A diagonal effective channel matrix indicates the capability of simultaneous transmission of multiple data streams.

```
chan_eff = Fbb*Frf*chanmat*Wrf*Wbb
chan_eff = 2\times2 complex
1.0000 - 0.0000i 0.0000 + 0.0000i
0.0000 + 0.0000i 1.0000 + 0.0000i
```


## Input Arguments

## chanmat - Channel response matrix

complex-valued $N_{\mathrm{t}}$-by- $N_{\mathrm{r}}$ matrix | complex-valued $L$-by- $N_{\mathrm{t}}$-by- $N_{\mathrm{r}}$ array
Channel response matrix, specified as an $N_{\mathrm{t}}$-by- $N_{\mathrm{r}}$ matrix or a complex-valued $L$-by- $N_{\mathrm{t}}-$ by $-N_{\mathrm{r}}$ array where

- $N_{\mathrm{t}}$ is the number of elements in the transmitting array.
- $N_{\mathrm{r}}$ is the number of elements in the receiving array.
- $L$ is the number of subcarriers.

Data Types: double
Complex Number Support: Yes
ns - Number of independent data streams
positive integer
Number of independent data streams propagated through the channel, specified as a positive integer.
Data Types: double

## ntrf - Number of RF chains in transmit array

positive integer
Number of RF chains in the transmit array, specified as a positive integer.
Data Types: double
at - Collection of possible analog weights
complex-valued $N_{\mathrm{t}}$-by- $P$ matrix | complex-valued $N_{\mathrm{t}}$-by- $P$-by- $L$ array
Collection of possible analog weights for wprf, specified as a complex-valued matrix or array.

- When chanmat is an $N_{\mathrm{t}}$-by- $N_{\mathrm{r}}$ matrix, at is a complex-valued $N_{\mathrm{t}}$-by- $P$ matrix. Each column represents a vector of analog weights.
- When chanmat is an $L$-by- $N_{\mathrm{t}}$-by- $N_{\mathrm{r}}$ array, at is a complex-valued $N_{\mathrm{t}}$-by- $P$-by- $L$ array. Each page is an $N_{\mathrm{t}}$-by- $P$ matrix. Each column represents a vector of analog weights.
- $N_{\mathrm{t}}$ is the number of elements in the transmitting array.
- $N_{\mathrm{r}}$ is the number of elements in the receiving array.
- $L$ is the number of subcarriers.
- $\quad P$ is the number of vectors of analog weights in the collection.

Data Types: double
Complex Number Support: Yes

## nrrf - Number of RF chains in receive array

positive integer
Number of RF chains in the receive array, specified as a positive integer.
Data Types: double

## ar - Collection of possible analog weights

complex-valued $N_{\mathrm{r}}$-by- $Q$ matrix | complex-valued $N_{\mathrm{r}}$-by- $Q$-by- $L$ array
Collection of possible analog weights for wprf, specified as a complex-valued matrix or array.

- When chanmat is an $N_{\mathrm{t}}$-by- $N_{\mathrm{r}}$ matrix, ar is a complex-valued $N_{\mathrm{r}}$-by- $Q$ matrix. Each column represents a vector of analog weights.
- When chanmat is an $L$-by- $N_{\mathrm{t}}$-by- $N_{\mathrm{r}}$ array, ar is a complex-valued $N_{\mathrm{r}}$-by- $Q$-by- $L$ array. Each page is an $N_{\mathrm{r}}$-by- $Q$ matrix. Each column represents a vector of analog weights.
- $N_{t}$ is the number of elements in the transmitting array.
- $N_{r}$ is the number of elements in the receiving array.
- $L$ is the number of subcarriers.
- $Q$ is the number of vectors of analog weights in the collection.


## Data Types: double

Complex Number Support: Yes

## npow - Noise power

0 (default) | nonnegative scalar
Noise power in each receive antenna element, specified as a nonnegative scalar. All subcarriers have the same noise power.
Data Types: double

## Output Arguments

## wpbb - Hybrid baseband precoding weights

complex-valued $N_{\mathrm{s}}$-by- $N_{\text {trf }}$ matrix | complex-valued $L$-by- $N_{\mathrm{s}}$-by- $N_{\text {trf }}$ array
Hybrid baseband precoding weights, returned as a complex-valued matrix or array.

- When chanmat is an $N_{\mathrm{t}}$-by- $N_{\mathrm{r}}$ matrix, wpbb is a complex-valued $N_{\mathrm{s}}$-by- $N_{\text {trf }}$ matrix.
- When chanmat is an $L$-by- $N_{\mathrm{t}}$-by- $N_{\mathrm{r}}$ array, wpbb is a complex-valued $L$-by- $N_{\mathrm{s}}$-by- $N_{\mathrm{trf}}$ array.
- $N_{s}$ is the number of independent data streams specified by the ns argument.
- $N_{\text {trf }}$ is the number of RF chains in the transmit array specified by the ntrf argument.
- $L$ is the number of subcarriers.


## wprf - Hybrid RF precoding weights

complex-valued $N_{\text {trf }}$ by- $N_{\mathrm{t}}$ matrix | complex-valued L-by- $N_{\text {trr }}$ by- $N_{\mathrm{t}}$ array
Hybrid RF precoding weights, returned as a complex-valued matrix or array.

- When chanmat is an $N_{\mathrm{t}}$-by- $N_{\mathrm{r}}$ matrix, wprf is a complex-valued $N_{\text {trf }}$-by- $N_{\mathrm{t}}$ matrix.
- When chanmat is an $L$-by- $N_{\mathrm{t}}$-by- $N_{\mathrm{r}}$ array, wprf is a complex-valued $L$-by- $N_{\mathrm{trf}}$ by- $N_{\mathrm{t}}$ array.
- $N_{t}$ is the number of elements in the transmitting array.
- $N_{t r f}$ is the number of RF chains in the transmit array specified by the ntrf argument.
- $L$ is the number of subcarriers.
wcbb - Hybrid baseband combining weights
complex-valued $N_{\text {rrf }}$ by- $N_{\mathrm{s}}$ matrix | complex-valued L-by- $N_{\text {rrf }}$ by- $N_{\mathrm{s}}$ array
Hybrid baseband combining weights, returned as a complex-valued matrix or array.
- When chanmat is an $N_{\mathrm{t}}$-by- $N_{\mathrm{r}}$ matrix, wcbb is a complex-valued $N_{\mathrm{rrf}}$-by- $N_{\mathrm{s}}$ matrix.
- When chanmat is an $L$-by- $N_{\mathrm{t}}$-by- $N_{\mathrm{r}}$ array, wcbb is a complex-valued $L$-by- $N_{\mathrm{rrf}}$ by- $N_{\mathrm{s}}$ array.
- $N_{\mathrm{s}}$ is the number of independent data streams specified by the ns argument.
- $N_{\text {rrf }}$ is the number of RF chains in the receive array specified by the nrrf argument.
- $L$ is the number of subcarriers.


## wcrf - Hybrid RF combining weights

complex-valued $N_{\mathrm{r}}$-by- $N_{\text {rrf }} \mid$ complex-valued $L$-by- $N_{\mathrm{r}}$-by- $N_{\text {rrf }}$ array
Hybrid RF combining weights, returned as a complex-valued matrix or array.

- When chanmat is an $N_{\mathrm{t}}$-by- $N_{\mathrm{r}}$ matrix, wcrf is a complex-valued $N_{\mathrm{r}}$-by- $N_{\text {rrf }}$ matrix.
- When chanmat is an $L$-by- $N_{\mathrm{t}}$-by- $N_{\mathrm{r}}$ array, wcrf is a complex-valued $L$-by- $N_{\mathrm{r}}$-by- $N_{\mathrm{rrf}}$ array.
- $N_{t}$ is the number of elements in the transmitting array.
- $N_{r r f}$ is the number of RF chains in the receive array specified by the nrrf argument.
- $L$ is the number of subcarriers.


## More About

## Precoding Weights

The matrix product of the precoding weights wpbb x wprf approximates the optimal full digital precoding weights of the channel matrix chanmat.

## Combining Weights

The combining weights wcbb and wcrf, together with the precoding weights, diagonalize the channel into independent subchannels. The matrix product wpbb x wprf $x$ chanmat $x$ wcrfx wcbb is approximately diagonal.

## Version History

Introduced in R2019b

## References

[1] Ayach, Omar El et al. "Spatially Sparse Precoding in Millimeter Wave MIMO Systems" IEEE Trans on Wireless Communications. Vol. 13, No. 3, March 2014.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.

## See Also

diagbfweights |ompdecomp|phased.ScatteringMIMOChannel|scatteringchanmtx

## ompdecomp

Decompose signal using orthogonal matching pursuit

## Syntax

[coeff,dictatom,atomidx,errnorm] = ompdecomp(X,dict)
[coeff,dictatom,atomidx,errnorm] = ompdecomp(X,dict,'MaxSparsity',nm)
[coeff,dictatom,atomidx,errnorm] = ompdecomp(X,dict,'NormWeight',wts)

## Description

[coeff,dictatom,atomidx,errnorm] = ompdecomp(X,dict) computes the decomposition matrices coeff and dictatom of the signal $X$. The product of the decomposition matrices, dictatom x coeff, approximates $X$. The atoms in dictatom are selected from dict. atomidx are the indices in dict corresponding to dictatom. errnorm is the decomposition error. The decomposition is based on an orthogonal matching pursuit (OMP) algorithm that minimizes the Frobenius norm \|X dictatom x coeff||.
[coeff,dictatom,atomidx,errnorm] = ompdecomp(X,dict,'MaxSparsity',nm) also specifies the maximum sparsity nm .
[coeff,dictatom,atomidx,errnorm] = ompdecomp(X,dict,'NormWeight', wts) minimizes the weighted Frobenius norm ||wts ${ }^{1 / 2}(\mathrm{X}$ - dictatom x coeff)|| using the weights wts.

## Examples

## Decompose ULA Beamsteering Weights

Given a set of optimal, full-digital, beamforming weights for an 8-element uniform linear array, decompose the weights into a product of analog and digital beamforming weights. Assume two RF chains. Show that the combined weights achieve a performance similar to the optimal weights.

Specify the optimal, full-digital, beamforming weights.

```
wopt = steervec((0:7)*0.5,[20 -40]);
```

Create a dictionary of steering vectors.
stvdict $=$ steervec((0:7)*0.5,-90:90);
Perform the decomposition using OMP. Set the maximum sparsity to two.

```
[wbb,wrf,wdictidx,normerr] = ompdecomp(wopt,stvdict,'MaxSparsity',2);
```

Compare the beam patterns derived from the optimal weights and the hybrid weights. The plot shows that the decomposition of wopt into wrf and wbb is almost exact.

```
plot(-90:90,abs(sum(wopt'*stvdict)),'-', ...
    -90:90,abs(sum((wrf*wbb)'*stvdict)),'--','LineWidth', 2)
xlabel('Angles (degrees)')
```

ylabel('Amplitude')
legend('Optimal','Hybrid')


## Input Arguments

X - Input data
complex-valued $N$-by- $N_{\mathrm{c}}$ matrix
Input data to be decomposed, specified as a complex-valued $N$-by- $N_{\mathrm{c}}$ matrix.
Data Types: double
Complex Number Support: Yes

## dict - Dictionary of atoms

complex-valued matrix
Dictionary of atoms, specified as a complex-valued matrix. The function uses a subset of atoms from the dictionary to construct the data.

Data Types: double
Complex Number Support: Yes
nm - Maximum sparsity
1 (default) | positive integer

Maximum sparsity of the decomposition, specified as a positive integer. The decomposition stops when the sparsity of nm is achieved.
Example: 5
Dependencies
Use this argument with the syntax specifying 'MaxSparsity'.
Data Types: double

## wts - Norm weights

$N$-by- $N$ identity matrix (default) | complex-valued $N$-by- $N$ matrix
Norm weights used by OMP to minimize the weighted Frobenius norm of \|wts ${ }^{1 / 2} \mathrm{x}(\mathrm{X}$ - dictatom x coeff)||, specified as a complex-valued $N$-by- $N$ matrix.
Example: 5
Dependencies
Use this argument with the syntax specifying 'NormWeight'.
Data Types: double
Complex Number Support: Yes

## Output Arguments

## coeff - Coefficients of basis atoms

$N_{\mathrm{s}}$-by- $\mathrm{N}_{\mathrm{c}}$ matrix
Coefficients of basis atoms, returned as an $N_{s}$-by- $N_{c}$ matrix. The rows represent the coefficients for the corresponding atoms in dictatom. $N_{\mathrm{s}}$ represents the number of atoms selected from the dictionary and is a measure of signal sparsity.
Data Types: double
Complex Number Support: Yes

## dictatom - Signal basis atoms

$N$-by- $N_{\mathrm{s}}$ matrix
Signal basis atoms, returned as an $N$-by- $N_{\mathrm{s}}$ matrix. The columns are the atoms forming the basis of the signal. These atoms are a subset of the dictionary specified in dict. $N_{\mathrm{s}}$ represents the number of selected atoms and is a measure of signal sparsity.
Data Types: double
Complex Number Support: Yes

## atomidx - Indices of selected atoms

integer-valued length $-N_{\mathrm{s}}$ row vector
Indices of the atoms selected from the dictionary dict, returned as a length- $N_{s}$ row vector where dict(:,atomidx) = dictatom.

Data Types: double
errnorm - Norm of decomposition error
0 (default) | nonnegative scalar

Norm of the decomposition error, returned as a nonnegative scalar.
Data Types: double

## More About

## Hybrid Beamforming Weights

In the context of hybrid beamforming, the coeff argument represents digital weights. dictatom represents analog weights and dict is a collection of steering vectors that can be used as analog weights.

## Version History

Introduced in R2019b

## References

[1] Ayach, Omar El et al. "Spatially Sparse Precoding in Millimeter Wave MIMO Systems" IEEE Trans on Wireless Communications. Vol. 13, No. 3, March 2014.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{Tm}}$.

## See Also

omphybweights | diagbfweights | phased.ScatteringMIMOChannel| scatteringchanmtx

## pambgfun

Periodic ambiguity function

## Syntax

```
pafmag = pambgfun(X,fs)
[pafmag,delay,doppler] = pambgfun(X,fs)
[pafmag,delay,doppler] = pambgfun(X,fs,P)
[pafmag,delay] = pambgfun(
```

$\qquad$

``` , 'Cut','Doppler')
[pafmag,delay] = pambgfun(
```

$\qquad$

``` , 'Cut', 'Doppler','CutValue', V)
[pafmag,doppler] = pambgfun(
```

$\qquad$

``` , 'Cut','Delay')
[pafmag,doppler] = pambgfun(__,'Cut','Delay','CutValue',V)
[pafmag,delay,doppler] = pambgfun(
```

$\qquad$

``` ,'Cut','2D')
pambgfun(
``` \(\qquad\)
``` )
```


## Description

pafmag = pambgfun $(X, f s)$ returns the magnitude of the normalized periodic ambiguity function (PAF) for one period of the periodic signal X . fs is the sampling rate.
[pafmag,delay,doppler] = pambgfun(X,fs) also returns the time delay vector, delay, and the Doppler shift vector, doppler. The delay vector is along the zero Doppler cut of the PAF. The Doppler shift vector is along the zero delay cut.
[pafmag, delay,doppler] = pambgfun( $\mathrm{X}, \mathrm{fs}, \mathrm{P}$ ) returns the magnitude of the normalized PAF for P periods of the periodic signal X .
[pafmag, delay] = pambgfun(__ , 'Cut', 'Doppler') returns the PAF, pafmag, along a zero Doppler cut. The delay argument contains the time delay vector corresponding to the columns of pafmag.
[pafmag, delay] = pambgfun(__, 'Cut','Doppler','CutValue', V) returns the PAF, pafmag, along a nonzero Doppler cut specified by V. The delay argument contains the time delay vector corresponding to the columns of pafmag.
[pafmag, doppler] = pambgfun(__, 'Cut','Delay') returns the PAF, pafmag, along the zero delay cut. The doppler argument contains the Doppler shift vector corresponding to the rows of pafmag.
[pafmag, doppler] = pambgfun(__, 'Cut','Delay','CutValue', V) returns the PAF, pafmag, along a nonzero delay cut specified by V . The doppler argument contains the Doppler shift vector corresponding to the rows of pafmag.
[pafmag, delay,doppler] = pambgfun( __ , 'Cut','2D') returns the PAF, pafmag, for all delays and Doppler shifts. The doppler argument contains the Doppler shift vector corresponding to the rows of pafmag. The delay argument contains the time delay vector corresponding to the columns of pafmag. You cannot use 'CutValue' when 'Cut' is set to '2D'.
pambgfun( $\qquad$ ) with no output arguments plots the PAF. When 'Cut ' is ' 2 D ', the function produces a contour plot of the PAF function. When 'Cut' is 'Delay' or 'Doppler', the function produces a line plot of the PAF cut.

## Examples

## Periodic Ambiguity Function for Rectangular Waveform

Plot the PAF function of a rectangular pulse waveform for one period. Assume the pulse repetition frequency (PRF) is 10.0 kHz and that the sampling frequency is a multiple of the PRF.

```
PRF = 10.0e3;
fs = 101*PRF;
waveform = phased.RectangularWaveform('SampleRate',fs,'PulseWidth',1e-5, ...
    'NumPulses',1,'PRF',PRF);
wav = waveform();
pamf = pambgfun(wav,fs);
imagesc(pamf)
axis equal
axis tight
```



## Periodic Ambiguity Function with Delay and Doppler Output

Plot the periodic ambiguity function of a rectangular pulse waveform for one period. Assume the pulse repetition frequency (PRF) is 10.0 kHz and that the sampling frequency is a multiple of the PRF. Return the Doppler and delay values from the pambgfun function.

```
PRF = 10.0e3;
fs = 101*PRF;
waveform = phased.RectangularWaveform('SampleRate',fs,'PulseWidth',1e-5, ...
    'NumPulses',1,'PRF',PRF);
wav = waveform();
[pamf,delays,doppler] = pambgfun(wav,fs);
```

Plot the periodic ambiguity function.

```
imagesc(delays*1e6,doppler/1000,pamf)
axis xy
xlabel('Delay (\musec)')
ylabel('Doppler Shift (kHz)')
colorbar
```



## Zero Delay Cut of Periodic Ambiguity Function

Plot a cut at zero delay for the periodic ambiguity function of a rectangular pulse waveform for five periods. Assume the pulse repetition frequency is 10.0 kHz and that the sampling frequency is a multiple of the PRF. Return the Doppler and delay values from the function.

```
PRF = 10.0e3;
fs = 101*PRF;
waveform = phased.RectangularWaveform('SampleRate',fs,'PulseWidth',le-5, ...
    'NumPulses',1,'PRF',PRF);
wav = waveform();
```

Find the periodic ambiguity functions along a zero delay cut for one and for five periods.

```
[pamf,delays,doppler] = pambgfun(wav,fs,1);
f1 = pamf(:,101);
[pamf,delays,doppler] = pambgfun(wav,fs,5);
f2 = pamf(:,101);
```

Plot the periodic ambiguity functions.

```
plot(doppler/1000,f1)
hold on
plot(doppler/1000,f2)
xlabel('Doppler Shift (kHz)')
legend('One-Period PAF','Five-Period PAF')
```



## Zero Doppler Cut of LFM Periodic Ambiguity Function

Plot the zero Doppler cut for the five-period periodic ambiguity function of a linear FM pulse waveform. Assume the pulse repetition frequency (PRF) is 10.0 kHz and that the sampling frequency is a multiple of the PRF. Return the Doppler and delay values from the pambgfun function.

```
PRF = 10.0e3;
fs = 200*PRF;
waveform = phased.LinearFMWaveform('SampleRate',fs,'PulseWidth',1e-5, ...
    'NumPulses',1,'PRF',PRF);
wav = waveform();
```

Find the five-period periodic ambiguity function along a zero Doppler cut.

```
[pamf,delays] = pambgfun(wav,fs,5,'Cut','Doppler');
```

Plot the periodic ambiguity functions.

```
plot(delays*1.0e6,pamf)
```

xlabel('Delay \mus')


## Non-Zero Doppler Cut of LFM Periodic Ambiguity Function

Plot a non-zero Doppler cut for the 5-period periodic ambiguity function of a linear FM pulse waveform by explicitly specifying the cut value. Assume the pulse repetition frequency is 10.0 e 3 Hz and that the sampling frequency is a multiple of the PRF. Return the Doppler and delay values from the function.

```
PRF = 10.0e3;
fs = 200*PRF;
waveform = phased.LinearFMWaveform('SampleRate',fs,'PulseWidth',1e-5,...
    'NumPulses',1,'PRF',PRF);
wav = waveform();
```

Find the 5-period periodic ambiguity function along a non-zero Doppler cut.

```
dopval = 20.0;
[pamf,delays] = pambgfun(wav,fs,5,'Cut','Doppler','CutValue',dopval);
```

Plot the periodic ambiguity functions.

```
plot(delays*1.0e6,pamf)
```

xlabel('Delay \mus')


## Zero-Delay Cut of FMCW Periodic Ambiguity Function

Plot a zero delay cut for the three-period periodic ambiguity function of an FMCW waveform. Assume a sweep bandwidth of 100 kHz with a sampling frequency of 1 MHz . Return and plot the Doppler shift values.

```
fs = 1.0e6;
waveform = phased.FMCWWaveform('SweepBandwidth',100.0e3,'SampleRate',fs, ...
    'OutputFormat','Sweeps','NumSweeps',1);
wav = waveform();
```

Find the three-period periodic ambiguity function along a zero delay cut.

```
[pamf,doppler] = pambgfun(wav,fs,3,'Cut','Delay');
```

Plot the zero delay cut of the periodic ambiguity function.
plot(doppler/1.0e3, pamf)
xlabel('Doppler Shift (kHz)')


## Nonzero Delay Cut of FMCW Periodic Ambiguity Function

Plot a non-zero delay cut of -20 $\mu$ s for the three-period periodic ambiguity function of an FMCW waveform. Assume a sweep bandwidth of 100 kHz with a sampling frequency of 1 MHz . Return and plot the Doppler shift values.

```
fs = 1.0e6;
waveform = phased.FMCWWaveform('SweepBandwidth',100.0e3,'SampleRate',fs, ...
    'OutputFormat','Sweeps','NumSweeps',1,'SweepTime',100e-6);
wav = waveform();
```

Find the three-period periodic ambiguity function along a nonzero Delay cut.

```
delayval = -20.0e-6;
[pamf,doppler] = pambgfun(wav,fs,3,'Cut','Delay','CutValue',delayval);
```

Plot the nonzero delay cut of the periodic ambiguity function.

```
plot(doppler/1.0e3,pamf)
grid
xlabel('Doppler Shift (kHz)')
```



## Linear FM Periodic Ambiguity Diagram Image

Display an image of the 9-period periodic ambiguity function for a linear FM pulse waveform. Assume the pulse repetition frequency is 10.0 e 3 Hz and that the sampling frequency is a multiple of the PRF.

```
PRF = 10.0e3;
fs = 200*PRF;
waveform = phased.LinearFMWaveform('SampleRate',fs,'PulseWidth',le-5,...
    'NumPulses',1,'PRF',PRF);
wav = waveform();
```

Compute and display the 9-period periodic ambiguity function for all delays and frequencies.

```
[pamf,delays,doppler] = pambgfun(wav,fs,9,'Cut','2D');
imagesc(delays*le6,doppler/le6,pamf)
title('Periodic Ambiguity Function')
xlabel('Delay \tau ({\mu}s)')
ylabel('Doppler Shift (MHz)')
axis xy
```



## Linear FM Periodic Ambiguity Diagram

Plot the seven-period periodic ambiguity function of a linear FM pulse waveform. Assume the pulse repetition frequency ( PRF ) is 10.0 kHz and that the sampling frequency is a multiple of the PRF.

```
PRF = 10.0e3;
fs = 200*PRF;
waveform = phased.LinearFMWaveform('SampleRate',fs,'PulseWidth',1e-5, ...
    'NumPulses',1,'PRF',PRF);
wav = waveform();
```

Find the periodic ambiguity function.

```
pambgfun(wav,fs,7,'Cut','2D')
```



## Input Arguments

X - Input pulse waveform
complex-valued vector
Input pulse waveform, specified as a complex-valued vector.
Example: [0, .1,.3,.4, .3, .1.0]
Data Types: double
Complex Number Support: Yes

## fs - Sampling frequency

positive scalar
Sampling frequency, specified as a positive scalar. Units are in hertz.
Example: 3e3
Data Types: double

## P - Number of periods

1 (default) | positive integer
Number of periods, specified as a positive integer.
Example: 5

## Data Types: double

## V - Optional time delay or Doppler shift at which ambiguity function cut is taken

0 (default) | real-valued scalar
When you set 'Cut' to 'Delay' or 'Doppler', use V to specify a nonzero cut value. You cannot use V when you set 'Cut' to '2D'.

When 'Cut' is set to 'Delay ', V is the time delay at which the cut is taken. Time delay units are in seconds.

When 'Cut' is set to 'Doppler', V is the Doppler frequency shift at which the cut is taken. Doppler units are in hertz.

Example: 10.0
Data Types: double

## Output Arguments

## pafmag - Normalized PAF function magnitude

real-valued $M$-by- $N$ matrix | real-valued $M$-element column vector | real-valued $N$-element row vector
Normalized PAF function magnitude, returned as a vector or a matrix of nonnegative real values. The dimensions of pafmag depend on the value of 'Cut'.

| 'Cut' | pafmagdimensions |
| :--- | :--- |
| '2D' | $M$-by- $N$ matrix. |
| 'Delay' | $M$-element column vector. |
| 'Doppler' | $N$-element row vector. |

$M$ is the number of Doppler frequencies and $N$ is the number of time delays.

## delay - Time delay vector

real-valued $N$-element vector
Time delay vector, returned as an $N$-by- 1 vector. If $N$ is the length of signal $X$, then the delay vector consist of $2 N-1$ samples in the range, $-(N / 2)-1, \ldots,(N / 2)-1)$.

## doppler - Doppler shift vector

real-valued $M$ vector
Doppler shift vector, returned as an $M$-by-1 vector of Doppler frequencies. The Doppler frequency vector consists of $M=2^{\text {ceil(log2 } N)}$ equally-spaced samples. Frequencies are $\left(-(M / 2) F_{s}, \ldots,(M / 2-1) F_{s}\right)$.

## More About

## Periodic Ambiguity Function

The periodic ambiguity function (PAF) is an extension of the ordinary ambiguity function to periodic waveforms.

Use this function analyze the response of a correlation receiver to a time-delayed or Doppler-shifted narrowband periodic waveform. Narrowband periodic signals consist of CW tones modulated by a
periodic complex envelope. These types of signals are commonly used in radar systems to form transmitted pulse trains.

A time periodic waveform has the property $y(t+T)=y(t)$, where $T$ is the period. The PAF function for an $N$-period waveform is defined as

$$
A_{N T}(\tau, \nu)=\frac{1}{N T} \int^{N T} y\left(t+\frac{\tau}{2}\right) y^{*}\left(t-\frac{\tau}{2}\right) e^{i 2 \pi \nu t} d t
$$

Taking advantage of the periodicity, you can rewrite the function as

$$
A_{N T}(\tau, \nu)=\frac{1}{N T} \sum_{n=1}^{N} e^{i 2 \pi \nu(n-1) T} \int_{0}^{T} u\left(t+\frac{\tau}{2}\right) u^{*}\left(t-\frac{\tau}{2}\right) e^{i 2 \pi \nu s} d s
$$

The last term on the right side is the one-period PAF function, $A_{T}(\tau, \nu)$. The first term on the right side is due to Doppler only. The Doppler term is proportional to the periodic sinc() function and you can rewrite the periodic ambiguity function as

$$
A_{N T}(\tau, \nu)=\frac{\sin 2 \Pi \nu N T}{N \sin 2 \Pi \nu T} e^{i 2 \Pi \nu(N-1) T} A_{T}(\tau, \nu)
$$

The Doppler term improves the Doppler resolution by a factor of $1 / N T$.
The one-period PAF function is not the same as the ordinary ambiguity because the integration limits are different.

## Version History <br> Introduced in R2016b

## References

[1] Levanon, N. and E. Mozeson. Radar Signals. Hoboken, NJ: John Wiley \& Sons, 2004.
[2] Mahafza, B. R., and A. Z. Elsherbeni. MATLAB Simulations for Radar Systems Design. Boca Raton, FL: CRC Press, 2004.
[3] Richards, M. A. Fundamentals of Radar Signal Processing. New York: McGraw-Hill, 2005.

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\mathrm{Tm}}$.
Usage notes and limitations:

- Does not support variable-size inputs.
- Supported only when output arguments are specified.


## See Also

## Functions

ambgfun | dutycycle

## Objects

phased.LinearFMWaveform|phased.MatchedFilter | phased.PhaseCodedWaveform | phased.RectangularWaveform | phased.SteppedFMWaveform

## phitheta2azel

Convert angles from phi/theta form to azimuth/elevation form

## Syntax

AzEl = phitheta2azel(PhiTheta)
AzEl = phitheta2azel(PhiTheta,RotAx)

## Description

AzEl = phitheta2azel(PhiTheta) converts the phi/theta angle on page 2-261 pairs to their corresponding azimuth/elevation angle on page 2-260 pairs.

AzEl = phitheta2azel(PhiTheta,RotAx) also specifies the choice of phi-theta angle convention using RotAx.

## Examples

## Convert Phi-Theta Coordinates to Azimuth-Elevation Coordinates

Find the azimuth-elevation representation for $\varphi=30^{\circ}$ and $\theta=0^{\circ}$. Use the phi-theta convention with $\varphi$ defined from the $y$-axis to the $z$-axis, and $\theta$ defined from the $x$-axis toward the $y z$-plane.

```
azel = phitheta2azel([30;10])
azel = 2×1
8.6822
4.9809
```


## Rotate and Convert Phi-Theta Coordinates to Azimuth-Elevation Coordinates

Find the azimuth-elevation representation for $\varphi=30^{\circ}$ and $\theta=0^{\circ}$. Use the phi-theta convention with $\varphi$ defined from the x -axis to the y -axis, and $\theta$ defined from the z -axis toward the xy-plane.

```
azel = phitheta2azel([30;10],false)
azel = 2×1
    30
    80
```

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## Input Arguments

## PhiTheta - Phi-theta angle pairs

two-row matrix
Phi and theta angles, specified as a two-row matrix. Each column of the matrix represents an angle in degrees, in the form [phi; theta].

Data Types: double

## RotAx - Phi-theta angle convention selection

true (default) | false
Phi-theta angle convention selection, specified as true or false.

- If RotAx is true, the phi angle of a direction vector is the angle from the $z$-axis to the projection of the vector into the $y z$-plane. The theta angle is defined from the $x$-axis to the direction vector. Positive values are toward the $y z$-plane.
- If RotAx is false, the phi angle is defined from the $x$-axis to the projection of the direction vector in the $x y$-plane. The angle is positive in the direction of the $y$-axis. The theta angle is defined from the $z$-axis to the direction vector and is positive in the direction of the $x y$-plane (see "Alternative Definition of Phi and Theta Angles" on page 2-262 ).

Data Types: logical

## Output Arguments

## AzEl - Azimuth-elevation angle pairs

two-row matrix
Azimuth and elevation angles, returned as a two-row matrix. Each column of the matrix represents an angle in degrees, in the form [azimuth; elevation]. The matrix dimensions of AzEl are the same as those of PhiTheta.

## More About

## Azimuth and Elevation Angles

The azimuth angle of a vector is the angle between the $x$-axis and the orthogonal projection of the vector onto the $x y$ plane. The angle is positive in going from the $x$ axis toward the $y$ axis. Azimuth angles lie between -180 and 180 degrees. The elevation angle is the angle between the vector and its orthogonal projection onto the $x y$-plane. The angle is positive when going toward the positive $z$-axis from the xy plane. By default, the boresight direction of an element or array is aligned with the positive $x$-axis. The boresight direction is the direction of the main lobe of an element or array.

Note The elevation angle is sometimes defined in the literature as the angle a vector makes with the positive $z$-axis. The MATLAB and Phased Array System Toolbox products do not use this definition.

This figure illustrates the azimuth angle and elevation angle for a vector shown as a green solid line.


## Phi and Theta Angles

The phi angle $(\varphi)$ is the angle from the positive $y$-axis to the vector's orthogonal projection onto the $y z$ plane. The angle is positive toward the positive $z$-axis. The phi angle is between 0 and 360 degrees. The theta angle $(\theta)$ is the angle from the $x$-axis to the vector itself. The angle is positive toward the $y z$ plane. The theta angle is between 0 and 180 degrees.

The figure illustrates phi and theta for a vector that appears as a green solid line.


The coordinate transformations between $\varphi / \theta$ and $a z / e l$ are described by the following equations

$$
\begin{aligned}
& \operatorname{sinel}=\sin \phi \sin \theta \\
& \tan a z=\cos \phi \tan \theta \\
& \cos \theta=\cos e l \cos a z \\
& \tan \phi=\tan e l / \sin a z
\end{aligned}
$$

## Alternative Definition of Phi and Theta Angles

The phi angle $(\varphi)$ is the angle from the positive $x$-axis to the vector's orthogonal projection onto the $x y$ plane. The angle is positive toward the positive $y$-axis. The phi angle is between 0 and 360 degrees. The theta angle $(\theta)$ is the angle from the $z$-axis to the vector itself. The angle is positive toward the $x y$ plane. The theta angle is between 0 and 180 degrees.

The figure illustrates $\varphi$ and $\theta$ for a vector that appears as a green solid line.


$$
\begin{aligned}
& \phi=a z \\
& \theta=90-e l \\
& a z=\phi \\
& e l=90-\theta
\end{aligned}
$$

This transformation applies when RotAx is false.

## Version History

Introduced in R2012a

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
Does not support variable-size inputs.

## See Also

azel2phitheta
Topics
"Spherical Coordinates"

## phitheta2azelpat

Convert radiation pattern from phi-theta coordinates to azimuth-elevation coordinates

## Syntax

```
pat_azel = phitheta2azelpat(pat_phitheta,phi,theta)
pat_azel = phitheta2azelpat(pat_phitheta,phi,theta,az,el)
pat_azel = phitheta2azelpat(__,'RotateZ2X',rotpatax)
[pat_azel,az_pat,el_pat] = phitheta2azelpat(___)
```


## Description

pat_azel = phitheta2azelpat(pat_phitheta, phi,theta) converts the antenna radiation pattern, pat_phitheta, from phi and theta coordinates to the pattern pat_azel in azimuth and elevation coordinates. phi and theta are the phi and theta coordinates at which pat_phitheta values are defined. The pat_azel matrix covers azimuth values from -180 to 180 degrees and elevation values from -90 to 90 degrees in one degree increments. The function interpolates the pat_phitheta matrix to estimate the response of the antenna in a given direction.
pat_azel = phitheta2azelpat(pat_phitheta, phi,theta,az,el) uses vectors az and el to specify the grid at which to sample pat_azel. To avoid interpolation errors, az should cover the range [-180, 180] and el should cover the range [-90, 90].
pat_azel = phitheta2azelpat (__, 'RotateZ2X', rotpatax) also specifies rotpatax to indicate the boresight direction of the pattern: $x$-axis or $z$-axis.
[pat_azel,az_pat,el_pat] = phitheta2azelpat( __ ) also returns vectors az_pat and el_pàt containing the azimuth and elevation angles at which pat_azel is sampled.

## Examples

## Convert Radiation Pattern to Azimuth and Elevation

Convert a radiation pattern to azimuth/elevation form, with the azimuth and elevation angles spaced $1^{\circ}$ apart.

Define the pattern in terms of $\varphi$ and $\theta$.

```
phi = 0:360;
theta = 0:180;
pat_phitheta = mag2db(repmat(cosd(theta)',1,numel(phi)));
```

Convert the pattern to azimuth/elevation space.

```
pat_azel = phitheta2azelpat(pat_phitheta,phi,theta);
```


## Plot Converted Radiation Pattern

Convert a radiation pattern from theta/phi coordinates to azimuth/elevation coordinates, with azimuth and elevation angles spaced $1^{\circ}$ apart.

Define the pattern in terms of phi, $\phi$, and theta, $\theta$, coordinates.

```
phi = 0:360;
theta = 0:180;
pat_phitheta = mag2db(repmat(cosd(theta)',1,numel(phi)));
```

Convert the pattern to azimuth/elevation coordinates. Get the azimuth and elevation angles for use in plotting.
[pat azel,az,el] = phitheta2azelpat(pat phitheta, phi,theta);
Plot the radiation pattern.

```
H = surf(az,el,pat_azel);
H.LineStyle = 'none';
xlabel('Azimuth (degrees)');
ylabel('Elevation (degrees)');
zlabel('Pattern');
```



## Convert Radiation Pattern from Alternate Phi-Theta Coordinates to Azimuth and Elevation

Convert a radiation pattern to the azimuth-elevation coordinates from alternative phi-theta coordinates, with the phi and theta angles spaced one degree apart.

Create a simple radiation pattern in terms of phi and theta. Add an offset to the pattern to suppress taking the logarithm of zero in mag2db.

```
phi = 0:360;
theta = 0:180;
pat_phitheta = mag2db(10*sind(theta').^2*cosd(phi).^4 + 1);
imagesc(phi,theta,pat_phitheta)
xlabel('Phi (deg)')
ylabel('Theta (deg)')
colorbar
```



```
[pat_azel,az_pat,el_pat] = phitheta2azelpat(pat_phitheta,phi,theta,'RotateZ2X',false);
imagesc(az_pat,el_pat,pat_azel)
xlabel('Azimuth (\overline{deg)')}
ylabel('Elevation (deg)')
colorbar
```



## Convert Radiation Pattern for Specific Azimuth/Elevation Values

Convert a radiation pattern from phi/theta coordinates to azimuth/elevation coordinates, with the azimuth and elevation angles spaced $5^{\circ}$ apart.

Define the pattern in terms of phi and theta.

```
phi = 0:360;
theta = 0:180;
pat_phitheta = mag2db(repmat(cosd(theta)',1,numel(phi)));
```

Define the set of azimuth and elevation angles at which to sample the pattern. Then, convert the pattern.

```
az = -180:5:180;
el = -90:5:90;
pat_azel = phitheta2azelpat(pat_phitheta,phi,theta,az,el);
```

Plot the radiation pattern.

```
H = surf(az,el,pat_azel);
H.LineStyle = 'none';
xlabel('Azimuth (degrees)');
ylabel('Elevation (degrees)');
zlabel('Pattern');
```



## Input Arguments

## pat_phitheta - Antenna radiation patter

real-valued $Q$-by-P matrix
Antenna radiation pattern in phi-theta coordinates, specified as a real-valued $Q$-by- $P$ matrix. pat_phitheta contains the magnitude pattern. $P$ is the length of the phi vector, and $Q$ is the length of the theta vector. Units are in dB .

Data Types: double

## phi - Phi angles

real-valued length- $P$ vector
Phi angles at which pat_phitheta is sampled, specified as a vector of real-valued length- $P$ vector. Phi angles lie between 0 and 360, inclusive. Units are in degrees.

Data Types: double

## theta - Theta angles

real-valued length- $Q$ vector
Theta angles at which pat_phitheta is sampled, specified as a vector of real-valued length- $Q$ vector. Theta angles lie between 0 and 180, inclusive. Units are in degrees.
Data Types: double

## az - Azimuth angles

[-180:180] (default) | real-valued length- $L$ vector
Azimuth angles at which pat_azel samples the pattern, specified as a vector of real-valued length- $L$ vector. Azimuth angles lie between -180 and 180, inclusive. Units are in degrees.
Data Types: double

## el - Elevation angles

[-90:90] (default) | real-valued length- $M$ vector
Elevation angles at which pat_azel samples the pattern, specified as a real-valued length- $M$ vector. Elevation angle lie between -90 and 90, inclusive. Units are in degrees.

## Data Types: double

## rotpatax - Pattern boresight direction selector

true (default) | false
Pattern boresight direction selector, specified as true or false.

- If rotpatax is true, the pattern boresight is along the $x$-axis. In this case, the $z$-axis of phi-theta space is aligned with the $x$-axis of azimuth and elevation space. The phi angle is defined from the $y$-axis to the $z$-axis and the theta angle is defined from the $x$-axis toward the $y z$-plane. (See "Phi and Theta Angles" on page 2-272).
- If rotpatax is false, the phi angle is defined from the $x$-axis to the $y$-axis and the theta angle is defined from the $z$-axis toward the $x y$-plane. (See "Alternative Definition of Phi and Theta" on page 2-273).

```
Data Types: logical
```


## Output Arguments

## pat_azel - Antenna radiation pattern in azimuth-elevation coordinates <br> real-valued $M$-by-L matrix

Antenna radiation pattern in azimuth-elevation coordinates, returned as a real-valued $M$-by- $L$ matrix. pat_azel represents the magnitude pattern. $L$ is the length of the az_pat vector, and $M$ is the length of the el_pat vector. Units are in dB .

## az_pat - Azimuth angles

real-valued length- $L$ vector
Azimuth angles at which the pat_azel output pattern is sampled, returned as a real-valued length- $L$ vector. Units are in degrees.

## el_pat - Elevation angles

real-valued length- $M$ vector
Elevation angles at which the pat_azel output pattern is sampled, returned as a real-valued length$M$ vector. Units are in degrees.

## More About

## Azimuth and Elevation Angles

The azimuth angle of a vector is the angle between the $x$-axis and the orthogonal projection of the vector onto the xy plane. The angle is positive in going from the $x$ axis toward the $y$ axis. Azimuth angles lie between -180 and 180 degrees. The elevation angle is the angle between the vector and its orthogonal projection onto the $x y$-plane. The angle is positive when going toward the positive $z$-axis from the xy plane. By default, the boresight direction of an element or array is aligned with the positive $x$-axis. The boresight direction is the direction of the main lobe of an element or array.

Note The elevation angle is sometimes defined in the literature as the angle a vector makes with the positive $z$-axis. The MATLAB and Phased Array System Toolbox products do not use this definition.

This figure illustrates the azimuth angle and elevation angle for a vector shown as a green solid line.


## Phi and Theta Angles

The phi angle $(\varphi)$ is the angle from the positive $y$-axis to the vector's orthogonal projection onto the $y z$ plane. The angle is positive toward the positive $z$-axis. The phi angle is between 0 and 360 degrees. The theta angle $(\theta)$ is the angle from the $x$-axis to the vector itself. The angle is positive toward the $y z$ plane. The theta angle is between 0 and 180 degrees.

The figure illustrates phi and theta for a vector that appears as a green solid line.


The coordinate transformations between $\varphi / \theta$ and $a z / e l$ are described by the following equations

$$
\begin{aligned}
& \sin e l=\sin \phi \sin \theta \\
& \tan a z=\cos \phi \tan \theta \\
& \cos \theta=\operatorname{cose} l \cos a z \\
& \tan \phi=\operatorname{tanel} / \sin a z
\end{aligned}
$$

## Alternative Definition of Phi and Theta

The phi angle $(\varphi)$ is the angle from the positive $x$-axis to the vector's orthogonal projection onto the $x y$ plane. The angle is positive toward the positive $y$-axis. The phi angle is between 0 and 360 degrees. The theta angle $(\theta)$ is the angle from the $z$-axis to the vector itself. The angle is positive toward the $x y$ plane. The theta angle is between 0 and 180 degrees.

The figure illustrates $\varphi$ and $\theta$ for a vector that appears as a green solid line.


$$
\begin{aligned}
& \phi=a z \\
& \theta=90-e l \\
& a z=\phi \\
& e l=90-\theta
\end{aligned}
$$

## Version History

Introduced in R2012a

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
Does not support variable-size inputs.

## See Also

phased.CustomAntennaElement | phitheta2azel|azel2phitheta|azel2phithetapat
Topics
Antenna Array Analysis with Custom Radiation Pattern
"Spherical Coordinates"

## phitheta2uv

Convert phi/theta angles to $u / v$ coordinates

## Syntax

UV = phitheta2uv(PhiTheta)

## Description

UV = phitheta2uv(PhiTheta) converts the phi/theta angle on page 2-276 pairs to their corresponding $u / v$ space on page 2-277 coordinates.

## Examples

## Conversion of Phi-Theta Pair

Find the corresponding $u-v$ representation for $\varphi=30^{\circ}$ and $\varphi=0^{\circ}$.
$u v=$ phitheta2uv([30; 0])
$u v=2 \times 1$
0
0

## Input Arguments

## PhiTheta - Phi/theta angle pairs

two-row matrix
Phi and theta angles, specified as a two-row matrix. Each column of the matrix represents an angle in degrees, in the form [phi; theta].

Data Types: double

## Output Arguments

UV - Angle in u/v space
two-row matrix
Angle in $u / v$ space, returned as a two-row matrix. Each column of the matrix represents an angle in the form $[u ; v]$. The matrix dimensions of UV are the same as those of PhiTheta.

## More About

## Phi Angle, Theta Angle

The phi angle $(\varphi)$ is the angle from the positive $y$-axis to the vector's orthogonal projection onto the $y z$ plane. The angle is positive toward the positive $z$-axis. The phi angle is between 0 and 360 degrees. The theta angle $(\theta)$ is the angle from the $x$-axis to the vector itself. The angle is positive toward the $y z$ plane. The theta angle is between 0 and 180 degrees.

The figure illustrates phi and theta for a vector that appears as a green solid line.


The coordinate transformations between $\varphi / \theta$ and $a z / e l$ are described by the following equations

$$
\begin{aligned}
& \sin e l=\sin \phi \sin \theta \\
& \tan a z=\cos \phi \tan \theta \\
& \cos \theta=\operatorname{cosel} \cos a z \\
& \tan \phi=\operatorname{tanel} / \sin a z
\end{aligned}
$$

## U/V Space

The $u / v$ coordinates for the hemisphere $x \geq 0$ are derived from the phi and theta angles on page 2276.

The relations are

$$
\begin{aligned}
& u=\sin \theta \cos \phi \\
& v=\sin \theta \sin \phi
\end{aligned}
$$

In these expressions, $\varphi$ and $\theta$ are the phi and theta angles, respectively.
To convert azimuth and elevation to $u$ and $v$ use the transformation

$$
\begin{aligned}
& u=\operatorname{coselsin} a z \\
& v=\operatorname{sinel}
\end{aligned}
$$

which is valid only in the range $a b s(a z) \leq=90$.
The values of $u$ and $v$ satisfy the inequalities

$$
\begin{aligned}
& -1 \leq u \leq 1 \\
& -1 \leq v \leq 1 \\
& u^{2}+v^{2} \leq 1
\end{aligned}
$$

Conversely, the phi and theta angles can be written in terms of $u$ and $v$ using

$$
\begin{aligned}
& \tan \phi=v / u \\
& \sin \theta=\sqrt{u^{2}+v^{2}}
\end{aligned}
$$

The azimuth and elevation angles can also be written in terms of $u$ and $v$ :

$$
\sin e l=v
$$

$$
\tan a z=\frac{u}{\sqrt{1-u^{2}-v^{2}}}
$$

## Version History <br> Introduced in R2012a

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:

Does not support variable-size inputs.

## See Also

uv2phitheta

## Topics

"Spherical Coordinates"

## phitheta2uvpat

Convert radiation pattern from phi/theta form to $u / v$ form

## Syntax

pat_uv = phitheta2uvpat(pat_phitheta, phi,theta)
pat_uv = phitheta2uvpat(pat_phitheta,phi,theta,u,v)
[pat_uv,u_pat,v_pat] = phitheta2uvpat( $\qquad$ )

## Description

pat uv = phitheta2uvpat(pat phitheta, phi, theta) expresses the antenna radiation pattern pat_phitheta in $u / v$ space on page 2-284 coordinates instead of $\varphi / \theta$ angle on page 2-283 coordinates. pat_phitheta samples the pattern at $\varphi$ angles in phi and $\theta$ angles in theta. The pat_uv matrix uses a default grid that covers $u$ values from -1 to 1 and $v$ values from -1 to 1 . In this grid, pat_uv is uniformly sampled with a step size of 0.01 for $u$ and $v$. The function interpolates to estimate the response of the antenna at a given direction. Values in pat_uv are NaN for $u$ and $v$ values outside the unit circle because $u$ and $v$ are undefined outside the unit circle.
pat_uv = phitheta2uvpat (pat_phitheta, phi, theta, $u, v$ ) uses vectors $u$ and $v$ to specify the grid at which to sample pat_uv. To avoid interpolation errors, $u$ should cover the range $[-1,1]$ and $v$ should cover the range $[-1,1]$.
[pat_uv,u_pat,v_pat] = phitheta2uvpat( $\qquad$ ) returns vectors containing the $u$ and $v$ coordinates at which pat_uv samples the pattern, using any of the input arguments in the previous syntaxes.

## Examples

## Conversion of Radiation Pattern

Convert a radiation pattern to $u$-v form, with the $u$ and $v$ coordinates spaced by 0.01 .
Define the pattern in terms of $\varphi$ and $\theta$.

```
phi = 0:360;
theta = 0:90;
pat_phitheta = mag2db(repmat(cosd(theta)',1,numel(phi)));
```

Convert the pattern to $u-v$ form.

```
pat_uv = phitheta2uvpat(pat_phitheta,phi,theta);
```


## Convert and Plot Radiation Pattern

Convert a radiation pattern to $u-v$ coordinates, with the $u$ and $v$ coordinates spaced by 0.01 .

Define the pattern in terms of $\phi$ and $\theta$.
phi = 0:360;
theta $=0: 90$;
pat_phitheta $=$ mag2db(repmat(cosd(theta)',1, numel(phi)));
Convert the pattern to $u-v$ coordinates. Store the $u$ and $v$ coordinates for use in plotting.
[pat_uv,u,v] = phitheta2uvpat(pat_phitheta,phi,theta);
Plot the result.
H = surf(u,v,pat_uv);
H.LineStyle = 'nōne';
xlabel('u');
ylabel('v');
zlabel('Pattern');


## Convert Radiation Pattern for Specific U/V Values

Convert a radiation pattern to $u-v$ coordinates, with the $u$ and $v$ coordinates spaced by 0.05 .
Define the pattern in terms of $\phi$ and $\theta$.

```
phi = 0:360;
theta = 0:90;
pat_phitheta = mag2db(repmat(cosd(theta)',1,numel(phi)));
```

Define the set of $u$ and $v$ coordinates at which to sample the pattern. Then, convert the pattern.

```
u = -1:0.05:1;
v = -1:0.05:1;
pat_uv = phitheta2uvpat(pat_phitheta,phi,theta,u,v);
```

Plot the result.
H = surf(u,v,pat_uv);
H.LineStyle = 'none';
xlabel('u');
ylabel('v');
zlabel('Pattern');


## Input Arguments

## pat_phitheta - Antenna radiation pattern in phi/theta form

Q-by-P matrix
Antenna radiation pattern in phi/theta form, specified as a Q-by-P matrix. pat_phitheta samples the 3-D magnitude pattern in decibels, in terms of $\varphi$ and $\theta$ angles. $P$ is the length of the phi vector, and Q is the length of the theta vector.

Data Types: double
phi - Phi angles
vector of length $P$
Phi angles at which pat_phitheta samples the pattern, specified as a vector of length P. Each $\varphi$ angle is in degrees, between 0 and 180.

Data Types: double

## theta - Theta angles

vector of length Q
Theta angles at which pat_phitheta samples the pattern, specified as a vector of length Q. Each $\theta$ angle is in degrees, between 0 and 90 . Such angles are in the hemisphere for which $u$ and $v$ are defined.
Data Types: double

## u-u coordinates

[-1:0.01:1] (default) | vector of length L
$u$ coordinates at which pat_uv samples the pattern, specified as a vector of length L. Each $u$ coordinate is between -1 and 1 .
Data Types: double

## $\mathbf{v}$ - $\mathbf{v}$ coordinates

[-1:0.01:1] (default) | vector of length M
$v$ coordinates at which pat_uv samples the pattern, specified as a vector of length M. Each $v$ coordinate is between -1 and 1 .
Data Types: double

## Output Arguments

## pat_uv - Antenna radiation pattern in u/v form <br> M-by-L matrix

Antenna radiation pattern in $u / v$ form, returned as an M-by-L matrix. pat_uv samples the 3-D magnitude pattern in decibels, in terms of $u$ and $v$ coordinates. Lis the length of the $u$ vector, and M is the length of the $v$ vector. Values in pat_uv are NaN for $u$ and $v$ values outside the unit circle because $u$ and $v$ are undefined outside the unit circle.

## u_pat - u coordinates <br> vector of length $L$

$u$ coordinates at which pat_uv samples the pattern, returned as a vector of length $L$.

## v_pat - v coordinates

vector of length $M$
$v$ coordinates at which pat_uv samples the pattern, returned as a vector of length M.

## More About

## Phi Angle, Theta Angle

The phi angle $(\varphi)$ is the angle from the positive $y$-axis to the vector's orthogonal projection onto the $y z$ plane. The angle is positive toward the positive $z$-axis. The phi angle is between 0 and 360 degrees. The theta angle $(\theta)$ is the angle from the $x$-axis to the vector itself. The angle is positive toward the $y z$ plane. The theta angle is between 0 and 180 degrees.

The figure illustrates phi and theta for a vector that appears as a green solid line.


The coordinate transformations between $\varphi / \theta$ and $a z / e l$ are described by the following equations

$$
\begin{aligned}
& \sin e l=\sin \phi \sin \theta \\
& \tan a z=\cos \phi \tan \theta \\
& \cos \theta=\operatorname{cosel} e \cos a z \\
& \tan \phi=\tan e l / \sin a z
\end{aligned}
$$

## U/V Space

The $u$ and $v$ coordinates are the direction cosines of a vector with respect to the $y$-axis and $z$-axis, respectively.

The $u / v$ coordinates for the hemisphere $x \geq 0$ are derived from the phi and theta angles on page 2283, as follows:

$$
\begin{aligned}
& u=\sin \theta \cos \phi \\
& v=\sin \theta \sin \phi
\end{aligned}
$$

In these expressions, $\varphi$ and $\theta$ are the phi and theta angles, respectively.
To convert azimuth and elevation to $u$ and $v$ use the transformation

$$
\begin{aligned}
& u=\operatorname{coselsin} a z \\
& v=\text { sinel }
\end{aligned}
$$

which is valid only in the range $a b s(a z) \leq=90$.
The values of $u$ and $v$ satisfy the inequalities

$$
\begin{aligned}
& -1 \leq u \leq 1 \\
& -1 \leq v \leq 1 \\
& u^{2}+v^{2} \leq 1
\end{aligned}
$$

Conversely, the phi and theta angles can be written in terms of $u$ and $v$ using

$$
\begin{aligned}
\tan \phi & =v / u \\
\sin \theta & =\sqrt{u^{2}+v^{2}}
\end{aligned}
$$

The azimuth and elevation angles can also be written in terms of $u$ and $v$ :

$$
\begin{aligned}
& \text { sinel }=v \\
& \tan a z=\frac{u}{\sqrt{1-u^{2}-v^{2}}}
\end{aligned}
$$

## Version History <br> Introduced in R2012a

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:

Does not support variable-size inputs.

## See Also

phased. CustomAntennaElement | phitheta2uv|uv2phitheta|uv2phithetapat

## Topics

"Spherical Coordinates"

## physconst

Physical constants

## Syntax

const $=$ physconst(name)

## Description

const $=$ physconst (name) returns the value of the physical constant const specified by the name argument.

## Examples

## Convert Frequency to Wavelength

Determine the wavelength of a 1 GHz electromagnetic wave.

```
freq = le9;
lambda = physconst('LightSpeed')/freq
lambda = 0.2998
```


## Thermal Noise Power

Determine the thermal noise power per unit bandwidth in the in-phase (I) and quadrature (Q) channels of a receiver. Specify a receiver temperature of 290 K .

```
T = 290;
k = physconst('Boltzmann');
```

Compute the noise power per unit bandwidth, split evenly between the I and Q channels. Units are in dB.

Noise_power $=10 * \log 10(k * T / 2)$
Noise_power = -206.9855

## Input Arguments

## name - Name of physical constant

'LightSpeed'|'Boltzmann'| 'EarthRadius'
Name of physical constant, specified as 'LightSpeed', 'Boltzmann', or 'EarthRadius '. See "Physical Constants" on page 2-287 for a list of values for physical constants used in Phased Array System Toolbox.

Example: 'LightSpeed'

## Output Arguments

## const - Value of physical constant

real-valued scalar
Value of physical constant, returned as a real-valued scalar. All values are in SI units.

## More About

## Physical Constants

This table lists the supported constants and their values in SI units.

| Constant | Description | Value |
| :--- | :--- | :--- |
| 'LightSpeed ' | Speed of light in vacuum | $299,792,458 \mathrm{~m} / \mathrm{s}$. Most <br> commonly denoted by $c$. |
| 'Boltzmann ' | Boltzmann constant relating <br> kinetic energy to temperature | $1.3806504 \times 10^{-23} \mathrm{~J} / \mathrm{K} 2006$. <br> NIST value, most commonly <br> denoted by $k$. |
| 'EarthRadius ' | Mean radius of the Earth | $6,371,000 \mathrm{~m}$ |

## Version History

Introduced in R2011a

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.
The function does not support variable-size inputs.

## See Also

## External Websites

https://physics.nist.gov/cuu/Constants/index.html

## pilotcalib

Array calibration using pilot sources

## Syntax

```
estpos = pilotcalib(nompos,x,pilotang)
[estpos,esttaper] = pilotcalib(nompos,x,pilotang)
[estpos,esttaper] = pilotcalib(nompos,x,pilotang,nomtaper)
[estpos,esttaper] = pilotcalib(nompos,x,pilotang,nomtaper,uncerts)
```


## Description

estpos = pilotcalib(nompos,x,pilotang) returns the estimated element positions, estpos, of a sensor array. The argument nompos represents the relative nominal positions of the sensor array before calibration. The nominal position is relative to the first element of the array. The argument $x$ represents the signals received by the array coming from the pilot sources. The argument pilotang contains the known directions of each of the pilot sources. Three or more pilot sources are required in this case.
[estpos,esttaper] = pilotcalib(nompos,x,pilotang) also returns the estimated array taper, esttaper. Each element of esttaper contains the estimated taper value of the corresponding array element. In this case, the prior nominal taper is one for each element. Four or more pilot sources are required in this case.
[estpos,esttaper] = pilotcalib(nompos,x,pilotang, nomtaper) specifies nomtaper as the nominal taper of the array. Four or more pilot sources are required in this case.
[estpos,esttaper] = pilotcalib(nompos,x,pilotang, nomtaper, uncerts) specifies uncerts as the configuration settings to use for calibrating array uncertainties. Configuration settings determine which parameters to estimate.

## Examples

## Estimate ULA Element Positions Using Pilot Calibration

Construct a 7 -element ULA array of isotropic antenna elements spaced one-half wavelength apart. Assume the array is geometrically perturbed in three dimensions. Perform pilot calibration on the array using 4 pilot sources at azimuth and elevation angles of $(-60,0),(10,-40),(40,0)$, and $(120,45)$ degrees. For the calibration process, pilot signals have an SNR of 30 dB . Each pilot signal contains 10,000 samples. Assume the signals have a frequency of 600 MHz .

## Set up the ULA with nominal parameters

```
fc = 600e6;
c = physconst('LightSpeed');
lam = c/fc;
d = 0.5*lam;
sIso = phased.IsotropicAntennaElement('FrequencyRange',[100,900]*1e6);
Nelem = 7;
```

```
NominalTaper = ones(1,Nelem);
sULA = phased.ULA('Element',sIso,'NumElements',Nelem,'ElementSpacing',d,...
    'Taper',NominalTaper);
```


## Create the pilot signals

Randomly perturb the element positions with a Gaussian distribution having 0.1 wavelength standard deviation. Do not perturb the position of the first element or the tapers.

```
posstd = 0.1;
rng default
NominalElementPositions = getElementPosition(sULA)/lam;
ReferenceElement = NominalElementPositions(:,1);
PositionPert = [zeros(3,1),posstd*randn(3,Nelem-1)];
ActualElementPositions = NominalElementPositions + PositionPert;
ActualTaper = NominalTaper;
```

Generate the signals using the actual positions and tapers.

```
Nsamp = 10000;
ncov = 0.001;
PilotAng = [-60,10,40,120; 0,-40,0,45];
Npilot = size(PilotAng,2);
for n = 1:Npilot
    X(:,:,n) = sensorsig(ActualElementPositions,...
        Nsamp,PilotAng(:,n),ncov,'Taper',ActualTaper.');
end
```


## Perform the pilot calibration

```
estpos = pilotcalib(NominalElementPositions - ReferenceElement*ones(1,Nelem),...
    X,PilotAng);
```

Add back the position of the reference sensor.

```
estpos = estpos + NominalElementPositions(:,1)*ones(1,Nelem);
```


## Examine the root mean squared (RMS) error of the calibrated parameters

Compute the RMS value of the initial position error.

```
numpos = 3*Nelem;
initposRMSE = sqrt(sum(PositionPert(:).^2)/numpos);
```

Compute the RMS value of the calibrated position error.

```
solvposErr = ActualElementPositions - estpos;
solvposRMSE = sqrt(sum(solvposErr(:).^2)/(numpos));
```

Compare the calibrated RMS position error to the initial position RMS error. The calibration reduces the RMS position error.

```
disp(solvposRMSE/initposRMSE)
```

    2.3493e-04
    
## Estimate ULA Element Position and Taper Errors Using Pilot Calibration

Construct a 7 -element ULA array of isotropic antenna elements spaced one-half wavelength apart. Assume the array is geometrically perturbed in three dimensions. Perform pilot calibration on the array using 4 pilot sources at azimuth and elevation angles of ( $-60,0$ ), ( 10,80 ), ( $40,-40$ ), and ( $-80,0$ ) degrees. For the calibration process, pilot signals have an SNR of 30 dB . Each pilot signal contains 10,000 samples. Assume the signals have a frequency of 600 MHz .

## Set up the ULA with nominal parameters

```
fc = 600e6;
c = physconst('LightSpeed');
lam = c/fc;
d = 0.5*lam;
sIso = phased.IsotropicAntennaElement('FrequencyRange',[100,900]*1e6);
Nelem = 7;
NominalTaper = ones(1,Nelem);
sULA = phased.ULA('Element',sIso,'NumElements',Nelem,'ElementSpacing',d,...
    'Taper',NominalTaper);
```


## Create the pilot signals

Randomly perturb the element positions using a Gaussian distribution that has a standard deviation of 0.1 wavelength. Do not perturb the position of the first element.

```
posstd = 0.1;
rng default
NominalElementPositions = getElementPosition(sULA)/lam;
ReferenceElement = NominalElementPositions(:,1);
PositionPert = [zeros(3,1),posstd*randn(3,Nelem-1)];
ActualElementPositions = NominalElementPositions + PositionPert;
Perturb the taper in magnitude and phase. Do not perturb the first taper.
```

```
tapermagstd = 0.15;
```

tapermagstd = 0.15;
taperphasestd = 0.15;
taperphasestd = 0.15;
tapermagpert = tapermagstd*[0; randn(Nelem-1,1)];
tapermagpert = tapermagstd*[0; randn(Nelem-1,1)];
ActualTaper = NominalTaper' + tapermagpert;
ActualTaper = NominalTaper' + tapermagpert;
taperphasepert = taperphasestd*[0;randn(Nelem-1,1)];
taperphasepert = taperphasestd*[0;randn(Nelem-1,1)];
ActualTaper = ActualTaper.*exp(li*taperphasepert);

```
ActualTaper = ActualTaper.*exp(li*taperphasepert);
```

Generate the signals using the perturbed positions, tapers and four pilot sources.

```
Nsamp = 10000;
ncov = 0.001;
PilotAng = [-60,10,40,-80; 10,80,-40,0];
Npilot = size(PilotAng,2);
for n = 1:Npilot
    X(:,:,n) = sensorsig(ActualElementPositions,Nsamp,...,
        PilotAng(:,n),ncov,'Taper',ActualTaper);
end
```


## Perform the pilot calibration

```
[estpos,esttaper] = pilotcalib(...
    NominalElementPositions - ReferenceElement*ones(1,Nelem),...
    X,PilotAng);
```

Add back the position of the reference sensor.

```
estpos = estpos + NominalElementPositions(:,1)*ones(1,Nelem);
```


## Examine the root mean square (RMS) error of the calibrated parameters

Compute the RMS values of the initial taper perturbations.
tapermagpertRMSE = sqrt(tapermagpert'*tapermagpert/Nelem);
taperphasepertRMSE = sqrt(taperphasepert'*taperphasepert/Nelem);
Compute the RMS value of the calibrated taper magnitude error.

```
diff = abs(ActualTaper) - abs(esttaper);
diff2 = diff'*diff;
tapermagsolvRMSE = sqrt(diff2/Nelem);
```

Compare the calibrated RMS magnitude error to the initial RMS magnitude error. The calibration reduces the RMS magnitude error.

```
disp(tapermagsolvRMSE/tapermagpertRMSE)
```

$6.7715 e-04$
Compute the RMS value of the calibrated taper phase error.

```
diff = unwrap(angle(ActualTaper) - angle(esttaper));
diff2 = diff'*diff;
tapersolvphaseRMSE = sqrt(diff2/Nelem);
```

Compare the calibrated RMS phase error to the initial RMS phase error. The calibration reduces the RMS phase error.

```
disp(tapersolvphaseRMSE/taperphasepertRMSE)
```

0.0021

```
% Compute the RMS value of the initial position error.
numpos = 3*Nelem;
initposRMSE = sqrt(sum(PositionPert(:).^2)/numpos);
```

Compute the RMS value of the calibrated position error.

```
solvposErr = ActualElementPositions - estpos;
solvposRMSE = sqrt(sum(solvposErr(:).^2)/(numpos));
```

Compare the calibrated RMS position error to the initial position RMS error. The calibration reduces the RMS position error.

```
disp(solvposRMSE/initposRMSE)
    3.6308e-04
```


## Estimate URA Element Position Errors Using Pilot Calibration

Construct a 9 -element URA of isotropic antenna elements spaced one-half wavelength apart. Assume the array has been geometrically perturbed in all directions except for the first element. Perform pilot calibration on the array using 5 pilot sources at azimuth and elevation angles of ( $-60,0$ ), ( $10,-40$ ),
$(40,0),(120,45)$, and $(170,50)$ degrees. For the calibration process, pilot signals have an SNR of 30 dB. Each pilot signal contains 10,000 samples. Assume the signals have a frequency of 600 MHz .

## Create the array

For convenience, use a phased.URA System object ${ }^{\text {TM }}$ to set the nominal position and taper values.

```
fc = 300e6;
c = physconst('LightSpeed');
lam = c/fc;
d = 0.5*lam;
sIso = phased.IsotropicAntennaElement('FrequencyRange',[100,900]*1e6);
sURA = phased.URA('Element',sIso,'Size',[3,3],...
    'ElementSpacing',d,'Taper',ones(3,3));
Nelem = getNumElements(sURA);
taper = getTaper(sURA);
```


## Create the pilot signals

Randomly perturb the element positions using a Gaussian distribution that has a standard deviation of 0.1 wavelength. Do not perturb the position of the first element.

```
posstd = 0.1;
rng default
NominalElementPositions = getElementPosition(sURA)/lam;
ReferenceElement = NominalElementPositions(:,1);
PositionPert = [zeros(3,1),posstd*randn(3,Nelem-1)];
ActualElementPositions = NominalElementPositions + PositionPert;
```

Perturb the taper in magnitude and phase. Do not perturb the first taper.

```
NominalTaper = getTaper(sURA);
tapermagstd = 0.1;
taperphasestd = 0.1;
tapermagpert = tapermagstd*[0; randn(Nelem-1,1)];
ActualTaper = NominalTaper + tapermagpert;
taperphasepert = taperphasestd*[0; randn(Nelem-1,1)];
ActualTaper = ActualTaper.*exp(1i*taperphasepert);
```

Generate the pilot signals using the perturbed positions and tapers.

```
Nsamp = 10000;
ncov = 0.001;
PilotAng = [-60,10,40,120,170; 0,-40,0,45,50];
Npilot = size(PilotAng,2);
for n = 1:Npilot
    X(:,:,n) = sensorsig(ActualElementPositions,Nsamp,...
        PilotAng(:,n),ncov,'Taper',ActualTaper);
end
```


## Perform the pilot calibration

```
[estpos,esttaper] = pilotcalib(NominalElementPositions - ReferenceElement*ones(1,Nelem),...
```

    X, PilotAng,NominalTaper);
    Add back the position of the reference sensor.

```
estpos = estpos + NominalElementPositions(:,1)*ones(1,Nelem);
```


## Examine the root mean square (RMS) error of the calibrated parameters

Compute the RMS values of the initial taper perturbations to compare with the RMS values of the calibrated parameters.

```
tapermagpertRMSE = sqrt(tapermagpert'*tapermagpert/Nelem);
taperphasepertRMSE = sqrt(taperphasepert'*taperphasepert/Nelem);
```

Compute the RMS value of the calibrated taper magnitude error.

```
diff = abs(ActualTaper) - abs(esttaper);
diff2 = diff'*diff;
tapermagsolvRMSE = sqrt(diff2/Nelem);
```

Compare the calibrated RMS magnitude error to the initial RMS error. The calibration reduces the RMS magnitude error.

```
disp(tapermagsolvRMSE/tapermagpertRMSE)
    0.0014
```

Compute the RMS value of the calibrated taper phase error.

```
diff = unwrap(angle(ActualTaper) - angle(esttaper));
diff2 = diff'*diff;
tapersolvphaseRMSE = sqrt(diff2/Nelem);
```

Compare the calibrated RMS phase error to the initial RMS error. The calibration reduces the RMS phase error.

```
disp(tapersolvphaseRMSE/taperphasepertRMSE)
```

    0.0015
    Compute the RMS value of the initial position error.

```
numpos = 3*Nelem;
initposRMSE = sqrt(sum(PositionPert(:).^2)/numpos);
Compute the RMS value of the calibrated position error.
```

```
solvposErr = ActualElementPositions - estpos;
solvposRMSE = sqrt(sum(solvposErr(:).^2)/(numpos));
```

Compare the calibrated RMS position error to initial position RMS error. The calibration reduces the RMS position error.

```
disp(solvposRMSE/initposRMSE)
    7.1582e-04
```


## Estimate Selected ULA Parameters Using Pilot Calibration

Construct a 6 -element ULA of isotropic antenna elements that are spaced one-half wavelength apart. Assume the array has been geometrically perturbed in the $x-y$ plane and contains an unknown taper error. Perform pilot calibration on the array using four pilot sources at azimuth and elevation angles of $(-60,0),(10,-40),(40,0)$, and $(120,45)$ degrees. For the calibration process, pilot signals have an

SNR of 30 dB . Each pilot signal contains 10,000 samples. Assume the signals have a frequency of 600 MHz.

## Set up the ULA with nominal parameters

```
fc = 600e6;
c = physconst('LightSpeed');
lam = c/fc;
d = 0.5*lam;
sIso = phased.IsotropicAntennaElement('FrequencyRange',[100,900]*1e6);
Nelem = 6;
NominalTaper = ones(1,Nelem);
sULA = phased.ULA('Element',sIso,'NumElements',Nelem,'ElementSpacing',d,...
    'Taper',NominalTaper);
```


## Create the pilot signals

Randomly perturb the element positions using a Gaussian distribution that has a standard deviation of 0.13 wavelength. Do not perturb the position of the first element.

```
posstd = 0.13;
rng default
NominalElementPositions = getElementPosition(sULA)/lam;
ReferenceElement = NominalElementPositions(:,1);
PositionPert = [zeros(3,1),posstd*randn(3,Nelem-1)];
ActualElementPositions = NominalElementPositions + PositionPert;
```

Perturb the taper in magnitude and phase. Do not perturb the first taper.

```
tapermagstd = 0.15;
taperphasestd = 0.15;
tapermagpert = tapermagstd*[0; randn(Nelem-1,1)];
ActualTaper = NominalTaper' + tapermagpert;
taperphasepert = taperphasestd*[0;randn(Nelem-1,1)];
ActualTaper = ActualTaper.*exp(1i*taperphasepert);
```

Generate the signals using the perturbed positions and tapers.

```
Nsamp = 10000;
ncov = 0.001;
PilotAng = [-60,10,40,120; 0,-40,0,45];
Npilot = size(PilotAng,2);
for n = 1:Npilot
    X(:,:,n) = sensorsig(ActualElementPositions,Nsamp,...
        PilotAng(:,n),ncov,'Taper',ActualTaper);
end
```


## Perform the pilot calibration

Turn off estimation of taper weights.

```
[estpos,esttaper] = pilotcalib(NominalElementPositions - ReferenceElement*ones(1,Nelem),...
    X,PilotAng,NominalTaper.',[1,1,1,0]');
```

Add back the position of the reference sensor.

```
estpos = estpos + NominalElementPositions(:,1)*ones(1,Nelem);
```


## Examine the root mean square (RMS) error of the calibrated parameters

Compute the RMS values of the initial taper perturbations to compare with the RMS values of the calibrated parameters.

```
tapermagpertRMSE = sqrt(tapermagpert'*tapermagpert/Nelem);
taperphasepertRMSE = sqrt(taperphasepert'*taperphasepert/Nelem);
```

Compute the RMS value of the calibrated taper magnitude error.

```
diff = abs(ActualTaper) - abs(esttaper);
diff2 = diff'*diff;
tapermagsolvRMSE = sqrt(diff2/Nelem);
```

Compare the calibrated RMS magnitude error to the initial RMS error. The calibration reduces the RMS magnitude error.

```
disp(tapermagsolvRMSE/tapermagpertRMSE)
    1.0000
```

Compute the RMS value of the calibrated taper phase error.

```
diff = unwrap(angle(ActualTaper) - angle(esttaper));
diff2 = diff'*diff;
tapersolvphaseRMSE = sqrt(diff2/Nelem);
```

Compare the calibrated RMS phase error to the initial RMS error. The calibration reduces the RMS phase error.

```
disp(tapersolvphaseRMSE/taperphasepertRMSE)
    1
```

Compute the RMS value of the initial position error.

```
numpos = 3*Nelem;
initposRMSE = sqrt(sum(PositionPert(:).^2)/numpos);
```

Compute the RMS value of the calibrated position error.

```
solvposErr = ActualElementPositions - estpos;
solvposRMSE = sqrt(sum(solvposErr(:).^2)/(numpos));
```

Compare the calibrated RMS position error to initial position RMS error. The calibration reduces the RMS position error.

```
disp(solvposRMSE/initposRMSE)
    0.1502
```


## Input Arguments

## nompos - Nominal relative element positions

real-valued 3 -by- $N$ matrix
Nominal relative element positions, specified as a real-valued 3-by- $N$ matrix. The dimension $N$ is the number of elements in the sensor array. Elements positions are relative to the first element of the
array and are specified in units of signal wavelength. Each column of nompos represents the [ $x ; y ; z$ ] coordinates of the corresponding element. The nominal position of all sensors must be within one-half of a wavelength of their actual positions for successful calibration.
Data Types: double
x - Pilot signals
complex-valued $L$-by- $N$-by-M matrix
Pilot signals, specified as a complex-valued $L$-by- $N$-by- $M$ matrix. The argument x represents the signals received by the array when pilot sources are transmitting. The dimension $L$ is the number of snapshots of each pilot source signal. The dimension $N$ is the number of array elements. The dimension $M$ is the number of pilot sources.
Data Types: double
Complex Number Support: Yes
pilotang - Pilot angles
real-valued 2-by-M matrix
Pilot angles, specified as a real-valued 2-by- $M$ matrix. The dimension $M$ is the number of pilot sources. Each column contains the direction of the pilot source in the form [azimuth; elevation]. Angle units are in degrees. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$ and the elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$. The azimuth angle is measured from the $x$-axis to the projection of the source direction into the $x y$ plane, positive toward the $y$-axis. The elevation angle is defined as the angle from the $x y$ plane to the source direction, positive toward the $z$-axis. Calibration source directions must span sufficiently diverse azimuth and elevation angles.
Data Types: double

## nomtaper - Nominal taper

1 (default) | complex-valued N -by-1 column vector
Nominal taper of array elements, specified as a complex-valued $N$-by- 1 column vector. The dimension $N$ is the number of array elements. Each component represents the nominal taper of the corresponding element.
Data Types: double
Complex Number Support: Yes
uncerts - Uncertainty estimation configuration
[ $1,1,1,1]$ (default) | 1-by-4 vector of ones and zeros
Uncertainty estimation configuration, specified as a 1-by-4 vector consisting of 0's and 1's. The vector uncerts determines which uncertainties to estimated. The vector takes the form of [xflag; $y f l a g ; ~ z f l a g ; ~ t a p e r f l a g] . ~ S e t ~ x f l a g, ~ y f l a g, ~ o r ~ z f l a g ~ t o ~ 1 ~ t o ~ e s t i m a t e ~ u n c e r t a i n t i e s ~ i n ~ t h e ~ x, ~$ $y$, or $z$ axes. Set taperflag to 1 to estimate uncertainties in the taper. The number of pilot sources must greater than or equal to the number of 1's in the vector.

For example, set uncerts to $[0 ; 1 ; 1 ; 1]$ to estimate uncertainties in the $y$ and $z$ element position components and the taper simultaneously.
Data Types: double

## Output Arguments

## estpos - Estimated positions

real-valued 3-by- $N$ matrix
Estimated element positions, returned as a real-valued 3-by-N matrix. Units are in signal wavelength. The dimension $N$ is the number of array elements. Each column of estpos represents the [x;y;z] coordinates of the corresponding element.

```
esttaper - Estimated taper
complex-valued \(N\)-by-1 column vector
```

Estimated taper values, returned as a complex-valued $N$-by- 1 column vector. The dimension $N$ is the number of array elements. Each element of esttaper represents the taper of the corresponding sensor element.

## Algorithms

This algorithm requires that the pilot sources be independent narrowband plane-wave signals incoming from the far field region of the array. In addition, signals must not exhibit multipath propagation effects or coherence. All elements in the sensor array are assumed to be isotropic.

The algorithm calibrates relative positions of the array sensors with respect to the first sensor. To use the algorithm, first subtract the position of the first element from each element, then pass the relative array into the function as the nominal position argument to produced the calibrated relative positions. Finally, add back the first element position to all the relative positions to create the fully calibrated array.

## Version History

## Introduced in R2015a

## References

[1] N. Fistas and A. Manikas, "A New General Global Array Calibration Method", IEEE Proceedings of ICASSP, Vol. IV, pp. 73-76, April 1994.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{Tm}}$.
Usage notes and limitations:
Does not support variable-size inputs.

## pol2circpol

Convert linear component representation of field to circular component representation

## Syntax

cfv $=$ pol2circpol(fv)

## Description

cfv = pol2circpol(fv) converts the linear polarization components of the field or fields contained in $f v$ to their equivalent circular polarization components in cfv. The expression of a field in terms of a two-row vector of linear polarization components is called the Jones vector formalism.

## Examples

## Convert Linear to Circular Polarization Components

Express a $45^{\circ}$ linear polarized field in terms of right-circular and left-circular components.

```
fv = [2;2]
fv = 2×1
    2
    2
cfv = pol2circpol(fv)
cfv = 2x1 complex
    1.4142 - 1.4142i
    1.4142 + 1.4142i
```


## Convert Linear Polarization Components to Circular Polarization Components

Specify two input fields [ $1+1 i ;-1+1 i]$ and $[1 ; 1]$ in the same matrix. The first field is a linear representation of a left-circularly polarized field and the second is a linearly polarized field.

```
fv=[1+1i 1;-1+1i 1]
fv = 2x2 complex
    1.0000 + 1.0000i 1.0000 + 0.0000i
    -1.0000 + 1.0000i 1.0000 + 0.0000i
cfv = pol2circpol(fv)
```

```
cfv = 2x2 complex
    1.4142 + 1.4142i 0.7071 - 0.7071i
    0.0000 + 0.0000i 0.7071 + 0.7071i
```


## Input Arguments

fv - Field vector in linear component representation
1 -by- $N$ complex-valued row vector or a 2 -by- $N$ complex-valued matrix
Field vector in its linear component representation specified as a 1-by- $N$ complex row vector or a 2 -by- $N$ complex matrix. If $f v$ is a matrix, each column in $f v$ represents a field in the form of [Eh;Ev], where Eh and Ev are the field's horizontal and vertical polarization components. If $f v$ is a vector, each entry in $f v$ is assumed to contain the polarization ratio, Ev/Eh. For a row vector, the value Inf designates the case when the ratio is computed for a field with $\mathrm{Eh}=0$.
Example: [1;-i]
Example: $2+\mathrm{pi} / 3 * \mathrm{i}$
Data Types: double
Complex Number Support: Yes

## Output Arguments

## cfv - Field vector in circular component representation

1 -by- $N$ complex-valued row vector or 2 -by- $N$ complex-valued matrix
Field vector in circular component representation returned as a 1-by- $N$ complex-valued row vector or 2 -by-Ncomplex-valued matrix. cfv has the same dimensions as $f v$. If $f v$ is a matrix, each column of cfv contains the circular polarization components, [ $\mathrm{El} ; \mathrm{Er}$ ], of the field where El and Er are the left-circular and right-circular polarization components. If $f v$ is a row vector, then cfv is also a row vector and each entry in cfv contains the circular polarization ratio, defined as $\mathrm{Er} / \mathrm{El}$.

## Version History

Introduced in R2013a

## References

[1] Mott, H., Antennas for Radar and Communications, John Wiley \& Sons, 1992.
[2] Jackson, J.D. , Classical Electrodynamics, 3rd Edition, John Wiley \& Sons, 1998, pp. 299-302
[3] Born, M. and E. Wolf, Principles of Optics, 7th Edition, Cambridge: Cambridge University Press, 1999, pp 25-32.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

Usage notes and limitations:
Does not support variable-size inputs.

## See Also <br> circpol2pol|polellip|polratio|stokes

## polellip

Parameters of ellipse traced out by tip of a polarized field vector

## Syntax

```
tau = polellip(fv)
[tau,epsilon] = polellip(fv)
[tau,epsilon,ar] = polellip(fv)
[tau,epsilon,ar,rs] = polellip(fv)
polellip(fv)
```


## Description

tau = polellip(fv) returns the tilt angle, in degrees, of the polarization ellipse of a field or set of fields specified in fv . fv contains the linear polarization components of a field in either one of two forms: (1) each column represents a field in the form of [Eh;Ev], where Eh and Ev are the field's horizontal and vertical linear polarization components or (2) each column contains the polarization ratio, Ev/Eh. The expression of a field in terms of a two-row vector of linear polarization components is called the Jones vector formalism.
[tau,epsilon] = polellip(fv) returns, in addition, a row vector, epsilon, containing the ellipticity angle (in degrees) of the polarization ellipses. The ellipticity angle is the angle determined by the ratio of the length of the semi-minor axis to semi-major axis and lies in the range $\left[-45^{\circ}, 45^{\circ}\right]$. This syntax can use any of the input arguments in the previous syntax.
[tau,epsilon,ar] = polellip(fv) returns, in addition, a row vector, ar, containing the axial ratios of the polarization ellipses. The axial ratio is defined as the ratio of the lengths of the semimajor axis of the ellipse to the semi-minor axis. This syntax can use any of the input arguments in the previous syntaxes.
[tau,epsilon,ar,rs] = polellip(fv) returns, in addition, a cell array of character vectors, rs, containing the rotation senses of the polarization ellipses. Each entry in the array is one of 'Linear', 'Left Circular', 'Right Circular', 'Left Elliptical' or 'Right Elliptical '. This syntax can use any of the input arguments in the previous syntaxes.
polellip(fv) plots the polarization ellipse of the field specified in $f v$. This syntax requires that $f v$ have only one column. Unlike the returned arguments, the size of the drawn ellipse depends upon the magnitude of $f v$.

## Examples

## Tilt Angle for Linearly Polarized Field

Create an input field that is linearly polarized by setting both the horizontal and vertical components to have the same phase. Then, compute the tilt angle.

```
fv = [2;1];
tau = polellip(fv)
```

tau $=26.5651$
For linear polarization, tau is computed using tau $=\operatorname{atan}(f v(2) / f v(1)) * 180 / p i$.

## Tilt Angle and Ellipticity for Elliptically Polarized Field

Start with an elliptically polarized input field (the horizontal and vertical components differ in magnitude and in phase). Choose the phase difference to be $90^{\circ}$.

```
fv = [3*exp(-i*pi/2);1];
[tau,epsilon] = polellip(fv)
tau = 1.3156e-15
epsilon = 18.4349
```

The tilt vanishes because of the $90^{\circ}$ phase difference between the horizontal and vertical components of the field.

## Tilt Angle, Ellipticity and Axial Ratio for Elliptically Polarized Field

Start with an elliptically polarized input field (the horizontal and vertical components differ in magnitude and in phase). Choose the phase difference to be $60^{\circ}$.

```
fv = [2*exp(-i*pi/3);1];
[tau,epsilon,ar] = polellip(fv)
tau = 16.8450
epsilon = 21.9269
ar = -2.4842
```

The nonzero tilt occurs because of the $60^{\circ}$ phase difference. The negative value of the axial ratio indicates left elliptical polarization.

## Tilt Angle, Ellipticity, Axial Ratio and Rotation Sense for Elliptically Polarized Field

Start with an elliptically polarized input field (the horizontal and vertical components differ in magnitude and in phase). Choose the phase difference to be $60^{\circ}$.

```
fv = [2*exp(-i*pi/3);1];
[tau,epsilon,ar,rs] = polellip(fv)
tau = 16.8450
epsilon = 21.9269
ar = -2.4842
```

```
rs = 1x1 cell array
    {'Left Elliptical'}
```

A nonzero tilt occurs because of the $60^{\circ}$ phase difference. The rotation sense is 'Left Elliptical' indicating that the tip of the field vector is moving clockwise when looking towards the source of the field.

## Polarization Ellipse

Draw the figure of an elliptically polarized field. Begin with an elliptically polarized input field (the horizontal and vertical components differ in magnitude and in phase) and choose the phase difference to be 60 degrees.

```
fv = [2*exp(-i*pi/3);1];
```

polellip(fv)


The rotation sense is 'Left Elliptical' as shown by the direction of the arrow on the ellipse. The filled circle at the origin indicates that the observer is looking towards the source of the field.

## Input Argument

## fv - Field vector in linear component representation

1 -by- $N$ complex-valued row vector or 2 -by- $N$ complex-valued matrix
Field vector in linear component representation specified as a 1-by- $N$ complex-valued row vector or 2 -by- $N$ complex-valued matrix. Each column contains an instance of a field specification. If $f v$ is a matrix, each column in fv represents a field in the form of [Eh;Ev], where Eh and Ev are the field's linear horizontal and vertical polarization components. If $f v$ is a row vector, then the row contains the ratio of the vertical to horizontal components of the field Ev/Eh. For a row vector, the value Inf is allowed to designate the case when the ratio is computed for Eh $=0$. Eh and Ev cannot both be set to zero.

Example: [1;-i]
Example: $2+\mathrm{pi} / 3^{*} \mathrm{i}$
Data Types: double
Complex Number Support: Yes

## Output Arguments

## tau - Tilt angle of polarization ellipse

1 -by- $N$ real-valued row vector
Tilt angle of polarization ellipse returned as a 1-by-N real-valued row vector. Each entry in tau contains the tilt angle of the polarization ellipse associated with each column of the field fv. The tilt angle is the angle between the semi-major axis of the ellipse and the horizontal axis (i.e. xaxis) and lies in the range $[-90,90]^{\circ}$.

## epsilon - Ellipticity angle of the polarization ellipse

1 -by- $N$ real-valued row vector
Ellipticity angle of the polarization ellipse returned as 1-by- $N$ real-valued row vector. Each entry in epsilon contains the ellipticity angle of the polarization ellipse associated with each column of the field fv . The ellipticity angle describes the shape of the ellipse and lies in the range $\left[-45^{\circ}, 45^{\circ}\right]$.

## ar - Axial ratio of the polarization ellipse

1 -by- $N$ real-valued row vector
Axial ratio of the polarization ellipse returned as a 1-by- $N$ real-valued row vector. Each entry in ar contains the axial ratio of the polarization ellipse associated with each column of the field fv. The axial ratio is the signed ratio of the major-axis length to the minor-axis length of the polarization ellipse. Its absolute value is always greater than or equal to one. The sign of ar carries the rotational sense of the vector - a negative sign denotes left-handed rotation and a positive sign denotes righthanded rotation.

## rs - Rotation sense of the polarization ellipse

1 -by- $N$ cell array of character vectors
Rotation sense of the polarization ellipse returned as a 1-by- $N$ cell array of character vectors. Each entry in rs contains the rotation sense of the polarization ellipse associated with each column of the field fv. The rotation sense can be one of 'Linear', 'Left Circular', 'Right Circular', 'Left Elliptical' or 'Right Elliptical'.

## Version History

Introduced in R2013a

## References

[1] Mott, H., Antennas for Radar and Communications, John Wiley \& Sons, 1992.
[2] Jackson, J.D. , Classical Electrodynamics, 3rd Edition, John Wiley \& Sons, 1998, pp. 299-302
[3] Born, M. and E. Wolf, Principles of Optics, 7th Edition, Cambridge: Cambridge University Press, 1999, pp 25-32.

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:
Does not support variable-size inputs.

## See Also

circpol2pol|pol2circpol|polratio|stokes

## polloss

Polarization loss

## Syntax

```
rho = polloss(fv_tr,fv_rcv)
rho = polloss(fv_tr,fv_rcv,pos_rcv)
rho = polloss(fv-tr,fv-rcv,pos-rcv,axes_rcv)
rho = polloss(fv_tr,fv_rcv,pos_rcv,axes_rcv,pos tr)
rho = polloss(fv_tr,fv_rcv,pos_rcv,axes_rcv,pos_tr,axes_tr)
```


## Description

rho $=$ polloss (fv_tr,fv_rcv) returns the loss, in decibels, because of mismatch between the polarization of a transmitted field, $f v \_t r$, and the polarization of the receiving antenna, $f v \_r c v$. The field vector lies in a plane orthogonal to the direction of propagation from the transmitter to the receiver. The transmitted field is represented as a 2 -by- 1 column vector [Eh;Ev]. In this vector, Eh and Ev are the field's horizontal and vertical linear polarization components with respect to the transmitter's local coordinate system. The receiving antenna's polarization is specified by a 2 -by- 1 column vector, fv _rcv. You can also specify this polarization in the form of [Eh;Ev] with respect to the receiving antenna's local coordinate system. In this syntax, both local coordinate axes align with the global coordinate system.
rho $=$ polloss(fv_tr,fv_rcv, pos_rcv) specifies, in addition, the position of the receiver. The receiver is defined as a 3 -by- $\overline{1}$ column vector, $[x ; y ; z$ ], with respect to the global coordinate system (position units are in meters). This syntax can use any of the input arguments in the previous syntax.
rho = polloss(fv_tr,fv_rcv,pos_rcv,axes_rcv) specifies, in addition, the orthonormal axes, axes rcv. These axes $\bar{d}$ efine the receiver's local coordinate system as a 3 -by- 3 matrix. The first column gives the $x$-axis of the local system with respect to the global coordinate system. The second and third columns give the $y$ and $z$ axes, respectively. This syntax can use any of the input arguments in the previous syntaxes.
rho = polloss(fv_tr,fv_rcv,pos_rcv,axes_rcv,pos_tr) specifies, in addition, the position of the transmitter as a 3-by-1 column vector, [x;y;z], with respect to the global coordinate system (position units are in meters). This syntax can use any of the input arguments in the previous syntaxes.
rho = polloss(fv_tr,fv_rcv, pos_rcv,axes_rcv, pos_tr, axes_tr) specifies, in addition, the orthonormal axes, axes_ $\bar{t} r$. These axes define the transmitter's local coordinate system as a 3-by-3 matrix. The first column gives the $x$-axis of the local system with respect to the global coordinate system. The second and third columns give the $y$ and $z$ axes, respectively. This syntax can use any of the input arguments in the previous syntaxes.

## Examples

## Mismatch Between $45^{\circ}$ Polarized Field and Horizontally Polarized Receiver

Begin with a $45^{\circ}$ polarized transmitted field and a receiver that is horizontally polarized. By default, the transmitter and receiver local axes coincide with the global coordinate system. Compute the polarization loss in dB .

```
fv_tr = [1;1];
fv_rcv = [1;0];
rhō = polloss(fv_tr,fv_rcv)
rho = 3.0103
```

The loss is 3 dB as expected because only half the power of the field matches to the receive antenna polarization.

## Polarization Loss Unaffected by Receiver Position

Begin with identical transmitter and receiver polarizations. Place the receiver at a position 100 meters along the $y$-axis. The transmitter is at the origin (its default position) and both local coordinate axes coincide with the global coordinate system (by default). First, compute the polarization loss. Then, move the receiver 100 meters along the $x$-axis, and compute the polarization loss again.

```
fv_tr = [1;0];
fv_rcv = [1;0];
pos_rcv = [0;100;0];
rho(1) = polloss(fv_tr,fv_rcv,pos_rcv);
pos_rcv = [100;100;苟;
rho(2) = polloss(fv_tr,fv_rcv,pos_rcv)
rho = 1\times2
    0 0
```

No polarization loss occurs at either position. The spherical basis vectors of each antenna are parallel to other antenna and the polarization vectors are the same.

## Loss Due to Receiver Axes Rotation

Start with identical transmitter and receiver polarizations. Put the receiver at a position 100 meters along the $y$-axis. The transmitter is at the origin (default) and both local coordinate axes coincide with the global coordinate system (default). Compute the loss, and then rotate the receiver $30^{\circ}$ around the $y$-axis. This rotation changes the azimuth and elevation of the transmitter with respect to the receiver and, therefore, the direction of polarization.

```
fv_tr = [1;0];
fv_rcv = [1;0];
pos_rcv = [0;100;0];
ax_rcv = azelaxes(0,0);
rhō(1) = polloss(fv_tr,fv_rcv,pos_rcv,ax_rcv);
```

```
ax_rcv = roty(30)*ax_rcv;
rhō(2) = polloss(fv_\overline{tr},fv_rcv,pos_rcv,ax_rcv)
rho = 1\times2
    0 1.2494
```

The receiver polarization vector remains unchanged. However, rotating the local coordinate system changes the direction of the field of the receiving antenna polarization with respect to global coordinates. This change results in a 1.2 dB loss.

## Polarization Loss Unaffected by Transmitter Position

Start with identical transmitter and receiver polarizations. Put the receiver at a position 100 meters along the $y$-axis. The transmitter is at the origin (default) and both local coordinate axes coincide with the global coordinate system (default). First, compute the polarization loss. Then, move the transmitter 100 meters along the $x$-axis and 100 meters along the $y$-axis, and compute the polarization loss again.

```
fv_tr = [1;0];
fv_rcv = [1;0];
pos_rcv = [0;100;0];
ax_rcv = azelaxes(0,0);
pos_tr = [0;0;0];
rho\overline{(1) = polloss(fv_tr,fv_rcv,pos_rcv,ax_rcv,pos_tr);}
pos_tr = [100;100;0];
rho(2) = polloss(fv_tr,fv_rcv,pos_rcv,ax_rcv,pos_tr)
rho = 1\times2
    0}
```

There is no polarization loss at either position because the spherical basis vectors of each antenna are parallel to their counterparts and the polarization vectors are the same.

## Plot Polarization Loss as Receiving Antenna Rotates

Specifying identical transmitter and receiver polarizations, plot the loss as the local receiving antenna axes rotate around the $x$-axis.

```
fv_tr = [1;0];
fv_rcv = [1;0];
```

The position of the transmitting antenna is at the origin and its local axes align with the global coordinate system. The position of the receiving antenna is 100 meters along the global $x$-axis. However, its local $x$-axis points towards the transmitting antenna.

```
pos_tr = [0;0;0];
axes_tr = azelaxes(0,0);
```

```
pos_rcv = [100;0;0];
axes_rcv0 = rotz(180)*azelaxes(0,0);
```

Rotate the receiving antenna around its local $x$-axis in one-degree increments. Compute the loss for each angle.

```
angles = [0:1:359];
n = size(angles,2);
rho = zeros(1,n); % Initialize space
for k = 1:n
    axes_rcv = rotx(angles(k))*axes_rcv0;
    rho(\overline{k}) = polloss(fv_tr,fv_rcv,pos_tr,axes_tr,...
        pos_rcv,axes_rcv);
end
```

Plot the polarization loss.

```
hp = plot(angles,rho);
hax = hp.Parent;
hax.XLim = [0,360];
xticks = (0:(n-1))*45;
hax.XTick = xticks;
grid;
title('Polarization loss versus receiving antenna rotation')
xlabel('Rotation angle (degrees)');
ylabel('Loss (dB)');
```



The angle-loss plot shows nulls (Inf dB) at 90 degrees and 270 degrees where the polarizations are orthogonal.

## Input Arguments

fv_tr - Transmitted field vector in linear component representation
2-by-1 complex-valued column vector
The transmitted field vector in linear component representation specified as a 2-by-1, complex-valued column vector [Eh;Ev]. In this vector, Eh and Ev are the field's horizontal and vertical linear components.
Example: [1;1]
Data Types: double
Complex Number Support: Yes
fv_rcv - Receiver polarization vector in linear component representation
2-by-1 complex-valued column vector
Receiver polarization vector in linear component representation specified as a 2 -by-1, complex-valued column vector [ $\mathrm{Eh} ; \mathrm{Ev}$ ]. In this vector, Eh and Ev are the polarization vector's horizontal and vertical linear components.

## Example: [0;1]

Data Types: double
Complex Number Support: Yes

## pos_rcv - Receiving antenna position

[0;0;0] (default) | 3 -by-1 real-valued column vector
Receiving antenna position specified as a 3-by-1, real-valued column vector. The components of pos_rcv are specified in the global coordinate system as $[x ; y ; z]$.
Example: [1000;0;0]
Data Types: double

## axes_rcv - Receiving antenna local coordinate axes

3-by-3 identity matrix (default) | 3-by-3 real-valued matrix
Receiving antenna local coordinate axes specified as a 3-by-3, real-valued matrix. Each column is a unit vector specifying the local coordinate system's orthonormal $x, y$, and $z$ axes, respectively, with respect to the global coordinate system. Each column is written in [ $x ; y ; z$ ] form. If axes_rcv is specified as the identity matrix, the local coordinate system is aligned with the global coordinate system.
Example: [1, 0, 0; 0, 1, 0; 0,0 , 1]
Data Types: double

## pos_tr - Transmitter position

[0;0;0] (default) | 3-by-1 real-valued column vector
Transmitter position specified as a 3-by-1, real-valued column vector. The components of pos_tr are specified in the global coordinate system as $[x ; y ; z]$.

## Example: [0;0;0]

Data Types: double

## axes_tr - Transmitting antenna local coordinate axes

3-by-3 identity matrix (default) | 3-by-3 real-valued matrix
Transmitting antenna local coordinate axes specified as a 3-by-3, real-valued matrix. Each column is a unit vector specifying the local coordinate system's orthonormal $x, y$, and $z$ axes, respectively, with respect to the global coordinate system. Each column is written in [ $x ; y ; z$ ] form. If axes_tr is the identity matrix, the local coordinate system is aligned with the global coordinate system.
Example: [1, 0, 0; 0, 1, 0; 0,0 , 1]
Data Types: double

## Output Arguments

## rho - Polarization loss

scalar
Polarization loss returned as scalar in decibel units. The polarization loss is the projection of the normalized transmitted field vector into the normalized receiving antenna polarization vector. Its value lies between zero and unity. When converted into dB , (and a sign changed to show loss as positive) its value lies between 0 and - Inf.

## More About

## Polarization Loss Due to Field and Receiver Mismatch

Loss occurs when a receiver is not matched to the polarization of an incident electromagnetic field.
In the case of the polarization of a field emitted by a transmitting antenna, first, look at the far zone of the transmitting antenna, as shown in the following figure. At this location-which is the location of the receiving antenna-the electromagnetic field is orthogonal to the direction from transmitter to receiver.

You can represent the transmitted electromagnetic field, $f v \_t r$, by the components of a vector with respect to a spherical basis of the transmitter's local coordinate system. The orientation of this basis depends on its direction from the origin. The direction is specified by the azimuth and elevation of the receiving antenna with respect to the transmitter's local coordinate system. Then, the transmitter's polarization, in terms of the spherical basis vectors of the transmitter's local coordinate system, is

$$
\mathbf{E}=E_{H} \widehat{\mathbf{e}}_{a z}+E_{V} \widehat{\mathbf{e}}_{e l}=E_{m} \mathbf{P}_{i}
$$

In the same manner, the receiver's polarization vector, fv _rcv, is defined with respect to a spherical basis in the receiver's local coordinate system. Now, the azimuth and elevation specify the transmitter's position with respect to the receiver's local coordinate system. You can write the receiving antennas polarization in terms of the spherical basis vectors of the receiver's local coordinate system:

$$
\mathbf{P}=P_{H} \widehat{\mathbf{e}}_{a z}^{\prime}+P_{V} \widehat{\mathbf{e}}_{e l}^{\prime}
$$

This figure shows the construction of the different transmitter and receiver local coordinate systems. It also shows the spherical basis vectors with which to write the field components.


The polarization loss is the projection (or dot product) of the normalized transmitted field vector onto the normalized receiver polarization vector. Notice that the loss occurs because of the mismatch in direction of the two vectors not in their magnitudes. Because the vectors are defined in different coordinate systems, they must be converted to the global coordinate system in order to form the projection. The polarization loss is defined by:

$$
\rho=\frac{\left|\mathbf{E}_{i} \cdot \mathbf{P}\right|^{2}}{\left|\mathbf{E}_{i}\right|^{2}|\mathbf{P}|^{2}}
$$

## Version History

Introduced in R2013a

## References

[1] Mott, H. Antennas for Radar and Communications.John Wiley \& Sons, 1992.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{Tm}}$.
Usage notes and limitations:

Does not support variable-size inputs.

## See Also

polellip|stokes

## polratio

Ratio of vertical to horizontal linear polarization components of a field

## Syntax

$\mathrm{p}=$ polratio(fv)

## Description

$\mathrm{p}=$ pol ratio(fv) returns the ratio of the vertical to horizontal component of the field or set of fields contained in fv.

Each column of fv contains the linear polarization components of a field in the form [Eh;Ev], where Eh and Ev are the field's linear horizontal and vertical polarization components. The expression of a field in terms of a two-row vector of linear polarization components is called the Jones vector formalism. The argument fv can refer to either the electric or magnetic part of an electromagnetic wave.

Each entry in $p$ contains the ratio Ev/Eh of the components of $f v$.

## Examples

## Polarization Ratio for $45^{\circ}$ Linearly Polarized Field

Determine the polarization ratio for a linearly polarized field (when the horizontal and vertical components of a field have the same phase).

```
fv = [2;2];
p = polratio(fv)
p = 1
```

The polarization ratio is real. Because the components have equal amplitudes, the polarization ratio is unity.

## Polarization Ratios for Two Fields

Compute the polarization ratios for two fields. The first field is $(2 ; i)$ and the second is $(i ; 1)$.

```
fv = [2,1i;1i,1];
p = polratio(fv)
p = 1\times2 complex
    0.0000 + 0.5000i 0.0000 - 1.0000i
```


## Polarization Ratio for Vertically Polarized Field

Determine the polarization ratio for a vertically polarized field (the horizontal component of the field vanishes).

```
fv = [0;2];
p = polratio(fv)
p = Inf
```

The polarization ratio is infinite as expected from the definition, Ev/Eh.

## Input Arguments

## fv - Field vector in linear component representation <br> 2-by- $N$ complex-valued matrix

Field vector in linear component representation specified as a 2-by- $N$ complex-valued matrix. Each column of fv contains an instance of a field specified by [Eh; Ev], where Eh and Ev are the field's linear horizontal and vertical polarization components. Two rows of the same column cannot both be zero.

Example: [2 , i; i, 1]
Data Types: double
Complex Number Support: Yes

## Output Arguments

## p - Polarization ratio

1-by- $N$ complex-valued row vector
Polarization ratio returned as a 1-by- $N$ complex-valued row vector. p contains the ratio of the components of the second row of fv to the first row, Ev/Eh.

## Version History

## Introduced in R2013a

## References

[1] Mott, H., Antennas for Radar and Communications, John Wiley \& Sons, 1992.
[2] Jackson, J.D. , Classical Electrodynamics, 3rd Edition, John Wiley \& Sons, 1998, pp. 299-302
[3] Born, M. and E. Wolf, Principles of Optics, 7th Edition, Cambridge: Cambridge University Press, 1999, pp 25-32.

## Extended Capabilities

$\mathbf{C} / \mathbf{C}++$ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

Usage notes and limitations:
Does not support variable-size inputs.
See Also
circpol2pol|pol2circpol|polellip|stokes

## polsignature

Copolarization and cross-polarization signatures

## Syntax

```
resp = polsignature(rcsmat)
resp = polsignature(rcsmat,type)
resp = polsignature(rcsmat,type,epsilon)
resp = polsignature(rcsmat,type,epsilon,tau)
polsignature(
``` \(\qquad\)
``` )
```


## Description

resp $=$ polsignature(rcsmat) returns the normalized radar cross-section copolarization (co-pol) signature, resp (in square meters), determined from the scattering cross section matrix, rcsmat of an object. The signature is a function of the transmitting antenna polarization, specified by the ellipticity angle and the tilt angle of the polarization ellipse. In this syntax case, the ellipticity angle takes the values [-45:45] and the tilt angle takes the values [-90:90]. The output resp is a 181-by-91 matrix whose elements correspond to the signature at each ellipticity angle-tilt angle pair.
resp = polsignature(rcsmat,type), in addition, specifies the polarization signature type as one of ' $c$ '|' $x$ ', where ' $c$ ' creates the copolarization signature and ' $x$ ' creates the crosspolarization (cross-pol) signature. The default value of this parameter is ' $c$ '. The output resp is a 181-by-91 matrix whose elements correspond to the signature at each ellipticity angle-tilt angle pair. This syntax can use the input arguments in the previous syntax.
resp = polsignature(rcsmat,type,epsilon), in addition, specifies the transmit antenna polarization's ellipticity angle (in degrees) as a length- $M$ vector. The angle epsilon must lie between $-45^{\circ}$ and $45^{\circ}$. The argument resp is a 181-by-M matrix whose elements correspond to the signature at each ellipticity angle-tilt angle pair. This syntax can use any of the input arguments in the previous syntaxes.
resp = polsignature(rcsmat,type,epsilon,tau), in addition, specifies the tilt angle of the polarization ellipse of the transmitted wave (in degrees) as a length- $N$ vector. The angle tau must be between $-90^{\circ}$ and $90^{\circ}$. The signature, resp, is represented as a function of the transmitting antenna polarization. The transmitting antenna polarization is characterized by the ellipticity angle, epsilon, and the tilt angle, tau. The argument resp is a $N$-by- $M$ matrix whose elements correspond to the signature at each ellipticity angle-tilt angle pair. This syntax can use any of the input arguments in the previous syntaxes.
polsignature( $\qquad$ ) plots a three dimensional surface using any of the syntax forms specified above.

## Examples

## Copolarization Signature of a Dihedral

Calculate and plot the copolarization response to the scattering cross-section matrix, rscmat, of a dihedral object. Specify the ellipticity angle values as [-45:45] and the tilt angle values as [-90:90]. Display the response matrix as an image.

Calculate the copolarization response.

```
rscmat = [-1,0;0,1];
resp = polsignature(rscmat);
```

Plot the copolarization response.

```
el = [-45:45];
tilt = [-90:90];
imagesc(el,tilt,resp);
ylabel('Tilt (degrees)');
xlabel('Ellipticity Angle (degrees)')
axis image
ax = gca;
ax.XTick = [-45:15:45];
ax.YTick = [-90:15:90];
title('Co-polarization signature of dihedral');
colorbar;
```



## Cross-Polarization Signature of a Dihedral

Calculate and plot the cross-polarization response to the scattering cross-section matrix, rscmat, of a dihedral object. Specify the ellipticity angle values as [-45:45] and the tilt angle values as [-90:90]. Display the response matrix as an image.

Calculate the cross-polarization response. To do this, set the type argument to ' x '.

```
rscmat = [-1,0;0,1];
resp = polsignature(rscmat,'x');
```

Plot the cross-polarization response.

```
el = [-45:45];
tilt = [-90:90];
imagesc(el,tilt,resp);
ylabel('Tilt (degrees)');
xlabel('Ellipticity Angle (degrees)');
axis image
ax = gca;
ax.XTick = [-45:15:45];
ax.YTick = [-90:15:90];
title('Cross-polarization signature of dihedral');
colorbar;
```



## Signatures for Linear Polarization with Varied Tilt Angles

Set the ellipticity angle to zero, and vary the tilt angle from -90 to +90 degrees to generate all possible linear polarization directions. Then, plot both the copolarization and cross-polarization signatures.

```
rscmat = [-1,0;0,1];
el = [0];
respc = polsignature(rscmat,'c',el);
respx = polsignature(rscmat,'x',el);
tilt = [-90:90];
plot(tilt,respc,'b',tilt,respx,'r')
ax = gca;
ax.XLim = [-90,90];
ax.XTick = [-90:15:90];
legend('Co-polarization','Cross-polarization')
title('Signatures for linear polarization')
xlabel('Tilt angle (degrees)')
ylabel('Signature')
```



## Copolarization Signature of Dihedral for Left and Right Circular Polarizations

This example shows how to obtain numerical values for the polarization signatures of a dihedral target for left and right circularly polarized incident waves.

Specify the radar cross-section matrix of a dihedral

```
rscmat = [-1,0;0,1];
```

Specify a left circularly-polarized wave and obtain its tilt angle and ellipticity.

```
fv = 1/sqrt(2)*[1;1i];
[tilt_lcp,el_lcp] = polellip(fv);
disp([\tilt_lc̄p,el_lcp])
    45 45
```

Specify a right circularly-polarized wave by complex conjugation of a left circularly-polarized wave. Obtain the polarization ellipse tilt angle and ellipticity.

```
[tilt_rcp,el_rcp] = polellip(conj(fv));
disp([tilt_rcp,el_rcp])
    4 5
        -45
```

Both tilt angles are 45 degrees. Compute the copolarization and cross-polarization signatures for the two waves.

```
el = [el_lcp, el_rcp];
tilt = tīlt_rcp;
respc = polsignature(rscmat,'c',el,tilt);
respx = polsignature(rscmat,'x',el,tilt);
disp(respc)
    1
disp(respx)
    1
```


## Surface Plot of Copolarization Signature of General Target

Use a general RCSM matrix to create a 3-D surface plot.

```
rscmat = [1i*2,0.5; 0.5, -1i];
el = [-45:45];
tilt = [-90:90];
```

With no output arguments, polsignature automatically creates a surface plot.

```
polsignature(rscmat,'c',el,tilt);
```



## Input Arguments

## rcsmat - Radar cross-section scattering matrix

## 2-by-2 complex-valued matrix

Radar cross-section scattering matrix (RCSM) of an object specified as a 2-by-2, complex-valued matrix. The radar cross-section scattering matrix describes the polarization of a scattered wave as a function of the polarization of an incident wave upon a target. The response to an incident wave can be construct from the individual responses to the incident field's horizontal and vertical polarization components. These components are taken with respect to the transmit antenna or array local coordinate system. The scattered wave can be decomposed into horizontal and vertical polarization components with respect to the receive antenna or array local coordinate system. The matrix RCSM contains four components [rcs_hh rcs_hv; rcs_vh rcs_vv] where each component is the radar cross section defined by the polarization of the transmit and receive antennas.

- rcs_hh - Horizontal response due to horizontal transmit polarization component
- rcs_hv - Horizontal response due to vertical transmit polarization component
- rcs_vh - Vertical response due to horizontal transmit polarization component
- rcs_vv - Vertical response due to vertical transmit polarization component

In the monostatic radar case, when the wave is backscattered, the RCSM matrix is symmetric.
Example: [-1,1i;1i,1]

## Data Types: double

Complex Number Support: Yes

## type - Polarization signature type <br> ' C' (default) | single character ' C' | 'x'

Polarization signature type of the scattered wave specified by a single character: ' c ' denoting the copolarized signature or ' $x$ ' denoting the cross-polarized signature.
Example: ' x '
Data Types: char
epsilon - Ellipticity angle of the polarization ellipse of the transmitted wave
[-45:45] (default) | scalar or 1-by-M real-valued row vector
Ellipticity angle of the polarization ellipse of the transmitted wave specified as a length- $M$ vector. Units are degrees. The ellipticity angle describes the shape of the ellipse. By definition, the tangent of the ellipticity angle is the signed ratio of the semiminor axis to semimajor axis of the polarization ellipse. Since the absolute value of this ratio cannot exceed unity, the ellipticity angle lies between $\pm 45^{\circ}$.

Example: [-45:0.5:45]
Data Types: double

## tau - Tilt angle of the polarization ellipse of the transmitted wave

[-90:90] (default) | scalar or 1-by- $N$ real-valued row vector.
Tilt angle of the polarization ellipse of the transmitted wave specified as a length- $N$ vector. Units are degrees. The tilt angle is defined as the angle between the semimajor axis of the ellipse and the $x$ axis. Because the ellipse is symmetrical, an ellipse with a tilt angle of $100^{\circ}$ is the same ellipse as one with a tilt angle of $-80^{\circ}$. Therefore, the tilt angle need only be specified between $\pm 90^{\circ}$.
Example: [-30:2:30]
Data Types: double

## Output Arguments

## resp - Normalized magnitude response

scalar or $N$-by- $M$ real-valued matrix.
Normalized magnitude response returned as a scalar or $N$-by- $M$, real-valued matrix having values between 0 and 1. resp returns a value for each ellipticity-tilt angle pair.

## More About

## Scattering Cross-Section Matrix

Scattering cross-section matrix determines response of an object to incident polarized electromagnetic field.

When a polarized plane wave is incident on an object, the amplitude and polarization of the scattered wave may change with respect to the incident wave polarization. The polarization may depend upon the direction from which the scattered wave is observed. The exact way that the polarization changes
depends upon the properties of the scattering object. The quantity describing the response of an object to the incident field is called the scattering cross-section matrix, $S$. The scattering matrix can be measured as follows: when a unit amplitude horizontally polarized wave is scattered, both a horizontal and vertical scattered component are produced. Call these two components $S_{H H}$ and $S_{V H}$. These are complex numbers containing the amplitude and phase changes from the incident wave. Similarly, when a unit amplitude vertically polarized wave is scattered, the horizontal and vertical scattered component produced are $S_{H V}$ and $S_{V V}$. Because any incident field can be decomposed into horizontal and vertical components, stack these quantities into a matrix and write the scattered field in terms of the incident field

$$
\left[\begin{array}{l}
E_{H}^{(s c)} \\
E_{V}^{(s c)}
\end{array}\right]=\left[\begin{array}{ll}
S_{H H} & S_{V H} \\
S_{H V} & S_{V V}
\end{array}\right]\left[\begin{array}{l}
E_{H}^{(i n c)} \\
E_{V}^{(i n c)}
\end{array}\right]=S\left[\begin{array}{l}
E_{H}^{(i n c)} \\
E_{V}^{(i n c)}
\end{array}\right]
$$

The scattering cross section matrix depends upon the angles that the incident and scattered fields make with the object. When the incident field is backscattered to the transmitting antenna, the scattering matrix is symmetric.

## Polarization Signature

Polarization signature for visualizing scattering cross-section matrix.
To understand how the scattered wave depends upon the polarization of the incident wave, an examination of all possible scattered field polarizations for each incident polarization is required. Because this amount of data is difficult to visualize, you can look at two particular scattered polarizations:

- Choose one polarization that has the same polarization as the incident field (copolarization)
- Choose a second one that is orthogonal to the polarization of the incident field (cross-polarization)

Both the incident and orthogonal polarization states can be specified in terms of the tilt angleellipticity angle pair ( $\tau, \varepsilon$ ). From the incident field tilt and ellipticity angles, the unit incident polarization vector can be expressed as

$$
\left[\begin{array}{l}
E_{H}^{(i n c)} \\
E_{V}^{(i n c)}
\end{array}\right]=\left[\begin{array}{cc}
\cos \tau & -\sin \tau \\
\sin \tau & \cos \tau
\end{array}\right]\left[\begin{array}{c}
\cos \varepsilon \\
j \sin \varepsilon
\end{array}\right]
$$

while the orthogonal polarization vector is

$$
\left[\begin{array}{l}
E_{H}^{(i n c) \perp} \\
E_{V}^{(i n c)} \perp
\end{array}\right]=\left[\begin{array}{cc}
-\sin \tau & -\cos \tau \\
\cos \tau & -\sin \tau
\end{array}\right]\left[\begin{array}{c}
\cos \varepsilon \\
-j \sin \varepsilon
\end{array}\right]
$$

To form the copolarization signature, use the RCSM matrix, $S$, to compute:

$$
P^{(c o)}=\left[E_{H}^{(i n c)} E_{V}^{(i n c)}\right] * S\left[\begin{array}{l}
E_{H}^{(i n c)} \\
E_{V}^{(i n c)}
\end{array}\right]
$$

where [ ]* denotes complex conjugation. For the cross-polarization signature, compute

$$
P^{(\text {cross })}=\left[\begin{array}{ll}
E_{H}^{(\text {inc }) \perp} & E_{V}^{(\text {inc }) \perp}
\end{array}\right] * S\left[\begin{array}{l}
E_{H}^{(\text {inc })} \\
E_{V}^{(i n c)}
\end{array}\right]
$$

The output of this function is the absolute value of each signature normalized by its maximum value.

## Version History <br> Introduced in R2013a <br> References

[1] Mott, H. Antennas for Radar and Communications.John Wiley \& Sons, 1992.
[2] Fawwaz, U. and C. Elachi. Radar Polarimetry for Geoscience Applications. Artech House, 1990.
[3] Lee, J. and E. Pottier. Polarimetric Radar Imaging: From Basics to Applications. CRC Press, 2009.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:

- Does not support variable-size inputs.
- Supported only when output arguments are specified.

See Also<br>polellip|polloss|stokes

## pulsint

Pulse integration

## Syntax

$Y=$ pulsint $(X)$
$Y=$ pulsint (X,METHOD)

## Description

$Y=$ pulsint ( $X$ ) performs video (noncoherent) integration of the pulses in $X$ and returns the integrated output in $Y$. Each column of $X$ is one pulse.
$Y=$ pulsint ( $\mathrm{X}, \mathrm{METHOD}$ ) performs pulse integration using the specified method. METHOD is "coherent" or "noncoherent".

## Examples

## Noncoherent and Coherent Integration of Pulses

Generate ten pulses of a sinusoid with added Gaussian white noise. Plot the pulse magnitudes.

```
npulse = 10;
x = repmat(sin(2*pi*(0:99)'/100),1,npulse) + 0.1*randn(100,npulse);
plot(abs(x))
ylabel("Magnitude")
title("Pulses")
```



Perform noncoherent integration of the pulses. Repeat the computation, but now perform coherent integration. Plot the magnitudes of the integrated pulses

```
yn = pulsint(x);
subplot(2,1,1)
plot(abs(yn))
ylabel("Magnitude")
title("Noncoherent Integrated Pulse")
yc = pulsint(x,"coherent");
subplot(2,1,2)
plot(abs(yc))
ylabel("Magnitude")
title("Coherent Integrated Pulse")
```



## Input Arguments

## X - Pulse input data

matrix
Pulse input data, specified as a matrix. Each column of $X$ is one pulse.
Example: sin(pi./[32 32].*(0:2047)')+randn(2048,2)/10
Data Types: double

## METHOD - Pulse integration method

"noncoherent" (default)| "coherent"
Pulse integration method, specified as "coherent" or "noncoherent". METHOD is the method used to integrate the pulses in the columns of $X$. The values are not case sensitive.
Data Types: char \| string

## Output Arguments

Y - Integrated pulse
column vector
Integrated pulse, returned as an $N$-by- 1 column vector, where $N$ is the number of rows in the input X .

## More About

## Coherent Integration

Let $X_{i j}$ denote the $(i, j)$-th entry of an $M$-by- $N$ matrix of pulses $X$.
The coherent integration of the pulses in $X$ is:

$$
Y_{i}=\sum_{j=1}^{N} X_{i j}
$$

## Noncoherent (video) Integration

Let $X_{i j}$ denote the $(i, j)$-th entry of an $M$-by- $N$ matrix of pulses $X$.
The noncoherent (video) integration of the pulses in $X$ is:

$$
Y_{i}=\sqrt{\sum_{j=1}^{N}\left|X_{i j}\right|^{2}}
$$

## Version History <br> Introduced in R2011a

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:
Does not support variable-size inputs.

## References

[1] Richards, M. A. Fundamentals of Radar Signal Processing. New York: McGraw-Hill, 2005.

## See Also

phased.MatchedFilter

## radialspeed

Relative radial speed

## Syntax

Rspeed = radialspeed(Pos,V)
Rspeed = radialspeed(Pos,V,RefPos)
Rspeed $=$ radialspeed(Pos,V,RefPos,RefV)

## Description

Rspeed = radialspeed (Pos, V ) returns the radial speed of the given platforms relative to a reference platform. The platforms have positions Pos and velocities V. The reference platform is stationary and is located at the origin.

Rspeed $=$ radialspeed(Pos, V, RefPos) specifies the position of the reference platform.
Rspeed $=$ radialspeed(Pos,V,RefPos,RefV) specifies the velocity of the reference platform.

## Examples

## Radial Speed of Target Relative to Stationary Platform

Calculate the radial speed of a target relative to a stationary platform. Assume the target is located at $(20,20,0)$ meters in Cartesian coordinates and is moving with velocity $(10,10,0)$ meters per second. The reference platform is located at $(1,1,0)$.

```
rspeed = radialspeed([20; 20; 0],[10; 10; 0],[1; 1; 0])
rspeed = -14.1421
```

Negative radial speed indicates that the target is receding from the platform.

## Input Arguments

## Pos - Positions of platforms

## matrix

Positions of platforms, specified as a 3-by-N matrix. Each column specifies a position in the form [ $x ; y$; $z$ ], in meters.

## Example: [20; 20; 0]

Data Types: double

## V - Velocities of platforms

matrix

Velocities of platforms, specified as a 3-by-N matrix. Each column specifies a velocity in the form [ $x$; $y$; $z]$, in meters per second.
Example: [10; 10; 0]
Data Types: double
RefPos - Position of reference platform
[0; 0; 0] (default)|vector
Position of reference platform, specified as a 3-by-1 vector. The vector has the form $[x ; y ; z]$, in meters.

Example: [1; 1; 0]
Data Types: double

## RefV - Velocity of reference platform

[0; 0; 0] (default) | vector
Velocity of reference platform, specified as a 3-by-1 vector. The vector has the form $[x ; y ; z]$, in meters per second.
Example: [1; -1; 0]
Data Types: double

## Output Arguments

## Rspeed - Radial speed

vector
Radial speed in meters per second, returned as an N-by-1 vector. Each number in the vector represents the radial speed of the corresponding platform. Positive numbers indicate that the platform is approaching the reference platform. Negative numbers indicate that the platform is moving away from the reference platform.

## Version History

## Introduced in R2011a

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder ${ }^{\mathrm{TM}}$.
Usage notes and limitations:
Does not support variable-size inputs.

## See Also

phased.Platform|speed2dop

## Topics

"Doppler Shift and Pulse-Doppler Processing"
"Motion Modeling in Phased Array Systems"

## rainpl

RF signal attenuation due to rainfall

## Syntax

$L=$ rainpl(range,freq, rainrate)
$L=r a i n p l(r a n g e, f r e q, r a i n r a t e, e l e v)$
$L=r a i n p l(r a n g e, f r e q, r a i n r a t e, e l e v, t a u)$
$L=$ rainpl(range,freq, rainrate,elev,tau,pct)

## Description

$L=r a i n p l(r a n g e, f r e q, r a i n r a t e)$ returns the signal attenuation, $L$, due to rainfall. In this syntax, attenuation is a function of signal path length, range, signal frequency, freq, and rain rate, rainrate. The path elevation angle and polarization tilt angles are assumed to zero.

The rainpl function applies the International Telecommunication Union (ITU) rainfall attenuation model to calculate path loss of signals propagating in a region of rainfall [1]. The function applies when the signal path is contained entirely in a uniform rainfall environment. Rain rate does not vary along the signal path. The attenuation model applies only for frequencies at $1-1000 \mathrm{GHz}$.
$\mathrm{L}=$ rainpl(range,freq,rainrate, elev) also specifies the elevation angle, elev, of the propagation path.
$\mathrm{L}=$ rainpl(range, freq, rainrate, elev, tau) also specifies the polarization tilt angle, tau, of the signal.

L = rainpl(range,freq, rainrate,elev,tau,pct) also specifies the specified percentage of time, pct. pct is a scalar in the range of 0.001-1, inclusive. The attenuation, $L$, is computed from a power law using the long-term statistical $0.01 \%$ rain rate (in $\mathrm{mm} / \mathrm{h}$ ).

## Examples

## Signal Attenuation Due to Rainfall

Compute the signal attenuation due to rainfall for a 20 GHz signal over a distance of 10 km in light and heavy rain.

Propagate the signal in a light rainfall of $1 \mathrm{~mm} / \mathrm{hr}$.

```
rr = 1.0;
L = rainpl(10000,20.0e9,rr)
L = 1.3009
```

Propagate the signal in a heavy rainfall of $10 \mathrm{~mm} / \mathrm{hr}$.

```
rr = 10.0;
L = rainpl(10000,20.0e9,rr)
```


## Signal Attenuation Due to Rainfall as Function of Frequency

Plot the signal attenuation due to a $20 \mathrm{~mm} / \mathrm{hr}$ statistical rainfall for signals in the frequency range from 1 to 1000 GHz . The path distance is 10 km .
$r r=20.0 ;$
freq $=$ [1:1000]*1e9;
L = rainpl(10000,freq,rr);
semilogx (freq/le9, L)
grid
xlabel('Frequency (GHz)')
ylabel('Attenuation (dB)')


## Signal Attenuation Due to Rainfall as Function of Elevation Angle

Compute the signal attenuation due to heavy rain as a function of elevation angle. Elevation angles vary from 0 to 90 degrees. Assume a path distance of 100 km and a signal frequency of 100 GHz .

Set the rain rate to $10 \mathrm{~mm} / \mathrm{hr}$.

```
rr = 10.0;
```

Set the elevation angles, frequency, range.

```
elev = [0:1:90];
freq = 100.0e9;
rng = 100000.0*ones(size(elev));
```

Compute and plot the loss.

```
L = rainpl(rng,freq,rr,elev);
plot(elev,L)
grid
xlabel('Path Elevation (degrees)')
ylabel('Attenuation (dB)')
```



## Signal Attenuation Due to Rainfall as Function of Polarization

Compute the signal attenuation due to heavy rainfall as a function of the polarization tilt angle. Assume a path distance of 100 km , a signal frequency of 100 GHz , and a path elevation angle of 0 degrees. Set the rainfall rate to $10 \mathrm{~mm} /$ hour. Plot the signal attenuation versus polarization tilt angle.

Set the polarization tilt angle to vary from -90 to 90 degrees.

```
tau = -90:90;
```

Set the elevation angle, frequency, path distance, and rain rate.

```
elev = 0;
freq = 100.0e9;
rng = 100e3*ones(size(tau));
rr = 10.0;
```

Compute and plot the attenuation.
L = rainpl(rng,freq,rr,elev,tau);
plot(tau,L)
grid
xlabel('Tilt Angle (degrees)')
ylabel('Attenuation (dB)')


## Input Arguments

## range - Signal path length

nonnegative real-valued scalar | nonnegative real-valued $M$-by- 1 column vector | nonnegative realvalued 1-by-M row vector

Signal path length, specified as a nonnegative real-valued scalar, or as a $M$-by-1 or 1-by- $M$ vector. Units are in meters.

Example: [13000.0,14000.0]

## freq - Signal frequency

positive real-valued scalar | nonnegative real-valued $N$-by-1 column vector | nonnegative real-valued 1-by- $N$ row vector

Signal frequency, specified as a positive real-valued scalar, or as a nonnegative $N$-by-1 or 1-by- $N$ vector. Frequencies must lie in the range $1-1000 \mathrm{GHz}$.
Example: [1400.0e6, 2.0e9]

## rainrate - Long-term statistical rain rate

nonnegative real-valued scalar
Long-term statistical rain rate, specified as a nonnegative real-valued scalar. The long-term statistical rain rate is the rain rate that is exceeded $0.01 \%$ of the time. You can adjust the percent of time using the pct argument. Units are in $\mathrm{mm} / \mathrm{hr}$.

## Example: 1.5

## elev - Signal path elevation angle

0.0 (default) | real-valued scalar | real-valued $M$-by-1 column vector | real-valued 1-by- $M$ row vector

Signal path elevation angle, specified as a real-valued scalar, or as an $M$-by-1 or 1-by- $M$ vector. Units are in degrees between $-90^{\circ}$ and $90^{\circ}$. If elev is a scalar, all propagation paths have the same elevation angle. If elev is a vector, its length must match the dimension of range and each element in elev corresponds to a propagation range in range.
Example: [0,45]

## tau - Tilt angle of polarization ellipse

0.0 (default) | real-valued scalar | real-valued $M$-by-1 column vector | real-valued 1-by- $M$ row vector

Tilt angle of the signal polarization ellipse, specified as a real-valued scalar, or as an M-by-1 or 1-by$M$ vector. Units are in degrees between $-90^{\circ}$ and $90^{\circ}$. If tau is a scalar, all signals have the same tilt angle. If tau is a vector, its length must match the dimension of range. In that case, each element in tau corresponds to a propagation path in range.

The tilt angle is defined as the angle between the semi-major axis of the polarization ellipse and the $x$ axis. Because the ellipse is symmetrical, a tilt angle of $100^{\circ}$ corresponds to the same polarization state as a tilt angle of $-80^{\circ}$. Thus, the tilt angle need only be specified between $\pm 90^{\circ}$.
Example: [45, 30]

## pct - Exceedance percentage of rainfall

0.01 (default) | positive scalar between 0.001 and 1

Exceedance percentage of rainfall, specified as a positive scalar between 0.001 and 1. The long-term statistical rain rate is the rain rate that is exceeded pct of the time. Units are dimensionless.
Data Types: double

## Output Arguments

## L - Signal attenuation

real-valued $M$-by- $N$ matrix

Signal attenuation, returned as a real-valued $M$-by- $N$ matrix. Each matrix row represents a different path where $M$ is the number of paths. Each column represents a different frequency where $N$ is the number of frequencies. Units are in dB.

## More About

## Rainfall Attenuation Model

This model calculates the attenuation of signals that propagate through regions of rainfall. Rain attenuation is a dominant fading mechanism and can vary from location-to-location and from year-toyear.

Electromagnetic signals are attenuated when propagating through a region of rainfall. Rainfall attenuation is computed according to the ITU rainfall model Recommendation ITU-R P.838-3: Specific attenuation model for rain for use in prediction methods. The model computes the specific attenuation (attenuation per kilometer) of a signal as a function of rainfall rate, signal frequency, polarization, and path elevation angle. The specific attenuation, $\gamma_{R}$, is modeled as a power law with respect to rain rate

$$
\gamma_{R}=k R^{\alpha},
$$

where $R$ is rain rate. Units are in $\mathrm{mm} / \mathrm{hr}$. The parameter $k$ and exponent $\alpha$ depend on the frequency, the polarization state, and the elevation angle of the signal path. The specific attenuation model is valid for frequencies from 1-1000 GHz.

To compute the total attenuation for narrowband signals along a path, the function multiplies the specific attenuation by the an effective propagation distance, $d_{\text {eff }}$. Then, the total attenuation is $L=$ $d_{\text {eff }} Y_{R}$.

The effective distance is the geometric distance, $d$, multiplied by a scale factor

$$
r=\frac{1}{0.477 d^{0.633} R_{0.01}^{0.073 \alpha} f^{0.123}-10.579(1-\exp (-0.024 d))}
$$

where $f$ is the frequency. The article Recommendation ITU-R P.530-17 (12/2017): Propagation data and prediction methods required for the design of terrestrial line-of-sight systems presents a complete discussion for computing attenuation.

The rain rate, $R$, used in these computations is the long-term statistical rain rate, $R_{0.01}$. This is the rain rate that is exceeded $0.01 \%$ of the time. The calculation of the statistical rain rate is discussed in Recommendation ITU-R P.837-7 (06/2017): Characteristics of precipitation for propagation modelling. This article also explains how to compute the attenuation for other percentages from the $0.01 \%$ value.

You can apply the attenuation model to wideband signals. First, divide the wideband signal into frequency subbands and apply attenuation to each subband. Then, sum all attenuated subband signals into the total attenuated signal.

## Version History

## Introduced in R2016a

## References

[1] Radiocommunication Sector of International Telecommunication Union. Recommendation ITU-R P.838-3: Specific attenuation model for rain for use in prediction methods. 2005.
[2] Radiocommunication Sector of International Telecommunication Union. Recommendation ITU-R P.530-17: Propagation data and prediction methods required for the design of terrestrial line-of-sight systems. 2017.
[3] Recommendation ITU-R P.837-7: Characteristics of precipitation for propagation modelling
[4] Seybold, J. Introduction to RF Propagation. New York: Wiley \& Sons, 2005.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
Does not support variable-size inputs.

## See Also

fspl | gaspl| fogpl| cranerainpl| LOSChannel | WidebandLOSChannel

## range2beat

Convert range to beat frequency

## Syntax

```
fb = range2beat(r,slope)
fb = range2beat(r,slope,c)
```


## Description

$\mathrm{fb}=$ range2beat ( r , slope) converts the range of a dechirped linear FMCW signal to the corresponding beat frequency on page 2-341. slope is the slope of the FMCW sweep.
$\mathrm{fb}=$ range2beat ( $\mathrm{r}, \mathrm{slope}, \mathrm{c}$ ) specifies the signal propagation speed.

## Examples

## Maximum Beat Frequency in FMCW Radar System

Calculate the maximum beat frequency in MHz for an upsweep FMCW waveform. The waveform sweeps a 300 MHz band in 1 ms . Assume that the waveform can detect a stationary target as far as 18 km .

```
slope = 300e6/1e-3;
r = 18e3;
fb = range2beat(r,slope)/le6
fb = 36.0249
```


## Input Arguments

## r - Range

array of nonnegative numbers
Range, specified as an array of nonnegative numbers in meters.
Data Types: double
slope - Sweep slope
nonzero scalar
Slope of FMCW sweep, specified as a nonzero scalar in hertz per second.
Data Types: double
c - Signal propagation speed
speed of light (default) | positive scalar
Signal propagation speed, specified as a positive scalar in meters per second.

## Data Types: double

## Output Arguments

## fb - Beat frequency of dechirped signal <br> array of nonnegative numbers

Beat frequency of dechirped signal, returned as an array of nonnegative numbers in hertz. Each entry in fb is the beat frequency corresponding to the corresponding range in r . The dimensions of fb match the dimensions of $r$.

Data Types: double

## More About

## Beat Frequency

For an up-sweep or down-sweep FMCW signal, the beat frequency is $F_{t}-F_{r}$. In this expression, $F_{t}$ is the transmitted signal's carrier frequency, and $F_{r}$ is the received signal's carrier frequency.

For an FMCW signal with triangular sweep, the upsweep and downsweep have separate beat frequencies.

## Algorithms

The function computes $2 * r *$ slope/c.

## Version History

## Introduced in R2012b

## References

[1] Pace, Phillip. Detecting and Classifying Low Probability of Intercept Radar. Artech House, Boston, 2009.
[2] Skolnik, M.I. Introduction to Radar Systems. New York: McGraw-Hill, 1980.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:
Does not support variable-size inputs.

## See Also

beat2range | dechirp|rdcoupling|stretchfreq2rng|phased.FMCWWaveform

## Topics

"Automotive Adaptive Cruise Control Using FMCW Technology" (Radar Toolbox)

## range2bw

Convert range resolution to required bandwidth

## Syntax

```
bw = range2bw(rngres)
bw = range2bw(rngres,c)
```


## Description

Note The use of range2bw is not recommended. Use rangeres2bw instead.
bw = range2bw(rngres) returns the bandwidth needed to distinguish two targets separated by a given range. Such capability is often referred to as range resolution. The propagation is assumed to be two-way, as in a monostatic radar system.
bw $=$ range2bw(rngres,c) specifies the signal propagation speed.

## Input Arguments

## rngres - Target range resolution

positive scalar | MATLAB array of positive real values
Target range resolution in meters, specified as a scalar or a MATLAB array of positive real values.
Data Types: double
c - Signal propagation speed
speed of light (default) | positive scalar
Signal propagation speed, specified as a positive scalar. Units are in meters per second.
Data Types: double

## Output Arguments

## bw - Required bandwidth

positive scalar | MATLAB array of positive real values
Required bandwidth in hertz, returned as a MATLAB array of positive real values. The dimensions of bw are the same as those of rngres.

## Tips

- This function assumes two-way propagation. For one-way propagation, you can find the required bandwidth by multiplying the output of this function by 2 .


## Algorithms

The function computes c/(2*rngres).

## Version History

Introduced in R2012b

## References

[1] Skolnik, M. Introduction to Radar Systems, 3rd Ed. New York: McGraw-Hill, 2001.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
Does not support variable-size inputs.

## See Also

## Functions

bw2 range | time2range | range2time
Objects
phased.FMCWWaveform

## Topics

"Automotive Adaptive Cruise Control Using FMCW Technology" (Radar Toolbox)

## range2time

Convert propagation distance to propagation time

## Syntax

$\mathrm{t}=$ range2time(r)
$\mathrm{t}=$ range2time( $\mathrm{r}, \mathrm{c}$ )

## Description

$\mathrm{t}=$ range2time $(\mathrm{r})$ returns the time a signal takes to propagate a given distance. The propagation is assumed to be two-way, as in a monostatic radar system.
$t=r a n g e 2 t i m e(r, c)$ specifies the signal propagation speed.

## Examples

## PRF for Specified Unambiguous Range

Calculate the required PRF in Hertz for a monostatic radar system so that it can have a maximum unambiguous range of 15 km .

```
r = 15.0e3;
prf = 1/range2time(r)
prf = 9.9931e+03
```


## Input Arguments

r-Signal range<br>array of nonnegative numbers

Signal range in meters, specified as an array of nonnegative numbers.
Data Types: double
c - Signal propagation speed
speed of light (default) | positive scalar
Signal propagation speed, specified as a positive scalar in meters per second.
Data Types: double

## Output Arguments

Propagation time in seconds, returned as an array of nonnegative numbers. The dimensions of $t$ are the same as those of $r$.

## Algorithms

The function computes $2 * r / c$.

## Version History

Introduced in R2012b

## References

[1] Skolnik, M. Introduction to Radar Systems, 3rd Ed. New York: McGraw-Hill, 2001.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:
Does not support variable-size inputs.

See Also<br>time2range | range2bw | phased. FMCWWaveform<br>Topics<br>"Automotive Adaptive Cruise Control Using FMCW Technology" (Radar Toolbox)

## range2tl

Compute underwater sound transmission loss from range

## Syntax

```
tl = range2tl(rng,freq,depth)
```


## Description

$t l=r a n g e 2 t l(r n g, f r e q$, depth $)$ returns the transmission loss, $t l$, for a sound wave of frequency freq arriving from a source at distance rng. The channel depth is depth. The transmission loss is due to geometrical spreading and frequency-dependent absorption. This function is the inverse of tl2 range.

## Examples

## Estimate Transmission Loss from Range

Find the transmission loss (in dB ) for a sonar operating at 2 kHz in a channel that is 200 m deep. The sound path is 1000.0 m long.

```
rng = 1000.0;
freq = 2000.0;
depth = 200;
tl = range2tl(rng,freq,depth)
tl = 50.1261
```


## Input Arguments

## rng - Distance from sound source to receiver

positive scalar
Distance from sound source to receiver, specified as a positive scalar. Units are in meters.
Example: 10e3
Data Types: double

## freq - Frequency of sound positive scalar

Frequency of sound, specified as a positive scalar. Units are in Hz.
Example: 1e3
Data Types: double

## depth - Channel depth

positive scalar

Channel depth, specified as a positive scalar. Units are in meters.
Example: 200
Data Types: double

## Output Arguments

## tl - Transmission loss

positive scalar
Transmission loss, returned as a positive scalar. Units are in dB .
Data Types: double

## Limitations

- The transmission loss model assumes that seawater salinity is $35 \mathrm{ppt}, \mathrm{pH}$ is 8 , and temperature is $10^{\circ} \mathrm{C}$.
- The transmission loss model is valid for frequencies less than or equal to 2.0 MHz .


## Version History <br> Introduced in R2017b

## References

[1] Ainslie M. A. and J.G. McColm. "A simplified formula for viscous and chemical absorption in sea water." Journal of the Acoustical Society of America, Vol. 103, Number 3, 1998, pp. 1671--1672.
[2] Urick, Robert J. Principles of Underwater Sound, 3rd ed. Los Altos, CA:Peninsula Publishing, 1983.

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder ${ }^{\mathrm{TM}}$.
Usage notes and limitations:
Does not support variable-size inputs.

## See Also

sonareqtl| sonareqsnr|sonareqsl|tl2range

## Topics

"Transmission Loss (TL)"
"Sonar Equation"

## External Websites

http://resource.npl.co.uk/acoustics/techguides/seaabsorption/\#content

## rangeMigrationFMCW

Range migration image formation algorithm for frequency-modulated CW waveform

## Syntax

```
slcimg = rangeMigrationFMCW(raw,waveform,fc,v,rc)
slcimg = rangeMigrationFMCW(raw,waveform,fc,v,rc,Name=Value)
```


## Description

slcimg = rangeMigrationFMCW(raw, waveform,fc, v, rc) returns a single-look complex image of raw synthetic aperture radar (SAR) data obtained with a frequency modulated continuous wave (FMCW) waveform. The function uses the range migration algorithm.
slcimg $=$ rangeMigrationFMCW(raw, waveform, fc, v, rc, Name=Value) specifies additional inputs using name-value arguments. You can specify the squint angle of the antenna and the signal propagation speed.

## Examples

## Single-Look Complex Image from Unfocused FMCW Data

Load a file that contains simulated unfocused synthetic aperture radar (SAR) data obtained with a frequency modulated continuous wave waveform sampled at 15 MHz . The waveform has a sweep time of 25 microseconds, a sweep bandwidth of 20 MHz , and sweeps in the "Down" direction.

```
data = load("RangeMigrationFMCWExampleData");
raw = data.raw;
wvf = phased.FMCWWaveform(SampleRate=15e6, ...
    SweepTime=2.5e-5,SweepBandwidth=20e6,SweepDirection="Down");
```

The system works at an operating frequency of 3 GHz . The platform moves at a velocity of 200 meters per second and the distance between the beam center on the ground and the radar is 46.672 meters.

```
fc = 3e9;
v = 200;
rc = 46.672;
```

Generate a single-look complex image from the data. Plot the image and zoom in on the first 20 alongrange samples.

```
slcimg = rangeMigrationFMCW(raw,wvf,fc,v,rc);
imagesc(abs(slcimg(1:20,:)))
xlabel("Cross-Range Samples")
ylabel("Range Samples")
```



## Input Arguments

## raw - Raw SAR data

matrix
Raw SAR data, specified as a matrix. The data is the unfocused in-phase and quadrature (I/Q) raw data collected by the SAR system. The rows of raw correspond to the along-range samples. The columns of raw correspond to the pulses received as the platform moves along the cross-range direction. raw must have at least two rows.

Data Types: double

## waveform - Input waveform

phased. FMCWWaveform object
Input waveform, specified as a phased. FMCWWaveform object.
Example:
phased.FMCWWaveform(SweepBandwidth=100e3,0utputFormat="Sweeps", NumSweeps=2)
Data Types: double

## v - Platform velocity

positive scalar
Platform velocity, specified as a positive scalar. Units are in meters per second.

## Data Types: double

## fc - Operating frequency

positive scalar
Operating frequency, specified as a positive scalar. Units are in Hz.
Example: 2.8 e 9 Hz specifies a typical S-band operating-frequency value for airport and weather radar systems.
Data Types: double

## rc - Distance between radar and beam center <br> positive scalar

Distance between radar and beam center on the ground, specified as a positive scalar. Units are in meters.

Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Example: SquintAngle=45, PropagationSpeed=343

## SquintAngle - Squint angle

0 (default) | scalar in the range (-90, 90)
Squint angle of the antenna from the broadside direction in degrees, specified as a scalar in the range (-90, 90).
Data Types: double

## PropagationSpeed - Signal propagation speed

physconst("LightSpeed") (default) | positive scalar
Signal propagation speed in meters per second, specified as a positive scalar.
Example: 343 meters per second approximates the speed of sound at sea level and at a temperature of $20^{\circ} \mathrm{C}$ under normal atmospheric conditions.
Data Types: double

## Output Arguments

## slcimg - Single-look complex image

matrix
Single-look complex (SLC) image, returned as a matrix. slcimg is the same size as raw and contains the focused data processed by the range migration algorithm.

## Version History

Introduced in R2022a

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.

## See Also

phased.FMCWWaveform | rangeMigrationLFM | rangeMigrationSFM

## Topics

"Stripmap Synthetic Aperture Radar (SAR) Image Formation" (Radar Toolbox)
"Squinted Spotlight Synthetic Aperture Radar (SAR) Image Formation" (Radar Toolbox)
"Synthetic Aperture Radar System Simulation and Image Formation" (Radar Toolbox)

## rangeMigrationLFM

Range migration image formation algorithm for linear FM waveform

## Syntax

```
slcimg = rangeMigrationLFM(raw,waveform,fc,v,rc)
slcimg = rangeMigrationLFM(raw,waveform,fc,v,rc,Name=Value)
```


## Description

slcimg = rangeMigrationLFM(raw,waveform,fc,v,rc) returns a single-look complex image of raw synthetic aperture radar (SAR) data obtained with a linear frequency modulated (LFM) pulse waveform. The function uses the range migration algorithm.
slcimg = rangeMigrationLFM(raw,waveform, fc, v,rc,Name=Value) specifies additional inputs using name-value arguments. You can specify the squint angle of the antenna and the signal propagation speed.

## Examples

## Single-Look Complex Image from Unfocused LFM SAR Data

Load a file that contains simulated unfocused synthetic aperture radar (SAR) data obtained with a linear frequency modulated waveform. The waveform has a sample rate of 45 MHz , a pulse width of 3 microseconds, a pulse repetition frequency of 960 seconds, and a sweep bandwidth of $c / 10 \mathrm{~Hz}$, where $c$ is the numerical value of the speed of light.

```
data = load("RangeMigrationLFMExampleData");
raw = data.raw;
wvf = phased.LinearFMWaveform(SampleRate=45e6, ...
    PulseWidth=3e-6,PRF=960,SweepBandwidth=physconst("LightSpeed")/10);
```

The system works at an operating frequency of 4 GHz . The platform moves at a velocity of 100 meters per second and the distance between the beam center on the ground and the radar is 1118 meters.

```
fc = 4e9;
v = 100;
rc = 1118;
```

Generate a single-look complex image from the data. Plot the image.

```
slcimg = rangeMigrationLFM(raw,wvf,fc,v,rc);
imagesc(abs(slcimg))
xlabel("Cross-Range Samples")
ylabel("Range Samples")
```



## Input Arguments

## raw - Raw SAR data

matrix
Raw SAR data, specified as a matrix. The data is the unfocused in-phase and quadrature (I/Q) raw data collected by the SAR system. The rows of raw correspond to the along-range samples. The columns of raw correspond to the pulses received as the platform moves along the cross-range direction. raw must have at least two rows.

Data Types: double

## waveform - Input waveform

phased. LinearFMWaveform object
Input waveform, specified as a phased. LinearFMWaveform object.
Example:
phased.LinearFMWaveform(SampleRate=500e3,'SweepBandwidth' , 200e3, PulseWidth=1e -3, PRF=1e3)

Data Types: double

## fc - Operating frequency

positive scalar

Operating frequency, specified as a positive scalar. Units are in Hz .
Example: 2.8 e 9 Hz specifies a typical S-band operating-frequency value for airport and weather radar systems.
Data Types: double
v - Platform velocity
positive scalar
Platform velocity, specified as a positive scalar. Units are in meters per second.
Data Types: double
rc - Distance between radar and beam center
positive scalar
Distance between radar and beam center on the ground, specified as a positive scalar. Units are in meters.
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Example: SquintAngle=45, PropagationSpeed=343

## SquintAngle - Squint angle

0 (default) | scalar in the range (-90, 90)
Squint angle of the antenna from the broadside direction in degrees, specified as a scalar in the range (-90, 90).
Data Types: double
PropagationSpeed - Signal propagation speed
physconst("LightSpeed") (default)| positive scalar
Signal propagation speed in meters per second, specified as a positive scalar.
Example: 343 meters per second approximates the speed of sound at sea level and at a temperature of $20^{\circ} \mathrm{C}$ under normal atmospheric conditions.
Data Types: double

## Output Arguments

slcimg - Single-look complex image
matrix
Single-look complex (SLC) image, returned as a matrix. slcimg is the same size as raw and contains the focused data processed by the range migration algorithm.

## Version History

Introduced in R2022a

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{Tm}}$.

## See Also

phased.LinearFMWaveform | rangeMigrationFMCW | rangeMigrationSFM

Topics<br>"Stripmap Synthetic Aperture Radar (SAR) Image Formation" (Radar Toolbox)<br>"Squinted Spotlight Synthetic Aperture Radar (SAR) Image Formation" (Radar Toolbox)<br>"Synthetic Aperture Radar System Simulation and Image Formation" (Radar Toolbox)

## rangeMigrationSFM

Range migration image formation algorithm for stepped FM waveform

## Syntax

```
slcimg = rangeMigrationSFM(raw,waveform,fc,v,rc)
slcimg = rangeMigrationSFM(raw,waveform,fc,v,rc,Name=Value)
```


## Description

slcimg = rangeMigrationSFM(raw,waveform,fc,v,rc) returns a single-look complex image of raw synthetic aperture radar (SAR) data obtained with a stepped frequency modulated (SFM) pulse waveform. The function uses the range migration algorithm.
slcimg = rangeMigrationSFM(raw,waveform, fc, v,rc,Name=Value) specifies additional inputs using name-value arguments. You can specify the squint angle of the antenna and the signal propagation speed.

## Examples

## Single-Look Complex Image from Unfocused SFM SAR Data

Load a file that contains simulated unfocused synthetic aperture radar (SAR) data obtained with a stepped frequency modulated waveform. The waveform has a sample rate of 200 MHz , a pulse width of 250 nanoseconds, a pulse repetition frequency of $2 / 3 \mathrm{MHz}$, a frequency step size of 200 kHz , and 128 frequency steps.

```
data = load('RangeMigrationSFMExampleData.mat');
raw = data.raw;
wvf = phased.SteppedFMWaveform(SampleRate=200e6, ...
    PulseWidth=250e-9,PRF=2e6/3,FrequencyStep=200e3,NumSteps=128);
```

The system works at an operating frequency of 4 GHz . The platform moves at a velocity of 400 meters per second and the distance between the beam center on the ground and the radar is 60 meters.

```
fc = 4e9;
v = 400;
rc = 60;
```

Generate a single-look complex image from the data. Plot the image.

```
slcimg = rangeMigrationSFM(raw,wvf,fc,v,rc);
imagesc(abs(slcimg))
xlabel('Cross-Range Samples')
ylabel('Range Samples')
```



## Input Arguments

## raw - Raw SAR data

matrix
Raw SAR data, specified as a matrix. The data is the unfocused in-phase and quadrature (I/Q) raw data collected by the SAR system. The rows of raw correspond to the frequency steps. The columns of raw correspond to the bursts. raw must have at least two rows.
Data Types: double

## waveform - Input waveform

phased.SteppedFMWaveform object
Input waveform, specified as a phased.SteppedFMWaveform object.
Example: phased.SteppedFMWaveform(NumSteps=3,FrequencyStep=20e3)
Data Types: double

## v - Platform velocity

positive scalar
Platform velocity, specified as a positive scalar. Units are in meters per second.
Data Types: double

## fc - Operating frequency

positive scalar
Operating frequency, specified as a positive scalar. Units are in Hz.
Example: 2.8 e 9 Hz specifies a typical S-band operating-frequency value for airport and weather radar systems.
Data Types: double
rc - Distance between radar and beam center
positive scalar
Distance between radar and beam center on the ground, specified as a positive scalar. Units are in meters.
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

## Example: SquintAngle=45, PropagationSpeed=343

## SquintAngle - Squint angle

0 (default) | scalar in the range (-90, 90)
Squint angle of the antenna from the broadside direction in degrees, specified as a scalar in the range (-90, 90).

Data Types: double

## PropagationSpeed - Signal propagation speed

physconst("LightSpeed") (default) | positive scalar
Signal propagation speed in meters per second, specified as a positive scalar.
Example: 343 meters per second approximates the speed of sound at sea level and at a temperature of $20^{\circ} \mathrm{C}$ under normal atmospheric conditions.
Data Types: double

## Output Arguments

## slcimg - Single-look complex image

matrix
Single-look complex (SLC) image, returned as a matrix. slcimg is the same size as raw and contains the focused data processed by the range migration algorithm.

## Version History

## Introduced in R2022a

## References

[1] Cumming, Ian G., and Frank Hay-chee Wong. Digital Processing of Synthetic Aperture Radar Data: Algorithms and Implementation. Artech House Remote Sensing Library. Boston: Artech House, 2005.
[2] Tolman, Matthew A. "A Detailed Look at the Omega-k Algorithm for Processing Synthetic Aperture Radar Data.". MS thesis, Brigham Young University, 2008.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.

See Also<br>phased.SteppedFMWaveform | rangeMigrationFMCW | rangeMigrationLFM<br>\section*{Topics}<br>"Stripmap Synthetic Aperture Radar (SAR) Image Formation" (Radar Toolbox)<br>"Squinted Spotlight Synthetic Aperture Radar (SAR) Image Formation" (Radar Toolbox)<br>"Synthetic Aperture Radar System Simulation and Image Formation" (Radar Toolbox)

## rangeDopplerImagerLFM

Range migration image formation algorithm for linear FM waveform

## Syntax

```
slcimg = rangeDopplerImagerLFM(raw,waveform,fc,v,rc)
slcimg = rangeDopplerImagerLFM(raw,waveform,fc,v,rc,Name=Value)
```


## Description

slcimg = rangeDopplerImagerLFM(raw, waveform,fc,v,rc) returns a single-look complex image slcimg generated from raw synthetic aperture radar (SAR) data obtained using a linear frequency modulated (LFM) pulse phased. LinearFMWaveform waveform. fc specifies the operating frequency. $v$ specifies the platform speed. rc is the radar-to-beamcenter distance. The function uses the range migration algorithm.
slcimg = rangeDopplerImagerLFM(raw,waveform,fc,v,rc,Name=Value) specifies additional inputs using name-value arguments. Name-value pairs let you specify squint angle, sqa, and propagation speed, c.

## Examples

## Generate Image for Unfocused SAR

Generate a complex-valued single-look SAR image from simulated unfocused raw data. The radar transmits an LFM waveform. The LFM waveform has a 3 microsec duration with a PRF of 960 Hz . The radar has an operating frequency of 9 GHZ with a pulse sweep bandwidth of 29.979 MHz . The radar platform moves at $100 \mathrm{~m} / \mathrm{s}$. The radar-to-beamcenter distance is 1.118 km .

FIrst, load the raw image data from a mat-file. The raw data consists of a 481-by-577 complex-valued matrix. Then compute the focused SAR image.

```
load('RangeMigrationLFMExampleData.mat')
slcimg = rangeDopplerImagerLFM(raw,waveform,fc,v,rc);
imagesc(abs(slcimg))
title('SLC Image')
xlabel('Cross-Range Samples')
ylabel('Range Samples')
```



## Input Arguments

## raw - Unfocused IQ raw SAR data

$M$-by- $N$ complex-valued matrix
Unfocused IQ raw SAR data, specified as an $M$-by- $N$ complex-valued matrix. The data is the unfocused in-phase and quadrature (I/Q) raw data collected by the SAR system. Rows of raw correspond to along-range samples. The columns of raw correspond to the pulses received as the platform moves along the cross-range direction. raw must have at least two rows.

Data Types: double

## waveform - Input waveform

phased. LinearFMWaveform object
Input waveform, specified as a phased. LinearFMWaveform object.
Example:
phased.LinearFMWaveform(SampleRate=500e3,'SweepBandwidth',200e3,PulseWidth=1e -3, PRF=1e3)

Data Types: double

## fc - Operating frequency

positive scalar

Operating frequency, specified as a positive scalar. Units are in Hz .
Example: 2.8 e 9 Hz specifies a typical S-band operating-frequency value for airport and weather radar systems.
Data Types: double
v - Platform velocity
positive scalar
Platform velocity, specified as a positive scalar. Units are in meters per second.
Data Types: double
rc - Distance between radar and beam center
positive scalar
Distance between radar and beam center on the ground, specified as a positive scalar. Units are in meters.
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Example: SquintAngle=45, PropagationSpeed=343

## SquintAngle - Squint angle

0 (default) | scalar in the range (-90, 90)
Squint angle of the antenna from the broadside direction in degrees, specified as a scalar in the range (-90, 90).
Data Types: double
PropagationSpeed - Signal propagation speed
physconst("LightSpeed") (default)| positive scalar
Signal propagation speed in meters per second, specified as a positive scalar.
Example: 343 meters per second approximates the speed of sound at sea level and at a temperature of $20^{\circ} \mathrm{C}$ under normal atmospheric conditions.
Data Types: double

## Output Arguments

slcimg - Single-look complex image
matrix
Single-look complex (SLC) image, returned as a matrix. slcimg is the same size as raw and contains the focused data processed by the range migration algorithm.

## Version History

Introduced in R2022a

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.

## See Also

phased.LinearFMWaveform | rangeMigrationFMCW | rangeMigrationSFM

Topics<br>"Stripmap Synthetic Aperture Radar (SAR) Image Formation" (Radar Toolbox)<br>"Squinted Spotlight Synthetic Aperture Radar (SAR) Image Formation" (Radar Toolbox)<br>"Synthetic Aperture Radar System Simulation and Image Formation" (Radar Toolbox)

## rotpat

Rotate radiation pattern

## Syntax

```
rpat = rotpat(pat,az,el,rotax)
rpat = rotpat(pat,az,el,rotax,expval)
```


## Description

rpat $=$ rotpat (pat,az,el, rotax) rotates a radiation pattern, pat, into a new pattern, rpat, whose boresight is aligned with the $x$-axis of a new local coordinate system defined by rotax. az and el specify the azimuth and elevation angles at which the original pattern is sampled.
rpat $=$ rotpat (pat, az,el, rotax, expval) also specifies an extrapolated value to be used when az and el do not cover the entire 3-D space.

Tip You can use this function to rotate real and complex scalar radiation patterns as well as the orthogonal components of polarized fields. To rotate polarized fields, rotate the horizontal and vertical polarization components separately.

## Examples

## Rotate Pattern of Short-Dipole Antenna

Use a short-dipole antenna to create a polarized radiation pattern. Rotate the pattern and use the rotated pattern as the radiation pattern of a custom antenna.

Create a phased.ShortDipoleAntennaElement antenna object with default properties. The short-dipole antenna radiates polarized radiation. Obtain and display the radiation for all directions.

```
antennal = phased.ShortDipoleAntennaElement;
el = -90:90;
az = -180:180;
pat_h = zeros(numel(el),numel(az),'like',1+li);
pat_v = pat_h;
fc = 3e8;
for m = 1:numel(el)
    temp = antennal(fc,[az;el(m)*ones(1,numel(az))]);
    pat_h(m,:) = temp.H;
    pat_v(m,:) = temp.v;
end
pattern(antenna1,fc,'Type','Power')
```



Rotate the antenna pattern around the $y$-axis by 135 degrees followed by a rotation around the $x$-axis by 65 degrees.

```
newax = rotx(65)*roty(135);
pat2_h = rotpat(pat_h,az,el,newax);
pat2_v = rotpat(pat_v,az,el,newax);
```

Insert the rotated pattern into a phased.CustomAntennaElement object. Set the antenna polarization properties so that the element radiates horizontal and vertical polarized fields. Then display the rotated pattern in three dimensions.

```
antenna2 = phased.CustomAntennaElement( ...
    'SpecifyPolarizationPattern',true, ...
    'HorizontalMagnitudePattern',mag2db(abs(pat2 h)), ...
    'HorizontalPhasePattern',rad2deg(angle(pat2 h)), ...
    'VerticalMagnitudePattern',mag2db(abs(pat2_v)), ...
    'VerticalPhasePattern',rad2deg(angle(pat2_v)));
pattern(antenna2,fc,'Type','Power')
```



## Rotate Pattern of Cosine Antenna

Create a radiation pattern for a cosine antenna using a phased. CosineAntennaElement object. Rotate the pattern to use in a phased.CustomAntennaElement antenna object.

First obtain the radiation pattern for a phased.CosineAntennaElement object over a limited range of directions. The field is not polarized.

```
antennal = phased.CosineAntennaElement('CosinePower',[5,5]);
az = -60:65;
el = -60:60;
pat = zeros(numel(el),numel(az),'like',1);
fc = 300e6;
for m = 1:numel(el)
    temp = antennal(fc,[az;el(m)*ones(1,numel(az))]);
    pat(m,:) = temp;
end
```

Display the original pattern.

```
imagesc(az,el,abs(pat))
axis xy
axis equal
axis tight
xlabel('Azimuth (deg)')
```

```
ylabel('Elevation (deg)')
title('Original Radiation Pattern')
colorbar
```



Rotate the antenna pattern by 20 degrees around the $z$-axis and 50 degrees around the $x$-axis. Then display the rotated pattern.

```
newax = rotx(50)*rotz(20);
rpat = rotpat(pat,az,el,newax);
imagesc(az,el,abs(rpat))
axis xy
axis equal
axis tight
xlabel('Azimuth (deg)')
ylabel('Elevation (deg)')
title('Rotated Radiation Pattern')
colorbar
```



Use the rotated pattern in a custom antenna element and display the pattern in 3-D.
antenna2 $=$ phased.CustomAntennaElement (..
'AzimuthAngles', az, 'ElevationAngles',el, 'SpecifyPolarizationPattern',false, ...
'MagnitudePattern',mag2db(abs(rpat)), ...
'PhasePattern',zeros(size(rpat)));
pattern(antenna2,fc,'Type','Power')


## Input Arguments

## pat - Radiation pattern

complex-valued $N$-by- $M$ matrix | complex-valued $N$-by- $M$-by- $L$ array
Radiation pattern, specified as a complex-valued $N$-by- $M$ matrix or complex-valued $N$-by- $M$-by- $L$ array. $N$ is the length of the el vector and $M$ is the length of the az vector. Each column corresponds to one of the azimuth angles specified in the az argument. Each row corresponds to one of the elevation angles specified in the el argument. You can specify multiple radiation patterns using $L$ pages. For example, you can use pages to specify radiation patterns at different frequencies. The main lobe of each pattern is assumed to point along the $x$-axis. Units are in meters-squared.

Data Types: double

## az - Azimuth angles

- 180: 180 (default) | 1-by-M real-valued row vector

Azimuth angles for computing 3-D radiation pattern, specified as a 1-by-M real-valued row vector where $M$ is the number of azimuth angles. Each entry corresponds to one of the columns of the matrix specified in the pat argument. Angle units are in degrees. Azimuth angles must lie between $180^{\circ}$ and $180^{\circ}$, inclusive.

The azimuth angle is the angle between the $x$-axis and the projection of the direction vector onto the $x y$-plane. The azimuth angle is positive when measured from the $x$-axis toward the $y$-axis.

Example: -45:2:45
Data Types: double

## el - Elevation angles

-90:90 (default) | 1-by- $N$ real-valued row vector
Elevation angles for computing directivity and pattern, specified as a 1-by- $N$ real-valued row vector where $N$ is the number of elevation angles. Each entry corresponds to one of the rows of the matrix specified in the pat argument. Angle units are in degrees. Elevation angles must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive.

The elevation angle is the angle between the direction vector and $x y$-plane. The elevation angle is positive when measured toward the $z$-axis.

Example: -75:1:70
Data Types: double

## rotax - Rotation matrix

real-valued orthonormal 3-by-3 matrix | real-valued orthonormal 3-by-3-by-P array of orthonormal matrices

Rotation matrix, specified as a real-valued orthonormal 3-by-3 matrix or a real-valued 3-by-3-by- $P$ array. The columns represent the $x, y$, and $z$ directions of the rotated coordinate system with respect to the original coordinate system. The $P$ pages specify different rotation matrices.

This table describes how dimensions of the output pattern rpat depend on the dimensions of the pat and rotax arguments.

Dimensions of rpat

| Dimensions of pat | Dimensions of rotax |  |
| :--- | :--- | :--- |
| $M$-by- $N$ | 3 -by-3 | 3-by-3-by- $P$ |
| $M$-by- $N$-by- $L$ | $\begin{array}{l}\text { Rotate a single pattern by a } \\ \text { single rotation matrix. Output } \\ \text { dimensions of rpat are } M \text {-by- } N .\end{array}$ | $\begin{array}{l}\text { Rotate a single pattern by } P \\ \text { different rotation matrices. } \\ \text { Output dimensions of rpat are } \\ M-b y-~\end{array}$-by- $P$. |$]$| Rotate $L$ patterns by the same |
| :--- |
| rotation matrix. Output |
| dimensions of rpat are $M$-by- $N$ - |
| by- $L$. | | In this case, $P$ must equal $L$ and |
| :--- |
| the function rotates each |
| pattern by the corresponding |
| rotation matrix. Output |
| dimensions of rpat are $M$-by- $N-$ |
| by- $L$. |

## Example: $\operatorname{rotx}(45) * \operatorname{roty}(30)$

Data Types: double

## expval - Extrapolation value

0 (default) | scalar
Extrapolation value, specified as a scalar. This scalar is the extrapolated value when the rotated patterns do not fill the entire 3-D space specified by az and el. In general, consider setting expval to 0 if the pattern is specified in a linear scale or - inf if the pattern is specified in a dB scale.

Example: -inf
Data Types: double

## Output Arguments

## rpat - Rotated radiation pattern

complex-valued $N$-by- $M$ matrix | complex-valued $N$-by- $M$-by- $P$ array
Rotated radiation pattern, returned as a complex-valued $N$-by- $M$ matrix or complex-valued $N$-by- $M$-by$P$ array. $N$ is the length of the el vector. $M$ is the length of the az vector. The dimensionality of pat and rotax determine the value of $P$ as discussed in the rotax input argument. Units are in meterssquared.
Data Types: double

## Version History

Introduced in R2019a

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{Tm}}$.

## See Also

rotx|roty|rotz

## tl2range

Compute range from underwater transmission loss

## Syntax

$r n g=t l 2$ range(tl,freq, depth)

## Description

$r n g=t l 2$ range ( $t l, f r e q$, depth $)$ returns the range, $r n g$, to the source of a sound wave with frequency freq from the transmission loss, $t l$. The channel depth is depth and the sound frequency is freq. The transmission loss is due to geometrical spreading and frequency-dependent absorption. This function is the inverse of range $2 t l$ function.

## Examples

## Estimate Range from Transmission Loss

Find the distance traveled by a sound wave with a transmission loss of 50 dB . The sonar operates at 2 kHz in a channel 200 m deep.

```
tl = 50.0;
freq = 2000.0;
depth = 200.0;
rng = tl2range(tl,freq,depth)
rng = 972.1666
```


## Input Arguments

## tl - Transmission loss from source to receiver

positive scalar
Transmission loss from source to receiver, specified as a positive scalar. Units are in dB.
Data Types: double

## freq - Frequency of sound

positive scalar less than or equal to 2 MHz
Frequency of sound, specified as a positive scalar less than or equal to 2 MHz . Units are in Hz .
Example: 1e3
Data Types: double
depth - Depth of sound channel
positive scalar
Depth of sound channel, specified as a positive scalar. Units are in meters.

Example: 200
Data Types: double

## Output Arguments

rng - Distance from source to receiver
positive scalar
Distance from source to receiver, returned as a positive scalar. Units are in meters.
Data Types: double

## Limitations

- The transmission loss model assumes that seawater salinity is $35 \mathrm{ppt}, \mathrm{pH}$ is 8 , and temperature is $10^{\circ} \mathrm{C}$.
- The transmission loss model is valid for frequencies less than or equal to 2.0 MHz .


## Version History

Introduced in R2017b

## References

[1] Ainslie M. A. and J.G. McColm. "A simplified formula for viscous and chemical absorption in sea water." Journal of the Acoustical Society of America, Vol. 103, Number 3, 1998, pp. 1671-1672.
[2] Urick, Robert J, Principles of Underwater Sound, 3rd ed. Peninsula Publishing, Los Altos, CA, 1983.

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
Does not support variable-size inputs.

## See Also

sonareqtl| sonareqsnr|sonareqsl|range2tl
Topics
"Transmission Loss (TL)"
"Sonar Equation"

## External Websites

http://resource.npl.co.uk/acoustics/techguides/seaabsorption/\#content

## rangeangle

Range and angle calculation

## Syntax

[rng,ang] = rangeangle(pos)
[rng,ang] = rangeangle(pos,refpos)
[rng,ang] = rangeangle(pos,refpos,refaxes)
[rng,ang] = rangeangle( $\qquad$ ,model)

## Description

The function rangeangle determines the propagation path length and path direction of a signal from a source point or set of source points to a reference point. The function supports two propagation models - the free space model and the two-ray model. The free space model is a single line-of-sight path from a source point to a reference point. The two-ray multipath model generates two paths. The first path follows the free-space path. The second path is a reflected path off a boundary plane at $z=$ 0 . Path directions are defined with respect to either the global coordinate system at the reference point or a local coordinate system at the reference point. Distances and angles at the reference point do not depend upon which direction the signal is travelling along the path.
[rng,ang] = rangeangle(pos) returns the propagation path length, rng, and direction angles, ang, of a signal path from a source point or set of source points, pos, to the origin of the global coordinate system. The direction angles are the azimuth and elevation with respect to the global coordinate axes at the origin. Signals follow a line-of-sight path from the source point to the origin. The line-of-sight path corresponds to the geometric straight line between the points.
[rng,ang] = rangeangle(pos,refpos) also specifies a reference point or set of reference points, refpos. rng now contains the propagation path length from the source points to the reference points. The direction angles are the azimuth and elevation with respect to the global coordinate axes at the reference points. You can specify multiple points and multiple reference points.
[rng,ang] = rangeangle(pos,refpos,refaxes) also specifies local coordinate system axes, refaxes, at the reference points. Direction angles are the azimuth and elevation with respect to the local coordinate axes centered at refpos.
[rng, ang] = rangeangle(__ , model), also specifies a propagation model. When model is set to "freespace", the signal propagates along a line-of-sight path from source point to reception point. When model is set to "two-ray", the signal propagates along two paths from source point to reception point. The first path is the line-of-sight path. The second path is the reflecting path. In this case, the function returns the distances and angles for two paths for each source point and corresponding reference point.

## Examples

## Range and Angle Computation

Compute the range and angle of a target located at $(1000,2000,50)$ meters from the origin.

```
TargetLoc = [1000;2000;50];
[tgtrng,tgtang] = rangeangle(TargetLoc)
tgtrng = 2.2366e+03
tgtang = 2×1
    63.4349
        1.2810
```


## Range and Angle With Respect to Local Origin

Compute the range and angle of a target located at $(1000,2000,50)$ meters with respect to a local origin at $(100,100,10)$ meters.

```
TargetLoc = [1000;2000;50];
Origin = [100;100;10];
[tgtrng,tgtang] = rangeangle(TargetLoc,Origin)
tgtrng = 2.1028e+03
tgtang = 2×1
    64.6538
    1.0900
```


## Range and Angle With Respect to Local Coordinates

Compute the range and angle of a target located at $(1000,2000,50)$ meters but with respect to a local coordinate system origin at $(100,100,10)$ meters. Choose a local coordinate reference frame that is rotated about the z -axis by $45^{\circ}$ from the global coordinate axes.

```
targetpos = [1000;2000;50];
origin = [100;100;10];
refaxes = [1/sqrt(2) -1/sqrt(2) 0; 1/sqrt(2) 1/sqrt(2) 0; 0 0 1];
[tgtrng,tgtang] = rangeangle(targetpos,origin,refaxes)
tgtrng = 2.1028e+03
tgtang = 2×1
    19.6538
    1.0900
```


## Two-Ray Range and Angle

Compute the two-ray propagation distances and arrival angles of rays from a source located at (1000, $1000,500)$ meters from the origin. The receiver is located at $(100,100,200)$ meters from the origin.

```
sourceLoc = [1000;1000;500];
receiverLoc = [100;100;200];
[sourcerngs,sourceangs] = rangeangle(sourceLoc,receiverLoc,"two-ray")
sourcerngs = 1\times2
103 x
    1.3077 1.4526
sourceangs = 2\times2
    45.0000 45.0000
    13.2627 -28.8096
```



Find the range and angle of the same target with the same origin but with respect to a local coordinate axes. The local coordinate axes are rotated around the z -axis by 45 degrees from the global coordinate axes.

```
refaxes = rotz(45);
[sourcerngs,sourceangs] = rangeangle(sourceLoc,receiverLoc,refaxes,"two-ray")
```

```
sourcerngs = 1\times2
103 x
    1.3077 1.4526
sourceangs = 2×2
    13.2627 0
```


## Range and Angle With Respect to Two Origins

Compute the ranges and angles of two targets located at $(1000,200,500)$ and $(2500,80,-100)$ meters with respect to two local origins at $(100,300,-40)$ and $(500,-60,10)$ meters. Specify two different sets of local axes.

```
targetPos = [1000,2500;200,80;500,-100];
origins = [100,500;300,-60;-40,10];
ax(:,:,1) = rotx(40)*rotz(10);
ax(:,:,2) = roty(5)*rotx(10);
[tgtrng,tgtang] = rangeangle(targetPos,origins,ax)
tgtrng = 1\times2
10}\mp@subsup{0}{}{3}
    1.0543 2.0079
tgtang = 2\times2
    6.7285 4.2597
    26.9567 1.1254
```


## Input Arguments

## pos - Source point position

real-valued 3-by-1 vector | real-valued 3-by-N matrix
Source point position in meters, specified as a real-valued 3-by-1 vector or a real-valued 3-by-N matrix. A matrix represents multiple source points. The columns contain the Cartesian coordinates of $N$ points in the form [x;y;z].

When pos is a 3 -by- $N$ matrix, you must specify refpos as a 3 -by- $N$ matrix for $N$ reference positions. If all the reference points are identical, you can specify refpos by a single 3-by-1 vector.
Example: [1000;2000;50]
Data Types: double

## refpos - Reference point position

[0;0;0] (default) | real-valued 3-by-1 vector | real-valued 3-by-N matrix

Reference point position in meters, specified as a real-valued 3-by-1 vector or a real-valued 3-by- $N$ matrix. A matrix represents multiple reference points. The columns contain the Cartesian coordinates of $N$ points ins the form [x;y;z].

When refpos is a 3 -by- $N$ matrix, you must specify pos as a 3 -by- $N$ matrix for $N$ source positions. If all the source points are identical, you can specify pos by a single 3-by-1 vector.

Position units are meters.
Example: [100;100;10]
Data Types: double
refaxes - Local coordinate system axes
[1 $000 ; 0$ 1 0;0 0 1] (default) |real-valued 3-by-3 matrix | real-valued 3-by-3-by- $N$ array
Local coordinate system axes, specified as a real-valued 3-by-3 matrix or a 3-by-3-by- $N$ array. For an array, each page corresponds to a local coordinate axes at each reference point. The columns in refaxes specify the direction of the coordinate axes for the local coordinate system in Cartesian coordinates. $N$ must match the number of columns in pos or refpos when these dimensions are greater than one.

## Example: rotz (45)

Data Types: double

## model - Propagation model

"freespace" (default) | "two-ray"
Propagation model, specified as "freespace" or "two-ray". Choosing "freespace" invokes the free space propagation model. Choosing "two-ray" invokes the two-ray propagation model.
Data Types: char \| string

## Output Arguments

## rng - Propagation range

real-valued 1-by- $N$ vector | real-valued 1-by- $2 N$ vector
Propagation range in meters, returned as a real-valued $1-b y-N$ vector or real-valued $1-b y-2 N$ vector.

- When model is set to "freespace", the size of rng is 1-by- $N$. The propagation range is the length of the direct path from the position defined in pos to the corresponding reference position defined in refpos.
- When model is set to "two-ray", rng contains the ranges for the direct path and the reflected path. Alternate columns of rng refer to the line-of-sight path and reflected path, respectively for the same source-reference point pair.


## ang - Azimuth and elevation angles

real-valued 2 -by- $N$ matrix | real-valued 2 -by- $2 N$ matrix
Azimuth and elevation angles in degrees, returned as a 2 -by- $N$ matrix or 2 -by- $2 N$ matrix. Each column represents a direction angle in the form [azimuth; elevation].

- When model is set to "freespace", ang is a 2 -by- $N$ matrix and represents the angle of the path from a source point to a reference point.
- When model is set to "two-ray", ang is a 2-by-2N matrix. Alternate columns of ang refer to the line-of-sight path and reflected path, respectively.


## More About

## Angles in Local and Global Coordinate Systems

The rangeangle function returns the path distance and path angles in either the global or local coordinate systems. Every antenna or microphone element and array has a gain pattern that is expressed in local angular coordinates of azimuth and elevation. As the element or array moves or rotates, the gain pattern is carried with it. To determine the strength of a signal, you must know the angle that the signal path makes with respect to the local angular coordinates of the element or array. By default, the rangeangle function determines the angle a signal path makes with respect to global coordinates. If you add the refaxes argument, you can compute the angles with respect to local coordinates. As an illustration, this figure shows a 5-by-5 uniform rectangular array (URA) rotated from the global coordinates ( $x y z$ ) using refaxes. The $x^{\prime}$ axis of the local coordinate system ( $x^{\prime} y^{\prime} z^{\prime}$ ) is aligned with the main axis of the array and moves as the array moves. The path length is independent of orientation. The global coordinate system defines the azimuth and elevation angles ( $\Phi, \theta$ ) and the local coordinate system defines the azimuth and elevations angles ( $\Phi^{\prime}, \theta^{\prime}$ ).


## Local and Global Coordinate Axes

## Free Space Propagation Model

The free-space signal propagation model states that a signal propagating from one point to another in a homogeneous, isotropic medium travels in a straight line, called the line-of-sight or direct path. The straight line is defined by the geometric vector from the radiation source to the destination. Similar assumptions are made for sonar but the term isovelocity channel is used in place of free space.

## Two-Ray Propagation Model

A two-ray propagation channel is the next step up in complexity from a free-space channel and is the simplest case of a multipath propagation environment. The free-space channel models a straight-line line-of-sight path from point 1 to point 2 . In a two-ray channel, the medium is specified as a homogeneous, isotropic medium with a reflecting planar boundary. The boundary is always set at $z=$ 0 . There are at most two rays propagating from point 1 to point 2 . The first ray path propagates along the same line-of-sight path as in the free-space channel (see the phased. FreeSpace System object). The line-of-sight path is often called the direct path. The second ray reflects off the boundary before propagating to point 2. According to the Law of Reflection, the angle of reflection equals the angle of incidence. In short-range simulations such as cellular communications systems and automotive radars, you can assume that the reflecting surface, the ground or ocean surface, is flat.

The figure illustrates two propagation paths. From the source position, $s_{s}$, and the receiver position, $s_{r}$, you can compute the arrival angles of both paths, $\theta_{l o s}^{\prime}$ and $\theta_{r p}^{\prime}$. The arrival angles are the elevation and azimuth angles of the arriving radiation with respect to a local coordinate system. In this case, the local coordinate system coincides with the global coordinate system. You can also compute the transmitting angles, $\theta_{l o s}$ and $\theta_{r p}$. In the global coordinates, the angle of reflection at the boundary is the same as the angles $\theta_{r p}$ and $\theta_{r p}^{\prime}$. The reflection angle is important to know when you use angledependent reflection-loss data. You can determine the reflection angle by using the rangeangle function and setting the reference axes to the global coordinate system. The total path length for the line-of-sight path is shown in the figure by $R_{\text {los }}$ which is equal to the geometric distance between source and receiver. The total path length for the reflected path is $R_{r p}=R_{1}+R_{2}$. The quantity $L$ is the ground range between source and receiver.


You can easily derive exact formulas for path lengths and angles in terms of the ground range and object heights in the global coordinate system.

$$
\begin{aligned}
& \vec{R}=\vec{x}_{s}-\vec{x}_{r} \\
& R_{\text {los }}=|\vec{R}|=\sqrt{\left(z_{r}-z_{S}\right)^{2}+L^{2}} \\
& R_{1}=\frac{z_{r}}{z_{r}+z_{z}} \sqrt{\left(z_{r}+z_{s}\right)^{2}+L^{2}} \\
& R_{2}=\frac{z_{s}}{z_{S}+z_{r}} \sqrt{\left(z_{r}+z_{S}\right)^{2}+L^{2}} \\
& R_{r p}=R_{1}+R_{2}=\sqrt{\left(z_{r}+z_{S}\right)^{2}+L^{2}} \\
& \tan \theta_{l o s}=\frac{\left(z_{s}-z_{r}\right)}{L} \\
& \tan \theta_{r p}=-\frac{\left(z_{S}+z_{r}\right)}{L} \\
& \theta_{\text {los }}^{\prime}=-\theta_{\text {los }} \\
& \theta_{r p}^{\prime}=\theta_{r p}
\end{aligned}
$$

## Version History

Introduced in R2011a

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\text {TM }}$.
Usage notes and limitations:
Does not support variable-size inputs.

## See Also

global2localcoord|local2globalcoord|azel2uv|azel2phitheta

## Topics

"Global and Local Coordinate Systems"

## rdcoupling

Range Doppler coupling

## Syntax

```
dr = rdcoupling(fd,slope)
dr = rdcoupling(fd,slope,c)
```


## Description

$d r=r d c o u p l i n g(f d, s l o p e)$ returns the range offset on page 2-384 due to the Doppler shift in a linear frequency modulated signal. For example, the signal can be a linear FM pulse or an FMCW signal. slope is the slope of the linear frequency modulation.
$d r=r d c o u p l i n g(f d, s l o p e, c)$ specifies the signal propagation speed.

## Examples

## Target Range After Correcting for Doppler Shift

Calculate the true range of the target for an FMCW waveform that sweeps a band of 30 MHz in 2 ms . The dechirped target echo has a beat frequency of 1 kHz . The processing of the target return indicates a Doppler shift of 100 Hz .

```
slope = 30e6/2e-3;
fb = 1e3;
fd = 100;
r = beat2range(fb,slope) - rdcoupling(fd,slope)
r = 10.9924
```


## Input Arguments

## fd - Doppler shift

array of real numbers
Doppler shift, specified as an array of real numbers.
Data Types: double
slope - Slope of linear frequency modulation
nonzero scalar
Slope of linear frequency modulation, specified as a nonzero scalar in hertz per second.

## Data Types: double

## c - Signal propagation speed

speed of light (default) | positive scalar

Signal propagation speed, specified as a positive scalar in meters per second.
Data Types: double

## Output Arguments

dr - Range offset due to Doppler shift
real scalar
Range offset due to Doppler shift, returned as an array of real numbers. The dimensions of dr match the dimensions of fd .

## More About

## Range Offset

The range offset is the difference between the estimated range and the true range. The difference arises from coupling between the range and Doppler shift.

## Algorithms

The function computes $-c^{*} \mathrm{fd} /(2 *$ slope $)$.

## Version History

Introduced in R2012b

## References

[1] Barton, David K. Radar System Analysis and Modeling. Boston: Artech House, 2005.
[2] Richards, M. A. Fundamentals of Radar Signal Processing. New York: McGraw-Hill, 2005.

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:
Does not support variable-size inputs.

## See Also

beat2range | dechirp | range2beat | stretchfreq2rng|phased.FMCWWaveform |
phased.LinearFMWaveform

## Topics

"Automotive Adaptive Cruise Control Using FMCW Technology" (Radar Toolbox)

## rocpfa

Receiver operating characteristic curves by false-alarm probability

## Syntax

[Pd,SNR] = rocpfa(Pfa)
[Pd,SNR] = rocpfa(Pfa,Name=Value)
rocpfa(...)

## Description

[Pd,SNR] = rocpfa(Pfa) returns the single-pulse detection probabilities, Pd , and required SNR values, SNR, for the false-alarm probabilities in the row or column vector Pfa. By default, for each false-alarm probability, the detection probabilities are computed for 101 equally spaced SNR values between 0 and 20 dB . The ROC curve is constructed assuming a single pulse in coherent receiver with a nonfluctuating target.
[Pd,SNR] = rocpfa(Pfa,Name=Value) returns detection probabilities and SNR values with additional options specified by one or more name-value arguments.
rocpfa(... ) plots the ROC curves.

## Examples

Plot ROC Curves for Different PFAs
Plot ROC curves for false-alarm probabilities of $1 \mathrm{e}-8,1 \mathrm{e}-6$, and $1 \mathrm{e}-3$, assuming no pulse integration.

```
Pfa = [1e-8 le-6 le-3];
rocpfa(Pfa,SignalType="NonfluctuatingCoherent")
```



## Input Arguments

## Pfa - False-alarm probabilities

vector
False-alarm probabilities, specified as a row or column vector.
Example: [1e-8 1e-6 1e-3]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.
Example: $\mathrm{MaxSNR}=15$,NumPoints=64,NumPulses=10
Before R2021a, use commas to separate each name and value, and enclose Name in quotes.
Example: 'MaxSNR',15,'NumPoints', 64, 'NumPulses', 10

## MaxSNR - Maximum SNR to include in the ROC calculation

20 (default) | positive scalar
Maximum SNR to include in the ROC calculation, specified as a positive scalar.

Data Types: double

## MinSNR - Minimum SNR to include in the ROC calculation <br> 0 (default) | positive scalar

Minimum SNR to include in the ROC calculation, specified as a positive scalar.
Data Types: double

## NumPoints - Number of SNR values to use when calculating the ROC curves

101 (default) | positive integer
Number of SNR values to use when calculating the ROC curves, specified as a positive integer. The actual values are equally spaced between MinSNR and MaxSNR.

Data Types: double

## NumPulses - Number of pulses to integrate

1 (default) | positive integer
Number of pulses to integrate when calculating the ROC curves, specified as a positive integer. A value of 1 indicates no pulse integration.

## Data Types: double

## SignalType - Type of received signal

"NonfluctuatingCoherent" (default)| "NonfluctuatingNoncoherent" | "Real" | "Swerling1" | "Swerling2" | "Swerling3" | "Swerling4"

This property specifies the type of received signal or, equivalently, the probability density functions (PDF) used to compute the ROC. Valid values are: "Real", "NonfluctuatingCoherent", "NonfluctuatingNoncoherent", "Swerling1", "Swerling2", "Swerling3", and "Swerling4". Values are not case sensitive.

The "NonfluctuatingCoherent" signal type assumes that the noise in the received signal is a complex-valued, Gaussian random variable. This variable has independent zero-mean real and imaginary parts each with variance $\sigma^{2} / 2$ under the null hypothesis. In the case of a single pulse in a coherent receiver with complex white Gaussian noise, the probability of detection, $P_{\mathrm{D}}$, for a given false-alarm probability, $P_{\mathrm{FA}}$ is:

$$
P_{D}=\frac{1}{2} \operatorname{erfc}\left(\operatorname{erfc}^{-1}\left(2 P_{F A}\right)-\sqrt{\chi}\right)
$$

where erfc and erfc ${ }^{-1}$ are the complementary error function and that function's inverse, and $\chi$ is the SNR not expressed in decibels.

For details about the other supported signal types, see [1] on page 2-388.

## Data Types: char | string

## Output Arguments

## Pd - Detection probabilities

vector
Detection probabilities corresponding to the false-alarm probabilities, returned as a vector. For each false-alarm probability in Pfa, Pd contains one column of detection probabilities.

## SNR - Signal-to-noise ratios

column vector
Signal-to-noise ratios, returned as a column vector. By default, the SNR values are 101 equally spaced values between 0 and 20. To change the range of SNR values, use the optional MinSNR or MaxSNR input argument. To change the number of SNR values, use the optional NumPoints input argument.

## Version History

Introduced in R2011a

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:

- Does not support variable-size inputs.
- Supported only when output arguments are specified.


## References

[1] Richards, M. A. Fundamentals of Radar Signal Processing. New York: McGraw-Hill, 2005, pp 298336.

See Also<br>npwgnthresh | rocsnr | shnidman

## rocsnr

Receiver operating characteristic curves by SNR

## Syntax

[Pd,Pfa] = rocsnr(SNRdB)
[Pd,Pfa] = rocsnr(SNRdB,Name=Value)
rocsnr( $\qquad$ )

## Description

[Pd,Pfa] = rocsnr(SNRdB) returns the single-pulse detection probabilities, Pd, and false-alarm probabilities, Pfa, for the SNRs in the vector SNRdB. By default, for each SNR, the detection probabilities are computed for 101 false-alarm probabilities between 1e-10 and 1. The false-alarm probabilities are logarithmically equally spaced. The ROC curve is constructed assuming a coherent receiver with a nonfluctuating target.
[Pd,Pfa] = rocsnr(SNRdB,Name=Value) returns detection probabilities and false-alarm probabilities with additional options specified by one or more name-value arguments.
rocsnr( $\qquad$ ) plots the ROC curves.

## Examples

## ROC Curves for Different SNRs

Plot ROC curves for different SNRs for a single pulse.

```
SNRdB = [3 6 9 12];
[Pd,Pfa] = rocsnr(SNRdB,SignalType="NonfluctuatingCoherent");
semilogx(Pfa,Pd)
grid on
xlabel("P_{fa}")
ylabel("P_d")
legend("SNR "+SNRdB+" dB",Location="northwest")
title("Receiver Operating Characteristic (ROC) Curves")
```



## Input Arguments

## SNRdB - Signal-to-noise ratios

vector
Signal-to-noise ratios in decibels, specified as a row or column vector.
Example: [3 6 9 12]
Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.
Example: MinPfa=1e-8,NumPoints=64,NumPulses=10
Before R2021a, use commas to separate each name and value, and enclose Name in quotes.
Example: 'MinPfa',1e-8,'NumPoints', 64, 'NumPulses', 10

## MaxPfa - Maximum false-alarm probability to include in the ROC calculation

1 (default) | positive scalar
Maximum false-alarm probability to include in the ROC calculation, specified as a positive scalar.

## Data Types: double

## MinPfa - Minimum false-alarm probability to include in the ROC calculation <br> 1e-10 (default) | positive scalar

Minimum false-alarm probability to include in the ROC calculation, specified as a positive scalar.
Data Types: double

## NumPulses - Number of pulses to integrate

1 (default) | positive integer
Number of pulses to integrate when calculating the ROC curves, specified as a positive integer. A value of 1 indicates no pulse integration.

Data Types: double

## NumPoints - Number of SNR values to use when calculating the ROC curves <br> 101 (default) | positive integer

Number of SNR values to use when calculating the ROC curves, specified as a positive integer. The actual values are equally spaced between MinSNR and MaxSNR.
Data Types: double
SignalType - Type of received signal
"NonfluctuatingCoherent" (default)| "NonfluctuatingNoncoherent" | "Real" |
"Swerling1" | "Swerling2" | "Swerling3" | "Swerling4"
This property specifies the type of received signal or, equivalently, the probability density functions (PDF) used to compute the ROC. Valid values are: "Real", "NonfluctuatingCoherent", "NonfluctuatingNoncoherent", "Swerling1", "Swerling2", "Swerling3", and "Swerling4". Values are not case sensitive.

The "NonfluctuatingCoherent" signal type assumes that the noise in the received signal is a complex-valued, Gaussian random variable. This variable has independent zero-mean real and imaginary parts each with variance $\sigma^{2} / 2$ under the null hypothesis. In the case of a single pulse in a coherent receiver with complex white Gaussian noise, the probability of detection, $P_{\mathrm{D}}$, for a given false-alarm probability, $P_{\mathrm{FA}}$ is:

$$
P_{D}=\frac{1}{2} \operatorname{erfc}\left(\operatorname{erfc}^{-1}\left(2 P_{F A}\right)-\sqrt{\chi}\right)
$$

where erfc and erfc ${ }^{-1}$ are the complementary error function and that function's inverse, and $\chi$ is the SNR not expressed in decibels.

For details about the other supported signal types, see [1].
Data Types: char | string

## Output Arguments

## Pd - Detection probabilities

vector
Detection probabilities corresponding to the false-alarm probabilities, returned as a vector. For each SNR in SNRdB, Pd contains one column of detection probabilities.

## Pfa - False-alarm probabilities <br> column vector

False-alarm probabilities, returned as a column vector. By default, the false-alarm probabilities are 101 logarithmically equally spaced values between $1 \mathrm{e}-10$ and 1 . To change the range of probabilities, use the optional MinPfa or MaxPfa input argument. To change the number of probabilities, use the optional NumPoints input argument.

## Version History

Introduced in R2011a

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder ${ }^{\mathrm{TM}}$.
Usage notes and limitations:

- Does not support variable-size inputs.
- Supported only when output arguments are specified.


## References

[1] Richards, M. A. Fundamentals of Radar Signal Processing. New York: McGraw-Hill, 2005, pp 298336.

## See Also

npwgnthresh | rocpfa | shnidman

## rootmusicdoa

Direction of arrival using Root MUSIC

## Syntax

```
ang = rootmusicdoa(R,nsig)
ang = rootmusicdoa(
```

$\qquad$

``` ,'Name','Value')
```


## Description

ang $=$ rootmusicdoa( $R$, nsig) estimates the directions of arrival, ang, of a set of plane waves received on a uniform line array (ULA). The estimation uses the root MUSIC algorithm. The input arguments are the estimated spatial covariance matrix between sensor elements, R , and the number of arriving signals, nsig. In this syntax, sensor elements are spaced one-half wavelength apart.
ang = rootmusicdoa( $\qquad$ , 'Name', 'Value') allows you to specify additional input parameters in the form of Name-Value pairs. This syntax can use any of the input arguments in the previous syntax.

## Examples

## Three Signals Arriving at Half-Wavelength-Spaced ULA

Assume a half-wavelength spaced uniform line array with 10 elements. Three plane waves arrive from the $0^{\circ},-25^{\circ}$, and $30^{\circ}$ azimuth directions. Elevation angles are $0^{\circ}$. The noise is spatially and temporally white Gaussian noise.

Set the SNR for each signal to 5 dB . Find the arrival angles.

```
N = 10;
d = 0.5;
elementPos = (0:N-1)*d;
angles = [0 -25 30];
Nsig = 3;
R = sensorcov(elementPos,angles,db2pow(-5));
doa = rootmusicdoa(R,Nsig)
doa = 1\times3
    0.0000 30.0000 -25.0000
```

These angles agree with the known input angles.

## Three Signals Arriving at 0.4-Wavelength-Spaced ULA

Assume a uniform line array 10 elements, as in the previous example. But now the element spacing is smaller than one-half wavelength. Three plane waves arrive from the $0^{\circ},-25^{\circ}$, and $30^{\circ}$ azimuth
directions. Elevation angles are $0^{\circ}$. The noise is spatially and temporally white Gaussian noise. The SNR for each signal is 5 dB .

Set element spacing to 0.4 wavelengths using the ElementSpacing name-value pair. Then, find the arrival angles.

```
N = 10;
d = 0.4;
elementPos = (0:N-1)*d;
angles = [0 -25 30];
Nsig = 3;
R = sensorcov(elementPos,angles,db2pow(-5));
doa = rootmusicdoa(R,Nsig,'ElementSpacing',d)
doa = 1\times3
    -25.0000 30.0000 0.0000
```

The solution agrees with the known angles.

## Input Arguments

## R - Spatial covariance matrix

complex-valued positive-definite $N$-by- $N$ matrix
Spatial covariance matrix, specified as a complex-valued, positive-definite, $N$-by- $N$ matrix. In this matrix, $N$ represents the number of elements in the ULA array. If R is not Hermitian, a Hermitian matrix is formed by averaging the matrix and its conjugate transpose, ( $R+R^{\prime}$ )/2.
Example: [ 4.3162, -0.2777-0.2337i; $-0.2777+0.2337 i, 4.3162]$
Data Types: double
Complex Number Support: Yes

## nsig - Number of arriving signals

positive integer
Number of arriving signals, specified as a positive integer. The number of signals must be smaller than the number of elements in the ULA array.

## Example: 2

Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Namel=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.
Example: 'ElementSpacing', 0.4

## ElementSpacing - ULA element spacing

0.5 (default) | real-valued positive scalar

ULA element spacing, specified as a real-valued, positive scalar. Position units are measured in terms of signal wavelength.

Example: 0.4
Data Types: double

## Output Arguments

## ang - Directions of arrival angles

real-valued 1-by-M row vector
Directions of arrival angle, returned as a real-valued, 1-by- $M$ vector. The dimension $M$ is the number of arriving signals specified in the argument nsig. Angle units are degrees and angle values lie between $-90^{\circ}$ and $90^{\circ}$.

## Version History

Introduced in R2013a

## References

[1] Van Trees, H.L. Optimum Array Processing. New York: Wiley-Interscience, 2002.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:
Does not support variable-size inputs.

See Also<br>aictest|espritdoa|spsmooth|phased.RootMUSICEstimator

## rotx

Rotation matrix for rotations around x-axis

## Syntax

$R=\operatorname{rot} x(a n g)$

## Description

$R=\operatorname{rotx}(a n g)$ creates a 3-by-3 matrix for rotating a 3-by-1 vector or 3-by-N matrix of vectors around the $x$-axis by ang degrees. When acting on a matrix, each column of the matrix represents a different vector. For the rotation matrix R and vector v , the rotated vector is given by $\mathrm{R}^{*} \mathrm{v}$.

## Examples

## Rotation Matrix for $\mathbf{3 0 ^ { \circ }}$ Rotation

Construct the matrix for a rotation of a vector around the x -axis by $30^{\circ}$. Then let the matrix operate on a vector.

```
R = rotx(30)
R = 3\times3
    1.0000 rrer
            0 0.5000 0.8660
x = [2;-2;4];
y = R*x
y = 3x1
    2.0000
    -3.7321
    2.4641
```

Under a rotation around the $x$-axis, the $x$-component of a vector is invariant.

## Input Arguments

## ang - Rotation angle

real-valued scalar
Rotation angle specified as a real-valued scalar. The rotation angle is positive if the rotation is in the counter-clockwise direction when viewed by an observer looking along the $x$-axis towards the origin. Angle units are in degrees.

Example: 30.0
Data Types: double

## Output Arguments

## R - Rotation matrix

real-valued orthogonal matrix
3-by-3 rotation matrix returned as

$$
R_{\chi}(\alpha)=\left[\begin{array}{ccc}
1 & 0 & 0 \\
0 & \cos \alpha & -\sin \alpha \\
0 & \sin \alpha & \cos \alpha
\end{array}\right]
$$

for a rotation angle $\alpha$.

## More About

## Rotation Matrices

Rotation matrices are used to rotate a vector into a new direction.
In transforming vectors in three-dimensional space, rotation matrices are often encountered. Rotation matrices are used in two senses: they can be used to rotate a vector into a new position or they can be used to rotate a coordinate basis (or coordinate system) into a new one. In this case, the vector is left alone but its components in the new basis will be different from those in the original basis. In Euclidean space, there are three basic rotations: one each around the $x, y$ and $z$ axes. Each rotation is specified by an angle of rotation. The rotation angle is defined to be positive for a rotation that is counterclockwise when viewed by an observer looking along the rotation axis towards the origin. Any arbitrary rotation can be composed of a combination of these three (Euler's rotation theorem). For example, you can rotate a vector in any direction using a sequence of three rotations:
$\mathbf{v}^{\prime}=A \mathbf{v}=R_{z}(\gamma) R_{y}(\beta) R_{x}(\alpha) \mathbf{v}$.
The rotation matrices that rotate a vector around the $\mathrm{x}, \mathrm{y}$, and z -axes are given by:

- Counterclockwise rotation around x -axis

$$
R_{\chi}(\alpha)=\left[\begin{array}{ccc}
1 & 0 & 0 \\
0 & \cos \alpha & -\sin \alpha \\
0 & \sin \alpha & \cos \alpha
\end{array}\right]
$$

- Counterclockwise rotation around y-axis

$$
R_{y}(\beta)=\left[\begin{array}{ccc}
\cos \beta & 0 & \sin \beta \\
0 & 1 & 0 \\
-\sin \beta & 0 & \cos \beta
\end{array}\right]
$$

- Counterclockwise rotation around z-axis

$$
R_{z}(\gamma)=\left[\begin{array}{ccc}
\cos \gamma & -\sin \gamma & 0 \\
\sin \gamma & \cos \gamma & 0 \\
0 & 0 & 1
\end{array}\right]
$$

The following three figures show what positive rotations look like for each rotation axis:



For any rotation, there is an inverse rotation satisfying $A^{-1} A=1$. For example, the inverse of the xaxis rotation matrix is obtained by changing the sign of the angle:

$$
R_{\chi}^{-1}(\alpha)=R_{\chi}(-\alpha)=\left[\begin{array}{ccc}
1 & 0 & 0 \\
0 & \cos \alpha & \sin \alpha \\
0 & -\sin \alpha & \cos \alpha
\end{array}\right]=R_{\chi}^{\prime}(\alpha)
$$

This example illustrates a basic property: the inverse rotation matrix is the transpose of the original. Rotation matrices satisfy $A^{\prime} A=1$, and consequently $\operatorname{det}(A)=1$. Under rotations, vector lengths are preserved as well as the angles between vectors.

We can think of rotations in another way. Consider the original set of basis vectors, $\mathbf{i}, \mathbf{j}, \mathbf{k}$, and rotate them all using the rotation matrix $A$. This produces a new set of basis vectors $\mathbf{i}^{\prime}, \mathbf{j}, \mathbf{k}^{\prime}$ related to the original by:

$$
\begin{aligned}
\mathbf{i}^{\prime} & =A \mathbf{i} \\
\mathbf{j}^{\prime} & =A \mathbf{j} \\
\mathbf{k}^{\prime} & =A \mathbf{k}
\end{aligned}
$$

Using the transpose, you can write the new basis vectors as a linear combinations of the old basis vectors:

$$
\left[\begin{array}{l}
\mathbf{i}^{\prime} \\
\mathbf{j}^{\prime} \\
\mathbf{k}^{\prime}
\end{array}\right]=A^{\prime}\left[\begin{array}{l}
\mathbf{i} \\
\mathbf{j} \\
\mathbf{k}
\end{array}\right]
$$

Now any vector can be written as a linear combination of either set of basis vectors:

$$
\mathbf{v}=v_{x} \mathbf{i}+v_{y} \mathbf{j}+v_{z} \mathbf{k}=v_{\chi}^{\prime} \mathbf{i}^{\prime}+v_{y}^{\prime} \mathbf{j}^{\prime}+v_{z}^{\prime} \mathbf{k}^{\prime}
$$

Using algebraic manipulation, you can derive the transformation of components for a fixed vector when the basis (or coordinate system) rotates. This transformation uses the transpose of the rotation matrix.

$$
\left[\begin{array}{l}
v_{x}^{\prime} \\
v^{\prime} y \\
v_{z}^{\prime}
\end{array}\right]=A^{-1}\left[\begin{array}{l}
v_{x} \\
v_{y} \\
v_{z}
\end{array}\right]=A^{\prime}\left[\begin{array}{c}
v_{x} \\
v_{y} \\
v_{z}
\end{array}\right]
$$

The next figure illustrates how a vector is transformed as the coordinate system rotates around the x axis. The figure after shows how this transformation can be interpreted as a rotation of the vector in the opposite direction.



## Version History <br> Introduced in R2013a

## References

[1] Goldstein, H., C. Poole and J. Safko, Classical Mechanics, 3rd Edition, San Francisco: Addison Wesley, 2002, pp. 142-144.

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{Tm}}$.
Usage notes and limitations:
Does not support variable-size inputs.

## See Also

roty | rotz

## roty

Rotation matrix for rotations around $y$-axis

## Syntax

$R=\operatorname{roty}(a n g)$

## Description

$\mathrm{R}=\operatorname{roty}(\mathrm{ang})$ creates a 3 -by- 3 matrix used to rotate a 3 -by-1 vector or 3 -by- $N$ matrix of vectors around the $y$-axis by ang degrees. When acting on a matrix, each column of the matrix represents a different vector. For the rotation matrix $R$ and vector $v$, the rotated vector is given by $R^{*} v$.

## Examples

## Rotation Matrix for $45^{\circ}$ Rotation

Construct the matrix for a rotation of a vector around the $y$-axis by $45^{\circ}$. Then let the matrix operate on a vector.

```
R = roty(45)
R = 3\times3
\begin{tabular}{rrr}
0.7071 & 0 & 0.7071 \\
-0.7071 & 1.0000 & 0 \\
& 0 & 0.7071
\end{tabular}
v = [1;-2;4];
y = R*v
y = 3x1
    3.5355
    -2.0000
    2.1213
```

Under a rotation around the $y$-axis, the $y$-component of a vector is invariant.

## Input Arguments

## ang - Rotation angle

real-valued scalar
Rotation angle specified as a real-valued scalar. The rotation angle is positive if the rotation is in the counter-clockwise direction when viewed by an observer looking along the $y$-axis towards the origin. Angle units are in degrees.

Example: 30.0
Data Types: double

## Output Arguments

## R - Rotation matrix

real-valued orthogonal matrix
3-by-3 rotation matrix returned as

$$
R_{y}(\beta)=\left[\begin{array}{ccc}
\cos \beta & 0 & \sin \beta \\
0 & 1 & 0 \\
-\sin \beta & 0 & \cos \beta
\end{array}\right]
$$

for a rotation angle $\beta$.

## More About

## Rotation Matrices

Rotation matrices are used to rotate a vector into a new direction.
In transforming vectors in three-dimensional space, rotation matrices are often encountered. Rotation matrices are used in two senses: they can be used to rotate a vector into a new position or they can be used to rotate a coordinate basis (or coordinate system) into a new one. In this case, the vector is left alone but its components in the new basis will be different from those in the original basis. In Euclidean space, there are three basic rotations: one each around the $\mathrm{x}, \mathrm{y}$ and z axes. Each rotation is specified by an angle of rotation. The rotation angle is defined to be positive for a rotation that is counterclockwise when viewed by an observer looking along the rotation axis towards the origin. Any arbitrary rotation can be composed of a combination of these three (Euler's rotation theorem). For example, you can rotate a vector in any direction using a sequence of three rotations:
$\mathbf{v}^{\prime}=A \mathbf{v}=R_{z}(\gamma) R_{y}(\beta) R_{x}(\alpha) \mathbf{v}$.
The rotation matrices that rotate a vector around the $\mathrm{x}, \mathrm{y}$, and z -axes are given by:

- Counterclockwise rotation around x -axis

$$
R_{\chi}(\alpha)=\left[\begin{array}{ccc}
1 & 0 & 0 \\
0 & \cos \alpha & -\sin \alpha \\
0 & \sin \alpha & \cos \alpha
\end{array}\right]
$$

- Counterclockwise rotation around y-axis

$$
R_{y}(\beta)=\left[\begin{array}{ccc}
\cos \beta & 0 & \sin \beta \\
0 & 1 & 0 \\
-\sin \beta & 0 & \cos \beta
\end{array}\right]
$$

- Counterclockwise rotation around z -axis

$$
R_{z}(\gamma)=\left[\begin{array}{ccc}
\cos \gamma & -\sin \gamma & 0 \\
\sin \gamma & \cos \gamma & 0 \\
0 & 0 & 1
\end{array}\right]
$$

The following three figures show what positive rotations look like for each rotation axis:



For any rotation, there is an inverse rotation satisfying $A^{-1} A=1$. For example, the inverse of the xaxis rotation matrix is obtained by changing the sign of the angle:

$$
R_{\chi}^{-1}(\alpha)=R_{\chi}(-\alpha)=\left[\begin{array}{ccc}
1 & 0 & 0 \\
0 & \cos \alpha & \sin \alpha \\
0 & -\sin \alpha & \cos \alpha
\end{array}\right]=R_{\chi}^{\prime}(\alpha)
$$

This example illustrates a basic property: the inverse rotation matrix is the transpose of the original. Rotation matrices satisfy $A^{\prime} A=1$, and consequently $\operatorname{det}(A)=1$. Under rotations, vector lengths are preserved as well as the angles between vectors.

We can think of rotations in another way. Consider the original set of basis vectors, $\mathbf{i}, \mathbf{j}, \mathbf{k}$, and rotate them all using the rotation matrix $A$. This produces a new set of basis vectors $\mathbf{i}^{\prime}, \mathbf{j}, \mathbf{k}^{\prime}$ related to the original by:

$$
\begin{aligned}
\mathbf{i}^{\prime} & =A \mathbf{i} \\
\mathbf{j}^{\prime} & =A \mathbf{j} \\
\mathbf{k}^{\prime} & =A \mathbf{k}
\end{aligned}
$$

Using the transpose, you can write the new basis vectors as a linear combinations of the old basis vectors:

$$
\left[\begin{array}{l}
\mathbf{i}^{\prime} \\
\mathbf{j}^{\prime} \\
\mathbf{k}^{\prime}
\end{array}\right]=A^{\prime}\left[\begin{array}{l}
\mathbf{i} \\
\mathbf{j} \\
\mathbf{k}
\end{array}\right]
$$

Now any vector can be written as a linear combination of either set of basis vectors:

$$
\mathbf{v}=v_{x} \mathbf{i}+v_{y} \mathbf{j}+v_{z} \mathbf{k}=v_{x}^{\prime} \mathbf{i}^{\prime}+v_{y}^{\prime} \mathbf{j}^{\prime}+v_{z}^{\prime} \mathbf{k}^{\prime}
$$

Using algebraic manipulation, you can derive the transformation of components for a fixed vector when the basis (or coordinate system) rotates. This transformation uses the transpose of the rotation matrix.

$$
\left[\begin{array}{l}
v_{x}^{\prime} \\
v^{\prime} y \\
v_{z}^{\prime}
\end{array}\right]=A^{-1}\left[\begin{array}{l}
v_{x} \\
v_{y} \\
v_{z}
\end{array}\right]=A^{\prime}\left[\begin{array}{c}
v_{x} \\
v_{y} \\
v_{z}
\end{array}\right]
$$

The next figure illustrates how a vector is transformed as the coordinate system rotates around the x axis. The figure after shows how this transformation can be interpreted as a rotation of the vector in the opposite direction.



## Version History <br> Introduced in R2013a

## References

[1] Goldstein, H., C. Poole and J. Safko, Classical Mechanics, 3rd Edition, San Francisco: Addison Wesley, 2002, pp. 142-144.

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
Does not support variable-size inputs.

## See Also

rotx|rotz

## rotz

Rotation matrix for rotations around z -axis

## Syntax

$R=\operatorname{rotz}(a n g)$

## Description

$R=\operatorname{rotz}($ ang $)$ creates a 3-by-3 matrix used to rotate a 3 -by-1 vector or 3-by-N matrix of vectors around the z -axis by ang degrees. When acting on a matrix, each column of the matrix represents a different vector. For the rotation matrix R and vector v , the rotated vector is given by $\mathrm{R}^{*} \mathrm{v}$.

## Examples

## Rotation Matrix for $45^{\circ}$ Rotation

Construct the matrix for the rotation of a vector around the z -axis by $45^{\circ}$. Then let the matrix operate on a vector.

```
R = rotz(45)
R = 3\times3
    0.7071 -0.7071 0
    0.7071 0.7071 0
        0 0 1.0000
v = [1;-2;4];
y = R*v
y = 3x1
    2.1213
    -0.7071
    4.0000
```

Under a rotation around the z -axis, the $z$-component of a vector is invariant.

## Input Arguments

## ang - Rotation angle

real-valued scalar
Rotation angle specified as a real-valued scalar. The rotation angle is positive if the rotation is in the counter-clockwise direction when viewed by an observer looking along the z -axis towards the origin. Angle units are in degrees.

Example: 45.0
Data Types: double

## Output Arguments

## R - Rotation matrix

real-valued orthogonal matrix
3-by-3 rotation matrix returned as

$$
R_{z}(\gamma)=\left[\begin{array}{ccc}
\cos \gamma & -\sin \gamma & 0 \\
\sin \gamma & \cos \gamma & 0 \\
0 & 0 & 1
\end{array}\right]
$$

for a rotation angle $\gamma$.

## More About

## Rotation Matrices

Rotation matrices are used to rotate a vector into a new direction.
In transforming vectors in three-dimensional space, rotation matrices are often encountered. Rotation matrices are used in two senses: they can be used to rotate a vector into a new position or they can be used to rotate a coordinate basis (or coordinate system) into a new one. In this case, the vector is left alone but its components in the new basis will be different from those in the original basis. In Euclidean space, there are three basic rotations: one each around the $\mathrm{x}, \mathrm{y}$ and z axes. Each rotation is specified by an angle of rotation. The rotation angle is defined to be positive for a rotation that is counterclockwise when viewed by an observer looking along the rotation axis towards the origin. Any arbitrary rotation can be composed of a combination of these three (Euler's rotation theorem). For example, you can rotate a vector in any direction using a sequence of three rotations:
$\mathbf{v}^{\prime}=A \mathbf{v}=R_{z}(\gamma) R_{y}(\beta) R_{x}(\alpha) \mathbf{v}$.
The rotation matrices that rotate a vector around the $\mathrm{x}, \mathrm{y}$, and z -axes are given by:

- Counterclockwise rotation around x -axis

$$
R_{\chi}(\alpha)=\left[\begin{array}{ccc}
1 & 0 & 0 \\
0 & \cos \alpha & -\sin \alpha \\
0 & \sin \alpha & \cos \alpha
\end{array}\right]
$$

- Counterclockwise rotation around y-axis

$$
R_{y}(\beta)=\left[\begin{array}{ccc}
\cos \beta & 0 & \sin \beta \\
0 & 1 & 0 \\
-\sin \beta & 0 & \cos \beta
\end{array}\right]
$$

- Counterclockwise rotation around z-axis

$$
R_{z}(\gamma)=\left[\begin{array}{ccc}
\cos \gamma & -\sin \gamma & 0 \\
\sin \gamma & \cos \gamma & 0 \\
0 & 0 & 1
\end{array}\right]
$$

The following three figures show what positive rotations look like for each rotation axis:



For any rotation, there is an inverse rotation satisfying $A^{-1} A=1$. For example, the inverse of the $x$ axis rotation matrix is obtained by changing the sign of the angle:

$$
R_{\chi}^{-1}(\alpha)=R_{\chi}(-\alpha)=\left[\begin{array}{ccc}
1 & 0 & 0 \\
0 & \cos \alpha & \sin \alpha \\
0 & -\sin \alpha & \cos \alpha
\end{array}\right]=R_{\chi}^{\prime}(\alpha)
$$

This example illustrates a basic property: the inverse rotation matrix is the transpose of the original. Rotation matrices satisfy $A^{\prime} A=1$, and consequently $\operatorname{det}(A)=1$. Under rotations, vector lengths are preserved as well as the angles between vectors.

We can think of rotations in another way. Consider the original set of basis vectors, $\mathbf{i}, \mathbf{j}, \mathbf{k}$, and rotate them all using the rotation matrix $A$. This produces a new set of basis vectors $\mathbf{i}^{\prime}, \mathbf{j},{ }^{\prime} \mathbf{k}^{\prime}$ related to the original by:

$$
\begin{aligned}
\mathbf{i}^{\prime} & =A \mathbf{i} \\
\mathbf{j}^{\prime} & =A \mathbf{j} \\
\mathbf{k}^{\prime} & =A \mathbf{k}
\end{aligned}
$$

Using the transpose, you can write the new basis vectors as a linear combinations of the old basis vectors:

$$
\left[\begin{array}{l}
\mathbf{i}^{\prime} \\
\mathbf{j}^{\prime} \\
\mathbf{k}^{\prime}
\end{array}\right]=A^{\prime}\left[\begin{array}{l}
\mathbf{i} \\
\mathbf{j} \\
\mathbf{k}
\end{array}\right]
$$

Now any vector can be written as a linear combination of either set of basis vectors:

$$
\mathbf{v}=v_{x} \mathbf{i}+v_{y} \mathbf{j}+v_{z} \mathbf{k}=v_{\chi}^{\prime} \mathbf{i}^{\prime}+v_{y}^{\prime} \mathbf{j}^{\prime}+v_{z}^{\prime} \mathbf{k}^{\prime}
$$

Using algebraic manipulation, you can derive the transformation of components for a fixed vector when the basis (or coordinate system) rotates. This transformation uses the transpose of the rotation matrix.

$$
\left[\begin{array}{l}
v_{x}^{\prime} \\
v^{\prime} y \\
v_{z}^{\prime}
\end{array}\right]=A^{-1}\left[\begin{array}{l}
v_{x} \\
v_{y} \\
v_{z}
\end{array}\right]=A^{\prime}\left[\begin{array}{c}
v_{x} \\
v_{y} \\
v_{z}
\end{array}\right]
$$

The next figure illustrates how a vector is transformed as the coordinate system rotates around the x axis. The figure after shows how this transformation can be interpreted as a rotation of the vector in the opposite direction.



## Version History <br> Introduced in R2013a

## References

[1] Goldstein, H., C. Poole and J. Safko, Classical Mechanics, 3rd Edition, San Francisco: Addison Wesley, 2002, pp. 142-144.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
Does not support variable-size inputs.

## See Also

rotx| roty

## sensorcov

Sensor spatial covariance matrix

## Syntax

```
xcov = sensorcov(pos,ang)
xcov = sensorcov(pos,ang,ncov)
xcov = sensorcov(pos,ang,ncov,scov)
```


## Description

$x \operatorname{cov}=\operatorname{sensorcov}(p o s, a n g)$ returns the sensor spatial covariance matrix, xcov, for narrowband plane wave signals arriving at a sensor array. The sensor array is defined by the sensor positions specified in the pos argument. The signal arrival directions are specified by azimuth and elevation angles in the ang argument. In this syntax, the noise power is assumed to be zero at all sensors, and the signal power is assumed to be unity for all signals.
xcov = sensorcov(pos,ang,ncov) specifies, in addition, the spatial noise covariance matrix, ncov. This value represents the noise power on each sensor as well as the correlation of the noise between sensors. In this syntax, the signal power is assumed to be unity for all signals. This syntax can use any of the input arguments in the previous syntax.
xcov $=$ sensorcov(pos,ang, ncov, scov) specifies, in addition, the signal covariance matrix, scov, which represents the power in each signal and the correlation between signals. This syntax can use any of the input arguments in the previous syntaxes.

## Examples

## Covariance Matrix for Two Signals Without Noise

Create a covariance matrix for a 3 -element, half-wavelength-spaced uniform line array. Use the default syntax, which assumes no noise power and unit signal power.

```
N = 3;
d = 0.5;
elementPos = (0:N-1)*d;
xcov = sensorcov(elementPos,[30 60])
xcov = 3\times3 complex
    2.0000 + 0.0000i -0.9127 - 1.4086i -0.3339 + 0.7458i
    -0.9127 + 1.4086i 2.0000 + 0.0000i -0.9127 - 1.4086i
    -0.3339 - 0.7458i -0.9127 + 1.4086i 2.0000 + 0.0000i
```

The diagonal terms of the matrix represent the sum of the two signal powers.

## Covariance Matrix for Two Independent Signals with 10 dB SNR

Create a spatial covariance matrix for a 3 -element, half-wavelength-spaced uniform line array. Assume there are two incoming signals with unit power and there is additive noise with -10 dB power.

```
N = 3;
d = 0.5;
elementPos = (0:N-1)*d;
xcov = sensorcov(elementPos,[30 35],db2pow(-10))
xcov = 3\times3 complex
    2.1000 + 0.0000i -0.2291 - 1.9734i -1.8950 + 0.4460i
    -0.2291 + 1.9734i 2.1000 + 0.0000i -0.2291 - 1.9734i
    -1.8950 - 0.4460i -0.2291 + 1.9734i 2.1000 + 0.0000i
```

The diagonal terms represent the two signal powers plus noise power at each sensor.

## Covariance Matrix for Two Correlated Signals with 10 dB SNR

Compute the covariance matrix for a 3 -element half-wavelength spaced line array when there is some correlation between two signals. The correlation can model, for example, multipath propagation caused by reflection from a surface. Assume an additive noise power value of -10 dB .

```
N = 3;
d = 0.5;
elementPos = (0:N-1)*d;
scov = [1, 0.8; 0.8, 1];
xcov = sensorcov(elementPos,[30 35],db2pow(-10),scov)
xcov = 3x3 complex
    3.7000 + 0.0000i -0.4124 - 3.5521i -3.4111 + 0.8028i
    -0.4124 + 3.5521i 3.6574 + 0.0000i -0.4026 - 3.4682i
    -3.4111 - 0.8028i -0.4026 + 3.4682i 3.5321 + 0.0000i
```


## Input Arguments

## pos - Positions of array sensor elements

1 -by- $N$ real-valued vector | 2 -by- $N$ real-valued matrix | 3 -by- $N$ real-valued matrix
Positions of the elements of a sensor array, specified as a 1-by- $N$ vector, a 2 -by- $N$ matrix, or a 3 -by- $N$ matrix. In this vector or matrix, $N$ represents the number of elements of the array. Each column of pos represents the coordinates of an element. If pos is a 1 -by- $N$ vector, then it represents the $y$ coordinate of the sensor elements of a line array. The $x$ and $z$-coordinates are assumed to be zero. When pos is a 2 -by- $N$ matrix, it represents the ( $y, z$ )-coordinates of the sensor elements of a planar array. This array is assumed to lie in the $y z$-plane. The $x$-coordinates are assumed to be zero. When pos is a 3 -by- $N$ matrix, then the array can have an arbitrary shape. Sensor positions are in terms of signal wavelength.

Example: [0,0,0; 0.1,0.4,0.3; 1,1,1]
Data Types: double

## ang - Arrival directions of incoming signals

1-by- $M$ real-valued vector | 2 -by- $M$ real-valued matrix
Arrival directions of incoming signals specified as a 1 -by- $M$ vector or a 2 -by- $M$ matrix, where $M$ is the number of incoming signals. If ang is a 2-by- $M$ matrix, each column specifies the direction in azimuth and elevation of the incoming signal [az;el]. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$ and the elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$. The azimuth angle is the angle between the $x$ axis and the projection of the arrival direction vector onto the $x y$ plane. It is positive when measured from the $x$-axis toward the $y$-axis. The elevation angle is the angle between the arrival direction vector and $x y$-plane. It is positive when measured towards the $z$ axis. If ang is a $1-b y-M$ vector, then it represents a set of azimuth angles with the elevation angles assumed to be zero. Angle units are specified in degrees.
Example: [45;0]
Data Types: double

## ncov - Noise spatial covariance matrix

0 (default) | non-negative real-valued scalar | 1 -by- $N$ non-negative real-valued vector $\mid N$-by- $N$ positive definite, complex-valued matrix

Noise spatial covariance matrix specified as a non-negative, real-valued scalar, a non-negative, 1-by- $N$ real-valued vector or an $N$-by- $N$, positive definite, complex-valued matrix. In this argument, $N$ is the number of sensor elements. Using a non-negative scalar results in a noise spatial covariance matrix that has identical white noise power values (in watts) along its diagonal and has off-diagonal values of zero. Using a non-negative real-valued vector results in a noise spatial covariance that has diagonal values corresponding to the entries in ncov and has off-diagonal entries of zero. The diagonal entries represent the independent white noise power values (in watts) in each sensor. If ncov is $N$-by- $N$ matrix, this value represents the full noise spatial covariance matrix between all sensor elements.
Example: [1,1,4,6]
Data Types: double
Complex Number Support: Yes

## scov - Signal covariance matrix

1 (default) | non-negative real-valued scalar | 1-by-M non-negative real-valued vector | $N$-by- $M$ positive semidefinite, complex-valued matrix

Signal covariance matrix specified as a non-negative, real-valued scalar, a 1 -by- $M$ non-negative, realvalued vector or an $M$-by- $M$ positive semidefinite, matrix representing the covariance matrix between $M$ signals. The number of signals is specified in ang. If scov is a nonnegative scalar, it assigns the same power (in watts) to all incoming signals which are assumed to be uncorrelated. If scov is a 1-by- $M$ vector, it assigns the separate power values (in watts) to each incoming signal which are also assumed to be uncorrelated. If scov is an $M$-by- $M$ matrix, then it represents the full covariance matrix between all incoming signals.

Example: [1 0 ; 0 2]
Data Types: double
Complex Number Support: Yes

## Output Arguments

## xcov - Sensor spatial covariance matrix

complex-valued $N$-by- $N$ matrix
Sensor spatial covariance matrix returned as a complex-valued, $N$-by- $N$ matrix. In this matrix, $N$ represents the number of sensor elements of the array.

## Version History

Introduced in R2013a

## References

[1] Van Trees, H.L. Optimum Array Processing. New York, NY: Wiley-Interscience, 2002.
[2] Johnson, Don H. and D. Dudgeon. Array Signal Processing. Englewood Cliffs, NJ: Prentice Hall, 1993.
[3] Van Veen, B.D. and K. M. Buckley. "Beamforming: A versatile approach to spatial filtering". IEEE ASSP Magazine, Vol. 5 No. 2 pp. 4-24.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:
Does not support variable-size inputs.

## See Also

cbfweights|lcmvweights|mvdrweights|steervec| sensorsig|phased.SteeringVector

## sensorsig

Simulate received signal at sensor array

## Syntax

```
x = sensorsig(pos,ns,ang)
x = sensorsig(pos,ns,ang,ncov)
x = sensorsig(pos,ns,ang,ncov,scov)
x = sensorsig(pos,ns,ang,ncov,scov,'Taper',taper)
[x,rt] = sensorsig(
```

$\qquad$

```
[x,rt,r] = sensorsig(
```

$\qquad$

## Description

$\mathrm{x}=$ sensorsig(pos,ns,ang) simulates the received narrowband plane wave signals at a sensor array. pos represents the positions of the array elements, each of which is assumed to be isotropic. ns indicates the number of snapshots of the simulated signal. ang represents the incoming directions of each plane wave signal. The plane wave signals are assumed to be constant-modulus signals with random phases.
$x=$ sensorsig(pos,ns,ang, ncov) describes the noise across all sensor elements. ncov specifies the noise power or covariance matrix. The noise is a Gaussian distributed signal.
$x=$ sensorsig(pos,ns,ang, ncov, scov) specifies the power or covariance matrix for the incoming signals.
x = sensorsig(pos,ns,ang,ncov,scov,'Taper',taper) specifies the array taper as a comma-separated pair consisting of 'Taper' and a scalar or column vector.
[ $\mathrm{x}, \mathrm{rt}$ ] = sensorsig( $\qquad$ ) also returns the theoretical covariance matrix of the received signal, using any of the input arguments in the previous syntaxes.
[x,rt,r] = sensorsig( ___ ) also returns the sample covariance matrix of the received signal.

## Examples

## Received Signal and Direction-of-Arrival Estimation

Simulate the received signal at an array, and use the data to estimate the arrival directions.
Create an 8 -element uniform linear array whose elements are spaced half a wavelength apart.

```
fc = 3e8;
c = 3e8;
lambda = c/fc;
array = phased.ULA(8,lambda/2);
```

Simulate 100 snapshots of the received signal at the array. Assume there are two signals, coming from azimuth $30^{\circ}$ and $60^{\circ}$, respectively. The noise is white across all array elements, and the SNR is 10 dB .
x = sensorsig(getElementPosition(array)/lambda,...
100,[30 60],db2pow(-10));
Use a beamscan spatial spectrum estimator to estimate the arrival directions, based on the simulated data.

```
estimator = phased.BeamscanEstimator('SensorArray',array,...
    'PropagationSpeed ',c,'OperatingFrequency',fc,...
    'DOAOutputPort',true,'NumSignals',2);
[~,ang_est] = estimator(x);
```

Plot the spatial spectrum resulting from the estimation process.

```
plotSpectrum(estimator)
```

Beamscan Spatial Spectrum


The plot shows peaks at $30^{\circ}$ and $60^{\circ}$.

## Signals With Different Power Levels

Simulate receiving two uncorrelated incoming signals that have different power levels. A vector named scov stores the power levels.

Create an 8 -element uniform linear array whose elements are spaced half a wavelength apart.
fc = 3e8;
c = 3e8;

```
lambda = c/fc;
ha = phased.ULA(8,lambda/2);
```

Simulate 100 snapshots of the received signal at the array. Assume that one incoming signal originates from 30 degrees azimuth and has a power of 3 W . A second incoming signal originates from 60 degrees azimuth and has a power of 1 W . The two signals are not correlated with each other. The noise is white across all array elements, and the SNR is 10 dB .

```
ang = [30 60];
scov = [3 1];
x = sensorsig(getElementPosition(ha)/lambda,...
    100,ang,db2pow(-10),scov);
```

Use a beamscan spatial spectrum estimator to estimate the arrival directions, based on the simulated data.

```
hdoa = phased.BeamscanEstimator('SensorArray',ha,...
    'PropagationSpeed',c,'OperatingFrequency',fc,...
    'DOAOutputPort',true,'NumSignals',2);
[~,ang_est] = step(hdoa,x);
```

Plot the spatial spectrum resulting from the estimation process.

```
plotSpectrum(hdoa);
```



The plot shows a high peak at 30 degrees and a lower peak at 60 degrees.

## Reception of Correlated Signals

Simulate the reception of three signals, two of which are correlated.
Create a signal covariance matrix in which the first and third of three signals are correlated with each other.

```
scov = [1 0 0.6;...
    0 2 0;...
    0.6 0 1];
```

Simulate receiving 100 snapshots of three incoming signals from $30^{\circ}, 40^{\circ}$, and $60^{\circ}$ azimuth, respectively. The array that receives the signals is an 8 -element uniform linear array whose elements are spaced one-half wavelength apart. The noise is white across all array elements, and the SNR is 10 dB.

```
pos = (0:7)*0.5;
ns = 100;
ang = [30 40 60];
ncov = db2pow(-10);
x = sensorsig(pos,ns,ang,ncov,scov);
```


## Theoretical and Empirical Covariance of Received Signal

Simulate receiving a signal at a URA. Compare the signal theoretical covariance with its sample covariance.

Create a 2 -by- 2 uniform rectangular array having elements spaced $1 / 4$-wavelength apart.
pos $=0.25 *[0000 ;-11-11 ;-1-111] ;$
Define the noise power independently for each of the four array elements. Each entry in ncov is the noise power of an array element. This element position is the corresponding column in pos. Assume the noise is uncorrelated across elements.

```
ncov = db2pow([-9 -10 -10 -11]);
```

Simulate 100 snapshots of the received signal at the array, and store the theoretical and empirical covariance matrices. Assume that one incoming signal originates from $30^{\circ}$ azimuth and $10^{\circ}$ elevation. A second incoming signal originates from $50^{\circ}$ azimuth and $0^{\circ}$ elevation. The signals have a power of 1 W and are uncorrelated.

```
ns = 100;
ang1 = [30; 10];
ang2 = [50; 0];
ang = [ang1, ang2];
rng default
[x,rt,r] = sensorsig(pos,ns,ang,ncov);
```

View the magnitudes of the theoretical covariance and sample covariance.

```
abs(rt)
```

```
ans = 4×4
    2.1259 1.8181 1.9261 1.9754
    1.8181 2.1000 1.5263 1.9261
    1.9261 1.5263 2.1000 1.8181
    1.9754 1.9261 1.8181 2.0794
abs(r)
ans = 4\times4
    2.2107 1.7961 2.0205 1.9813
    1.7961 1.9858 1.5163 1.8384
    2.0205 1.5163 2.1762 1.8072
    1.9813 1.8384 1.8072 2.0000
```


## Correlation of Noise Between Sensors

Simulate receiving a signal at a ULA, where the noise between different sensors is correlated.
Create a 4-element uniform linear array whose elements are spaced one-half wavelength apart.
pos $=0.5$ * (0:3);
Define the noise covariance matrix. The value in the ( $k, j_{\_}$) position in the ncov matrix is the covariance between the $k$ and $j$ array elements listed in array.

```
ncov = 0.1 * [1 0.1 0 0; 0.1 1 0.1 0; 0 0.1 1 0.1; 0 0 0.1 1];
```

Simulate 100 snapshots of the received signal at the array. Assume that one incoming signal originates from $60^{\circ}$ azimuth.

```
ns = 100;
ang = 60;
[x,rt,r] = sensorsig(pos,ns,ang,ncov);
```

View the theoretical and sample covariance matrices for the received signal.

```
rt,r
rt = 4×4 complex
    1.1000 + 0.0000i
    -0.9027 + 0.4086i
        0.6661-0.7458i -0.9027 + 0.4086i 1.1000 + 0.0000i -0.9027-0.4086i
    -0.3033 + 0.9529i 0.6661 - 0.7458i -0.9027 + 0.4086i 1.1000 + 0.0000i
r = 4*4 complex
    1.1059 + 0.0000
    1.0037 + 0.0000i -0.8458-0.3456i
    0.6550-0.7017i -0.8458 + 0.3456i 1.0260 + 0.0000i -0.8775 - 0.3753i
    -0.3151 + 0.9363i 0.6578-0.6750i -0.8775 + 0.3753i 1.0606 + 0.0000i
```


## Input Arguments

## pos - Positions of elements in sensor array

1 -by-N vector | 2 -by-N matrix | 3-by-N matrix
Positions of elements in sensor array, specified as an N-column vector or matrix. The values in the matrix are in units of signal wavelength. For example, [ $\left.\begin{array}{lll}0 & 1 & 2\end{array}\right]$ describes three elements that are spaced one signal wavelength apart. N is the number of elements in the array.

Dimensions of pos:

- For a linear array along the y axis, specify the y coordinates of the elements in a 1-by-N vector.
- For a planar array in the $y z$ plane, specify the $y$ and $z$ coordinates of the elements in columns of a 2-by-N matrix.
- For an array of arbitrary shape, specify the $\mathrm{x}, \mathrm{y}$, and z coordinates of the elements in columns of a 3-by-N matrix.

Data Types: double
ns - Number of snapshots of simulated signal
positive integer scalar
Number of snapshots of simulated signal, specified as a positive integer scalar. The function returns this number of samples per array element.

## Data Types: double

## ang - Directions of incoming plane wave signals

1-by-M vector | 2 -by-M matrix
Directions of incoming plane wave signals, specified as an M-column vector or matrix in degrees. M is the number of incoming signals.

Dimensions of ang:

- If ang is a 2-by-M matrix, each column specifies a direction. Each column is in the form [azimuth; elevation]. The azimuth angle on page 2-425 must be between -180 and 180 degrees, inclusive. The elevation angle must be between -90 and 90 degrees, inclusive.
- If ang is a 1 -by-M vector, each entry specifies an azimuth angle. In this case, the corresponding elevation angle is assumed to be 0 .

Data Types: double

## ncov - Noise characteristics

0 (default) | nonnegative scalar | 1-by-N vector of positive numbers | N-by-N positive definite matrix
Noise characteristics, specified as a nonnegative scalar, 1-by-N vector of positive numbers, or N-by-N positive definite matrix.

Dimensions of ncov:

- If ncov is a scalar, it represents the noise power of the white noise across all receiving sensor elements, in watts. In particular, a value of 0 indicates that there is no noise.
- If ncov is a 1-by-N vector, each entry represents the noise power of one of the sensor elements, in watts. The noise is uncorrelated across sensors.
- If ncov is an N-by-N matrix, it represents the covariance matrix for the noise across all sensor elements.

Data Types: double

## scov - Incoming signal characteristics

1 (default) | positive scalar | 1-by-M vector of positive numbers | M-by-M positive semidefinite matrix
Incoming signal characteristics, specified as a positive scalar, 1-by-M vector of positive numbers, or M-by-M positive semidefinite matrix.

Dimensions of scov:

- If scov is a scalar, it represents the power of all incoming signals, in watts. In this case, all incoming signals are uncorrelated and share the same power level.
- If scov is a 1 -by-M vector, each entry represents the power of one of the incoming signals, in watts. In this case, all incoming signals are uncorrelated with each other.
- If scov is an M-by-M matrix, it represents the covariance matrix for all incoming signals. The matrix describes the correlation among the incoming signals. In this case, scov can be real or complex.

Data Types: double

## taper - Array element taper

1 (default) | scalar | $N$-by- 1 column vector
Array element taper, specified as a scalar or complex-valued $N$-by- 1 column vector. The dimension $N$ is the number of array elements. If taper is a scalar, all elements in the array use the same value. If taper is a vector, each entry specifies the taper applied to the corresponding array element.

Data Types: double
Complex Number Support: Yes

## Output Arguments

## x - Received signal

complex ns-by-N matrix
Received signal at sensor array, returned as a complex ns-by-N matrix. Each column represents the received signal at the corresponding element of the array. Each row represents a snapshot.

## rt - Theoretical covariance matrix

complex N-by-N matrix
Theoretical covariance matrix of the received signal, returned as a complex N -by-N matrix.

## r - Sample covariance matrix

complex N-by-N matrix
Sample covariance matrix of the received signal, returned as a complex N -by- N matrix. N is the number of array elements. The function derives this matrix from $x$.

Note If you specify this output argument, consider making ns greater than or equal to N. Otherwise, $r$ is rank deficient.

## More About

## Azimuth Angle, Elevation Angle

The azimuth angle of a vector is the angle between the $x$-axis and the orthogonal projection of the vector onto the $x y$ plane. The angle is positive in going from the $x$ axis toward the $y$ axis. Azimuth angles lie between - 180 and 180 degrees. The elevation angle is the angle between the vector and its orthogonal projection onto the $x y$-plane. The angle is positive when going toward the positive $z$-axis from the xy plane. By default, the boresight direction of an element or array is aligned with the positive $x$-axis. The boresight direction is the direction of the main lobe of an element or array.

Note The elevation angle is sometimes defined in the literature as the angle a vector makes with the positive $z$-axis. The MATLAB and Phased Array System Toolbox products do not use this definition.

This figure illustrates the azimuth angle and elevation angle for a vector shown as a green solid line.


## Version History

Introduced in R2012b

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:
Does not support variable-size inputs.

## See Also

phased.SteeringVector

## shnidman

Required SNR using Shnidman's equation

## Syntax

```
SNR = shnidman(Pd,Pfa)
SNR = shnidman(Pd,Pfa,N)
SNR = shnidman(Pd,Pfa,N,Sw)
```


## Description

SNR = shnidman(Pd,Pfa) returns the required signal-to-noise ratio in decibels for the specified detection and false-alarm probabilities using Shnidman's equation. The SNR is determined for a single pulse and a "Swerling Case Number" on page 2-429 of 0, a nonfluctuating target.

SNR = shnidman(Pd,Pfa,N) returns the required SNR for a nonfluctuating target based on the noncoherent integration of $N$ pulses.

SNR = shnidman(Pd, Pfa, $N, S W$ ) returns the required SNR for the Swerling case number Sw.

## Examples

## Compute Single-Pulse SNR

Find and compare the required single-pulse SNR for Swerling cases I and III. The Swerling case I has no dominant scatterer while the Swerling case III has a dominant scatterer.

Specify the false-alarm and detection probabilities.

```
pfa = 1e-6:1e-5:.001;
Pd = 0.9;
```

Allocate arrays for plotting.

```
SNR Sw1 = zeros(1,length(pfa));
SNR_Sw3 = zeros(1,length(pfa));
```

Loop over PFAs for both scatterer cases.

```
for j=1:length(pfa)
    SNR_Sw1(j) = shnidman(Pd,pfa(j),1,1);
    SNR_SW3(j) = shnidman(Pd,pfa(j),1,3);
end
```

Plot the SNR vs PFA.

```
semilogx(pfa,SNR_Sw1)
hold on
semilogx(pfa,SNR_Sw3)
hold off
```

```
xlabel("False-Alarm Probability")
ylabel("SNR")
title("Required Single-Pulse SNR for Pd = "+Pd)
legend("Swerling Case "+["I" "III"],Location="southwest")
```



The presence of a dominant scatterer reduces the required SNR for the specified detection and falsealarm probabilities.

## Input Arguments

## Pd - Probability of detection

positive scalar
Probability of detection, specified as a positive scalar.
Data Types: double

## Pfa - Probability of false alarm

positive scalar
Probability of false alarm, specified as a positive scalar.
Data Types: double

## N - Number of pulses for noncoherent integration

1 (default) | positive scalar

Number of pulses for noncoherent integration, specified as a positive scalar.
Data Types: double
Sw - Swerling case number
0 (default) | 1 | 2 | $3 \mid 4$
Swerling case number, specified as $0,1,2,3$, or 4 . For more information, see "Swerling Case Number" on page 2-429
Data Types: double

## More About

## Shnidman's Equation

Shnidman's equation is a series of equations that yield an estimate of the SNR required for a specified false-alarm and detection probability. Like Albersheim's equation, Shnidman's equation is applicable to a single pulse or the noncoherent integration of $N$ pulses. Unlike Albersheim's equation, Shnidman's equation holds for square-law detectors and is applicable to fluctuating targets. An important parameter in Shnidman's equation is the Swerling case number.

## Swerling Case Number

The Swerling case numbers characterize the detection problem for fluctuating pulses in terms of:

- A decorrelation model for the received pulses
- The distribution of scatterers affecting the probability density function (PDF) of the target radar cross section (RCS).

The Swerling case numbers consider all combinations of two decorrelation models (scan-to-scan; pulse-to-pulse) and two RCS PDFs (based on the presence or absence of a dominant scatterer).

| Swerling Case Number | Description |
| :--- | :--- |
| 0 (alternatively designated as 5) | Nonfluctuating pulses. |
| I | Scan-to-scan decorrelation. Rayleigh/exponential <br> PDF-A number of randomly distributed scatterers <br> with no dominant scatterer. |
| II | Pulse-to-pulse decorrelation. Rayleigh/ <br> exponential PDF- A number of randomly <br> distributed scatterers with no dominant scatterer. |
| III | Scan-to-scan decorrelation. Chi-square PDF with <br> 4 degrees of freedom. A number of scatterers <br> with one dominant. |
| IV | Pulse-to-pulse decorrelation. Chi-square PDF with <br> 4 degrees of freedom. A number of scatterers <br> with one dominant. |

## Version History

## Introduced in R2011a

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
Does not support variable-size inputs.

## References

[1] Richards, M. A. Fundamentals of Radar Signal Processing. New York: McGraw-Hill, 2005.

## See Also

albersheim

## sonareqsI

Compute source level using the sonar equation

## Syntax

SL = sonareqsl(SNR,NL,DI,TL)
SL = sonareqsl(SNR,NL,DI,TL,TS)

## Description

SL = sonareqsl(SNR,NL,DI,TL) returns the source level of a signal, SL, required to achieve a specified received signal-to-noise ratio, SNR. Source level is computed using the "Sonar Equation". Specify the received noise level, NL, receiver directivity index, DI, and the transmission loss, TL. Use this syntax to evaluate passive sonar system performance.

SL = sonareqsl(SNR,NL,DI,TL,TS) returns the source level taking into account the target strength TS. Use this syntax to evaluate active sonar system performance, where the transmitted signal is reflected from a target. TL represents one-way transmission loss.

## Examples

## Estimate Source Level from Passive Sonar Equation

Estimate the source level of a signal arriving from a source with an SNR of 10 dB . The noise level is 75 dB , the receive array directivity index is 25 dB , and the transmission loss is 140 dB .

```
SNR = 10;
NL = 75.0;
DI = 25.0;
TL = 140.0;
SL = sonareqsl(SNR,NL,DI,TL)
SL = 200
```


## Estimate Source Level from Active Sonar Equation

Estimate the source level of a signal transmitted by a source with SNR of 15 dB and reflected from a target with $25 \mathrm{~dB} / / 1 \mathrm{~m}^{2}$ target strength. The noise level is $45 \mathrm{~dB} / / 1 \mu \mathrm{~Pa}$, the receive array directivity index is 25 dB , and the one-way transmission loss is 60 dB .

```
SNR = 15.0;
NL = 45.0;
DI = 25.0;
TL = 60.0;
TS = 25.0;
SL = sonareqsl(SNR,NL,DI,TL,TS)
SL = 130
```


## Input Arguments

## SNR — Received signal-to-noise ratio

scalar
Received signal-to-noise ratio, specified as a scalar. Units are in dB.
Example: 10
Data Types: double

## NL - Received noise level

scalar
Received noise level, specified as a scalar. Noise level is the ratio of the noise intensity to a reference intensity, converted to dB . The reference intensity is the intensity of a sound wave having a root-mean-square (rms) pressure of $1 \mu \mathrm{~Pa}$. Units are in $\mathrm{dB} / / 1 \mu \mathrm{~Pa}$.

Example: 70
Data Types: double

## DI - Receiver directivity index

scalar
Receiver directivity index, specified as a scalar. Units are in dB.
Example: 30
Data Types: double

## TL - Transmission loss

positive scalar
Transmission loss (TL), specified as a positive scalar. Transmission loss is the attenuation of sound intensity as the sound propagates through the underwater channel. Transmission loss is defined as the ratio of sound intensity at 1 m from a source to the sound intensity at distance $R$. For active sonar, TL represents one-way transmission loss.

$$
T L=10 \log \frac{I_{\mathrm{s}}}{I(R)}
$$

Units are in dB .
Example: 120
Data Types: double

## TS - Target strength

scalar
Target strength, specified as a scalar. Target strength is the ratio of the intensity of a reflected signal at 1 m from a target to the incident intensity. Target strength is the sonar analog to radar cross section. Units are in $\mathrm{dB} / / 1 \mathrm{~m}^{2}$.
Example: 5
Data Types: double

## Output Arguments

## SL - Sonar source level <br> scalar

Sonar source level, returned as a scalar. Source level is the ratio of the source intensity to a reference intensity, converted to dB . The reference intensity is the intensity of a sound wave having an rms pressure of $1 \mu \mathrm{~Pa}$. Units are in $\mathrm{dB} / / 1 \mu \mathrm{~Pa}$.

## Version History

Introduced in R2017b

## References

[1] Ainslie M. A. and J.G. McColm. "A simplified formula for viscous and chemical absorption in sea water." Journal of the Acoustical Society of America, Vol. 103, Number 3, 1998, pp. 1671--1672.
[2] Urick, Robert J, Principles of Underwater Sound, 3rd ed. Peninsula Publishing, Los Altos, CA, 1983.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
Does not support variable-size inputs.

## See Also

range2tl|sonareqsnr|sonareqtl|tl2range
Topics
"Sonar Equation"
"Element Directivity"

## sonareqsnr

Compute SNR using the sonar equation

## Syntax

```
SNR = sonareqsnr(SL,NL,DI,TL)
SNR = sonareqsnr(SL,NL,DI,TL,TS)
```


## Description

SNR = sonareqsnr(SL,NL,DI,TL) returns the received signal-to-noise ratio, SNR, from the source level, SL, received noise level, NL, receiver directivity index, DI, and transmission loss, TL. SNR is computed using the "Sonar Equation". Use this syntax to evaluate passive sonar system performance.

SNR = sonareqsnr(SL,NL, DI, TL, TS ) returns SNR taking into account the target strength TS. Use this syntax to evaluate active sonar system performance, where the transmitted signal is reflected from a target.

## Examples

## Estimate SNR from Passive Sonar Equation

Estimate the SNR of a signal arriving from a source with a source level of 200 dB . The noise level is 75 dB , the receive array directivity index is 25 dB , and the transmission loss is 140 dB .

```
SL = 200.0;
NL = 75.0;
DI = 25.0;
TL = 140.0;
SNR = sonareqsnr(SL,NL,DI,TL)
SNR = 10
```


## Estimate SNR from Active Sonar Equation

Estimate the SNR of a signal transmitted by a source with a source level of $130 \mathrm{~dB} / / 1 \mu \mathrm{~Pa}$ and reflected from a target with $25 \mathrm{~dB} / / 1 \mathrm{~m}^{2}$ target strength. The noise level is $45 \mathrm{~dB} / / 1 \mu \mathrm{~Pa}$, the receive array directivity is 25 dB , and the one-way transmission loss is 60 dB .

```
SL = 130.0;
NL = 45.0;
DI = 25.0;
TL = 60.0;
TS = 25.0;
SNR = sonareqsnr(SL,NL,DI,TL,TS)
SNR = 15
```


## Input Arguments

## SL - Sonar source level

scalar
Sonar source level, specified as a scalar. Source level is the ratio of the source intensity to a reference intensity, converted to dB . The reference intensity is the intensity of a sound wave having a root-mean-square (rms) pressure of $1 \mu \mathrm{~Pa}$. Units are in $\mathrm{dB} / / 1 \mu \mathrm{~Pa}$.
Example: 90
Data Types: double

## NL - Received noise level

## scalar

Received noise level, specified as a scalar. Noise level is the ratio of the noise intensity to a reference intensity, converted to dB . The reference intensity is the intensity of a sound wave having a root-mean-square (rms) pressure of $1 \mu \mathrm{~Pa}$. Units are in $\mathrm{dB} / / 1 \mu \mathrm{~Pa}$.
Example: 70
Data Types: double

## DI - Receiver directivity index

scalar
Receiver directivity index, specified as a scalar. Units are in dB .
Example: 30
Data Types: double

## TL - Transmission loss

positive scalar
Transmission loss (TL), specified as a positive scalar. Transmission loss is the attenuation of sound intensity as the sound propagates through the underwater channel. Transmission loss is defined as the ratio of sound intensity at 1 m from a source to the sound intensity at distance $R$. For active sonar, TL represents one-way transmission loss.

$$
T L=10 \log \frac{I_{\mathrm{s}}}{I(R)}
$$

Units are in dB.
Example: 120
Data Types: double

## TS - Target strength <br> scalar

Target strength, specified as a scalar. Target strength is the ratio of the intensity of a reflected signal at 1 m from a target to the incident intensity. Target strength is the sonar analog to radar cross section. Units are in $\mathrm{dB} / / 1 \mathrm{~m}^{2}$.
Example: 5

Data Types: double

## Output Arguments

## SNR - Received signal-to-noise ratio

real scalar
Received signal-to-noise ratio, returned as a scalar.
Data Types: double

## Version History

## Introduced in R2017b

## References

[1] Ainslie M. A. and J.G. McColm. "A simplified formula for viscous and chemical absorption in sea water." Journal of the Acoustical Society of America, Vol. 103, Number 3, 1998, pp. 1671--1672.
[2] Urick, Robert J, Principles of Underwater Sound, 3rd ed. Peninsula Publishing, Los Altos, CA, 1983.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:
Does not support variable-size inputs.

## See Also

range2tl| sonareqsl|sonareqtl|tl2range

## Topics

"Sonar Equation"
"Element Directivity"

## sonareqtl

Compute transmission loss using the sonar equation

## Syntax

TL = sonareqtl(SL,SNR,NL,DI)
TL = sonareqtl(SL,SNR,NL,DI,TS)

## Description

TL = sonareqtl(SL, SNR ,NL, DI) returns the transmission loss of a signal from source to receiver that produces the signal-to-noise ratio, SNR. Transmission loss is computed using the "Sonar Equation". Required inputs are the source level, SL, received noise level, NL, and receiver directivity index, DI. Use this syntax to evaluate passive sonar system performance.
$T L=$ sonareqtl(SL,SNR,NL, DI,TS) returns the one-way transmission loss. The signal is reflected from a target with a target strength, TS. Use this syntax to evaluate active sonar system performance, where the transmitted signal is reflected from a target.

## Examples

## Estimate Transmission Loss from Passive Sonar Equation

Estimate the transmission loss of a signal arriving from a source with source level of 200 dB . The received SNR is 10 dB , the noise level is 75 dB , and the receive array directivity index is 25 dB .

```
SNR = 10;
SL = 200.0;
NL = 75.0;
DI = 25.0;
TL = sonareqtl(SL,SNR,NL,DI)
TL = 140
```


## Estimate Transmission Loss from Active Sonar Equation

Estimate the one-way transmission loss of a signal transmitted by a source with source level of 130 $\mathrm{dB} / / 1 \mu \mathrm{~Pa}$ and reflected from a target with $25 \mathrm{~dB} / / 1 \mathrm{~m}^{2}$ target strength. The noise level is $45 \mathrm{~dB} / / 1$ $\mu \mathrm{Pa}$, the receive array directivity is 25 dB .

```
SL = 130.0;
SNR = 15.0;
NL = 45.0;
DI = 25.0;
TS = 25.0;
TL = sonareqtl(SL,SNR,NL,DI,TS)
TL = 60
```


## Input Arguments

## SL - Sonar source level

scalar
Sonar source level, specified as a scalar. Source level is the ratio of the source intensity to a reference intensity, converted to dB . The reference intensity is the intensity of a sound wave having a root-mean-square (rms) pressure of $1 \mu \mathrm{~Pa}$. Units are in $\mathrm{dB} / / 1 \mu \mathrm{~Pa}$.
Example: 90
Data Types: double
SNR - Received signal-to-noise ratio
scalar
Received signal-to-noise ratio, specified as a scalar. Units are in dB.
Example: 10
Data Types: double

## NL - Received noise level

scalar
Received noise level, specified as a scalar. Noise level is the ratio of the noise intensity to a reference intensity, converted to dB . The reference intensity is the intensity of a sound wave having a root-mean-square (rms) pressure of $1 \mu \mathrm{~Pa}$. Units are in $\mathrm{dB} / / 1 \mu \mathrm{~Pa}$.
Example: 70
Data Types: double

## DI - Receiver directivity index

scalar
Receiver directivity index, specified as a scalar. Units are in dB.
Example: 30
Data Types: double

## TS - Target strength

scalar
Target strength, specified as a scalar. Target strength is the ratio of the intensity of a reflected signal at 1 m from a target to the incident intensity. Target strength is the sonar analog to radar cross section. Units are in $\mathrm{dB} / / 1 \mathrm{~m}^{2}$.
Example: 5
Data Types: double

## Output Arguments

## TL - Transmission loss

positive scalar

Transmission loss, returned as a positive scalar. Transmission loss is the attenuation of sound intensity as the sound propagates through the underwater channel. Transmission loss is defined as the ratio of sound intensity at 1 m from a source to the sound intensity at distance $R$. When target strength, TS , is specified, transmission loss is two-way.

## Version History

## Introduced in R2017b

## References

[1] Ainslie M. A. and J.G. McColm. "A simplified formula for viscous and chemical absorption in sea water." Journal of the Acoustical Society of America, Vol. 103, Number 3, 1998, pp. 1671--1672.
[2] Urick, Robert J, Principles of Underwater Sound, 3rd ed. Peninsula Publishing, Los Altos, CA, 1983.

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:
Does not support variable-size inputs.

## See Also

range2tl|sonareqsl|tl2range | sonareqsnr

## Topics

"Sonar Equation"
"Element Directivity"

## scatteringchanmtx

Scattering channel matrix

## Syntax

```
chmat = scatteringchanmtx(txarraypos,rxarraypos,numscat)
chmat = scatteringchanmtx(txarraypos,rxarraypos,numscat,angrange)
chmat = scatteringchanmtx(txarraypos,rxarraypos,txang,rxang,G)
```


## Description

chmat $=$ scatteringchanmtx(txarraypos,rxarraypos,numscat) returns the channel matrix, chmat, for a MIMO channel consisting of a transmitting array, a receiver array, and multiple scatterers. The transmitting array is located at txarraypos and the receiving array at rxarraypos. numscat is the number of point scatterers.

The function generates numscat random transmission directions and numscat random receiving directions. The channel matrix describes multipath propagation through the numscat paths. By assumption, all paths arrive at the receiving array simultaneously implying that the channel is frequency flat. Flat frequency means that the spectrum of the signal is not changed. Path gains are derived from a zero-mean, unit-variance, complex-valued normal distribution.
chmat = scatteringchanmtx(txarraypos,rxarraypos,numscat,angrange) also specifies the angular range, angrange, for transmitting and receiving angles.
chmat $=$ scatteringchanmtx(txarraypos,rxarraypos,txang,rxang, G) also specifies transmitting angles, txang, receiving angles, rxang, and path gains, G.

## Examples

## Compute Channel Matrix for Random Signal Paths

Compute the channel matrix for a 13 -element transmitting array and a 15 -element receiving array. Assume that there are 17 randomly located scatterers. The arrays are uniform linear arrays with 0.45 -wavelength spacing. The receiving array is 300 wavelengths away from the transmitting array. Use the channel matrix to compute a propagated signal from the transmitting array to the receiving array.

Specify the arrays. Element spacing is in units of wavelength.

```
numtx = 13;
sp = 0.45;
txpos = (0:numtx-1)*sp;
numrx = 15;
rxpos = 300 + (0:numrx-1)*sp;
```

Specify the number of scatterers and create the channel matrix.

```
numscat = 17;
chmat = scatteringchanmtx(txpos,rxpos,numscat);
```

Create a signal consisting of zeros and ones. Then, propagate the signal from the transmitter to receiver.

```
x = randi(2,[100 numtx])-1;
```

y = x*chmat;

## Compute Channel Matrix for Constrained Random Signal Paths

Compute the channel matrix for a 4 -by- 4 transmitting URA array and a 5-by-5 receiving URA array. Assume that 17 scatterers are randomly located within a specified angular range. The element spacing for both arrays is one-half wavelength. The receive array is 500 wavelengths away from the transmitting array along the $x$-axis. Use the channel matrix to compute a propagated signal from the transmitting array to the receiving array. Constrain the angular span for the transmitting and receiving directions.

Specify the 4 -by- 4 transmitting array. Element spacing is in units of wavelength.

```
Nt = 4;
sp = 0.5;
ygridtx = (0:Nt-1)*sp - (Nt-1)/2*sp;
zgridtx = (0:Nt-1)*sp - (Nt-1)/2*sp;
[ytx,ztx] = meshgrid(ygridtx,zgridtx);
txpos = [zeros(1,Nt*Nt);ytx(:).';ztx(:).'];
```

Specify the 5 -by- 5 receiving array. Element spacing is in units of wavelength.

```
Nr = 5;
sp = 0.5;
ygridrx = (0:Nr-1)*sp - (Nr-1)/2*sp;
zgridrx = (0:Nr-1)*sp - (Nr-1)/2*sp;
[yrx,zrx] = meshgrid(ygridrx,zgridrx);
rxpos = [500*ones(1,Nr*Nr);yrx(:).';zrx(:).'];
```

Set the angular limits for transmitting and receiving.

- The azimuth angle limits for the transmitter are $-45^{\circ}$ to $+45^{\circ}$.
- The azimuth angle limits for the receiver are $-75^{\circ}$ to $+50^{\circ}$.
- The elevation angle limits for the transmitter are $-12^{\circ}$ to $+12^{\circ}$.
- The elevation angle limits for the receiver are $-30^{\circ}$ to $+30^{\circ}$.

```
angrange = [-45 45 -75 50; -12 12 -30 30];
```

Specify the number of scatterers and create the channel matrix.

```
numscat = 6;
chmat = scatteringchanmtx(txpos,rxpos,numscat,angrange);
```

Create a 100 -sample signal consisting of zeros and ones. Then, propagate the signal from the transmitting array to the receiving array.

```
x = randi(2,[100 Nt*Nt])-1;
y = x*chmat;
```


## Compute Channel Matrix for Specified Signal Paths

Compute the channel matrix for a 4-by-4 transmitting URA array and a 5-by-5 receiving URA array. Assume there are 3 scatterers with known directions. The element spacings for both arrays is onehalf wavelength. The receive array is 500 wavelengths away from the transmitting array along the $x$ axis. Use the channel matrix to compute a propagated signal from the transmitting array to the receiving array. Specify the transmitting and receiving directions. The number of directions determines the number of scatterers.

Specify the 4 -by- 4 transmitting array. Element spacing is in units of wavelength.

```
Nt = 4;
sp = 0.5;
ygridtx = (0:Nt-1)*sp - (Nt-1)/2*sp;
zgridtx = (0:Nt-1)*sp - (Nt-1)/2*sp;
[ytx,ztx] = meshgrid(ygridtx,zgridtx);
txpos = [zeros(1,Nt*Nt);ytx(:).';ztx(:).'];
```

Specify the 5 -by- 5 receiving array. Element spacing is in units of wavelength.

```
Nr = 5;
sp = 0.5;
ygridrx = (0:Nr-1)*sp - (Nr-1)/2*sp;
zgridrx = (0:Nr-1)*sp - (Nr-1)/2*sp;
[yrx,zrx] = meshgrid(ygridrx,zgridrx);
rxpos = [500*ones(1,Nr*Nr);yrx(:).';zrx(:).'];
```

Specify the transmitting and receiving angles and the gains. Then, create the channel matrix.

```
txang = [20 -10 40; 0 12 -12];
rxang = [70 -5.5 27.2; 4 1 -10];
gains = [1 1+1i 2-3*1i];
chmat = scatteringchanmtx(txpos,rxpos,txang,rxang,gains);
```

Create a 100 -sample signal consisting of zeros and ones. Then, propagate the signal from the transmitting array to the receiving array.

```
x = randi(2,[100 Nt*Nt])-1;
```

$y=x *$ chmat ;

## Input Arguments

## txarraypos - Positions of elements in transmitting array

real-valued 1-by- $N_{\mathrm{t}}$ row vector | real-valued 2-by- $N_{\mathrm{t}}$ matrix | real-valued 3-by- $N_{\mathrm{t}}$ matrix
Transmitting array element positions, specified as a real-valued 1-by- $N_{t}$ row vector, 2 -by- $N_{\mathrm{t}}$ matrix, or 3 -by- $N_{\mathrm{t}}$ matrix. $N_{\mathrm{t}}$ is the number of elements in the transmitting array.

| txarraypos | Dimensions of Transmitting Array |
| :--- | :--- |
| 1 -by- $N_{\mathrm{t}}$ row vector | All transmitting array elements lie along the $y$ - <br> axis. The vector specifies the $y$-coordinates of the <br> array elements. |


| txarraypos | Dimensions of Transmitting Array |
| :--- | :--- |
| 2-by- $N_{\mathrm{t}}$ matrix | All transmitting array elements lie in the $y z-$ <br> plane. Each column of the matrix specifies the $y$ <br> and $z$ coordinates of an array element. |
| 3-by- $N_{\mathrm{t}}$ matrix | The transmitting array elements have arbitrary 3- <br> D coordinates. Each column of the matrix <br> specifies the $x, y$, and $z$ coordinates of an array <br> element. |

Units are in wavelengths.
Example: [-2.0,-1.0,0.0,1.0,2.0]
Data Types: double
rxarraypos - Positions of elements in receiving array
real-valued 1-by- $N_{\mathrm{r}}$ row vector | real-valued 2-by- $N_{\mathrm{r}}$ matrix | real-valued 3-by- $N_{\mathrm{r}}$ matrix
Receiving array element positions, specified as a real-valued 1-by- $N_{\mathrm{r}}$ row vector, 2-by-vmatrix, or 3-by- $N_{\mathrm{r}}$ matrix. $N_{\mathrm{t}}$ is the number of elements in the transmitting array.

| rxarraypos | Dimensions of Receiving Array |
| :--- | :--- |
| 1-by- $N_{\mathrm{r}}$ row vector | All receiving array elements lie along the $y$-axis. <br> The vector specifies the $y$-coordinates of the <br> array elements. |
| 2-by- $N_{\mathrm{r}}$ matrix | All receiving array elements lie in the $y z$-plane. <br> Each column of the matrix specifies the $y$ and $z$ <br> coordinates of an array element. |
| 3 -by- $N_{\mathrm{r}}$ matrix | The receiving array elements have arbitrary 3-D <br> coordinates. Each column of the matrix specifies <br> the $x, y$, and $z$ coordinates of an array element. |

Units are in wavelengths.
Example: [-2.0,-1.0,0.0,1.0,2.0]
Data Types: double

## numscat - Number of scatterers

positive integer
Number of scatters, specified as a positive integer

## Example: 7

Data Types: double
angrange - Angular range of transmission and reception directions
real-valued 1-by-2 row vector | real-valued row 1-by-4 vector | real-valued 2-by-2 matrix | real-valued 2-by-4 matrix

Angular range of transmitting and receiving directions, specified as one of the values in this table.

| Size of angrange | Angular range |
| :--- | :--- |
| real-valued 1-by-2 row vector | Specify the same azimuth angle direction span <br> for the transmitting and receiving arrays by using <br> the minimum and maximum azimuth angles, <br> [az_min az_max]. The elevation direction span <br> is $-90^{\circ}$ to to $90^{\circ}$. |
| real-valued 1-by-4 row vector | Specify the azimuth angle direction range for the <br> transmitting and receiving arrays by using <br> [tx_az_min tx_az_max rx_az_min <br> rx_az_max]. The first two values are the <br> minimum and maximum of the transmitting array <br> directions. The last two values are the minimum <br> and maximum of the receiving array directions. <br> The range of the elevation angles is -90 |
| real-valued $+90^{\circ}$. |  |$|$| Specify the same azimuth and elevation angle |
| :--- |
| direction spans for the transmitting and receiving |
| arrays by using the minimum and maximum |
| azimuth and elevation angles, [az_min |
| az_max; el_min el_max]. |

Units are in degrees.
Example: [-45 45-30 30; -10 20-5 30]
Data Types: double

## txang - Transmission path angles

real-valued 1-by- $N_{\mathrm{s}}$ row vector | real-valued 2-by- $N_{\mathrm{s}}$ matrix
Transmission path angles, specified as a real-valued 1-by- $N_{\mathrm{s}}$ row vector or a 2-by- $N_{\mathrm{s}}$ matrix. $N_{\mathrm{s}}$ is the number of scatterers specified by numscat.

- When txang is a vector, each element specifies the azimuth angle of a path. The elevation angle of the path is zero degrees.
- When txang is a matrix, each column specifies the azimuth and elevation angles of a path in the form [az;el].

Example: [4 -2; 0 35]
Data Types: double
rxang - Receiving path angles
real-valued 1-by- $N_{\mathrm{s}}$ row vector | real-valued 2-by- $N_{\mathrm{s}}$ matrix

Receiving path angles, specified as a real-valued 1-by- $N_{s}$ row vector or a 2 -by- $N_{\mathrm{s}}$ matrix. $N_{\mathrm{s}}$ is the number of scatterers specified by numscat.

- When rxang is a vector, each element specifies the azimuth angle of a path. The elevation angle of the path is zero degrees.
- When rxang is a matrix, each column specifies the azimuth and elevation angles of a path in the form [az;el].

Example: [4-2; 0 35]
Data Types: double

## G - Path gains

1-by- $N_{s}$ complex-valued row vector
Path gains, specified as a 1-by- $N_{s}$ complex-valued row vector. $N_{s}$ is the number of scatterers specified by numscat. The gains apply to the corresponding paths. Units are dimensionless.

```
Example: exp(1i*pi/3)
```

Data Types: double

## Output Arguments

## chmat - MIMO channel matrix

$N_{t}$-by- $N_{r}$ complex-valued matrix
MIMO channel matrix, returned as an $N_{\mathrm{t}}-$ by- $N_{\mathrm{r}}$ complex-valued matrix. $N_{\mathrm{t}}$ is the number of elements in the transmitting array. $N_{\mathrm{r}}$ is the number of elements in the receiving array.
Data Types: double

## Version History <br> Introduced in R2017a

## References

[1] Heath, R. Jr. et al. "An Overview of Signal Processing Techniques for Millimeter Wave MIMO Systems", arXiv.org:1512.03007 [cs.IT], 2015.
[2] Tse, D. and P. Viswanath, Fundamentals of Wireless Communications, Cambridge: Cambridge University Press, 2005.
[3] Paulraj, A. Introduction to Space-Time Wireless Communications, Cambridge: Cambridge University Press, 2003.

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder $^{\text {TM }}$.
Usage notes and limitations:

- Does not support variable-size inputs.


## See Also

## Functions

blkdiagbfweights|diagbfweights|waterfill
Objects
phased.ScatteringMIMOChannel

## speed2dop

Convert speed to Doppler shift

## Syntax

```
dps = speed2dop(radvel,lambda)
```


## Description

dps = speed2dop(radvel, lambda) returns the one-way Doppler shift in hertz corresponding to the radial velocity radvel for the wavelength lambda.

## Examples

## Calculate Doppler Shift from Speed

Calculate the Doppler shift in hertz for a given carrier wavelength and source speed. The radar frequency is 24.15 GHz . Assume a radial speed of $35.76 \mathrm{~m} / \mathrm{s}$.

```
radvel = 35.76;
```

f0 = 24.15e9;
lambda = physconst('LightSpeed')/f0;
doppler_shift = speed2dop(radvel,lambda)
doppler_shift = 2.8807e+03

## Input Arguments

```
radvel - Radial velocity
```

scalar | vector | matrix
Radial velocity in meters per second, specified as a scalar, vector, or matrix.
Data Types: double

## lambda - Wavelength

positive scalar
Wavelength in meters, specified as a positive scalar.
Data Types: double

## Output Arguments

dps - One-way Doppler shift
scalar | vector | matrix
One-way Doppler shift in hertz, returned as a scalar, vector, or matrix.

## More About

## Doppler-Radial Velocity Relation

The Doppler shift of a source relative to a receiver can be computed from the relative radial velocity between the source and receiver:

$$
\Delta f=\frac{V_{S, r}}{\lambda}
$$

where $\Delta f$ is the Doppler shift in hertz, $V_{s, r}$ denotes the radial velocity of the source relative to the receiver, and $\lambda$ is the carrier frequency wavelength in meters.

## Version History

Introduced in R2011a

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
Does not support variable-size inputs.

## References

[1] Rappaport, T. Wireless Communications: Principles \& Practices. Upper Saddle River, NJ: Prentice Hall, 1996.
[2] Skolnik, M. Introduction to Radar Systems, 3rd Ed. New York: McGraw-Hill, 2001.

See Also<br>dop2speed | dopsteeringvec

## sph2cartvec

Convert vector from spherical basis components to Cartesian components

## Syntax

vr = sph2cartvec(vs,az,el)

## Description

$\mathrm{vr}=\mathrm{sph} 2 \mathrm{cartvec}(\mathrm{vs}, \mathrm{az}, \mathrm{el})$ converts the components of a vector or set of vectors, vs , from their spherical basis representation to their representation in a local Cartesian coordinate system. A spherical basis representation is the set of components of a vector projected into the right-handed spherical basis given by ( $\widehat{\mathbf{e}}_{a z}, \widehat{\mathbf{e}}_{e l}, \widehat{\mathbf{e}}_{R}$ ). The orientation of a spherical basis depends upon its location on the sphere as determined by azimuth, az, and elevation, el.

## Examples

## Cartesian Representation of Azimuthal Vector

Start with a vector in a spherical basis located at $45^{\circ}$ azimuth, $45^{\circ}$ elevation. The vector points along the azimuth direction. Compute the vector components with respect to Cartesian coordinates.

```
vs = [1;0;0];
vr = sph2cartvec(vs,45,45)
vr = 3x1
    -0.7071
    0.7071
            0
```


## Input Arguments

## vs - Vector in spherical basis representation

3-by-1 column vector | 3 -by-N matrix
Vector in spherical basis representation specified as a 3-by-1 column vector or 3 -by- $N$ matrix. Each column of vs contains the three components of a vector in the right-handed spherical basis $\left(\widehat{\mathbf{e}}_{a z}, \widehat{\mathbf{e}}_{e l}, \widehat{\mathbf{e}}_{R}\right)$.

Example: [4.0; -3.5; 6.3]
Data Types: double
Complex Number Support: Yes

## az - Azimuth angle

scalar in range [-180,180]

Azimuth angle specified as a scalar in the closed range [-180,180]. Angle units are in degrees. To define the azimuth angle of a point on a sphere, construct a vector from the origin to the point. The azimuth angle is the angle in the $x y$-plane from the positive $x$-axis to the vector's orthogonal projection into the $x y$-plane. As examples, zero azimuth angle and zero elevation angle specify a point on the $x$-axis while an azimuth angle of $90^{\circ}$ and an elevation angle of zero specify a point on the $y$ axis.

Example: 45
Data Types: double

## el - Elevation angle

scalar in range [-90,90]
Elevation angle specified as a scalar in the closed range [-90,90]. Angle units are in degrees. To define the elevation of a point on the sphere, construct a vector from the origin to the point. The elevation angle is the angle from its orthogonal projection into the $x y$-plane to the vector itself. As examples, zero elevation angle defines the equator of the sphere and $\pm 90^{\circ}$ elevation define the north and south poles, respectively.

Example: 30
Data Types: double

## Output Arguments

## vr - Vector in Cartesian representation

3-by-1 column vector | 3-by-N matrix
Cartesian vector returned as a 3 -by- 1 column vector or 3 -by- $N$ matrix having the same dimensions as vs. Each column of $v r$ contains the three components of the vector in the right-handed $x, y, z$ basis.

## More About

## Spherical basis representation of vectors

Spherical basis vectors are a local set of basis vectors which point along the radial and angular directions at any point in space.

The spherical basis is a set of three mutually orthogonal unit vectors ( $\widehat{\mathbf{e}}_{a z}, \widehat{\mathbf{e}}_{e l}, \widehat{\mathbf{e}}_{R}$ ) defined at a point on the sphere. The first unit vector points along lines of azimuth at constant radius and elevation. The second points along the lines of elevation at constant azimuth and radius. Both are tangent to the surface of the sphere. The third unit vector points radially outward.

The orientation of the basis changes from point to point on the sphere but is independent of $R$ so as you move out along the radius, the basis orientation stays the same. The following figure illustrates the orientation of the spherical basis vectors as a function of azimuth and elevation:


For any point on the sphere specified by $a z$ and $e l$, the basis vectors are given by:

$$
\begin{aligned}
& \widehat{\mathbf{e}}_{\mathbf{a z}}=-\sin (a z) \widehat{\mathbf{i}}+\cos (a z) \widehat{\mathbf{j}} \\
& \widehat{\mathbf{e}}_{\mathbf{e l}}=-\sin (e l) \cos (a z) \widehat{\mathbf{i}}-\sin (e l) \sin (a z) \widehat{\mathbf{j}}+\cos (e l) \widehat{\mathbf{k}} \\
& \widehat{\mathbf{e}}_{\mathbf{R}}=\cos (e l) \cos (a z) \widehat{\mathbf{i}}+\cos (e l) \sin (a z) \widehat{\mathbf{j}}+\sin (e l) \widehat{\mathbf{k}} .
\end{aligned}
$$

Any vector can be written in terms of components in this basis as $\mathbf{v}=v_{a z} \widehat{\mathbf{e}}_{\mathbf{a z}}+v_{e l} \widehat{\mathbf{e}}_{\mathbf{e l}}+v_{R} \widehat{\mathbf{e}}_{\mathbf{R}}$. The transformations between spherical basis components and Cartesian components take the form

$$
\left[\begin{array}{l}
v_{x} \\
v_{y} \\
v_{z}
\end{array}\right]=\left[\begin{array}{ccc}
-\sin (a z) & -\sin (e l) \cos (a z) & \cos (e l) \cos (a z) \\
\cos (a z) & -\sin (e l) \sin (a z) & \cos (e l) \sin (a z) \\
0 & \cos (e l) & \sin (e l)
\end{array}\right]\left[\begin{array}{c}
v_{a z} \\
v_{e l} \\
v_{R}
\end{array}\right]
$$

and

$$
\left[\begin{array}{l}
v_{a z} \\
v_{e l} \\
v_{R}
\end{array}\right]=\left[\begin{array}{ccc}
-\sin (a z) & \cos (a z) & 0 \\
-\sin (e l) \cos (a z) & -\sin (e l) \sin (a z) & \cos (e l) \\
\cos (e l) \cos (a z) & \cos (e l) \sin (a z) & \sin (e l)
\end{array}\right]\left[\begin{array}{c}
v_{x} \\
v_{y} \\
v_{z}
\end{array}\right] .
$$

## Version History

Introduced in R2013a

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
Does not support variable-size inputs.
See Also
azelaxes|cart2sphvec

## spsmooth

Spatial smoothing

## Syntax

RSM $=\operatorname{spsmooth}(R, L)$
RSM $=\operatorname{spsmooth}(R, L, ' f b ')$

## Description

RSM $=\operatorname{spsmooth}(R, L)$ computes an averaged spatial covariance matrix, RSM, from the full spatial covariance matrix, R, using spatial smoothing (see Van Trees [1], p. 605). Spatial smoothing creates a smaller averaged covariance matrix over $L$ maximum overlapped subarrays. $L$ is a positive integer less than $N$. The resulting covariance matrix, RSM, has dimensions ( $N-L+1$ )-by- $(N-L+1)$. Spatial smoothing is useful when two or more signals are correlated.

RSM $=\operatorname{spsmooth}\left(R, L,{ }^{\prime} f b^{\prime}\right)$ computes an averaged covariance matrix and at the same time performing forward-backward averaging. This syntax can use any of the input arguments in the previous syntax.

## Examples

## Comparison of Smoothed and Nonsmoothed Covariance Matrices

Construct a 10 -element half-wavelength-spaced uniform line array receiving two plane waves arriving from $0^{\circ}$ and $-25^{\circ}$ azimuth. Both elevation angles are $0^{\circ}$. Assume the two signals are partially correlated. The SNR for each signal is 5 dB . The noise is spatially and temporally Gaussian white noise. First, create the spatial covariance matrix from the signal and noise. Then, solve for the number of signals, using rootmusicdoa. Next, perform spatial smoothing on the covariance matrix, using spsmooth, and solve for the signal arrival angles again using rootmusicdoa.

Set up the array and signals. Then, generate the spatial covariance matrix for the array from the signals and noise.

```
N = 10;
d = 0.5;
elementPos = (0:N-1)*d;
angles = [0 -25];
ac = [1 1/5];
scov = ac'*ac;
R = sensorcov(elementPos,angles,db2pow(-5),scov);
```

Solve for the arrival angles using the original covariance matrix.

```
Nsig = 2;
doa = rootmusicdoa(R,Nsig)
doa = 1×2
```


## $0.3603 \quad 79.2382$

The solved-for arrival angles are wrong - they do not agree with the known angles of arrival used to create the covariance matrix.

Next, solve for the arrival angles using a smoothed covariance matrix. Perform spatial smoothing to detect L-1 coherent signals. Choose $\mathrm{L}=3$.

```
Nsig = 2;
L = 2;
RSM = spsmooth(R,L);
doasm = rootmusicdoa(RSM,Nsig)
doasm = 1×2
```

    \(-25.0000 \quad 0.0000\)
    In this case, computed angles do agree with the known angles of arrival.

## Input Arguments

## R - Spatial covariance matrix

complex-valued positive-definite $N$-by- $N$ matrix.
Spatial covariance matrix, specified as a complex-valued, positive-definite $N$-by- $N$ matrix. In this matrix, $N$ represents the number of sensor elements.
Example: [ 4.3162, -0.2777-0.2337i; -0.2777 + 0.2337i , 4.3162]
Data Types: double
Complex Number Support: Yes

## L - Maximum number of overlapped subarrays

positive integer
Maximum number of overlapped subarrays, specified as a positive integer. The value $L$ must be less than the number of sensors, $N$.

Example: 2
Data Types: double

## Output Arguments

## RSM - Smoothed covariance matrix

complex-valued $M$-by- $M$ matrix
Smoothed covariance matrix, returned as a complex-valued, $M$-by- $M$ matrix. The dimension $M$ is given by $M=N-L+1$.

## Version History <br> Introduced in R2013a

## References

[1] Van Trees, H.L. Optimum Array Processing. New York, NY: Wiley-Interscience, 2002.

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
Does not support variable-size inputs.

## See Also

aictest|espritdoa|mdltest|rootmusicdoa

## steervec

Steering vector

## Syntax

```
sv = steervec(pos,ang)
sv = steervec(pos,ang,nqbits)
```


## Description

sv = steervec(pos,ang) returns the steering vector sv for each incoming plane wave or set of plane waves impinging on a sensor array. The steering vector represents the set of phase-delays for an incoming wave at each sensor element. The pos argument specifies the positions of the sensor array elements. The ang argument specifies the incoming wave arrival directions in terms of azimuth and elevation angles. The steering vector, sv, is an $N$-by- $M$ complex-valued matrix. In this matrix, $N$ represents the number of element positions in the sensor array while $M$ represents the number of incoming waves. Each column of sv contains the steering vector for the corresponding direction specified in ang. All elements in the sensor array are assumed to be isotropic.
sv = steervec(pos,ang, nqbits) returns quantized narrowband steering vector when the number of phase shifter bits is set to nqbits.

## Examples

## Line Array Steering Vector

Specify a uniform line array of five elements spaced 10 cm apart. Then, specify an incoming plane wave with a frequency of 1 GHz and an arrival direction of $45^{\circ}$ azimuth and $0^{\circ}$ elevation. Compute the steering vector of this wave.

```
elementPos = (0:.1:.4);
c = physconst('LightSpeed');
fc = 1e9;
lam = c/fc;
ang = [45;0];
sv = steervec(elementPos/lam,ang)
sv = 5x1 complex
    1.0000 + 0.0000i
    0.0887 + 0.9961i
    -0.9843 + 0.1767i
    -0.2633 - 0.9647i
    0.9376 - 0.3478i
```


## Quantized Line Array Steering Vector

Specify a uniform line array (ULA) containing five isotropic elements spaced 10 cm apart. Then, specify an incoming plane wave having a frequency of 1 GHz and an arrival direction of $45^{\circ}$ azimuth and $0^{\circ}$ elevation. Compute the steering vector of this wave. Quantize the steering vector to three bits.

```
elementPos = (0:.1:.4);
c = physconst('LightSpeed');
fc = 1e9;
lam = c/fc;
ang = [45;0];
sv = steervec(elementPos/lam,ang,3)
sv = 5x1 complex
    1.0000 + 0.0000i
    0.0000 + 1.0000i
    -1.0000 + 0.0000i
    -0.0000 - 1.0000i
    1.0000 + 0.0000i
```


## Input Arguments

## pos - Positions of array sensor elements

1-by- $N$ real-valued vector | 2 -by- $N$ real-valued matrix | 3 -by- $N$ real-valued matrix
Positions of the elements of a sensor array, specified as a 1 -by- $N$ vector, a 2 -by- $N$ matrix, or a 3 -by- $N$ matrix. In this vector or matrix, $N$ represents the number of elements of the array. Each column of pos represents the coordinates of an element. If pos is a 1 -by- $N$ vector, then it represents the $y$ coordinate of the sensor elements of a line array. The $x$ and $z$-coordinates are assumed to be zero. When pos is a 2 -by- $N$ matrix, it represents the ( $y, z$ )-coordinates of the sensor elements of a planar array. This array is assumed to lie in the $y z$-plane. The $x$-coordinates are assumed to be zero. When pos is a 3 -by- $N$ matrix, then the array can have an arbitrary shape. Sensor positions are in terms of signal wavelength.
Example: [0,0,0; 0.1,0.4,0.3; 1,1,1]
Data Types: double

## ang - Arrival directions of incoming signals

1-by-M real-valued vector | 2 -by- $M$ real-valued matrix
Arrival directions of incoming signals specified as a 1 -by- $M$ vector or a 2 -by- $M$ matrix, where $M$ is the number of incoming signals. If ang is a 2 -by- $M$ matrix, each column specifies the direction in azimuth and elevation of the incoming signal [az;el]. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$ and the elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$. The azimuth angle is the angle between the $x$ axis and the projection of the arrival direction vector onto the $x y$ plane. It is positive when measured from the $x$-axis toward the $y$-axis. The elevation angle is the angle between the arrival direction vector and $x y$-plane. It is positive when measured towards the $z$ axis. If ang is a 1 -by- $M$ vector, then it represents a set of azimuth angles with the elevation angles assumed to be zero. Angle units are specified in degrees.
Example: [45;0]
Data Types: double

## nqbits - Number of phase shifter quantization bits

0 (default) | non-negative integer
Number of bits used to quantize the phase shift in beamformer or steering vector weights, specified as a non-negative integer. A value of zero indicates that no quantization is performed.
Example: 5

## Output Arguments

## sv - Steering vector

$N$-by-M complex-valued matrix
Steering vector returned as an $N$-by- $M$ complex-valued matrix. In this matrix, $N$ represents the number of sensor elements of the array and $M$ represents the number of incoming plane waves. Each column of sv corresponds to the same column in ang.

## Version History

Introduced in R2013a

## References

[1] Van Trees, H.L. Optimum Array Processing. New York, NY: Wiley-Interscience, 2002.
[2] Johnson, Don H. and D. Dudgeon. Array Signal Processing. Englewood Cliffs, NJ: Prentice Hall, 1993.
[3] Van Veen, B.D. and K. M. Buckley. "Beamforming: A versatile approach to spatial filtering". IEEE ASSP Magazine, Vol. 5 No. 2 pp. 4-24.

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using MATLAB® Coder $^{\text {rm }}$.
Usage notes and limitations:
Does not support variable-size inputs.

## See Also

cbfweights |lcmvweights |mvdrweights | sensorcov| phased. SteeringVector

## stokes

Stokes parameters of polarized field

## Syntax

```
G = stokes(fv)
stokes(fv)
```


## Description

G = stokes(fv) returns the four Stokes parameters G of a polarized field or set of fields specified in fv. The field should be expressed in terms of linear polarization components. The expression of a field in terms of a two-row vector of linear polarization components is called the Jones vector formalism.
stokes(fv) displays the Stokes parameters corresponding to fv as points on the Poincare sphere.

## Examples

## Stokes Vector

Create a left circularly-polarized field. Convert it to a linear representation and compute the Stokes vector.
cfv = [2;0];
fv = circpol2pol(cfv);
G = stokes(fv)
G $=4 \times 1$
4.0000

0
0
4.0000

## Poincare Sphere

Display points on the Poincare sphere for a left circularly-polarized field and a $45^{\circ}$ linear polarized field.

```
fv = [sqrt(2)/2, 1; sqrt(2)/2*1i, 1];
G = stokes(fv)
G = 4\times2
```

            0
        2.0000
    1.0000
        0
    stokes(fv);

```

\section*{Poincare Sphere}


The point at the north pole represents the left circularly-polarized field. The point on the equator represents the \(45^{\circ}\) linear polarized field.

\section*{Input Arguments}
fv - Field vector in linear polarization representation or linear polarization ratio
1 -by- \(N\) complex-value row vector or 2 -by- \(N\) complex-value matrix
Field vector in its linear polarization representation specified as a 2 -by- \(N\) complex-valued matrix or in its linear polarization ratio representation specified as a 1-by- \(N\) complex-valued row vector. If \(f v\) is a matrix, each column of fv represents a field in the form [Eh;Ev], where Eh and Ev are its horizontal and vertical linear polarization components. The expression of a field in terms of a two-row vector of linear polarization components is called the Jones vector formalism. If \(f v\) is a vector, each entry in \(f v\) is contains the polarization ratio, Ev/Eh.

Example: [sqrt(2)/2*1i; 1]
Data Types: double
Complex Number Support: Yes

\section*{Output Arguments}

\section*{G - Stokes parameters}

4 -by- \(N\) matrix of Stokes parameters.
\(G\) contains the four Stokes parameters for each polarized field specified in \(f v\). The Stokes parameters are computed from combinations of intensities of the field:
- \(G_{0}\) describes the total intensity of the field.
- \(G_{1}\) describes the preponderance of horizontal linear polarization intensity over vertical linear polarization intensity.
- \(G_{2}\) describes the preponderance of \(+45^{\circ}\) linear polarization intensity over \(-45^{\circ}\) linear polarization intensity.
- \(G_{3}\) describes the preponderance of right circular polarization intensity over left circular polarization intensity.

\section*{Version History}

\section*{Introduced in R2013a}

\section*{References}
[1] Mott, H., Antennas for Radar and Communications, John Wiley \& Sons, 1992.
[2] Jackson, J.D. , Classical Electrodynamics, 3rd Edition, John Wiley \& Sons, 1998, pp. 299-302.
[3] Born, M. and E. Wolf, Principles of Optics, 7th Edition, Cambridge: Cambridge University Press, 1999, pp 25-32.

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder \(^{\text {TM }}\).
Usage notes and limitations:
- Does not support variable-size inputs.
- Supported only when output arguments are specified.

\section*{See Also}
circpol2pol|pol2circpol|polellip|polratio

\section*{stretchfreq2rng}

Convert frequency offset to range

\section*{Syntax}

R = stretchfreq2rng(FREQ, SLOPE,REFRNG)
R = stretchfreq2rng(FREQ,SLOPE,REFRNG, V)

\section*{Description}

R = stretchfreq2rng(FREQ,SLOPE,REFRNG) returns the range corresponding to the frequency offset FREQ. The computation assumes you obtained FREQ through stretch processing with a reference range of REFRNG. The sweeping slope of the linear FM waveform is SLOPE.
\(R=s t r e t c h f r e q 2 r n g(F R E Q, S L O P E, R E F R N G, V)\) specifies the propagation speed \(V\).

\section*{Examples}

\section*{Range Corresponding to Frequency Offset}

Calculate the range corresponding to a frequency offset of 2 kHz obtained from stretch processing. Assume the reference range is 5000 m and the linear FM waveform has a sweeping slope of \(2 \mathrm{GHz} / \mathrm{s}\).
\(r=s t r e t c h f r e q 2 r n g(2 e 3,2 e 9,5000)\)
\(r=4.8501 \mathrm{e}+03\)

\section*{Input Arguments}

\section*{FREQ - Frequency offset}
scalar | vector
Frequency offset in hertz, specified as a scalar or vector.
Data Types: double

\section*{SLOPE - Sweeping slope of the linear FM waveform}
nonzero scalar
Sweeping slope of the linear FM waveform, in hertz per second, specified as a nonzero scalar.
Data Types: double

\section*{REFRNG - Reference range}
scalar
Reference range in meters, specified as a scalar.
Data Types: double

\section*{V - Propagation speed}
physconst("LightSpeed") (default) | positive scalar
Propagation speed in meters per second, specified as a positive scalar.
Data Types: double

\section*{Output Arguments}

R - Range
scalar | vector
Range in meters, returned as a scalar or vector. \(R\) has the same dimensions as FREQ .

\section*{Version History}

Introduced in R2012a

\section*{References}
[1] Richards, M. A. Fundamentals of Radar Signal Processing. New York: McGraw-Hill, 2005.

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder \(^{\text {TM }}\).
Usage notes and limitations:
Does not support variable-size inputs.
```

See Also
phased.LinearFMWaveform|phased.StretchProcessor|ambgfun|beat2range |
range2beat|rdcoupling
Topics
"Range Estimation Using Stretch Processing"
"Stretch Processing"

```

\section*{systemp}

Receiver system-noise temperature

\section*{Syntax}

STEMP = systemp(NF)
STEMP = systemp(NF,REFTEMP)

\section*{Description}

STEMP = systemp (NF) calculates the effective system-noise temperature, STEMP, in kelvin, based on the noise figure, NF, in decibels. The reference temperature is 290 K .

STEMP = systemp (NF,REFTEMP) specifies the reference temperature.

\section*{Examples}

\section*{Compute System Noise Temperature}

Calculate the system noise temperature of a receiver with a 300 K reference temperature and a 5 dB noise figure.
\(\mathrm{T}=\operatorname{systemp}(5,300)\)
\(\mathrm{T}=948.6833\)

\section*{Input Arguments}

\author{
NF - Noise figure \\ nonnegative scalar
}

Noise figure in decibels, specified as a nonnegative scalar. The noise figure is the ratio of the actual output noise power in a receiver to the noise power output of an ideal receiver.

\section*{Data Types: double}

\section*{REFTEMP - Reference temperature}

290 (default) | nonnegative scalar
Reference temperature in kelvins, specified as a nonnegative scalar. The output of an ideal receiver has a white noise power spectral density that is approximately the Boltzmann constant times the reference temperature in kelvin.

Data Types: double

\section*{Output Arguments}

\section*{STEMP - Effective system-noise temperature}
nonnegative scalar

Effective system-noise temperature in kelvins, returned as a nonnegative scalar. The effective systemnoise temperature is REFTEMP*10^(NF/10).

\section*{Version History}

\section*{Introduced in R2011a}

\section*{References}
[1] Skolnik, M. Introduction to Radar Systems. New York: McGraw-Hill, 1980.

\section*{Extended Capabilities}

\section*{C/C++ Code Generation}

Generate C and \(\mathrm{C}++\) code using MATLAB® Coder \(^{\mathrm{TM}}\).
Usage notes and limitations:
Does not support variable-size inputs.

\section*{See Also}
noisepow | phased.ReceiverPreamp

\section*{taylortaperc}

Taylor nbar taper for arrays

\section*{Syntax}

W = taylortaperc(pos,diam)
W = taylortaperc(pos,diam,nbar)
W = taylortaperc(pos,diam, nbar,sll)
W = taylortaperc(pos,diam,nbar,sll,cpos)

\section*{Description}
\(\mathrm{W}=\) taylortaperc(pos,diam) returns the value of a Taylor n-bar taper, W , at sensor element positions specified by pos in a circular aperture having diameter diam.

W = taylortaperc(pos,diam, nbar) also specifies, nbar, the number of approximately constantlevel sidelobes next to the mainlobe.

W = taylortaperc(pos,diam,nbar,sll) also specifies the maximum sidelobe level, sll, relative to the mainlobe peak.
\(\mathrm{W}=\) taylortaperc(pos,diam,nbar,sll,cpos) also specifies the center of the array, cpos. Without this argument, the function sets the array center to the computed centroid of the array.

\section*{Examples}

\section*{Default Taylor Taper Circular Array}

Apply a Taylor nbar taper to a circular aperture array. Obtain the circular aperture by cropping a square uniform rectangular array into a circle. Let all the parameters remain at their default values: nbar is 4 and the sidelobe level is -30 . Let the center of the array be the centroid of the array elements. Plot the array power pattern at 300 MHz .

Create a square URA with a side length of 10 m . Set the element spacing to 0.5 m . The spacing is equal to one-half wavelength at this frequency.
```

fc = 300.0e6;
diam = 10.0;
d = 0.5;
nelem = ceil(diam/d);
pos = getElementPosition(phased.URA(nelem,d));

```

Use the phased. ConformalArray System object \({ }^{\text {TM }}\) to model a circular array. Create a circular array by removing all elements outside a radius one-half the side-length of the URA. Then apply the Taylor nbar tapering to the array.
```

pos(:,sum(pos.^2) > (diam/2)^2) = [];
antenna = phased.ConformalArray('ElementPosition',pos);
antenna.Taper = taylortaperc(pos,diam);

```

View the array.
viewArray(antenna,'ShowTaper',true)

\section*{Array Geometry}


Display the array power pattern as a function of azimuth angle.
clf
pattern(antenna,fc,-90:1:90,0,'CoordinateSystem','rectangular','Type','powerdb')


\section*{Taylor Taper Circular Array Specifying Nbar}

Apply a Taylor nbar taper to a circular aperture array. Create the circular aperture by cropping a square uniform rectangular array into a circle. Set the value of nbar to 2 . Let the sidelobe level assume a default value of -30. Let the center of the array be the centroid of the array elements. Plot the array power pattern at 300 MHz .

Create a square URA with a side length of 10 m . Set the element spacing to 0.5 m . The spacing is equal to one-half wavelength at this frequency.
```

fc = 300.0e6;
diam = 10.0;
d = 0.5;
nbar = 2;
nelem = ceil(diam/d);
pos = getElementPosition(phased.URA(nelem,d));

```

Use the phased. ConformalArray System object \({ }^{\text {TM }}\) to model a circular array. Create a circular array by removing all elements outside a radius one-half the side-length of the URA. Then apply the Taylor nbar tapering to the array.
```

pos(:,sum(pos.^2) > (diam/2)^2) = [];
antenna = phased.ConformalArray('ElementPosition',pos);
antenna.Taper = taylortaperc(pos,diam,nbar);

```

View the array.
viewArray(antenna,'ShowTaper',true)

\section*{Array Geometry}


Display the array power pattern as a function of azimuth angle.
clf
pattern(antenna,fc,-90:1:90,0,'CoordinateSystem','rectangular','Type','powerdb')


\section*{Taylor Taper Circular Array Specifying Sidelobe Level}

Apply a Taylor nbar taper to a circular aperture array. Create the circular aperture by cropping a square uniform rectangular array into a circle. Set the value of nbar to 4 . Set the sidelobe level to 25 . Let the center of the array be the centroid of the array elements. Plot the array power pattern at 300 MHz .

First, create a square URA with a side length of 10 m . Set the element spacing to 0.5 m . The spacing is equal to one-half wavelength at this frequency.
```

fc = 300.0e6;
diam = 10.0;
d = 0.5;
nbar = 2;
sll = -25;
nelem = ceil(diam/d);
pos = getElementPosition(phased.URA(nelem,d));

```

Use the phased.ConformalArray System object \({ }^{\mathrm{TM}}\) to model a circular array. Create a circular array by removing all elements outside a radius one-half the side-length of the URA. Then apply the Taylor nbar tapering to the array.
```

pos(:,sum(pos.^2) > (diam/2)^2) = [];
antenna = phased.ConformalArray('ElementPosition',pos);
antenna.Taper = taylortaperc(pos,diam,nbar,sll);

```

View the array.
viewArray(antenna,'ShowTaper',true)

\section*{Array Geometry}


Display the array power pattern as a function of azimuth angle.
clf
pattern(antenna,fc,-90:1:90,0,'CoordinateSystem','rectangular','Type','powerdb')


\section*{Taylor Taper Circular Array Specifying Array Center}

Apply a Taylor nbar taper to a circular aperture array. Create the circular aperture by cropping a square uniform rectangular array into a circle. Set the sidelobe level to -25 . Set the center of the array to the origin. Plot the array power pattern at 300 MHz .

Create a square URA with a side length of 10 m . Set the element spacing to 0.5 m . The spacing is equal to one-half wavelength at this frequency.
```

fc = 300.0e6;
diam = 10.0;
d = 0.5;
sll = -25;

```

Compute nbar from the sidelobe level.
\(A=\operatorname{acosh}\left(10^{\wedge}(-s l l / 20)\right) / p i ;\)
nbar \(=\operatorname{ceil}\left(2^{*} \mathrm{~A}^{\wedge} 2+0.5\right)\)
nbar = 4
Create the URA element positions.
```

cpos = [0;0;0];
nelem = ceil(diam/d);
pos = getElementPosition(phased.URA(nelem,d));

```

Use the phased.ConformalArray System object \({ }^{\mathrm{TM}}\) to model a circular array. Create a circular array by removing all elements outside a radius one-half the side-length of the URA. Then apply the Taylor nbar tapering to the array.
```

pos(:,sum(pos.^2) > (diam/2)^2) = [];

```
antenna = phased.ConformalArray('ElementPosition',pos);
antenna. Taper \(=\) taylortaperc(pos,diam,nbar,sll,cpos);

View the array.
viewArray(antenna,'ShowTaper',true)

\section*{Array Geometry}


Display the array power pattern as a function of azimuth angle.
```

clf
pattern(antenna,fc,-90:1:90,0,'CoordinateSystem','rectangular','Type','powerdb')

```


\section*{Input Arguments}

\section*{pos - Position of array elements}

2 -by- \(N\) real-valued matrix | 3-by- \(N\) real-valued matrix
Position of array elements, specified as a 2 -by- \(N\) or 3-by- \(N\) real-valued matrix where \(N\) is the number of elements. If pos is a 2 -by- \(N\) matrix, then all elements lie in the \(z=0\) plane. Each column specifies the position, \([x ; y]\), of the element. If pos is a 3 -by- \(N\) matrix, its columns represent the positions of array elements in \([\mathrm{x} ; \mathrm{y} ; \mathrm{z}]\) format. W is an \(N\)-by- 1 column vector containing the Taylor tapers. The 2-by- \(N\) form is designed for planar arrays although you can use the 3-by- \(N\) form and set the third row to zero. Position units are in meters.

Example: \([-5,-5,5,5 ;-5,5,5,-5]\)
Data Types: double

\section*{diam - Array diameter}
positive scalar
Array diameter, specified as a positive scalar. Diameter units are in meters.
Example: 15.5
Data Types: double

\section*{nbar - Number of nearly equal sidelobes}

4 (default) | positive integer

Number of nearly equal sidelobes on each side of the mainlobe, specified as a positive integer. Units are dimensionless.

Example: 3
Data Types: double

\section*{sll - Maximum sidelobe level}
-30.0 (default) | negative scalar
Maximum sidelobe, specified as a negative scalar. Sidelobe levels are referenced to the mainlobe. Units are in dB .

Example: -10.0
Data Types: double
cpos - Array center
array centroid (default) | real-valued 2-by-1 vector | real-valued 3-by-1 vector
Array center, specified as a real-valued 2-by-1 or 3-by-1 vector. Units are in meters. Use a 2 -by-1 vector when the element positions are specified as a 2 -by- \(N\) matrix. The default value is the computed centroid of all the array elements.
Example: [5;-10;3]
Data Types: double

\section*{Output Arguments}

\section*{W - Taylor weights}
real-valued \(N\)-by-1 column vector
Taylor weights, returned as a real-valued \(N\)-by- 1 column vector. \(N\) is the number of array elements. Units are dimensionless.

\section*{Algorithms}

\section*{Compute Minimum Value of \(\mathbf{N}\)-bar}

A useful guideline for choosing a value of nbar that meets the required sidelobe level (sll), as specified in the sll argument, is to satisfy the inequality
\[
\bar{n} \geq \frac{2}{\Pi^{2}}\left(\cosh ^{-1}\left(10^{-\frac{s l l}{20}}\right)\right)^{2}+0.5
\]

This is a recommendation and you may be able to use a smaller value.

\section*{Version History}

Introduced in R2016b

\section*{References}
[1] Taylor, T. "Design of Circular Aperture for Narrow Beamwidth and Low Sidelobes." IRE Trans. on Antennas and Propagation. Vol. 5, No. 1, January 1960, pp. 17-22.
[2] Van Trees, H. L. Optimal Array Processing: Part 4 of Detection, Estimation, and Modulation Theory. New York: A. J. Wiley \& Sons, Inc., 2002.
[3] Hansen, R. C. "Tables of Taylor Distributions for Circular Aperture Antennas." IRE Trans. on Antenna and Propagation.Vol. 8, No. 1, January 1960, pp. 23-26.
[4] Hansen, R. C. "Array Pattern Control and Synthesis." Proceedings of the IEEE. Vol. 80, No. 1, January 1992, pp. 141-151.

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® \({ }^{\circledR}\) Coder \(^{\mathrm{Tm}}\).
Usage notes and limitations:
Does not support variable-size inputs.

\section*{See Also}
taylorwin

\section*{time2range}

Convert propagation time to propagation distance

\section*{Syntax}
```

r = time2range(t)
r = time2range(t,c)

```

\section*{Description}
\(r=t i m e 2 r a n g e(t)\) returns the distance a signal propagates during \(t\) seconds. The propagation is assumed to be two-way, as in a monostatic radar system.
\(r=\) time 2 range \((t, c)\) specifies the signal propagation speed.

\section*{Examples}

\section*{Minimum Detectable Range for Specified Pulse Width}

Calculate the minimum detectable range for a monostatic radar system where the pulse width is 2 ms .
\(\mathrm{t}=2 \mathrm{e}-3\);
\(r=\) time2range(t)
\(r=2.9979 \mathrm{e}+05\)

\section*{Input Arguments}
t - Propagation time
array of positive numbers
Propagation time in seconds, specified as an array of positive numbers.
c - Signal propagation speed
speed of light (default) | positive scalar
Signal propagation speed, specified as a positive scalar in meters per second.
Data Types: double

\section*{Output Arguments}

\section*{r - Propagation distance}
array of positive numbers
Propagation distance in meters, returned as an array of positive numbers. The dimensions of \(r\) are the same as those of \(t\).

Data Types: double

\section*{Algorithms}

The function computes \(\mathrm{c} * \mathrm{t} / 2\).

\section*{Version History}

Introduced in R2012b

\section*{References}
[1] Skolnik, M. Introduction to Radar Systems, 3rd Ed. New York: McGraw-Hill, 2001.

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and \(\mathrm{C}++\) code using MATLAB® \({ }^{\circledR}\) Coder \(^{\mathrm{TM}}\).
Usage notes and limitations:
Does not support variable-size inputs.

\author{
See Also \\ range2time | range2bw | phased.FMCWWaveform
}

\section*{unigrid}

Uniform grid

\section*{Syntax}
```

grd = unigrid(startval,stp,endval)
grd = unigrid(startval,stp,endval,intype)

```

\section*{Description}
grd \(=\) unigrid(startval, stp, endval) returns a uniformly sampled grid from the closed interval [startval, endval], starting from startval. stp specifies the step size. This syntax is the same as calling startval:stp:endval.
grd = unigrid(startval,stp,endval,intype) specifies whether the interval is closed, or semi-open.

\section*{Examples}

\section*{Create Uniform Grids}

Create a uniform closed interval grid with a positive increment.
```

grid = unigrid(0,0.1,1);

```
grid(1)
ans \(=0\)
grid(end)
ans \(=1\)

Note that \(\operatorname{grid}(1)=0\) and \(\operatorname{grid}(\) end \()=1\).
Create a uniform grid with a semi-open interval.
```

grid = unigrid(0,0.1,1,'[)');

```
grid(1)
ans \(=0\)
grid(end)
ans \(=0.9000\)
In this case, grid(end) \(=0.9\)
Create a decreasing grid with a semi-open interval.
grid \(=\operatorname{unigrid}\left(1,-0.2,0, '[)^{\prime}\right)\)
grid \(=1 \times 5\)
1.0000
0.8000
0.6000
0.4000
0.2000

\section*{Input Arguments}
startval - Start value
real scalar
Start value of the uniform grid, specified as a real scalar.
Data Types: double
endval - End value
real scalar
End value of the uniform grid, specified as a real scalar.
Data Types: double
stp - Step size
real scalar
Step size, specified as a real scalar
Data Types: double

\section*{intype - Interval type}
" []" (default) | " [)"
Interval type, specified as " []", which represents a closed interval, or " [ ) ", which represents a semi-open interval. Specifying a closed interval does not always cause grd to contain the value endval. The inclusion of endval in a closed interval also depends on the step size stp.
Data Types: char | string

\section*{Version History}

\section*{Introduced in R2011a}

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and C++ code using MATLAB® Coder \(^{\mathrm{Tm}}\).
Usage notes and limitations:
Does not support variable-size inputs.

\section*{See Also}
linspace | val2ind

\section*{uv2azel}

Convert \(u / v\) coordinates to azimuth/elevation angles

\section*{Syntax}

AzEl = uv2azel(UV)

\section*{Description}
\(\mathrm{AzEl}=\mathrm{uv} 2 \mathrm{azel}(\mathrm{UV})\) converts the \(u / v\) space on page 2-482 coordinates to their corresponding azimuth/elevation angle on page 2-483 pairs.

\section*{Examples}

\section*{Conversion of U/V Coordinates to AzEI}

Find the corresponding azimuth/elevation representation for \(u=0.5\) and \(v=0\).
```

azel = uv2azel([0.5; 0])

```
azel \(=2 \times 1\)
30.0000

0

\section*{Input Arguments}

\section*{UV - Angle in u/v space}
two-row matrix
Angle in \(u / v\) space, specified as a two-row matrix. Each column of the matrix represents a pair of coordinates in the form [ \(u ; v\) ]. Each coordinate is between -1 and 1, inclusive. Also, each pair must satisfy \(u^{2}+v^{2} \leq 1\).
Data Types: double

\section*{Output Arguments}

\section*{AzEl - Azimuth/elevation angle pairs}
two-row matrix
Azimuth and elevation angles, returned as a two-row matrix. Each column of the matrix represents an angle in degrees, in the form [azimuth; elevation]. The matrix dimensions of AzEl are the same as those of UV.

\section*{More About}

\section*{U/V Space}

The \(u / v\) coordinates for the positive hemisphere \(x \geq 0\) can be derived from the phi and theta angles on page 2-482.

The relation between the two coordinates is
\[
\begin{aligned}
& u=\sin \theta \cos \phi \\
& v=\sin \theta \sin \phi
\end{aligned}
\]

In these expressions, \(\varphi\) and \(\theta\) are the phi and theta angles, respectively.
To convert azimuth and elevation to \(u\) and \(v\) use the transformation
\[
\begin{aligned}
& u=\text { coselsinaz } \\
& v=\text { sinel }
\end{aligned}
\]
which is valid only in the range \(a b s(a z) \leq=90\).
The values of \(u\) and \(v\) satisfy the inequalities
\[
\begin{aligned}
& -1 \leq u \leq 1 \\
& -1 \leq v \leq 1 \\
& u^{2}+v^{2} \leq 1
\end{aligned}
\]

Conversely, the phi and theta angles can be written in terms of \(u\) and \(v\) using
\[
\begin{aligned}
\tan \phi & =v / u \\
\sin \theta & =\sqrt{u^{2}+v^{2}}
\end{aligned}
\]

The azimuth and elevation angles can also be written in terms of \(u\) and \(v\) :
\[
\begin{aligned}
& \sin e l=v \\
& \tan a z=\frac{u}{\sqrt{1-u^{2}-v^{2}}}
\end{aligned}
\]

\section*{Phi Angle, Theta Angle}

The phi angle \((\varphi)\) is the angle from the positive \(y\)-axis to the vector's orthogonal projection onto the \(y z\) plane. The angle is positive toward the positive \(z\)-axis. The phi angle is between 0 and 360 degrees. The theta angle \((\theta)\) is the angle from the \(x\)-axis to the vector itself. The angle is positive toward the \(y z\) plane. The theta angle is between 0 and 180 degrees.

The figure illustrates phi and theta for a vector that appears as a green solid line.


The coordinate transformations between \(\varphi / \theta\) and \(a z / e l\) are described by the following equations
\[
\begin{aligned}
& \sin e l=\sin \phi \sin \theta \\
& \tan a z=\cos \phi \tan \theta \\
& \cos \theta=\operatorname{cosel} \cos a z \\
& \tan \phi=\tan e l / \sin a z
\end{aligned}
\]

\section*{Azimuth Angle, Elevation Angle}

The azimuth angle of a vector is the angle between the \(x\)-axis and the orthogonal projection of the vector onto the \(x y\) plane. The angle is positive in going from the \(x\) axis toward the \(y\) axis. Azimuth angles lie between -180 and 180 degrees. The elevation angle is the angle between the vector and its orthogonal projection onto the \(x y\)-plane. The angle is positive when going toward the positive \(z\)-axis from the xy plane. By default, the boresight direction of an element or array is aligned with the positive \(x\)-axis. The boresight direction is the direction of the main lobe of an element or array.

Note The elevation angle is sometimes defined in the literature as the angle a vector makes with the positive \(z\)-axis. The MATLAB and Phased Array System Toolbox products do not use this definition.

This figure illustrates the azimuth angle and elevation angle for a vector shown as a green solid line.


\section*{Version History}

Introduced in R2012a

\section*{Extended Capabilities}

C/C++ Code Generation
Generate C and C++ code using MATLAB® \({ }^{\circledR}\) Coder \(^{\text {TM }}\).
Usage notes and limitations:

Does not support variable-size inputs.

\section*{See Also}
azel2uv

\section*{Topics}
"Spherical Coordinates"

\section*{uv2azelpat}

Convert radiation pattern from \(\mathrm{u} / \mathrm{v}\) form to azimuth/elevation form

\section*{Syntax}
```

pat_azel = uv2azelpat(pat_uv,u,v)
pat_azel = uv2azelpat(pat_uv,u,v,az,el)
[pat_azel,az_pat,el_pat] = uv2azelpat(

```
\(\qquad\)
``` )
```


## Description

pat_azel = uv2azelpat(pat_uv,u,v) expresses the antenna radiation pattern pat_azel in azimuth/elevation angle on page 2-491 coordinates instead of $u / v$ space on page 2-490 coordinates. pat_uv samples the pattern at $u$ angles in $u$ and $v$ angles in $v$. The pat_azel matrix uses a default grid that covers azimuth values from -90 to 90 degrees and elevation values from - 90 to 90 degrees. In this grid, pat_azel is uniformly sampled with a step size of 1 for azimuth and elevation. The function interpolates to estimate the response of the antenna at a given direction.
pat_azel = uv2azelpat(pat_uv,u,v,az,el) uses vectors az and el to specify the grid at which to sample pat_azel. To avoid interpolation errors, az should cover the range [-90, 90] and el should cover the range [-90, 90].
[pat_azel,az_pat,el_pat] = uv2azelpat( $\qquad$ ) returns vectors containing the azimuth and elevation angles at which pat_azel samples the pattern, using any of the input arguments in the previous syntaxes.

## Examples

## Convert Radiation Pattern

Convert a radiation pattern to azimuth/elevation form with the angles spaced $1^{\circ}$ apart.
Define the pattern in terms of $u$ and $v$. Because $u$ and $v$ values outside the unit circle are not physical, set the pattern values in this region to zero.

```
u = -1:0.01:1;
v = -1:0.01:1;
[u_grid,v_grid] = meshgrid(u,v);
pat_uv = sqrt(1 - u_grid.^2 - v_grid.^2);
pat_uv(hypot(u_grid,v_grid) >= \overline{1})=0;
```

Convert the pattern to azimuth/elevation space.

```
pat_azel = uv2azelpat(pat_uv,u,v);
```

Plot Converted Radiation Pattern
Convert a radiation pattern to azimuth/elevation form with the angles spaced $1^{\circ}$ apart.

Define the pattern in terms of $u$ and $v$. Because $u$ and $v$ values outside the unit circle are not physical, set the pattern values in this region to zero.

```
u = -1:0.01:1;
v = -1:0.01:1;
[u_grid,v_grid] = meshgrid(u,v);
pat_uv = sqrt(1 - u_grid.^2 - v_grid.^2);
pat_uv(hypot(u_grid,v_grid) >= \overline{1})=0;
```

Convert the pattern to azimuth/elevation space. Store the azimuth and elevation angles for plotting.

```
[pat_azel,az,el] = uv2azelpat(pat_uv,u,v);
```

Plot the pattern.

```
H = surf(az,el,pat_azel);
H.LineStyle = 'none';
xlabel('Azimuth (degrees)')
ylabel('Elevation (degrees)')
zlabel('Pattern')
```



## Convert Radiation Pattern Using Specific Azimuth/Elevation Values

Convert a radiation pattern to azimuth/elevation form, with the angles spaced $5^{\circ}$ apart.

Define the pattern in terms of $u$ and $v$. Because $u$ and $v$ values outside the unit circle are not physical, set the pattern values in this region to zero.
$\mathrm{u}=-1: 0.01: 1$;
v = -1:0.01:1;
[u_grid,v_grid] = meshgrid(u,v);

pat_uv(hypot(u_grid,v_grid) >= 1) = 0;
Define the set of azimuth and elevation angles at which to sample the pattern. Then convert the pattern.
az = -90:5:90;
el = -90:5:90;
pat_azel = uv2azelpat(pat_uv,u,v,az,el);
Plot the pattern.
H = surf(az,el,pat_azel);
H.LineStyle = 'none';
xlabel('Azimuth (degrees)')
ylabel('Elevation (degrees)')
zlabel('Pattern')


## Input Arguments

## pat_uv - Antenna radiation pattern in u/v form

Q-by-P matrix
Antenna radiation pattern in $u / v$ form, specified as a Q-by-P matrix. pat_uv samples the 3-D
magnitude pattern in decibels in terms of $u$ and $v$ coordinates. P is the length of the u vector and Q is the length of the $v$ vector.
Data Types: double
u-u coordinates
vector of length $P$
$u$ coordinates at which pat_uv samples the pattern, specified as a vector of length P. Each coordinate is between -1 and 1.
Data Types: double

## v - v coordinates

vector of length Q
$v$ coordinates at which pat_uv samples the pattern, specified as a vector of length Q. Each coordinate is between -1 and 1 .
Data Types: double

## az - Azimuth angles

[-90:90] (default) | vector of length L
Azimuth angles at which pat_azel samples the pattern, specified as a vector of length L. Each azimuth angle is in degrees, between -90 and 90 . Such azimuth angles are in the hemisphere for which $u$ and $v$ are defined.
Data Types: double

## el - Elevation angles

[-90:90] (default) | vector of length M
Elevation angles at which pat_azel samples the pattern, specified as a vector of length M. Each elevation angle is in degrees, between -90 and 90 .
Data Types: double

## Output Arguments

## pat_azel - Antenna radiation pattern in azimuth-elevation coordinates <br> real-valued $M$-by- $L$ matrix

Antenna radiation pattern in azimuth-elevation coordinates, returned as a real-valued $M$-by- $L$ matrix. pat_azel represents the magnitude pattern. $L$ is the length of the az_pat vector, and $M$ is the length of the el_pat vector. Units are in dB .

## az_pat - Azimuth angles

real-valued length- $L$ vector

Azimuth angles at which the pat_azel output pattern is sampled, returned as a real-valued length- $L$ vector. Units are in degrees.

## el_pat - Elevation angles

real-valued length- $M$ vector
Elevation angles at which the pat_azel output pattern is sampled, returned as a real-valued length$M$ vector. Units are in degrees.

## More About

## U/V Space

The $u$ and $v$ coordinates are the direction cosines of a vector with respect to the $y$-axis and $z$-axis, respectively.

The $u / v$ coordinates for the hemisphere $x \geq 0$ are derived from the phi and theta angles on page 2490, as follows:

$$
\begin{aligned}
& u=\sin \theta \cos \phi \\
& v=\sin \theta \sin \phi
\end{aligned}
$$

In these expressions, $\varphi$ and $\theta$ are the phi and theta angles, respectively.
To convert azimuth and elevation to $u$ and $v$ use the transformation

$$
\begin{aligned}
& u=\text { coselsinaz } \\
& v=\text { sinel }
\end{aligned}
$$

which is valid only in the range $a b s(a z) \leq=90$.
The values of $u$ and $v$ satisfy the inequalities

$$
\begin{aligned}
& -1 \leq u \leq 1 \\
& -1 \leq v \leq 1 \\
& u^{2}+v^{2} \leq 1
\end{aligned}
$$

Conversely, the phi and theta angles can be written in terms of $u$ and $v$ using

$$
\begin{aligned}
\tan \phi & =v / u \\
\sin \theta & =\sqrt{u^{2}+v^{2}}
\end{aligned}
$$

The azimuth and elevation angles can also be written in terms of $u$ and $v$ :

$$
\begin{aligned}
& \text { sinel }=v \\
& \tan a z=\frac{u}{\sqrt{1-u^{2}-v^{2}}}
\end{aligned}
$$

## Phi Angle, Theta Angle

The phi angle $(\varphi)$ is the angle from the positive $y$-axis to the vector's orthogonal projection onto the $y z$ plane. The angle is positive toward the positive $z$-axis. The phi angle is between 0 and 360 degrees.

The theta angle $(\theta)$ is the angle from the $x$-axis to the vector itself. The angle is positive toward the $y z$ plane. The theta angle is between 0 and 180 degrees.

The figure illustrates phi and theta for a vector that appears as a green solid line.


The coordinate transformations between $\varphi / \theta$ and $a z / e l$ are described by the following equations

$$
\begin{aligned}
& \sin e l=\sin \phi \sin \theta \\
& \tan a z=\cos \phi \tan \theta \\
& \cos \theta=\operatorname{cosel} \cos a z \\
& \tan \phi=\operatorname{tanel} / \sin a z
\end{aligned}
$$

## Azimuth Angle, Elevation Angle

The azimuth angle of a vector is the angle between the $x$-axis and the orthogonal projection of the vector onto the $x y$ plane. The angle is positive in going from the $x$ axis toward the $y$ axis. Azimuth
angles lie between -180 and 180 degrees. The elevation angle is the angle between the vector and its orthogonal projection onto the $x y$-plane. The angle is positive when going toward the positive $z$-axis from the $x y$ plane. By default, the boresight direction of an element or array is aligned with the positive $x$-axis. The boresight direction is the direction of the main lobe of an element or array.

Note The elevation angle is sometimes defined in the literature as the angle a vector makes with the positive $z$-axis. The MATLAB and Phased Array System Toolbox products do not use this definition.

This figure illustrates the azimuth angle and elevation angle for a vector shown as a green solid line.


## Version History <br> Introduced in R2012a

## Extended Capabilities

## C/C++ Code Generation

Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
Does not support variable-size inputs.

## See Also

phased.CustomAntennaElement | uv2azel|azel2uv |azel2uvpat

## Topics

"Spherical Coordinates"

## uv2phitheta

Convert u/v coordinates to phi/theta angles

## Syntax

PhiTheta = uv2phitheta(UV)

## Description

PhiTheta $=$ uv2phitheta(UV) converts the $u / v$ space on page 2-495 coordinates to their corresponding phi/theta angle on page 2-495 pairs.

## Examples

## Conversion of U/V Coordinates

Find the corresponding $\varphi / \theta$ representation for $u=0.5$ and $v=0$.
PhiTheta $=$ uv2phitheta([0.5; 0])
PhiTheta $=2 \times 1$

0
30.0000

## Input Arguments

## UV - Angle in u/v space

two-row matrix
Angle in $u / v$ space, specified as a two-row matrix. Each column of the matrix represents a pair of coordinates in the form [ $u ; v$ ]. Each coordinate is between -1 and 1, inclusive. Also, each pair must satisfy $u^{2}+v^{2} \leq 1$.
Data Types: double

## Output Arguments

## PhiTheta - Phi/theta angle pairs

two-row matrix
Phi and theta angles, returned as a two-row matrix. Each column of the matrix represents an angle in degrees, in the form [phi; theta]. The matrix dimensions of PhiTheta are the same as those of UV.

## More About

## U/V Space

The $u / v$ coordinates for the positive hemisphere $x \geq 0$ can be derived from the phi and theta angles on page 2-495.

The relation between the two coordinates is

$$
\begin{aligned}
& u=\sin \theta \cos \phi \\
& v=\sin \theta \sin \phi
\end{aligned}
$$

In these expressions, $\varphi$ and $\theta$ are the phi and theta angles, respectively.
To convert azimuth and elevation to $u$ and $v$ use the transformation

$$
\begin{aligned}
& u=\operatorname{cosel} \sin a z \\
& v=\text { sinel }
\end{aligned}
$$

which is valid only in the range $a b s(a z) \leq=90$.
The values of $u$ and $v$ satisfy the inequalities

$$
\begin{aligned}
& -1 \leq u \leq 1 \\
& -1 \leq v \leq 1 \\
& u^{2}+v^{2} \leq 1
\end{aligned}
$$

Conversely, the phi and theta angles can be written in terms of $u$ and $v$ using

$$
\begin{aligned}
& \tan \phi=v / u \\
& \sin \theta=\sqrt{u^{2}+v^{2}}
\end{aligned}
$$

The azimuth and elevation angles can also be written in terms of $u$ and $v$ :

$$
\begin{aligned}
& \text { sinel }=v \\
& \tan a z=\frac{u}{\sqrt{1-u^{2}-v^{2}}}
\end{aligned}
$$

## Phi Angle, Theta Angle

The phi angle $(\varphi)$ is the angle from the positive $y$-axis to the vector's orthogonal projection onto the $y z$ plane. The angle is positive toward the positive $z$-axis. The phi angle is between 0 and 360 degrees. The theta angle $(\theta)$ is the angle from the $x$-axis to the vector itself. The angle is positive toward the $y z$ plane. The theta angle is between 0 and 180 degrees.

The figure illustrates phi and theta for a vector that appears as a green solid line.


The coordinate transformations between $\varphi / \theta$ and $a z / e l$ are described by the following equations

$$
\begin{aligned}
& \sin e l=\sin \phi \sin \theta \\
& \tan a z=\cos \phi \tan \theta \\
& \cos \theta=\operatorname{cose} l \cos a z \\
& \tan \phi=\tan e l / \sin a z
\end{aligned}
$$

## Version History

Introduced in R2012a

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
Does not support variable-size inputs.

## See Also

phitheta2uv

## Topics

"Spherical Coordinates"

## uv2phithetapat

Convert radiation pattern from $\mathrm{u} / \mathrm{v}$ form to phi/theta form

## Syntax

```
pat_phitheta = uv2phithetapat(pat_uv,u,v)
pat_phitheta = uv2phithetapat(pat_uv,u,v,phi,theta)
[pat_phitheta,phi_pat,theta_pat] = uv2phithetapat(
```

$\qquad$ )

## Description

pat_phitheta $=$ uv2phithetapat(pat_uv,u,v) expresses the antenna radiation pattern pat_phitheta in $\varphi / \theta$ angle on page 2-502 coordinates instead of $u / v$ space on page 2-502 coordinates. pat_uv samples the pattern at $u$ angles in $u$ and $v$ angles in v. The pat_phitheta matrix uses a default grid that covers $\varphi$ values from 0 to 360 degrees and $\theta$ values from 0 to 90 degrees. In this grid, pat_phitheta is uniformly sampled with a step size of 1 for $\varphi$ and $\theta$. The function interpolates to estimate the response of the antenna at a given direction.
pat_phitheta $=u v 2$ phithetapat(pat_uv,u,v,phi,theta) uses vectors phi and theta to specify the grid at which to sample pat_phitheta. To avoid interpolation errors, phi should cover the range [ 0,360 ], and theta should cover the range [ 0,90 ].
[pat_phitheta, phi_pat,theta_pat] = uv2phithetapat( $\qquad$ ) returns vectors containing the $\varphi$ and $\theta$ angles at which pat_phitheta samples the pattern, using any of the input arguments in the previous syntaxes.

## Examples

## Convert Radiation Pattern to $\boldsymbol{\varphi}-\boldsymbol{\theta}$

Convert a radiation pattern to $\varphi-\theta$ space with the angles spaced $1^{\circ}$ apart.
Define the pattern in terms of $u$ and $v$. Because $u$ and $v$ values outside the unit circle are not physical, set the pattern values in this region to zero.

```
u = -1:0.01:1;
v = -1:0.01:1;
[u_grid,v_grid] = meshgrid(u,v);
pat_uv = sqrt(1 - u_grid.^2 - v_grid.^2);
pat_uv(hypot(u_grid,v_grid) >= \overline{1}) = 0;
```

Convert the pattern to $\varphi-\theta$ space.

```
[pat_phitheta,phi,theta] = uv2phithetapat(pat_uv,u,v);
```


## Plot Converted Radiation Pattern

Convert a radiation pattern to $\phi-\theta$ space with the angles spaced one degree apart.

Define the pattern in terms of $u$ and $v$. For values outside the unit circle, $u$ and $v$ are undefined, and the pattern value is 0 .

```
u = -1:0.01:1;
v = -1:0.01:1;
[u_grid,v_grid] = meshgrid(u,v);
pat_uv = sqrt(1 - u_grid.^2 - v_grid.^2);
pat_uv(hypot(u_grid,v_grid) >= \overline{1})=0;
```

Convert the pattern to $\phi-\theta$ space. Store the $\phi$ and $\theta$ angles for use in plotting.
[pat_phitheta,phi,theta] = uv2phithetapat(pat_uv,u,v);
Plot the result.
H = surf(phi, theta, pat_phitheta);
H.LineStyle = 'none';
xlabel('Phi (degrees)');
ylabel('Theta (degrees)');
zlabel('Pattern');


## Convert Radiation Pattern Using Specific Phi/Theta Values

Convert a radiation pattern to $\phi-\theta$ space with the angles spaced five degrees apart.

Define the pattern in terms of $u$ and $v$. For values outside the unit circle, $u$ and $v$ are undefined, and the pattern value is 0 .

```
u = -1:0.01:1;
v = -1:0.01:1;
[u_grid,v_grid] = meshgrid(u,v);
pat_uv = sqrt(1 - u_grid.^2 - v_grid.^2);
pat_uv(hypot(u_grid,v_grid) >= 1) = 0;
```

Define the set of $\phi$ and $\theta$ angles at which to sample the pattern. Then, convert the pattern.
phi = 0:5:360;
theta = 0:5:90;
pat_phitheta = uv2phithetapat(pat_uv,u,v,phi,theta);
Plot the result.
$H=\operatorname{surf}\left(p h i, t h e t a, p a t \_p h i t h e t a\right) ;$
H.LineStyle = 'none';
xlabel('Phi (degrees)');
ylabel('Theta (degrees)');
zlabel('Pattern');


## Input Arguments

## pat_uv - Antenna radiation pattern in u/v form

Q-by-P matrix

Antenna radiation pattern in $u / v$ form, specified as a Q-by-P matrix. pat_uv samples the 3-D magnitude pattern in decibels, in terms of $u$ and $v$ coordinates. P is the length of the u vector, and Q is the length of the $v$ vector.
Data Types: double
u-u coordinates
vector of length $P$
$u$ coordinates at which pat_uv samples the pattern, specified as a vector of length P. Each coordinate is between -1 and 1 .
Data Types: double
v - v coordinates
vector of length Q
$v$ coordinates at which pat_uv samples the pattern, specified as a vector of length Q. Each coordinate is between -1 and 1 .
Data Types: double
phi - Phi angles
[0:360] (default) | vector of length L
Phi angles at which pat_phitheta samples the pattern, specified as a vector of length L. Each $\varphi$ angle is in degrees, between 0 and 360 .
Data Types: double

## theta - Theta angles

[0:90] (default) | vector of length M
Theta angles at which pat_phitheta samples the pattern, specified as a vector of length M. Each $\theta$ angle is in degrees, between 0 and 90 . Such $\theta$ angles are in the hemisphere for which $u$ and $v$ are defined.

Data Types: double

## Output Arguments

pat_phitheta - Antenna radiation pattern in phi-theta coordinates
real-valued $M$-by-L matrix
Antenna radiation pattern in phi-theta coordinates, returned as a real-valued $M$-by- $L$ matrix. pat_phitheta represents the magnitude pattern. $L$ is the length of the phi_pat vector, and $M$ is the length of the theta_pat vector. Units are in dB .
phi_pat - Phi angles
real-valued length- $L$ vector
Phi angles at which the pat_phitheta pattern is sampled, returned as a real-valued length $L$ vector. Units are in degrees.

## theta_pat - Theta angles

real-valued length- $M$ vector

Theta angles at which the pat_phitheta pattern is sampled, returned as a real-valued length- $M$ vector. Units are in degrees.

## More About

## U/V Space

The $u$ and $v$ coordinates are the direction cosines of a vector with respect to the $y$-axis and $z$-axis, respectively.

The $u / v$ coordinates for the hemisphere $x \geq 0$ are derived from the phi and theta angles on page 2502, as follows:

$$
\begin{aligned}
& u=\sin \theta \cos \phi \\
& v=\sin \theta \sin \phi
\end{aligned}
$$

In these expressions, $\varphi$ and $\theta$ are the phi and theta angles, respectively.
To convert azimuth and elevation to $u$ and $v$ use the transformation

$$
\begin{aligned}
& u=\text { coselsinaz } \\
& v=\text { sinel }
\end{aligned}
$$

which is valid only in the range $a b s(a z) \leq=90$.
The values of $u$ and $v$ satisfy the inequalities

$$
\begin{aligned}
& -1 \leq u \leq 1 \\
& -1 \leq v \leq 1 \\
& u^{2}+v^{2} \leq 1
\end{aligned}
$$

Conversely, the phi and theta angles can be written in terms of $u$ and $v$ using

$$
\begin{aligned}
& \tan \phi=v / u \\
& \sin \theta=\sqrt{u^{2}+v^{2}}
\end{aligned}
$$

The azimuth and elevation angles can also be written in terms of $u$ and $v$ :

$$
\begin{aligned}
& \text { sinel }=v \\
& \tan a z=\frac{u}{\sqrt{1-u^{2}-v^{2}}}
\end{aligned}
$$

## Phi Angle, Theta Angle

The phi angle $(\varphi)$ is the angle from the positive $y$-axis to the vector's orthogonal projection onto the $y z$ plane. The angle is positive toward the positive $z$-axis. The phi angle is between 0 and 360 degrees. The theta angle $(\theta)$ is the angle from the $x$-axis to the vector itself. The angle is positive toward the $y z$ plane. The theta angle is between 0 and 180 degrees.

The figure illustrates phi and theta for a vector that appears as a green solid line.


The coordinate transformations between $\varphi / \theta$ and $a z / e l$ are described by the following equations

$$
\begin{aligned}
& \sin e l=\sin \phi \sin \theta \\
& \tan a z=\cos \phi \tan \theta \\
& \cos \theta=\cos e l \cos a z \\
& \tan \phi=\tan e l / \sin a z
\end{aligned}
$$

## Version History

Introduced in R2012a

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
Does not support variable-size inputs.

```
See Also
phased.CustomAntennaElement |uv2phitheta|phitheta2uv|phitheta2uvpat
Topics
"Spherical Coordinates"
```


## val2ind

Uniform grid index

## Syntax

```
indx = val2ind(val,delta)
indx = val2ind(val,delta,startval)
```


## Description

indx = val2ind(val, delta) returns the index of the value val in a uniform grid with a spacing between elements of delta. The first element of the uniform grid is zero. If val does not correspond exactly to an element of the grid, the next element is returned. If val is a vector, then indx is a vector of the same size.
indx = val2ind(val, delta, startval) specifies the starting value of the uniform grid as startval.

## Examples

## Compute Index of Value in Grid

Find the index corresponding to 0.0001 in a uniform grid with 1 MHz sampling rate.

```
fs = 1e6;
indx = val2ind(0.0001,1/fs)
indx = 101
```


## Compute Indices of Values in Grid

Find the indices corresponding to a vector of values in a uniform grid with 1 kHz sampling rate. Values are not divisible by $1 / \mathrm{fs}$.

```
fs = 1.0e3;
values =[0.0095 0.0125 0.0225];
indx = val2ind(values,1/fs)
indx = 1\times3
    11 14 24
```


## Input Arguments

val - Data values
scalar | vector

Data values, specified as a scalar or vector.
Example:[3.4 6.3 9.8 12.1]
Data Types: double
delta - Spacing between grid elements
positive scalar
Spacing between grid elements, specified as a positive scalar.
Example: 1/1e3
Data Types: double

## startval - Starting value of the uniform grid

0 (default) | real scalar
Starting value of the uniform grid, specified as a scalar startval must be smaller than or equal to the minimum value in val.

Data Types: double

## Version History

Introduced in R2011a

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:
Does not support variable-size inputs.

## See Also

find | sub2ind | unigrid
Topics
"Array Indexing"

## waterfill

Waterfill MIMO power distribution

## Syntax

```
P = waterfill(Pt,Pn)
waterfill(Pt,Pn)
```


## Description

$\mathrm{P}=$ waterfill(Pt,Pn) optimally distributes the total transmitted power, Pt , among multiple channels to maximize channel capacity. The argument Pn represents the noise in each channel. The function can optimize independent subcarriers simultaneously.
waterfill(Pt,Pn) displays a waterfill diagram.

## Examples

## Compute Distributed Power Using Waterfill

Using the waterfill algorithm, compute the distributed power per channel for two subcarriers. There are four channels per subcarrier.

Specify the same total power for both subcarriers using a scalar value.
Pt = 10;
Specify the noise power. The rows correspond to the subcarriers and the columns to the channels.

```
Pn = [1 4 6 3; 5 4 3 6];
P = waterfill(Pt,Pn)
P = 2×4
    5 2 0 3
    2 3
```

Now, specify a different total power for each subcarrier.

```
Pt = [10,5];
P = waterfill(Pt,Pn)
P = 2×4
    5.0000 2.0000 0 3.0000
    0.6667 1.6667 2.6667 0
```


## Plot Distributed Power Using Waterfill

Using the waterfill algorithm, plot the distributed power per channel for two subcarriers. There are four channels per subcarrier.

Specify a different total power for each subcarrier.
Pt = [10,5];
Specify the noise power. The rows correspond to the subcarriers and the columns to the channels.
Pn = [1 463 3; 546 6;
Display the waterfill plot.
waterfill(Pt,Pn)


## Input Arguments

## Pt - Total transmitted power

positive scalar | positive-valued $L$-element row or column vector
Total transmitted power per subcarrier, specified as a positive-valued $L$-element row or column vector where $L$ is the number of subcarriers. When Pt is a scalar, all subcarriers have the same power. When Pt is a vector, the total power in a subcarriers is given by the corresponding element in Pt. Units are arbitrary.

Example: [20 30]
Data Types: double

## Pn - Channel noise power

positive-valued $N$-element row or column vector | positive-valued $L$-by- $N$-element matrix
Channel noise powers, specified as a positive-valued $N$-element row or column vector or a positivevalued $L$-by- $N$-element matrix. $N$ is the number of channels and $L$ is the number of subcarriers. If Pn is a vector, each element represents the noise power in the corresponding channel. The noise powers for each channel is the same for all subcarriers. If Pn is a matrix, an element in the matrix represents the noise power in the corresponding channel at the corresponding subcarrier. Units are arbitrary but must match the units for Pt.

Example: [10 20 15]
Data Types: double

## Output Arguments

## P - Allocated power per channel <br> positive-valued $L$-by- $N$-element matrix

Allocated power per channel, specified as a positive-valued $L$-by- $N$-element matrix. $N$ is the number of channels and $L$ is the number of subcarriers. Units are the same as the transmitted power, Pt. Each row corresponds to a subcarrier and specifies the distributed power for the channels in the subcarrier. Units are the same as for Pt and Pn.

Data Types: double

## Algorithms

The number of subcarriers is determined by either the dimensions of Pt or Pn .

- When you specify Pt as an $L$-element vector, there are $L$ subcarriers with different total powers. If you specify Pn as $N$-element vector, this noise power vector is the same for all subcarriers. If you specify Pn as an $L$-by- $N$ matrix, each row applies to the corresponding subcarrier.
- When you specify Pt as a scalar, Pn determines the number of subcarriers. If you specify Pn as an $N$-element vector, each element is the noise power in a channel and there is only one subcarrier. If you specify Pn as an $L$-by- $N$ matrix, there are $L$ subcarriers all having the same transmitted power.


## Version History

Introduced in R2017a

## References

[1] Heath, R. Jr. et al. "An Overview of Signal Processing Techniques for Millimeter Wave MIMO Systems", arXiv.org:1512.03007 [cs.IT], 2015.
[2] Tse, D. and P. Viswanath, Fundamentals of Wireless Communications, Cambridge: Cambridge University Press, 2005.
[3] Paulraj, A. Introduction to Space-Time Wireless Communications, Cambridge: Cambridge University Press, 2003.

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using MATLAB® Coder $^{\mathrm{TM}}$.
Usage notes and limitations:

- Does not support variable-size inputs.
- Supported only when output arguments are specified.


## See Also

## Functions

diagbfweights|scatteringchanmtx
Objects
phased.ScatteringMIMOChannel

## tirempl

Path loss using Terrain Integrated Rough Earth Model (TIREM)

## Syntax

```
pl = tirempl(r,z,f)
pl = tirempl(r,z,f,Name,Value)
[pl,output] = tirempl(
```

$\qquad$

## Description

$p l=$ tirempl $(r, z, f)$ returns the path loss in $d B$ for a signal with frequency $f$ when it is propagated over terrain. You can specify terrain using numeric vectors for distance $r$ and elevation $z$ along the great circle path between the transmitter and the receiver. The Terrain Integrated Rough Earth Model ${ }^{\text {TM }}$ (TIREM ${ }^{\mathrm{TM}}$ ) model combines physics with empirical data to provide path loss estimates. The TIREM model is valid from 1 MHz to 1000 GHz .

Note tirempl requires access to the external TIREM library. Use tiremSetup to set up access.
$\mathrm{pl}=$ tirempl(r,z,f,Name,Value) returns the path loss in dB with additional options specified by name-value pairs.
[pl,output] = tirempl( __ ) returns the path loss, pl , and the output structure containing the information on the TIREM analysis.

## Examples

## Path Loss Over Flat Terrain

Calculate the path loss over flat terrain. Define the terrain profile for distances up to 10 km with step size of 100 m .

```
freq = 28e9;
r = 0:100:10000;
z = zeros(1,numel(r));
    Lterrain1 = tirempl(r,z,freq,...
        'TransmitterAntennaHeight',5, ...
        'ReceiverAntennaHeight',5)
Lterrain1 =
    142.6089
```


## Input Arguments

r-Distances
numeric vector

Distances along the great circle path between the transmitter and the receiver, specified as a numeric vector with each value in meters. The number of distance values must be equal to the number of elevation values.
Data Types: double
z - Elevation
numeric vector
Elevation values corresponding to the distance values along the great circle path between the transmitter and the receiver, specified as a numeric vector with each value in meters. The number of elevation values must be equal to the number of distance values.

Data Types: double

## f - Frequency of propagated signal

scalar | numeric vector
Frequency of the propagated signal, specified as a scalar or numeric vector with each element unit in Hz.

## Data Types: double

## Name-Value Pair Arguments

Specify optional pairs of arguments as Name1=Value1, . . . NameN=ValueN, where Name is the argument name and Value is the corresponding value. Name-value arguments must appear after other arguments, but the order of the pairs does not matter.

Before R2021a, use commas to separate each name and value, and enclose Name in quotes.
Example: 'TransmitterAntennaHeight' , 50
TransmitterAntennaHeight - Transmitter antenna height above ground
10 (default) | numeric scalar
Transmitter antenna height above the ground, specified as a numeric scalar in the range of 0 to 30000. The height is measured from ground elevation to the center of the antenna.

## Data Types: double

## ReceiverAntennaHeight - Receiver antenna height above ground <br> 1 (default) | numeric scalar

Receiver antenna height above the ground, specified as a numeric scalar in the range of 0 to 30000 . The height is measured from ground elevation to the center of the antenna.
Data Types: double
AntennaPolarization - Polarization of transmitter and receiver antennas
'horizontal' (default)|'vertical'
Polarization of the transmitter and the receiver antennas, specified as 'horizontal ' or 'vertical'.

Data Types: string | char
GroundConductivity - Conductivity of ground
0.005 (default) | numeric scalar

Conductivity of the ground, specified as a numeric scalar in the range of 0.00005 to 100 in Siemens per meter. This value is used to calculate the path loss due to ground reflection. The default value corresponds to the average ground conductivity.

## Data Types: double

## GroundPermittivity - Relative permittivity of ground <br> 15 (default) | numeric scalar

Relative permittivity of the ground, specified as a numeric scalar in the range of 1 to100. Relative permittivity is the ratio of absolute material permittivity to the permittivity of vacuum. This value is used to calculate the path loss due to ground reflection. The default value corresponds to the average ground permittivity.

## Data Types: double

## AtmosphericRefractivity - Atmospheric refractivity near ground <br> 301 (default) | numeric scalar

Atmospheric refractivity near the ground, specified as a numeric scalar in N-units in the range of 250 to 400 . This value is used to calculate the path loss due to atmospheric refraction and tropospheric scatter. The default value corresponds to average atmospheric conditions.
Data Types: double

## Humidity - Absolute air humidity near ground <br> 9 (default) | numeric scalar

Absolute air humidity near the ground, specified as a numeric scalar in $\mathrm{g} / \mathrm{m}^{\wedge}{ }^{3}$ in the range of 50 to 110. This value is used to calculate path loss due to atmospheric absorption. The default value corresponds to the absolute humidity of air at 15 degrees Celsius and 70 percent relative humidity.
Data Types: double

## Output Arguments

## pl - Path loss

scalar | 1-by- $N$ vector
Path loss, returned as a scalar or 1-by- $N$ vector with each element unit in decibels. $N$ is the number of frequencies defined in the input $f$.

Path loss is calculated from free-space loss, terrain diffraction, ground reflection, refraction through the atmosphere, tropospheric scatter, and atmospheric absorption.

## output - Information of TIREM analysis

structure
Information of TIREM analysis, returned as a structure. Each field of the structure represents an output from TIREM analysis.

## Version History

Introduced in R2019b

## See Also

tiremSetup

## Topics

"Access TIREM Software"

## tiremSetup

Set up access to Terrain Integrated Rough Earth Model (TIREM)

## Syntax

tiremSetup
tiremSetup(libfolder)
libfolder = tiremSetup

## Description

tiremSetup opens a dialog to select the Terrain Integrated Rough Earth Model (TIREM) library folder. The TIREM library folder must contain the tirem3 shared library, where the full library name is platform dependent. For more information, see ."Platform dependent library names" on page 2515
tiremSetup (libfolder) sets the TIREM library folder to libfolder.
libfolder $=$ tiremSetup returns the current TIREM library folder.

## Input Arguments

libfolder - Name of TIREM library folder
character vector
Name of the TIREM library folder, specified as a character vector.
Data Types: char | string

## Output Arguments

libfolder - Current TIREM library folder
character vector | string scalar
Current TIREM library folder, returned as a character vector or a string scalar. If TIREM access has not been setup, libfolder is empty.

## More About

Platform dependent library names

| Platform | Shared library name |
| :--- | :--- |
| Windows | libtirem3.dll or tirem3.dll |
| Linux | libtirem3.so |
| Mac | libtirem3.dylib |

# Version History <br> Introduced in R2019b 

## See Also

tirempl

## Topics

"Access TIREM Software"

Blocks

## ADPCA Canceller

Adaptive displaced phase center array (ADPCA) pulse canceller for a uniform linear array


## Libraries:

Phased Array System Toolbox / Space-Time Adaptive Processing

## Description

The ADPCA Canceller block filters clutter impinging on a uniform linear array using a displaced phase center array pulse canceller.

## Ports

Input
$\mathbf{X}$ - Input signal
$M$-by- $N$-by- $P$ complex-valued matrix
Input signal, specified as an $M$-by- $N$-by- $P$ complex-valued array. $M$ is the number of range samples, $N$ is the number of channels, and $P$ is the number of pulses.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

## Data Types: double

Idx - Index of range cells
positive integer
Index of range cells to compute processing weights.
Example: 1
Data Types: double
PRF - Pulse repetition frequency
positive scalar
Pulse repetition frequency of current pulse, specified as a positive scalar.

## Dependencies

To enable this port, set the Specify PRF as parameter to Input port.
Data Types: double
Ang - Targeting direction
2-by-1 real-valued vector
Targeting direction, specified as a 2-by-1 real-valued vector. The vector takes the form of [AzimuthAngle;ElevationAngle]. Angle units are in degrees. The azimuth angle must lie
between $-180^{\circ}$ and $180^{\circ}$, inclusive, and the elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive. Angles are defined with respect to the local coordinate system of the array.

## Dependencies

To enable this port, set the Specify direction as parameter to Input port.
Data Types: double
Dop - Targeting Doppler frequency
scalar
Targeting Doppler frequency of current pulse, specified as a scalar.

## Dependencies

This port appears when the Output pre-Doppler result check box is cleared and the Specify targeting Doppler as parameter is set to Input port.
Data Types: double

## Output

$\mathbf{Y}$ - Beamformed output
M-by-1 complex-valued vector
Processing output, returned as an $M$-by- 1 complex-valued vector. The quantity $M$ is the number of range samples in the input port $X$.
Data Types: double
W - Processing weights
length $N^{*} P$ complex-valued vector
Processing weights, returned as Length $N^{*} P$ complex-valued vector. The quantity $N$ is the number of channels and $P$ is the number of pulses. When the Specify sensor array as parameter is set to Partitioned array or Replicated subarray, $N$ represents the number of subarrays. $L$ is the number of desired beamforming directions specified in the Ang input port or by the Beamforming direction (deg) parameter. There is one set of weights for each beamforming direction.

## Dependencies

To enable this port, select the Enable weights output check box.
Data Types: double

## Parameters

## Main Tab

Signal propagation speed (m/s) - Signal propagation speed
physconst('LightSpeed') (default)| real-valued positive scalar

Signal propagation speed, specified as a real-valued positive scalar. The default value of the speed of light is the value returned by physconst('LightSpeed'). Units are in meters per second.

Example: 3e8

## Data Types: double

Operating frequency (Hz) - System operating frequency
3e8 (default) | positive real scalar

System operating frequency, specified as a positive scalar. Units are in Hz .
Specify PRF as - Source of PRF value
Property (default)|Input port

Source of PRF value, specified as Property or Input port. When set to Property, the Pulse repetition frequency ( Hz ) parameter sets the PRF. When set to Input port, pass in the PRF using the PRF input port.

Pulse repetition frequency (Hz) - Pulse repetition frequency
1 (default) | positive scalar

Pulse repetition frequency, PRF, specified as a positive scalar. Units are in Hertz. Set this parameter to the same value set in any Waveform library block used in the simulation.

## Dependencies

To enable this parameter, set the Specify PRF as parameter to Property.
Specify direction as - Specify source of targeting directions
Property (default)|Input port

Specify whether the targeting direction for the STAP processor block comes from a block parameter or from the ANG input port. Values of this parameter are

| Property | - For the ADPCA Canceller and DPCA Canceller blocks, targeting <br> direction is specified using Receiving mainlobe direction <br> (deg). |
| :--- | :--- |
| - For the SMI Beamformer block, targeting direction is specified |  |
| using Targeting direction. |  |
| These parameters appear only when the Specify direction as |  |
| parameter is set to Property. |  |

Receiving mainlobe direction (deg) - Pointing direction of main lobe of array
[0;0] (default) | real-valued 2-by-1 vector

Specify the direction of the main lobe of the receiving sensor array as a real-valued 2-by-1 vector. The direction is specified in the format of [AzimuthAngle; ElevationAngle]. The azimuth angle should be between $-180^{\circ}$ and $180^{\circ}$ and the elevation angle should be between $-90^{\circ}$ and $90^{\circ}$.
Example: [100;-45]

## Dependencies

To enable this parameter, set Specify direction as to Property.
Number of bits in phase shifters - Number of phase shift quantization bits
0 (default) | nonnegative integer

The number of bits used to quantize the phase shift component of beamformer or steering vector weights. Specify the number of bits as a non-negative integer. A value of zero indicates that no quantization is performed.

Specify targeting Doppler as - Source of targeting Doppler
Property (default)|Input port

Specify whether targeting Doppler values for the STAP processor comes from the Targeting Doppler $(\mathbf{H z})$ parameter of this block or using the DOP input port. For the ADPCA Canceller and DPCA Canceller blocks, the Specify targeting Doppler as parameter appears only when the Output pre-
Doppler result check box is cleared. Values of this parameter are

| Property | Specify targeting Doppler values using the Targeting Doppler <br> parameter of the block. The Targeting Doppler parameter appears <br> only when Specify targeting Doppler as is set to Property. |
| :--- | :--- |
| Input port | Specify targeting Doppler values using the Dop input port. This port <br> appears only when Specify targeting Doppler as is set to Input <br> port. |

Targeting Doppler (Hz) - Targeting Doppler of STAP processor
0 (default) | scalar

Targeting Doppler of STAP processor, specified as a scalar.

## Dependencies

- To enable this parameter for the SMI Beamformer block, set Specify targeting Doppler as to Property.
- To enable this parameter for the ADPCA Canceller and DPCA Canceller blocks, first clear the Output pre-Doppler result check box. Then set the Specify targeting Doppler as parameter to Property.

Number of guard cells - Number of guard cells using for training
2 (default) | positive even integer

Number of guard cells used for training, specified as a positive, even integer. Whenever possible, the set of guard cells is equally divided into regions before and after the test cell.

Number of training cells - Number of cells used for training
2 (default) | positive even integer

Number of cells used for training, specified as a positive even integer. Whenever possible, the set of training cells is equally divided into regions before and after the test cell.

Enable weights output - Option to output beamformer weights
off (default) | on

Select this check box to obtain the beamformer weights from the output port, W .
Output pre-Doppler result - Output results before Doppler filtering
on (default) | off

Select this check box to output the results before Doppler filtering. Clear this check box to output the processing result after Doppler filtering. Selecting this check box will remove the Specify targeting
Doppler as and Targeting Doppler (Hz) parameters.
Simulate using - Block simulation method
Interpreted Execution (default) | Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).

```
Programmatic Use
Block Parameter:SimulateUsing
Type:enum
```

Values:Interpreted Execution, Code Generation
Default:Interpreted Execution
Sensor Arrays Tab
Specify sensor array as - Method to specify array
Array (no subarrays) (default)|MATLAB expression

Method to specify array, specified as Array (no subarrays) or MATLAB expression.

- Array (no subarrays) - use the block parameters to specify the array.
- MATLAB expression - create the array using a MATLAB expression.

Expression - MATLAB expression used to create an array
Phased Array System Toolbox array System object

MATLAB expression used to create an array, specified as a valid Phased Array System Toolbox array System object.
Example: phased.URA('Size', [5,3])
Dependencies
To enable this parameter, set Specify sensor array as to MATLAB expression.

## Element Parameters

Element type - Array element types
Isotropic Antenna (default)|Cosine Antenna|Custom Antenna|Omni Microphone| Custom Microphone

Antenna or microphone type, specified as one of the following:

- Isotropic Antenna
- Cosine Antenna
- Custom Antenna
- Omni Microphone
- Custom Microphone

Operating frequency range $\mathbf{( H z )}$ - Operating frequency range of the antenna or microphone element
[0,1e20] (default) | real-valued 1-by-2 row vector

Specify the operating frequency range of the antenna or microphone element as a 1-by-2 row vector in the form [LowerBound, UpperBound]. The element has no response outside this frequency range. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Isotropic Antenna, Cosine Antenna, or Omni Microphone.

Operating frequency vector (Hz) - Operating frequency range of custom antenna or microphone elements
[0,1e20] (default) | real-valued row vector

Specify the frequencies at which to set antenna and microphone frequency responses as a 1-by-L row vector of increasing real values. The antenna or microphone element has no response outside the frequency range specified by the minimum and maximum elements of this vector. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone. Use Frequency responses (dB) to set the responses at these frequencies.

Baffle the back of the element - Set back response of an Isotropic Antenna element or an Omni Microphone element to zero
off (default) | on

Select this check box to baffle the back response of the element. When back baffled, the responses at all azimuth angles beyond $\pm 90^{\circ}$ from broadside are set to zero. The broadside direction is defined as $0^{\circ}$ azimuth angle and $0^{\circ}$ elevation angle.

## Dependencies

To enable this check box, set Element type to Isotropic Antenna or Omni Microphone.
Exponent of cosine pattern - Exponents of azimuth and elevation cosine patterns
[1.5 1.5] (default) | nonnegative scalar | real-valued 1-by-2 matrix of nonnegative values

Specify the exponents of the cosine pattern as a nonnegative scalar or a real-valued 1-by-2 matrix of nonnegative values. When Exponent of cosine pattern is a 1-by-2 vector, the first element is the exponent in the azimuth direction and the second element is the exponent in the elevation direction. When you set this parameter to a scalar, both the azimuth direction and elevation direction cosine patterns are raised to the same power.

## Dependencies

To enable this parameter, set Element type to Cosine Antenna.
Frequency responses (dB) - Antenna and microphone frequency response
[0,0] (default) | real-valued row vector

Frequency response of a custom antenna or custom microphone for the frequencies defined by the Operating frequency vector ( $\mathbf{H z}$ ) parameter. The dimensions of Frequency responses (dB) must match the dimensions of the vector specified by the Operating frequency vector $(\mathbf{H z})$ parameter.

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone.
Input Pattern Coordinate System - Coordinate system of custom antenna pattern az-el (default)|phi-theta

Coordinate system of custom antenna pattern, specified az-el or phi-theta. When you specify azel, use the Azimuth angles (deg) and Elevations angles (deg) parameters to specify the coordinates of the pattern points. When you specify phi-theta, use the Phi angles (deg) and Theta angles (deg) parameters to specify the coordinates of the pattern points.

Dependencies
To enable this parameter, set Element type to Custom Antenna.
Azimuth angles (deg) - Azimuth angles of antenna radiation pattern
[-180:180] (default) | real-valued row vector

Specify the azimuth angles at which to calculate the antenna radiation pattern as a 1 -by- $P$ row vector. $P$ must be greater than 2. Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to az-el.

Elevation angles (deg) - Elevation angles of antenna radiation pattern
[-90:90] (default) | real-valued row vector

Specify the elevation angles at which to compute the radiation pattern as a 1-by- $Q$ vector. $Q$ must be greater than 2. Angle units are in degrees. Elevation angles must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input
Pattern Coordinate System parameter to az-el.
Phi Angles (deg) - Phi angle coordinates of custom antenna radiation pattern
$0: 360$ | real-valued 1-by-P row vector

Phi angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by-P row vector. $P$ must be greater than 2 . Angle units are in degrees. Phi angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input
Pattern Coordinate System parameter to phi-theta.
Theta Angles (deg) - Theta angle coordinates of custom antenna radiation pattern
$0: 180$ | real-valued 1-by- $Q$ row vector

Theta angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by$Q$ row vector. $Q$ must be greater than 2. Angle units are in degrees. Theta angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Magnitude pattern (dB) - Magnitude of combined antenna radiation pattern zeros $(181,361)$ (default) | real-valued $Q$-by- $P$ matrix | real-valued $Q$-by- $P$-by- $L$ array

Magnitude of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector ( $\mathbf{H z}$ ).

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (Hz) parameter.


## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Phase pattern (deg) - Custom antenna radiation phase pattern zeros $(181,361)$ (default) | real-valued $Q$-by-P matrix | real-valued $Q$-by- $P$-by-L array

Phase of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector ( $\mathbf{H z}$ ).

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (


## Dependencies

To enable this parameter, set Element type to Custom Antenna.

MatchArrayNormal - Rotate antenna element to array normal
on (default) | off

Select this check box to rotate the antenna element pattern to align with the array normal. When not selected, the element pattern is not rotated.

When the antenna is used in an antenna array and the Input Pattern Coordinate System parameter is az-el, selecting this check box rotates the pattern so that the $x$-axis of the element coordinate system points along the array normal. Not selecting uses the element pattern without the rotation.

When the antenna is used in an antenna array and Input Pattern Coordinate System is set to phitheta, selecting this check box rotates the pattern so that the $z$-axis of the element coordinate system points along the array normal.

Use the parameter in conjunction with the Array normal parameter of the URA and UCA arrays.

## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Polar pattern frequencies (Hz) - Polar pattern microphone response frequencies
1 e3 (default) | real scalar | real-valued 1-by-L row vector

Polar pattern microphone response frequencies, specified as a real scalar, or a real-valued, 1-by-L vector. The response frequencies lie within the frequency range specified by the Operating frequency vector $(\mathrm{Hz})$ vector.

## Dependencies

To enable this parameter, set Element type set to Custom Microphone.
Polar pattern angles (deg) - Polar pattern response angles
[-180:180] (default) | real-valued -by-P row vector

Specify the polar pattern response angles, as a 1-by- $P$ vector. The angles are measured from the central pickup axis of the microphone and must be between $-180^{\circ}$ and $180^{\circ}$, inclusive.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.
Polar pattern (dB) - Custom microphone polar response
zeros (1,361) (default) | real-valued $L$-by-P matrix

Specify the magnitude of the custom microphone element polar patterns as an $L$-by- $P$ matrix. $L$ is the number of frequencies specified in Polar pattern frequencies (Hz). $P$ is the number of angles specified in Polar pattern angles (deg). Each row of the matrix represents the magnitude of the polar pattern measured at the corresponding frequency specified in Polar pattern frequencies (Hz) and all angles specified in Polar pattern angles (deg). The pattern is measured in the azimuth plane. In the azimuth plane, the elevation angle is $0^{\circ}$ and the central pickup axis is $0^{\circ}$ degrees
azimuth and $0^{\circ}$ degrees elevation. The polar pattern is symmetric around the central axis. You can construct the microphone response pattern in 3-D space from the polar pattern.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.

## Array Parameters

Specify sensor array as - Type of array
Array (no subarrays) (default)|MATLAB expression

Specify a ULA sensor array directly or by using a MATLAB expression.

## Types

## Array (no subarrays)

MATLAB expression
Number of elements - Number of array elements in $U$
2 (default) | positive integer greater than or equal to two

The number of array elements for ULA arrays, specified as an integer greater than or equal to two.
Example: 11
Data Types: double
Element spacing - Distance between ULA elements
0.5 (default) | positive scalar

Distance between adjacent ULA elements, specified as a positive scalar. Units are in meters.
Example: 1.5
Array axis - Linear axis direction of ULA
y (default) |x|z

Linear axis direction of ULA, specified as $y, x$, or $z$. All ULA array elements are uniformly spaced along this axis in the local array coordinate system.

## Dependencies

- To enable this parameter, set Geometry to ULA.
- This parameter is also enabled when the block only supports ULA arrays.

Taper - ULA array taper
1 (default) | complex-valued vector

Tapers, also known as element weights, are applied to sensor elements in the array. Tapers are used to modify both the amplitude and phase of the transmitted or received data.

Specify element tapering as a complex-valued scalar or a complex-valued 1-by- $N$ row vector. In this vector, $N$ represents the number of elements in the array. If Taper is a scalar, the same weight is applied to each element. If Taper is a vector, a weight from the vector is applied to the corresponding sensor element. A weight must be applied to each element in the sensor array.
Example: [0.5;1;0.5]
Data Types: double
Expression - MATLAB expression used to create an array
Phased Array System Toolbox array System object

MATLAB expression used to create a ULA array, specified as a valid Phased Array System Toolbox array System object.

Example: phased.ULA('NumElements',13)

## Dependencies

To enable this parameter, set Specify sensor array as to MATLAB expression.

## Version History

Introduced in R2014b

## See Also

phased.ADPCACanceller

## Angle Doppler Response

Angle-Doppler response


## Libraries:

Phased Array System Toolbox / Space-Time Adaptive Processing

## Description

The Angle Doppler Response block computes the angle-Doppler response of the input signal. The output response is a matrix whose rows represent Doppler bins and whose columns represent angle bins.

## Ports

## Input

X - Input data
$M$-by- $N$ complex-valued matrix | $M^{*} N$-element complex-valued vector
Input signal, specified as an $M$-by- $N$ complex-valued matrix or an $M^{*} N$ complex-valued vector. $M$ is the number of array elements or the number of subarrays, if the array supports subarrays, specified in the Sensor Array panel. $N$ is the number of data samples. $N$ must be greater than or equal to two.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
Data Types: double
PRF - Pulse repetition frequency
positive scalar
Pulse repetition frequency of current pulse, specified as a positive scalar.

## Dependencies

To enable this port, set the Specify PRF as parameter to Input port.
Data Types: double
EI - Elevation angle
scalar
Elevation angle, specified as a scalar. Angle units are in degrees. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive.

## Dependencies

To enable this port, set Source of elevation angle to Input port.
Data Types: double

## Output

Resp - Angle-Doppler response
$P$-by- $Q$ complex-valued matrix
Angle Doppler response, returned as a $P$-by- $Q$ matrix. $P$ is specified by the Number of Doppler bins parameter and $Q$ is specified by the Number of angle bins parameter.

Data Types: double
Ang - Response-matrix angle values
Q-by-1 real-valued vector
Response-matrix angle values, returned as a $Q$-by-1 real-valued vector. The angle values correspond to the columns of the angle-Doppler response matrix. $Q$ is specified by the Number of angle bins parameter.
Data Types: double
Dop - Response-matrix Doppler values
$P$-by-1 real-valued vector
Response-matrix Doppler values, returned as a $P$-by-1 real-valued vector. The Doppler values correspond to the rows of the angle-Doppler response matrix. $P$ is specified by the Number of Doppler bins parameter.
Data Types: double

## Parameters

## Main Tab

Signal propagation speed ( $\mathbf{m} / \mathbf{s}$ ) - Signal propagation speed
physconst('LightSpeed') (default)| real-valued positive scalar

Signal propagation speed, specified as a real-valued positive scalar. The default value of the speed of light is the value returned by physconst('LightSpeed'). Units are in meters per second.
Example: 3e8
Data Types: double
Operating frequency (Hz) - System operating frequency
$3 e 8$ (default) | positive real scalar

System operating frequency, specified as a positive scalar. Units are in Hz.
Specify PRF as - Source of PRF value
Property (default)|Input port

Source of PRF value, specified as Property or Input port. When specifier as Property, the Pulse repetition frequency $(\mathbf{H z})$ parameter sets the PRF. When set to Input port, pass in the PRF using the PRF input port.

Pulse repetition frequency (Hz) - Pulse repetition frequency
1 (default) | positive scalar

Pulse repetition frequency, PRF, specified as a positive scalar. Units are in Hertz. Set this parameter to the same value set in any Waveform library block used in the simulation.

## Dependencies

To enable this parameter, set the Specify PRF as parameter to Property.
Source of elevation angle - Elevation angle source
Property (default)|Input port

Elevation angle source, specified as Property or Input port. Values of this parameter are

| Property | The Elevation angle (deg) parameter of this block specifies <br> the elevation angle. |
| :--- | :--- |
| Input port | The elevation angle is set using the El input port. |

Elevation angle (deg) - Elevation angle used to calculate the angle-Doppler response
0 (default) | scalar

Elevation angle used to calculate the angle-Doppler response, specified as a scalar. Units are degrees. The angle must be between $-90^{\circ}$ and $90^{\circ}$.
Example: -45

## Dependencies

To enable this parameter, set Source of elevation angle to Property

## Data Types: double

Number of angle bins - Number of angle samples
256 (default) | positive integer greater than two

The number of samples in the angular domain used to calculate the angle-Doppler response, specified as a positive integer greater than two.
Example: 600
Data Types: double
Number of Doppler bins - Number of angle samples
256 (default) | positive integer greater than two

The number of samples in the Doppler domain used to calculate the angle-Doppler response, specified as a positive integer greater than two.
Example: 128
Data Types: double

## Simulate using - Block simulation method <br> Interpreted Execution (default)|Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).
Programmatic Use
Block Parameter:SimulateUsing
Type:enum
Values:Interpreted Execution, Code Generation
Default:Interpreted Execution

## Sensor Arrays Tab

Specify sensor array as - Method to specify array
Array (no subarrays) (default)|Partitioned array|Replicated subarray|MATLAB expression

Method to specify array, specified as Array (no subarrays) or MATLAB expression.

- Array (no subarrays) - use the block parameters to specify the array.
- Partitioned array - use the block parameters to specify the array.
- Replicated subarray - use the block parameters to specify the array.
- MATLAB expression - create the array using a MATLAB expression.

Expression - MATLAB expression used to create an array
Phased Array System Toolbox array System object

MATLAB expression used to create an array, specified as a valid Phased Array System Toolbox array System object.

Example: phased.URA('Size', [5,3])

## Dependencies

To enable this parameter, set Specify sensor array as to MATLAB expression.

## Element Parameters

Element type - Array element types
Isotropic Antenna (default)|Cosine Antenna|Custom Antenna|Omni Microphone|
Custom Microphone

Antenna or microphone type, specified as one of the following:

- Isotropic Antenna
- Cosine Antenna
- Custom Antenna
- Omni Microphone
- Custom Microphone

Operating frequency range $\mathbf{( H z )}$ - Operating frequency range of the antenna or microphone element
[0,1e20] (default) | real-valued 1-by-2 row vector

Specify the operating frequency range of the antenna or microphone element as a 1-by-2 row vector in the form [LowerBound, UpperBound]. The element has no response outside this frequency range. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Isotropic Antenna, Cosine Antenna, or Omni Microphone.

Operating frequency vector ( $\mathbf{H z}$ ) - Operating frequency range of custom antenna or microphone elements
[0,1e20] (default) | real-valued row vector

Specify the frequencies at which to set antenna and microphone frequency responses as a 1-by- $L$ row vector of increasing real values. The antenna or microphone element has no response outside the frequency range specified by the minimum and maximum elements of this vector. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone. Use Frequency responses (dB) to set the responses at these frequencies.

Baffle the back of the element - Set back response of an Isotropic Antenna element or an Omni Microphone element to zero
off (default) | on

Select this check box to baffle the back response of the element. When back baffled, the responses at all azimuth angles beyond $\pm 90^{\circ}$ from broadside are set to zero. The broadside direction is defined as $0^{\circ}$ azimuth angle and $0^{\circ}$ elevation angle.

## Dependencies

To enable this check box, set Element type to Isotropic Antenna or Omni Microphone.
Exponent of cosine pattern - Exponents of azimuth and elevation cosine patterns
[1.5 1.5] (default) | nonnegative scalar | real-valued 1-by-2 matrix of nonnegative values

Specify the exponents of the cosine pattern as a nonnegative scalar or a real-valued 1-by-2 matrix of nonnegative values. When Exponent of cosine pattern is a 1 -by-2 vector, the first element is the exponent in the azimuth direction and the second element is the exponent in the elevation direction. When you set this parameter to a scalar, both the azimuth direction and elevation direction cosine patterns are raised to the same power.

## Dependencies

To enable this parameter, set Element type to Cosine Antenna.
Frequency responses (dB) - Antenna and microphone frequency response
[0,0] (default) | real-valued row vector

Frequency response of a custom antenna or custom microphone for the frequencies defined by the Operating frequency vector $(\mathbf{H z})$ parameter. The dimensions of Frequency responses (dB) must match the dimensions of the vector specified by the Operating frequency vector $(\mathbf{H z})$ parameter.

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone.
Input Pattern Coordinate System - Coordinate system of custom antenna pattern
az-el (default)|phi-theta

Coordinate system of custom antenna pattern, specified az-el or phi-theta. When you specify azel, use the Azimuth angles (deg) and Elevations angles (deg) parameters to specify the coordinates of the pattern points. When you specify phi-theta, use the Phi angles (deg) and Theta angles (deg) parameters to specify the coordinates of the pattern points.

## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Azimuth angles (deg) - Azimuth angles of antenna radiation pattern
[-180:180] (default) | real-valued row vector

Specify the azimuth angles at which to calculate the antenna radiation pattern as a 1-by- $P$ row vector. $P$ must be greater than 2. Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to az-el.

Elevation angles (deg) - Elevation angles of antenna radiation pattern
[-90:90] (default) | real-valued row vector

Specify the elevation angles at which to compute the radiation pattern as a 1-by- $Q$ vector. $Q$ must be greater than 2. Angle units are in degrees. Elevation angles must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to az-el.

Phi Angles (deg) - Phi angle coordinates of custom antenna radiation pattern
$0: 360$ | real-valued 1-by-P row vector

Phi angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by-P row vector. $P$ must be greater than 2 . Angle units are in degrees. Phi angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Theta Angles (deg) - Theta angle coordinates of custom antenna radiation pattern 0 : 180 | real-valued 1-by- $Q$ row vector

Theta angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by$Q$ row vector. $Q$ must be greater than 2 . Angle units are in degrees. Theta angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Magnitude pattern (dB) - Magnitude of combined antenna radiation pattern
zeros $(181,361)$ (default) | real-valued $Q$-by- $P$ matrix | real-valued $Q$-by- $P$-by- $L$ array

Magnitude of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector ( $\mathbf{H z}$ ).

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector (Hz) parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (Hz) parameter.


## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Phase pattern (deg) - Custom antenna radiation phase pattern
zeros $(181,361)$ (default) | real-valued $Q$-by-P matrix | real-valued $Q$-by- $P$-by-L array

Phase of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector $(\mathbf{H z})$.

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (

Dependencies
To enable this parameter, set Element type to Custom Antenna.
MatchArrayNormal - Rotate antenna element to array normal on (default) | off

Select this check box to rotate the antenna element pattern to align with the array normal. When not selected, the element pattern is not rotated.

When the antenna is used in an antenna array and the Input Pattern Coordinate System parameter is az-el, selecting this check box rotates the pattern so that the $x$-axis of the element coordinate system points along the array normal. Not selecting uses the element pattern without the rotation.

When the antenna is used in an antenna array and Input Pattern Coordinate System is set to phitheta, selecting this check box rotates the pattern so that the $z$-axis of the element coordinate system points along the array normal.

Use the parameter in conjunction with the Array normal parameter of the URA and UCA arrays.

## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Polar pattern frequencies (Hz) - Polar pattern microphone response frequencies
1e3 (default) | real scalar | real-valued 1-by-L row vector

Polar pattern microphone response frequencies, specified as a real scalar, or a real-valued, 1-by-L vector. The response frequencies lie within the frequency range specified by the Operating frequency vector $(\mathrm{Hz})$ vector.

## Dependencies

To enable this parameter, set Element type set to Custom Microphone.
Polar pattern angles (deg) - Polar pattern response angles
[-180:180] (default) | real-valued -by-P row vector

Specify the polar pattern response angles, as a 1-by- $P$ vector. The angles are measured from the central pickup axis of the microphone and must be between $-180^{\circ}$ and $180^{\circ}$, inclusive.

Dependencies
To enable this parameter, set Element type to Custom Microphone.
Polar pattern (dB) - Custom microphone polar response
zeros ( 1,361 ) (default) | real-valued $L$-by- $P$ matrix

Specify the magnitude of the custom microphone element polar patterns as an $L$-by- $P$ matrix. $L$ is the number of frequencies specified in Polar pattern frequencies ( $\mathbf{H z}$ ). $P$ is the number of angles specified in Polar pattern angles (deg). Each row of the matrix represents the magnitude of the polar pattern measured at the corresponding frequency specified in Polar pattern frequencies (Hz) and all angles specified in Polar pattern angles (deg). The pattern is measured in the azimuth plane. In the azimuth plane, the elevation angle is $0^{\circ}$ and the central pickup axis is $0^{\circ}$ degrees azimuth and $0^{\circ}$ degrees elevation. The polar pattern is symmetric around the central axis. You can construct the microphone response pattern in 3-D space from the polar pattern.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.

## Array Parameters

Geometry - Array geometry
ULA (default) | URA | UCA | Conformal Array

Array geometry, specified as one of

- ULA - Uniform linear array
- URA - Uniform rectangular array
- UCA - Uniform circular array
- Conformal Array - arbitrary element positions

Number of elements - Number of array elements
2 for ULA arrays and 5 for UCA arrays (default) | integer greater than or equal to 2

The number of array elements for ULA or UCA arrays, specified as an integer greater than or equal to 2.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

## Dependencies

To enable this parameter, set Geometry to ULA or UCA.
Element spacing (m) - Spacing between array elements
0.5 for ULA arrays and [0.5,0.5] for URA arrays (default) | positive scalar for ULA or URA arrays | 2-element vector of positive values for URA arrays

Spacing between adjacent array elements:

- ULA - specify the spacing between two adjacent elements in the array as a positive scalar.
- URA - specify the spacing as a positive scalar or a 1-by-2 vector of positive values. If Element spacing (m) is a scalar, the row and column spacings are equal. If Element spacing (m) is a vector, the vector has the form [SpacingBetweenArrayRows, SpacingBetweenArrayColumns].
- When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.


## Dependencies

To enable this parameter, set Geometry to ULA or URA.
Array axis - Linear axis direction of ULA
$y$ (default) $|x| z$

Linear axis direction of ULA, specified as $y, x$, or $z$. All ULA array elements are uniformly spaced along this axis in the local array coordinate system.

## Dependencies

- To enable this parameter, set Geometry to ULA.
- This parameter is also enabled when the block only supports ULA arrays.

Array size - Dimensions of URA array
[2, 2] (default) | positive integer | 1-by-2 vector of positive integers

Dimensions of a URA array, specified as a positive integer or 1-by-2 vector of positive integers.

- If Array size is a 1 -by- 2 vector, the vector has the form [NumberOfArrayRows, NumberOfArrayColumns].
- If Array size is an integer, the array has the same number of rows and columns.
- When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

For a URA, array elements are indexed from top to bottom along the leftmost column, and then continue to the next columns from left to right. In this figure, the Array size value of [3, 2] creates an array having three rows and two columns.

## Size and Element Indexing Order

for Uniform Rectangular Arrays
Example: Size $=[3,2]$


## Dependencies

To enable this parameter, set Geometry to URA.
Element lattice - Lattice of URA element positions
Rectangular (default) | Triangular

Lattice of URA element positions, specified as Rectangular or Triangular.

- Rectangular - Aligns all the elements in row and column directions.
- Triangular - Shifts the even-row elements of a rectangular lattice toward the positive row-axis direction. The displacement is one-half the element spacing along the row dimension.


## Dependencies

To enable this parameter, set Geometry to URA.
Array normal - Array normal direction
$x$ for URA arrays or $z$ for UCA arrays (default) | y

Array normal direction, specified as $x, y$, or $z$.

Elements of planar arrays lie in a plane orthogonal to the selected array normal direction. Element boresight directions point along the array normal direction.

| Array Normal Parameter Value | Element Positions and Boresight Directions |
| :--- | :--- |
| $x$ | Array elements lie in the $y z$-plane. All element <br> boresight vectors point along the $x$-axis. |
| $y$ | Array elements lie in the $z x$-plane. All element <br> boresight vectors point along the $y$-axis. |
| $z$ | Array elements lie in the $x y$-plane. All element <br> boresight vectors point along the $z$-axis. |

## Dependencies

To enable this parameter, set Geometry to URA or UCA.
Radius of UCA (m) - UCA array radius
0.5 (default) | positive scalar

Radius of UCA array, specified as a positive scalar.

## Dependencies

To enable this parameter, set Geometry to UCA.
Element positions (m) - Positions of conformal array elements
[ $0 ; 0 ; 0$ ] (default) | 3-by-Nmatrix of real values

Positions of the elements in a conformal array, specified as a $3-b y-N$ matrix of real values, where $N$ is the number of elements in the conformal array. Each column of this matrix represents the position [ $x ; y ; z$ ] of an array element in the array local coordinate system. The origin of the local coordinate system is $(0,0,0)$. Units are in meters.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

## Dependencies

To enable this parameter set Geometry to Conformal Array.
Element normals (deg) - Direction of conformal array element normal vectors
[0;0]|2-by-1 column vector | 2 -by- $N$ matrix

Direction of element normal vectors in a conformal array, specified as a 2-by-1 column vector or a 2-by- $N$ matrix. $N$ indicates the number of elements in the array. For a matrix, each column specifies the normal direction of the corresponding element in the form [azimuth; elevation] with respect to the local coordinate system. The local coordinate system aligns the positive $x$-axis with the direction normal to the conformal array. If the parameter value is a 2 -by- 1 column vector, the same pointing direction is used for all array elements.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

You can use the Element positions (m) and Element normals (deg) parameters to represent any arrangement in which pairs of elements differ by certain transformations. The transformations can combine translation, azimuth rotation, and elevation rotation. However, you cannot use transformations that require rotation about the normal direction.

## Dependencies

To enable this parameter, set Geometry to Conformal Array.
Taper - Array element tapers
1 (default) | complex-valued scalar | complex-valued row vector

Element tapering, specified as a complex-valued scalar or a complex-valued 1-by- $N$ row vector. In this vector, $N$ represents the number of elements in the array.

Also known as element weights, tapers multiply the array element responses. Tapers modify both amplitude and phase of the response to reduce side lobes or steer the main response axis.

If Taper is a scalar, the same weight is applied to each element. If Taper is a vector, a weight from the vector is applied to the corresponding sensor element. The number of weights must match the number of elements of the array.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

Subarray definition matrix - Define elements belonging to subarrays
logical matrix

Specify the subarray selection as an $M$-by- $N$ matrix. $M$ is the number of subarrays and $N$ is the total number of elements in the array. Each row of the matrix represents a subarray and each entry in the row indicates when an element belongs to the subarray. When the entry is zero, the element does not belong the subarray. A nonzero entry represents a complex-valued weight applied to the corresponding element. Each row must contain at least one nonzero entry.

The phase center of each subarray lies at the subarray geometric center. The subarray geometric center depends on the Subarray definition matrix and Geometry parameters.

## Dependencies

To enable this parameter, set Specify sensor array as to Partitioned array.
Subarray steering method - Specify subarray steering method None (default) | Phase | Time

Subarray steering method, specified as one of

- None
- Phase
- Time
- Custom

Selecting Phase or Time opens the Steer input port on the Narrowband Receive Array, Narrowband Transmit Array, Wideband Receive Array, Wideband Transmit Array blocks, Constant Gamma Clutter, and GPU Constant Gamma Clutter blocks.

Selecting Custom opens the WS input port on the Narrowband Receive Array, Narrowband Transmit Array, Wideband Receive Array, Wideband Transmit Array blocks, Constant Gamma Clutter, and GPU Constant Gamma Clutter blocks.

## Dependencies

To enable this parameter, set Specify sensor array as to Partitioned array or Replicated subarray.

Phase shifter frequency (Hz) - Subarray phase shifting frequency
3.0 e 8 (default) | positive real-valued scalar

Operating frequency of subarray steering phase shifters, specified as a positive real-valued scalar. Units are Hz.

## Dependencies

To enable this parameter, set Sensor array to Partitioned array or Replicated subarray and set Subarray steering method to Phase.

Number of bits in phase shifters - Subarray steering phase shift quantization bits
0 (default) | non-negative integer

Subarray steering phase shift quantization bits, specified as a non-negative integer. A value of zero indicates that no quantization is performed.

## Dependencies

To enable this parameter, set Sensor array to Partitioned array or Replicated subarray and set Subarray steering method to Phase.

Subarrays layout - Subarray position specification
Rectangular (default) | Custom

Specify the layout of replicated subarrays as Rectangular or Custom.

- When you set this parameter to Rectangular, use the Grid size and Grid spacing parameters to place the subarrays.
- When you set this parameter to Custom, use the Subarray positions (m) and Subarray normals parameters to place the subarrays.


## Dependencies

To enable this parameter, set Sensor array to Replicated subarray
Grid size - Dimensions of rectangular subarray grid
[1,2] (default)

Rectangular subarray grid size, specified as a single positive integer, or a 1-by-2 row vector of positive integers.

If Grid size is an integer scalar, the array has an equal number of subarrays in each row and column.
If Grid size is a 1-by-2 vector of the form [NumberOfRows, NumberOfColumns], the first entry is the number of subarrays along each column. The second entry is the number of subarrays in each row. A row is along the local $y$-axis, and a column is along the local $z$-axis. The figure here shows how you can replicate a 3-by-2 URA subarray using a Grid size of [1,2].
$3 \times 2$ Element URA
Replicated on a $1 \times 2$ Grid


## Dependencies

To enable this parameter, set Sensor array to Replicated subarray and Subarrays layout to Rectangular.

Grid spacing ( $\mathbf{m}$ ) - Spacing between subarrays on rectangular grid
Auto (default) | positive real-valued scalar | 1-by-2 vector of positive real-values

The rectangular grid spacing of subarrays, specified as a positive, real-valued scalar, a 1-by-2 row vector of positive, real-values, or Auto. Units are in meters.

- If Grid spacing is a scalar, the spacing along the row and the spacing along the column is the same.
- If Grid spacing is a 1-by-2 row vector, the vector has the form [SpacingBetweenRows,SpacingBetweenColumn]. The first entry specifies the spacing between rows along a column. The second entry specifies the spacing between columns along a row.
- If Grid spacing is set to Auto, replication preserves the element spacing of the subarray for both rows and columns while building the full array. This option is available only when you specify Geometry as ULA or URA.


## Dependencies

To enable this parameter, set Sensor array to Replicated subarray and Subarrays layout to Rectangular.

Subarray positions (m) - Positions of subarrays
[0,0;0.5,0.5;0,0] (default)| 3-by- $N$ real-valued matrix

Positions of the subarrays in the custom grid, specified as a real 3-by- $N$ matrix, where $N$ is the number of subarrays in the array. Each column of the matrix represents the position of a single subarray in the array local coordinate system. The coordinates are expressed in the form [x; y; z]. Units are in meters.

Dependencies
To enable this parameter, set Sensor array to Replicated subarray and Subarrays layout to Custom.

Subarray normals - Direction of subarray normal vectors
[0,0;0,0] (default)| 2-by- $N$ real matrix

Specify the normal directions of the subarrays in the array. This parameter value is a 2 -by- $N$ matrix, where $N$ is the number of subarrays in the array. Each column of the matrix specifies the normal direction of the corresponding subarray, in the form [azimuth; elevation]. Angle units are in degrees. Angles are defined with respect to the local coordinate system.

You can use the Subarray positions and Subarray normals parameters to represent any arrangement in which pairs of subarrays differ by certain transformations. The transformations can combine translation, azimuth rotation, and elevation rotation. However, you cannot use transformations that require rotation about the normal.

## Dependencies

To enable this parameter, set the Sensor array parameter to Replicated subarray and the Subarrays layout to Custom.

## Version History <br> Introduced in R2014b

## See Also

phased.AngleDopplerResponse

## Azimuth Broadside Converter

Convert azimuth angle to broadside angle or broadside angle to azimuth angle

## Libraries:



Phased Array System Toolbox / Environment and Target

## Description

The Azimuth Broadside Converter block converts an angle direction expressed in terms of "Broadside Angles" into the equivalent azimuth angle or converts from azimuth angle into the equivalent broadside angle. In both cases, you must specify the elevation angle.

## Ports

Input
az - Azimuth angle
scalar | vector of real-values
Azimuth angle of direction, specified as a scalar or vector of real-values. Units are in degrees. When $a z$ is a vector, the dimensions of az and el must match.

## Dependencies

To enable this port, set Conversion Mode to azimuth -> broadside.
Data Types: double
bsd - Broadside angle
scalar | vector of real-values
Broadside angle of direction, specified as a scalar or vector of real-values. Units are in degrees. When bsd is a vector, the dimensions of bsd and el must match.

## Dependencies

To enable this port, set Conversion Mode to broadside -> azimuth.

## Data Types: double

el - Elevation angle
scalar | vector of real-values
Elevation angle of direction, specified as a scalar or vector of real-values. Units are in degrees. The dimensions of el must match the dimensions of az and bsd.
Data Types: double

## Output

az - Azimuth angle
scalar | vector of real-values

Azimuth angle of direction, returned as a scalar or vector of real-values. Units are in degrees.

## Dependencies

To enable this port, set Conversion Mode to broadside -> azimuth.
Data Types: double
bsd - Broadside angle
scalar | vector of real-values
Broadside angle of direction, returned as a scalar or vector of real-values. Units are in degrees.
Dependencies
To enable this port, set Conversion Mode to azimuth -> broadside.
Data Types: double

## Parameters

Conversion mode - Angle conversion type
broadside -> azimuth (default) | azimuth -> broadside

Angle conversion type, specified as

## broadside -> azimuth

azimuth -> broadside

Version History<br>Introduced in R2014b<br>See Also<br>az2broadside|broadside2az

Convert direction expressed in broadside and elevation angles to azimuth and elevation angles.
Convert direction expressed in azimuth and elevation angles to broadside and elevation angles.

# Backscatter Radar Target 

Backscatter radar target


## Libraries:

Phased Array System Toolbox / Environment and Target

## Description

The Backscatter Radar Target block models the monostatic radar reflections of nonpolarized electromagnetic signals from a target. Target model includes all four Swerling target fluctuation models and non-fluctuating model. You can model several targets simultaneously by specifying multiple radar cross-section (RCS) matrices.

## Ports

## Input

## $\mathbf{X}$ - Narrowband signal

N -by-1 complex-valued vector | N -by-M complex-valued matrix
Narrowband nonpolarized signal, specified as an $N$-by- 1 complex-valued vector or an $N$-by- $M$ complex-valued matrix. The quantity $N$ is the number of signal samples and $M$ is the number of signals reflecting from the target. Each column corresponds to an independent signal incident at a different reflecting angle.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

## Data Types: double

Ang - Incident signal direction
2-by-1 real-valued column vector | 2 -by- $M$ real-valued column matrix
Incident signal direction, specified as a 2 -by- 1 real-valued column vector or a 2 -by- $M$ real-valued column matrix. $M$ is the number of signals reflecting from the target. Each column of Ang specifies the incident direction of the corresponding signal in the form of an
[AzimuthAngle;ElevationAngle] pair. Units are degrees. The number of columns in Ang must match the number of independent signals in $X$.
Example: [30;45]
Data Types: double
Update - Switch to update RCS
false|true
Switch to update RCS fluctuation model values, specified as false or true. When Update is true, the RCS value is updated. If Update is false, the RCS remains unchanged.

## Dependencies

To enable this port, set the Fluctuation model drop-down menu to Swerling1, Swerling2, Swerling3, or Swerling4.

## Output

Port_1 - Narrowband reflected signal
1-by- $M$ complex-valued vector $\mid N$-by- $M$ complex-valued matrix
Narrowband nonpolarized signal, specified as an 1-by- $M$ complex-valued vector or a $N$-by- $M$ complexvalued matrix. Each column contains an independent signal reflected from the target.

The quantity $N$ is the number of signal samples and $M$ is the number of signals reflecting off the target. Each column corresponds to a different reflecting angle.

The output port contains signal samples arriving at the signal destination within the current input time frame. When the propagation time from source to destination exceeds the current time frame duration, the output does not contain all contributions from the input of the current time frame.

## Parameters

Azimuth angles (deg) - Azimuth angles
[-180:180] (default) | 1-by-P real-valued row vector | $P$-by-1 real-valued column vector
Specify the azimuth angles used to define the angular coordinates of the RCS pattern (m^2) parameter. Specify azimuth angles as a length $P$ vector. Units are degrees. $P$ must be greater than two. This parameter determines the incident azimuthal arrival angle of any element of the crosssection patterns.
Data Types: double
Elevation angles (deg) - Elevation angles

## [-90:90] (default) | 1-by-Q real-valued row vector | $Q$-by-1 real-valued column vector

Specify the elevation angles used to define the angular coordinates of the RCS pattern (m^2) parameter. Specify elevation angles as a length $Q$ vector. Units are degrees. $Q$ must be greater than two. This parameter determines the incident elevation arrival angle of any element of the crosssection patterns.

## RCS pattern ( $\mathbf{m}^{\wedge} \mathbf{2}$ ) - Radar cross-section pattern

ones (181, 361) (default) | Q-by-P real-valued matrix | Q-by-P-by-M real-valued array | 1-by-P realvalued vector $\mid M$-by- $P$ real-valued matrix

Radar cross-section pattern, specified as a $Q$-by- $P$ real-valued matrix or a $Q$-by- $P$-by- $M$ real-valued array.

- $Q$ is the length of the vector in the Elevation angles (deg) parameter.
- $P$ is the length of the vector in the Azimuth angles (deg) parameter.
- $M$ is the number of target patterns. The number of patterns corresponds to the number of signals passed into the input port $X$. You can, however, use a single pattern to model multiple signals reflecting from a single target.

You can, however, use a single pattern to model multiple signals reflecting from a single target. Pattern units are square-meters.

Pattern units are square-meters.
Fluctuation model - Target fluctuation model
Nonfluctuating (default)|Swerling1|Swerling2 | Swerling3|Swerling4
Specify the statistical model of the target as either Nonfluctuating, Swerling1, Swerling2, Swerling3, or Swerling4. When you set this parameter to a value other than Nonfluctuating, you then set radar cross-sections parameters using the Update input port.

Propagation speed (m/s) - Signal propagation speed
physconst('LightSpeed') (default) | real-valued positive scalar

Signal propagation speed, specified as a real-valued positive scalar. The default value of the speed of light is the value returned by physconst ('LightSpeed'). Units are in meters per second.
Example: 3e8
Data Types: double
Operating frequency (Hz) - Operating frequency

## 3 e8 (default) | positive scalar

Carrier frequency of the signal that reflects from the target, specified as a positive scalar. Units are in hertz.

Data Types: double
Simulate using - Block simulation method
Interpreted Execution (default) |Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.

When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).
Programmatic Use
Block Parameter:SimulateUsing
Type:enum
Values:Interpreted Execution, Code Generation
Default:Interpreted Execution

## Version History

Introduced in R2016a

See Also<br>phased.BackscatterRadarTarget

## Beamscan Spectrum

Beamscan spatial spectrum estimator

## Libraries:



Phased Array System Toolbox / Direction of Arrival

## Description

The Beamscan Spectrum block estimates the 2-D spatial spectrum of incoming narrowband signals by scanning a range of azimuth and elevation angles using a narrowband conventional beamformer. The block optionally calculates the direction of arrival of a specified number of signals by locating peaks of the spectrum.

## Ports

Input
X - Received signal
$M$-by- $N$ complex-valued matrix
Received signal, specified as an $M$-by- $N$ complex-valued matrix. The quantity $M$ is the length of the signal, the number of sample values contained in the signal. The quantity $N$ is the number of sensor elements in the array.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
Data Types: double

## Output

$\mathbf{Y}$ - Beamscan 2-D spatial spectrum
non-negative real-valued $P$-by- $Q$ matrix
2Magnitude of the estimated 2-D spatial spectrum, returned as a non-negative, returned as a realvalued $P$-by- $Q$ matrix. Each entry represents the magnitude of the estimated MUSIC spatial spectrum. Each entry corresponds to an angle specified by the Azimuth scan angles (deg) and Elevation scan angles (deg) parameters. $P$ equals the length of the vector specified in Azimuth scan angles (deg) and $Q$ equals the length of the vector specified in Elevation scan angles (deg).

## Data Types: double

Ang - Directions of arrival
non-negative, real-valued 2-by-L matrix
Directions of arrival of the signals, returned as a real-valued 2-by- $L$ matrix. $L$ is the number of signals specified by the Number of signals parameter. The direction of arrival angle is defined by the azimuth and elevation angles of the source with respect to the array local coordinate system. The first
row of the matrix contains the azimuth angles and the second row contains the elevation angles. If the object cannot identify peaks in the spectrum, it will return NaN. Angle units are in degrees.

## Dependencies

To enable this output port, select the Enable DOA output check box.
Data Types: double

## Parameters

Signal propagation speed (m/s) - Signal propagation speed
physconst('LightSpeed') (default) | real-valued positive scalar

Signal propagation speed, specified as a real-valued positive scalar. The default value of the speed of light is the value returned by physconst('LightSpeed '). Units are in meters per second.

## Example: 3e8

Data Types: double
Operating frequency $(\mathrm{Hz})$ - System operating frequency
3e8 (default) | positive real scalar

System operating frequency, specified as a positive scalar. Units are in Hz.
Number of bits in phase shifters - Number of phase shift quantization bits
0 (default) | nonnegative integer

The number of bits used to quantize the phase shift component of beamformer or steering vector weights. Specify the number of bits as a non-negative integer. A value of zero indicates that no quantization is performed.

Forward-backward averaging - Enable forward-backward averaging off (default) | on

Select this parameter to use forward-backward averaging to estimate the covariance matrix for sensor arrays with a conjugate symmetric array manifold structure.

Azimuth scan angles (deg) - Scan angles in azimuth direction

- 180: 180 (default) | real-valued vector

Scan angles in azimuthal direction, specified as a real-valued vector. The angles must lie be between $180^{\circ}$ and $180^{\circ}$, inclusive. You must specify the angles in ascending order. Units are in degrees.

Data Types: double
Elevation scan angles (deg) - Scan angles in elevation direction
-90:90 (default) | real-valued vector

Scan angles in elevation direction, specified as a real-valued vector. The angles must lie be between $90^{\circ}$ and $90^{\circ}$, inclusive. You must specify the angles in ascending order. Units are in degrees.

## Data Types: double

Enable DOA output - Output directions of arrival through output port
off (default) | on

Select this parameter to output the signals directions of arrival (DOA) through the Ang output port.
Number of signals - Expected number of arriving signals
1 (default) | positive integer

Specify the expected number of signals for DOA estimation as a positive scalar integer.

## Dependencies

To enable this parameter, select the Enable DOA output check box.
Data Types: double
Simulate using - Block simulation method
Interpreted Execution (default) | Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).

Programmatic Use
Block Parameter:SimulateUsing
Type:enum
Values:Interpreted Execution, Code Generation
Default:Interpreted Execution
Sensor Array Tab
Specify sensor array as - Method to specify array
Array (no subarrays) (default)|MATLAB expression

Method to specify array, specified as Array (no subarrays) or MATLAB expression.

- Array (no subarrays) - use the block parameters to specify the array.
- MATLAB expression - create the array using a MATLAB expression.

Expression - MATLAB expression used to create an array
Phased Array System Toolbox array System object

MATLAB expression used to create an array, specified as a valid Phased Array System Toolbox array System object.

Example: phased.URA('Size', [5,3])

## Dependencies

To enable this parameter, set Specify sensor array as to MATLAB expression.

## Element Parameters

Element type - Array element types
Isotropic Antenna (default)|Cosine Antenna|Custom Antenna|Omni Microphone|
Custom Microphone

Antenna or microphone type, specified as one of the following:

- Isotropic Antenna
- Cosine Antenna
- Custom Antenna
- Omni Microphone
- Custom Microphone

Operating frequency range $(\mathbf{H z})$ - Operating frequency range of the antenna or microphone element
[0,1e20] (default) | real-valued 1-by-2 row vector

Specify the operating frequency range of the antenna or microphone element as a 1-by-2 row vector in the form [LowerBound, UpperBound]. The element has no response outside this frequency range. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Isotropic Antenna, Cosine Antenna, or Omni Microphone.

Operating frequency vector ( Hz ) - Operating frequency range of custom antenna or microphone elements
[0,1e20] (default) | real-valued row vector

Specify the frequencies at which to set antenna and microphone frequency responses as a 1-by-L row vector of increasing real values. The antenna or microphone element has no response outside the frequency range specified by the minimum and maximum elements of this vector. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone. Use Frequency responses (dB) to set the responses at these frequencies.

Baffle the back of the element - Set back response of an Isotropic Antenna element or an Omni Microphone element to zero off (default) | on

Select this check box to baffle the back response of the element. When back baffled, the responses at all azimuth angles beyond $\pm 90^{\circ}$ from broadside are set to zero. The broadside direction is defined as $0^{\circ}$ azimuth angle and $0^{\circ}$ elevation angle.

## Dependencies

To enable this check box, set Element type to Isotropic Antenna or Omni Microphone.
Exponent of cosine pattern - Exponents of azimuth and elevation cosine patterns [1.5 1.5] (default) | nonnegative scalar | real-valued 1-by-2 matrix of nonnegative values

Specify the exponents of the cosine pattern as a nonnegative scalar or a real-valued 1-by-2 matrix of nonnegative values. When Exponent of cosine pattern is a 1-by-2 vector, the first element is the exponent in the azimuth direction and the second element is the exponent in the elevation direction. When you set this parameter to a scalar, both the azimuth direction and elevation direction cosine patterns are raised to the same power.

## Dependencies

To enable this parameter, set Element type to Cosine Antenna.
Frequency responses (dB) - Antenna and microphone frequency response
[0,0] (default) | real-valued row vector

Frequency response of a custom antenna or custom microphone for the frequencies defined by the Operating frequency vector (Hz) parameter. The dimensions of Frequency responses (dB) must match the dimensions of the vector specified by the Operating frequency vector (Hz) parameter.

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone.
Input Pattern Coordinate System - Coordinate system of custom antenna pattern
az-el (default)| phi-theta

Coordinate system of custom antenna pattern, specified az-el or phi-theta. When you specify azel, use the Azimuth angles (deg) and Elevations angles (deg) parameters to specify the coordinates of the pattern points. When you specify phi-theta, use the Phi angles (deg) and Theta angles (deg) parameters to specify the coordinates of the pattern points.

## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Azimuth angles (deg) - Azimuth angles of antenna radiation pattern
[-180:180] (default) | real-valued row vector

Specify the azimuth angles at which to calculate the antenna radiation pattern as a 1 -by- $P$ row vector. $P$ must be greater than 2. Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to az-el.

Elevation angles (deg) - Elevation angles of antenna radiation pattern
[-90:90] (default) | real-valued row vector

Specify the elevation angles at which to compute the radiation pattern as a 1-by- $Q$ vector. $Q$ must be greater than 2. Angle units are in degrees. Elevation angles must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to az-el.

Phi Angles (deg) - Phi angle coordinates of custom antenna radiation pattern
$0: 360 \mid$ real-valued 1-by-P row vector

Phi angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by- $P$ row vector. $P$ must be greater than 2 . Angle units are in degrees. Phi angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Theta Angles (deg) - Theta angle coordinates of custom antenna radiation pattern 0:180 | real-valued 1-by-Q row vector

Theta angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by$Q$ row vector. $Q$ must be greater than 2 . Angle units are in degrees. Theta angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Magnitude pattern (dB) - Magnitude of combined antenna radiation pattern
zeros $(181,361)$ (default) | real-valued $Q$-by- $P$ matrix | real-valued $Q$-by- $P$-by-L array

Magnitude of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector $(\mathbf{H z})$.

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector (Hz) parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (Hz) parameter.


## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Phase pattern (deg) - Custom antenna radiation phase pattern
zeros $(181,361)$ (default) | real-valued $Q$-by- $P$ matrix | real-valued $Q$-by- $P$-by-L array

Phase of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector ( $\mathbf{H z}$ ).

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (


## Dependencies

To enable this parameter, set Element type to Custom Antenna.
MatchArrayNormal - Rotate antenna element to array normal on (default) | off

Select this check box to rotate the antenna element pattern to align with the array normal. When not selected, the element pattern is not rotated.

When the antenna is used in an antenna array and the Input Pattern Coordinate System parameter is az-el, selecting this check box rotates the pattern so that the $x$-axis of the element coordinate system points along the array normal. Not selecting uses the element pattern without the rotation.

When the antenna is used in an antenna array and Input Pattern Coordinate System is set to phitheta, selecting this check box rotates the pattern so that the $z$-axis of the element coordinate system points along the array normal.

Use the parameter in conjunction with the Array normal parameter of the URA and UCA arrays.

## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Polar pattern frequencies (Hz) - Polar pattern microphone response frequencies
1e3 (default) | real scalar | real-valued 1-by-L row vector

Polar pattern microphone response frequencies, specified as a real scalar, or a real-valued, 1-by-L vector. The response frequencies lie within the frequency range specified by the Operating
frequency vector $(\mathrm{Hz})$ vector.

## Dependencies

To enable this parameter, set Element type set to Custom Microphone.
Polar pattern angles (deg) - Polar pattern response angles
[-180:180] (default) | real-valued -by-P row vector

Specify the polar pattern response angles, as a 1-by- $P$ vector. The angles are measured from the central pickup axis of the microphone and must be between $-180^{\circ}$ and $180^{\circ}$, inclusive.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.
Polar pattern (dB) - Custom microphone polar response
zeros ( 1,361 ) (default) | real-valued $L$-by- $P$ matrix

Specify the magnitude of the custom microphone element polar patterns as an $L$-by- $P$ matrix. $L$ is the number of frequencies specified in Polar pattern frequencies $\mathbf{( H z )} . P$ is the number of angles
specified in Polar pattern angles (deg). Each row of the matrix represents the magnitude of the polar pattern measured at the corresponding frequency specified in Polar pattern frequencies (Hz) and all angles specified in Polar pattern angles (deg). The pattern is measured in the azimuth plane. In the azimuth plane, the elevation angle is $0^{\circ}$ and the central pickup axis is $0^{\circ}$ degrees azimuth and $0^{\circ}$ degrees elevation. The polar pattern is symmetric around the central axis. You can construct the microphone response pattern in 3-D space from the polar pattern.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.

## Array Parameters

Geometry - Array geometry
ULA (default) | URA | UCA | Conformal Array

Array geometry, specified as one of

- ULA - Uniform linear array
- URA - Uniform rectangular array
- UCA - Uniform circular array
- Conformal Array - arbitrary element positions

Number of elements - Number of array elements
2 for ULA arrays and 5 for UCA arrays (default) | integer greater than or equal to 2

The number of array elements for ULA or UCA arrays, specified as an integer greater than or equal to 2.

## Dependencies

To enable this parameter, set Geometry to ULA or UCA.
Element spacing (m) - Spacing between array elements
0.5 for ULA arrays and [0.5,0.5] for URA arrays (default) | positive scalar for ULA or URA arrays | 2 -element vector of positive values for URA arrays

Spacing between adjacent array elements:

- ULA - specify the spacing between two adjacent elements in the array as a positive scalar.
- URA - specify the spacing as a positive scalar or a 1 -by-2 vector of positive values. If Element spacing (m) is a scalar, the row and column spacings are equal. If Element spacing (m) is a vector, the vector has the form [SpacingBetweenArrayRows, SpacingBetweenArrayColumns].


## Dependencies

To enable this parameter, set Geometry to ULA or URA.
Array axis - Linear axis direction of ULA
$y$ (default) $|x| z$

Linear axis direction of ULA, specified as $y$, $x$, or $z$. All ULA array elements are uniformly spaced along this axis in the local array coordinate system.

## Dependencies

- To enable this parameter, set Geometry to ULA.
- This parameter is also enabled when the block only supports ULA arrays.

Array size - Dimensions of URA array

## [2,2] (default) | positive integer | 1-by-2 vector of positive integers

Dimensions of a URA array, specified as a positive integer or 1-by-2 vector of positive integers.

- If Array size is a 1 -by- 2 vector, the vector has the form [NumberOfArrayRows, NumberOfArrayColumns].
- If Array size is an integer, the array has the same number of elements in each row and column.

For a URA, array elements are indexed from top to bottom along the leftmost array column, and continued to the next columns from left to right. In this figure, the Array size value of [3, 2] creates an array having three rows and two columns.

## Size and Element Indexing Order

for Uniform Rectangular Arrays
Example: Size $=[3,2]$


## Dependencies

To enable this parameter, set Geometry to URA.
Element lattice - Lattice of URA element positions
Rectangular (default) | Triangular

Lattice of URA element positions, specified as Rectangular or Triangular.

- Rectangular - Aligns all the elements in row and column directions.
- Triangular - Shifts the even-row elements of a rectangular lattice toward the positive row-axis direction. The displacement is one-half the element spacing along the row dimension.


## Dependencies

To enable this parameter, set Geometry to URA.
Array normal - Array normal direction
$x$ for URA arrays or $z$ for UCA arrays (default) | y

Array normal direction, specified as $x, y$, or $z$.
Elements of planar arrays lie in a plane orthogonal to the selected array normal direction. Element boresight directions point along the array normal direction.

| Array Normal Parameter Value | Element Positions and Boresight Directions |
| :--- | :--- |
| x | Array elements lie in the $y z$-plane. All element <br> boresight vectors point along the $x$-axis. |
| y | Array elements lie in the $z x$-plane. All element <br> boresight vectors point along the $y$-axis. |
| $z$ | Array elements lie in the $x y$-plane. All element <br> boresight vectors point along the $z$-axis. |

## Dependencies

To enable this parameter, set Geometry to URA or UCA.
Radius of UCA (m) - UCA array radius
0.5 (default) | positive scalar

Radius of UCA array, specified as a positive scalar.

## Dependencies

To enable this parameter, set Geometry to UCA.

## Element positions (m) - Positions of conformal array elements <br> [0;0;0] (default) | 3-by-Nmatrix of real values

Positions of the elements in a conformal array, specified as a 3 -by- $N$ matrix of real values, where $N$ is the number of elements in the conformal array. Each column of this matrix represents the position [ $x ; y ; z$ ] of an array element in the array local coordinate system. The origin of the local coordinate system is ( $0,0,0$ ). Units are in meters.

## Dependencies

To enable this parameter set Geometry to Conformal Array.

## Data Types: double

Element normals (deg) - Direction of conformal array element normal vectors
[0;0] | 2-by-1 column vector | 2-by-N matrix

Direction of element normal vectors in a conformal array, specified as a 2 -by- 1 column vector or a 2 -by- $N$ matrix. $N$ indicates the number of elements in the array. If the parameter value is a matrix, each
column specifies the normal direction of the corresponding element in the form [azimuth;elevation] with respect to the local coordinate system. The local coordinate system aligns the positive $x$-axis with the direction normal to the conformal array. If the parameter value is a 2-by-1 column vector, the same pointing direction is used for all array elements.

You can use the Element positions (m) and Element normals (deg) parameters to represent any arrangement in which pairs of elements differ by certain transformations. The transformations can combine translation, azimuth rotation, and elevation rotation. However, you cannot use transformations that require rotation about the normal direction.

To enable this parameter, set Geometry to Conformal Array.
Data Types: double
Taper - Array element tapers
1 (default) | complex scalar | complex-valued row vector

Specify element tapering as a complex-valued scalar or a complex-valued 1-by- $N$ row vector. In this vector, $N$ represents the number of elements in the array.

Also known as element weights, tapers multiply the array element responses. Tapers modify both amplitude and phase of the response to reduce side lobes or steer the main response axis.

If Taper is a scalar, the same weight is applied to each element. If Taper is a vector, a weight from the vector is applied to the corresponding sensor element. The number of weights must match the number of elements of the array.

Data Types: double

## Version History

Introduced in R2014b

## See Also

phased.BeamscanEstimator2D|phased.ConformalArray|phased.UCA|phased.ULA| phased.URA

## Beamspace ESPRIT DOA

Beamspace ESPRIT direction of arrival (DOA) estimator for ULA


## Libraries:

Phased Array System Toolbox / Direction of Arrival

## Description

The Beamspace ESPRIT DOA block estimates the direction of arrival of a specified number of narrowband signals incident on a uniform linear array using the estimation of signal parameters via rotational invariance technique (ESPRIT) algorithm in beamspace.

## Ports

## Input

Port_1 - Input signal
$N$-by-M complex-valued matrix
Input signal, specified as an $N$-by- $M$ complex-valued matrix. $N$ corresponds to the number of samples. $M$ corresponds to the number data channels.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
Data Types: single | double
Output
Ang - Estimated broadside direction-of-arrival angles
$M$-by-1 real-valued vector
Estimated broadside direction-of-arrival angles, returned as an $M$-by-1 real-valued vector. Units are in degrees.
Data Types: double

## Parameters

## Main Tab

Signal propagation speed (m/s) - Signal propagation speed
physconst('LightSpeed') (default) | real-valued positive scalar

Signal propagation speed, specified as a real-valued positive scalar. The default value of the speed of light is the value returned by physconst ('LightSpeed'). Units are in meters per second.
Example: 3e8

## Data Types: double

Operating frequency $(\mathrm{Hz})$ - System operating frequency
3e8 (default) | positive real scalar

System operating frequency, specified as a positive scalar. Units are in Hz .
Number of signals - Number of signals
1 (default) | positive integer scalar
Specify the number of signals as a positive integer scalar.
Spatial smoothing - Enable spatial smoothing
0 (default) | non-negative integer

Specify the amount of averaging used by spatial smoothing to estimate the covariance matrix as a nonnegative integer. Each increase in smoothing handles one extra coherent source, but reduces the effective number of elements by one. The maximum value of this parameter is $N-2$, where $N$ is the number of sensors in the ULA.

Type of least squares method - Type of least squares method

## TLS (default) | LS

Specify the least squares method used for ESPRIT as one of TLS or LS where TLS refers to total least squares and LSrefers to least squares.

Beam fan center direction (deg) - Beam fan center direction
0 (default)
Specify the direction of the center of the beam fan, in degrees, as a real scalar value between $-90^{\circ}$ and $90^{\circ}$.

Source of number of beams - Source of number of beams

## Auto (default) | Property

Specify the source of the number of beams as one of Auto or Property. If you set this parameter to Auto, the number of beams equals $N-L$, where $N$ is the number of array elements and $L$ is the value of Spatial smoothing.

Number of beams - Number of beams

## 2

Specify the number of beams as a positive scalar integer. The lower the number of beams, the greater the reduction in computational cost.

## Dependencies

This parameter appears when you set Source of number of beams to Property.

## Simulate using - Block simulation method <br> Interpreted Execution (default)|Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).
Programmatic Use
Block Parameter:SimulateUsing
Type:enum
Values:Interpreted Execution, Code Generation
Default:Interpreted Execution

## Sensor Array Tab

Specify sensor array as - Method to specify array
Array (no subarrays) (default)|MATLAB expression

Method to specify array, specified as Array (no subarrays) or MATLAB expression.

- Array (no subarrays) - use the block parameters to specify the array.
- MATLAB expression - create the array using a MATLAB expression.


## Element Parameters

Element type - Array element types
Isotropic Antenna (default)|Cardioid Antenna|Cosine Antenna|Custom Antenna| Gaussian Antenna|Sinc Antenna|Omni Microphone|Custom Microphone

Antenna or microphone type, specified as one of the following:

- Isotropic Antenna
- Cardioid Antenna
- Cosine Antenna
- Custom Antenna
- Gaussian Antenna
- Sinc Antenna
- Omni Microphone
- Custom Microphone

Operating frequency range $(\mathbf{H z})$ - Operating frequency range of the antenna or microphone element
[0,1e20] (default) | real-valued 1-by-2 row vector

Specify the operating frequency range of the antenna or microphone element as a 1-by-2 row vector in the form [LowerBound, UpperBound]. The element has no response outside this frequency range. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Isotropic Antenna, Cosine Antenna, or Omni Microphone.

Baffle the back of the element - Set back response of an Isotropic Antenna element or an Omni Microphone element to zero
off (default) | on

Select this check box to baffle the back response of the element. When back baffled, the responses at all azimuth angles beyond $\pm 90^{\circ}$ from broadside are set to zero. The broadside direction is defined as $0^{\circ}$ azimuth angle and $0^{\circ}$ elevation angle.

## Dependencies

To enable this check box, set Element type to Isotropic Antenna or Omni Microphone.
Null axis direction - Null axis direction
$-x$ (default) $|+x|+y|-y|+z \mid-z$

## Dependencies

To enable this parameter, set Element type to Cardioid Antenna.

Exponent of cosine pattern - Exponents of azimuth and elevation cosine patterns [1.5 1.5] (default) | nonnegative scalar | real-valued 1-by-2 matrix of nonnegative values

Specify the exponents of the cosine pattern as a nonnegative scalar or a real-valued 1-by-2 matrix of nonnegative values. When Exponent of cosine pattern is a 1-by-2 vector, the first element is the exponent in the azimuth direction and the second element is the exponent in the elevation direction. When you set this parameter to a scalar, both the azimuth direction and elevation direction cosine patterns are raised to the same power.

## Dependencies

To enable this parameter, set Element type to Cosine Antenna.
Operating frequency vector ( Hz ) - Operating frequency range of custom antenna or microphone elements
[0,1e20] (default) | real-valued row vector

Specify the frequencies at which to set antenna and microphone frequency responses as a 1-by-L row vector of increasing real values. The antenna or microphone element has no response outside the frequency range specified by the minimum and maximum elements of this vector. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone. Use Frequency responses (dB) to set the responses at these frequencies.

Frequency responses (dB) - Antenna and microphone frequency response
[0,0] (default) | real-valued row vector

Frequency response of a custom antenna or custom microphone for the frequencies defined by the Operating frequency vector ( $\mathbf{H z}$ ) parameter. The dimensions of Frequency responses (dB) must match the dimensions of the vector specified by the Operating frequency vector $(\mathbf{H z})$ parameter.

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone.
Input Pattern Coordinate System - Coordinate system of custom antenna pattern az-el (default) | phi-theta

Coordinate system of custom antenna pattern, specified az-el or phi-theta. When you specify azel, use the Azimuth angles (deg) and Elevations angles (deg) parameters to specify the coordinates of the pattern points. When you specify phi-theta, use the Phi angles (deg) and Theta angles (deg) parameters to specify the coordinates of the pattern points.

## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Azimuth angles (deg) - Azimuth angles of antenna radiation pattern
[-180:180] (default) | real-valued row vector

Specify the azimuth angles at which to calculate the antenna radiation pattern as a 1 -by- $P$ row vector. $P$ must be greater than 2. Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to az-el.

Elevation angles (deg) - Elevation angles of antenna radiation pattern
[-90:90] (default) | real-valued row vector

Specify the elevation angles at which to compute the radiation pattern as a 1-by- $Q$ vector. $Q$ must be greater than 2. Angle units are in degrees. Elevation angles must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to az-el.

Phi Angles (deg) - Phi angle coordinates of custom antenna radiation pattern $0: 360$ | real-valued 1-by-P row vector

Phi angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by- $P$ row vector. $P$ must be greater than 2 . Angle units are in degrees. Phi angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Theta Angles (deg) - Theta angle coordinates of custom antenna radiation pattern
0:180 | real-valued 1-by-Q row vector

Theta angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by$Q$ row vector. $Q$ must be greater than 2 . Angle units are in degrees. Theta angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input
Pattern Coordinate System parameter to phi-theta.
Magnitude pattern (dB) - Magnitude of combined antenna radiation pattern zeros $(181,361)$ (default) | real-valued $Q$-by- $P$ matrix | real-valued $Q$-by- $P$-by-L array

Magnitude of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector ( $\mathbf{H z}$ ).

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (Hz) parameter.


## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Phase pattern (deg) - Custom antenna radiation phase pattern
zeros $(181,361)$ (default) | real-valued $Q$-by-P matrix | real-valued $Q$-by- $P$-by-L array

Phase of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector ( $\mathbf{H z}$ ).

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (


## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Align element normal with array normal - Align element normal with array normal
on (default) | off

## Dependencies

This parameter is enabled when Element type is set to Custom Antenna.
Radiation pattern beamwidth (deg) - Radiation pattern beamwidth [10,10] (default)

## Dependencies

This parameter is enabled when Element type is set to Gaussian Antenna.
Polar pattern frequencies $(\mathbf{H z})$ - Polar pattern microphone response frequencies
1 e3 (default) | real scalar | real-valued 1-by- $L$ row vector

Polar pattern microphone response frequencies, specified as a real scalar, or a real-valued, 1-by- $L$ vector. The response frequencies lie within the frequency range specified by the Operating
frequency vector ( $\mathbf{H z}$ ) vector.

## Dependencies

To enable this parameter, set Element type set to Custom Microphone.
Polar pattern angles (deg) - Polar pattern response angles
[-180:180] (default) | real-valued -by-P row vector

Specify the polar pattern response angles, as a 1-by- $P$ vector. The angles are measured from the central pickup axis of the microphone and must be between $-180^{\circ}$ and $180^{\circ}$, inclusive.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.
Polar pattern (dB) - Custom microphone polar response
zeros ( 1,361 ) (default) | real-valued $L$-by-P matrix

Specify the magnitude of the custom microphone element polar patterns as an $L$-by- $P$ matrix. $L$ is the number of frequencies specified in Polar pattern frequencies (Hz). $P$ is the number of angles specified in Polar pattern angles (deg). Each row of the matrix represents the magnitude of the polar pattern measured at the corresponding frequency specified in Polar pattern frequencies (Hz) and all angles specified in Polar pattern angles (deg). The pattern is measured in the azimuth plane. In the azimuth plane, the elevation angle is $0^{\circ}$ and the central pickup axis is $0^{\circ}$ degrees azimuth and $0^{\circ}$ degrees elevation. The polar pattern is symmetric around the central axis. You can construct the microphone response pattern in 3-D space from the polar pattern.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.

## ULA Parameters

Number of elements - Number of array elements in $U$
2 (default) | positive integer greater than or equal to two

The number of array elements for ULA arrays, specified as an integer greater than or equal to two.

## Example: 11

Data Types: double
Element spacing - Distance between ULA elements
0.5 (default) | positive scalar

Distance between adjacent ULA elements, specified as a positive scalar. Units are in meters.
Example: 1.5
Array axis - Linear axis direction of ULA
$y$ (default) $|x| z$

Linear axis direction of ULA, specified as $y$, $x$, or $z$. All ULA array elements are uniformly spaced along this axis in the local array coordinate system.

Dependencies

- To enable this parameter, set Geometry to ULA.
- This parameter is also enabled when the block only supports ULA arrays.

Taper - ULA array taper
1 (default) | complex-valued vector

Tapers, also known as element weights, are applied to sensor elements in the array. Tapers are used to modify both the amplitude and phase of the transmitted or received data.

Specify element tapering as a complex-valued scalar or a complex-valued 1-by- $N$ row vector. In this vector, $N$ represents the number of elements in the array. If Taper is a scalar, the same weight is applied to each element. If Taper is a vector, a weight from the vector is applied to the corresponding sensor element. A weight must be applied to each element in the sensor array.
Example: [0.5;1;0.5]
Data Types: double
Expression - MATLAB expression used to create an array
Phased Array System Toolbox array System object

MATLAB expression used to create a ULA array, specified as a valid Phased Array System Toolbox array System object.

Example: phased.ULA('NumElements ', 13)
Dependencies
To enable this parameter, set Specify sensor array as to MATLAB expression.

## Version History

Introduced in R2014b

## See Also

phased. BeamspaceESPRITEstimator

## CFAR Detector

Constant false alarm rate (CFAR) detector


## Libraries:

Phased Array System Toolbox / Detection

## Description

The CFAR Detector block implements a one-dimensional constant false-alarm rate (CFAR) detector. Detection processing is performed on selected elements (called cells) of the input data. A detection is declared when an image cell value exceeds a threshold. To maintain a constant false alarm-rate, the threshold is set to a multiple of the image noise power. The detector estimates noise power for a cell-under-test (CUT) from surrounding cells using one of three cell averaging methods, or an order statistics method. The cell-averaging methods are cell averaging (CA), greatest-of cell averaging (GOCA), or smallest-of cell averaging (SOCA).

For more information about CFAR detectors, see [1].
For each test cell, the detector:
1 estimates the noise statistic from the cell values in the training band surrounding the CUT cell.
2 computes the threshold by multiplying the noise estimate by the threshold factor.
3 compares the CUT cell value to the threshold to determine whether a target is present or absent. If the value is greater than the threshold, a target is present.

## Ports

## Input

$\mathbf{X}$ - Cell matrix
real-valued $M$-by-1 column vector | real-valued $M$-by- $N$ matrix
Cell matrix, specified as a real-valued $M$-by- 1 column vector or a real-valued $M$-by- $N$ matrix.
The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

## Data Types: single | double

Idx - Index of cells under test
real-valued length- $D$ vector
Cells-under-test (CUT), specified as a real-valued length- $D$ vector. Indices specify the input elements or cells under test on which to perform detection processing. When X is a vector, Idx specifies the element. When $X$ is a matrix, Idx specifies the row of the element. The same index applies to all columns of the matrix. Detection is performed independently along each column of Xww for the indices specified in Idx.

Data Types: double
K - Threshold factor
positive scalar
Threshold factor, used to calculate the detection threshold, specified as a positive scalar.
Dependencies
To enable this port, set the Threshold factor method parameter to Input port.
Data Types: double

## Output

$\mathbf{Y}$ - Detection results
$D$-by-1 vector | $D$-by- $N$ matrix | 1-by-L | 2 -by- $L$ matrix
The format of $Y$ depends on the Output format property.

- When Output format is 'Cut result', Y is a $D$-by- 1 vector or a $D$-by- $N$ matrix containing logical detection results. $D$ is the length of $\operatorname{Idx}$ and $N$ is the number of columns of X . The rows of $Y$ correspond to the rows in Idx. For each row, $Y$ contains 1 in a column if there is a detection in the corresponding column of X . Otherwise, Y contains a 0.
- When Output format is 'Detection report', Y is a 1-by-L vector or a 2 -by- $L$ matrix containing detections indices. $L$ is the number of detections found in the input data. When X is a column vector, Y contains the index for each detection in X . When X is a matrix, Y contains the row and column indices of each detection in $X$. Each column of $Y$ has the form [detrow; detcol]. When the Source of number of detections property is set to 'Property', $L$ equals the value of the Maximum number of detections parameter. If the number of actual detections is less than this value, columns without detections are set to NaN .

Data Types: double
Th - Detection threshold
scalar
Detection threshold applied to cells under test, returned as a scalar.

- When Output format is 'CUT result', Th port outputs the detection threshold whenever an element of Y is 1 and NaN whenever an element of Y is 0 . The output of Th has the same size as Y .
- When Output format is 'Detection index', the Th port outputs a detection threshold for each corresponding detection in Y.When the Source of the number of detections parameter is set to 'Property', the number of detections is set by the Maximum number of detections parameter. If the number of actual detections is less than this value, the columns without detections are set to NaN .

Dependencies
To enable this port, select the Output detection threshold check box.
Data Types: double
$\mathbf{N}$ - Estimated noise power
positive scalar

Estimated noise power for each detected cell under test, returned as a positive scalar.

- When Output format is 'CUT result', N returns a noise power estimate when Y is 1 and NaN whenever Y is zero. The output from port N has the same size as Y .
- When Output format is 'Detection index', M returns a noise power estimate for each corresponding detection in Y . When the Source of the number of detections property is set to 'Property ', $L$ equals the value of the Maximum number of detections parameter. If the number of actual detections is less than this value, columns without detections are set to NaN .


## Dependencies

To enable this port, select the Output estimated noise power check box.
Data Types: double

## Parameters

CFAR algorithm - CFAR algorithm
CA (default) | GOCA | SOCA | OS
Specify the CFAR detection algorithm using one of the values

| CA | Cell-averaging |
| :--- | :--- |
| GOCA | Greatest-of cell averaging |
| OS | Order statistic |
| SOCA | Smallest-of cell averaging |

Number of guard cells - Number of guard cells

## 2 (default)

Specify the number of guard cells used in training as an even integer. This parameter specifies the total number of cells on both sides of the cell under test.

Number of training cells - Number of training cells

## 2 (default)

Specify the number of training cells used in training as an even integer. Whenever possible, the training cells are equally divided before and after the cell under test.

Rank of order statistic - Rank of order statistic

## 1 (default)

Specify the rank of the order statistic as a positive integer scalar. The value must be less than or equal to the value of Number of training cells.

## Dependencies

This parameter appears when CFAR algorithm is set to OS.

Threshold factor method - Methods of obtaining threshold factor

## Auto (default)|Input port|Custom

Specify whether the threshold factor comes from an automatic calculation, the Custom threshold factor parameter, or an input argument. Values of this parameter are:

| Auto | The application calculates the threshold factor automatically <br> based on the desired probability of false alarm specified in <br> the Probability of false alarm parameter. The calculation <br> assumes each independent signal in the input is a single pulse <br> coming out of a square law detector with no pulse integration. <br> The calculation also assumes the noise is white Gaussian. |
| :--- | :--- |
| Custom | The Custom threshold factor parameter specifies the <br> threshold factor. |
| Input port | Threshold factor is set using the input port K. This port <br> appears only when Threshold factor method is set to <br> Input port. |

Probability of false alarm - Desired probability of false alarm

## 0.1 (default)

Specify the desired probability of false alarm as a scalar between 0 and 1 (not inclusive).

## Dependencies

This parameter appears only when you set Threshold factor method to Auto.
Custom threshold factor - Custom threshold factor
1 (default)
Specify the custom threshold factor as a positive scalar.

## Dependencies

This parameter appears only when you set Threshold factor method to Custom.
Output format - Format of detection results

## CUT result (default)|Detection index

Specify the format of detection results returned in output port Y as CUT result or Detection index.

- When set to CUT result, the results are logical detection values (1 or 0) for each tested cell. 1 indicates that the value of the tested cell exceeds a detection threshold.
- When set to Detection index, the results form a vector or matrix containing the indices of tested cells which exceed a detection threshold.

Output detection threshold - Output detection threshold
off (default) | on

Select this check box to create an output port Th containing the detection threshold.
Output estimated noise power - Output estimated noise power
off (default) | on
Select this check box to create an output port N containing the estimated noise.
Source of the number of detections - Source of the number of detections
Auto (default) | Property
Specify the source of the number of detections as Auto or Property. When you select Auto, the number of detection indices reported is the total number of cells under test that have detections. If you select Property, the number of reported detections is determined by the value of the Maximum number of detections parameter.

## Dependencies

To enable this parameter, set the Output format parameter to Detection index.
Maximum number of detections - Maximum number of detections to report
1 (default)
Specify the maximum number of detection indices to report as a positive integer.

## Dependencies

To enable this parameter, set the Output format parameter to Detection index and the Source of the number of detections parameter to Property.

Simulate using - Block simulation method
Interpreted Execution (default) |Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).
Programmatic Use
Block Parameter:SimulateUsing
Type:enum
Values:Interpreted Execution, Code Generation
Default:Interpreted Execution

## Version History

Introduced in R2014b

## See Also

## Functions

npwgnthresh | rocpfa
Objects
phased.CFARDetector | phased.CFARDetector2D

## Blocks

2-D CFAR Detector

## 2-D CFAR Detector

Two-dimensional constant false alarm rate (CFAR) detector

## Libraries:

Phased Array System Toolbox / Detection

## Description

The 2-D CFAR Detector block implements a constant false-alarm rate detector for two dimensional image data. A detection is declared when an image cell value exceeds a threshold. To maintain a constant false alarm-rate, the threshold is set to a multiple of the image noise power. The detector estimates noise power from neighboring cells surrounding the cell-under-test (CUT) using one of three cell averaging methods, or an order statistics method. The cell-averaging methods are cellaveraging (CA), greatest-of cell averaging (GOCA), or smallest-of cell averaging (SOCA).

For each test cell, the detector:
1 estimates the noise statistic from the cell values in the training band surrounding the CUT cell.
2 computes the threshold by multiplying the noise estimate by the threshold factor.
3 compares the CUT cell value to the threshold to determine whether a target is present or absent. If the value is greater than the threshold, a target is present.

## Ports

## Input

X - Input image
real $M$-by- $N$ matrix | real $M$-by- $N$-by- $P$ array
Input image, specified as a real $M$-by- $N$ matrix or real $M$-by- $N$-by- $P$ array. $M$ and $N$ represent the rows and columns of the matrix. Each page is a different 2-D signal.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
Data Types: double
idx - Location of test cells
2-by-L matrix of positive integers
Location of test cells, specified as a 2-by- $L$ matrix of positive integers, where $L$ is the number of test cells. Each column of idx specifies the row and column index of a CUT cell. The locations of CUT cells are restricted so that their training regions lie completely within the input images.

Data Types: double
K - Detection threshold factor
positive scalar
Threshold factor used to calculate the detection threshold, specified as a positive scalar.
Dependencies
To enable this port, set the Threshold factor method parameter to 'Input port'
Data Types: double

## Output

$\mathbf{Y}$ - Detection results
logical matrix (default) | real-valued matrix
Detection results, whose format depends on the Output Format property

- When OutputFormat is 'Cut result', Y is a $D$-by- $P$ matrix containing logical detection results for cells under test. $D$ is the length of cutidx and $P$ is the number of pages of $X$. The rows of $Y$ correspond to the rows of cutidx. For each row, Y contains 1 in a column if there is a detection in the corresponding cell in $X$. Otherwise, $Y$ contains a 0.
- When OutputFormat is Detection index, Y is a $K$-by- $L$ matrix containing detections indices. $K$ is the number of dimensions of $X$. $L$ is the number of detections found in the input data. When $X$ is a matrix, Y contains the row and column indices of each detection in X in the form [detrow; detcol]. When X is an array, Y contains the row, column, and page indices of each detection in X in the form [detrow; detcol; detpage]. When the NumDetectionsSource property is set to 'Property', $L$ equals the value of the NumDetections property. If the number of actual detections is less than this value, columns without detections are set to NaN .

Data Types: double
Th - Computed detection threshold
real-valued matrix
Computed detection threshold for each detected cell, returned as a real-valued matrix. Th has the same dimensions as Y .

- When OutputFormat is 'CUT result', Th returns the detection threshold whenever an element of $Y$ is 1 and $N a N$ whenever an element of $Y$ is 0 .
- When OutputFormat is Detection index, th returns a detection threshold for each corresponding detection in Y. When the NumDetectionsSource property is set to 'Property', $L$ equals the value of the NumDetections property. If the number of actual detections is less than this value, columns without detections are set to NaN .


## Dependencies

To enable this port, select the Output detection threshold checkbox.
Data Types: double
$\mathbf{N}$ - Estimated noise power
real-valued matrix

Estimated noise power for each detected cell, returned as a real-valued matrix. noise has the same dimensions as Y .

- When OutputFormat is 'CUT result', noise returns the noise power whenever an element of $Y$ is 1 and NaN whenever an element of Y is 0 .
- When OutputFormat is 'Detection index', noise returns a noise power for each corresponding detection in Y. When the NumDetectionsSource property is set to 'Property', $L$ equals the value of the NumDetections property. If the number of actual detections is less than this value, columns without detections are set to NaN .


## Dependencies

To enable this port, select the Output estimated noise power checkbox.
Data Types: double

## Parameters

CFAR algorithm - Noise power estimation algorithm
CA (default) | GOCA | SOCA | OS

Noise power estimation algorithm, specified as CA, GOCA, SOCA, or OS. For CA, GOCA, SOCA, the noise power is the sample mean derived from the training band. For $0 S$, the noise power is the $k$ th cell value obtained from a numerical ordering of all training cell values. Set $k$ by the Rank of order statistic parameter. See "Training cells" on page 3-68.

| Averaging Method | Description |
| :--- | :--- |
| CA - Cell-averaging algorithm | Computes the sample mean of all training cells <br> surrounding the CUT cell. |
| GOCA - Greatest-of cell-averaging algorithm | Splits the 2-D training window surrounding the <br> CUT cell into left and right halves. Then, the <br> algorithm computes the sample mean for each <br> half and selects the largest mean. |
| SOCA - Smallest-of cell-averaging algorithm | Splits the 2-D training window surrounding the <br> CUT cell into left and right halves. Then, the <br> algorithm computes the sample mean for each <br> half and selects the smallest mean. |
| OS - Order statistic algorithm | Sorts training cells in ascending order of numeric <br> values. Then the algorithm selects the $k$ th value <br> from the list. $k$ is the rank specified by the Rank <br> parameter. |

Rank of order statistic - Rank of order statistic
1 (default) | positive integer

Specify the rank of the order statistic used in the 2-D CFAR algorithm as a positive integer. The value of this parameter must lie between 1 and $N_{\text {train, }}$ where $N_{\text {train }}$ is the number of training cells. A value of 1 selects the smallest value in the training region.

## Dependencies

To enable this parameter, set the CFAR Algorithm parameter to OS.
Size in cells of the guard region band - Widths of guard band
[1,1] (default) | nonnegative integer scalar | 2-element vector of positive integers

The number of row and column guard cells on each side of the cell under test as nonnegative integers. The first element specifies the guard band size along the row dimension. The second element specifies the guard band size along the row dimension. Specifying Size in cells of the guard region band as a scalar is equivalent to specifying a vector with the same value for both dimensions. For example, a value of [11], indicates that there is a one-guard-cell-wide region surrounding each CUT cell.

Size in cells of the training region band - Widths of training band [1,1] (default) | nonnegative integer scalar | 2 -element vector of positive integers

Size in cells of the training region band, specified as a nonnegative integer or 1-by-2 matrix of nonnegative integers. The first element specifies the training band size along the row dimension, and the second along the column dimension. Specifying Size in cells of the training region band as a scalar is equivalent to specifying a vector with the same value for both dimensions. For example, a value of [11] indicates that there is a one-training-cell-wide region surrounding the guard region for each cell under test.

Threshold factor method - Method to determine threshold factor
Auto (default)|Input port|Custom

Method to determine threshold factor, specified as Auto, Input port, or Custom.

- When you choose Auto, the threshold factor is determined from the estimated noise statistic and the probability of false alarm.
- When you choose Input Port, set the threshold factor using the K input port.
- When you choose Custom, set the threshold factor using the Custom threshold factor parameter.

Custom threshold factor - Custom threshold factor
1 (default) | positive scalar

Custom threshold factor, specified as a positive scalar.

## Dependencies

To enable this parameter, set the Threshold factor method parameter to Custom.
Probability of false alarm - Probability of false alarm
0.1 (default) | real scalar between 0 and 1

Probability of false alarm, specified as a real scalar between 0 and 1 . You can calculate the threshold factor from the required probability of false alarm.

## Dependencies

To enable this parameter, set the Threshold factor method property to Auto.
OutputFormat - Format of detection results
CUT result (default)|Detection index

Format of detection results, specified as CUT result or Detection index.

- When set to 'CUT result', the detection results are logical detection values (1 or 0 ) for each tested cell.
- When set to 'Detection index', the results form a vector or matrix containing the indices of tested cells that exceed a detection threshold.

Output threshold detection - Enable detection threshold output off (default) | on

Select this check box to enable the output of detection thresholds via the Th output port.
Output estimated noise power - Enable detection threshold output off (default) | on

Select this check box to enable the output of estimated noise power via the $N$ output port.
Source of the number of detections - Source of the number of detections to report Auto (default) | Property

Source of the number of detections, specified as Auto or Property. When you select Auto, the number of detection indices reported is the total number of cells under test that have detections. If you select Property, the number of reported detections is determined by the value of the Maximum number of detections parameter.

## Dependencies

To enable this parameter, set the Output format parameter to Detection index.

## Data Types: char

Maximum number of detections - Maximum number of detection indices to report
1 (default) | positive integer

Maximum number of detection indices to report, specified as a positive integer.

## Dependencies

To enable this parameter, set the Output format parameter to Detection index and the Source of the number of detections parameter to Property.
Data Types: double

## Algorithms

CFAR 2-D requires an estimate of the noise power. Noise power is computed from cells that are assumed not to contain any target signal. These cells are the training cells. Training cells form a band around the cell-under-test (CUT) cell but may be separated from the CUT cell by a guard band. The detection threshold is computed by multiplying the noise power by the threshold factor.


For GOCA and SOCA averaging, the noise power is derived from the mean value of one of the left or right halves of the training cell region.

Because the number of columns in the training region is odd, the cells in the middle column are assigned equally to either the left or right half.

When using the order-statistic method, the rank cannot be larger than the number of cells in the training cell region, $N_{\text {train }}$. You can compute $N_{\text {train }}$.

- $N_{T C}$ is the number of training band columns.
- $N_{T R}$ is the number of training band rows.
- $N_{G C}$ is the number of guard band columns.
- $N_{G R}$ is the number of guard band rows.

The total number of cells in the combined training region, guard region, and CUT cell is $N_{\text {total }}=\left(2 N_{T C}\right.$ $\left.+2 N_{G C}+1\right)\left(2 N_{T R}+2 N_{G R}+1\right)$.

The total number of cells in the combined guard region and CUT cell is $N_{\text {guard }}=\left(2 N_{G C}+1\right)\left(2 N_{G R}+1\right)$.
The number of training cells is $N_{\text {train }}=N_{\text {total }}-N_{\text {guard }}$.
By construction, the number of training cells is always even. Therefore, to implement a median filter, you can choose a rank of $N_{\text {train }} / 2$ or $N_{\text {train }} / 2+1$.

## Version History <br> Introduced in R2016b

## See Also

## Functions

npwgnthresh | rocpfa

## Objects

phased.CFARDetector | phased.CFARDetector2D

## Blocks

CFAR Detector

## Custom FM Waveform

Custom FM pulse waveform


## Libraries:

Phased Array System Toolbox / Waveforms

## Description

The Custom FM Waveform block generates a custom FM pulse waveform with specified pulse width, pulse repetition frequency (PRF), and sweep bandwidth. The block outputs an integer number of pulses or an integral number of samples.

## Ports

Input
PRFIdx - PRF Index
positive integer
Index to select the pulse repetition frequency (PRF), specified as a positive integer. The index selects the PRF from the predefined vector of values specified by the Pulse repetition frequency ( Hz ) parameter.
Example: 4

## Dependencies

To enable this port, select Enable PRF selection input.

## Data Types: double

FreqOffset - Frequency offset
scalar
Frequency offset in Hz , specified as a scalar.
Example: 2e3

## Dependencies

To enable this port, set Source of Frequency Offset to Input port.
Data Types: double

## Output

Y - Pulse waveform
complex-valued vector
Pulse waveform samples, returned as a complex-valued vector.
Data Types: double

PRF - Pulse repetition frequency
positive scalar
Pulse repetition frequency of current pulse, returned as a positive scalar.

## Dependencies

To enable this port, set the Output signal format parameter to Pulses and then select the Enable PRF output parameter.

Data Types: double
Coeff - Matched filter coefficients
vector | matrix
Matched filter coefficients, returned as a vector or matrix.

## Dependencies

To enable this port, select Enable Matched Filter Coefficients Output.

## Data Types: double

## Parameters

To edit block parameters interactively, use the Property Inspector. From the Simulink Toolstrip, on the Simulation tab, in the Prepare gallery, select Property Inspector.

Sample rate (Hz) - Sample rate of the output waveform
1e6 (default) | positive scalar

Sample rate of the output waveform, specified as a positive scalar. The ratio of Sample rate (Hz) to each element in the Pulse repetition frequency ( $\mathbf{H z}$ ) vector must be an integer. This restriction is equivalent to requiring that the pulse repetition interval is an integral multiple of the sample interval.

Programmatic Use<br>Block Parameter:SampleRate<br>Type:double<br>Values:positive scalar<br>Default:1e6<br>Method to specify pulse duration - Pulse duration as time or duty cycle Pulse width (default)| Duty cycle

Method to set the pulse duration, specified as Pulse width or Duty cycle. When you set this parameter to Pulse width, the pulse duration is set using the Pulse width (s) parameter. When you set this parameter to Duty cycle, the pulse duration is computed from the values of the Pulse repetition frequency $(\mathbf{H z})$ and Duty Cycle parameters.

Programmatic Use
Block Parameter:DurationSpecification
Type:string
Values:string
Default:'Pulse width'

Pulse width (s) - Time duration of pulse
50e-6 (default) | positive scalar

The duration of each pulse, specified as a positive scalar. Set the product of Pulse width (s) and Pulse repetition frequency to be less than or equal to one. This restriction ensures that the pulse width is smaller than the pulse repetition interval. Units are in seconds.

Example: 300e-6

## Dependencies

To enable this parameter, set the Method to specify pulse duration parameter to Pulse width.
Programmatic Use
Block Parameter:PulseWidth
Type:double
Values:string
Default:50e-6
Duty cycle - Waveform duty cycle
0.5 (default) | scalar in the range [0,1]

Waveform duty cycle, specified as a scalar in the range [0,1].
Example: 0.7

## Dependencies

To enable this parameter, set the Method to specify pulse duration parameter to Duty cycle.
Programmatic Use
Block Parameter:DutyCycle
Type:double
Values:positive scalar
Default:1e6
Pulse repetition frequency ( Hz ) - Pulse repetition frequency
le4 (default) | positive scalar

Pulse repetition frequency, $P R F$, specified as a scalar or a row vector. Units are in Hz. The pulse repetition interval, $P R I$, is the inverse of the pulse repetition frequency, $P R F$. The value of Pulse repetition frequency $(\mathbf{H z})$ must satisfy these constraints:

- The product of Pulse width and Pulse repetition frequency (Hz) must be less than or equal to one. This condition expresses the requirement that the pulse width is less than one pulse repetition interval. For the phase-coded waveform, the pulse width is the product of the chip width and number of chips.
- The ratio of sample rate to any element of Pulse repetition frequency must be an integer. This condition expresses the requirement that the number of samples in one pulse repetition interval is an integer.

You can select the value of $P R F$ by using block parameter settings alone or in conjunction with the input port, PRFIdx.

- When the Enable PRF selection input parameter is not selected, set the PRF using block parameters.
- To implement a constant $P R F$, specify Pulse repetition frequency ( Hz ) as a positive scalar.
- To implement a staggered $P R F$, specify Pulse repetition frequency ( $\mathbf{H z}$ ) as a row vector with positive values. After the waveform reaches the last element of the vector, the process continues cyclically with the first element of the vector. When PRF is staggered, the time between successive output pulses cycles through the successive values of the $P R F$ vector.
- When the Enable PRF selection input parameter is selected, you can implement a selectable $P R F$ by specifying Pulse repetition frequency ( Hz ) as a row vector with positive real-valued entries. But this time, when you execute the block, select a $P R F$ by passing an index into the $P R F$ vector into the PRFIdx port.

In all cases, the number of output samples is fixed when you set the Output signal format to Samples. When you use a varying PRF and set Output signal format to Pulses, the number of output samples can vary.

Programmatic Use
Block Parameter:PRF
Type:double
Values:positive scalar
Default:1e6
Enable PRF selection input - Select predefined PRF
off (default) | on

Select this parameter to enable the PRFIdx port.

- When enabled, pass in an index into a vector of predefined PRFs. Set predefined PRFs using the Pulse repetition frequency ( Hz ) parameter.
- When not enabled, the block cycles through the vector of PRFs specified by the Pulse repetition frequency ( Hz ) parameter. If Pulse repetition frequency $(\mathbf{H z})$ is a scalar, the PRF is constant.

Programmatic Use
Block Parameter:PRFSelectionInputPort
Type:logical
Values:positive scalar
Default:off
Source of simulation sample time - Source of simulation sample time
Derive from waveform parameters (default)|Inherit from Simulink engine

Source of simulation sample time, specified as Derive from waveform parameters or Inherit from Simulink engine. When set to Derive from waveform parameters, the block runs at a variable rate determined by the PRF of the selected waveform. The elapsed time is variable. When set to Inherit from Simulink engine, the block runs at a fixed rate so the elapsed time is a constant.

## Dependencies

To enable this parameter, select the Enable PRF selection input parameter.

## Programmatic Use <br> Block Parameter:SimulationTimeSource <br> Type:enum <br> Values:Derive from waveform parameters, Inherit from Simulink engine <br> Default:Derive from waveform parameters <br> Frequency modulation - Wavefform requency modulation function <br> length- $M$ real-valued vector | function handle | cell array

Waveform frequency modulation function, specified as a length- $M$ real-valued vector, function handle, or cell array.

- If the FrequencyModulation property is a vector, it specifies samples of the instantaneous frequency at $M$ points as $\left[f_{1}, f_{2}, \ldots, f_{\mathrm{M}}\right.$ ]. The waveform sweeps the specified frequencies such for the $k^{\text {th }}$ pulse with start time $t_{\mathrm{k}}$ and duration $T_{\mathrm{k}}$, the instantaneous frequency at time

$$
t_{m}=t_{k}+(m-1) T_{k} /(M-1)
$$

is equal to $f_{\mathrm{m}}$ where $t_{\mathrm{k}} \leqq t_{\mathrm{m}} \leqq t_{\mathrm{k}}+T_{\mathrm{k}}$ and $m=1 \ldots . M$. The instantaneous frequencies between time $t_{\mathrm{m}}$ and $t_{\mathrm{m}+1}$ are found by linearly interpolating between $f_{\mathrm{m}}$ and $f_{\mathrm{m}+1}$. The resulting custom FM waveform can be considered as a piecewise LFM waveform consisting of M-1 LFM sections of equal duration.

- If the FrequencyModulation property is a function handle, the function must have the following syntax: $\mathrm{f}=\mathrm{fmFcn}(\mathrm{t})$ where $f$ is the instantaneous frequency at time $t . t$ is the time at which to compute the instantaneous frequency. The values in $t$ are between 0 and the pulse width.
- If the FrequencyModulation property is a cell array, then the first cell must be a function handle as specified above. The remaining entries in the cell array are the additional input arguments to the function, if any.

Programmatic Use
Block Parameter:FrequencyModulation
Type:char, string, function
Values:char. string
Default:Hyperbolic
Data Types: char \| string
Envelope function - FM signal amplitude envelope
Rectangular (default) | Gaussian | Hamming | Chebyshev | Hann | Kaiser | Taylor

FM signal amplitude envelope function, specified as Rectangular, Gaussian, Hamming, Chebyshev, Hann, Kaiser, or Taylor.

## Programmatic Use

Block Parameter:Envelope
Type:enum
Values:Rectangular, Gaussian, Hamming, Chebyshev, Hann, Kaiser, or Taylor
Default:Rectangular
Source of Frequency Offset - Source of frequency offset
Property (default)| Input port

Source of frequency offset, specified as Property or Input port.

- When set to Property, the offset is determined by the value of the Frequency Offset parameter.
- When set to Input port, the offset is determined by the value of the FreqOffset port.

Programmatic Use
Block Parameter:Frequency0ffsetSource
Type:enum
Values:Property, Input Port
Default:Property
Frequency Offset (Hz) - Frequency offset
0 (default) | scalar

Frequency offset, specified as a scalar. Units are in Hz .
Example: 2e3

## Dependencies

To enable this parameter set the Source of Frequency Offset parameter to Input port.
Programmatic Use
Block Parameter:Frequency0ffset
Type:double
Values:scalar
Default:0
Output signal format - Format of the output signal
Pulses (default)| Samples

The format of the output signal, specified as Pulses or Samples.
If you set this parameter to Samples, the output of the block consists of multiple samples. The number of samples is the value of the Number of samples in output parameter.

If you set this parameter to Pulses, the output of the block consists of multiple pulses. The number of pulses is the value of the Number of pulses in output parameter.

Programmatic Use
Block Parameter:OutputFormat
Type:enum
Values:Pulses Samples
Default:Pulses
Number of samples in output - Number of samples in output
100 (default) | positive integer

Number of samples in the block output, specified as a positive integer.
Example: 1000

## Dependencies

To enable this parameter, set the Output signal format parameter to Samples.

Programmatic Use<br>Block Parameter:NumSamples<br>Type:double<br>Values:positive scalar<br>Default:100<br>Data Types: double

Number of pulses in output - Number of pulses in output
1 (default) | positive integer

Number of pulses in the block output, specified as a positive integer.
Example: 2

## Dependencies

To enable this parameter, set the Output signal format parameter to Pulses.
Programmatic Use
Block Parameter:NumPulses
Type:double
Values:positive scalar
Default:1
Data Types: double
Enable PRF Output - Enable output of PRF
off (default) | on

Select this parameter to enable the PRF output port.

## Dependencies

To enable this parameter, set Output signal format to Pulses.
Programmatic Use
Block Parameter:PRFOutputPort
Type:enum
Values:off on
Default:off
Enable Matched Filter Coeficients Output - Enable output of matched filter coefficients off (default) | on

Select this parameter to enable the Coeff output port.

## Programmatic Use

Block Parameter:CoefficientOutputPort
Type:enum
Values:off on
Default:off
Simulate using - Block simulation method
Interpreted Execution (default)|Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).

Programmatic Use<br>Block Parameter:SimulateUsing<br>Type:enum<br>Values:Interpreted Execution, Code Generation<br>Default:Interpreted Execution

## Version History

## Introduced in R2023a

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using Simulink ${ }_{\circledR}$ Coder ${ }^{\mathrm{TM}}$.

See Also<br>phased.CustomFMWaveform|phased.NonlinearFMWaveform

## Data Cube Slicer

Slice data cube along specified dimensions


## Libraries:

Phased Array System Toolbox / Space-Time Adaptive Processing

## Description

The Data Cube Slicer block slices a data cube through a specified plane. The input is a data cube of dimensions $M$-by- $Q$-by- $N$. The first dimension is range, or fast time. The second dimension is angle, or channels. The third dimension is Doppler, or slow time.

## Ports

Input
$\mathbf{X}$ - Input data cube
$M$-by-Q-by- $N$ complex-valued array
Input data cube, specified as an $M$-by- $Q$-by- $N$ complex-valued matrix.

```
Data Types: double
Complex Number Support: Yes
```

Idx - Slice-plane index
positive integer
Slice-plane index, specified as a positive integer. This index selects which slice to use to create the two-dimensional output.
Data Types: double

## Output

Port_1 - Output
complex-valued matrix
Collapsed data cube, returned as a complex-valued matrix.

- If you set the Output Slice parameter to Angle-Doppler, the slice is the constant-range or fasttime plane. The output has dimensions $Q$-by- $N$.
- If you set the Output Slice parameter to Range-Doppler, the slice is the constant-angle plane. The output has dimension $M$-by- $N$.
- If you set the Output Slice parameter to Range-angle, the slice is the constant-Doppler plane. The output has dimension $M$-by- $Q$.

Data Types: double
Complex Number Support: Yes

## Parameters

Output Slice - Output slice
Angle-Doppler (default) | Range-Doppler | Range-angle
Output slice, specified as Angle-Doppler, Range-Doppler, or Range-angle. The output slices are:

| Slice plane | Slice dimensions |
| :--- | :--- |
| Angle-Doppler | $Q$-by- $N$ |
| Range-Doppler | $M$-by- $N$ |
| Range-angle | $M$-by- $Q$ |

## Version History

Introduced in R2014b

## Extended Capabilities

C/C++ Code Generation
Generate C and $\mathrm{C}++$ code using Simulink $®$ Coder $^{\mathrm{TM}}$.

## Dechirp Mixer

Dechirping operation on input signal
$\geq$ Refx $x$

## Libraries:

Phased Array System Toolbox / Detection

## Description

The Dechirp block mixes the incoming signal from the X port with a reference signal incoming through the RefX port. The signals can be complex baseband signals. The input signal can be a matrix where each column is an independent channel. The reference signal is a vector. The reference signal is complex-conjugated and then multiplied with each signal column to compute the output.

## Ports

Input
RefX - Reference signal
complex-valued $M$-by-1 vector
Reference signal, specified as a complex-valued $M$-by-1 vector.
Data Types: single | double
Complex Number Support: Yes
$\mathbf{X}$ - Input signal
complex-valued $M$-by- $N$ matrix
Input signal, specified as a complex-valued $M$-by- $N$ matrix. Each column of X is an independent signal and is individually mixed with the signal input to the RefX port.

Data Types: single | double
Complex Number Support: Yes

## Output

Port_1 - Dechirped output signal
$M$-by- $N$ matrix
Dechirped signal, returned as an $M$-by- $N$ matrix. Each column of the Port_1 port is the mixed output for the corresponding column of $X$.
Data Types: single | double
Complex Number Support: Yes

## Version History <br> Introduced in R2014b

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using Simulink ${ }^{\circledR}$ Coder ${ }^{\mathrm{TM}}$.
Usage notes and limitations:
Does not support variable-size inputs.

## See Also

dechirp

## Doppler Estimator

Doppler estimation


## Libraries:

Phased Array System Toolbox / Detection

## Description

The Doppler Estimator block estimates the Doppler (radial speed) of target detections obtained from the radar response data.

## Ports

## Input

Resp - Doppler-processed response data cube
complex-valued $P$-by-1 column vector | complex-valued $M$-by- $P$ matrix | complex-valued $M$-by- $N$-by- $P$ array

Doppler-processed response data cube, specified as a complex-valued $P$-by- 1 column vector, a complex-valued $M$-by- $P$ matrix, or a complex-valued $M$-by- $N$-by- $P$ array. $M$ represents the number of range samples, $N$ is the number of sensor elements or beams, and $P$ is the number of Doppler bins.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
Data Types: double
Doppler - Doppler grid values along Doppler dimension
real-valued $P$-by-1 column vector
Doppler grid values along the Doppler dimension, specified as a real-valued $P$-by- 1 column vector. Doppler defines the Doppler values corresponding to the Doppler dimension of data input to the Resp port. Doppler values must be monotonically increasing and equally spaced. Units are in hertz or meters/sec.

Example: [-0.3,-0.2,-0.1,0,0.1,0.2,0.3]
Data Types: double
Detldx - Detection indices
real-valued $N_{d}$-by- $Q$ matrix
Detection indices, specified as a real-valued $N_{d}$-by- $Q$ matrix. $Q$ is the number of detections and $N_{d}$ is the number of dimensions in the response data cube, Resp. Each column of DetIdx contains the indices of a detection in the response data cube.

NoisePower - Noise power at detection locations
positive scalar | real-valued 1-by-Q row vector of positive values

Noise power at detection locations, specified as a positive scalar or real-valued 1-by-Q row vector positive values. $Q$ is the number of detections specified in the DetIdx input port.

## Dependencies

To enable this port, select the Output variance for parameter estimates parameter, and then set Source of noise power parameter to Input port.

Clusters - Cluster IDs real-valued 1-by-Q row vector of positive values

Cluster IDs, specified as a real-valued 1-by- $Q$ row vector, where $Q$ is the number of detections specified in the DetIdx input port. Each element of Clusters corresponds to an element of DetIdx.

## Dependencies

To enable this input port, select the Enable cluster ID input checkbox.

## Output

Est - Doppler estimate
real-valued $K$-by-1 column vector
Doppler estimates, returned as a real-valued $K$-by- 1 column vector.

- When Enable cluster ID input is not selected, each Doppler estimate corresponds to one of the columns in the DetIdx input port. Then $K$ equals the number of elements, $Q$, of DetIdx.
- When Enable cluster ID input is selected, each Doppler estimate corresponds to one of the cluster IDs in the Clustersinput port. Then $K$ equals the number of unique cluster IDs.

Var - Doppler estimation variance
positive, real-valued $K$-by- 1 column vector
Doppler estimation variance, returned as a positive, real-valued $K$-by- 1 column vector, where $K$ is the dimension of Est. Each element of Var corresponds to an element of Est. The estimator variance is computed using the Ziv-Zakai bound.

## Dependencies

To enable this port, select the Output variance for parameter estimates parameter.

## Parameters

Maximum number of estimates - Maximum number of estimates to report 1 (default) | positive integer

The maximum number of estimates to report, specified as a positive integer. When the number of requested estimates is greater than the number elements in DetIdx, the remainder is filled with NaN .

## Data Types: double

Enable cluster ID input - Enable cluster ID input off (default) | on

Enable the Cluster input port to pass in cluster association information.

## Data Types: Boolean

Output variance for parameter estimates - Enable output variance port off (default) |on

Enables the output of the parameter estimate variances via the Var port.
Data Types: Boolean
Number of pulses in Doppler processed waveform - Number of pulses
2 (default) | positive integer

Number of pulses in Doppler processed waveform, specified as a positive integer.

## Dependencies

To enable this parameter, select the Output variance for parameter estimates Output variance for parameter estimates parameter.

Data Types: double
Source of noise power - Source of noise power values
Property (default) | Input port

Source of the noise power, specified as Property or Input port. If you set this parameter to Property, use the Noise power parameter to set the noise power at the detection locations. When set the parameter to Input port, specify noise power via the NoisePower input port.

Noise power - Noise power values
1.0 (default) | positive scalar

Noise power for detections, specified as a positive scalar. The same noise power value is applied to all detections. Noise power is in linear units.

## Dependencies

To enable this parameter, select the Output variance for parameter estimates checkbox and set the Source of noise power parameter to Property.
Data Types: double
Simulate using - Block simulation method
Interpreted Execution (default)|Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are
satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).

Programmatic Use<br>Block Parameter:SimulateUsing<br>Type:enum<br>Values:Interpreted Execution, Code Generation<br>Default:Interpreted Execution

## Version History

Introduced in R2017a

## See Also

## Blocks

CFAR Detector | 2-D CFAR Detector | Range Doppler Response
Objects
phased.CFARDetector| phased.CFARDetector2D|phased.DopplerEstimator|
phased.RangeDopplerResponse

## DPCA Canceller

Displaced phase center array (DPCA) pulse canceller for a uniform linear array


## Libraries:

Phased Array System Toolbox / Space-Time Adaptive Processing

## Description

The DPCA Canceller block filters clutter impinging on a uniform linear array using a displaced phase center array pulse canceller.

## Ports

Input
$\mathbf{X}$ - Input signal
$M$-by- $N$-by- $P$ complex-valued matrix
Input signal, specified as an $M$-by- $N$-by- $P$ complex-valued array. $M$ is the number of range samples, $N$ is the number of channels, and $P$ is the number of pulses.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

## Data Types: double

Idx - Index of range cells
positive integer
Index of range cells to compute processing weights.
Example: 1
Data Types: double
PRF - Pulse repetition frequency
positive scalar
Pulse repetition frequency of current pulse, specified as a positive scalar.

## Dependencies

To enable this port, set the Specify PRF as parameter to Input port.
Data Types: double
Ang - Targeting direction
2-by-1 real-valued vector
Targeting direction, specified as a 2-by-1 real-valued vector. The vector takes the form of [AzimuthAngle;ElevationAngle]. Angle units are in degrees. The azimuth angle must lie
between $-180^{\circ}$ and $180^{\circ}$, inclusive, and the elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive. Angles are defined with respect to the local coordinate system of the array.

## Dependencies

To enable this port, set the Specify direction as parameter to Input port.
Data Types: double
Dop - Targeting Doppler frequency scalar

Targeting Doppler frequency of current pulse, specified as a scalar.

## Dependencies

This port appears when the Output pre-Doppler result check box is cleared and the Specify targeting Doppler as parameter is set to Input port.
Data Types: double
Output
Y - Beamformed output
M-by-1 complex-valued vector
Processing output, returned as an $M$-by- 1 complex-valued vector. The quantity $M$ is the number of range samples in the input port $X$.
Data Types: double
W - Processing weights
length $N^{*} P$ complex-valued vector
Processing weights, returned as Length $N^{*} P$ complex-valued vector. The quantity $N$ is the number of channels and $P$ is the number of pulses. When the Specify sensor array as parameter is set to Partitioned array or Replicated subarray, $N$ represents the number of subarrays. $L$ is the number of desired beamforming directions specified in the Ang input port or by the Beamforming direction (deg) parameter. There is one set of weights for each beamforming direction.

## Dependencies

To enable this port, select the Enable weights output check box.
Data Types: double

## Parameters

## Main Tab

Signal propagation speed (m/s) - Signal propagation speed
physconst('LightSpeed') (default)| real-valued positive scalar

Signal propagation speed, specified as a real-valued positive scalar. The default value of the speed of light is the value returned by physconst ('LightSpeed ' ). Units are in meters per second.
Example: 3e8

## Data Types: double

Operating frequency (Hz) - System operating frequency
3e8 (default) | positive real scalar

System operating frequency, specified as a positive scalar. Units are in Hz .
Specify PRF as - Source of PRF value
Property (default)|Input port

Source of PRF value, specified as Property or Input port. When set to Property, the Pulse repetition frequency ( Hz ) parameter sets the PRF. When set to Input port, pass in the PRF using the PRF input port.

Pulse repetition frequency (Hz) - Pulse repetition frequency
1 (default) | positive scalar

Pulse repetition frequency, PRF, specified as a positive scalar. Units are in Hertz. Set this parameter to the same value set in any Waveform library block used in the simulation.

## Dependencies

To enable this parameter, set the Specify PRF as parameter to Property.
Specify direction as - Specify source of targeting directions
Property (default)|Input port

Specify whether the targeting direction for the STAP processor block comes from a block parameter or from the ANG input port. Values of this parameter are

| Property | - For the ADPCA Canceller and DPCA Canceller blocks, targeting <br> direction is specified using Receiving mainlobe direction <br> (deg). |
| :--- | :--- |
| - For the SMI Beamformer block, targeting direction is specified |  |
| using Targeting direction. |  |
| These parameters appear only when the Specify direction as |  |
| parameter is set to Property. |  |

Receiving mainlobe direction (deg) - Pointing direction of main lobe of array
[0;0] (default) | real-valued 2-by-1 vector

Specify the direction of the main lobe of the receiving sensor array as a real-valued 2-by-1 vector. The direction is specified in the format of [AzimuthAngle; ElevationAngle]. The azimuth angle should be between $-180^{\circ}$ and $180^{\circ}$ and the elevation angle should be between $-90^{\circ}$ and $90^{\circ}$.
Example: [100;-45]

## Dependencies

To enable this parameter, set Specify direction as to Property.
Number of bits in phase shifters - Number of phase shift quantization bits
0 (default) | nonnegative integer

The number of bits used to quantize the phase shift component of beamformer or steering vector weights. Specify the number of bits as a non-negative integer. A value of zero indicates that no quantization is performed.

Specify targeting Doppler as - Source of targeting Doppler
Property (default)|Input port

Specify whether targeting Doppler values for the STAP processor comes from the Targeting Doppler $(\mathbf{H z})$ parameter of this block or using the DOP input port. For the ADPCA Canceller and DPCA Canceller blocks, the Specify targeting Doppler as parameter appears only when the Output preDoppler result check box is cleared. Values of this parameter are

| Property | Specify targeting Doppler values using the Targeting Doppler <br> parameter of the block. The Targeting Doppler parameter appears <br> only when Specify targeting Doppler as is set to Property. |
| :--- | :--- |
| Input port | Specify targeting Doppler values using the Dop input port. This port <br> appears only when Specify targeting Doppler as is set to Input <br> port. |

Targeting Doppler (Hz) - Targeting Doppler of STAP processor
0 (default) | scalar

Targeting Doppler of STAP processor, specified as a scalar.

## Dependencies

- To enable this parameter for the SMI Beamformer block, set Specify targeting Doppler as to Property.
- To enable this parameter for the ADPCA Canceller and DPCA Canceller blocks, first clear the Output pre-Doppler result check box. Then set the Specify targeting Doppler as parameter to Property.

Enable weights output - Option to output beamformer weights off (default) | on

Select this check box to obtain the beamformer weights from the output port, W .
Output pre-Doppler result - Output results before Doppler filtering
on (default) | off

Select this check box to output the results before Doppler filtering. Clear this check box to output the processing result after Doppler filtering. Selecting this check box will remove the Specify targeting Doppler as and Targeting Doppler (Hz) parameters.

Simulate using - Block simulation method
Interpreted Execution (default) | Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).

## Programmatic Use

Block Parameter:SimulateUsing
Type:enum
Values:Interpreted Execution, Code Generation
Default:Interpreted Execution
Sensor Arrays Tab
Specify sensor array as - Method to specify array
Array (no subarrays) (default)|MATLAB expression

Method to specify array, specified as Array (no subarrays) or MATLAB expression.

- Array (no subarrays) - use the block parameters to specify the array.
- MATLAB expression - create the array using a MATLAB expression.

Expression - MATLAB expression used to create an array
Phased Array System Toolbox array System object

MATLAB expression used to create an array, specified as a valid Phased Array System Toolbox array System object.

Example: phased.URA('Size', [5,3])

## Dependencies

To enable this parameter, set Specify sensor array as to MATLAB expression.

## Element Parameters

Element type - Array element types
Isotropic Antenna (default)|Cosine Antenna|Custom Antenna|Omni Microphone|
Custom Microphone

Antenna or microphone type, specified as one of the following:

- Isotropic Antenna
- Cosine Antenna
- Custom Antenna
- Omni Microphone
- Custom Microphone

Operating frequency range $\mathbf{( H z )}$ - Operating frequency range of the antenna or microphone element
[0,1e20] (default) | real-valued 1-by-2 row vector

Specify the operating frequency range of the antenna or microphone element as a 1-by-2 row vector in the form [LowerBound, UpperBound]. The element has no response outside this frequency range. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Isotropic Antenna, Cosine Antenna, or Omni Microphone.

Operating frequency vector ( $\mathbf{H z}$ ) - Operating frequency range of custom antenna or microphone elements
[0,1e20] (default) | real-valued row vector

Specify the frequencies at which to set antenna and microphone frequency responses as a 1-by- $L$ row vector of increasing real values. The antenna or microphone element has no response outside the frequency range specified by the minimum and maximum elements of this vector. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone. Use Frequency responses (dB) to set the responses at these frequencies.

Baffle the back of the element - Set back response of an Isotropic Antenna element or an Omni Microphone element to zero
off (default) | on

Select this check box to baffle the back response of the element. When back baffled, the responses at all azimuth angles beyond $\pm 90^{\circ}$ from broadside are set to zero. The broadside direction is defined as $0^{\circ}$ azimuth angle and $0^{\circ}$ elevation angle.

## Dependencies

To enable this check box, set Element type to Isotropic Antenna or Omni Microphone.
Exponent of cosine pattern - Exponents of azimuth and elevation cosine patterns
[1.5 1.5] (default) | nonnegative scalar | real-valued 1-by-2 matrix of nonnegative values

Specify the exponents of the cosine pattern as a nonnegative scalar or a real-valued 1-by-2 matrix of nonnegative values. When Exponent of cosine pattern is a 1-by-2 vector, the first element is the exponent in the azimuth direction and the second element is the exponent in the elevation direction. When you set this parameter to a scalar, both the azimuth direction and elevation direction cosine patterns are raised to the same power.

## Dependencies

To enable this parameter, set Element type to Cosine Antenna.
Frequency responses (dB) - Antenna and microphone frequency response
[0,0] (default) | real-valued row vector

Frequency response of a custom antenna or custom microphone for the frequencies defined by the Operating frequency vector ( Hz ) parameter. The dimensions of Frequency responses (dB) must match the dimensions of the vector specified by the Operating frequency vector $(\mathbf{H z})$ parameter.

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone.
Input Pattern Coordinate System - Coordinate system of custom antenna pattern
az-el (default)|phi-theta

Coordinate system of custom antenna pattern, specified az-el or phi-theta. When you specify azel, use the Azimuth angles (deg) and Elevations angles (deg) parameters to specify the coordinates of the pattern points. When you specify phi-theta, use the Phi angles (deg) and Theta angles (deg) parameters to specify the coordinates of the pattern points.

## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Azimuth angles (deg) - Azimuth angles of antenna radiation pattern
[-180:180] (default) | real-valued row vector

Specify the azimuth angles at which to calculate the antenna radiation pattern as a 1-by- $P$ row vector. $P$ must be greater than 2. Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to az-el.

Elevation angles (deg) - Elevation angles of antenna radiation pattern
[-90:90] (default) | real-valued row vector

Specify the elevation angles at which to compute the radiation pattern as a 1-by- $Q$ vector. $Q$ must be greater than 2. Angle units are in degrees. Elevation angles must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to az-el.

Phi Angles (deg) - Phi angle coordinates of custom antenna radiation pattern
$0: 360$ | real-valued 1-by-P row vector

Phi angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by-P row vector. $P$ must be greater than 2 . Angle units are in degrees. Phi angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Theta Angles (deg) - Theta angle coordinates of custom antenna radiation pattern 0 : 180 | real-valued 1-by- $Q$ row vector

Theta angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by$Q$ row vector. $Q$ must be greater than 2 . Angle units are in degrees. Theta angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Magnitude pattern (dB) - Magnitude of combined antenna radiation pattern zeros $(181,361)$ (default) | real-valued $Q$-by- $P$ matrix | real-valued $Q$-by- $P$-by- $L$ array

Magnitude of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector $(\mathbf{H z})$.

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector (Hz) parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (Hz) parameter.


## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Phase pattern (deg) - Custom antenna radiation phase pattern
zeros $(181,361)$ (default) | real-valued $Q$-by-P matrix | real-valued $Q$-by- $P$-by-L array

Phase of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector $(\mathbf{H z})$.

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector (Hz) parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (

Dependencies
To enable this parameter, set Element type to Custom Antenna.
MatchArrayNormal - Rotate antenna element to array normal on (default) | off

Select this check box to rotate the antenna element pattern to align with the array normal. When not selected, the element pattern is not rotated.

When the antenna is used in an antenna array and the Input Pattern Coordinate System parameter is az-el, selecting this check box rotates the pattern so that the $x$-axis of the element coordinate system points along the array normal. Not selecting uses the element pattern without the rotation.

When the antenna is used in an antenna array and Input Pattern Coordinate System is set to phitheta, selecting this check box rotates the pattern so that the $z$-axis of the element coordinate system points along the array normal.

Use the parameter in conjunction with the Array normal parameter of the URA and UCA arrays.
Dependencies
To enable this parameter, set Element type to Custom Antenna.
Polar pattern frequencies (Hz) - Polar pattern microphone response frequencies
1 e3 (default) | real scalar | real-valued 1-by-L row vector

Polar pattern microphone response frequencies, specified as a real scalar, or a real-valued, 1 -by- $L$ vector. The response frequencies lie within the frequency range specified by the Operating frequency vector $(\mathrm{Hz})$ vector.

## Dependencies

To enable this parameter, set Element type set to Custom Microphone.
Polar pattern angles (deg) - Polar pattern response angles
[-180:180] (default) | real-valued -by-P row vector

Specify the polar pattern response angles, as a 1-by- $P$ vector. The angles are measured from the central pickup axis of the microphone and must be between $-180^{\circ}$ and $180^{\circ}$, inclusive.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.
Polar pattern (dB) - Custom microphone polar response
zeros (1,361) (default) | real-valued L-by-P matrix

Specify the magnitude of the custom microphone element polar patterns as an $L$-by- $P$ matrix. $L$ is the number of frequencies specified in Polar pattern frequencies ( $\mathbf{H z}$ ). $P$ is the number of angles specified in Polar pattern angles (deg). Each row of the matrix represents the magnitude of the polar pattern measured at the corresponding frequency specified in Polar pattern frequencies (Hz) and all angles specified in Polar pattern angles (deg). The pattern is measured in the azimuth plane. In the azimuth plane, the elevation angle is $0^{\circ}$ and the central pickup axis is $0^{\circ}$ degrees azimuth and $0^{\circ}$ degrees elevation. The polar pattern is symmetric around the central axis. You can construct the microphone response pattern in 3-D space from the polar pattern.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.

## Array Parameters

Specify sensor array as - Type of array
Array (no subarrays) (default)|MATLAB expression

Specify a ULA sensor array directly or by using a MATLAB expression.

## Types

## Array (no subarrays)

MATLAB expression
Number of elements - Number of array elements in $U$
2 (default) | positive integer greater than or equal to two

The number of array elements for ULA arrays, specified as an integer greater than or equal to two.
Example: 11
Data Types: double
Element spacing - Distance between ULA elements
0.5 (default) | positive scalar

Distance between adjacent ULA elements, specified as a positive scalar. Units are in meters.
Example: 1.5
Array axis - Linear axis direction of ULA
$y$ (default) $|x| z$

Linear axis direction of ULA, specified as $y$, $x$, or $z$. All ULA array elements are uniformly spaced along this axis in the local array coordinate system.

## Dependencies

- To enable this parameter, set Geometry to ULA.
- This parameter is also enabled when the block only supports ULA arrays.

Taper - ULA array taper
1 (default) | complex-valued vector

Tapers, also known as element weights, are applied to sensor elements in the array. Tapers are used to modify both the amplitude and phase of the transmitted or received data.

Specify element tapering as a complex-valued scalar or a complex-valued 1-by- $N$ row vector. In this vector, $N$ represents the number of elements in the array. If Taper is a scalar, the same weight is applied to each element. If Taper is a vector, a weight from the vector is applied to the corresponding sensor element. A weight must be applied to each element in the sensor array.

## Example: [0.5;1;0.5]

Data Types: double
Expression - MATLAB expression used to create an array
Phased Array System Toolbox array System object

MATLAB expression used to create a ULA array, specified as a valid Phased Array System Toolbox array System object.

Example: phased.ULA('NumElements',13)
Dependencies
To enable this parameter, set Specify sensor array as to MATLAB expression.

## Version History

Introduced in R2014b

## See Also

phased.DPCACanceller

## ESPRIT DOA

ESPRIT direction of arrival (DOA) estimator for ULA

## Libraries:



Phased Array System Toolbox / Direction of Arrival

## Description

The ESPRIT DOA block estimates the direction of arrival of a specified number of narrowband signals incident on a uniform linear array using the ESPRIT algorithm.

## Ports

## Input

Port_1 - Input signal
$N$-by-M complex-valued matrix
Input signal, specified as an $N$-by- $M$ complex-valued matrix. $N$ corresponds to the number of samples. $M$ corresponds to the number data channels.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
Data Types: double

## Output

Ang - Estimated broadside direction-of-arrival angles
$M$-by-1 real-valued vector
Estimated broadside direction-of-arrival angles, returned as an $M$-by-1 real-valued vector. Units are in degrees.

Data Types: double

## Parameters

## Main Tab

Signal propagation speed (m/s) - Signal propagation speed
physconst('LightSpeed') (default) | real-valued positive scalar

Signal propagation speed, specified as a real-valued positive scalar. The default value of the speed of light is the value returned by physconst ('LightSpeed'). Units are in meters per second.
Example: 3e8

## Data Types: double

Operating frequency (Hz) - System operating frequency
3e8 (default) | positive real scalar

System operating frequency, specified as a positive scalar. Units are in Hz .
Number of signals - Number of signals
1 (default) | positive integer scalar
Specify the number of signals as a positive integer scalar.
Spatial smoothing - Enable spatial smoothing
0 (default) | non-negative integer

Specify the amount of averaging used by spatial smoothing to estimate the covariance matrix as a nonnegative integer. Each increase in smoothing handles one extra coherent source, but reduces the effective number of elements by one. The maximum value of this parameter is $N-2$, where $N$ is the number of sensors in the ULA.

Type of least squares method - Type of least squares method
TLS (default) | LS
Specify the least squares method used for ESPRIT as one of TLS or LS where TLS refers to total least squares and LSrefers to least squares.

Forward-backward averaging - Enable forward-backward averaging
off (default) | on

Select this parameter to use forward-backward averaging to estimate the covariance matrix for sensor arrays with a conjugate symmetric array manifold structure.

Row weighting factor - Row weighting factor

## 1 (default)

Specify the row weighting factor for signal subspace eigenvectors as a positive integer scalar. This parameter controls the weights applied to the selection matrices. In most cases higher value are better. However, the value can never be greater than ( $N-1$ )/2 where $N$ is the number of elements of the array.

Simulate using - Block simulation method
Interpreted Execution (default) | Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).

```
Programmatic Use
Block Parameter:SimulateUsing
Type:enum
Values:Interpreted Execution, Code Generation
Default:Interpreted Execution
```


## Sensor Array Tab

Specify sensor array as - Method to specify array
Array (no subarrays) (default)|MATLAB expression

Method to specify array, specified as Array (no subarrays) or MATLAB expression.

- Array (no subarrays) - use the block parameters to specify the array.
- MATLAB expression - create the array using a MATLAB expression.


## Element Parameters

Element type - Array element types
Isotropic Antenna (default)|Cardioid Antenna|Cosine Antenna|Custom Antenna| Gaussian Antenna|Sinc Antenna|Omni Microphone|Custom Microphone

Antenna or microphone type, specified as one of the following:

- Isotropic Antenna
- Cardioid Antenna
- Cosine Antenna
- Custom Antenna
- Gaussian Antenna
- Sinc Antenna
- Omni Microphone
- Custom Microphone

Operating frequency range $(\mathbf{H z})$ - Operating frequency range of the antenna or microphone element
[0,1e20] (default) | real-valued 1-by-2 row vector

Specify the operating frequency range of the antenna or microphone element as a 1-by-2 row vector in the form [LowerBound, UpperBound]. The element has no response outside this frequency range. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Isotropic Antenna, Cosine Antenna, or Omni Microphone.

Baffle the back of the element - Set back response of an Isotropic Antenna element or an Omni Microphone element to zero
off (default) | on

Select this check box to baffle the back response of the element. When back baffled, the responses at $0^{\circ}$ azimuth angles beyond $\pm 90^{\circ}$ from broadside are set to zero. The broadside direction is defined as $0^{\circ}$ azimuth angle and $0^{\circ}$ elevation angle.

## Dependencies

To enable this check box, set Element type to Isotropic Antenna or Omni Microphone.
Null axis direction - Null axis direction
$-x$ (default) $|+x|+y|-y|+z \mid-z$

## Dependencies

To enable this parameter, set Element type to Cardioid Antenna.
Exponent of cosine pattern - Exponents of azimuth and elevation cosine patterns
[1.5 1.5] (default) | nonnegative scalar | real-valued 1-by-2 matrix of nonnegative values

Specify the exponents of the cosine pattern as a nonnegative scalar or a real-valued 1-by-2 matrix of nonnegative values. When Exponent of cosine pattern is a 1-by-2 vector, the first element is the exponent in the azimuth direction and the second element is the exponent in the elevation direction. When you set this parameter to a scalar, both the azimuth direction and elevation direction cosine patterns are raised to the same power.

## Dependencies

To enable this parameter, set Element type to Cosine Antenna.

Operating frequency vector (Hz) - Operating frequency range of custom antenna or microphone elements
[0,1e20] (default) | real-valued row vector

Specify the frequencies at which to set antenna and microphone frequency responses as a 1-by-L row vector of increasing real values. The antenna or microphone element has no response outside the frequency range specified by the minimum and maximum elements of this vector. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone. Use Frequency responses (dB) to set the responses at these frequencies.

Frequency responses (dB) - Antenna and microphone frequency response
[0,0] (default) | real-valued row vector

Frequency response of a custom antenna or custom microphone for the frequencies defined by the Operating frequency vector (Hz) parameter. The dimensions of Frequency responses (dB) must match the dimensions of the vector specified by the Operating frequency vector $(\mathbf{H z})$ parameter.

Dependencies
To enable this parameter, set Element type to Custom Antenna or Custom Microphone.
Input Pattern Coordinate System - Coordinate system of custom antenna pattern az-el (default)|phi-theta

Coordinate system of custom antenna pattern, specified az-el or phi-theta. When you specify azel, use the Azimuth angles (deg) and Elevations angles (deg) parameters to specify the coordinates of the pattern points. When you specify phi-theta, use the Phi angles (deg) and Theta angles (deg) parameters to specify the coordinates of the pattern points.

## Dependencies

To enable this parameter, set Element type to Custom Antenna.

## Azimuth angles (deg) - Azimuth angles of antenna radiation pattern

[-180: 180] (default) | real-valued row vector

Specify the azimuth angles at which to calculate the antenna radiation pattern as a 1 -by- $P$ row vector. $P$ must be greater than 2. Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to az-el.

Elevation angles (deg) - Elevation angles of antenna radiation pattern
[-90:90] (default) | real-valued row vector

Specify the elevation angles at which to compute the radiation pattern as a 1-by- $Q$ vector. $Q$ must be greater than 2. Angle units are in degrees. Elevation angles must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to az-el.

Phi Angles (deg) - Phi angle coordinates of custom antenna radiation pattern
$0: 360$ | real-valued 1-by-P row vector

Phi angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by-P row vector. $P$ must be greater than 2 . Angle units are in degrees. Phi angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Theta Angles (deg) - Theta angle coordinates of custom antenna radiation pattern 0:180 | real-valued 1-by- $Q$ row vector

Theta angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by$Q$ row vector. $Q$ must be greater than 2. Angle units are in degrees. Theta angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Magnitude pattern (dB) - Magnitude of combined antenna radiation pattern zeros $(181,361)$ (default) | real-valued $Q$-by- $P$ matrix | real-valued $Q$-by- $P$-by-L array

Magnitude of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector ( $\mathbf{H z}$ ).

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector $(\mathbf{H z})$ parameter.


## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Phase pattern (deg) - Custom antenna radiation phase pattern
zeros $(181,361)$ (default) | real-valued $Q$-by- $P$ matrix | real-valued $Q$-by- $P$-by- $L$ array

Phase of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector ( $\mathbf{H z}$ ).

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (

Dependencies
To enable this parameter, set Element type to Custom Antenna.
Align element normal with array normal - Align element normal with array normal
on (default) | off

## Dependencies

This parameter is enabled when Element type is set to Custom Antenna.
Radiation pattern beamwidth (deg) - Radiation pattern beamwidth
[10,10] (default)

## Dependencies

This parameter is enabled when Element type is set to Gaussian Antenna.
Polar pattern frequencies (Hz) - Polar pattern microphone response frequencies
1e3 (default) | real scalar | real-valued 1-by-L row vector

Polar pattern microphone response frequencies, specified as a real scalar, or a real-valued, 1 -by- $L$ vector. The response frequencies lie within the frequency range specified by the Operating frequency vector $(\mathrm{Hz})$ vector.

## Dependencies

To enable this parameter, set Element type set to Custom Microphone.

Polar pattern angles (deg) - Polar pattern response angles
[-180:180] (default) | real-valued -by-P row vector

Specify the polar pattern response angles, as a 1-by- $P$ vector. The angles are measured from the central pickup axis of the microphone and must be between $-180^{\circ}$ and $180^{\circ}$, inclusive.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.
Polar pattern (dB) - Custom microphone polar response
zeros $(1,361)$ (default) | real-valued $L$-by-P matrix

Specify the magnitude of the custom microphone element polar patterns as an $L$-by- $P$ matrix. $L$ is the number of frequencies specified in Polar pattern frequencies $\mathbf{( H z )} . P$ is the number of angles specified in Polar pattern angles (deg). Each row of the matrix represents the magnitude of the polar pattern measured at the corresponding frequency specified in Polar pattern frequencies (Hz) and all angles specified in Polar pattern angles (deg). The pattern is measured in the azimuth plane. In the azimuth plane, the elevation angle is $0^{\circ}$ and the central pickup axis is $0^{\circ}$ degrees azimuth and $0^{\circ}$ degrees elevation. The polar pattern is symmetric around the central axis. You can construct the microphone response pattern in 3-D space from the polar pattern.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.

## ULA Parameters

Number of elements - Number of array elements in $U$
2 (default) | positive integer greater than or equal to two

The number of array elements for ULA arrays, specified as an integer greater than or equal to two.
Example: 11
Data Types: double
Element spacing - Distance between ULA elements
0.5 (default) | positive scalar

Distance between adjacent ULA elements, specified as a positive scalar. Units are in meters.
Example: 1.5
Array axis - Linear axis direction of ULA
$y$ (default) $|x| z$

Linear axis direction of ULA, specified as $y, x$, or $z$. All ULA array elements are uniformly spaced along this axis in the local array coordinate system.

## Dependencies

- To enable this parameter, set Geometry to ULA.
- This parameter is also enabled when the block only supports ULA arrays.

Taper - ULA array taper
1 (default) | complex-valued vector

Tapers, also known as element weights, are applied to sensor elements in the array. Tapers are used to modify both the amplitude and phase of the transmitted or received data.

Specify element tapering as a complex-valued scalar or a complex-valued 1-by- $N$ row vector. In this vector, $N$ represents the number of elements in the array. If Taper is a scalar, the same weight is applied to each element. If Taper is a vector, a weight from the vector is applied to the corresponding sensor element. A weight must be applied to each element in the sensor array.
Example: [0.5;1;0.5]
Data Types: double
Expression - MATLAB expression used to create an array
Phased Array System Toolbox array System object

MATLAB expression used to create a ULA array, specified as a valid Phased Array System Toolbox array System object.
Example: phased.ULA('NumElements',13)

## Dependencies

To enable this parameter, set Specify sensor array as to MATLAB expression.

## Version History <br> Introduced in R2014b

## See Also

phased.ESPRITEstimator

## FMCW Waveform

Frequency-modulated continuous (FMCW) waveform source

## Libraries:

Phased Array System Toolbox / Waveforms

## Description

The FMCW Waveform block generates a frequency modulated continuous wave (FMCW) waveform with a specified sweep time and sweep bandwidth. The block output can be either an integer number of pulses or samples.

## Ports

## Output

Port_1 - FMCW Waveform
complex-valued column vector
FMCW waveform, returned as a complex-valued column vector containing the waveform samples.

- If the Output signal format parameter is set to Samples, then the output of the port consists of the number of samples set by the Number of samples in output parameter.
- If the Output signal format parameter is set to Sweeps, then the output of the port consists of the number of sweeps set by the Number of sweeps in output parameter. Also, if the Sweep direction parameter is set to Triangle each sweep is one-half period in duration.


## Parameters

Sample rate (Hz) - Sample rate of the output waveform
le6 (default) | positive scalar

Sample rate of the output waveform, specified as a positive scalar. The ratio of Sample rate (Hz) to each element in the Pulse repetition frequency (Hz) vector must be an integer. This restriction is equivalent to requiring that the pulse repetition interval is an integral multiple of the sample interval.

```
Programmatic Use
Block Parameter:SampleRate
Type:double
Values:positive scalar
Default:1e6
Sweep time (s) - Duration of each linear FM sweep
```

1e-4 (default)

Specify the duration, in seconds, of the upsweep or the downsweep of the signal as a scalar or row vector of positive, real numbers. The product of the Sample rate value and each Sweep time entry must be an integer.

To implement a varying sweep time, specify Sweep time as a row vector. The waveform uses successive entries of the vector as the sweep time for successive periods of the waveform. If the last element of the vector is reached, the process continues cyclically with the first entry of the vector.

If Sweep time and Sweep bandwidth are both row vectors, the vectors must have the same length.
If Sweep direction is Up or Down, the sweep period equals the sweep time. If Sweep direction is Triangle, the sweep period is twice the sweep time because each period consists of an upsweep segment and a downsweep segment.

## Sweep bandwidth (Hz) - FM sweep bandwidth

1e5 (default)
Specify the bandwidth of the linear FM sweeping, in hertz, as a scalar or row vector of positive, real numbers.

To implement a varying bandwidth, specify Sweep bandwidth as a row vector. The waveform uses successive entries of the vector as the sweep bandwidth for successive periods of the waveform. If the waveform reaches the last element of the Sweep bandwidth vector, the process continues cyclically with the first entry of the vector.

If Sweep time and Sweep bandwidth are both row vectors, the vectors must have the same length.
Sweep direction - FM sweep direction
Up (default) | Down | Triangle
Specify the direction of the linear FM sweep as one of Up, Down, or Triangle.
Sweep interval - Location of FM sweep interval
Positive (default)| Symmetric
If you set this parameter value to Positive, the waveform sweeps in the interval between 0 and $B$, where $B$ is the value of the Sweep bandwidth parameter. If you set this parameter to Symmetric, the waveform sweeps in the interval between $-B / 2$ and $B / 2$.

Output signal format - Output signal format
Sweeps (default) | Samples
Specify the format of the output signal as Sweeps or Samples.
If you set this parameter to Sweeps, the output of the block is in the form of multiple sweeps. The number of sweeps is the value of the Number of sweeps in output parameter.

If you set this parameter to Samples, the output of the block is in the form of multiple samples. The number of samples is the value of the Number of samples in output parameter.

If the Sweep direction parameter is set to Triangle, each sweep is one-half of a period.

Number of samples in output - Number of samples in output 100 (default) | positive integer

Number of samples in the block output, specified as a positive integer.

## Example: 1000

## Dependencies

To enable this parameter, set the Output signal format parameter to Samples.
Programmatic Use
Block Parameter:NumSamples
Type:double
Values:positive scalar
Default:100
Data Types: double
Number of sweeps in output - Number of sweeps in output
1 (default)
Specify the number of sweeps in the block output as a positive integer. This parameter appears only when you set Output signal format to Sweeps.

Simulate using - Block simulation method
Interpreted Execution (default)|Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).
Programmatic Use
Block Parameter:SimulateUsing
Type:enum
Values:Interpreted Execution, Code Generation
Default:Interpreted Execution

## Version History

Introduced in R2014b

## See Also

phased. FMCWWaveform

## Free Space

Free space environment


## Libraries:

Phased Array System Toolbox / Environment and Target

## Description

The Free Space Channel block propagates a signal from one point to another in space. The block models propagation time, free space propagation loss and Doppler shift. The block assumes that the propagation speed is much greater than the target or array speed in which case the stop-and-hop model is valid.

When propagating a signal in free-space to an object and back, you have the choice of either using a single block to compute a two-way free space propagation delay or two blocks to perform one-way propagation delays in each direction. Because the free-space propagation delay is not necessarily an integer multiple of the sampling interval, it may turn out that the total round trip delay in samples when you use a two-way propagation block differs from the delay in samples when you use two oneway propagation blocks. For this reason, it is recommended that, when possible, you use a single twoway propagation block.

## Ports

## Input

## X - Narrowband signal <br> $M$-element complex-valued column vector, $M$-by- $N$ complex-valued matrix.

Narrowband signal, specified as an $M$-element complex-valued column vector or $M$-by- $N$ complexvalued matrix. The quantity $M$ is the number of sample values of the signal and $N$ is the number of signals to propagate. When you specify $N$ signals, you need to specify $N$ signal origins or $N$ signal destinations.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

Pos1 - Signal origin
3-by-1 real-valued column vector | 3 -by- $N$ real-valued matrix
Signal origin, specified as a 3-by-1 real-valued column vector or 3-by- $N$ real-valued matrix. The quantity $N$ is the number of propagated signals and equals the dimension specified in the signal into the port $X$. If Pos 1 is a column vector, it takes the form $[x ; y ; z]$. If Pos 1 is a matrix, each column specifies a different signal origin and has the form [x; y; z]. Pos1 and Pos2 cannot both be specified as matrices - at least one must be a 3-by-1 column vector. Position units are meters.
Data Types: double

## Pos2 - Signal destination

3-by-1 real-valued column vector | 3-by-N real-valued matrix
Signal destination, specified as a 3-by-1 real-valued column vector or 3 -by- $N$ real-valued matrix. The quantity $N$ is the number of propagated signals and equals the dimension specified in the signal into the port $X$. If Pos2 is a column vector, it takes the form $[x ; y ; z]$. If Pos2 is a matrix, each column specifies a different signal origin and has the form [x; y; z]. Pos2 and Pos1 cannot both be specified as matrices - at least one must be a 3-by-1 column vector. Position units are meters.

## Data Types: double

Vel1 - Signal origin velocity
3-by-1 real-valued column vector | 3 -by-N real-valued matrix
Signal origin velocity, specified as a 3-by-1 real-valued column vector or 3-by- $N$ real-valued matrix. The quantity $N$ is the number of propagated signals and equals the dimension specified in the signal into the port X . If Vel 1 is a column vector, it takes the form [ $\mathrm{Vx} ; \mathrm{Vy} ; \mathrm{zV}$ ]. If Vel1 is a matrix, each column specifies a different signal origin and has the form [ Vx ; Vy ; Vz ]. Vell and Vel2 cannot both be specified as matrices - at least one must be a 3 -by- 1 column vector. Position units are meters.

Data Types: double
Vel2 - Signal destination velocity
3-by-1 real-valued column vector | 3-by-N real-valued matrix
Signal destination velocity, specified as a 3-by-1 real-valued column vector or 3-by-N real-valued matrix. The quantity $N$ is the number of propagated signals and equals the dimension specified in the signal into the port X . If $\mathrm{Vel2}$ is a column vector, it takes the form [ $\mathrm{Vx} ; \mathrm{Vy} ; \mathrm{zV}$ ]. If $\mathrm{Vel2}$ is a matrix, each column specifies a different signal origin and has the form [ $\mathrm{Vx} ; \mathrm{Vy}$; Vz ]. Vel2 and Vell cannot both be specified as matrices - at least one must be a 3-by-1 column vector. Position units are meters.

Data Types: double

## Output

Port_1 - Propagated narrowband signal
$M$-element complex-valued column vector, $M$-by- $N$ complex-valued matrix.
Propagated signal, returned as a $M$-element complex-valued column vector, $M$-by- $N$ complex-valued matrix.

If X is a column vector or matrix, Y is also a column vector or matrix with the same dimensions.
The output $Y$ contains signal samples arriving at the signal destination within the current time frame. The current time frame is defined as the time spanned by the current input. Whenever it takes longer than the current time frame for the signal to propagate from the origin to the destination, the output contains no contribution from the input of the current time frame.

## Parameters

Propagation speed (m/s) - Signal propagation speed physconst('LightSpeed') (default)| positive scalar

Signal propagation speed, specified as a real-valued positive scalar. The default value of the speed of light is the value returned by physconst ('LightSpeed').

## Data Types: double

Signal carrier frequency (Hz) - Signal carrier frequency
3 e8 (default) | positive real-valued scalar

Signal carrier frequency, specified as a positive real-valued scalar. Units are in hertz.
Data Types: double
Perform two-way propagation - Perform two-way propagation
off (default) | on
Select this check box to perform round-trip propagation between the origin and destination. Otherwise the block performs one-way propagation from the origin to the destination.

Inherit sample rate - Inherit sample rate from upstream blocks
on (default) | off

Select this parameter to inherit the sample rate from upstream blocks. Otherwise, specify the sample rate using the Sample rate ( $\mathbf{H z}$ ) parameter.

Data Types: Boolean
Sample rate (Hz) - Sampling rate of signal
1e6 (default) | positive real-valued scalar

Specify the signal sampling rate as a positive scalar. Units are in Hz.

## Dependencies

To enable this parameter, clear the Inherit sample rate check box.
Data Types: double
Maximum one-way propagation distance (m) - Maximum one-way propagation distance

## 10e3 (default)

The maximum distance, in meters, between the origin and the destination as a positive scalar. Amplitudes of any signals that propagate beyond this distance will be set to zero.

Simulate using - Block simulation method
Interpreted Execution (default)|Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).

```
Programmatic Use
Block Parameter:SimulateUsing
Type:enum
Values:Interpreted Execution, Code Generation
Default:Interpreted Execution
```


## Algorithms

When the origin and destination are stationary relative to each other, the block output can be written as $y(t)=x(t-\tau) / L$. The quantity $\tau$ is the delay and $L$ is the propagation loss. The delay is computed from $\tau=R / c$ where $R$ is the propagation distance and $c$ is the propagation speed. The free space path loss is given by

$$
L_{f s p}=\frac{(4 \pi R)^{2}}{\lambda^{2}}
$$

where $\lambda$ is the signal wavelength.
This formula assumes that the target is in the far-field of the transmitting element or array. In the near-field, the free-space path loss formula is not valid and can result in losses smaller than one, equivalent to a signal gain. For this reason, the loss is set to unity for range values, $R \leq \lambda / 4 \pi$.

When there is relative motion between the origin and destination, the processing also introduces a frequency shift. This shift corresponds to the Doppler shift between the origin and destination. The frequency shift is $v / \lambda$ for one-way propagation and $2 v / \lambda$ for two-way propagation. The parameter $v$ is the relative speed of the destination with respect to the origin.

## Version History

Introduced in R2014b

## See Also

Wideband Free Space \| phased.FreeSpace

## Frost Beamformer

Frost beamformer


## Libraries:

Phased Array System Toolbox / Beamforming

## Description

The Frost Beamformer block implements a Frost beamformer. A Frost beamformer consists of a timedomain MVDR beamformer followed by a bank of FIR filters. The MVDR beamformer steers the beam towards a given direction while the FIR filters preserve the input signal power.

## Ports

## Input

$\mathbf{X}$ - Input signal
$M$-by- $N$ complex-valued matrix
Input signal, specified as an $M$-by- $N$ matrix, where $M$ is the number of samples in the data, and $N$ is the number of array elements.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
Data Types: double
XT - Training signal
$M$-by- $N$ complex-valued matrix
Input signal, specified as an $M$-by- $N$ matrix, where $M$ is the number of samples in the data, and $N$ is the number of array elements.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

## Dependencies

To enable this port, select the Enable training data input check box.

## Data Types: double

Ang - Beamforming direction
2-by-1 real-valued vector
Beamforming direction, specified as a 2-by-1 real-valued vector taking the form of [AzimuthAngle;ElevationAngle]. Angle units are in degrees. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive, and the elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive. Angles are defined with respect to the local coordinate system of the array.

## Dependencies

To enable this port, set the Source of beamforming direction parameter to Input port.
Data Types: double

## Output

Y - Beamformed output
M-by-1 complex-valued vector
Beamformed output, returned as an $M$-by- 1 complex-valued vector. The quantity $M$ is the number of signal samples.
Data Types: double
W - Beamforming weights
$N$-by-1 complex-valued vector
Beamformed weights, returned as an $N$-by- 1 complex-valued vector. The quantity $N$ is the number of array elements. When the Specify sensor array as parameter is set to Partitioned array or Replicated subarray, $N$ represents the number of subarrays.

## Dependencies

To enable this port, select the Enable weights output check box.
Data Types: double

## Parameters

## Main Tab

Signal propagation speed (m/s) - Signal propagation speed
physconst('LightSpeed') (default)| real-valued positive scalar

Signal propagation speed, specified as a real-valued positive scalar. The default value of the speed of light is the value returned by physconst('LightSpeed'). Units are in meters per second.

## Example: 3e8

Data Types: double
Inherit sample rate - Inherit sample rate from upstream blocks
on (default) | off

Select this parameter to inherit the sample rate from upstream blocks. Otherwise, specify the sample rate using the Sample rate ( Hz ) parameter.
Data Types: Boolean
Sample rate (Hz) - Sampling rate of signal
le6 (default) | positive real-valued scalar

Specify the signal sampling rate as a positive scalar. Units are in Hz .

## Dependencies

To enable this parameter, clear the Inherit sample rate check box.
Data Types: double
FIR filter length - FIR filter length
1 (default) | positive integer

The length of the FIR filter used to process each sensor element data, specified as a positive integer.
Data Types: double
Diagonal loading factor - Diagonal loading factor for stability
nonnegative scalar

Specify the diagonal loading factor as a nonnegative scalar. Diagonal loading is a technique used to achieve robust beamforming performance, especially when the sample support is small.

Enable training data input - Enable the use of training data off (default) | on

Select this check box to specify additional training data via the input port XT. To use the input signal as the training data, clear the check box which removes the port.

Source of beamforming direction - Source of beamforming direction
Property (default)|Input port

Source of beamforming direction, specified as Property or Input port. When you set Source of beamforming direction to Property, you then set the direction using the Beamforming direction (deg) parameter. When you select Input port, the direction is determined by the input to the Ang port.

Beamforming direction (deg) - Beamforming direction
2-by-1 real-valued vector

Beamforming direction, specified as a 2-by-1 real-valued vector taking the form
[AzimuthAngle; ElevationAngle]. Angle units are in degrees. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$. Angles are defined with respect to the local coordinate system of the array.

## Dependencies

To enable this parameter, set the Source of beamforming direction parameter to Property.
Enable weights output - Option to output beamformer weights
off (default) | on

Select this check box to obtain the beamformer weights from the output port, W.

## Simulate using - Block simulation method <br> Interpreted Execution (default)|Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted | The block executes <br> Execution <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).
Programmatic Use
Block Parameter:SimulateUsing
Type:enum
Values:Interpreted Execution, Code Generation
Default:Interpreted Execution

## Sensor Arrays Tab

Specify sensor array as - Method to specify array
Array (no subarrays) (default)|MATLAB expression

Method to specify array, specified as Array (no subarrays) or MATLAB expression.

- Array (no subarrays) - use the block parameters to specify the array.
- MATLAB expression - create the array using a MATLAB expression.

Expression - MATLAB expression used to create an array
Phased Array System Toolbox array System object

MATLAB expression used to create an array, specified as a valid Phased Array System Toolbox array System object.

Example: phased.URA('Size', [5,3])

## Dependencies

To enable this parameter, set Specify sensor array as to MATLAB expression.

## Element type - Array element types

Isotropic Antenna (default)|Cosine Antenna|Custom Antenna|Omni Microphone| Custom Microphone

Antenna or microphone type, specified as one of the following:

- Isotropic Antenna
- Cosine Antenna
- Custom Antenna
- Omni Microphone
- Custom Microphone

Operating frequency range $(\mathbf{H z})$ - Operating frequency range of the antenna or microphone element
[0,1e20] (default) | real-valued 1-by-2 row vector

Specify the operating frequency range of the antenna or microphone element as a 1-by-2 row vector in the form [LowerBound, UpperBound]. The element has no response outside this frequency range. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Isotropic Antenna, Cosine Antenna, or Omni Microphone.

Operating frequency vector (Hz) - Operating frequency range of custom antenna or microphone elements
[0,1e20] (default) | real-valued row vector

Specify the frequencies at which to set antenna and microphone frequency responses as a 1-by- $L$ row vector of increasing real values. The antenna or microphone element has no response outside the frequency range specified by the minimum and maximum elements of this vector. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone. Use Frequency responses (dB) to set the responses at these frequencies.

Baffle the back of the element - Set back response of an Isotropic Antenna element or an Omni Microphone element to zero off (default) | on

Select this check box to baffle the back response of the element. When back baffled, the responses at all azimuth angles beyond $\pm 90^{\circ}$ from broadside are set to zero. The broadside direction is defined as $0^{\circ}$ azimuth angle and $0^{\circ}$ elevation angle.

## Dependencies

To enable this check box, set Element type to Isotropic Antenna or Omni Microphone.
Exponent of cosine pattern - Exponents of azimuth and elevation cosine patterns
[1.5 1.5] (default) | nonnegative scalar | real-valued 1-by-2 matrix of nonnegative values

Specify the exponents of the cosine pattern as a nonnegative scalar or a real-valued 1-by-2 matrix of nonnegative values. When Exponent of cosine pattern is a 1-by-2 vector, the first element is the exponent in the azimuth direction and the second element is the exponent in the elevation direction. When you set this parameter to a scalar, both the azimuth direction and elevation direction cosine patterns are raised to the same power.

## Dependencies

To enable this parameter, set Element type to Cosine Antenna.
Frequency responses (dB) - Antenna and microphone frequency response
[0,0] (default) | real-valued row vector

Frequency response of a custom antenna or custom microphone for the frequencies defined by the Operating frequency vector ( $\mathbf{H z}$ ) parameter. The dimensions of Frequency responses (dB) must match the dimensions of the vector specified by the Operating frequency vector (Hz) parameter.

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone.
Input Pattern Coordinate System - Coordinate system of custom antenna pattern az-el (default) | phi-theta

Coordinate system of custom antenna pattern, specified az-el or phi-theta. When you specify azel, use the Azimuth angles (deg) and Elevations angles (deg) parameters to specify the coordinates of the pattern points. When you specify phi-theta, use the Phi angles (deg) and Theta angles (deg) parameters to specify the coordinates of the pattern points.

## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Azimuth angles (deg) - Azimuth angles of antenna radiation pattern
[-180:180] (default) | real-valued row vector

Specify the azimuth angles at which to calculate the antenna radiation pattern as a 1 -by- $P$ row vector. $P$ must be greater than 2. Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input
Pattern Coordinate System parameter to az-el.
Elevation angles (deg) - Elevation angles of antenna radiation pattern
[-90:90] (default) | real-valued row vector

Specify the elevation angles at which to compute the radiation pattern as a 1-by- $Q$ vector. $Q$ must be greater than 2. Angle units are in degrees. Elevation angles must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input
Pattern Coordinate System parameter to az-el.
Phi Angles (deg) - Phi angle coordinates of custom antenna radiation pattern
$0: 360 \mid$ real-valued 1 -by-P row vector

Phi angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by-P row vector. $P$ must be greater than 2 . Angle units are in degrees. Phi angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Theta Angles (deg) - Theta angle coordinates of custom antenna radiation pattern
$0: 180$ | real-valued 1-by- $Q$ row vector

Theta angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by$Q$ row vector. $Q$ must be greater than 2. Angle units are in degrees. Theta angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Magnitude pattern (dB) - Magnitude of combined antenna radiation pattern zeros $(181,361)$ (default) | real-valued $Q$-by-P matrix | real-valued $Q$-by- $P$-by-L array

Magnitude of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector $(\mathbf{H z})$.

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathrm{Hz})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector $(\mathbf{H z})$ parameter.


## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Phase pattern (deg) - Custom antenna radiation phase pattern
zeros $(181,361)$ (default) | real-valued $Q$-by-P matrix | real-valued $Q$-by- $P$-by-L array

Phase of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector ( $\mathbf{H z}$ ).

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (

Dependencies
To enable this parameter, set Element type to Custom Antenna.
MatchArrayNormal - Rotate antenna element to array normal
on (default) | off

Select this check box to rotate the antenna element pattern to align with the array normal. When not selected, the element pattern is not rotated.

When the antenna is used in an antenna array and the Input Pattern Coordinate System parameter is az-el, selecting this check box rotates the pattern so that the $x$-axis of the element coordinate system points along the array normal. Not selecting uses the element pattern without the rotation.

When the antenna is used in an antenna array and Input Pattern Coordinate System is set to phitheta, selecting this check box rotates the pattern so that the $z$-axis of the element coordinate system points along the array normal.

Use the parameter in conjunction with the Array normal parameter of the URA and UCA arrays.
Dependencies
To enable this parameter, set Element type to Custom Antenna.
Polar pattern frequencies (Hz) - Polar pattern microphone response frequencies
1 e3 (default) | real scalar | real-valued 1-by-L row vector

Polar pattern microphone response frequencies, specified as a real scalar, or a real-valued, 1-by- $L$ vector. The response frequencies lie within the frequency range specified by the Operating frequency vector $(\mathbf{H z})$ vector.

## Dependencies

To enable this parameter, set Element type set to Custom Microphone.
Polar pattern angles (deg) - Polar pattern response angles
[-180:180] (default) | real-valued -by-P row vector

Specify the polar pattern response angles, as a 1-by- $P$ vector. The angles are measured from the central pickup axis of the microphone and must be between $-180^{\circ}$ and $180^{\circ}$, inclusive.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.
Polar pattern (dB) - Custom microphone polar response
zeros $(1,361)$ (default) | real-valued $L$-by- $P$ matrix

Specify the magnitude of the custom microphone element polar patterns as an $L$-by- $P$ matrix. $L$ is the number of frequencies specified in Polar pattern frequencies ( $\mathbf{H z}$ ). $P$ is the number of angles specified in Polar pattern angles (deg). Each row of the matrix represents the magnitude of the polar pattern measured at the corresponding frequency specified in Polar pattern frequencies (Hz) and all angles specified in Polar pattern angles (deg). The pattern is measured in the azimuth plane. In the azimuth plane, the elevation angle is $0^{\circ}$ and the central pickup axis is $0^{\circ}$ degrees azimuth and $0^{\circ}$ degrees elevation. The polar pattern is symmetric around the central axis. You can construct the microphone response pattern in 3-D space from the polar pattern.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.

## Array Parameters

Geometry - Array geometry
ULA (default) | URA | UCA | Conformal Array

Array geometry, specified as one of

- ULA - Uniform linear array
- URA - Uniform rectangular array
- UCA - Uniform circular array
- Conformal Array - arbitrary element positions

Number of elements - Number of array elements
2 for ULA arrays and 5 for UCA arrays (default) | integer greater than or equal to 2

The number of array elements for ULA or UCA arrays, specified as an integer greater than or equal to 2.

## Dependencies

To enable this parameter, set Geometry to ULA or UCA.
Element spacing (m) - Spacing between array elements
0.5 for ULA arrays and [0.5,0.5] for URA arrays (default) | positive scalar for ULA or URA arrays | 2 -element vector of positive values for URA arrays

Spacing between adjacent array elements:

- ULA - specify the spacing between two adjacent elements in the array as a positive scalar.
- URA - specify the spacing as a positive scalar or a 1 -by-2 vector of positive values. If Element spacing (m) is a scalar, the row and column spacings are equal. If Element spacing (m) is a vector, the vector has the form [SpacingBetweenArrayRows, SpacingBetweenArrayColumns].


## Dependencies

To enable this parameter, set Geometry to ULA or URA.
Array axis - Linear axis direction of ULA
$y$ (default) $|x| z$

Linear axis direction of ULA, specified as $y, x$, or $z$. All ULA array elements are uniformly spaced along this axis in the local array coordinate system.

## Dependencies

- To enable this parameter, set Geometry to ULA.
- This parameter is also enabled when the block only supports ULA arrays.

Array size - Dimensions of URA array
$[2,2]$ (default) | positive integer | 1-by-2 vector of positive integers

Dimensions of a URA array, specified as a positive integer or 1-by-2 vector of positive integers.

- If Array size is a 1 -by- 2 vector, the vector has the form [NumberOfArrayRows, NumberOfArrayColumns].
- If Array size is an integer, the array has the same number of elements in each row and column.

For a URA, array elements are indexed from top to bottom along the leftmost array column, and continued to the next columns from left to right. In this figure, the Array size value of [3,2] creates an array having three rows and two columns.

## Size and Element Indexing Order

for Uniform Rectangular Arrays
Example: Size $=[3,2]$


## Dependencies

To enable this parameter, set Geometry to URA.
Element lattice - Lattice of URA element positions
Rectangular (default) | Triangular

Lattice of URA element positions, specified as Rectangular or Triangular.

- Rectangular - Aligns all the elements in row and column directions.
- Triangular - Shifts the even-row elements of a rectangular lattice toward the positive row-axis direction. The displacement is one-half the element spacing along the row dimension.


## Dependencies

To enable this parameter, set Geometry to URA.
Array normal - Array normal direction
$x$ for URA arrays or $z$ for UCA arrays (default) | y

Array normal direction, specified as $x, y$, or $z$.
Elements of planar arrays lie in a plane orthogonal to the selected array normal direction. Element boresight directions point along the array normal direction.

| Array Normal Parameter Value | Element Positions and Boresight Directions |
| :--- | :--- |
| $x$ | Array elements lie in the $y z$-plane. All element <br> boresight vectors point along the $x$-axis. |
| $y$ | Array elements lie in the $z x$-plane. All element <br> boresight vectors point along the $y$-axis. |
| $z$ | Array elements lie in the $x y$-plane. All element <br> boresight vectors point along the $z$-axis. |

## Dependencies

To enable this parameter, set Geometry to URA or UCA.

## Radius of UCA (m) - UCA array radius

0.5 (default) | positive scalar

Radius of UCA array, specified as a positive scalar.

## Dependencies

To enable this parameter, set Geometry to UCA.
Element positions (m) - Positions of conformal array elements
[0;0;0] (default)|3-by-Nmatrix of real values

Positions of the elements in a conformal array, specified as a 3 -by- $N$ matrix of real values, where $N$ is the number of elements in the conformal array. Each column of this matrix represents the position [ $x ; y ; z$ ] of an array element in the array local coordinate system. The origin of the local coordinate system is ( $0,0,0$ ). Units are in meters.

## Dependencies

To enable this parameter set Geometry to Conformal Array.

## Data Types: double

Element normals (deg) - Direction of conformal array element normal vectors
[0;0]|2-by-1 column vector | 2 -by- $N$ matrix

Direction of element normal vectors in a conformal array, specified as a 2 -by-1 column vector or a 2-by- $N$ matrix. $N$ indicates the number of elements in the array. If the parameter value is a matrix, each column specifies the normal direction of the corresponding element in the form
[azimuth;elevation] with respect to the local coordinate system. The local coordinate system aligns the positive $x$-axis with the direction normal to the conformal array. If the parameter value is a 2 -by- 1 column vector, the same pointing direction is used for all array elements.

You can use the Element positions (m) and Element normals (deg) parameters to represent any arrangement in which pairs of elements differ by certain transformations. The transformations can combine translation, azimuth rotation, and elevation rotation. However, you cannot use transformations that require rotation about the normal direction.

To enable this parameter, set Geometry to Conformal Array.

Data Types: double
Taper - Array element tapers
1 (default) | complex scalar | complex-valued row vector

Specify element tapering as a complex-valued scalar or a complex-valued 1-by- $N$ row vector. In this vector, $N$ represents the number of elements in the array.

Also known as element weights, tapers multiply the array element responses. Tapers modify both amplitude and phase of the response to reduce side lobes or steer the main response axis.

If Taper is a scalar, the same weight is applied to each element. If Taper is a vector, a weight from the vector is applied to the corresponding sensor element. The number of weights must match the number of elements of the array.
Data Types: double

## Version History

Introduced in R2014b

## See Also

phased.FrostBeamformer

## GCC DOA and TOA

Generalized cross-correlator with phase transform


## Libraries:

Phased Array System Toolbox / Direction of Arrival

## Description

The GCC DOA and TOA block estimates the direction of arrival and time of arrival of a signal at an array. The block uses a generalized cross-correlation with phase transform (GCC-PHAT) algorithm.

## Ports

## Input

Port_1 - Received signal
$M$-by- $N$ complex-valued matrix
Received signal, input as an $M$-by- $N$ complex-valued matrix. The quantity $M$ is the number of sample values (snapshots) of the signal and $N$ is the number of sensor elements in the array. For subarrays, $N$ is the number of subarrays.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
Data Types: single | double
Complex Number Support: Yes

## Output

Ang - Direction of arrival
2-by-1 real-valued column vector | scalar
Direction of arrival of a signal, output as a 2-by-1 real-valued column vector in the form [azimuth;elevation]. If the array is a uniform linear array, Ang is a scalar representing the broadside angle. Angle units are in degrees defined with respect to the local coordinate system of the array.

Data Types: double
Tau - Time delays of arrival
1-by- $P$ real-valued row vector
Time delays of arrival, output as 1-by- $P$ real-valued row vector. $P$ is the number of sensor pairs selected from the array.

- When Source of sensor pairs is set to Auto, $P=N-1 . N$ is the number of elements in the array.
- When Source of sensor pairs is set to Property, $P$ is the number of sensor pairs specified by the Sensor pairs parameter.

Time units are seconds.

## Dependencies

To enable this port, select the Enable delay output check box.
Data Types: double
Rxy - Estimated cross-correlation
(2M+1)-by-P complex-valued matrix
Estimated cross-correlation between pairs of sensors, output as a ( $2 M+1$ )-by- $P$ complex-valued matrix, where $P$ is the number of sensor pairs selected from the array. $M$ is the number of time samples in the input signal.

- When Source of sensor pairs is set to Auto, $P=N-1 . N$ is the number of elements in the array. The columns in Rxy contain the correlations between the first sensor and all other sensors.
- When Source of sensor pairs is set to Property, $P$ is the number of sensor pairs specified by the Sensor pairs parameter. Each column in Rxy contains the correlation for the corresponding pair of sensors.


## Dependencies

To enable this port, select the Enable correlation output check box.
Data Types: double
Complex Number Support: Yes

## Lag - Time lags

M-by-1 real-valued column vector
Time lags, output as an ( $2 M+1$ )-by-1 real-valued column vector. $M$ is the number of time samples in the input signal. Each time lag applies to the corresponding row in the cross-correlation matrix.

## Dependencies

To enable this port, select the Enable correlation output check box.
Data Types: double

## Parameters

## Main Tab

Signal propagation speed (m/s) - Signal propagation speed
physconst('LightSpeed') (default)| real-valued positive scalar

Signal propagation speed, specified as a real-valued positive scalar. The default value of the speed of light is the value returned by physconst('LightSpeed '). Units are in meters per second.

## Example: 3e8

Data Types: double
Inherit sample rate - Inherit sample rate from upstream blocks on (default) | off

Select this parameter to inherit the sample rate from upstream blocks. Otherwise, specify the sample rate using the Sample rate (Hz) parameter.
Data Types: Boolean
Sample rate (Hz) - Sampling rate of signal
1e6 (default) | positive real-valued scalar

Specify the signal sampling rate as a positive scalar. Units are in Hz.

## Dependencies

To enable this parameter, clear the Inherit sample rate check box.
Data Types: double
Source of sensor pairs - Source of sensor pairs
Auto (default) | Property
Source

| Property | When you set this parameter to Property, specify the sensor <br> pairs for computing correlation using the Sensor <br> pairs parameter. |
| :--- | :--- |
| Auto | When you set this parameter to Auto, correlations are <br> computed between the first element and all other elements. <br> The first element serves as the reference channel. |

## Sensor pairs - Sensor pairs

## [2;1] (default)

Sensor pairs, specified as a 2-by-M matrix of strictly positive integers.

## Dependencies

This parameter appears only when you set the Source of sensor pairs parameter to Property.
Enable correlation output - Option to enable correlation output
off (default) | on
Check this box to output the correlations computed using the GCC-PHAT algorithm as well as the corresponding lags between sensor pairs. Correlation values are output via the Rxy port. Lag values are output via the Lags port. These ports appear only when you check the Enable correlation output box. Clear this check box to disable output of correlations.

Enable delay output - Option to enable delay output
off (default) | on

Select this check box to output the delay corresponding to the arrival angle of a signal between each sensor pair. The delay is output in the Tau port. This port appears only when you check the Enable delay output box. Clear this check box to disable output of delays.

Simulate using - Block simulation method
Interpreted Execution (default) | Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).

```
Programmatic Use
Block Parameter:SimulateUsing
Type:enum
Values:Interpreted Execution, Code Generation
Default:Interpreted Execution
```


## Sensor Array Tab

```
Specify sensor array as - Method to specify array
Array (no subarrays) (default)|Partitioned array|Replicated subarray|MATLAB expression
```

Method to specify array, specified as Array (no subarrays) or MATLAB expression.

- Array (no subarrays) - use the block parameters to specify the array.
- Partitioned array - use the block parameters to specify the array.
- Replicated subarray - use the block parameters to specify the array.
- MATLAB expression - create the array using a MATLAB expression.


## Element Parameters

Element type - Array element types
Isotropic Antenna (default)|Cardioid Antenna|Cosine Antenna|Custom Antenna| Gaussian Antenna|Sinc Antenna|Omni Microphone|Custom Microphone

Antenna or microphone type, specified as one of the following:

- Isotropic Antenna
- Cardioid Antenna
- Cosine Antenna
- Custom Antenna
- Gaussian Antenna
- Sinc Antenna
- Omni Microphone
- Custom Microphone

Operating frequency range $(\mathbf{H z})$ - Operating frequency range of the antenna or microphone element
[0,1e20] (default) | real-valued 1-by-2 row vector

Specify the operating frequency range of the antenna or microphone element as a 1-by-2 row vector in the form [LowerBound, UpperBound]. The element has no response outside this frequency range. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Isotropic Antenna, Cosine Antenna, or Omni Microphone.

Baffle the back of the element - Set back response of an Isotropic Antenna element or an Omni Microphone element to zero
off (default) | on

Select this check box to baffle the back response of the element. When back baffled, the responses at all azimuth angles beyond $\pm 90^{\circ}$ from broadside are set to zero. The broadside direction is defined as $0^{\circ}$ azimuth angle and $0^{\circ}$ elevation angle.

## Dependencies

To enable this check box, set Element type to Isotropic Antenna or Omni Microphone.
Null axis direction - Null axis direction
-x (default) | $+\mathrm{x}|+\mathrm{y}|-\mathrm{y}|+\mathrm{z}|-\mathrm{z}$

## Dependencies

To enable this parameter, set Element type to Cardioid Antenna.
Exponent of cosine pattern - Exponents of azimuth and elevation cosine patterns
[1.5 1.5] (default) | nonnegative scalar | real-valued 1-by-2 matrix of nonnegative values

Specify the exponents of the cosine pattern as a nonnegative scalar or a real-valued 1-by-2 matrix of nonnegative values. When Exponent of cosine pattern is a 1-by-2 vector, the first element is the exponent in the azimuth direction and the second element is the exponent in the elevation direction. When you set this parameter to a scalar, both the azimuth direction and elevation direction cosine patterns are raised to the same power.

## Dependencies

To enable this parameter, set Element type to Cosine Antenna.
Operating frequency vector ( Hz ) - Operating frequency range of custom antenna or microphone elements
[0,1e20] (default) | real-valued row vector

Specify the frequencies at which to set antenna and microphone frequency responses as a 1-by-L row vector of increasing real values. The antenna or microphone element has no response outside the frequency range specified by the minimum and maximum elements of this vector. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone. Use Frequency responses (dB) to set the responses at these frequencies.

Frequency responses (dB) - Antenna and microphone frequency response [0, 0] (default) | real-valued row vector

Frequency response of a custom antenna or custom microphone for the frequencies defined by the Operating frequency vector (Hz) parameter. The dimensions of Frequency responses (dB) must match the dimensions of the vector specified by the Operating frequency vector $(\mathbf{H z})$ parameter.

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone.
Input Pattern Coordinate System - Coordinate system of custom antenna pattern
az-el (default)|phi-theta

Coordinate system of custom antenna pattern, specified az-el or phi-theta. When you specify azel, use the Azimuth angles (deg) and Elevations angles (deg) parameters to specify the coordinates of the pattern points. When you specify phi-theta, use the Phi angles (deg) and Theta angles (deg) parameters to specify the coordinates of the pattern points.
Dependencies
To enable this parameter, set Element type to Custom Antenna.

Azimuth angles (deg) - Azimuth angles of antenna radiation pattern
[-180:180] (default) | real-valued row vector

Specify the azimuth angles at which to calculate the antenna radiation pattern as a 1 -by- $P$ row vector. $P$ must be greater than 2. Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to az-el.

Elevation angles (deg) - Elevation angles of antenna radiation pattern
[-90:90] (default) | real-valued row vector

Specify the elevation angles at which to compute the radiation pattern as a 1-by- $Q$ vector. $Q$ must be greater than 2. Angle units are in degrees. Elevation angles must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to az-el.

Phi Angles (deg) - Phi angle coordinates of custom antenna radiation pattern
$0: 360$ | real-valued 1-by-P row vector

Phi angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by- $P$ row vector. $P$ must be greater than 2 . Angle units are in degrees. Phi angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Theta Angles (deg) - Theta angle coordinates of custom antenna radiation pattern 0:180 | real-valued 1-by-Q row vector

Theta angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by$Q$ row vector. $Q$ must be greater than 2 . Angle units are in degrees. Theta angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Magnitude pattern (dB) - Magnitude of combined antenna radiation pattern zeros $(181,361)$ (default) | real-valued $Q$-by- $P$ matrix | real-valued $Q$-by- $P$-by- $L$ array

Magnitude of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi - theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector ( $\mathbf{H z}$ ).

- If this parameter is a $Q$-by-P matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (Hz) parameter.


## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Phase pattern (deg) - Custom antenna radiation phase pattern
zeros $(181,361)$ (default) | real-valued $Q$-by- $P$ matrix | real-valued $Q$-by- $P$-by- $L$ array

Phase of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi - theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector ( $\mathbf{H z}$ ).

- If this parameter is a $Q$-by-P matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (


## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Align element normal with array normal - Align element normal with array normal
on (default) | off

## Dependencies

This parameter is enabled when Element type is set to Custom Antenna.
Radiation pattern beamwidth (deg) - Radiation pattern beamwidth
[10,10] (default)

## Dependencies

This parameter is enabled when Element type is set to Gaussian Antenna.
Polar pattern frequencies (Hz) - Polar pattern microphone response frequencies
1 e3 (default) | real scalar | real-valued 1-by-L row vector

Polar pattern microphone response frequencies, specified as a real scalar, or a real-valued, 1-by- $L$ vector. The response frequencies lie within the frequency range specified by the Operating frequency vector $(\mathbf{H z})$ vector.

## Dependencies

To enable this parameter, set Element type set to Custom Microphone.
Polar pattern angles (deg) - Polar pattern response angles
[-180:180] (default) | real-valued -by-P row vector

Specify the polar pattern response angles, as a 1-by- $P$ vector. The angles are measured from the central pickup axis of the microphone and must be between $-180^{\circ}$ and $180^{\circ}$, inclusive.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.
Polar pattern (dB) - Custom microphone polar response
zeros (1,361) (default) | real-valued $L$-by- $P$ matrix

Specify the magnitude of the custom microphone element polar patterns as an $L$-by- $P$ matrix. $L$ is the number of frequencies specified in Polar pattern frequencies $(\mathbf{H z}) . P$ is the number of angles specified in Polar pattern angles (deg). Each row of the matrix represents the magnitude of the polar pattern measured at the corresponding frequency specified in Polar pattern frequencies $(\mathbf{H z})$ and all angles specified in Polar pattern angles (deg). The pattern is measured in the azimuth plane. In the azimuth plane, the elevation angle is $0^{\circ}$ and the central pickup axis is $0^{\circ}$ degrees azimuth and $0^{\circ}$ degrees elevation. The polar pattern is symmetric around the central axis. You can construct the microphone response pattern in 3-D space from the polar pattern.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.

## Array Parameters

Geometry - Array geometry
ULA (default) | URA | UCA | Conformal Array

Array geometry, specified as one of

- ULA - Uniform linear array
- URA - Uniform rectangular array
- UCA - Uniform circular array
- Conformal Array - arbitrary element positions

Number of elements - Number of array elements
2 for ULA arrays and 5 for UCA arrays (default) | integer greater than or equal to 2

The number of array elements for ULA or UCA arrays, specified as an integer greater than or equal to 2.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

## Dependencies

To enable this parameter, set Geometry to ULA or UCA.
Array size - Dimensions of URA array
[2,2] (default) | positive integer | 1-by-2 vector of positive integers

Dimensions of a URA array, specified as a positive integer or 1-by-2 vector of positive integers.

- If Array size is a 1 -by-2 vector, the vector has the form [NumberOfArrayRows, NumberOfArrayColumns].
- If Array size is an integer, the array has the same number of rows and columns.
- When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

For a URA, array elements are indexed from top to bottom along the leftmost column, and then continue to the next columns from left to right. In this figure, the Array size value of [3, 2] creates an array having three rows and two columns.

Size and Element Indexing Order
for Uniform Rectangular Arrays
Example: Size $=[3,2]$


## Dependencies

To enable this parameter, set Geometry to URA.

## Element spacing (m) - Spacing between array elements

0.5 for ULA arrays and [0.5,0.5] for URA arrays (default) | positive scalar for ULA or URA arrays | 2-element vector of positive values for URA arrays

Spacing between adjacent array elements:

- ULA - specify the spacing between two adjacent elements in the array as a positive scalar.
- URA - specify the spacing as a positive scalar or a 1-by-2 vector of positive values. If Element spacing (m) is a scalar, the row and column spacings are equal. If Element spacing (m) is a vector, the vector has the form [SpacingBetweenArrayRows, SpacingBetweenArrayColumns].
- When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.


## Dependencies

To enable this parameter, set Geometry to ULA or URA.
Array axis - Linear axis direction of ULA
$y$ (default) $|x| z$

Linear axis direction of ULA, specified as $y, x$, or $z$. All ULA array elements are uniformly spaced along this axis in the local array coordinate system.

## Dependencies

- To enable this parameter, set Geometry to ULA.
- This parameter is also enabled when the block only supports ULA arrays.

Element lattice - Lattice of URA element positions
Rectangular (default)| Triangular

Lattice of URA element positions, specified as Rectangular or Triangular.

- Rectangular - Aligns all the elements in row and column directions.
- Triangular - Shifts the even-row elements of a rectangular lattice toward the positive row-axis direction. The displacement is one-half the element spacing along the row dimension.


## Dependencies

To enable this parameter, set Geometry to URA.
Array normal - Array normal direction
$x$ for URA arrays or $z$ for UCA arrays (default) | y

Array normal direction, specified as $x, y$, or $z$.
Elements of planar arrays lie in a plane orthogonal to the selected array normal direction. Element boresight directions point along the array normal direction.

| Array Normal Parameter Value | Element Positions and Boresight Directions |
| :--- | :--- |
| $x$ | Array elements lie in the $y z$-plane. All element <br> boresight vectors point along the $x$-axis. |
| $y$ | Array elements lie in the $z x$-plane. All element <br> boresight vectors point along the $y$-axis. |
| $z$ | Array elements lie in the $x y$-plane. All element <br> boresight vectors point along the $z$-axis. |

## Dependencies

To enable this parameter, set Geometry to URA or UCA.
Radius of UCA (m) - UCA array radius
0.5 (default) | positive scalar

Radius of UCA array, specified as a positive scalar.

## Dependencies

To enable this parameter, set Geometry to UCA.
Element positions (m) - Positions of conformal array elements [0;0;0] (default) | 3-by-Nmatrix of real values

Positions of the elements in a conformal array, specified as a 3 -by- $N$ matrix of real values, where $N$ is the number of elements in the conformal array. Each column of this matrix represents the position [ $x ; y ; z$ ] of an array element in the array local coordinate system. The origin of the local coordinate system is ( $0,0,0$ ). Units are in meters.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

## Dependencies

To enable this parameter set Geometry to Conformal Array.
Element normals (deg) - Direction of conformal array element normal vectors [0;0] | 2-by-1 column vector | 2 -by- $N$ matrix

Direction of element normal vectors in a conformal array, specified as a 2-by-1 column vector or a 2-by- $N$ matrix. $N$ indicates the number of elements in the array. For a matrix, each column specifies the normal direction of the corresponding element in the form [azimuth; elevation] with respect to the local coordinate system. The local coordinate system aligns the positive $x$-axis with the direction normal to the conformal array. If the parameter value is a 2 -by- 1 column vector, the same pointing direction is used for all array elements.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

You can use the Element positions (m) and Element normals (deg) parameters to represent any arrangement in which pairs of elements differ by certain transformations. The transformations can
combine translation, azimuth rotation, and elevation rotation. However, you cannot use transformations that require rotation about the normal direction.

## Dependencies

To enable this parameter, set Geometry to Conformal Array.
Taper - Array element tapers
1 (default) | complex-valued scalar | complex-valued row vector

Element tapering, specified as a complex-valued scalar or a complex-valued 1-by- $N$ row vector. In this vector, $N$ represents the number of elements in the array.

Also known as element weights, tapers multiply the array element responses. Tapers modify both amplitude and phase of the response to reduce side lobes or steer the main response axis.

If Taper is a scalar, the same weight is applied to each element. If Taper is a vector, a weight from the vector is applied to the corresponding sensor element. The number of weights must match the number of elements of the array.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

Subarray definition matrix - Define elements belonging to subarrays
logical matrix

Specify the subarray selection as an $M$-by- $N$ matrix. $M$ is the number of subarrays and $N$ is the total number of elements in the array. Each row of the matrix represents a subarray and each entry in the row indicates when an element belongs to the subarray. When the entry is zero, the element does not belong the subarray. A nonzero entry represents a complex-valued weight applied to the corresponding element. Each row must contain at least one nonzero entry.

The phase center of each subarray lies at the subarray geometric center. The subarray geometric center depends on the Subarray definition matrix and Geometry parameters.

## Dependencies

To enable this parameter, set Specify sensor array as to Partitioned array.
Subarray steering method - Specify subarray steering method
None (default) | Phase | Time

Subarray steering method, specified as one of

- None
- Phase
- Time
- Custom

Selecting Phase or Time opens the Steer input port on the Narrowband Receive Array, Narrowband Transmit Array, Wideband Receive Array, Wideband Transmit Array blocks, Constant Gamma Clutter, and GPU Constant Gamma Clutter blocks.

Selecting Custom opens the WS input port on the Narrowband Receive Array, Narrowband Transmit Array, Wideband Receive Array, Wideband Transmit Array blocks, Constant Gamma Clutter, and GPU Constant Gamma Clutter blocks.

## Dependencies

To enable this parameter, set Specify sensor array as to Partitioned array or Replicated subarray.

Phase shifter frequency (Hz) - Subarray phase shifting frequency
3.0 e 8 (default) | positive real-valued scalar

Operating frequency of subarray steering phase shifters, specified as a positive real-valued scalar.
Units are Hz.

## Dependencies

To enable this parameter, set Sensor array to Partitioned array or Replicated subarray and set Subarray steering method to Phase.

Number of bits in phase shifters - Subarray steering phase shift quantization bits
0 (default) | non-negative integer

Subarray steering phase shift quantization bits, specified as a non-negative integer. A value of zero indicates that no quantization is performed.

## Dependencies

To enable this parameter, set Sensor array to Partitioned array or Replicated subarray and set Subarray steering method to Phase.

Subarrays layout - Subarray position specification
Rectangular (default) | Custom

Specify the layout of replicated subarrays as Rectangular or Custom.

- When you set this parameter to Rectangular, use the Grid size and Grid spacing parameters to place the subarrays.
- When you set this parameter to Custom, use the Subarray positions (m) and Subarray normals parameters to place the subarrays.


## Dependencies

To enable this parameter, set Sensor array to Replicated subarray
Grid size - Dimensions of rectangular subarray grid [1,2] (default)

Rectangular subarray grid size, specified as a single positive integer, or a 1-by-2 row vector of positive integers.

If Grid size is an integer scalar, the array has an equal number of subarrays in each row and column. If Grid size is a 1-by-2 vector of the form [NumberOfRows, NumberOfColumns], the first entry is
the number of subarrays along each column. The second entry is the number of subarrays in each row. A row is along the local $y$-axis, and a column is along the local $z$-axis. The figure here shows how you can replicate a 3-by-2 URA subarray using a Grid size of [1,2].
$3 \times 2$ Element URA
Replicated on a $1 \times 2$ Grid


## Dependencies

To enable this parameter, set Sensor array to Replicated subarray and Subarrays layout to Rectangular.

Grid spacing ( $\mathbf{m}$ ) - Spacing between subarrays on rectangular grid
Auto (default) | positive real-valued scalar | 1-by-2 vector of positive real-values

The rectangular grid spacing of subarrays, specified as a positive, real-valued scalar, a 1-by-2 row vector of positive, real-values, or Auto. Units are in meters.

- If Grid spacing is a scalar, the spacing along the row and the spacing along the column is the same.
- If Grid spacing is a 1-by-2 row vector, the vector has the form [SpacingBetweenRows, SpacingBetweenColumn]. The first entry specifies the spacing between rows along a column. The second entry specifies the spacing between columns along a row.
- If Grid spacing is set to Auto, replication preserves the element spacing of the subarray for both rows and columns while building the full array. This option is available only when you specify Geometry as ULA or URA.


## Dependencies

To enable this parameter, set Sensor array to Replicated subarray and Subarrays layout to Rectangular.

Subarray positions (m) - Positions of subarrays
[0,0;0.5,0.5;0,0] (default)| 3-by-N real-valued matrix

Positions of the subarrays in the custom grid, specified as a real 3-by- $N$ matrix, where $N$ is the number of subarrays in the array. Each column of the matrix represents the position of a single subarray in the array local coordinate system. The coordinates are expressed in the form $[x ; y ; z]$. Units are in meters.

## Dependencies

To enable this parameter, set Sensor array to Replicated subarray and Subarrays layout to Custom.

Subarray normals - Direction of subarray normal vectors
[0, 0;0,0] (default) | 2 -by- $N$ real matrix

Specify the normal directions of the subarrays in the array. This parameter value is a 2 -by- $N$ matrix, where $N$ is the number of subarrays in the array. Each column of the matrix specifies the normal direction of the corresponding subarray, in the form [azimuth; elevation]. Angle units are in degrees. Angles are defined with respect to the local coordinate system.

You can use the Subarray positions and Subarray normals parameters to represent any arrangement in which pairs of subarrays differ by certain transformations. The transformations can combine translation, azimuth rotation, and elevation rotation. However, you cannot use transformations that require rotation about the normal.

## Dependencies

To enable this parameter, set the Sensor array parameter to Replicated subarray and the Subarrays layout to Custom.

Expression - MATLAB expression used to create an array
Phased Array System Toolbox array System object

MATLAB expression used to create an array, specified as a valid Phased Array System Toolbox array System object.

Example: phased.URA('Size', [5,3])

## Dependencies

To enable this parameter, set Specify sensor array as to MATLAB expression.

## Version History

## Introduced in R2015b

## See Also

phased.GCCEstimator|gccphat

## GSC Beamformer

Generalized sidelobe canceller


## Libraries:

Phased Array System Toolbox / Beamforming

## Description

The GSC Beamformerblock implements a generalized sidelobe cancellation (GSC) beamformer. A GSC beamformer splits an arrays incoming signals and sends them through a conventional beamformer path and a sidelobe canceling path. The algorithm first presteers the array to the beamforming direction and then adaptively chooses filter weights to minimize power at the output of the sidelobe canceling path. The algorithm uses least mean squares (LMS) to compute the adaptive weights. The final beamformed signal is the difference between the outputs of the two paths.

## Ports

## Input

X - Input signal
$M$-by- $N$ complex-valued matrix
Input signal, specified as an $M$-by- $N$ matrix, where $M$ is the number of samples in the data, and $N$ is the number of array elements.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

## Data Types: double

Ang - Beamforming direction
2 -by-1 real-valued vector
Beamforming direction, specified as a 2 -by- 1 real-valued vector, where taking the form of [AzimuthAngle;ElevationAngle]. Angle units are in degrees. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive, and the elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive. Angles are defined with respect to the local coordinate system of the array.

## Dependencies

To enable this port, set the Source of beamforming direction parameter to Input port.
Data Types: double

## Output

$\mathbf{Y}$ - Beamformed output
$M$-by-1 complex-valued vector

Beamformed output, returned as an $M$-by- 1 complex-valued vector. The quantity $M$ is the number of signal samples.

## Parameters

## Main Tab

Signal propagation speed (m/s) - Signal propagation speed
physconst('LightSpeed') (default)| real-valued positive scalar

Signal propagation speed, specified as a real-valued positive scalar. The default value of the speed of light is the value returned by physconst('LightSpeed'). Units are in meters per second.

## Example: 3e8

Data Types: double
Inherit sample rate - Inherit sample rate from upstream blocks
on (default) | off

Select this parameter to inherit the sample rate from upstream blocks. Otherwise, specify the sample rate using the Sample rate (Hz) parameter.
Data Types: Boolean
Sample rate (Hz) - Sampling rate of signal
1e6 (default) | positive real-valued scalar

Specify the signal sampling rate as a positive scalar. Units are in Hz .

## Dependencies

To enable this parameter, clear the Inherit sample rate check box.

## Data Types: double

Signal path FIR filter length - Length of the FIR filter along the signal path
1 (default) | positive integer

Length of the signal path FIR filter, specified as a positive integer. The FIR filter is a delta function.
Adaptive filter step size - LMS adaptive filter step size factor
0.1 (default) | positive scalar

The adaptive filter step size factor, specified as a positive scalar. This quantity, when divided by the total power in the sidelobe canceling path, determines the actual adaptive filter step size used by the LMS algorithm.

Beamforming direction (deg) - Beamforming direction
2-by-1 real-valued vector

Beamforming direction, specified as a 2-by-1 real-valued vector taking the form
[AzimuthAngle;ElevationAngle]. Angle units are in degrees. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$. Angles are defined with respect to the local coordinate system of the array.

## Dependencies

To enable this parameter, set the Source of beamforming direction parameter to Property.
Source of beamforming direction - Source of beamforming direction
Property (default)|Input port

Source of beamforming direction, specified as Property or Input port. When you set Source of beamforming direction to Property, you then set the direction using the Beamforming direction (deg) parameter. When you select Input port, the direction is determined by the input to the Ang port.

## Simulate using - Block simulation method

Interpreted Execution (default)|Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).

```
Programmatic Use
Block Parameter:SimulateUsing
Type:enum
```

Values:Interpreted Execution, Code Generation
Default:Interpreted Execution
Sensor Arrays Tab
Specify sensor array as - Method to specify array
Array (no subarrays) (default)|MATLAB expression

Method to specify array, specified as Array (no subarrays) or MATLAB expression.

- Array (no subarrays) - use the block parameters to specify the array.
- MATLAB expression - create the array using a MATLAB expression.

Expression - MATLAB expression used to create an array
Phased Array System Toolbox array System object

MATLAB expression used to create an array, specified as a valid Phased Array System Toolbox array System object.
Example: phased.URA('Size', [5, 3])
Dependencies
To enable this parameter, set Specify sensor array as to MATLAB expression.

## Element Parameters

Element type - Array element types
Isotropic Antenna (default)|Cosine Antenna|Custom Antenna|Omni Microphone| Custom Microphone

Antenna or microphone type, specified as one of the following:

- Isotropic Antenna
- Cosine Antenna
- Custom Antenna
- Omni Microphone
- Custom Microphone

Operating frequency range $\mathbf{( H z )}$ - Operating frequency range of the antenna or microphone element
[0, 1e20] (default) | real-valued 1-by-2 row vector

Specify the operating frequency range of the antenna or microphone element as a 1-by-2 row vector in the form [LowerBound, UpperBound]. The element has no response outside this frequency range. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Isotropic Antenna, Cosine Antenna, or Omni Microphone.

Operating frequency vector (Hz) - Operating frequency range of custom antenna or microphone elements
[0,1e20] (default) | real-valued row vector

Specify the frequencies at which to set antenna and microphone frequency responses as a 1-by-L row vector of increasing real values. The antenna or microphone element has no response outside the frequency range specified by the minimum and maximum elements of this vector. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone. Use Frequency responses (dB) to set the responses at these frequencies.

Baffle the back of the element - Set back response of an Isotropic Antenna element or an Omni Microphone element to zero off (default) | on

Select this check box to baffle the back response of the element. When back baffled, the responses at all azimuth angles beyond $\pm 90^{\circ}$ from broadside are set to zero. The broadside direction is defined as $0^{\circ}$ azimuth angle and $0^{\circ}$ elevation angle.

## Dependencies

To enable this check box, set Element type to Isotropic Antenna or Omni Microphone.
Exponent of cosine pattern - Exponents of azimuth and elevation cosine patterns
[1.5 1.5] (default) | nonnegative scalar | real-valued 1-by-2 matrix of nonnegative values

Specify the exponents of the cosine pattern as a nonnegative scalar or a real-valued 1-by-2 matrix of nonnegative values. When Exponent of cosine pattern is a 1-by-2 vector, the first element is the exponent in the azimuth direction and the second element is the exponent in the elevation direction. When you set this parameter to a scalar, both the azimuth direction and elevation direction cosine patterns are raised to the same power.

## Dependencies

To enable this parameter, set Element type to Cosine Antenna.
Frequency responses (dB) - Antenna and microphone frequency response
[0,0] (default) | real-valued row vector

Frequency response of a custom antenna or custom microphone for the frequencies defined by the Operating frequency vector (Hz) parameter. The dimensions of Frequency responses (dB) must match the dimensions of the vector specified by the Operating frequency vector $(\mathbf{H z})$ parameter.

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone.
Input Pattern Coordinate System - Coordinate system of custom antenna pattern az-el (default)|phi-theta

Coordinate system of custom antenna pattern, specified az-el or phi-theta. When you specify azel, use the Azimuth angles (deg) and Elevations angles (deg) parameters to specify the coordinates of the pattern points. When you specify phi-theta, use the Phi angles (deg) and Theta angles (deg) parameters to specify the coordinates of the pattern points.

Dependencies
To enable this parameter, set Element type to Custom Antenna.
Azimuth angles (deg) - Azimuth angles of antenna radiation pattern
[-180:180] (default) | real-valued row vector

Specify the azimuth angles at which to calculate the antenna radiation pattern as a 1-by-P row vector. $P$ must be greater than 2. Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to az-el.

Elevation angles (deg) - Elevation angles of antenna radiation pattern
[-90:90] (default) | real-valued row vector

Specify the elevation angles at which to compute the radiation pattern as a 1-by- $Q$ vector. $Q$ must be greater than 2. Angle units are in degrees. Elevation angles must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input
Pattern Coordinate System parameter to az-el.
Phi Angles (deg) - Phi angle coordinates of custom antenna radiation pattern
$0: 360 \mid$ real-valued 1-by-P row vector

Phi angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by- $P$ row vector. $P$ must be greater than 2 . Angle units are in degrees. Phi angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input
Pattern Coordinate System parameter to phi-theta.
Theta Angles (deg) - Theta angle coordinates of custom antenna radiation pattern
$0: 180$ | real-valued 1-by- $Q$ row vector

Theta angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by$Q$ row vector. $Q$ must be greater than 2 . Angle units are in degrees. Theta angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Magnitude pattern (dB) - Magnitude of combined antenna radiation pattern zeros $(181,361)$ (default) | real-valued $Q$-by- $P$ matrix | real-valued $Q$-by- $P$-by- $L$ array

Magnitude of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector ( $\mathbf{H z}$ ).

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector (Hz) parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (Hz) parameter.


## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Phase pattern (deg) - Custom antenna radiation phase pattern zeros $(181,361)$ (default) | real-valued $Q$-by-P matrix | real-valued $Q$-by- $P$-by-L array

Phase of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector ( $\mathbf{H z}$ ).

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector (Hz) parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (


## Dependencies

To enable this parameter, set Element type to Custom Antenna.

MatchArrayNormal - Rotate antenna element to array normal
on (default) | off

Select this check box to rotate the antenna element pattern to align with the array normal. When not selected, the element pattern is not rotated.

When the antenna is used in an antenna array and the Input Pattern Coordinate System parameter is az-el, selecting this check box rotates the pattern so that the $x$-axis of the element coordinate system points along the array normal. Not selecting uses the element pattern without the rotation.

When the antenna is used in an antenna array and Input Pattern Coordinate System is set to phitheta, selecting this check box rotates the pattern so that the $z$-axis of the element coordinate system points along the array normal.

Use the parameter in conjunction with the Array normal parameter of the URA and UCA arrays.

## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Polar pattern frequencies (Hz) - Polar pattern microphone response frequencies
1e3 (default) | real scalar | real-valued 1-by-L row vector

Polar pattern microphone response frequencies, specified as a real scalar, or a real-valued, 1-by-L vector. The response frequencies lie within the frequency range specified by the Operating frequency vector $(\mathrm{Hz})$ vector.

## Dependencies

To enable this parameter, set Element type set to Custom Microphone.
Polar pattern angles (deg) - Polar pattern response angles
[-180:180] (default) | real-valued -by-P row vector

Specify the polar pattern response angles, as a 1-by- $P$ vector. The angles are measured from the central pickup axis of the microphone and must be between $-180^{\circ}$ and $180^{\circ}$, inclusive.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.
Polar pattern (dB) - Custom microphone polar response
zeros $(1,361)$ (default) | real-valued $L$-by-P matrix

Specify the magnitude of the custom microphone element polar patterns as an $L$-by- $P$ matrix. $L$ is the number of frequencies specified in Polar pattern frequencies $(\mathbf{H z}) . P$ is the number of angles specified in Polar pattern angles (deg). Each row of the matrix represents the magnitude of the polar pattern measured at the corresponding frequency specified in Polar pattern frequencies (Hz) and all angles specified in Polar pattern angles (deg). The pattern is measured in the azimuth plane. In the azimuth plane, the elevation angle is $0^{\circ}$ and the central pickup axis is $0^{\circ}$ degrees
azimuth and $0^{\circ}$ degrees elevation. The polar pattern is symmetric around the central axis. You can construct the microphone response pattern in 3-D space from the polar pattern.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.

## Array Parameters

Geometry - Array geometry
ULA (default) | URA | UCA | Conformal Array

Array geometry, specified as one of

- ULA - Uniform linear array
- URA - Uniform rectangular array
- UCA - Uniform circular array
- Conformal Array - arbitrary element positions

Number of elements - Number of array elements
2 for ULA arrays and 5 for UCA arrays (default) | integer greater than or equal to 2

The number of array elements for ULA or UCA arrays, specified as an integer greater than or equal to 2.

## Dependencies

To enable this parameter, set Geometry to ULA or UCA.
Element spacing (m) - Spacing between array elements

## 0.5 for ULA arrays and [0.5,0.5] for URA arrays (default) | positive scalar for ULA or URA arrays | 2-element vector of positive values for URA arrays

Spacing between adjacent array elements:

- ULA - specify the spacing between two adjacent elements in the array as a positive scalar.
- URA - specify the spacing as a positive scalar or a 1-by-2 vector of positive values. If Element spacing (m) is a scalar, the row and column spacings are equal. If Element spacing (m) is a vector, the vector has the form [SpacingBetweenArrayRows, SpacingBetweenArrayColumns].


## Dependencies

To enable this parameter, set Geometry to ULA or URA.
Array axis - Linear axis direction of ULA
y (default) $|x| z$

Linear axis direction of ULA, specified as $y, x$, or $z$. All ULA array elements are uniformly spaced along this axis in the local array coordinate system.

## Dependencies

- To enable this parameter, set Geometry to ULA.
- This parameter is also enabled when the block only supports ULA arrays.

Array size - Dimensions of URA array
[2,2] (default) | positive integer | 1-by-2 vector of positive integers

Dimensions of a URA array, specified as a positive integer or 1-by-2 vector of positive integers.

- If Array size is a 1 -by-2 vector, the vector has the form
[NumberOfArrayRows, NumberOfArrayColumns].
- If Array size is an integer, the array has the same number of elements in each row and column.

For a URA, array elements are indexed from top to bottom along the leftmost array column, and continued to the next columns from left to right. In this figure, the Array size value of [3,2] creates an array having three rows and two columns.

## Size and Element Indexing Order

for Uniform Rectangular Arrays
Example: Size $=[3,2]$


## Dependencies

To enable this parameter, set Geometry to URA.
Element lattice - Lattice of URA element positions
Rectangular (default) | Triangular

Lattice of URA element positions, specified as Rectangular or Triangular.

- Rectangular - Aligns all the elements in row and column directions.
- Triangular - Shifts the even-row elements of a rectangular lattice toward the positive row-axis direction. The displacement is one-half the element spacing along the row dimension.


## Dependencies

To enable this parameter, set Geometry to URA.
Array normal - Array normal direction
$x$ for URA arrays or $z$ for UCA arrays (default) | y

Array normal direction, specified as $x, y$, or $z$.
Elements of planar arrays lie in a plane orthogonal to the selected array normal direction. Element boresight directions point along the array normal direction.

| Array Normal Parameter Value | Element Positions and Boresight Directions |
| :--- | :--- |
| $x$ | Array elements lie in the $y z$-plane. All element <br> boresight vectors point along the $x$-axis. |
| $y$ | Array elements lie in the $z x$-plane. All element <br> boresight vectors point along the $y$-axis. |
| $z$ | Array elements lie in the $x y$-plane. All element <br> boresight vectors point along the $z$-axis. |

## Dependencies

To enable this parameter, set Geometry to URA or UCA.
Radius of UCA (m) - UCA array radius
0.5 (default) | positive scalar

Radius of UCA array, specified as a positive scalar.

## Dependencies

To enable this parameter, set Geometry to UCA.

```
Element positions (m) - Positions of conformal array elements
[0;0;0] (default)|3-by-Nmatrix of real values
```

Positions of the elements in a conformal array, specified as a 3-by- $N$ matrix of real values, where $N$ is the number of elements in the conformal array. Each column of this matrix represents the position [ $x ; y ; z$ ] of an array element in the array local coordinate system. The origin of the local coordinate system is $(0,0,0)$. Units are in meters.

## Dependencies

To enable this parameter set Geometry to Conformal Array.

## Data Types: double

Element normals (deg) - Direction of conformal array element normal vectors
[0;0]|2-by-1 column vector | 2 -by- $N$ matrix

Direction of element normal vectors in a conformal array, specified as a 2-by-1 column vector or a 2-by- $N$ matrix. $N$ indicates the number of elements in the array. If the parameter value is a matrix, each
column specifies the normal direction of the corresponding element in the form
[azimuth;elevation] with respect to the local coordinate system. The local coordinate system aligns the positive $x$-axis with the direction normal to the conformal array. If the parameter value is a 2-by- 1 column vector, the same pointing direction is used for all array elements.

You can use the Element positions (m) and Element normals (deg) parameters to represent any arrangement in which pairs of elements differ by certain transformations. The transformations can combine translation, azimuth rotation, and elevation rotation. However, you cannot use transformations that require rotation about the normal direction.

To enable this parameter, set Geometry to Conformal Array.
Data Types: double
Taper - Array element tapers
1 (default) | complex scalar | complex-valued row vector

Specify element tapering as a complex-valued scalar or a complex-valued 1-by- $N$ row vector. In this vector, $N$ represents the number of elements in the array.

Also known as element weights, tapers multiply the array element responses. Tapers modify both amplitude and phase of the response to reduce side lobes or steer the main response axis.

If Taper is a scalar, the same weight is applied to each element. If Taper is a vector, a weight from the vector is applied to the corresponding sensor element. The number of weights must match the number of elements of the array.
Data Types: double

## More About

## Generalized Sidelobe Cancellation

The generalized sidelobe canceller (GSC) is an efficient implementation of a linear constraint minimum variance (LCMV) beamformer. LCMV beamforming minimizes the output power of an array while preserving the power in one or more specified directions. This type of beamformer is called a constrained beamformer. You can compute exact weights for the constrained beamformer but the computation is costly when the number of elements is large. The computation requires the inversion of a large spatial covariance matrix. The GSC formulation converts the adaptive constrained optimization LCMV problem into an adaptive unconstrained problem, which simplifies the implementation.

In the GSC algorithm, incoming sensor data is split into two signal paths as shown in the block diagram. The upper path is a conventional beamformer. The lower path is an adaptive unconstrained beamformer whose purpose is to minimize the GSC output power. The GSC algorithm consists of these steps:

1 Presteer the element sensor data by time-shifting the incoming signals. Presteering time-aligns all sensor element signals. The time shifts depend on the arrival angle of the signal.
2 Pass the presteered signals through the upper path into a conventional beamformer with fixed weights, $\mathbf{w}_{\text {conv }}$.
3 Also pass the presteered signals through the lower path into the blocking matrix, B. The blocking matrix is orthogonal to the signal and removes the signal from the lower path.

4 Filter the lower path signals through a bank of FIR filters. The FilterLength property sets the length of the filters. The filter coefficients are the adaptive filter weights, $\mathbf{w}_{a d}$.
5 Compute the difference between the upper and lower signal paths. This difference is the beamformed GSC output.
6 Feed the beamformed output back into the filter. Adapt the filter weights using a least meansquare (LMS) algorithm. The adaptive LMS step size is the quantity set by the LMSStepSizeFactor property, divided by the total signal power.


## Version History

Introduced in R2016b

See Also<br>phased.GSCBeamformer

## LCMV Beamformer

Narrowband linear constraint minimum variance (LCMV) beamformer

## Libraries:

Phased Array System Toolbox / Beamforming

## Description

The LCMV Beamformer block performs narrowband linear-constraint minimum-variance (LCMV) beamforming. The number of constraints must be less than the number of elements or subarrays in the array.

## Ports

## Input

$\mathbf{X}$ - Input signal
$M$-by- $N$ complex-valued matrix
Input signals to beamformer, specified as an $M$-by- $N$ complex-valued matrix. $M$ is the number of signal samples. $N$ is the number of sensor array elements.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
Data Types: double
XT - Training signal
$P$-by- $N$ complex-valued matrix
Training input signal, specified as a $P$-by- $N$ complex-valued matrix. $P$ is the number of samples in the training input signal. $N$ is the number of elements of the sensor array. $P$ must be greater than $N$.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

## Dependencies

To enable this port, select the Enable training data input checkbox.
Data Types: double

## Output

$\mathbf{Y}$ - Beamformed output
$M$-by-1 complex-valued column vector

Beamformed output, specified as an $M$-by-1 complex-valued column vector. $M$ is the number of signal samples.

Data Types: double
W - Beamformer weights output
$N$-by-1 complex-valued column vector
Beamformer weights output, specified as an $N$-by- 1 complex-valued column vector. $N$ is the number of array elements.

## Dependencies

To enable this port, select the Enable weights output checkbox.
Data Types: double

## Parameters

Constraint matrix - LCMV beamformer constraint matrix complex ([1;1]) (default) | $N$-by-K complex-valued matrix

LCMV beamformer constraint matrix specified as an $N$-by- K complex-valued matrix. Each column of the matrix is a constraint. $N$ is the number of elements in the sensor array and $K$ is the number of constraints. $K$ must be less than or equal to the number of sensors, $N, K \leq N$

Desired response vector - Desired response for LCMV beamforming
1 (default) | real-valued $K$-by-1 column vector

Desired response of the LCMV beamformer, specified as a real-valued $K$-by- 1 column vector. $K$ is the number of constraints in the Constraint matrix. Each element in the vector defines the desired response of the constraint specified in the corresponding column of the Constraint matrix parameter.

Diagonal loading factor - Diagonal loading factor
positive scalar

Diagonal loading factor, specified as a positive scalar. Diagonal loading is a technique used to achieve robust beamforming performance, especially when the sample support is small.

Enable training data input - Enable training data input port
off (default) | on

Enable training data input port, specified as off or on. To enable the training data input port, XT, select this checkbox.

Enable weights output - Enable output of beamformer weights
off (default) | on

Enable beamforming weights output port, specified as off or on. To enable the beamforming weights output port, W , select this checkbox.

## Simulate using - Block simulation method <br> Interpreted Execution (default)|Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).
Programmatic Use
Block Parameter:SimulateUsing
Type:enum
Values:Interpreted Execution, Code Generation
Default:Interpreted Execution

## Version History

Introduced in R2014b

## See Also

phased.LCMVBeamformer

## Linear FM Waveform

Linear FM (LFM) pulse waveform

## Libraries:

Linear FM
Phased Array System Toolbox / Waveforms

## Description

The Linear FM Waveform block generates a linear FM pulse waveform with specified pulse width, pulse repetition frequency (PRF), and sweep bandwidth. The block outputs an integer number of pulses or samples.

## Ports

Input
PRFIdx - PRF Index
positive integer
Index to select the pulse repetition frequency (PRF), specified as a positive integer. The index selects the PRF from the predefined vector of values specified by the Pulse repetition frequency ( $\mathbf{H z}$ ) parameter.
Example: 4

## Dependencies

To enable this port, select Enable PRF selection input.
Data Types: double
FreqOffset - Frequency offset
scalar
Frequency offset in Hz , specified as a scalar.
Example: 2e3

## Dependencies

To enable this port, set Source of Frequency Offset to Input port.
Data Types: double

## Output

Y - Pulse waveform
complex-valued vector
Pulse waveform samples, returned as a complex-valued vector.
Data Types: double

PRF - Pulse repetition frequency
positive scalar
Pulse repetition frequency of current pulse, returned as a positive scalar.

## Dependencies

To enable this port, set the Output signal format parameter to Pulses and then select the Enable PRF output parameter.
Data Types: double
Coeff - Matched filter coefficients
vector | matrix
Matched filter coefficients, returned as a vector or matrix.

## Dependencies

To enable this port, select Enable Matched Filter Coefficients Output.

## Data Types: double

## Parameters

Sample rate (Hz) - Sample rate of the output waveform
le6 (default) | positive scalar

Sample rate of the output waveform, specified as a positive scalar. The ratio of Sample rate (Hz) to each element in the Pulse repetition frequency (Hz) vector must be an integer. This restriction is equivalent to requiring that the pulse repetition interval is an integral multiple of the sample interval.

Programmatic Use<br>Block Parameter:SampleRate<br>Type:double<br>Values:positive scalar<br>Default:1e6

Method to specify pulse duration - Pulse duration as time or duty cycle
Pulse width (default)|Duty cycle

Method to set the pulse duration, specified as Pulse width or Duty cycle. When you set this parameter to Pulse width, the pulse duration is set using the Pulse width (s) parameter. When you set this parameter to Duty cycle, the pulse duration is computed from the values of the Pulse repetition frequency ( Hz ) and Duty Cycle parameters.

```
Programmatic Use
Block Parameter:DurationSpecification
Type:string
Values:string
Default:'Pulse width'
Pulse width (s) - Time duration of pulse
50e-6 (default) | positive scalar
```

The duration of each pulse, specified as a positive scalar. Set the product of Pulse width (s) and Pulse repetition frequency to be less than or equal to one. This restriction ensures that the pulse width is smaller than the pulse repetition interval. Units are in seconds.

Example: 300e-6

## Dependencies

To enable this parameter, set the Method to specify pulse duration parameter to Pulse width.

## Programmatic Use

Block Parameter:PulseWidth
Type:double
Values:string
Default:50e-6
Duty cycle - Waveform duty cycle
0.5 (default) | scalar in the range [0,1]

Waveform duty cycle, specified as a scalar in the range [0,1].
Example: 0.7

## Dependencies

To enable this parameter, set the Method to specify pulse duration parameter to Duty cycle.
Programmatic Use
Block Parameter:DutyCycle
Type:double
Values:positive scalar
Default:1e6
Pulse repetition frequency (Hz) - Pulse repetition frequency
le4 (default) | positive scalar

Pulse repetition frequency, $P R F$, specified as a scalar or a row vector. Units are in Hz . The pulse repetition interval, $P R I$, is the inverse of the pulse repetition frequency, $P R F$. The value of Pulse repetition frequency ( Hz ) must satisfy these constraints:

- The product of Pulse width and Pulse repetition frequency $\mathbf{( H z )}$ must be less than or equal to one. This condition expresses the requirement that the pulse width is less than one pulse repetition interval. For the phase-coded waveform, the pulse width is the product of the chip width and number of chips.
- The ratio of sample rate to any element of Pulse repetition frequency must be an integer. This condition expresses the requirement that the number of samples in one pulse repetition interval is an integer.

You can select the value of $P R F$ by using block parameter settings alone or in conjunction with the input port, PRFIdx.

- When the Enable PRF selection input parameter is not selected, set the PRF using block parameters.
- To implement a constant $P R F$, specify Pulse repetition frequency ( $\mathbf{H z}$ ) as a positive scalar.
- To implement a staggered $P R F$, specify Pulse repetition frequency $(\mathbf{H z})$ as a row vector with positive values. After the waveform reaches the last element of the vector, the process continues cyclically with the first element of the vector. When PRF is staggered, the time between successive output pulses cycles through the successive values of the $P R F$ vector.
- When the Enable PRF selection input parameter is selected, you can implement a selectable $P R F$ by specifying Pulse repetition frequency $(\mathbf{H z})$ as a row vector with positive real-valued entries. But this time, when you execute the block, select a PRF by passing an index into the PRF vector into the PRFIdx port.

In all cases, the number of output samples is fixed when you set the Output signal format to Samples. When you use a varying PRF and set Output signal format to Pulses, the number of output samples can vary.

Programmatic Use<br>Block Parameter:PRF<br>Type:double<br>Values:positive scalar<br>Default:1e6

Enable PRF selection input - Select predefined PRF
off (default) | on

Select this parameter to enable the PRFIdx port.

- When enabled, pass in an index into a vector of predefined PRFs. Set predefined PRFs using the Pulse repetition frequency $(\mathbf{H z})$ parameter.
- When not enabled, the block cycles through the vector of PRFs specified by the Pulse repetition frequency ( Hz ) parameter. If Pulse repetition frequency $(\mathbf{H z})$ is a scalar, the PRF is constant.

Programmatic Use
Block Parameter:PRFSelectionInputPort
Type:logical
Values:positive scalar
Default:off
Sweep bandwidth (Hz) - Bandwidth of FM sweep
1e5 (default) | positive scalar

Bandwidth of the linear FM sweep in Hz , specified as a positive scalar.
Example: 1e3
Sweep direction - Direction of FM sweep
Up (default) | Down

Specify the direction of the linear FM sweep as Up (increasing frequency) or Down (decreasing frequency).

Sweep interval - FM frequency sweep interval
Positive (default)| Symmetric

FM frequency sweep interval, specified as Positive or Symmetric. If you set this parameter to Positive, the waveform sweeps the frequency interval between 0 and $B$, where $B$ is the value of the Sweep bandwidth parameter. If you set this parameter value to Symmetric, the waveform sweeps the interval between $-B / 2$ and $B / 2$.

Envelope function - FM signal amplitude envelope
Rectangular (default)| Gaussian

FM signal amplitude envelope, specified as Rectangular or Gaussian.
Source of Frequency Offset - Source of frequency offset
Property (default)| Input port

Source of frequency offset, specified as Property or Input port.

- When set to Property, the offset is determined by the value of the Frequency Offset parameter.
- When set to Input port, the offset is determined by the value of the FreqOffset port.

Programmatic Use
Block Parameter:FrequencyOffsetSource
Type:enum
Values: Property, Input Port
Default:Property
Frequency Offset (Hz) - Frequency offset
0 (default) | scalar

Frequency offset, specified as a scalar. Units are in Hz.
Example: 2e3

## Dependencies

To enable this parameter set the Source of Frequency Offset parameter to Input port.

## Programmatic Use

Block Parameter:FrequencyOffset
Type:double
Values:scalar
Default:0
Source of simulation sample time - Source of simulation sample time
Derive from waveform parameters (default)|Inherit from Simulink engine

Source of simulation sample time, specified as Derive from waveform parameters or Inherit from Simulink engine. When set to Derive from waveform parameters, the block runs at a variable rate determined by the PRF of the selected waveform. The elapsed time is variable. When set to Inherit from Simulink engine, the block runs at a fixed rate so the elapsed time is a constant.

## Dependencies

To enable this parameter, select the Enable PRF selection input parameter.

## Programmatic Use

Block Parameter:SimulationTimeSource
Type:enum
Values:Derive from waveform parameters, Inherit from Simulink engine
Default:Derive from waveform parameters
Output signal format - Format of the output signal
Pulses (default)| Samples

The format of the output signal, specified as Pulses or Samples.
If you set this parameter to Samples, the output of the block consists of multiple samples. The number of samples is the value of the Number of samples in output parameter.

If you set this parameter to Pulses, the output of the block consists of multiple pulses. The number of pulses is the value of the Number of pulses in output parameter.
Programmatic Use
Block Parameter:OutputFormat
Type:enum
Values:Pulses Samples
Default:Pulses
Number of samples in output - Number of samples in output
100 (default) | positive integer

Number of samples in the block output, specified as a positive integer.
Example: 1000

## Dependencies

To enable this parameter, set the Output signal format parameter to Samples.
Programmatic Use
Block Parameter:NumSamples
Type:double
Values:positive scalar
Default:100
Data Types: double
Number of pulses in output - Number of pulses in output
1 (default) | positive integer

Number of pulses in the block output, specified as a positive integer.
Example: 2

## Dependencies

To enable this parameter, set the Output signal format parameter to Pulses.

Programmatic Use<br>Block Parameter:NumPulses<br>Type:double<br>Values:positive scalar<br>Default:1<br>Data Types: double

Enable PRF Output - Enable output of PRF
off (default) |on

Select this parameter to enable the PRF output port.

## Dependencies

To enable this parameter, set Output signal format to Pulses.

```
Programmatic Use
Block Parameter:PRF0utputPort
Type:enum
Values:off on
Default:off
Enable Matched Filter Coeficients Output - Enable output of matched filter coefficients off (default) | on
```

Select this parameter to enable the Coeff output port.

```
Programmatic Use
Block Parameter:Coefficient0utputPort
Type:enum
Values:off on
Default:off
Simulate using - Block simulation method
Interpreted Execution (default)|Code Generation
```

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).
Programmatic Use
Block Parameter:SimulateUsing
Type:enum
Values:Interpreted Execution, Code Generation
Default:Interpreted Execution

## Version History

Introduced in R2014b

## See Also

phased. LinearFMWaveform

## LOS Channel

Narrowband line-of-sight propagation channel

## Libraries:

Phased Array System Toolbox / Environment and Target

## Description

The LOS Channel block propagates signals from a point in space to another point in space by line-ofsight (LOS) channels. The block can also propagate signals from one point to multiple points or from multiple points back to one point. The block models propagation time, free-space propagation loss, Doppler shift, and atmospheric as well as weather loss. The block assumes that the propagation speed is much greater than the object speed in which case the stop-and-hop model is valid.

When propagating a signal in an LOS channel to an object and back, you can use a single block to compute two-way LOS channel propagation delays or two blocks to perform two one-way propagation delays in each direction. Because the LOS channel propagation delay is not necessarily an integer multiple of the sampling interval, it can turn out that the total round trip delay in samples when you use a two-way propagation block differs from the delay in samples when you use two one-way propagation blocks. For this reason, it is recommended that, when possible, you use a single two-way propagation block.

## Ports

## Input

## $\mathbf{X}$ - Narrowband signal

$M$-element complex-valued column vector, $M$-by- $N$ complex-valued matrix.
Narrowband signal, specified as an $M$-element complex-valued column vector or $M$-by- $N$ complexvalued matrix. The quantity $M$ is the number of sample values of the signal and $N$ is the number of signals to propagate. When you specify $N$ signals, you need to specify $N$ signal origins or $N$ signal destinations.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

Pos1 - Signal origin
3-by-1 real-valued column vector | 3 -by- N real-valued matrix
Signal origin, specified as a 3-by-1 real-valued column vector or 3-by-N real-valued matrix. The quantity $N$ is the number of propagated signals and equals the dimension specified in the signal input port X. If Pos1 is a column vector, it takes the form [x; y; z]. If Pos 1 is a matrix, each column specifies a different signal origin and has the form [x; y; z]. Pos1 and Pos2 cannot both be specified as matrices - at least one must be a 3-by-1 column vector. Position units are meters.
Data Types: double

## Pos2 - Signal destination

3-by-1 real-valued column vector | 3-by-N real-valued matrix
Signal destination, specified as a 3-by-1 real-valued column vector or 3-by-N real-valued matrix. The quantity $N$ is the number of propagated signals and equals the dimension specified in the signal in the input port X. If Pos2 is a column vector, it takes the form [x; y; z]. If Pos2 is a matrix, each column specifies a different signal origin and has the form [x; y; z]. Pos2 and Pos1 cannot both be specified as matrices - at least one must be a 3-by-1 column vector. Position units are meters.
Data Types: double
Vel1 - Signal origin velocity
3-by-1 real-valued column vector | 3-by-N real-valued matrix
Signal origin velocity, specified as a 3-by-1 real-valued column vector or 3-by- $N$ real-valued matrix. The quantity $N$ is the number of propagated signals and equals the dimension specified in the signal into the port X . If Vell is a column vector, it takes the form [ $\mathrm{Vx} ; \mathrm{Vy} ; \mathrm{zV}$ ]. If Vel1 is a matrix, each column specifies a different signal origin and has the form [ $\mathrm{Vx} ; \mathrm{Vy}$; Vz ]. The dimensions of Vell must agree with the dimensions of Pos1. Vel1 and Vel2 cannot both be specified as matrices - at least one must be a 3 -by- 1 column vector. Position units are meters.
Data Types: double
Vel2 - Signal destination velocity
3-by-1 real-valued column vector | 3-by-N real-valued matrix
Signal destination velocity, specified as a 3-by-1 real-valued column vector or 3-by- N real-valued matrix. The quantity $N$ is the number of propagated signals and equals the dimension specified in the signal into the port X . If $\mathrm{Vel2}$ is a column vector, it takes the form [ $\mathrm{Vx} ; \mathrm{Vy} ; \mathrm{zV}$ ]. If $\mathrm{Vel2}$ is a matrix, each column specifies a different signal origin and has the form [ $\mathrm{Vx} ; \mathrm{Vy}$; Vz ]. The dimensions of Vel2 must agree with the dimensions of Pos2. Vel2 and Vel1 cannot both be specified as matrices - at least one must be a 3-by-1 column vector. Position units are meters.
Data Types: double

## Output

Port_1 - Propagated narrowband signal
$M$-element complex-valued column vector, $M$-by- $N$ complex-valued matrix.
Propagated signal, returned as a $M$-element complex-valued column vector, $M$-by- $N$ complex-valued matrix. Y will have the same dimensions as X .

The output $Y$ contains signal samples arriving at the signal destination within the current time frame. The current time frame is defined as the time spanned by the current input. Whenever it takes longer than the current time frame for the signal to propagate from the origin to the destination, the output contains no contribution from the input of the current time frame.

## Parameters

Propagation speed (m/s) - Signal propagation speed physconst('LightSpeed') (default)| positive scalar

Signal propagation speed, specified as a real-valued positive scalar. The default value of the speed of light is the value returned by physconst ('LightSpeed').

## Data Types: double

Signal carrier frequency (Hz) - Signal carrier frequency
$3 e 8$ (default) | positive real-valued scalar

Signal carrier frequency, specified as a positive real-valued scalar. Units are in hertz.
Data Types: double
Specify atmospheric parameters - Enable atmospheric attenuation model
off (default) | on

Select this parameter to enable to add signal attenuation caused by atmospheric gases, rain, fog, or clouds. When you select this parameter, the Temperature (degrees Celsius), Dry air pressure ( Pa ), Water vapour density ( $\mathrm{g} / \mathrm{m}^{\wedge} 3$ ), Liquid water density ( $\mathrm{g} / \mathrm{m}^{\wedge} 3$ ), and Rain rate ( $\mathrm{mm} / \mathrm{hr}$ ) parameters appear in the dialog box.
Data Types: Boolean
Temperature (degrees Celsius) - Ambient temperature
15 (default) | real-valued scalar

Ambient temperature, specified as a real-valued scalar. Units are in degrees Celsius.

## Dependencies

To enable this parameter, select the Specify atmospheric parameters checkbox.
Data Types: double
Dry air pressure (Pa) - Atmospheric dry air pressure
101.325e3 (default) | positive real-valued scalar

Atmospheric dry air pressure, specified as a positive real-valued scalar. Units are in pascals (Pa). The default value of this parameter corresponds to one standard atmosphere.

## Dependencies

To enable this parameter, select the Specify atmospheric parameters checkbox.

## Data Types: double

Water vapour density (g/m^3) - Atmospheric water vapor density
7.5 (default) | positive real-valued scalar

Atmospheric water vapor density, specified as a positive real-valued scalar. Units are in $\mathrm{g} / \mathrm{m}^{3}$.
Dependencies
To enable this parameter, select the Specify atmospheric parameters checkbox.

## Data Types: datetime

Liquid water density ( $\mathbf{g} / \mathbf{m}^{\wedge} \mathbf{3}$ ) — Liquid water density
0.0 (default) | nonnegative real-valued scalar

Liquid water density of fog or clouds, specified as a nonnegative real-valued scalar. Units are in $\mathrm{g} / \mathrm{m}^{3}$. Typical values for liquid water density are 0.05 for medium fog and 0.5 for thick fog.

## Dependencies

To enable this parameter, select the Specify atmospheric parameters checkbox.

## Data Types: double

Rain rate ( $\mathrm{mm} / \mathrm{hr}$ ) - Rainfall rate
0.0 (default) | non-negative real-valued scalar

Rainfall rate, specified as a nonnegative real-valued scalar. Units are in $\mathrm{mm} / \mathrm{hr}$.

## Dependencies

To enable this parameter, select the Specify atmospheric parameters checkbox.

## Data Types: double

Perform two-way propagation - Enable two-way propagation
off (default) | on
Select this check box to perform round-trip propagation between the origin and destination. Otherwise the block performs one-way propagation from the origin to the destination.

Inherit sample rate - Inherit sample rate from upstream blocks
on (default) | off

Select this parameter to inherit the sample rate from upstream blocks. Otherwise, specify the sample rate using the Sample rate (Hz) parameter.
Data Types: Boolean
Sample rate (Hz) - Sampling rate of signal
1e6 (default) | positive real-valued scalar

Specify the signal sampling rate as a positive scalar. Units are in Hz .

## Dependencies

To enable this parameter, clear the Inherit sample rate check box.

## Data Types: double

Maximum one-way propagation distance (m) - Maximum one-way propagation distance
10e3 (default) | positive real-valued scalar

Specify the maximum distance between the signal origin and the destination as a positive scalar. Units are in meters. Amplitudes of any signals that propagate beyond this distance will be set to zero.

Simulate using - Block simulation method
Interpreted Execution (default) |Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).

```
Programmatic Use
Block Parameter:SimulateUsing
Type:enum
Values:Interpreted Execution, Code Generation
Default:Interpreted Execution
```


## More About

## Attenuation and Loss Factors

Attenuation or path loss in the Wideband LOS channel consists of four components. $L=L_{f s p} L_{g} L_{c} L_{r}$, where

- $L_{f s p}$ is the free-space path attenuation
- $L_{g}$ is the atmospheric path attenuation
- $L_{c}$ is the fog and cloud path attenuation
- $L_{r}$ is the rain path attenuation

Each component is in magnitude units, not in dB.

## Propagation Delay, Doppler, and Free-Space Path Loss

When the origin and destination are stationary relative to each other, you can write the output signal of a free-space channel as $Y(t)=\chi(t-\tau) / L_{f s p}$. The quantity $\tau$ is the signal delay and $L_{f s p}$ is the free-space path loss. The delay $\tau$ is given by $R / c$, where $R$ is the propagation distance and $c$ is the propagation speed. The free-space path loss is given by

$$
L_{f s p}=\frac{(4 \Pi R)^{2}}{\lambda^{2}}
$$

where $\lambda$ is the signal wavelength.
This formula assumes that the target is in the far field of the transmitting element or array. In the near field, the free-space path loss formula is not valid and can result in a loss smaller than one, equivalent to a signal gain. Therefore, the loss is set to unity for range values, $R \leq \lambda / 4 \Pi$.

When the origin and destination have relative motion, the processing also introduces a Doppler frequency shift. The frequency shift is $v / \lambda$ for one-way propagation and $2 v / \lambda$ for two-way propagation. The quantity $v$ is the relative speed of the destination with respect to the origin.

## Atmospheric Gas Attenuation Model

This model calculates the attenuation of signals that propagate through atmospheric gases.
Electromagnetic signals attenuate when they propagate through the atmosphere. This effect is due primarily to the absorption resonance lines of oxygen and water vapor, with smaller contributions coming from nitrogen gas. The model also includes a continuous absorption spectrum below 10 GHz . The ITU model Recommendation ITU-R P.676-10: Attenuation by atmospheric gases is used. The model computes the specific attenuation (attenuation per kilometer) as a function of temperature, pressure, water vapor density, and signal frequency. The atmospheric gas model is valid for frequencies from 1-1000 GHz and applies to polarized and nonpolarized fields.

The formula for specific attenuation at each frequency is

$$
\gamma=\gamma_{o}(f)+\gamma_{w}(f)=0.1820 f N^{\prime \prime}(f)
$$

The quantity $N^{\prime \prime}()$ is the imaginary part of the complex atmospheric refractivity and consists of a spectral line component and a continuous component:

$$
N^{\prime \prime}(f)=\sum_{i} S_{i} F_{i}+N^{\prime \prime}{ }_{D}(f)
$$

The spectral component consists of a sum of discrete spectrum terms composed of a localized frequency bandwidth function, $F(f)_{\mathrm{i}}$, multiplied by a spectral line strength, $S_{\mathrm{i}}$. For atmospheric oxygen, each spectral line strength is

$$
S_{i}=a_{1} \times 10^{-7}\left(\frac{300}{T}\right)^{3} \exp \left[a_{2}\left(1-\left(\frac{300}{T}\right)\right] P .\right.
$$

For atmospheric water vapor, each spectral line strength is

$$
S_{i}=b_{1} \times 10^{-1}\left(\frac{300}{T}\right)^{3.5} \exp \left[b_{2}\left(1-\left(\frac{300}{T}\right)\right] W .\right.
$$

$P$ is the dry air pressure, $W$ is the water vapor partial pressure, and $T$ is the ambient temperature. Pressure units are in hectoPascals ( hPa ) and temperature is in degrees Kelvin. The water vapor partial pressure, $W$, is related to the water vapor density, $\rho$, by

$$
W=\frac{\rho T}{216.7} .
$$

The total atmospheric pressure is $P+W$.
For each oxygen line, $S_{i}$ depends on two parameters, $a_{1}$ and $a_{2}$. Similarly, each water vapor line depends on two parameters, $b_{1}$ and $b_{2}$. The ITU documentation cited at the end of this section contains tabulations of these parameters as functions of frequency.

The localized frequency bandwidth functions $F_{i}(f)$ are complicated functions of frequency described in the ITU references cited below. The functions depend on empirical model parameters that are also tabulated in the reference.

To compute the total attenuation for narrowband signals along a path, the function multiplies the specific attenuation by the path length, $R$. Then, the total attenuation is $L_{g}=R\left(\gamma_{o}+\gamma_{w}\right)$.

You can apply the attenuation model to wideband signals. First, divide the wideband signal into frequency subbands, and apply attenuation to each subband. Then, sum all attenuated subband signals into the total attenuated signal.

## Fog and Cloud Attenuation Model

This model calculates the attenuation of signals that propagate through fog or clouds.
Fog and cloud attenuation are the same atmospheric phenomenon. The ITU model, Recommendation ITU-R P.840-6: Attenuation due to clouds and fog is used. The model computes the specific attenuation (attenuation per kilometer), of a signal as a function of liquid water density, signal frequency, and temperature. The model applies to polarized and nonpolarized fields. The formula for specific attenuation at each frequency is

$$
\gamma_{C}=K_{l}(f) M,
$$

where $M$ is the liquid water density in $\mathrm{gm} / \mathrm{m}^{3}$. The quantity $K_{l}(f)$ is the specific attenuation coefficient and depends on frequency. The cloud and fog attenuation model is valid for frequencies $10-1000 \mathrm{GHz}$. Units for the specific attenuation coefficient are $(\mathrm{dB} / \mathrm{km}) /\left(\mathrm{g} / \mathrm{m}^{3}\right)$.

To compute the total attenuation for narrowband signals along a path, the function multiplies the specific attenuation by the path length $R$. Total attenuation is $L_{c}=R \gamma_{c}$.

You can apply the attenuation model to wideband signals. First, divide the wideband signal into frequency subbands, and apply narrowband attenuation to each subband. Then, sum all attenuated subband signals into the total attenuated signal.

## Rainfall Attenuation Model

This model calculates the attenuation of signals that propagate through regions of rainfall. Rain attenuation is a dominant fading mechanism and can vary from location-to-location and from year-toyear.

Electromagnetic signals are attenuated when propagating through a region of rainfall. Rainfall attenuation is computed according to the ITU rainfall model Recommendation ITU-R P.838-3: Specific attenuation model for rain for use in prediction methods. The model computes the specific attenuation (attenuation per kilometer) of a signal as a function of rainfall rate, signal frequency, polarization, and path elevation angle. The specific attenuation, $\gamma_{R}$, is modeled as a power law with respect to rain rate

$$
\gamma_{R}=k R^{\alpha}
$$

where $R$ is rain rate. Units are in $\mathrm{mm} / \mathrm{hr}$. The parameter $k$ and exponent $\alpha$ depend on the frequency, the polarization state, and the elevation angle of the signal path. The specific attenuation model is valid for frequencies from 1-1000 GHz.

To compute the total attenuation for narrowband signals along a path, the function multiplies the specific attenuation by the an effective propagation distance, $d_{\text {eff }}$. Then, the total attenuation is $L=$ $d_{\text {eff }} \gamma_{R}$.

The effective distance is the geometric distance, $d$, multiplied by a scale factor

$$
r=\frac{1}{0.477 d^{0.633} R_{0.01}^{0.073 \alpha} f^{0.123}-10.579(1-\exp (-0.024 d))}
$$

where $f$ is the frequency. The article Recommendation ITU-R P.530-17 (12/2017): Propagation data and prediction methods required for the design of terrestrial line-of-sight systems presents a complete discussion for computing attenuation.

The rain rate, $R$, used in these computations is the long-term statistical rain rate, $R_{0.01}$. This is the rain rate that is exceeded $0.01 \%$ of the time. The calculation of the statistical rain rate is discussed in Recommendation ITU-R P.837-7 (06/2017): Characteristics of precipitation for propagation modelling. This article also explains how to compute the attenuation for other percentages from the $0.01 \%$ value.

You can apply the attenuation model to wideband signals. First, divide the wideband signal into frequency subbands and apply attenuation to each subband. Then, sum all attenuated subband signals into the total attenuated signal.

## Version History

## Introduced in R2016a

## See Also

phased. LOSChannel

## Matched Filter

Matched filter


## Libraries:

Phased Array System Toolbox / Detection

## Description

The Matched Filter block implements matched filtering of an input signal. Matched filtering is an FIR filtering operation with the coefficients equal to the time reversed samples of the transmitted signal. The filter can improve SNR before detection.

## Ports

Input
$\mathbf{X}$ - Input signal
$M$-by- $N$ complex valued matrix
Input signal, specified as an $M$-by- $N$ complex valued matrix. Matched filtering is applied along the first dimension. The input $X$ and the output $Y$ have the same dimensions. The initial transient is removed from the filtered result.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
Data Types: double
Coeff - Matched filter coefficients
$M$-length complex column vector
Matched filter coefficients, specified as an $M$-length complex column vector.

## Dependencies

To enable this port, set the Source of coefficients pull-down menu Input port.
Data Types: double

## Output

$\mathbf{Y}$ - Matched filter output
$M$-by- $N$ complex valued matrix
Matched filter output, returned as an $M$-by- $N$ complex valued matrix. The dimensions of $Y$ are the same as the dimensions of $X$.

Data Types: double

G - Matched-filter gain
$N$-length real-valued
Matched-filter gain, returned as an $N$ real-valued matrix. Gain is computed for each column of X . Units are in dB.

Dependencies
To enable this port, select the Enable SNR gain output check box.
Data Types: double

## Parameters

Source of coefficients - Source of matched filter coefficients
Property (default)|Input port
Specify whether the matched filter coefficients come from Coefficients or from an input port.

| Property | Matched filter coefficients are specified by Coefficients . |
| :--- | :--- |
| Input port | Matched filter coefficients are specified via the input port <br> Coeff. |

Coefficients - Matched filter coefficients
[1;1] (default)
Specify the matched filter coefficients as a column vector. This parameter appears when you set
Source of coefficients to Property.
Spectrum window - Window for spectrum weighting

```
None (default) | Hamming | Chebyshev | Hann | Kaiser | Taylor
```

Specify the window used for spectrum weighting using one of

## None

## Hamming

Chebyshev
Hann
Kaiser
Taylor
Spectrum weighting is often used with linear FM waveforms to reduce sidelobe levels in the time domain. The block computes the window length internally to match the FFT length.

## Spectrum window range (Hz) - Spectrum window coverage region

```
[0, le5] (default)
```

Specify the spectrum region, in hertz, on which the spectrum window is applied as a 1-by-2 vector in the form of [StartFrequency, EndFrequency].

Note that both StartFrequency and EndFrequency are measured in baseband. That is, they are within [-Fs/2, Fs/2], where Fs is the sample rate specified in any of the waveform library blocks. The parameter StartFrequency must be less than EndFrequency.

## Dependencies

This parameter appears when you set the Spectrum window parameter to any value other than None.

Inherit sample rate - Inherit sample rate from upstream blocks
on (default) | off

Select this parameter to inherit the sample rate from upstream blocks. Otherwise, specify the sample rate using the Sample rate (Hz) parameter.

Data Types: Boolean
Sample rate (Hz) - Sample rate of the output waveform
le6 (default) | positive scalar

Sample rate of the output waveform, specified as a positive scalar. The ratio of Sample rate (Hz) to each element in the Pulse repetition frequency (Hz) vector must be an integer. This restriction is equivalent to requiring that the pulse repetition interval is an integral multiple of the sample interval.

```
Programmatic Use
Block Parameter:SampleRate
Type:double
Values:positive scalar
Default:1e6
```

Sidelobe attenuation level - Window sidelobe attenuation level

## 30 (default)

Specify the sidelobe attenuation level, in dB, of a Chebyshev or Taylor window as a positive scalar.

## Dependencies

This parameter appears when you set Spectrum window to Chebyshev or Taylor.
Kaiser shape parameter - Kaiser shape parameter

## 0.5 (default)

Specify the parameter that affects the Kaiser window sidelobe attenuation as a nonnegative scalar. Please refer to the function kaiser for more details.

## Dependencies

This parameter appears when you set the Spectrum window parameter to Kaiser.
Number of constant level sidelobes - Number of nearly constant sidelobes in Taylor window
4 (default)

Specify the number of nearly-constant-level sidelobes adjacent to the mainlobe in a Taylor window as a positive integer.

## Dependencies

This parameter appears when you set the Spectrum window parameter to Taylor.
Enable SNR gain output - Enable SNR gain output
off (default) | on
Select this check this box to obtain the matched filter SNR gain via the output port G. The output port appears only when this box is selected.

Simulate using - Block simulation method
Interpreted Execution (default)|Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).

Programmatic Use<br>Block Parameter:SimulateUsing<br>Type:enum<br>Values:Interpreted Execution, Code Generation<br>Default:Interpreted Execution

# Version History 

Introduced in R2014b

## See Also

phased.MatchedFilter

## MFSK Waveform

Multiple frequency shift keying (MFSK) continuous waveform


## Libraries:

Phased Array System Toolbox / Waveforms

## Description

The MFSK Waveform block generates a multiple frequency-shift keying (MFSK) continuous waveform with a specified step time, sweep bandwidth, frequency offset, and number of steps. The block outputs an integer number of samples, steps, or sweeps. For details on the structure of an MFSK waveform, see phased.MFSKWaveform.

## Ports

## Output

Port_1 - MFSK Waveform
complex-valued column vector
MFSK waveform, returned as a complex-valued column vector containing the waveform samples.

- If the Output signal format parameter is set to Steps, the output of the port consists of the number of steps set by the Number of frequency steps in output parameter.
- If the Output signal format parameter is set to Samples, the output of the port consists of the number of samples set by the Number of samples in output parameter.
- If the Output signal format parameter is set to Sweeps, the output of the port consists of the number of sweeps set by the Number of sweeps in output parameter.


## Parameters

Sample rate (Hz) - Sample rate
151e6 (default) | positive scalar
Sample rate of the signal, specified as a positive scalar. Units are in hertz.
Sweep bandwidth (Hz) - MFSK sweep bandwidth

## 150e6 (default) | positive scalar

Bandwidth of the MFSK sweep, specified as a positive scalar. Units are in hertz.
Frequency step burst time (s) - Frequency step burst time

## 5e-6 (default) | positive scalar

Time duration of each frequency step, specified as a positive scalar. Units are in seconds.

Number of steps per sweep - Total number of frequency steps

## 512 (default) | even positive scalar

Total number of steps in each sweep, specified as an even positive integer.
Chirp offset frequency (Hz) - Chirp offset frequency

- 294e3 (default) | real scalar

Chirp offset frequency, specified as a real scalar. Units are in hertz. The offset determines the frequency translation between the two sequences.

Output signal format - Output signal format

## Steps (default) | Samples | Sweeps

Format of the output signal, specified as one of the following:

- Steps - The block outputs the number of samples contained in an integer number of frequency steps specified by the Number of frequency steps in output parameter.
- Samples - The block outputs the number of samples specified in the Number of samples in output parameter.
- Sweeps - The block outputs the number of samples contained in an integer number of sweeps specified by the Number of sweeps in output parameter.

Number of sweeps in output - Number of sweeps in output

## 1 (default) | positive integer

Number of sweeps in the block output, specified as a positive integer.

## Dependencies

This parameter appears only when you set Output signal format to Sweeps.
Number of frequency steps in output - Number of frequency steps in output

## 1 (default) | positive integer

Number of steps in the block output, specified as a positive integer.

## Dependencies

This parameter appears only when you set Output signal format to Steps.
Number of samples in output - Number of samples in output
100 (default) | positive integer

Number of samples in the block output, specified as a positive integer.

## Example: 1000

## Dependencies

To enable this parameter, set the Output signal format parameter to Samples.

```
Programmatic Use
Block Parameter:NumSamples
Type:double
Values:positive scalar
Default:100
Data Types: double
Simulate using - Block simulation method
Interpreted Execution (default)|Code Generation
```

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).

## Programmatic Use

Block Parameter:SimulateUsing
Type:enum
Values:Interpreted Execution, Code Generation
Default:Interpreted Execution

## Version History

## Introduced in R2015a

## See Also

phased.MFSKWaveform

## Monopulse Feed

Create monopulse sum and difference channels


## Libraries:

Phased Array System Toolbox / Direction of Arrival

## Description

The Monopulse Feed block forms the sum and difference channels used for amplitude monopulse directing finding. Sum and difference channels are derived from signals received by an array. You can feed these channels into the Monopulse Estimator block.

## Ports

Input
$\mathbf{X}$ - Input signal
complex-valued $M$-by- $N$ matrix
Input signal, specified as a complex-valued $M$-by- $N$ matrix, where $M$ is the number of samples or snapshots of data, and $N$ is the number of array elements. If the array contains subarrays, then $N$ is the number of subarrays.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
Data Types: double
STEER - Array steering direction
scalar | real-valued 2-by-1 column vector
Array steering direction, specified as a scalar or real-valued 2-by-1 column vector.

- When you set the Monopulse coverage parameter to Azimuth, the steering direction is a scalar and represents the azimuth steering angle.
- When you set the Monopulse coverage parameter to 3D, the steering direction vector has the form [azimuthAngle; elevationAngle], where azimuthAngle is the azimuth steering angle, and elevationAngle is the elevation steering angle.

Units are in degrees. Azimuth angles lie between $-180^{\circ}$ and $180^{\circ}$, inclusive, and elevation angles lie between $-90^{\circ}$ and $90^{\circ}$, inclusive.
Example: [40;10]
Data Types: double

## Output

SIGMA - Sum-channel signal
complex-valued $M$-by-1 column vector
Sum-channel signal, returned as a complex-valued $M$-by- 1 column vector, where $M$ is the number of rows of $X$.

Data Types: double
Complex Number Support: Yes
DeltaAz - Azimuth-difference channel signal
complex-valued $M$-by- 1 column vector
Azimuth-difference channel signal, returned as a complex-valued $M$-by- 1 column vector, where $M$ is the number of rows of $X$.
Data Types: double
Complex Number Support: Yes
DeltaEI - Elevation-difference channel signal
complex-valued $M$-by-1 vector
Elevation difference-channel signal, returned as a complex-valued $M$-by- 1 column vector, where $M$ is the number of rows of $X$.

## Dependencies

To enable this output port, set the Monopulse coverage parameter to 3D.

```
Data Types: double
Complex Number Support: Yes
```

ANG - Estimated direction of target
real-valued 2-by-1 vector
Estimated direction of target, returned as a real-valued 2-by-1 vector in the form [azimuth, elevation]. Units are in degrees.

## Dependencies

To enable this output port, select the Output angle estimate check box.
Data Types: double

## Parameters

## Main Tab

Signal propagation speed (m/s) - Signal propagation speed
physconst('LightSpeed') (default) | real-valued positive scalar

Signal propagation speed, specified as a real-valued positive scalar. The default value of the speed of light is the value returned by physconst ('LightSpeed'). Units are in meters per second.
Example: 3e8

## Data Types: double

Operating frequency (Hz) - System operating frequency
3e8 (default) | positive real scalar

System operating frequency, specified as a positive scalar. Units are in Hz .
Monopulse coverage - Monopulse coverage directions
3D (default) | Azimuth

Coverage directions of monopulse feed, specified as 3D or Azimuth. When you set this parameter to 3D, the monopulse feed forms the sum channel and both azimuth and elevation difference channels. When you set this parameter to Azimuth, the monopulse feed forms the sum channel and the azimuth difference channel.

Squint angle (degrees) - Squint angle
10 (default) | scalar | real-valued 2-by-1 vector

Squint angle, specified as a scalar or real-valued 2 -by-1 vector. The squint angle is the separation angle between the sum beam and the beams along the azimuth and elevation directions.

- When you set the Monopulse coverage parameter to Azimuth, set the Squint angle parameter to a scalar.
- When you set the Monopulse coverage parameter to 3D, you can specify the squint angle as either a scalar or vector. If you set the Squint angle parameter to a scalar, the squint angle is the same along both the azimuth and elevation directions. If you set the Squint angle parameter to a 2 -by- 1 vector, its elements specify the squint angle along the azimuth and elevation directions.

Example: [20;5]
Output angle estimate - Enable angle estimate output
off (default) | on

Select this check box to output an estimate of the target direction angle using the ANG output port.
Generate Monopulse Tracker - Create Monopulse estimator block
button

Click this button to create a Monopulse Estimate block based on the parameters in this block.
Simulate using - Block simulation method
Interpreted Execution (default) | Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).

```
Programmatic Use
Block Parameter:SimulateUsing
Type:enum
Values:Interpreted Execution, Code Generation
Default:Interpreted Execution
```


## Sensor Arrays Tab

```
Specify sensor array as - Method to specify array
Array (no subarrays) (default)|Partitioned array|Replicated subarray|MATLAB expression
```

Method to specify array, specified as Array (no subarrays) or MATLAB expression.

- Array (no subarrays) - use the block parameters to specify the array.
- Partitioned array - use the block parameters to specify the array.
- Replicated subarray - use the block parameters to specify the array.
- MATLAB expression - create the array using a MATLAB expression.

Expression - MATLAB expression used to create an array
Phased Array System Toolbox array System object

MATLAB expression used to create an array, specified as a valid Phased Array System Toolbox array System object.

Example: phased.URA('Size', [5, 3])

## Dependencies

To enable this parameter, set Specify sensor array as to MATLAB expression.

## Element Parameters

Element type - Array element types
Isotropic Antenna (default)|Cosine Antenna|Custom Antenna|Omni Microphone | Custom Microphone

Antenna or microphone type, specified as one of the following:

- Isotropic Antenna
- Cosine Antenna
- Custom Antenna
- Omni Microphone
- Custom Microphone

Operating frequency range $(\mathbf{H z})$ - Operating frequency range of the antenna or microphone element
[0, 1e20] (default) | real-valued 1-by-2 row vector

Specify the operating frequency range of the antenna or microphone element as a 1-by-2 row vector in the form [LowerBound, UpperBound]. The element has no response outside this frequency range. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Isotropic Antenna, Cosine Antenna, or Omni Microphone.

Operating frequency vector (Hz) - Operating frequency range of custom antenna or microphone elements
[0,1e20] (default) | real-valued row vector

Specify the frequencies at which to set antenna and microphone frequency responses as a 1-by- $L$ row vector of increasing real values. The antenna or microphone element has no response outside the frequency range specified by the minimum and maximum elements of this vector. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone. Use Frequency responses (dB) to set the responses at these frequencies.

Baffle the back of the element - Set back response of an Isotropic Antenna element or an Omni Microphone element to zero off (default) | on

Select this check box to baffle the back response of the element. When back baffled, the responses at all azimuth angles beyond $\pm 90^{\circ}$ from broadside are set to zero. The broadside direction is defined as $0^{\circ}$ azimuth angle and $0^{\circ}$ elevation angle.

## Dependencies

To enable this check box, set Element type to Isotropic Antenna or Omni Microphone.
Exponent of cosine pattern - Exponents of azimuth and elevation cosine patterns
[1.5 1.5] (default) | nonnegative scalar | real-valued 1-by-2 matrix of nonnegative values

Specify the exponents of the cosine pattern as a nonnegative scalar or a real-valued 1-by-2 matrix of nonnegative values. When Exponent of cosine pattern is a 1-by-2 vector, the first element is the exponent in the azimuth direction and the second element is the exponent in the elevation direction. When you set this parameter to a scalar, both the azimuth direction and elevation direction cosine patterns are raised to the same power.

## Dependencies

To enable this parameter, set Element type to Cosine Antenna.
Frequency responses (dB) - Antenna and microphone frequency response
[0,0] (default) | real-valued row vector

Frequency response of a custom antenna or custom microphone for the frequencies defined by the Operating frequency vector ( $\mathbf{H z}$ ) parameter. The dimensions of Frequency responses (dB) must match the dimensions of the vector specified by the Operating frequency vector (Hz) parameter.

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone.
Input Pattern Coordinate System - Coordinate system of custom antenna pattern az-el (default)|phi-theta

Coordinate system of custom antenna pattern, specified az-el or phi-theta. When you specify azel, use the Azimuth angles (deg) and Elevations angles (deg) parameters to specify the coordinates of the pattern points. When you specify phi-theta, use the Phi angles (deg) and Theta angles (deg) parameters to specify the coordinates of the pattern points.

## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Azimuth angles (deg) - Azimuth angles of antenna radiation pattern
[-180:180] (default) | real-valued row vector

Specify the azimuth angles at which to calculate the antenna radiation pattern as a 1 -by- $P$ row vector. $P$ must be greater than 2 . Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input
Pattern Coordinate System parameter to az-el.
Elevation angles (deg) - Elevation angles of antenna radiation pattern
[-90:90] (default) | real-valued row vector

Specify the elevation angles at which to compute the radiation pattern as a 1-by- $Q$ vector. $Q$ must be greater than 2. Angle units are in degrees. Elevation angles must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input
Pattern Coordinate System parameter to az-el.
Phi Angles (deg) - Phi angle coordinates of custom antenna radiation pattern
$0: 360 \mid$ real-valued 1 -by-P row vector

Phi angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by-P row vector. $P$ must be greater than 2 . Angle units are in degrees. Phi angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Theta Angles (deg) - Theta angle coordinates of custom antenna radiation pattern
$0: 180$ | real-valued 1-by- $Q$ row vector

Theta angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by$Q$ row vector. $Q$ must be greater than 2. Angle units are in degrees. Theta angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Magnitude pattern (dB) - Magnitude of combined antenna radiation pattern zeros $(181,361)$ (default) | real-valued $Q$-by-P matrix | real-valued $Q$-by- $P$-by-L array

Magnitude of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector $(\mathbf{H z})$.

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector (Hz) parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector $(\mathbf{H z})$ parameter.


## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Phase pattern (deg) - Custom antenna radiation phase pattern
zeros $(181,361)$ (default) | real-valued $Q$-by-P matrix | real-valued $Q$-by- $P$-by-L array

Phase of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector ( $\mathbf{H z}$ ).

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (


## Dependencies

To enable this parameter, set Element type to Custom Antenna.
MatchArrayNormal - Rotate antenna element to array normal
on (default) | off

Select this check box to rotate the antenna element pattern to align with the array normal. When not selected, the element pattern is not rotated.

When the antenna is used in an antenna array and the Input Pattern Coordinate System parameter is az-el, selecting this check box rotates the pattern so that the $x$-axis of the element coordinate system points along the array normal. Not selecting uses the element pattern without the rotation.

When the antenna is used in an antenna array and Input Pattern Coordinate System is set to phitheta, selecting this check box rotates the pattern so that the $z$-axis of the element coordinate system points along the array normal.

Use the parameter in conjunction with the Array normal parameter of the URA and UCA arrays.

## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Polar pattern frequencies (Hz) - Polar pattern microphone response frequencies
1 e3 (default) | real scalar | real-valued 1-by-L row vector

Polar pattern microphone response frequencies, specified as a real scalar, or a real-valued, 1-by- $L$ vector. The response frequencies lie within the frequency range specified by the Operating frequency vector $(\mathbf{H z})$ vector.

## Dependencies

To enable this parameter, set Element type set to Custom Microphone.
Polar pattern angles (deg) - Polar pattern response angles
[-180:180] (default) | real-valued -by-P row vector

Specify the polar pattern response angles, as a 1-by- $P$ vector. The angles are measured from the central pickup axis of the microphone and must be between $-180^{\circ}$ and $180^{\circ}$, inclusive.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.
Polar pattern (dB) - Custom microphone polar response
zeros (1, 361) (default) | real-valued $L$-by- $P$ matrix

Specify the magnitude of the custom microphone element polar patterns as an $L$-by- $P$ matrix. $L$ is the number of frequencies specified in Polar pattern frequencies ( $\mathbf{H z}$ ). $P$ is the number of angles specified in Polar pattern angles (deg). Each row of the matrix represents the magnitude of the polar pattern measured at the corresponding frequency specified in Polar pattern frequencies (Hz) and all angles specified in Polar pattern angles (deg). The pattern is measured in the azimuth plane. In the azimuth plane, the elevation angle is $0^{\circ}$ and the central pickup axis is $0^{\circ}$ degrees azimuth and $0^{\circ}$ degrees elevation. The polar pattern is symmetric around the central axis. You can construct the microphone response pattern in 3-D space from the polar pattern.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.

## Array Parameters

Geometry - Array geometry
ULA (default) | URA | UCA | Conformal Array

Array geometry, specified as one of

- ULA - Uniform linear array
- URA - Uniform rectangular array
- UCA - Uniform circular array
- Conformal Array - arbitrary element positions

Number of elements - Number of array elements
2 for ULA arrays and 5 for UCA arrays (default) | integer greater than or equal to 2

The number of array elements for ULA or UCA arrays, specified as an integer greater than or equal to 2.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

## Dependencies

To enable this parameter, set Geometry to ULA or UCA.
Element spacing (m) - Spacing between array elements
0.5 for ULA arrays and [0.5,0.5] for URA arrays (default) | positive scalar for ULA or URA arrays | 2-element vector of positive values for URA arrays

Spacing between adjacent array elements:

- ULA - specify the spacing between two adjacent elements in the array as a positive scalar.
- URA - specify the spacing as a positive scalar or a 1-by-2 vector of positive values. If Element spacing (m) is a scalar, the row and column spacings are equal. If Element spacing (m) is a vector, the vector has the form [SpacingBetweenArrayRows, SpacingBetweenArrayColumns].
- When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.


## Dependencies

To enable this parameter, set Geometry to ULA or URA.
Array axis - Linear axis direction of ULA
y (default) $|x| z$

Linear axis direction of ULA, specified as $y, x$, or $z$. All ULA array elements are uniformly spaced along this axis in the local array coordinate system.

## Dependencies

- To enable this parameter, set Geometry to ULA.
- This parameter is also enabled when the block only supports ULA arrays.

Array size - Dimensions of URA array
[2,2] (default) | positive integer | 1-by-2 vector of positive integers

Dimensions of a URA array, specified as a positive integer or 1-by-2 vector of positive integers.

- If Array size is a 1-by-2 vector, the vector has the form [NumberOfArrayRows, NumberOfArrayColumns].
- If Array size is an integer, the array has the same number of rows and columns.
- When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

For a URA, array elements are indexed from top to bottom along the leftmost column, and then continue to the next columns from left to right. In this figure, the Array size value of [3,2] creates an array having three rows and two columns.

## Size and Element Indexing Order

for Uniform Rectangular Arrays
Example: Size $=[3,2]$


## Dependencies

To enable this parameter, set Geometry to URA.
Element lattice - Lattice of URA element positions
Rectangular (default) | Triangular

Lattice of URA element positions, specified as Rectangular or Triangular.

- Rectangular - Aligns all the elements in row and column directions.
- Triangular - Shifts the even-row elements of a rectangular lattice toward the positive row-axis direction. The displacement is one-half the element spacing along the row dimension.


## Dependencies

To enable this parameter, set Geometry to URA.
Array normal - Array normal direction
$x$ for URA arrays or $z$ for UCA arrays (default) | y

Array normal direction, specified as $\mathrm{x}, \mathrm{y}$, or z .

Elements of planar arrays lie in a plane orthogonal to the selected array normal direction. Element boresight directions point along the array normal direction.

| Array Normal Parameter Value | Element Positions and Boresight Directions |
| :--- | :--- |
| $x$ | Array elements lie in the $y z$-plane. All element <br> boresight vectors point along the $x$-axis. |
| $y$ | Array elements lie in the $z x$-plane. All element <br> boresight vectors point along the $y$-axis. |
| $z$ | Array elements lie in the $x y$-plane. All element <br> boresight vectors point along the $z$-axis. |

## Dependencies

To enable this parameter, set Geometry to URA or UCA.
Radius of UCA (m) - UCA array radius
0.5 (default) | positive scalar

Radius of UCA array, specified as a positive scalar.

## Dependencies

To enable this parameter, set Geometry to UCA.
Element positions (m) - Positions of conformal array elements
[0;0;0] (default) | 3-by-Nmatrix of real values

Positions of the elements in a conformal array, specified as a $3-b y-N$ matrix of real values, where $N$ is the number of elements in the conformal array. Each column of this matrix represents the position [ $x ; y ; z$ ] of an array element in the array local coordinate system. The origin of the local coordinate system is $(0,0,0)$. Units are in meters.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

## Dependencies

To enable this parameter set Geometry to Conformal Array.
Element normals (deg) - Direction of conformal array element normal vectors
[0;0]|2-by-1 column vector | 2 -by- $N$ matrix

Direction of element normal vectors in a conformal array, specified as a 2-by-1 column vector or a 2-by- $N$ matrix. $N$ indicates the number of elements in the array. For a matrix, each column specifies the normal direction of the corresponding element in the form [azimuth; elevation] with respect to the local coordinate system. The local coordinate system aligns the positive $x$-axis with the direction normal to the conformal array. If the parameter value is a 2 -by- 1 column vector, the same pointing direction is used for all array elements.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

You can use the Element positions (m) and Element normals (deg) parameters to represent any arrangement in which pairs of elements differ by certain transformations. The transformations can combine translation, azimuth rotation, and elevation rotation. However, you cannot use transformations that require rotation about the normal direction.

## Dependencies

To enable this parameter, set Geometry to Conformal Array.
Taper - Array element tapers
1 (default) | complex-valued scalar | complex-valued row vector

Element tapering, specified as a complex-valued scalar or a complex-valued 1-by- $N$ row vector. In this vector, $N$ represents the number of elements in the array.

Also known as element weights, tapers multiply the array element responses. Tapers modify both amplitude and phase of the response to reduce side lobes or steer the main response axis.

If Taper is a scalar, the same weight is applied to each element. If Taper is a vector, a weight from the vector is applied to the corresponding sensor element. The number of weights must match the number of elements of the array.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

Subarray definition matrix - Define elements belonging to subarrays
logical matrix

Specify the subarray selection as an $M$-by- $N$ matrix. $M$ is the number of subarrays and $N$ is the total number of elements in the array. Each row of the matrix represents a subarray and each entry in the row indicates when an element belongs to the subarray. When the entry is zero, the element does not belong the subarray. A nonzero entry represents a complex-valued weight applied to the corresponding element. Each row must contain at least one nonzero entry.

The phase center of each subarray lies at the subarray geometric center. The subarray geometric center depends on the Subarray definition matrix and Geometry parameters.

## Dependencies

To enable this parameter, set Specify sensor array as to Partitioned array.
Subarray steering method - Specify subarray steering method None (default) | Phase | Time

Subarray steering method, specified as one of

- None
- Phase
- Time
- Custom

Selecting Phase or Time opens the Steer input port on the Narrowband Receive Array, Narrowband Transmit Array, Wideband Receive Array, Wideband Transmit Array blocks, Constant Gamma Clutter, and GPU Constant Gamma Clutter blocks.

Selecting Custom opens the WS input port on the Narrowband Receive Array, Narrowband Transmit Array, Wideband Receive Array, Wideband Transmit Array blocks, Constant Gamma Clutter, and GPU Constant Gamma Clutter blocks.

## Dependencies

To enable this parameter, set Specify sensor array as to Partitioned array or Replicated subarray.

Phase shifter frequency (Hz) - Subarray phase shifting frequency
3.0 e 8 (default) | positive real-valued scalar

Operating frequency of subarray steering phase shifters, specified as a positive real-valued scalar. Units are Hz.

## Dependencies

To enable this parameter, set Sensor array to Partitioned array or Replicated subarray and set Subarray steering method to Phase.

Number of bits in phase shifters - Subarray steering phase shift quantization bits
0 (default) | non-negative integer

Subarray steering phase shift quantization bits, specified as a non-negative integer. A value of zero indicates that no quantization is performed.

## Dependencies

To enable this parameter, set Sensor array to Partitioned array or Replicated subarray and set Subarray steering method to Phase.

Subarrays layout - Subarray position specification
Rectangular (default) | Custom

Specify the layout of replicated subarrays as Rectangular or Custom.

- When you set this parameter to Rectangular, use the Grid size and Grid spacing parameters to place the subarrays.
- When you set this parameter to Custom, use the Subarray positions (m) and Subarray normals parameters to place the subarrays.

Dependencies
To enable this parameter, set Sensor array to Replicated subarray
Grid size - Dimensions of rectangular subarray grid
[1,2] (default)

Rectangular subarray grid size, specified as a single positive integer, or a 1-by-2 row vector of positive integers.

If Grid size is an integer scalar, the array has an equal number of subarrays in each row and column.
If Grid size is a 1-by-2 vector of the form [NumberOfRows, NumberOfColumns], the first entry is the number of subarrays along each column. The second entry is the number of subarrays in each row. A row is along the local $y$-axis, and a column is along the local $z$-axis. The figure here shows how you can replicate a 3-by-2 URA subarray using a Grid size of [1,2].
$3 \times 2$ Element URA
Replicated on a $1 \times 2$ Grid


## Dependencies

To enable this parameter, set Sensor array to Replicated subarray and Subarrays layout to Rectangular.

Grid spacing ( $\mathbf{m}$ ) - Spacing between subarrays on rectangular grid
Auto (default) | positive real-valued scalar | 1-by-2 vector of positive real-values

The rectangular grid spacing of subarrays, specified as a positive, real-valued scalar, a 1-by-2 row vector of positive, real-values, or Auto. Units are in meters.

- If Grid spacing is a scalar, the spacing along the row and the spacing along the column is the same.
- If Grid spacing is a 1-by-2 row vector, the vector has the form [SpacingBetweenRows,SpacingBetweenColumn]. The first entry specifies the spacing between rows along a column. The second entry specifies the spacing between columns along a row.
- If Grid spacing is set to Auto, replication preserves the element spacing of the subarray for both rows and columns while building the full array. This option is available only when you specify Geometry as ULA or URA.


## Dependencies

To enable this parameter, set Sensor array to Replicated subarray and Subarrays layout to Rectangular.

Subarray positions (m) - Positions of subarrays
[0,0;0.5,0.5;0,0] (default)| 3-by- $N$ real-valued matrix

Positions of the subarrays in the custom grid, specified as a real 3-by- $N$ matrix, where $N$ is the number of subarrays in the array. Each column of the matrix represents the position of a single subarray in the array local coordinate system. The coordinates are expressed in the form [x; y; z]. Units are in meters.

Dependencies
To enable this parameter, set Sensor array to Replicated subarray and Subarrays layout to Custom.

Subarray normals - Direction of subarray normal vectors
[0,0;0,0] (default)| 2-by- $N$ real matrix

Specify the normal directions of the subarrays in the array. This parameter value is a 2 -by- $N$ matrix, where $N$ is the number of subarrays in the array. Each column of the matrix specifies the normal direction of the corresponding subarray, in the form [azimuth; elevation]. Angle units are in degrees. Angles are defined with respect to the local coordinate system.

You can use the Subarray positions and Subarray normals parameters to represent any arrangement in which pairs of subarrays differ by certain transformations. The transformations can combine translation, azimuth rotation, and elevation rotation. However, you cannot use transformations that require rotation about the normal.

## Dependencies

To enable this parameter, set the Sensor array parameter to Replicated subarray and the Subarrays layout to Custom.

## Version History <br> Introduced in R2018b

## See Also

phased. MonopulseFeed

## Monopulse Estimator

Estimate target direction from sum and difference channels


## Libraries:

Phased Array System Toolbox / Direction of Arrival

## Description

The Monopulse Estimator estimates the direction of arrival of a narrowband signal based on an initial guess by applying amplitude monopulse processing on sum and difference channel signals received by an array. You can create these channels using the Monopulse Feed block.

## Ports

## Input

SIGMA - Sum-channel signal
complex-valued $N$-by-1 column vector
Sum-channel signal, specified as a complex-valued $N$-by- 1 column vector. $N$ is the number of snapshots in the signal.
Data Types: double
Complex Number Support: Yes
DeltaAz - Azimuth difference-channel signal
complex-valued $N$-by-1 column vector
Azimuth difference-channel signal, specified as a complex-valued $N$-by-1 column vector. $N$ is the number of snapshots in the signal.
Data Types: double
Complex Number Support: Yes
DeltaEI - Elevation difference-channel signal
complex-valued $M$-by- 1
Elevation difference-channel signal, specified as a complex-valued $N$-by- 1 column vector. $N$ is the number of snapshots in the signal.

## Dependencies

To enable this output port, set the Monopulse coverage parameter to 3D.
Data Types: double
Complex Number Support: Yes
STEER - Array steering direction
scalar | real-valued 2-by-1 column vector
Array steering direction, specified as a scalar or real-valued 2-by-1 column vector.

- When you set the Monopulse coverage parameter to Azimuth, the steering direction is a scalar and represents the azimuth steering angle.
- When you set the Monopulse coverage parameter to 3D, the steering direction vector has the form [azimuthAngle; elevationAngle], where azimuthAngle is the azimuth steering angle, and elevationAngle is the elevation steering angle.

Units are in degrees. Azimuth angles lie between $-180^{\circ}$ and $180^{\circ}$, inclusive, and elevation angles lie between $-90^{\circ}$ and $90^{\circ}$, inclusive.

Example: [40;10]
Data Types: double

## Output

Az - Estimated azimuth direction of target
real-valued 1-by- $N$ vector
Estimated azimuth direction of target, returned as a real-valued 1-by-N. The vector elements contain the estimated target direction azimuth angle at each signal snapshot. Units are in degrees.

## Dependencies

To enable this output port, set the Monopulse coverage to Azimuth and the OutputFormat to Angle.

## Data Types: double

$\mathbf{d A z}$ - Estimated offset of azimuth direction of target
real-valued 1-by- $N$ vector
Estimated offset of azimuth direction of target, returned as a real-valued 1 -by- $N$ vector. The vector elements contain the offset of the estimated target direction azimuth angle from the azimuth steering direction at each signal snapshot. Units are in degrees.

## Dependencies

To enable this output port, set the Monopulse coverage to Azimuth and the OutputFormat to Angle offset.
Data Types: double
AzEI - Estimated direction of target
real-valued 2 -by- $N$ matrix
Estimated direction of target, returned as a real-valued 2-by- $N$ matrix. Each column contains the estimated target direction in the form [azimuthAngle; elevationAngle], where azimuthAngle is the estimated azimuth angle, and elevationAngle is estimated elevation angle. Units are in degrees.

## Dependencies

To enable this output port, set the Monopulse coverage to 3D and the OutputFormat to Angle.

## Data Types: double

dAzEI - Estimated offset of direction of target
real-valued 2 -by- $N$ matrix

Estimated offset of direction of target, returned as a real-valued 2-by- $N$ matrix. The offset is the difference between the target direction and the steering vector. Each column contains the estimated offset of the target direction in the form [dazimuthAngle; delevationAngle], where dazimuthAngle is the estimated azimuth angle offset, and delevationAngle is estimated elevation angle offset. Units are in degrees.

## Dependencies

To enable this output port, set the Monopulse coverage to 3D and the OutputFormat to Angle offset.
Data Types: double
AzRatio - Ratio of sum and azimuth difference channels
real-valued 1-by- $N$ vector
Ratio of sum and azimuth difference channels, returned as a real-valued 1-by- $N$ vector. The elements contain the ratio of the sum to azimuth difference channel at each signal snapshot.

## Dependencies

To enable this output port, set the Monopulse coverage to Azimuth and select the Output sum difference ratio check box.
Data Types: double
AzEIRatio - Ratio of sum channel to azimuth and elevation difference channels real-valued 2-by- $N$ matrix

Ratio of sum and azimuth and elevation difference channels, returned as a real-valued 2 -by- $N$ matrix. The elements of the first row contain the ratio of the sum to azimuth difference channel at each signal snapshot. The elements of the second row contain the ratio of the sum to elevation difference channel at each signal snapshot.

## Dependencies

To enable this output port, set the Monopulse coverage to 3D and select the Output sum difference ratio check box.

Data Types: double

## Parameters

## Main Tab

Signal propagation speed (m/s) - Signal propagation speed
physconst('LightSpeed') (default)| real-valued positive scalar

Signal propagation speed, specified as a real-valued positive scalar. The default value of the speed of light is the value returned by physconst('LightSpeed'). Units are in meters per second.

Example: 3e8
Data Types: double
Operating frequency $(\mathbf{H z})$ - System operating frequency
3e8 (default) | positive real scalar

System operating frequency, specified as a positive scalar. Units are in Hz .
Monopulse coverage - Monopulse coverage directions
3D (default) | Azimuth

Monopulse coverage directions, specified as 3D or Azimuth. When you set this parameter to 3D, the monopulse estimator uses the sum channel and both azimuth and elevation difference channels. When you set this parameter to Azimuth, the monopulse estimator uses the sum channel and the azimuth difference channel.

Squint angle (degrees) - Squint angle
10 (default) | scalar | real-valued 2-by-1 vector

Squint angle, specified as a scalar or real-valued 2-by-1 vector. The squint angle is the separation angle between the sum beam and the beams along the azimuth and elevation directions.

- When you set the Monopulse coverage parameter to Azimuth, set the Squint angle parameter to a scalar.
- When you set the Monopulse coverage parameter to 3D, you can specify the squint angle as either a scalar or vector. If you set the Squint angle parameter to a scalar, the squint angle is the same along both the azimuth and elevation directions. If you set the Squint angle parameter to a 2 -by- 1 vector, its elements specify the squint angle along the azimuth and elevation directions.

Example: [20;5]
Output format - Output direction format
Angle (default) | Angle offset

Format of direction output, specified Angle or Angle offset. When you set this parameter to Angle, the output port is labeled AzEl or Az and is the actual direction of the target. When you set this property to Angle offset, the output port is labeled dAzEl or dAz and is the angle offset of the target from the array steering direction.

Output sum difference ratio - Enable sum-difference ratio output port off (default) | on

Select this check box to output the ratio of the sum and difference channels in the azimuth and elevation directions. When you set the Monopulse coverage to Azimuth, the block outputs the sumazimuth difference ratio using the AzRatio port. When you set the Monopulse coverage to 3D, the block outputs the sum-azimuth difference and sum-elevation difference channels ratio using the AzElRatio port.

Generate Monopulse Feed - Create monopulse feed block
button

Click this button to create a Monopulse Feed block based on the parameters in this block.

## Simulate using - Block simulation method <br> Interpreted Execution (default)|Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).

## Programmatic Use

Block Parameter:SimulateUsing
Type:enum
Values:Interpreted Execution, Code Generation
Default:Interpreted Execution

## Sensor Arrays Tab

Specify sensor array as - Method to specify array
Array (no subarrays) (default)|Partitioned array|Replicated subarray|MATLAB expression

Method to specify array, specified as Array (no subarrays) or MATLAB expression.

- Array (no subarrays) - use the block parameters to specify the array.
- Partitioned array - use the block parameters to specify the array.
- Replicated subarray - use the block parameters to specify the array.
- MATLAB expression - create the array using a MATLAB expression.

Expression - MATLAB expression used to create an array
Phased Array System Toolbox array System object

MATLAB expression used to create an array, specified as a valid Phased Array System Toolbox array System object.

Example: phased.URA('Size', [5,3])

## Dependencies

To enable this parameter, set Specify sensor array as to MATLAB expression.

## Element Parameters

Element type - Array element types
Isotropic Antenna (default)|Cosine Antenna|Custom Antenna|Omni Microphone| Custom Microphone

Antenna or microphone type, specified as one of the following:

- Isotropic Antenna
- Cosine Antenna
- Custom Antenna
- Omni Microphone
- Custom Microphone

Operating frequency range (Hz) - Operating frequency range of the antenna or microphone element
[0,1e20] (default) | real-valued 1-by-2 row vector

Specify the operating frequency range of the antenna or microphone element as a 1-by-2 row vector in the form [LowerBound, UpperBound]. The element has no response outside this frequency range. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Isotropic Antenna, Cosine Antenna, or Omni Microphone.

Operating frequency vector ( $\mathbf{H z}$ ) - Operating frequency range of custom antenna or microphone elements
[0,1e20] (default) | real-valued row vector

Specify the frequencies at which to set antenna and microphone frequency responses as a 1-by- $L$ row vector of increasing real values. The antenna or microphone element has no response outside the frequency range specified by the minimum and maximum elements of this vector. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone. Use Frequency responses (dB) to set the responses at these frequencies.

Baffle the back of the element - Set back response of an Isotropic Antenna element or an Omni Microphone element to zero
off (default) | on

Select this check box to baffle the back response of the element. When back baffled, the responses at all azimuth angles beyond $\pm 90^{\circ}$ from broadside are set to zero. The broadside direction is defined as $0^{\circ}$ azimuth angle and $0^{\circ}$ elevation angle.

Dependencies
To enable this check box, set Element type to Isotropic Antenna or Omni Microphone.
Exponent of cosine pattern - Exponents of azimuth and elevation cosine patterns
[1.5 1.5] (default) | nonnegative scalar | real-valued 1-by-2 matrix of nonnegative values

Specify the exponents of the cosine pattern as a nonnegative scalar or a real-valued 1-by-2 matrix of nonnegative values. When Exponent of cosine pattern is a 1-by-2 vector, the first element is the exponent in the azimuth direction and the second element is the exponent in the elevation direction. When you set this parameter to a scalar, both the azimuth direction and elevation direction cosine patterns are raised to the same power.

## Dependencies

To enable this parameter, set Element type to Cosine Antenna.
Frequency responses (dB) - Antenna and microphone frequency response
[0,0] (default) | real-valued row vector

Frequency response of a custom antenna or custom microphone for the frequencies defined by the Operating frequency vector (Hz) parameter. The dimensions of Frequency responses (dB) must match the dimensions of the vector specified by the Operating frequency vector $(\mathbf{H z})$ parameter.

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone.
Input Pattern Coordinate System - Coordinate system of custom antenna pattern
az-el (default)|phi-theta

Coordinate system of custom antenna pattern, specified az-el or phi-theta. When you specify azel, use the Azimuth angles (deg) and Elevations angles (deg) parameters to specify the coordinates of the pattern points. When you specify phi-theta, use the Phi angles (deg) and Theta angles (deg) parameters to specify the coordinates of the pattern points.

## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Azimuth angles (deg) - Azimuth angles of antenna radiation pattern
[-180:180] (default) | real-valued row vector

Specify the azimuth angles at which to calculate the antenna radiation pattern as a 1-by- $P$ row vector. $P$ must be greater than 2. Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to az-el.

Elevation angles (deg) - Elevation angles of antenna radiation pattern
[-90:90] (default) | real-valued row vector

Specify the elevation angles at which to compute the radiation pattern as a 1-by- $Q$ vector. $Q$ must be greater than 2. Angle units are in degrees. Elevation angles must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to az-el.

Phi Angles (deg) - Phi angle coordinates of custom antenna radiation pattern
$0: 360$ | real-valued 1-by-P row vector

Phi angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by-P row vector. $P$ must be greater than 2 . Angle units are in degrees. Phi angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Theta Angles (deg) - Theta angle coordinates of custom antenna radiation pattern 0 : 180 | real-valued 1-by- $Q$ row vector

Theta angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by$Q$ row vector. $Q$ must be greater than 2 . Angle units are in degrees. Theta angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Magnitude pattern (dB) - Magnitude of combined antenna radiation pattern zeros $(181,361)$ (default) | real-valued $Q$-by- $P$ matrix | real-valued $Q$-by- $P$-by- $L$ array

Magnitude of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector $(\mathbf{H z})$.

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector (Hz) parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (Hz) parameter.


## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Phase pattern (deg) - Custom antenna radiation phase pattern
zeros $(181,361)$ (default) | real-valued $Q$-by-P matrix | real-valued $Q$-by- $P$-by-L array

Phase of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector $(\mathbf{H z})$.

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector (Hz) parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (

Dependencies
To enable this parameter, set Element type to Custom Antenna.
MatchArrayNormal - Rotate antenna element to array normal on (default) | off

Select this check box to rotate the antenna element pattern to align with the array normal. When not selected, the element pattern is not rotated.

When the antenna is used in an antenna array and the Input Pattern Coordinate System parameter is az-el, selecting this check box rotates the pattern so that the $x$-axis of the element coordinate system points along the array normal. Not selecting uses the element pattern without the rotation.

When the antenna is used in an antenna array and Input Pattern Coordinate System is set to phitheta, selecting this check box rotates the pattern so that the $z$-axis of the element coordinate system points along the array normal.

Use the parameter in conjunction with the Array normal parameter of the URA and UCA arrays.

## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Polar pattern frequencies (Hz) - Polar pattern microphone response frequencies
1e3 (default) | real scalar | real-valued 1-by-L row vector

Polar pattern microphone response frequencies, specified as a real scalar, or a real-valued, 1-by-L vector. The response frequencies lie within the frequency range specified by the Operating frequency vector $(\mathrm{Hz})$ vector.

## Dependencies

To enable this parameter, set Element type set to Custom Microphone.
Polar pattern angles (deg) - Polar pattern response angles
[-180:180] (default) | real-valued -by-P row vector

Specify the polar pattern response angles, as a 1-by- $P$ vector. The angles are measured from the central pickup axis of the microphone and must be between $-180^{\circ}$ and $180^{\circ}$, inclusive.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.
Polar pattern (dB) - Custom microphone polar response
zeros $(1,361)$ (default) | real-valued $L$-by- $P$ matrix

Specify the magnitude of the custom microphone element polar patterns as an $L$-by- $P$ matrix. $L$ is the number of frequencies specified in Polar pattern frequencies ( $\mathbf{H z}$ ). $P$ is the number of angles specified in Polar pattern angles (deg). Each row of the matrix represents the magnitude of the polar pattern measured at the corresponding frequency specified in Polar pattern frequencies (Hz) and all angles specified in Polar pattern angles (deg). The pattern is measured in the azimuth plane. In the azimuth plane, the elevation angle is $0^{\circ}$ and the central pickup axis is $0^{\circ}$ degrees azimuth and $0^{\circ}$ degrees elevation. The polar pattern is symmetric around the central axis. You can construct the microphone response pattern in 3-D space from the polar pattern.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.

## Array Parameters

Geometry - Array geometry
ULA (default) | URA | UCA | Conformal Array

Array geometry, specified as one of

- ULA - Uniform linear array
- URA - Uniform rectangular array
- UCA - Uniform circular array
- Conformal Array - arbitrary element positions

Number of elements - Number of array elements
2 for ULA arrays and 5 for UCA arrays (default) | integer greater than or equal to 2

The number of array elements for ULA or UCA arrays, specified as an integer greater than or equal to 2.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

## Dependencies

To enable this parameter, set Geometry to ULA or UCA.
Element spacing (m) - Spacing between array elements
0.5 for ULA arrays and [0.5,0.5] for URA arrays (default) | positive scalar for ULA or URA arrays | 2 -element vector of positive values for URA arrays

Spacing between adjacent array elements:

- ULA - specify the spacing between two adjacent elements in the array as a positive scalar.
- URA - specify the spacing as a positive scalar or a 1 -by-2 vector of positive values. If Element spacing (m) is a scalar, the row and column spacings are equal. If Element spacing (m) is a vector, the vector has the form [SpacingBetweenArrayRows, SpacingBetweenArrayColumns].
- When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

Dependencies
To enable this parameter, set Geometry to ULA or URA.
Array axis - Linear axis direction of ULA
$y$ (default) $|x| z$

Linear axis direction of ULA, specified as $y, x$, or $z$. All ULA array elements are uniformly spaced along this axis in the local array coordinate system.

## Dependencies

- To enable this parameter, set Geometry to ULA.
- This parameter is also enabled when the block only supports ULA arrays.

Array size - Dimensions of URA array
[2,2] (default) | positive integer | 1-by-2 vector of positive integers

Dimensions of a URA array, specified as a positive integer or 1-by-2 vector of positive integers.

- If Array size is a 1 -by-2 vector, the vector has the form [NumberOfArrayRows, NumberOfArrayColumns].
- If Array size is an integer, the array has the same number of rows and columns.
- When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

For a URA, array elements are indexed from top to bottom along the leftmost column, and then continue to the next columns from left to right. In this figure, the Array size value of [3, 2] creates an array having three rows and two columns.

## Size and Element Indexing Order

for Uniform Rectangular Arrays
Example: Size $=[3,2]$


## Dependencies

To enable this parameter, set Geometry to URA.
Element lattice - Lattice of URA element positions
Rectangular (default) | Triangular

Lattice of URA element positions, specified as Rectangular or Triangular.

- Rectangular - Aligns all the elements in row and column directions.
- Triangular - Shifts the even-row elements of a rectangular lattice toward the positive row-axis direction. The displacement is one-half the element spacing along the row dimension.


## Dependencies

To enable this parameter, set Geometry to URA.
Array normal - Array normal direction
$x$ for URA arrays or $z$ for UCA arrays (default) | y

Array normal direction, specified as $x, y$, or $z$.

Elements of planar arrays lie in a plane orthogonal to the selected array normal direction. Element boresight directions point along the array normal direction.

| Array Normal Parameter Value | Element Positions and Boresight Directions |
| :--- | :--- |
| $x$ | Array elements lie in the $y z$-plane. All element <br> boresight vectors point along the $x$-axis. |
| $y$ | Array elements lie in the $z x$-plane. All element <br> boresight vectors point along the $y$-axis. |
| $z$ | Array elements lie in the $x y$-plane. All element <br> boresight vectors point along the $z$-axis. |

## Dependencies

To enable this parameter, set Geometry to URA or UCA.
Radius of UCA (m) - UCA array radius
0.5 (default) | positive scalar

Radius of UCA array, specified as a positive scalar.

## Dependencies

To enable this parameter, set Geometry to UCA.
Element positions (m) - Positions of conformal array elements
[0;0;0] (default)| 3-by-Nmatrix of real values

Positions of the elements in a conformal array, specified as a $3-b y-N$ matrix of real values, where $N$ is the number of elements in the conformal array. Each column of this matrix represents the position [ $x ; y ; z$ ] of an array element in the array local coordinate system. The origin of the local coordinate system is $(0,0,0)$. Units are in meters.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

## Dependencies

To enable this parameter set Geometry to Conformal Array.
Element normals (deg) - Direction of conformal array element normal vectors
[0;0]|2-by-1 column vector | 2 -by- $N$ matrix

Direction of element normal vectors in a conformal array, specified as a 2-by-1 column vector or a 2-by- $N$ matrix. $N$ indicates the number of elements in the array. For a matrix, each column specifies the normal direction of the corresponding element in the form [azimuth; elevation] with respect to the local coordinate system. The local coordinate system aligns the positive $x$-axis with the direction normal to the conformal array. If the parameter value is a 2 -by- 1 column vector, the same pointing direction is used for all array elements.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

You can use the Element positions (m) and Element normals (deg) parameters to represent any arrangement in which pairs of elements differ by certain transformations. The transformations can combine translation, azimuth rotation, and elevation rotation. However, you cannot use transformations that require rotation about the normal direction.

## Dependencies

To enable this parameter, set Geometry to Conformal Array.
Taper - Array element tapers
1 (default) | complex-valued scalar | complex-valued row vector

Element tapering, specified as a complex-valued scalar or a complex-valued 1-by- $N$ row vector. In this vector, $N$ represents the number of elements in the array.

Also known as element weights, tapers multiply the array element responses. Tapers modify both amplitude and phase of the response to reduce side lobes or steer the main response axis.

If Taper is a scalar, the same weight is applied to each element. If Taper is a vector, a weight from the vector is applied to the corresponding sensor element. The number of weights must match the number of elements of the array.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

Subarray definition matrix - Define elements belonging to subarrays
logical matrix

Specify the subarray selection as an $M$-by- $N$ matrix. $M$ is the number of subarrays and $N$ is the total number of elements in the array. Each row of the matrix represents a subarray and each entry in the row indicates when an element belongs to the subarray. When the entry is zero, the element does not belong the subarray. A nonzero entry represents a complex-valued weight applied to the corresponding element. Each row must contain at least one nonzero entry.

The phase center of each subarray lies at the subarray geometric center. The subarray geometric center depends on the Subarray definition matrix and Geometry parameters.

## Dependencies

To enable this parameter, set Specify sensor array as to Partitioned array.
Subarray steering method - Specify subarray steering method None (default) | Phase | Time

Subarray steering method, specified as one of

- None
- Phase
- Time
- Custom

Selecting Phase or Time opens the Steer input port on the Narrowband Receive Array, Narrowband Transmit Array, Wideband Receive Array, Wideband Transmit Array blocks, Constant Gamma Clutter, and GPU Constant Gamma Clutter blocks.

Selecting Custom opens the WS input port on the Narrowband Receive Array, Narrowband Transmit Array, Wideband Receive Array, Wideband Transmit Array blocks, Constant Gamma Clutter, and GPU Constant Gamma Clutter blocks.

## Dependencies

To enable this parameter, set Specify sensor array as to Partitioned array or Replicated subarray.

Phase shifter frequency (Hz) - Subarray phase shifting frequency
3.0 e 8 (default) | positive real-valued scalar

Operating frequency of subarray steering phase shifters, specified as a positive real-valued scalar. Units are Hz.

## Dependencies

To enable this parameter, set Sensor array to Partitioned array or Replicated subarray and set Subarray steering method to Phase.

Number of bits in phase shifters - Subarray steering phase shift quantization bits
0 (default) | non-negative integer

Subarray steering phase shift quantization bits, specified as a non-negative integer. A value of zero indicates that no quantization is performed.

## Dependencies

To enable this parameter, set Sensor array to Partitioned array or Replicated subarray and set Subarray steering method to Phase.

Subarrays layout - Subarray position specification
Rectangular (default) | Custom

Specify the layout of replicated subarrays as Rectangular or Custom.

- When you set this parameter to Rectangular, use the Grid size and Grid spacing parameters to place the subarrays.
- When you set this parameter to Custom, use the Subarray positions (m) and Subarray normals parameters to place the subarrays.

Dependencies
To enable this parameter, set Sensor array to Replicated subarray
Grid size - Dimensions of rectangular subarray grid
[1,2] (default)

Rectangular subarray grid size, specified as a single positive integer, or a 1-by-2 row vector of positive integers.

If Grid size is an integer scalar, the array has an equal number of subarrays in each row and column. If Grid size is a 1-by-2 vector of the form [NumberOfRows, NumberOfColumns], the first entry is the number of subarrays along each column. The second entry is the number of subarrays in each row. A row is along the local $y$-axis, and a column is along the local $z$-axis. The figure here shows how you can replicate a 3-by-2 URA subarray using a Grid size of [1,2].
$3 \times 2$ Element URA
Replicated on a $1 \times 2$ Grid


## Dependencies

To enable this parameter, set Sensor array to Replicated subarray and Subarrays layout to Rectangular.

Grid spacing ( $\mathbf{m}$ ) - Spacing between subarrays on rectangular grid
Auto (default) | positive real-valued scalar | 1-by-2 vector of positive real-values

The rectangular grid spacing of subarrays, specified as a positive, real-valued scalar, a 1-by-2 row vector of positive, real-values, or Auto. Units are in meters.

- If Grid spacing is a scalar, the spacing along the row and the spacing along the column is the same.
- If Grid spacing is a 1-by-2 row vector, the vector has the form [SpacingBetweenRows, SpacingBetweenColumn]. The first entry specifies the spacing between rows along a column. The second entry specifies the spacing between columns along a row.
- If Grid spacing is set to Auto, replication preserves the element spacing of the subarray for both rows and columns while building the full array. This option is available only when you specify Geometry as ULA or URA.


## Dependencies

To enable this parameter, set Sensor array to Replicated subarray and Subarrays layout to Rectangular.

Subarray positions (m) - Positions of subarrays
[0,0;0.5,0.5;0,0] (default) | 3 -by- $N$ real-valued matrix

Positions of the subarrays in the custom grid, specified as a real 3-by- $N$ matrix, where $N$ is the number of subarrays in the array. Each column of the matrix represents the position of a single subarray in the array local coordinate system. The coordinates are expressed in the form [x; y; z]. Units are in meters.

Dependencies
To enable this parameter, set Sensor array to Replicated subarray and Subarrays layout to Custom.

Subarray normals - Direction of subarray normal vectors
[0,0;0,0] (default)| 2-by- $N$ real matrix

Specify the normal directions of the subarrays in the array. This parameter value is a 2 -by- $N$ matrix, where $N$ is the number of subarrays in the array. Each column of the matrix specifies the normal direction of the corresponding subarray, in the form [azimuth; elevation]. Angle units are in degrees. Angles are defined with respect to the local coordinate system.

You can use the Subarray positions and Subarray normals parameters to represent any arrangement in which pairs of subarrays differ by certain transformations. The transformations can combine translation, azimuth rotation, and elevation rotation. However, you cannot use transformations that require rotation about the normal.

## Dependencies

To enable this parameter, set the Sensor array parameter to Replicated subarray and the Subarrays layout to Custom.

## Version History <br> Introduced in R2018b

## See Also

phased.MonopulseEstimator

## MVDR Beamformer

Narrowband MVDR (Capon) beamformer

## Libraries:



Phased Array System Toolbox / Beamforming

## Description

The MVDR Beamformer block performs minimum variance distortionless response (MVDR) beamforming. The block preserves the signal power in the given direction while suppressing interference and noise from other directions. The MVDR beamformer is also called the Capon beamformer.

## Ports

Input
$\mathbf{X}$ - Input signal
$M$-by- $N$ complex-valued matrix
Input signal, specified as an $M$-by- $N$ matrix, where $M$ is the number of samples in the data, and $N$ is the number of array elements.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
Data Types: double
XT - Training signal
$M$-by- $N$ complex-valued matrix
Training signal, specified as an $M$-by- $N$ matrix, where $M$ is the number of samples in the data, and $N$ is the number of array elements.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

## Dependencies

To enable this port, select the Enable training data input check box.
Data Types: double
Ang - Beamforming direction
2-by-1 real-valued vector | 2-by-L real-valued matrix
Beamforming direction, specified as a 2 -by- $L$ real-valued matrix, where $L$ is the number of beamforming directions. Each column takes the form of [AzimuthAngle; ElevationAngle]. Angle
units are in degrees. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive, and the elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive. Angles are defined with respect to the local coordinate system of the array.

## Dependencies

To enable this port, set the Source of beamforming direction parameter to Input port.
Data Types: double

## Output

Y - Beamformed output
M-by-L complex-valued matrix
Beamformed output, returned as an $M$-by- $L$ complex-valued matrix. The quantity $M$ is the number of signal samples and $L$ is the number of desired beamforming directions specified by the Beamforming direction parameter or from the Ang port.

Data Types: double
W - Beamforming weights
$N$-by-L complex-valued matrix
Beamformed weights, returned as an $N$-by- $L$ complex-valued matrix. The quantity $N$ is the number of array elements. When the Specify sensor array as parameter is set to Partitioned array or Replicated subarray, $N$ represents the number of subarrays. $L$ is the number of desired beamforming directions specified in the Ang port or by the Beamforming direction (deg) property. There is one set of weights for each beamforming direction.

## Dependencies

To enable this port, select the Enable weights output checkbox.
Data Types: double

## Parameters

## Main tab

Signal propagation speed (m/s) - Signal propagation speed
physconst('LightSpeed') (default)| real-valued positive scalar

Signal propagation speed, specified as a real-valued positive scalar. The default value of the speed of light is the value returned by physconst('LightSpeed'). Units are in meters per second.

Example: 3e8
Data Types: double
Operating frequency (Hz) - System operating frequency
$3 e 8$ (default) | positive real scalar

System operating frequency, specified as a positive scalar. Units are in Hz.

## Diagonal loading factor - Diagonal loading factor for stability nonnegative scalar

Specify the diagonal loading factor as a nonnegative scalar. Diagonal loading is a technique used to achieve robust beamforming performance, especially when the sample support is small.

Enable training data input - Enable the use of training data off (default) | on

Select this check box to specify additional training data via the input port XT. To use the input signal as the training data, clear the check box which removes the port.

Source of beamforming direction - Source of beamforming direction
Property (default)|Input port

Source of beamforming direction, specified as Property or Input port. When you set Source of beamforming direction to Property, you then set the direction using the Beamforming direction (deg) parameter. When you select Input port, the direction is determined by the input to the Ang port.

Beamforming direction (deg) - Beamforming directions
2-by-L real-valued matrix

Beamforming directions, specified as a 2 -by- $L$ real-valued matrix, where $L$ is the number of beamforming directions. Each column takes the form [AzimuthAngle;ElevationAngle]. Angle units are in degrees. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$. Angles are defined with respect to the local coordinate system of the array.

## Dependencies

To enable this parameter, set the Source of beamforming direction parameter to Property.
Number of bits in phase shifters - Number of phase shift quantization bits
0 (default) | nonnegative integer

The number of bits used to quantize the phase shift component of beamformer or steering vector weights. Specify the number of bits as a non-negative integer. A value of zero indicates that no quantization is performed.

Enable weights output - Option to output beamformer weights
off (default) | on

Select this check box to obtain the beamformer weights from the output port, W .
Simulate using - Block simulation method
Interpreted Execution (default) |Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to
run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).
Programmatic Use
Block Parameter:SimulateUsing
Type:enum
Values:Interpreted Execution, Code Generation
Default:Interpreted Execution

## Sensor Arrays Tab

## Specify sensor array as - Method to specify array

Array (no subarrays) (default)|Partitioned array|Replicated subarray|MATLAB expression

Method to specify array, specified as Array (no subarrays) or MATLAB expression.

- Array (no subarrays) - use the block parameters to specify the array.
- Partitioned array - use the block parameters to specify the array.
- Replicated subarray - use the block parameters to specify the array.
- MATLAB expression - create the array using a MATLAB expression.

Expression - MATLAB expression used to create an array
Phased Array System Toolbox array System object

MATLAB expression used to create an array, specified as a valid Phased Array System Toolbox array System object.

Example: phased.URA('Size', [5,3])

## Dependencies

To enable this parameter, set Specify sensor array as to MATLAB expression.

## Element Parameters

Element type - Array element types
Isotropic Antenna (default)|Cosine Antenna|Custom Antenna|Omni Microphone| Custom Microphone

Antenna or microphone type, specified as one of the following:

- Isotropic Antenna
- Cosine Antenna
- Custom Antenna
- Omni Microphone
- Custom Microphone

Operating frequency range (Hz) - Operating frequency range of the antenna or microphone element
[0, 1e20] (default) | real-valued 1-by-2 row vector

Specify the operating frequency range of the antenna or microphone element as a 1-by-2 row vector in the form [LowerBound, UpperBound]. The element has no response outside this frequency range. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Isotropic Antenna, Cosine Antenna, or Omni Microphone.

Operating frequency vector ( $\mathbf{H z}$ ) - Operating frequency range of custom antenna or microphone elements
[0,1e20] (default) | real-valued row vector

Specify the frequencies at which to set antenna and microphone frequency responses as a 1-by- $L$ row vector of increasing real values. The antenna or microphone element has no response outside the frequency range specified by the minimum and maximum elements of this vector. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone. Use Frequency responses (dB) to set the responses at these frequencies.

Baffle the back of the element - Set back response of an Isotropic Antenna element or an Omni Microphone element to zero off (default) | on

Select this check box to baffle the back response of the element. When back baffled, the responses at all azimuth angles beyond $\pm 90^{\circ}$ from broadside are set to zero. The broadside direction is defined as $0^{\circ}$ azimuth angle and $0^{\circ}$ elevation angle.

## Dependencies

To enable this check box, set Element type to Isotropic Antenna or Omni Microphone.
Exponent of cosine pattern - Exponents of azimuth and elevation cosine patterns
[1.5 1.5] (default) | nonnegative scalar | real-valued 1-by-2 matrix of nonnegative values

Specify the exponents of the cosine pattern as a nonnegative scalar or a real-valued 1-by-2 matrix of nonnegative values. When Exponent of cosine pattern is a 1-by-2 vector, the first element is the exponent in the azimuth direction and the second element is the exponent in the elevation direction. When you set this parameter to a scalar, both the azimuth direction and elevation direction cosine patterns are raised to the same power.

## Dependencies

To enable this parameter, set Element type to Cosine Antenna.
Frequency responses (dB) - Antenna and microphone frequency response
[0,0] (default) | real-valued row vector

Frequency response of a custom antenna or custom microphone for the frequencies defined by the Operating frequency vector ( $\mathbf{H z}$ ) parameter. The dimensions of Frequency responses (dB) must match the dimensions of the vector specified by the Operating frequency vector (Hz) parameter.

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone.
Input Pattern Coordinate System - Coordinate system of custom antenna pattern az-el (default)|phi-theta

Coordinate system of custom antenna pattern, specified az-el or phi-theta. When you specify azel, use the Azimuth angles (deg) and Elevations angles (deg) parameters to specify the coordinates of the pattern points. When you specify phi-theta, use the Phi angles (deg) and Theta angles (deg) parameters to specify the coordinates of the pattern points.

## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Azimuth angles (deg) - Azimuth angles of antenna radiation pattern
[-180:180] (default) | real-valued row vector

Specify the azimuth angles at which to calculate the antenna radiation pattern as a 1 -by- $P$ row vector. $P$ must be greater than 2 . Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to az-el.

Elevation angles (deg) - Elevation angles of antenna radiation pattern
[-90:90] (default) | real-valued row vector

Specify the elevation angles at which to compute the radiation pattern as a 1-by- $Q$ vector. $Q$ must be greater than 2. Angle units are in degrees. Elevation angles must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to az-el.

Phi Angles (deg) - Phi angle coordinates of custom antenna radiation pattern
$0: 360$ | real-valued 1-by-P row vector

Phi angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by- $P$ row vector. $P$ must be greater than 2 . Angle units are in degrees. Phi angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Theta Angles (deg) - Theta angle coordinates of custom antenna radiation pattern
$0: 180$ | real-valued 1 -by- $Q$ row vector

Theta angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by$Q$ row vector. $Q$ must be greater than 2 . Angle units are in degrees. Theta angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Magnitude pattern (dB) - Magnitude of combined antenna radiation pattern zeros $(181,361)$ (default) | real-valued $Q$-by-P matrix | real-valued $Q$-by- $P$-by- $L$ array

Magnitude of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector $(\mathbf{H z})$.

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathrm{Hz})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector $(\mathbf{H z})$ parameter.


## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Phase pattern (deg) - Custom antenna radiation phase pattern
zeros $(181,361)$ (default) | real-valued $Q$-by-P matrix | real-valued $Q$-by- $P$-by-L array

Phase of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector ( $\mathbf{H z}$ ).

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (


## Dependencies

To enable this parameter, set Element type to Custom Antenna.
MatchArrayNormal - Rotate antenna element to array normal
on (default) | off

Select this check box to rotate the antenna element pattern to align with the array normal. When not selected, the element pattern is not rotated.

When the antenna is used in an antenna array and the Input Pattern Coordinate System parameter is az-el, selecting this check box rotates the pattern so that the $x$-axis of the element coordinate system points along the array normal. Not selecting uses the element pattern without the rotation.

When the antenna is used in an antenna array and Input Pattern Coordinate System is set to phitheta, selecting this check box rotates the pattern so that the $z$-axis of the element coordinate system points along the array normal.

Use the parameter in conjunction with the Array normal parameter of the URA and UCA arrays.

## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Polar pattern frequencies (Hz) - Polar pattern microphone response frequencies
1 e3 (default) | real scalar | real-valued 1-by-L row vector

Polar pattern microphone response frequencies, specified as a real scalar, or a real-valued, 1-by- $L$ vector. The response frequencies lie within the frequency range specified by the Operating frequency vector $(\mathbf{H z})$ vector.

## Dependencies

To enable this parameter, set Element type set to Custom Microphone.
Polar pattern angles (deg) - Polar pattern response angles
[-180:180] (default) | real-valued -by-P row vector

Specify the polar pattern response angles, as a 1-by- $P$ vector. The angles are measured from the central pickup axis of the microphone and must be between $-180^{\circ}$ and $180^{\circ}$, inclusive.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.
Polar pattern (dB) - Custom microphone polar response
zeros (1,361) (default) | real-valued L-by-P matrix

Specify the magnitude of the custom microphone element polar patterns as an $L$-by- $P$ matrix. $L$ is the number of frequencies specified in Polar pattern frequencies $\mathbf{( H z )} . P$ is the number of angles specified in Polar pattern angles (deg). Each row of the matrix represents the magnitude of the polar pattern measured at the corresponding frequency specified in Polar pattern frequencies (Hz) and all angles specified in Polar pattern angles (deg). The pattern is measured in the azimuth plane. In the azimuth plane, the elevation angle is $0^{\circ}$ and the central pickup axis is $0^{\circ}$ degrees azimuth and $0^{\circ}$ degrees elevation. The polar pattern is symmetric around the central axis. You can construct the microphone response pattern in 3-D space from the polar pattern.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.

## Array Parameters

Geometry - Array geometry
ULA (default) | URA | UCA | Conformal Array

Array geometry, specified as one of

- ULA - Uniform linear array
- URA - Uniform rectangular array
- UCA - Uniform circular array
- Conformal Array - arbitrary element positions

Number of elements - Number of array elements
2 for ULA arrays and 5 for UCA arrays (default) | integer greater than or equal to 2

The number of array elements for ULA or UCA arrays, specified as an integer greater than or equal to 2.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

## Dependencies

To enable this parameter, set Geometry to ULA or UCA.
Element spacing (m) - Spacing between array elements
0.5 for ULA arrays and [0.5,0.5] for URA arrays (default) | positive scalar for ULA or URA arrays | 2 -element vector of positive values for URA arrays

Spacing between adjacent array elements:

- ULA - specify the spacing between two adjacent elements in the array as a positive scalar.
- URA - specify the spacing as a positive scalar or a 1 -by-2 vector of positive values. If Element spacing (m) is a scalar, the row and column spacings are equal. If Element spacing (m) is a vector, the vector has the form [SpacingBetweenArrayRows,SpacingBetweenArrayColumns].
- When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.


## Dependencies

To enable this parameter, set Geometry to ULA or URA.
Array axis - Linear axis direction of ULA
$y$ (default) $|x| z$

Linear axis direction of ULA, specified as $y, x$, or $z$. All ULA array elements are uniformly spaced along this axis in the local array coordinate system.

## Dependencies

- To enable this parameter, set Geometry to ULA.
- This parameter is also enabled when the block only supports ULA arrays.

Array size - Dimensions of URA array
[2, 2] (default) | positive integer | 1-by-2 vector of positive integers

Dimensions of a URA array, specified as a positive integer or 1-by-2 vector of positive integers.

- If Array size is a 1-by-2 vector, the vector has the form [NumberOfArrayRows, NumberOfArrayColumns].
- If Array size is an integer, the array has the same number of rows and columns.
- When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

For a URA, array elements are indexed from top to bottom along the leftmost column, and then continue to the next columns from left to right. In this figure, the Array size value of [3,2] creates an array having three rows and two columns.

## Size and Element Indexing Order

for Uniform Rectangular Arrays
Example: Size $=[3,2]$


## Dependencies

To enable this parameter, set Geometry to URA.
Element lattice - Lattice of URA element positions
Rectangular (default) | Triangular

Lattice of URA element positions, specified as Rectangular or Triangular.

- Rectangular - Aligns all the elements in row and column directions.
- Triangular - Shifts the even-row elements of a rectangular lattice toward the positive row-axis direction. The displacement is one-half the element spacing along the row dimension.


## Dependencies

To enable this parameter, set Geometry to URA.
Array normal - Array normal direction
$x$ for URA arrays or $z$ for UCA arrays (default) | y

Array normal direction, specified as $\mathrm{x}, \mathrm{y}$, or z .

Elements of planar arrays lie in a plane orthogonal to the selected array normal direction. Element boresight directions point along the array normal direction.

| Array Normal Parameter Value | Element Positions and Boresight Directions |
| :--- | :--- |
| $x$ | Array elements lie in the $y z$-plane. All element <br> boresight vectors point along the $x$-axis. |
| $y$ | Array elements lie in the $z x$-plane. All element <br> boresight vectors point along the $y$-axis. |
| $z$ | Array elements lie in the $x y$-plane. All element <br> boresight vectors point along the $z$-axis. |

## Dependencies

To enable this parameter, set Geometry to URA or UCA.
Radius of UCA (m) - UCA array radius
0.5 (default) | positive scalar

Radius of UCA array, specified as a positive scalar.

## Dependencies

To enable this parameter, set Geometry to UCA.
Element positions (m) - Positions of conformal array elements
[0;0;0] (default)| 3-by-Nmatrix of real values

Positions of the elements in a conformal array, specified as a $3-b y-N$ matrix of real values, where $N$ is the number of elements in the conformal array. Each column of this matrix represents the position [ $x ; y ; z$ ] of an array element in the array local coordinate system. The origin of the local coordinate system is $(0,0,0)$. Units are in meters.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

## Dependencies

To enable this parameter set Geometry to Conformal Array.
Element normals (deg) - Direction of conformal array element normal vectors
[0;0]|2-by-1 column vector | 2 -by- $N$ matrix

Direction of element normal vectors in a conformal array, specified as a 2-by-1 column vector or a 2-by- $N$ matrix. $N$ indicates the number of elements in the array. For a matrix, each column specifies the normal direction of the corresponding element in the form [azimuth; elevation] with respect to the local coordinate system. The local coordinate system aligns the positive $x$-axis with the direction normal to the conformal array. If the parameter value is a 2 -by- 1 column vector, the same pointing direction is used for all array elements.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

You can use the Element positions (m) and Element normals (deg) parameters to represent any arrangement in which pairs of elements differ by certain transformations. The transformations can combine translation, azimuth rotation, and elevation rotation. However, you cannot use transformations that require rotation about the normal direction.

## Dependencies

To enable this parameter, set Geometry to Conformal Array.
Taper - Array element tapers
1 (default) | complex-valued scalar | complex-valued row vector

Element tapering, specified as a complex-valued scalar or a complex-valued 1-by- $N$ row vector. In this vector, $N$ represents the number of elements in the array.

Also known as element weights, tapers multiply the array element responses. Tapers modify both amplitude and phase of the response to reduce side lobes or steer the main response axis.

If Taper is a scalar, the same weight is applied to each element. If Taper is a vector, a weight from the vector is applied to the corresponding sensor element. The number of weights must match the number of elements of the array.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

Subarray definition matrix - Define elements belonging to subarrays
logical matrix

Specify the subarray selection as an $M$-by- $N$ matrix. $M$ is the number of subarrays and $N$ is the total number of elements in the array. Each row of the matrix represents a subarray and each entry in the row indicates when an element belongs to the subarray. When the entry is zero, the element does not belong the subarray. A nonzero entry represents a complex-valued weight applied to the corresponding element. Each row must contain at least one nonzero entry.

The phase center of each subarray lies at the subarray geometric center. The subarray geometric center depends on the Subarray definition matrix and Geometry parameters.

## Dependencies

To enable this parameter, set Specify sensor array as to Partitioned array.
Subarray steering method - Specify subarray steering method None (default) | Phase | Time

Subarray steering method, specified as one of

- None
- Phase
- Time
- Custom

Selecting Phase or Time opens the Steer input port on the Narrowband Receive Array, Narrowband Transmit Array, Wideband Receive Array, Wideband Transmit Array blocks, Constant Gamma Clutter, and GPU Constant Gamma Clutter blocks.

Selecting Custom opens the WS input port on the Narrowband Receive Array, Narrowband Transmit Array, Wideband Receive Array, Wideband Transmit Array blocks, Constant Gamma Clutter, and GPU Constant Gamma Clutter blocks.

## Dependencies

To enable this parameter, set Specify sensor array as to Partitioned array or Replicated subarray.

Phase shifter frequency (Hz) - Subarray phase shifting frequency
3.0 e 8 (default) | positive real-valued scalar

Operating frequency of subarray steering phase shifters, specified as a positive real-valued scalar. Units are Hz.

## Dependencies

To enable this parameter, set Sensor array to Partitioned array or Replicated subarray and set Subarray steering method to Phase.

Number of bits in phase shifters - Subarray steering phase shift quantization bits
0 (default) | non-negative integer

Subarray steering phase shift quantization bits, specified as a non-negative integer. A value of zero indicates that no quantization is performed.

## Dependencies

To enable this parameter, set Sensor array to Partitioned array or Replicated subarray and set Subarray steering method to Phase.

Subarrays layout - Subarray position specification
Rectangular (default) | Custom

Specify the layout of replicated subarrays as Rectangular or Custom.

- When you set this parameter to Rectangular, use the Grid size and Grid spacing parameters to place the subarrays.
- When you set this parameter to Custom, use the Subarray positions (m) and Subarray normals parameters to place the subarrays.

Dependencies
To enable this parameter, set Sensor array to Replicated subarray
Grid size - Dimensions of rectangular subarray grid
[1,2] (default)

Rectangular subarray grid size, specified as a single positive integer, or a 1-by-2 row vector of positive integers.

If Grid size is an integer scalar, the array has an equal number of subarrays in each row and column. If Grid size is a 1-by-2 vector of the form [NumberOfRows, NumberOfColumns], the first entry is the number of subarrays along each column. The second entry is the number of subarrays in each row. A row is along the local $y$-axis, and a column is along the local $z$-axis. The figure here shows how you can replicate a 3-by-2 URA subarray using a Grid size of [1,2].
$3 \times 2$ Element URA
Replicated on a $1 \times 2$ Grid


## Dependencies

To enable this parameter, set Sensor array to Replicated subarray and Subarrays layout to Rectangular.

Grid spacing ( $\mathbf{m}$ ) - Spacing between subarrays on rectangular grid
Auto (default) | positive real-valued scalar | 1-by-2 vector of positive real-values

The rectangular grid spacing of subarrays, specified as a positive, real-valued scalar, a 1-by-2 row vector of positive, real-values, or Auto. Units are in meters.

- If Grid spacing is a scalar, the spacing along the row and the spacing along the column is the same.
- If Grid spacing is a 1-by-2 row vector, the vector has the form [SpacingBetweenRows, SpacingBetweenColumn]. The first entry specifies the spacing between rows along a column. The second entry specifies the spacing between columns along a row.
- If Grid spacing is set to Auto, replication preserves the element spacing of the subarray for both rows and columns while building the full array. This option is available only when you specify Geometry as ULA or URA.


## Dependencies

To enable this parameter, set Sensor array to Replicated subarray and Subarrays layout to Rectangular.

Subarray positions (m) - Positions of subarrays
[0,0;0.5,0.5;0,0] (default) | 3 -by- $N$ real-valued matrix

Positions of the subarrays in the custom grid, specified as a real 3-by- $N$ matrix, where $N$ is the number of subarrays in the array. Each column of the matrix represents the position of a single subarray in the array local coordinate system. The coordinates are expressed in the form [x; y; z]. Units are in meters.

Dependencies
To enable this parameter, set Sensor array to Replicated subarray and Subarrays layout to Custom.

Subarray normals - Direction of subarray normal vectors
[0,0;0,0] (default)| 2-by- $N$ real matrix

Specify the normal directions of the subarrays in the array. This parameter value is a 2 -by- $N$ matrix, where $N$ is the number of subarrays in the array. Each column of the matrix specifies the normal direction of the corresponding subarray, in the form [azimuth; elevation]. Angle units are in degrees. Angles are defined with respect to the local coordinate system.

You can use the Subarray positions and Subarray normals parameters to represent any arrangement in which pairs of subarrays differ by certain transformations. The transformations can combine translation, azimuth rotation, and elevation rotation. However, you cannot use transformations that require rotation about the normal.

## Dependencies

To enable this parameter, set the Sensor array parameter to Replicated subarray and the Subarrays layout to Custom.

## Version History <br> Introduced in R2014b

## See Also

phased.MVDRBeamformer

## MUSIC Spectrum

MUSIC 2D spatial spectrum estimator

## Libraries:

Phased Array System Toolbox / Direction of Arrival

## Description

The MUSIC Spectrum block uses the MUltiple SIgnal Classification (MUSIC) algorithm to estimate the spatial spectrum of incoming narrowband signals. The block optionally calculates the direction of arrival of a specified number of signals by finding the peaks of the spectrum.

## Ports

## Input

Port 1 - Received signal
$M$-by- $N$ complex-valued matrix
Received signal, specified as an $M$-by- $N$ complex-valued matrix. The quantity $M$ is the length of the signal, the number of sample values contained in the signal. The quantity $N$ is the number of sensor elements in the array.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
Data Types: double

## Output

Y - MUSIC 2-D spatial spectrum
non-negative real-valued $P$-by- $Q$ matrix
2-D MUSIC spatial spectrum, returned as a non-negative, returned as a real-valued $P$-by- $Q$ matrix. Each entry represents the magnitude of the estimated MUSIC spatial spectrum. Each entry corresponds to an angle specified by the Azimuth scan angles (deg) and Elevation scan angles (deg) parameters. $P$ equals the length of the vector specified in Azimuth scan angles (deg) and $Q$ equals the length of the vector specified in Elevation scan angles (deg).

Data Types: double
Ang - Directions of arrival
non-negative, real-valued 2-by-L matrix
Directions of arrival of the signals, returned as a real-valued 2-by- $L$ matrix. $L$ is the number of signals specified by the Number of signals parameter. The direction of arrival angle is defined by the azimuth and elevation angles of the source with respect to the array local coordinate system. The first row of the matrix contains the azimuth angles and the second row contains the elevation angles. If the object cannot identify peaks in the spectrum, it will return NaN. Angle units are in degrees.

## Dependencies

Select the Enable DOA output parameter to enable this output port.
Data Types: double

## Parameters

Main Tab
Signal propagation speed (m/s) - Signal propagation speed
physconst('LightSpeed') (default) | real-valued positive scalar

Signal propagation speed, specified as a real-valued positive scalar. The default value of the speed of light is the value returned by physconst('LightSpeed '). Units are in meters per second.

## Example: 3e8

Data Types: double
Operating frequency (Hz) - System operating frequency
3e8 (default) | positive real scalar

System operating frequency, specified as a positive scalar. Units are in Hz .
Forward-backward averaging - Enable forward-backward averaging
off (default) | on

Select this parameter to use forward-backward averaging to estimate the covariance matrix for sensor arrays with a conjugate symmetric array manifold structure.

Azimuth scan angles (deg) - Azimuth scan angles
-90:90 (default) | real-valued scalar | real-valued row vector

Azimuth scan angles, specified as a real-valued row vector. The angle values must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive, and specified in ascending order. Angle units are in degrees.

Elevation scan angles (deg) - Elevation scan angles
0 (default) | real-valued scalar | real-valued row vector

Elevation scan angles, specified as a scalar or real-valued row vector. The angle values must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive, and specified in ascending order. Angle units are in degrees.

Enable DOA output - Output directions of arrival through output port off (default) | on

Select this parameter to output the signals directions of arrival (DOA) through the Ang output port.
Number of signals - Expected number of arriving signals
1 (default) | positive integer

Specify the expected number of signals for DOA estimation as a positive scalar integer.
Simulate using - Block simulation method
Interpreted Execution (default) |Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).

## Programmatic Use

Block Parameter:SimulateUsing
Type:enum
Values:Interpreted Execution, Code Generation
Default:Interpreted Execution

## Sensor Array Tab

Specify sensor array as - Method to specify array
Array (no subarrays) (default)|MATLAB expression

Method to specify array, specified as Array (no subarrays) or MATLAB expression.

- Array (no subarrays) - use the block parameters to specify the array.
- MATLAB expression - create the array using a MATLAB expression.

Expression - MATLAB expression used to create an array
Phased Array System Toolbox array System object

MATLAB expression used to create an array, specified as a valid Phased Array System Toolbox array System object.

Example: phased.URA('Size', [5,3])

## Dependencies

To enable this parameter, set Specify sensor array as to MATLAB expression.

## Element Parameters

Element type - Array element types
Isotropic Antenna (default)|Cosine Antenna|Custom Antenna|Omni Microphone|
Custom Microphone

Antenna or microphone type, specified as one of the following:

- Isotropic Antenna
- Cosine Antenna
- Custom Antenna
- Omni Microphone
- Custom Microphone

Operating frequency range (Hz) - Operating frequency range of the antenna or microphone element
[0,1e20] (default) | real-valued 1-by-2 row vector

Specify the operating frequency range of the antenna or microphone element as a 1-by-2 row vector in the form [LowerBound, UpperBound]. The element has no response outside this frequency range. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Isotropic Antenna, Cosine Antenna, or Omni Microphone.

Operating frequency vector ( $\mathbf{H z}$ ) - Operating frequency range of custom antenna or microphone elements
[0,1e20] (default) | real-valued row vector

Specify the frequencies at which to set antenna and microphone frequency responses as a 1-by-L row vector of increasing real values. The antenna or microphone element has no response outside the frequency range specified by the minimum and maximum elements of this vector. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone. Use Frequency responses (dB) to set the responses at these frequencies.

Baffle the back of the element - Set back response of an Isotropic Antenna element or an Omni Microphone element to zero
off (default) | on

Select this check box to baffle the back response of the element. When back baffled, the responses at all azimuth angles beyond $\pm 90^{\circ}$ from broadside are set to zero. The broadside direction is defined as $0^{\circ}$ azimuth angle and $0^{\circ}$ elevation angle.

## Dependencies

To enable this check box, set Element type to Isotropic Antenna or Omni Microphone.
Exponent of cosine pattern - Exponents of azimuth and elevation cosine patterns
[1.5 1.5] (default) | nonnegative scalar | real-valued 1-by-2 matrix of nonnegative values

Specify the exponents of the cosine pattern as a nonnegative scalar or a real-valued 1-by-2 matrix of nonnegative values. When Exponent of cosine pattern is a 1-by-2 vector, the first element is the exponent in the azimuth direction and the second element is the exponent in the elevation direction. When you set this parameter to a scalar, both the azimuth direction and elevation direction cosine patterns are raised to the same power.

## Dependencies

To enable this parameter, set Element type to Cosine Antenna.
Frequency responses (dB) - Antenna and microphone frequency response
[0,0] (default) | real-valued row vector

Frequency response of a custom antenna or custom microphone for the frequencies defined by the Operating frequency vector ( Hz ) parameter. The dimensions of Frequency responses (dB) must match the dimensions of the vector specified by the Operating frequency vector $(\mathbf{H z})$ parameter.

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone.
Input Pattern Coordinate System - Coordinate system of custom antenna pattern
az-el (default)|phi-theta

Coordinate system of custom antenna pattern, specified az-el or phi-theta. When you specify azel, use the Azimuth angles (deg) and Elevations angles (deg) parameters to specify the coordinates of the pattern points. When you specify phi-theta, use the Phi angles (deg) and Theta angles (deg) parameters to specify the coordinates of the pattern points.

## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Azimuth angles (deg) - Azimuth angles of antenna radiation pattern
[-180:180] (default) | real-valued row vector

Specify the azimuth angles at which to calculate the antenna radiation pattern as a 1-by- $P$ row vector. $P$ must be greater than 2. Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to az-el.

Elevation angles (deg) - Elevation angles of antenna radiation pattern
[-90:90] (default) | real-valued row vector

Specify the elevation angles at which to compute the radiation pattern as a 1-by- $Q$ vector. $Q$ must be greater than 2. Angle units are in degrees. Elevation angles must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to az-el.

Phi Angles (deg) - Phi angle coordinates of custom antenna radiation pattern
$0: 360$ | real-valued 1-by-P row vector

Phi angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by-P row vector. $P$ must be greater than 2 . Angle units are in degrees. Phi angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Theta Angles (deg) - Theta angle coordinates of custom antenna radiation pattern 0 : 180 | real-valued 1-by- $Q$ row vector

Theta angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by$Q$ row vector. $Q$ must be greater than 2 . Angle units are in degrees. Theta angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Magnitude pattern (dB) - Magnitude of combined antenna radiation pattern
zeros $(181,361)$ (default) | real-valued $Q$-by- $P$ matrix | real-valued $Q$-by- $P$-by- $L$ array

Magnitude of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector ( $\mathbf{H z}$ ).

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector (Hz) parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (Hz) parameter.


## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Phase pattern (deg) - Custom antenna radiation phase pattern
zeros (181,361) (default) | real-valued $Q$-by-P matrix | real-valued $Q$-by-P-by-L array

Phase of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector $(\mathbf{H z})$.

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (

Dependencies
To enable this parameter, set Element type to Custom Antenna.
MatchArrayNormal - Rotate antenna element to array normal on (default) | off

Select this check box to rotate the antenna element pattern to align with the array normal. When not selected, the element pattern is not rotated.

When the antenna is used in an antenna array and the Input Pattern Coordinate System parameter is az-el, selecting this check box rotates the pattern so that the $x$-axis of the element coordinate system points along the array normal. Not selecting uses the element pattern without the rotation.

When the antenna is used in an antenna array and Input Pattern Coordinate System is set to phitheta, selecting this check box rotates the pattern so that the $z$-axis of the element coordinate system points along the array normal.

Use the parameter in conjunction with the Array normal parameter of the URA and UCA arrays.

## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Polar pattern frequencies (Hz) - Polar pattern microphone response frequencies
1e3 (default) | real scalar | real-valued 1-by-L row vector

Polar pattern microphone response frequencies, specified as a real scalar, or a real-valued, 1-by-L vector. The response frequencies lie within the frequency range specified by the Operating frequency vector $(\mathrm{Hz})$ vector.

## Dependencies

To enable this parameter, set Element type set to Custom Microphone.
Polar pattern angles (deg) - Polar pattern response angles
[-180:180] (default) | real-valued -by-P row vector

Specify the polar pattern response angles, as a 1-by- $P$ vector. The angles are measured from the central pickup axis of the microphone and must be between $-180^{\circ}$ and $180^{\circ}$, inclusive.

Dependencies
To enable this parameter, set Element type to Custom Microphone.
Polar pattern (dB) - Custom microphone polar response
zeros ( 1,361 ) (default) | real-valued $L$-by- $P$ matrix

Specify the magnitude of the custom microphone element polar patterns as an $L$-by- $P$ matrix. $L$ is the number of frequencies specified in Polar pattern frequencies ( $\mathbf{H z}$ ). $P$ is the number of angles specified in Polar pattern angles (deg). Each row of the matrix represents the magnitude of the polar pattern measured at the corresponding frequency specified in Polar pattern frequencies (Hz) and all angles specified in Polar pattern angles (deg). The pattern is measured in the azimuth plane. In the azimuth plane, the elevation angle is $0^{\circ}$ and the central pickup axis is $0^{\circ}$ degrees azimuth and $0^{\circ}$ degrees elevation. The polar pattern is symmetric around the central axis. You can construct the microphone response pattern in 3-D space from the polar pattern.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.

## Array Parameters

Geometry - Array geometry
ULA (default) | URA | UCA | Conformal Array

Array geometry, specified as one of

- ULA - Uniform linear array
- URA - Uniform rectangular array
- UCA - Uniform circular array
- Conformal Array - arbitrary element positions

Number of elements - Number of array elements
2 for ULA arrays and 5 for UCA arrays (default) | integer greater than or equal to 2

The number of array elements for ULA or UCA arrays, specified as an integer greater than or equal to 2.

## Dependencies

To enable this parameter, set Geometry to ULA or UCA.
Element spacing (m) - Spacing between array elements
0.5 for ULA arrays and [0.5,0.5] for URA arrays (default) | positive scalar for ULA or URA arrays | 2 -element vector of positive values for URA arrays

Spacing between adjacent array elements:

- ULA - specify the spacing between two adjacent elements in the array as a positive scalar.
- URA - specify the spacing as a positive scalar or a 1 -by-2 vector of positive values. If Element spacing (m) is a scalar, the row and column spacings are equal. If Element spacing (m) is a vector, the vector has the form [SpacingBetweenArrayRows,SpacingBetweenArrayColumns].


## Dependencies

To enable this parameter, set Geometry to ULA or URA.
Array axis - Linear axis direction of ULA
$y$ (default) $|x| z$

Linear axis direction of ULA, specified as $y, x$, or $z$. All ULA array elements are uniformly spaced along this axis in the local array coordinate system.

## Dependencies

- To enable this parameter, set Geometry to ULA.
- This parameter is also enabled when the block only supports ULA arrays.

Array size - Dimensions of URA array
[2,2] (default) | positive integer | 1-by-2 vector of positive integers

Dimensions of a URA array, specified as a positive integer or 1-by-2 vector of positive integers.

- If Array size is a 1 -by- 2 vector, the vector has the form [NumberOfArrayRows, NumberOfArrayColumns].
- If Array size is an integer, the array has the same number of elements in each row and column.

For a URA, array elements are indexed from top to bottom along the leftmost array column, and continued to the next columns from left to right. In this figure, the Array size value of [3,2] creates an array having three rows and two columns.

## Size and Element Indexing Order

for Uniform Rectangular Arrays
Example: Size $=[3,2]$


## Dependencies

To enable this parameter, set Geometry to URA.
Element lattice - Lattice of URA element positions
Rectangular (default) | Triangular

Lattice of URA element positions, specified as Rectangular or Triangular.

- Rectangular - Aligns all the elements in row and column directions.
- Triangular - Shifts the even-row elements of a rectangular lattice toward the positive row-axis direction. The displacement is one-half the element spacing along the row dimension.


## Dependencies

To enable this parameter, set Geometry to URA.
Array normal - Array normal direction
$x$ for URA arrays or $z$ for UCA arrays (default) | y

Array normal direction, specified as $x, y$, or $z$.
Elements of planar arrays lie in a plane orthogonal to the selected array normal direction. Element boresight directions point along the array normal direction.

| Array Normal Parameter Value | Element Positions and Boresight Directions |
| :--- | :--- |
| $x$ | Array elements lie in the $y z$-plane. All element <br> boresight vectors point along the $x$-axis. |
| $y$ | Array elements lie in the $z x$-plane. All element <br> boresight vectors point along the $y$-axis. |
| $z$ | Array elements lie in the $x y$-plane. All element <br> boresight vectors point along the $z$-axis. |

## Dependencies

To enable this parameter, set Geometry to URA or UCA.

## Radius of UCA (m) - UCA array radius

0.5 (default) | positive scalar

Radius of UCA array, specified as a positive scalar.

## Dependencies

To enable this parameter, set Geometry to UCA.
Element positions (m) - Positions of conformal array elements
[0;0;0] (default) | 3-by-Nmatrix of real values

Positions of the elements in a conformal array, specified as a 3 -by- $N$ matrix of real values, where $N$ is the number of elements in the conformal array. Each column of this matrix represents the position [ $x ; y ; z$ ] of an array element in the array local coordinate system. The origin of the local coordinate system is ( $0,0,0$ ). Units are in meters.

## Dependencies

To enable this parameter set Geometry to Conformal Array.

## Data Types: double

Element normals (deg) - Direction of conformal array element normal vectors
[ $0 ; 0$ ] | 2 -by-1 column vector | 2 -by- $N$ matrix

Direction of element normal vectors in a conformal array, specified as a 2-by-1 column vector or a 2-by- $N$ matrix. $N$ indicates the number of elements in the array. If the parameter value is a matrix, each column specifies the normal direction of the corresponding element in the form
[azimuth; elevation] with respect to the local coordinate system. The local coordinate system aligns the positive $x$-axis with the direction normal to the conformal array. If the parameter value is a 2 -by-1 column vector, the same pointing direction is used for all array elements.

You can use the Element positions (m) and Element normals (deg) parameters to represent any arrangement in which pairs of elements differ by certain transformations. The transformations can combine translation, azimuth rotation, and elevation rotation. However, you cannot use transformations that require rotation about the normal direction.

To enable this parameter, set Geometry to Conformal Array.

Data Types: double
Taper - Array element tapers
1 (default) | complex scalar | complex-valued row vector

Specify element tapering as a complex-valued scalar or a complex-valued 1-by- $N$ row vector. In this vector, $N$ represents the number of elements in the array.

Also known as element weights, tapers multiply the array element responses. Tapers modify both amplitude and phase of the response to reduce side lobes or steer the main response axis.

If Taper is a scalar, the same weight is applied to each element. If Taper is a vector, a weight from the vector is applied to the corresponding sensor element. The number of weights must match the number of elements of the array.
Data Types: double

## Version History

Introduced in R2016b

## See Also

## Blocks

ULA MUSIC Spectrum
Objects
phased.MUSICEstimator2D | phased.MUSICEstimator|phased.ConformalArray| phased.UCA|phased.ULA|phased.URA

Functions
musicdoa

## Topics

"MUSIC Super-Resolution DOA Estimation"

## MVDR Spectrum

Minimum variation distortionless response (MVDR) spatial spectrum estimator


## Libraries:

Phased Array System Toolbox / Direction of Arrival

## Description

The narrowband MVDR Spectrum block estimates the spatial spectrum of incoming narrowband signals by scanning a range of azimuth and elevation angles using an MVDR conventional beamformer. The block optionally calculates the direction of arrival of a specified number of signals by estimating the peaks of the spectrum. This estimator is also referred to as a Capon estimator.

## Ports

## Input

In - Input data
complex-valued matrix
Input data, specified as a complex-valued matrix whose columns correspond to channels. Rows correspond to samples.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

## Data Types: double | single

## Output

$\mathbf{Y}$ - Two-dimensional spatial spectrum
real-valued matrix
Spatial spectrum, returned as a real-valued matrix representing the magnitude of the estimated 2-D spatial spectrum. The row dimension of $Y$ is equal to the number of angles in the Elevation scan angles (deg) parameter and the column dimension of $Y$ is equal to the number of angles in the Azimuth scan angles (deg) parameter.
Data Types: double
Ang - Estimated direction of arrival
two-row real-valued matrix
Estimated direction of arrival, returned as a two-row real-valued matrix where the first row represents estimated azimuth angles and the second row represents estimated elevation angles. Units are in degrees.

## Dependencies

To enable this port, select the Enable DOA output check box.

Data Types: double

## Parameters

## Main Tab

Signal propagation speed (m/s) - Signal propagation speed
physconst('LightSpeed') (default)| real-valued positive scalar

Signal propagation speed, specified as a real-valued positive scalar. The default value of the speed of light is the value returned by physconst ('LightSpeed '). Units are in meters per second.

Example: 3e8
Data Types: double
Operating frequency ( Hz ) - System operating frequency
3e8 (default) | positive real scalar

System operating frequency, specified as a positive scalar. Units are in Hz .
Number of bits in phase shifters - Number of phase shift quantization bits
0 (default) | nonnegative integer

The number of bits used to quantize the phase shift component of beamformer or steering vector weights. Specify the number of bits as a non-negative integer. A value of zero indicates that no quantization is performed.

Forward-backward averaging - Enable forward-backward averaging off (default) | on

Select this parameter to use forward-backward averaging to estimate the covariance matrix for sensor arrays with a conjugate symmetric array manifold structure.

Azimuth scan angles (deg) - Azimuth scan angles
-90:90 (default)
Specify the azimuth scan angles, in degrees, as a real vector. The angles must be between $-180^{\circ}$ and $180^{\circ}$, inclusive. You must specify the angles in ascending order.

Elevation scan angles (deg) - Elevation scan angles
0 (default)
Specify the elevation scan angles, in degrees, as a real vector or scalar. The angles must be between $90^{\circ}$ and $90^{\circ}$, inclusive. You must specify the angles in an ascending order.

Enable DOA output - Output directions of arrival through output port
off (default) | on

Select this parameter to output the signals directions of arrival (DOA) through the Ang output port.
Number of signals - Expected number of arriving signals
1 (default) | positive integer

Specify the expected number of signals for DOA estimation as a positive scalar integer.
Simulate using - Block simulation method
Interpreted Execution (default)|Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).
Programmatic Use
Block Parameter:SimulateUsing
Type:enum
Values:Interpreted Execution, Code Generation
Default:Interpreted Execution
Expression - MATLAB expression used to create an array
Phased Array System Toolbox array System object

MATLAB expression used to create an array, specified as a valid Phased Array System Toolbox array System object.

Example: phased.URA('Size', [5,3])

## Dependencies

To enable this parameter, set Specify sensor array as to MATLAB expression.

## Sensor Array Tab

Specify sensor array as - Method to specify array
Array (no subarrays) (default)|MATLAB expression

Method to specify array, specified as Array (no subarrays) or MATLAB expression.

- Array (no subarrays) - use the block parameters to specify the array.
- MATLAB expression - create the array using a MATLAB expression.


## Element Parameters

Element type - Array element types
Isotropic Antenna (default)|Cardioid Antenna|Cosine Antenna|Custom Antenna| Gaussian Antenna|Sinc Antenna|Omni Microphone|Custom Microphone

Antenna or microphone type, specified as one of the following:

- Isotropic Antenna
- Cardioid Antenna
- Cosine Antenna
- Custom Antenna
- Gaussian Antenna
- Sinc Antenna
- Omni Microphone
- Custom Microphone

Operating frequency range $(\mathbf{H z})$ - Operating frequency range of the antenna or microphone element
[0,1e20] (default) | real-valued 1-by-2 row vector

Specify the operating frequency range of the antenna or microphone element as a 1 -by-2 row vector in the form [LowerBound, UpperBound]. The element has no response outside this frequency range. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Isotropic Antenna, Cosine Antenna, or Omni Microphone.

Baffle the back of the element - Set back response of an Isotropic Antenna element or an Omni Microphone element to zero off (default) | on

Select this check box to baffle the back response of the element. When back baffled, the responses at all azimuth angles beyond $\pm 90^{\circ}$ from broadside are set to zero. The broadside direction is defined as $0^{\circ}$ azimuth angle and $0^{\circ}$ elevation angle.

## Dependencies

To enable this check box, set Element type to Isotropic Antenna or Omni Microphone.
Null axis direction - Null axis direction
$-x$ (default) $|+x|+y|-y|+z \mid-z$

## Dependencies

To enable this parameter, set Element type to Cardioid Antenna.
Exponent of cosine pattern - Exponents of azimuth and elevation cosine patterns [1.5 1.5] (default) | nonnegative scalar | real-valued 1-by-2 matrix of nonnegative values

Specify the exponents of the cosine pattern as a nonnegative scalar or a real-valued 1-by-2 matrix of nonnegative values. When Exponent of cosine pattern is a 1-by-2 vector, the first element is the exponent in the azimuth direction and the second element is the exponent in the elevation direction. When you set this parameter to a scalar, both the azimuth direction and elevation direction cosine patterns are raised to the same power.

## Dependencies

To enable this parameter, set Element type to Cosine Antenna.
Operating frequency vector ( Hz ) - Operating frequency range of custom antenna or microphone elements
[0,1e20] (default) | real-valued row vector

Specify the frequencies at which to set antenna and microphone frequency responses as a 1-by-L row vector of increasing real values. The antenna or microphone element has no response outside the frequency range specified by the minimum and maximum elements of this vector. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone. Use Frequency responses (dB) to set the responses at these frequencies.

Frequency responses (dB) - Antenna and microphone frequency response [0,0] (default) | real-valued row vector

Frequency response of a custom antenna or custom microphone for the frequencies defined by the Operating frequency vector ( $\mathbf{H z}$ ) parameter. The dimensions of Frequency responses (dB) must match the dimensions of the vector specified by the Operating frequency vector (Hz) parameter.

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone.

Input Pattern Coordinate System - Coordinate system of custom antenna pattern
az-el (default)|phi-theta

Coordinate system of custom antenna pattern, specified az-el or phi-theta. When you specify azel, use the Azimuth angles (deg) and Elevations angles (deg) parameters to specify the coordinates of the pattern points. When you specify phi-theta, use the Phi angles (deg) and Theta angles (deg) parameters to specify the coordinates of the pattern points.

Dependencies
To enable this parameter, set Element type to Custom Antenna.
Azimuth angles (deg) - Azimuth angles of antenna radiation pattern
[-180:180] (default) | real-valued row vector

Specify the azimuth angles at which to calculate the antenna radiation pattern as a 1-by-P row vector. $P$ must be greater than 2. Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input
Pattern Coordinate System parameter to az-el.
Elevation angles (deg) - Elevation angles of antenna radiation pattern
[-90:90] (default) | real-valued row vector

Specify the elevation angles at which to compute the radiation pattern as a 1-by- $Q$ vector. $Q$ must be greater than 2. Angle units are in degrees. Elevation angles must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to az-el.

Phi Angles (deg) - Phi angle coordinates of custom antenna radiation pattern $0: 360$ | real-valued 1 -by- P row vector

Phi angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by-P row vector. $P$ must be greater than 2 . Angle units are in degrees. Phi angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Theta Angles (deg) - Theta angle coordinates of custom antenna radiation pattern $0: 180$ | real-valued 1-by- $Q$ row vector

Theta angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by$Q$ row vector. $Q$ must be greater than 2. Angle units are in degrees. Theta angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Magnitude pattern (dB) - Magnitude of combined antenna radiation pattern zeros $(181,361)$ (default) | real-valued $Q$-by-P matrix | real-valued $Q$-by-P-by-L array

Magnitude of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector ( $\mathbf{H z}$ ).

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathrm{Hz})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (Hz) parameter.


## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Phase pattern (deg) - Custom antenna radiation phase pattern
zeros $(181,361)$ (default) | real-valued $Q$-by-P matrix | real-valued $Q$-by-P-by-L array

Phase of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector $(\mathbf{H z})$.

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector (Hz) parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (


## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Align element normal with array normal - Align element normal with array normal on (default) | off

## Dependencies

This parameter is enabled when Element type is set to Custom Antenna.
Radiation pattern beamwidth (deg) - Radiation pattern beamwidth
[10,10] (default)

## Dependencies

This parameter is enabled when Element type is set to Gaussian Antenna.
Polar pattern frequencies (Hz) - Polar pattern microphone response frequencies
1e3 (default) | real scalar | real-valued 1-by-L row vector

Polar pattern microphone response frequencies, specified as a real scalar, or a real-valued, 1-by-L vector. The response frequencies lie within the frequency range specified by the Operating
frequency vector (Hz) vector.

## Dependencies

To enable this parameter, set Element type set to Custom Microphone.
Polar pattern angles (deg) - Polar pattern response angles
[ - 180: 180] (default) | real-valued -by-P row vector

Specify the polar pattern response angles, as a 1-by- $P$ vector. The angles are measured from the central pickup axis of the microphone and must be between $-180^{\circ}$ and $180^{\circ}$, inclusive.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.
Polar pattern (dB) - Custom microphone polar response
zeros $(1,361)$ (default) | real-valued $L$-by-P matrix

Specify the magnitude of the custom microphone element polar patterns as an $L$-by- $P$ matrix. $L$ is the number of frequencies specified in Polar pattern frequencies $(\mathbf{H z}) . P$ is the number of angles specified in Polar pattern angles (deg). Each row of the matrix represents the magnitude of the polar pattern measured at the corresponding frequency specified in Polar pattern frequencies $(\mathbf{H z})$ and all angles specified in Polar pattern angles (deg). The pattern is measured in the azimuth plane. In the azimuth plane, the elevation angle is $0^{\circ}$ and the central pickup axis is $0^{\circ}$ degrees azimuth and $0^{\circ}$ degrees elevation. The polar pattern is symmetric around the central axis. You can construct the microphone response pattern in 3-D space from the polar pattern.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.

## Array Parameters

Geometry - Array geometry
ULA (default) | URA | UCA | Conformal Array

Array geometry, specified as one of

- ULA - Uniform linear array
- URA - Uniform rectangular array
- UCA - Uniform circular array
- Conformal Array - arbitrary element positions

Number of elements - Number of array elements
2 for ULA arrays and 5 for UCA arrays (default) | integer greater than or equal to 2

The number of array elements for ULA or UCA arrays, specified as an integer greater than or equal to 2.

## Dependencies

To enable this parameter, set Geometry to ULA or UCA.
Element spacing (m) - Spacing between array elements
0.5 for ULA arrays and [0.5,0.5] for URA arrays (default) | positive scalar for ULA or URA arrays | 2-element vector of positive values for URA arrays

Spacing between adjacent array elements:

- ULA - specify the spacing between two adjacent elements in the array as a positive scalar.
- URA - specify the spacing as a positive scalar or a 1-by-2 vector of positive values. If Element spacing (m) is a scalar, the row and column spacings are equal. If Element spacing (m) is a vector, the vector has the form [SpacingBetweenArrayRows, SpacingBetweenArrayColumns].


## Dependencies

To enable this parameter, set Geometry to ULA or URA.
Array axis - Linear axis direction of ULA
$y$ (default) $|x| z$

Linear axis direction of ULA, specified as $y, x$, or $z$. All ULA array elements are uniformly spaced along this axis in the local array coordinate system.

## Dependencies

- To enable this parameter, set Geometry to ULA.
- This parameter is also enabled when the block only supports ULA arrays.

Array size - Dimensions of URA array
[2,2] (default) | positive integer | 1-by-2 vector of positive integers

Dimensions of a URA array, specified as a positive integer or 1-by-2 vector of positive integers.

- If Array size is a 1-by-2 vector, the vector has the form [Number0fArrayRows, NumberOfArrayColumns].
- If Array size is an integer, the array has the same number of elements in each row and column.

For a URA, array elements are indexed from top to bottom along the leftmost array column, and continued to the next columns from left to right. In this figure, the Array size value of [3, 2] creates an array having three rows and two columns.

## Size and Element Indexing Order

for Uniform Rectangular Arrays
Example: Size $=[3,2]$


## Dependencies

To enable this parameter, set Geometry to URA.
Element lattice - Lattice of URA element positions
Rectangular (default) | Triangular

Lattice of URA element positions, specified as Rectangular or Triangular.

- Rectangular - Aligns all the elements in row and column directions.
- Triangular - Shifts the even-row elements of a rectangular lattice toward the positive row-axis direction. The displacement is one-half the element spacing along the row dimension.


## Dependencies

To enable this parameter, set Geometry to URA.

Array normal - Array normal direction
x for URA arrays or $z$ for UCA arrays (default) | y

Array normal direction, specified as $x, y$, or $z$.
Elements of planar arrays lie in a plane orthogonal to the selected array normal direction. Element boresight directions point along the array normal direction.

| Array Normal Parameter Value | Element Positions and Boresight Directions |
| :--- | :--- |
| $x$ | Array elements lie in the $y z$-plane. All element <br> boresight vectors point along the $x$-axis. |
| $y$ | Array elements lie in the $z x$-plane. All element <br> boresight vectors point along the $y$-axis. |
| $z$ | Array elements lie in the $x y$-plane. All element <br> boresight vectors point along the $z$-axis. |

## Dependencies

To enable this parameter, set Geometry to URA or UCA.
Radius of UCA ( $\mathbf{m}$ ) - UCA array radius
0.5 (default) | positive scalar

Radius of UCA array, specified as a positive scalar.

## Dependencies

To enable this parameter, set Geometry to UCA.
Element positions (m) - Positions of conformal array elements [0;0;0] (default) | 3 -by-Nmatrix of real values

Positions of the elements in a conformal array, specified as a 3 -by- $N$ matrix of real values, where $N$ is the number of elements in the conformal array. Each column of this matrix represents the position [ $x ; y ; z$ ] of an array element in the array local coordinate system. The origin of the local coordinate system is $(0,0,0)$. Units are in meters.

## Dependencies

To enable this parameter set Geometry to Conformal Array.
Data Types: double
Element normals (deg) - Direction of conformal array element normal vectors
[0;0] | 2-by-1 column vector | 2-by-N matrix

Direction of element normal vectors in a conformal array, specified as a 2-by-1 column vector or a 2-by- $N$ matrix. $N$ indicates the number of elements in the array. If the parameter value is a matrix, each column specifies the normal direction of the corresponding element in the form [azimuth; elevation] with respect to the local coordinate system. The local coordinate system
aligns the positive $x$-axis with the direction normal to the conformal array. If the parameter value is a 2-by-1 column vector, the same pointing direction is used for all array elements.

You can use the Element positions (m) and Element normals (deg) parameters to represent any arrangement in which pairs of elements differ by certain transformations. The transformations can combine translation, azimuth rotation, and elevation rotation. However, you cannot use transformations that require rotation about the normal direction.

To enable this parameter, set Geometry to Conformal Array.
Data Types: double
Taper - Array element tapers
1 (default) | complex scalar | complex-valued row vector

Specify element tapering as a complex-valued scalar or a complex-valued 1-by- $N$ row vector. In this vector, $N$ represents the number of elements in the array.

Also known as element weights, tapers multiply the array element responses. Tapers modify both amplitude and phase of the response to reduce side lobes or steer the main response axis.

If Taper is a scalar, the same weight is applied to each element. If Taper is a vector, a weight from the vector is applied to the corresponding sensor element. The number of weights must match the number of elements of the array.

Data Types: double

# Version History 

Introduced in R2014b

## See Also

phased.MVDREstimator2D

## Narrowband Receive Array

Receive narrowband radiation using phased array


## Libraries:

Phased Array System Toolbox / Transmitters and Receivers

## Description

The Narrowband Receive Array block implements a narrowband receive array collecting incoming radiation. The array processes narrowband plane waves incident on the sensor elements of the array. The delay at each element is approximated using the corresponding phase shift in the time domain.

## Ports

Input
X - Incident signals
complex-valued $M$-by-Lmatrix
Incident signals, specified as a complex-valued $M$-by- $L$ matrix, where $M$ is the number of samples in the data, and $L$ is the number of incident signals. Each column of $X$ is a far field signal.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
Data Types: double | single
Ang - Incident signal directions
2-by-1 real-valued vector | 2-by-L real-valued matrix
Incident directions of signals, specified as a real-valued 2-by-L matrix. Each column specifies the incident direction of the corresponding column of $X$ and takes the form [azimuth; elevation]. Units are in degrees. The azimuth angle must lie in the range from $-180^{\circ}$ to $180^{\circ}$, inclusive. The elevation angle must lie in the range from $-90^{\circ}$ to $90^{\circ}$, inclusive.
Data Types: single | double
W - Element or subarray weights
complex-valued $P$-by-1 vector
Element or subarray weights, specified as a complex-valued $P$-by- 1 column vector where $P$ is the number of array elements (or subarrays when the array supports subarrays).

## Dependencies

To enable this port, select the Enable weights input check box.
Data Types: single | double

WS - Subarray element weights
complex-valued $N_{\text {SE }}$-by-L matrix
Subarray element weights, specified as a complex-valued $N_{\mathrm{SE}}$-by-L matrix. $N_{\mathrm{SE}}$ is the number of subarrays. $L$ is the number of incident signals. The same weight is applied to the individual elements within a subarray.

Subarray Element Weights

| Specify sensor array as: | Subarray Weights |
| :--- | :--- |
| Replicated subarray | All subarrays have the same dimensions and <br> sizes. Then, the subarray weights form an $N_{\text {SE }}$-by- <br> $N$ matrix. $N_{\mathrm{SE}}$ is the number of elements in each <br> subarray and $N$ is the number of subarrays. Each <br> column of WS specifies the weights for the <br> corresponding subarray. |
| Partitioned array | Subarrays can have different dimensions and <br> sizes. In this case, you can specify subarray <br> weights as |
|  | an $N_{\text {SE }}$-by- $N$ matrix, where $N_{\text {SE }}$ is now the <br> number of elements in the largest subarray. <br> The first $Q$ entries in each column are the <br> element weights for the subarray where $Q$ is <br> the number of elements in the subarray. If all <br> the subarrays have the same size, $Q=N_{\mathrm{SE}}$. |
|  | a 1-by- $N$ cell array. Each cell contains a <br> column vector of weights for the <br> corresponding subarray. The column vectors <br> have lengths equal to the number of elements <br> in the corresponding subarray. |

## Dependencies

To enable this port, set the Specify sensor array as parameter to Partitioned array or Replicated subarray and set the Subarray steering method to Custom.
Data Types: double | single
Steer - Subarray steering angle
real-valued length-2 column vector
Subarray steering angle, specified as a real-valued length-2 column vector. The vector has the form [azimuth; elevation], in degrees. Units are in degrees. The azimuth angle must lie in the range from $180^{\circ}$ to $180^{\circ}$, inclusive. The elevation angle must lie in the range from $-90^{\circ}$ to $90^{\circ}$, inclusive.

## Dependencies

To enable this port, set the Specify sensor array as parameter to Partitioned array or Replicated subarray and set the Subarray steering method to Phase or Time.
Data Types: single|double

```
Output
Y - Collected signals
complex-valued M-by-P matrix
```

Collected signals, returned as a complex-valued $M$-by- $P$ matrix. $M$ is the length of the input signal. $P$ is the number of array elements (or subarrays when subarrays are supported). Each column corresponds to the signal collected by the corresponding array element (or corresponding subarrays when subarrays are supported).
Data Types: double | single

## Parameters

## Main Tab

Signal propagation speed (m/s) - Signal propagation speed
physconst('LightSpeed') (default)| real-valued positive scalar

Signal propagation speed, specified as a real-valued positive scalar. The default value of the speed of light is the value returned by physconst('LightSpeed'). Units are in meters per second.

## Example: 3e8

Data Types: double
Operating frequency (Hz) - System operating frequency
3e8 (default) | positive real scalar

System operating frequency, specified as a positive scalar. Units are in Hz .

## Sensor gain measure - Sensor gain measure

dB (default) | dBi

Sensor gain measure, specified as dB or dBi .

- When you set this parameter to dB, the input signal power is scaled by the sensor power pattern (in dB ) in the corresponding direction and then combined.
- When you set this parameter to dBi , the input signal power is scaled by the directivity pattern (in dBi ) in the corresponding direction and then combined. This option is useful when you want to compare results with the values computed by the radar equation that uses dBi to specify the antenna gain. The computation using the dBi option is costly as it requires an integration over all directions to compute the total radiated power of the sensor.

Data Types: char | string
Enable weights input - Option to input weights
off (default) | on

Select this check box to specify array weights via the input port W . The input port appears only when this box is selected.

## Simulate using - Block simulation method <br> Interpreted Execution (default)|Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).
Programmatic Use
Block Parameter:SimulateUsing
Type:enum
Values:Interpreted Execution, Code Generation
Default:Interpreted Execution
Clicking the Analyze button opens the Sensor Array Analyzer app. The app lets you examine important array properties such as array response and array geometry.

## Specify sensor array as - Method to specify array

Array (no subarrays) (default)|Partitioned array|Replicated subarray|MATLAB expression

Method to specify array, specified as Array (no subarrays) or MATLAB expression.

- Array (no subarrays) - use the block parameters to specify the array.
- Partitioned array - use the block parameters to specify the array.
- Replicated subarray - use the block parameters to specify the array.
- MATLAB expression - create the array using a MATLAB expression.


## Element Parameters

Element type - Array element types
Isotropic Antenna (default)|Cosine Antenna|Custom Antenna|Omni Microphone| Custom Microphone

Antenna or microphone type, specified as one of the following:

- Isotropic Antenna
- Cosine Antenna
- Custom Antenna
- Omni Microphone
- Custom Microphone

Operating frequency range $(\mathbf{H z})$ - Operating frequency range of the antenna or microphone element
[0, 1e20] (default) | real-valued 1-by-2 row vector

Specify the operating frequency range of the antenna or microphone element as a 1-by-2 row vector in the form [LowerBound, UpperBound]. The element has no response outside this frequency range. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Isotropic Antenna, Cosine Antenna, or Omni Microphone.

Operating frequency vector (Hz) - Operating frequency range of custom antenna or microphone elements
[0,1e20] (default) | real-valued row vector

Specify the frequencies at which to set antenna and microphone frequency responses as a 1-by- $L$ row vector of increasing real values. The antenna or microphone element has no response outside the frequency range specified by the minimum and maximum elements of this vector. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone. Use Frequency responses (dB) to set the responses at these frequencies.

Baffle the back of the element - Set back response of an Isotropic Antenna element or an Omni Microphone element to zero off (default) | on

Select this check box to baffle the back response of the element. When back baffled, the responses at all azimuth angles beyond $\pm 90^{\circ}$ from broadside are set to zero. The broadside direction is defined as $0^{\circ}$ azimuth angle and $0^{\circ}$ elevation angle.

## Dependencies

To enable this check box, set Element type to Isotropic Antenna or Omni Microphone.
Exponent of cosine pattern - Exponents of azimuth and elevation cosine patterns
[1.5 1.5] (default) | nonnegative scalar | real-valued 1-by-2 matrix of nonnegative values

Specify the exponents of the cosine pattern as a nonnegative scalar or a real-valued 1-by-2 matrix of nonnegative values. When Exponent of cosine pattern is a 1-by-2 vector, the first element is the exponent in the azimuth direction and the second element is the exponent in the elevation direction. When you set this parameter to a scalar, both the azimuth direction and elevation direction cosine patterns are raised to the same power.

## Dependencies

To enable this parameter, set Element type to Cosine Antenna.
Frequency responses (dB) - Antenna and microphone frequency response
[0,0] (default) | real-valued row vector

Frequency response of a custom antenna or custom microphone for the frequencies defined by the Operating frequency vector ( Hz ) parameter. The dimensions of Frequency responses (dB) must match the dimensions of the vector specified by the Operating frequency vector $(\mathbf{H z})$ parameter.

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone.
Input Pattern Coordinate System - Coordinate system of custom antenna pattern az-el (default) | phi-theta

Coordinate system of custom antenna pattern, specified az-el or phi-theta. When you specify azel, use the Azimuth angles (deg) and Elevations angles (deg) parameters to specify the coordinates of the pattern points. When you specify phi-theta, use the Phi angles (deg) and Theta angles (deg) parameters to specify the coordinates of the pattern points.

## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Azimuth angles (deg) - Azimuth angles of antenna radiation pattern
[-180:180] (default) | real-valued row vector

Specify the azimuth angles at which to calculate the antenna radiation pattern as a 1-by-P row vector. $P$ must be greater than 2. Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to az-el.

Elevation angles (deg) - Elevation angles of antenna radiation pattern [-90:90] (default) | real-valued row vector

Specify the elevation angles at which to compute the radiation pattern as a 1-by- $Q$ vector. $Q$ must be greater than 2. Angle units are in degrees. Elevation angles must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to az-el.

Phi Angles (deg) - Phi angle coordinates of custom antenna radiation pattern $0: 360$ | real-valued 1-by-P row vector

Phi angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by-P row vector. $P$ must be greater than 2 . Angle units are in degrees. Phi angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Theta Angles (deg) - Theta angle coordinates of custom antenna radiation pattern $0: 180$ | real-valued 1-by- $Q$ row vector

Theta angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by$Q$ row vector. $Q$ must be greater than 2 . Angle units are in degrees. Theta angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Magnitude pattern (dB) - Magnitude of combined antenna radiation pattern zeros $(181,361)$ (default) | real-valued $Q$-by- $P$ matrix | real-valued $Q$-by- $P$-by- $L$ array

Magnitude of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector ( $\mathbf{H z}$ ).

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector $(\mathbf{H z})$ parameter.


## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Phase pattern (deg) - Custom antenna radiation phase pattern zeros $(181,361)$ (default) | real-valued $Q$-by- $P$ matrix | real-valued $Q$-by- $P$-by-L array

Phase of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector ( $\mathbf{H z}$ ).

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (


## Dependencies

To enable this parameter, set Element type to Custom Antenna.
MatchArrayNormal - Rotate antenna element to array normal on (default) | off

Select this check box to rotate the antenna element pattern to align with the array normal. When not selected, the element pattern is not rotated.

When the antenna is used in an antenna array and the Input Pattern Coordinate System parameter is az-el, selecting this check box rotates the pattern so that the $x$-axis of the element coordinate system points along the array normal. Not selecting uses the element pattern without the rotation.

When the antenna is used in an antenna array and Input Pattern Coordinate System is set to phitheta, selecting this check box rotates the pattern so that the $z$-axis of the element coordinate system points along the array normal.

Use the parameter in conjunction with the Array normal parameter of the URA and UCA arrays.

## Dependencies

To enable this parameter, set Element type to Custom Antenna.

Polar pattern frequencies (Hz) - Polar pattern microphone response frequencies 1 e3 (default) | real scalar | real-valued 1-by-L row vector

Polar pattern microphone response frequencies, specified as a real scalar, or a real-valued, 1-by- $L$ vector. The response frequencies lie within the frequency range specified by the Operating frequency vector $(\mathbf{H z})$ vector.

## Dependencies

To enable this parameter, set Element type set to Custom Microphone.
Polar pattern angles (deg) - Polar pattern response angles
[-180: 180] (default) | real-valued -by-P row vector

Specify the polar pattern response angles, as a 1-by-P vector. The angles are measured from the central pickup axis of the microphone and must be between $-180^{\circ}$ and $180^{\circ}$, inclusive.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.
Polar pattern (dB) - Custom microphone polar response
zeros (1,361) (default) | real-valued $L$-by- $P$ matrix

Specify the magnitude of the custom microphone element polar patterns as an $L$-by- $P$ matrix. $L$ is the number of frequencies specified in Polar pattern frequencies ( $\mathbf{H z}$ ). $P$ is the number of angles specified in Polar pattern angles (deg). Each row of the matrix represents the magnitude of the polar pattern measured at the corresponding frequency specified in Polar pattern frequencies (Hz) and all angles specified in Polar pattern angles (deg). The pattern is measured in the azimuth plane. In the azimuth plane, the elevation angle is $0^{\circ}$ and the central pickup axis is $0^{\circ}$ degrees azimuth and $0^{\circ}$ degrees elevation. The polar pattern is symmetric around the central axis. You can construct the microphone response pattern in 3-D space from the polar pattern.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.

## Array Parameters

Geometry - Array geometry
ULA (default) | URA | UCA | Conformal Array

Array geometry, specified as one of

- ULA - Uniform linear array
- URA - Uniform rectangular array
- UCA - Uniform circular array
- Conformal Array - arbitrary element positions

Number of elements - Number of array elements
2 for ULA arrays and 5 for UCA arrays (default) | integer greater than or equal to 2

The number of array elements for ULA or UCA arrays, specified as an integer greater than or equal to 2.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

## Dependencies

To enable this parameter, set Geometry to ULA or UCA.
Element spacing (m) - Spacing between array elements
0.5 for ULA arrays and [0.5, 0.5$]$ for URA arrays (default) | positive scalar for ULA or URA arrays | 2 -element vector of positive values for URA arrays

Spacing between adjacent array elements:

- ULA - specify the spacing between two adjacent elements in the array as a positive scalar.
- URA - specify the spacing as a positive scalar or a 1-by-2 vector of positive values. If Element spacing (m) is a scalar, the row and column spacings are equal. If Element spacing (m) is a vector, the vector has the form
[SpacingBetweenArrayRows,SpacingBetweenArrayColumns].
- When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

Dependencies
To enable this parameter, set Geometry to ULA or URA.
Array axis - Linear axis direction of ULA
$y$ (default) $|x| z$

Linear axis direction of ULA, specified as $y, x$, or $z$. All ULA array elements are uniformly spaced along this axis in the local array coordinate system.

## Dependencies

- To enable this parameter, set Geometry to ULA.
- This parameter is also enabled when the block only supports ULA arrays.

Array size - Dimensions of URA array
$[2,2]$ (default) | positive integer | 1-by-2 vector of positive integers

Dimensions of a URA array, specified as a positive integer or 1-by-2 vector of positive integers.

- If Array size is a 1 -by- 2 vector, the vector has the form [NumberOfArrayRows, NumberOfArrayColumns].
- If Array size is an integer, the array has the same number of rows and columns.
- When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

For a URA, array elements are indexed from top to bottom along the leftmost column, and then continue to the next columns from left to right. In this figure, the Array size value of [3,2] creates an array having three rows and two columns.

## Size and Element Indexing Order

for Uniform Rectangular Arrays
Example: Size $=[3,2]$


## Dependencies

To enable this parameter, set Geometry to URA.
Element lattice - Lattice of URA element positions
Rectangular (default) | Triangular

Lattice of URA element positions, specified as Rectangular or Triangular.

- Rectangular - Aligns all the elements in row and column directions.
- Triangular - Shifts the even-row elements of a rectangular lattice toward the positive row-axis direction. The displacement is one-half the element spacing along the row dimension.


## Dependencies

To enable this parameter, set Geometry to URA.
Array normal - Array normal direction
$x$ for URA arrays or $z$ for UCA arrays (default) | y

Array normal direction, specified as $x, y$, or $z$.
Elements of planar arrays lie in a plane orthogonal to the selected array normal direction. Element boresight directions point along the array normal direction.

| Array Normal Parameter Value | Element Positions and Boresight Directions |
| :--- | :--- |
| $x$ | Array elements lie in the $y z$-plane. All element <br> boresight vectors point along the $x$-axis. |
| $y$ | Array elements lie in the $z x$-plane. All element <br> boresight vectors point along the $y$-axis. |
| $z$ | Array elements lie in the $x y$-plane. All element <br> boresight vectors point along the $z$-axis. |

## Dependencies

To enable this parameter, set Geometry to URA or UCA.
Radius of UCA (m) - UCA array radius
0.5 (default) | positive scalar

Radius of UCA array, specified as a positive scalar.

## Dependencies

To enable this parameter, set Geometry to UCA.
Element positions (m) - Positions of conformal array elements [0;0;0] (default) | 3-by-Nmatrix of real values

Positions of the elements in a conformal array, specified as a 3 -by- $N$ matrix of real values, where $N$ is the number of elements in the conformal array. Each column of this matrix represents the position [ $x ; y ; z$ ] of an array element in the array local coordinate system. The origin of the local coordinate system is ( $0,0,0$ ). Units are in meters.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

## Dependencies

To enable this parameter set Geometry to Conformal Array.
Element normals (deg) - Direction of conformal array element normal vectors [0;0] | 2-by-1 column vector | 2 -by- $N$ matrix

Direction of element normal vectors in a conformal array, specified as a 2-by-1 column vector or a 2-by- $N$ matrix. $N$ indicates the number of elements in the array. For a matrix, each column specifies the normal direction of the corresponding element in the form [azimuth; elevation] with respect to the local coordinate system. The local coordinate system aligns the positive $x$-axis with the direction normal to the conformal array. If the parameter value is a 2 -by- 1 column vector, the same pointing direction is used for all array elements.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

You can use the Element positions (m) and Element normals (deg) parameters to represent any arrangement in which pairs of elements differ by certain transformations. The transformations can
combine translation, azimuth rotation, and elevation rotation. However, you cannot use transformations that require rotation about the normal direction.

## Dependencies

To enable this parameter, set Geometry to Conformal Array.
Taper - Array element tapers
1 (default) | complex-valued scalar | complex-valued row vector

Element tapering, specified as a complex-valued scalar or a complex-valued 1-by- $N$ row vector. In this vector, $N$ represents the number of elements in the array.

Also known as element weights, tapers multiply the array element responses. Tapers modify both amplitude and phase of the response to reduce side lobes or steer the main response axis.

If Taper is a scalar, the same weight is applied to each element. If Taper is a vector, a weight from the vector is applied to the corresponding sensor element. The number of weights must match the number of elements of the array.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

Subarray definition matrix - Define elements belonging to subarrays
logical matrix

Specify the subarray selection as an $M$-by- $N$ matrix. $M$ is the number of subarrays and $N$ is the total number of elements in the array. Each row of the matrix represents a subarray and each entry in the row indicates when an element belongs to the subarray. When the entry is zero, the element does not belong the subarray. A nonzero entry represents a complex-valued weight applied to the corresponding element. Each row must contain at least one nonzero entry.

The phase center of each subarray lies at the subarray geometric center. The subarray geometric center depends on the Subarray definition matrix and Geometry parameters.

## Dependencies

To enable this parameter, set Specify sensor array as to Partitioned array.
Subarray steering method - Specify subarray steering method
None (default) | Phase | Time

Subarray steering method, specified as one of

- None
- Phase
- Time
- Custom

Selecting Phase or Time opens the Steer input port on the Narrowband Receive Array, Narrowband Transmit Array, Wideband Receive Array, Wideband Transmit Array blocks, Constant Gamma Clutter, and GPU Constant Gamma Clutter blocks.

Selecting Custom opens the WS input port on the Narrowband Receive Array, Narrowband Transmit Array, Wideband Receive Array, Wideband Transmit Array blocks, Constant Gamma Clutter, and GPU Constant Gamma Clutter blocks.

## Dependencies

To enable this parameter, set Specify sensor array as to Partitioned array or Replicated subarray.

Phase shifter frequency (Hz) - Subarray phase shifting frequency
3.0 e 8 (default) | positive real-valued scalar

Operating frequency of subarray steering phase shifters, specified as a positive real-valued scalar.
Units are Hz.

## Dependencies

To enable this parameter, set Sensor array to Partitioned array or Replicated subarray and set Subarray steering method to Phase.

Number of bits in phase shifters - Subarray steering phase shift quantization bits
0 (default) | non-negative integer

Subarray steering phase shift quantization bits, specified as a non-negative integer. A value of zero indicates that no quantization is performed.

## Dependencies

To enable this parameter, set Sensor array to Partitioned array or Replicated subarray and set Subarray steering method to Phase.

Subarrays layout - Subarray position specification
Rectangular (default) | Custom

Specify the layout of replicated subarrays as Rectangular or Custom.

- When you set this parameter to Rectangular, use the Grid size and Grid spacing parameters to place the subarrays.
- When you set this parameter to Custom, use the Subarray positions (m) and Subarray normals parameters to place the subarrays.


## Dependencies

To enable this parameter, set Sensor array to Replicated subarray
Grid size - Dimensions of rectangular subarray grid [1,2] (default)

Rectangular subarray grid size, specified as a single positive integer, or a 1-by-2 row vector of positive integers.

If Grid size is an integer scalar, the array has an equal number of subarrays in each row and column. If Grid size is a 1-by-2 vector of the form [NumberOfRows, NumberOfColumns], the first entry is
the number of subarrays along each column. The second entry is the number of subarrays in each row. A row is along the local $y$-axis, and a column is along the local $z$-axis. The figure here shows how you can replicate a 3-by-2 URA subarray using a Grid size of [1,2].
$3 \times 2$ Element URA
Replicated on a $1 \times 2$ Grid


## Dependencies

To enable this parameter, set Sensor array to Replicated subarray and Subarrays layout to Rectangular.

Grid spacing ( $\mathbf{m}$ ) - Spacing between subarrays on rectangular grid
Auto (default) | positive real-valued scalar | 1-by-2 vector of positive real-values

The rectangular grid spacing of subarrays, specified as a positive, real-valued scalar, a 1-by-2 row vector of positive, real-values, or Auto. Units are in meters.

- If Grid spacing is a scalar, the spacing along the row and the spacing along the column is the same.
- If Grid spacing is a 1 -by-2 row vector, the vector has the form [SpacingBetweenRows, SpacingBetweenColumn]. The first entry specifies the spacing between rows along a column. The second entry specifies the spacing between columns along a row.
- If Grid spacing is set to Auto, replication preserves the element spacing of the subarray for both rows and columns while building the full array. This option is available only when you specify Geometry as ULA or URA.


## Dependencies

To enable this parameter, set Sensor array to Replicated subarray and Subarrays layout to Rectangular.

Subarray positions (m) - Positions of subarrays
[0,0;0.5,0.5;0,0] (default)| 3-by-N real-valued matrix

Positions of the subarrays in the custom grid, specified as a real 3-by- $N$ matrix, where $N$ is the number of subarrays in the array. Each column of the matrix represents the position of a single subarray in the array local coordinate system. The coordinates are expressed in the form [x; y; z]. Units are in meters.

## Dependencies

To enable this parameter, set Sensor array to Replicated subarray and Subarrays layout to Custom.

Subarray normals - Direction of subarray normal vectors
[0, 0;0,0] (default) | 2 -by- $N$ real matrix

Specify the normal directions of the subarrays in the array. This parameter value is a 2 -by- $N$ matrix, where $N$ is the number of subarrays in the array. Each column of the matrix specifies the normal direction of the corresponding subarray, in the form [azimuth; elevation]. Angle units are in degrees. Angles are defined with respect to the local coordinate system.

You can use the Subarray positions and Subarray normals parameters to represent any arrangement in which pairs of subarrays differ by certain transformations. The transformations can combine translation, azimuth rotation, and elevation rotation. However, you cannot use transformations that require rotation about the normal.

## Dependencies

To enable this parameter, set the Sensor array parameter to Replicated subarray and the Subarrays layout to Custom.

## Version History

Introduced in R2014a

## See Also

phased.Collector

## Narrowband Transmit Array

Narrowband transmit array


## Libraries:

Phased Array System Toolbox / Transmitters and Receivers

## Description

The Narrowband Transmit Array block generates narrowband plane waves in the far field of the array by adding the far-field radiated signals of each element. Think of the block output as the field at a reference distance from the element or from the center of the array.

## Ports

## Input

X - Radiated signals
complex-valued $M$-by-1 vector | complex-valued $M$-by- $N$ matrix
Radiate signals, specified as a complex-valued $M$-by- 1 vector or complex-valued $M$-by- $N$ matrix. $M$ is the length of the signal, and $N$ is the number of array elements (or subarrays when subarrays are supported).

Dimensions of $X$

| Dimension | Signal |
| :--- | :--- |
| $M$-by-1 vector | The same signal is radiated from all array <br> elements (or all subarrays when subarrays are <br> supported). |
| $M$-by $-N$ matrix | Each column corresponds to the signal radiated <br> by the corresponding array element (or <br> corresponding subarrays when subarrays are <br> supported). |

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

## Data Types: double <br> Complex Number Support: Yes

Ang - Input
real-valued 2-by-L matrix
Radiating directions of signals, specified as a real-valued 2-by-L matrix. Each column specifies a radiating direction in the form [AzimuthAngle; ElevationAngle]. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive. Units are in degrees.

Example: [30,20;45,0]
Data Types: double
W - Element or subarray weights
$N$-by-1 column vector
Element or subarray weights, specified as a complex-valued $N$-by- 1 column vector where $N$ is the number of array elements (or subarrays when the array supports subarrays).

## Dependencies

To enable this port, select the Enable weights input check box.

## Data Types: double

WS - Subarray element weights input port
complex-valued $N_{\text {SE }}$-by- $N$ matrix | 1-by- $N$ cell array
Subarray element weights, specified as complex-valued $N_{\text {SE }}$-by- $N$ matrix or 1-by- $N$ cell array where $N$ is the number of subarrays. These weights are applied to the individual elements within a subarray.

## Subarray element weights

| Sensor Array | Subarray weights |
| :--- | :--- |
| Replicated subarray | All subarrays have the same dimensions and <br> sizes. Then, the subarray weights form an $N_{\text {SE }}$-by- <br> $N$ matrix. $N_{\mathrm{SE}}$ is the number of elements in each <br> subarray and $N$ is the number of subarrays. Each <br> column of WS specifies the weights for the <br> corresponding subarray. |
| Partitioned array | Subarrays may not have the same dimensions and <br> sizes. In this case, you can specify subarray <br> weights as |
|  | an $N_{\mathrm{SE}}$-by- $N$ matrix, where $N_{\text {SE }}$ is now the <br> number of elements in the largest subarray. <br> The first $Q$ entries in each column are the <br> element weights for the subarray where $Q$ is <br> the number of elements in the subarray. |
|  | a 1-by- $N$ cell array. Each cell contains a <br> column vector of weights for the <br> corresponding subarray. The column vectors <br> have lengths equal to the number of elements <br> in the corresponding subarray. |

## Dependencies

To enable this port, specify the Specify sensor array as parameter as Replicated subarray or Partitioned array and then select Custom from the Subarray steering method drop down menu.

Data Types: double
Steer - Input
real-valued 2-by-1 vector

Subarray steering angle, specified as a length- 2 column vector. The vector has the form [azimuthAngle;elevationAngle]. The azimuth angle must be between $-180^{\circ}$ and $180^{\circ}$, inclusive. The elevation angle must be between $-90^{\circ}$ and $90^{\circ}$, inclusive. Units are in degrees.

## Dependencies

To enable this port, select Phase or Time from the Subarray steering method pull down menu.

## Data Types: double

## Output

Output 1 - Output
complex-valued M-by-L matrix
Radiated signals, specified as a complex-valued $M$-by- $L$ matrix, where $L$ is the number of radiating angles, ANG and $M$ is the length of the input signal, X .

## Data Types: double

## Parameters

## Main Tab

Propagation speed (m/s) - Signal propagation speed
physconst('LightSpeed') (default)| positive scalar

Signal propagation speed, specified as a real-valued positive scalar. The default value of the speed of light is the value returned by physconst('LightSpeed').

## Data Types: double

Operating frequency $(\mathbf{H z})$ - System operating frequency
3e8 (default) | positive real scalar

System operating frequency, specified as a positive scalar. Units are in Hz .

## Sensor gain measure - Specify sensor gain

dB (default) | dBi
Specify sensor gain measure as dB or dBi .

- When you set this parameter to dB, the input signal power is scaled by the sensor power pattern (in dB ) at the corresponding direction and then combined.
- When you set this parameter to dBi , the input signal power is scaled by the directivity pattern (in dBi ) at the corresponding direction and then combined. This option is useful when you want to compare results with the values computed by the radar equation that uses dBi to specify the antenna gain. The computation using the dBi option is expensive as it requires an integration over all directions to compute the total radiated power of the sensor. The default value is dB .

Enable weights input - Enable weights input
off (default) | on

Select this check box to specify array weights using the input port W . The input port appears only when this box is checked.

Simulate using - Block simulation method
Interpreted Execution (default)|Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).

## Programmatic Use

Block Parameter:SimulateUsing
Type:enum
Values:Interpreted Execution, Code Generation
Default:Interpreted Execution

## Sensor Array Tab

Specify sensor array as - Method to specify array
Array (no subarrays) (default)|Single element|Partitioned array|Replicated subarray|MATLAB expression

Specify sensor element or sensor array. A sensor array can also contain subarrays or be a partitioned array. This parameter can also be expressed as a MATLAB expression.

Types

## Single element <br> Array (no subarrays) <br> Partitioned array <br> Replicated subarray <br> MATLAB expression

## Element Parameters

Element type - Array element types
Isotropic Antenna (default)|Cardioid Antenna|Cosine Antenna|Custom Antenna| Gaussian Antenna|Sinc Antenna|Omni Microphone|Custom Microphone

Antenna or microphone type, specified as one of the following:

- Isotropic Antenna
- Cardioid Antenna
- Cosine Antenna
- Custom Antenna
- Gaussian Antenna
- Sinc Antenna
- Omni Microphone
- Custom Microphone

Operating frequency range $(\mathbf{H z})$ - Operating frequency range of the antenna or microphone element
[0, 1e20] (default) | real-valued 1-by-2 row vector

Specify the operating frequency range of the antenna or microphone element as a 1-by-2 row vector in the form [LowerBound, UpperBound]. The element has no response outside this frequency range. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Isotropic Antenna, Cosine Antenna, or Omni Microphone.

Baffle the back of the element - Set back response of an Isotropic Antenna element or an Omni Microphone element to zero off (default) | on

Select this check box to baffle the back response of the element. When back baffled, the responses at all azimuth angles beyond $\pm 90^{\circ}$ from broadside are set to zero. The broadside direction is defined as $0^{\circ}$ azimuth angle and $0^{\circ}$ elevation angle.

## Dependencies

To enable this check box, set Element type to Isotropic Antenna or Omni Microphone.

Null axis direction - Null axis direction
$-x$ (default) $|+x|+y|-y|+z \mid-z$

## Dependencies

To enable this parameter, set Element type to Cardioid Antenna.
Exponent of cosine pattern - Exponents of azimuth and elevation cosine patterns
[1.5 1.5] (default) | nonnegative scalar | real-valued 1-by-2 matrix of nonnegative values

Specify the exponents of the cosine pattern as a nonnegative scalar or a real-valued 1-by-2 matrix of nonnegative values. When Exponent of cosine pattern is a 1 -by-2 vector, the first element is the exponent in the azimuth direction and the second element is the exponent in the elevation direction. When you set this parameter to a scalar, both the azimuth direction and elevation direction cosine patterns are raised to the same power.

## Dependencies

To enable this parameter, set Element type to Cosine Antenna.
Operating frequency vector (Hz) - Operating frequency range of custom antenna or microphone elements
[0,1e20] (default) | real-valued row vector

Specify the frequencies at which to set antenna and microphone frequency responses as a 1-by- $L$ row vector of increasing real values. The antenna or microphone element has no response outside the frequency range specified by the minimum and maximum elements of this vector. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone. Use Frequency responses (dB) to set the responses at these frequencies.

Frequency responses (dB) - Antenna and microphone frequency response [0,0] (default) | real-valued row vector

Frequency response of a custom antenna or custom microphone for the frequencies defined by the Operating frequency vector (Hz) parameter. The dimensions of Frequency responses (dB) must match the dimensions of the vector specified by the Operating frequency vector $(\mathbf{H z})$ parameter.

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone.
Input Pattern Coordinate System - Coordinate system of custom antenna pattern az-el (default)|phi-theta

Coordinate system of custom antenna pattern, specified az-el or phi-theta. When you specify azel, use the Azimuth angles (deg) and Elevations angles (deg) parameters to specify the coordinates of the pattern points. When you specify phi-theta, use the Phi angles (deg) and Theta angles (deg) parameters to specify the coordinates of the pattern points.

## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Azimuth angles (deg) - Azimuth angles of antenna radiation pattern
[-180:180] (default) | real-valued row vector

Specify the azimuth angles at which to calculate the antenna radiation pattern as a 1 -by- $P$ row vector. $P$ must be greater than 2. Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to az-el.

Elevation angles (deg) - Elevation angles of antenna radiation pattern
[-90:90] (default) | real-valued row vector

Specify the elevation angles at which to compute the radiation pattern as a 1-by- $Q$ vector. $Q$ must be greater than 2. Angle units are in degrees. Elevation angles must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to az-el.

Phi Angles (deg) - Phi angle coordinates of custom antenna radiation pattern
$0: 360$ | real-valued 1-by-P row vector

Phi angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by-P row vector. $P$ must be greater than 2 . Angle units are in degrees. Phi angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Theta Angles (deg) - Theta angle coordinates of custom antenna radiation pattern
0:180 | real-valued 1-by- $Q$ row vector

Theta angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by$Q$ row vector. $Q$ must be greater than 2. Angle units are in degrees. Theta angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Magnitude pattern (dB) - Magnitude of combined antenna radiation pattern
zeros $(181,361)$ (default) | real-valued $Q$-by- $P$ matrix | real-valued $Q$-by- $P$-by- $L$ array

Magnitude of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi - theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector ( $\mathbf{H z}$ ).

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (Hz) parameter.


## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Phase pattern (deg) - Custom antenna radiation phase pattern
zeros $(181,361)$ (default) | real-valued $Q$-by- $P$ matrix | real-valued $Q$-by- $P$-by- $L$ array

Phase of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi - theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector ( $\mathbf{H z}$ ).

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (


## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Align element normal with array normal - Align element normal with array normal on (default) | off

## Dependencies

This parameter is enabled when Element type is set to Custom Antenna.
Radiation pattern beamwidth (deg) - Radiation pattern beamwidth [10,10] (default)

## Dependencies

This parameter is enabled when Element type is set to Gaussian Antenna.
Polar pattern frequencies (Hz) - Polar pattern microphone response frequencies
1 e3 (default) | real scalar | real-valued 1-by-L row vector

Polar pattern microphone response frequencies, specified as a real scalar, or a real-valued, 1-by- $L$ vector. The response frequencies lie within the frequency range specified by the Operating frequency vector $(\mathbf{H z})$ vector.

## Dependencies

To enable this parameter, set Element type set to Custom Microphone.
Polar pattern angles (deg) - Polar pattern response angles
[-180: 180] (default) | real-valued -by-P row vector

Specify the polar pattern response angles, as a 1-by- $P$ vector. The angles are measured from the central pickup axis of the microphone and must be between $-180^{\circ}$ and $180^{\circ}$, inclusive.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.
Polar pattern (dB) - Custom microphone polar response zeros (1,361) (default) | real-valued L-by-P matrix

Specify the magnitude of the custom microphone element polar patterns as an $L$-by- $P$ matrix. $L$ is the number of frequencies specified in Polar pattern frequencies ( $\mathbf{H z}$ ). $P$ is the number of angles specified in Polar pattern angles (deg). Each row of the matrix represents the magnitude of the polar pattern measured at the corresponding frequency specified in Polar pattern frequencies (Hz) and all angles specified in Polar pattern angles (deg). The pattern is measured in the azimuth plane. In the azimuth plane, the elevation angle is $0^{\circ}$ and the central pickup axis is $0^{\circ}$ degrees azimuth and $0^{\circ}$ degrees elevation. The polar pattern is symmetric around the central axis. You can construct the microphone response pattern in 3-D space from the polar pattern.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.

## Array Parameters

Geometry - Array geometry
ULA (default) | URA | UCA | Conformal Array

Array geometry, specified as one of

- ULA - Uniform linear array
- URA - Uniform rectangular array
- UCA - Uniform circular array
- Conformal Array - arbitrary element positions

Number of elements - Number of array elements
2 for ULA arrays and 5 for UCA arrays (default) | integer greater than or equal to 2

The number of array elements for ULA or UCA arrays, specified as an integer greater than or equal to 2.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.
Dependencies
To enable this parameter, set Geometry to ULA or UCA.
Array size - Dimensions of URA array
[2,2] (default) | positive integer | 1-by-2 vector of positive integers

Dimensions of a URA array, specified as a positive integer or 1-by-2 vector of positive integers.

- If Array size is a 1 -by-2 vector, the vector has the form [NumberOfArrayRows, NumberOfArrayColumns].
- If Array size is an integer, the array has the same number of rows and columns.
- When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

For a URA, array elements are indexed from top to bottom along the leftmost column, and then continue to the next columns from left to right. In this figure, the Array size value of [3, 2] creates an array having three rows and two columns.

Size and Element Indexing Order
for Uniform Rectangular Arrays
Example: Size $=[3,2]$


## Dependencies

To enable this parameter, set Geometry to URA.
Element spacing (m) - Spacing between array elements

## 0.5 for ULA arrays and [0.5,0.5] for URA arrays (default) | positive scalar for ULA or URA arrays | 2 -element vector of positive values for URA arrays

Spacing between adjacent array elements:

- ULA - specify the spacing between two adjacent elements in the array as a positive scalar.
- URA - specify the spacing as a positive scalar or a 1 -by-2 vector of positive values. If Element spacing (m) is a scalar, the row and column spacings are equal. If Element spacing (m) is a vector, the vector has the form [SpacingBetweenArrayRows,SpacingBetweenArrayColumns].
- When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.


## Dependencies

To enable this parameter, set Geometry to ULA or URA.
Array axis - Linear axis direction of ULA
$y$ (default) $|x| z$

Linear axis direction of ULA, specified as $y$, $x$, or $z$. All ULA array elements are uniformly spaced along this axis in the local array coordinate system.

## Dependencies

- To enable this parameter, set Geometry to ULA.
- This parameter is also enabled when the block only supports ULA arrays.

Element lattice - Lattice of URA element positions
Rectangular (default) | Triangular

Lattice of URA element positions, specified as Rectangular or Triangular.

- Rectangular - Aligns all the elements in row and column directions.
- Triangular - Shifts the even-row elements of a rectangular lattice toward the positive row-axis direction. The displacement is one-half the element spacing along the row dimension.

Dependencies
To enable this parameter, set Geometry to URA.
Array normal - Array normal direction
$x$ for URA arrays or $z$ for UCA arrays (default) | y

Array normal direction, specified as $x, y$, or $z$.
Elements of planar arrays lie in a plane orthogonal to the selected array normal direction. Element boresight directions point along the array normal direction.

| Array Normal Parameter Value | Element Positions and Boresight Directions |
| :--- | :--- |
| x | Array elements lie in the $y z$-plane. All element <br> boresight vectors point along the $x$-axis. |
| y | Array elements lie in the $z x$-plane. All element <br> boresight vectors point along the $y$-axis. |
| z | Array elements lie in the $x y$-plane. All element <br> boresight vectors point along the $z$-axis. |

## Dependencies

To enable this parameter, set Geometry to URA or UCA.
Radius of UCA (m) - UCA array radius
0.5 (default) | positive scalar

Radius of UCA array, specified as a positive scalar.

## Dependencies

To enable this parameter, set Geometry to UCA.
Element positions (m) - Positions of conformal array elements
[0;0;0] (default)| 3-by-Nmatrix of real values

Positions of the elements in a conformal array, specified as a 3 -by- $N$ matrix of real values, where $N$ is the number of elements in the conformal array. Each column of this matrix represents the position [ $x ; y ; z$ ] of an array element in the array local coordinate system. The origin of the local coordinate system is $(0,0,0)$. Units are in meters.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

## Dependencies

To enable this parameter set Geometry to Conformal Array.
Element normals (deg) - Direction of conformal array element normal vectors [0;0] | 2-by-1 column vector | 2 -by- $N$ matrix

Direction of element normal vectors in a conformal array, specified as a 2-by-1 column vector or a 2-by- $N$ matrix. $N$ indicates the number of elements in the array. For a matrix, each column specifies the normal direction of the corresponding element in the form [azimuth; elevation] with respect to the local coordinate system. The local coordinate system aligns the positive $x$-axis with the direction normal to the conformal array. If the parameter value is a 2 -by- 1 column vector, the same pointing direction is used for all array elements.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

You can use the Element positions (m) and Element normals (deg) parameters to represent any arrangement in which pairs of elements differ by certain transformations. The transformations can combine translation, azimuth rotation, and elevation rotation. However, you cannot use transformations that require rotation about the normal direction.

## Dependencies

To enable this parameter, set Geometry to Conformal Array.

## Taper - Array element tapers

1 (default) | complex-valued scalar | complex-valued row vector

Element tapering, specified as a complex-valued scalar or a complex-valued 1-by-N row vector. In this vector, $N$ represents the number of elements in the array.

Also known as element weights, tapers multiply the array element responses. Tapers modify both amplitude and phase of the response to reduce side lobes or steer the main response axis.

If Taper is a scalar, the same weight is applied to each element. If Taper is a vector, a weight from the vector is applied to the corresponding sensor element. The number of weights must match the number of elements of the array.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

## Subarray definition matrix - Define elements belonging to subarrays

```
logical matrix
```

Specify the subarray selection as an $M$-by- $N$ matrix. $M$ is the number of subarrays and $N$ is the total number of elements in the array. Each row of the matrix represents a subarray and each entry in the row indicates when an element belongs to the subarray. When the entry is zero, the element does not belong the subarray. A nonzero entry represents a complex-valued weight applied to the corresponding element. Each row must contain at least one nonzero entry.

The phase center of each subarray lies at the subarray geometric center. The subarray geometric center depends on the Subarray definition matrix and Geometry parameters.

## Dependencies

To enable this parameter, set Specify sensor array as to Partitioned array.
Subarray steering method - Specify subarray steering method
None (default) | Phase | Time

Subarray steering method, specified as one of

- None
- Phase
- Time
- Custom

Selecting Phase or Time opens the Steer input port on the Narrowband Receive Array, Narrowband Transmit Array, Wideband Receive Array, Wideband Transmit Array blocks, Constant Gamma Clutter, and GPU Constant Gamma Clutter blocks.

Selecting Custom opens the WS input port on the Narrowband Receive Array, Narrowband Transmit Array, Wideband Receive Array, Wideband Transmit Array blocks, Constant Gamma Clutter, and GPU Constant Gamma Clutter blocks.

## Dependencies

To enable this parameter, set Specify sensor array as to Partitioned array or Replicated subarray.

Phase shifter frequency (Hz) - Subarray phase shifting frequency
3.0 e 8 (default) | positive real-valued scalar

Operating frequency of subarray steering phase shifters, specified as a positive real-valued scalar. Units are Hz.

## Dependencies

To enable this parameter, set Sensor array to Partitioned array or Replicated subarray and set Subarray steering method to Phase.

Number of bits in phase shifters - Subarray steering phase shift quantization bits
0 (default) | non-negative integer

Subarray steering phase shift quantization bits, specified as a non-negative integer. A value of zero indicates that no quantization is performed.

## Dependencies

To enable this parameter, set Sensor array to Partitioned array or Replicated subarray and set Subarray steering method to Phase.

Subarrays layout - Subarray position specification
Rectangular (default) | Custom

Specify the layout of replicated subarrays as Rectangular or Custom.

- When you set this parameter to Rectangular, use the Grid size and Grid spacing parameters to place the subarrays.
- When you set this parameter to Custom, use the Subarray positions (m) and Subarray normals parameters to place the subarrays.

Dependencies
To enable this parameter, set Sensor array to Replicated subarray
Grid size - Dimensions of rectangular subarray grid

```
[1,2] (default)
```

Rectangular subarray grid size, specified as a single positive integer, or a 1-by-2 row vector of positive integers.

If Grid size is an integer scalar, the array has an equal number of subarrays in each row and column. If Grid size is a 1-by-2 vector of the form [NumberOfRows, NumberOfColumns], the first entry is the number of subarrays along each column. The second entry is the number of subarrays in each row. A row is along the local $y$-axis, and a column is along the local $z$-axis. The figure here shows how you can replicate a 3-by-2 URA subarray using a Grid size of [1,2].
$3 \times 2$ Element URA
Replicated on a $1 \times 2$ Grid


## Dependencies

To enable this parameter, set Sensor array to Replicated subarray and Subarrays layout to Rectangular.

Grid spacing ( $\mathbf{m}$ ) - Spacing between subarrays on rectangular grid
Auto (default) | positive real-valued scalar | 1-by-2 vector of positive real-values

The rectangular grid spacing of subarrays, specified as a positive, real-valued scalar, a 1-by-2 row vector of positive, real-values, or Auto. Units are in meters.

- If Grid spacing is a scalar, the spacing along the row and the spacing along the column is the same.
- If Grid spacing is a 1 -by- 2 row vector, the vector has the form [SpacingBetweenRows, SpacingBetweenColumn]. The first entry specifies the spacing between rows along a column. The second entry specifies the spacing between columns along a row.
- If Grid spacing is set to Auto, replication preserves the element spacing of the subarray for both rows and columns while building the full array. This option is available only when you specify Geometry as ULA or URA.


## Dependencies

To enable this parameter, set Sensor array to Replicated subarray and Subarrays layout to Rectangular.

Subarray positions (m) - Positions of subarrays
[0,0;0.5, 0.5;0,0] (default)| 3-by-N real-valued matrix

Positions of the subarrays in the custom grid, specified as a real 3-by- $N$ matrix, where $N$ is the number of subarrays in the array. Each column of the matrix represents the position of a single subarray in the array local coordinate system. The coordinates are expressed in the form $[x ; y ; z]$. Units are in meters.

## Dependencies

To enable this parameter, set Sensor array to Replicated subarray and Subarrays layout to Custom.

Subarray normals - Direction of subarray normal vectors
[0, 0;0,0] (default) | 2 -by- $N$ real matrix

Specify the normal directions of the subarrays in the array. This parameter value is a 2 -by- $N$ matrix, where $N$ is the number of subarrays in the array. Each column of the matrix specifies the normal direction of the corresponding subarray, in the form [azimuth; elevation]. Angle units are in degrees. Angles are defined with respect to the local coordinate system.

You can use the Subarray positions and Subarray normals parameters to represent any arrangement in which pairs of subarrays differ by certain transformations. The transformations can combine translation, azimuth rotation, and elevation rotation. However, you cannot use transformations that require rotation about the normal.

## Dependencies

To enable this parameter, set the Sensor array parameter to Replicated subarray and the Subarrays layout to Custom.

Expression - MATLAB expression used to create an array
Phased Array System Toolbox array System object

MATLAB expression used to create an array, specified as a valid Phased Array System Toolbox array System object.

Example: phased.URA('Size', [5,3])
Dependencies
To enable this parameter, set Specify sensor array as to MATLAB expression.
Analyze - Launch Sensor Array Analyzer
(default)
Clicking the Analyze button launches the Sensor Array Analyzer app. The app lets you examine important array properties such as array response and array geometry.

## Version History

Introduced in R2014b

See Also<br>phased.Radiator

## Nonlinear FM Waveform

Nonlinear FM pulse waveform


Libraries:
Phased Array System Toolbox / Waveforms

## Description

The Nonlinear FM Waveform block generates a nonlinear FM pulse waveform with specified pulse width, pulse repetition frequency (PRF), and sweep bandwidth. The block outputs an integer number of pulses or an integral number of samples.

## Ports

Input
PRFIdx - PRF Index
positive integer
Index to select the pulse repetition frequency (PRF), specified as a positive integer. The index selects the PRF from the predefined vector of values specified by the Pulse repetition frequency ( Hz ) parameter.
Example: 4

## Dependencies

To enable this port, select Enable PRF selection input.

## Data Types: double

FreqOffset - Frequency offset
scalar
Frequency offset in Hz , specified as a scalar.
Example: 2e3

## Dependencies

To enable this port, set Source of Frequency Offset to Input port.

## Data Types: double

## Output

Y - Pulse waveform
complex-valued vector
Pulse waveform samples, returned as a complex-valued vector.
Data Types: double

PRF - Pulse repetition frequency
positive scalar
Pulse repetition frequency of current pulse, returned as a positive scalar.

## Dependencies

To enable this port, set the Output signal format parameter to Pulses and then select the Enable PRF output parameter.

Data Types: double
Coeff - Matched filter coefficients
vector | matrix
Matched filter coefficients, returned as a vector or matrix.

## Dependencies

To enable this port, select Enable Matched Filter Coefficients Output.

## Data Types: double

## Parameters

To edit block parameters interactively, use the Property Inspector. From the Simulink Toolstrip, on the Simulation tab, in the Prepare gallery, select Property Inspector.

Sample rate (Hz) - Sample rate of the output waveform
1e6 (default) | positive scalar

Sample rate of the output waveform, specified as a positive scalar. The ratio of Sample rate (Hz) to each element in the Pulse repetition frequency (Hz) vector must be an integer. This restriction is equivalent to requiring that the pulse repetition interval is an integral multiple of the sample interval.

Programmatic Use<br>Block Parameter:SampleRate<br>Type:double<br>Values:positive scalar<br>Default:1e6<br>Method to specify pulse duration - Pulse duration as time or duty cycle Pulse width (default)| Duty cycle

Method to set the pulse duration, specified as Pulse width or Duty cycle. When you set this parameter to Pulse width, the pulse duration is set using the Pulse width (s) parameter. When you set this parameter to Duty cycle, the pulse duration is computed from the values of the Pulse repetition frequency $(\mathbf{H z})$ and Duty Cycle parameters.

Programmatic Use
Block Parameter:DurationSpecification
Type:string
Values:string
Default:'Pulse width'

Pulse width (s) - Time duration of pulse
50e-6 (default) | positive scalar

The duration of each pulse, specified as a positive scalar. Set the product of Pulse width (s) and Pulse repetition frequency to be less than or equal to one. This restriction ensures that the pulse width is smaller than the pulse repetition interval. Units are in seconds.

Example: 300e-6

## Dependencies

To enable this parameter, set the Method to specify pulse duration parameter to Pulse width.
Programmatic Use
Block Parameter:PulseWidth
Type:double
Values:string
Default:50e-6
Duty cycle - Waveform duty cycle
0.5 (default) | scalar in the range [0,1]

Waveform duty cycle, specified as a scalar in the range [0,1].
Example: 0.7

## Dependencies

To enable this parameter, set the Method to specify pulse duration parameter to Duty cycle.
Programmatic Use
Block Parameter:DutyCycle
Type:double
Values:positive scalar
Default:1e6
Pulse repetition frequency ( Hz ) - Pulse repetition frequency
le4 (default) | positive scalar

Pulse repetition frequency, $P R F$, specified as a scalar or a row vector. Units are in Hz. The pulse repetition interval, $P R I$, is the inverse of the pulse repetition frequency, $P R F$. The value of Pulse repetition frequency $(\mathbf{H z})$ must satisfy these constraints:

- The product of Pulse width and Pulse repetition frequency (Hz) must be less than or equal to one. This condition expresses the requirement that the pulse width is less than one pulse repetition interval. For the phase-coded waveform, the pulse width is the product of the chip width and number of chips.
- The ratio of sample rate to any element of Pulse repetition frequency must be an integer. This condition expresses the requirement that the number of samples in one pulse repetition interval is an integer.

You can select the value of $P R F$ by using block parameter settings alone or in conjunction with the input port, PRFIdx.

- When the Enable PRF selection input parameter is not selected, set the PRF using block parameters.
- To implement a constant $P R F$, specify Pulse repetition frequency ( $\mathbf{H z}$ ) as a positive scalar.
- To implement a staggered $P R F$, specify Pulse repetition frequency $(\mathbf{H z})$ as a row vector with positive values. After the waveform reaches the last element of the vector, the process continues cyclically with the first element of the vector. When PRF is staggered, the time between successive output pulses cycles through the successive values of the PRF vector.
- When the Enable PRF selection input parameter is selected, you can implement a selectable $P R F$ by specifying Pulse repetition frequency $(\mathbf{H z})$ as a row vector with positive real-valued entries. But this time, when you execute the block, select a $P R F$ by passing an index into the $P R F$ vector into the PRFIdx port.

In all cases, the number of output samples is fixed when you set the Output signal format to Samples. When you use a varying PRF and set Output signal format to Pulses, the number of output samples can vary.

## Programmatic Use

Block Parameter:PRF
Type:double
Values:positive scalar
Default:1e6
Enable PRF selection input - Select predefined PRF
off (default) | on

Select this parameter to enable the PRFIdx port.

- When enabled, pass in an index into a vector of predefined PRFs. Set predefined PRFs using the Pulse repetition frequency $(\mathbf{H z})$ parameter.
- When not enabled, the block cycles through the vector of PRFs specified by the Pulse repetition frequency (Hz) parameter. If Pulse repetition frequency ( Hz ) is a scalar, the PRF is constant.

Programmatic Use
Block Parameter:PRFSelectionInputPort
Type:logical
Values:positive scalar
Default:off

Frequency modulation - Frequency modulation
Polynomial (default) | Hyperbolic|Hybrid Linear-Tangent| Stepped Price

Frequency modulation of the nonlinear FM waveform, specified as Polynomial, Hyperbolic, Hybrid Linear-Tangent, or Stepped Price.

- When set to Polynomial the block generates a waveform with an instantaneous frequency that follows a polynomial function. The coefficients of the polynomial are specified by the Coefficients of a Polynomial FM parameter. The resulting frequency function is normalized such that each pulse sweeps the bandwidth specified in Sweep bandwidth (Hz). The Sweep interval parameter is inactive when Frequency modulation is set to Polynomial.
- When set to Hyperbolic the block generates a hyperbolic frequency modulated (HFM) waveform. Use the Start frequency of a hyperbolic FM parameter to set the start frequency of the hyperbolic sweep. The Sweep interval parameter is inactive in this case.
- When set to Hybrid Linear-Tangent the block generates a hybrid NLFM waveform that combines an LFM with a tan-FM as described by Collins and Atkins [1]. The balance between LFM and tan-FM is specified by the Balance between linear FM and tan-FM parameter, and the portion of the $\tan (x)$ curve used for tan-FM is specified by the Tangent curve portion parameter.
- When set to Stepped Price the block generates a stepped version of the Price's NLFM waveform as given by Levanon and Mozeson [2]. The Sweep interval parameter is inactive when Frequency modulation parameter is set to Stepped Price. In this case the sweep bandwidth is determined by the bandwidth factors specified in the Bandwidth factors parameter and the number of frequency steps specified in Number of frequency steps parameter.

Example: Stepped Price
Programmatic Use
Block Parameter:FrequencyModulation
Type:char, string
Values:char. string
Default:Hyperbolic
Data Types: char|string
Coefficients of a polynomial FM - Coefficients of polynomial frequency function
[1 0 0] (default) | ( $N+1$ )-length real-valued vector

Coefficients of the polynomial frequency function, specified as a length- $(N+1)$ real-valued vector. The vector represents the coefficients of an $N$-th degree polynomial. The first entry in the vector is the coefficient of the highest power $N$ of the polynomial. The last entry is the coefficient of the power zero term of the polynomial.
Example: [0.5, 1, 1, 0.5]

## Dependencies

To enable this property, set the Frequency modulation parameter to Polynomial.

## Programmatic Use

Block Parameter:PolynomialCoefficients
Type:double
Values:vector
Default:[1 0 0]
Data Types: double
Sweep bandwidth (Hz) - Bandwidth of nonlinear FM sweep
100e3 (default) | positive scalar

Bandwidth of the linear FM sweep, specified as a positive scalar. Units are in Hz .
Example: 50e3

## Programmatic Use <br> Block Parameter:SweepBandwidth

Type:double
Values:positive scalar
Default:100e3
Sweep direction - Direction of nonlinear FM sweep
Up (default) | Down

Direction of nonlinear FM sweep as Up (increasing frequency) or Down (decreasing frequency).
Programmatic Use
Block Parameter:SweepDirection
Type:enum
Values:Up, Down
Default:Up
Sweep interval - FM frequency sweep interval
Positive (default)|Symmetric

FM frequency sweep interval, specified as Positive or Symmetric. If you set this parameter to Positive, the waveform sweeps the frequency interval between 0 and $B$, where $B$ is the value of the Sweep bandwidth parameter. If you set this parameter value to Symmetric, the waveform sweeps the interval between $-B / 2$ and $B / 2$.

Programmatic Use
Block Parameter:SweepInterval
Type:enum
Values:Symmetric, Positive
Default:Positive
Envelope function - FM signal amplitude envelope
Rectangular (default) | Gaussian | Hamming | Chebyshev | Hann | Kaiser | Taylor

FM signal amplitude envelope function, specified as Rectangular, Gaussian, Hamming, Chebyshev, Hann, Kaiser, or Taylor.

Programmatic Use
Block Parameter:Envelope
Type:enum
Values:Rectangular, Gaussian, Hamming, Chebyshev, Hann, Kaiser, or Taylor
Default:Rectangular
Source of Frequency Offset - Source of frequency offset
Property (default)| Input port

Source of frequency offset, specified as Property or Input port.

- When set to Property, the offset is determined by the value of the Frequency Offset parameter.
- When set to Input port, the offset is determined by the value of the FreqOffset port.

Programmatic Use
Block Parameter:FrequencyOffsetSource

```
Type:enum
Values:Property, Input Port
Default:Property
Frequency Offset (Hz) - Frequency offset
0 (default) | scalar
```

Frequency offset, specified as a scalar. Units are in Hz.
Example: 2e3
Dependencies
To enable this parameter set the Source of Frequency Offset parameter to Input port.
Programmatic Use
Block Parameter:Frequency0ffset
Type:double
Values:scalar
Default:0
Output signal format - Format of the output signal
Pulses (default) | Samples

The format of the output signal, specified as Pulses or Samples.
If you set this parameter to Samples, the output of the block consists of multiple samples. The number of samples is the value of the Number of samples in output parameter.

If you set this parameter to Pulses, the output of the block consists of multiple pulses. The number of pulses is the value of the Number of pulses in output parameter.

Programmatic Use
Block Parameter:0utputFormat
Type:enum
Values:Pulses Samples
Default:Pulses
Number of samples in output - Number of samples in output
100 (default) | positive integer

Number of samples in the block output, specified as a positive integer.
Example: 1000

## Dependencies

To enable this parameter, set the Output signal format parameter to Samples.
Programmatic Use
Block Parameter:NumSamples
Type:double
Values:positive scalar
Default:100

## Data Types: double

Number of pulses in output - Number of pulses in output
1 (default) | positive integer

Number of pulses in the block output, specified as a positive integer.
Example: 2

## Dependencies

To enable this parameter, set the Output signal format parameter to Pulses.

```
Programmatic Use
Block Parameter:NumPulses
Type:double
Values:positive scalar
Default:1
Data Types: double
```

Enable PRF Output - Enable output of PRF
off (default) | on

Select this parameter to enable the PRF output port.

## Dependencies

To enable this parameter, set Output signal format to Pulses.

## Programmatic Use

Block Parameter:PRFOutputPort
Type:enum
Values:off on
Default:off
Enable Matched Filter Coeficients Output - Enable output of matched filter coefficients
off (default) | on

Select this parameter to enable the Coeff output port.

```
Programmatic Use
Block Parameter:Coefficient0utputPort
Type:enum
Values:off on
Default:off
Simulate using - Block simulation method
Interpreted Execution (default)| Code Generation
```

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).

## Programmatic Use

Block Parameter:SimulateUsing
Type:enum
Values:Interpreted Execution, Code Generation
Default:Interpreted Execution

## Version History

## Introduced in R2023a

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using Simulink ${ }^{\circledR}$ Coder ${ }^{\mathrm{TM}}$.

## See Also

phased.NonlinearFMWaveform

## Phase Coded Waveform

Phase-coded pulse waveform

## Libraries:

Phase-Coded
Phased Array System Toolbox / Waveforms

## Description

The Phase-Coded Waveform block generates samples of a phase-coded pulse waveform with specified chip width, pulse repetition frequency (PRF), and phase code. The block outputs an integer number of pulses or samples.

## Ports

Input
PRFIdx - PRF Index
positive integer
Index to select the pulse repetition frequency (PRF), specified as a positive integer. The index selects the PRF from the predefined vector of values specified by the Pulse repetition frequency ( $\mathbf{H z}$ ) parameter.
Example: 4

## Dependencies

To enable this port, select Enable PRF selection input.
Data Types: double
FreqOffset - Frequency offset
scalar
Frequency offset in Hz , specified as a scalar.
Example: 2e3

## Dependencies

To enable this port, set Source of Frequency Offset to Input port.
Data Types: double

## Output

Y - Pulse waveform
complex-valued vector
Pulse waveform samples, returned as a complex-valued vector.
Data Types: double

PRF - Pulse repetition frequency
positive scalar
Pulse repetition frequency of current pulse, returned as a positive scalar.
Dependencies
To enable this port, set the Output signal format parameter to Pulses and then select the Enable PRF output parameter.

Data Types: double
Coeff - Matched filter coefficients
vector
Matched filter coefficients, returned as a vector.

## Dependencies

To enable this port, select Enable Matched Filter Coefficients Output.
Data Types: double

## Parameters

Sample rate (Hz) - Sample rate of the output waveform
1e6 (default) | positive scalar

Sample rate of the output waveform, specified as a positive scalar. Set the ratio of the Sample rate $(\mathrm{Hz})$ parameter to the Pulse repetition frequency $(\mathbf{H z})$ parameter to an integer.

- The ratio of Sample rate $(\mathbf{H z})$ to each element in the Pulse repetition frequency $(\mathbf{H z})$ vector must be an integer. This restriction is equivalent to requiring that the pulse repetition interval is an integral multiple of the sample interval.
- The product of Sample rate ( $\mathbf{H z}$ ) and Chip width (s) must be an integer. This restriction is equivalent to requiring that the chip width is an integer multiple of the sample interval.

Units are in Hz .

## Example: 5e3

Phase code - Code type used for phase modulation
Frank (default)

Code type used for phase modulation, specified as one of

- Barker
- Frank
- P1
- P2
- P3
- P4
- $P x$
- Zadoff-Chu

Example: P2
Chip width (s) - Chip time duration
1e-5 (default) | positive scalar

Duration of every chip in a phase-coded waveform, specified as a positive scalar. The value of this parameter must satisfy these constraints:

- The product of Chip width (s), Number of chips, and Pulse repetition frequency (Hz) must be less than or equal to one. This restriction is equivalent to requiring that the pulse length is less than the pulse repetition interval.
- The product of Sample rate (Hz) and Chip width (s) must be an integer. This restriction is equivalent to requiring that the chip width is an integer multiple of the sample interval.

Units are in seconds.
Example: 2e-4
Number of chips - Number of chips in waveform
4 (default) | positive integer

Number of chips in a phase-coded waveform, specified as a positive integer. The product of the Chip width (s), Number of chips, and Pulse repetition frequency (Hz) parameters must be less than or equal to one. This restriction is equivalent to requiring that the chip width is an integer multiple of the sample interval.

The table shows additional constraints on the number of chips for different code types.

| If the Phase code parameter is... | Then the Number of chips parameter must <br> be... |
| :--- | :--- |
| Frank, P1, or Px | A perfect square |
| P2 | An even number that is a perfect square |
| Barker | $2,3,4,5,7,11$, or 13 |

## Example: 9

Zadoff-Chu sequence index - Sequence index for Zadoff-Chu code type
1 (default) | positive integer
Sequence index for Zadoff-Chu code type, specified as a positive integer. The values of the ZadoffChu sequence index and the Number of chips parameters must be relatively prime.

## Example: 2

## Dependencies

To enable this parameter, set Phase Code to Zadoff-Chu.
Pulse repetition frequency $(\mathbf{H z})$ - Pulse repetition frequency
1e4 (default) | positive scalar

Pulse repetition frequency, $P R F$, specified as a scalar or a row vector. Units are in Hz . The pulse repetition interval, $P R I$, is the inverse of the pulse repetition frequency, $P R F$. The value of Pulse repetition frequency ( Hz ) must satisfy these constraints:

- The product of Pulse width and Pulse repetition frequency $\mathbf{( H z )}$ must be less than or equal to one. This condition expresses the requirement that the pulse width is less than one pulse repetition interval. For the phase-coded waveform, the pulse width is the product of the chip width and number of chips.
- The ratio of sample rate to any element of Pulse repetition frequency must be an integer. This condition expresses the requirement that the number of samples in one pulse repetition interval is an integer.

You can select the value of $P R F$ by using block parameter settings alone or in conjunction with the input port, PRFIdx.

- When the Enable PRF selection input parameter is not selected, set the PRF using block parameters.
- To implement a constant $P R F$, specify Pulse repetition frequency ( Hz ) as a positive scalar.
- To implement a staggered $P R F$, specify Pulse repetition frequency ( $\mathbf{H z}$ ) as a row vector with positive values. After the waveform reaches the last element of the vector, the process continues cyclically with the first element of the vector. When PRF is staggered, the time between successive output pulses cycles through the successive values of the PRF vector.
- When the Enable PRF selection input parameter is selected, you can implement a selectable $P R F$ by specifying Pulse repetition frequency ( $\mathbf{H z}$ ) as a row vector with positive real-valued entries. But this time, when you execute the block, select a $P R F$ by passing an index into the $P R F$ vector into the PRFIdx port.

In all cases, the number of output samples is fixed when you set the Output signal format to Samples. When you use a varying PRF and set Output signal format to Pulses, the number of output samples can vary.

```
Programmatic Use
Block Parameter:PRF
Type:double
Values:positive scalar
Default:1e6
Enable PRF selection input - Select predefined PRF
off (default) | on
```

Select this parameter to enable the PRFIdx port.

- When enabled, pass in an index into a vector of predefined PRFs. Set predefined PRFs using the Pulse repetition frequency $(\mathbf{H z})$ parameter.
- When not enabled, the block cycles through the vector of PRFs specified by the Pulse repetition frequency ( Hz ) parameter. If Pulse repetition frequency $(\mathbf{H z})$ is a scalar, the PRF is constant.

```
Programmatic Use
Block Parameter:PRFSelectionInputPort
```

Type:logical
Values:positive scalar
Default:off
Source of Frequency Offset - Source of frequency offset
Property (default)| Input port

Source of frequency offset, specified as Property or Input port.

- When set to Property, the offset is determined by the value of the Frequency Offset parameter.
- When set to Input port, the offset is determined by the value of the FreqOffset port.


## Programmatic Use

Block Parameter:Frequency0ffsetSource
Type:enum
Values:Property, Input Port
Default:Property
Frequency Offset (Hz) - Frequency offset
0 (default) | scalar

Frequency offset, specified as a scalar. Units are in Hz.
Example: 2e3

## Dependencies

To enable this parameter set the Source of Frequency Offset parameter to Input port.

## Programmatic Use

Block Parameter:Frequency0ffset
Type:double
Values:scalar
Default:0
Source of simulation sample time - Source of simulation sample time
Derive from waveform parameters (default)|Inherit from Simulink engine

Source of simulation sample time, specified as Derive from waveform parameters or Inherit from Simulink engine. When set to Derive from waveform parameters, the block runs at a variable rate determined by the PRF of the selected waveform. The elapsed time is variable. When set to Inherit from Simulink engine, the block runs at a fixed rate so the elapsed time is a constant.

## Dependencies

To enable this parameter, select the Enable PRF selection input parameter.
Programmatic Use
Block Parameter:SimulationTimeSource
Type:enum
Values:Derive from waveform parameters, Inherit from Simulink engine Default:Derive from waveform parameters

Output signal format - Format of the output signal
Pulses (default)| Samples

The format of the output signal, specified as Pulses or Samples.
If you set this parameter to Samples, the output of the block consists of multiple samples. The number of samples is the value of the Number of samples in output parameter.

If you set this parameter to Pulses, the output of the block consists of multiple pulses. The number of pulses is the value of the Number of pulses in output parameter.

Programmatic Use
Block Parameter:0utputFormat
Type:enum
Values:Pulses Samples
Default:Pulses
Number of samples in output - Number of samples in output
100 (default) | positive integer

Number of samples in the block output, specified as a positive integer.
Example: 1000
Dependencies
To enable this parameter, set the Output signal format parameter to Samples.

## Programmatic Use

Block Parameter:NumSamples
Type:double
Values:positive scalar
Default:100
Data Types: double
Number of pulses in output - Number of pulses in output
1 (default) | positive integer

Number of pulses in the block output, specified as a positive integer.
Example: 2

## Dependencies

To enable this parameter, set the Output signal format parameter to Pulses.
Programmatic Use
Block Parameter:NumPulses
Type:double
Values:positive scalar
Default:1
Data Types: double

Enable PRF Output - Enable output of PRF
off (default) | on

Select this parameter to enable the PRF output port.

## Dependencies

To enable this parameter, set Output signal format to Pulses.
Programmatic Use
Block Parameter:PRF0utputPort
Type:enum
Values:off on
Default:off
Enable Matched Filter Coeficients Output - Enable output of matched filter coefficients off (default) | on

Select this parameter to enable the Coeff output port.
Programmatic Use
Block Parameter:CoefficientOutputPort
Type:enum
Values:off on
Default:off
Simulate using - Block simulation method
Interpreted Execution (default)|Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).
Programmatic Use
Block Parameter:SimulateUsing
Type:enum
Values:Interpreted Execution, Code Generation
Default:Interpreted Execution

## Version History

Introduced in R2014b

## See Also

phased. PhaseCodedWaveform

## Phase Shift Beamformer

Narrowband phase-shift beamformer


## Libraries:

Phased Array System Toolbox / Beamforming

## Description

The Phase Shift Beamformer block performs delay-and-sum beamforming. The delay is approximated using the phase-shift approximation in the time domain.

## Ports

Input
$\mathbf{X}$ - Input signal
$M$-by- $N$ complex-valued matrix
Input signal, specified as an $M$-by- $N$ matrix, where $M$ is the number of samples in the data, and $N$ is the number of array elements.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

Data Types: double
Ang - Beamforming direction
2-by-1 real-valued vector | 2-by-L real-valued matrix
Beamforming direction, specified as a 2-by- $L$ real-valued matrix, where $L$ is the number of beamforming directions. Each column takes the form of [AzimuthAngle; ElevationAngle]. Angle units are in degrees. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive, and the elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive. Angles are defined with respect to the local coordinate system of the array.

## Dependencies

To enable this port, set the Source of beamforming direction parameter to Input port.

## Data Types: double

## Output

Y - Beamformed output
M-by-L complex-valued matrix
Beamformed output, returned as an $M$-by- $L$ complex-valued matrix. The quantity $M$ is the number of signal samples and $L$ is the number of desired beamforming directions specified by the Beamforming direction parameter or from the Ang port.

## Data Types: double

W - Beamforming weights
$N$-by-L complex-valued matrix
Beamformed weights, returned as an $N$-by- $L$ complex-valued matrix. The quantity $N$ is the number of array elements. When the Specify sensor array as parameter is set to Partitioned array or Replicated subarray, $N$ represents the number of subarrays. $L$ is the number of desired beamforming directions specified in the Ang port or by the Beamforming direction (deg) property. There is one set of weights for each beamforming direction.

## Dependencies

To enable this port, select the Enable weights output checkbox.
Data Types: double

## Parameters

Main tab
Signal propagation speed ( $\mathbf{m} / \mathbf{s}$ ) - Signal propagation speed
physconst('LightSpeed') (default) | real-valued positive scalar

Signal propagation speed, specified as a real-valued positive scalar. The default value of the speed of light is the value returned by physconst('LightSpeed'). Units are in meters per second.
Example: 3e8
Data Types: double
Operating frequency (Hz) - System operating frequency
3e8 (default) | positive real scalar

System operating frequency, specified as a positive scalar. Units are in Hz .
Source of beamforming direction - Source of beamforming direction
Property (default)|Input port

Source of beamforming direction, specified as Property or Input port. When you set Source of beamforming direction to Property, you then set the direction using the Beamforming direction (deg) parameter. When you select Input port, the direction is determined by the input to the Ang port.

Beamforming direction (deg) - Beamforming directions
2-by-L real-valued matrix

Beamforming directions, specified as a 2 -by- $L$ real-valued matrix, where $L$ is the number of beamforming directions. Each column takes the form [AzimuthAngle; ElevationAngle]. Angle units are in degrees. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$. Angles are defined with respect to the local coordinate system of the array.

## Dependencies

To enable this parameter, set the Source of beamforming direction parameter to Property.
Number of bits in phase shifters - Number of phase shift quantization bits
0 (default) | nonnegative integer

The number of bits used to quantize the phase shift component of beamformer or steering vector weights. Specify the number of bits as a non-negative integer. A value of zero indicates that no quantization is performed.

Weights normalizing method - Specify weights normalization method Distortionless (default)|Preserve power

Specify this parameter to set the weights normalizing method. Choose Distortionless to set the gain in the beamforming direction to zero dB. Choose Preserve power to set the norm of the weights to one.

Enable weights output - Option to output beamformer weights
off (default) | on

Select this check box to obtain the beamformer weights from the output port, W .
Simulate using - Block simulation method
Interpreted Execution (default) |Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).
Programmatic Use
Block Parameter:SimulateUsing
Type:enum
Values:Interpreted Execution, Code Generation
Default:Interpreted Execution

## Sensor Arrays Tab

Specify sensor array as - Method to specify array
Array (no subarrays) (default)|Partitioned array|Replicated subarray|MATLAB expression

Method to specify array, specified as Array (no subarrays) or MATLAB expression.

- Array (no subarrays) - use the block parameters to specify the array.
- Partitioned array - use the block parameters to specify the array.
- Replicated subarray - use the block parameters to specify the array.
- MATLAB expression - create the array using a MATLAB expression.

Expression - MATLAB expression used to create an array
Phased Array System Toolbox array System object

MATLAB expression used to create an array, specified as a valid Phased Array System Toolbox array System object.
Example: phased.URA('Size', [5,3])

## Dependencies

To enable this parameter, set Specify sensor array as to MATLAB expression.

## Element Parameters

Element type - Array element types
Isotropic Antenna (default)|Cosine Antenna|Custom Antenna|Omni Microphone| Custom Microphone

Antenna or microphone type, specified as one of the following:

- Isotropic Antenna
- Cosine Antenna
- Custom Antenna
- Omni Microphone
- Custom Microphone

Operating frequency range $(\mathbf{H z})$ - Operating frequency range of the antenna or microphone element
[0, 1e20] (default) | real-valued 1-by-2 row vector

Specify the operating frequency range of the antenna or microphone element as a 1-by-2 row vector in the form [LowerBound, UpperBound]. The element has no response outside this frequency range. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Isotropic Antenna, Cosine Antenna, or Omni Microphone.

Operating frequency vector ( Hz ) - Operating frequency range of custom antenna or microphone elements
[0, 1e20] (default) | real-valued row vector

Specify the frequencies at which to set antenna and microphone frequency responses as a 1-by-L row vector of increasing real values. The antenna or microphone element has no response outside the frequency range specified by the minimum and maximum elements of this vector. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone. Use Frequency responses (dB) to set the responses at these frequencies.

Baffle the back of the element - Set back response of an Isotropic Antenna element or an Omni Microphone element to zero
off (default) | on

Select this check box to baffle the back response of the element. When back baffled, the responses at all azimuth angles beyond $\pm 90^{\circ}$ from broadside are set to zero. The broadside direction is defined as $0^{\circ}$ azimuth angle and $0^{\circ}$ elevation angle.

## Dependencies

To enable this check box, set Element type to Isotropic Antenna or Omni Microphone.
Exponent of cosine pattern - Exponents of azimuth and elevation cosine patterns [1.5 1.5] (default) | nonnegative scalar | real-valued 1-by-2 matrix of nonnegative values

Specify the exponents of the cosine pattern as a nonnegative scalar or a real-valued 1-by-2 matrix of nonnegative values. When Exponent of cosine pattern is a 1-by-2 vector, the first element is the
exponent in the azimuth direction and the second element is the exponent in the elevation direction. When you set this parameter to a scalar, both the azimuth direction and elevation direction cosine patterns are raised to the same power.

## Dependencies

To enable this parameter, set Element type to Cosine Antenna.
Frequency responses (dB) - Antenna and microphone frequency response [0,0] (default) | real-valued row vector

Frequency response of a custom antenna or custom microphone for the frequencies defined by the Operating frequency vector ( Hz ) parameter. The dimensions of Frequency responses (dB) must match the dimensions of the vector specified by the Operating frequency vector $(\mathbf{H z})$ parameter.

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone.
Input Pattern Coordinate System - Coordinate system of custom antenna pattern
az-el (default)| phi-theta

Coordinate system of custom antenna pattern, specified az-el or phi-theta. When you specify azel, use the Azimuth angles (deg) and Elevations angles (deg) parameters to specify the coordinates of the pattern points. When you specify phi-theta, use the Phi angles (deg) and Theta angles (deg) parameters to specify the coordinates of the pattern points.

## Dependencies

To enable this parameter, set Element type to Custom Antenna.

## Azimuth angles (deg) - Azimuth angles of antenna radiation pattern

[-180:180] (default) | real-valued row vector

Specify the azimuth angles at which to calculate the antenna radiation pattern as a 1-by-P row vector. $P$ must be greater than 2. Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to az-el.

Elevation angles (deg) - Elevation angles of antenna radiation pattern
[-90:90] (default) | real-valued row vector

Specify the elevation angles at which to compute the radiation pattern as a 1-by- $Q$ vector. $Q$ must be greater than 2. Angle units are in degrees. Elevation angles must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to az-el.

Phi Angles (deg) - Phi angle coordinates of custom antenna radiation pattern
$0: 360$ | real-valued 1-by-P row vector

Phi angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by-P row vector. $P$ must be greater than 2 . Angle units are in degrees. Phi angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Theta Angles (deg) - Theta angle coordinates of custom antenna radiation pattern
0 : 180 | real-valued 1-by- $Q$ row vector

Theta angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by$Q$ row vector. $Q$ must be greater than 2 . Angle units are in degrees. Theta angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Magnitude pattern (dB) - Magnitude of combined antenna radiation pattern zeros $(181,361)$ (default) | real-valued $Q$-by-P matrix | real-valued $Q$-by- $P$-by- $L$ array

Magnitude of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector ( $\mathbf{H z}$ ).

- If this parameter is a $Q$-by-P matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (Hz) parameter.


## Dependencies

To enable this parameter, set Element type to Custom Antenna.

## Phase pattern (deg) - Custom antenna radiation phase pattern

zeros $(181,361)$ (default) | real-valued $Q$-by- $P$ matrix | real-valued $Q$-by- $P$-by- $L$ array

Phase of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector $(\mathbf{H z})$.

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathrm{Hz})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (


## Dependencies

To enable this parameter, set Element type to Custom Antenna.
MatchArrayNormal - Rotate antenna element to array normal
on (default) | off

Select this check box to rotate the antenna element pattern to align with the array normal. When not selected, the element pattern is not rotated.

When the antenna is used in an antenna array and the Input Pattern Coordinate System parameter is az-el, selecting this check box rotates the pattern so that the $x$-axis of the element coordinate system points along the array normal. Not selecting uses the element pattern without the rotation.

When the antenna is used in an antenna array and Input Pattern Coordinate System is set to phitheta, selecting this check box rotates the pattern so that the $z$-axis of the element coordinate system points along the array normal.

Use the parameter in conjunction with the Array normal parameter of the URA and UCA arrays.

## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Polar pattern frequencies (Hz) - Polar pattern microphone response frequencies 1 e3 (default) | real scalar | real-valued 1-by-L row vector

Polar pattern microphone response frequencies, specified as a real scalar, or a real-valued, 1-by-L vector. The response frequencies lie within the frequency range specified by the Operating frequency vector $(\mathrm{Hz})$ vector.

## Dependencies

To enable this parameter, set Element type set to Custom Microphone.
Polar pattern angles (deg) - Polar pattern response angles
[-180:180] (default) | real-valued -by-P row vector

Specify the polar pattern response angles, as a 1-by- $P$ vector. The angles are measured from the central pickup axis of the microphone and must be between $-180^{\circ}$ and $180^{\circ}$, inclusive.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.
Polar pattern (dB) - Custom microphone polar response
zeros (1,361) (default) | real-valued L-by-P matrix

Specify the magnitude of the custom microphone element polar patterns as an $L$-by- $P$ matrix. $L$ is the number of frequencies specified in Polar pattern frequencies $(\mathbf{H z}) . P$ is the number of angles specified in Polar pattern angles (deg). Each row of the matrix represents the magnitude of the polar pattern measured at the corresponding frequency specified in Polar pattern frequencies (Hz) and all angles specified in Polar pattern angles (deg). The pattern is measured in the azimuth plane. In the azimuth plane, the elevation angle is $0^{\circ}$ and the central pickup axis is $0^{\circ}$ degrees azimuth and $0^{\circ}$ degrees elevation. The polar pattern is symmetric around the central axis. You can construct the microphone response pattern in 3-D space from the polar pattern.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.

## Array Parameters

## Geometry - Array geometry

ULA (default) | URA | UCA | Conformal Array

Array geometry, specified as one of

- ULA - Uniform linear array
- URA - Uniform rectangular array
- UCA - Uniform circular array
- Conformal Array - arbitrary element positions

Number of elements - Number of array elements
2 for ULA arrays and 5 for UCA arrays (default) | integer greater than or equal to 2

The number of array elements for ULA or UCA arrays, specified as an integer greater than or equal to 2.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

## Dependencies

To enable this parameter, set Geometry to ULA or UCA.
Element spacing (m) - Spacing between array elements
0.5 for ULA arrays and [0.5, 0.5] for URA arrays (default) | positive scalar for ULA or URA arrays | 2 -element vector of positive values for URA arrays

Spacing between adjacent array elements:

- ULA - specify the spacing between two adjacent elements in the array as a positive scalar.
- URA - specify the spacing as a positive scalar or a 1 -by-2 vector of positive values. If Element spacing (m) is a scalar, the row and column spacings are equal. If Element spacing (m) is a vector, the vector has the form [SpacingBetweenArrayRows,SpacingBetweenArrayColumns].
- When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.


## Dependencies

To enable this parameter, set Geometry to ULA or URA.
Array axis - Linear axis direction of ULA
$y$ (default) $|x| z$

Linear axis direction of ULA, specified as $y, x$, or $z$. All ULA array elements are uniformly spaced along this axis in the local array coordinate system.

## Dependencies

- To enable this parameter, set Geometry to ULA.
- This parameter is also enabled when the block only supports ULA arrays.

Array size - Dimensions of URA array
[2,2] (default) | positive integer | 1-by-2 vector of positive integers

Dimensions of a URA array, specified as a positive integer or 1-by-2 vector of positive integers.

- If Array size is a 1 -by- 2 vector, the vector has the form [NumberOfArrayRows, NumberOfArrayColumns].
- If Array size is an integer, the array has the same number of rows and columns.
- When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

For a URA, array elements are indexed from top to bottom along the leftmost column, and then continue to the next columns from left to right. In this figure, the Array size value of [3, 2] creates an array having three rows and two columns.

Size and Element Indexing Order
for Uniform Rectangular Arrays
Example: Size $=[3,2]$


## Dependencies

To enable this parameter, set Geometry to URA.
Element lattice - Lattice of URA element positions
Rectangular (default) |Triangular

Lattice of URA element positions, specified as Rectangular or Triangular.

- Rectangular - Aligns all the elements in row and column directions.
- Triangular - Shifts the even-row elements of a rectangular lattice toward the positive row-axis direction. The displacement is one-half the element spacing along the row dimension.


## Dependencies

To enable this parameter, set Geometry to URA.
Array normal - Array normal direction
$x$ for URA arrays or $z$ for UCA arrays (default) | y

Array normal direction, specified as $x, y$, or $z$.
Elements of planar arrays lie in a plane orthogonal to the selected array normal direction. Element boresight directions point along the array normal direction.

| Array Normal Parameter Value | Element Positions and Boresight Directions |
| :--- | :--- |
| x | Array elements lie in the $y z$-plane. All element <br> boresight vectors point along the $x$-axis. |
| y | Array elements lie in the $z x$-plane. All element <br> boresight vectors point along the $y$-axis. |

# Array Normal Parameter Value 

Element Positions and Boresight Directions
Z

Array elements lie in the xy-plane. All element boresight vectors point along the $z$-axis.

## Dependencies

To enable this parameter, set Geometry to URA or UCA.
Radius of UCA ( $\mathbf{m}$ ) - UCA array radius
0.5 (default) | positive scalar

Radius of UCA array, specified as a positive scalar.

## Dependencies

To enable this parameter, set Geometry to UCA.
Element positions (m) - Positions of conformal array elements
[0;0;0] (default) | 3-by-Nmatrix of real values

Positions of the elements in a conformal array, specified as a 3 -by- $N$ matrix of real values, where $N$ is the number of elements in the conformal array. Each column of this matrix represents the position [ $x ; y ; z$ ] of an array element in the array local coordinate system. The origin of the local coordinate system is ( $0,0,0$ ). Units are in meters.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

## Dependencies

To enable this parameter set Geometry to Conformal Array.
Element normals (deg) - Direction of conformal array element normal vectors [0;0] | 2-by-1 column vector | 2 -by-N matrix

Direction of element normal vectors in a conformal array, specified as a 2-by-1 column vector or a 2-by- $N$ matrix. $N$ indicates the number of elements in the array. For a matrix, each column specifies the normal direction of the corresponding element in the form [azimuth; elevation] with respect to the local coordinate system. The local coordinate system aligns the positive $x$-axis with the direction normal to the conformal array. If the parameter value is a 2 -by- 1 column vector, the same pointing direction is used for all array elements.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

You can use the Element positions (m) and Element normals (deg) parameters to represent any arrangement in which pairs of elements differ by certain transformations. The transformations can combine translation, azimuth rotation, and elevation rotation. However, you cannot use transformations that require rotation about the normal direction.

## Dependencies

To enable this parameter, set Geometry to Conformal Array.

Taper - Array element tapers
1 (default) | complex-valued scalar | complex-valued row vector

Element tapering, specified as a complex-valued scalar or a complex-valued 1-by- $N$ row vector. In this vector, $N$ represents the number of elements in the array.

Also known as element weights, tapers multiply the array element responses. Tapers modify both amplitude and phase of the response to reduce side lobes or steer the main response axis.

If Taper is a scalar, the same weight is applied to each element. If Taper is a vector, a weight from the vector is applied to the corresponding sensor element. The number of weights must match the number of elements of the array.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

Subarray definition matrix - Define elements belonging to subarrays
logical matrix

Specify the subarray selection as an $M$-by- $N$ matrix. $M$ is the number of subarrays and $N$ is the total number of elements in the array. Each row of the matrix represents a subarray and each entry in the row indicates when an element belongs to the subarray. When the entry is zero, the element does not belong the subarray. A nonzero entry represents a complex-valued weight applied to the corresponding element. Each row must contain at least one nonzero entry.

The phase center of each subarray lies at the subarray geometric center. The subarray geometric center depends on the Subarray definition matrix and Geometry parameters.

## Dependencies

To enable this parameter, set Specify sensor array as to Partitioned array.
Subarray steering method - Specify subarray steering method None (default) | Phase | Time

Subarray steering method, specified as one of

- None
- Phase
- Time
- Custom

Selecting Phase or Time opens the Steer input port on the Narrowband Receive Array, Narrowband Transmit Array, Wideband Receive Array, Wideband Transmit Array blocks, Constant Gamma Clutter, and GPU Constant Gamma Clutter blocks.

Selecting Custom opens the WS input port on the Narrowband Receive Array, Narrowband Transmit Array, Wideband Receive Array, Wideband Transmit Array blocks, Constant Gamma Clutter, and GPU Constant Gamma Clutter blocks.

## Dependencies

To enable this parameter, set Specify sensor array as to Partitioned array or Replicated subarray.

Phase shifter frequency (Hz) - Subarray phase shifting frequency
3.0e8 (default) | positive real-valued scalar

Operating frequency of subarray steering phase shifters, specified as a positive real-valued scalar. Units are Hz.

## Dependencies

To enable this parameter, set Sensor array to Partitioned array or Replicated subarray and set Subarray steering method to Phase.

Number of bits in phase shifters - Subarray steering phase shift quantization bits
0 (default) | non-negative integer

Subarray steering phase shift quantization bits, specified as a non-negative integer. A value of zero indicates that no quantization is performed.

## Dependencies

To enable this parameter, set Sensor array to Partitioned array or Replicated subarray and set Subarray steering method to Phase.

Subarrays layout - Subarray position specification
Rectangular (default) | Custom

Specify the layout of replicated subarrays as Rectangular or Custom.

- When you set this parameter to Rectangular, use the Grid size and Grid spacing parameters to place the subarrays.
- When you set this parameter to Custom, use the Subarray positions (m) and Subarray normals parameters to place the subarrays.


## Dependencies

To enable this parameter, set Sensor array to Replicated subarray
Grid size - Dimensions of rectangular subarray grid [1,2] (default)

Rectangular subarray grid size, specified as a single positive integer, or a 1-by-2 row vector of positive integers.

If Grid size is an integer scalar, the array has an equal number of subarrays in each row and column. If Grid size is a 1-by-2 vector of the form [NumberOfRows, NumberOfColumns], the first entry is the number of subarrays along each column. The second entry is the number of subarrays in each row. A row is along the local $y$-axis, and a column is along the local $z$-axis. The figure here shows how you can replicate a 3-by-2 URA subarray using a Grid size of [1,2].
$3 \times 2$ Element URA
Replicated on a $1 \times 2$ Grid


## Dependencies

To enable this parameter, set Sensor array to Replicated subarray and Subarrays layout to Rectangular.

Grid spacing ( $\mathbf{m}$ ) - Spacing between subarrays on rectangular grid
Auto (default) | positive real-valued scalar | 1-by-2 vector of positive real-values

The rectangular grid spacing of subarrays, specified as a positive, real-valued scalar, a 1-by-2 row vector of positive, real-values, or Auto. Units are in meters.

- If Grid spacing is a scalar, the spacing along the row and the spacing along the column is the same.
- If Grid spacing is a 1-by-2 row vector, the vector has the form
[SpacingBetweenRows, SpacingBetweenColumn]. The first entry specifies the spacing between rows along a column. The second entry specifies the spacing between columns along a row.
- If Grid spacing is set to Auto, replication preserves the element spacing of the subarray for both rows and columns while building the full array. This option is available only when you specify Geometry as ULA or URA.


## Dependencies

To enable this parameter, set Sensor array to Replicated subarray and Subarrays layout to Rectangular.

Subarray positions (m) - Positions of subarrays
[0,0;0.5,0.5;0,0] (default)| 3-by-N real-valued matrix

Positions of the subarrays in the custom grid, specified as a real 3-by- $N$ matrix, where $N$ is the number of subarrays in the array. Each column of the matrix represents the position of a single subarray in the array local coordinate system. The coordinates are expressed in the form $[x ; y ; z]$. Units are in meters.

## Dependencies

To enable this parameter, set Sensor array to Replicated subarray and Subarrays layout to Custom.

Subarray normals - Direction of subarray normal vectors
[0,0;0,0] (default) | 2 -by- $N$ real matrix

Specify the normal directions of the subarrays in the array. This parameter value is a 2 -by- $N$ matrix, where $N$ is the number of subarrays in the array. Each column of the matrix specifies the normal direction of the corresponding subarray, in the form [azimuth; elevation]. Angle units are in degrees. Angles are defined with respect to the local coordinate system.

You can use the Subarray positions and Subarray normals parameters to represent any arrangement in which pairs of subarrays differ by certain transformations. The transformations can combine translation, azimuth rotation, and elevation rotation. However, you cannot use transformations that require rotation about the normal.

## Dependencies

To enable this parameter, set the Sensor array parameter to Replicated subarray and the Subarrays layout to Custom.

## Version History

Introduced in R2014b

See Also<br>phased.PhaseShiftBeamformer

## Motion Platform

Motion platform



## Libraries:

Phased Array System Toolbox / Environment and Target

## Description

The Motion Platform block models the motion of multiple platforms such as airplanes, ground vehicles, and/or receiving and transmitting sensors arrays, determining their positions and velocities. The platforms move along trajectories determined by initial positions and velocities, according to which motion model you choose - the velocity or acceleration model. The platform positions and velocities are updated at each simulation step. In addition, you can specify initial orientations for the platforms and obtain orientation updates.

## Ports

## Input

Ref - Reference time input
scalar
Reference time input, specified as a scalar. Units are in seconds.

## Dependencies

To enable this port, set the Source of elapsed simulation time parameter to Derive from reference input port.
Data Types: double
Vel - Platform velocity input
real-valued 3 -by- $N$ matrix
Platform velocity, specified as a real-valued 3 -by- $N$ matrix where $N$ is the number of platforms to model. Units are meters per second.

## Dependencies

To enable this port, set the Model of object motion parameter to Velocity and the Source of velocity parameter to Input port.

Data Types: double
Acl - Platform acceleration input
real-valued 3 -by- $N$ matrix
Platform acceleration input, specified as a real-valued 3-by- $N$ matrix where $N$ is the number of platforms to model. Units are meters per second-squared.

## Dependencies

To enable this port, set the Model of object motion parameter to Acceleration and the Source of acceleration parameter to Input port.

## Data Types: double

## Output

Pos - Platform position output
real-valued 3 -by- $N$ matrix
Current position of platform, returned as a real-valued 3-by-1 column vector in the form of $[x ; y ; z]$ or a real-valued 3 -by- $N$ matrix where $N$ is the number of platforms to model. Each column takes the form [x;y;z]. Units are meters.

## Data Types: double

Vel - Platform velocity output
real-valued 3 -by- $N$ matrix
Current velocity of platform, specify as a real-valued 3-by-1 column vector in the form of [vx; vy; vz] or a real-valued 3 -by- $N$ matrix where $N$ is the number of platforms to model. Each column taking the form [ $\mathrm{vx} ; \mathrm{vy} ; \mathrm{vz}$ ]. Velocity units are meters per second.
Data Types: double
LAxes - Platform orientation output
real-valued 3-by-3-by-N matrix
Current platform orientation axes, returned as real-valued 3-by-3-by- $N$ matrix where $N$ is the number of platforms to model. Each 3-by-3 submatrix is an orthonormal matrix. This output is enabled when you set the OrientationAxesOutputPort property to true. The current platform axes rotate around the normal vector to the path of the platform.

## Dependencies

To enable this port, select the Enable orientation axes output check box.

## Data Types: double

## Parameters

Model of object motion - Object motion model

## Velocity (default) |Acceleration | Custom

Specify the object motion model as Velocity, Acceleration, or Custom. When you set this parameter to Velocity, the platform follows a constant velocity trajectory during each simulation step. When you set this parameter to Acceleration, the platform follows a constant acceleration trajectory during each simulation step. When you set the parameter to Custom, the platform motion follows a sequence of waypoints specified by the Custom trajectory waypoints parameter. The object performs a piecewise cubic interpolation on the waypoints to derive the position and velocity at each time step.

Initial position (m) - Initial position of platform

## [0;0;0] (default)

Specify the initial position of the platform in meters as a $3-b y-N$ matrix where each column represents the initial position of a platform in the form $[x ; y ; z]$. The quantity $N$ is the number of platforms.

Initial velocity (m/s) - Initial velocity of platform
[0;0;0] (default)
Specify the initial velocity of the platform in $\mathrm{m} / \mathrm{s}$ as a $3-\mathrm{by}-N$ matrix where each column represents the initial velocity of a platform in the form [vx; vy;vz]. The quantity $N$ is the number of platforms.

## Dependencies

This parameter appears only when you set the Source of velocity or the Source of acceleration parameters to Input port.

Source of velocity - Source of velocity data

## Property (default)|Input port

This parameter appears only when you set the Model of object motion parameter to Velocity. Then, you must supply velocity data for the model. Specify the Source of velocity data as either coming from a Property or an Input port.

| Source of velocity | Use these model parameters or ports |
| :--- | :--- |
| Property | Initial position (m) parameter <br> Velocity (m/s) parameter |
| Input port | Initial position (m) parameter <br> Initial velocity (m/s) parameter <br> Vel input port |

## Dependencies

This parameter appears only when you set the Model of object motion parameter to Velocity.
Velocity (m/s) - Current velocity of platform

## [0;0;0] (default)

Specify the current velocity of the platforms in $\mathrm{m} / \mathrm{s}$ as a 3-by- $N$ matrix where each column represents the current velocity of a platform in the form [vx;vy;vz].

## Dependencies

This parameter appears only when you set the Model of object motion parameter to Velocity and set the Source of velocity parameter to Property.

Source of acceleration - Source of acceleration data
Property (default) | Input port

This parameter appears only when you set the Model of object motion parameter to Acceleration. Then, you must supply acceleration values for the model. Specify the Source of acceleration data as either coming from a Property or an Input port.

| Source of acceleration | Use these model parameters or ports |
| :--- | :--- |
| Property | Initial Position (m) parameter <br> Initial Velocity (m/s) parameter <br> Acceleration (m/s^2) parameter |
| Input port | Initial Position (m) parameter <br> Initial Velocity (m/s) parameter <br> Acl input port |

## Dependencies

This parameter appears only when you set the Model of object motion parameter to Acceleration.

Acceleration (m/s^2) - Acceleration of platform

## [0;0;0] (default)

Specify the current acceleration of the platforms in $\mathrm{m} / \mathrm{s}^{\wedge} 2$ as a 3 -by- $N$ matrix where each column represents the current acceleration of a platform in the form [ax;ay;az].

## Dependencies

This parameter appears when you set the Model of object motion parameter to Acceleration and set the Source of acceleration parameter to Property.

Custom trajectory waypoints - Custom trajectory waypoints
$[0,0,0,0,0,0,0 ; 1,0,0,0,0,0,0]$ (default)
Custom trajectory waypoints, specified as a real-valued $M$-by- $L$ matrix, or $M$-by- $L$-by- $N$ array. $M$ is the number of waypoints. $L$ is either 4 or 7 .

- When $L$ is 4 , the first column indicates the times at which the platform position is measured. Columns 2-4 are position measurements in $\mathrm{x}, \mathrm{y}$, and z coordinates. The velocity is derived from the position measurements.
- When $L$ is 7, columns 5-7 in the matrix are velocity measurements in $\mathrm{x}, \mathrm{y}$, and z coordinates.

When you set the Custom trajectory waypoints parameter to a three-dimensional array, the number of pages, $N$, represent the number of platforms. Time units are in seconds, position units are in meters, and velocity units are in meters per second.

## Dependencies

To enable this property, set the Model of object motion property to Custom.
Mechanical scanning mode - Mechanical scanning mode

## None (default)|Circular|Sector

Mechanical scan mode for platform, specified as None, Circular, or Sector, where None is the default. When you set the Mechanical scanning mode parameter to Circular, the platform scan clockwise 360 degrees continuously in the azimuthal direction of the platform orientation axes. When you set the Mechanical scanning mode parameter to Sector, the platform scans clockwise in the azimuthal direction in the platform orientation axes within a range specified by the Azimuth scan angle span (deg) parameter. When the platform scan reaches the span limits, the scan reverses direction and scans back to the other scan limit. Scanning happens within the orientation axes of the platform.

Initial scan angle (deg) - Initial scan angle of platform
0 (default)
Initial scan angle of platform, specified as a $1-$ by- $N$ vector where $N$ is the number of platforms. The scanning occurs in the local coordinate system of the platform. The Initial orientation axes parameter specifies the original local coordinate system. At the start of the simulation, the orientation axes specified by the Initial orientation axes are rotated by the angle specified in the InitialScanAngleInitial scan angle (deg) parameter. The default value is zero. Units are in degrees.

## Dependencies

This parameter applies when you set the Mechanical scanning mode parameter to Circular or Sector.

## Azimuth scan angle span (deg) - Azimuth span

[-60,60] (default)
Specify the azimuth angle span as an $N$-by- 2 matrix where $N$ is the number of platforms. Each row of the matrix specifies the scan range of the corresponding platform in the form
[ScanAngleLowerBound ScanAngleHigherBound]. The default value is [-60 60]. Units are in degrees.

## Dependencies

To enable this parameter, set the Mechanical scanning mode parameter to Sector.

## Azimuth scan rate (deg/s) - Azimuth scan rate

10 (default)
Specify the azimuth scan rate as a 1 -by- $N$ vector where $N$ is the number of platforms. Each entry in the vector is the azimuth scan rate for the corresponding platform. The default value is 10 degrees/ second. Units are in degrees/second.

## Dependencies

To enable this parameter, set the Mechanical scanning mode parameter to Circular or Sector.
Initial orientation axes - Initial orientation axes of platform
eye(3) (default)

Specify the three axes that define the initial local $(x, y, z)$ coordinate system at the platform as a 3-by-3-by- $N$ matrix. Each column of the matrix represents an axis of the local coordinate system. The three axes must be orthonormal.

Enable orientation axes output - Output orientation axes
off (default) | on
Select this check box to obtain the instantaneous orientation axes of the platform via the output port LAxes. The port appears only when the check box is selected.

Source of elapsed simulation time - Source of elapsed simulation time
Auto (default)|Derive from reference input port
Specify the source for elapsed simulation time as Auto or Derive from reference input port. When you choose Auto, the block computes the elapsed time. When you choose Derive from reference input port, the block uses the time duration of a reference signal passed into the Ref input port.

Inherit sample rate - Inherit sample rate from upstream blocks
on (default) | off

Select this parameter to inherit the sample rate from upstream blocks. Otherwise, specify the sample rate using the Sample rate (Hz) parameter.
Data Types: Boolean
Sample rate (Hz) - Sampling rate of signal
le6 (default) | positive real-valued scalar

Specify the signal sampling rate as a positive scalar. Units are in Hz.

## Dependencies

To enable this parameter, clear the Inherit sample rate check box.
Data Types: double
Simulate using - Block simulation method
Interpreted Execution (default) |Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).

## Programmatic Use

Block Parameter:SimulateUsing
Type:enum
Values:Interpreted Execution, Code Generation
Default:Interpreted Execution

## Version History

Introduced in R2014b

## See Also

phased.Platform

## Pulse Integrator

Coherent or noncoherent pulse integration

$>\times$| Coherent |
| :--- |
| 10-Pulse |
| Integrator |$\quad \Sigma \times>$

## Libraries:

Phased Array System Toolbox / Detection

## Description

The Pulse Integrator block performs coherent or noncoherent integration of successive pulses of a signal and puts out an integrated output. You can specify how many pulses to integrate and the number of overlapped pulses in successive integrations.

## Ports

Input
$\mathbf{x}$ - Pulse input data
matrix
Pulse input data, specified as a matrix. Each column of $x$ is one pulse.
Data Types: double
Output
£x - Integrated pulse
column vector
Integrated pulse, returned as an $N$-by- 1 column vector, where $N$ is the number of rows in the input x .
Data Types: double

## Parameters

Integration method - Integration method

## Coherent (default) | Noncoherent

Specify the integration method as Coherent or Noncoherent.
Number of pulses to integrate - Number of pulses to integrate
10 (default)
Specify the number of pulses to integrate as an integer.
Integration overlap (in pulses) - Integration overlap
0 (default)

Specify the number of overlapped pulses in successive integrations as an integer. This number must be less than the value specified in Number of pulses to integrate.

## Version History

Introduced in R2014b

## See Also

pulsint

## Radar Target

Radar target


## Libraries:

Phased Array System Toolbox / Environment and Target

## Description

The Radar Target block models a radar target that reflects the signal according to the specified radar cross section (RCS). The block supports a non-fluctuating target model and all four Swerling target models. The block does not support polarized signals.

## Ports

Input
X - Incident signal
complex-valued $N$-by-1 column vector | complex-valued $N$-by- $M$ matrix
Incident signal, specified as a complex-valued $N$-by- 1 column vector or complex-valued $N$-by- $M$ matrix. The value $M$ is the number of signals. Each signal corresponds to a different target. The value $N$ is the number of samples in each signal.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

## Data Types: double

## RCS - Mean radar cross-section

nonnegative scalar | 1 -by- $M$ row vector of nonnegative values
Mean radar cross-section, specified as nonnegative scalar or 1-by- $M$ row vector of nonnegative values. $M$ is the number of targets. This parameter applies to fluctuating and non-fluctuating targets. If you specify $M$ incident signals, you can specify the radar cross-section as a scalar or as a 1-by-M vector. For a scalar, the same value will be applied to all signals. Units are in $\mathrm{m}^{2}$.

## Dependencies

To enable this port, set the Source of mean radar cross section pull down menu to Input port.

## Data Types: double

Update - Indicator to update radar cross-section
$0 \mid 1$
Indicator to update radar cross-section for fluctuating targets, specified as 0 or 1 . When set to 0 , the radar cross-section is constant. When set to 1 , the radar cross-section fluctuates.

## Dependencies

To enable this port, set the Fluctuation model pull down menu to anything except Nonfluctuating.

Data Types: double

## Output

Out - Reflected signal
complex-valued $N$-by-1 column vector | complex-valued $N$-by- $M$ matrix
Reflected signal, returned as a complex-valued $N$-by- 1 column vector or complex-valued $N$-by- $M$ matrix. The value $M$ is the number of signals. Each signal corresponds to a different target. The value $N$ is the number of samples in each signal.

## Parameters

Source of mean radar cross section - Source of mean radar cross section
Property (default)|Input port
Specify whether the target's mean radar cross-section (RCS) value comes from the Mean radar cross section parameter of this block or from an input port. Values of this parameter are

| Property | The Mean radar cross section parameter for this block <br> specifies the mean RCS value. |
| :--- | :--- |
| Input port | Choosing this value creates the RCS input port to specify the <br> mean radar cross-section. |

Mean radar cross section ( $\mathbf{m}^{\wedge} \mathbf{2}$ ) - Mean radar cross section
1
Specify the mean value of the target's radar cross section, in square meters, as a nonnegative scalar. This parameter appears only when the Source of mean radar cross section parameter is set to Property.

Fluctuation model - Fluctuation model
Nonfluctuating (default) | Swerling1 | Swerling2 | Swerling3 | Swerling4
Specify the statistical model of the target as one of Nonfluctuating, Swerling1, Swerling2, Swerling3, or Swerling4. Setting this parameter to a value other than Nonfluctuating, allows setting cross-sections parameters via an input port, Update.

Propagation speed (m/s) - Signal propagation speed
physconst('LightSpeed') (default)| positive scalar

Signal propagation speed, specified as a real-valued positive scalar. The default value of the speed of light is the value returned by physconst('LightSpeed').
Data Types: double

Operating frequency (Hz) - Operating frequency

## $3 e 8$ (default) | positive real scalar

Specify the carrier frequency of the signal that reflects from the target, as a positive scalar in hertz.
Simulate using - Block simulation method
Interpreted Execution (default) | Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).

Programmatic Use<br>Block Parameter:SimulateUsing<br>Type:enum<br>Values:Interpreted Execution, Code Generation<br>Default:Interpreted Execution

## Version History

## Introduced in R2014b

## See Also

phased.RadarTarget

## Range Angle Calculator

Range and angle calculations


## Libraries:

Phased Array System Toolbox / Environment and Target

## Description

The Range Angle Calculator block calculates the range and/or the azimuth and elevation angles of several positions with respect to a reference position and with respect to a reference axes orientation. The reference position and reference axes can be specified in the block dialog or passed in through input ports.

## Ports

## Input

Pos - Source point position
real-valued 3 -by-1 vector | real-valued 3 -by- $N$ matrix
Source point position, specified as a real-valued 3-by-1 vector or a real-valued 3-by- $N$ matrix where $N$ is the number of source points. Each column contains the Cartesian coordinates of a point in the form [x;y;z].

When Pos is a 3 -by- $N$ matrix, you must specify RefPos as a 3 -by- $N$ matrix for $N$ reference positions. If all the reference points are identical, you can specify RefPos by a single 3-by-1 vector. Units are in meters.
Example: [1000;2000;50]
Data Types: double
RefPos - Reference point position
[0;0;0] (default) | real-valued 3-by-1 vector | real-valued 3-by-N matrix
Reference point position, specified as a real-valued 3-by-1 vector or a real-valued 3-by- N matrix where $N$ is the number of reference points. Each column contains the Cartesian coordinates of point in the form $[x ; y ; z]$.

When RefPos is a 3 -by- $N$ matrix, you must specify Pos as a 3 -by- $N$ matrix for $N$ source positions. If all the source points are identical, you can specify Pos by a single 3-by-1 vector. Reference position units are meters.

## Example: [100;100;10]

## Dependencies

To enable this port, set the Reference position source drop down menu to Input port.
Data Types: double

RefAxes - Local coordinate system axes
[1 0 0;0 1 0;0 0 1] (default) | real-valued 3-by-3 vector | real-valued 3-by-3-by-N array
Local coordinate system axes, specified as a real-valued 3-by-3 matrix or a 3-by-3-by- $N$ array. For an array, each page corresponds to a local coordinate axes at each reference point. The columns in RefAxes specify the direction of the coordinate axes for the local coordinate system in Cartesian coordinates. $N$ must match the number of columns in Pos or RefPos when these dimensions are greater than one.
Example: [100;100;10]

## Dependencies

To enable this port, set the Reference axes source drop down menu to Input port.
Data Types: double

## Output

Ang - Azimuth and elevation angles
real-valued 2-by- $N$ matrix | real-valued 2-by-2N matrix
Azimuth and elevation angles in degrees, returned as a 2 -by- $N$ matrix or 2 -by- $2 N$ matrix. Each column represents a direction angle in the form [azimuth;elevation].

When Propagation model is set to Free space, Ang is a 2 -by- $N$ matrix and represents the angle of the path from a source point to a reference point.

When Propagation model is set to Two-ray, Ang is a 2 -by- $2 N$ matrix. Alternate columns of Ang refer to the line-of-sight path and reflected path, respectively.

## Dependencies

To enable this port, set the Output(s) drop down menu to Angle or Range and Angle.
Data Types: double
Range - Propagation range
real-valued 1-by- $N$ vector | real-valued 1-by- $2 N$ vector
Propagation range, returned as a real-valued 1-by- $N$ vector or real-valued 1-by- $2 N$ vector.
When Propagation model is set to Free space, the size of Range is 1-by- $N$. The propagation range is the length of the direct path from the position defined in Pos to the corresponding reference position defined in RefPos.

When Propagation model is set to Two-ray, Range contains the ranges for the direct path and the reflected path. Alternate columns of Range refer to the line-of-sight path and reflected path, respectively for the same source-reference point pair.

## Dependencies

To enable this port, set the Output(s) drop down menu to Range or Range and Angle.

[^8]
## Parameters

Propagation model - Propagation model
Free space (default)|Two-ray
Specify the propagation model by setting this parameter to Free space or Two-ray.
Reference position source - Reference position source
Property (default)|Input port
Specify the reference position source by setting this parameter to Property or Input port. If Reference position source is set to Property, set the position using the Reference position parameter. If Reference position source is set to Input port, use the input port labeled RefPos.

Reference position - Reference position
[0;0;0] (default)
Specify the reference position as a 3-by-1 vector of rectangular coordinates in meters in the form [x;y;z]. The reference position serves as the origin of the local coordinate system. Ranges and angles of the input positions are measured with respect to the reference position. This parameter appears only when Reference position source is set to Property.

Reference axes source - Reference axes source
Property (default)|Input port
Specify the reference axes source by setting this parameter to Property or Input port. If Reference axes source is set to Property, set the axes using the Reference axes parameter. If Reference axes source is set to Input port, use the input port labeled RefAxes.

## Reference axes - Reference axes

eye(3)
Specify the reference axes of the local coordinate system with which to calculate range and angles in the form of a 3-by-3 orthonormal matrix. Each column of the matrix specifies the direction of an axis for the local coordinate system in the form of [x; y; z] with origin at the reference position. This parameter appears only when Reference axes source is set to Property.

Output(s) - Output(s)
Angle (default) | Range | Range and Angle
Specify the desired output(s) of the block. Each type of output is sent to a different port depending on the parameter value.

| Value | Port |
| :--- | :--- |
| Angle | Ang |
| Range | Range |


| Value | Port |
| :--- | :--- |
| Range and Angle | Ang and Range |

Simulate using - Block simulation method
Interpreted Execution (default)|Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).

Programmatic Use<br>Block Parameter:SimulateUsing<br>Type:enum<br>Values:Interpreted Execution, Code Generation<br>Default:Interpreted Execution

## Version History

Introduced in R2014b

## See Also

rangeangle

## Range-Angle Response

Obtain range-angle response map for array


## Libraries:

Phased Array System Toolbox / Detection

## Description

The Range-Angle Response block computes the range-angle map of an input signal. The output response is a matrix or a three-dimensional array whose rows represent range gates and columns represent angles. Pages represent

## Ports

## Input

X - Input signal data cube
complex-valued $K$-by- $N$ matrix | complex-valued $K$-by- $N$-by-L array
Input signal cube, specified as a complex-valued $K$-by- $N$ matrix or complex-valued $K$-by- $N$-by- $L$ array. The contents of the data cube depend on the type of range-angle processing specified by the different syntaxes.

- $K$ is the number of fast-time or range samples.
- $N$ is the number of independent spatial channels such as sensors or directions.
- $L$ is the slow-time dimension that corresponds to the number of pulses or sweeps in the input signal.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

PRF - Pulse repetition frequency
positive scalar
Pulse repetition frequency

## Dependencies

To enable this input argument, set the value of Range processing method to FFT and do not select the Dechirp input signal check box.

## Data Types: double

Xref - Reference signal used for dechirping
complex-valued $K$-by- 1 column vector
Reference signal used for dechirping, specified as a complex-valued $K$-by- 1 column vector. The number of rows must equal the length of the fast-time dimension of $X$.

## Dependencies

To enable this input argument, set the value of Range processing method to FFT and select the Dechirp input signal check box.
Data Types: double
Coeff - Matched filter coefficients
complex-valued $P$-by-1 column vector
Matched filter coefficients, specified as a complex-valued $P$-by- 1 column vector. $P$ must be less than or equal to $K$. $K$ is the number of fast-time or range sample.

## Dependencies

To enable this input argument, set the value of Range processing method to Matched filter.
Data Types: double
EI - Elevation angle
scalar
Elevation angle of response, specified as a scalar between $-90^{\circ}$ and $+90^{\circ}$. The range-angle response is computed for this elevation. Units are in degrees.

## Dependencies

To enable this argument, set the Source of elevation angle parameter to Input port.
Data Types: double

## Output

Resp - Range response data cube
complex-valued $M$-element column vector | complex-valued $M$-by- $L$ matrix | complex-valued $M$-by- $N$ by-L array

Range response data cube, returned as one of the following:

- Complex-valued $M$-element column vector
- Complex-valued $M$-by- $L$ matrix
- Complex-valued $M$-by- $N$ by- $L$ array

The value of $M$ depends on the type of processing

| Range Processing Method | Value of $\boldsymbol{M}$ |
| :--- | :--- |
| FFT | If you set the Source of FFT length in range <br> processing parameter to Auto, then $M=K$, the <br> length of the fast-time dimension of X. Otherwise, <br> $M$ equals the value of the FFT length in range <br> processing parameter. |
| Matched filter | $M=K$, the length of the fast-time dimension of X. |

Data Types: double

Range - Range values along range dimension
real-valued $M$-by-1 column vector
Range values along range dimension, returned as a real-valued $M$-by- 1 column vector. This vector defines the ranges that correspond to the fast-time dimension of the RESP output data cube. $M$ is the length of the fast-time dimension of RESP. Range values are monotonically increasing and equally spaced. Units are in meters.

Data Types: double
Ang - Angle values along angle direction
$P$-by-1 real-valued vector
Angle values corresponding to the samples along angle direction, returned as a $P$-by- 1 real-valued vector. Units are in degrees.

Data Types: double

## Parameters

## Main Tab

Signal propagation speed (m/s) - Signal propagation speed
physconst('LightSpeed') (default)| real-valued positive scalar

Signal propagation speed, specified as a real-valued positive scalar. The default value of the speed of light is the value returned by physconst ('LightSpeed '). Units are in meters per second.
Example: 3e8
Data Types: double
Operating frequency (Hz) - System operating frequency
3e8 (default) | positive real scalar

System operating frequency, specified as a positive scalar. Units are in Hz.
Range processing method - Range processing method
Matched filter (default)|FFT

Range processing method, specified as Matched filter or FFT.

- Matched filter - The object match-filters the incoming signal. This approach is commonly used for pulsed signals, where the matched filter is the time reverse of the transmitted signal.
- FFT - The object applies an FFT to the input signal. This approach is commonly used for chirped signals such as FMCW and linear FM pulsed signals.

Data Types: char
Inherit sample rate - Inherit sample rate from upstream blocks
on (default) | off

Select this parameter to inherit the sample rate from upstream blocks. Otherwise, specify the sample rate using the Sample rate (Hz) parameter.
Data Types: Boolean
Sample rate (Hz) - Sampling rate of signal
1e6 (default) | positive real-valued scalar

Specify the signal sampling rate as a positive scalar. Units are in Hz .

## Dependencies

To enable this parameter, clear the Inherit sample rate check box.
Data Types: double
FM sweep slope (Hz/s) - Linear FM sweep slope
1.0e9 (default) | scalar

Linear FM sweep slope, specified as a scalar. The fast-time dimension of the X input port must correspond to sweeps having this slope.
Example: 1.5e9

## Dependencies

To enable this parameter, set the Range processing method parameter to FFT.
Data Types: double
Dechirp input signal - Enable dechirping of input signals
on (default) | off

Option to enable dechirping of input signals, specified as on or off. Not selecting this check box indicates that the input signal is already dechirped and no dechirp operation is necessary. Select this check box when the input signal requires dechirping.

## Dependencies

To enable this parameter, set the Range processing method parameter to FFT.
Data Types: Boolean
Source of FFT length in range - Source of FFT length for range processing of dechirped signals Auto (default) | Property

Source of the FFT length used for the range processing of dechirped signals, specified as Auto or Property.

- Auto - The FFT length equals the length of the fast-time dimension of the input data cube.
- Property - Specify the FFT length by using the FFT length in range processing parameter.


## Dependencies

To enable this parameter, set the Range processing method parameter to FFT.

## Data Types: char

FFT length in range processing - FFT length used for range processing
1024 (default) | positive integer

FFT length used for range processing, specified as a positive integer.

## Dependencies

To enable this parameter, set the Range processing method parameter to FFT and the Source of FFT length in range processing parameter to Property.
Data Types: double
Range processing window - FFT weighting window for range processing
None (default) | Hamming | Chebyshev | Hann | Kaiser | Taylor

FFT weighting window for range processing, specified as None, Hamming, Chebyshev, Hann, Kaiser, or Taylor.

If you set this parameter to Taylor, the generated Taylor window has four nearly constant sidelobes next to the mainlobe.

## Dependencies

To enable this parameter, set the Range processing method parameter to FFT.
Data Types: char
Range sidelobe attenuation level - Sidelobe attenuation for range processing
30 (default) | scalar

Sidelobe attenuation for range processing, specified as a positive scalar. This attenuation applies only to Kaiser, Chebyshev, or Taylor windows. Units are in dB.

## Dependencies

To enable this parameter, set the Range processing method parameter to FFT and the Range processing window parameter to Kaiser, Chebyshev, or Kaiser.

Set reference range at center - Set reference range at center of range grid
on (default) | off

Set reference range at center of range grid, specified as on or off. Selecting this check box enables you to set the reference range at the center of the range grid. Otherwise, the reference range corresponds to the beginning of the range grid.

## Dependencies

To enable this parameter, set the Range processing method to FFT.

## Data Types: Boolean

Reference range (m) - Reference range of range grid
0.0 (default) | nonnegative scalar

Reference range of the range grid, specified as a nonnegative scalar.

- If you set the Range processing method parameter to 'Matched filter', the reference range is set to the start of the range grid.
- If you set the Range processing method parameter to FFT, the reference range is determined by the Set reference range at center parameter.
- When you select the Set reference range at center check box, the reference range is set to the center of the range grid.
- Otherwise, the reference range is set to the start of the range grid.

Units are in meters.
Example: 1000.0
Data Types: double
Source of elevation angle - Source of elevation angle
Property (default) | Input port

Source of elevation angle, specified as Property or Input port.

| Property | The elevation angle comes from the Elevation angle (deg) <br> parameter. |
| :--- | :--- |
| Input port | The elevation angle comes from an input port. |

Elevation angle (deg) - Elevation angle used to calculate range-angle response
0 (default) | scalar

Elevation angle used to calculate range-angle response, specified as a scalar. The angle must be between --90 and 90 degrees. This property applies when you set the ElevationAngleSource property to 'Property'. The default value of this property is 0 .

Angle span (deg) - Angle response span
[-90 90] (default) | real-valued 1-by-2 vector

Angle response span, specified as a real-valued 2-by-1 vector. The object calculates the range-angle response within the angle range, [min_angle max_angle].

## Example: [-45 45]

Data Types: 12wqqqq` | qdouble
Number of angle bins - Number of samples in angle span
positive integer greater than two

Number of samples in angle span used to calculate range-angle response, specified as a positive integer greater than two.
Example: [256]

## Data Types: double

Simulate using - Block simulation method
Interpreted Execution (default) | Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).

## Programmatic Use

Block Parameter:SimulateUsing
Type:enum
Values:Interpreted Execution, Code Generation
Default:Interpreted Execution

## Sensor Arrays Tab

Specify sensor array as - Method to specify array
Array (no subarrays) (default)|Partitioned array|Replicated subarray|MATLAB expression

Method to specify array, specified as Array (no subarrays) or MATLAB expression.

- Array (no subarrays) - use the block parameters to specify the array.
- Partitioned array - use the block parameters to specify the array.
- Replicated subarray - use the block parameters to specify the array.
- MATLAB expression - create the array using a MATLAB expression.

Expression - MATLAB expression used to create an array
Phased Array System Toolbox array System object

MATLAB expression used to create an array, specified as a valid Phased Array System Toolbox array System object.

Example: phased.URA('Size', [5,3])

## Dependencies

To enable this parameter, set Specify sensor array as to MATLAB expression.

## Element Parameters

Element type - Array element types
Isotropic Antenna (default)|Cosine Antenna|Custom Antenna|Omni Microphone| Custom Microphone

Antenna or microphone type, specified as one of the following:

- Isotropic Antenna
- Cosine Antenna
- Custom Antenna
- Omni Microphone
- Custom Microphone

Operating frequency range $(\mathrm{Hz})$ - Operating frequency range of the antenna or microphone element
[0,1e20] (default) | real-valued 1-by-2 row vector

Specify the operating frequency range of the antenna or microphone element as a 1-by-2 row vector in the form [LowerBound, UpperBound]. The element has no response outside this frequency range. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Isotropic Antenna, Cosine Antenna, or Omni Microphone.

Operating frequency vector ( Hz ) - Operating frequency range of custom antenna or microphone elements
[0,1e20] (default) | real-valued row vector

Specify the frequencies at which to set antenna and microphone frequency responses as a 1-by- $L$ row vector of increasing real values. The antenna or microphone element has no response outside the frequency range specified by the minimum and maximum elements of this vector. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone. Use Frequency responses (dB) to set the responses at these frequencies.

Baffle the back of the element - Set back response of an Isotropic Antenna element or an Omni Microphone element to zero
off (default) | on

Select this check box to baffle the back response of the element. When back baffled, the responses at all azimuth angles beyond $\pm 90^{\circ}$ from broadside are set to zero. The broadside direction is defined as $0^{\circ}$ azimuth angle and $0^{\circ}$ elevation angle.

## Dependencies

To enable this check box, set Element type to Isotropic Antenna or Omni Microphone.
Exponent of cosine pattern - Exponents of azimuth and elevation cosine patterns
[1.5 1.5] (default) | nonnegative scalar | real-valued 1-by-2 matrix of nonnegative values

Specify the exponents of the cosine pattern as a nonnegative scalar or a real-valued 1-by-2 matrix of nonnegative values. When Exponent of cosine pattern is a 1-by-2 vector, the first element is the exponent in the azimuth direction and the second element is the exponent in the elevation direction. When you set this parameter to a scalar, both the azimuth direction and elevation direction cosine patterns are raised to the same power.

## Dependencies

To enable this parameter, set Element type to Cosine Antenna.
Frequency responses (dB) - Antenna and microphone frequency response [0,0] (default) | real-valued row vector

Frequency response of a custom antenna or custom microphone for the frequencies defined by the Operating frequency vector (Hz) parameter. The dimensions of Frequency responses (dB) must match the dimensions of the vector specified by the Operating frequency vector $(\mathbf{H z})$ parameter.

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone.
Input Pattern Coordinate System - Coordinate system of custom antenna pattern az-el (default)|phi-theta

Coordinate system of custom antenna pattern, specified az-el or phi-theta. When you specify azel, use the Azimuth angles (deg) and Elevations angles (deg) parameters to specify the coordinates of the pattern points. When you specify phi-theta, use the Phi angles (deg) and Theta angles (deg) parameters to specify the coordinates of the pattern points.

## Dependencies

To enable this parameter, set Element type to Custom Antenna.

Azimuth angles (deg) - Azimuth angles of antenna radiation pattern
[-180:180] (default) | real-valued row vector

Specify the azimuth angles at which to calculate the antenna radiation pattern as a 1 -by- $P$ row vector. $P$ must be greater than 2. Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to az-el.

Elevation angles (deg) - Elevation angles of antenna radiation pattern
[-90:90] (default) | real-valued row vector

Specify the elevation angles at which to compute the radiation pattern as a 1-by- $Q$ vector. $Q$ must be greater than 2. Angle units are in degrees. Elevation angles must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input
Pattern Coordinate System parameter to az-el.
Phi Angles (deg) - Phi angle coordinates of custom antenna radiation pattern
$0: 360 \mid$ real-valued 1-by-P row vector

Phi angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by- $P$ row vector. $P$ must be greater than 2 . Angle units are in degrees. Phi angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Theta Angles (deg) - Theta angle coordinates of custom antenna radiation pattern 0:180 | real-valued 1-by- $Q$ row vector

Theta angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by$Q$ row vector. $Q$ must be greater than 2 . Angle units are in degrees. Theta angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Magnitude pattern (dB) - Magnitude of combined antenna radiation pattern zeros $(181,361)$ (default) | real-valued $Q$-by- $P$ matrix | real-valued $Q$-by- $P$-by-L array

Magnitude of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector $(\mathbf{H z})$.

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector (Hz) parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector ( $\mathbf{H z}$ ) parameter.


## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Phase pattern (deg) - Custom antenna radiation phase pattern
zeros $(181,361)$ (default) | real-valued $Q$-by- $P$ matrix | real-valued $Q$-by- $P$-by-L array

Phase of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector ( $\mathbf{H z}$ ).

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (


## Dependencies

To enable this parameter, set Element type to Custom Antenna.
MatchArrayNormal - Rotate antenna element to array normal on (default) | off

Select this check box to rotate the antenna element pattern to align with the array normal. When not selected, the element pattern is not rotated.

When the antenna is used in an antenna array and the Input Pattern Coordinate System parameter is az-el, selecting this check box rotates the pattern so that the $x$-axis of the element
coordinate system points along the array normal. Not selecting uses the element pattern without the rotation.

When the antenna is used in an antenna array and Input Pattern Coordinate System is set to phitheta, selecting this check box rotates the pattern so that the $z$-axis of the element coordinate system points along the array normal.

Use the parameter in conjunction with the Array normal parameter of the URA and UCA arrays.

## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Polar pattern frequencies (Hz) - Polar pattern microphone response frequencies
1e3 (default) | real scalar | real-valued 1-by-L row vector

Polar pattern microphone response frequencies, specified as a real scalar, or a real-valued, 1-by- $L$ vector. The response frequencies lie within the frequency range specified by the Operating
frequency vector $(\mathrm{Hz})$ vector.

## Dependencies

To enable this parameter, set Element type set to Custom Microphone.
Polar pattern angles (deg) - Polar pattern response angles
[-180:180] (default) | real-valued -by-P row vector

Specify the polar pattern response angles, as a 1-by- $P$ vector. The angles are measured from the central pickup axis of the microphone and must be between $-180^{\circ}$ and $180^{\circ}$, inclusive.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.
Polar pattern (dB) - Custom microphone polar response
zeros ( 1,361 ) (default) | real-valued L-by-P matrix

Specify the magnitude of the custom microphone element polar patterns as an $L$-by- $P$ matrix. $L$ is the number of frequencies specified in Polar pattern frequencies $\mathbf{( H z )} . P$ is the number of angles specified in Polar pattern angles (deg). Each row of the matrix represents the magnitude of the polar pattern measured at the corresponding frequency specified in Polar pattern frequencies (Hz) and all angles specified in Polar pattern angles (deg). The pattern is measured in the azimuth plane. In the azimuth plane, the elevation angle is $0^{\circ}$ and the central pickup axis is $0^{\circ}$ degrees azimuth and $0^{\circ}$ degrees elevation. The polar pattern is symmetric around the central axis. You can construct the microphone response pattern in 3-D space from the polar pattern.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.

## Array Parameters

Geometry - Array geometry
ULA (default) | URA | UCA | Conformal Array

Array geometry, specified as one of

- ULA - Uniform linear array
- URA - Uniform rectangular array
- UCA - Uniform circular array
- Conformal Array - arbitrary element positions

Number of elements - Number of array elements
2 for ULA arrays and 5 for UCA arrays (default) | integer greater than or equal to 2

The number of array elements for ULA or UCA arrays, specified as an integer greater than or equal to 2.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

## Dependencies

To enable this parameter, set Geometry to ULA or UCA.
Element spacing (m) - Spacing between array elements
0.5 for ULA arrays and [ $0.5,0.5$ ] for URA arrays (default) | positive scalar for ULA or URA arrays | 2 -element vector of positive values for URA arrays

Spacing between adjacent array elements:

- ULA - specify the spacing between two adjacent elements in the array as a positive scalar.
- URA - specify the spacing as a positive scalar or a 1 -by-2 vector of positive values. If Element spacing (m) is a scalar, the row and column spacings are equal. If Element spacing (m) is a vector, the vector has the form [SpacingBetweenArrayRows,SpacingBetweenArrayColumns].
- When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.


## Dependencies

To enable this parameter, set Geometry to ULA or URA.
Array axis - Linear axis direction of ULA
$y$ (default) $|x| z$

Linear axis direction of ULA, specified as $y, x$, or $z$. All ULA array elements are uniformly spaced along this axis in the local array coordinate system.

## Dependencies

- To enable this parameter, set Geometry to ULA.
- This parameter is also enabled when the block only supports ULA arrays.

Array size - Dimensions of URA array

## [2,2] (default) | positive integer | 1-by-2 vector of positive integers

Dimensions of a URA array, specified as a positive integer or 1-by-2 vector of positive integers.

- If Array size is a 1-by-2 vector, the vector has the form [Number0fArrayRows, NumberOfArrayColumns].
- If Array size is an integer, the array has the same number of rows and columns.
- When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

For a URA, array elements are indexed from top to bottom along the leftmost column, and then continue to the next columns from left to right. In this figure, the Array size value of [3,2] creates an array having three rows and two columns.

## Size and Element Indexing Order

for Uniform Rectangular Arrays
Example: Size = [3,2]


## Dependencies

To enable this parameter, set Geometry to URA.
Element lattice - Lattice of URA element positions
Rectangular (default) | Triangular

Lattice of URA element positions, specified as Rectangular or Triangular.

- Rectangular - Aligns all the elements in row and column directions.
- Triangular - Shifts the even-row elements of a rectangular lattice toward the positive row-axis direction. The displacement is one-half the element spacing along the row dimension.


## Dependencies

To enable this parameter, set Geometry to URA.

Array normal - Array normal direction
x for URA arrays or $z$ for UCA arrays (default) | y

Array normal direction, specified as $x, y$, or $z$.
Elements of planar arrays lie in a plane orthogonal to the selected array normal direction. Element boresight directions point along the array normal direction.

| Array Normal Parameter Value | Element Positions and Boresight Directions |
| :--- | :--- |
| $x$ | Array elements lie in the $y z$-plane. All element <br> boresight vectors point along the $x$-axis. |
| $y$ | Array elements lie in the $z x$-plane. All element <br> boresight vectors point along the $y$-axis. |
| $z$ | Array elements lie in the $x y$-plane. All element <br> boresight vectors point along the $z$-axis. |

## Dependencies

To enable this parameter, set Geometry to URA or UCA.
Radius of UCA (m) - UCA array radius
0.5 (default) | positive scalar

Radius of UCA array, specified as a positive scalar.

## Dependencies

To enable this parameter, set Geometry to UCA.
Element positions (m) - Positions of conformal array elements
[0;0;0] (default)| 3-by-Nmatrix of real values

Positions of the elements in a conformal array, specified as a 3 -by- $N$ matrix of real values, where $N$ is the number of elements in the conformal array. Each column of this matrix represents the position [ $x ; y ; z$ ] of an array element in the array local coordinate system. The origin of the local coordinate system is $(0,0,0)$. Units are in meters.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

## Dependencies

To enable this parameter set Geometry to Conformal Array.
Element normals (deg) - Direction of conformal array element normal vectors
[0;0] | 2-by-1 column vector | 2-by-N matrix

Direction of element normal vectors in a conformal array, specified as a 2-by-1 column vector or a 2-by- $N$ matrix. $N$ indicates the number of elements in the array. For a matrix, each column specifies the normal direction of the corresponding element in the form [azimuth; elevation] with respect to
the local coordinate system. The local coordinate system aligns the positive $x$-axis with the direction normal to the conformal array. If the parameter value is a 2 -by- 1 column vector, the same pointing direction is used for all array elements.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

You can use the Element positions (m) and Element normals (deg) parameters to represent any arrangement in which pairs of elements differ by certain transformations. The transformations can combine translation, azimuth rotation, and elevation rotation. However, you cannot use transformations that require rotation about the normal direction.

## Dependencies

To enable this parameter, set Geometry to Conformal Array.

## Taper - Array element tapers <br> 1 (default) | complex-valued scalar | complex-valued row vector

Element tapering, specified as a complex-valued scalar or a complex-valued 1-by- $N$ row vector. In this vector, $N$ represents the number of elements in the array.

Also known as element weights, tapers multiply the array element responses. Tapers modify both amplitude and phase of the response to reduce side lobes or steer the main response axis.

If Taper is a scalar, the same weight is applied to each element. If Taper is a vector, a weight from the vector is applied to the corresponding sensor element. The number of weights must match the number of elements of the array.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

Subarray definition matrix - Define elements belonging to subarrays
logical matrix

Specify the subarray selection as an $M$-by- $N$ matrix. $M$ is the number of subarrays and $N$ is the total number of elements in the array. Each row of the matrix represents a subarray and each entry in the row indicates when an element belongs to the subarray. When the entry is zero, the element does not belong the subarray. A nonzero entry represents a complex-valued weight applied to the corresponding element. Each row must contain at least one nonzero entry.

The phase center of each subarray lies at the subarray geometric center. The subarray geometric center depends on the Subarray definition matrix and Geometry parameters.

## Dependencies

To enable this parameter, set Specify sensor array as to Partitioned array.
Subarray steering method - Specify subarray steering method None (default) | Phase | Time

Subarray steering method, specified as one of

- None
- Phase
- Time
- Custom

Selecting Phase or Time opens the Steer input port on the Narrowband Receive Array, Narrowband Transmit Array, Wideband Receive Array, Wideband Transmit Array blocks, Constant Gamma Clutter, and GPU Constant Gamma Clutter blocks.

Selecting Custom opens the WS input port on the Narrowband Receive Array, Narrowband Transmit Array, Wideband Receive Array, Wideband Transmit Array blocks, Constant Gamma Clutter, and GPU Constant Gamma Clutter blocks.

## Dependencies

To enable this parameter, set Specify sensor array as to Partitioned array or Replicated subarray.

Phase shifter frequency (Hz) - Subarray phase shifting frequency
3.0e8 (default) | positive real-valued scalar

Operating frequency of subarray steering phase shifters, specified as a positive real-valued scalar. Units are Hz.

## Dependencies

To enable this parameter, set Sensor array to Partitioned array or Replicated subarray and set Subarray steering method to Phase.

Number of bits in phase shifters - Subarray steering phase shift quantization bits
0 (default) | non-negative integer

Subarray steering phase shift quantization bits, specified as a non-negative integer. A value of zero indicates that no quantization is performed.

## Dependencies

To enable this parameter, set Sensor array to Partitioned array or Replicated subarray and set Subarray steering method to Phase.

Subarrays layout - Subarray position specification
Rectangular (default) | Custom

Specify the layout of replicated subarrays as Rectangular or Custom.

- When you set this parameter to Rectangular, use the Grid size and Grid spacing parameters to place the subarrays.
- When you set this parameter to Custom, use the Subarray positions (m) and Subarray normals parameters to place the subarrays.


## Dependencies

To enable this parameter, set Sensor array to Replicated subarray
Grid size - Dimensions of rectangular subarray grid
[1,2] (default)

Rectangular subarray grid size, specified as a single positive integer, or a 1-by-2 row vector of positive integers.

If Grid size is an integer scalar, the array has an equal number of subarrays in each row and column. If Grid size is a 1-by-2 vector of the form [NumberOfRows, NumberOfColumns], the first entry is the number of subarrays along each column. The second entry is the number of subarrays in each row. A row is along the local $y$-axis, and a column is along the local $z$-axis. The figure here shows how you can replicate a 3-by-2 URA subarray using a Grid size of [1,2].
$3 \times 2$ Element URA
Replicated on a $1 \times 2$ Grid


## Dependencies

To enable this parameter, set Sensor array to Replicated subarray and Subarrays layout to Rectangular.

Grid spacing ( $\mathbf{m}$ ) - Spacing between subarrays on rectangular grid Auto (default) | positive real-valued scalar | 1-by-2 vector of positive real-values

The rectangular grid spacing of subarrays, specified as a positive, real-valued scalar, a 1-by-2 row vector of positive, real-values, or Auto. Units are in meters.

- If Grid spacing is a scalar, the spacing along the row and the spacing along the column is the same.
- If Grid spacing is a 1-by-2 row vector, the vector has the form [SpacingBetweenRows,SpacingBetweenColumn]. The first entry specifies the spacing between rows along a column. The second entry specifies the spacing between columns along a row.
- If Grid spacing is set to Auto, replication preserves the element spacing of the subarray for both rows and columns while building the full array. This option is available only when you specify Geometry as ULA or URA.


## Dependencies

To enable this parameter, set Sensor array to Replicated subarray and Subarrays layout to Rectangular.

Subarray positions (m) - Positions of subarrays
[0,0;0.5, 0.5;0,0] (default) | 3-by- $N$ real-valued matrix

Positions of the subarrays in the custom grid, specified as a real 3-by- $N$ matrix, where $N$ is the number of subarrays in the array. Each column of the matrix represents the position of a single subarray in the array local coordinate system. The coordinates are expressed in the form [x; y; z]. Units are in meters.

## Dependencies

To enable this parameter, set Sensor array to Replicated subarray and Subarrays layout to Custom.

Subarray normals - Direction of subarray normal vectors
[0,0;0,0] (default) | 2-by- $N$ real matrix

Specify the normal directions of the subarrays in the array. This parameter value is a 2 -by- $N$ matrix, where $N$ is the number of subarrays in the array. Each column of the matrix specifies the normal direction of the corresponding subarray, in the form [azimuth; elevation]. Angle units are in degrees. Angles are defined with respect to the local coordinate system.

You can use the Subarray positions and Subarray normals parameters to represent any arrangement in which pairs of subarrays differ by certain transformations. The transformations can combine translation, azimuth rotation, and elevation rotation. However, you cannot use transformations that require rotation about the normal.

## Dependencies

To enable this parameter, set the Sensor array parameter to Replicated subarray and the Subarrays layout to Custom.

## Version History

Introduced in R2018b

See Also<br>phased.RangeAngleResponse

## Range Doppler Response

Range-Doppler response

Libraries:
Phased Array System Toolbox / Detection

## Description

The Range-Doppler Response block computes the range-Doppler map of an input signal. The output response is a matrix whose rows represent range gates and whose columns represent Doppler bins.

## Ports

Input
X - Input
complex-valued $K$-by- $L$ matrix | $K$-by- $N$-by-L array
Input data, specified as a complex-valued $K$-by- $L$ matrix or $K$-by- $N$-by- $L$ array where

- $K$ denotes the number of fast-time samples.
- $N$ denotes the number of channels such as beams or sensors. When $N$ is one, only a single data channel is present.
- $L$ denotes the number of pulses for matched-filter processing and the number of sweeps for FFT processing.

Data Types: single | double
Coeff - Matched filter coefficients
column vector
Matched filter coefficients, specified as a column vector.

## Dependencies

To enable this port, set the Range processing method to Matched filter.
Data Types: single | double
XRef - Reference signal
vector
Reference signal, specified as a

## Dependencies

To enable this port, set the Range processing method to FFT and then select the Dechirp input signal check box.
Data Types: double

PRF - Pulse repetition frequency
positive scalar
Pulse repetition frequency, specified as a positive scalar. prf must be less than or equal to the sample rate specified in the SampleRate property divided by the length of the first dimension of the input signal, x. You can specify this argument as single or double precision.

## Dependencies

To enable this port, set the Source of pulse repetition frequency drop down menu to Input port.
Data Types: double

## Output

Resp - Range-Doppler response
complex
Range-Doppler, returned as a complex-valued $M$-by- $P$ matrix or an $M$-by- $N$-by- $P$ array.
Range - Range samples
vector
Range samples at which the range-Doppler response is evaluated. The output is a column vector of length $M$.

Data Types: double
Dop - Doppler or speed samples
vector
Doppler samples or speed samples at which the range-Doppler response is evaluated. returned as a column vector of length $P$. Whether Dop contains Doppler or speed samples depends on the Doppler output parameter.

Data Types: double

## Parameters

Range processing method - Range processing method

Matched filter (default)| FFT
Specify the method of range processing as Matched filter or FFT

| Matched filter | Applies a matched filter to the incoming signal. This technique is <br> commonly used for pulsed signals, where the matched filter is the <br> time reverse of the transmitted signal. Choosing this option creates <br> the Coeff input port. |
| :--- | :--- |
| FFT | Performs range processing by applying an FFT to the input signal. <br> This approach is commonly used with FMCW and linear FM pulsed <br> signals. |

Propagation speed ( $\mathbf{m} / \mathbf{s}$ ) - Signal propagation speed physconst('LightSpeed') (default) | positive scalar

Signal propagation speed, specified as a real-valued positive scalar. The default value of the speed of light is the value returned by physconst('LightSpeed').
Data Types: double
Inherit sample rate - Inherit sample rate from upstream blocks
on (default) | off

Select this parameter to inherit the sample rate from upstream blocks. Otherwise, specify the sample rate using the Sample rate $(\mathbf{H z})$ parameter.
Data Types: Boolean
Sample rate (Hz) - Sampling rate of signal
le6 (default) | positive real-valued scalar

Specify the signal sampling rate as a positive scalar. Units are in Hz .

## Dependencies

To enable this parameter, clear the Inherit sample rate check box.

## Data Types: double

Reference range (m) - Reference range
0 (default)
Specify the reference range of the range grid as a nonnegative scalar.

- If you set the Range processing method parameter to Matched filter, the reference range is set to the start of the range grid.
- If you set the Range processing method property to FFT, the reference range depends on the Set reference range at center check box.
- When you select the Set reference range at center check box, the reference range is set to the center of the range grid.
- If you do not select the Set reference range at center check box, the reference range is set to the start of the range grid.

Units are in meters.
Source of pulse repetition frequency - Source of pulse repetition frequency

## Auto (default) | Property | Input port

Specify the source of pulse repetition frequency as

- Auto - automatically compute the pulse repetition frequency (PRF). The PRF is the sample rate of the signal divided by the number of rows in the input port signal, $X$.
- Property - specify the pulse repetition frequency using the PRF parameter.
- Input port— specify the PRF using the PRF input port.

Use the Property or Input port option when the pulse repetition frequency cannot be determined by the signal duration, as is the case with range-gated data.

Pulse repetition frequency of the input signal (Hz) - Pulse repetition frequency of the input signal

## 10e3 (default)

Specify the pulse repetition frequency of the input signal as a positive scalar. PRF must be less than or equal to the sample rate divided by the number of rows of the input signal. When the signal length is variable, use the maximum possible number of rows of the input signal instead.

## Dependencies

To enable this parameter, set the Source of pulse repetition frequency parameter to Property.
Source of FFT length in Doppler processing - Source of FFT length in Doppler processing
Auto (default) | Property
Specify how the block determines the length of the FFT used in Doppler processing. Values of this parameter are

| Auto | The FFT length equals the number of rows of the input signal. |
| :--- | :--- |
| Property | The FFT length in Doppler processing parameter of this block <br> specifies the FFT length. |

FFT length in Doppler processing - FFT length in Doppler processing

## 1024

Specify the length of the FFT used in Doppler processing as a positive integer.

## Dependencies

This parameter appears only when you set Source of FFT length in Doppler processing to Property.

Doppler processing window - Doppler processing window
None (default) | Hamming | Chebyshev | Hann | Kaiser | Taylor
Specify the window used for Doppler processing using one of
None
Hamming
Chebyshev
Hann
Kaiser
Taylor

If you set this parameter to Taylor, the generated Taylor window has four nearly-constant sidelobes adjacent to the mainlobe.

Doppler sidelobe attenuation level - Doppler sidelobe attenuation level
30 (default)
Specify the sidelobe attenuation level as a positive scalar, in decibels.

## Dependencies

This parameter appears only when Doppler processing window is set to Kaiser, Chebyshev, or Taylor.

Doppler output - Doppler output
Frequency (default) | Speed
Specify the Doppler domain output as Frequency or Speed

| Frequency | Doppler shift, in hertz. |
| :--- | :--- |
| Speed | Radial speed corresponding to Doppler shift, in meters per second. |

Signal carrier frequency (Hz) - Signal carrier frequency
3e8 (default) | positive real-valued scalar

Signal carrier frequency, specified as a positive real-valued scalar. Units are in hertz.
Data Types: double
FM sweep slope (Hz/s) - FM sweep slope
1e9 (default)
Specify the slope of the linear FM sweeping, in hertz per second, as a scalar.

## Dependencies

This parameter appears only when you set Range processing method to FFT.
Dechirp input signal - Dechirp input signal
off (default) | on
Select this check box to make the block perform the dechirp operation on the input signal. Clear this check box to indicate that the input signal is already dechirped and no dechirp operation is necessary.

## Dependencies

This check box appears only when you set Range processing method to FFT.
Source of FFT length in range processing - Source of FFT length in range processing

## Auto (default) | Property

Specify how the block determines the FFT length in range processing. Values of this parameter are

| Auto | The FFT length equals the number of rows of the input signal. |
| :--- | :--- |
| Property | The FFT length is specified by FFT length in range processing . |

This parameter appears only when you set Range processing method to FFT.
FFT length in range processing - FFT length in range processing

## 1024 (default)

Specify the FFT length in the range domain as a positive integer.

## Dependencies

This parameter appears only when you set Range processing method to FFT and Source of FFT length in range processing to Property.

Range processing window - Range processing window
None (default) | Hamming | Chebyshev | Hann | Kaiser | Taylor
Specify the window used for range processing using one of
None
Hamming
Chebyshev
Hann
Kaiser
Taylor
If you set this parameter to Taylor, the generated Taylor window has four nearly-constant sidelobes adjacent to the mainlobe.

## Dependencies

This parameter appears only when you set Range processing method to FFT.

## Set reference range at center - Set reference range at center

## on (default) | off

Set reference range at the center of range grid, specified as on or off. Selecting this check box, enables you to set the reference range at the center of the range grid. Otherwise, the reference range is set to the beginning of the range grid.

Range sidelobe attenuation level - Range sidelobe attenuation level
30 (default)
Specify the sidelobe attenuation level as a positive scalar, in decibels.

## Dependencies

This parameter appears only when you set Range processing method to FFT and Range processing window to Kaiser, Chebyshev, or Taylor.

Simulate using - Block simulation method
Interpreted Execution (default) | Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).

## Programmatic Use

Block Parameter:SimulateUsing
Type:enum
Values:Interpreted Execution, Code Generation
Default:Interpreted Execution

## Version History

Introduced in R2014b

See Also<br>phased.RangeDopplerResponse

## Range Estimator

Range estimation


## Libraries:

Phased Array System Toolbox / Detection

## Description

The Range Estimator block estimates the range of target detections obtained from the radar response data.

## Ports

## Input

Resp - Range-processed response data cube
complex-valued $P$-by-1 column vector | complex-valued $M$-by- $P$ matrix | complex-valued $M$-by- $N$-by- $P$ matrix

Range-processed response data cube, specified as a complex-valued $P$-by- 1 column vector, a complexvalued $M$-by- $P$ matrix, or a complex-valued $M$-by- $N$-by- $P$ array. $M$ represents the number of range samples, $N$ is the number of sensor elements or beams, and $P$ is the number of Doppler bins.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

## Data Types: double

Range - Range grid values along range dimension
real-valued $M$-by-1 column vector
Range grid values along the range dimension of the data cube input, Resp, specified as a real-valued $M$-by- 1 column vector. Range values must be monotonically increasing and equally spaced. Units are in meters.
Example: [-0.3,-0.2,-0.1,0,0.1,0.2,0.3]
Data Types: double

## Detldx - Detection indices

real-valued $N_{d}$-by-Q matrix
Detection indices, specified as a real-valued $N_{d}$-by- $Q$ matrix. $Q$ is the number of detections and $N_{d}$ is the number of dimensions in the response data cube, Resp. Each column of DetIdx contains the indices of a detection in the response data cube.

NoisePower - Noise power at detection locations
positive scalar | real-valued 1-by-Q row vector of positive values

Noise power at detection locations, specified as a positive scalar or real-valued 1-by- $Q$ row vector positive values. $Q$ is the number of detections specified in the DetIdx input port.

## Dependencies

To enable this port, select the Output variance for parameter estimates parameter, and then set Source of noise power parameter to Input port.

Clusters - Cluster IDs real-valued 1-by- $Q$ row vector of positive values

Cluster IDs, specified as a real-valued 1-by- $Q$ row vector, where $Q$ is the number of detections specified in the DetIdx input port. Each element of Clusters corresponds to an element of DetIdx.

## Dependencies

To enable this input port, select the Enable cluster ID input checkbox.

## Output

Est - Range estimate
real-valued $K$-by- 1 column vector
Range estimates, specified as a real-valued $K$-by- 1 column vector.

- When Enable cluster ID input is not selected, each range estimate corresponds to one of the columns of the DetIdx input port. Then $K$ equals the column dimension, $Q$, of DetIdx.
- When Enable cluster ID input is selected, each range estimate corresponds to one of the cluster IDs in the Clusters input port. Then $K$ equals the number of unique cluster IDs.

Var - Range estimation variance
positive, real-valued $K$-by- 1 column vector
Range estimation variance, returned as a positive, real-valued $K$-by- 1 column vector, where $K$ is the dimension of Est. Each element of Var corresponds to an element of Est. The estimator variance is computed using the Ziv-Zakai bound.

## Dependencies

To enable this output port, select the Output variance for parameter estimates parameter.

## Parameters

Maximum number of estimates - Maximum number of estimates to report
1 (default) | positive integer

The maximum number of estimates to report, specified as a positive integer. When the number of requested estimates is greater than the number elements in DetIdx, the remainder is filled with NaN .

## Data Types: double

Enable cluster ID input - Enable cluster ID input off (default) | on

Enable the Cluster input port to pass in cluster association information.

## Data Types: Boolean

Output variance for parameter estimates - Enable output variance port off (default) | on

Enables the output of the parameter estimate variances via the Var port.
Data Types: Boolean
Root-mean-square range resolution - Range resolution
2 (default) | positive scalar

Root-mean-square range resolution of the detection, specified as a positive scalar. This parameter must have the same units as the Range input port.

## Dependencies

To enable this parameter, select the Output variance for parameter estimates parameter.
Data Types: double
Source of noise power - Source of noise power values
Property (default)|Input port

Source of the noise power, specified as Property or Input port. If you set this parameter to Property, use the Noise power parameter to set the noise power at the detection locations. When set the parameter to Input port, specify noise power via the NoisePower input port.

Noise power - Noise power values
1.0 (default) | positive scalar

Noise power for detections, specified as a positive scalar. The same noise power value is applied to all detections. Noise power is in linear units.

## Dependencies

To enable this parameter, select the Output variance for parameter estimates checkbox and set the Source of noise power parameter to Property.
Data Types: double
Simulate using - Block simulation method
Interpreted Execution (default)|Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are
satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).

Programmatic Use<br>Block Parameter:SimulateUsing<br>Type:enum<br>Values:Interpreted Execution, Code Generation<br>Default:Interpreted Execution

## Version History

Introduced in R2017a

## See Also

## Blocks

CFAR Detector | 2-D CFAR Detector | Range Doppler Response | Range Response
Objects
phased.CFARDetector| phased.CFARDetector2D|phased.RangeEstimator|
phased.RangeResponse|phased.RangeDopplerResponse

## Range Response

Range response


## Libraries:

Phased Array System Toolbox / Detection

## Description

The Range Response block performs range filtering on fast-time (range) data, using either a matched filter or an FFT-based algorithm. The output is typically used as input to a detector. Matched filtering improves the SNR of pulsed waveforms. For continuous FM signals, FFT processing extracts the beat frequency of FMCW waveforms. Beat frequency is directly related to range.

The input to the block is a radar data cube. The organization of the data cube follows the Phased Array System Toolbox convention. The first dimension of the cube represents the fast time samples or ranges of the received signals. The second dimension represents multiple spatial channels such as different sensors or beams. The third dimension, slow time, represent pulses. Range filtering operates along the fast-time dimension of the cube. Processing along the other dimensions is not performed. If the data contains only one channel or pulse, the data cube can contain fewer than three dimensions. Because this object performs no Doppler processing, you can use it to process noncoherent radar pulses.

The output of the block is also a data cube with the same number of dimensions as the input. Its first dimension contains range-processed data but its length can differ from the first dimension of the input data cube.

## Ports

## Input

X - Input data cube
complex-valued $K$-by-1 column vector | complex-valued $K$-by- $L$ matrix | complex-valued $K$-by- $N$-by- $L$ array

Input data cube, specified as a complex-valued $K$-by- 1 column vector, a complex-valued $K$-by- $L$ matrix, or a complex-valued $K$-by- $N$-by- $L$ array.

- $K$ is the number of range or time samples.
- $N$ is the number of independent channels such as sensors or directions.
- $L$ is the number of pulses or sweeps in the input signal.

See "Radar Data Cube Concept".
Each $K$-element column vector is processed independently.
For an FMCW waveform, with a triangle sweep, the sweeps alternate between positive and negative slopes. However, Range Response is designed to process consecutive sweeps of the same slope. To apply the Range Response block for a triangle-sweep system, use one of the following approaches:

- Specify a positive Sweep slope parameter value, with $X$ corresponding to upsweeps only. After obtaining the Doppler or speed values, divide them by 2.
- Specify a negative Sweep slope parameter value, with X corresponding to downsweeps only. After obtaining the Doppler or speed values, divide them by 2.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

## Data Types: double

Coeff - Matched filter coefficients
complex-valued column vector
Matched filter coefficients, specified as a complex-valued column vector. The length of the vector must be less than or equal to the number of rows in the input data, $K$.

## Dependencies

To enable this port, set Range processing method to Matched filter.

## Data Types: double

XRef - Reference signal
complex-valued $K$-by- 1 column vector
Reference signal used for dechirping the input signal, specified as a complex-valued $K$-by- 1 column vector. The number of rows must equal the length of the first dimension of $X$.

## Dependencies

To enable this port, set Range processing method to FFT and select the Dechirp input signal parameter.
Data Types: double

## Output

Resp - Range response data cube
complex-valued $M$-element column vector | complex-valued $M$-by-L matrix | complex-valued $M$-by- $N$ by-L array

Range response data cube, returned as a

- Complex-valued $M$-element column vector
- Complex-valued $M$-by- $L$ matrix
- Complex-valued $M$-by- $N$ by-L array

See "Radar Data Cube Concept". The value of $M$ depends on the type of processing

| Range processing method | Dechirp input signal | Value of $M$ |
| :--- | :--- | :--- |
| FFT | off | If you set the Source of FFT <br> length in range processing to <br> Auto, $M=K$, the length of the <br> first dimension of $x$. Otherwise, <br> $M$ equals the value of the FFT <br> length in range processing <br> parameter. |
| $M$ equals the number of rows, $K$, <br> Matched the input signal. |  |  |
|  | on | $M$ equals the number of rows, $K$, <br> of the input signal. |

Data Types: double
Range - Range values along range dimension
real-valued $M$-by- 1 column vector
Range values along the first dimension of the Resp output data port, specified as a real-valued $M$ -by-1 column vector. This quantity defines the range values along the first dimension of the Resp output port data. Units are in meters.

Data Types: double

## Parameters

Range processing method - Range processing method
Matched filter (default) | FFT

Range processing method, specified as Matched filter or FFT.

| Matched filter | The block applies a matched filter to the incoming signal. This <br> approach is commonly used for pulsed signals, where the matched <br> filter is the time reverse of the transmitted signal. |
| :--- | :--- |
| FFT | The block applies an FFT to the input signal. This approach is <br> commonly used for FMCW and linear FM pulsed signals. |

## Data Types: char

Propagation speed (m/s) - Signal propagation speed
physconst('LightSpeed') (default)| positive scalar

Signal propagation speed, specified as a real-valued positive scalar. The default value of the speed of light is the value returned by physconst('LightSpeed').

## Data Types: double

Inherit sample rate - Inherit sample rate from upstream blocks
on (default) | off

Select this parameter to inherit the sample rate from upstream blocks. Otherwise, specify the sample rate using the Sample rate (Hz) parameter.
Data Types: Boolean
Sample rate (Hz) - Sampling rate of signal
le6 (default) | positive real-valued scalar

Specify the signal sampling rate as a positive scalar. Units are in Hz .

## Dependencies

To enable this parameter, clear the Inherit sample rate check box.
Data Types: double
FM sweep slope (Hz/s) - FM sweep slope
le9 (default) | scalar

Specify the slope of the linear FM sweep as a scalar. This parameter must match the actual sweep of the input data in port $X$.

## Dependencies

To enable this parameter, set Range processing method to FFT.
Data Types: double
Dechirp input signal - Enable dechirping of input signal
on (default) | off

Select this parameter to enable dechirping of input signal.

## Dependencies

To enable this parameter, set Range processing method to FFT.
Data Types: Boolean
Source of FFT length in range processing - Source of FFT length for range processing Auto (default) | Property

Source of FFT length for range processing, specified as Auto or Property

| Auto | The FFT length equals the number of rows of the input data cube. |
| :--- | :--- |
| Property | Specify FFT length in the FFT length in range processing <br> parameter. |

## Dependencies

To enable this parameter, set Range processing method to FFT.
Data Types: char

FFT length in range processing - Range processing FFT length
1024 (default) | positive integer

FFT length for range processing, specified as a positive integer.

## Dependencies

To enable this parameter, set Range processing method to FFT and Source of FFT length in range processing to Property.
Data Types: double
Range processing window - Range FFT weighting window
None (default) | Hamming | Chebyshev | Hann | Kaiser | Taylor

Range FFT weighting window, specified as None, Hamming, Chebyshev, Hann, Kaiser, or Taylor.
If you set this property to Taylor, the generated Taylor window has four nearly constant sidelobes next to the mainlobe.

## Dependencies

To enable this parameter, set Range processing method to FFT.

## Data Types: char

Range sidelobe attenuation level - Sidelobe attenuation for range processing
30 (default) | positive scalar

Sidelobe attenuation for range processing, specified as a positive scalar. Units are in dB .

## Dependencies

To enable this parameter, set Range processing method to FFT and Range processing window to Kaiser, Chebyshev, or Taylor.
Data Types: double
Set reference range at center - Set reference range at center of range grid
on (default) | off

Set reference range at the center of range grid, specified as on or off. Selecting this check box, enables you to set the reference range at the center of the range grid. Otherwise, the reference range is set to the beginning of the range grid.

## Dependencies

To enable this property, set the Range processing method to FFT.
Reference range (m) - Reference range of range grid
0.0 (default) | nonnegative scalar

Reference range of the range grid, specified as a nonnegative scalar.

- If you set the Range processing method parameter to Matched filter, the reference range is set to the start of the range grid.
- If you set the Range processing method property to FFT, the reference range depends on the Set reference range at center check box.
- When you select the Set reference range at center check box, the reference range is set to the center of the range grid.
- If you do not select the Set reference range at center check box, the reference range is set to the start of the range grid.

Units are in meters.
Example: 1000.0
Data Types: double
Simulate using - Block simulation method
Interpreted Execution (default)|Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).

```
Programmatic Use
Block Parameter:SimulateUsing
Type:enum
Values:Interpreted Execution, Code Generation
```

Default:Interpreted Execution

## Version History

Introduced in R2017a

## References

[1] Richards, M. Fundamentals of Radar Signal Processing, 2nd ed. McGraw-Hill Professional Engineering, 2014.
[2] Richards, M., J. Scheer, and W. Holm, Principles of Modern Radar: Basic Principles. SciTech Publishing, 2010.

## See Also

## Blocks

Range Doppler Response
Functions
chebwin | dechirp | hann | hamming | kaiser | taylorwin
Objects
phased.RangeResponse | phased.RangeDopplerResponse | phased.CFARDetector | phased.CFARDetector2D

## Receiver Preamp

Receiver preamplifier


## Libraries:

Phased Array System Toolbox / Transmitters and Receivers

## Description

The Receiver Preamp block implements a receiver preamplifier that amplifies an input signal and adds thermal noise. In addition, you can add phase noise using an input port.

## Ports

## Input

$\mathbf{X}$ - Input signal
complex-valued matrix
Input signal, specified as a complex-valued matrix.
The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
Data Types: double
TR - Enable enabling signal
logical-valued scalar | scalar
Enable enabling signal, specified as a column vector whose length equals the number of rows in the input signal X. Every element of TR that equals 0 or false indicates that the receiver is turned off, and no input signal passes through the receiver. Every element of TR that is nonzero or true indicates that the receiver is turned on, and the input signal passes through.

## Dependencies

To enable this port, select the Enable enabling signal input check box.

## Data Types: double | Boolean

Ph - Input phase noise
scalar
Phase noise for each input sample of $X$, specified as a column vector whose length equals the number of rows in X .

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

## Dependencies

To enable this port, select the Enable phase noise input check box.

## Data Types: double

## Output

Out 1 - Output
complex-valued matrix
Output signal, returned as a complex-valued matrix.
Data Types: double

## Parameters

Gain (dB) - Gain of receiver
20 (default)
Specify a scalar containing the gain in dB of the receiver preamplifier.
Loss factor (dB) - Loss factor of receiver
0 (default)
Specify a scalar containing the loss factor in dB of the receiver preamplifier.
Noise specification method - Noise specification method
Noise temperature (default)|Noise power
Specify the receiver noise as Noise power or Noise temperature.
Noise power (W) - Noise power

## 0 (default)

Specify a scalar containing the noise power in watts at the receiver preamplifier. If the receiver has multiple channels or sensors, the noise bandwidth applies to each channel or sensor.

## Dependencies

This parameter appears only when you set Noise specification method to Noise power.
Noise figure (dB) - Noise figure of receiver

## 0 (default)

Specify a scalar containing the noise figure of the receiver preamplifier. Units are in dB . If the receiver has multiple channels or sensors, the noise figure applies to each channel or sensor. This parameter appears only when you set Noise specification method to Noise temperature.

## Dependencies

This parameter appears only when you set Noise specification method to Noise temperature.

## Reference temperature (K) - Reference temperature of receiver

290 (default)
A scalar containing the reference temperature in degrees kelvin of the receiver preamplifier. If the receiver has multiple channels or sensors, the reference temperature applies to each channel or sensor.

## Dependencies

This parameter appears only when you set Noise specification method to Noise temperature.
Inherit sample rate - Inherit sample rate
on (default) | off
Select this check box to inherit the sample rate from upstream blocks. Otherwise, specify the sample rate using the Sample rate parameter.

## Dependencies

This parameter appears only when you set Noise specification method to Noise temperature.
Sample rate (Hz) - Sampling rate of signal
le6 (default) | positive real-valued scalar

Specify the signal sampling rate as a positive scalar. Units are in Hz .

## Dependencies

To enable this parameter, clear the Inherit sample rate check box.

## Data Types: double

Enable enabling signal input - Add input to specify enabling signal
off (default) | on
Select this check box to allow input of the receiver-enabling signal via the input port TR. T

## Dependencies

This parameter appears only when you set Noise specification method to Noise temperature.
Enable phase noise input - Add input to specify phase noise

```
off (default) | on
```

Select this check box to allow input of phase noise for each incoming sample using the input port Ph. You can use this information to emulate coherent-on-receive systems.

## Dependencies

This parameter appears only when you set Noise specification method to Noise temperature.
Simulate using - Block simulation method
Interpreted Execution (default)|Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).

## Programmatic Use

Block Parameter:SimulateUsing
Type:enum
Values:Interpreted Execution, Code Generation
Default:Interpreted Execution

## Version History

Introduced in R2014b

## See Also

phased.ReceiverPreamp

## Rectangular Waveform

Rectangular pulse waveform

## Libraries:

Rectangular
Phased Array System Toolbox / Detection

## Description

The Rectangular Waveform block generates a rectangular pulse waveform with a specified pulse width and pulse repetition frequency (PRF). The block outputs an integral number of pulses or samples.

## Ports

Input
PRFIdx - PRF Index
positive integer
Index to select the pulse repetition frequency (PRF), specified as a positive integer. The index selects the PRF from the predefined vector of values specified by the Pulse repetition frequency ( $\mathbf{H z}$ ) parameter.
Example: 4

## Dependencies

To enable this port, select Enable PRF selection input.

## Data Types: double

FreqOffset - Frequency offset
scalar
Frequency offset in Hz , specified as a scalar.
Example: 2e3

## Dependencies

To enable this port, set Source of Frequency Offset to Input port.
Data Types: double

## Output

Y - Pulse waveform
complex-valued vector
Pulse waveform samples, returned as a complex-valued vector.
Data Types: double

PRF - Pulse repetition frequency
positive scalar
Pulse repetition frequency of current pulse, returned as a positive scalar.

## Dependencies

To enable this port, set the Output signal format parameter to Pulses and then select the Enable PRF output parameter.

Data Types: double
Coeff - Matched filter coefficients
vector | matrix
Matched filter coefficients, returned as a vector or matrix.

## Dependencies

To enable this port, select Enable Matched Filter Coefficients Output.

## Data Types: double

## Parameters

Sample rate (Hz) - Sample rate of the output waveform
1e6 (default) | positive scalar

Sample rate of the output waveform, specified as a positive scalar. The ratio of Sample rate (Hz) to each element in the Pulse repetition frequency (Hz) vector must be an integer. This restriction is equivalent to requiring that the pulse repetition interval is an integral multiple of the sample interval.

Programmatic Use<br>Block Parameter:SampleRate<br>Type:double<br>Values:positive scalar<br>Default:1e6

Method to specify pulse duration - Pulse duration as time or duty cycle
Pulse width (default)| Duty cycle

Method to set the pulse duration, specified as Pulse width or Duty cycle. When you set this parameter to Pulse width, the pulse duration is set using the Pulse width (s) parameter. When you set this parameter to Duty cycle, the pulse duration is computed from the values of the Pulse repetition frequency $(\mathrm{Hz})$ and Duty Cycle parameters.

```
Programmatic Use
Block Parameter:DurationSpecification
Type:string
Values:string
Default:'Pulse width'
Pulse width (s) - Time duration of pulse
50e-6 (default) | positive scalar
```

The duration of each pulse, specified as a positive scalar. Set the product of Pulse width (s) and Pulse repetition frequency to be less than or equal to one. This restriction ensures that the pulse width is smaller than the pulse repetition interval. Units are in seconds.
Example: 300e-6

## Dependencies

To enable this parameter, set the Method to specify pulse duration parameter to Pulse width.

## Programmatic Use

Block Parameter:PulseWidth
Type:double
Values:string
Default:50e-6
Duty cycle - Waveform duty cycle
0.5 (default) | scalar in the range [0,1]

Waveform duty cycle, specified as a scalar in the range [0,1].
Example: 0.7

## Dependencies

To enable this parameter, set the Method to specify pulse duration parameter to Duty cycle.
Programmatic Use
Block Parameter:DutyCycle
Type:double
Values:positive scalar
Default:1e6
Pulse repetition frequency (Hz) - Pulse repetition frequency
le4 (default) | positive scalar

Pulse repetition frequency, $P R F$, specified as a scalar or a row vector. Units are in Hz . The pulse repetition interval, $P R I$, is the inverse of the pulse repetition frequency, $P R F$. The value of Pulse repetition frequency $(\mathbf{H z})$ must satisfy these constraints:

- The product of Pulse width and Pulse repetition frequency $\mathbf{( H z )}$ must be less than or equal to one. This condition expresses the requirement that the pulse width is less than one pulse repetition interval. For the phase-coded waveform, the pulse width is the product of the chip width and number of chips.
- The ratio of sample rate to any element of Pulse repetition frequency must be an integer. This condition expresses the requirement that the number of samples in one pulse repetition interval is an integer.

You can select the value of $P R F$ by using block parameter settings alone or in conjunction with the input port, PRFIdx.

- When the Enable PRF selection input parameter is not selected, set the PRF using block parameters.
- To implement a constant $P R F$, specify Pulse repetition frequency (Hz) as a positive scalar.
- To implement a staggered $P R F$, specify Pulse repetition frequency (Hz) as a row vector with positive values. After the waveform reaches the last element of the vector, the process continues cyclically with the first element of the vector. When $P R F$ is staggered, the time between successive output pulses cycles through the successive values of the $P R F$ vector.
- When the Enable PRF selection input parameter is selected, you can implement a selectable $P R F$ by specifying Pulse repetition frequency (Hz) as a row vector with positive real-valued entries. But this time, when you execute the block, select a $P R F$ by passing an index into the $P R F$ vector into the PRFIdx port.

In all cases, the number of output samples is fixed when you set the Output signal format to Samples. When you use a varying $P R F$ and set Output signal format to Pulses, the number of output samples can vary.

Programmatic Use
Block Parameter:PRF
Type:double
Values:positive scalar
Default:1e6
Enable PRF selection input - Select predefined PRF
off (default) | on

Select this parameter to enable the PRFIdx port.

- When enabled, pass in an index into a vector of predefined PRFs. Set predefined PRFs using the Pulse repetition frequency $(\mathbf{H z})$ parameter.
- When not enabled, the block cycles through the vector of PRFs specified by the Pulse repetition frequency (Hz) parameter. If Pulse repetition frequency (Hz) is a scalar, the PRF is constant.


## Programmatic Use

Block Parameter:PRFSelectionInputPort
Type:logical
Values:positive scalar
Default:off
Source of Frequency Offset - Source of frequency offset
Property (default)| Input port

Source of frequency offset, specified as Property or Input port.

- When set to Property, the offset is determined by the value of the Frequency Offset parameter.
- When set to Input port, the offset is determined by the value of the FreqOffset port.


## Programmatic Use

Block Parameter:Frequency0ffsetSource
Type:enum
Values:Property, Input Port
Default:Property
Frequency Offset (Hz) - Frequency offset
0 (default) | scalar

Frequency offset, specified as a scalar. Units are in Hz.
Example: 2e3

## Dependencies

To enable this parameter set the Source of Frequency Offset parameter to Input port.
Programmatic Use
Block Parameter:FrequencyOffset
Type:double
Values:scalar
Default:0
Source of simulation sample time - Source of simulation sample time
Derive from waveform parameters (default)|Inherit from Simulink engine

Source of simulation sample time, specified as Derive from waveform parameters or Inherit from Simulink engine. When set to Derive from waveform parameters, the block runs at a variable rate determined by the PRF of the selected waveform. The elapsed time is variable. When set to Inherit from Simulink engine, the block runs at a fixed rate so the elapsed time is a constant.

## Dependencies

To enable this parameter, select the Enable PRF selection input parameter.

## Programmatic Use

Block Parameter:SimulationTimeSource
Type:enum
Values:Derive from waveform parameters, Inherit from Simulink engine
Default:Derive from waveform parameters
Output signal format - Format of the output signal
Pulses (default)| Samples

The format of the output signal, specified as Pulses or Samples.
If you set this parameter to Samples, the output of the block consists of multiple samples. The number of samples is the value of the Number of samples in output parameter.

If you set this parameter to Pulses, the output of the block consists of multiple pulses. The number of pulses is the value of the Number of pulses in output parameter.

Programmatic Use<br>Block Parameter:0utputFormat<br>Type:enum<br>Values:Pulses Samples<br>Default:Pulses<br>Number of samples in output - Number of samples in output<br>100 (default) | positive integer

Number of samples in the block output, specified as a positive integer.

## Example: 1000

## Dependencies

To enable this parameter, set the Output signal format parameter to Samples.

## Programmatic Use

Block Parameter:NumSamples
Type:double
Values:positive scalar
Default:100
Data Types: double
Number of pulses in output - Number of pulses in output
1 (default) | positive integer

Number of pulses in the block output, specified as a positive integer.
Example: 2

## Dependencies

To enable this parameter, set the Output signal format parameter to Pulses.

```
Programmatic Use
Block Parameter:NumPulses
Type:double
Values:positive scalar
Default:1
Data Types: double
```

Enable PRF Output - Enable output of PRF
off (default) | on

Select this parameter to enable the PRF output port.

## Dependencies

To enable this parameter, set Output signal format to Pulses.

## Programmatic Use

Block Parameter:PRF0utputPort
Type:enum
Values:off on
Default:off
Enable Matched Filter Coeficients Output - Enable output of matched filter coefficients off (default) | on

Select this parameter to enable the Coeff output port.

```
Programmatic Use
Block Parameter:CoefficientOutputPort
Type:enum
Values:off on
Default:off
Simulate using - Block simulation method
Interpreted Execution (default)| Code Generation
```

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted | The block executes <br> Execution <br> interpreter. | The block executes <br> ising the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).

Programmatic Use<br>Block Parameter:SimulateUsing<br>Type:enum<br>Values:Interpreted Execution, Code Generation<br>Default:Interpreted Execution

## Version History

## Introduced in R2014b

## See Also

phased.RectangularWaveform

## Angle-Time Intensity Scope

Angle-time intensity scope


Libraries:

Phased Array System Toolbox / Sinks

## Description

The Angle-Time Intensity Scope block creates a scrolling display of angle response intensities as a function of time. The input consists of angle responses for a pulse or FMCW signal. Each frame of data creates a new line on the scope. The scope serves as a display of the angle response.


Ports
Input
X - Input data
real-valued length- $M$ vector
Input data, specified as a real-valued length- $M$ vector of angle responses. Each vector corresponds to a line of data. The block can accept single precision data type input, but converts the data to double precision for display.
Data Types: double | single

## Parameters

Angle offset (degree) - Angle offset
0.0 (default) | scalar

Angle offset, specified as a scalar. This property defines the angle value of the first column of the display. Units are in degrees.

```
Programmatic Use
Block Parameter:AngleOffset
Type:double
Values:scalar |
Default:0.0
Data Types: double
```

Angle resolution (degree) - Angle difference between samples
1.0 (default) | positive scalar

Angle separation between samples, specified as a positive scalar. This property defines the angle difference between columns of the scope. Units are in degrees.

## Programmatic Use <br> Block Parameter:AngleResolution <br> Type:double <br> Values:positive scalar| <br> Default:0.0 <br> Data Types: double <br> Time span (s) - Time span of display <br> Auto (default)

Time span of the intensity display, specified as a positive scalar. When the Time span (s) is set to Auto the simulation stops at the default stop time of the simulation. Units are in seconds.

Programmatic Use
Block Parameter:TimeSpan
Type:double
Values:scalar
Default:0.1
Data Types: double
Time resolution (s) - Time difference between rows
Auto (default)
Time interval between rows, specified as a positive scalar. This property defines the time duration between rows of the scope. When the Time resolution (s) parameter is set to Auto the block uses the Compiled Sample Time value during simulation. At all other times, the block uses the value specified by this parameter. Units are in seconds.

## Programmatic Use

Block Parameter:TimeResolution
Type:double
Values:positive scalar

Default:0.001
Data Types: double
Grid - Show Cartesian grid overlay on (default) | off

Show Cartesian grid overlay. To show the grid, select the check box.
Programmatic Use
Block Parameter:ShowGrid
Type:logical
Values:1|0
Default:1
Ticks - Show tick value labels
on (default) | off
Show value labels on tick marks. To display the labels, select the check box.
Programmatic Use
Block Parameter:ShowTicks
Type:logical
Values:1|0
Default:1
Labels
Angle label - Angle-axis label
'Angle (degree) ' (default) | character vector $\mid$ string
Angle-axis label, specified as a character vector or a string.
Example: 'Angle (rad)'
Tunable: Yes
Programmatic Use
Block Parameter:AngleLabel
Type:string
Values:string
Default:'Angle (degree)'
Data Types: char|string
Time label - Time axis label
'Time History (s)' (default)|string
Time-axis label, specified as a string.
Tunable: Yes
Programmatic Use
Block Parameter:TimeLabel
Type:string
Values:string
Default:'Time History (s)'

Data Types: string
Title - Window title
Angle vs. Time' (default) | string
Window title, specified as a string.
Tunable: Yes
Programmatic Use
Block Parameter:Title
Type:string
Values:string
Default:'Doppler vs. Time'
Data Types: char
Colorbar label - Color bar label
'dB' (default)|string
Color bar label, specified as a string.
Tunable: Yes
Programmatic Use
Block Parameter:ColorBarLabel
Type:string
Values:string
Default:'dB'
Data Types: string

## Block Characteristics

| Data Types | double $\mid$ single |
| :--- | :--- |
| Direct Feedthrough | no |
| Multidimensional <br> Signals | no |
| Variable-Size Signals | no |
| Zero-Crossing <br> Detection | no |

## More About

## Description

This section shows how to run the scope, configure the settings to show labels for the various features and use the cursor to examine data. The scope is based on the phased. ATIScope System object. Using the scope to display response corresponds to setting the IQDataInput property of the phased.ATIScope System object to false.

## Run the Scope

After selecting and opening the block, the scope displays a single tab PLOT. Click the tab to show all the controls available for the block. The Settings menu displays all the settable parameters for the scope. The Step Back, Run, Step Forward, and Stop buttons control the simulation. The Data Cursors button lets you examine data values on the display.


## Scope Parameter Settings

Clicking the Settings button on the PLOT tab opens the parameter window with the DATA AND AXES and LABELS parameters.

Angle-Time Intensity Scope Settings

```
- DATA AND AXES
```

| Angle offset (degree) |  | 0 |  | Angle resolution (degree) |  | 1 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Time span (s) |  | Auto | $\checkmark$ | Time resolution (s) |  | Auto |
| $\checkmark$ Grid | $\square$ Ticks |  |  |  |  |  |
| - LABELS |  |  |  |  |  |  |
| Angle label | Angle (degree) |  |  | Time label | Time History (s) |  |
| Title | Angle vs. Time |  |  | Colorbar label | dB |  |

## DATA AND AXES

- Angle offset (Hz) - Use this field to set the frequency offset of the $x$-axis.
- Angle resolution (Hz) - Use this field to set the granularity of the x-axis.
- Time span (s) - Use this field to set the duration of the y-axis.
- Time resolution (s) - Use this field to set the granularity of the y-axis.


## LABELS

- Angle label - Use this field to set the $y$-axis label.
- Time label - Use this field to set the $y$-axis label.
- Title - Use this field to set the display title.
- Colorbar label - Set this field to set the color bar label.


Stopped

## Using Cursors

Click the Data Cursors button to display the screen cursors. Each cursor consists of intersecting horizontal and vertical cursors that define a point on the display. Positioning two cursors on the display shows the difference between the intensities at the two cursor points.


## Version History

Introduced in R2022b

## Extended Capabilities

## C/C++ Code Generation

Generate C and C++ code using Simulink ${ }^{\circledR}$ Coder $^{\text {TM }}$.

This block can be used for simulation visibility in systems that generate code but is not included in the generated code.

## See Also

Range-Time Intensity Scope | Doppler-Time Intensity Scope \| phased.ATIScope | phased.DTIScope | phased.RTIScope

## Range-Time Intensity Scope

Range-time intensity scope


Libraries:<br>Phased Array System Toolbox / Sinks

## Description

The Range-Tine Intensity Scope block creates a scrolling display of range response intensities as a function of time. The input consists of range responses for a pulse or FMCW signal. Each frame of data creates a new line on the scope. The scope serves only as a display of the range response. Using the response as input corresponds to setting the IQDataInput property of the phased.RTIScope System object to false.


## Ports

## Input

X - Input data
real-valued length- $M$ vector
Input data, specified as a real-valued length- $M$ vector of range responses. Each vector corresponds to a line of data. The block accepts single precision data type input, but converts the data to double precision for display.
Data Types: double | single

## Parameters

## Data and Axes

Range Offset (m) - Range offset
0.0 (default) | positive scalar

Range offset, specified as a positive scalar. This parameter defines the range value of the first column of the display. Units are in meters.

## Programmatic Use

Block Parameter:RangeOffset
Type:double
Values:scalar
Default:0
Data Types: double
Time Span (s) - Time span of display
0.1 (default) | positive scalar

Time span of the intensity display, specified as a positive scalar. Units are in seconds.

Programmatic Use<br>Block Parameter:TimeSpan<br>Type:double<br>Values:scalar<br>Default:1<br>Data Types: double

Range Resolution (m) - Range difference between samples
1 (default) | positive scalar
Range distance between samples, specified as a positive scalar. This parameter defines the distance between columns of the scope. Units are in meters.

```
Programmatic Use
Block Parameter:RangeResolution
Type:double
Values:positive scalar
Default:25
Data Types: double
```

Time Resolution (s) - Time difference between rows
0.001 (default) | positive scalar

Time interval between samples, specified as a positive scalar. This parameter defines the time interval between the rows of the scope. Units are in seconds.

Programmatic Use
Block Parameter:TimeResolution
Type:double
Values:positive scalar
Default:0.00033356
Data Types: double

Show Grid - Show Cartesian grid overlay
on (default) | off
Show Cartesian grid overlay. To show the grid, select the check box.

```
Programmatic Use
Block Parameter:ShowGrid
Type:logical
Values:1|0
Default:1
```

Show Ticks - Show tick value labels
on (default) | off

Show value labels on tick marks. The display the labels on, select the check box.

```
Programmatic Use
Block Parameter:ShowTicks
Type:logical
Values:1 | 0
Default:1
Labels
Range Label - Range axis label
'Range (m) ' (default) | string
```

Range-axis label, specified as a string.
Tunable: Yes
Programmatic Use
Block Parameter:RangeLabel
Type:string
Values:string
Default:'Range (m)'
Data Types: char
Time Label - Time axis label
Time History (s)' (default)|string
Time-axis label, specified as a string.
Tunable: Yes
Programmatic Use
Block Parameter:TimeLabel
Type:string
Values:string
Default:'Time History (s)'
Data Types: string
Title - Window title
'Range vs. Time' (default) | string
Window title, specified as a string.

Tunable: Yes
Programmatic Use
Block Parameter:Title
Type:string
Values:string
Default:Range vs. Time'
Data Types: char
Colorbar Label - Color bar
'mag ' (default) | string
Color bar label, specified as a string.
Tunable: Yes
Programmatic Use
Block Parameter:ColorBarLabel
Type:string
Values:string
Default: 'mag'
Data Types: string

## Block Characteristics

| Data Types | double \| single |
| :--- | :--- |
| Direct Feedthrough | no |
| Multidimensional <br> Signals | no |
| Variable-Size Signals | no |
| Zero-Crossing <br> Detection | no |

## Algorithms

This section shows how to run the scope, configure the settings to show labels for the various features and use the cursor to examine data.

## Run the Scope

After selecting and opening the block, the scope displays a single tab PLOT. Opening this tab shows all the controls available for the block. The Settings menu displays all the settable parameters for the scope. The Step Back, Run, Step Forward, and Stop buttons control the simulation. The Data Cursors button lets you examine data values on the display.


## Scope Parameter Settings

Selecting the Settings menu from PLOT panel scope opens the parameter window with the DATA AND AXES and LABELS panels.


## DATA AND AXES

- Range Offset (m) - Use this field to set the offset of the x -axis.
- Range Resolution (m) - Use this field to set the granularity of the x-axis.
- Time Span (s) - Use this field to set the duration of the $y$-axis.
- Time Resolution (s) - Use this field to set the granularity of the $y$-axis.


## Labels

- Range Label - Use this field to set the $x$-axis label.
- Time Label - Use this field to set the y-axis label.
- Title - Use this field to set the display title.
- Colorbar Label - Use this field to set the color bar label.



## Using Cursors

Select the Cursors Button to display the screen cursors. Each cursor consists of intersecting horizontal and vertical lines that define a point on the display. Positioning two cursors on the display shows the difference between the intensities at the two cursor points.


Stopped

## Version History

Introduced in R2022a

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using Simulink ${ }_{\circledR}$ Coder ${ }^{\mathrm{TM}}$.
This block can be used for simulation visibility in systems that generate code but

## See Also

Doppler-Time Intensity Scope | Angle-Time Intensity Scope | phased. DTIScope | phased.RTIScope

## Doppler-Time Intensity Scope

Doppler-time intensity scope
Libraries:
Phased Array System Toolbox / Sinks

## Description

The Doppler-Time Intensity Scope block creates a scrolling display of Doppler response intensities as a function of time. The input consists of Doppler responses for a pulse or FMCW signal. Each frame of data creates a new line on the scope. The scope serves only as a display of the Doppler response. Using the response as input corresponds to setting the IQDataInput property of the phased.DTIScope System object to false.


## Ports

## Input

X - Input data
real-valued length- $M$ vector
Input data, specified as a real-valued length- $M$ vector of Doppler responses. Each vector corresponds to a line of data. The block accepts single precision data type input, but converts the data to double precision for display.
Data Types: double | single

## Parameters

Doppler Output - Doppler output domain
'Frequency ' (default) | 'Speed '
Doppler output domain, specified as 'Frequency ' or 'Speed '. If you set this property to
' Frequency ' , the Doppler domain is Doppler shift. Units are in Hz. If you set this property to
'Speed ' ', the Doppler domain is radial speed. Units are in m/s.
Programmatic Use
Block Parameter:DopplerOutput
Type:character vector
Values: 'Frequency' | 'Speed'
Default:'Frequency'
Data Types: string
Propagation Speed ( $\mathbf{m} / \mathbf{s}$ ) - Signal propagation speed
physconst("LightSpeed") (default)| positive scalar
Signal propagation speed, specified as a positive scalar. To obtain the speed of light in SI units, use physconst. Units are in meters/second.
Example: 3e8
Programmatic Use
Block Parameter:PropagationSpeed
Type:double
Values:positive scalar
Default:physconst("LightSpeed")
Data Types: double
Doppler Offset (Hz) - Doppler axis offset
0.0 (default) | scalar

Doppler axis offset, specified as a scalar. This property applies a frequency offset to the Doppler axis. Units are in Hz .

Programmatic Use
Block Parameter:DopplerOffset
Type:double
Values:scalar
Default:0
Data Types: double
Time Span (s) - Time span of display
0.100 (default) | positive scalar

Time span of the intensity display, specified as a positive scalar. Units are in seconds.

```
Programmatic Use
Block Parameter:TimeSpan
Type:double
Values:scalar
Default:0.1
```


## Data Types: double

Operating Frequency (Hz) - Operating frequency
300e6 (default) | positive scalar
Operating frequency, specified as a positive scalar. Units are in Hz.

```
Programmatic Use
Block Parameter:OperatingFrequency
Type:double
Values:scalar
Default:300000000
Data Types: double
```

Doppler Resolution (Hz) - Doppler interval between samples
1.0 (default) | positive scalar

Doppler interval between samples, specified as a positive scalar. This property defines the Doppler frequency difference between the scope columns. Units are in Hz.

```
Programmatic Use
Block Parameter:DopplerResolution
Type:double
Values:positive scalar
Default:1
Data Types: double
```

Time Resolution (s) - Time difference between rows
0.001 (default) | positive scalar

Time interval between samples, specified as a positive scalar. This property defines the time duration between rows of scope. Units are in seconds.

```
Programmatic Use
Block Parameter:TimeResolution
Type:double
Values:positive scalar
Default:0.001
Data Types: double
```

Show Grid - Show Cartesian grid overlay
on (default) | off
Show Cartesian grid overlay. To show the grid, select the check box.
Programmatic Use
Block Parameter:ShowGrid
Type:logical
Values:1|0
Default:1
Show Ticks - Show tick value labels
on (default) | off
Show value labels on tick marks. The display the labels on, select the check box.

```
Programmatic Use
Block Parameter:ShowTicks
Type:logical
Values:1 | 0
Default:1
Labels
Time Label - Time axis label
'Time (s)' (default)| string
```

Time-axis label, specified as a string.
Tunable: Yes
Programmatic Use
Block Parameter:TimeLabel
Type:string
Values:string
Default:'Time History (s)'
Data Types: string
Colorbar Label - Color bar label
' dB' (default) | string
Color bar label, specified as a string.
Tunable: Yes
Programmatic Use
Block Parameter:ColorBarLabel
Type:string
Values:string
Default:'dB'
Data Types: string
Title - Window title
'Doppler vs. Time' (default)|string
Window title, specified as a string.
Tunable: Yes
Programmatic Use
Block Parameter:Title
Type:string
Values:string
Default:'Doppler vs. Time'
Data Types: char

## Block Characteristics

Data Types $\quad$ double | single

| Direct Feedthrough | no |
| :--- | :--- |
| Multidimensional <br> Signals | no |
| Variable-Size Signals | no |
| Zero-Crossing <br> Detection | no |

## Algorithms

This section shows how to run the scope, configure the settings to show labels for the various features and use the cursor to examine data.

## Run the Scope

After selecting and opening the block, the scope displays a single tab PLOT. Opening this tab shows all the controls available for the block. The Settings menu displays all the settable parameters for the scope. The Step Back, Run, Step Forward, and Stop buttons control the simulation. The Data Cursors button lets you examine data values on the display.


## Scope Parameter Settings

Selecting the Settings menu from PLOT panel scope opens the parameter window with the DATA AND AXES and LABELS panels.


## DATA AND AXES

- Doppler Output - Use this field to choose Frequency for the Doppler shift or Speed for the radial speed.
- Operating Frequency (Hz) - Use this field to set the scaling on the $x$-axis.
- Doppler Offset (Hz) - Use this field to set the frequency offset of the x-axis.
- Doppler Resolution (Hz) - Use this field to set the granularity of the x -axis.
- Time Span (s) - Use this field to set the duration of the $y$-axis.
- Time Resolution (s) - Use this field to set the granularity of the $y$-axis.


## Labels

- Time Label - Use this field to set the y-axis label.
- Title - Use this field to set the display title.
- Colorbar Label - Set this field to set the color bar label.


Stopped

## Using Cursors

Select the Cursors Button to display the screen cursors. Each cursor consists of intersecting horizontal and vertical cursors that define a point on the display. Positioning two cursors on the display shows the difference between the intensities at the two cursor points.


Stopped

## Version History

Introduced in R2022a

## Extended Capabilities

C/C++ Code Generation
Generate C and C++ code using Simulink ${ }^{\circledR}$ Coder $^{\mathrm{TM}}$.
This block can be used for simulation visibility in systems that generate code but is not included in the generated code.

## See Also

Range-Time Intensity Scope | Angle-Time Intensity Scope | phased.DTIScope | phased.RTIScope

## Root MUSIC DOA

Root multiple signal classification (MUSIC) direction of arrival (DOA) estimator for ULA and UCA

## Libraries:

Phased Array System Toolbox / Direction of Arrival

## Description

The Root MUSIC DOA block estimates the direction of arrival of a specified number of narrowband signals incident on a uniform linear array or uniform circular array using the root multiple signal classification (Root MUSIC) algorithm.

## Ports

## Input

In - Input signal
complex-value matrix
Input signal, specified as a complex-value matrix. Matrix columns correspond to signal channels.
The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

## Data Types: single | double

EIAng - Elevation angle
scalar
Elevation angle, specified as a scalar between $-90^{\circ}$ and $90^{\circ}$. The elevation angles for all signals must be the same as required by the phase mode excitation algorithm. Units are in degrees.

## Dependencies

To enable this port, set the Geometry pull down menu in the Sensor Array panel to UCA.

## Data Types: single | double

## Output

Ang - Output
real-valued row vector
Estimated broadside direction-of-arrival angles, returned as real-valued row vector. Units are in degrees.
Data Types: double

## Parameters

## Main Tab

Signal propagation speed ( $\mathbf{m} / \mathbf{s}$ ) - Signal propagation speed
physconst('LightSpeed') (default) | real-valued positive scalar

Signal propagation speed, specified as a real-valued positive scalar. The default value of the speed of light is the value returned by physconst ('LightSpeed'). Units are in meters per second.
Example: 3e8
Data Types: double
Operating frequency $(\mathbf{H z})$ - System operating frequency
3e8 (default) | positive real scalar

System operating frequency, specified as a positive scalar. Units are in Hz .
Number of signals - Number of signals
1 (default) | positive integer scalar
Specify the number of signals as a positive integer scalar.
Forward-backward averaging - Enable forward-backward averaging
off (default) | on

Select this parameter to use forward-backward averaging to estimate the covariance matrix for sensor arrays with a conjugate symmetric array manifold structure.

Spatial smoothing - Enable spatial smoothing
0 (default) | non-negative integer

Specify the amount of averaging used by spatial smoothing to estimate the covariance matrix as a nonnegative integer. Each increase in smoothing handles one extra coherent source, but reduces the effective number of elements by one. The maximum value of this parameter is $N-2$, where $N$ is the number of sensors in the ULA.

Simulate using - Block simulation method
Interpreted Execution (default)|Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations
run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).

## Programmatic Use

Block Parameter:SimulateUsing
Type:enum
Values:Interpreted Execution, Code Generation
Default:Interpreted Execution

## Sensor Array Tab

Specify sensor array as - Method to specify array
Array (no subarrays) (default)|MATLAB expression

Method to specify array, specified as Array (no subarrays) or MATLAB expression.

- Array (no subarrays) - use the block parameters to specify the array.
- MATLAB expression - create the array using a MATLAB expression.


## Element Parameters

## Element type - Array element types

Isotropic Antenna (default)|Cardioid Antenna|Cosine Antenna|Custom Antenna| Gaussian Antenna|Sinc Antenna|Omni Microphone|Custom Microphone

Antenna or microphone type, specified as one of the following:

- Isotropic Antenna
- Cardioid Antenna
- Cosine Antenna
- Custom Antenna
- Gaussian Antenna
- Sinc Antenna
- Omni Microphone
- Custom Microphone

Operating frequency range $(\mathbf{H z})$ - Operating frequency range of the antenna or microphone element
[0,1e20] (default) | real-valued 1-by-2 row vector

Specify the operating frequency range of the antenna or microphone element as a 1-by-2 row vector in the form [LowerBound, UpperBound]. The element has no response outside this frequency range. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Isotropic Antenna, Cosine Antenna, or Omni Microphone.

Baffle the back of the element - Set back response of an Isotropic Antenna element or an Omni Microphone element to zero
off (default) | on

Select this check box to baffle the back response of the element. When back baffled, the responses at $0^{\circ}$ all azimuth angles beyond $\pm 90^{\circ}$ from broadside are set to zero. The broadside direction is defined as $0^{\circ}$ azimuth angle and $0^{\circ}$ elevation angle.

## Dependencies

To enable this check box, set Element type to Isotropic Antenna or Omni Microphone.
Null axis direction - Null axis direction
$-x$ (default) $|+x|+y|-y|+z \mid-z$

## Dependencies

To enable this parameter, set Element type to Cardioid Antenna.
Exponent of cosine pattern - Exponents of azimuth and elevation cosine patterns
[1.5 1.5] (default) | nonnegative scalar | real-valued 1-by-2 matrix of nonnegative values

Specify the exponents of the cosine pattern as a nonnegative scalar or a real-valued 1-by-2 matrix of nonnegative values. When Exponent of cosine pattern is a 1 -by-2 vector, the first element is the exponent in the azimuth direction and the second element is the exponent in the elevation direction. When you set this parameter to a scalar, both the azimuth direction and elevation direction cosine patterns are raised to the same power.

## Dependencies

To enable this parameter, set Element type to Cosine Antenna.
Operating frequency vector ( $\mathbf{H z}$ ) - Operating frequency range of custom antenna or microphone elements
[0,1e20] (default) | real-valued row vector

Specify the frequencies at which to set antenna and microphone frequency responses as a 1-by- $L$ row vector of increasing real values. The antenna or microphone element has no response outside the frequency range specified by the minimum and maximum elements of this vector. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone. Use Frequency responses (dB) to set the responses at these frequencies.

Frequency responses (dB) - Antenna and microphone frequency response
[0,0] (default) | real-valued row vector

Frequency response of a custom antenna or custom microphone for the frequencies defined by the Operating frequency vector ( $\mathbf{H z}$ ) parameter. The dimensions of Frequency responses (dB) must match the dimensions of the vector specified by the Operating frequency vector $(\mathbf{H z})$ parameter.

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone.
Input Pattern Coordinate System - Coordinate system of custom antenna pattern az-el (default) | phi-theta

Coordinate system of custom antenna pattern, specified az-el or phi-theta. When you specify azel, use the Azimuth angles (deg) and Elevations angles (deg) parameters to specify the coordinates of the pattern points. When you specify phi-theta, use the Phi angles (deg) and Theta angles (deg) parameters to specify the coordinates of the pattern points.

## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Azimuth angles (deg) - Azimuth angles of antenna radiation pattern
[-180:180] (default) | real-valued row vector

Specify the azimuth angles at which to calculate the antenna radiation pattern as a 1 -by- $P$ row vector. $P$ must be greater than 2. Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to az-el.

Elevation angles (deg) - Elevation angles of antenna radiation pattern
[-90:90] (default) | real-valued row vector

Specify the elevation angles at which to compute the radiation pattern as a 1-by- $Q$ vector. $Q$ must be greater than 2. Angle units are in degrees. Elevation angles must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to az-el.

Phi Angles (deg) - Phi angle coordinates of custom antenna radiation pattern
$0: 360$ | real-valued 1-by-P row vector

Phi angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by-P row vector. $P$ must be greater than 2 . Angle units are in degrees. Phi angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Theta Angles (deg) - Theta angle coordinates of custom antenna radiation pattern 0:180 | real-valued 1-by- $Q$ row vector

Theta angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by$Q$ row vector. $Q$ must be greater than 2 . Angle units are in degrees. Theta angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Magnitude pattern (dB) - Magnitude of combined antenna radiation pattern zeros $(181,361)$ (default) | real-valued $Q$-by-P matrix | real-valued $Q$-by-P-by-L array

Magnitude of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector $(\mathbf{H z})$.

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (Hz) parameter.


## Dependencies

To enable this parameter, set Element type to Custom Antenna.

Phase pattern (deg) - Custom antenna radiation phase pattern
zeros $(181,361)$ (default) | real-valued $Q$-by- $P$ matrix | real-valued $Q$-by- $P$-by- $L$ array

Phase of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector $(\mathbf{H z})$.

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (


## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Align element normal with array normal - Align element normal with array normal
on (default) | off

## Dependencies

This parameter is enabled when Element type is set to Custom Antenna.
Radiation pattern beamwidth (deg) - Radiation pattern beamwidth
[10, 10] (default)

## Dependencies

This parameter is enabled when Element type is set to Gaussian Antenna.
Polar pattern frequencies (Hz) - Polar pattern microphone response frequencies
1e3 (default) | real scalar | real-valued 1-by-L row vector

Polar pattern microphone response frequencies, specified as a real scalar, or a real-valued, 1-by- $L$ vector. The response frequencies lie within the frequency range specified by the Operating frequency vector ( $\mathbf{H z}$ ) vector.

## Dependencies

To enable this parameter, set Element type set to Custom Microphone.
Polar pattern angles (deg) - Polar pattern response angles
[-180: 180] (default) | real-valued -by-P row vector

Specify the polar pattern response angles, as a 1-by- $P$ vector. The angles are measured from the central pickup axis of the microphone and must be between $-180^{\circ}$ and $180^{\circ}$, inclusive.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.
Polar pattern (dB) - Custom microphone polar response
zeros (1,361) (default) | real-valued L-by-P matrix

Specify the magnitude of the custom microphone element polar patterns as an $L$-by- $P$ matrix. $L$ is the number of frequencies specified in Polar pattern frequencies $\mathbf{( H z )} . P$ is the number of angles specified in Polar pattern angles (deg). Each row of the matrix represents the magnitude of the polar pattern measured at the corresponding frequency specified in Polar pattern frequencies (Hz) and all angles specified in Polar pattern angles (deg). The pattern is measured in the azimuth plane. In the azimuth plane, the elevation angle is $0^{\circ}$ and the central pickup axis is $0^{\circ}$ degrees azimuth and $0^{\circ}$ degrees elevation. The polar pattern is symmetric around the central axis. You can construct the microphone response pattern in 3-D space from the polar pattern.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.

## Array Parameters

Geometry - Geometry
ULA (default) | UCA
Specify the array geometry as one of the following

- ULA - Uniform Line Array
- UCA - Uniform Circular Array

Number of elements - Number of array elements in $U$
2 (default) | positive integer greater than or equal to two

The number of array elements for ULA arrays, specified as an integer greater than or equal to two.
Example: 11
Data Types: double
Element spacing - Distance between ULA elements
0.5 (default) | positive scalar

Distance between adjacent ULA elements, specified as a positive scalar. Units are in meters.
Example: 1.5
Array axis - Linear axis direction of ULA
y (default) $|x| z$

Linear axis direction of ULA, specified as $y, x$, or $z$. All ULA array elements are uniformly spaced along this axis in the local array coordinate system.

## Dependencies

- To enable this parameter, set Geometry to ULA.
- This parameter is also enabled when the block only supports ULA arrays.

Array normal - Array normal direction
$x$ for URA arrays or $z$ for UCA arrays (default) | y

Array normal direction, specified as $x, y$, or $z$.
Elements of planar arrays lie in a plane orthogonal to the selected array normal direction. Element boresight directions point along the array normal direction.

| Array Normal Parameter Value | Element Positions and Boresight Directions |
| :--- | :--- |
| $x$ | Array elements lie in the $y z$-plane. All element <br> boresight vectors point along the $x$-axis. |
| $y$ | Array elements lie in the $z x$-plane. All element <br> boresight vectors point along the $y$-axis. |
| $z$ | Array elements lie in the $x y$-plane. All element <br> boresight vectors point along the $z$-axis. |

## Dependencies

To enable this parameter, set Geometry to URA or UCA.

## Radius of UCA (m) - UCA array radius

0.5 (default) | positive scalar

Radius of UCA array, specified as a positive scalar.

## Dependencies

To enable this parameter, set Geometry to UCA.
Taper - ULA array taper
1 (default) | complex-valued vector

Tapers, also known as element weights, are applied to sensor elements in the array. Tapers are used to modify both the amplitude and phase of the transmitted or received data.

Specify element tapering as a complex-valued scalar or a complex-valued 1-by- $N$ row vector. In this vector, $N$ represents the number of elements in the array. If Taper is a scalar, the same weight is applied to each element. If Taper is a vector, a weight from the vector is applied to the corresponding sensor element. A weight must be applied to each element in the sensor array.
Example: [0.5;1;0.5]
Data Types: double

Expression - MATLAB expression used to create an array
Phased Array System Toolbox array System object

MATLAB expression used to create a ULA array, specified as a valid Phased Array System Toolbox array System object.

Example: phased.ULA('NumElements',13)
Dependencies
To enable this parameter, set Specify sensor array as to MATLAB expression.

## Version History

Introduced in R2014b

See Also<br>phased.RootMUSICEstimator

## Root WSF DOA

Root weighted subspace fitting (WSF) direction of arrival (DOA) estimator for ULA

## Libraries:



Phased Array System Toolbox / Direction of Arrival

## Description

The Root WSF DOA block estimates the direction of arrival of a specified number of narrowband signals incident on a uniform linear array (ULA) using the root-weighted subspace fitting (RootWSF) algorithm.

## Ports

## Input

In - Input signal
$M$-by- $N$ complex-valued matrix
Input signal, specified as an $M$-by- $N$ complex-valued matrix. $M$ is the number of samples in the signals. The $N$ columns of the matrix correspond to different signals.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
Data Types: single | double

## Output

Ang - Estimated broadside DOA angles
$P$-length row vector
Estimated broadside direction-of-arrival (DOA) angles, returned as a $P$-length row vector. Units are in degrees.
Data Types: double

## Parameters

## Main Tab

Signal propagation speed (m/s) - Signal propagation speed
physconst('LightSpeed') (default)| real-valued positive scalar

Signal propagation speed, specified as a real-valued positive scalar. The default value of the speed of light is the value returned by physconst ('LightSpeed' ). Units are in meters per second.
Example: 3e8

## Data Types: double

Operating frequency $(\mathrm{Hz})$ - System operating frequency
3e8 (default) | positive real scalar

System operating frequency, specified as a positive scalar. Units are in Hz .
Number of signals - Number of signals
1 (default) | positive integer scalar
Specify the number of signals as a positive integer scalar.
Iterative method - Iterative method
IMODE (default) | IQML
Specify the iterative method as one of IMODE or IQML.
Maximum number of iterations - Maximum number of iterations

## Inf (default)

Specify the maximum number of iterations as a positive integer or Inf.
Simulate using - Block simulation method
Interpreted Execution (default)|Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).
Programmatic Use
Block Parameter:SimulateUsing
Type:enum
Values:Interpreted Execution, Code Generation
Default:Interpreted Execution

## Sensor Array Tab

Specify sensor array as - Method to specify array
Array (no subarrays) (default)|MATLAB expression

Method to specify array, specified as Array (no subarrays) or MATLAB expression.

- Array (no subarrays) - use the block parameters to specify the array.
- MATLAB expression - create the array using a MATLAB expression.


## Element Parameters

Element type - Array element types
Isotropic Antenna (default)|Cardioid Antenna|Cosine Antenna|Custom Antenna| Gaussian Antenna|Sinc Antenna|Omni Microphone|Custom Microphone

Antenna or microphone type, specified as one of the following:

- Isotropic Antenna
- Cardioid Antenna
- Cosine Antenna
- Custom Antenna
- Gaussian Antenna
- Sinc Antenna
- Omni Microphone
- Custom Microphone

Operating frequency range $\mathbf{( H z )}$ - Operating frequency range of the antenna or microphone element
[0,1e20] (default) | real-valued 1-by-2 row vector

Specify the operating frequency range of the antenna or microphone element as a 1-by-2 row vector in the form [LowerBound, UpperBound]. The element has no response outside this frequency range. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Isotropic Antenna, Cosine Antenna, or Omni Microphone.

Baffle the back of the element - Set back response of an Isotropic Antenna element or an Omni Microphone element to zero off (default) | on

Select this check box to baffle the back response of the element. When back baffled, the responses at all azimuth angles beyond $\pm 90^{\circ}$ from broadside are set to zero. The broadside direction is defined as $0^{\circ}$ azimuth angle and $0^{\circ}$ elevation angle.

Dependencies
To enable this check box, set Element type to Isotropic Antenna or Omni Microphone.
Null axis direction - Null axis direction
$-x$ (default) $|+x|+y|-y|+z \mid-z$

## Dependencies

To enable this parameter, set Element type to Cardioid Antenna.
Exponent of cosine pattern - Exponents of azimuth and elevation cosine patterns
$\left[\begin{array}{ll}1.5 & 1.5\end{array}\right]$ (default) | nonnegative scalar | real-valued 1-by-2 matrix of nonnegative values

Specify the exponents of the cosine pattern as a nonnegative scalar or a real-valued 1-by-2 matrix of nonnegative values. When Exponent of cosine pattern is a 1-by-2 vector, the first element is the exponent in the azimuth direction and the second element is the exponent in the elevation direction. When you set this parameter to a scalar, both the azimuth direction and elevation direction cosine patterns are raised to the same power.

## Dependencies

To enable this parameter, set Element type to Cosine Antenna.
Operating frequency vector ( $\mathbf{H z}$ ) - Operating frequency range of custom antenna or microphone elements
[0, 1e20] (default) | real-valued row vector

Specify the frequencies at which to set antenna and microphone frequency responses as a 1-by-L row vector of increasing real values. The antenna or microphone element has no response outside the frequency range specified by the minimum and maximum elements of this vector. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone. Use Frequency responses (dB) to set the responses at these frequencies.

Frequency responses (dB) - Antenna and microphone frequency response
[0,0] (default) | real-valued row vector

Frequency response of a custom antenna or custom microphone for the frequencies defined by the Operating frequency vector ( Hz ) parameter. The dimensions of Frequency responses (dB) must match the dimensions of the vector specified by the Operating frequency vector ( $\mathbf{H z}$ ) parameter.

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone.
Input Pattern Coordinate System - Coordinate system of custom antenna pattern
az-el (default)| phi-theta

Coordinate system of custom antenna pattern, specified az-el or phi-theta. When you specify azel, use the Azimuth angles (deg) and Elevations angles (deg) parameters to specify the coordinates of the pattern points. When you specify phi-theta, use the Phi angles (deg) and Theta angles (deg) parameters to specify the coordinates of the pattern points.

## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Azimuth angles (deg) - Azimuth angles of antenna radiation pattern
[-180:180] (default) | real-valued row vector

Specify the azimuth angles at which to calculate the antenna radiation pattern as a 1-by-P row vector. $P$ must be greater than 2. Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to az-el.

Elevation angles (deg) - Elevation angles of antenna radiation pattern
[-90:90] (default) | real-valued row vector

Specify the elevation angles at which to compute the radiation pattern as a 1-by- $Q$ vector. $Q$ must be greater than 2. Angle units are in degrees. Elevation angles must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to az-el.

Phi Angles (deg) - Phi angle coordinates of custom antenna radiation pattern $0: 360$ | real-valued 1-by-P row vector

Phi angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by-P row vector. $P$ must be greater than 2 . Angle units are in degrees. Phi angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Theta Angles (deg) - Theta angle coordinates of custom antenna radiation pattern 0:180 | real-valued 1-by- $Q$ row vector

Theta angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by$Q$ row vector. $Q$ must be greater than 2. Angle units are in degrees. Theta angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Magnitude pattern (dB) - Magnitude of combined antenna radiation pattern zeros (181,361) (default) | real-valued $Q$-by-P matrix | real-valued $Q$-by- $P$-by-L array

Magnitude of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector ( $\mathbf{H z}$ ).

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector ( Hz ) parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector ( $\mathbf{H z}$ ) parameter.


## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Phase pattern (deg) - Custom antenna radiation phase pattern zeros $(181,361)$ (default) | real-valued $Q$-by- $P$ matrix | real-valued $Q$-by- $P$-by-L array

Phase of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector $(\mathbf{H z})$.

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (


## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Align element normal with array normal - Align element normal with array normal on (default) | off

## Dependencies

This parameter is enabled when Element type is set to Custom Antenna.
Radiation pattern beamwidth (deg) - Radiation pattern beamwidth
[10,10] (default)

## Dependencies

This parameter is enabled when Element type is set to Gaussian Antenna.
Polar pattern frequencies (Hz) - Polar pattern microphone response frequencies
1e3 (default) | real scalar | real-valued 1-by-L row vector

Polar pattern microphone response frequencies, specified as a real scalar, or a real-valued, 1-by-L vector. The response frequencies lie within the frequency range specified by the Operating frequency vector $(\mathrm{Hz})$ vector.

## Dependencies

To enable this parameter, set Element type set to Custom Microphone.
Polar pattern angles (deg) - Polar pattern response angles
[-180:180] (default) | real-valued -by-P row vector

Specify the polar pattern response angles, as a 1-by- $P$ vector. The angles are measured from the central pickup axis of the microphone and must be between $-180^{\circ}$ and $180^{\circ}$, inclusive.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.

Polar pattern (dB) - Custom microphone polar response
zeros (1,361) (default) | real-valued L-by-P matrix

Specify the magnitude of the custom microphone element polar patterns as an $L$-by- $P$ matrix. $L$ is the number of frequencies specified in Polar pattern frequencies ( $\mathbf{H z}$ ). $P$ is the number of angles specified in Polar pattern angles (deg). Each row of the matrix represents the magnitude of the polar pattern measured at the corresponding frequency specified in Polar pattern frequencies (Hz) and all angles specified in Polar pattern angles (deg). The pattern is measured in the azimuth plane. In the azimuth plane, the elevation angle is $0^{\circ}$ and the central pickup axis is $0^{\circ}$ degrees azimuth and $0^{\circ}$ degrees elevation. The polar pattern is symmetric around the central axis. You can construct the microphone response pattern in 3-D space from the polar pattern.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.

## ULA Parameters

Number of elements - Number of array elements in U
2 (default) | positive integer greater than or equal to two

The number of array elements for ULA arrays, specified as an integer greater than or equal to two.
Example: 11
Data Types: double
Element spacing - Distance between ULA elements
0.5 (default) | positive scalar

Distance between adjacent ULA elements, specified as a positive scalar. Units are in meters.
Example: 1.5
Array axis - Linear axis direction of ULA
$y$ (default) $|x| z$

Linear axis direction of ULA, specified as $y, x$, or $z$. All ULA array elements are uniformly spaced along this axis in the local array coordinate system.

## Dependencies

- To enable this parameter, set Geometry to ULA.
- This parameter is also enabled when the block only supports ULA arrays.

Taper - ULA array taper
1 (default) | complex-valued vector

Tapers, also known as element weights, are applied to sensor elements in the array. Tapers are used to modify both the amplitude and phase of the transmitted or received data.

Specify element tapering as a complex-valued scalar or a complex-valued 1-by- $N$ row vector. In this vector, $N$ represents the number of elements in the array. If Taper is a scalar, the same weight is
applied to each element. If Taper is a vector, a weight from the vector is applied to the corresponding sensor element. A weight must be applied to each element in the sensor array.

Example: [0.5;1;0.5]
Data Types: double
Expression - MATLAB expression used to create an array
Phased Array System Toolbox array System object

MATLAB expression used to create a ULA array, specified as a valid Phased Array System Toolbox array System object.
Example: phased.ULA('NumElements',13)

## Dependencies

To enable this parameter, set Specify sensor array as to MATLAB expression.

## Version History <br> Introduced in R2014b

## See Also

phased.RootWSFEstimator

## SMI Beamformer

Sample matrix inversion (SMI) beamformer

## Libraries:

Phased Array System Toolbox / Space-Time Adaptive Processing

## Description

The SMI Beamformer block implements a sample matrix inversion (SMI) space-time adaptive beamformer employing the sample space-time covariance matrix.

## Ports

Input
$\mathbf{X}$ - Input signal
$M$-by- $N$-by- $P$ complex-valued matrix
Input signal, specified as an $M$-by- $N$-by- $P$ complex-valued array. $M$ is the number of range samples, $N$ is the number of channels, and $P$ is the number of pulses.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

## Data Types: double

Idx - Index of range cells
positive integer
Index of range cells to compute processing weights.
Example: 1
Data Types: double
PRF - Pulse repetition frequency
positive scalar
Pulse repetition frequency of current pulse, specified as a positive scalar.

## Dependencies

To enable this port, set the Specify PRF as parameter to Input port.
Data Types: double
Ang - Targeting direction
2-by-1 real-valued vector
Targeting direction, specified as a 2-by-1 real-valued vector. The vector takes the form of [AzimuthAngle;ElevationAngle]. Angle units are in degrees. The azimuth angle must lie
between $-180^{\circ}$ and $180^{\circ}$, inclusive, and the elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive. Angles are defined with respect to the local coordinate system of the array.

## Dependencies

To enable this port, set the Specify direction as parameter to Input port.
Data Types: double
Dop - Targeting Doppler frequency
scalar
Targeting Doppler frequency of current pulse, specified as a scalar.

## Dependencies

To enable this port, set the Specify targeting Doppler as parameter to Input port.
Data Types: double

## Output

Y - Beamformed output
M-by-1 complex-valued vector
Processing output, returned as an $M$-by- 1 complex-valued vector. The quantity $M$ is the number of range samples in the input port $X$.

Data Types: double
W - Processing weights
length $N^{*} P$ complex-valued vector
Processing weights, returned as Length $N^{*} P$ complex-valued vector. The quantity $N$ is the number of channels and $P$ is the number of pulses. When the Specify sensor array as parameter is set to Partitioned array or Replicated subarray, $N$ represents the number of subarrays. $L$ is the number of desired beamforming directions specified in the Ang input port or by the Beamforming direction (deg) parameter. There is one set of weights for each beamforming direction.

## Dependencies

To enable this port, select the Enable weights output check box.

## Data Types: double

## Parameters

## Main Tab

Signal propagation speed ( $\mathbf{m} / \mathbf{s}$ ) - Signal propagation speed
physconst('LightSpeed') (default)| real-valued positive scalar

Signal propagation speed, specified as a real-valued positive scalar. The default value of the speed of light is the value returned by physconst ('LightSpeed'). Units are in meters per second.
Example: 3e8
Data Types: double

Operating frequency (Hz) - System operating frequency
3 e8 (default) | positive real scalar

System operating frequency, specified as a positive scalar. Units are in Hz .
Specify PRF as - Source of PRF value
Property (default)|Input port

Source of PRF value, specified as Property or Input port. When set to Property, the Pulse repetition frequency ( Hz ) parameter sets the PRF. When set to Input port, pass in the PRF using the PRF input port.

Pulse repetition frequency (Hz) - Pulse repetition frequency
1 (default) | positive scalar

Pulse repetition frequency, PRF, specified as a positive scalar. Units are in Hertz. Set this parameter to the same value set in any Waveform library block used in the simulation.

## Dependencies

To enable this parameter, set the Specify PRF as parameter to Property.
Specify direction as - Specify source of targeting directions
Property (default)| Input port

Specify whether the targeting direction for the STAP processor block comes from a block parameter or from the ANG input port. Values of this parameter are

| Property | - For the ADPCA Canceller and DPCA Canceller blocks, targeting <br> direction is specified using Receiving mainlobe direction <br> (deg). <br> For the SMI Beamformer block, targeting direction is specified <br> using Targeting direction. <br> These parameters appear only when the Specify direction as <br> parameter is set to Property. |
| :--- | :--- |
| Input port | Enter the targeting directions using the Ang input port. This port <br> appears only when Specify direction as is set to Input port. |

Targeting direction (deg) - Processor targeting direction
[0;0] (default) | real-valued length-2 column vector

Processor targeting direction, specified as a real-valued length-2 column vector of azimuth and elevation angles, [AzimuthAngle;ElevationAngle]. The azimuth angle is between $-180^{\circ}$ and $180^{\circ}$ and the elevation angle is between $-90^{\circ}$ and $90^{\circ}$. Units are in degrees.

## Dependencies

To enable this parameter, set Specify direction as to Property.

Number of bits in phase shifters - Number of phase shift quantization bits
0 (default) | nonnegative integer

The number of bits used to quantize the phase shift component of beamformer or steering vector weights. Specify the number of bits as a non-negative integer. A value of zero indicates that no quantization is performed.

Specify targeting Doppler as - Source of targeting Doppler
Property (default)|Input port

Specify whether targeting Doppler values for the STAP processor comes from the Targeting Doppler (Hz) parameter of this block or using the DOP input port. For the ADPCA Canceller and DPCA Canceller blocks, the Specify targeting Doppler as parameter appears only when the Output preDoppler result check box is cleared. Values of this parameter are

| Property | Specify targeting Doppler values using the Targeting Doppler <br> parameter of the block. The Targeting Doppler parameter appears <br> only when Specify targeting Doppler as is set to Property. |
| :--- | :--- |
| Input port | Specify targeting Doppler values using the Dop input port. This port <br> appears only when Specify targeting Doppler as is set to Input <br> port. |

Targeting Doppler (Hz) - Targeting Doppler of STAP processor
0 (default) | scalar

Targeting Doppler of STAP processor, specified as a scalar.
Dependencies

- To enable this parameter for the SMI Beamformer block, set Specify targeting Doppler as to Property.
- To enable this parameter for the ADPCA Canceller and DPCA Canceller blocks, first clear the Output pre-Doppler result check box. Then set the Specify targeting Doppler as parameter to Property.

Number of guard cells - Number of guard cells using for training
2 (default) | positive even integer

Number of guard cells used for training, specified as a positive, even integer. Whenever possible, the set of guard cells is equally divided into regions before and after the test cell.

Number of training cells - Number of cells used for training
2 (default) | positive even integer

Number of cells used for training, specified as a positive even integer. Whenever possible, the set of training cells is equally divided into regions before and after the test cell.

Enable weights output - Option to output beamformer weights
off (default) | on

Select this check box to obtain the beamformer weights from the output port, W.
Simulate using - Block simulation method
Interpreted Execution (default)|Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).
Programmatic Use
Block Parameter:SimulateUsing
Type:enum
Values:Interpreted Execution, Code Generation
Default:Interpreted Execution

## Sensor Arrays Tab

Specify sensor array as - Method to specify array
Array (no subarrays) (default)|Partitioned array|Replicated subarray|MATLAB expression

Method to specify array, specified as Array (no subarrays) or MATLAB expression.

- Array (no subarrays) - use the block parameters to specify the array.
- Partitioned array - use the block parameters to specify the array.
- Replicated subarray - use the block parameters to specify the array.
- MATLAB expression - create the array using a MATLAB expression.

Expression - MATLAB expression used to create an array
Phased Array System Toolbox array System object

MATLAB expression used to create an array, specified as a valid Phased Array System Toolbox array System object.

Example: phased.URA('Size', [5,3])

## Dependencies

To enable this parameter, set Specify sensor array as to MATLAB expression.

## Element Parameters

Element type - Array element types
Isotropic Antenna (default)|Cosine Antenna|Custom Antenna|Omni Microphone| Custom Microphone

Antenna or microphone type, specified as one of the following:

- Isotropic Antenna
- Cosine Antenna
- Custom Antenna
- Omni Microphone
- Custom Microphone

Operating frequency range $(\mathbf{H z})$ - Operating frequency range of the antenna or microphone element
[0,1e20] (default) | real-valued 1-by-2 row vector

Specify the operating frequency range of the antenna or microphone element as a 1-by-2 row vector in the form [LowerBound, UpperBound]. The element has no response outside this frequency range. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Isotropic Antenna, Cosine Antenna, or Omni Microphone.

Operating frequency vector ( $\mathbf{H z}$ ) - Operating frequency range of custom antenna or microphone elements
[0,1e20] (default) | real-valued row vector

Specify the frequencies at which to set antenna and microphone frequency responses as a 1-by-L row vector of increasing real values. The antenna or microphone element has no response outside the
frequency range specified by the minimum and maximum elements of this vector. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone. Use Frequency responses (dB) to set the responses at these frequencies.

Baffle the back of the element - Set back response of an Isotropic Antenna element or an Omni Microphone element to zero
off (default) | on

Select this check box to baffle the back response of the element. When back baffled, the responses at all azimuth angles beyond $\pm 90^{\circ}$ from broadside are set to zero. The broadside direction is defined as $0^{\circ}$ azimuth angle and $0^{\circ}$ elevation angle.

## Dependencies

To enable this check box, set Element type to Isotropic Antenna or Omni Microphone.
Exponent of cosine pattern - Exponents of azimuth and elevation cosine patterns [1.5 1.5] (default) | nonnegative scalar | real-valued 1-by-2 matrix of nonnegative values

Specify the exponents of the cosine pattern as a nonnegative scalar or a real-valued 1-by-2 matrix of nonnegative values. When Exponent of cosine pattern is a 1-by-2 vector, the first element is the exponent in the azimuth direction and the second element is the exponent in the elevation direction. When you set this parameter to a scalar, both the azimuth direction and elevation direction cosine patterns are raised to the same power.

## Dependencies

To enable this parameter, set Element type to Cosine Antenna.
Frequency responses (dB) - Antenna and microphone frequency response
[0, 0] (default) | real-valued row vector

Frequency response of a custom antenna or custom microphone for the frequencies defined by the Operating frequency vector $(\mathbf{H z})$ parameter. The dimensions of Frequency responses (dB) must match the dimensions of the vector specified by the Operating frequency vector $(\mathbf{H z})$ parameter.

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone.
Input Pattern Coordinate System - Coordinate system of custom antenna pattern
az-el (default)| phi-theta

Coordinate system of custom antenna pattern, specified az-el or phi-theta. When you specify azel, use the Azimuth angles (deg) and Elevations angles (deg) parameters to specify the coordinates of the pattern points. When you specify phi-theta, use the Phi angles (deg) and Theta angles (deg) parameters to specify the coordinates of the pattern points.

## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Azimuth angles (deg) - Azimuth angles of antenna radiation pattern
[-180:180] (default) | real-valued row vector

Specify the azimuth angles at which to calculate the antenna radiation pattern as a 1 -by- $P$ row vector. $P$ must be greater than 2. Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to az-el.

Elevation angles (deg) - Elevation angles of antenna radiation pattern
[-90:90] (default) | real-valued row vector

Specify the elevation angles at which to compute the radiation pattern as a 1-by-Q vector. $Q$ must be greater than 2. Angle units are in degrees. Elevation angles must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to az-el.

Phi Angles (deg) - Phi angle coordinates of custom antenna radiation pattern
$0: 360$ | real-valued 1 -by- $P$ row vector

Phi angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by-P row vector. $P$ must be greater than 2 . Angle units are in degrees. Phi angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Theta Angles (deg) - Theta angle coordinates of custom antenna radiation pattern
$0: 180$ | real-valued 1-by- $Q$ row vector

Theta angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by$Q$ row vector. $Q$ must be greater than 2. Angle units are in degrees. Theta angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Magnitude pattern (dB) - Magnitude of combined antenna radiation pattern
zeros $(181,361)$ (default) | real-valued $Q$-by- $P$ matrix | real-valued $Q$-by- $P$-by- $L$ array

Magnitude of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector ( $\mathbf{H z}$ ).

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (Hz) parameter.


## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Phase pattern (deg) - Custom antenna radiation phase pattern
zeros (181, 361) (default) | real-valued $Q$-by-P matrix | real-valued $Q$-by- $P$-by- $L$ array

Phase of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi - theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector ( $\mathbf{H z}$ ).

- If this parameter is a $Q$-by-P matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (


## Dependencies

To enable this parameter, set Element type to Custom Antenna.
MatchArrayNormal - Rotate antenna element to array normal
on (default) | off

Select this check box to rotate the antenna element pattern to align with the array normal. When not selected, the element pattern is not rotated.

When the antenna is used in an antenna array and the Input Pattern Coordinate System parameter is az-el, selecting this check box rotates the pattern so that the $x$-axis of the element coordinate system points along the array normal. Not selecting uses the element pattern without the rotation.

When the antenna is used in an antenna array and Input Pattern Coordinate System is set to phitheta, selecting this check box rotates the pattern so that the $z$-axis of the element coordinate system points along the array normal.

Use the parameter in conjunction with the Array normal parameter of the URA and UCA arrays.

## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Polar pattern frequencies (Hz) - Polar pattern microphone response frequencies
1e3 (default) | real scalar | real-valued 1-by-L row vector

Polar pattern microphone response frequencies, specified as a real scalar, or a real-valued, 1-by-L vector. The response frequencies lie within the frequency range specified by the Operating frequency vector $(\mathrm{Hz})$ vector.

## Dependencies

To enable this parameter, set Element type set to Custom Microphone.
Polar pattern angles (deg) - Polar pattern response angles
[-180:180] (default) | real-valued -by-P row vector

Specify the polar pattern response angles, as a 1-by- $P$ vector. The angles are measured from the central pickup axis of the microphone and must be between $-180^{\circ}$ and $180^{\circ}$, inclusive.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.
Polar pattern (dB) - Custom microphone polar response
zeros $(1,361)$ (default) | real-valued $L$-by-P matrix

Specify the magnitude of the custom microphone element polar patterns as an $L$-by- $P$ matrix. $L$ is the number of frequencies specified in Polar pattern frequencies (Hz). $P$ is the number of angles specified in Polar pattern angles (deg). Each row of the matrix represents the magnitude of the polar pattern measured at the corresponding frequency specified in Polar pattern frequencies (Hz) and all angles specified in Polar pattern angles (deg). The pattern is measured in the azimuth plane. In the azimuth plane, the elevation angle is $0^{\circ}$ and the central pickup axis is $0^{\circ}$ degrees azimuth and $0^{\circ}$ degrees elevation. The polar pattern is symmetric around the central axis. You can construct the microphone response pattern in 3-D space from the polar pattern.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.

## Array Parameters

Geometry - Array geometry
ULA (default) | URA | UCA | Conformal Array

Array geometry, specified as one of

- ULA - Uniform linear array
- URA - Uniform rectangular array
- UCA - Uniform circular array
- Conformal Array - arbitrary element positions

Number of elements - Number of array elements
2 for ULA arrays and 5 for UCA arrays (default) | integer greater than or equal to 2

The number of array elements for ULA or UCA arrays, specified as an integer greater than or equal to 2.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

## Dependencies

To enable this parameter, set Geometry to ULA or UCA.
Element spacing (m) - Spacing between array elements
0.5 for ULA arrays and [0.5, 0.5] for URA arrays (default) | positive scalar for ULA or URA arrays |

2 -element vector of positive values for URA arrays

Spacing between adjacent array elements:

- ULA - specify the spacing between two adjacent elements in the array as a positive scalar.
- URA - specify the spacing as a positive scalar or a 1 -by-2 vector of positive values. If Element spacing (m) is a scalar, the row and column spacings are equal. If Element spacing (m) is a vector, the vector has the form [SpacingBetweenArrayRows, SpacingBetweenArrayColumns].
- When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.


## Dependencies

To enable this parameter, set Geometry to ULA or URA.

## Array axis - Linear axis direction of ULA

$y$ (default) $|x| z$

Linear axis direction of ULA, specified as $y, x$, or $z$. All ULA array elements are uniformly spaced along this axis in the local array coordinate system.

## Dependencies

- To enable this parameter, set Geometry to ULA.
- This parameter is also enabled when the block only supports ULA arrays.

Array size - Dimensions of URA array
[2,2] (default) | positive integer | 1-by-2 vector of positive integers

Dimensions of a URA array, specified as a positive integer or 1-by-2 vector of positive integers.

- If Array size is a 1 -by- 2 vector, the vector has the form [NumberOfArrayRows, NumberOfArrayColumns].
- If Array size is an integer, the array has the same number of rows and columns.
- When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

For a URA, array elements are indexed from top to bottom along the leftmost column, and then continue to the next columns from left to right. In this figure, the Array size value of [3, 2] creates an array having three rows and two columns.

## Size and Element Indexing Order

for Uniform Rectangular Arrays
Example: Size $=[3,2]$


## Dependencies

To enable this parameter, set Geometry to URA.
Element lattice - Lattice of URA element positions
Rectangular (default) | Triangular

Lattice of URA element positions, specified as Rectangular or Triangular.

- Rectangular - Aligns all the elements in row and column directions.
- Triangular - Shifts the even-row elements of a rectangular lattice toward the positive row-axis direction. The displacement is one-half the element spacing along the row dimension.


## Dependencies

To enable this parameter, set Geometry to URA.
Array normal - Array normal direction
$x$ for URA arrays or $z$ for UCA arrays (default) | y

Array normal direction, specified as $x, y$, or $z$.
Elements of planar arrays lie in a plane orthogonal to the selected array normal direction. Element boresight directions point along the array normal direction.

| Array Normal Parameter Value | Element Positions and Boresight Directions |
| :--- | :--- |
| $x$ | Array elements lie in the $y z$-plane. All element <br> boresight vectors point along the $x$-axis. |
| $y$ | Array elements lie in the $z x$-plane. All element <br> boresight vectors point along the $y$-axis. |
| $z$ | Array elements lie in the $x y$-plane. All element <br> boresight vectors point along the $z$-axis. |

## Dependencies

To enable this parameter, set Geometry to URA or UCA.
Radius of UCA (m) - UCA array radius
0.5 (default) | positive scalar

Radius of UCA array, specified as a positive scalar.

## Dependencies

To enable this parameter, set Geometry to UCA.
Element positions (m) - Positions of conformal array elements
[0;0;0] (default) | 3-by-Nmatrix of real values

Positions of the elements in a conformal array, specified as a 3 -by- $N$ matrix of real values, where $N$ is the number of elements in the conformal array. Each column of this matrix represents the position [ $x ; y ; z$ ] of an array element in the array local coordinate system. The origin of the local coordinate system is $(0,0,0)$. Units are in meters.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

## Dependencies

To enable this parameter set Geometry to Conformal Array.
Element normals (deg) - Direction of conformal array element normal vectors [0;0] | 2-by-1 column vector | 2 -by- $N$ matrix

Direction of element normal vectors in a conformal array, specified as a 2-by-1 column vector or a 2-by- $N$ matrix. $N$ indicates the number of elements in the array. For a matrix, each column specifies the normal direction of the corresponding element in the form [azimuth; elevation] with respect to the local coordinate system. The local coordinate system aligns the positive $x$-axis with the direction normal to the conformal array. If the parameter value is a 2 -by- 1 column vector, the same pointing direction is used for all array elements.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

You can use the Element positions (m) and Element normals (deg) parameters to represent any arrangement in which pairs of elements differ by certain transformations. The transformations can combine translation, azimuth rotation, and elevation rotation. However, you cannot use transformations that require rotation about the normal direction.

## Dependencies

To enable this parameter, set Geometry to Conformal Array.
Taper - Array element tapers
1 (default) | complex-valued scalar | complex-valued row vector

Element tapering, specified as a complex-valued scalar or a complex-valued 1-by- $N$ row vector. In this vector, $N$ represents the number of elements in the array.

Also known as element weights, tapers multiply the array element responses. Tapers modify both amplitude and phase of the response to reduce side lobes or steer the main response axis.

If Taper is a scalar, the same weight is applied to each element. If Taper is a vector, a weight from the vector is applied to the corresponding sensor element. The number of weights must match the number of elements of the array.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

Subarray definition matrix - Define elements belonging to subarrays
logical matrix

Specify the subarray selection as an $M$-by- $N$ matrix. $M$ is the number of subarrays and $N$ is the total number of elements in the array. Each row of the matrix represents a subarray and each entry in the row indicates when an element belongs to the subarray. When the entry is zero, the element does not belong the subarray. A nonzero entry represents a complex-valued weight applied to the corresponding element. Each row must contain at least one nonzero entry.

The phase center of each subarray lies at the subarray geometric center. The subarray geometric center depends on the Subarray definition matrix and Geometry parameters.

## Dependencies

To enable this parameter, set Specify sensor array as to Partitioned array.
Subarray steering method - Specify subarray steering method None (default) | Phase | Time

Subarray steering method, specified as one of

- None
- Phase
- Time
- Custom

Selecting Phase or Time opens the Steer input port on the Narrowband Receive Array, Narrowband Transmit Array, Wideband Receive Array, Wideband Transmit Array blocks, Constant Gamma Clutter, and GPU Constant Gamma Clutter blocks.

Selecting Custom opens the WS input port on the Narrowband Receive Array, Narrowband Transmit Array, Wideband Receive Array, Wideband Transmit Array blocks, Constant Gamma Clutter, and GPU Constant Gamma Clutter blocks.

## Dependencies

To enable this parameter, set Specify sensor array as to Partitioned array or Replicated subarray.

Phase shifter frequency (Hz) - Subarray phase shifting frequency
3.0e8 (default) | positive real-valued scalar

Operating frequency of subarray steering phase shifters, specified as a positive real-valued scalar. Units are Hz.

## Dependencies

To enable this parameter, set Sensor array to Partitioned array or Replicated subarray and set Subarray steering method to Phase.

Number of bits in phase shifters - Subarray steering phase shift quantization bits
0 (default) | non-negative integer

Subarray steering phase shift quantization bits, specified as a non-negative integer. A value of zero indicates that no quantization is performed.

## Dependencies

To enable this parameter, set Sensor array to Partitioned array or Replicated subarray and set Subarray steering method to Phase.

Subarrays layout - Subarray position specification
Rectangular (default) | Custom

Specify the layout of replicated subarrays as Rectangular or Custom.

- When you set this parameter to Rectangular, use the Grid size and Grid spacing parameters to place the subarrays.
- When you set this parameter to Custom, use the Subarray positions (m) and Subarray normals parameters to place the subarrays.


## Dependencies

To enable this parameter, set Sensor array to Replicated subarray
Grid size - Dimensions of rectangular subarray grid
[1,2] (default)

Rectangular subarray grid size, specified as a single positive integer, or a 1-by-2 row vector of positive integers.

If Grid size is an integer scalar, the array has an equal number of subarrays in each row and column. If Grid size is a 1-by-2 vector of the form [NumberOfRows, NumberOfColumns], the first entry is the number of subarrays along each column. The second entry is the number of subarrays in each row. A row is along the local $y$-axis, and a column is along the local $z$-axis. The figure here shows how you can replicate a 3-by-2 URA subarray using a Grid size of [1,2].
$3 \times 2$ Element URA
Replicated on a $1 \times 2$ Grid


## Dependencies

To enable this parameter, set Sensor array to Replicated subarray and Subarrays layout to Rectangular.

Grid spacing ( $\mathbf{m}$ ) - Spacing between subarrays on rectangular grid Auto (default) | positive real-valued scalar | 1-by-2 vector of positive real-values

The rectangular grid spacing of subarrays, specified as a positive, real-valued scalar, a 1-by-2 row vector of positive, real-values, or Auto. Units are in meters.

- If Grid spacing is a scalar, the spacing along the row and the spacing along the column is the same.
- If Grid spacing is a 1-by-2 row vector, the vector has the form [SpacingBetweenRows, SpacingBetweenColumn]. The first entry specifies the spacing between rows along a column. The second entry specifies the spacing between columns along a row.
- If Grid spacing is set to Auto, replication preserves the element spacing of the subarray for both rows and columns while building the full array. This option is available only when you specify Geometry as ULA or URA.


## Dependencies

To enable this parameter, set Sensor array to Replicated subarray and Subarrays layout to Rectangular.

Subarray positions (m) - Positions of subarrays
[0,0;0.5, 0.5;0,0] (default)| 3-by- $N$ real-valued matrix

Positions of the subarrays in the custom grid, specified as a real 3-by- $N$ matrix, where $N$ is the number of subarrays in the array. Each column of the matrix represents the position of a single subarray in the array local coordinate system. The coordinates are expressed in the form $[x ; y ; z]$. Units are in meters.

## Dependencies

To enable this parameter, set Sensor array to Replicated subarray and Subarrays layout to Custom.

Subarray normals - Direction of subarray normal vectors
[0,0;0,0] (default) | 2 -by- $N$ real matrix

Specify the normal directions of the subarrays in the array. This parameter value is a 2 -by- $N$ matrix, where $N$ is the number of subarrays in the array. Each column of the matrix specifies the normal direction of the corresponding subarray, in the form [azimuth; elevation]. Angle units are in degrees. Angles are defined with respect to the local coordinate system.

You can use the Subarray positions and Subarray normals parameters to represent any arrangement in which pairs of subarrays differ by certain transformations. The transformations can combine translation, azimuth rotation, and elevation rotation. However, you cannot use transformations that require rotation about the normal.

## Dependencies

To enable this parameter, set the Sensor array parameter to Replicated subarray and the Subarrays layout to Custom.

## Version History

## Introduced in R2014b

## See Also

phased.STAPSMIBeamformer

## Scattering MIMO Channel

## Scattering MIMO propagation channel



## Libraries:

Phased Array System Toolbox / Environment and Target

## Description

The Scattering MIMO Channel models a 3-D multipath propagation channel in which radiated signals from a transmitting array are reflected from multiple scatters back towards a receiving array. In this channel, propagation paths are direct paths (line-of-sight) from point to point. The block models range-dependent time delay, gain, Doppler shift, phase change, and atmospheric loss due to gases, rain, fog, and clouds. You can optionally propagate a signal via a direct path from transmitter to receiver.

The attenuation models for atmospheric gases and rain are valid for electromagnetic signals in the frequency range $1-1000 \mathrm{GHz}$ but the attenuation model for fog and clouds is valid for only 10-1000 GHz . Outside these frequency ranges, the object uses the nearest valid value.

## Ports

## Input

$\mathbf{X}$ - Transmitted narrowband signal
$M$-by- $N_{t}$ complex-valued matrix
The transmitted narrowband signal, specified as an $M$-by- $N_{t}$ complex-valued matrix. The quantity $M$ is the number of samples in the signal, and $N_{t}$ is the number of transmitting array elements. Each column represents the signal transmitted by the corresponding array element.
Example: [1,1; j,1;0.5,0]
The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

## Dependencies

To enable this port, set the Polarization configuration parameter to None or Combined.

## Data Types: double <br> Complex Number Support: Yes

XH - Transmitted narrowband H-polarization signal
$M$-by- $N_{t}$ complex-valued matrix
Transmitted narrowband $H$-polarization signal, specified as an $M$-by- $N_{t}$ complex-valued matrix. The quantity $M$ is the number of samples in the signal, and $N_{t}$ is the number of transmitting array elements. Each column represents the signal transmitted by the corresponding array element.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
Example: [1,1;j,1;0.5,0]

## Dependencies

To enable this port, set the Polarization configuration parameter to Dual.

## Data Types: double <br> Complex Number Support: Yes

XV - Transmitted narrowband V-polarization signal
$M$-by- $N_{t}$ complex-valued matrix
Transmitted narrowband $V$-polarization signal, specified as an $M$-by- $N_{t}$ complex-valued matrix. The quantity $M$ is the number of samples in the signal, and $N_{t}$ is the number of transmitting array elements. Each column represents the signal transmitted by the corresponding array element.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

## Dependencies

To enable this port, set the Polarization configuration parameter to Dual.

## Data Types: double <br> Complex Number Support: Yes

TxPos - Position of transmitting antenna array
3-by-1 real-valued column vector
Position of transmitting antenna array, specified as a 3-by-1 real-valued column vector taking the form [ $x ; y ; z$ ]. The vector elements correspond to the $x, y$, and $z$ positions of the array. Units are in meters.

## Dependencies

To enable this port, set the Source of transmit array motion parameter to Input port.

## Data Types: double

TxVel - Velocity of transmitting antenna array
3-by-1 real-valued column vector
Velocity of transmitting antenna array, specified as a 3-by-1 real-valued column vector taking the form [vx;vy;vz]. The vector elements correspond to the $x, y$, and $z$ velocities of the array. Units are in meters per second.

## Dependencies

To enable this port, set the Source of transmit array motion parameter to Input port.

## Data Types: double

TxAxes - Axes orientation of transmitting antenna array
3-by-3 real orthonormal matrix

Axes orientation of transmitting antenna array, specified as a 3-by-3 real orthonormal matrix. The matrix defines the orientation of the array local coordinate system with respect to the global coordinates. Matrix columns correspond to the directions of the $x, y$, and $z$ axes of the local coordinate system. Units are dimensionless.

## Dependencies

To enable this port, set the Source of transmit array motion parameter to Input port.
Data Types: double
RxPos - Position of receiving antenna array
3-by-1 real-valued column vector
Position of receiving antenna array, specified as a 3-by-1 real-valued column vector taking the form [ $x ; y ; z]$. The vector elements correspond to the $x, y$, and $z$ positions of the array. Units are in meters.

## Dependencies

To enable this port, set the Source of receive array motion parameter to Input port.

## Data Types: double

RxVel - Velocity of receiving antenna array
3-by-1 real-valued column vector
Velocity of receiving antenna array, specified as a 3-by-1 real-valued column vector taking the form [vx;vy;vz]. The vector elements correspond to the $x, y$, and $z$ velocities of the array. Units are in meters per second.

## Dependencies

To enable this port, set the Source of receive array motion parameter to Input port.

## Data Types: double

RxAxes - Axes orientation of receiving antenna array
3-by-3 real orthonormal matrix
Axes orientation of receiving antenna array, specified as a 3-by-3 real orthonormal matrix. The matrix defines the orientation of the array local coordinate system with respect to the global coordinates. Matrix columns correspond to the directions of the $x, y$, and $z$ axes of the local coordinate system. Units are dimensionless.

## Dependencies

To enable this port, set the Source of receive array motion parameter to Input port.

## Data Types: double

ScatPos - Positions of scatterers
3-by- $N_{s}$ real-valued matrix
Position of scatterers, specified as a 3-by- $N_{s}$ real-valued matrix. Each column of the matrix takes the form $[x ; y ; z]$, containing the $x, y$, and $z$ positions of a scatterer. Units are in meters.

## Dependencies

To enable this port, set the Scatterer specification parameter to Input port.
Data Types: double
ScatVel - Velocities of scatterers
3 -by- $N_{s}$ real-valued matrix
Velocities of scatterers, specified as a 3-by- $N_{s}$ real-valued matrix. Each matrix column has the form [ $\mathrm{vx} ; \mathrm{vy} ; \mathrm{vz}$ ], containing the $x, y$, and $z$ velocities of a scatterer. Units are in meters per second.

## Dependencies

To enable this port, set the Scatterer specification parameter to Input port.
Data Types: double
ScatCoef - Scattering coefficients
1 -by- $N_{s}$ complex-valued row vector
Scattering coefficients, specified as a 1-by- $N_{s}$ complex-valued row vector. Each vector element specifies the scattering coefficient of the corresponding scatterer. Units are dimensionless.
Dependencies
To enable this port, set the Scatterer specification parameter to Input port.
Data Types: double
Output
$\mathbf{Y}$ - Received narrowband signal
$M$-by- $N_{r}$ complex-valued matrix
Received narrowband signal, returned as an $M$-by- $N_{r}$ complex-valued matrix. The quantity $M$ is the number of samples in the signal, and $N_{r}$ is the number of receiving array elements. Each column represents the signal received by the corresponding array element.

## Dependencies

To enable this port, set the Polarization configuration parameter to None or Combined.
Data Types: double
Complex Number Support: Yes
YH - Received narrowband H-polarization signal
complex-valued $M$-by- $N_{r}$ matrix
Received narrowband $H$-polarization signal, returned as a complex-valued $M$-by- $N_{r}$ matrix. $M$ is the number of samples in the signal, and $N_{r}$ is the number of receiving array elements. Each column represents the signal received by the corresponding array element.

## Dependencies

To enable this port, set the Polarization configuration parameter to Dual.
Data Types: double
Complex Number Support: Yes

YV - Received narrowband V-polarization signal
complex-valued $M$-by- $N_{r}$ matrix
Received narrowband $V$-polarization signal, returned as a complex-valued $M$-by- $N_{r}$ matrix. $M$ is the number of samples in the signal, and $N_{r}$ is the number of receiving array elements. Each column represents the signal received by the corresponding array element.

## Dependencies

To enable this port, set the Polarization configuration parameter to Dual.
Data Types: double
Complex Number Support: Yes
CS - Channel response
$N_{t}$-by- $N_{r}$-by- $N_{s}$ complex-valued MATLAB array
Channel response, returned as an $N_{t}$-by- $N_{r}$-by- $N_{s}$ complex-valued MATLAB array. $N_{t}$ is the number of transmitting array elements. $N_{r}$ is the number of receiving array elements. $N_{s}$ is the number of scatterers. Each page of the array corresponds to the channel response matrix for a specific scatterer.

## Dependencies

To enable this port, select the Output channel response check box.
Data Types: double
Complex Number Support: Yes
Tau - Path delays
1 -by- $N_{s}$ real-valued vector
Path delays, returned as a 1-by- $N_{s}$ real-valued vector. $N_{s}$ is the number of scatterers. Each element corresponds to the path time delay from the transmitting array phase center to the scatterer and then to the receiving array phase center.

## Dependencies

To enable this port, select the Output channel response checkbox.

```
Data Types: double
```


## Parameters

## Main Tab

Propagation speed (m/s) - Signal propagation speed
physconst('LightSpeed') (default)| positive scalar

Signal propagation speed, specified as a real-valued positive scalar. The default value of the speed of light is the value returned by physconst('LightSpeed').
Data Types: double
Signal carrier frequency (Hz) - Signal carrier frequency
$3 e 8$ (default) | positive real-valued scalar

Signal carrier frequency, specified as a positive real-valued scalar. Units are in hertz.
Data Types: double
Polarization configuration - Polarization configuration
None (default) | Combined | Dual

Polarization configuration, specified as None, Combined, or Dual. When you set this parameter to None, the output field is considered a scalar field. When you set this parameter to None, the radiated fields are polarized and are interpreted as a single signal in the sensor's inherent polarization. When you set this parameter to Dual, the $H$ and $V$ polarization components of the radiated field are independent signals.
Data Types: char
Specify atmospheric parameters - Enable atmospheric attenuation model
off (default) | on

Select this parameter to enable to add signal attenuation caused by atmospheric gases, rain, fog, or clouds. When you select this parameter, the Temperature (degrees Celsius), Dry air pressure (Pa), Water vapour density ( $\mathrm{g} / \mathrm{m}^{\wedge} 3$ ), Liquid water density ( $\mathrm{g} / \mathrm{m}^{\wedge} 3$ ), and Rain rate ( $\mathrm{mm} / \mathrm{hr}$ ) parameters appear in the dialog box.
Data Types: Boolean
Temperature (degrees Celsius) - Ambient temperature
15 (default) | real-valued scalar

Ambient temperature, specified as a real-valued scalar. Units are in degrees Celsius.

## Dependencies

To enable this parameter, select the Specify atmospheric parameters checkbox.

## Data Types: double

Dry air pressure ( Pa ) - Atmospheric dry air pressure
101.325 e 3 (default) | positive real-valued scalar

Atmospheric dry air pressure, specified as a positive real-valued scalar. Units are in pascals (Pa). The default value of this parameter corresponds to one standard atmosphere.

## Dependencies

To enable this parameter, select the Specify atmospheric parameters checkbox.
Data Types: double
Water vapour density (g/m^3) - Atmospheric water vapor density 7.5 (default) | positive real-valued scalar

Atmospheric water vapor density, specified as a positive real-valued scalar. Units are in $\mathrm{g} / \mathrm{m}^{3}$.

## Dependencies

To enable this parameter, select the Specify atmospheric parameters checkbox.
Data Types: datetime
Liquid water density ( $\mathbf{g} / \mathbf{m}^{\wedge} \mathbf{3}$ ) - Liquid water density
0.0 (default) | nonnegative real-valued scalar

Liquid water density of fog or clouds, specified as a nonnegative real-valued scalar. Units are in $\mathrm{g} / \mathrm{m}^{3}$. Typical values for liquid water density are 0.05 for medium fog and 0.5 for thick fog.

## Dependencies

To enable this parameter, select the Specify atmospheric parameters checkbox.
Data Types: double
Rain rate ( $\mathbf{m m} / \mathbf{h r}$ ) - Rainfall rate
0.0 (default) | non-negative real-valued scalar

Rainfall rate, specified as a nonnegative real-valued scalar. Units are in mm/hr.

## Dependencies

To enable this parameter, select the Specify atmospheric parameters checkbox.
Data Types: double
Inherit sample rate - Inherit sample rate from upstream blocks
on (default) | off

Select this parameter to inherit the sample rate from upstream blocks. Otherwise, specify the sample rate using the Sample rate ( $\mathbf{H z}$ ) parameter.

## Data Types: Boolean

Sample rate (Hz) - Sampling rate of signal
le6 (default) | positive real-valued scalar

Specify the signal sampling rate as a positive scalar. Units are in Hz .

## Dependencies

To enable this parameter, clear the Inherit sample rate check box.
Data Types: double
Simulate direct path propagation - Enable propagation along direct path
off (default) | on

Select this check box to enable signal propagation along the line-of-sight direct path from the transmitting array to the receiving array with no scattering.

## Data Types: Boolean

Maximum delay (s) - Maximum signal delay
10e-6 (default) | positive scalar

The maximum signal delay, specified as a positive scalar. Delays greater than this value are ignored.
Data Types: double
Output channel response - Enable output of channel response
off (default) | on

Select this checkbox to output the channel response and time delay via the output ports CS and Tau.

## Data Types: Boolean

Simulate using - Block simulation method
Interpreted Execution (default)|Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).

```
Programmatic Use
Block Parameter:SimulateUsing
Type:enum
```

Values:Interpreted Execution, Code Generation
Default:Interpreted Execution
Transmit and Receive Array Tabs
Specify sensor array as - Method to specify array
Array (no subarrays) (default)|MATLAB expression

Method to specify array, specified as Array (no subarrays) or MATLAB expression.

- Array (no subarrays) - use the block parameters to specify the array.
- MATLAB expression - create the array using a MATLAB expression.

Expression - MATLAB expression used to create an array
Phased Array System Toolbox array System object

MATLAB expression used to create an array, specified as a valid Phased Array System Toolbox array System object.
Example: phased.URA('Size', [5, 3])

## Dependencies

To enable this parameter, set Specify sensor array as to MATLAB expression.

## Element Parameters

Element type - Array element types
Isotropic Antenna (default)|Cosine Antenna|Custom Antenna|Omni Microphone| Custom Microphone

Antenna or microphone type, specified as one of the following:

- Isotropic Antenna
- Cosine Antenna
- Custom Antenna
- Omni Microphone
- Custom Microphone

Operating frequency range $\mathbf{( H z )}$ - Operating frequency range of the antenna or microphone element
[0,1e20] (default) | real-valued 1-by-2 row vector

Specify the operating frequency range of the antenna or microphone element as a 1-by-2 row vector in the form [LowerBound, UpperBound]. The element has no response outside this frequency range. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Isotropic Antenna, Cosine Antenna, or Omni Microphone.

Operating frequency vector (Hz) - Operating frequency range of custom antenna or microphone elements
[0,1e20] (default) | real-valued row vector

Specify the frequencies at which to set antenna and microphone frequency responses as a 1-by-L row vector of increasing real values. The antenna or microphone element has no response outside the frequency range specified by the minimum and maximum elements of this vector. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone. Use Frequency responses (dB) to set the responses at these frequencies.

Baffle the back of the element - Set back response of an Isotropic Antenna element or an Omni Microphone element to zero
off (default) | on

Select this check box to baffle the back response of the element. When back baffled, the responses at all azimuth angles beyond $\pm 90^{\circ}$ from broadside are set to zero. The broadside direction is defined as $0^{\circ}$ azimuth angle and $0^{\circ}$ elevation angle.

## Dependencies

To enable this check box, set Element type to Isotropic Antenna or Omni Microphone.
Exponent of cosine pattern - Exponents of azimuth and elevation cosine patterns
[1.5 1.5] (default) | nonnegative scalar | real-valued 1-by-2 matrix of nonnegative values

Specify the exponents of the cosine pattern as a nonnegative scalar or a real-valued 1-by-2 matrix of nonnegative values. When Exponent of cosine pattern is a 1-by-2 vector, the first element is the exponent in the azimuth direction and the second element is the exponent in the elevation direction. When you set this parameter to a scalar, both the azimuth direction and elevation direction cosine patterns are raised to the same power.

## Dependencies

To enable this parameter, set Element type to Cosine Antenna.
Frequency responses (dB) - Antenna and microphone frequency response
[0,0] (default) | real-valued row vector

Frequency response of a custom antenna or custom microphone for the frequencies defined by the Operating frequency vector ( $\mathbf{H z}$ ) parameter. The dimensions of Frequency responses (dB) must match the dimensions of the vector specified by the Operating frequency vector $(\mathbf{H z})$ parameter.

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone.
Input Pattern Coordinate System - Coordinate system of custom antenna pattern az-el (default) | phi-theta

Coordinate system of custom antenna pattern, specified az-el or phi-theta. When you specify azel, use the Azimuth angles (deg) and Elevations angles (deg) parameters to specify the coordinates of the pattern points. When you specify phi-theta, use the Phi angles (deg) and Theta angles (deg) parameters to specify the coordinates of the pattern points.

To enable this parameter, set Element type to Custom Antenna.
Azimuth angles (deg) - Azimuth angles of antenna radiation pattern
[-180:180] (default) | real-valued row vector

Specify the azimuth angles at which to calculate the antenna radiation pattern as a 1-by-P row vector. $P$ must be greater than 2. Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to az-el.

Elevation angles (deg) - Elevation angles of antenna radiation pattern
[-90:90] (default) | real-valued row vector

Specify the elevation angles at which to compute the radiation pattern as a 1-by- $Q$ vector. $Q$ must be greater than 2. Angle units are in degrees. Elevation angles must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input
Pattern Coordinate System parameter to az-el.
Phi Angles (deg) - Phi angle coordinates of custom antenna radiation pattern
$0: 360$ | real-valued 1-by-P row vector

Phi angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by- $P$ row vector. $P$ must be greater than 2 . Angle units are in degrees. Phi angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input
Pattern Coordinate System parameter to phi-theta.
Theta Angles (deg) - Theta angle coordinates of custom antenna radiation pattern
$0: 180$ | real-valued 1-by- $Q$ row vector

Theta angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by$Q$ row vector. $Q$ must be greater than 2. Angle units are in degrees. Theta angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Magnitude pattern (dB) - Magnitude of combined antenna radiation pattern zeros $(181,361)$ (default) | real-valued $Q$-by- $P$ matrix | real-valued $Q$-by- $P$-by- $L$ array

Magnitude of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector ( $\mathbf{H z}$ ).

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (Hz) parameter.


## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Phase pattern (deg) - Custom antenna radiation phase pattern zeros $(181,361)$ (default) | real-valued $Q$-by-P matrix | real-valued $Q$-by- $P$-by-L array

Phase of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector ( $\mathbf{H z}$ ).

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (


## Dependencies

To enable this parameter, set Element type to Custom Antenna.

MatchArrayNormal - Rotate antenna element to array normal
on (default) | off

Select this check box to rotate the antenna element pattern to align with the array normal. When not selected, the element pattern is not rotated.

When the antenna is used in an antenna array and the Input Pattern Coordinate System parameter is az-el, selecting this check box rotates the pattern so that the $x$-axis of the element coordinate system points along the array normal. Not selecting uses the element pattern without the rotation.

When the antenna is used in an antenna array and Input Pattern Coordinate System is set to phitheta, selecting this check box rotates the pattern so that the $z$-axis of the element coordinate system points along the array normal.

Use the parameter in conjunction with the Array normal parameter of the URA and UCA arrays.

## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Polar pattern frequencies (Hz) - Polar pattern microphone response frequencies
1e3 (default) | real scalar | real-valued 1-by-L row vector

Polar pattern microphone response frequencies, specified as a real scalar, or a real-valued, 1-by- $L$ vector. The response frequencies lie within the frequency range specified by the Operating frequency vector $(\mathrm{Hz})$ vector.

## Dependencies

To enable this parameter, set Element type set to Custom Microphone.
Polar pattern angles (deg) - Polar pattern response angles
[-180:180] (default) | real-valued -by-P row vector

Specify the polar pattern response angles, as a 1-by- $P$ vector. The angles are measured from the central pickup axis of the microphone and must be between $-180^{\circ}$ and $180^{\circ}$, inclusive.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.
Polar pattern (dB) - Custom microphone polar response
zeros ( 1,361 ) (default) | real-valued $L$-by- $P$ matrix

Specify the magnitude of the custom microphone element polar patterns as an $L$-by- $P$ matrix. $L$ is the number of frequencies specified in Polar pattern frequencies $(\mathbf{H z}) . P$ is the number of angles specified in Polar pattern angles (deg). Each row of the matrix represents the magnitude of the polar pattern measured at the corresponding frequency specified in Polar pattern frequencies (Hz) and all angles specified in Polar pattern angles (deg). The pattern is measured in the azimuth plane. In the azimuth plane, the elevation angle is $0^{\circ}$ and the central pickup axis is $0^{\circ}$ degrees
azimuth and $0^{\circ}$ degrees elevation. The polar pattern is symmetric around the central axis. You can construct the microphone response pattern in 3-D space from the polar pattern.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.

## Array Parameters

Geometry - Array geometry
ULA (default) | URA | UCA | Conformal Array

Array geometry, specified as one of

- ULA - Uniform linear array
- URA - Uniform rectangular array
- UCA - Uniform circular array
- Conformal Array - arbitrary element positions

Number of elements - Number of array elements
2 for ULA arrays and 5 for UCA arrays (default) | integer greater than or equal to 2

The number of array elements for ULA or UCA arrays, specified as an integer greater than or equal to 2.

## Dependencies

To enable this parameter, set Geometry to ULA or UCA.
Element spacing (m) - Spacing between array elements

## 0.5 for ULA arrays and [0.5,0.5] for URA arrays (default) | positive scalar for ULA or URA arrays | 2 -element vector of positive values for URA arrays

Spacing between adjacent array elements:

- ULA - specify the spacing between two adjacent elements in the array as a positive scalar.
- URA - specify the spacing as a positive scalar or a 1 -by-2 vector of positive values. If Element spacing (m) is a scalar, the row and column spacings are equal. If Element spacing (m) is a vector, the vector has the form [SpacingBetweenArrayRows, SpacingBetweenArrayColumns].


## Dependencies

To enable this parameter, set Geometry to ULA or URA.
Array axis - Linear axis direction of ULA
$y$ (default) $|x| z$

Linear axis direction of ULA, specified as $y, x$, or $z$. All ULA array elements are uniformly spaced along this axis in the local array coordinate system.

## Dependencies

- To enable this parameter, set Geometry to ULA.
- This parameter is also enabled when the block only supports ULA arrays.

Array size - Dimensions of URA array
[2,2] (default) | positive integer | 1-by-2 vector of positive integers

Dimensions of a URA array, specified as a positive integer or 1-by-2 vector of positive integers.

- If Array size is a 1-by-2 vector, the vector has the form
[Number0fArrayRows, NumberOfArrayColumns].
- If Array size is an integer, the array has the same number of elements in each row and column.

For a URA, array elements are indexed from top to bottom along the leftmost array column, and continued to the next columns from left to right. In this figure, the Array size value of [3,2] creates an array having three rows and two columns.

## Size and Element Indexing Order

for Uniform Rectangular Arrays
Example: Size $=[3,2]$


## Dependencies

To enable this parameter, set Geometry to URA.
Element lattice - Lattice of URA element positions
Rectangular (default) |Triangular

Lattice of URA element positions, specified as Rectangular or Triangular.

- Rectangular - Aligns all the elements in row and column directions.
- Triangular - Shifts the even-row elements of a rectangular lattice toward the positive row-axis direction. The displacement is one-half the element spacing along the row dimension.


## Dependencies

To enable this parameter, set Geometry to URA.
Array normal - Array normal direction
$x$ for URA arrays or $z$ for UCA arrays (default) | y

Array normal direction, specified as $x, y$, or $z$.
Elements of planar arrays lie in a plane orthogonal to the selected array normal direction. Element boresight directions point along the array normal direction.

| Array Normal Parameter Value | Element Positions and Boresight Directions |
| :--- | :--- |
| x | Array elements lie in the $y z$-plane. All element <br> boresight vectors point along the $x$-axis. |
| y | Array elements lie in the $z x$-plane. All element <br> boresight vectors point along the $y$-axis. |
| $z$ | Array elements lie in the $x y$-plane. All element <br> boresight vectors point along the $z$-axis. |

## Dependencies

To enable this parameter, set Geometry to URA or UCA.
Radius of UCA (m) - UCA array radius
0.5 (default) | positive scalar

Radius of UCA array, specified as a positive scalar.

## Dependencies

To enable this parameter, set Geometry to UCA.

## Element positions (m) - Positions of conformal array elements <br> [0;0;0] (default) | 3-by-Nmatrix of real values

Positions of the elements in a conformal array, specified as a 3 -by- $N$ matrix of real values, where $N$ is the number of elements in the conformal array. Each column of this matrix represents the position [ $x ; y ; z$ ] of an array element in the array local coordinate system. The origin of the local coordinate system is ( $0,0,0$ ). Units are in meters.

## Dependencies

To enable this parameter set Geometry to Conformal Array.

## Data Types: double

Element normals (deg) - Direction of conformal array element normal vectors
[0;0] | 2-by-1 column vector | 2-by-N matrix

Direction of element normal vectors in a conformal array, specified as a 2 -by- 1 column vector or a 2 -by- $N$ matrix. $N$ indicates the number of elements in the array. If the parameter value is a matrix, each
column specifies the normal direction of the corresponding element in the form [azimuth;elevation] with respect to the local coordinate system. The local coordinate system aligns the positive $x$-axis with the direction normal to the conformal array. If the parameter value is a 2-by- 1 column vector, the same pointing direction is used for all array elements.

You can use the Element positions (m) and Element normals (deg) parameters to represent any arrangement in which pairs of elements differ by certain transformations. The transformations can combine translation, azimuth rotation, and elevation rotation. However, you cannot use transformations that require rotation about the normal direction.

To enable this parameter, set Geometry to Conformal Array.
Data Types: double
Taper - Array element tapers
1 (default) | complex scalar | complex-valued row vector

Specify element tapering as a complex-valued scalar or a complex-valued 1-by- $N$ row vector. In this vector, $N$ represents the number of elements in the array.

Also known as element weights, tapers multiply the array element responses. Tapers modify both amplitude and phase of the response to reduce side lobes or steer the main response axis.

If Taper is a scalar, the same weight is applied to each element. If Taper is a vector, a weight from the vector is applied to the corresponding sensor element. The number of weights must match the number of elements of the array.
Data Types: double

## Motion Tab

Source of transmit array motion - Specify the source of the transmitting array motion parameters Property (default)| Input port

Source of transmitting array motion parameters, specified as Property or Input port.

- When you select Property, specify the array location and orientation using the Position of the transmit array (m) and Orientation of the transmit array parameters. The array is stationary.
- When you select Input port, specify the array location, velocity, and orientation using the TxPos, TxVel, and TxAxes input ports of the block.

Data Types: char
Position of the transmit array ( $\mathbf{m}$ ) - Position of transmitting array
[0;0;0] (default) | real-valued 3-by-1 vector

The position of the transmitting array phase center, specified as a real-valued, 3-by-1 vector in Cartesian form $[x ; y ; z$ ] with respect to the global coordinate system. Units are in meters.

## Dependencies

To enable this parameter, set the Source of transmit array motion parameter to Property.
Data Types: double

Orientation of the transmit array - Set the orientation of transmitting array axes eye $(3,3)$ (default) | real-valued 3-by-3 orthonormal matrix

The orientation of transmitting array, specified as a real-valued, 3-by-3 orthonormal matrix. The matrix specifies the directions of the three axes that define the local coordinate system of the array with respect to the global coordinate system. The columns of the array correspond to the $x, y$, and $z$ axes, respectively.

## Dependencies

To enable this parameter, set the Source of transmit array motion parameter to Property.

## Data Types: double

Source of receive array motion - Specify the source of the receiving array motion parameters Property (default)| Input port

Source of receiving array motion parameters, specified as Property or Input port.

- When you select Property, specify the array location and orientation using the Position of the receive array ( $\mathbf{m}$ ) and Orientation of the receive array parameters. The array is stationary.
- When you select Input port, specify the array location, velocity, and orientation using the RxPos, RxVel, and RxAxes input ports of the block.


## Data Types: char

Position of the receive array ( $\mathbf{m}$ ) - Position of receiving array
[physconst('LightSpeed' )/1e5; 0;0] (default)| real-valued 3-by-1 vector

The position of the receiving array phase center, specified as a real-valued, 3-by-1 vector in Cartesian form $[x ; y ; z]$ with respect to the global coordinate system. Units are in meters.

## Dependencies

To enable this parameter, set the Source of receive array motion parameter to Property.
Data Types: double
Orientation of the receive array - Set the orientation of receiving array axes eye $(3,3)$ (default) | real-valued 3-by-3 orthonormal matrix

The orientation of receiving array, specified as a real-valued, 3-by-3 orthonormal matrix. The matrix specifies the directions of the three axes that define the local coordinate system of the array with respect to the global coordinate system. The columns of the array correspond to the $x, y$, and $z$ axes, respectively.

## Dependencies

To enable this parameter, set the Source of receive array motion parameter to Property.

## Data Types: double

Scatterer specification - Specify source of scatterer parameters
Auto (default)| Property|Input port

The source of scatterer parameters, specified as Auto, Property, or Input port.

- When you set this parameter to Auto, all scatterer positions and coefficients are randomly generated. Scatterer velocities are zero. The generated positions are contained within the region set by the Boundary of scatterer positions parameter. Set the number of scatterers using the Number of scatterers parameter.
- When you set this property to Property, set the scatterer positions using the Positions of scatterers (m) parameter. Set the scattering coefficients using the Scattering coefficients parameter. Scatterer velocities are zero.
- When you set this parameter to Input port, you specify the scatterer positions, velocities, and scattering coefficients using the ScatPos, ScatVel, and ScatCoef block input ports.

Data Types: char
Number of scatterers - Number of scatterers
1 (default) | nonnegative integer

The number of scatterers, specified as a nonnegative integer.

## Dependencies

To enable this property, set the Scatterer specification parameter to Auto.

## Data Types: double

Boundary of scatterer positions - Constrain scatterer positions within a boundary [0,1000] (default) | 1-by-2 real-valued vector | 3-by-2 real-valued matrix

The boundary scatterer positions, specified as a 1-by-2 real-valued row vector or a 3-by-2 real-valued matrix. If the boundary is a 1 -by-2 row vector, the vector contains the minimum and maximum, [minbdry maxbdry], for all three dimensions. If the boundary is a 3-by-2 matrix, the matrix specifies boundaries in all three dimensions in the form [x_minbdry x_maxbdry;y_minbdry y_maxbdry; z_minbdry z_maxbdry].

## Dependencies

To enable this property, set the Scatterer specification parameter to Auto.
Data Types: double
Positions of scatterers (m) - Positions of scatterers
[physconst('LightSpeed' )*5e-6;0;0] (default)|real-valued 3-by- $N_{s}$ matrix

The positions of the scatterers, specified as real-valued 3 -by- $N_{s}$ matrix. $N_{s}$ is the number of scatterers. Each column represents a different scatterer and has the Cartesian form $[x ; y ; z]$ with respect to the global coordinate system. Units are in meters.

## Dependencies

To enable this property, set the Scatterer specification parameter to Property.
Data Types: double

ScattererCoefficient - Scattering coefficients
1 (default) | complex-valued 1-by- $N_{s}$ matrix

Scattering coefficients, specified as a complex-valued 1-by- $N_{s}$ vector. $N_{s}$ is the number of scatterers. Units are dimensionless.

Dependencies
To enable this property, set the Scatterer specification parameter to Property.
Data Types: double

## Version History

Introduced in R2017a

## See Also

Objects
phased.ScatteringMIMOChannel

## Stepped FM Waveform

Stepped FM pulse waveform

## Libraries:

Stepped FM
Phased Array System Toolbox / Waveforms

## Description

The Stepped FM Waveform block generates a stepped FM pulse waveform with a specified pulse width, pulse repetition frequency (PRF), and number of frequency steps. The transmitted frequency is incremented in constant steps over the duration of the pulse. The block outputs an integral number of pulses or samples.

## Ports

## Input

PRFIdx - PRF Index
positive integer
Index to select the pulse repetition frequency (PRF), specified as a positive integer. The index selects the PRF from the predefined vector of values specified by the Pulse repetition frequency ( $\mathbf{H z}$ ) parameter.

Example: 4

## Dependencies

To enable this port, select Enable PRF selection input.
Data Types: double
FreqOffset - Frequency offset
scalar
Frequency offset in Hz , specified as a scalar.
Example: 2e3

## Dependencies

To enable this port, set Source of Frequency Offset to Input port.
Data Types: double

## Output

Y - Pulse waveform
complex-valued vector
Pulse waveform samples, returned as a complex-valued vector.

Data Types: double
PRF - Pulse repetition frequency
positive scalar
Pulse repetition frequency of current pulse, returned as a positive scalar.

## Dependencies

To enable this port, set the Output signal format parameter to Pulses and then select the Enable PRF output parameter.

Data Types: double
Coeff - Matched filter coefficients
vector | matrix
Matched filter coefficients, returned as a vector or matrix.

## Dependencies

To enable this port, select Enable Matched Filter Coefficients Output.
Data Types: double

## Parameters

Sample rate (Hz) - Sample rate of the output waveform
1e6 (default) | positive scalar

Sample rate of the output waveform, specified as a positive scalar. The ratio of Sample rate (Hz) to each element in the Pulse repetition frequency (Hz) vector must be an integer. This restriction is equivalent to requiring that the pulse repetition interval is an integral multiple of the sample interval.

```
Programmatic Use
Block Parameter:SampleRate
Type:double
Values:positive scalar
Default:1e6
```

Method to specify pulse duration - Pulse duration as time or duty cycle Pulse width (default)| Duty cycle

Method to set the pulse duration, specified as Pulse width or Duty cycle. When you set this parameter to Pulse width, the pulse duration is set using the Pulse width (s) parameter. When you set this parameter to Duty cycle, the pulse duration is computed from the values of the Pulse repetition frequency $(\mathbf{H z})$ and Duty Cycle parameters.

## Programmatic Use

Block Parameter:DurationSpecification
Type:string
Values:string
Default:'Pulse width'

Pulse width (s) - Time duration of pulse
50e-6 (default) | positive scalar

The duration of each pulse, specified as a positive scalar. Set the product of Pulse width (s) and Pulse repetition frequency to be less than or equal to one. This restriction ensures that the pulse width is smaller than the pulse repetition interval. Units are in seconds.

Example: 300e-6

## Dependencies

To enable this parameter, set the Method to specify pulse duration parameter to Pulse width.
Programmatic Use
Block Parameter:PulseWidth
Type:double
Values:string
Default:50e-6
Duty cycle - Waveform duty cycle
0.5 (default) | scalar in the range [0,1]

Waveform duty cycle, specified as a scalar in the range [0,1].
Example: 0.7

## Dependencies

To enable this parameter, set the Method to specify pulse duration parameter to Duty cycle.
Programmatic Use
Block Parameter:DutyCycle
Type:double
Values:positive scalar
Default:1e6
Pulse repetition frequency ( Hz ) - Pulse repetition frequency
le4 (default) | positive scalar

Pulse repetition frequency, $P R F$, specified as a scalar or a row vector. Units are in Hz. The pulse repetition interval, $P R I$, is the inverse of the pulse repetition frequency, $P R F$. The value of Pulse repetition frequency $(\mathbf{H z})$ must satisfy these constraints:

- The product of Pulse width and Pulse repetition frequency (Hz) must be less than or equal to one. This condition expresses the requirement that the pulse width is less than one pulse repetition interval. For the phase-coded waveform, the pulse width is the product of the chip width and number of chips.
- The ratio of sample rate to any element of Pulse repetition frequency must be an integer. This condition expresses the requirement that the number of samples in one pulse repetition interval is an integer.

You can select the value of $P R F$ by using block parameter settings alone or in conjunction with the input port, PRFIdx.

- When the Enable PRF selection input parameter is not selected, set the PRF using block parameters.
- To implement a constant $P R F$, specify Pulse repetition frequency (Hz) as a positive scalar.
- To implement a staggered $P R F$, specify Pulse repetition frequency $(\mathbf{H z})$ as a row vector with positive values. After the waveform reaches the last element of the vector, the process continues cyclically with the first element of the vector. When PRF is staggered, the time between successive output pulses cycles through the successive values of the PRF vector.
- When the Enable PRF selection input parameter is selected, you can implement a selectable $P R F$ by specifying Pulse repetition frequency ( Hz ) as a row vector with positive real-valued entries. But this time, when you execute the block, select a PRF by passing an index into the PRF vector into the PRFIdx port.

In all cases, the number of output samples is fixed when you set the Output signal format to Samples. When you use a varying $P R F$ and set Output signal format to Pulses, the number of output samples can vary.

## Programmatic Use

Block Parameter:PRF
Type:double
Values:positive scalar
Default:1e6
Enable PRF selection input - Select predefined PRF
off (default) | on

Select this parameter to enable the PRFIdx port.

- When enabled, pass in an index into a vector of predefined PRFs. Set predefined PRFs using the Pulse repetition frequency $(\mathrm{Hz})$ parameter.
- When not enabled, the block cycles through the vector of PRFs specified by the Pulse repetition frequency ( Hz ) parameter. If Pulse repetition frequency $(\mathbf{H z}$ ) is a scalar, the PRF is constant.


## Programmatic Use

Block Parameter:PRFSelectionInputPort
Type:logical
Values:positive scalar
Default:off
Frequency step (Hz) - Linear frequency step size
2e4 (default) | positive scalar

Specify the linear frequency step size as a positive scalar. Units are in Hertz.
Example: 1e3
Number of frequency steps - Number of frequency steps in pulse
5 (default) | positive integer

Specify the number of frequency steps as a positive integer. When the Number of frequency steps is 1 , the stepped FM waveform reduces to a rectangular waveform.

## Example: 8

Source of simulation sample time - Source of simulation sample time Derive from waveform parameters (default)|Inherit from Simulink engine

Source of simulation sample time, specified as Derive from waveform parameters or Inherit from Simulink engine. When set to Derive from waveform parameters, the block runs at a variable rate determined by the PRF of the selected waveform. The elapsed time is variable. When set to Inherit from Simulink engine, the block runs at a fixed rate so the elapsed time is a constant.

## Dependencies

To enable this parameter, select the Enable PRF selection input parameter.

```
Programmatic Use
Block Parameter:SimulationTimeSource
Type:enum
Values:Derive from waveform parameters, Inherit from Simulink engine
Default:Derive from waveform parameters
Source of Frequency Offset - Source of frequency offset
Property (default)|Input port
```

Source of frequency offset, specified as Property or Input port.

- When set to Property, the offset is determined by the value of the Frequency Offset parameter.
- When set to Input port, the offset is determined by the value of the FreqOffset port.


## Programmatic Use

Block Parameter:FrequencyOffsetSource
Type:enum
Values:Property, Input Port
Default:Property
Frequency Offset (Hz) - Frequency offset
0 (default) | scalar

Frequency offset, specified as a scalar. Units are in Hz.
Example: 2e3

## Dependencies

To enable this parameter set the Source of Frequency Offset parameter to Input port.

## Programmatic Use

Block Parameter:Frequency0ffset
Type:double
Values:scalar
Default:0
Output signal format - Format of the output signal
Pulses (default)| Samples

The format of the output signal, specified as Pulses or Samples.
If you set this parameter to Samples, the output of the block consists of multiple samples. The number of samples is the value of the Number of samples in output parameter.

If you set this parameter to Pulses, the output of the block consists of multiple pulses. The number of pulses is the value of the Number of pulses in output parameter.

```
Programmatic Use
Block Parameter:OutputFormat
Type:enum
Values:Pulses Samples
Default:Pulses
Number of samples in output - Number of samples in output
100 (default) | positive integer
```

Number of samples in the block output, specified as a positive integer.
Example: 1000

## Dependencies

To enable this parameter, set the Output signal format parameter to Samples.

## Programmatic Use

Block Parameter:NumSamples
Type:double
Values:positive scalar
Default:100
Data Types: double
Number of pulses in output - Number of pulses in output
1 (default) | positive integer

Number of pulses in the block output, specified as a positive integer.
Example: 2

## Dependencies

To enable this parameter, set the Output signal format parameter to Pulses.

## Programmatic Use

Block Parameter:NumPulses
Type:double
Values:positive scalar
Default:1
Data Types: double
Enable PRF Output - Enable output of PRF
off (default) | on

Select this parameter to enable the PRF output port.

## Dependencies

To enable this parameter, set Output signal format to Pulses.
Programmatic Use
Block Parameter:PRF0utputPort
Type:enum
Values:off on
Default:off
Enable Matched Filter Coeficients Output - Enable output of matched filter coefficients off (default) | on

Select this parameter to enable the Coeff output port.

## Programmatic Use

Block Parameter:CoefficientOutputPort
Type:enum
Values:off on
Default:off
Simulate using - Block simulation method
Interpreted Execution (default)|Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).
Programmatic Use
Block Parameter:SimulateUsing
Type:enum
Values:Interpreted Execution, Code Generation
Default:Interpreted Execution

## Version History

Introduced in R2014b

## See Also

phased.SteppedFMWaveform

## Stretch Processor

Stretch processor for linear FM waveforms


## Libraries:

Phased Array System Toolbox / Detection

## Description

The Stretch Processor block applies stretch processing on a linear FM waveform. Also known as dechirping, stretch processing is an alternative to matched filtering for linear FM waveforms.

## Ports

## Input

X - Input signal
$M$-by- $P$ complex-valued matrix
Input signal, specified as an $M$-by- $P$ complex-valued array. $M$ is the number of samples and $P$ is the number of pulses.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
Data Types: double
PRF - Pulse repetition frequency
positive scalar
Pulse repetition frequency of current pulse, specified as a positive scalar.

## Dependencies

To enable this port, set the Specify PRF as parameter to Input port.

## Data Types: double

## Output

Y - Stretch processed signal
$M$-by-P complex-valued matrix
Stretch processed signal, returned as an $M$-by- $P$ complex-valued array. $M$ is the number of samples and $P$ is the number of pulses.

## Parameters

Sample rate (Hz) - Sample rate of the output waveform
1e6 (default) | positive scalar

Sample rate of the output waveform, specified as a positive scalar. The ratio of Sample rate (Hz) to each element in the Pulse repetition frequency ( $\mathbf{H z )}$ vector must be an integer. This restriction is equivalent to requiring that the pulse repetition interval is an integral multiple of the sample interval.
Programmatic Use
Block Parameter:SampleRate
Type:double
Values:positive scalar
Default:1e6
Pulse width (s) - Time duration of pulse
50e-6 (default) | positive scalar

The duration of each pulse, specified as a positive scalar. Set the product of Pulse width (s) and Pulse repetition frequency to be less than or equal to one. This restriction ensures that the pulse width is smaller than the pulse repetition interval. Units are in seconds.

Example: 300e-6
Specify PRF as - Source of PRF value
Property (default) |Auto|Input port

Source of PRF value for the stretch processor, specified as Property, Auto, or Input port. When set to Property, the Pulse repetition frequency (Hz) parameter sets the PRF. When set to Input port, pass in the PRF using the PRF input port. When set to Auto, PRF is computed from the number of rows in the input signal.

## Pulse repetition frequency $(\mathbf{H z})$ - Pulse repetition frequency <br> le4 (default) | positive scalar

Pulse repetition frequency, PRF, specified as a positive scalar. Units are in Hertz. Set this parameter to the same value set in any Waveform library block used in the simulation.

## Dependencies

To enable this parameter, set the Specify PRF as parameter to Property.
FM sweep slope ( $\mathrm{Hz} / \mathbf{s}$ ) - Slope of linear FM sweep
2e9 (default) | scalar

Slope of the linear FM sweeping as a scalar, specified as a scalar. Units are in Hertz per second.
Example: 1e3

FM sweep interval - Direction of FM sweep
Positive (default)|Symmetric

FM sweep interval, specified as Positive or Symmetric. If you set this parameter value to Positive, the waveform sweeps the frequency bandwidth between 0 and $B$, where $B$ is the frequency bandwidth. If you set this parameter value to Symmetric, the waveform sweeps in the interval between $-B / 2$ and $B / 2$.

Signal propagation speed (m/s) - Signal propagation speed
physconst('LightSpeed') (default)| real-valued positive scalar

Signal propagation speed, specified as a real-valued positive scalar. The default value of the speed of light is the value returned by physconst('LightSpeed'). Units are in meters per second.

Example: 3e8
Data Types: double
Reference range ( $\mathbf{m}$ ) - Center of ranges of interest
5000 (default) | positive scalar

Center of ranges of interest, specified as a positive scalar. The reference range must be within the unambiguous range of one pulse. Units are in meters.

Example: 10e3
Reference span (m) - Span of ranges of interest
500 (default) | positive scalar

Span of ranges of interest, specified as a positive scalar. The span of ranges is centered on the range specified by the Reference range (m) parameter. Units are in meters.

Example: 1e3
Source of simulation sample time - Source of simulation sample time
Derive from waveform parameters (default)|Inherit from Simulink engine

Source of simulation sample time, specified as Derive from waveform parameters or Inherit from Simulink engine. When set to Derive from waveform parameters, the block runs at a variable rate determined by the PRF of the selected waveform. The elapsed time is variable. When set to Inherit from Simulink engine, the block runs at a fixed rate so the elapsed time is a constant.

## Dependencies

To enable this parameter, select the Enable PRF selection input parameter.

## Programmatic Use

Block Parameter:SimulationTimeSource
Type:enum
Values:Derive from waveform parameters, Inherit from Simulink engine

Default:Derive from waveform parameters
Output signal format - Format of the output signal
Pulses (default)| Samples

The format of the output signal, specified as Pulses or Samples.
If you set this parameter to Samples, the output of the block consists of multiple samples. The number of samples is the value of the Number of samples in output parameter.

If you set this parameter to Pulses, the output of the block consists of multiple pulses. The number of pulses is the value of the Number of pulses in output parameter.

## Programmatic Use

Block Parameter:OutputFormat
Type:enum
Values:Pulses Samples
Default:Pulses
Number of samples in output - Number of samples in output
100 (default) | positive integer

Number of samples in the block output, specified as a positive integer.
Example: 1000

## Dependencies

To enable this parameter, set the Output signal format parameter to Samples.
Programmatic Use
Block Parameter:NumSamples
Type:double
Values:positive scalar
Default:100
Data Types: double
Number of pulses in output - Number of pulses in output
1 (default) | positive integer

Number of pulses in the block output, specified as a positive integer.
Example: 2

## Dependencies

To enable this parameter, set the Output signal format parameter to Pulses.
Programmatic Use
Block Parameter:NumPulses
Type:double
Values:positive scalar
Default:1
Data Types: double

Enable PRF Output - Enable output of PRF
off (default) | on

Select this parameter to enable the PRF output port.

## Dependencies

To enable this parameter, set Output signal format to Pulses.
Programmatic Use
Block Parameter:PRFOutputPort
Type:enum
Values:off on
Default:off
Simulate using - Block simulation method
Interpreted Execution (default)|Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).
Programmatic Use
Block Parameter:SimulateUsing
Type:enum
Values:Interpreted Execution, Code Generation
Default:Interpreted Execution

# Version History <br> Introduced in R2014b 

See Also<br>phased.StretchProcessor

# Subband MVDR Beamformer 

Subband MVDR (Capon) beamformer

## Libraries:

Phased Array System Toolbox / Beamforming

## Description

The Subband MVDR Beamformer block performs minimum variance distortionless response (MVDR) beamforming on wideband signals. Signals are decomposed into frequency subbands and narrowband MVDR beamforming is performed in each band. The resulting subband signals are summed to form the output signal. MVDR beamforming preserves signal power in a given direction while suppressing interference and noise from other directions. The MVDR beamformer is also called the Capon beamformer.

## Ports

## Input

$\mathbf{X}$ - Input signal
$M$-by- $N$ complex-valued matrix
Input signal, specified as an $M$-by- $N$ matrix, where $M$ is the number of samples in the data, and $N$ is the number of array elements.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

## Data Types: double

XT - Training signal
$M$-by- $N$ complex-valued matrix
Input signal, specified as an $M$-by- $N$ matrix, where $M$ is the number of samples in the data, and $N$ is the number of array elements.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

## Dependencies

To enable this port, select the Enable training data input check box.
Data Types: double
Ang - Beamforming direction
2-by-1 real-valued vector | 2 -by- $L$ real-valued matrix

Beamforming direction, specified as a 2 -by- $L$ real-valued matrix, where $L$ is the number of beamforming directions. Each column takes the form of [AzimuthAngle; ElevationAngle]. Angle units are in degrees. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive, and the elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive. Angles are defined with respect to the local coordinate system of the array.

## Dependencies

To enable this port, set the Source of beamforming direction parameter to Input port.
Data Types: double

## Output

Y - Beamformed output
M-by-L complex-valued matrix
Beamformed output, returned as an $M$-by- $L$ complex-valued matrix. The quantity $M$ is the number of signal samples and $L$ is the number of desired beamforming directions specified by the Beamforming direction parameter or from the Ang port.
Data Types: double
Freq - Subband center frequencies
$K$-by-1 real-valued column vector
Subband center frequencies, returned as $K$-by- 1 real-valued column vector. The quantity $K$ is the number of subbands specified by the Number of subbands property.

## Dependencies

To enable this port, select the Enable subband center frequencies output checkbox.
Data Types: double
W - Beamforming weights
$N$-by-L complex-valued matrix
Beamformed weights, returned as an $N$-by-L complex-valued matrix. The quantity $N$ is the number of array elements. When the Specify sensor array as parameter is set to Partitioned array or Replicated subarray, $N$ represents the number of subarrays. $L$ is the number of desired beamforming directions specified in the Ang port or by the Beamforming direction (deg) property. There is one set of weights for each beamforming direction.

## Dependencies

To enable this port, select the Enable weights output checkbox.
Data Types: double

## Parameters

## Main tab

Signal propagation speed ( $\mathbf{m} / \mathbf{s}$ ) - Signal propagation speed
physconst('LightSpeed') (default) | real-valued positive scalar

Signal propagation speed, specified as a real-valued positive scalar. The default value of the speed of light is the value returned by physconst ('LightSpeed '). Units are in meters per second.

## Example: 3e8

Data Types: double
Operating frequency (Hz) - System operating frequency
$3 e 8$ (default) | positive real scalar

System operating frequency, specified as a positive scalar. Units are in Hz.
Inherit sample rate - Inherit sample rate from upstream blocks
on (default) | off

Select this parameter to inherit the sample rate from upstream blocks. Otherwise, specify the sample rate using the Sample rate ( $\mathbf{H z}$ ) parameter.
Data Types: Boolean
Sample rate (Hz) - Sampling rate of signal
le6 (default) | positive real-valued scalar

Specify the signal sampling rate as a positive scalar. Units are in Hz .

## Dependencies

To enable this parameter, clear the Inherit sample rate check box.
Data Types: double
Number of subbands - Number of processing subbands
64 (default) | positive integer

Number of processing subbands, specified as a positive integer.
Example: 128
Diagonal loading factor - Diagonal loading factor for stability nonnegative scalar

Specify the diagonal loading factor as a nonnegative scalar. Diagonal loading is a technique used to achieve robust beamforming performance, especially when the sample support is small.

Enable training data input - Enable the use of training data
off (default) | on

Select this check box to specify additional training data via the input port XT . To use the input signal as the training data, clear the check box which removes the port.

Source of beamforming direction - Source of beamforming direction
Property (default)| Input port

Source of beamforming direction, specified as Property or Input port. When you set Source of beamforming direction to Property, you then set the direction using the Beamforming direction (deg) parameter. When you select Input port, the direction is determined by the input to the Ang port.

## Beamforming direction (deg) - Beamforming directions

2 -by-L real-valued matrix

Beamforming directions, specified as a 2 -by- $L$ real-valued matrix, where $L$ is the number of beamforming directions. Each column takes the form [AzimuthAngle;ElevationAngle]. Angle units are in degrees. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$. Angles are defined with respect to the local coordinate system of the array.

## Dependencies

To enable this parameter, set the Source of beamforming direction parameter to Property.
Enable weights output - Option to output beamformer weights
off (default) | on

Select this check box to obtain the beamformer weights from the output port, W .
Enable subband center frequencies output - Enable the output of subband center frequencies
off (default) | on
Select this check box to obtain the center frequencies of each subband via the output port, Freq.
Simulate using - Block simulation method
Interpreted Execution (default)|Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).
Programmatic Use
Block Parameter:SimulateUsing
Type:enum
Values:Interpreted Execution, Code Generation
Default:Interpreted Execution

## Sensor Arrays Tab

Specify sensor array as - Method to specify array
Array (no subarrays) (default)| Partitioned array|Replicated subarray|MATLAB expression

Method to specify array, specified as Array (no subarrays) or MATLAB expression.

- Array (no subarrays) - use the block parameters to specify the array.
- Partitioned array - use the block parameters to specify the array.
- Replicated subarray - use the block parameters to specify the array.
- MATLAB expression - create the array using a MATLAB expression.

Expression - MATLAB expression used to create an array
Phased Array System Toolbox array System object

MATLAB expression used to create an array, specified as a valid Phased Array System Toolbox array System object.

Example: phased.URA('Size', [5,3])

## Dependencies

To enable this parameter, set Specify sensor array as to MATLAB expression.

## Element Parameters

Element type - Array element types
Isotropic Antenna (default)|Cosine Antenna|Custom Antenna|Omni Microphone| Custom Microphone

Antenna or microphone type, specified as one of the following:

- Isotropic Antenna
- Cosine Antenna
- Custom Antenna
- Omni Microphone
- Custom Microphone

Operating frequency range (Hz) - Operating frequency range of the antenna or microphone element
[0, 1e20] (default) | real-valued 1-by-2 row vector

Specify the operating frequency range of the antenna or microphone element as a 1-by-2 row vector in the form [LowerBound, UpperBound]. The element has no response outside this frequency range. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Isotropic Antenna, Cosine Antenna, or Omni Microphone.

Operating frequency vector ( $\mathbf{H z}$ ) - Operating frequency range of custom antenna or microphone elements
[0, 1e20] (default) | real-valued row vector

Specify the frequencies at which to set antenna and microphone frequency responses as a 1-by-L row vector of increasing real values. The antenna or microphone element has no response outside the frequency range specified by the minimum and maximum elements of this vector. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone. Use Frequency responses (dB) to set the responses at these frequencies.

Baffle the back of the element - Set back response of an Isotropic Antenna element or an Omni Microphone element to zero
off (default) | on

Select this check box to baffle the back response of the element. When back baffled, the responses at all azimuth angles beyond $\pm 90^{\circ}$ from broadside are set to zero. The broadside direction is defined as $0^{\circ}$ azimuth angle and $0^{\circ}$ elevation angle.

## Dependencies

To enable this check box, set Element type to Isotropic Antenna or Omni Microphone.
Exponent of cosine pattern - Exponents of azimuth and elevation cosine patterns [1.5 1.5] (default) | nonnegative scalar | real-valued 1-by-2 matrix of nonnegative values

Specify the exponents of the cosine pattern as a nonnegative scalar or a real-valued 1-by-2 matrix of nonnegative values. When Exponent of cosine pattern is a 1-by-2 vector, the first element is the
exponent in the azimuth direction and the second element is the exponent in the elevation direction. When you set this parameter to a scalar, both the azimuth direction and elevation direction cosine patterns are raised to the same power.

## Dependencies

To enable this parameter, set Element type to Cosine Antenna.
Frequency responses (dB) - Antenna and microphone frequency response [0,0] (default) | real-valued row vector

Frequency response of a custom antenna or custom microphone for the frequencies defined by the Operating frequency vector (Hz) parameter. The dimensions of Frequency responses (dB) must match the dimensions of the vector specified by the Operating frequency vector $(\mathbf{H z})$ parameter.

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone.
Input Pattern Coordinate System - Coordinate system of custom antenna pattern
az-el (default)| phi-theta

Coordinate system of custom antenna pattern, specified az-el or phi-theta. When you specify azel, use the Azimuth angles (deg) and Elevations angles (deg) parameters to specify the coordinates of the pattern points. When you specify phi-theta, use the Phi angles (deg) and Theta angles (deg) parameters to specify the coordinates of the pattern points.

## Dependencies

To enable this parameter, set Element type to Custom Antenna.

## Azimuth angles (deg) - Azimuth angles of antenna radiation pattern

[-180:180] (default) | real-valued row vector

Specify the azimuth angles at which to calculate the antenna radiation pattern as a 1 -by- $P$ row vector. $P$ must be greater than 2. Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to az-el.

Elevation angles (deg) - Elevation angles of antenna radiation pattern
[-90:90] (default) | real-valued row vector

Specify the elevation angles at which to compute the radiation pattern as a 1-by- $Q$ vector. $Q$ must be greater than 2. Angle units are in degrees. Elevation angles must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to az-el.

Phi Angles (deg) - Phi angle coordinates of custom antenna radiation pattern
$0: 360$ | real-valued 1-by-P row vector

Phi angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by-P row vector. $P$ must be greater than 2 . Angle units are in degrees. Phi angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input
Pattern Coordinate System parameter to phi-theta.
Theta Angles (deg) - Theta angle coordinates of custom antenna radiation pattern
0:180 | real-valued 1-by- $Q$ row vector

Theta angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by$Q$ row vector. $Q$ must be greater than 2 . Angle units are in degrees. Theta angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Magnitude pattern (dB) - Magnitude of combined antenna radiation pattern zeros $(181,361)$ (default) | real-valued $Q$-by-P matrix | real-valued $Q$-by-P-by-L array

Magnitude of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector $(\mathbf{H z})$.

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (Hz) parameter.


## Dependencies

To enable this parameter, set Element type to Custom Antenna.

Phase pattern (deg) - Custom antenna radiation phase pattern
zeros $(181,361)$ (default) | real-valued $Q$-by- $P$ matrix | real-valued $Q$-by- $P$-by- $L$ array

Phase of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi - theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector ( $\mathbf{H z}$ ).

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (


## Dependencies

To enable this parameter, set Element type to Custom Antenna.
MatchArrayNormal - Rotate antenna element to array normal
on (default) | off

Select this check box to rotate the antenna element pattern to align with the array normal. When not selected, the element pattern is not rotated.

When the antenna is used in an antenna array and the Input Pattern Coordinate System parameter is az-el, selecting this check box rotates the pattern so that the $x$-axis of the element coordinate system points along the array normal. Not selecting uses the element pattern without the rotation.

When the antenna is used in an antenna array and Input Pattern Coordinate System is set to phitheta, selecting this check box rotates the pattern so that the $z$-axis of the element coordinate system points along the array normal.

Use the parameter in conjunction with the Array normal parameter of the URA and UCA arrays.

## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Polar pattern frequencies (Hz) - Polar pattern microphone response frequencies 1e3 (default) | real scalar | real-valued 1-by-L row vector

Polar pattern microphone response frequencies, specified as a real scalar, or a real-valued, 1-by- $L$ vector. The response frequencies lie within the frequency range specified by the Operating frequency vector $(\mathbf{H z})$ vector.

## Dependencies

To enable this parameter, set Element type set to Custom Microphone.
Polar pattern angles (deg) - Polar pattern response angles
[-180:180] (default) | real-valued -by-P row vector

Specify the polar pattern response angles, as a 1-by- $P$ vector. The angles are measured from the central pickup axis of the microphone and must be between $-180^{\circ}$ and $180^{\circ}$, inclusive.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.
Polar pattern (dB) - Custom microphone polar response
zeros $(1,361)$ (default) | real-valued $L$-by-P matrix

Specify the magnitude of the custom microphone element polar patterns as an $L$-by- $P$ matrix. $L$ is the number of frequencies specified in Polar pattern frequencies $(\mathbf{H z}) . P$ is the number of angles specified in Polar pattern angles (deg). Each row of the matrix represents the magnitude of the polar pattern measured at the corresponding frequency specified in Polar pattern frequencies (Hz) and all angles specified in Polar pattern angles (deg). The pattern is measured in the azimuth plane. In the azimuth plane, the elevation angle is $0^{\circ}$ and the central pickup axis is $0^{\circ}$ degrees azimuth and $0^{\circ}$ degrees elevation. The polar pattern is symmetric around the central axis. You can construct the microphone response pattern in 3-D space from the polar pattern.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.

## Array Parameters

Geometry - Array geometry
ULA (default) | URA | UCA | Conformal Array

Array geometry, specified as one of

- ULA - Uniform linear array
- URA - Uniform rectangular array
- UCA - Uniform circular array
- Conformal Array - arbitrary element positions

Number of elements - Number of array elements
2 for ULA arrays and 5 for UCA arrays (default) | integer greater than or equal to 2

The number of array elements for ULA or UCA arrays, specified as an integer greater than or equal to 2.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

## Dependencies

To enable this parameter, set Geometry to ULA or UCA.
Element spacing (m) - Spacing between array elements
0.5 for ULA arrays and [0.5, 0.5] for URA arrays (default) | positive scalar for ULA or URA arrays | 2 -element vector of positive values for URA arrays

Spacing between adjacent array elements:

- ULA - specify the spacing between two adjacent elements in the array as a positive scalar.
- URA - specify the spacing as a positive scalar or a 1 -by-2 vector of positive values. If Element spacing (m) is a scalar, the row and column spacings are equal. If Element spacing (m) is a vector, the vector has the form [SpacingBetweenArrayRows,SpacingBetweenArrayColumns].
- When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.


## Dependencies

To enable this parameter, set Geometry to ULA or URA.
Array axis - Linear axis direction of ULA
$y$ (default) $|x| z$

Linear axis direction of ULA, specified as $y$, $x$, or $z$. All ULA array elements are uniformly spaced along this axis in the local array coordinate system.

## Dependencies

- To enable this parameter, set Geometry to ULA.
- This parameter is also enabled when the block only supports ULA arrays.

Array size - Dimensions of URA array
[2,2] (default) | positive integer | 1-by-2 vector of positive integers

Dimensions of a URA array, specified as a positive integer or 1-by-2 vector of positive integers.

- If Array size is a 1 -by- 2 vector, the vector has the form [NumberOfArrayRows, NumberOfArrayColumns].
- If Array size is an integer, the array has the same number of rows and columns.
- When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

For a URA, array elements are indexed from top to bottom along the leftmost column, and then continue to the next columns from left to right. In this figure, the Array size value of [3,2] creates an array having three rows and two columns.

Size and Element Indexing Order
for Uniform Rectangular Arrays
Example: Size $=[3,2]$


## Dependencies

To enable this parameter, set Geometry to URA.
Element lattice - Lattice of URA element positions
Rectangular (default) |Triangular

Lattice of URA element positions, specified as Rectangular or Triangular.

- Rectangular - Aligns all the elements in row and column directions.
- Triangular - Shifts the even-row elements of a rectangular lattice toward the positive row-axis direction. The displacement is one-half the element spacing along the row dimension.


## Dependencies

To enable this parameter, set Geometry to URA.
Array normal - Array normal direction
$x$ for URA arrays or $z$ for UCA arrays (default) | y

Array normal direction, specified as $x, y$, or $z$.
Elements of planar arrays lie in a plane orthogonal to the selected array normal direction. Element boresight directions point along the array normal direction.

| Array Normal Parameter Value | Element Positions and Boresight Directions |
| :--- | :--- |
| x | Array elements lie in the $y z$-plane. All element <br> boresight vectors point along the $x$-axis. |
| y | Array elements lie in the $z x$-plane. All element <br> boresight vectors point along the $y$-axis. |

Array elements lie in the xy-plane. All element boresight vectors point along the $z$-axis.

## Dependencies

To enable this parameter, set Geometry to URA or UCA.
Radius of UCA ( $\mathbf{m}$ ) - UCA array radius
0.5 (default) | positive scalar

Radius of UCA array, specified as a positive scalar.

## Dependencies

To enable this parameter, set Geometry to UCA.
Element positions (m) - Positions of conformal array elements
[0;0;0] (default)| 3-by-Nmatrix of real values

Positions of the elements in a conformal array, specified as a 3 -by- $N$ matrix of real values, where $N$ is the number of elements in the conformal array. Each column of this matrix represents the position [ $x ; y ; z$ ] of an array element in the array local coordinate system. The origin of the local coordinate system is ( $0,0,0$ ). Units are in meters.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

## Dependencies

To enable this parameter set Geometry to Conformal Array.
Element normals (deg) - Direction of conformal array element normal vectors [0;0] | 2-by-1 column vector | 2 -by-N matrix

Direction of element normal vectors in a conformal array, specified as a 2-by-1 column vector or a 2-by- $N$ matrix. $N$ indicates the number of elements in the array. For a matrix, each column specifies the normal direction of the corresponding element in the form [azimuth; elevation] with respect to the local coordinate system. The local coordinate system aligns the positive $x$-axis with the direction normal to the conformal array. If the parameter value is a 2 -by- 1 column vector, the same pointing direction is used for all array elements.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

You can use the Element positions (m) and Element normals (deg) parameters to represent any arrangement in which pairs of elements differ by certain transformations. The transformations can combine translation, azimuth rotation, and elevation rotation. However, you cannot use transformations that require rotation about the normal direction.

## Dependencies

To enable this parameter, set Geometry to Conformal Array.

Taper - Array element tapers
1 (default) | complex-valued scalar | complex-valued row vector

Element tapering, specified as a complex-valued scalar or a complex-valued 1-by- $N$ row vector. In this vector, $N$ represents the number of elements in the array.

Also known as element weights, tapers multiply the array element responses. Tapers modify both amplitude and phase of the response to reduce side lobes or steer the main response axis.

If Taper is a scalar, the same weight is applied to each element. If Taper is a vector, a weight from the vector is applied to the corresponding sensor element. The number of weights must match the number of elements of the array.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

Subarray definition matrix - Define elements belonging to subarrays
logical matrix

Specify the subarray selection as an $M$-by- $N$ matrix. $M$ is the number of subarrays and $N$ is the total number of elements in the array. Each row of the matrix represents a subarray and each entry in the row indicates when an element belongs to the subarray. When the entry is zero, the element does not belong the subarray. A nonzero entry represents a complex-valued weight applied to the corresponding element. Each row must contain at least one nonzero entry.

The phase center of each subarray lies at the subarray geometric center. The subarray geometric center depends on the Subarray definition matrix and Geometry parameters.

## Dependencies

To enable this parameter, set Specify sensor array as to Partitioned array.
Subarray steering method - Specify subarray steering method None (default) | Phase | Time

Subarray steering method, specified as one of

- None
- Phase
- Time
- Custom

Selecting Phase or Time opens the Steer input port on the Narrowband Receive Array, Narrowband Transmit Array, Wideband Receive Array, Wideband Transmit Array blocks, Constant Gamma Clutter, and GPU Constant Gamma Clutter blocks.

Selecting Custom opens the WS input port on the Narrowband Receive Array, Narrowband Transmit Array, Wideband Receive Array, Wideband Transmit Array blocks, Constant Gamma Clutter, and GPU Constant Gamma Clutter blocks.

## Dependencies

To enable this parameter, set Specify sensor array as to Partitioned array or Replicated subarray.

Phase shifter frequency (Hz) - Subarray phase shifting frequency
3.0 e 8 (default) | positive real-valued scalar

Operating frequency of subarray steering phase shifters, specified as a positive real-valued scalar. Units are Hz.

## Dependencies

To enable this parameter, set Sensor array to Partitioned array or Replicated subarray and set Subarray steering method to Phase.

Number of bits in phase shifters - Subarray steering phase shift quantization bits
0 (default) | non-negative integer

Subarray steering phase shift quantization bits, specified as a non-negative integer. A value of zero indicates that no quantization is performed.

## Dependencies

To enable this parameter, set Sensor array to Partitioned array or Replicated subarray and set Subarray steering method to Phase.

Subarrays layout - Subarray position specification
Rectangular (default) | Custom

Specify the layout of replicated subarrays as Rectangular or Custom.

- When you set this parameter to Rectangular, use the Grid size and Grid spacing parameters to place the subarrays.
- When you set this parameter to Custom, use the Subarray positions (m) and Subarray normals parameters to place the subarrays.


## Dependencies

To enable this parameter, set Sensor array to Replicated subarray
Grid size - Dimensions of rectangular subarray grid [1,2] (default)

Rectangular subarray grid size, specified as a single positive integer, or a 1-by-2 row vector of positive integers.

If Grid size is an integer scalar, the array has an equal number of subarrays in each row and column. If Grid size is a 1 -by-2 vector of the form [NumberOfRows, NumberOfColumns], the first entry is the number of subarrays along each column. The second entry is the number of subarrays in each row. A row is along the local $y$-axis, and a column is along the local $z$-axis. The figure here shows how you can replicate a 3-by-2 URA subarray using a Grid size of [1,2].
$3 \times 2$ Element URA
Replicated on a $1 \times 2$ Grid


## Dependencies

To enable this parameter, set Sensor array to Replicated subarray and Subarrays layout to Rectangular.

Grid spacing ( $\mathbf{m}$ ) - Spacing between subarrays on rectangular grid
Auto (default) | positive real-valued scalar | 1-by-2 vector of positive real-values

The rectangular grid spacing of subarrays, specified as a positive, real-valued scalar, a 1-by-2 row vector of positive, real-values, or Auto. Units are in meters.

- If Grid spacing is a scalar, the spacing along the row and the spacing along the column is the same.
- If Grid spacing is a 1-by-2 row vector, the vector has the form
[SpacingBetweenRows, SpacingBetweenColumn]. The first entry specifies the spacing between rows along a column. The second entry specifies the spacing between columns along a row.
- If Grid spacing is set to Auto, replication preserves the element spacing of the subarray for both rows and columns while building the full array. This option is available only when you specify Geometry as ULA or URA.


## Dependencies

To enable this parameter, set Sensor array to Replicated subarray and Subarrays layout to Rectangular.

Subarray positions (m) - Positions of subarrays
[0,0;0.5, 0.5;0,0] (default) | 3-by- $N$ real-valued matrix

Positions of the subarrays in the custom grid, specified as a real 3-by- $N$ matrix, where $N$ is the number of subarrays in the array. Each column of the matrix represents the position of a single subarray in the array local coordinate system. The coordinates are expressed in the form $[x ; y ; z]$. Units are in meters.

## Dependencies

To enable this parameter, set Sensor array to Replicated subarray and Subarrays layout to Custom.

Subarray normals - Direction of subarray normal vectors
[0,0;0,0] (default) | 2-by- $N$ real matrix

Specify the normal directions of the subarrays in the array. This parameter value is a 2 -by- $N$ matrix, where $N$ is the number of subarrays in the array. Each column of the matrix specifies the normal direction of the corresponding subarray, in the form [azimuth; elevation]. Angle units are in degrees. Angles are defined with respect to the local coordinate system.

You can use the Subarray positions and Subarray normals parameters to represent any arrangement in which pairs of subarrays differ by certain transformations. The transformations can combine translation, azimuth rotation, and elevation rotation. However, you cannot use transformations that require rotation about the normal.

## Dependencies

To enable this parameter, set the Sensor array parameter to Replicated subarray and the Subarrays layout to Custom.

## Version History

Introduced in R2015b

See Also<br>phased.SubbandMVDRBeamformer

# Subband Phase Shift Beamformer 

Subband phase shift beamformer


Libraries:
Phased Array System Toolbox / Beamforming

## Description

The Subband Phase Shift Beamformer block performs delay-and-sum beamforming in the frequency domain. The signal is divided into frequency subbands. In each subband, a phase shift at the subband center frequency approximates the time delay. The resulting subband signals are summed to form the frequency-domain output signal and then converted to the time domain.

## Ports

Input
$\mathbf{X}$ - Input signal
$M$-by- $N$ complex-valued matrix
Input signal, specified as an $M$-by- $N$ matrix, where $M$ is the number of samples in the data, and $N$ is the number of array elements.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
Data Types: double
Ang - Beamforming direction
2-by-1 real-valued vector | 2-by-L real-valued matrix
Beamforming direction, specified as a 2 -by- $L$ real-valued matrix, where $L$ is the number of beamforming directions. Each column takes the form of [AzimuthAngle; ElevationAngle]. Angle units are in degrees. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive, and the elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive. Angles are defined with respect to the local coordinate system of the array.

Dependencies
To enable this port, set the Source of beamforming direction parameter to Input port.
Data Types: double

## Output

$\mathbf{Y}$ - Beamformed output
$M$-by-L complex-valued matrix

Beamformed output, returned as an $M$-by- $L$ complex-valued matrix. The quantity $M$ is the number of signal samples and $L$ is the number of desired beamforming directions specified by the Beamforming direction parameter or from the Ang port.

## Data Types: double

Freq - Subband center frequencies
K-by-1 real-valued column vector
Subband center frequencies, returned as $K$-by- 1 real-valued column vector. The quantity $K$ is the number of subbands specified by the Number of subbands property.

## Dependencies

To enable this port, select the Enable subband center frequencies output checkbox.
Data Types: double
W - Beamforming weights
$N$-by-L complex-valued matrix
Beamformed weights, returned as an $N$-by- $L$ complex-valued matrix. The quantity $N$ is the number of array elements. When the Specify sensor array as parameter is set to Partitioned array or Replicated subarray, $N$ represents the number of subarrays. $L$ is the number of desired beamforming directions specified in the Ang port or by the Beamforming direction (deg) property. There is one set of weights for each beamforming direction.

## Dependencies

To enable this port, select the Enable weights output checkbox.

## Data Types: double

## Parameters

Main tab
Signal propagation speed (m/s) - Signal propagation speed
physconst('LightSpeed') (default)| real-valued positive scalar

Signal propagation speed, specified as a real-valued positive scalar. The default value of the speed of light is the value returned by physconst('LightSpeed'). Units are in meters per second.

## Example: 3e8

Data Types: double
Operating frequency (Hz) - System operating frequency
3 e8 (default) | positive real scalar

System operating frequency, specified as a positive scalar. Units are in Hz.
Inherit sample rate - Inherit sample rate from upstream blocks
on (default) | off

Select this parameter to inherit the sample rate from upstream blocks. Otherwise, specify the sample rate using the Sample rate (Hz) parameter.
Data Types: Boolean
Sample rate (Hz) - Sampling rate of signal
le6 (default) | positive real-valued scalar

Specify the signal sampling rate as a positive scalar. Units are in Hz .

## Dependencies

To enable this parameter, clear the Inherit sample rate check box.
Data Types: double
Number of subbands - Number of processing subbands
64 (default) | positive integer

Number of processing subbands, specified as a positive integer.
Example: 128
Source of beamforming direction - Source of beamforming direction
Property (default)|Input port

Source of beamforming direction, specified as Property or Input port. When you set Source of beamforming direction to Property, you then set the direction using the Beamforming direction (deg) parameter. When you select Input port, the direction is determined by the input to the Ang port.

Beamforming direction (deg) - Beamforming directions
2-by-L real-valued matrix

Beamforming directions, specified as a 2 -by- $L$ real-valued matrix, where $L$ is the number of beamforming directions. Each column takes the form [AzimuthAngle;ElevationAngle]. Angle units are in degrees. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$. Angles are defined with respect to the local coordinate system of the array.

## Dependencies

To enable this parameter, set the Source of beamforming direction parameter to Property.
Enable weights output - Option to output beamformer weights
off (default) | on

Select this check box to obtain the beamformer weights from the output port, W.
Enable subband center frequencies output - Enable the output of subband center frequencies
off (default) | on

Select this check box to obtain the center frequencies of each subband via the output port, Freq.
Simulate using - Block simulation method
Interpreted Execution (default) | Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).

## Programmatic Use

Block Parameter:SimulateUsing
Type:enum
Values:Interpreted Execution, Code Generation
Default:Interpreted Execution

## Sensor Arrays Tab

Specify sensor array as - Method to specify array
Array (no subarrays) (default)| Partitioned array|Replicated subarray|MATLAB expression

Method to specify array, specified as Array (no subarrays) or MATLAB expression.

- Array (no subarrays) - use the block parameters to specify the array.
- Partitioned array - use the block parameters to specify the array.
- Replicated subarray - use the block parameters to specify the array.
- MATLAB expression - create the array using a MATLAB expression.

Expression - MATLAB expression used to create an array
Phased Array System Toolbox array System object

MATLAB expression used to create an array, specified as a valid Phased Array System Toolbox array System object.

Example: phased.URA('Size', [5,3])

## Dependencies

To enable this parameter, set Specify sensor array as to MATLAB expression.

## Element Parameters

Element type - Array element types
Isotropic Antenna (default)|Cosine Antenna|Custom Antenna|Omni Microphone| Custom Microphone

Antenna or microphone type, specified as one of the following:

- Isotropic Antenna
- Cosine Antenna
- Custom Antenna
- Omni Microphone
- Custom Microphone

Operating frequency range $(\mathrm{Hz})$ - Operating frequency range of the antenna or microphone element
[0,1e20] (default) | real-valued 1-by-2 row vector

Specify the operating frequency range of the antenna or microphone element as a 1-by-2 row vector in the form [LowerBound, UpperBound]. The element has no response outside this frequency range. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Isotropic Antenna, Cosine Antenna, or Omni Microphone.

Operating frequency vector ( Hz ) - Operating frequency range of custom antenna or microphone elements
[0,1e20] (default) | real-valued row vector

Specify the frequencies at which to set antenna and microphone frequency responses as a 1-by- $L$ row vector of increasing real values. The antenna or microphone element has no response outside the frequency range specified by the minimum and maximum elements of this vector. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone. Use Frequency responses (dB) to set the responses at these frequencies.

Baffle the back of the element - Set back response of an Isotropic Antenna element or an Omni Microphone element to zero
off (default) | on

Select this check box to baffle the back response of the element. When back baffled, the responses at all azimuth angles beyond $\pm 90^{\circ}$ from broadside are set to zero. The broadside direction is defined as $0^{\circ}$ azimuth angle and $0^{\circ}$ elevation angle.

## Dependencies

To enable this check box, set Element type to Isotropic Antenna or Omni Microphone.
Exponent of cosine pattern - Exponents of azimuth and elevation cosine patterns
[1.5 1.5] (default) | nonnegative scalar | real-valued 1-by-2 matrix of nonnegative values

Specify the exponents of the cosine pattern as a nonnegative scalar or a real-valued 1-by-2 matrix of nonnegative values. When Exponent of cosine pattern is a 1-by-2 vector, the first element is the exponent in the azimuth direction and the second element is the exponent in the elevation direction. When you set this parameter to a scalar, both the azimuth direction and elevation direction cosine patterns are raised to the same power.

## Dependencies

To enable this parameter, set Element type to Cosine Antenna.
Frequency responses (dB) - Antenna and microphone frequency response [0,0] (default) | real-valued row vector

Frequency response of a custom antenna or custom microphone for the frequencies defined by the Operating frequency vector (Hz) parameter. The dimensions of Frequency responses (dB) must match the dimensions of the vector specified by the Operating frequency vector $(\mathbf{H z})$ parameter.

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone.
Input Pattern Coordinate System - Coordinate system of custom antenna pattern az-el (default)|phi-theta

Coordinate system of custom antenna pattern, specified az-el or phi-theta. When you specify azel, use the Azimuth angles (deg) and Elevations angles (deg) parameters to specify the coordinates of the pattern points. When you specify phi-theta, use the Phi angles (deg) and Theta angles (deg) parameters to specify the coordinates of the pattern points.

## Dependencies

To enable this parameter, set Element type to Custom Antenna.

Azimuth angles (deg) - Azimuth angles of antenna radiation pattern
[-180:180] (default) | real-valued row vector

Specify the azimuth angles at which to calculate the antenna radiation pattern as a 1 -by- $P$ row vector. $P$ must be greater than 2. Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to az-el.

Elevation angles (deg) - Elevation angles of antenna radiation pattern
[-90:90] (default) | real-valued row vector

Specify the elevation angles at which to compute the radiation pattern as a 1-by- $Q$ vector. $Q$ must be greater than 2. Angle units are in degrees. Elevation angles must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input
Pattern Coordinate System parameter to az-el.
Phi Angles (deg) - Phi angle coordinates of custom antenna radiation pattern
$0: 360 \mid$ real-valued 1-by-P row vector

Phi angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by- $P$ row vector. $P$ must be greater than 2 . Angle units are in degrees. Phi angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Theta Angles (deg) - Theta angle coordinates of custom antenna radiation pattern 0:180 | real-valued 1-by- $Q$ row vector

Theta angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by$Q$ row vector. $Q$ must be greater than 2 . Angle units are in degrees. Theta angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Magnitude pattern (dB) - Magnitude of combined antenna radiation pattern zeros $(181,361)$ (default) | real-valued $Q$-by- $P$ matrix | real-valued $Q$-by- $P$-by-L array

Magnitude of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector $(\mathbf{H z})$.

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector ( $\mathbf{H z}$ ) parameter.


## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Phase pattern (deg) - Custom antenna radiation phase pattern
zeros $(181,361)$ (default) | real-valued $Q$-by- $P$ matrix | real-valued $Q$-by- $P$-by-L array

Phase of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector $(\mathbf{H z})$.

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector (Hz) parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (


## Dependencies

To enable this parameter, set Element type to Custom Antenna.
MatchArrayNormal - Rotate antenna element to array normal on (default) | off

Select this check box to rotate the antenna element pattern to align with the array normal. When not selected, the element pattern is not rotated.

When the antenna is used in an antenna array and the Input Pattern Coordinate System parameter is az-el, selecting this check box rotates the pattern so that the $x$-axis of the element
coordinate system points along the array normal. Not selecting uses the element pattern without the rotation.

When the antenna is used in an antenna array and Input Pattern Coordinate System is set to phitheta, selecting this check box rotates the pattern so that the $z$-axis of the element coordinate system points along the array normal.

Use the parameter in conjunction with the Array normal parameter of the URA and UCA arrays.

## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Polar pattern frequencies (Hz) - Polar pattern microphone response frequencies
1e3 (default) | real scalar | real-valued 1-by-L row vector

Polar pattern microphone response frequencies, specified as a real scalar, or a real-valued, 1-by-L vector. The response frequencies lie within the frequency range specified by the Operating
frequency vector $(\mathrm{Hz})$ vector.

## Dependencies

To enable this parameter, set Element type set to Custom Microphone.
Polar pattern angles (deg) - Polar pattern response angles
[-180:180] (default) | real-valued -by-P row vector

Specify the polar pattern response angles, as a 1-by- $P$ vector. The angles are measured from the central pickup axis of the microphone and must be between $-180^{\circ}$ and $180^{\circ}$, inclusive.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.
Polar pattern (dB) - Custom microphone polar response
zeros ( 1,361 ) (default) | real-valued L-by-P matrix

Specify the magnitude of the custom microphone element polar patterns as an $L$-by- $P$ matrix. $L$ is the number of frequencies specified in Polar pattern frequencies ( $\mathbf{H z}$ ). $P$ is the number of angles specified in Polar pattern angles (deg). Each row of the matrix represents the magnitude of the polar pattern measured at the corresponding frequency specified in Polar pattern frequencies (Hz) and all angles specified in Polar pattern angles (deg). The pattern is measured in the azimuth plane. In the azimuth plane, the elevation angle is $0^{\circ}$ and the central pickup axis is $0^{\circ}$ degrees azimuth and $0^{\circ}$ degrees elevation. The polar pattern is symmetric around the central axis. You can construct the microphone response pattern in 3-D space from the polar pattern.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.

## Array Parameters

Geometry - Array geometry
ULA (default) | URA | UCA | Conformal Array

Array geometry, specified as one of

- ULA - Uniform linear array
- URA - Uniform rectangular array
- UCA - Uniform circular array
- Conformal Array - arbitrary element positions

Number of elements - Number of array elements
2 for ULA arrays and 5 for UCA arrays (default) | integer greater than or equal to 2

The number of array elements for ULA or UCA arrays, specified as an integer greater than or equal to 2.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

## Dependencies

To enable this parameter, set Geometry to ULA or UCA.
Element spacing (m) - Spacing between array elements
0.5 for ULA arrays and [0.5, 0.5] for URA arrays (default) | positive scalar for ULA or URA arrays | 2 -element vector of positive values for URA arrays

Spacing between adjacent array elements:

- ULA - specify the spacing between two adjacent elements in the array as a positive scalar.
- URA - specify the spacing as a positive scalar or a 1 -by-2 vector of positive values. If Element spacing (m) is a scalar, the row and column spacings are equal. If Element spacing (m) is a vector, the vector has the form [SpacingBetweenArrayRows,SpacingBetweenArrayColumns].
- When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.


## Dependencies

To enable this parameter, set Geometry to ULA or URA.
Array axis - Linear axis direction of ULA
$y$ (default) $|x| z$

Linear axis direction of ULA, specified as $y, x$, or $z$. All ULA array elements are uniformly spaced along this axis in the local array coordinate system.

## Dependencies

- To enable this parameter, set Geometry to ULA.
- This parameter is also enabled when the block only supports ULA arrays.

Array size - Dimensions of URA array

## [2,2] (default) | positive integer | 1-by-2 vector of positive integers

Dimensions of a URA array, specified as a positive integer or 1-by-2 vector of positive integers.

- If Array size is a 1-by-2 vector, the vector has the form [Number0fArrayRows, NumberOfArrayColumns].
- If Array size is an integer, the array has the same number of rows and columns.
- When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

For a URA, array elements are indexed from top to bottom along the leftmost column, and then continue to the next columns from left to right. In this figure, the Array size value of [3,2] creates an array having three rows and two columns.

## Size and Element Indexing Order

for Uniform Rectangular Arrays
Example: Size = [3,2]


## Dependencies

To enable this parameter, set Geometry to URA.
Element lattice - Lattice of URA element positions
Rectangular (default)|Triangular

Lattice of URA element positions, specified as Rectangular or Triangular.

- Rectangular - Aligns all the elements in row and column directions.
- Triangular - Shifts the even-row elements of a rectangular lattice toward the positive row-axis direction. The displacement is one-half the element spacing along the row dimension.


## Dependencies

To enable this parameter, set Geometry to URA.

Array normal - Array normal direction
$x$ for URA arrays or $z$ for UCA arrays (default) | y

Array normal direction, specified as $x, y$, or $z$.
Elements of planar arrays lie in a plane orthogonal to the selected array normal direction. Element boresight directions point along the array normal direction.

| Array Normal Parameter Value | Element Positions and Boresight Directions |
| :--- | :--- |
| $x$ | Array elements lie in the $y z$-plane. All element <br> boresight vectors point along the $x$-axis. |
| $y$ | Array elements lie in the $z x$-plane. All element <br> boresight vectors point along the $y$-axis. |
| $z$ | Array elements lie in the $x y$-plane. All element <br> boresight vectors point along the $z$-axis. |

## Dependencies

To enable this parameter, set Geometry to URA or UCA.
Radius of UCA (m) - UCA array radius
0.5 (default) | positive scalar

Radius of UCA array, specified as a positive scalar.

## Dependencies

To enable this parameter, set Geometry to UCA.
Element positions (m) - Positions of conformal array elements
[0;0;0] (default)| 3-by-Nmatrix of real values

Positions of the elements in a conformal array, specified as a 3 -by- $N$ matrix of real values, where $N$ is the number of elements in the conformal array. Each column of this matrix represents the position [ $x ; y ; z$ ] of an array element in the array local coordinate system. The origin of the local coordinate system is $(0,0,0)$. Units are in meters.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

## Dependencies

To enable this parameter set Geometry to Conformal Array.
Element normals (deg) - Direction of conformal array element normal vectors
[0;0] | 2-by-1 column vector | 2-by-N matrix

Direction of element normal vectors in a conformal array, specified as a 2-by-1 column vector or a 2-by- $N$ matrix. $N$ indicates the number of elements in the array. For a matrix, each column specifies the normal direction of the corresponding element in the form [azimuth; elevation] with respect to
the local coordinate system. The local coordinate system aligns the positive $x$-axis with the direction normal to the conformal array. If the parameter value is a 2 -by- 1 column vector, the same pointing direction is used for all array elements.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

You can use the Element positions (m) and Element normals (deg) parameters to represent any arrangement in which pairs of elements differ by certain transformations. The transformations can combine translation, azimuth rotation, and elevation rotation. However, you cannot use transformations that require rotation about the normal direction.

## Dependencies

To enable this parameter, set Geometry to Conformal Array.

## Taper - Array element tapers <br> 1 (default) | complex-valued scalar | complex-valued row vector

Element tapering, specified as a complex-valued scalar or a complex-valued 1-by- $N$ row vector. In this vector, $N$ represents the number of elements in the array.

Also known as element weights, tapers multiply the array element responses. Tapers modify both amplitude and phase of the response to reduce side lobes or steer the main response axis.

If Taper is a scalar, the same weight is applied to each element. If Taper is a vector, a weight from the vector is applied to the corresponding sensor element. The number of weights must match the number of elements of the array.

When you set Specify sensor array as to Replicated subarray, this parameter applies to each subarray.

Subarray definition matrix - Define elements belonging to subarrays
logical matrix

Specify the subarray selection as an $M$-by- $N$ matrix. $M$ is the number of subarrays and $N$ is the total number of elements in the array. Each row of the matrix represents a subarray and each entry in the row indicates when an element belongs to the subarray. When the entry is zero, the element does not belong the subarray. A nonzero entry represents a complex-valued weight applied to the corresponding element. Each row must contain at least one nonzero entry.

The phase center of each subarray lies at the subarray geometric center. The subarray geometric center depends on the Subarray definition matrix and Geometry parameters.

## Dependencies

To enable this parameter, set Specify sensor array as to Partitioned array.
Subarray steering method - Specify subarray steering method None (default) | Phase | Time

Subarray steering method, specified as one of

- None
- Phase
- Time
- Custom

Selecting Phase or Time opens the Steer input port on the Narrowband Receive Array, Narrowband Transmit Array, Wideband Receive Array, Wideband Transmit Array blocks, Constant Gamma Clutter, and GPU Constant Gamma Clutter blocks.

Selecting Custom opens the WS input port on the Narrowband Receive Array, Narrowband Transmit Array, Wideband Receive Array, Wideband Transmit Array blocks, Constant Gamma Clutter, and GPU Constant Gamma Clutter blocks.

## Dependencies

To enable this parameter, set Specify sensor array as to Partitioned array or Replicated subarray.

Phase shifter frequency (Hz) - Subarray phase shifting frequency
3.0e8 (default) | positive real-valued scalar

Operating frequency of subarray steering phase shifters, specified as a positive real-valued scalar. Units are Hz.

## Dependencies

To enable this parameter, set Sensor array to Partitioned array or Replicated subarray and set Subarray steering method to Phase.

Number of bits in phase shifters - Subarray steering phase shift quantization bits
0 (default) | non-negative integer

Subarray steering phase shift quantization bits, specified as a non-negative integer. A value of zero indicates that no quantization is performed.

## Dependencies

To enable this parameter, set Sensor array to Partitioned array or Replicated subarray and set Subarray steering method to Phase.

Subarrays layout - Subarray position specification
Rectangular (default) | Custom

Specify the layout of replicated subarrays as Rectangular or Custom.

- When you set this parameter to Rectangular, use the Grid size and Grid spacing parameters to place the subarrays.
- When you set this parameter to Custom, use the Subarray positions (m) and Subarray normals parameters to place the subarrays.


## Dependencies

To enable this parameter, set Sensor array to Replicated subarray
Grid size - Dimensions of rectangular subarray grid
[1,2] (default)

Rectangular subarray grid size, specified as a single positive integer, or a 1-by-2 row vector of positive integers.

If Grid size is an integer scalar, the array has an equal number of subarrays in each row and column. If Grid size is a 1 -by-2 vector of the form [NumberOfRows, NumberOfColumns], the first entry is the number of subarrays along each column. The second entry is the number of subarrays in each row. A row is along the local $y$-axis, and a column is along the local $z$-axis. The figure here shows how you can replicate a 3-by-2 URA subarray using a Grid size of [1,2].
$3 \times 2$ Element URA
Replicated on a $1 \times 2$ Grid


## Dependencies

To enable this parameter, set Sensor array to Replicated subarray and Subarrays layout to Rectangular.

Grid spacing ( $\mathbf{m}$ ) - Spacing between subarrays on rectangular grid Auto (default) | positive real-valued scalar | 1-by-2 vector of positive real-values

The rectangular grid spacing of subarrays, specified as a positive, real-valued scalar, a 1-by-2 row vector of positive, real-values, or Auto. Units are in meters.

- If Grid spacing is a scalar, the spacing along the row and the spacing along the column is the same.
- If Grid spacing is a 1-by-2 row vector, the vector has the form [SpacingBetweenRows,SpacingBetweenColumn]. The first entry specifies the spacing between rows along a column. The second entry specifies the spacing between columns along a row.
- If Grid spacing is set to Auto, replication preserves the element spacing of the subarray for both rows and columns while building the full array. This option is available only when you specify Geometry as ULA or URA.


## Dependencies

To enable this parameter, set Sensor array to Replicated subarray and Subarrays layout to Rectangular.

Subarray positions (m) - Positions of subarrays
[0,0;0.5,0.5;0,0] (default)|3-by- $N$ real-valued matrix

Positions of the subarrays in the custom grid, specified as a real 3-by- $N$ matrix, where $N$ is the number of subarrays in the array. Each column of the matrix represents the position of a single subarray in the array local coordinate system. The coordinates are expressed in the form [x; y; z]. Units are in meters.

## Dependencies

To enable this parameter, set Sensor array to Replicated subarray and Subarrays layout to Custom.

Subarray normals - Direction of subarray normal vectors
[0,0;0,0] (default) | 2-by- $N$ real matrix

Specify the normal directions of the subarrays in the array. This parameter value is a 2 -by- $N$ matrix, where $N$ is the number of subarrays in the array. Each column of the matrix specifies the normal direction of the corresponding subarray, in the form [azimuth; elevation]. Angle units are in degrees. Angles are defined with respect to the local coordinate system.

You can use the Subarray positions and Subarray normals parameters to represent any arrangement in which pairs of subarrays differ by certain transformations. The transformations can combine translation, azimuth rotation, and elevation rotation. However, you cannot use transformations that require rotation about the normal.

## Dependencies

To enable this parameter, set the Sensor array parameter to Replicated subarray and the Subarrays layout to Custom.

## Version History

Introduced in R2014b

See Also<br>phased.SubbandPhaseShiftBeamformer

# Time Delay Beamformer 

Time-delay beamformer


## Libraries:

Phased Array System Toolbox / Beamforming

## Description

The Time Delay Beamformer block performs delay-and-sum beamforming. Plane-wave signals arriving at the array elements are time-aligned and then summed. Time alignment is achieved by transforming the signals into the frequency domain and applying linear phase shifts corresponding to a time delay. The individual signals are then added and converted back to the time domain.

## Ports

Input
$\mathbf{X}$ - Input signal
$M$-by- $N$ complex-valued matrix
Input signal, specified as an $M$-by- $N$ matrix, where $M$ is the number of samples in the data, and $N$ is the number of array elements.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

## Data Types: double

Ang - Beamforming direction
2-by-1 real-valued vector
Beamforming direction, specified as a 2-by-1 real-valued vector. The vector takes the form of [AzimuthAngle;ElevationAngle]. Angle units are in degrees. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive, and the elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive. Angles are defined with respect to the local coordinate system of the array.

## Dependencies

To enable this port, set the Source of beamforming direction parameter to Input port.

## Data Types: double

## Output

Y - Beamformed output
$M$-by-1 complex-valued vector
Beamformed output, returned as an $M$-by- 1 complex-valued vector. The quantity $M$ is the number of signal samples.

## Data Types: double

W - Beamforming weights
$N$-by-1 complex-valued vector
Beamformed weights, returned as an $N$-by- 1 complex-valued vector. The quantity $N$ is the number of array elements. When the Specify sensor array as parameter is set to Partitioned array or Replicated subarray, $N$ represents the number of subarrays.

## Dependencies

To enable this port, select the Enable weights output checkbox.
Data Types: double

## Parameters

## Main tab

Signal propagation speed (m/s) - Signal propagation speed
physconst('LightSpeed') (default)| real-valued positive scalar

Signal propagation speed, specified as a real-valued positive scalar. The default value of the speed of light is the value returned by physconst('LightSpeed'). Units are in meters per second.

Example: 3e8
Data Types: double
Inherit sample rate - Inherit sample rate from upstream blocks
on (default) | off

Select this parameter to inherit the sample rate from upstream blocks. Otherwise, specify the sample rate using the Sample rate (Hz) parameter.

Data Types: Boolean
Sample rate (Hz) - Sampling rate of signal
1e6 (default) | positive real-valued scalar

Specify the signal sampling rate as a positive scalar. Units are in Hz.

## Dependencies

To enable this parameter, clear the Inherit sample rate check box.
Data Types: double
Source of beamforming direction - Source of beamforming direction
Property (default)|Input port

Source of beamforming direction, specified as Property or Input port. When you set Source of beamforming direction to Property, you then set the direction using the Beamforming
direction (deg) parameter. When you select Input port, the direction is determined by the input to the Ang port.

## Beamforming direction (deg) - Beamforming direction

2-by-1 real-valued vector

Beamforming direction, specified as a 2-by-1 real-valued vector taking the form
[AzimuthAngle;ElevationAngle]. Angle units are in degrees. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$. Angles are defined with respect to the local coordinate system of the array.

## Dependencies

To enable this parameter, set the Source of beamforming direction parameter to Property.
Enable weights output - Option to output beamformer weights
off (default) | on

Select this check box to obtain the beamformer weights from the output port, W.
Simulate using - Block simulation method
Interpreted Execution (default)|Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).

Programmatic Use
Block Parameter:SimulateUsing
Type:enum
Values:Interpreted Execution, Code Generation
Default:Interpreted Execution
Sensor Arrays Tab
Specify sensor array as - Method to specify array
Array (no subarrays) (default)|MATLAB expression

Method to specify array, specified as Array (no subarrays) or MATLAB expression.

- Array (no subarrays) - use the block parameters to specify the array.
- MATLAB expression - create the array using a MATLAB expression.

Expression - MATLAB expression used to create an array
Phased Array System Toolbox array System object

MATLAB expression used to create an array, specified as a valid Phased Array System Toolbox array System object.

Example: phased.URA('Size', [5, 3])

## Dependencies

To enable this parameter, set Specify sensor array as to MATLAB expression.

## Element Parameters

Element type - Array element types
Isotropic Antenna (default)|Cosine Antenna|Custom Antenna|Omni Microphone|
Custom Microphone

Antenna or microphone type, specified as one of the following:

- Isotropic Antenna
- Cosine Antenna
- Custom Antenna
- Omni Microphone
- Custom Microphone

Operating frequency range $(\mathbf{H z})$ - Operating frequency range of the antenna or microphone element
[0,1e20] (default) | real-valued 1-by-2 row vector

Specify the operating frequency range of the antenna or microphone element as a 1-by-2 row vector in the form [LowerBound, UpperBound]. The element has no response outside this frequency range. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Isotropic Antenna, Cosine Antenna, or Omni Microphone.

Operating frequency vector ( Hz ) - Operating frequency range of custom antenna or microphone elements
[0,1e20] (default) | real-valued row vector

Specify the frequencies at which to set antenna and microphone frequency responses as a 1-by-L row vector of increasing real values. The antenna or microphone element has no response outside the frequency range specified by the minimum and maximum elements of this vector. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone. Use Frequency responses (dB) to set the responses at these frequencies.

Baffle the back of the element - Set back response of an Isotropic Antenna element or an Omni Microphone element to zero off (default) | on

Select this check box to baffle the back response of the element. When back baffled, the responses at all azimuth angles beyond $\pm 90^{\circ}$ from broadside are set to zero. The broadside direction is defined as $0^{\circ}$ azimuth angle and $0^{\circ}$ elevation angle.

## Dependencies

To enable this check box, set Element type to Isotropic Antenna or Omni Microphone.
Exponent of cosine pattern - Exponents of azimuth and elevation cosine patterns [1.5 1.5] (default) | nonnegative scalar | real-valued 1-by-2 matrix of nonnegative values

Specify the exponents of the cosine pattern as a nonnegative scalar or a real-valued 1-by-2 matrix of nonnegative values. When Exponent of cosine pattern is a 1-by-2 vector, the first element is the exponent in the azimuth direction and the second element is the exponent in the elevation direction. When you set this parameter to a scalar, both the azimuth direction and elevation direction cosine patterns are raised to the same power.

## Dependencies

To enable this parameter, set Element type to Cosine Antenna.
Frequency responses (dB) - Antenna and microphone frequency response
[0,0] (default) | real-valued row vector

Frequency response of a custom antenna or custom microphone for the frequencies defined by the Operating frequency vector (Hz) parameter. The dimensions of Frequency responses (dB) must match the dimensions of the vector specified by the Operating frequency vector (Hz) parameter.

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone.
Input Pattern Coordinate System - Coordinate system of custom antenna pattern
az-el (default)| phi-theta

Coordinate system of custom antenna pattern, specified az-el or phi-theta. When you specify azel, use the Azimuth angles (deg) and Elevations angles (deg) parameters to specify the coordinates of the pattern points. When you specify phi-theta, use the Phi angles (deg) and Theta angles (deg) parameters to specify the coordinates of the pattern points.

## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Azimuth angles (deg) - Azimuth angles of antenna radiation pattern
[-180:180] (default) | real-valued row vector

Specify the azimuth angles at which to calculate the antenna radiation pattern as a 1-by-P row vector. $P$ must be greater than 2. Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to az-el.

Elevation angles (deg) - Elevation angles of antenna radiation pattern
[-90:90] (default) | real-valued row vector

Specify the elevation angles at which to compute the radiation pattern as a 1-by- $Q$ vector. $Q$ must be greater than 2. Angle units are in degrees. Elevation angles must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to az-el.

Phi Angles (deg) - Phi angle coordinates of custom antenna radiation pattern
$0: 360 \mid$ real-valued 1-by-P row vector

Phi angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by-P row vector. $P$ must be greater than 2 . Angle units are in degrees. Phi angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Theta Angles (deg) - Theta angle coordinates of custom antenna radiation pattern 0:180 | real-valued 1-by-Q row vector

Theta angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by$Q$ row vector. $Q$ must be greater than 2 . Angle units are in degrees. Theta angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Magnitude pattern (dB) - Magnitude of combined antenna radiation pattern
zeros $(181,361)$ (default) | real-valued $Q$-by- $P$ matrix | real-valued $Q$-by- $P$-by-L array

Magnitude of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector $(\mathbf{H z})$.

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector (Hz) parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (Hz) parameter.


## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Phase pattern (deg) - Custom antenna radiation phase pattern
zeros $(181,361)$ (default) | real-valued $Q$-by- $P$ matrix | real-valued $Q$-by- $P$-by-L array

Phase of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector ( $\mathbf{H z}$ ).

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (


## Dependencies

To enable this parameter, set Element type to Custom Antenna.
MatchArrayNormal - Rotate antenna element to array normal on (default) | off

Select this check box to rotate the antenna element pattern to align with the array normal. When not selected, the element pattern is not rotated.

When the antenna is used in an antenna array and the Input Pattern Coordinate System parameter is az-el, selecting this check box rotates the pattern so that the $x$-axis of the element coordinate system points along the array normal. Not selecting uses the element pattern without the rotation.

When the antenna is used in an antenna array and Input Pattern Coordinate System is set to phitheta, selecting this check box rotates the pattern so that the $z$-axis of the element coordinate system points along the array normal.

Use the parameter in conjunction with the Array normal parameter of the URA and UCA arrays.

## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Polar pattern frequencies (Hz) - Polar pattern microphone response frequencies
1 e3 (default) | real scalar | real-valued 1-by-L row vector

Polar pattern microphone response frequencies, specified as a real scalar, or a real-valued, 1-by-L vector. The response frequencies lie within the frequency range specified by the Operating
frequency vector $(\mathrm{Hz})$ vector.

## Dependencies

To enable this parameter, set Element type set to Custom Microphone.
Polar pattern angles (deg) - Polar pattern response angles
[-180:180] (default) | real-valued -by-P row vector

Specify the polar pattern response angles, as a 1-by- $P$ vector. The angles are measured from the central pickup axis of the microphone and must be between $-180^{\circ}$ and $180^{\circ}$, inclusive.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.
Polar pattern (dB) - Custom microphone polar response
zeros ( 1,361 ) (default) | real-valued $L$-by- $P$ matrix

Specify the magnitude of the custom microphone element polar patterns as an $L$-by- $P$ matrix. $L$ is the number of frequencies specified in Polar pattern frequencies ( $\mathbf{H z}$ ). $P$ is the number of angles
specified in Polar pattern angles (deg). Each row of the matrix represents the magnitude of the polar pattern measured at the corresponding frequency specified in Polar pattern frequencies (Hz) and all angles specified in Polar pattern angles (deg). The pattern is measured in the azimuth plane. In the azimuth plane, the elevation angle is $0^{\circ}$ and the central pickup axis is $0^{\circ}$ degrees azimuth and $0^{\circ}$ degrees elevation. The polar pattern is symmetric around the central axis. You can construct the microphone response pattern in 3-D space from the polar pattern.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.

## Array Parameters

Geometry - Array geometry
ULA (default) | URA | UCA | Conformal Array

Array geometry, specified as one of

- ULA - Uniform linear array
- URA - Uniform rectangular array
- UCA - Uniform circular array
- Conformal Array - arbitrary element positions

Number of elements - Number of array elements
2 for ULA arrays and 5 for UCA arrays (default) | integer greater than or equal to 2

The number of array elements for ULA or UCA arrays, specified as an integer greater than or equal to 2.

## Dependencies

To enable this parameter, set Geometry to ULA or UCA.
Element spacing (m) - Spacing between array elements
0.5 for ULA arrays and [0.5, 0.5] for URA arrays (default) | positive scalar for ULA or URA arrays | 2 -element vector of positive values for URA arrays

Spacing between adjacent array elements:

- ULA - specify the spacing between two adjacent elements in the array as a positive scalar.
- URA - specify the spacing as a positive scalar or a 1 -by-2 vector of positive values. If Element spacing (m) is a scalar, the row and column spacings are equal. If Element spacing (m) is a vector, the vector has the form [SpacingBetweenArrayRows,SpacingBetweenArrayColumns].


## Dependencies

To enable this parameter, set Geometry to ULA or URA.
Array axis - Linear axis direction of ULA
$y$ (default) $|x| z$

Linear axis direction of ULA, specified as $y, x$, or $z$. All ULA array elements are uniformly spaced along this axis in the local array coordinate system.

## Dependencies

- To enable this parameter, set Geometry to ULA.
- This parameter is also enabled when the block only supports ULA arrays.

Array size - Dimensions of URA array

## [2,2] (default) | positive integer | 1-by-2 vector of positive integers

Dimensions of a URA array, specified as a positive integer or 1-by-2 vector of positive integers.

- If Array size is a 1 -by- 2 vector, the vector has the form [NumberOfArrayRows, NumberOfArrayColumns].
- If Array size is an integer, the array has the same number of elements in each row and column.

For a URA, array elements are indexed from top to bottom along the leftmost array column, and continued to the next columns from left to right. In this figure, the Array size value of [3, 2] creates an array having three rows and two columns.

## Size and Element Indexing Order

for Uniform Rectangular Arrays
Example: Size $=[3,2]$


## Dependencies

To enable this parameter, set Geometry to URA.
Element lattice - Lattice of URA element positions
Rectangular (default) |Triangular

Lattice of URA element positions, specified as Rectangular or Triangular.

- Rectangular - Aligns all the elements in row and column directions.
- Triangular - Shifts the even-row elements of a rectangular lattice toward the positive row-axis direction. The displacement is one-half the element spacing along the row dimension.


## Dependencies

To enable this parameter, set Geometry to URA.
Array normal - Array normal direction
$x$ for URA arrays or $z$ for UCA arrays (default) | y

Array normal direction, specified as $x, y$, or $z$.
Elements of planar arrays lie in a plane orthogonal to the selected array normal direction. Element boresight directions point along the array normal direction.

| Array Normal Parameter Value | Element Positions and Boresight Directions |
| :--- | :--- |
| x | Array elements lie in the $y z$-plane. All element <br> boresight vectors point along the $x$-axis. |
| y | Array elements lie in the $z x$-plane. All element <br> boresight vectors point along the $y$-axis. |
| $z$ | Array elements lie in the $x y$-plane. All element <br> boresight vectors point along the $z$-axis. |

## Dependencies

To enable this parameter, set Geometry to URA or UCA.
Radius of UCA (m) - UCA array radius
0.5 (default) | positive scalar

Radius of UCA array, specified as a positive scalar.

## Dependencies

To enable this parameter, set Geometry to UCA.

## Element positions (m) - Positions of conformal array elements <br> [0;0;0] (default) | 3-by-Nmatrix of real values

Positions of the elements in a conformal array, specified as a 3 -by- $N$ matrix of real values, where $N$ is the number of elements in the conformal array. Each column of this matrix represents the position [ $x ; y ; z$ ] of an array element in the array local coordinate system. The origin of the local coordinate system is ( $0,0,0$ ). Units are in meters.

## Dependencies

To enable this parameter set Geometry to Conformal Array.

## Data Types: double

Element normals (deg) - Direction of conformal array element normal vectors
[0;0] | 2-by-1 column vector | 2-by-N matrix

Direction of element normal vectors in a conformal array, specified as a 2 -by- 1 column vector or a 2 -by- $N$ matrix. $N$ indicates the number of elements in the array. If the parameter value is a matrix, each
column specifies the normal direction of the corresponding element in the form [azimuth;elevation] with respect to the local coordinate system. The local coordinate system aligns the positive $x$-axis with the direction normal to the conformal array. If the parameter value is a 2-by-1 column vector, the same pointing direction is used for all array elements.

You can use the Element positions (m) and Element normals (deg) parameters to represent any arrangement in which pairs of elements differ by certain transformations. The transformations can combine translation, azimuth rotation, and elevation rotation. However, you cannot use transformations that require rotation about the normal direction.

To enable this parameter, set Geometry to Conformal Array.
Data Types: double
Taper - Array element tapers
1 (default) | complex scalar | complex-valued row vector

Specify element tapering as a complex-valued scalar or a complex-valued 1-by- $N$ row vector. In this vector, $N$ represents the number of elements in the array.

Also known as element weights, tapers multiply the array element responses. Tapers modify both amplitude and phase of the response to reduce side lobes or steer the main response axis.

If Taper is a scalar, the same weight is applied to each element. If Taper is a vector, a weight from the vector is applied to the corresponding sensor element. The number of weights must match the number of elements of the array.

Data Types: double

## Version History <br> Introduced in R2014b

## See Also

phased.TimeDelayBeamformer

# Time Delay LCMV Beamformer 

Time delay LCMV beamformer


## Libraries:

Phased Array System Toolbox / Beamforming

## Description

The Time Delay LCMV Beamformer block performs time-delay linear constraint minimum variance (LCMV) beamforming.

## Ports

Input
$\mathbf{X}$ - Input signal
$M$-by- $N$ complex-valued matrix
Input signal, specified as an $M$-by- $N$ matrix, where $M$ is the number of samples in the data, and $N$ is the number of array elements.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
Data Types: double
XT - Training signal
$M$-by- $N$ complex-valued matrix
Input signal, specified as an $M$-by- $N$ matrix, where $M$ is the number of samples in the data, and $N$ is the number of array elements.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

## Dependencies

To enable this port, select the Enable training data input check box.
Data Types: double
Ang - Beamforming direction
2-by-1 real-valued vector
Beamforming direction, specified as a 2 -by-1 real-valued matrix taking the form of [AzimuthAngle;ElevationAngle]. Angle units are in degrees. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive, and the elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive. Angles are defined with respect to the local coordinate system of the array.

## Dependencies

To enable this port, set the Source of beamforming direction parameter to Input port.
Data Types: double

## Output

Y - Beamformed output
M-by-1 complex-valued vector
Beamformed output, returned as an $M$-by- 1 complex-valued vector. The quantity $M$ is the number of signal samples.

Data Types: double
W - Beamforming weights
$N$-by-1 complex-valued vector
Beamformed weights, returned as an $N$-by-1 complex-valued vector. The quantity $N$ is the number of array elements. When the Specify sensor array as parameter is set to Partitioned array or Replicated subarray, $N$ represents the number of subarrays.

## Dependencies

To enable this port, select the Enable weights output checkbox.
Data Types: double

## Parameters

## Main tab

Signal propagation speed (m/s) - Signal propagation speed
physconst('LightSpeed') (default)|real-valued positive scalar

Signal propagation speed, specified as a real-valued positive scalar. The default value of the speed of light is the value returned by physconst('LightSpeed '). Units are in meters per second.

## Example: 3e8

Data Types: double
Inherit sample rate - Inherit sample rate from upstream blocks
on (default) | off

Select this parameter to inherit the sample rate from upstream blocks. Otherwise, specify the sample rate using the Sample rate (Hz) parameter.
Data Types: Boolean
Sample rate (Hz) - Sampling rate of signal
le6 (default) | positive real-valued scalar

Specify the signal sampling rate as a positive scalar. Units are in Hz .

## Dependencies

To enable this parameter, clear the Inherit sample rate check box.
Data Types: double
FIR filter length - FIR filter length
1 (default) | positive integer

The length of the FIR filter used to process each sensor element data, specified as a positive integer.
Data Types: double
Constraint matrix - Constraint matrix used for time-delay LCMV beamformer
[1;1] | complex-valued $M$-by- $K$ matrix

The constraint matrix used for time-delay LCMV beamformer, specified as a complex-valuedM-by-K matrix. Each column of the matrix is a constraint and $M$ is the degrees of freedom of the beamformer. For a time delay LCMV beamformer, $M$ is given by the product of the number of elements of the array and the value of the FIR filter length parameter.
Data Types: double
Desired response vector - Desired response of time-delay LCMV beamformer
1 (default) | $K$ column vector

Desired response used for time-delay LCMV beamformer, specified as a length- $K$ column vector. $K$ is the number of constraints in the Constraint matrix parameter. Each element in the vector defines the desired response of the constraint specified in the corresponding column of the Constraint matrix parameter matrix.

Diagonal loading factor - Diagonal loading factor for stability
nonnegative scalar

Specify the diagonal loading factor as a nonnegative scalar. Diagonal loading is a technique used to achieve robust beamforming performance, especially when the sample support is small.

Enable training data input - Enable the use of training data
off (default) | on

Select this check box to specify additional training data via the input port XT. To use the input signal as the training data, clear the check box which removes the port.

Source of beamforming direction - Source of beamforming direction
Property (default)|Input port

Source of beamforming direction, specified as Property or Input port. When you set Source of beamforming direction to Property, you then set the direction using the Beamforming direction (deg) parameter. When you select Input port, the direction is determined by the input to the Ang port.

## Beamforming direction (deg) - Beamforming direction

2-by-1 real-valued vector

Beamforming direction, specified as a 2 -by-1 real-valued vector taking the form
[AzimuthAngle;ElevationAngle]. Angle units are in degrees. The azimuth angle must lie between $-180^{\circ}$ and $180^{\circ}$. The elevation angle must lie between $-90^{\circ}$ and $90^{\circ}$. Angles are defined with respect to the local coordinate system of the array.

## Dependencies

To enable this parameter, set the Source of beamforming direction parameter to Property.
Enable weights output - Option to output beamformer weights
off (default) | on

Select this check box to obtain the beamformer weights from the output port, W .
Simulate using - Block simulation method
Interpreted Execution (default)|Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).

## Programmatic Use <br> Block Parameter:SimulateUsing

```
Type:enum
Values:Interpreted Execution, Code Generation
Default:Interpreted Execution
Sensor Arrays Tab
Specify sensor array as - Method to specify array
Array (no subarrays) (default)|MATLAB expression
```

Method to specify array, specified as Array (no subarrays) or MATLAB expression.

- Array (no subarrays) - use the block parameters to specify the array.
- MATLAB expression - create the array using a MATLAB expression.

Expression - MATLAB expression used to create an array
Phased Array System Toolbox array System object

MATLAB expression used to create an array, specified as a valid Phased Array System Toolbox array System object.

Example: phased.URA('Size', [5,3])

## Dependencies

To enable this parameter, set Specify sensor array as to MATLAB expression.

## Element Parameters

Element type - Array element types
Isotropic Antenna (default)|Cosine Antenna|Custom Antenna|Omni Microphone| Custom Microphone

Antenna or microphone type, specified as one of the following:

- Isotropic Antenna
- Cosine Antenna
- Custom Antenna
- Omni Microphone
- Custom Microphone

Operating frequency range $(\mathbf{H z})$ - Operating frequency range of the antenna or microphone element
[0,1e20] (default) | real-valued 1-by-2 row vector

Specify the operating frequency range of the antenna or microphone element as a 1-by-2 row vector in the form [LowerBound, UpperBound]. The element has no response outside this frequency range. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Isotropic Antenna, Cosine Antenna, or Omni Microphone.

Operating frequency vector ( Hz ) - Operating frequency range of custom antenna or microphone elements
[0,1e20] (default) | real-valued row vector

Specify the frequencies at which to set antenna and microphone frequency responses as a 1-by-L row vector of increasing real values. The antenna or microphone element has no response outside the frequency range specified by the minimum and maximum elements of this vector. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone. Use Frequency responses (dB) to set the responses at these frequencies.

Baffle the back of the element - Set back response of an Isotropic Antenna element or an Omni Microphone element to zero off (default) | on

Select this check box to baffle the back response of the element. When back baffled, the responses at all azimuth angles beyond $\pm 90^{\circ}$ from broadside are set to zero. The broadside direction is defined as $0^{\circ}$ azimuth angle and $0^{\circ}$ elevation angle.

## Dependencies

To enable this check box, set Element type to Isotropic Antenna or Omni Microphone.
Exponent of cosine pattern - Exponents of azimuth and elevation cosine patterns [1.5 1.5] (default)| nonnegative scalar | real-valued 1-by-2 matrix of nonnegative values

Specify the exponents of the cosine pattern as a nonnegative scalar or a real-valued 1-by-2 matrix of nonnegative values. When Exponent of cosine pattern is a 1-by-2 vector, the first element is the exponent in the azimuth direction and the second element is the exponent in the elevation direction. When you set this parameter to a scalar, both the azimuth direction and elevation direction cosine patterns are raised to the same power.

## Dependencies

To enable this parameter, set Element type to Cosine Antenna.
Frequency responses (dB) - Antenna and microphone frequency response
[0,0] (default) | real-valued row vector

Frequency response of a custom antenna or custom microphone for the frequencies defined by the Operating frequency vector ( Hz ) parameter. The dimensions of Frequency responses (dB) must match the dimensions of the vector specified by the Operating frequency vector ( $\mathbf{H z}$ ) parameter.

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone.
Input Pattern Coordinate System - Coordinate system of custom antenna pattern
az-el (default)| phi-theta

Coordinate system of custom antenna pattern, specified az-el or phi-theta. When you specify azel, use the Azimuth angles (deg) and Elevations angles (deg) parameters to specify the coordinates of the pattern points. When you specify phi-theta, use the Phi angles (deg) and Theta angles (deg) parameters to specify the coordinates of the pattern points.

## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Azimuth angles (deg) - Azimuth angles of antenna radiation pattern
[-180:180] (default) | real-valued row vector

Specify the azimuth angles at which to calculate the antenna radiation pattern as a 1 -by- $P$ row vector. $P$ must be greater than 2. Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to az-el.

Elevation angles (deg) - Elevation angles of antenna radiation pattern
[-90:90] (default) | real-valued row vector

Specify the elevation angles at which to compute the radiation pattern as a 1-by- $Q$ vector. $Q$ must be greater than 2. Angle units are in degrees. Elevation angles must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to az-el.

Phi Angles (deg) - Phi angle coordinates of custom antenna radiation pattern
$0: 360 \mid$ real-valued 1-by-P row vector

Phi angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by- $P$ row vector. $P$ must be greater than 2 . Angle units are in degrees. Phi angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Theta Angles (deg) - Theta angle coordinates of custom antenna radiation pattern 0:180 | real-valued 1-by-Q row vector

Theta angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by$Q$ row vector. $Q$ must be greater than 2 . Angle units are in degrees. Theta angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Magnitude pattern (dB) - Magnitude of combined antenna radiation pattern
zeros $(181,361)$ (default) | real-valued $Q$-by- $P$ matrix | real-valued $Q$-by- $P$-by- $L$ array

Magnitude of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector $(\mathbf{H z})$.

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector (Hz) parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (Hz) parameter.


## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Phase pattern (deg) - Custom antenna radiation phase pattern
zeros $(181,361)$ (default) | real-valued $Q$-by- $P$ matrix | real-valued $Q$-by- $P$-by-L array

Phase of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector ( $\mathbf{H z}$ ).

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (


## Dependencies

To enable this parameter, set Element type to Custom Antenna.
MatchArrayNormal - Rotate antenna element to array normal on (default) | off

Select this check box to rotate the antenna element pattern to align with the array normal. When not selected, the element pattern is not rotated.

When the antenna is used in an antenna array and the Input Pattern Coordinate System parameter is az-el, selecting this check box rotates the pattern so that the $x$-axis of the element coordinate system points along the array normal. Not selecting uses the element pattern without the rotation.

When the antenna is used in an antenna array and Input Pattern Coordinate System is set to phitheta, selecting this check box rotates the pattern so that the $z$-axis of the element coordinate system points along the array normal.

Use the parameter in conjunction with the Array normal parameter of the URA and UCA arrays.

## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Polar pattern frequencies (Hz) - Polar pattern microphone response frequencies
1e3 (default) | real scalar | real-valued 1-by-L row vector

Polar pattern microphone response frequencies, specified as a real scalar, or a real-valued, 1-by-L vector. The response frequencies lie within the frequency range specified by the Operating
frequency vector $(\mathrm{Hz})$ vector.

## Dependencies

To enable this parameter, set Element type set to Custom Microphone.
Polar pattern angles (deg) - Polar pattern response angles
[-180:180] (default) | real-valued -by-P row vector

Specify the polar pattern response angles, as a 1-by- $P$ vector. The angles are measured from the central pickup axis of the microphone and must be between $-180^{\circ}$ and $180^{\circ}$, inclusive.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.
Polar pattern (dB) - Custom microphone polar response
zeros ( 1,361 ) (default) | real-valued $L$-by- $P$ matrix

Specify the magnitude of the custom microphone element polar patterns as an $L$-by- $P$ matrix. $L$ is the number of frequencies specified in Polar pattern frequencies $\mathbf{( H z )} . P$ is the number of angles
specified in Polar pattern angles (deg). Each row of the matrix represents the magnitude of the polar pattern measured at the corresponding frequency specified in Polar pattern frequencies (Hz) and all angles specified in Polar pattern angles (deg). The pattern is measured in the azimuth plane. In the azimuth plane, the elevation angle is $0^{\circ}$ and the central pickup axis is $0^{\circ}$ degrees azimuth and $0^{\circ}$ degrees elevation. The polar pattern is symmetric around the central axis. You can construct the microphone response pattern in 3-D space from the polar pattern.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.

## Array Parameters

Geometry - Array geometry
ULA (default) | URA | UCA | Conformal Array

Array geometry, specified as one of

- ULA - Uniform linear array
- URA - Uniform rectangular array
- UCA - Uniform circular array
- Conformal Array - arbitrary element positions

Number of elements - Number of array elements
2 for ULA arrays and 5 for UCA arrays (default) | integer greater than or equal to 2

The number of array elements for ULA or UCA arrays, specified as an integer greater than or equal to 2.

## Dependencies

To enable this parameter, set Geometry to ULA or UCA.
Element spacing (m) - Spacing between array elements
0.5 for ULA arrays and [0.5,0.5] for URA arrays (default) | positive scalar for ULA or URA arrays | 2 -element vector of positive values for URA arrays

Spacing between adjacent array elements:

- ULA - specify the spacing between two adjacent elements in the array as a positive scalar.
- URA - specify the spacing as a positive scalar or a 1 -by-2 vector of positive values. If Element spacing (m) is a scalar, the row and column spacings are equal. If Element spacing (m) is a vector, the vector has the form [SpacingBetweenArrayRows, SpacingBetweenArrayColumns].


## Dependencies

To enable this parameter, set Geometry to ULA or URA.
Array axis - Linear axis direction of ULA
$y$ (default) $|x| z$

Linear axis direction of ULA, specified as $y$, $x$, or $z$. All ULA array elements are uniformly spaced along this axis in the local array coordinate system.

## Dependencies

- To enable this parameter, set Geometry to ULA.
- This parameter is also enabled when the block only supports ULA arrays.

Array size - Dimensions of URA array
[2,2] (default) | positive integer | 1-by-2 vector of positive integers

Dimensions of a URA array, specified as a positive integer or 1-by-2 vector of positive integers.

- If Array size is a 1 -by- 2 vector, the vector has the form [NumberOfArrayRows, NumberOfArrayColumns].
- If Array size is an integer, the array has the same number of elements in each row and column.

For a URA, array elements are indexed from top to bottom along the leftmost array column, and continued to the next columns from left to right. In this figure, the Array size value of [3, 2] creates an array having three rows and two columns.

## Size and Element Indexing Order

for Uniform Rectangular Arrays
Example: Size $=[3,2]$


## Dependencies

To enable this parameter, set Geometry to URA.
Element lattice - Lattice of URA element positions
Rectangular (default) | Triangular

Lattice of URA element positions, specified as Rectangular or Triangular.

- Rectangular - Aligns all the elements in row and column directions.
- Triangular - Shifts the even-row elements of a rectangular lattice toward the positive row-axis direction. The displacement is one-half the element spacing along the row dimension.


## Dependencies

To enable this parameter, set Geometry to URA.
Array normal - Array normal direction
$x$ for URA arrays or $z$ for UCA arrays (default) | y

Array normal direction, specified as $x, y$, or $z$.
Elements of planar arrays lie in a plane orthogonal to the selected array normal direction. Element boresight directions point along the array normal direction.

| Array Normal Parameter Value | Element Positions and Boresight Directions |
| :--- | :--- |
| $x$ | Array elements lie in the $y z$-plane. All element <br> boresight vectors point along the $x$-axis. |
| $y$ | Array elements lie in the $z x$-plane. All element <br> boresight vectors point along the $y$-axis. |
| $z$ | Array elements lie in the $x y$-plane. All element <br> boresight vectors point along the $z$-axis. |

## Dependencies

To enable this parameter, set Geometry to URA or UCA.
Radius of UCA (m) - UCA array radius
0.5 (default) | positive scalar

Radius of UCA array, specified as a positive scalar.

## Dependencies

To enable this parameter, set Geometry to UCA.

```
Element positions (m) - Positions of conformal array elements
[0;0;0] (default)|3-by-Nmatrix of real values
```

Positions of the elements in a conformal array, specified as a 3 -by- $N$ matrix of real values, where $N$ is the number of elements in the conformal array. Each column of this matrix represents the position [ $x ; y ; z$ ] of an array element in the array local coordinate system. The origin of the local coordinate system is ( $0,0,0$ ). Units are in meters.

## Dependencies

To enable this parameter set Geometry to Conformal Array.

## Data Types: double

Element normals (deg) - Direction of conformal array element normal vectors
[0;0] | 2-by-1 column vector | 2-by-N matrix

Direction of element normal vectors in a conformal array, specified as a 2-by-1 column vector or a 2-by- $N$ matrix. $N$ indicates the number of elements in the array. If the parameter value is a matrix, each
column specifies the normal direction of the corresponding element in the form [azimuth;elevation] with respect to the local coordinate system. The local coordinate system aligns the positive $x$-axis with the direction normal to the conformal array. If the parameter value is a 2-by-1 column vector, the same pointing direction is used for all array elements.

You can use the Element positions (m) and Element normals (deg) parameters to represent any arrangement in which pairs of elements differ by certain transformations. The transformations can combine translation, azimuth rotation, and elevation rotation. However, you cannot use transformations that require rotation about the normal direction.

To enable this parameter, set Geometry to Conformal Array.
Data Types: double
Taper - Array element tapers
1 (default) | complex scalar | complex-valued row vector

Specify element tapering as a complex-valued scalar or a complex-valued 1-by- $N$ row vector. In this vector, $N$ represents the number of elements in the array.

Also known as element weights, tapers multiply the array element responses. Tapers modify both amplitude and phase of the response to reduce side lobes or steer the main response axis.

If Taper is a scalar, the same weight is applied to each element. If Taper is a vector, a weight from the vector is applied to the corresponding sensor element. The number of weights must match the number of elements of the array.

Data Types: double

## Version History <br> Introduced in R2014b

## See Also

phased.TimeDelayLCMVBeamformer

## Time Varying Gain

Time varying gain (TVG) control


## Libraries:

Phased Array System Toolbox / Detection

## Description

The Time Varying Gain block applies a time-varying gain to input signals to compensate for geometric range loss at each range gate. Time varying gain (TVG) is sometimes called automatic gain control (AGC).

## Ports

Input
Port_1 - Input signal
vector | matrix
Input signal, specified as a vector or matrix.
The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
Data Types: double | single
Port_2 - Range loss
column vector
Range loss, specified as a column vector. The length of p must be equal to or greater than the number of rows of $X$.

The process equalizes power levels across all samples to match a given reference range. The compensated signal is returned in Y . X can be a column vector, a matrix, or a cube. The gain is applied to each column in $X$ independently. The number of rows in $X$ cannot exceed the length of the loss vector specified in the RangeLoss property. $Y$ has the same dimensionality as $X$. $X$ can be single or double precision.

## Dependencies

To enable this port, set Source of range losses parameter to Input port.

## Data Types: double | single

## Output

Port_1 - Range-compensated input signal
vector | matrix

Range-compensated Input signal, returned as a vector or matrix. The output has the same size as the input signal.

## Data Types: double | single

## Parameters

Source of range losses - Source of range losses
Property (default)|Input Port
Range loss source, specified as Property or Input Port.

| Property | Range losses are specified by the Range loss (dB) <br> parameter. |
| :--- | :--- |
| Input port | Range losses are specified using the input port L. |

Range losses (dB) - Loss at each input sample range
0 (default)
Loss at each input sample range, specified as a vector - elements correspond to the samples in the input signal. Units are in dB.

Reference range loss (dB) - Loss at reference range
0 (default)
Specify the loss at a given reference range as a scalar. Units are in dB .
Simulate using - Block simulation method
Interpreted Execution (default)|Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).
Programmatic Use
Block Parameter:SimulateUsing
Type:enum
Values:Interpreted Execution, Code Generation
Default:Interpreted Execution

## Version History

Introduced in R2014b

## See Also

phased.TimeVaryingGain

## Transmitter

Amplify and transmit a signal


## Libraries:

Phased Array System Toolbox / Transmitters and Receivers

## Description

The Transmitter block amplifies and transmits waveform pulses. The transmitter can either maintain coherence between pulses or insert phase noise.

## Ports

Input
Input 1 - Input signal
complex-valued vector
Input signal, specified as a complex-valued vector.
Data Types: double

## Output

$\mathbf{Y}$ - Transmitted signal
complex-valued vector
Transmitted signal, returned as a complex-valued vector. The transmitted signal is the amplified input signal Input 1 where the amplification is based on the characteristics of the transmitter, such as the peak power and the gain.
Data Types: double
TR — Transmitter status
logical vector
Transmitter status, output as a logical vector where true indicates the transmitter is on for the corresponding sample time, and false indicates the transmitter is off.

## Dependencies

To enable this port, select the Enable transmitter status output check box.
Data Types: double
Ph - Output phase noise
vector
Added phase noise, output as a vector. Random phase noise added to each transmitted sample. PHNOISE is a vector which has the same dimension as Y. Each element in PHNOISE contains the random phase between 0 and $2 *$ pi, added to the corresponding sample in Y by the transmitter.

## Dependencies

To enable this port, select the Enable pulse phase noise output check box and deselect the Preserve coherence among pulses check box.

Data Types: double

## Parameters

Peak power (W) - Peak power
5000 (default) | positive scalar
Transmitted peak power, specified as a positive scalar. Units are in Watts.
Gain (dB) - Transmitter gain
20 (default) | scalar
Transmit gain, specified as a scalar. Units are in dB.
Loss factor (dB) - Loss factor
0 (default)
Transmit loss factor, specified as a nonnegative scalar. Units are in dB.
Enable transmitter status output - Enable transmitter status output
off (default) | on
Select this check box to send the transmitter-in-use status for each output sample from the output port TR. From the output port, a 1 indicates that the transmitter is on, and a 0 indicates that the transmitter is off.

Preserve coherence among pulses - Preserve coherence among pulses
on (default) | off
Select this check box to preserve coherence among transmitted pulses. When you select this box, the transmitter does not introduce any random phases to the output pulses. When you clear this box, the transmitter adds a random phase noise to each transmitted pulse. The random phase noise is introduced by multiplying the pulse value by $e^{i \phi}$ where $\phi$ is a uniform random variable on the interval [0,2п].

Enable pulse phase noise output - Enable pulse phase noise output
off (default) | on
Select this check box to create an output port, Ph , with the output sample's random phase noise introduced if Preserve coherence among pulses is cleared. The output port can be directed to a receiver to simulate coherent-on-receive systems.

## Dependencies

This check box appears only when Preserve coherence among pulses is deselected.

## Simulate using - Block simulation method <br> Interpreted Execution (default)|Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).
Programmatic Use
Block Parameter:SimulateUsing
Type:enum
Values:Interpreted Execution, Code Generation
Default:Interpreted Execution

## Version History

## Introduced in R2014b

## See Also

phased.Transmitter

## ULA Beamscan Spectrum

Beamscan spatial spectrum estimator for ULA

## Libraries:

Phased Array System Toolbox / Direction of Arrival

## Description

The ULA Beamscan Spectrum block estimates the spatial spectrum of incoming narrowband signals by scanning a region of broadside angles using a narrowband conventional beamformer applied to a uniform linear array. The block optionally calculates the direction of arrival of a specified number of signals by estimating peaks of the spectrum.

## Ports

Input
Port 1 - Received signal
$M$-by- $N$ complex-valued matrix
Received signal, specified as an $M$-by- $N$ complex-valued matrix. The quantity $M$ is the number of sample values (snapshots) contained in the signal and $N$ is the number of sensor elements in the array.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
Data Types: double

## Output

$\mathbf{Y}$ - Beamscan spatial spectrum
non-negative, real-valued column vector
Beamscan spatial spectrum, returned as a non-negative, real-valued column vector representing the magnitude of the estimated beamscan spatial spectrum. Each entry corresponds to an angle specified by the Scan angles (deg) parameter.

## Data Types: double

Ang - Directions of arrival
non-negative, real-valued column vector
Directions of arrival of the signals, returned as a real-valued row vector. The direction of arrival angle is the broadside angle between the source direction and the array axis. Angle units are in degrees. The length of the vector is the number of signals specified by the Number of signals parameter. If the object cannot identify peaks in the spectrum, it will return NaN .

## Dependencies

To enable this output port, select the Enable DOA output check box.
Data Types: double

## Parameters

Signal propagation speed (m/s) - Signal propagation speed
physconst('LightSpeed') (default)| real-valued positive scalar

Signal propagation speed, specified as a real-valued positive scalar. The default value of the speed of light is the value returned by physconst('LightSpeed'). Units are in meters per second.

## Example: 3e8

Data Types: double
Operating frequency $(\mathbf{H z})$ - System operating frequency
3e8 (default) | positive real scalar

System operating frequency, specified as a positive scalar. Units are in Hz .
Number of bits in phase shifters - Number of phase shift quantization bits
0 (default) | nonnegative integer

The number of bits used to quantize the phase shift component of beamformer or steering vector weights. Specify the number of bits as a non-negative integer. A value of zero indicates that no quantization is performed.

Forward-backward averaging - Enable forward-backward averaging
off (default) | on

Select this parameter to use forward-backward averaging to estimate the covariance matrix for sensor arrays with a conjugate symmetric array manifold structure.

Spatial smoothing - Enable spatial smoothing
0 (default) | non-negative integer

Specify the amount of averaging used by spatial smoothing to estimate the covariance matrix as a nonnegative integer. Each increase in smoothing handles one extra coherent source, but reduces the effective number of elements by one. The maximum value of this parameter is $N-2$, where $N$ is the number of sensors in the ULA.

Scan angles (deg) - Search angles for spectrum peaks
-90:90 (default) | real-valued row vector

Specify the scan angles in degrees as a real-valued row vector. The angles are array broadside angles and must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive. You must specify the angles in increasing order.

Enable DOA output - Output directions of arrival through output port
off (default) | on

Select this parameter to output the signals directions of arrival (DOA) through the Ang output port.
Number of signals - Expected number of arriving signals
1 (default) | positive integer

Specify the expected number of signals for DOA estimation as a positive scalar integer.

## Dependencies

To enable this parameter, select the Enable DOA output check box.
Data Types: double
Simulate using - Block simulation method
Interpreted Execution (default)|Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted | The block executes <br> Execution <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).

```
Programmatic Use
Block Parameter:SimulateUsing
Type:enum
```

Values:Interpreted Execution, Code Generation
Default:Interpreted Execution
Sensor Array Tab
Specify sensor array as - Method to specify array
Array (no subarrays) (default)|MATLAB expression

Method to specify array, specified as Array (no subarrays) or MATLAB expression.

- Array (no subarrays) - use the block parameters to specify the array.
- MATLAB expression - create the array using a MATLAB expression.

Expression - MATLAB expression used to create an array
Phased Array System Toolbox array System object

MATLAB expression used to create an array, specified as a valid Phased Array System Toolbox array System object.
Example: phased.URA('Size', [5, 3])
Dependencies
To enable this parameter, set Specify sensor array as to MATLAB expression.

## Element Parameters

Element type - Array element types
Isotropic Antenna (default)|Cosine Antenna|Custom Antenna|Omni Microphone| Custom Microphone

Antenna or microphone type, specified as one of the following:

- Isotropic Antenna
- Cosine Antenna
- Custom Antenna
- Omni Microphone
- Custom Microphone

Operating frequency range $(\mathbf{H z})$ - Operating frequency range of the antenna or microphone element
[0, 1e20] (default) | real-valued 1-by-2 row vector

Specify the operating frequency range of the antenna or microphone element as a 1-by-2 row vector in the form [LowerBound, UpperBound]. The element has no response outside this frequency range. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Isotropic Antenna, Cosine Antenna, or Omni Microphone.

Operating frequency vector (Hz) - Operating frequency range of custom antenna or microphone elements
[0,1e20] (default) | real-valued row vector

Specify the frequencies at which to set antenna and microphone frequency responses as a 1-by-L row vector of increasing real values. The antenna or microphone element has no response outside the frequency range specified by the minimum and maximum elements of this vector. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone. Use Frequency responses (dB) to set the responses at these frequencies.

Baffle the back of the element - Set back response of an Isotropic Antenna element or an Omni Microphone element to zero off (default) | on

Select this check box to baffle the back response of the element. When back baffled, the responses at all azimuth angles beyond $\pm 90^{\circ}$ from broadside are set to zero. The broadside direction is defined as $0^{\circ}$ azimuth angle and $0^{\circ}$ elevation angle.

## Dependencies

To enable this check box, set Element type to Isotropic Antenna or Omni Microphone.
Exponent of cosine pattern - Exponents of azimuth and elevation cosine patterns
[1.5 1.5] (default) | nonnegative scalar | real-valued 1-by-2 matrix of nonnegative values

Specify the exponents of the cosine pattern as a nonnegative scalar or a real-valued 1-by-2 matrix of nonnegative values. When Exponent of cosine pattern is a 1-by-2 vector, the first element is the exponent in the azimuth direction and the second element is the exponent in the elevation direction. When you set this parameter to a scalar, both the azimuth direction and elevation direction cosine patterns are raised to the same power.

## Dependencies

To enable this parameter, set Element type to Cosine Antenna.
Frequency responses (dB) - Antenna and microphone frequency response
[0,0] (default) | real-valued row vector

Frequency response of a custom antenna or custom microphone for the frequencies defined by the Operating frequency vector $(\mathbf{H z})$ parameter. The dimensions of Frequency responses (dB) must match the dimensions of the vector specified by the Operating frequency vector $(\mathbf{H z})$ parameter.

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone.
Input Pattern Coordinate System - Coordinate system of custom antenna pattern az-el (default) | phi-theta

Coordinate system of custom antenna pattern, specified az-el or phi-theta. When you specify azel, use the Azimuth angles (deg) and Elevations angles (deg) parameters to specify the coordinates of the pattern points. When you specify phi-theta, use the Phi angles (deg) and Theta angles (deg) parameters to specify the coordinates of the pattern points.

Dependencies
To enable this parameter, set Element type to Custom Antenna.
Azimuth angles (deg) - Azimuth angles of antenna radiation pattern
[-180:180] (default) | real-valued row vector

Specify the azimuth angles at which to calculate the antenna radiation pattern as a 1-by-P row vector. $P$ must be greater than 2. Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to az-el.

Elevation angles (deg) - Elevation angles of antenna radiation pattern
[-90:90] (default) | real-valued row vector

Specify the elevation angles at which to compute the radiation pattern as a 1-by- $Q$ vector. $Q$ must be greater than 2. Angle units are in degrees. Elevation angles must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input
Pattern Coordinate System parameter to az-el.
Phi Angles (deg) - Phi angle coordinates of custom antenna radiation pattern
$0: 360 \mid$ real-valued 1-by-P row vector

Phi angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by- $P$ row vector. $P$ must be greater than 2 . Angle units are in degrees. Phi angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input
Pattern Coordinate System parameter to phi-theta.
Theta Angles (deg) - Theta angle coordinates of custom antenna radiation pattern
$0: 180$ | real-valued 1-by- $Q$ row vector

Theta angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by$Q$ row vector. $Q$ must be greater than 2 . Angle units are in degrees. Theta angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Radiation pattern (dB) - Custom antenna radiation pattern zeros $(181,361)$ | complex-valued matrix | complex-valued MATLAB array

Magnitude of the combined polarized antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$ -by- $P$-by- $L$ array. The value of $Q$ must equal the value of $Q$ specified by Elevation angles (deg). The value of $P$ must equal the value of $P$ specified by Azimuth angles (deg). The value of $L$ must equal the value of $L$ specified by Operating frequency vector $(\mathbf{H z})$.

## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Polar pattern frequencies (Hz) - Polar pattern microphone response frequencies
1 e3 (default) | real scalar | real-valued 1-by-L row vector

Polar pattern microphone response frequencies, specified as a real scalar, or a real-valued, 1-by-L vector. The response frequencies lie within the frequency range specified by the Operating frequency vector $(\mathrm{Hz})$ vector.

## Dependencies

To enable this parameter, set Element type set to Custom Microphone.
Polar pattern angles (deg) - Polar pattern response angles
[-180:180] (default) | real-valued -by-P row vector

Specify the polar pattern response angles, as a 1-by- $P$ vector. The angles are measured from the central pickup axis of the microphone and must be between $-180^{\circ}$ and $180^{\circ}$, inclusive.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.
Polar pattern (dB) - Custom microphone polar response
zeros $(1,361)$ (default) | real-valued $L$-by- $P$ matrix

Specify the magnitude of the custom microphone element polar patterns as an $L$-by- $P$ matrix. $L$ is the number of frequencies specified in Polar pattern frequencies (Hz). $P$ is the number of angles specified in Polar pattern angles (deg). Each row of the matrix represents the magnitude of the polar pattern measured at the corresponding frequency specified in Polar pattern frequencies ( Hz ) and all angles specified in Polar pattern angles (deg). The pattern is measured in the azimuth plane. In the azimuth plane, the elevation angle is $0^{\circ}$ and the central pickup axis is $0^{\circ}$ degrees azimuth and $0^{\circ}$ degrees elevation. The polar pattern is symmetric around the central axis. You can construct the microphone response pattern in 3-D space from the polar pattern.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.

## Array Parameters

Number of elements - Number of array elements in $U$
2 (default) | positive integer greater than or equal to two

The number of array elements for ULA arrays, specified as an integer greater than or equal to two.
Example: 11
Data Types: double
Element spacing - Distance between ULA elements
0.5 (default) | positive scalar

Distance between adjacent ULA elements, specified as a positive scalar. Units are in meters.
Example: 1.5
Array axis - Linear axis direction of ULA
$y$ (default) $|x| z$
Linear axis direction of ULA, specified as $y$, $x$, or $z$. Then, all ULA array elements are uniformly spaced along this axis in the local array coordinate system.

Taper - Array element tapers
1 (default) | complex scalar | complex-valued row vector

Specify element tapering as a complex-valued scalar or a complex-valued 1-by- $N$ row vector. In this vector, $N$ represents the number of elements in the array.

Also known as element weights, tapers multiply the array element responses. Tapers modify both amplitude and phase of the response to reduce side lobes or steer the main response axis.

If Taper is a scalar, the same weight is applied to each element. If Taper is a vector, a weight from the vector is applied to the corresponding sensor element. The number of weights must match the number of elements of the array.
Data Types: double

## Version History

## Introduced in R2014b

## See Also

phased.BeamscanEstimator

## ULA MVDR Spectrum

MVDR spatial spectrum estimator for ULA


## Library

Direction of Arrival (DOA)
phaseddoalib

## Description

The ULA MVDR Spectrum block estimates the spatial spectrum of incoming narrowband signals by scanning a region of broadside angles using a narrowband minimum variance distortionless response (MVDR) beamformer for a uniform linear array. The block optionally calculates the direction of arrival (DOA) of a specified number of signals by estimating peaks of the spectrum. The MVDR DOA estimator is also called the Capon DOA estimator.

## Parameters

## Signal Propagation speed (m/s)

Specify the propagation speed of the signal, in meters per second, as a positive scalar. You can use the function physconst to specify the speed of light.
Operating frequency ( Hz )
Specify the operating frequency of the system, in hertz, as a positive scalar.

## Number of bits in phase shifters

The number of bits used to quantize the phase shift component of beamformer or steering vector weights. Specify the number of bits as a non-negative integer. A value of zero indicates that no quantization is performed.

## Forward-backward averaging

Select this parameter to use forward-backward averaging to estimate the covariance matrix for sensor arrays with a conjugate symmetric array manifold.

## Spatial smoothing

Specify the amount of averaging, $L$, used by spatial smoothing to estimate the covariance matrix as a nonnegative integer. Each increase in smoothing handles one extra coherent source, but reduces the effective number of elements by one. The maximum value of this parameter is $N-2$, where $N$ is the number of sensors.

## Scan angles (deg)

Specify the scan angles in degrees as a real vector. The angles are broadside angles and must be between $-90^{\circ}$ and $90^{\circ}$, inclusive. You must specify the angles in increasing order.

## Enable DOA output

Select this parameter to output the signals directions of arrival (DOA) through the Ang output port. Selecting this parameter enables the Number of signals parameter.

## Number of signals

Specify the number of signals for DOA estimation as a positive scalar integer. This parameter appears when you select the Enable DOA output check box.

## Simulate using

Block simulation method, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster than they would in interpreted execution. You can run repeated executions without recompiling. However, if you change any block parameters, then the block automatically recompiles before execution.

When setting this parameter, you must take into account the overall model simulation mode. The table shows how the Simulate using parameter interacts with the overall simulation mode.

When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the <br> model are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).

## Array Parameters

## Specify sensor array as

Specify a ULA sensor array directly or by using a MATLAB expression.

## Types

```
Array (no subarrays)
MATLAB expression
```


## Number of elements

Specifies the number of elements in the array as an integer.

## Element spacing

Specify the spacing, in meters, between two adjacent elements in the array.

## Array axis

This parameter appears when the Geometry parameter is set to ULA or when the block only supports a ULA array geometry. Specify the array axis as $x, y$, or $z$. All ULA array elements are uniformly spaced along this axis in the local array coordinate system.

## Taper

Tapers, also known as element weights, are applied to sensor elements in the array. Tapers are used to modify both the amplitude and phase of the transmitted or received data.

Specify element tapering as a complex-valued scalar or a complex-valued 1 -by- $N$ row vector. In this vector, $N$ represents the number of elements in the array. If Taper is a scalar, the same weight is applied to each element. If Taper is a vector, a weight from the vector is applied to the corresponding sensor element. A weight must be applied to each element in the sensor array.

## Expression

A valid MATLAB expression containing a constructor for a uniform linear array, for example, phased.ULA.

## Sensor Array Tab: Element Parameters

## Element type

Specify antenna or microphone type as

- Isotropic Antenna
- Cosine Antenna
- Custom Antenna
- Omni Microphone
- Custom Microphone


## Exponent of cosine pattern

This parameter appears when you set Element type to Cosine Antenna.
Specify the exponent of the cosine pattern as a scalar or a 1-by-2 vector. You must specify all values as non-negative real numbers. When you set Exponent of cosine pattern to a scalar, both the azimuth direction cosine pattern and the elevation direction cosine pattern are raised to the specified value. When you set Exponent of cosine pattern to a 1-by-2 vector, the first element is the exponent for the azimuth direction cosine pattern and the second element is the exponent for the elevation direction cosine pattern.

## Operating frequency range ( Hz )

This parameter appears when Element type is set to Isotropic Antenna, Cosine Antenna, or Omni Microphone.

Specify the operating frequency range, in hertz, of the antenna element as a 1-by-2 row vector in the form [LowerBound, UpperBound]. The antenna element has no response outside the specified frequency range.
Operating frequency vector ( Hz )
This parameter appears when Element type is set to Custom Antenna or Custom Microphone.

Specify the frequencies, in Hz , at which to set the antenna and microphone frequency responses as a 1 -by-L row vector of increasing values. Use Frequency responses to set the frequency responses. The antenna or microphone element has no response outside the frequency range specified by the minimum and maximum elements of Operating frequency vector ( $\mathbf{H z}$ ).

## Frequency responses (dB)

This parameter appears when Element type is set to Custom Antenna or Custom Microphone.

Specify this parameter as the frequency response of an antenna or microphone, in decibels, for the frequencies defined by Operating frequency vector (Hz). Specify Frequency responses (dB) as a 1-by-L vector matching the dimensions of the vector specified in Operating frequency vector (Hz).

## Input Pattern Coordinate System

Coordinate system of custom antenna pattern, specified az-el or phi-theta. When you specify az-el, use the Azimuth angles (deg) and Elevations angles (deg) parameters to specify the coordinates of the pattern points. When you specify phi-theta, use the Phi angles (deg) and Theta angles (deg) parameters to specify the coordinates of the pattern points.

## Azimuth angles (deg)

This parameter appears when Element type is set to Custom Antenna and the Input Pattern Coordinate System parameter is set to az-el.

Specify the azimuth angles at which to calculate the antenna radiation pattern as a 1 -by- $P$ row vector. $P$ must be greater than 2. Angle units are in degrees. Azimuth angles must lie between $180^{\circ}$ and $180^{\circ}$ and be in strictly increasing order.

## Elevation angles (deg)

This parameter appears when Element type is set to Custom Antenna and the Input Pattern Coordinate System parameter is set to az-el.

Specify the elevation angles at which to compute the radiation pattern as a 1-by- $Q$ vector. $Q$ must be greater than 2. Angle units are in degrees. Elevation angles must lie between $-90^{\circ}$ and $90^{\circ}$ and be in strictly increasing order.

## Phi Angles (deg)

This parameter appears when Element type is set to Custom Antenna and the Input Pattern Coordinate System parameter is set to phi-theta.

Phi angles of points at which to specify the antenna radiation pattern, specify as a 1-by-P row vector. $P$ must be greater than 2 . Angle units are in degrees. Phi angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Theta Angles (deg)

This parameter appears when Element type is set to Custom Antenna and the Input Pattern Coordinate System parameter is set to phi-theta.

Theta angles of points at which to specify the antenna radiation pattern, specify as a 1-by- $Q$ row vector. $Q$ must be greater than 2 . Angle units are in degrees. Theta angles must lie between $0^{\circ}$ and $180^{\circ}$ and be in strictly increasing order.
Magnitude pattern (dB)
This parameter appears when the Element type is set to Custom Antenna.

Magnitude of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$ -by-L array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector ( $\mathbf{H z}$ ).

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (Hz) parameter.


## Phase pattern (dB)

This parameter appears when the Element type is set to Custom Antenna.
Phase of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector ( $\mathbf{H z}$ ).

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (Hz) parameter.


## MatchArrayNormal

This parameter appears when the Element type is set to Custom Antenna.
Select this check box to rotate the antenna element pattern to align with the array normal. When not selected, the element pattern is not rotated.

When the antenna is used in an antenna array and the Input Pattern Coordinate System parameter is az-el, selecting this check box rotates the pattern so that the $x$-axis of the element coordinate system points along the array normal. Not selecting uses the element pattern without the rotation.

When the antenna is used in an antenna array and Input Pattern Coordinate System is set to phi-theta, selecting this check box rotates the pattern so that the $z$-axis of the element coordinate system points along the array normal.

Use the parameter in conjunction with the Array normal parameter of the URA and UCA arrays.

## Polar pattern frequencies (Hz)

This parameter appears when the Element type is set to Custom Microphone.
Specify the measuring frequencies of the polar patterns as a 1 -by- $M$ vector. The measuring frequencies lie within the frequency range specified by the Operating frequency vector ( $\mathbf{H z}$ ) parameter. Frequency units are in Hz.

## Polar pattern angles (deg)

This parameter appears when Element type is set to Custom Microphone.
Specify the measuring angles of the polar patterns, as a 1 -by- $N$ vector. The angles are measured from the central pickup axis of the microphone, and must be between $-180^{\circ}$ and $180^{\circ}$, inclusive.

## Polar pattern (dB)

This parameter appears when Element type is set to Custom Microphone.
Specify the magnitude of the microphone element polar pattern as an $M$-by- $N$ matrix. $M$ is the number of measuring frequencies specified in Polar pattern frequencies (Hz). $N$ is the number of measuring angles specified in Polar pattern angles (deg). Each row of the matrix represents the magnitude of the polar pattern measured at the corresponding frequency specified in Polar pattern frequencies (Hz) and all angles specified in Polar pattern angles (deg). Assume that the pattern is measured in the azimuth plane. In the azimuth plane, the elevation angle is $0^{\circ}$ and the central pickup axis is $0^{\circ}$ degrees azimuth and $0^{\circ}$ degrees elevation. Assume that the polar pattern is symmetric around the central axis. You can construct the microphone's response pattern in 3-D space from the polar pattern.

## Baffle the back of the element

This check box appears only when the Element type parameter is set to Isotropic Antenna or Omni Microphone.

Select this check box to baffle the back of the antenna element. In this case, the antenna responses to all azimuth angles beyond $\pm 90^{\circ}$ from broadside are set to zero. Define the broadside direction as $0^{\circ}$ azimuth angle and $0^{\circ}$ elevation angle.

## Ports

Note The block input and output ports correspond to the input and output parameters described in the step method of the underlying System object. See link at the bottom of this page.

| Port | Description | Supported Data Types |
| :--- | :--- | :--- |
| In | Input signal. <br> The size of the first dimension of <br> the input matrix can vary to <br> simulate a changing signal <br> length. A size change can occur, <br> for example, in the case of a <br> pulse waveform with variable <br> pulse repetition frequency. | Double-precision floating point |
| Ang | Estimated broadside DOA <br> angles. | Double-precision floating point |
| Y | Estimated spatial spectrum. | Double-precision floating point |

## Version History

Introduced in R2014b

## See Also

phased.MVDREstimator

## ULA MUSIC Spectrum

MUSIC spatial spectrum estimator for ULA

## Libraries:

Phased Array System Toolbox / Direction of Arrival

## Description

The ULA MUSIC Spectrum block estimates the spatial spectrum of incoming narrowband signals using the MUSIC algorithm. The algorithm computes the MUSIC pseudo-spectrum of a ULA by scanning a region of broadside angles. The block optionally calculates the direction of arrival (DOA) of a specified number of signals by estimating peaks of the spectrum.

## Ports

Input
Port 1 - Received signal
$M$-by- $N$ complex-valued matrix
Received signal, specified as an $M$-by- $N$ complex-valued matrix. The quantity $M$ is the number of sample values (snapshots) contained in the signal and $N$ is the number of sensor elements in the array.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.
Data Types: double

## Output

Y - MUSIC spatial spectrum
non-negative, real-valued column vector
MUSIC spatial spectrum, returned as a non-negative, real-valued column vector representing the magnitude of the estimated MUSIC spatial spectrum. Each entry corresponds to an angle specified by the Scan angles (deg) parameter.
Data Types: double
Ang - Directions of arrival
non-negative, real-valued column vector
Directions of arrival of the signals, returned as a real-valued row vector. The direction of arrival angle is the broadside angle between the source direction and the array axis. The length of the vector is the number of signals specified by the Number of signals parameter. If the object cannot identify peaks in the spectrum, it will return NaN . Angle units are in degrees.

## Dependencies

Select the Enable DOA output parameter to enable this output port.
Data Types: double

## Parameters

## Main Tab

Signal propagation speed (m/s) - Signal propagation speed
physconst('LightSpeed') (default)| real-valued positive scalar

Signal propagation speed, specified as a real-valued positive scalar. The default value of the speed of light is the value returned by physconst('LightSpeed '). Units are in meters per second.
Example: 3e8
Data Types: double
Operating frequency (Hz) - System operating frequency
3 e8 (default) | positive real scalar

System operating frequency, specified as a positive scalar. Units are in Hz.
Forward-backward averaging - Enable forward-backward averaging
off (default) | on

Select this parameter to use forward-backward averaging to estimate the covariance matrix for sensor arrays with a conjugate symmetric array manifold structure.

Spatial smoothing - Enable spatial smoothing
0 (default) | non-negative integer

Specify the amount of averaging used by spatial smoothing to estimate the covariance matrix as a nonnegative integer. Each increase in smoothing handles one extra coherent source, but reduces the effective number of elements by one. The maximum value of this parameter is $N-2$, where $N$ is the number of sensors in the ULA.

Scan angles (deg) - Search angles for spectrum peaks

- 90: 90 (default) | real-valued row vector

Specify the scan angles in degrees as a real-valued row vector. The angles are array broadside angles and must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive. You must specify the angles in increasing order.

Enable DOA output - Output directions of arrival through output port off (default) | on

Select this parameter to output the signals directions of arrival (DOA) through the Ang output port.

Number of signals - Expected number of arriving signals
1 (default) | positive integer

Specify the expected number of signals for DOA estimation as a positive scalar integer.
Simulate using - Block simulation method
Interpreted Execution (default)|Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).
Programmatic Use
Block Parameter:SimulateUsing
Type:enum
Values:Interpreted Execution, Code Generation
Default:Interpreted Execution

## Sensor Array Tab

Specify sensor array as - Method to specify array
Array (no subarrays) (default)|MATLAB expression

Method to specify array, specified as Array (no subarrays) or MATLAB expression.

- Array (no subarrays) - use the block parameters to specify the array.
- MATLAB expression - create the array using a MATLAB expression.

Expression - MATLAB expression used to create an array
Phased Array System Toolbox array System object

MATLAB expression used to create an array, specified as a valid Phased Array System Toolbox array System object.

Example: phased.URA('Size', [5,3])

## Dependencies

To enable this parameter, set Specify sensor array as to MATLAB expression.

## Element Parameters

Element type - Array element types
Isotropic Antenna (default)|Cosine Antenna|Custom Antenna|Omni Microphone| Custom Microphone

Antenna or microphone type, specified as one of the following:

- Isotropic Antenna
- Cosine Antenna
- Custom Antenna
- Omni Microphone
- Custom Microphone

Operating frequency range $(\mathbf{H z})$ - Operating frequency range of the antenna or microphone element
[0,1e20] (default) | real-valued 1-by-2 row vector

Specify the operating frequency range of the antenna or microphone element as a 1-by-2 row vector in the form [LowerBound, UpperBound]. The element has no response outside this frequency range. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Isotropic Antenna, Cosine Antenna, or Omni Microphone.

Operating frequency vector (Hz) - Operating frequency range of custom antenna or microphone elements
[0,1e20] (default) | real-valued row vector

Specify the frequencies at which to set antenna and microphone frequency responses as a 1-by- $L$ row vector of increasing real values. The antenna or microphone element has no response outside the frequency range specified by the minimum and maximum elements of this vector. Frequency units are in Hz .

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone. Use Frequency responses (dB) to set the responses at these frequencies.

Baffle the back of the element - Set back response of an Isotropic Antenna element or an Omni Microphone element to zero
off (default) | on

Select this check box to baffle the back response of the element. When back baffled, the responses at all azimuth angles beyond $\pm 90^{\circ}$ from broadside are set to zero. The broadside direction is defined as $0^{\circ}$ azimuth angle and $0^{\circ}$ elevation angle.

## Dependencies

To enable this check box, set Element type to Isotropic Antenna or Omni Microphone.
Exponent of cosine pattern - Exponents of azimuth and elevation cosine patterns
[1.5 1.5] (default) | nonnegative scalar | real-valued 1-by-2 matrix of nonnegative values

Specify the exponents of the cosine pattern as a nonnegative scalar or a real-valued 1-by-2 matrix of nonnegative values. When Exponent of cosine pattern is a 1-by-2 vector, the first element is the exponent in the azimuth direction and the second element is the exponent in the elevation direction. When you set this parameter to a scalar, both the azimuth direction and elevation direction cosine patterns are raised to the same power.

## Dependencies

To enable this parameter, set Element type to Cosine Antenna.
Frequency responses (dB) - Antenna and microphone frequency response [0,0] (default) | real-valued row vector

Frequency response of a custom antenna or custom microphone for the frequencies defined by the Operating frequency vector (Hz) parameter. The dimensions of Frequency responses (dB) must match the dimensions of the vector specified by the Operating frequency vector $(\mathbf{H z})$ parameter.

## Dependencies

To enable this parameter, set Element type to Custom Antenna or Custom Microphone.
Input Pattern Coordinate System - Coordinate system of custom antenna pattern az-el (default)|phi-theta

Coordinate system of custom antenna pattern, specified az-el or phi-theta. When you specify azel, use the Azimuth angles (deg) and Elevations angles (deg) parameters to specify the coordinates of the pattern points. When you specify phi-theta, use the Phi angles (deg) and Theta angles (deg) parameters to specify the coordinates of the pattern points.

## Dependencies

To enable this parameter, set Element type to Custom Antenna.

Azimuth angles (deg) - Azimuth angles of antenna radiation pattern
[-180:180] (default) | real-valued row vector

Specify the azimuth angles at which to calculate the antenna radiation pattern as a 1 -by- $P$ row vector. $P$ must be greater than 2. Azimuth angles must lie between $-180^{\circ}$ and $180^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to az-el.

Elevation angles (deg) - Elevation angles of antenna radiation pattern
[-90:90] (default) | real-valued row vector

Specify the elevation angles at which to compute the radiation pattern as a 1-by- $Q$ vector. $Q$ must be greater than 2. Angle units are in degrees. Elevation angles must lie between $-90^{\circ}$ and $90^{\circ}$, inclusive, and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to az-el.

Phi Angles (deg) - Phi angle coordinates of custom antenna radiation pattern $0: 360 \mid$ real-valued 1-by-P row vector

Phi angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by- $P$ row vector. $P$ must be greater than 2 . Angle units are in degrees. Phi angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Dependencies

To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Theta Angles (deg) - Theta angle coordinates of custom antenna radiation pattern $0: 180$ | real-valued 1-by- $Q$ row vector

Theta angles of points at which to specify the antenna radiation pattern, specify as a real-valued 1-by$Q$ row vector. $Q$ must be greater than 2 . Angle units are in degrees. Theta angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.
Dependencies
To enable this parameter, set the Element type parameter to Custom Antenna and the Input Pattern Coordinate System parameter to phi-theta.

Radiation pattern (dB) - Custom antenna radiation pattern zeros $(181,361)$ | complex-valued matrix | complex-valued MATLAB array

Magnitude of the combined polarized antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$ -by- $P$-by- $L$ array. The value of $Q$ must equal the value of $Q$ specified by Elevation angles (deg). The
value of $P$ must equal the value of $P$ specified by Azimuth angles (deg). The value of $L$ must equal the value of $L$ specified by Operating frequency vector ( $\mathbf{H z}$ ).

## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Magnitude pattern (dB) - Magnitude of combined antenna radiation pattern
zeros $(181,361)$ (default) | real-valued $Q$-by-P matrix | real-valued $Q$-by- $P$-by-L array

Magnitude of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector ( $\mathbf{H z}$ ).

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (Hz) parameter.


## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Phase pattern (deg) - Custom antenna radiation phase pattern
zeros $(181,361)$ (default) | real-valued $Q$-by-P matrix | real-valued $Q$-by- $P$-by-L array

Phase of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector $(\mathbf{H z})$.

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (


## Dependencies

To enable this parameter, set Element type to Custom Antenna.

MatchArrayNormal - Rotate antenna element to array normal
on (default) | off

Select this check box to rotate the antenna element pattern to align with the array normal. When not selected, the element pattern is not rotated.

When the antenna is used in an antenna array and the Input Pattern Coordinate System parameter is az-el, selecting this check box rotates the pattern so that the $x$-axis of the element coordinate system points along the array normal. Not selecting uses the element pattern without the rotation.

When the antenna is used in an antenna array and Input Pattern Coordinate System is set to phitheta, selecting this check box rotates the pattern so that the $z$-axis of the element coordinate system points along the array normal.

Use the parameter in conjunction with the Array normal parameter of the URA and UCA arrays.

## Dependencies

To enable this parameter, set Element type to Custom Antenna.
Polar pattern frequencies (Hz) - Polar pattern microphone response frequencies
1e3 (default) | real scalar | real-valued 1-by-L row vector

Polar pattern microphone response frequencies, specified as a real scalar, or a real-valued, 1-by-L vector. The response frequencies lie within the frequency range specified by the Operating frequency vector $(\mathrm{Hz})$ vector.

## Dependencies

To enable this parameter, set Element type set to Custom Microphone.
Polar pattern angles (deg) - Polar pattern response angles
[-180:180] (default) | real-valued -by-P row vector

Specify the polar pattern response angles, as a 1-by- $P$ vector. The angles are measured from the central pickup axis of the microphone and must be between $-180^{\circ}$ and $180^{\circ}$, inclusive.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.
Polar pattern (dB) - Custom microphone polar response
zeros ( 1,361 ) (default) | real-valued $L$-by- $P$ matrix

Specify the magnitude of the custom microphone element polar patterns as an $L$-by- $P$ matrix. $L$ is the number of frequencies specified in Polar pattern frequencies $(\mathbf{H z}) . P$ is the number of angles specified in Polar pattern angles (deg). Each row of the matrix represents the magnitude of the polar pattern measured at the corresponding frequency specified in Polar pattern frequencies (Hz) and all angles specified in Polar pattern angles (deg). The pattern is measured in the azimuth plane. In the azimuth plane, the elevation angle is $0^{\circ}$ and the central pickup axis is $0^{\circ}$ degrees
azimuth and $0^{\circ}$ degrees elevation. The polar pattern is symmetric around the central axis. You can construct the microphone response pattern in 3-D space from the polar pattern.

## Dependencies

To enable this parameter, set Element type to Custom Microphone.

## Array Parameters

Number of elements - Number of array elements in $U$
2 (default) | positive integer greater than or equal to two

The number of array elements for ULA arrays, specified as an integer greater than or equal to two.
Example: 11
Data Types: double
Element spacing - Distance between ULA elements
0.5 (default) | positive scalar

Distance between adjacent ULA elements, specified as a positive scalar. Units are in meters.
Example: 1.5
Array axis - Linear axis direction of ULA
$y$ (default) $|x| z$
Linear axis direction of ULA, specified as $y, x$, or $z$. Then, all ULA array elements are uniformly spaced along this axis in the local array coordinate system.

Taper - Array element tapers
1 (default) | complex scalar | complex-valued row vector

Specify element tapering as a complex-valued scalar or a complex-valued 1-by- $N$ row vector. In this vector, $N$ represents the number of elements in the array.

Also known as element weights, tapers multiply the array element responses. Tapers modify both amplitude and phase of the response to reduce side lobes or steer the main response axis.

If Taper is a scalar, the same weight is applied to each element. If Taper is a vector, a weight from the vector is applied to the corresponding sensor element. The number of weights must match the number of elements of the array.
Data Types: double

## Version History <br> Introduced in R2016b

## See Also

## Blocks

MUSIC Spectrum
Objects
phased.MUSICEstimator|phased.ULA

## Functions

musicdoa

## Topics

"MUSIC Super-Resolution DOA Estimation"

## ULA Sum and Difference Monopulse

Sum-and-difference monopulse tracker for ULA


## Library

Direction of Arrival (DOA)
phaseddoalib

## Description

The ULA Sum-and-Difference Monopulse block estimates the direction of arrival of a narrowband signal on a uniform linear array based on an initial guess using a sum-and-difference monopulse algorithm. The block obtains the difference steering vector by phase-reversing the latter half of the sum steering vector.

## Parameters

## Signal Propagation speed (m/s)

Specify the propagation speed of the signal, in meters per second, as a positive scalar. You can use the function physconst to specify the speed of light.

## Operating frequency ( Hz )

Specify the operating frequency of the system, in hertz, as a positive scalar.

## Number of bits in phase shifters

The number of bits used to quantize the phase shift component of beamformer or steering vector weights. Specify the number of bits as a non-negative integer. A value of zero indicates that no quantization is performed.

## Simulate using

Block simulation method, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster than they would in interpreted execution. You can run repeated executions without recompiling. However, if you change any block parameters, then the block automatically recompiles before execution.

When setting this parameter, you must take into account the overall model simulation mode. The table shows how the Simulate using parameter interacts with the overall simulation mode.

When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the <br> model are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).

## Array Parameters

## Specify sensor array as

Specify a ULA sensor array directly or by using a MATLAB expression.

## Types

```
Array (no subarrays)
MATLAB expression
```


## Number of elements

Specifies the number of elements in the array as an integer.

## Element spacing

Specify the spacing, in meters, between two adjacent elements in the array.

## Array axis

This parameter appears when the Geometry parameter is set to ULA or when the block only supports a ULA array geometry. Specify the array axis as $x, y$, or $z$. All ULA array elements are uniformly spaced along this axis in the local array coordinate system.

## Taper

Tapers, also known as element weights, are applied to sensor elements in the array. Tapers are used to modify both the amplitude and phase of the transmitted or received data.

Specify element tapering as a complex-valued scalar or a complex-valued 1-by- $N$ row vector. In this vector, $N$ represents the number of elements in the array. If Taper is a scalar, the same weight is applied to each element. If Taper is a vector, a weight from the vector is applied to the corresponding sensor element. A weight must be applied to each element in the sensor array.

## Expression

A valid MATLAB expression containing a constructor for a uniform linear array, for example, phased.ULA.

## Sensor Array Tab: Element Parameters

## Element type

Specify antenna or microphone type as

- Isotropic Antenna
- Cosine Antenna
- Custom Antenna
- Omni Microphone
- Custom Microphone


## Exponent of cosine pattern

This parameter appears when you set Element type to Cosine Antenna.

Specify the exponent of the cosine pattern as a scalar or a 1-by-2 vector. You must specify all values as non-negative real numbers. When you set Exponent of cosine pattern to a scalar, both the azimuth direction cosine pattern and the elevation direction cosine pattern are raised to the specified value. When you set Exponent of cosine pattern to a 1-by-2 vector, the first element is the exponent for the azimuth direction cosine pattern and the second element is the exponent for the elevation direction cosine pattern.

## Operating frequency range $(\mathbf{H z})$

This parameter appears when Element type is set to Isotropic Antenna, Cosine Antenna, or Omni Microphone.

Specify the operating frequency range, in hertz, of the antenna element as a 1-by-2 row vector in the form [LowerBound, UpperBound]. The antenna element has no response outside the specified frequency range.
Operating frequency vector $(\mathbf{H z})$
This parameter appears when Element type is set to Custom Antenna or Custom Microphone.

Specify the frequencies, in Hz , at which to set the antenna and microphone frequency responses as a 1-by- $L$ row vector of increasing values. Use Frequency responses to set the frequency responses. The antenna or microphone element has no response outside the frequency range specified by the minimum and maximum elements of Operating frequency vector $(\mathbf{H z})$.

## Frequency responses (dB)

This parameter appears when Element type is set to Custom Antenna or Custom Microphone.

Specify this parameter as the frequency response of an antenna or microphone, in decibels, for the frequencies defined by Operating frequency vector (Hz). Specify Frequency responses (dB) as a 1-by- $L$ vector matching the dimensions of the vector specified in Operating frequency vector (Hz).

## Input Pattern Coordinate System

Coordinate system of custom antenna pattern, specified az-el or phi-theta. When you specify az-el, use the Azimuth angles (deg) and Elevations angles (deg) parameters to specify the coordinates of the pattern points. When you specify phi-theta, use the Phi angles (deg) and Theta angles (deg) parameters to specify the coordinates of the pattern points.

## Azimuth angles (deg)

This parameter appears when Element type is set to Custom Antenna and the Input Pattern Coordinate System parameter is set to az-el.

Specify the azimuth angles at which to calculate the antenna radiation pattern as a 1 -by- $P$ row vector. $P$ must be greater than 2. Angle units are in degrees. Azimuth angles must lie between $180^{\circ}$ and $180^{\circ}$ and be in strictly increasing order.

## Elevation angles (deg)

This parameter appears when Element type is set to Custom Antenna and the Input Pattern Coordinate System parameter is set to az-el.

Specify the elevation angles at which to compute the radiation pattern as a 1-by- $Q$ vector. $Q$ must be greater than 2. Angle units are in degrees. Elevation angles must lie between $-90^{\circ}$ and $90^{\circ}$ and be in strictly increasing order.

## Phi Angles (deg)

This parameter appears when Element type is set to Custom Antenna and the Input Pattern Coordinate System parameter is set to phi-theta.

Phi angles of points at which to specify the antenna radiation pattern, specify as a 1-by-P row vector. $P$ must be greater than 2 . Angle units are in degrees. Phi angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Theta Angles (deg)

This parameter appears when Element type is set to Custom Antenna and the Input Pattern Coordinate System parameter is set to phi-theta.

Theta angles of points at which to specify the antenna radiation pattern, specify as a 1-by- $Q$ row vector. $Q$ must be greater than 2 . Angle units are in degrees. Theta angles must lie between $0^{\circ}$ and $180^{\circ}$ and be in strictly increasing order.

## Magnitude pattern (dB)

This parameter appears when the Element type is set to Custom Antenna.
Magnitude of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$ -by-L array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector $(\mathbf{H z})$.

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (Hz) parameter.


## Phase pattern (dB)

This parameter appears when the Element type is set to Custom Antenna.
Phase of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector $(\mathbf{H z})$.

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector ( $\mathbf{H z}$ ) parameter.
- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (Hz) parameter.


## MatchArrayNormal

This parameter appears when the Element type is set to Custom Antenna.
Select this check box to rotate the antenna element pattern to align with the array normal. When not selected, the element pattern is not rotated.

When the antenna is used in an antenna array and the Input Pattern Coordinate System parameter is az-el, selecting this check box rotates the pattern so that the $x$-axis of the element coordinate system points along the array normal. Not selecting uses the element pattern without the rotation.

When the antenna is used in an antenna array and Input Pattern Coordinate System is set to phi-theta, selecting this check box rotates the pattern so that the $z$-axis of the element coordinate system points along the array normal.

Use the parameter in conjunction with the Array normal parameter of the URA and UCA arrays.

## Polar pattern frequencies ( Hz )

This parameter appears when the Element type is set to Custom Microphone.
Specify the measuring frequencies of the polar patterns as a 1 -by- $M$ vector. The measuring frequencies lie within the frequency range specified by the Operating frequency vector ( $\mathbf{H z}$ ) parameter. Frequency units are in Hz .

## Polar pattern angles (deg)

This parameter appears when Element type is set to Custom Microphone.
Specify the measuring angles of the polar patterns, as a 1 -by- $N$ vector. The angles are measured from the central pickup axis of the microphone, and must be between $-180^{\circ}$ and $180^{\circ}$, inclusive.

## Polar pattern (dB)

This parameter appears when Element type is set to Custom Microphone.
Specify the magnitude of the microphone element polar pattern as an $M$-by- $N$ matrix. $M$ is the number of measuring frequencies specified in Polar pattern frequencies (Hz). $N$ is the number
of measuring angles specified in Polar pattern angles (deg). Each row of the matrix represents the magnitude of the polar pattern measured at the corresponding frequency specified in Polar pattern frequencies (Hz) and all angles specified in Polar pattern angles (deg). Assume that the pattern is measured in the azimuth plane. In the azimuth plane, the elevation angle is $0^{\circ}$ and the central pickup axis is $0^{\circ}$ degrees azimuth and $0^{\circ}$ degrees elevation. Assume that the polar pattern is symmetric around the central axis. You can construct the microphone's response pattern in 3-D space from the polar pattern.

## Baffle the back of the element

This check box appears only when the Element type parameter is set to Isotropic Antenna or Omni Microphone.

Select this check box to baffle the back of the antenna element. In this case, the antenna responses to all azimuth angles beyond $\pm 90^{\circ}$ from broadside are set to zero. Define the broadside direction as $0^{\circ}$ azimuth angle and $0^{\circ}$ elevation angle.

## Ports

Note The block input and output ports correspond to the input and output parameters described in the step method of the underlying System object. See link at the bottom of this page.

| Port | Description | Supported Data Types |
| :--- | :--- | :--- |
| $X$ | Input signal. <br> The size of the first dimension of <br> the input matrix can vary to <br> simulate a changing signal <br> length. A size change can occur, <br> for example, in the case of a <br> pulse waveform with variable <br> pulse repetition frequency. | Double-precision floating point |
| Steer | Initial estimate of broadside <br> DOA angles. | Double-precision floating point |
| Ang | Estimated broadside DOA <br> angles. | Double-precision floating point |

## Version History <br> \section*{Introduced in R2014b}

## See Also

phased.SumDifferenceMonopulseTracker

## URA Sum and Difference Monopulse

Sum-and-difference monopulse for URA


## Library

Direction of Arrival (DOA)
phaseddoalib

## Description

The URA Sum-and-Difference Monopulse block estimates the direction of arrival of a narrowband signal on a uniform rectangular array (URA) based on an initial guess using a sum-and-difference monopulse algorithm. The block obtains the difference steering vector by phase-reversing the latter half of the sum steering vector.

## Parameters

## Signal Propagation speed (m/s)

Specify the propagation speed of the signal, in meters per second, as a positive scalar. You can use the function physconst to specify the speed of light.

## Operating frequency ( Hz )

Specify the operating frequency of the system, in hertz, as a positive scalar.

## Number of bits in phase shifters

The number of bits used to quantize the phase shift component of beamformer or steering vector weights. Specify the number of bits as a non-negative integer. A value of zero indicates that no quantization is performed.

## Simulate using

Block simulation method, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster than they would in interpreted execution. You can run repeated executions without recompiling. However, if you change any block parameters, then the block automatically recompiles before execution.

When setting this parameter, you must take into account the overall model simulation mode. The table shows how the Simulate using parameter interacts with the overall simulation mode.

When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the <br> model are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).

## Array Parameters

## Specify sensor array as

Specify a ULA sensor array directly or by using a MATLAB expression.
Types

```
Array (no subarrays)
MATLAB expression
```


## Array size

Specify the size of the array as a positive integer or 1-by-2 vector of positive integers.

- If Array size is a 1 -by- 2 vector, the vector has the form [NumberOfArrayRows, NumberOfArrayColumns].
- If Array size is an integer, the array has the same number of rows and columns.

Elements are indexed from top to bottom along a column and continuing to the next columns from left to right. In this figure, an Array size of [3,2] produces an array has three rows and two columns.

## Size and Element Indexing Order <br> for Uniform Rectangular Arrays <br> Example: Size = [3,2]



## Element spacing

Specify the element spacing of the array, in meters, as a 1-by-2 vector or a scalar. If Element spacing is a 1 -by- 2 vector, the vector has the form [SpacingBetweenRows, SpacingBetweenColumns]. For a discussion of these quantities, see phased.URA. If Element spacing is a scalar, the spacings between rows and columns are equal.

## Element lattice

Specify the element lattice as one of Rectangular or Triangular.

- Rectangular - Aligns all the elements in row and column directions.
- Triangular - Shifts the even-row elements of a rectangular lattice toward the positive-row axis direction. The elements are shifted a distance of half the element spacing along the row.


## Array normal

This parameter appears when you set Geometry to URA or UCA. Specify the Array normal as x, $y$, or $z$. All URA and UCA array elements are placed in the $y z, z x$, or $x y$-planes, respectively, of the array coordinate system.

## Taper

Tapers, also known as element weights, are applied to sensor elements in the array. Tapers are used to modify both the amplitude and phase of the transmitted or received data.

Specify element tapering as a complex-valued scalar or complex-valued $M$-by- $N$ matrix. In this matrix, $M$ is the number of elements along the $z$-axis, and $N$ is the number of elements along the $y$-axis. $M$ and $N$ correspond to the values of [NumberofRows, NumberOfColumns] in the Array size matrix. If Taper is a scalar, the same weight is applied to each element. If the value of Taper is a matrix, a weight from the matrix is applied to the corresponding sensor element. A weight must be applied to each element in the sensor array.

## Expression

A valid MATLAB expression containing a constructor for a uniform rectangular array, for example, phased.URA.

## Sensor Array Tab: Element Parameters

## Element type

Specify antenna or microphone type as

- Isotropic Antenna
- Cosine Antenna
- Custom Antenna
- Omni Microphone
- Custom Microphone


## Exponent of cosine pattern

This parameter appears when you set Element type to Cosine Antenna.
Specify the exponent of the cosine pattern as a scalar or a 1 -by- 2 vector. You must specify all values as non-negative real numbers. When you set Exponent of cosine pattern to a scalar, both the azimuth direction cosine pattern and the elevation direction cosine pattern are raised to the specified value. When you set Exponent of cosine pattern to a 1 -by-2 vector, the first element is the exponent for the azimuth direction cosine pattern and the second element is the exponent for the elevation direction cosine pattern.

## Operating frequency range (Hz)

This parameter appears when Element type is set to Isotropic Antenna, Cosine Antenna, or Omni Microphone.

Specify the operating frequency range, in hertz, of the antenna element as a 1-by-2 row vector in the form [LowerBound, UpperBound]. The antenna element has no response outside the specified frequency range.
Operating frequency vector (Hz)
This parameter appears when Element type is set to Custom Antenna or Custom Microphone.

Specify the frequencies, in Hz , at which to set the antenna and microphone frequency responses as a 1 -by-L row vector of increasing values. Use Frequency responses to set the frequency responses. The antenna or microphone element has no response outside the frequency range specified by the minimum and maximum elements of Operating frequency vector (Hz).

## Frequency responses (dB)

This parameter appears when Element type is set to Custom Antenna or Custom Microphone.

Specify this parameter as the frequency response of an antenna or microphone, in decibels, for the frequencies defined by Operating frequency vector (Hz). Specify Frequency responses (dB) as a 1-by-L vector matching the dimensions of the vector specified in Operating frequency vector ( Hz ).

Input Pattern Coordinate System
Coordinate system of custom antenna pattern, specified az-el or phi-theta. When you specify az-el, use the Azimuth angles (deg) and Elevations angles (deg) parameters to specify the coordinates of the pattern points. When you specify phi-theta, use the Phi angles (deg) and Theta angles (deg) parameters to specify the coordinates of the pattern points.

## Azimuth angles (deg)

This parameter appears when Element type is set to Custom Antenna and the Input Pattern Coordinate System parameter is set to az-el.

Specify the azimuth angles at which to calculate the antenna radiation pattern as a 1 -by- $P$ row vector. $P$ must be greater than 2. Angle units are in degrees. Azimuth angles must lie between $180^{\circ}$ and $180^{\circ}$ and be in strictly increasing order.

## Elevation angles (deg)

This parameter appears when Element type is set to Custom Antenna and the Input Pattern Coordinate System parameter is set to az-el.

Specify the elevation angles at which to compute the radiation pattern as a 1-by- $Q$ vector. $Q$ must be greater than 2. Angle units are in degrees. Elevation angles must lie between $-90^{\circ}$ and $90^{\circ}$ and be in strictly increasing order.

## Phi Angles (deg)

This parameter appears when Element type is set to Custom Antenna and the Input Pattern Coordinate System parameter is set to phi-theta.

Phi angles of points at which to specify the antenna radiation pattern, specify as a 1 -by- $P$ row vector. $P$ must be greater than 2 . Angle units are in degrees. Phi angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Theta Angles (deg)

This parameter appears when Element type is set to Custom Antenna and the Input Pattern Coordinate System parameter is set to phi-theta.

Theta angles of points at which to specify the antenna radiation pattern, specify as a 1-by- $Q$ row vector. $Q$ must be greater than 2 . Angle units are in degrees. Theta angles must lie between $0^{\circ}$ and $180^{\circ}$ and be in strictly increasing order.

## Magnitude pattern (dB)

This parameter appears when the Element type is set to Custom Antenna.
Magnitude of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$ -by-L array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector $(\mathbf{H z})$.

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (Hz) parameter.


## Phase pattern (dB)

This parameter appears when the Element type is set to Custom Antenna.

Phase of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi - theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector (Hz).

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector ( $\mathbf{H z}$ ) parameter.


## MatchArrayNormal

This parameter appears when the Element type is set to Custom Antenna.
Select this check box to rotate the antenna element pattern to align with the array normal. When not selected, the element pattern is not rotated.

When the antenna is used in an antenna array and the Input Pattern Coordinate System parameter is az-el, selecting this check box rotates the pattern so that the $x$-axis of the element coordinate system points along the array normal. Not selecting uses the element pattern without the rotation.

When the antenna is used in an antenna array and Input Pattern Coordinate System is set to phi-theta, selecting this check box rotates the pattern so that the $z$-axis of the element coordinate system points along the array normal.

Use the parameter in conjunction with the Array normal parameter of the URA and UCA arrays.

## Polar pattern frequencies $(\mathbf{H z})$

This parameter appears when the Element type is set to Custom Microphone.
Specify the measuring frequencies of the polar patterns as a 1-by-M vector. The measuring frequencies lie within the frequency range specified by the Operating frequency vector ( $\mathbf{H z}$ ) parameter. Frequency units are in Hz .

## Polar pattern angles (deg)

This parameter appears when Element type is set to Custom Microphone.
Specify the measuring angles of the polar patterns, as a $1-b y-N$ vector. The angles are measured from the central pickup axis of the microphone, and must be between $-180^{\circ}$ and $180^{\circ}$, inclusive.

## Polar pattern (dB)

This parameter appears when Element type is set to Custom Microphone.

Specify the magnitude of the microphone element polar pattern as an $M$-by- $N$ matrix. $M$ is the number of measuring frequencies specified in Polar pattern frequencies (Hz). $N$ is the number of measuring angles specified in Polar pattern angles (deg). Each row of the matrix represents the magnitude of the polar pattern measured at the corresponding frequency specified in Polar pattern frequencies (Hz) and all angles specified in Polar pattern angles (deg). Assume that the pattern is measured in the azimuth plane. In the azimuth plane, the elevation angle is $0^{\circ}$ and the central pickup axis is $0^{\circ}$ degrees azimuth and $0^{\circ}$ degrees elevation. Assume that the polar pattern is symmetric around the central axis. You can construct the microphone's response pattern in 3-D space from the polar pattern.

## Baffle the back of the element

This check box appears only when the Element type parameter is set to Isotropic Antenna or Omni Microphone.

Select this check box to baffle the back of the antenna element. In this case, the antenna responses to all azimuth angles beyond $\pm 90^{\circ}$ from broadside are set to zero. Define the broadside direction as $0^{\circ}$ azimuth angle and $0^{\circ}$ elevation angle.

## Ports

Note The block input and output ports correspond to the input and output parameters described in the step method of the underlying System object. See link at the bottom of this page.

| Port | Description | Supported Data Types |
| :--- | :--- | :--- |
| X | Input signal. <br> The size of the first dimension of <br> the input matrix can vary to <br> simulate a changing signal <br> length. A size change can occur, <br> for example, in the case of a <br> pulse waveform with variable <br> pulse repetition frequency. | Double-precision floating point |
| Steer | Initial estimate of arrival <br> directions. | Double-precision floating point |
| Ang | Estimate of arrival directions. | Double-precision floating point |

## Version History

Introduced in R2014b

## See Also

phased.SumDifferenceMonopulseTracker2D

# Wideband Backscatter Radar Target 

Backscatter wideband signals from radar target


## Libraries:

Phased Array System Toolbox / Environment and Target

## Description

The Wideband Backscatter Radar Target block models the monostatic reflection of nonpolarized wideband electromagnetic signals from a radar target. The target radar cross-section (RCS) model includes four Swerling target fluctuation models and a nonfluctuating model. You can model several targets simultaneously by specifying multiple radar cross-section RCS matrices.

## Ports

## Input

$\mathbf{X}$ - Wideband incident nonpolarized signal
N -by-1 complex-valued vector | N -by-M complex-valued matrix
Wideband incident nonpolarized signal, specified as an $N$-by-1 complex-valued vector or an $N$-by- $M$ complex-valued matrix. The quantity $N$ is the number of signal samples, and $M$ is the number of independent signals reflecting off the target. Each column contains an independent signal to be reflected from the target.

The size of the first dimension of the input matrix can vary to simulate a changing signal length. A size change can occur, for example, in the case of a pulse waveform with variable pulse repetition frequency.

## Data Types: double

Ang - Incident signal direction
2-by-1 real-valued column vector | 2 -by- $M$ real-valued column matrix
Incident signal direction, specified as a 2-by-1 real-valued column vector or a 2 -by- $M$ real-valued column matrix. $M$ is the number of signals reflecting from the target. Each column of Ang specifies the incident direction of the corresponding signal in the form of an
[AzimuthAngle;ElevationAngle] pair. Units are degrees. The number of columns in Ang must match the number of independent signals in X .
Example: [30;45]
Data Types: double
Update - Switch to update RCS
false|true
Switch to update RCS fluctuation model values, specified as false or true. When Update is true, the RCS value is updated. If Update is false, the RCS remains unchanged.

## Dependencies

To enable this port, set the Fluctuation model drop-down menu to Swerling1, Swerling2, Swerling3, or Swerling4.

## Output

Port_1 - Narrowband reflected signal
1-by- $M$ complex-valued vector | $N$-by- $M$ complex-valued matrix
Wideband nonpolarized signal, specified as an 1 -by- $M$ complex-valued vector or a $N$-by- $M$ complexvalued matrix. Each column contains an independent signal reflected from the target.

The quantity $N$ is the number of signal samples and $M$ is the number of signals reflecting off the target. Each column corresponds to a different reflecting angle.

The output port contains signal samples arriving at the signal destination within the current input time frame. When the propagation time from source to destination exceeds the current time frame duration, the output does not contain all contributions from the input of the current time frame.

## Parameters

## Backscatter pattern frequency vector (Hz) - Wideband backscatter pattern frequencies

## [0, 1e20] (default) | real-valued row vector of positive values in strictly increasing order

Specify the frequencies used in the RCS matrix. The elements of this vector must be in strictly increasing order. The target has no response outside this frequency range. Frequencies are defined with respect to the physical frequency band, not the baseband. Frequency units are in Hz .

## Data Types: double

## Azimuth angles (deg) - Azimuth angles

[-180:180] (default) | 1-by-P real-valued row vector | $P$-by-1 real-valued column vector
Azimuth angles used to define the angular coordinates of each column of the matrices specified by the RCS pattern ( $\mathbf{m}^{\wedge} \mathbf{2}$ ) parameter. Specify the azimuth angles as a length $P$ vector. $P$ must be greater than two. Angle units are in degrees.
Example: [-45:0.1:45]
Data Types: double
Elevation angles (deg) - Elevation angles
[-90:90] (default) | 1-by-Q real-valued row vector | $Q$-by-1 real-valued column vector

Elevation angles used to define the angular coordinates of each row of the matrices specified by the RCS pattern ( $\mathbf{m}^{\wedge} \mathbf{2}$ ) parameter. Specify the elevation angles as a length $Q$ vector. $Q$ must be greater than two. Angle units are in degrees.
Example: [-30:0.1:30]
Data Types: double

RCS pattern ( $\mathbf{m}^{\wedge} \mathbf{2}$ ) - Radar cross-section pattern
ones $(181,361)$ (default) | Q-by-P real-valued matrix | Q-by-P-by-K real-valued array | 1-by-P-by-K real-valued array | $K$-by- $P$ real-valued matrix

Radar cross-section pattern, specified as a real-valued matrix or array.

| Dimensions | Application |
| :--- | :--- |
| $Q$-by- $P$ matrix | Specifies a matrix of RCS values as a function of <br> $Q$ elevation angles and $P$ azimuth angles. The <br> same RCS matrix is used for all frequencies. |
| $Q$-by- $P$-by- $K$ array | Specifies an array of RCS patterns as a function <br> of $Q$ elevation angles, $P$ azimuth angles, and $K$ <br> frequencies. If $K=1$, the RCS pattern is <br> equivalent to a $Q$-by- $P$ matrix. |
| 1 -by- $P$-by- $K$ array | Specifies a matrix of RCS values as a function of <br> $P$ azimuth angles and $K$ frequencies. These <br> dimension formats apply when there is only one <br> elevation angle. |
| K-by- $P$ matrix |  |

- $Q$ is the length of the vector specified by the Elevation angles (deg) parameter.
- $P$ is the length of the vector specified by the Azimuth angles (deg) parameter.
- $K$ is the number of frequencies specified by the Backscatter pattern frequency vector ( Hz ) parameter.

You can specify patterns for $L$ targets by putting $L$ patterns into a cell array. All patterns must have the same dimensions. The value of $L$ must match the column dimensions of the signals passed as input into the block. You can, however, use one pattern to model $L$ multiple targets.

RCS units are in square meters.
Example: [1,2;2,1]
Data Types: double
Fluctuation model - Target fluctuation model
Nonfluctuating (default) | Swerling1 | Swerling2 | Swerling3 | Swerling4

Target fluctuation model, specified as Nonfluctuating, Swerling1, Swerling2, Swerling3, or Swerling4. If you set this parameter to a value other than Nonfluctuating, you must pass either true or false into the Update Update port.

Propagation speed (m/s) - Signal propagation speed
physconst('LightSpeed') (default)| positive scalar

Signal propagation speed, specified as a real-valued positive scalar. The default value of the speed of light is the value returned by physconst('LightSpeed').

## Data Types: double

Operating frequency ( Hz ) - Signal carrier frequency
300.0 e 6 (default) | positive real-valued scalar

Signal carrier frequency, specified as a positive real-valued scalar. Units are in hertz.
Inherit sample rate - Inherit sample rate from upstream blocks
on (default) | off

Select this parameter to inherit the sample rate from upstream blocks. Otherwise, specify the sample rate using the Sample rate ( $\mathbf{H z )}$ parameter.
Data Types: Boolean
Sample rate (Hz) - Sampling rate of signal
le6 (default) | positive real-valued scalar

Specify the signal sampling rate as a positive scalar. Units are in Hz .

## Dependencies

To enable this parameter, clear the Inherit sample rate check box.
Data Types: double
Number of subbands - Number of processing subbands
64 (default) | positive integer

Number of processing subbands, specified as a positive integer.
Example: 128
Simulate using - Block simulation method
Interpreted Execution (default)|Code Generation

Block simulation, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster with generated code than in interpreted execution. You can run repeated executions without recompiling, but if you change any block parameters, then the block automatically recompiles before execution.

This table shows how the Simulate using parameter affects the overall simulation behavior.
When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the model <br> are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).
Programmatic Use
Block Parameter:SimulateUsing
Type:enum
Values:Interpreted Execution, Code Generation
Default:Interpreted Execution

## Version History

Introduced in R2016b

## See Also

## Objects

phased.BackscatterRadarTarget | phased.RadarTarget

## Blocks

Backscatter Radar Target | Radar Target

## Wideband Free Space

Wideband free space environment


## Library

Environment and Target
phasedenvlib

## Description

The Wideband Free Space Channel block propagates the signal from one point to another in space. The block models propagation time, free space propagation loss and Doppler shift. The block assumes that the propagation speed is much greater than the target or array speed in which case the stop-andhop model is valid.

When propagating a signal in free-space to an object and back, you have the choice of either using a single block to compute a two-way free space propagation delay or two blocks to perform one-way propagation delays in each direction. Because the free-space propagation delay is not necessarily an integer multiple of the sampling interval, it may turn out that the total round trip delay in samples when you use a two-way propagation block differs from the delay in samples when you use two oneway propagation blocks. For this reason, it is recommended that, when possible, you use a single twoway propagation block.

## Parameters

## Signal Propagation speed (m/s)

Specify the propagation speed of the signal, in meters per second, as a positive scalar. You can use the function physconst to specify the speed of light.

## Signal carrier frequency (Hz)

Specify the carrier frequency of the signal in hertz of the narrowband signal as a positive scalar.

## Number of subbands

The number of subbands used for subband processing, specified as a positive integer.

## Perform two-way propagation

Select this check box to perform round-trip propagation between the origin and destination. Otherwise the block performs one-way propagation from the origin to the destination.

## Inherit sample rate

Select this check box to inherit the sample rate from upstream blocks. Otherwise, specify the sample rate using the Sample rate (Hz) parameter.

## Sample rate (Hz)

Specify the signal sampling rate (in hertz) as a positive scalar. This parameter appears only when the Inherit sample rate parameter is not selected.

## Maximum one-way propagation distance (m)

The maximum distance , in meters, between the origin and the destination as a positive scalar. Amplitudes of any signals that propagate beyond this distance will be set to zero.

## Simulate using

Block simulation method, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster than they would in interpreted execution. You can run repeated executions without recompiling. However, if you change any block parameters, then the block automatically recompiles before execution.

When setting this parameter, you must take into account the overall model simulation mode. The table shows how the Simulate using parameter interacts with the overall simulation mode.

When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the <br> model are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).

## Ports

Note The block input and output ports correspond to the input and output parameters described in the step method of the underlying System object. See link at the bottom of this page.

| Port | Description | Supported Data Types |
| :--- | :--- | :--- |
| $X$ | Input signal. | Double-precision floating point |
| Pos1 | Signal source position. | Double-precision floating point |
| Pos2 | Signal destination position. | Double-precision floating point |


| Port | Description | Supported Data Types |
| :--- | :--- | :--- |
| Vel1 | Signal source velocity. | Double-precision floating point |
| Vel2 | Signal destination velocity. | Double-precision floating point |
| Out | Propagated signal. | Double-precision floating point |

## Algorithms

When the origin and destination are stationary relative to each other, the block output can be written as $y(t)=x(t-\tau) / L$. The quantity $\tau$ is the delay and $L$ is the propagation loss. The delay is computed from $\tau=R / c$ where $R$ is the propagation distance and $c$ is the propagation speed. The free space path loss is given by

$$
L_{f s p}=\frac{(4 \pi R)^{2}}{\lambda^{2}}
$$

where $\lambda$ is the signal wavelength.
This formula assumes that the target is in the far-field of the transmitting element or array. In the near-field, the free-space path loss formula is not valid and can result in losses smaller than one, equivalent to a signal gain. For this reason, the loss is set to unity for range values, $R \leq \lambda / 4 \pi$.

When there is relative motion between the origin and destination, the processing also introduces a frequency shift. This shift corresponds to the Doppler shift between the origin and destination. The frequency shift is $v / \lambda$ for one-way propagation and $2 v / \lambda$ for two-way propagation. The parameter $v$ is the relative speed of the destination with respect to the origin.

## Version History

Introduced in R2015b

## See Also

phased.WidebandFreeSpace

## Wideband LOS Channel

## Wideband line-of-sight propagation channel



## Library

Environment and Target
phasedenvlib

## Description

The Wideband LOS Channel block propagates signals from one point in space to multiple points or from multiple points back to one point via line-of-sight (LOS) channels. The block models propagation time, free-space propagation loss, Doppler shift, and atmospheric as well as weather loss. The block assumes that the propagation speed is much greater than the object's speed in which case the stop-and-hop model is valid.

When propagating a signal in an LOS channel to an object and back, you have the choice of either using a single block to compute two-way LOS channel propagation delay or two blocks to perform one-way propagation delays in each direction. Because the LOS channel propagation delay is not necessarily an integer multiple of the sampling interval, it may turn out that the total round trip delay in samples when you use a two-way propagation block differs from the delay in samples when you use two one-way propagation blocks. For this reason, it is recommended that, when possible, you use a single two-way propagation block.

## Parameters

## Signal Propagation speed (m/s)

Specify the propagation speed of the signal, in meters per second, as a positive scalar. You can use the function physconst to specify the speed of light.

## Signal carrier frequency (Hz)

Specify the carrier frequency of the signal in hertz of the narrowband signal as a positive scalar.

## Number of subbands

The number of subbands used for subband processing, specified as a positive integer.

## Specify atmospheric parameters

Select this check box to enable atmospheric attenuation modeling.

## Temperature (degrees Celsius)

Ambient atmospheric temperature, specified as a real-valued scalar. Units are degrees Celsius. This parameter appears when you select the Specify atmospheric parameters check box. Units are degrees Celsius.

## Dry air pressure (Pa)

Atmospheric dry air pressure, specified as a positive real-valued scalar. Units are Pascals (Pa). The value 101325 for this property corresponds to one standard atmosphere. This parameter appears when you select the Specify atmospheric parameters check box.

## Water vapour density ( $\mathrm{g} / \mathrm{m}^{\wedge} 3$ )

Atmospheric water vapor density, specified as a positive real-valued scalar. Units are $\mathrm{gm} / \mathrm{m}^{3}$. This parameter appears when you select the Specify atmospheric parameters check box.

## Liquid water density ( $\mathrm{g} / \mathrm{m}^{\wedge} 3$ )

Liquid water density of fog or clouds, specified as a non-negative real-valued scalar. Units are $\mathrm{gm} / \mathrm{m}^{3}$. Typical values for liquid water density are 0.05 for medium fog and 0.5 for thick fog. This parameter appears when you select the Specify atmospheric parameters check box.

## Rain rate (mm/hr)

Rainfall rate, specified as a non-negative real-valued scalar. Units are in mm/hour. This parameter appears when you select the Specify atmospheric parameters check box.

## Perform two-way propagation

Select this check box to perform round-trip propagation between the origin and destination. Otherwise the block performs one-way propagation from the origin to the destination.

## Inherit sample rate

Select this check box to inherit the sample rate from upstream blocks. Otherwise, specify the sample rate using the Sample rate (Hz) parameter.

## Sample rate (Hz)

Specify the signal sampling rate (in hertz) as a positive scalar. This parameter appears only when the Inherit sample rate parameter is not selected.

## Maximum one-way propagation distance (m)

The maximum distance between the signal origin and the destination, specified as a positive scalar. Units are in meters. Amplitudes of any signals that propagate beyond this distance will be set to zero.

## Simulate using

Block simulation method, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster than they would in interpreted execution. You can run repeated executions without recompiling. However, if you change any block parameters, then the block automatically recompiles before execution.

When setting this parameter, you must take into account the overall model simulation mode. The table shows how the Simulate using parameter interacts with the overall simulation mode.

When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the <br> model are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).

## Ports

Note The block input and output ports correspond to the input and output parameters described in the step method of the underlying System object. See link at the bottom of this page.

| Port | Description | Supported Data Types |
| :--- | :--- | :--- |
| X | Input signal. | Double-precision floating point |
| Pos1 | Signal source position. | Double-precision floating point |
| Pos2 | Signal destination position. | Double-precision floating point |
| Vel1 | Signal source velocity. | Double-precision floating point |
| Vel2 | Signal destination velocity. | Double-precision floating point |
| Out | Propagated signal. | Double-precision floating point |

## More About

## Attenuation and Loss Factors

Attenuation or path loss in the Wideband LOS channel consists of four components. $L=L_{f s p} L_{g} L_{c} L_{r}$, where

- $L_{f s p}$ is the free-space path attenuation
- $L_{g}$ is the atmospheric path attenuation
- $L_{c}$ is the fog and cloud path attenuation
- $L_{r}$ is the rain path attenuation

Each component is in magnitude units, not in dB.

## Propagation Delay, Doppler, and Free-Space Path Loss

When the origin and destination are stationary relative to each other, you can write the output signal of a free-space channel as $Y(t)=x(t-\tau) / L_{f s p}$. The quantity $\tau$ is the signal delay and $L_{f s p}$ is the free-space path loss. The delay $\tau$ is given by $R / c$, where $R$ is the propagation distance and $c$ is the propagation speed. The free-space path loss is given by

$$
L_{f s p}=\frac{(4 \pi R)^{2}}{\lambda^{2}},
$$

where $\lambda$ is the signal wavelength.
This formula assumes that the target is in the far field of the transmitting element or array. In the near field, the free-space path loss formula is not valid and can result in a loss smaller than one, equivalent to a signal gain. Therefore, the loss is set to unity for range values, $R \leq \lambda / 4 \pi$.

When the origin and destination have relative motion, the processing also introduces a Doppler frequency shift. The frequency shift is $v / \lambda$ for one-way propagation and $2 v / \lambda$ for two-way propagation. The quantity $v$ is the relative speed of the destination with respect to the origin.

## Atmospheric Gas Attenuation Model

This model calculates the attenuation of signals that propagate through atmospheric gases.
Electromagnetic signals attenuate when they propagate through the atmosphere. This effect is due primarily to the absorption resonance lines of oxygen and water vapor, with smaller contributions coming from nitrogen gas. The model also includes a continuous absorption spectrum below 10 GHz . The ITU model Recommendation ITU-R P.676-10: Attenuation by atmospheric gases is used. The model computes the specific attenuation (attenuation per kilometer) as a function of temperature, pressure, water vapor density, and signal frequency. The atmospheric gas model is valid for frequencies from 1-1000 GHz and applies to polarized and nonpolarized fields.

The formula for specific attenuation at each frequency is

$$
\gamma=\gamma_{0}(f)+\gamma_{w}(f)=0.1820 f N^{\prime \prime}(f) .
$$

The quantity $N^{\prime \prime}()$ is the imaginary part of the complex atmospheric refractivity and consists of a spectral line component and a continuous component:

$$
N^{\prime \prime}(f)=\sum_{i} S_{i} F_{i}+N^{\prime \prime}{ }_{D}(f)
$$

The spectral component consists of a sum of discrete spectrum terms composed of a localized frequency bandwidth function, $F(f)_{i}$, multiplied by a spectral line strength, $S_{\mathrm{i}}$. For atmospheric oxygen, each spectral line strength is

$$
S_{i}=a_{1} \times 10^{-7}\left(\frac{300}{T}\right)^{3} \exp \left[a_{2}\left(1-\left(\frac{300}{T}\right)\right] P .\right.
$$

For atmospheric water vapor, each spectral line strength is

$$
S_{i}=b_{1} \times 10^{-1}\left(\frac{300}{T}\right)^{3.5} \exp \left[b_{2}\left(1-\left(\frac{300}{T}\right)\right] W .\right.
$$

$P$ is the dry air pressure, $W$ is the water vapor partial pressure, and $T$ is the ambient temperature. Pressure units are in hectoPascals ( hPa ) and temperature is in degrees Kelvin. The water vapor partial pressure, $W$, is related to the water vapor density, $\rho$, by

$$
W=\frac{\rho T}{216.7} .
$$

The total atmospheric pressure is $P+W$.

For each oxygen line, $S_{i}$ depends on two parameters, $a_{1}$ and $a_{2}$. Similarly, each water vapor line depends on two parameters, $b_{1}$ and $b_{2}$. The ITU documentation cited at the end of this section contains tabulations of these parameters as functions of frequency.

The localized frequency bandwidth functions $F_{i}(f)$ are complicated functions of frequency described in the ITU references cited below. The functions depend on empirical model parameters that are also tabulated in the reference.

To compute the total attenuation for narrowband signals along a path, the function multiplies the specific attenuation by the path length, $R$. Then, the total attenuation is $L_{g}=R\left(\gamma_{o}+\gamma_{w}\right)$.

You can apply the attenuation model to wideband signals. First, divide the wideband signal into frequency subbands, and apply attenuation to each subband. Then, sum all attenuated subband signals into the total attenuated signal.

## Fog and Cloud Attenuation Model

This model calculates the attenuation of signals that propagate through fog or clouds.
Fog and cloud attenuation are the same atmospheric phenomenon. The ITU model, Recommendation ITU-R P.840-6: Attenuation due to clouds and fog is used. The model computes the specific attenuation (attenuation per kilometer), of a signal as a function of liquid water density, signal frequency, and temperature. The model applies to polarized and nonpolarized fields. The formula for specific attenuation at each frequency is

$$
\gamma_{C}=K_{l}(f) M,
$$

where $M$ is the liquid water density in $\mathrm{gm} / \mathrm{m}^{3}$. The quantity $K_{l}(f)$ is the specific attenuation coefficient and depends on frequency. The cloud and fog attenuation model is valid for frequencies $10-1000 \mathrm{GHz}$. Units for the specific attenuation coefficient are $(\mathrm{dB} / \mathrm{km}) /\left(\mathrm{g} / \mathrm{m}^{3}\right)$.

To compute the total attenuation for narrowband signals along a path, the function multiplies the specific attenuation by the path length $R$. Total attenuation is $L_{c}=R \gamma_{c}$.

You can apply the attenuation model to wideband signals. First, divide the wideband signal into frequency subbands, and apply narrowband attenuation to each subband. Then, sum all attenuated subband signals into the total attenuated signal.

## Rainfall Attenuation Model

This model calculates the attenuation of signals that propagate through regions of rainfall. Rain attenuation is a dominant fading mechanism and can vary from location-to-location and from year-toyear.

Electromagnetic signals are attenuated when propagating through a region of rainfall. Rainfall attenuation is computed according to the ITU rainfall model Recommendation ITU-R P.838-3: Specific attenuation model for rain for use in prediction methods. The model computes the specific attenuation (attenuation per kilometer) of a signal as a function of rainfall rate, signal frequency, polarization, and path elevation angle. The specific attenuation, $\gamma_{R}$, is modeled as a power law with respect to rain rate

$$
\gamma_{R}=k R^{\alpha},
$$

where $R$ is rain rate. Units are in $\mathrm{mm} / \mathrm{hr}$. The parameter $k$ and exponent $\alpha$ depend on the frequency, the polarization state, and the elevation angle of the signal path. The specific attenuation model is valid for frequencies from 1-1000 GHz.

To compute the total attenuation for narrowband signals along a path, the function multiplies the specific attenuation by the an effective propagation distance, $d_{\text {eff. }}$. Then, the total attenuation is $L=$ $d_{\text {eff }} Y_{R}$.

The effective distance is the geometric distance, $d$, multiplied by a scale factor

$$
r=\frac{1}{0.477 d^{0.633} R_{0.01}^{0.073 \alpha} f^{0.123}-10.579(1-\exp (-0.024 d))}
$$

where $f$ is the frequency. The article Recommendation ITU-R P.530-17 (12/2017): Propagation data and prediction methods required for the design of terrestrial line-of-sight systems presents a complete discussion for computing attenuation.

The rain rate, $R$, used in these computations is the long-term statistical rain rate, $R_{0.01}$. This is the rain rate that is exceeded $0.01 \%$ of the time. The calculation of the statistical rain rate is discussed in Recommendation ITU-R P.837-7 (06/2017): Characteristics of precipitation for propagation modelling. This article also explains how to compute the attenuation for other percentages from the $0.01 \%$ value.

You can apply the attenuation model to wideband signals. First, divide the wideband signal into frequency subbands and apply attenuation to each subband. Then, sum all attenuated subband signals into the total attenuated signal.

## Subband Frequency Processing

Subband processing decomposes a wideband signal into multiple subbands and applies narrowband processing to the signal in each subband. The signals for all subbands are summed to form the output signal.

When using wideband frequency System objects or blocks, you specify the number of subbands, $N_{\mathrm{B}}$, in which to decompose the wideband signal. Subband center frequencies and widths are automatically computed from the total bandwidth and number of subbands. The total frequency band is centered on the carrier or operating frequency, $f_{c}$. The overall bandwidth is given by the sample rate, $f_{s}$. Frequency subband widths are $\Delta f=f_{s} / N_{\mathrm{B}}$. The center frequencies of the subbands are

$$
f_{m}=\left\{\begin{array}{c}
f_{c}-\frac{f_{s}}{2}+(m-1) \Delta f, \quad N_{B} \text { even } \\
f_{c}-\frac{\left(N_{B}-1\right) f_{s}}{2 N_{B}}+(m-1) \Delta f, \quad N_{B} \text { odd }
\end{array}, \quad m=1, \ldots, N_{B}\right.
$$

Some System objects let you obtain the subband center frequencies as output when you run the object. The returned subband frequencies are ordered consistently with the ordering of the discrete Fourier transform. Frequencies above the carrier appear first, followed by frequencies below the carrier.

## Version History

## Introduced in R2016a

## See Also

## Objects

phased.WidebandLOSChannel|phased.LOSChannel

# Wideband Receive Array 

Wideband receive array


## Library

Transmitters and Receivers
phasedtxrxlib

## Description

The Wideband Receive Array block receives wideband plane waves incident on the elements of a sensor array. The block divides the input signal into subbands and then applies a phase shift in each subband according to the incident direction. The resulting subband signals are then combined to form the output.

## Parameters

## Signal Propagation speed (m/s)

Specify the propagation speed of the signal, in meters per second, as a positive scalar. You can use the function physconst to specify the speed of light.

## Inherit sample rate

Select this check box to inherit the sample rate from upstream blocks. Otherwise, specify the sample rate using the Sample rate (Hz) parameter.

## Sample rate (Hz)

Specify the signal sampling rate (in hertz) as a positive scalar. This parameter appears only when the Inherit sample rate parameter is not selected.

## Assume modulated input

Select this check this box to indicate that the input signal is demodulated at a carrier frequency.

## Carrier frequency

This parameter appears when the Assume modulated input check box is selected. The parameter specifies the carrier frequency, in hertz, as a positive scalar.

## Number of subbands

Number of processing subbands, specified as a positive integer.

## Sensor gain measure

Sensor gain measure, specified as dB or dBi.

- When you set this parameter to dB , the input signal power is scaled by the sensor power pattern (in dB ) at the corresponding direction and then combined.
- When you set this parameter to dBi , the input signal power is scaled by the directivity pattern (in dBi ) at the corresponding direction and then combined. This option is useful when you want to compare results with the values computed by the radar equation that uses dBi to specify the antenna gain. The computation using the dBi option is expensive as it requires an integration over all directions to compute the total radiated power of the sensor. The default value is dB .


## Enable weights input

Select this check box to specify array weights using the input port W . The input port appears only when this box is checked.

## Simulate using

Block simulation method, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster than they would in interpreted execution. You can run repeated executions without recompiling. However, if you change any block parameters, then the block automatically recompiles before execution.

When setting this parameter, you must take into account the overall model simulation mode. The table shows how the Simulate using parameter interacts with the overall simulation mode.

When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the <br> model are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).

## Array Parameters

## Specify sensor array as

Specify sensor element or sensor array. A sensor array can also contain subarrays or be a partitioned array. This parameter can also be expressed as a MATLAB expression.

Types
Single element
Array (no subarrays)
Partitioned array
Replicated subarray
MATLAB expression

## Geometry

Specify the array geometry as one of the following:

- ULA - Uniform linear array
- URA - Uniform rectangular array
- UCA - Uniform circular array
- Conformal Array - arbitrary element positions


## Number of elements

Number of array elements.
Number of array elements, specified as a positive integer. This parameter appears when the Geometry is set to ULA or UCA. If Sensor Array has a Replicated subarray option, this parameter applies to the subarray.

## Array size

This parameter appears when Geometry is set to URA. When Sensor Array is set to Replicated subarray, this parameter applies to the subarrays.

Specify the size of the array as a positive integer or 1-by-2 vector of positive integers.

- If Array size is a 1 -by- 2 vector, the vector has the form [NumberOfArrayRows, NumberOfArrayColumns].
- If Array size is an integer, the array has the same number of rows and columns.

For a URA, elements are indexed from top to bottom along a column and continuing to the next columns from left to right. In this figure, an Array size of [3,2] produces an array of three rows and two columns.

Size and Element Indexing Order
for Uniform Rectangular Arrays
Example: Size = [3,2]


## Element spacing (m)

This parameter appears when Geometry is set to ULA or URA. When Sensor Array has the Replicated subarray option, this parameter applies to the subarrays.

- For a ULA, specify the spacing, in meters, between two adjacent elements in the array as a scalar.
- For a URA, specify the element spacing of the array, in meters, as a 1 -by-2 vector or a scalar. If Element spacing is a 1 -by-2 vector, the vector has the form
[SpacingBetweenRows, SpacingBetweenColumns]. For a discussion of these quantities, see phased.URA. If Element spacing is a scalar, the spacings between rows and columns are equal.


## Array axis

This parameter appears when the Geometry parameter is set to ULA or when the block only supports a ULA array geometry. Specify the array axis as $x, y$, or $z$. All ULA array elements are uniformly spaced along this axis in the local array coordinate system.

## Array normal

This parameter appears when you set Geometry to URA or UCA. Specify the Array normal as x, $y$, or $z$. All URA and UCA array elements are placed in the $y z, z x$, or $x y$-planes, respectively, of the array coordinate system.

## Radius of UCA (m)

Radius of a uniform circular array specified as a positive scalar. Units are meters.
This parameter appears when the Geometry is set to UCA.

## Taper

Tapers, also known as element weights, are applied to sensor elements in the array. Tapers are used to modify both the amplitude and phase of the transmitted or received data.

This parameter applies to all array types, but when you set Sensor Array to Replicated subarray, this parameter applies to subarrays.

- For a ULA or UCA, specify element tapering as a complex-valued scalar or a complex-valued 1-by- $N$ row vector. In this vector, $N$ represents the number of elements in the array. If Taper is a scalar, the same weight is applied to each element. If Taper is a vector, a weight from the vector is applied to the corresponding sensor element. A weight must be applied to each element in the sensor array.
- For a URA, specify element tapering as a complex-valued scalar or complex-valued $M$-by- $N$ matrix. In this matrix, $M$ is the number of elements along the $z$-axis, and $N$ is the number of elements along the $y$-axis. $M$ and $N$ correspond to the values of
[NumberofArrayRows, NumberOfArrayColumns] in the Array size matrix. If Taper is a scalar, the same weight is applied to each element. If Taper is a matrix, a weight from the matrix is applied to the corresponding sensor element. A weight must be applied to each element in the sensor array.
- For a Conformal Array, specify element tapering as a complex-valued scalar or complexvalued 1 -by- $N$ vector. In this vector, $N$ is the number of elements in the array as determined by the size of the Element positions vector. If Taper is a scalar, the same weight is applied to each element. If the value of Taper is a vector, a weight from the vector is applied to the corresponding sensor element. A weight must be applied to each element in the sensor array.


## Element lattice

This parameter appears when Geometry is set to URA. When Sensor Array is set to Replicated subarray, this parameter applies to the subarray.

Specify the element lattice as Rectangular or Triangular

- Rectangular - Aligns all the elements in row and column directions.
- Triangular - Shifts the even-row elements of a rectangular lattice toward the positive-row axis direction. The displacement is one-half the element spacing along the row dimension.


## Element positions (m)

This parameter appears when Geometry is set to Conformal Array. When Sensor Array is set to Replicated subarray, this parameter applies to subarrays.

Specify the positions of conformal array elements as a 3 -by- $N$ matrix, where $N$ is the number of elements in the conformal array. Each column of Element positions (m) represents the position of a single element, in the form [ $x ; y ; z$ ], in the array's local coordinate system. The local coordinate system has its origin at an arbitrary point. Units are in meters.

## Element normals (deg)

This parameter appears when Geometry is set to Conformal Array. When Sensor Array is set to Replicated subarray, this parameter applies to subarrays.

Specify the normal directions of the elements in a conformal array as a 2 -by- $N$ matrix or a 2 -by- 1 column vector in degrees. The variable $N$ indicates the number of elements in the array. If Element normals (deg) is a matrix, each column specifies the normal direction of the corresponding element in the form [azimuth; elevation], with respect to the local coordinate system. The local coordinate system aligns the positive $x$-axis with the direction normal to the conformal array. If Element normals (deg) is a 2-by-1 column vector, the vector specifies the same pointing direction for all elements in the array.

You can use the Element positions (m) and Element normals (deg) parameters to represent any arrangement in which pairs of elements differ by certain transformations. You can combine translation, azimuth rotation, and elevation rotation transformations. However, you cannot use transformations that require rotation about the normal.

## Subarray definition matrix

This parameter appears when Specify sensor array as is set to Partitioned array.
Specify the subarray selection as an $M$-by- $N$ matrix. $M$ is the number of subarrays and $N$ is the total number of elements in the array. Each row of the matrix corresponds to a subarray and each entry in the row indicates whether or not an element belongs to the subarray. When the entry is zero, the element does not belong the subarray. A nonzero entry represents a complex-valued weight applied to the corresponding element. Each row must contain at least one nonzero entry.

The phase center of each subarray is its geometric center. Subarray definition matrix and Geometry determine the geometric center.

## Subarray steering method

This parameter appears when the Specify sensor array as parameter is set to Partitioned array or Replicated subarray.

Specify the subarray steering method as either

- None
- Phase
- Time
- Custom

Selecting Phase or Time opens the Steer input port on the Narrowband Receive Array, Narrowband Transmit Array, Wideband Receive Array, Wideband Transmit Array blocks, Constant Gamma Clutter, and GPU Constant Gamma Clutter blocks.

Selecting Custom opens the WS input port on the Narrowband Receive Array, Narrowband Transmit Array, Wideband Receive Array, Wideband Transmit Array blocks, Constant Gamma Clutter, and GPU Constant Gamma Clutter blocks.
Phase shifter frequency (Hz)
This parameter appears when you set Sensor array to Partitioned array or Replicated subarray and you set Subarray steering method to Phase.

Specify the operating frequency, in hertz, of phase shifters to perform subarray steering as a positive scalar.

## Number of bits in phase shifters

This parameter appears when you set Sensor array to Partitioned array or Replicated subarray and you set Subarray steering method to Phase.

The number of bits used to quantize the phase shift component of beamformer or steering vector weights. Specify the number of bits as a non-negative integer. A value of zero indicates that no quantization is performed.

## Subarrays layout

This parameter appears when you set Sensor array to Replicated subarray.
Specify the layout of the replicated subarrays as Rectangular or Custom.
Grid size
This parameter appears when you set Sensor array to Replicated subarray and Subarrays layout to Rectangular.

Rectangular subarray grid size, specified as a single positive integer or a positive integer-valued 1-by-2 row vector.

If Grid size is an integer scalar, the array has an equal number of subarrays in each row and column. If Grid size is a 1 -by- 2 vector of the form [NumberOfRows, NumberOfColumns], the first entry is the number of subarrays along each column. The second entry is the number of subarrays in each row. A row is along the local $y$-axis, and a column is along the local $z$-axis. The figure here shows how you can replicate a 3-by-2 URA subarray using a Grid size of [1,2].
$3 \times 2$ Element URA
Replicated on a $1 \times 2$ Grid


## Grid spacing

This parameter appears when you set Sensor array to Replicated subarray and Subarrays layout to Rectangular.

Specify the rectangular grid spacing of subarrays as a real-valued positive scalar, a 1-by-2 row vector, or Auto. Grid spacing units are expressed in meters.

- If Grid spacing is a scalar, the spacing along the row and the spacing along the column is the same.
- If Grid spacing is a 1 -by-2 row vector, the vector has the form [SpacingBetweenRows, SpacingBetweenColumn]. The first entry specifies the spacing between rows along a column. The second entry specifies the spacing between columns along a row.
- If Grid spacing is set to Auto, replication preserves the element spacing of the subarray for both rows and columns while building the full array. This option is available only when you specify Geometry as ULA or URA.


## Subarray positions (m)

This parameter appears when you set Sensor array to Replicated subarray and Subarrays layout to Custom.

Specify the positions of the subarrays in the custom grid as a 3 -by- $N$ matrix, where $N$ is the number of subarrays in the array. Each column of the matrix represents the position of a single subarray, in meters, in the array's local coordinate system. The coordinates are expressed in the form [x; y; z].
Subarray normals
This parameter appears when you set the Sensor array parameter to Replicated subarray and the Subarrays layout to Custom.

Specify the normal directions of the subarrays in the array. This parameter value is a 2 -by- $N$ matrix, where $N$ is the number of subarrays in the array. Each column of the matrix specifies the normal direction of the corresponding subarray, in the form [azimuth; elevation]. Each angle is in degrees and is defined in the local coordinate system.

You can use the Subarray positions and Subarray normals parameters to represent any arrangement in which pairs of subarrays differ by certain transformations. The transformations can combine translation, azimuth rotation, and elevation rotation. However, you cannot use transformations that require rotation about the normal.

## Expression

A valid MATLAB expression containing an array constructor, for example, phased.URA.

## Sensor Array Tab: Element Parameters

## Element type

Specify antenna or microphone type as

- Isotropic Antenna
- Cosine Antenna
- Custom Antenna
- Omni Microphone
- Custom Microphone


## Exponent of cosine pattern

This parameter appears when you set Element type to Cosine Antenna.
Specify the exponent of the cosine pattern as a scalar or a 1-by-2 vector. You must specify all values as non-negative real numbers. When you set Exponent of cosine pattern to a scalar, both the azimuth direction cosine pattern and the elevation direction cosine pattern are raised to the specified value. When you set Exponent of cosine pattern to a 1-by-2 vector, the first element is the exponent for the azimuth direction cosine pattern and the second element is the exponent for the elevation direction cosine pattern.

## Operating frequency range ( Hz )

This parameter appears when Element type is set to Isotropic Antenna, Cosine Antenna, or Omni Microphone.

Specify the operating frequency range, in hertz, of the antenna element as a 1-by-2 row vector in the form [LowerBound, UpperBound]. The antenna element has no response outside the specified frequency range.
Operating frequency vector $(\mathrm{Hz})$
This parameter appears when Element type is set to Custom Antenna or Custom Microphone.

Specify the frequencies, in Hz , at which to set the antenna and microphone frequency responses as a 1 -by-L row vector of increasing values. Use Frequency responses to set the frequency responses. The antenna or microphone element has no response outside the frequency range specified by the minimum and maximum elements of Operating frequency vector ( Hz ).

## Frequency responses (dB)

This parameter appears when Element type is set to Custom Antenna or Custom Microphone.

Specify this parameter as the frequency response of an antenna or microphone, in decibels, for the frequencies defined by Operating frequency vector (Hz). Specify Frequency responses (dB) as a 1 -by-L vector matching the dimensions of the vector specified in Operating frequency vector (Hz).

## Input Pattern Coordinate System

Coordinate system of custom antenna pattern, specified az-el or phi-theta. When you specify az-el, use the Azimuth angles (deg) and Elevations angles (deg) parameters to specify the coordinates of the pattern points. When you specify phi-theta, use the Phi angles (deg) and Theta angles (deg) parameters to specify the coordinates of the pattern points.

## Azimuth angles (deg)

This parameter appears when Element type is set to Custom Antenna and the Input Pattern Coordinate System parameter is set to az-el.

Specify the azimuth angles at which to calculate the antenna radiation pattern as a 1-by- $P$ row vector. $P$ must be greater than 2 . Angle units are in degrees. Azimuth angles must lie between $180^{\circ}$ and $180^{\circ}$ and be in strictly increasing order.

## Elevation angles (deg)

This parameter appears when Element type is set to Custom Antenna and the Input Pattern Coordinate System parameter is set to az-el.

Specify the elevation angles at which to compute the radiation pattern as a 1-by- $Q$ vector. $Q$ must be greater than 2. Angle units are in degrees. Elevation angles must lie between $-90^{\circ}$ and $90^{\circ}$ and be in strictly increasing order.

## Phi Angles (deg)

This parameter appears when Element type is set to Custom Antenna and the Input Pattern Coordinate System parameter is set to phi-theta.

Phi angles of points at which to specify the antenna radiation pattern, specify as a 1-by-P row vector. $P$ must be greater than 2 . Angle units are in degrees. Phi angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Theta Angles (deg)

This parameter appears when Element type is set to Custom Antenna and the Input Pattern Coordinate System parameter is set to phi-theta.

Theta angles of points at which to specify the antenna radiation pattern, specify as a 1-by- $Q$ row vector. $Q$ must be greater than 2 . Angle units are in degrees. Theta angles must lie between $0^{\circ}$ and $180^{\circ}$ and be in strictly increasing order.

## Magnitude pattern (dB)

This parameter appears when the Element type is set to Custom Antenna.
Magnitude of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$ -by-L array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector ( $\mathbf{H z}$ ).

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (Hz) parameter.


## Phase pattern (dB)

This parameter appears when the Element type is set to Custom Antenna.
Phase of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector $(\mathbf{H z})$.

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (Hz) parameter.
- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (Hz) parameter.


## MatchArrayNormal

This parameter appears when the Element type is set to Custom Antenna.
Select this check box to rotate the antenna element pattern to align with the array normal. When not selected, the element pattern is not rotated.

When the antenna is used in an antenna array and the Input Pattern Coordinate System parameter is az-el, selecting this check box rotates the pattern so that the $x$-axis of the element coordinate system points along the array normal. Not selecting uses the element pattern without the rotation.

When the antenna is used in an antenna array and Input Pattern Coordinate System is set to phi-theta, selecting this check box rotates the pattern so that the $z$-axis of the element coordinate system points along the array normal.

Use the parameter in conjunction with the Array normal parameter of the URA and UCA arrays.

## Polar pattern frequencies (Hz)

This parameter appears when the Element type is set to Custom Microphone.

Specify the measuring frequencies of the polar patterns as a 1 -by- $M$ vector. The measuring frequencies lie within the frequency range specified by the Operating frequency vector ( $\mathbf{H z}$ ) parameter. Frequency units are in Hz.

## Polar pattern angles (deg)

This parameter appears when Element type is set to Custom Microphone.
Specify the measuring angles of the polar patterns, as a 1 -by- $N$ vector. The angles are measured from the central pickup axis of the microphone, and must be between $-180^{\circ}$ and $180^{\circ}$, inclusive.

## Polar pattern (dB)

This parameter appears when Element type is set to Custom Microphone.
Specify the magnitude of the microphone element polar pattern as an $M$-by- $N$ matrix. $M$ is the number of measuring frequencies specified in Polar pattern frequencies (Hz). $N$ is the number of measuring angles specified in Polar pattern angles (deg). Each row of the matrix represents the magnitude of the polar pattern measured at the corresponding frequency specified in Polar pattern frequencies (Hz) and all angles specified in Polar pattern angles (deg). Assume that the pattern is measured in the azimuth plane. In the azimuth plane, the elevation angle is $0^{\circ}$ and the central pickup axis is $0^{\circ}$ degrees azimuth and $0^{\circ}$ degrees elevation. Assume that the polar pattern is symmetric around the central axis. You can construct the microphone's response pattern in 3-D space from the polar pattern.
Baffle the back of the element
This check box appears only when the Element type parameter is set to Isotropic Antenna or Omni Microphone.

Select this check box to baffle the back of the antenna element. In this case, the antenna responses to all azimuth angles beyond $\pm 90^{\circ}$ from broadside are set to zero. Define the broadside direction as $0^{\circ}$ azimuth angle and $0^{\circ}$ elevation angle.

## Ports

Note The block input and output ports correspond to the input and output parameters described in the step method of the underlying System object. See link at the bottom of this page.

| Port | Description | Supported Data Types |
| :--- | :--- | :--- |
| X | Arriving signals input port <br> The size of the first dimension of <br> the input matrix can vary to <br> simulate a changing signal <br> length. A size change can occur, <br> for example, in the case of a <br> pulse waveform with variable <br> pulse repetition frequency. | Double-precision floating point |
| Ang | Incident directions of signals <br> input port. | Double-precision floating point |


| Port | Description | Supported Data Types |
| :--- | :--- | :--- |
| W | Array or subarray weights input <br> port. To enable this port, select <br> the Enable weights input <br> check box. | Double-precision floating point |
| WS | Subarray element weights input <br> port. To enable this port select <br> Custom from the Subarray <br> steering method pull down <br> menu. |  |
| Steer | Steering angle input port. To <br> enable this port, select Phase <br> or Time from the Subarray <br> steering method pull down <br> menu. | Double-precision floating point |
| Out | Collected signals | Double-precision floating point |

## Version History

Introduced in R2014b

## See Also

phased.WidebandCollector

# Wideband Transmit Array 

Wideband transmit array



## Library

Transmitters and Receivers
phasedtxrxlib

## Description

The Wideband Transmit Array block transmits wideband plane waves from the elements of a sensor array. The block divides the transmitted signals into subbands and then applies a phase shift for each subband according to the radiating direction. The resulting subband signals are then combined to form the output.

## Parameters

## Signal Propagation speed (m/s)

Specify the propagation speed of the signal, in meters per second, as a positive scalar. You can use the function physconst to specify the speed of light.

## Inherit sample rate

Select this check box to inherit the sample rate from upstream blocks. Otherwise, specify the sample rate using the Sample rate (Hz) parameter.

## Sample rate (Hz)

Specify the signal sampling rate (in hertz) as a positive scalar. This parameter appears only when the Inherit sample rate parameter is not selected.

## Assume modulated input

Select this check this box to indicate that the input signal is demodulated at a carrier frequency.

## Carrier frequency

This parameter appears when the Assume modulated input check box is selected. The parameter specifies the carrier frequency, in hertz, as a positive scalar.

## Number of subbands

The number of subbands used for subband processing, specified as a positive integer.

## Sensor gain measure

Sensor gain measure, specified as dB or dBi.

- When you set this parameter to dB , the input signal power is scaled by the sensor power pattern (in dB ) at the corresponding direction and then combined.
- When you set this parameter to dBi , the input signal power is scaled by the directivity pattern (in dBi ) at the corresponding direction and then combined. This option is useful when you want to compare results with the values computed by the radar equation that uses dBi to specify the antenna gain. The computation using the dBi option is expensive as it requires an integration over all directions to compute the total radiated power of the sensor. The default value is dB .


## Enable weights input

Select this check box to specify array weights using the input port W . The input port appears only when this box is checked.

## Simulate using

Block simulation method, specified as Interpreted Execution or Code Generation. If you want your block to use the MATLAB interpreter, choose Interpreted Execution. If you want your block to run as compiled code, choose Code Generation. Compiled code requires time to compile but usually runs faster.

Interpreted execution is useful when you are developing and tuning a model. The block runs the underlying System object in MATLAB. You can change and execute your model quickly. When you are satisfied with your results, you can then run the block using Code Generation. Long simulations run faster than they would in interpreted execution. You can run repeated executions without recompiling. However, if you change any block parameters, then the block automatically recompiles before execution.

When setting this parameter, you must take into account the overall model simulation mode. The table shows how the Simulate using parameter interacts with the overall simulation mode.

When the Simulink model is in Accelerator mode, the block mode specified using Simulate using overrides the simulation mode.

## Acceleration Modes

| Block Simulation | Simulation Behavior |  |  |
| :--- | :--- | :--- | :--- |
|  | Normal | Accelerator | Rapid Accelerator |
| Interpreted <br> Execution | The block executes <br> using the MATLAB <br> interpreter. | The block executes <br> using the MATLAB <br> interpreter. | Creates a standalone <br> executable from the <br> model. |
| Code Generation | The block is compiled. | All blocks in the <br> model are compiled. |  |

For more information, see "Choosing a Simulation Mode" (Simulink).

## Array Parameters

## Specify sensor array as

Specify sensor element or sensor array. A sensor array can also contain subarrays or be a partitioned array. This parameter can also be expressed as a MATLAB expression.

Types
Single element
Array (no subarrays)
Partitioned array
Replicated subarray
MATLAB expression

## Geometry

Specify the array geometry as one of the following:

- ULA - Uniform linear array
- URA - Uniform rectangular array
- UCA - Uniform circular array
- Conformal Array - arbitrary element positions


## Number of elements

Number of array elements.
Number of array elements, specified as a positive integer. This parameter appears when the Geometry is set to ULA or UCA. If Sensor Array has a Replicated subarray option, this parameter applies to the subarray.

## Array size

This parameter appears when Geometry is set to URA. When Sensor Array is set to Replicated subarray, this parameter applies to the subarrays.

Specify the size of the array as a positive integer or 1-by-2 vector of positive integers.

- If Array size is a 1 -by- 2 vector, the vector has the form [NumberOfArrayRows, NumberOfArrayColumns].
- If Array size is an integer, the array has the same number of rows and columns.

For a URA, elements are indexed from top to bottom along a column and continuing to the next columns from left to right. In this figure, an Array size of [3,2] produces an array of three rows and two columns.

Size and Element Indexing Order
for Uniform Rectangular Arrays
Example: Size = [3,2]


## Element spacing (m)

This parameter appears when Geometry is set to ULA or URA. When Sensor Array has the Replicated subarray option, this parameter applies to the subarrays.

- For a ULA, specify the spacing, in meters, between two adjacent elements in the array as a scalar.
- For a URA, specify the element spacing of the array, in meters, as a 1 -by-2 vector or a scalar. If Element spacing is a 1 -by-2 vector, the vector has the form
[SpacingBetweenRows,SpacingBetweenColumns]. For a discussion of these quantities, see phased.URA. If Element spacing is a scalar, the spacings between rows and columns are equal.


## Array axis

This parameter appears when the Geometry parameter is set to ULA or when the block only supports a ULA array geometry. Specify the array axis as $x, y$, or $z$. All ULA array elements are uniformly spaced along this axis in the local array coordinate system.

## Array normal

This parameter appears when you set Geometry to URA or UCA. Specify the Array normal as x, $y$, or $z$. All URA and UCA array elements are placed in the $y z, z x$, or $x y$-planes, respectively, of the array coordinate system.

## Radius of UCA (m)

Radius of a uniform circular array specified as a positive scalar. Units are meters.
This parameter appears when the Geometry is set to UCA.

## Taper

Tapers, also known as element weights, are applied to sensor elements in the array. Tapers are used to modify both the amplitude and phase of the transmitted or received data.

This parameter applies to all array types, but when you set Sensor Array to Replicated subarray, this parameter applies to subarrays.

- For a ULA or UCA, specify element tapering as a complex-valued scalar or a complex-valued 1-by- $N$ row vector. In this vector, $N$ represents the number of elements in the array. If Taper is a scalar, the same weight is applied to each element. If Taper is a vector, a weight from the vector is applied to the corresponding sensor element. A weight must be applied to each element in the sensor array.
- For a URA, specify element tapering as a complex-valued scalar or complex-valued $M$-by- $N$ matrix. In this matrix, $M$ is the number of elements along the $z$-axis, and $N$ is the number of elements along the $y$-axis. $M$ and $N$ correspond to the values of
[NumberofArrayRows, NumberOfArrayColumns] in the Array size matrix. If Taper is a scalar, the same weight is applied to each element. If Taper is a matrix, a weight from the matrix is applied to the corresponding sensor element. A weight must be applied to each element in the sensor array.
- For a Conformal Array, specify element tapering as a complex-valued scalar or complexvalued 1 -by- $N$ vector. In this vector, $N$ is the number of elements in the array as determined by the size of the Element positions vector. If Taper is a scalar, the same weight is applied to each element. If the value of Taper is a vector, a weight from the vector is applied to the corresponding sensor element. A weight must be applied to each element in the sensor array.


## Element lattice

This parameter appears when Geometry is set to URA. When Sensor Array is set to Replicated subarray, this parameter applies to the subarray.

Specify the element lattice as Rectangular or Triangular

- Rectangular - Aligns all the elements in row and column directions.
- Triangular - Shifts the even-row elements of a rectangular lattice toward the positive-row axis direction. The displacement is one-half the element spacing along the row dimension.


## Element positions (m)

This parameter appears when Geometry is set to Conformal Array. When Sensor Array is set to Replicated subarray, this parameter applies to subarrays.

Specify the positions of conformal array elements as a 3 -by- $N$ matrix, where $N$ is the number of elements in the conformal array. Each column of Element positions (m) represents the position of a single element, in the form [ $x ; y ; z$ ], in the array's local coordinate system. The local coordinate system has its origin at an arbitrary point. Units are in meters.

## Element normals (deg)

This parameter appears when Geometry is set to Conformal Array. When Sensor Array is set to Replicated subarray, this parameter applies to subarrays.

Specify the normal directions of the elements in a conformal array as a 2 -by- $N$ matrix or a 2 -by- 1 column vector in degrees. The variable $N$ indicates the number of elements in the array. If Element normals (deg) is a matrix, each column specifies the normal direction of the corresponding element in the form [azimuth; elevation], with respect to the local coordinate system. The local coordinate system aligns the positive $x$-axis with the direction normal to the conformal array. If Element normals (deg) is a 2-by-1 column vector, the vector specifies the same pointing direction for all elements in the array.

You can use the Element positions (m) and Element normals (deg) parameters to represent any arrangement in which pairs of elements differ by certain transformations. You can combine translation, azimuth rotation, and elevation rotation transformations. However, you cannot use transformations that require rotation about the normal.

## Subarray definition matrix

This parameter appears when Specify sensor array as is set to Partitioned array.
Specify the subarray selection as an $M$-by- $N$ matrix. $M$ is the number of subarrays and $N$ is the total number of elements in the array. Each row of the matrix corresponds to a subarray and each entry in the row indicates whether or not an element belongs to the subarray. When the entry is zero, the element does not belong the subarray. A nonzero entry represents a complex-valued weight applied to the corresponding element. Each row must contain at least one nonzero entry.

The phase center of each subarray is its geometric center. Subarray definition matrix and Geometry determine the geometric center.

## Subarray steering method

This parameter appears when the Specify sensor array as parameter is set to Partitioned array or Replicated subarray.

Specify the subarray steering method as either

- None
- Phase
- Time
- Custom

Selecting Phase or Time opens the Steer input port on the Narrowband Receive Array, Narrowband Transmit Array, Wideband Receive Array, Wideband Transmit Array blocks, Constant Gamma Clutter, and GPU Constant Gamma Clutter blocks.

Selecting Custom opens the WS input port on the Narrowband Receive Array, Narrowband Transmit Array, Wideband Receive Array, Wideband Transmit Array blocks, Constant Gamma Clutter, and GPU Constant Gamma Clutter blocks.
Phase shifter frequency (Hz)
This parameter appears when you set Sensor array to Partitioned array or Replicated subarray and you set Subarray steering method to Phase.

Specify the operating frequency, in hertz, of phase shifters to perform subarray steering as a positive scalar.

## Number of bits in phase shifters

This parameter appears when you set Sensor array to Partitioned array or Replicated subarray and you set Subarray steering method to Phase.

The number of bits used to quantize the phase shift component of beamformer or steering vector weights. Specify the number of bits as a non-negative integer. A value of zero indicates that no quantization is performed.

## Subarrays layout

This parameter appears when you set Sensor array to Replicated subarray.
Specify the layout of the replicated subarrays as Rectangular or Custom.
Grid size
This parameter appears when you set Sensor array to Replicated subarray and Subarrays layout to Rectangular.

Rectangular subarray grid size, specified as a single positive integer or a positive integer-valued 1-by-2 row vector.

If Grid size is an integer scalar, the array has an equal number of subarrays in each row and column. If Grid size is a 1 -by- 2 vector of the form [NumberOfRows, NumberOfColumns], the first entry is the number of subarrays along each column. The second entry is the number of subarrays in each row. A row is along the local $y$-axis, and a column is along the local $z$-axis. The figure here shows how you can replicate a 3-by-2 URA subarray using a Grid size of [1,2].
$3 \times 2$ Element URA
Replicated on a $1 \times 2$ Grid


## Grid spacing

This parameter appears when you set Sensor array to Replicated subarray and Subarrays layout to Rectangular.

Specify the rectangular grid spacing of subarrays as a real-valued positive scalar, a 1-by-2 row vector, or Auto. Grid spacing units are expressed in meters.

- If Grid spacing is a scalar, the spacing along the row and the spacing along the column is the same.
- If Grid spacing is a 1 -by-2 row vector, the vector has the form [SpacingBetweenRows, SpacingBetweenColumn]. The first entry specifies the spacing between rows along a column. The second entry specifies the spacing between columns along a row.
- If Grid spacing is set to Auto, replication preserves the element spacing of the subarray for both rows and columns while building the full array. This option is available only when you specify Geometry as ULA or URA.


## Subarray positions (m)

This parameter appears when you set Sensor array to Replicated subarray and Subarrays layout to Custom.

Specify the positions of the subarrays in the custom grid as a 3 -by- $N$ matrix, where $N$ is the number of subarrays in the array. Each column of the matrix represents the position of a single subarray, in meters, in the array's local coordinate system. The coordinates are expressed in the form [x; y; z].
Subarray normals
This parameter appears when you set the Sensor array parameter to Replicated subarray and the Subarrays layout to Custom.

Specify the normal directions of the subarrays in the array. This parameter value is a 2 -by- $N$ matrix, where $N$ is the number of subarrays in the array. Each column of the matrix specifies the normal direction of the corresponding subarray, in the form [azimuth; elevation]. Each angle is in degrees and is defined in the local coordinate system.

You can use the Subarray positions and Subarray normals parameters to represent any arrangement in which pairs of subarrays differ by certain transformations. The transformations can combine translation, azimuth rotation, and elevation rotation. However, you cannot use transformations that require rotation about the normal.

## Expression

A valid MATLAB expression containing an array constructor, for example, phased.URA.

## Sensor Array Tab: Element Parameters

## Element type

Specify antenna or microphone type as

- Isotropic Antenna
- Cosine Antenna
- Custom Antenna
- Omni Microphone
- Custom Microphone


## Exponent of cosine pattern

This parameter appears when you set Element type to Cosine Antenna.
Specify the exponent of the cosine pattern as a scalar or a 1-by-2 vector. You must specify all values as non-negative real numbers. When you set Exponent of cosine pattern to a scalar, both the azimuth direction cosine pattern and the elevation direction cosine pattern are raised to the specified value. When you set Exponent of cosine pattern to a 1-by-2 vector, the first element is the exponent for the azimuth direction cosine pattern and the second element is the exponent for the elevation direction cosine pattern.

## Operating frequency range ( Hz )

This parameter appears when Element type is set to Isotropic Antenna, Cosine Antenna, or Omni Microphone.

Specify the operating frequency range, in hertz, of the antenna element as a 1-by-2 row vector in the form [LowerBound, UpperBound]. The antenna element has no response outside the specified frequency range.
Operating frequency vector ( Hz )
This parameter appears when Element type is set to Custom Antenna or Custom Microphone.

Specify the frequencies, in Hz , at which to set the antenna and microphone frequency responses as a 1 -by-L row vector of increasing values. Use Frequency responses to set the frequency responses. The antenna or microphone element has no response outside the frequency range specified by the minimum and maximum elements of Operating frequency vector ( $\mathbf{H z}$ ).
Frequency responses (dB)
This parameter appears when Element type is set to Custom Antenna or Custom Microphone.

Specify this parameter as the frequency response of an antenna or microphone, in decibels, for the frequencies defined by Operating frequency vector (Hz). Specify Frequency responses (dB) as a 1 -by-L vector matching the dimensions of the vector specified in Operating frequency vector (Hz).

## Input Pattern Coordinate System

Coordinate system of custom antenna pattern, specified az-el or phi-theta. When you specify az-el, use the Azimuth angles (deg) and Elevations angles (deg) parameters to specify the coordinates of the pattern points. When you specify phi-theta, use the Phi angles (deg) and Theta angles (deg) parameters to specify the coordinates of the pattern points.

## Azimuth angles (deg)

This parameter appears when Element type is set to Custom Antenna and the Input Pattern Coordinate System parameter is set to az-el.

Specify the azimuth angles at which to calculate the antenna radiation pattern as a 1-by- $P$ row vector. $P$ must be greater than 2 . Angle units are in degrees. Azimuth angles must lie between $180^{\circ}$ and $180^{\circ}$ and be in strictly increasing order.

## Elevation angles (deg)

This parameter appears when Element type is set to Custom Antenna and the Input Pattern Coordinate System parameter is set to az-el.

Specify the elevation angles at which to compute the radiation pattern as a 1-by- $Q$ vector. $Q$ must be greater than 2. Angle units are in degrees. Elevation angles must lie between $-90^{\circ}$ and $90^{\circ}$ and be in strictly increasing order.

## Phi Angles (deg)

This parameter appears when Element type is set to Custom Antenna and the Input Pattern Coordinate System parameter is set to phi-theta.

Phi angles of points at which to specify the antenna radiation pattern, specify as a 1-by-P row vector. $P$ must be greater than 2 . Angle units are in degrees. Phi angles must lie between $0^{\circ}$ and $360^{\circ}$ and be in strictly increasing order.

## Theta Angles (deg)

This parameter appears when Element type is set to Custom Antenna and the Input Pattern Coordinate System parameter is set to phi-theta.

Theta angles of points at which to specify the antenna radiation pattern, specify as a 1-by- $Q$ row vector. $Q$ must be greater than 2 . Angle units are in degrees. Theta angles must lie between $0^{\circ}$ and $180^{\circ}$ and be in strictly increasing order.

## Magnitude pattern (dB)

This parameter appears when the Element type is set to Custom Antenna.
Magnitude of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$ -by-L array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector ( $\mathbf{H z}$ ).

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector ( Hz ) parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (Hz) parameter.


## Phase pattern (dB)

This parameter appears when the Element type is set to Custom Antenna.
Phase of the combined antenna radiation pattern, specified as a $Q$-by- $P$ matrix or a $Q$-by- $P$-by- $L$ array.

- When the Input Pattern Coordinate System parameter is set to az-el, $Q$ equals the length of the vector specified by the Elevation angles (deg) parameter and $P$ equals the length of the vector specified by the Azimuth angles (deg) parameter.
- When the Input Pattern Coordinate System parameter is set to phi-theta, $Q$ equals the length of the vector specified by the Theta Angles (deg) parameter and $P$ equals the length of the vector specified by the Phi Angles (deg) parameter.

The quantity $L$ equals the length of the Operating frequency vector $(\mathbf{H z})$.

- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If this parameter is a $Q$-by- $P$ matrix, the same pattern is applied to all frequencies specified in the Operating frequency vector $(\mathbf{H z})$ parameter.
- If the value is a $Q$-by- $P$-by- $L$ array, each $Q$-by- $P$ page of the array specifies a pattern for the corresponding frequency specified in the Operating frequency vector (Hz) parameter.


## MatchArrayNormal

This parameter appears when the Element type is set to Custom Antenna.
Select this check box to rotate the antenna element pattern to align with the array normal. When not selected, the element pattern is not rotated.

When the antenna is used in an antenna array and the Input Pattern Coordinate System parameter is az-el, selecting this check box rotates the pattern so that the $x$-axis of the element coordinate system points along the array normal. Not selecting uses the element pattern without the rotation.

When the antenna is used in an antenna array and Input Pattern Coordinate System is set to phi-theta, selecting this check box rotates the pattern so that the $z$-axis of the element coordinate system points along the array normal.

Use the parameter in conjunction with the Array normal parameter of the URA and UCA arrays.

## Polar pattern frequencies $(\mathbf{H z})$

This parameter appears when the Element type is set to Custom Microphone.

Specify the measuring frequencies of the polar patterns as a 1 -by- $M$ vector. The measuring frequencies lie within the frequency range specified by the Operating frequency vector ( $\mathbf{H z}$ ) parameter. Frequency units are in Hz.

## Polar pattern angles (deg)

This parameter appears when Element type is set to Custom Microphone.
Specify the measuring angles of the polar patterns, as a 1 -by- $N$ vector. The angles are measured from the central pickup axis of the microphone, and must be between $-180^{\circ}$ and $180^{\circ}$, inclusive.

## Polar pattern (dB)

This parameter appears when Element type is set to Custom Microphone.
Specify the magnitude of the microphone element polar pattern as an $M$-by- $N$ matrix. $M$ is the number of measuring frequencies specified in Polar pattern frequencies (Hz). $N$ is the number of measuring angles specified in Polar pattern angles (deg). Each row of the matrix represents the magnitude of the polar pattern measured at the corresponding frequency specified in Polar pattern frequencies (Hz) and all angles specified in Polar pattern angles (deg). Assume that the pattern is measured in the azimuth plane. In the azimuth plane, the elevation angle is $0^{\circ}$ and the central pickup axis is $0^{\circ}$ degrees azimuth and $0^{\circ}$ degrees elevation. Assume that the polar pattern is symmetric around the central axis. You can construct the microphone's response pattern in 3-D space from the polar pattern.
Baffle the back of the element
This check box appears only when the Element type parameter is set to Isotropic Antenna or Omni Microphone.

Select this check box to baffle the back of the antenna element. In this case, the antenna responses to all azimuth angles beyond $\pm 90^{\circ}$ from broadside are set to zero. Define the broadside direction as $0^{\circ}$ azimuth angle and $0^{\circ}$ elevation angle.

## Ports

Note The block input and output ports correspond to the input and output parameters described in the step method of the underlying System object. See link at the bottom of this page.

| Port | Description | Supported Data Types |
| :--- | :--- | :--- |
| X | Radiated signals input port <br> The size of the first dimension of <br> the input matrix can vary to <br> simulate a changing signal <br> length. A size change can occur, <br> for example, in the case of a <br> pulse waveform with variable <br> pulse repetition frequency. | Double-precision floating point |
| Ang | Radiating directions of signals <br> input port. | Double-precision floating point |


| Port | Description | Supported Data Types |
| :--- | :--- | :--- |
| W | Array or subarray weights input <br> port. To enable this port, select <br> the Enable weights input <br> check box. | Double-precision floating point |
| WS | Subarray element weights input <br> port. To enable this port select <br> Custom from the Subarray <br> steering method pull down <br> menu. |  |
| Steer | Steering angle input port. To <br> enable this port, select Phase <br> or Time from the Subarray <br> steering method pull down <br> menu. |  |
| Out | Radiated signals. | Double-precision floating point |

## Version History

Introduced in R2015b

## See Also

phased.WidebandRadiator

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4
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Apps

## Pulse Waveform Analyzer

Analyze performance characteristics of pulsed, frequency-modulated, and phase-coded waveforms

## Description

The Pulse Waveform Analyzer app lets you explore the properties of signals commonly used in radar. You can display 2-D and 3-D plots that let you visualize waveform time series and spectra.

The app lets you change waveform parameters and see how different parameter values affect the appearance and properties of the waveform. Waveform parameters include pulse repetition frequency (PRF), pulse duration, and bandwidth. The app displays basic waveform characteristics such as range resolution, Doppler resolution, and maximum range. When you launch the app, the Real and Imaginary and Spectrum tabs are shown by default. You can simultaneously overlay plots of multiple waveforms.

You can select different types of displays using this pull-down menu. You can also rearrange the tabs by using drag-and-drop to change the default layout.


The app lets you analyze these types of waveforms:

- Rectangular
- Linear frequency modulation (LFM)
- Stepped FM
- Phase-coded waveforms
- Frequency modulation constant waveform (FMCW)

You can export waveforms as workspace variables or files containing:

- Phased Array System Toolbox waveform objects such as phased. LinearFMWaveform.
- Radar Toolbox pulseWaveformLibrary objects.
- Radar Toolbox pulseCompressionLibrary objects.

You can use the waveform blocks, Matched Filter blocks, and Stretch Processor blocks in Simulink. You can also use the Pulse Waveform Library and Pulse Compression Library blocks available in Radar Toolbox.

You can also employ this app in sonar applications by choosing the appropriate propagation speed.


## Open the Pulse Waveform Analyzer App

- MATLAB toolstrip: On the Apps tab, under Signal Processing and Communications, select the app icon, or
- MATLAB command prompt: Enter pulseWaveformAnalyzer. For ways to use the app programmatically, see "Programmatic Use" on page 4-12.


## Examples

## Rectangular Waveform

This example shows how to analyze a rectangular waveform. An ideal rectangular waveform jumps instantaneously to a constant value and stays there for some duration. Rearrange the Parameters and Characteristics tabs to make the plots larger.

When you open the app, the Library tab shows the default rectangular waveform and the center panel displays the waveform shape or spectrum. First, set the Sample Rate (Hz) to 3 MHz . The same sample rate applies to all waveforms that you analyze.

You can rename the waveform by right-clicking its name. Change the name to RectangularPulse.


Design the pulse for a maximum range of 50 km . For this range, the time for a signal to propagate and return is $333 \mu$ s. Therefore, allow $333 \mu$ s between pulses, equivalent to a pulse repetition frequency (PRF) of 3000 Hz .

Set the Pulse Width to $50 \mu \mathrm{~s}$.
Change the value of the speed of light in the Propagation Speed field to a more precise value by entering physconst('Lightspeed'). You can use workspace variables and MATLAB functions in any editable field.

After you select the green check mark, the app displays a range resolution of approximately 7.5 km in the Characteristics tab. In this panel, you can scroll right to see other properties. The range resolution of a rectangular pulse is roughly $1 / 2$ the pulse-width multiplied by the speed of light. The Doppler resolution is approximately the width of the Fourier transform of the pulse.

In the center panel of the window, select the Real and Imaginary tab to plot the waveform.


Select the Spectrum tab in the center panel of the window to show the power spectral density.


You can display the joint range-Doppler resolution by selecting Surface from the Ambiguity Plots menu.


## Linear FM Waveform

This example shows how to improve range resolution using a linear FM waveform. In the previous example, the range resolution of the rectangular pulse was poor, approximately 7.5 km . You can improve the range resolution by choosing a signal with a larger bandwidth. A good choice is a linear FM pulse.

In the Parameters tab, change the Waveform to Linear FM. Then, change the waveform name to LinearFMWaveform. This type of pulse has a varying frequency, which can either increase or decrease as a linear function of time. Keep the sample rate at 3 MHz .

Choose the Sweep Direction as Up, and the Sweep Bandwidth as 1 MHz .
You can see that keeping the same pulse width as in the previous example, improves the range resolution to 150 m, as shown in the Characteristics tab.


While the range resolution gets better, the Doppler resolution is worse than the resolution of a rectangular waveform. You can see this by selecting the Surface ambiguity plot. The Ambiguity Function-Surface tab shows this tradeoff between Doppler resolution and range resolution.


## Linear FM Waveform Spectrogram

This example shows how to display the spectrogram of a linear FM waveform with and without frequency reassignment.

Use the same signal parameters as in the previous example.
Select Spectrogram from the Signal Plots drop-down menu. Then, select the Reassigned check box to show the frequency reassigned spectrogram (reassignment is turned on by default). Set the Threshold to -100 dB. Frequency reassignment is a technique for sharpening the magnitude spectrogram of a signal using information from its phase spectrum. For more information on frequency reassignment, see Fulop and Kelly (2006) [1].


You can vary the Threshold setting to show or hide weaker spectrum components.
To view the conventional spectrogram, clear the Reassigned check box.


Again, you can vary the Threshold Value setting to show or hide weaker spectrum components.

## Display and Analyze Two Signals

This example shows how to display the two signals simultaneously.
First, create a rectangular waveform with the same parameters as used in the first example. Then, rename the waveform to RectangularPulse.

Next, create an LFM waveform. Click the Add Waveform button. Rename the second waveform to LinearFMPulse. Set the waveform parameters to the same values as in the second example.

Select both waveforms in the Library panel using Ctrl+click. The display now shows the waveforms, spectra, and characteristics for both waveforms.



## Programmatic Use

You can run pulseWaveformAnalyzer from the command line.
pulseWaveformAnalyzer(wav) opens the Pulse Waveform Analyzer app and imports and plots the waveform wav. wav can be a variable in the workspace representing a waveform object such as:

```
wav = phased.LinearFMWaveform(SampleRate=1e6, ...
    SweepBandwidth=200e3, ...
    PulseWidth=1e-3,PRF=1e3);
pulseWaveformAnalyzer(wav)
```

or you can enter the object directly:
pulseWaveformAnalyzer(phased.LinearFMWaveform( ...
SampleRate=1e6, ...
SweepBandwidth=200e3, ...
PulseWidth=1e-3, PRF=1e3) )
pulseWaveformAnalyzer(wavlib) opens the Pulse Waveform Analyzer app and imports a pulseWaveformLibrary object, wavlib. For example, construct the waveform library object from three waveforms with a common sample rate of 1 MHz . Then run from the command line:

```
waveform1 = {'Rectangular','PRF',1e4,'PulseWidth', 50e-6};
waveform2 = {'LinearFM','PRF',1e4,'PulseWidth',50e-6, ...
    'SweepBandwidth',1e5,'SweepDirection','Up', ...
    'SweepInterval', 'Positive'};
waveform3 = {'PhaseCoded','PRF',le4,'Code','Zadoff-Chu', ...
```

'SequenceIndex',3,'ChipWidth',5e-6,'NumChips',8\};
fs = le6;
wavlib = pulseWaveformLibrary('SampleRate',fs, ...
'WaveformSpecification', \{waveform1,waveform2, waveform3\}); pulseWaveformAnalyzer(wavlib)

pulseWaveformAnalyzer(comprlib) opens the Pulse Waveform Analyzer app and imports a pulseCompressionLibrary object, comprlib. For example, using the waveforms from the "Rectangular Waveform" on page 4-4 and "Linear FM Waveform" on page 4-7 examples, create a matched filter for the rectangular waveform and a stretch processor for the linear FM waveform. Set the sample rate to 3 MHz , the pulse width of the rectangular wave to $25 \mu \mathrm{~s}$, the pulse width of the linear wave to $50 \mu \mathrm{~s}$, and the pulse repetition frequency to 3000 Hz . Export the compressed waveforms to the waveform app with these commands:

```
fs = 3e6;
rectpw = 25e-6;
linpw = 50e-6;
prf = 3e3;
waveform1 = {'Rectangular','PRF',prf,...
    'PulseWidth',rectpw};
waveform2 = {'LinearFM','PRF',prf,'PulseWidth',linpw,...
    'SweepBandwidth',le6,'SweepDirection','Up',...
    'SweepInterval','Positive'};
```

procspec1 = \{'MatchedFilter','SpectrumWindow','Hann'\};
procspec2 $=$ \{'StretchProcessor','ReferenceRange',5000,...
'RangeSpan' , 200, 'RangeWindow', 'Hamming'\};
comprlib = pulseCompressionLibrary(...
'WaveformSpecification', \{waveform1, waveform2\},...
'ProcessingSpecification',\{procspec1, procspec2\},...
'SampleRate',fs,'PropagationSpeed', physconst('Lightspeed'));
pulseWaveformAnalyzer(comprlib)


## Version History

## Introduced in R2014b

## References

[1] Fulop, Sean A., and Kelly Fitz. "Algorithms for Computing the Time-Corrected Instantaneous Frequency (Reassigned) Spectrogram, with Applications." The Journal of the Acoustical Society of America 119, no. 1 (January 2006): 360-71.

## See Also

Apps
Sensor Array Analyzer

## Sensor Array Analyzer

Analyze beam patterns and performance characteristics of linear, planar, 3-D, and arbitrary sensor arrays

## Description

The Sensor Array Analyzer app enables you to construct and analyze common sensor array configurations. These configurations range from 1-D to 3-D arrays of antennas, sonar transducers, and microphones, and can contain subarrays. After you specify array and sensor parameters, the app displays basic performance characteristics such as array directivity and array dimensions. You can then create various directivity plots and images.

## Array Types

You can use this app to show the directivity of these arrays:

## 2D Arrays

- Uniform Linear Array (ULA)
- Uniform Rectangular Array (URA)
- Uniform Circular Array (UCA)
- Uniform Hexagonal Array (UHA)
- Circular Planar Array
- Concentric Array


## 3D Arrays

- Spherical Array
- Cylindrical Array
- Arbitrary Array


## Subarrays

You can use this app to create and analyze arrays containing subarrays to:

- Replicate an array along a spatial grid.
- Partition a larger array into subarrays.


## Element Types

These elements are available to populate an array:

## Non-Polarized Antennas

- Cardioid Antenna
- Cosine Antenna
- Custom Antenna
- Gaussian Antenna
- Isotropic Antenna
- Sinc Antenna


## Polarized Antennas

- Crossed Dipole Antenna
- Custom Antenna
- NR Antenna
- Short Dipole Antenna


## Microphones

- Cardioid Microphone
- Custom Microphone
- Omnidirectional Microphone


## Sonar Transducers

- Isotropic Hydrophone
- Isotropic Projector


## Plot Options

The Sensor Array Analyzer app can create these types of plots:

- Array Geometry
- 2-D Array Patterns
- 3-D Array Pattern
- Grating Lobes



## Open the Sensor Array Analyzer App

- MATLAB toolstrip: On the Apps tab, under Signal Processing and Communications, click the app icon.
- MATLAB command prompt: Enter sensorArrayAnalyzer.


## Examples

## Uniform Linear Array (ULA)

This example analyzes a 10 -element uniform linear array (ULA) in a sonar application. The array consists of isotropic hydrophones. Design the array for a 10 KHz signal.

A uniform linear array has sensor elements that are equally spaced along a line.
Under the Analyzer tab, in the Array section of the toolstrip, select ULA. In the Element section of the toolstrip, select Hydrophone.

Select the Parameters tab and set the Number of Elements to 10. Set the Element Spacing to 0.5 wavelengths.

Design the array for a 10 KHz signal by setting Signal Frequencies (Hz) to 10000. Then click the Apply button. You can change many menu items and apply the changes at any time. The parameters that appear in this tab depend on your choice of array and element.

When you choose a sonar element, the app automatically sets the signal propagation speed in water to 1500 . You can set the signal propagation speed to any value by setting the Propagation Speed ( $\mathrm{m} / \mathrm{s}$ ).

Select the Array Geometry tab and use the check boxes to display element normals (Show Normals), element indices (Show Index), and element tapers (Show Tapers).


In the rightmost Array Characteristics panel, you can view the array directivity, half-power beam width (HPBW), first-null beam-width (FNBW), and side lobe level (SLL).

To display a directivity plot, go to the Plots section of the Analyzer tab. Select Azimuth Pattern from the 2D Pattern menu. The azimuth directivity pattern is now displayed in the center panel of the app. Select the Azimuth Pattern tab, and set the Coordinate to Rectangular.


You can see the main lobe of the array directivity function (also called the main beam) at $0^{\circ}$ and another main lobe at $\pm 180^{\circ}$. Two main lobes appear because of the cylindrical symmetry of the ULA array.

A beam scanner works by successively pointing the array main lobe in different directions. In the Steering tab, set Azimuth Angles (deg) to 30 and Elevation Angles (deg) to 0. This steers the
main lobe to $30^{\circ}$ in azimuth and $0^{\circ}$ elevation.


One disadvantage of a ULA is its large side lobes. An examination of the array directivity shows two side lobes close to each main lobe, each down by about only 13 dB . A strong side lobe inhibits the ability of the array to detect a weaker signal in the presence of a larger nearby signal. By using array tapering, you can reduce the side lobes.

Use the Taper option to specify the array taper as a Taylor window with Sidelobe Attenuation set to 30 dB and nbar set to 4 . Click the Apply button.


## Azimuth Response of Partitioned ULA

This example plots the azimuth response of a four-element ULA partitioned into two two-element ULAs.

Under the Analyzer tab, in the Array section of the toolstrip, select ULA. Create a ULA with default parameters (with the number of elements set to 4 and the element spacing set to 0.5 meters).


Select the Partition button on the Analyzer. Design the array for a 1 GHz signal by setting Signal Frequencies (Hz) to 1e9. Then click the Apply button. You can change many menu items and apply the changes at any time. The parameters that appear in this tab depend on your choice of array and element.


The subarray selection menu item should read [ones(1,2) zeros(1,2); zeros(1,2) ones (1,2)].

Select 2D Pattern in the Analyzer tab and choose the Azimuth pattern to visualize the 2-D azimuth pattern in polar coordinates.


## Re-Partition URA

A partitioned array consists of multiple subarrays in which each array element can be assigned to one or more subarrays. After creating the partition array, you can then re-assign elements to different subarrays. For example, create a 4-by-4 uniform rectangular array (URA) containing 16 elements. Selecting the Partition tab converts the URA into a 4-by-4 partitioned array with subarrays indicated by different colors. The partitioning is controlled by the Subarray Selection matrix.
[ ones(1,8) zeros(1,8); zeros(1,8) ones(1,8)]
The default subarray selection matrix assigns each element to one subarray. In this matrix, the number of columns equals the number of array elements. Each row corresponds to a subarray. This 2-by-16 matrix assigns elements $1-8$ to subarray 1 and elements $9-16$ to subarray 2 .

To re-partition an array, you can edit the Subarray Selection matrix. Select the Define Subarray tab to rearrange the elements belonging to the subarrays.


Selecting the Define Subarray tab brings up the subarray editor.


## You can:

- Select the pencil icon next to Subarray1 to edit the elements and weights in subarray 1.
- Select the pencil icon next to Subarray2 to edit the elements and weights in subarray 2.
- Select the green cross icon at the top to create an empty subarray.

Select Subarray 2 to display the element indices belonging to Subarray 2.


Remove element 9 and its weight. Select the green cross add a new subarray, Subarray 3. Then add element 9 to the new subarray.

4 Sensor Array Analyzer - SensorArraySession_partn_3*


The new subarray and its added element appears in yellow.

## Uniform Rectangular Array (URA)

This example shows how to construct a 6-by-6 uniform rectangular array (URA) designed to detect and localize a 100 MHz signal.

Under the Analyzer tab, in the Array section of the toolstrip, select URA. In the Element section of the toolstrip, select Isotropic.

Design the array for a 100 MHz signal by setting Signal Frequencies to 100 e 6 and the row and column Element Spacing to [0.5 0.5] wavelength.

Select the Parameters tab and set the Size to $[6,6]$.

From the Taper drop-down, choose Row and Column. Set Row Taper and Column Taper to a Taylor window using default taper parameters. Click the Apply button to apply the changes. You can change many menu items and apply the changes at any time. The parameters that appear in this tab depend on your choice of array and element.

The shape of the array is shown in this figure.


Next, display a 3-D array pattern by selecting 3D Pattern in the Plots section of the Analyzer tab.


A significant performance measure for any array is directivity. You can use the app to examine the effects of tapering on array directivity. Without tapering, the array directivity for this URA is 17.16 dB . With tapering, the array directivity is reduced to 16.03 dBi .

## Grating Lobes for a Rectangular Array

This example shows the grating lobe diagram of a 4 -by-4 uniform rectangular array (URA) designed to detect and localize a 300 MHz signal.

Under the Analyzer tab, in the Array section of the toolstrip, select URA. In the Element section of the toolstrip, select Isotropic. Set the Size to [4, 4]. In the Steering tab, set Azimuth Angles (deg) to 20 and Elevation Angles (deg) to 0.

Design the array for a 300 MHz signal by setting Signal Frequencies to 3 e 8 and the row and column Element Spacing to [0.7,0.7] wavelength. By setting the row and column Element
Spacing to [0.7, 0.7] wavelengths, you create a spatially under-sampled, array. Then click the Apply button.

Select Grating Lobe Diagram from the Plots section to plot the grating lobes.
This figure shows the grating lobe diagram produced when you beamform the array towards the angle [20,0]. The main lobe is designated by the small black-filled circle. The multiple grating lobes are designated by the small unfilled black circles. The larger black circle is called the physical region, for which $u^{2}+v^{2} \leq 1$. The main lobe always lies in the physical region. The grating lobes can sometimes lie outside the physical region. Any grating lobe in the physical region leads to an
ambiguity in the direction of the incoming wave. The green region shows where the main lobe can be pointed without any grating lobes appearing in the physical region. If the main lobe is set to point outside the green region, a grating lobe can move into the physical region.


The next figure shows what happens when the pointing direction lies outside the green region. In the Steering tab, set Azimuth Angles (deg) to 35 and Elevation Angles (deg) to 0. In this case, one grating lobe moves into the physical region.


## URA Containing Polarized Elements

1 Under the Analyzer tab, in the Array section of the toolstrip, select URA. In the Element section of the toolstrip, select Crossed Dipole. Select RHCP as the Polarization and set the Rotation Angle to $30^{\circ}$.
2 Design the array for a 100 MHz signal by setting Signal Frequencies to 100 e 6 and the row and column Element Spacing to [0.5 0.5] wavelength.
3 Select the Parameters tab and set the Size to [6,6].
4 From the Taper drop-down, choose Row and Column. Set Row Taper and Column Taper to a Taylor window using default taper parameters. Click the Apply button to apply the changes.


## Specify Arbitrary Array Geometry

This example shows how to construct a triangular array of three isotropic antenna elements.
You can specify an array which has an arbitrary placement of sensors. Select Arbitrary in the Array drop-down. Select Isotropic from the Element menu. Enter the elements positions in the Element Position field. The positions of the three elements are $[0,0,0 ; 0,0.5,0 ; 0,0.5,0.866]$. All elements have the same normal direction, pointing to $0^{\circ}$ azimuth and $20^{\circ}$ elevation and to set the normal in the Element Normal (deg) type [0 0 0; 2020 20] and click the Apply button. Select Array Geometry from the Plots section.


To show the 3-D array directivity, select 3D Pattern from the Plots tab.

- You can use the Orientation dialog box to change the orientation of the array.
- The Show Array check box toggles off and on the display of the array.
- The Show Local Coordinates check box toggles off and on the display of the local coordinate system.
- The Show Colorbar check box toggles off and on the colorbar showing field intensities.



## Specify Arbitrary Array Geometry Using Variables

This example illustrates an array with arbitrary geometry specified by MATLAB variables set at the command line. Enter the variables in the appropriate sensorArrayAnalyzer fields.

At the MATLAB command line, create an element position array, pos, an element normal array, nrm, and a taper value array, tpr.

```
pos = [0,0,0;0,0.5,0;0,0.5,0.866]
nrm = [0 0 0; 20 20 20];
tpr = [llll];
```

Enter these variables in the appropriate sensorArrayAnalyzer fields, click Apply button. To show the 3-D array directivity, click 3D Pattern from the Plots tab.


## URA With Custom Antenna Element

Use the same parameters as in the "Uniform Rectangular Array (URA)" on page 4-29 example and click the Apply button. In the Element section of the toolstrip, select Custom in the Antenna section.

For a custom antenna element, specify the magnitude and phase patterns. Because patterns usually require large matrices, it is better to use the command line to specify the magnitude and phase patterns. The magnitude pattern specified here has directionality along the $\pm x$-axes and is a function of azimuth and elevation. The phase pattern is all zeros. Alternatively, you can specify a pattern in terms of phi and theta angles by setting the Pattern Coordinate System parameter to phi-theta.

```
azpat = cosd([0:360]).^2 + 1;
elpat = cosd([-90:90]') + 1;
mag = elpat*azpat;
magdb = 10*log10(mag);
```

To show the 3-D array directivity, select 3D Pattern from the Plots tab.


- "Array Geometries and Analysis"


## Version History

Introduced in R2014b

## See Also

## Objects

phased.ReplicatedSubarray|phased.PartitionedArray

## Apps

Pulse Waveform Analyzer

## Topics

"Array Geometries and Analysis"

## Sonar Equation Calculator

Estimate maximum range, SNR, transmission loss and source level of a sonar system

## Description

The Sonar Equation Calculator app solves the basic sonar equation for monostatic sonar systems. The sonar equation relates transmission loss (or target range), source level, directivity, noise level, target strength, and signal SNR. You can solve for one of these quantities in terms of the others. Using this app, you can:

- Calculate the received SNR value from transmission loss (or equivalently, target range), source level, and noise level.
- Solve for transmission loss from sonar source level of the sonar, specified received SNR, and array directivity.
- Solve for target range from sonar source level of the sonar, specified received SNR, and array directivity.
- Calculate required source level from target range, source level, and received SNR.

| (A)Sonar Equation Calculator | - | $\square \times$ |
| :---: | :---: | :---: |
| File Help |  |  |
| Calculation: | Target Range | $\checkmark$ |
| Sonar Specifications |  |  |
| Mode: | Active | $\checkmark$ |
| Noise Level: | 73 | $\mathrm{dB} / / 1 \mu \mathrm{~Pa}$ |
| Directivity Index: | 20 | dB |
| Target Strength: | 25 | dB |
| Frequency: | 2 | $\mathrm{kHz} \quad \vee$ |
| Depth: | 10000 | m |
| Source Level: | 220 | $\mathrm{dB} / / 1 \mu \mathrm{~Pa}$ |
| SNR: >> | 10 | dB |
| Target Range: | $5.888 \mathrm{e}+04$ | m V |

## Open the Sonar Equation Calculator App

- MATLAB Toolstrip: On the Apps tab, under Signal Processing and Communications, click the app icon.
- MATLAB command line: Enter sonarEquationCalculator.


## Examples

## Maximum Detection Range of Active Sonar

Compute the maximum detection range of an active monostatic sonar designed to achieve an SNR of at least 10 dB . The operating frequency is 5 kHz , and the source level is 180 dB . Assume that the noise level is 73 dB , the receiver directivity is 20 dB , and the target strength is 10 dB .

- Set Calculation to Target Range.
- Set Mode to Active.
- Set Noise Level to $73 \mathrm{~dB} / / 1 \mu \mathrm{~Pa}$.
- Set receiver Directivity index to 20 dB .
- Set Target Strength to 10 dB .
- Set Frequency to 5 kHz .
- Set channel Depth to 100 m .
- Set Source Level to $180 \mathrm{~dB} / / 1 \mu \mathrm{~Pa}$.
- Set required SNR to 10 dB .

| (4) Sonar Equation Calculator | - | $\square \times$ |
| :---: | :---: | :---: |
| File Help |  |  |
| Calculation: | Target Range | $\checkmark$ |
| Sonar Specifications |  |  |
| Mode: | Active | $\checkmark$ |
| Noise Level: | 73 | $\mathrm{dB} / / 1 / \mathrm{Pa}$ |
| Directivity Index: | 20 | dB |
| Target Strength: | 10 | dB |
| Frequency: | 5 | $\mathrm{kHz} \quad \checkmark$ |
| Depth: | 100 | m |
| Source Level: | 180 | $\mathrm{dB} / / 1 \mu \mathrm{~Pa}$ |
| SNR: >> | 10 | dB |
| Target Range: | $1.461 \mathrm{e}+04$ | $\mathrm{m} \quad \checkmark$ |

The maximum target range is 14.61 km .

## Maximum Detection Range for Multiple Pulses

Use multiple pulses to reduce the source level while maintaining the same maximum target range.
Start with the values set in the "Maximum Detection Range of Active Sonar" on page 4-40 example.

- Click the arrows to the right of the SNR label to access the Detection Specifications for SNR options.
- Set Probability of Detection to 0.95.
- Set Probability of False Alarm to le-6.
- Set Number of Pulses to 10 .
- Reduce Source Level to 175.
- Set the Swerling Case Number to 0 assuming a nonfluctuating target.

| (4) Sonar Equation Calculator | - | $\square \times$ |
| :---: | :---: | :---: |
| File Help |  |  |
| Calculation: | Target Range | $\checkmark$ |
| Sonar Specifications |  |  |
| Mode: | Active | $\checkmark$ |
| Noise Level: | 73 | $\mathrm{dB} / / 14 \mathrm{~Pa}$ |
| Directivity Index: | 20 | dB |
| Target Strength: | 10 | dB |
| Frequency: | 5 | kHz |
| Depth: | 100 | m |
| Source Level: | 175 | $\mathrm{dB} / / 1 \mu \mathrm{~Pa}$ |
| SNR: < | 5.7183 | dB |
| Detection Specifications for SNR |  |  |
| Probability of Detection: | 0.95 |  |
| Probability of False Alarm: | 1e-6 |  |
| Number of Pulses: | 10 |  |
| Swerling Case Number: | $0 \quad \checkmark$ |  |
| Target Range: | $1.404 \mathrm{e}+04$ | $\mathrm{m} \quad \checkmark$ |

The maximum detection range is 14.81 km , approximately the same as in the previous example, but the source level is reduced by 5 dB .

## Required Source Level for Monostatic Sonar

Compute the source level for an active monostatic sonar with a received SNR of 15 dB . The target range is 5 km and the target strength is 25 dB . Assume a $5-\mathrm{kHz}$ sonar frequency.

- Set Calculation to Source Level.
- Set Mode to Active.
- Set Noise Level to 75.
- Set receiver Directivity index to 20 dB .
- Set Target Strength to 25.
- Click the arrows to the right of the Transmission Loss label to access the Calculation of Transmission Loss options.
- Set the Range to 10.0 km .
- Set the Frequency to 5 kHz .
- Set the Depth to 200 m.
- Set SNR to 15 dB .

| (4) Sonar Equation Calculator |  |  |  |  | $\times$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| File Help |  |  |  |  |  |
| Calculation: |  |  | Source L |  | $\checkmark$ |
| Sonar Specifications |  |  |  |  |  |
| Mode: |  |  | Active |  | $\checkmark$ |
| Noise Level: |  |  | 75 | dB//1 |  |
| Directivity Index: |  |  | 20 | dB |  |
| Target Strength: |  |  | 25 | dB |  |
| Transmission Loss: |  | < | 63.3125 | dB |  |
| Calculation of Transmission Loss |  |  |  |  |  |
| Target Range: |  |  | 10 | km | $\checkmark$ |
| Frequency: |  |  | 5 | kHz | $\checkmark$ |
| Depth: |  |  | 200 | m | $\checkmark$ |
| SNR: | 》 |  | 15 | dB |  |
| Source Level: |  |  | 171.6 | dB// |  |

The required source level is $171.6 \mathrm{~dB} / / 1 \mu \mathrm{~Pa}$.

## Received SNR for Monostatic Sonar

Compute the received SNR for a passive sonar with a source level of $140 \mathrm{db} / / 1 \mu \mathrm{~Pa}$ for a source 10.0 km away. Assume a $3-\mathrm{kHz}$ sonar frequency.

- Set Calculation to SNR.
- Set Mode to Passive.
- Set Noise Level to 75.
- Set receiver Directivity index to 20 dB .
- Click the arrows to the right of the Transmission Loss label to access the Calculation of Transmission Loss options.
- Set Range to 10.0 km .
- Set Frequency to 3 kHz .
- Set Depth to 200 m.
- Set Source Level to $140 \mathrm{~dB} / / 1 \mu \mathrm{~Pa}$.


The received SNR is 23.16 dB .

## Transmission Loss of Monostatic Active Sonar

Compute the transmission loss for an active sonar that results in an SNR of 15 dB . The source level is $215 \mathrm{~dB} / / 1 \mu \mathrm{~Pa}$. Assume that the noise level is $75 \mathrm{~dB} / / 1 \mu \mathrm{~Pa}$, the receiver directivity is 20 dB , and the target strength is 10 dB .

- Set Calculation to Transmission Loss.
- Set Mode to Active.
- Set Noise Level to 75 dB .
- Set receiver Directivity index to 20 dB .
- Set Target Strength to 25 dB .
- Set Source Level to 215 dB .
- Set required SNR to 15 dB .


The transmission loss is 85 dB .

## Parameters

Calculation - Select type of calculation
Target Range (default)|Transmission Loss|Source Level|SNR
Select the type of calculation:

- Target Range - solves for the maximum target range based on source level of the sonar and required received SNR.
- Transmission Loss -- computes the required transmit power from known target range and required received SNR.
- Source Level - computes the source level from the range or transmission loss, and received SNR.
- SNR - calculates the received SNR value based on known range and transmit power.

Mode - Type of sonar
Active (default) | Passive
Specify whether the sonar is operating in active mode or passive mode. Active mode means that a signal is transmitted from a source, reflects off a target, and returns to the receiver which is collocated with the source. Active mode requires the specification of the reflector target strength. Passive mode means that the signal is transmitted from a source to a receiver along a direct path.

## Noise Level - Noise Level

70 (default) | scalar
Noise level at sonar receiver, specified as a scalar. Units are $d B / / 1 \mu \mathrm{P}$.
Directivity Index - Directivity index of receive array or element
20 (default) | scalar
Directivity index of receive array or element, specified as a scalar. Units are dB.
Target Strength - Target strength of reflector
25 (default) | scalar
Target strength of reflector, specified as a scalar. Units are $\mathrm{dB} / / 1 \mathrm{~m}^{2}$.

## Dependencies

To enable this parameter, set the Mode parameter to Active.
Frequency - Sound frequency
2 (default) | positive scalar
Sound frequency, specified as a positive scalar. Default units are in $k H z$. You can also select $\mathrm{Hz}, \mathrm{kHz}$, or MHz.

```
Depth - Water channel depth
10000 (default) | positive scalar
```

Water channel depth. Default units are meters. You can select units in m, km, mi, or nmi.
Source Level - Source level of sonar transmitter
220 (default) | scalar
Source level of sonar transmitter, specified as a scalar. Units are $\mathrm{dB} / / 1 \mu \mathrm{P}$.
SNR — Output signal-to-noise ratio at receiver
10 (default)
Specify an SNR value, or calculate an SNR value using the Detection Specifications for SNR options. You can calculate the SNR required to achieve a particular probability of detection and probability of false alarm using the Shnidman equation. To calculate the SNR value:

1 Click the arrows to the right of the SNR label to access the Detection Specifications for SNR options.
2 Enter values for Probability of Detection, Probability of False Alarm, Number of Pulses, and Swerling Case Number.

## Dependencies

To enable this parameter, set Calculation to Target Range, Transmission Loss, or Source Level.

Probability of Detection - Detection probability used to estimate SNR 0.81029 (default)

Specify the detection probability used to estimate SNR using the Shnidman equation.

## Dependencies

To enable this parameter, set Calculation to Target Range, Transmission Loss, or Source Level, and select the Detection Specifications for SNR options for the SNR parameter.

Probability of False Alarm - False alarm probability used to estimate SNR 0.001 (default)

Specify the false alarm probability used to estimate SNR using the Shnidman equation.

## Dependencies

To enable this parameter, set Calculation to Target Range, Transmission Loss, or Source Level, and access the Detection Specifications for SNR options for the SNR parameter.

Number of Pulses - Number of pulses used to estimate SNR
1 (default)
Specify the number of pulses. You can specify multiple pulses for noncoherent integration in the Shnidman equation.

## Dependencies

To enable this parameter, set Calculation to Target Range, Transmission Loss, or Source Level, and select the Detection Specifications for SNR options for the SNR parameter.

Swerling Case Number - Swerling case number used estimate SNR
0 (default) | 1 | 2 | 3 | 4
Specify the Swerling case number used to estimate SNR using the Shnidman equation. Swerling numbers characterize the detection problem for fluctuating pulses in terms of:

- a decorrelation model for the received pulses.
- the distribution of scatterers affecting the probability density function (pdf) of the target radar cross section (RCS).

The Swerling cases include two decorrelation models (scan-to-scan or pulse-to-pulse) and two radar cross section pdfs (based on the presence or absence of a dominant scatterer):

- 0 - Nonfluctuating pulses.
- 1 - Scan-to-scan decorrelation: Several randomly distributed scatterers with no dominant scatterer described by a Rayleigh/exponential PDF.
- 2 - Pulse-to-pulse decorrelation: Several randomly distributed scatterers with no dominant scatterer described by a Rayleigh/exponential PDF.
- 3 - Scan-to-scan decorrelation: Several scatterers with one dominant scatterer described by a chisquare PDF with 4 degrees of freedom.
- 4 - Pulse-to-pulse decorrelation: Several scatterers with one dominant scatterer described by a chi-square PDF with 4 degrees of freedom.


## Dependencies

To enable this parameter, set Calculation to Target Range, Transmission Loss, or Source Level, and select the Detection Specifications for SNR options for the SNR parameter.

Transmission Loss - Transmission loss in channel 78.0614 (default) | scalar

Transmission loss in channel, specified as a scalar. Units are dB. For passive sonar modeling, specify a one-way transmission loss. For active sonar modeling, specify a two-way transmission loss. You can specify a transmission loss value, or calculate transmission loss using the Calculation of Transmission Loss options.

To calculate transmission loss:
1 Click the arrows to the right of the Transmission Loss label to access the Calculation of Transmission Loss menu.
2 Enter values for Target Range, Frequency, and Depth.

## Dependencies

To enable this parameter, set Calculation to Source Level or SNR.
Target Range - Target range
10000 (default) | positive scalar
Target range, specified as a positive scalar. When Mode is Passive, target range is from source to receiver. When Mode is Active, target range is from source to reflecting target. Default units are in meters. You can also select km, mi, or nmi.

## Dependencies

To enable this parameter, set the Calculation parameter to Source Level or SNR and click the arrow next to Calculation of Transmission Loss.

Frequency - Signal frequency
2 (default) | positive scalar
Signal frequency, specified as a positive scalar. Default units are in kHz. You can also select $\mathrm{Hz}, \mathrm{kHz}$, and MHz .

## Dependencies

To enable this parameter, set Calculation to Source Level or SNR and click the arrow next to Calculation of Transmission Loss.

Depth - Channel depth
10000 (default) | positive scalar
Channel depth, specified as a positive scalar. Default units are in meters. You can also select km, mi, and nmi.

Dependencies
To enable this parameter, set the Calculation parameter to Source Level or SNR and click the arrow next to Calculation of Transmission Loss.

## Version History <br> Introduced in R2017b

## See Also

## Apps

Sensor Array Analyzer
Functions
range2tl|sonareqsl|sonareqsnr|sonareqtl|tl2range
Topics
"Sonar Equation"


[^0]:    Array Span:
    $X$ axis $=2 \mathrm{~m}$
    Y axis $=2 \mathrm{~m}$
    $Z$ axis $=0 \mathrm{~m}$

[^1]:    Array Span:
    X axis $=0.000 \mathrm{~m}$
    $\mathrm{Y}_{\text {axis }}=2.000 \mathrm{~m}$
    $Z$ axis $=1.732 \mathrm{~m}$

[^2]:    Array Span:
    X axis $=0.0 \mathrm{~m}$
    $Y$ axis $=1.2 \mathrm{~m}$
    $Z$ axis $=1.2 \mathrm{~m}$

[^3]:    Array Span:
    X axis $=0.0 \mathrm{~m}$
    $Y$ axis $=1.2 \mathrm{~m}$
    $Z$ axis $=1.2 \mathrm{~m}$

[^4]:    Aperture Size:
    Y axis $=2.5 \mathrm{~m}$
    Element Spacing:
    $\Delta y=500 \mathrm{~mm}$
    Array Axis: $Y$ axis

[^5]:    Array Span: X axis $=0.0 \mathrm{~m}$ Y axis $=7.5 \mathrm{~m}$
    $Z$ axis $=0.0 \mathrm{~m}$

[^6]:    Aperture Size:
    $Y$ axis $=1.0 \mathrm{~m}$
    Z axis $=2.5 \mathrm{~m}$ Element Spacing: $\Delta y=500 \mathrm{~mm}$ $\Delta z=500 \mathrm{~mm}$

[^7]:    'Span ' - Show angle span measurement
    0 (default) | 1

[^8]:    Data Types: double

